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FINAL REPORT

# EXPERIMENTAL HINGELESS ROTOR CHARACTERISTICS AT FULL SCALE FIRST FLAP MODE FREQUENCIES

## INCLUDING ROTOR FREQUENCY RESPONSE TO SHAFT OSCILLATIONS

by W.A. Kuczynski

PHASE 3: CONTRACT NAS2 - 5419

Submitted to:

U.S. Army Air Mobility Research  
and Development Laboratory  
Ames Directorate,  
Moffet Field, California



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W.A. Kuczynski (Lockheed-California Co.)  
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FOREWORD

The results of the third phase of the Lockheed/U. S. Army Air Mobility Research and Development Laboratory (AMRDL) (Ames Directorate) "High Advance Ratio Research Program" (Contract NAS2-5419) are presented in this document. The research effort spanned the period from October 1971 to August 1972.

The success of this endeavor is directly attributable to the diligent efforts of the various AMRDL and Lockheed people who supported the program. Particular credit is due Mr. David Sharpe, the AMRDL Project Engineer.

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SUMMARY

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Phase 3 of the Lockheed/AMRDL (Ames Directorate) "High Advance Ratio Research Program" has been successfully completed. The primary objectives of the program were to experimentally determine the rotor frequency response to shaft pitching and rolling oscillations and to acquire steady response and frequency response data at high advance ratios for hingeless rotors with typical, full-scale, first flap mode natural frequencies. The acquisition of these experimental results would greatly enhance the hingeless rotor data bank established during the first two phases of the program.

Two minor modifications of the test model were required to fulfill these goals. First, the turnbuckles which had been used to manually position the model in pitch and roll, were replaced with electrically controlled hydraulic actuators. This provided the remotely operable shaft oscillation capability required for the frequency response tests. In order to obtain a lower flapping frequency, a set of 'supersoft' hub flexures were fabricated. The flapwise stiffness of these new restraints was 1/4 of the value for the softest flexure previously tested. (The rotor equipped with the 'supersoft' flexures is identified as configuration 5.)

Secondary objectives of the program included the further evaluation of both the Phase 2 hub moment feedback control system and the Phase 1 simplified rigid blade flapping theory with respect to shaft oscillations.

The experimental program was composed of three types of tests.

- open loop steady state tests where the rotor was excited with steady  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  and  $\alpha$  inputs
- open loop frequency response tests with sinusoidal swashplate ( $\theta_o$ ,  $\theta_s$  and  $\theta_c$ ) and shaft ( $\alpha$ ,  $\phi$ ) excitations
- closed loop frequency response tests with sinusoidal shaft excitations.



The steady state tests were conducted with only configuration 5. Three rotor speeds (550, 850 and 1,000 rpm) were tested which corresponded to non-dimensional flap frequencies ( $P$ ) of 1.28, 1.15 and 1.125. The maximum advance ratios attained for each frequency were  $\mu = 0.93$  at  $P = 1.28$  and  $\mu = 0.82$  at  $P = 1.15$ .  $P = 1.125$  was only tested at  $\mu = 0$ . The experimental data which are presented include steady rotor hub and shaft moments and lift and the harmonic content of the blade flapping moments at three radial positions.

Open loop frequency response tests with swashplate excitations were also conducted with only rotor configuration 5. Linear hub moment transfer functions were acquired at advance ratios from  $\mu = 0$  to 0.93 for  $P = 1.28$  and  $\mu = 0$  to 0.61 with  $P = 1.15$ .

Since frequency response testing with shaft oscillations was initiated during the Phase 3 program, tests were conducted with rotor configuration 1 (identified as such during the Phase 1 program) and configuration 5. Linear transfer functions with respect to shaft pitch and roll were determined for flap frequencies from  $P = 1.15$  to 1.56 and at advance ratios ranging from  $\mu = 0$  to 0.93.

Two tests were performed with configuration 1 in a closed loop mode. The specific objective was to determine the effectiveness of the Phase 2 hub moment feedback control system in relieving the rotor response to the shaft excitations. Advance ratios of  $\mu = 0$  and  $\mu = 0.28$  at a rotor speed of 800 rpm were considered.

