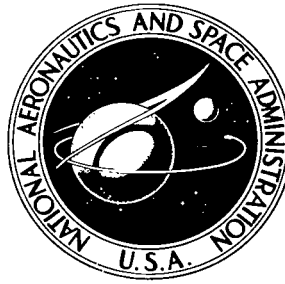


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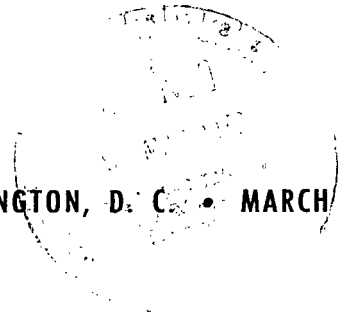
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**NAMER - A FORTRAN IV PROGRAM
FOR USE IN OPTIMIZING DESIGNS
OF TWO-LEVEL FACTORIAL EXPERIMENTS
GIVEN PARTIAL PRIOR INFORMATION**

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16. Abstract Under certain specified conditions, the Bayes procedure for designing two-level fractional factorial experiments is that which maximizes the expected utility over all possible choices of parameter-estimator matchings, physical-design variable matchings, defining parameter groups, and sequences of telescoping groups. NAMER computes the utility of all possible matchings of physical variables to design variables and parameters to estimators for a specified choice of defining parameter group or groups. The matching yielding the maximum expected utility is indicated, and detailed information is provided about the optimal matchings and utilities. Complete documentation is given; and an example illustrates input, output, and usage.			
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CONTENTS

	Page
SUMMARY	1
INTRODUCTION	2
SYMBOLS	3
REVIEW OF BAYES PROCEDURE AND STATEMENT OF COMPUTING PROBLEM	4
ALGORITHM	10
PROGRAM DESCRIPTION	16
Main Program NAMER	17
Subroutine PERM	18
Subroutine REMAX	18
Subroutine LINER	19
INPUT DESCRIPTION	20
OUTPUT DESCRIPTION	23
SPECIAL LEWIS RESEARCH CENTER ROUTINES	24
TIMING INFORMATION	26
APPENDIXES	
A - SAMPLE PROBLEM AND PROGRAM OUTPUT	27
B - FORTRAN LISTING	36
C - PROGRAM SYMBOLS	58
D - PROGRAM GENERAL FLOW DIAGRAM	61
REFERENCES	62

NAMER - A FORTRAN IV PROGRAM FOR USE IN OPTIMIZING DESIGNS OF
TWO-LEVEL FACTORIAL EXPERIMENTS GIVEN
PARTIAL PRIOR INFORMATION

by Steven M. Sidik

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SUMMARY

NAMER can be used to find the Bayes procedure for designing two-level fractional factorial experiments given partial prior information. The required prior information is

- (1) A statement for each parameter giving a prior probability that it is not zero
- (2) A statement of the probability of stopping at each contemplated stopping point
- (3) A statement of the value to the experimenter of an unbiased estimate for each parameter

The steps of the design and performance of the experiment may be represented as a finite discrete game between the experimenter and nature. The decision space E for the experimenter consists of the choice of initial defining parameter group, the choice of the sequence or sequences of subgroups that define the telescoping, the choice of physical-design variable matching, and the choice of parameter-estimator matching. The decision space N for nature consists of the choice of which of the parameters are zero and the choice of the stopping point of the experiment. The Bayes procedure maximizes the expected utility over all possible distinct choices of parameter-estimator matchings, physical-design variable matchings, and defining parameter groups for an assumed strategy for nature.

This report presents an algorithm and a computer program entitled NAMER which computes the expected utility of all possible physical-design variable matchings and parameter-estimator matchings for a specified choice of defining parameter groups. The matchings which maximize the expected utilities are saved and printed out. The computational procedure utilizes the group properties of the parameters and the standard ordering. Complete program documentation is presented including sample input and output and a sample problem illustrating the usage (appendix A), program listings (appendix B), a program symbol table (appendix C), and a general flow diagram of the computer program (appendix D).

INTRODUCTION

The two-level fractional factorial designs represent a class of designs of experiments which yield estimates of first-degree effects and interactions for a small amount of experimentation. The main disadvantage of this class of designs is that the estimates (using linear least-squares estimators) are always estimates of aliased combinations of parameters. To make conclusions about single parameters it is necessary to have some information about the parameters from a source other than the experiment. If such information is available before the experiment is performed, it may be incorporated into the design of the experiment.

There are many situations in practice in which an experimenter may have varying amounts of information concerning the variables he wishes to investigate. Sidik and Holms (ref. 1) have developed some optimal design procedures when the prior information is

- (1) A statement for each parameter giving a prior probability that it is not zero
- (2) A statement of the probability of stopping at each contemplated stopping point
- (3) A statement of the value to the experimenter of an unbiased estimate for each parameter

The steps of the design and performance of the experiment may be represented as a finite discrete game between the experimenter and nature. The decision space E for the experimenter consists of the choice of initial defining parameter group, the choice of the sequence or sequences of subgroups that define the telescoping, the choice of physical-design variable matching, and the choice of parameter-estimator matching. The decision space N for nature consists of the choice of which parameters are zero and the choice of the stopping point of the experiment.

The Bayes procedure maximizes the expected utility over all possible distinct choices of parameter-estimator matchings, physical-design variable matchings, and defining parameter groups for an assumed strategy for nature.

This report presents an algorithm and a computer program entitled NAMED which computes the expected utility of all possible physical-design variable matchings and parameter-estimator matchings for a specified choice of defining parameter group or groups. The computational procedure utilizes the group properties of the parameters and the standard ordering of the parameters.

The program can handle experiment designs for as many as nine factors and 32 stopping points. The relation among the stopping points is arbitrary so that, by proper input of data, multiply telescoping designs may be considered or as many as 32 single-stage designs may be analyzed simultaneously. The program output gives the physical-design variable matchings and the parameter-estimator matchings which are the Bayes decisions. Also those matchings which maximize the expected utility at each individual stopping point are printed out so that a security strategy may be specified.

If an experimental program has already begun so that a physical-design variable matching is specified, NAMER may still be used to change the choices of telescoping options based upon revised prior probabilities of stopping at each stopping point not yet reached.

The algorithm and program are fully described. Listings, sample input and output, and a sample problem illustrating the usage are given.

SYMBOLS

B	full parameter group
$B(h)$	subgroup of B used at the h^{th} stopping point of experiment
h	denotes stopping point of experiment
$i \otimes B(h)$	set of standard-order subscripts of elements of $\beta_i \otimes B(h)$
n	number of factors (independent variables)
$P[A]$	permutation of ordering A
$\Pr(A)$	probability of event A
p_b	prior probability of a block effect not being zero
p_i	probability that β_i is not equal to zero, $\Pr(\beta_i \neq 0)$
p_{sh}	probability experiment will stop exactly at h^{th} stopping point
U	maximized expected utility over stopping points for a given defining parameter group and matching of variables
$U(h)$	maximized expected utility of h^{th} stage for a given defining parameter group and matching of variables
$U(i, k)$	expected utility gained by assigning estimator for alias set $\beta_i \otimes B(h)$ to β_k , $k \in i \otimes B(h)$
$u_i(h)$	utility assigned to an unbiased estimate of β_i at h^{th} stopping point
X_A, X_B, \dots	independent variables (design)
X_1, X_2, \dots	independent variables (physical)
\otimes	group operation
Y	dependent (response) variable
$\beta_I, \beta_A, \beta_B, \dots$	parameters in a model equation relating design variables to dependent variable

- $\beta_i \otimes B(h)$ coset (alias set) obtained by multiplying all elements of $B(h)$ by β_i
- β_0, β_1, \dots parameters in a model equation relating physical variables to dependent variable
- δ random variable with mean zero and finite variance
- ϵ element of

REVIEW OF BAYES PROCEDURE AND STATEMENT OF COMPUTING PROBLEM

In a full factorial experiment with n independent variables X_A, X_B, \dots , each restricted to assuming only two values, there are 2^n possible distinct combinations of values. It is common practice to say the independent variables can assume either a "high" level or a "low" level. Each of the 2^n distinct combinations of levels is called a treatment combination. From such an experiment it is possible to estimate the β 's in an equation of the form

$$\begin{aligned}
 Y = & \beta_I + \beta_A X_A + \beta_B X_B + \beta_{BA} X_B X_A + \beta_C X_C + \beta_{CA} X_C X_A + \beta_{CB} X_C X_B \\
 & + \beta_{CBA} X_C X_B X_A + \dots + \beta_{\dots CBA} \dots X_C X_B X_A + \delta \quad (1)
 \end{aligned}$$

where δ is a random variable with mean zero and finite variance. (Note that the ordering of the subscripts is the reverse of that normally used. The reason for this will be explained shortly.)

A regular fractional replicate of the full factorial design does not allow separate estimation of all the β 's. Certain linear combinations of them can be estimated, however. The particular set of linear combinations which can be estimated depends upon the treatment combinations composing the fractional replicate or, equivalently, upon the choice of the design of the experiment. For example, a one-half replicate experiment on four independent variables would provide eight estimators which might be estimators of (depending upon the particular fraction):

$$\left. \begin{array}{ll}
 (\beta_I + \beta_{DCBA}) & (\beta_C + \beta_{DBA}) \\
 (\beta_A + \beta_{DCB}) & (\beta_{CA} + \beta_{DB}) \\
 (\beta_B + \beta_{DCA}) & (\beta_{CB} + \beta_{DA}) \\
 (\beta_{BA} + \beta_{DC}) & (\beta_{CBA} + \beta_D)
 \end{array} \right\} \quad (2)$$

From such estimators, nothing can be inferred about any single parameter without making some assumptions about the other parameter in the alias set.

The set of all 2^n contrasts which provide estimators of the parameters in a full factorial form a group under the appropriate operation. There is a one-to-one mapping from the group of contrasts onto the group B of parameters. Since the point of view of this report is based upon knowledge about parameters, it is more convenient for the development to be in terms of the parameter group. The operation defining a group with respect to the parameters is analogous to that used in the group of contrasts.

With every regular fractional replicate there is associated a defining parameter group (d. p. g.) which can be used to determine the aliased sets of parameters that can be estimated. Conversely, given a d. p. g. , there is a regular fractional replicate associated with it.

Holms (ref. 2) and Holms and Sidik (ref. 3) present a technique called telescoping sequences of blocks. This allows an experimenter to perform a factorial experiment in stages, where the starting stage is a small fractional replicate and the final stage is some larger fraction. Each succeeding stage adds treatment combinations to those run in the preceding stages. In order to retain the orthogonality and the orthogonal blocking, each stage must be a power of two times the size of the preceding stage and all the treatments run must form a regular fractional replicate. In what follows, we will restrict ourselves to single telescoping and consider the h^{th} stopping point to be the h^{th} stage. In the case of multiple telescoping, this would not be true, in general, for there could be many stopping points in a stage and the relations between groups are more complex. This is not essential to the discussion, however; and we consider single telescoping only to keep the notation simple.

Denote the d. p. g. at the starting stage as B(1) and the d. p. g. at the h^{th} stage as B(h). If the d. p. g. 's are such that B(h + 1) is a subgroup of B(h), the sequence of regular fractional replicates corresponding to them will form a telescoping sequence of blocks under the rules established in Holms and Sidik (ref. 3). At the h^{th} stage, the treatment combinations run should form the fractional replicate defined by B(h). The fractional replicate at the h + 1 stage can be achieved by adding to the treatment combinations defined by B(h) those treatments in the replicate defined by B(h + 1) but not yet performed.

As the experiment progresses through the stages, the number of alias sets increases, while the number of β 's in each alias set decreases. If the final stage is the full factorial, each parameter is separately estimable except that certain of the parameters are confounded with blocks. Whether block effects physically exist is a question the experimenter must answer.

It will be convenient at this point to introduce an alternate notation for equation (1). Let the n independent variables be denoted as X_1, \dots, X_n . Number the 2^n β 's of

equation (1) from β_0 to $\beta_{2^{n-1}}$ and consider the following equation which is similar to equation (1):

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_2 X_1 + \beta_4 X_3 + \cdots + \beta_{2^{n-1}} X_n X_{n-1} \cdots X_1 + \delta \quad (3)$$

Equation (1) and equation (3) are both written in what is called the standard order. If the subscripts of the β 's are rewritten as n-digit binary numbers, it becomes quite obvious how the terms and coefficients of equation (3) are related. For example, let $n = 4$ and consider the following equation, where the subscripts on the β 's are written as binary numbers:

$$\begin{aligned} Y = & \beta_0 + \beta_1 X_1 + \beta_{10} X_2 + \beta_{11} X_2 X_1 + \beta_{100} X_3 + \beta_{101} X_3 X_1 + \beta_{110} X_3 X_2 \\ & + \beta_{111} X_3 X_2 X_1 + \beta_{1000} X_4 + \beta_{1001} X_4 X_1 + \beta_{1010} X_4 X_2 + \beta_{1011} X_4 X_2 X_1 \\ & + \beta_{1100} X_4 X_3 + \beta_{1101} X_4 X_3 X_1 + \beta_{1110} X_4 X_3 X_2 + \beta_{1111} X_4 X_3 X_2 X_1 \end{aligned} \quad (4)$$

In general, a β whose subscript in binary notation has ones in the i_1, i_2, \dots, i_k locations from the right is the coefficient of the $X_{i_1} X_{i_2} \cdots X_{i_k}$ interaction.

The set of all 2^n coefficients or parameters form a group B under the appropriate operation. In the alphabetic notation this operation \otimes is simply commutative multiplication of the letter subscripts with the exponents reduced modulo 2. In the binary notation the operation may also be denoted \otimes and defined as

$$\beta_m \otimes \beta_k = \beta_{m_n m_{n-1} \cdots m_1} \otimes \beta_{k_n k_{n-1} \cdots k_1} = \beta_{d_n d_{n-1} \cdots d_1} \quad (5)$$

where $d_i = (k_i + m_i) \pmod{2}$. Thus $\beta_{CBA} \otimes \beta_{DCB} = \beta_{DC^2 B^2 A} = \beta_{DA}$, and $\beta_{0111} \otimes \beta_{1110} = \beta_{1001}$. The defining parameter groups that define the fractional replicates at the various stopping points are subgroups of B. The aliased sets of parameters at each stopping point are the cosets of B(h), which will be denoted $\beta_i \otimes B(h)$.

The principal reason for introducing these notations is that one major problem of finding an optimal design is one of finding an optimal matching of design variables to the physical variables of the particular experiment. The physical variables in an experiment will be denoted as X_1, X_2, \dots, X_n . It is assumed that the experimenter decides that these are the only independent variables to be investigated. Each X_i represents one of the physical variables and is fixed for the remainder of the experiment. For example,

$$X_1 = \text{Temperature}$$

$$X_2 = \text{Time}$$

$$\vdots$$

$$X_n = \text{Velocity}$$

The design variables will be denoted as X_A, X_B, X_C, \dots and so forth. These variables represent abstractions, and tables exist which tabulate experimental designs in terms of these design variables. When an experimenter consults one of these tables and chooses a design, he must then determine a matching of the design variables and the physical variables. Ordinarily the choice is arbitrary because the experimenter usually does not have prior information available which would indicate that one matching might be preferred to another. A combination of choices of d.p.g.'s, physical-design variable matching, and parameter-estimator matching completely specifies for the experimenter how to proceed with his experiment and estimation of parameters. Hence, such a combination of choices will be called a DESIGN.

Sidik and Holms (ref. 1) present an analysis of choosing a best DESIGN under the following conditions:

(1) For each β_i of equation (3), the experimenter can specify the probability that β_i is not equal to zero, $p_i = \Pr(\beta_i \neq 0)$.

(2) For each h denoting a possible stopping point of the experiment, the experimenter can specify the probability of stopping exactly at the h^{th} stopping point, p_{sh} .

(3) For each β_i of equation (3) and each h , the experimenter can specify the value to him of obtaining an unbiased estimate of β_i . This is denoted by $u_i(h)$.

None of the β 's may be separately estimated from a fractional factorial experiment unless some assumptions about certain of the β 's are introduced. Conditions (1) and (3) provide assumptions that will enable the experimenter to assign the estimator for an alias set to a single parameter from the alias set and evaluate the consequences of this.

Changing the matching of physical and design variables will usually change the alias sets. For example, if the matching for $n = 4$ is

$$X_1 = X_A$$

$$X_2 = X_B$$

$$X_3 = X_C$$

$$X_4 = X_D$$

then the alias set $(\beta_A, \beta_B, \beta_{DBA}, \beta_D)$ is mapped into $(\beta_{0001}, \beta_{0010}, \beta_{1011}, \beta_{1000}) = (\beta_1, \beta_2, \beta_{11}, \beta_8)$. But the matching

$$X_1 = X_B$$

$$X_2 = X_A$$

$$X_3 = X_D$$

$$X_4 = X_C$$

maps $(\beta_A, \beta_B, \beta_{DBA}, \beta_D)$ into $(\beta_{0010}, \beta_{0001}, \beta_{0111}, \beta_{0100}) = (\beta_2, \beta_1, \beta_7, \beta_4)$.

Before considering how best to match physical and design variables, let us assume that some such matching has been made. Then consider the problem of matching estimators and parameters at the h^{th} stopping point. The d.p.g. is $B(h)$ and the alias sets are all those distinct cosets of the form $\beta_i \otimes B(h) = \{\beta_{i_1}, \beta_{i_2}, \dots, \beta_{i_m}\}$.

If the parameter $\beta_k \in \beta_i \otimes B(h)$ and the estimator for that alias set is assigned to β_k , then, assuming independence, the prior probability that the estimator will be unbiased is

$$\prod_{\substack{j \in i \otimes B(h) \\ j \neq k}} (1 - p_j)$$

Since $u_i(h)$ is the utility of an unbiased estimate of β_i at the h^{th} stopping point,

$$U(i, k) = u_k(h) \prod_{\substack{j \in i \otimes B(h) \\ j \neq k}} (1 - p_j) \quad (6)$$

is the expected utility of the decision to assign the estimator for the alias set $\beta_i \otimes B(h)$ to the parameter β_k . Thus the Bayes strategy is to assign the estimator to the parameter of the alias set which maximizes this expected utility. One case deserves special mention.

Suppose an estimator is confounded with a block effect. It may be safely assumed that an unbiased estimate of a block effect has no utility to the experimenter. Let the prior probability of the block effect being nonzero be denoted by p_b . Then this information can be incorporated into the decision procedure by computing the expected utility as

$$U(i, k) = u_k(h) \left[\prod_{\substack{j \in i \otimes B(h) \\ j \neq k}} (1 - p_j) \right] (1 - p_b) \quad (7)$$

where $p_b = \Pr$ (the block effect does not equal 0).

With respect to block effects, it is important to note that, depending upon how the block parameters are defined, the estimator for the d. p. g. may also be confounded with blocks. Let $U(i, k_{\max}) = \max[U(i, k) : k \in i \otimes B(h)]$, where the $U(i, k)$ are computed as in equation (6) or equation (7), as appropriate. Then, for the assumed physical-design variable matching and the given d. p. g., the maximized expected utility at the h^{th} stopping point may be denoted by

$$U(h) = \sum U(i, k_{\max}) \quad (8)$$

where the summation is over all the distinct cosets at the h^{th} stopping point. By condition (2) (p. 7) it is also assumed that the experimenter can specify the probabilities of stopping exactly at each of the stopping points. Thus,

$$U = \sum_h p_{sh} U(h) \quad (9)$$

represents the maximized expected utility of the resulting DESIGN.

The Bayes procedure for choosing an optimal DESIGN is to compute the expected utility for each choice of DESIGN and then use any one which yields a maximum expected utility. This can be done by computing U as defined in equation (9) for each choice of physical-design variable matching and all possible distinct (that is, not equivalent under a permutation of letters) choices of d. p. g. 's. NAMER computes U for all possible physical-design variable matchings for a specified set of d. p. g. 's. Repeated application of NAMER to different choices of d. p. g. 's would then allow the experimenter to carry out the full Bayes procedure if he wished. Thus the computing problem is that of mechanizing the evaluation of U for all the matchings of design variables to physical variables.

ALGORITHM

The generation and evaluation of all the matchings of the physical and design variables present two computing problems. The first problem is the generation of all the matchings. This really amounts to computing all permutations of the design variables. The second problem is that of evaluating any given permutation.

The information necessary to evaluate a particular matching is (1) what parameters are in the alias sets, (2) the prior probabilities of the parameters, (3) the utility of unbiased estimates of each parameter, (4) the alias sets confounded with blocks, and (5) the prior probabilities of each block parameter not being zero. The computing procedure used by NAMER uses the group properties of the parameters and binary notation for the subscripts of the parameters. The parameters arranged in the standard order are uniquely identified by the standard-order subscript. Thus, arrays called PROB and UTIL may be set up such that the J^{th} entries are p_{J-1} and u_{J-1} , respectively. Also, arrays called BLOCK and PBLOCK may be set up which indicate the alias sets confounded with blocks and the probabilities associated with them. Then when information about β_J is needed to compute the expected utilities of equation (6) or (7), it can be immediately retrieved.

For the remainder of this discussion consider only a single stopping point since the following procedure will simply be repeated for each stopping point: To determine the alias sets, the d.p.g. must be known. Suppose the d.p.g. is stored in an array called DPG. The numbers in the array DPG are the standard-order subscripts of the parameters in the d.p.g. when the standard order is computed with respect to the design variables. For example, suppose the d.p.g. for the stopping point under consideration is $\{\beta_I, \beta_{CBA}, \beta_{DCB}, \beta_{DA}\}$, and the matching to be evaluated is

$$X_1 = X_A$$

$$X_2 = X_C$$

$$X_3 = X_B$$

$$X_4 = X_D$$

Then the set of standard-order subscripts would be $\{0000, 0111, 1110, 1001\}$ or $\{0, 7, 14, 9\}$. Since the d.p.g. must always contain the identity or β_I , this is redundant information to store. Hence, the numbers which should be stored in DPG are 7, 14, and 9.

The operation \otimes defined by equation (5) can be defined by the Exclusive Or (IEXOR) function (defined on p. 24), which is available in almost all computing languages. Thus to identify the alias set corresponding to any specified parameter, say β_J , all that is needed is to compute the Exclusive Or between J and each number in DPG. The result will be the standard-order subscripts of the parameters aliased with β_J .

If we specify that the numbers in BLOCK are the standard-order subscripts (with respect to the design variables) of one parameter from each of the alias sets confounded with blocks and that the respective elements of PBLOCK are the prior probabilities of the block parameters, then the same use of Exclusive Or can be applied. For example, suppose the d.p.g. under consideration is that given previously, $\{\beta_I, \beta_{CBA}, \beta_{DCB}, \beta_{DA}\}$. Also suppose it is known that $\{\beta_{BA}, \beta_C, \beta_{DCA}, \beta_{DB}\}$ and $\{\beta_{DC}, \beta_{DBA}, \beta_B, \beta_{CA}\}$ are each confounded with block parameters with prior probabilities of 0.50. Then one element from each of the two alias sets may be chosen to represent it. Suppose they are β_{BA} and β_{DC} . Then BLOCK(1) should be set to $11)_2 = 3$, and BLOCK(2) should be set to $1100)_2 = 12$; and PBLOCK(1) = PBLOCK(2) = 0.50.

It is now an easy task to compute the expected utilities of equations (6) and (7). It remains to find all the distinct alias sets in some economical manner. To do so, set up an array denoted T1 which is 2^n words long. This will be used as an indicator array to indicate if a parameter has been found in an alias set so far. Begin the computation for the stopping point by setting $U(h) = 0.0$ and initializing the T1 array to some value, say zero.

For each block effect set the element given by BLOCK in T1 to some indicator value not equal to the initialization value, say IRUN; and compute the Exclusive Or of that element and every value in DPG. This will yield the standard-order subscripts of all the parameters in the alias set. To indicate that these parameters have been identified as members of an alias set, set the locations of T1 corresponding to these parameters equal to IRUN. These standard-order subscripts and the value in PBLOCK indicate where to find the probabilities and utilities necessary for making the optimal estimator-parameter matching according to equation (7). Compute the expected utilities, identify the maximum, and add this value to $U(h)$.

Now begin searching T1 until a value not equal to IRUN is found. Suppose the subscript of this value is K . Then compute the EXOR of $K - 1$ with each number in DPG. Along with $K - 1$ itself, this will yield the standard-order subscripts of all parameters in the alias set containing β_{K-1} . To indicate that these parameters have been identified as members of an alias set, set the locations of T1 corresponding to these parameters equal to IRUN.

These standard-order subscripts provide the information needed to find the probabilities and utilities necessary for making the optimal estimator-parameter matching. Compute the expected utilities, identify the maximum, and add this value to $U(h)$.

Now continue searching T1 from the location $K + 1$ for another value not equal to IRUN. This will find the next parameter in the standard order which has not yet appeared in an alias set. Thus, the preceding evaluation procedure should be repeated until the end of the T1 array is reached. At that point, all the distinct alias sets will have been identified and evaluated once and only once. The value of $U(h)$ will then be the total maximized expected utility for the h^{th} stopping point corresponding to the optimal estimator-parameter matchings for the current physical-design variable matching.

This same procedure is simply repeated for each stopping point and then $U = \sum p_{sh} U(h)$ may be calculated. The matchings of physical-design variables which provide the largest values of $U(h)$ and U may be kept updated in several arrays. Then when all the permutations are completed, the optimal matchings will be available.

What must now be developed is a procedure for generating all the matchings of physical to design variables in some economical manner. Since all the permutations are to be evaluated, the result does not depend upon which matching is done first or in what order they are generated. Thus the starting permutation and the order of generation may be whatever is most convenient computationally. A simple convention used in NAMER is to begin with the matching

$$X_1 = X_A$$

$$X_2 = X_B$$

$$\begin{array}{c} \cdot \\ \cdot \\ \cdot \end{array}$$

The distinction has been made previously that the alphabetic subscripts are for the design variables and the numeric subscripts for the physical variables. Thus the preceding starting convention has both sets of variables in the standard ordering. Suppose the d.p.g. at a given stopping point is $\{\beta_I, \beta_{CBA}, \beta_{DCB}, \beta_{DA}\}$. Then for the matching

$$\left. \begin{array}{l} X_1 = X_A \\ X_2 = X_B \\ X_3 = X_C \\ X_4 = X_D \end{array} \right\} \quad (10)$$

the DPG array contains 0111 for (β_{CBA}) , 1110 for (β_{DCB}) , and 1001 for (β_{DA}) . To

evaluate a different matching, say

$$\left. \begin{aligned} X_1 &= X_A \\ X_2 &= X_C \\ X_3 &= X_D \\ X_4 &= X_B \end{aligned} \right\} \quad (11)$$

the DPG array should contain 1011 for (β_{CBA}) , 1110 for (β_{DCB}) , and 0101 for (β_{DA}) . The latter DPG can be derived from the former by permuting the binary digits according to the same permutation that gives the ordering X_B, X_D, X_C, X_A starting with X_D, X_C, X_B, X_A . Recall that the binary digits are numbered from right to left. Thus the different matchings of variables can be achieved by constructing all the $n!$ permutations of the rightmost n binary bits in the numbers in DPG. The same procedure applies to the BLOCK array for the same reasons.

Ord-Smith (ref. 4) has presented a survey of a number of possible permutation algorithms. Of these, the best for the purposes of NAMER is the one by Trotter (ref. 5). Trotters' algorithm computes all the permutations as a sequence of adjacent transpositions. To see why this is best, consider how to achieve the permutation of the binary bits by means of arithmetic and logical machine operations. Let M be the number to be changed and express it in binary as $M = m_n m_{n-1} \dots m_j m_{j-1} \dots m_1$ and suppose the digits m_j and m_{j-1} are to be transposed. Compute

$$I = \text{AND} \left(\begin{array}{ccccccc} & n & & & j & j-1 & 1 \\ 0 & 0 & 0 & \dots & 1 & 0 & \dots & 0, M \end{array} \right)$$

$$J = \text{AND} \left(\begin{array}{ccccccc} & n & & & j & j-1 & 1 \\ 0 & 0 & 0 & \dots & 0 & 1 & \dots & 0, M \end{array} \right)$$

$$K = \text{AND} \left(\begin{array}{ccccccc} & n & & & j & j-1 & \\ 1 & 1 & 1 & \dots & 0 & 0 & \dots & 1, M \end{array} \right)$$

$$I = I/2$$

$$J = J*2$$

$$M = I + J + K = m_n m_{n-1} \dots m_{j-1} m_j \dots m_1$$

Notice that the shifting of the digits m_j and m_{j-1} is accomplished by the multiplication and division by 2. If the permutations were not the result of transpositions of adjacent digits, a more general shift function would be needed or the use of powers of 2 would be needed. These would take more time to execute and/or more logic to control than the current method. This is an important consideration since the computing of the permutations accounts for a substantial portion of the computing job.

A third major problem involved in the program is that of providing the necessary output from the calculations in an economical and useful manner. To explain what NAMER does it will be convenient to introduce some notations for, and properties of, permutations. Let A denote the set of the first n letters of the alphabet arranged in order; that is, $A = \{A, B, C, D, \dots\}$. Let an ordering of A be the set of the first n letters of the alphabet arranged in some arbitrary order. Let a permutation on A or any particular ordering of A be a function denoted as

$$P = \begin{pmatrix} 1 & 2 & 3 & \dots & n \\ i_1 & i_2 & i_3 & \dots & i_n \end{pmatrix} \quad (12)$$

which means to take the j^{th} element of the ordering and make it the i_j^{th} element for $j = 1, 2, \dots, n$. Thus a permutation is a function which maps the set of all possible orderings of A one-to-one onto itself. Since the upper line of equation (12) is redundant, the notation for P is often reduced to $P = (i_1, i_2, \dots, i_n)$.

A transposition is a permutation which interchanges exactly two elements of A . Any permutation can be expressed as a product of transpositions of the form $(1, i_1)(2, i_2) \dots (n, i_n)$. Here (j, i_j) is an abbreviated notation for

$$\begin{pmatrix} 1 & 2 & \dots & j & \dots & i_j & \dots & n \\ 1 & 2 & \dots & i_j & \dots & j & \dots & n \end{pmatrix}$$

The product of transpositions may be expressed as a transposition vector $\langle i_1, \dots, i_n \rangle$. As an illustration note

$$\begin{aligned}
\mathbf{P} &= \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 1 & 5 & 2 & 4 \end{pmatrix} \\
&= (1, 3) \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 1 & 3 & 5 & 2 & 4 \end{pmatrix} \\
&= (1, 3)(2, 3) \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 5 & 3 & 4 \end{pmatrix} \\
&= (1, 3)(2, 3)(3, 5) \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 3 & 5 & 4 \end{pmatrix} \\
&= (1, 3)(2, 3)(3, 5)(4, 5)(5, 5) = \langle 3, 3, 5, 5, 5 \rangle
\end{aligned}$$

Then $P[ABCDE] = [BDAEC]$ directly and

$$\begin{aligned}
(1, 3)(2, 3)(3, 5)(4, 5)(5, 5)[ABCDE] &= (1, 3)(2, 3)(3, 5)(4, 5)[ABCDE] \\
&= (1, 3)(2, 3)(3, 5)[ABCED] \\
&= (1, 3)(2, 3)[ABDEC] \\
&= (1, 3)[ADBEC] \\
&= [BDAEC]
\end{aligned}$$

as a sequence of transpositions. This illustrates the equivalence of the two ways of expressing \mathbf{P} . It is obvious that the permutation expressed as a product of transpositions is most convenient for this computer application. Let NDPG be the number of defining parameter groups. Then the orderings $O_1, \dots, O_{\text{NDPG}+1}$ which yield the largest overall expected utility (O_1) and the largest utilities at each stopping point ($O_2, \dots, O_{\text{NDPG}+1}$) are the information the statistician seeks.

The program included in this report does not print all the information for every permutation since this would be much too large a volume of output. All that is saved are the orderings O_i ($i = 1, 2, \dots, \text{NDPG} + 1$). The initial letter-factor matching is the assignment of the i^{th} letter of the alphabet to i . After all the permutations are performed and evaluated, the program returns the order of the letters and the d. p. g. 's to their original state.

Then permutations P_i must be found to effect reorderings upon $A = \{A, B, C, D, E, \dots\}$ to achieve $O_1, O_2, \dots, O_{\text{NDCG}+1}$ in some efficient manner. Let

$$P_1[A] = O_1$$

$$P_2[A] = P_2[P_1^{-1}[P_1[A]]] = O_2$$

$$P_i[A] = P_i[P_{i-1}^{-1}[P_{i-1}[A]]] = O_i$$

and define $O_0 = A$, $P_0 = (1, 2, \dots, M)$. Then the sequence of permutations $P_i[P_{i-1}^{-1}[O_{i-1}]]$ should be determined. If $P = (p_1, \dots, p_m)$, then $P^{-1} = (r_1, \dots, r_m)$, where $r_{p_i} = i$. That is, r_j is the subscript of the location in P which contains j . If $Q = (q_1, \dots, q_m)$ and $P^{-1} = (r_1, \dots, r_m)$, then $QP^{-1} = (s_1, \dots, s_m)$, where $s_i = q_{r_i}$. That is, to get s_j , find the character in the j^{th} position of P^{-1} and then go to that location in Q to find s_j . Putting the two operations together - if

$$P = (p_1, \dots, p_m)$$

$$Q = (q_1, \dots, q_m)$$

then

$$QP^{-1} = (s_1, \dots, s_m)$$

where $s_i = q_{r_i}$. That is, find the subscript of the location in P which contains i and go to that location of Q to find s_i .