The discussion of the third phase of the "High Advance Ratio Research Program;" presented in this report, draws heavily upon the Phase 1 and Phase 2 documentation. This is particularly true in the descriptions of the test article, the data acquisition and analysis systems, and the theoretical analysis. The bulk of the text is devoted to the presentation and examination of representative experimental results. All the analyzed test data are documented in appendices in tabular and/or graphical formats.

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SECTION 1  
INTRODUCTION

The Lockheed/AMRDL (Ames Directorate) "High Advance Ratio Research Program" is a systematic investigation of the characteristics of hingeless rotors over an advance ratio range and at conditions which are applicable to pure helicopter, compound helicopter and slowed rotor flight vehicles. The goals of the program are being achieved by means of small scale rotor model testing in the AMRDL (Ames) 7 x 10 foot wind tunnel and associated simplified theoretical analyses.

Three phases of the research have been completed. The first, for which Reference 1 constitutes the program final report, was finished in February 1971. That effort included the investigation of hingeless rotor flapping stability and response to steady swashplate control and angle of attack excitations at low rotor lift levels. Tests were conducted at advance ratios from 0 to 2.15 for a large envelope of rotors defined by Lock number ( $\gamma$ ) and nondimensional flapping frequency ( $P$ ).

The Phase 2 effort (Reference 2) expanded the investigations to hingeless rotor frequency response with respect to swashplate ( $\theta_o, \theta_s, \theta_c$ ) excitations. The rotor model was also equipped with a hub moment feedback control system and the steady and frequency response characteristics of the resulting closed loop system were studied. The Phase 2 rotor configurations and test conditions were among those considered during Phase 1 to assure consistency with previous data.

The Phase 3 program, for which this document represents the contract final report, sought to expand the reservoir of experimental hingeless rotor data which had already been established. The expansion was accomplished in two ways. First, the test model was modified to free the rotor shaft in pitch and roll. This change made it possible to determine the experimental rotor frequency response to shaft pitch and roll oscillations. These data were acquired

for the Phase 2 rotor configurations and frequency response test conditions, again for data consistency.

The second means of enlarging the data bank was to test the 7-1/2 foot diameter rotor with a reduced hub stiffness. This was accomplished by softening the blade flexures in the flapwise direction. This modification facilitated a significant expansion of the previously tested advance ratio/flap frequency ( $\mu/P$ ) envelope. Full-scale flapping frequencies were achieved. All of the types of tests formerly conducted, plus frequency response with respect to rotor shaft oscillations, were performed with the softened rotor hub configuration.

Two secondary objectives of the Phase 3 program were to continue both the evaluation of the Phase 2 feedback control system and the assessment of the validity of the simplified rigid blade mathematical model.

Current plans call for another research program involving the High Advance Ratio Rotor Model. This investigation will have as its objectives the determination of the effects of blade stall and inflow on hingeless rotor dynamic characteristics. To this end, the rotor model will be tested at high lift levels. The experimental portion of the program is presently scheduled for February 1973. The AMRDL (Ames) 7 x 10 foot wind tunnel will again be the test site.

## SECTION 2

## SYMBOLS

a	lift curve slope
$a_1$	longitudinal rotor tilt, pitch up positive, deg
b	number of rotor blades
$b_1$	lateral rotor tilt, roll right positive, deg
c	blade chord, ft
$c_m$	pitching moment coefficient
	$c_m = \frac{kM_H}{\pi R^3 \rho (\Omega R)^2}$
$c_l$	rolling moment coefficient
	$c_l = \frac{kL_H}{\pi R^3 \rho (\Omega R)^2}$
k	ratio of the one-per-rev blade flap bending moment at $r = 0$ in. to the one-per-rev blade flap bending moment at $r = 3.3$ in.
l	vertical distance from model pitch and roll pivots to rotor plane, in.
$m_\alpha(\psi)$	nondimensional aerodynamic excitation of blade flapping by rotor angle of attack
$m_{\dot{\alpha}}(\psi)$	nondimensional aerodynamic excitation of blade flapping by rotor pitch rate
$m_\theta(\psi)$	nondimensional aerodynamic excitation of blade flapping by collective pitch
$m_{\dot{\phi}}(\psi)$	nondimensional aerodynamic excitation of blade flapping by rotor roll rate
r	blade radial station measured from the center of rotation, in.
v	rotor induced velocity, ft/sec
x	nondimensional blade radial station $x = r/R$
A	feedback control system gain parameter