PROGRAM DESCRIPTION

The NAMER program is composed of the main program NAMER and five subroutines: BLOK, LINER, PERMUT, REMACH, and RECT. They will be discussed in some detail after the following brief descriptions:

Program name	Calling name	Purpose
NAMER	Main program	Input; evaluation of each permutation; identifies and saves optimal matchings; overall program control.
BLOK		Block data subprogram.
PERM	PERMUT	Determines permutations and permutes DPG and BLOCK arrays.
REMAX	REMACH	Achieves rematchings of physical-design variables; outputs detailed description of matchings of physical-design variables and estimator-parameters by appropriate calls to LINE and ALINE.
LINER	LINE	Prints one line of output identifying an estimable parameter and the utility of the assignment of the estimator to the parameter.
	ALINE	If two or more members of an alias set are tied for maximum utility, ALINE identifies the remainder not printed by LINE.
ERECT	RECT	Prints summary output table of the Bayes matching of physical to design variables, the optimal matchings for each stopping point, and the utilities.

Main Program NAMER

NAMER is the main program and is divided into 16 major sections, as indicated by the comments cards in the listing.

Sections 1 to 10. - Read and write input information.

Section 11. - This section is the heart of the program, where each d. p. g. is evaluated and its contribution to the total expected utility computed for a given permutation of the letters. The section is divided into two subsections, 11A and 11B. Section 11A chooses the parameter-estimator matching for the alias sets which are confounded with blocks. Section 11B does the same for the remainder of the alias sets. The computations for IUTILF = 1, 2 are less complicated than those for IUTILF = 3, 4, 5. Thus these cases are separated in the program. See section 7 of the input description for further explanation of IUTILF.

Section 12. - The expected utility of this ordering (PBAYEX) and the expected utilities at the stopping points (PSUMX(-)) are compared to the best utilities to this point (PBAYES AND PSUM(-)). If any one or more is larger than the best so far, the current appropriate utility is placed in PBAYES or PSUM(-) and the ordering (indicated by the contents of IALPHA(-)) is saved in ISAVEP(-, I). The convention is that ISAVEP(-, 1) saves the ordering which gave the best weighted utility and ISAVEP(-, I + 1) saves the ordering which gave the best utility for the Ith d. p. g.

Section 13. - This section permutes the current letter-variable relation for the appropriate class or classes. If all possible distinct permutations have been realized, control passes to section 16. If not all permutations have been realized, control passes to section 14.

Section 14. - If current execution time exceeds that allowed, go to section 15. Otherwise go to section 11 to evaluate the current ordering.

Section 15. - All essential information is punched on cards to permit a restart of this case on another computer run beginning with the current ordering.

Section 16. - Print current clock time and call REMACH.

Subroutine PERM

This subroutine uses a FORTRAN translation of Trotter's routine (ref. 5) to permute the elements in an array as a sequence of transpositions of adjacent elements. The first two blocks are the logic which determines which two adjacent elements are to be transposed. The third block (beginning with line 44) is where the arrays IALPHA, DPG, and BLOCK are actually permuted.

Subroutine REMAX

This subroutine uses the information saved in section 12 of NAMER to recompute the utilities of the optimal matchings.

Section 1. - At this point, the DPG and BLOCK arrays contain the same values they had as initial input data. The permutation required to achieve the first optimal ordering is computed and stored in KPERM(-).

Section 2. - Write the letter-variable matching.

Sections 3 and 4. - Translate permutation vector into transposition vector, and permute BLOCK and DPG arrays.

Section 5. - Performs same function as section 11 of NAMER except that calls to LINE and ALINE are made as appropriate.

Section 6. - Output overall expected utility and expected utilities for each d. p. g.

Section 7. - Compute next permutation and shift to section 2.

To illustrate sections 1, 3, and 7 of REMAX consider the following example:

$$O_1 = [4 \ 1 \ 3 \ 2 \ 5] = P_1[A]$$

$$O_2 = [3 \ 4 \ 1 \ 5 \ 2] = P_2[A]$$

$$O_3 = [4 \ 1 \ 3 \ 2 \ 5] = P_3[A]$$

$$O_4 = [4 \ 3 \ 2 \ 1 \ 5] = P_4[A]$$

$$O_5 = [1 \ 4 \ 5 \ 2 \ 3] = P_5[A]$$

The sequence of values is as follows:

Sequence	KPERM	KKSAVE	K2CYCL	Ordering
1	$P_1 = (24315)$	$P_1 = (24315)$	{ 24345 }	[41325]
2	$P_2 = (35124)$		$(23154) = P_2 P_1^{-1}$	
3	$P_2 P_1^{-1} = (23154)$	$P_2 = (35124)$	{ 23355 }	[34152]
4	$P_3 = (24315)$		$(31254) = P_3 P_2^{-1}$	
5	$P_3 P_2^{-1} = (31254)$	$P_3 = (24315)$	{ 33355 }	[41325]
6	$P_4 = (43215)$		$(14235) = P_4 P_3^{-1}$	
7	$P_4 P_3^{-1} = (14235)$	$P_4 = (43215)$	{ 14445 }	[43215]
8	$P_5 = (14523)$		$(25413) = P_5 P_4^{-1}$	
9	$P_5 P_4^{-1} = (25413)$	$P_5 = (14523)$	{ 25455 }	[14523]

Subroutine LINER

This is a double-entry subroutine with entry points LINE and ALINE. LINE is called by output once for each alias set. The entries of the calling vector are the standard-order subscript number of the parameter in the alias set to which the estimator should be assigned and the expected utility of that assignment. The standard-order subscript is then used to identify the parameter in terms of the interaction of the independent variables it measures. This identification is then printed in numerical form and in Hollerith form using the first six characters of each factor identification card. The utility is also printed.

ALINE is called whenever there are two or more parameters aliased which give the same maximized expected utility. The call to LINE causes one of the aliased parameters to be identified and the expected utility of the estimator to be printed. The call to ALINE causes the remaining parameters to be identified. They are, however, identified only by the numerical form of their interaction.

INPUT DESCRIPTION

The following is a detailed description of the input data necessary to run a problem. There are nine basic sets of input data. Each is described in detail here. An example of the type of problem to which this program may be applied is given in reference 1 and a similar problem is discussed in appendix A. A sample set of data for this problem is given in table I. A pictorial illustration of the input deck setup is given in figure 1. Multiple cases may be run back-to-back. The last card of the last case should have ENDALL punched in the first six columns.

The nine basic sets of input data are as follows:

(1) IDENTIFICATION (13A6, A2) (IDENT). This is one card; all 80 columns are used for Hollerith identification of problem.

(2) MAXIMUM TIME (F6.0) (TMAXX). This is the maximum machine time in minutes permitted for this case. If this time is exceeded and the case is not fully evaluated, all pertinent information is punched on cards to permit a restart of the program.

(3) TYPE OF RUN (16) (ITYPRN).

(3A) SPECIFIED MATCHING (9A1) (XT3). A "1" for ITYPRN indicates this is a regular first-time run and data sets 4 to 9 will be read. A "2" indicates this is a restarted case and only those cards punched by the previous run need be read. A "3" indicates that only one matching will be evaluated. This matching is specified on the 3A card with the first n letters of the alphabet (excluding I) in the first n columns of the card in the order appropriate to the matching desired.

For example, if to indicate an evaluation of the following matching is desired

$$X_1 = X_B$$

$$X_2 = X_A$$

$$X_3 = X_D$$

$$X_4 = X_C$$

one card would be supplied with BADC in the first four columns.

(4) NUMBER OF FACTORS (16) (NFAC). Up to nine factors can be considered.

(5) FACTOR IDENTIFICATIONS (13A6, A2) (FAC). One card for each factor. The first six characters of each card are used as output identification, so they should serve as useful abbreviations.

(6) NUMBER OF CLASSES (16) (NCLASS).

(6A) NUMBER IN EACH CLASS (916) (NSUBI). NCLASS is the number of classes of factors. If this is 1, input set 6A is not read. If the number of classes is more than one, card 6A specifies the number of factors in each class. The factors within a class will be permuted among each other, but permutations between classes will not be permitted. The first NSUBI(1) factors will be assumed to belong to the first class, the next NSUBI(2) to the second class, and so forth. Holms and Sidik (ref. 6) present an experiment in which there are two classes of variables which could not be mixed. Most experiments have only one class.

(7) NUMBER OF NONZERO PROBABILITIES, UTILITY FUNCTION, AND CONSTANT (NPIN, IUTILF, UCOEF) (2I6, F10.9). The number of parameters with nonzero prior probabilities is specified in the first six columns. The choice of utility function is indicated in the second six columns. UCOEF is used in defining utility function 5 and is given in the next 10 columns. Each parameter with a nonzero prior probability or utility is identified in terms of the integer subscripts of the independent variables in the interaction with which it is associated. See the input set (8) description for further information. The possible choices of utility function here are

(a) IUTILF = 1

$$u_i = \begin{cases} 1.0 & \text{for unbiased estimators} \\ 0.0 & \text{for biased estimators} \end{cases}$$

(b) IUTILF = 2

$$u_i = \begin{cases} p_i & \text{for unbiased estimators} \\ 0.0 & \text{for biased estimators} \end{cases}$$

(c) IUTILF = 3

$$u_i = \begin{cases} x_i & \text{for unbiased estimators} \\ 0.0 & \text{for biased estimators} \end{cases}$$

where x_i is given with the p_i in input set (8).

(d) IUTILF = 4

$$u_i = \begin{cases} p_i x_i & \text{for unbiased estimators} \\ 0.0 & \text{for biased estimators} \end{cases}$$

where x_i and p_i are given in input set (8).

(e) IUTILF = 5

$$u_i = \begin{cases} \text{UCOEF} \cdot x_i + (1 - \text{UCOEF})p_i & \text{for unbiased estimators} \\ 0.0 & \text{for biased estimators} \end{cases}$$

where x_i and p_i are given in input set (8) and it is assumed $0.0 \leq \text{UCOEF} \leq 1.0$.

It should be noticed that these utility functions do not depend upon the stopping point as implied by condition (3) on page 7. To provide a capability of making the utility function depend upon the stopping point, the user can weight the stopping points by use of the weighting values WT(I) read in input set (9B). Thus the $u_i(h)$ used in the program are computed as $u_i(h) = u_i * \text{WT}(h)$.

(8) PRIOR PROBABILITIES AND UTILITIES (9I1, 2F10.0) (IT1, P, UT). Each parameter with nonzero prior probability is identified in terms of the integer subscripts of the independent variables in the interaction with which it is associated. These subscripts may be supplied in any order anywhere in the first nine columns of the card. The prior probability and the utility follow with 10 columns each, in F10.0 format. The utility need not be specified if IUTILF = 1 or 2 as previously described, for the program then supplies the utility. If IUTILF = 3, 4, or 5, the utility must be specified explicitly. For example, suppose the $X_2 X_3 X_5$ interaction parameter $\beta_{10110} = \beta_{22}$ is assumed to satisfy $P(\beta_{22} \neq 0) = 0.850$ with utility of 0.95. Then the card input could be bbb5b2b3b.850bbbbbb.95. If the prior probability of a parameter being nonzero is zero, no data need be supplied for that parameter.

(9) NUMBER OF DEFINING GROUPS (I6) (NDPG). For each d.p.g. (as many as 32 permitted) there must be one set of inputs 9A to 9E.

(9A) IDENTIFICATION OF STOPPING POINT (4A6) (IDDCG).

(9B) NUMBER OF GENERATORS, PRIOR PROBABILITY OF STOPPING, WEIGHTING VALUE (I6, F6.6, F6.0) (NGEN, PSTOP, WT). If the d.p.g. corresponds to a $(1/2)^r$ fractional replicate, r independent generators must be supplied. Program limitations restrict NGEN to values less than or equal to seven.

(9C) THE GENERATORS OF THE d.p.g. (9A1). The generators are supplied in terms of the first NFAC letters of the alphabet on the first nine columns of the card. There is one card per generator. For example, if the d.p.g. at a particular stopping point is $\{\beta_I, \beta_{EDCBA}, \beta_{CBA}, \beta_{ED}, \beta_{DA}, \beta_{ECB}, \beta_{DCB}, \beta_{EA}\}$, three generators are sufficient; and one such choice might be β_{CBA}, β_{ED} , and β_{DA} . Three cards which

will define the above d. p. g. might be

AbBbC

ED

bbAbbD

The order and position of the letters is unimportant as long as they are on the first nine columns of the card. If the number of generators is zero, no type-9C cards are read.

(9D) NUMBER OF BLOCK PARAMETERS (I6) (NBLOCK).

(9E) IDENTIFICATION OF ALIAS SETS CONFOUNDED WITH BLOCK EFFECTS AND THE PRIOR PROBABILITY ASSOCIATED WITH THE BLOCK EFFECTS (9A1, F5.5) (XT3, PBLOCK). Any single parameter from an alias set which is confounded with a block effect may be input in terms of the first NFAC letters of the alphabet in the first nine columns of one card. This is followed by the prior probability of the block effect on the next five columns. There is one card for each block effect that has a non-zero prior probability. If the alias set is the d. p. g., the first nine columns may be left blank.

OUTPUT DESCRIPTION

The first part of NAMER output is the printout of the input data. This is followed by $NDPG + 1$ printouts. The first set is for the Bayes DESIGN which optimizes the overall expected utility. The subsequent sets are for the DESIGNS that optimize the expected utilities for the individual stopping points. Each of these sets of output consists of the following:

- (1) The optimal matching
- (2) Tables of the parameters chosen to be estimated and the expected utilities of these choices
- (3) The overall expected utility and the expected utilities at the stopping points

For example, the first two pages of the sample output in appendix A indicate the input data. The next two pages provide the information about the Bayes DESIGN, as the label indicates. The Bayes matching is seen to be

$$X_1(\text{TEMP}) = X_C$$

$$X_2(\text{PRESS}) = X_D$$

$$X_3(\text{TIME}) = X_B$$

$$X_4(\text{VEL}) = X_E$$

$$X_5(\text{ANGLE}) = X_A$$

Then for d.p.g. number one (which is the 1/4 replicate of the full factorial) the choices of parameters to be estimated are indicated. Each parameter is identified in terms of the integer subscripts of the independent variables in the interaction with which it is associated. They are also identified by the Hollerith identifications input in section (5) of the input, and the utility of the choice is printed at the far right of each line. Thus the first line of output for d.p.g. number one indicates that the coefficient of $X_1X_2X_3 = X_CX_DX_B$ has been chosen from its alias set as the parameter to be estimated. This interaction is the TEMP×PRESS×TIME interaction, and the expected utility of this choice is 0.20. This utility value does not include the weighting factor at this point.

Below the detailed output for the three d.p.g.'s are printed the overall expected utility and the utilities for each of the d.p.g.'s for this matching.

Similar output provides the detailed output for the designs which maximize the expected utilities for each of the stopping points. The format and arrangement are the same as that described for the Bayes matching. This is followed on the last page by a summary table providing the various matchings, their expected overall utilities, and expected utilities at the stopping points.

SPECIAL LEWIS RESEARCH CENTER ROUTINES

Some of the following functions and subroutines available in the FORTRAN IV - Version 13 language at the Lewis Research Center may not be available (or not available in FORTRAN) at other computer installations. Thus, their usage is explained, and the user can write functions or subroutines providing the same capabilities in a language compatible with the available computer.

The functions and subroutines available at Lewis are the following:

(1) AND(A, B). A real function of the Real or Integer variables A and B. Like bit positions of A and B are compared. A 1 is placed in those positions of the result where there are 1's in both A and B, and a zero is placed in the result otherwise.

(2) IEXOR(A, B). An integer function of the Real or Integer arguments A and B. Like bit positions of A and B are compared. A 1 is placed in those positions of the result where exactly one of A or B is a 1, and a zero is placed in the result otherwise.

(3) IALS(N, X). An integer function of Integer N and Real or Integer X. The contents of X are shifted to the left N places and zeros put into the vacated rightmost positions.

(4) IARS(N, X). An integer function of Integer N and Real or Integer X. The contents of X are shifted to the right N places and zeros put into the vacated leftmost positions.

(5) BCREAD(X1, X2) and BCDUMP(X1, X2, K). These subprograms provide for input and output in absolute binary. A call to BCREAD(X1, X2) causes cards to be read in binary format at the rate of 22 words per card. The data are stored sequentially in the core, beginning with the address of the variable X1 and ending with the address of the variable X2. A call to BCDUMP(X1, X2, K) causes cards to be punched in binary format at the rate of 22 words per card. The data are taken sequentially from the core, beginning with the address of variable X1 and ending with the address of variable X2. K provides card numbering control and is always set to zero by NAMER.

As an example of the usage of these routines, consider the first call to BCREAD in section 10 of NAMER. DUMP1(1) is equivalenced to NFAC. NFAC is the first variable of nine variables in the labeled common block B1. LD1 is set to 9 at the start of NAMER. Thus, the call BCREAD (DUMP1(1), DUMP1(LD1)) causes the variables NFAC, NCLASS, NN, NDPG, PBAYES, and so forth, to be read from unit 5 in binary format.