$C(\psi)$	nondimensional aerodynamic damping of blade flapping
$C_T$	rotor thrust coefficient
	$C_T = \text{THRUST}/\pi R^2 \rho (\Omega R)^2$
HM	total rotor hub moment, in.-lb
	$HM = \sqrt{M_H^2 + L_H^2}$
$K(\psi)$	nondimensional aerodynamic spring rate of blade flapping
$K_\theta$	rotor stiffness, in.-lb/deg
L	feedback control system lag parameter
$L_H$	rotor hub roll moment resolved from rotating blade flapping moments measured at $r = 3.3$ in., roll right positive, in.-lb, $L_H$ is equivalent to $L_R$ (3.3 in.) in References 1 and 2
$L_s$	rotor shaft roll moment, roll right positive, in.-lb
$M_\beta$	rotating blade flapping moment, in.-lb
	$M_\beta(\psi) = M_{\beta_0} - \sum_{i=1}^n \left[ M_{\beta_{ic}} \cos(i\psi) + M_{\beta_{is}} \sin(i\psi) \right]$
$M_{\beta_0}$	constant component of rotating blade flapping moment, in.-lb
$M_{\beta_{ic}}$	$\cos(i\psi)$ harmonics of rotating blade flapping moment, in.-lb
$M_{\beta_{is}}$	$\sin(i\psi)$ harmonics of rotating blade flapping, in.-lb
$M_H$	rotor hub pitch moment resolved from rotating blade flapping moments measured at $r = 3.3$ in., in.-lb, pitch up positive, $M_H$ is equivalent to $M_R$ (3.3 in.) in References 1 and 2
$M_s$	rotor shaft pitch moment, pitch up positive, in.-lb
P	nondimensional blade flapping frequency
R	rotor blade radius, ft



SM total rotor shaft moment, in.-lb

$$SM = \sqrt{M_s^2 + L_s^2}$$

$\alpha$  rotor shaft pitch angle, pitch up positive, deg

$\theta_i$  blade flapping angles  $i = 1, 2, 3, 4$ , deg

$\gamma$  Lock number

$\theta_c$  lateral cyclic pitch, deg

$\theta_s$  longitudinal cyclic pitch, deg

$\theta_o$  collective pitch, deg

$\mu$  advance ratio

$\sigma$  rotor solidity,  $\sigma = bc/\pi R$

$\phi$  rotor shaft roll angle, roll right positive, deg

$\omega$  excitation frequency, rad/sec

$\Gamma$  feedback system cyclic control phase angle, deg

$\Delta$  feedback control system phase angle, deg

$\psi$  rotor azimuth angle, deg

$\Omega$  rotor rotational frequency, rad/sec

## SECTION 3

## MODEL DESCRIPTION

The versatility of the 7-1/2 foot diameter Lockheed/AMRDL High Advance Ratio Rotor Model has been developed during the course of the High Advance Ratio Research Program. The Phase 1 test article, which is described in detail in Reference 1, was a fixed shaft, direct swashplate controlled hingeless rotor with variable Lock number and natural flapping frequency. This basic configuration was enhanced during the second phase of the research program by the addition of an automatic hub moment feedback control system with variable gain, time constant and phasing capabilities. The bandwidths of the remotely controlled collective and cyclic pitch hydraulic actuators were also extended to permit meaningful frequency response testing. A description of the Phase 2 model can be found in Reference 2.

During the Phase 3 effort the capabilities of the rotor model were further expanded in two ways. First, the rotor hub flapping stiffness was reduced by fabricating a very soft set of flapping flexures (hereafter referred to as the 'supersoft' flexures). These flexures are characterized by a flapwise EI of  $11.5 \times 10^3$  lb-in.<sup>2</sup> and a chordwise EI of  $1.97 \times 10^6$  lb-in.<sup>2</sup> over the radial expanse  $r = 1.74$  in.  $\rightarrow$  4.55 in. Two specimens were fatigue tested, each to more than one million cycles, without failure, in order to establish a safe rotor moment endurance limit.