(6) TIME1(X). This subroutine enables the programmer to read the storage cell clock. The following illustrates the procedure for using TIME1 to calculate elapsed time.

```
CALL TIME1(X1)
      .
      .
      .
CALL TIME1(X2)
```

Then

$$X2 - X1 = \text{Clock pulses}$$

$$\frac{X2 - X1}{60} = \text{Elapsed time in seconds}$$

$$\frac{X2 - X1}{3600} = \text{Elapsed time in minutes}$$

(7) OR(A, B). A real function of the real or integer arguments A and B. Like bit positions of A and B are compared. A 1 is placed in those positions of the result where either or both of A and B are a 1. A zero is placed in those positions of the result wherever both A and B are zero.

TIMING INFORMATION

Several sample problems using single telescoping were run on NAMER to estimate the amount of time required by the program. For these problems, the first stage was assumed to be the smallest experiment large enough to estimate all main effects, and the last stage was the full factorial. Each problem was run once using utility function 2 and once using utility function 3. The results are summarized in table II and figure 2.

Lewis Research Center,

National Aeronautics and Space Administration,

Cleveland, Ohio, November 8, 1971,

132-80.

APPENDIX A

SAMPLE PROBLEM AND PROGRAM OUTPUT

Consider a five-factor experiment involving

X_1 = Temperature

X_2 = Pressure

X_3 = Time

X_4 = Velocity

X_5 = Angle

Suppose that the experimenter's facilities are such that he can only perform four treatment combinations at one time and be reasonably sure that experimental conditions are homogeneous. Thus his experiment should be designed as a blocked factorial design with blocks of size four. Assume also that he has enough materials at one time to perform eight treatment combinations, but no more, and that batches of uniform material are not available in quantities that will supply more than eight treatment combinations. Then the blocks of the experiment might be as shown in the illustration, where the two columns represent two different test facilities and the four rows represent four different batches of raw material.

		Column blocks (test facilities)	
		1	2
Row blocks (batches)	1	1, 1	1, 2
	2	2, 1	2, 2
	3	3, 1	3, 2
	4	4, 1	4, 2

The difference between the first block and the second block in a row is due to performing the experiment in two different test facilities. The differences between rows are due to possible effects of new batches of materials. Suppose the experimenter feels that there is a probability of 0.50 of there actually being a test facility block effect. Let the probability of there being an effect due to differing batches of raw materials be 1.0. Assume further that the probability of an interaction between these block effects is specified as zero. The stopping points of the experiment at each stage are

- (1) Stage one, after completion of blocks (1, 1), (1, 2)
- (2) Stage two, after completion of blocks (1, 1), (1, 2), (2, 1), (2, 2)
- (3) Stage three, after completion of the full factorial

Based upon his available resources and upon past histories of some similar projects he has worked on, the experimenter feels probabilities in the following table are appropriate:

Coefficient of-	Standard-order subscript	Prior probability of being nonzero
X_0	0	1.00
X_1	1	.80
X_2	2	↓
X_2X_1	3	
X_3	4	
X_3X_1	5	
X_3X_2	6	
$X_3X_2X_1$	7	1.0
X_4	8	.50
X_4X_1	9	.50
X_4X_3	12	.40
$X_4X_3X_1$	13	1.0
X_5	16	.40
X_5X_1	17	.30
X_5X_3	20	

Stopping probabilities: $p_{1s} = 0.30$, $p_{2s} = 0.40$,
 $p_{3s} = 0.30$

All the other coefficients have zero prior probability.

Assume the purpose of the experiment is to maximize the response. Also assume that the cost of the experiment is about proportional to the number of treatment combinations run. Then a reasonable choice for utility function might be

$$u_i(h) = \begin{cases} p_i/n_h & \text{if unbiased} \\ 0 & \text{if biased} \end{cases}$$

where n_h is the number of treatment combinations. To achieve this using NAMER, use utility function 2 and for the weighting values at the stages use $1/n_h$.

Rather than investigating all the possible nonequivalent d.p.g.'s and their telescoping options, the best matchings of physical-design variables and parameters to estimators will be determined for the following choices of d.p.g.'s:

$$B(1) = \{\beta_I, \beta_{CBA}, \beta_{EDC}, \beta_{EDBA}\}$$

$$B(2) = \{\beta_I, \beta_{EDBA}\}$$

$$B(3) = \{\beta_I\}$$

Using the d.p.g. $\{\beta_I, \beta_{CBA}, \beta_{DCB}, \beta_{DA}, \beta_{EDC}, \beta_{EDBA}, \beta_{EB}, \beta_{ECA}\}$ for block (1, 1) and the rules presented in reference 3, it may be shown that the following assignment of treatment combinations will lead to the block confounding presented in the table:

Block	Treatment
(1, 1)	(1), dca, ecb, edba
(1, 2)	ba, dcb, eca, ed
(2, 1)	db, cba, edc, ea
(2, 2)	da, c, edcba, eb
(3, 1)	a, dc, ecba, edb
(3, 2)	b, dcba, ec, eda
(4, 1)	dba, cb, edca, e
(4, 2)	d, ca, edcb, eba

Stage	Alias sets confounded with -	
	Test facility effect	Raw material effect
1	$\{\beta_{DA}, \beta_{DCB}, \beta_{ECA}, \beta_{EB}\}$	$\{\beta_I, \beta_{CBA}, \beta_{EDC}, \beta_{EDB}\}$
2	$\{\beta_{DA}, \beta_{EB}\}$	$\{\beta_I, \beta_{EDBA}\}$ $\{\beta_{CBA}, \beta_{EDC}\}$
3	$\{\beta_{DA}\}$	$\{\beta_I\}$ $\{\beta_{CBA}\}$ $\{\beta_{EDBA}\}$ $\{\beta_{EDC}\}$

The sample FORTRAN data sheets given in table II supply the data necessary to run this problem as described. The sample output for this problem follows.

NAMER OUTPUT NAMER SAMPLE PROBLEM
PROGRAM WILL DUMP FOR RESTART IF NOT FINISHED IN 2. MINUTES.

CURRENT EXECUTION TIME 0.00
THERE ARE 5 FACTORS. THEY ARE...

1 TEMP SOURCE TEMPERATURE
2 PRFSS SOURCE PRESSURE
3 TIME TIME DURATION
4 VEL SOURCE VELOCITY
5 ANGLE ANGLE OF INJECTION

15 PARAMETERS WITH NON-ZERO PRIOR PROBABILITIES AND UTILITIES

UTILITY FUNCTION 2

0	1.000000	1.000000
1	0.800000	0.800000
2	0.800000	0.800000
12	0.800000	0.800000
3	0.800000	0.800000
13	0.800000	0.800000
23	0.800000	0.800000
123	0.800000	0.800000
4	1.000000	1.000000
14	0.500000	0.500000
34	0.500000	0.500000
134	0.400000	0.400000
5	1.000000	1.000000
15	0.400000	0.400000
35	0.300000	0.300000

2 DEFINING PARAMETER GROUPS

1/4 REP--ROW 1

DPE 1
2 GENERATORS
PROB OF STOPPING 0.30000 WEIGHT 0.125000
ABC
CDE

THERE ARE 2 BLOCK PARAMETERS

AD 0.50000
1.00000

1/2 REP-- ROWS 1,2

DPG 2
1 GENERATORS
PROB OF STOPPING 0.40000 WEIGHT 0.06250
ABDE

THERE ARE 3 BLOCK PARAMETERS

AD 0.50000
1.00000
ABC 1.00000

FULL--ALL ROWS

DPG 3
0 GENERATORS
PROB OF STOPPING 0.30000 WEIGHT 0.031250

THERE ARE 5 BLOCK PARAMETERS

AD C.50000
1.00000
ABC 1.00000
ABDE 1.00000
CDE 1.00000
CURRENT EXECUTION TIME 0.01
CURRENT EXECUTION TIME 0.03

THIS MATCHING IS THE BAYES MATCHING

VARIABLE SHOULD BE CALLED
1 T F M P C
2 P R E S S D
3 T I M E B
4 V E L E
5 A N G L E A

DEFINING PARAMETER GROUP NO. 1
1/4 REP--ROW 1

* * * * *
*1 *2 *3 TEMP PRESS TIME C.200000
0* G MEAN C
*1 TEMP C.560000
*2 PRESS C.400000
*3 *4 TIME VEL C.200000
*3 *5 TIME ANGLE C.480000
*2 *3 PRESS TIME ANGLE C.200000
C.480000

DEFINING PARAMETER GROUP NO. 2
1/2 REP-- ROWS 1,2

* * * * *
0* G MEAN C.250000
*1 *3 *5 TEMP TIME ANGLE 0
*1 TEMP C
*2 PRESS C.800000
*1 *2 TEMP PRESS C.800000
*3 TIME C.800000
*1 *3 TEMP TIME C.800000
*2 *3 PRESS TIME C.800000
*1 *2 *3 TEMP PRESS TIME C.800000
*4 VEL 1.000000
*1 *3 *4 TEMP VEL C.500000
*3 *5 TIME ANGLE C.300000
*1 *3 *4 TEMP TIME VEL C.400000
*5 ANGLE 1.000000
*1 *5 TEMP ANGLE C.400000

DEFINING PARAMETER GROUP NO. 3
FULL--ALL ROWS

* * * * *
*2 *5 PRESS ANGLE 0
0* G MEAN C
*1 *3 *5 TEMP TIME ANGLE C
*2 *3 *4 *5 PRESS TIME VEL ANGLE C
*1 *2 *4 TEMP PRESS VEL 0
*1 TEMP C.800000
*2 PRESS C.800000
*1 *2 TEMP PRESS C.800000
*3 TIME C.800000
*1 *3 TEMP TIME C.800000
*2 *3 PRESS TIME C.800000
*1 *2 *3 TEMP PRESS TIME C.800000

```

*1      *4      VEL      1.000000
      *4      VEL      C.500000
*2      *4      PRESS     VEL      C
      *3 *4      TIME     VEL      C.500000
*1      *3 *4      TEMP     TIME     VEL      C.400000
      *2 *3 *4      PRESS     TIME     VEL      C
*1 *2 *3 *4      TEMP     PRESS     TIME     VEL      C
      *5      ANGLE      1.000000
*1      *5      TEMP     PRESS     ANGLE      C.400000
*1 *2      *5      TEMP     PRESS     ANGLE      C
      *3 *5      TIME     ANGLE      C.300000
      *2 *3 *5      PRESS     TIME     ANGLE      C
*1 *2 *3      *5      TEMP     PRESS     TIME     ANGLE      C
      *4 *5      VEL      ANGLE      C
*1      *4 *5      TEMP     PRESS     VEL      ANGLE      C
      *2 *4 *5      TEMP     PRESS     VEL      ANGLE      C
*1 *2      *4 *5      TEMP     PRESS     TIME     VEL      ANGLE      C
      *3 *4 *5      TEMP     TIME     VEL      ANGLE      C
*1      *3 *4 *5      TEMP     PRESS     TIME     VEL      ANGLE      C

```

FOR THE ABOVE PERMUTATION THE EXPECTED UTILITY IS 0.42169

THE EXPECTED UTILITIES AT THE STOPPING POINTS ARE.

```

DEFINING PARAMETER GROUP 1 0.31500
DEFINING PARAMETER GROUP 2 0.59062
DEFINING PARAMETER GROUP 3 0.30312

```

THIS MATCHING MAXIMIZES THE EXPECTED VALUE AT THE 1 STOPPING POINT 1/4 REP--ROW 1

```

VARIABLE      SHOULD BE CALLED
1 TEMP      D
2 PRESS     A
3 TIME      B
4 VEL      C
5 ANGLE     E

```

DEFINING PARAMETER GROUP NO. 1
1/4 REP--ROW 1

```

* * * * *
*1 *2      TEMP PRESS      0.168000
0*      G MEAN      C
*1      TEMP      C.800000
      *2      PRESS     C.400000
      *3      TIME     C.800000
*1 *3      TEMP     TIME     C.800000
      *4      VEL      C.120000
      *5      ANGLE      C.100000

```

DEFINING PARAMETER GROUP NO. 2
1/2 REP-- ROWS 1,2

```

* * * * *
*1 *2      TEMP PRESS      C.280000
0*      G MEAN      C
      *2 *3 *4      PRESS     TIME     VEL      C
*1      TEMP      C.800000
      *2      PRESS     C.800000
      *3      TIME     C.800000
*1 *3      TEMP     TIME     C.800000
      *2 *3      PRESS     TIME     C.480000
      *5      ANGLE      C.200000
*1      *4      VEL      1.000000
      *4      TEMP     PRESS     VEL      0.500000
      *2 *4      *4      VEL      C
*1 *2 *4      *1 *3 *4 *5      TEMP     PRESS     VEL      C
      *3 *4 *5      *3 *4 *5      TEMP     PRESS     TIME     VEL      C.500000
*1 *3 *4      TEMP     TIME     VEL      C.400000
*1 *2 *3 *4      TEMP     PRESS     TIME     VEL      C
      *4 *5

```

DEFINING PARAMETER GROUP NO. 3
FILL--ALL ROWS

```

* * * * *
*1 *2      TEMP PRESS      0.400000
0*      G MEAN      C
      *2 *3 *4      PRESS     TIME     VEL      C
*1 *2 *3 *5      TEMP     PRESS     TIME     VEL      ANGLE      C
*1      *4 *5      TEMP     PRESS     TIME     VEL      ANGLE      C
*1      *2      TEMP     PRESS     C.800000
      *3      PRESS     TIME     C.800000
*1 *3      TEMP     PRESS     TIME     C.800000
      *2 *3      PRESS     TIME     C.800000
*1 *2 *3      TEMP     PRESS     TIME     C.800000
      *4      VEL      1.000000
*1      *4      TEMP     PRESS     VEL      C.500000

```


*2 *3 *4		PRESS	TIME	VEL		0	
*1 *2 *3 *4		TEMP	PRESS	TIME	VEL	0	
	*5				ANGLE	1.000000	
*1		TEMP			ANGLE	0.400000	
	*2		PRESS		ANGLE	0	
*1 *2		TEMP	PRESS		ANGLE	0	
	*3			TIME	ANGLE	0.300000	
	*2 *3		PRESS	TIME	ANGLE	0	
*1 *2 *3		TEMP	PRESS	TIME	ANGLE	0	
	*4 *5			VEL	ANGLE	0	
*1		TEMP		VEL	ANGLE	0	
	*2 *4 *5		PRESS		VEL	ANGLE	0
*1 *2		TEMP	PRESS		VEL	ANGLE	0
	*3 *4 *5			TIME	VEL	ANGLE	0
*1		TEMP		TIME	VEL	ANGLE	0
*1 *2 *3 *4 *5		TEMP	PRESS	TIME	VEL	ANGLE	0

FOR THE ABOVE PERMUTATION THE EXPECTED UTILITY IS 0.41934

THE EXPECTED UTILITIES AT THE STOPPING POINTS ARE.

DEFINING PARAMETER GROUP	1	0.31500
DEFINING PARAMETER GROUP	2	0.59062
DEFINING PARAMETER GROUP	3	0.29531

THIS MATCHING MAXIMIZES THE EXPECTED VALUE AT THE 3 STOPPING POINT FULL--ALL ROWS

VARIABLE	SHOULD BE CALLED
1 TFMP	C
2 PPRESS	D
3 TIME	B
4 VFL	E
5 ANGLE	A

DEFINING PARAMETER GROUP NO. 1

1/4 REP--ROW 1

*1 *2 *3		TEMP	PRESS	TIME		0.200000
0*		G MEAN				0
*1		TEMP				0.560000
	*2		PRESS			0.400000
				VEL		0.200000
	*3			TIME		0.480000
	*2 *3		PRESS	TIME	ANGLE	0.200000
						0.480000

DEFINING PARAMETER GROUP NO. 2

1/2 REP-- ROWS 1,2

*3 *4			TIME	VEL		0.250000
0*		G MEAN				0
*1 *3 *5		TEMP	TIME		ANGLE	0
*1		TEMP				0.800000
	*2		PRESS			0.800000
*1 *2		TEMP	PRESS			0.800000
	*3			TIME		0.800000
*1 *3		TEMP	TIME			0.800000
	*2 *3		PRESS	TIME		0.800000
*1 *2 *3		TEMP	PRESS	TIME		0.800000
	*4			VEL		1.000000
*1		TEMP		VEL		0.500000
	*3 *5		TIME		ANGLE	0.300000
*1 *3 *4		TEMP	TIME	VEL		0.400000
	*5				ANGLE	1.000000
*1		TEMP			ANGLE	0.400000

DEFINING PARAMETER GROUP NO. 3

FULL--ALL ROWS

*2 *5			PRESS		ANGLE	0	
0*		G MEAN				0	
*1 *3 *5		TEMP	TIME		ANGLE	0	
	*2 *3 *4 *5		PRESS	TIME	VEL	ANGLE	0
*1 *2 *4		TEMP	PRESS		VEL		0
*1		TEMP					0.800000
	*2		PRESS				0.800000
*1 *2		TEMP	PRESS				0.800000
	*3			TIME			0.800000
*1 *3		TEMP	TIME				0.800000
	*2 *3		PRESS	TIME			0.800000
*1 *2 *3		TEMP	PRESS	TIME			0.800000
	*4			VEL			1.000000
*1		TEMP		VEL			0.500000
	*2 *4		PRESS		VEL		0
	*3 *4			TIME	VEL		0.500000

*1	*3	*4	TEMP	TIME	VEL		C.400000
*2	*3	*4	PRESS	TIME	VEL		C
*1	*2	*3	*4	TEMP	PRESS	TIME	VEL
		*5					ANGLE
*1			*5	TEMP			ANGLE
*1	*2		*5	TEMP	PRESS		ANGLE
	*3		*5			TIME	ANGLE
	*2	*3	*5			PRESS	TIME
*1	*2	*3	*5	TEMP	PRESS	TIME	ANGLE
		*4	*5				VEL
*1		*4	*5	TEMP			VEL
	*2	*4	*5		PRESS		VEL
*1	*2	*4	*5	TEMP	PRESS		VEL
	*3	*4	*5			TIME	VEL
*1	*3	*4	*5	TEMP		TIME	VEL
*1	*2	*3	*4	*5	TEMP	PRESS	TIME
						VEL	ANGLE

FOR THE ABOVE PERMUTATION THE EXPECTED UTILITY IS 0.42169

THE EXPECTED UTILITIES AT THE STOPPING POINTS ARE..

DEFINING PARAMETER GROUP	1	0.31500
DEFINING PARAMETER GROUP	2	0.59062
DEFINING PARAMETER GROUP	3	0.30312

SUMMARY OUTPUT TABLE

** BAYES ***	**** 1 *****	**** 2 *****	**** 3 *****	****
C	D	C	C	
C	A	B	D	
B	B	D	B	
E	C	A	E	
A	E	E	A	

EXPECTED UTILITY
OVER STOPPING PTS

0.42169	0.37074	0.41934	0.42169
---------	---------	---------	---------

EXPECTED UTILITY
AT EACH STOPPING PT

1	0.31500	0.39850	0.31500	0.31500
2	0.59062	0.41000	0.59062	0.59062
3	0.30312	0.29062	0.29531	0.30312
CURRENT EXECUTION TIME		0.07		

APPENDIX B

FORTRAN LISTING

```

$IBFTC BLOK
      BLOCK DATA
      COMMON/BDATA/      POWERS(11),      IALPHA(9),      ALPHA(10),
X IUNIN,                IUNOUT,          MASK,          NEG
C * * * * *
      INTEGER POWERS
      DATA (POWERS(I),I=1,11)/0,1,2,4,8,16,32,64,128,256,0/
      DATA (ALPHA(I),I=1,10)/ 1HA,1HB,1HC,1HD,1HE,1HF,1HG,1HH,1HJ,1H /
      DATA IUNIN/5/,IUNOUT/6/,MASK/01/,NEG/040000000000/
      END
1
2
3
4
5
6
7
8
9

$IBFTC NAMER  DEBUG
      COMMON/BDATA/      POWERS(11),      IALPHA(9),      ALPHA(10),
X IUNIN,                IUNOUT,          MASK,          NEG
      COMMON/B1/  NFAC,NCLASS,NN,NDPG,PBAYES,IRUN,PBAYEX,IUTILF,UTSWCH
      COMMON/B2/  DPG(128,32),BLOCK(128,32),IDPG(32),NBLOCK(32),IP(9),
X ID(9),NSUBI(9),LPERM(9),II(10),PSTOP(32),WT(32),PSUMX(32),PSUM(32)
      COMMON/REST/PROB(512), T1(512), PBLOCK(128,32), ISAVEP(9,33),
X UTIL(512), ULIST(128), IULIST(128), IDDCG(4,32)
      INTEGER POWERS, T1, DPG, BLOCK
      LOGICAL UTSWCH, LPERM
      REAL IDENT
      EQUIVALENCE (X,IX)
      DIMENSION DUMP1(1),DUMP2(1)
      EQUIVALENCE (DUMP1(1),NFAC),(DUMP2(1),IDPG(1))
      DIMENSION IT1(9),XT3(9),IDENT(14)
      DATA BLANK/6H /,ENDCRD/6HENDALL/
      COMMON/LINX/ XNOUT(5),HOLOUT(9),FAC(14,9)
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
C *****
LD1= 9
CALL TIME1(TSTART)
TMAX= 0.0
LD2 = 238
3

C *****
C
C   NAMER SECTION 1
C
10 READ(IUNIN,5000) IDENT
IF (IDENT(1).EQ.ENDCRD) STOP
WRITE(IUNOUT,5005) IDENT
5

C *****
C
C   NAMER SECTION 2
C
DO 12 J=1,5
12 XNOUT(J)=BLANK
DO 14 J=1,9
IALPHA(J)= J
8

```


14	HOLDOUT(J)=BLANK	40	
	READ(IUNIN,5010) TMAXX	41	24
	TMAX= TMAX + TMAXX	42	
	WRITE(IUNOUT,5020) TMAXX	43	25
	CALL TIME1(TPRINT)	44	26
	TPRINT=(TPRINT-TSTART)/3600.0	45	
	WRITE(IUNOUT,5025) TPRINT	46	
C		47	
C	*****	48	
C		49	
C	NAMER SECTION 3	50	
C		51	28
	READ(IUNIN,5045) ITYPRN	52	29
	GO TO (30,154,20),ITYPRN	53	
	20 RFAD(IUNIN,5070) (XT3(K),K=1,9)	54	
C		55	
C	*****	56	
C		57	
C	NAMER SECTION 4	58	
C		59	32
	30 READ(IUNIN,5045) NFAC	60	39
	IF((NFAC.LT.1).OR.(NFAC.GT.9)) GO TO 8020	61	
	WRITE(IUNOUT,5050) NFAC	62	43
	IF(ITYPRN.NF.3) GO TO 38	63	
	DO 35 K=1,NFAC	64	
	DO 32 L=1,NFAC	65	
	LL=L	66	
	IF(XT3(K).EQ.ALPHA(L)) GO TO 34	67	
	33 CONTINUE	68	
	GO TO 8010	69	
	24 ISAVFP(K,1)=LL	70	
	25 CONTINUE	71	
	28 CONTINUE	72	
C		73	
C	*****	74	
C		75	
C	NAMER SECTION 5	76	
C		77	
	DO 40 J=1,NFAC	78	
	RFAD(IUNIN,5000) (FAC(I,J),I=1,14)	79	69
	WRITE(IUNOUT,5055) J,(FAC(I,J),I=1,14)	80	74
	40 CONTINUE	81	
C		82	
C	*****	83	
C		84	
C	NAMER SECTION 6	85	
C		86	
	IT(1)=1	87	
	LPERM(1)=.TRUE.	88	
	NSUBI(1)=NFAC	89	
	READ(IUNIN,5045) NCLASS	90	82
	IF((NCLASS.LT.1).OR.(NCLASS.GT.9)) GO TO 8030	91	
	IF(NCLASS-1) 60,60,50	92	
	50 RFAD(IUNIN,5045) (NSUBI(I),I=1,NCLASS)	93	88
	WRITE(IUNOUT,7000) NCLASS,(NSUBI(I),I=1,NCLASS)	94	95
	DO 55 J=1,NCLASS	95	
	LPERM(J)=.TRUE.	96	
	IT(J+1)= IT(J)+NSUBI(J)	97	
	55 CONTINUE	98	
	60 NN= 2*NFAC	99	113
	DO 65 J=1,NN	100	
	T*(J)=C	101	
	PROR(J)=1 0	102	
	UTIL(J)=0 0	103	
	65 CONTINUE	104	
C		105	
C	*****	106	

```

C
C      NAMER SECTION 7
C
READ(IUNIN,5043) NPIN,IUTILF,UCOFF
WRITE(IUNOUT,6045) NPIN,IUTILF
UTSWCH=.FALSE.
IF((IUTILF.LT.1).OR.(IUTILF.GT.5)) GO TO 8035
IF((NPIN.LT.0).OR.(NPIN.GT.NN)) GO TO 8032
IF((UCOFF.LT.0.0).OR.(UCOFF.GT.1.0)) GO TO 8033
IF(IUTILF.GE.3) UTSWCH=.TRUE.
IF(IUTILF.EQ.5) WRITE(IUNOUT,7010) UCOFF
DO 90 J=1,NPIN
READ(IUNIN,5060) (IT1(I),I=1,9),P,UT
IF((P.GT.1.0).OR.(P.LT.0.0)) GO TO 8038
I=0
IT=0
KK=0
DO 67 K=1,9
KKX=10-K
KI=IT1(KKX)+1
I=I+POWERS(KI)
IF(KI-1) 67,67,66
66 IT=IT+IT1(KKX)*10**KK
KK=KK+1
67 CONTINUE
I=I+1
81 GO TO (82,84,86,88,87),IUTILF
82 UTIL(I)=1.0
GO TO 89
84 UTIL(I)=P
GO TO 89
86 UTIL(I)=UT
GO TO 89
87 UTIL(I)=UCOFF*UT+(1.0-UCOFF)*P
GO TO 89
88 UTIL(I)=UT*P
89 CONTINUE
WRITE(IUNOUT,6060) IT,P,UTIL(I)
PROB(I)=1.0-P
90 CONTINUE
C
C*****
C
C      NAMER SECTION 8
C
READ(IUNIN,5045) NDPG
IF((NDPG.LT.1).OR.(NDPG.GT.32)) GO TO 8140
WRITE(IUNOUT,6065) NDPG
DO 150 I=1,NDPG
READ(IUNIN,5000) (IDDCG(K,I),K=1,4)
WRITE(IUNOUT,6064) (IDDCG(K,I),K=1,4)
READ(IUNIN,5065) NGFN,PSTOP(I),WT(I)
IF((NGFN.LT.0).OR.(NGFN.GT.MINO(NFAC,7))) GO TO 8150
IF((PSTOP(I).LT.0.0).OR.(PSTOP(I).GT.1.0)) GO TO 8160
WRITE(IUNOUT,6066) I,NGFN,PSTOP(I),WT(I)
IDPG(I)=2**NGFN-1
C
C*****
C
C      NAMER SECTION 8A
C
IF(NGFN) 106,106,91
91 DO 105 J=1,NGFN
READ(IUNIN,5070) (XT3(K),K=1,9)
WRITE(IUNOUT,6070) (XT2(K),K=1,9)
KI=0
DO 100 K=1,9