The analytically determined natural frequencies of the rotor blade with the 'supersoft' flexure and no tip weight are presented as a function of rotor speed in Figure 1. Shake test results of this blade configuration are also plotted on the figure. Very good agreement is noted.

For purposes of identification, the rotor equipped with the 'supersoft' flexures and no tip weight ( $\gamma \approx 5.0$ ) is designated configuration 5. The other rotor tested during the Phase 3 program was configuration 1 which has heretofore

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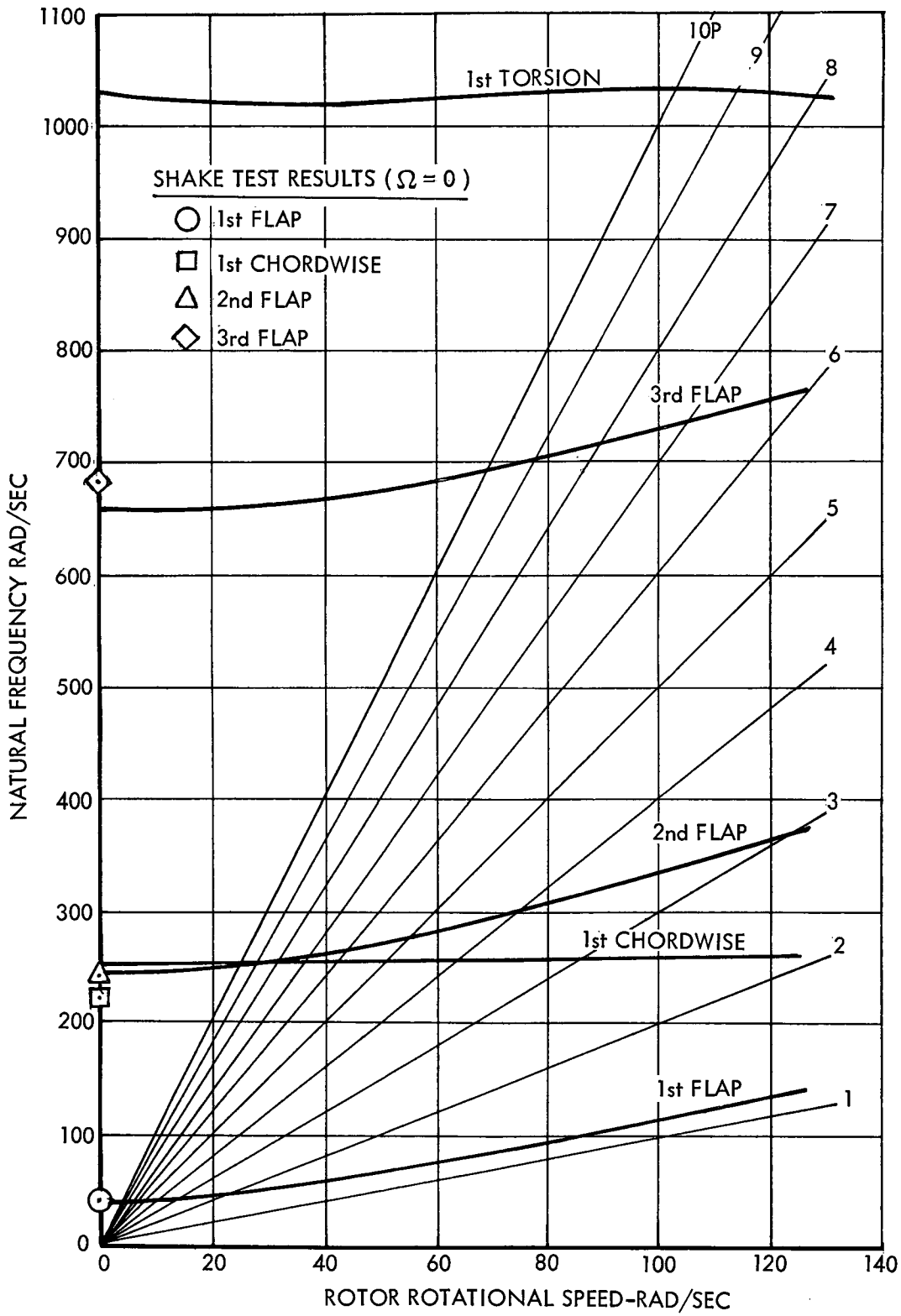