```

```

      DO 94 L=1,10
      LL=L
      IF(XT3(K).EQ ALPHA(L)) GO TO 98
94 CONTINUE
      GO TO 9050
      OR KKI=LL+1
      KI = KI + POWERS(KKI)
100 CONTINUE
      DPG(J, I)= KI
105 CONTINUE
106 IDI= IDPG(I)
      IF(IDI-1) 121,121,108
108 KP=4
      N1= NGFN
      LPTR=NGFN+1
      LLEN=0
      DO 120 J=2,NGFN
      KK=J-1
      IF(DPG(J, I),EQ,DPG(1, I)) GO TO 8060
      DO 110 K=1, KK
      DPG(LPTR, I)=IXOR(DPG(J, I),DPG(K, I))
      IF(DPG(LPTR, I),EQ DPG(1, I)) GO TO 8060
110 LPTR=LPTR+1
      IF(LLEN,EQ,0) GO TO 118
      DO 115 K=1, LLEN
      N=NGFN+K
      DPG(LPTR, I)=IXOR(DPG(J, I),DPG(N, I))
      IF(DPG(LPTR, I),EQ,DPG(1, I)) GO TO 8060
115 LPTR=LPTR+1
118 LLEN=2*LLEN+KK
120 CONTINUE
C
C*****
C
C      NAMER SECTION 8B
C
121 READ(IUNIN,5045) NBLOCK(I)
      NB = NBLOCK(I)
      IF((NR.LT.0).OR.(NR.GT.NN)) GO TO 8170
      WRITE(IUNOUT,6080) NB
      IF(NB) 150,150,122
122 DO 140 J=1,NB
      READ(IUNIN,5070) (XT3(K),K=1,9),PBLOCK(J, I)
      IF((PBLOCK(J, I).LT.0,0).OR.(PBLOCK(J, I).GT.1.0)) GO TO 8180
      WRITE(IUNOUT,6070) (XT3(K),K=1,9),PBLOCK(J, I)
      KI=0
      DO 130 K=1,9
      DO 124 l=1,10
      LL=l
      IF(XT3(K).EQ ALPHA(L)) GO TO 128
124 CONTINUE
      GO TO 8070
128 KKI=LL+1
      KI = KI + POWERS(KKI)
130 CONTINUE
      BLOCK(J, I) = KI
140 CONTINUE
150 CONTINUE
      IF(ITYPN,EQ,3) CALL ONCE($10)
C
C*****
C
C      NAMER SECTION 9
C
      PBAYFS=C.0
      DO 152 I=1,NDPG
      PSUM(I)=0.0

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152 CONTINUE	241	
IRUN = 20	242	
CALL TIME1(TPRINT)	243	370
TPRINT=(TPRINT-TSTART)/3600.0	244	
WRITE(IUNOUT,5025) TPRINT	245	372
GO TO 158	246	
C	247	
C*****	248	
C	249	
C NAMER SECTION 10	250	
C	251	
154 CONTINUE	252	
WRITE(IUNOUT,5040)	253	374
CALL BCREAD(DUMP1(1),DUMP1(LD1))	254	376
CALL BCREAD(DUMP2(1),DUMP2(LD2))	255	379
CALL BCREAD(IALPHA(1),IALPHA(NFAC))	256	382
CALL BCREAD(FAC(1,1),FAC(14,NFAC))	257	385
CALL BCREAD(PROB(1),PROB(NN))	258	388
CALL BCREAD(UTIL(1),UTIL(NN))	259	391
CALL BCREAD(ISAVEP(1,1),ISAVEP(NFAC,1))	260	394
CALL BCREAD(IDDCG(1,1),IDDCG(4,NDPG))	261	397
DO 156 I = 1,NDPG	262	
ID1 = IDPG(I)	263	
NB=NBLOCK(I)	264	
IF(ID1.NE.0)CALL BCREAD(DPG(1,I),DPG(ID1,I))	265	409
CALL BCREAD(ISAVEP(1,I+1),ISAVEP(NFAC,I+1))	266	413
IF(NB.EQ.0) GO TO 156	267	
CALL BCREAD(PBLOCK(1,I),PBLOCK(NB ,I))	268	420
CALL BCREAD(BLOCK(1,I),BLOCK(NB ,I))	269	424
156 CONTINUE	270	
C	271	
C*****	272	
158 CONTINUE	273	
C	274	
C*****	275	
C	276	
C NAMER SECTION 11	277	
C EVALUATE THE CURRENT ORDERING	278	
C	279	
DO 100C I=1,NDPG	280	
C	281	
C*****	282	
C	283	
C INITIALIZATIONS	284	
C	285	
IRUN=IRUN+1	286	
PSUMX(I)=0.0	287	
NB=NBLOCK(I)	288	
ID1 = IDPG(I)	289	
ID11=ID1+1	290	
C	291	
C*****	292	
C	293	
C NAMER SECTION 11A	294	
C	295	
C CHECK FOR BLOCK CONFOUNDING. IF THERE ARE NO BLOCK PARAMETERS	296	
C GO TO NAMER SECTION 11B	297	
C	298	
165 IF(NB) 228,228,166	299	
166 DO 226 K=1,NB	300	
KI= BLOCK(K,I)	301	
KI1 = KI+1	302	
T1(KI1)= IRUN	303	
C	304	
C-----	305	
C	306	
C IS THIS A FULL OR FRACTIONAL FACTORIAL	307	

C		308
	IF (IDI) 2035,167,171	309
167	PSUMX(I)= PSUMX(I)+UTIL(KI1)*(1.0-PBLOCK(K,I))	310
	GO TO 226	311
C		312
C	IF BLOCK PARAMETER HAS PRIOR PROB=1.0 THERE CAN BE NO UTILITY	313
C	FOR THIS ESTIMATOR. JUST TAG ALIASES.	314
C		315
171	IF(PBLOCK(K,I)-1.0) 176,173,173	316
172	DO 174 IK=1,IDI	317
	JJ = IEXOR(KI,DPG(IK,I))+1	318
	T1(JJ)= IRUN	319
174	CONTINUE	320
	GO TO 226	321
C		322
C	-----	323
C		324
C	INITIALIZE BEFORE FINDING OPTIMAL MATCHING OF PARAMETER TO ESTIMAT	325
C		326
176	PS= PROB(KI1)	327
	PR= PS	328
	UTILIST(1)= KI1	329
	ULIST(1)= UTIL(KI1)	330
	ISTAP=C	331
	IF(PS) 178,178,179	332
178	ISTAR=1	333
	UTILIST(1)= -UTIL(KI1)	334
	PR=1.0	335
179	IMAX= KI1	336
C		337
C	-----	338
C		339
C	FOR UTILITY FUNCTIONS 1 AND 2, PARAMETER WITH MAXIMUM PROBABILITY	340
C	HAS MAXIMUM UTILITY.	341
C		342
	IF(UTSWCH) GO TO 200	343
	DO 187 KK=1,IDI	344
	JJ = IEXOR(KI,DPG(KK,I))+1	345
	T1(JJ)= IRUN	346
	IF(PROB(JJ)) 2035,184,187	347
187	PR= PR*PROB(JJ)	348
	IF(PROB(JJ)-PS) 186,186,187	349
184	ISTAR= ISTAR+1	350
186	PS= PROB(JJ)	351
	IMAX= JJ	352
187	CONTINUE	353
C		354
C	COMPUTE UTILITY	355
C		356
	IF(ISTAR-1) 190,192,226	357
190	PR= PR/PROB(IMAX)	358
192	PSUMX(I)=PSUMX(I)+PR*UTIL(IMAX)*(1.0-PBLOCK(K,I))	359
	GO TO 226	360
C		361
C	-----	362
C		363
C	FOR ARBITRARY UTILITY FUNCTIONS COMPUTE UTILITY FOR EACH MATCHING	364
C		365
200	DO 206 KK=2,IDI	366
	JJ=IEXOR(KI,DPG(KK-1,I))+1	367
	T1(JJ)= IRUN	368
	UTILIST(KK)= JJ	369
	IF(PROB(JJ)) 204,204,202	370
202	PR= PR * PROB(JJ)	371
	ULIST(KK)= UTIL(JJ)	372
	GO TO 206	373

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511

250	JMAX=K	440	
	IF(UTSWCH) GO TO 430	441	
C		442	
C	-----	443	
C		444	
C	FOR UTILITY FUNCTIONS 1 AND 2, PARAMETER WITH MAXIMUM PROBABILITY	445	
C	HAS MAXIMUM UTILITY.	446	
C		447	
	DO 410 KK=1,IDI	448	
	JJ = IEXOR(KM1,DPG(KK,I))+1	449	609
	T1(JJ)=TRUN	450	
	IF(PROB(JJ)) 380,390,380	451	
390	PR= PR*PROB(JJ)	452	
	IF(PROB(JJ)-PS) 400,410,410	453	
390	ISTAR=ISTAR+1	454	
400	PS=PROB(JJ)	455	
	IMAX=JJ	456	
410	CONTINUE	457	
	GO TO 505	458	
C		459	
C	-----	460	
C		461	
C	FOR ARBITRARY UTILITY FUNCTIONS COMPUTE UTILITY FOR EACH MATCHING	462	
C		463	
430	DO 460 KK=2,IDI1	464	
	JJ= IEXOR(KM1,DPG(KK-1,I))+1	465	628
	T1(JJ)= IRUN	466	
	IULIST(KK)= JJ	467	
	IF(PROB(JJ)) 450,450,440	468	
440	PR= PR*PROB(JJ)	469	
	ULIST(KK)= UTIL(JJ)	470	
	GO TO 460	471	
450	ISTAR= ISTAR+1	472	
	ULIST(KK)= -UTIL(JJ)	473	
460	CONTINUE	474	
	GO TO 600	475	
C		476	
C	-----	477	
C		478	
C	INCREMENT UTILITY OF THIS DCG BY UTILITY OF ESTIMATOR	479	
C		480	
505	IF(ISTAR-1) 520,530,700	481	
520	PR= PR/PROB(IMAX)	482	
530	PSUMX(I)=PSUMX(I)+PR*UTIL(IMAX)	483	
	GO TO 700	484	
C		485	
C		486	
C		487	
600	IF(ISTAR-1) 620,660,700	488	
620	DO 630 KK=1,IDI1	489	
	JJ= IULIST(KK)	490	
	ULIST(KK)= ULIST(KK) * PR/PROB(JJ)	491	
630	CONTINUE	492	
	UMAX=0.0	493	
	DO 640 KK=1,IDI1	494	
	IF(ULIST(KK)-UMAX) 640,640,635	495	
635	UMAX= ULIST(KK)	496	
640	CONTINUE	497	
	PSUMX(I)= PSUMX(I)+UMAX	498	
	GO TO 700	499	
660	DO 670 KK=1,IDI1	500	
	KS= KK	501	
	TST=AND(ULIST(KK),NFG)	502	
	TST=OR(TST,MASK)	503	
	IF(TST) 680,2035,670	504	
670	CONTINUE	505	
690	PSUMX(I)= PSUMX(I) - ULIST(KS)*PR	506	

700 CONTINUE	507	
1000 CONTINUE	508	
C	509	
C*****	510	
C	511	
C NAMER SECTION 12	512	
C	513	
PBAYEX= 0.0	514	
DO 1020 I=1,NDPG	515	
PSUMX(I)= PSUMX(I)*WT(I)	516	
PBAYEX= PBAYEX + PSUMX(I)*PSTOP(I)	517	
1020 CONTINUE	518	
IF(PBAYEX-PBAYES) 1060,1060,1030	519	
1030 PBAYES=PBAYEX	520	
DO 1050 I=1,NFAC	521	
ISAVEP(I,1)=IALPHA(I)	522	
1050 CONTINUE	523	
1060 DO 1100 I=1,NDPG	524	
IF(PSUMX(I)-PSUM(I)) 1100,1100,1070	525	
1070 PSUM(I)=PSUMX(I)	526	
DO 1080 J=1,NFAC	527	
ISAVEP(J,I+1)= IALPHA(J)	528	
1080 CONTINUE	529	
1100 CONTINUE	530	
C	531	
C*****	532	
C	533	
C NAMER SECTION 13	534	
C	535	
DO 1150 K=1,NCLASS	536	
ISEND=II(K)	537	
CALL PERMUT(IALPHA(ISEND),NSUBI(K),LPERM(K),ISEND)	538	742
IF(LPERM(K)) GO TO 1150	539	
GO TO 2000	540	
1150 CONTINUE	541	
GO TO 2000	542	
C	543	
C*****	544	
C	545	
C NAMER SECTION 14	546	
C	547	
2000 CALL TIMEF(TNOW)	548	755
T=(TNOW-TSTART)/3600.	549	
IF(T-TMAX) 158,2010,2010	550	
C*****	551	
C	552	
C NAMER SECTION 15	553	
C	554	
2010 CONTINUE	555	
WRITE(IUNOUT,6090) T,IRUN	556	758
CALL BCDUMP(DUMP1(1),DUMP1(LD1),0)	557	760
CALL BCDUMP(DUMP2(1),DUMP2(LD2),0)	558	763
CALL BCDUMP(IALPHA(1),IALPHA(NFAC),0)	559	766
CALL BCDUMP(FAC(1,1),FAC(14,NFAC),0)	560	769
CALL BCDUMP(PROB(1),PROB(NN),0)	561	772
CALL BCDUMP(UTIL(1),UTIL(NN),0)	562	775
CALL BCDUMP(ISAVEP(1,1),ISAVEP(NFAC,1),0)	563	778
CALL BCDUMP(IDDCG(1,1),IDDCG(4,NDPG),0)	564	781
DO 2030 I=1,NDPG	565	
IDI=IDPG(I)	566	
NB=NBLOCK(I)	567	
IF(IDI.NE.0) CALL BCDUMP(DPG(1,I),DPG(IDI,I),0)	568	793
CALL BCDUMP(ISAVEP(1,I+1),ISAVEP(NFAC,I+1),0)	569	797
IF(NB.EQ.0) GO TO 2030	570	
CALL BCDUMP(PBLOCK(1,I),PBLOCK(NB ,I),0)	571	804
CALL BCDUMP(BLOCK(1,I),BLOCK(NB ,I),0)	572	808
2030 CONTINUE	573	
2035 STOP	574	


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C
C*****
C
C   NAMER SECTION  16
C
3000 CONTINUE
      CALL TIME1(TPRINT)
      TPRINT=( TPRINT-TSTART)/3600.0
      WRITE(IUNOUT,5025) TPRINT
      CALL REMACH
      CALL TIME1(TPRINT)
      TPRINT=( TPRINT-TSTART)/3600.0
      WRITE(IUNOUT,5025) TPRINT
      GO TO 10
C
C*****
5000 FORMAT(13A6,1A2)