Figure 1. Coupled Blade Natural Frequencies, Configuration 5

(Reference 1) been defined as the rotor equipped with the 'soft' flexure and no tip weight. 'Soft' is characterized by stiffness values of

$$EI_{\text{flap}} = 46.5 (10^3) \text{ lb-in.}^2$$

$$EI_{\text{chord}} = 2.24 (10^6) \text{ lb-in.}^2$$

from  $r = 1.74 \text{ in.} \rightarrow 4.55 \text{ in.}$

The second modification to the model consisted of installing remotely operated hydraulic actuators which controlled the rotor shaft pitch and roll positions. The break frequencies of the actuators were never reached during the test which included maximum shaft oscillation frequencies of 10 Hz in pitch and 14 Hz in roll. Thus it is known that the servo bandwidths exceed these values at the least.

The mechanization of shaft angular motion required that the model be pitched and rolled about pivots which were located 11.25 in. below the plane of the rotor. Thus an angular variation of the shaft generated linear translation of the rotor hub as well as the angular motion.

The physical characteristics of the model are summarized in Table I.

TABLE I

## LOCKHEED/AMRDL HIGH ADVANCE RATIO ROTOR MODEL CHARACTERISTICS

Number of Blades:	4
Radius:	45 in.
Chord:	4.5 in.
Solidity:	0.127
Airfoil Section:	NACA 0012
Blade Twist:	0 deg
Blade Precone:	0 deg
Lock Number ( $a = 2\pi$ ):	5.0, 3.0 (with tip weight)
First Flap Mode Natural Frequency:	Variable; tested range $1.125\Omega \rightarrow 2.32\Omega$
Blade Radially Distributed Mass and Stiffness Properties:	See Section 3 of Reference 1
Rotor Control System:	Direct swashplate or Electronic hub moment feedback
Features of Hub Moment Feedback Control System:	1st order lag filters Variable gain Variable time constant Variable control and feedback phasing
Drive System:	Two 37 HP variable frequency induction motors
Additional Model Features:	Resolved hub moments $\theta_o, \theta_s, \theta_c, \alpha$ and $\phi$ frequency response capability Distance from model pitch and roll pivots to rotor plane = 11.25 in.

SECTION 4  
DATA ACQUISITION SYSTEM

INSTRUMENTATION

The Phase 3 rotor model instrumentation consisted of all those sensors which had been installed for previous tests plus:

- a rotor shaft bending strain gage bridge aligned with blades 1 and 3 ( $\psi = 0^\circ$  and  $180^\circ$ ) and located 2 inches below the plane of the rotor and
- a linear position potentiometer which measured the model roll actuator ram position and thus the rotor shaft roll angle.

DATA RECORDING EQUIPMENT

The equipment utilized to record data for off-line analysis consisted of the following:

- AMRDL DATEX System
- Honeywell Medium Band Analog Tape Recorder
- Honeywell Viscorder (direct-write oscillograph)

A description of each of these devices can be found in Section 4 of Reference 1.

In order to maximize the visibility of the data while the test was in progress, a transfer function analyzer was used to determine rotor hub moment frequency response with respect to a selected excitation (i.e.,  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$ ,  $\alpha$ ,  $\phi$ ). X-Y-Y plotters were driven with the analyzer gain and phase signals. Thus hub pitching and rolling moment transfer functions were immediately available in a graphical form. These on-line data greatly enhanced the selection of excitation frequencies, especially at near resonance conditions.

Table II summarizes the Phase 3 data acquisition system.