5005 FORMAT(14H'NAMER OUTPUT 13A6,1A2/1H )
5010 FORMAT(F6.0)
5020 FORMAT(50H PROGRAM WILL DUMP FOR RESTART IF NOT FINISHED IN F10.0,
      X  9H MINUTES. /1H )
5025 FORMAT(25H CURRENT EXECUTION TIME   F12.2)
5030 FORMAT(L1)
5040 FORMAT(39H THIS IS A RESTART OF A PREVIOUS CASE /1H )
5042 FORMAT(2I6,F10.9)
5045 FORMAT(9I6)
5050 FORMAT(11H THERE ARE  I4,22H FACTORS.  THEY ARE... /1H )
5055 FORMAT(1X,I10,3X,13A6,A2)
5060 FORMAT(9I1,2F10.0)
5065 FORMAT(I6,F6.6,F6.0)
5070 FORMAT(9A1,F5.5)
5045 FORMAT(1HK I6,61H PARAMETERS WITH NON-ZERO PRIOR PROBABILITIES AND
      X UTILITIES /1X/19H UTILITY FUNCTION I2)
6060 FORMAT(1X,I9,2G14.6)
6065 FORMAT(1HK I6,26H DEFINING PARAMETER GROUPS /1X)
6064 FORMAT (1HK 120(1H-)/1HK 4A6)
6066 FORMAT(4KDPG I3/4H      I3,11H GENERATORS /
      X 21H  PROB OF STOPPING F10.5,13H      WEIGHT  F10.6)
6070 FORMAT(5X, 9A1, F10.5)
6080 FORMAT(10HK THERE ARE  I4, 17H BLCK PARAMETERS /1X)
6090 FORMAT(35H TIME EXCEEDED. DUMPING FOR RESTART /13H EXEC. TIME
      X  F7.2,5H MIN. /8H IRUM = I15)
7000 FORMAT(11HK THERE ARE  I3,21H CLASSES OF VARIABLES /5X,9I6)
7010 FORMAT(9HK UCOEF=  F12.9)
C*****
C   ERROR MESSAGES
C
8010 WRITE(IUNOUT,9010)
9010 FORMAT(40H ILLEGAL CHARACTER IN SPECIFIED MATCHING )
      GO TO 2035
8020 WRITE(IUNOUT,9020) NFAC
9020 FORMAT(33H NUMBER OF FACTORS OUT OF RANGE  I6)
      GO TO 2035
8030 WRITE(IUNOUT,9030) NCLASS
9030 FORMAT(29H NUMBER CLASSES OUT OF RANGE  I6)
      GO TO 2035
8032 WRITE(IUNOUT,9032) NPIN
9032 FORMAT(48H IMPROPER NUMBER OF NONZERO PRIOR PROBABILITIES  I6)
      GO TO 2035
8033 WRITE(IUNOUT,9033) UCOFF
9033 FORMAT(20H UCOEF OUT OF RANGE  G14.6)
      GO TO 2035
8035 WRITE(IUNOUT,9035) IUTILF
9035 FORMAT(37H UTILITY FUNCTION CHOICE ILLEGAL  I6)
      GO TO 2035
8038 WRITE(IUNOUT,9038) P

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9038	FORMAT(33H ILLEGAL INPUT PRIOR PROBABILITY G14.6)	641	
	GO TO 2035	642	
8050	WRITE(IUNOUT,9050)	643	837
9050	FORMAT(52H ILLEGAL CHARACTER USED TO INPUT A GENERATOR FOR DPG)	644	
	GO TO 2035	645	
8060	WRITE(IUNOUT,9060)	646	839
9060	FORMAT(28H GENERATORS NOT INDEPENDENT)	647	
	GO TO 2035	648	
8070	WRITE(IUNOUT,9070)	649	841
9070	FORMAT(45H ILLEGAL CHARACTER USED TO INPUT BLOCK EFFECT)	650	
	GO TO 2035	651	
8140	WRITE(IUNOUT,9140)	652	843
9140	FORMAT(20H INVALID NO. OF DPGS)	653	
	GO TO 2035	654	
8150	WRITE(IUNOUT,9150)	655	845
9150	FORMAT(26H INVALID NO. OF GENERATORS)	656	
	GO TO 2035	657	
8160	WRITE(IUNOUT,9160)	658	847
9160	FORMAT(27H STOPPING PROB OUT OF RANGE)	659	
	GO TO 2035	660	
8170	WRITE(IUNOUT,9170)	661	849
9170	FORMAT(29H INVALID NO. OF BLOCK EFFECTS)	662	
	GO TO 2035	663	
8180	WRITE(IUNOUT,9180)	664	851
9180	FORMAT(31H BLOCK EFFECT PROB OUT OF RANGE)	665	
	GO TO 2035	666	
	END	667	

\$IBFTC LINER

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SUBROUTINE LINE(I,U)
COMMON/BDATA/POWERS(11),IALPHA(9),ALPHA(10),IUNIN,IUNOUT,MASKK,NEG
COMMON/B1/ NFAC,NCLASS,NN,NDPG,PBAYES,IRUN,PBAYEX,IUTILF,UTSWCH
COMMON/LINX/ XNOUT(5),HOLOUT(9),FAC(14,9)
DIMENSION XNUMBER(9),BLANK(3),BLOCKS(4)
DATA(BLOCKS(I),I=1,4)/6HCONF0U,6HNDED W,6HITH BL,6HOCKS /
DATA(BLANK(I),I=1,3)/0777777606060,0606060777777,6H /
DATA(XNUMBER(I),I=1,9)/ 0605401777777, 0777777605402,
X 0605403777777, 0777777605404, 0605405777777, 0777777605406 ,
X 0605407777777, 0777777605410, 0605411777777 /
DATA MASK/03/,ZERO/6H 0* /,GMEAN/6HG MEAN/
EQUIVALENCE (X,IX) ,(Y,IY)
C
C*****
IX=I
IF(IX.EQ.0) WRITE(IUNOUT,5005) ZERO,GMEAN,U
IF(IX.EQ.0) RETURN
NF= NFAC
JJ=1
NF1=NF-1
DO 100 J=1,NF1,2
NF= NF-2
Y=AND(MASK,X)
IY=IY+1
GO TO (20,40,6C,80),IY
20 XNOUT(JJ)= BLANK(3)
HOLOUT(J)= BLANK(3)
HOLOUT(J+1)= BLANK(3)
GO TO 55

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C	40	XNOUT(JJ)= AND (BLANK(1),XNUMER(J))	31	
		HOLOUT(J)= FAC(1,J)	32	
		HOLOUT(J+1)= BLANK(3)	33	
		GO TO 55	34	
C	60	XNOUT(JJ)= AND(BLANK(2),XNUMER(J+1))	35	
		HOLOUT(J)= BLANK(3)	36	
		HOLOUT(J+1)= FAC(1,J+1)	37	
		GO TO 55	38	
C	80	XNOUT(JJ)= AND(XNUMER(J),XNUMER(J+1))	39	
		HOLOUT(J)= FAC(1,J)	40	
		HOLOUT(J+1)= FAC(1,J+1)	41	
C	95	IX=IARS(2,X)	42	
		JJ= JJ+1	43	
100		CONTINUE	44	
		IF(NF) 500,130,105	45	
105		X= AND(MASK,X)	46	43
		IX= IX+1	47	
		GO TO (110,120), IX	48	
110		XNOUT(JJ)= BLANK(3)	49	
		HOLOUT(NFAC)= BLANK(3)	50	
		GO TO 130	51	
120		XNOUT(JJ)= AND(BLANK(1),XNUMER(NFAC))	52	
		HOLOUT(NFAC)= FAC(1,NFAC)	53	
C	130	CONTINUE	54	
		WRITE(IUNOUT,5000)(XNOUT(I),I=1,5),(HOLOUT(I),I=1,9),U	55	
490		RETURN	56	
5000		FORMAT(1H 5A6,6X,9A6,G14.6)	57	
5005		FORMAT(1H A6,30X,A6,48X,G14.6)	58	
5010		FORMAT(1H 40X,A6)	59	
		ENTRY ALINE(IA,IALIAS)	60	
		DIMENSION IALIAS(1)	61	60
		DO 800 K=1,IA	62	
		IX=IALIAS(K)	63	
		IF(IX.EQ.0) WRITE(IUNOUT,5010) ZERO	64	
		IF(IX.EQ.0) RETURN	65	
		NF = NFAC	66	
		JJ = 1	67	
		NF1= NF-1	68	
		DO 700 J=1,NF1,2	69	
		NF = NF-2	70	
		Y= AND(MASK,X)	71	80
		IY= IY+1	72	
		GO TO (620,640,660,680),IY	73	
620		XNOUT(JJ)=BLANK(3)	74	
		GO TO 695	75	
640		XNOUT(JJ)= AND(BLANK(1),XNUMER(J))	76	
		GO TO 695	77	
660		XNOUT(JJ)=AND(BLANK(2),XNUMER(J+1))	78	
		GO TO 695	79	
680		XNOUT(JJ) = AND(XNUMER(J),XNUMER(J+1))	80	
695		IX=IARS(2,X)	81	
		JJ=JJ+1	82	
700		CONTINUE	83	
		IF(NF) 500,730,705	84	
705		X=AND(MASK,X)	85	
		IX=IX+1	86	
		GO TO (710,720),IX	87	107
710		XNOUT(JJ)= BLANK(3)	88	
		GO TO 730	89	
720		XNOUT(JJ)= AND(BLANK(1),XNUMER(NFAC))	90	
730		WRITE(IUNOUT,850)(XNOUT(I),I=1,5)	91	
			92	
			93	
			94	
			95	
			96	
			97	120

900 CONTINUE	98
950 FORMAT (40X,5A6)	99
RETURN	100
500 STOP	101
END	102

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SUBROUTINE RECT(N,X,Y,NFAC)	1	
DIMENSION X(9,33),Y(33,33),XOUT(9)	2	
COMMON/PDATA/POWERS(1,1),IALPHA(9),ALPHA(10),IUNIN,IUNOUT,MASK,NEG	3	
DATA JS/9/	4	
LOGICAL OUT	5	
OUT= .FALSE.	6	
JTIMFS=0	7	
JCOL= N	8	
IW=1	9	
5 IWW=1	10	
JNXT=JCOL-9	11	
IF(JNXT) 10,10,30	12	
10 JP= JCOL	13	
OUT=.TRUE.	14	
GO TO 50	15	
20 JCOL= JNXT	16	
JP=JP	17	
50 GO TO (52,54), IW	18	
52 IW=JP-1	19	
WRITE(IUNOUT,1001) (J,J=1,IW)	20	15
WRITE(IUNOUT,1002)	21	21
IW=2	22	
GO TO 56	23	
54 J1=JTIMFS	24	
JL=J1+JP-1	25	
WRITE(IUNOUT,1003) (J,J=J1,JL)	26	25
WRITE(IUNOUT,1002)	27	31
56 DO 100 I=1,NFAC	28	
DO 70 J=1,JP	29	
JJ=JTIMFS+J	30	
70 XOUT(J)= X(I,JJ)	31	
WRITE(IUNOUT,1005)(XOUT(K),K=1,JP)	32	41
100 CONTINUE	33	
WRITE(IUNOUT,1002)	34	48
DO 200 I=1,N	35	
DO 170 J=1,JP	36	
JJ= JTIMFS+J	37	
170 XOUT(J)= Y(I,JJ)	38	
GO TO (172,174), IWW	39	
172 WRITE(IUNOUT,1007)(XOUT(K),K=1,JP)	40	59
IWW=2	41	
WRITE(IUNOUT,1008)	42	65
GO TO 200	43	
174 J1 = I-1	44	
WRITE(IUNOUT,1009)J1,(XOUT(K),K=1,JP)	45	68
200 CONTINUE	46	
IF(OUT) RETURN	47	
JTIMFS= JTIMFS+JP	48	
GO TO 5	49	
1001 FORMAT(21H)SUMMARY OUTPUT TABLE / 1HK/8X,12H** BAYES ***,8(6H ***	50	
X* I2,6H *****)	51	
1002 FORMAT(1H)	52	
1003 FORMAT(21H)SUMMARY OUTPUT TABLE /1HK/9(6H ****I2,6H *****)	53	

1005	FORMAT(6X,9(7X,A1,6X))	54
1007	FORMAT(17HKEXPECTED UTILITY /18H OVER STOPPING PTS /1HK/ X 6X,9G14.5)	55
1008	FORMAT(17HKEXPECTED UTILITY /20H AT EACH STOPPING PT)	56
1009	FORMAT (1H I3,2X,9G14.5)	57
	END	58
		59

\$IBFTC PERM DEBUG

	SUBROUTINE PERMUT(IA,N,LOG,ISEND)	1
	COMMON/BDATA/ POWERS(11), IALPHA(9), ALPHA(10),	2
	X IUNIN, IUNOUT, MASK, NEG	3
	COMMON/B1/ NFAC,NCLASS,NN,NDPG,PBAYES,IRUN,PBAYEX,IUTILF,UTSWCH	4
	COMMON/B2/ DPG(128,32),BLOCK(128,32),IDPG(32),NBLOCK(32),IP(9),	5
	XID(9),NSUBI(9),LPERM(9),II(10),PSTOP(32),WT(32),PSUPX(32),PSUM(32)	6
	INTEGER POWERS,DPG,BLOCK	7
	LOGICAL LOG	8
	EQUIVALENCE (X,IX),(SI,IS),(SJ,JS)	9
	DIMENSION IA(1),MASK1(15),MASK2(15)	10
	EQUIVALENCE (MASK1,POWERS(2))	11
	DATA(MASK2(I),I=1,9)/07777777774,07777777771,07777777763,	12
	X 07777777747,07777777717,07777777637,07777777477,	13
	X 07777777177,07777776377 /	14
C		15
C	*****	16
	NT=N	17
	IF(NT-1) 500,500,5	18
	5 IF(.NOT.LOG) GO TO 20	19
	DO 10 K=2,NT	20
	IP(K)= 0	21
	ID(K)=1	22
	10 CONTINUE	23
	LOG= .FALSE.	24
C		25
C	*****	26
	20 K=0	27
	30 IQ= IP(NT) + ID(NT)	28
	IP(NT)= IQ	29
	IF(IQ-NT) 80,40,80	30
	40 ID(NT)= -1	31
	45 IF(NT-2)60,60,50	32
	50 NT=NT-1	33
	GO TO 30	34
	60 IQ=1	35
	LOG= .TRUE.	36
	GO TO 150	37
	80 IF(IQ) 150,85,150	38
	85 ID(NT)=1	39
	K= K+1	40
	GO TO 45	41
C		42
C	*****	43
	150 IQ= IQ+K	44
	I= IA(IQ)	45
	IA(IQ)= IA(IQ+1)	46
	IA(IQ+1)= I	47
	I2= ISEND+IQ	48
	M1= MASK1(I2-1)	49
	M2= MASK1(I2)	50
	M3= MASK2(I2-1)	51
	DO 400 I=1,NDPG	52
	IDI=IDPG(I)	53
	IB= NBLOCK(I)	54

```

C
C* * * * *
C
      IF( IDI) 240,240,190
190 DO 200 M=1,IDI
      IX = DPG(M,I)
      SI= AND(M1,IX)
      SJ= AND(M2,IX)
      X= AND(M3,IX)
      IS= IS*2
      JS=JS/2
      DPG(M, I)=IX+IS+JS
200 CONTINUE
C
C* * * * *
240 IF( IB) 400,400,250
250 DO 300 M=1,IB
      IX= BLOCK(M, I)
      SI= AND(M1,IX)
      SJ= AND(M2,IX)
      X= AND(M3,IX)
      IS= IS*2
      JS=JS/2
      BLOCK(M, I) = IX+IS+JS
300 CONTINUE
400 CONTINUE
500 RETURN
      END

```

\$IRFTC REMAX DERUG

```

SUBROUTINE REMACH
COMMON/BDATA/ POWERS(11), IALPHA(9), ALPHA(10),
X IUNIN, IUNOUT, MASK, NEG
COMMON/B1/ NFAC,NCLASS,NN,NDPG,PBAYES,IRUN,PBAYEX,IUTILF,UTSWCH
COMMON/B2/ DPG(128,32),BLOCK(128,32),IDPG(32),NBLOCK(32),IP(9),
XTD(9),NSUBI(9),LPERM(9),II(10),PSTOP(32),WT(32),PSUMX(32),PSUM(32)
COMMON/REST/PROB(512), T1(512), PBLOCK(128,32), ISAVEP(9,33),
X UTIL(512), ULIST(128), IULIST(128), IDDCG(4,32)
INTEGER POWERS, T1, DPG, BLOCK
COMMON/LINX/ XNOUT(5),HOLOUT(9),FAC(14,9)
LOGICAL UTSWCH,ONLY1
DIMENSION K2CYCL(9), KPERM(9)
DIMENSION MASK0(9), MASK1(9), KKSAVE(9)
EQUIVALENCE(MASK0,POWERS(2))
DATA (MASK1(I),I=1,9) / 0777777776,0777777775,0777777773,
X 0777777767,0777777757,0777777737,0777777677,0777777577,
X 0777777377 /
EQUIVALENCE (X,IX),(IS,SI),(JS,SJ)
DIMENSION IALIAS(128),SUMALF(9,33),SUMVAL(33,33)
C
C*****
C
C REMACH SECTION 1
C
ONLY1= .FALSE.
NDPG1= NDPG+1
GO TO 4
ENTRY ONCE(*)
NDPG1=1
ONLY1=.TRUE.

```

4	DD 10 LL=1,NFAC	31
	KKS= ISAVFP(LL,1)	32
	KPERM(KKS)=LL	33
10	KKSAVE(KKS)=LL	34
C		35
C	*****	36
C		37
	DD 250C L=1,NDPG1	38
C		39
C	*****	40
C		41
C	REMACF SECTION 2	42
C		43
	IF(ONLY1) GO TO 25	44
	NOUT= L-1	45
	IF(NOUT.EQ.0) WRITE(IUNOUT,5030)	46 23
	IF(NOUT.NE.0) WRITE(IUNOUT,5035) NOUT,(IDDCG(K,NOUT),K=1,4)	47 25
25	WRITE(IUNOUT,4090)	48 31
	DD 100 LL=1,NFAC	49
	KKS = ISAVEP(LL,L)	50
	WRITE(IUNOUT,4095)LL, FAC(1,LL),ALPHA(KKS)	51 35
	SUMALF(LL,L)= ALPHA(KKS)	52
100	CONTINUE	53
C		54
C	*****	55
C		56
C	REMACF SECTION 3	57
C		58
	DD 120 LLL=1,NFAC	59
	K?CYCL(LLL)= KPERM(LLL)	60
	DD 115 K= LLL,NFAC	61
	IF(KPERM(K)-LLL) 115,112,115	62
112	KPERM(K)= KPERM(LLL)	63
	GO TO 120	64
115	CONTINUE	65
120	CONTINUE	66
C		67
C	*****	68
C		69
C	REMACF SECTION 4	70
C		71
	NF1=NFAC-1	72
	DD 158 LLL=1,NF1	73
	I= NFAC-LLL	74
	J= K?CYCL(I)	75
	KK= J-I	76
	IF(KK) 158,158,130	77
130	MOI= MASK0(I)	78
	MOJ= MASK0(J)	79
	M1I= MASK1(I)	80
	M1J= MASK1(J)	81
C		82
C	*****	83
C		84
	DD 157 L4= 1,NDPG	85
	I4=IDPG(L4)	86
	IF(I4) 157,152,148	87
148	DD 150 L5=1,I4	88
	IX= DPG(L5,L4)	89
	SI= AND(MOI,X)	90
	SJ= AND(MOJ,X)	91
	X= AND(AND(M1I,X),M1J)	92
	IS=IALS(KK,SI)	93 85
	JS=IALS(KK,SJ)	94 87
	DPG(L5,L4)=IX+IS+JS	95
150	CONTINUE	96
C		97

178	ISTAR=1	163
	ULIST= -UTIL(KI1)	164
	IALIAS(1)= KI1	165
	PR=7,0	166
179	IMAX= KI1	167
C		168
C	-----	169
C		170
	IF(UTSWCH) GO TO 200	171
	DD 187 KK=1,IDI	172
	JJ=IEXOR(KI,DPG(KK,I))+1	173
	T1(JJ)= TRUN	174
	IF(PROB(JJ)) 7010,184,182	175
182	PR= PR*PROB(JJ)	176
	IF(PROB(JJ)-PS) 186,183,187	177
183	IA=IA+1	178
	IALIAS(IA)=JJ	179
	GO TO 187	180
184	ISTAR= ISTAR+1	181
	IALIAS(ISTAR)=JJ	182
186	PS= PROB(JJ)	183
	IMAX= JJ	184
	IA=0	185
187	CONTINUE	186
C		187
C	-----	188
C		189
	IF(ISTAR-1) 190,192,189	190
189	U=0.0	191
	IA = ISTAR -1	192
	INUT= IMAX	193
	GO TO 220	194
190	PR= PR/PROB(IMAX)	195
192	U=PR*UTIL(IMAX)*(1.0-PBLOCK(K,I))	196
	INUT=IMAX	197
	GO TO 220	198
C		199
C	-----	200
C		201
200	DD 206 KK=2,IDI1	202
	JJ=IEXOR(KI,DPG(KK-1,I))+1	203
	T1(JJ)= TRUN	204
	IULIST(KK)= JJ	205
	IF(PROB(JJ)) 7010,204,202	206
207	PR= PR * PROB(JJ)	207
	ULIST(KK)= UTIL(JJ)	208
	GO TO 206	209
204	ISTAR= ISTAR+1	210
	IALIAS(ISTAR)=JJ	211
	IMAX = JJ	212
	ULIST(KK)= -UTIL(JJ)	213
206	CONTINUE	214
C		215
C	-----	216
C		217
	IF(ISTAR-1) 208,214,189	218
208	DD 210 KK=1,IDI1	219
	JJ= IULIST(KK)	220
	ULIST(KK)= ULIST(KK)*PR/PROB(JJ)	221
210	CONTINUE	222
	UMAX=0,0	223
	INUT=IULIST(1)	224
	DD 213 KK=1,IDI1	225
	IF(IULIST(KK) - UMAX) 213,212,211	226
211	UMAX= ULIST(KK)	227
	IA=0	228
	INUT=IULIST(KK)	229
	GO TO 213	230

172

207

385	IA=IA+1	297
	IAL IAS(IA)=JJ	298
	GO TO 410	299
390	ISTAR=ISTAR+1	300
	IAL IAS(ISTAR)=JJ	301
400	PS=PROB(JJ)	302
	IMAX=JJ	303
	IA=0	304
410	CONTINUE	305
	GO TO 505	306
C	-----	307
C		308
C		309
430	DO 460 KK=2, ID11	310
	JJ=IFXOR(KM1,DPG(KK-1,I))+1	311
	T1(JJ)=TRUN	312
	IULIST(KK)=JJ	313
	IF(PROB(JJ)) 450,450,440	314
440	PR=PR*PROB(JJ)	315
	ULIST(KK)=UTIL(JJ)	316
	GO TO 460	317
450	ISTAR=ISTAR+1	318
	IAL IAS(ISTAR)=JJ	319
	IMAX=JJ	320
	ULIST(KK)=-UTIL(JJ)	321
460	CONTINUE	322
	GO TO 600	323
C	-----	324
C		325
C		326
505	IF(ISTAR-1) 520,530,510	327
510	U=0.0	328
	IA=ISTAR-1	329
	IOUT=IMAX	330
	GO TO 690	331
520	PR=PR/PROB(IMAX)	332
530	U=PR*UTIL(IMAX)	333
	IOUT=IMAX	334
	GO TO 690	335
C	-----	336
C		337
C		338
600	IF(ISTAR-1) 620,660,510	339
620	DO 630 KK=1, ID11	340
	JJ=IULIST(KK)	341
	ULIST(KK)=ULIST(KK)*PR/PROB(JJ)	342
630	CONTINUE	343
	UMAX=0.0	344
	IOUT=IULIST(1)	345
	DO 650 KK=1, ID11	346
	IF(ULIST(KK)-UMAX) 650,640,635	347
635	UMAX=ULIST(KK)	348
	IA=0	349
	IOUT=IULIST(KK)	350
	GO TO 650	351
640	IA=IA+1	352
	IAL IAS(IA)=IULIST(KK)	353
650	CONTINUE	354
	U=UMAX	355
	GO TO 690	356
C	-----	357
C		358
C		359
660	DO 670 KK=1, ID11	360
	KS=KK	361
	TST=AND(ULIST(KK),NFG)	362
	TST=OR(TST, MASK)	363
	IF(TST) 680,680,670	364

351

670 CONTINUE	365	
680 IOUT=IULIST(KS)	366	
U=-ULIST(KS)*PR	367	
C	368	
C-----	369	
C	370	
690 PSUMX(I)=PSUMX(I)+U	371	
IOUT=ICUT-1	372	
CALL LINE(IOUT,U)	373	426
IF(IA) 700,700,695	374	
695 DO 696 IIA=1,IA	375	
696 IALIAS(IIA)=IALIAS(IIA)-1	376	
CALL ALINF(IA,IALIAS)	377	436
700 CONTINUE	378	
1000 CONTINUE	379	
C	380	
C*****	381	
C	382	
C REMACH SECTION 6	383	
C	384	
PBAYEX= 0.0	385	
DO 1020 I=1,NDPG	386	
PSUMX(I)= PSUMX(I)*WT(I)	387	
PBAYEX= PBAYEX + PSUMX(I)*PSTOP(I)	388	
SUMVAL(I+1,L)= PSUMX(I)	389	
1020 CONTINUE	390	
SUMVAL(1,L)= PBAYEX	391	
WRITE(IUNOUT,5000) PBAYEX	392	453
WRITE(IUNOUT,5005) (I,PSUMX(I),I=1,NDPG)	393	
C	394	
C*****	395	
C	396	
C REMACH SECTION 7A	397	
C	398	454
IF(L-NDPG1) 1050,2700,2700	399	
1050 DO 1070 LL=1,NFAC	400	
J=ISAVEP(LL,L+1)	401	
KPERM(J)=LL	402	
1070 CONTINUE	403	
C	404	
C*****	405	
C	406	
C REMACH SECTION 7B	407	
DO 2000 LL=1,NFAC	408	
DO 1090 L4=1,NFAC	409	
IF(KKSAVE(L4)-LL) 1080,1075,1080	410	
1075 K2CYCL(LL)= KPERM(L4)	411	
GO TO 2000	412	
1080 CONTINUE	413	
2000 CONTINUE	414	
C	415	
C*****	416	
C	417	
C REMACH SECTION 7C	418	
DO 2010 LL=1,NFAC	419	
KKSAVE(LL)=KPERM(LL)	420	
KPERM(LL)= K2CYCL(LL)	421	
2010 CONTINUE	422	
C	423	
C*****	424	
C	425	
2500 CONTINUE	426	
2700 IF(ONLY1) RETURN	427	
CALL RECT(NDPG1,SUMALF,SUMVAL,NFAC)	428	456
RETURN	429	
C	430	
C*****	431	

5000	FORMAT(52HL FOR THE ABOVE PERMUTATION THE EXPECTED UTILITY IS	432	
	X G14.5)	433	
5005	FORMAT(53HK THE EXPECTED UTILITIES AT THE STOPPING POINTS ARE.. /	434	
	X (28H DEFINING PARAMETER GROUP I3,3X,G14.5))	435	
5010	FORMAT(16H ERROR IN OUTPUT)	436	
5020	FORMAT(30HKDEFINING PARAMETER GROUP NO. I3)	437	
5022	FORMAT (1H 4A6/60(2H *))	438	
5025	FORMAT(65(2H -))	439	
5030	FORMAT(37HI THIS MATCHING IS THE BAYES MATCHING)	440	
5035	FORMAT(52HI THIS MATCHING MAXIMIZES THE EXPECTED VALUE AT THE I2,	441	
	X 16H STOPPING POINT 4A6)	442	
4095	FORMAT(1H I6,1X,A6,19X,A1)	443	
4090	FORMAT(38HKVARIABLE SHOULD BE CALLED)	444	
C	*****	445	
C		446	
C	ERROR MESSAGE	447	
7010	WRITE(IUNOUT,8010)	448	498
8010	FORMAT(52H PROGRAM ERROR--PREVIOUSLY GOOD DATA HAS BECOME BAD)	449	
	STOP	450	
	END	451	

APPENDIX C

PROGRAM SYMBOLS

This appendix presents a listing of the major program variables used in NAMER. Dimensioned variables have their dimensions specified.

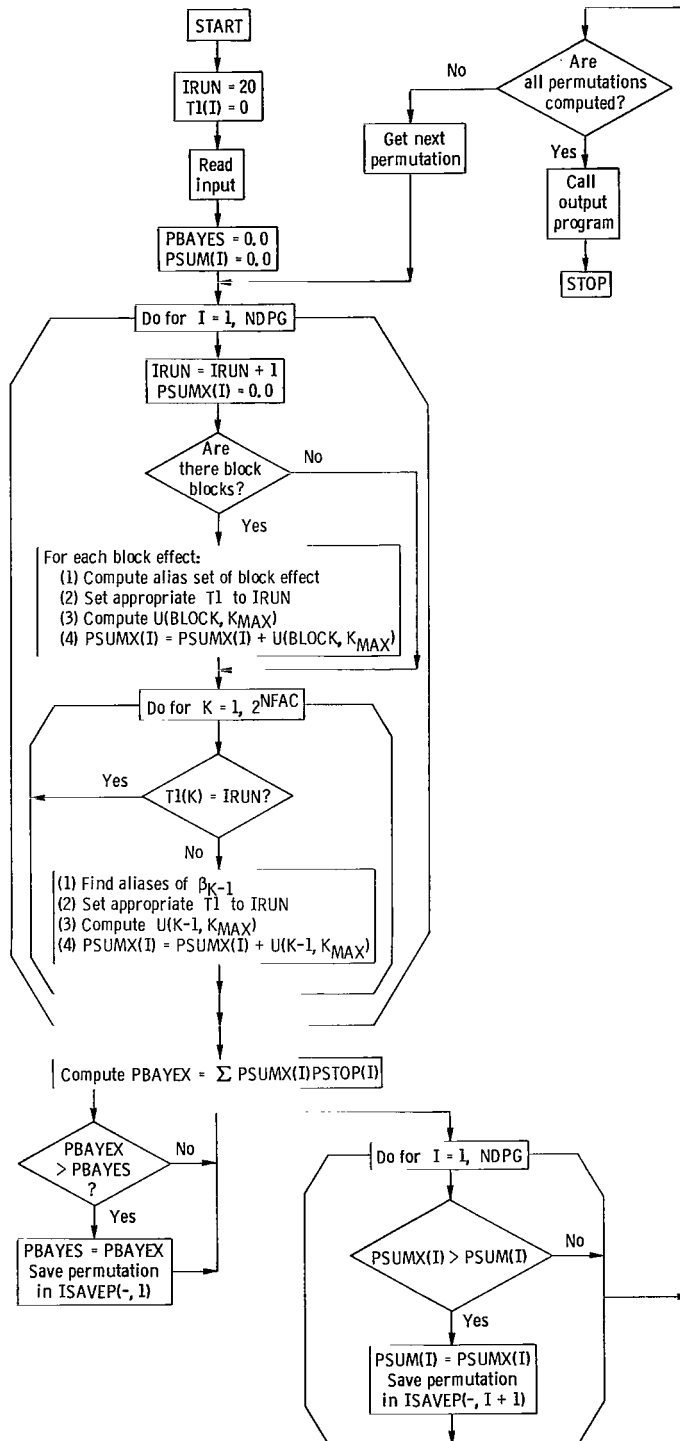
ALPHA(10)	First nine letters of the alphabet (excluding I) and a blank; used for output of optimal matchings.
BLOCK(128, 32)	Standard-order subscripts of representative members of alias sets confounded with blocks.
DPG(128, 32)	Standard-order subscripts of parameters in d. p. g. 's.
DUMP1, DUMP2	See section 5 of SPECIAL LEWIS RESEARCH CENTER ROUTINES.
FAC(14, 9)	Hollerith identification of factors.
HOLOUT(9)	Temporary storage for Hollerith output; used in LINER and initialized in NAMER.
IALIAS(128)	Standard-order number subscripts of parameters in an alias set, besides IOUT, which also maximize expected utility of eq. (6) or eq. (7).
IALPHA(9)	The integers 1 to 9; these are permuted by PERMUT and used to indicate optimal matchings for output.
ID(9)	Indicator vector used in PERMUT.
IDDCG(4, 32)	Hollerith identification of stopping points.
IDENT(14)	Hollerith identification of current problem.
IDPG(32)	Number of elements in each d. p. g. (not including identity).
II(10)	Subscripts of beginning locations of classes of factors.
IMAX, IOUT	Subscript of parameter which maximizes eq. (6) or eq. (7).
IP(9)	Indicator vector used in PERMUT.
IRUN	Running counter used as indicator of parameters evaluated.
ISAVEP(9, 33)	Optimal matchings.
ISTAR	Counter for number of parameters in an alias set with prior probability 1.0 of being nonzero.
ITYPRN	Type of run; see section 3 of INPUT DESCRIPTION.

IULIST(128)	Vector of subscripts of parameters in an alias set.
IUNIN	Variable input unit designation.
IUNOUT	Variable output unit designation.
IUTILF	Choice of function; see section 7 of INPUT DESCRIPTION.
KKSAVE(9)	Saves permutation vector required to achieve optimal matching.
KPERM(9)	Permutation vector.
K2CYCL(9)	Transposition vector for permutation in KPERM.
LD1, LD2	Delimiters for DUMP1 and DUMP2 vectors; see section (5) of SPECIAL LEWIS RESEARCH CENTER ROUTINES.
LPERM(9)	Logical variables controlling calls to PERMUT.
NBLOCK(32)	Number of alias sets confounded with blocks for each d. p. g.
NCLASS	Number of classes of factors; see section 3 of INPUT DESCRIPTION.
NDPG	Number of d. p. g. 's.
NFAC	Number of factors.
NN	2^{NFAC}
NSUBI(9)	Number of factors per class.
ONLY1	Logical variable set to .TRUE. if only a single specified matching is to be evaluated.
P	Temporary storage of input prior probability.
PBAYES	Overall expected utility of best matching evaluated so far.
PBAYEX	Overall expected utility of current matching.
PBLOCK(128, 32)	Prior probabilities of block effects being nonzero.
PR	Temporary storage used for calculation of $\prod (1 - p_i)$.
PROB(512)	Vector of $(1 - p_i)$.
PSTOP(32)	Probabilities of stopping exactly at each stopping point.
PSUM(32)	Expected utility at each stopping point of the best matching for that stopping point found so far.
PSUMX(32)	Expected utility at each stopping point of the current matching.
SUMALF(9, 33)	Saves optimal orderings for output of summary table.

SUMVAL(33,33)	Saves expected utilities of various optimal orderings for output of summary table.
TMAX	Maximum total running time permitted.
TMAXX	Maximum running time for current case.
T1(512)	Indicator array used in finding all distinct alias sets.
UCOEF	Constant used to define utility function 5; see section 7 of INPUT DESCRIPTION.
ULIST(128)	Vector of utilities corresponding to choices of parameters indicated in vector IULIST.
UMAX	Maximum of ULIST.
UT	Temporary storage used in input of utilities.
UTIL(512)	Vector of u_i .
UTSWCH	Logical variable used to indicate whether utility function 1 or 2 or utility function 3, 4, or 5 is being used.
WT(32)	Weighting values for the stopping points; see section 7 of INPUT DESCRIPTION.
XNOUT(5)	Temporary storage used in LINER for output of numerical identification of parameters chosen to be estimated.

APPENDIX D

PROGRAM GENERAL FLOW DIAGRAM



REFERENCES

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2. Holms, Arthur G. : Designs of Experiments as Telescoping Sequences of Blocks for Optimum Seeking (As Intended for Alloy Development). NASA TN D-4100, 1967.
3. Holms, Arthur G. ; and Sidik, Steven M. : Design of Experiments as "Doubly Telescoping" Sequences of Blocks with Application to a Nuclear Reactor Experiment. *Technometrics*, vol. 13, no. 3, Aug. 1971, pp. 559-574.
4. Ord-Smith, R. J. : Generation of Permutation Sequences: Part 1. *Computer J.*, vol. 13, no. 2, May 1970, pp. 152-155.
5. Trotter, H. F. : Algorithm 115 - PERM. *Comm. ACM*, vol. 5, no. 8, Aug. 1962, pp. 434-435.
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TABLE I. - SAMPLE INPUT FOR PROBLEM
DESCRIBED IN APPENDIX A

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
NAMES SAMPLE PROBLEM																							
2																							
1																							
5																							
TEMP	SOURCE	TEMPERATURE																					
PRESS	SOURCE	PRESSURE																					
TIME	TIME DURATION																						
VEL	SOURCE	VELOCITY																					
ANGLE	SOURCE	ANGLE																					
1																							
15																							
0																							
1																							
2																							
12																							
3																							
13																							
23																							
123																							
4																							
14																							
34																							
134																							
5																							
15																							
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24

35																							
.30																							
3																							
1/4 REP - ROW 1																							
2																							
.30																							
.125																							
ABC																							
CDE																							
2																							
AD																							
.50																							
1.0																							
1/2 REP - ROWS 1,2																							
1																							
.40																							
.0625																							
ABDE																							
3																							
AD																							
.50																							
1.0																							
ABC																							
1.0																							
FULL - ALL ROWS																							
0																							
.30																							
.03125																							
5																							
AD																							
.50																							
1.0																							
ABC																							
1.0																							
ABDE																							
1.0																							
CDE																							
1.0																							
ENDALL																							
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24

TABLE II. - ESTIMATE OF TIME REQUIRED BY PROGRAM - BASED ON
 RUNNING OF SAMPLE PROBLEMS

Utility function		Number of independent variables				
		5	6	7	8	9
2	Total time to evaluate all permutations, min	0.02	0.23	3.90	60.32	-----
	Time required to print out results, min	0.04	0.07	0.19	0.44	-----
	Number of d. p. g. 's	4	4	5	5	-----
	Time to evaluate all permutations divided by number of d. p. g. 's, min	0.005	0.058	0.780	12.06	^a 151.0
3	Total time to evaluate all permutations, min	0.03	0.27	4.64	75.67	-----
	Time required to print out results, min	0.04	0.08	0.22	0.47	-----
	Number of d. p. g. 's	4	4	5	5	-----
	Time to evaluate all permutations divided by number of d. p. g. 's	0.008	0.068	0.928	15.13	^a 224.0

^aEstimated from fig. 2.

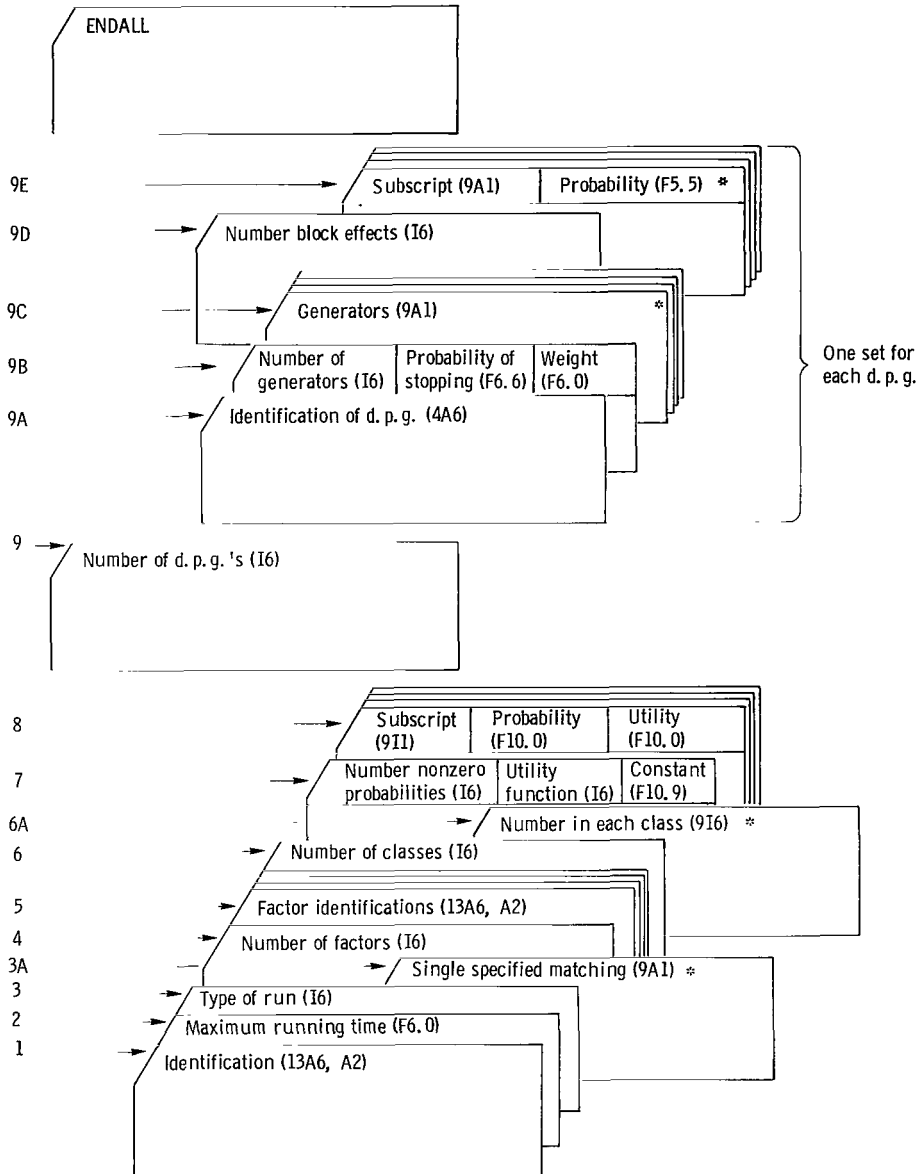


Figure 1. - Pictorial representation of data card arrangement. (Asterisk denotes cards which are optional. Presence depends on input information contained on earlier cards.)

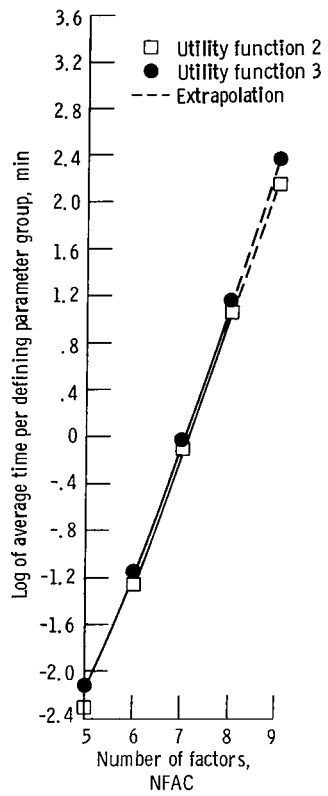


Figure 2. - Logarithm of average time required per defining parameter group as function of number of factors and choice of utility function.



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