TABLE II

SUMMARY OF THE PHASE 3 HIGH ADVANCE RATIO ROTOR MODEL DATA ACQUISITION SYSTEM

DATUM	INSTRUMENTATION	DATA ACQUISITION EQUIPMENT
Flap Bending Moment at Sta 22.3	Flap Bending Strain Gage at Sta 22.3	V, T+
Flap Bending Moment at Sta 13.15	Flap Bending Strain Gage at Sta 13.15	V, T+
Flap Bending Moment at Sta 3.3	Flap Bending Strain Gage at Sta 3.3	V, T
Flap Bending Moment at Sta 2.4	Flap Bending Strain Gage at Sta 2.4	*
Rotating Shaft Bending Moment	Strain Gage at $\psi = 0^\circ$ 2 in. below rotor plane	V, T
Resolved Rotor Hub Pitching and Rolling Moments at Sta 3.3	4-Flap Bending Strain Gages at Sta 3.3	V, T, D
Chord Bending Moment at Sta 13.15	Chord Bending Strain Gage at Sta 13.15	*
Chord Bending Moment at Sta 2.4	Chord Bending Strain Gage at Sta 2.4	V, T
Blade Torsion Moment at Sta 9.28	Torsion Gage at Sta 9.28	V, T+
Pitch Link Tension/Compression Load	Pitch Link Tension/Compression Strain Gage	V, T+
Instantaneous Pitch Angle of Blade No. 1	Blade Feathering Position Potentiometer (Pot.)	V, T
Body Moments and Forces	Body Mounted Strain Gage Balance	D (LIFT ON T+)
Applied Longitudinal Cyclic Pitch ( $\theta_s$ )	Longitudinal Cyclic Pitch Actuator Position Pot.	V, T, D
Applied Lateral Cyclic Pitch ( $\theta_c$ )	Lateral Cyclic Pitch Actuator Position Pot.	V, T, D
Applied Collective Pitch ( $\theta_o$ )	Collective Pitch Actuator Position Pot.	V, T, D
Rotor Shaft Pitch Angle ( $\alpha$ )	Model Pitch Actuator Linear Position Pot.	V, T, D
Rotor Shaft Roll Angle ( $\phi$ )	Model Roll Actuator Linear Position Pot.	V, T, D
Longitudinal Control Input ( $\theta_{long}$ )	Longitudinal Control Input Pot.	V; D
Lateral Control Input ( $\theta_{lat}$ )	Lateral Control Input Pot.	V, D
Pitch Feedback Control Signal ( $\delta_s$ )	Direct - Voltage Measurement	V, D
Roll Feedback Control Signal ( $\delta_c$ )	Direct - Voltage Measurement	V, D
Fore - Aft Model Acceleration	Accelerometer	V
Oscillator Output	Direct - Voltage Measurement	V, T
Rotor Rotational Speed	One-Per-Rev Magnetic Pickup	V, T, D
Body Moments and Forces	Wind Tunnel Balance	D
Tunnel Dynamic Pressure	Wind Tunnel Pitot Static Probe	D
Tunnel Temperature	Wind Tunnel Temperature Probe	D

V = Visicorder (Oscillograph), T = Analog Tape, D = Datex

\* Datum not recorded because slip rings unavailable.

+ Recorded on tape only during steady state tests.

## SECTION 5

## TEST PROGRAM

The test program was conducted at the facilities of the Ames Directorate of the U. S. Army Air Mobility Research and Development Laboratory (AMRDL) at Moffett Field, California. One week of whirl testing (February 23 - 29, 1972) was performed in the AMRDL Model Preparation Area following a thorough functional check of the model and data acquisition system. The wind tunnel tests spanned four consecutive weeks beginning on March 20, 1972 and were conducted in the AMRDL 7 x 10 foot wind tunnel. For a description of the tunnel, including the installation of the 7-1/2 foot diameter High Advance Ratio Rotor Model, the reader is referred to Pages 33 - 36 of Reference 1.

Three types of tests were required to fulfill the objectives of the research program. They were:

- open loop steady state response tests wherein steady collective pitch ( $\theta_o$ ) cyclic pitch ( $\theta_s$  and  $\theta_c$ ) and rotor shaft angle of attack ( $\alpha$ ) excitations were applied to the rotor;
- open loop frequency response tests where sinusoidally varying  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$ ,  $\alpha$  and rotor shaft roll ( $\phi$ ) excitations were applied to the rotor;
- and closed loop frequency response tests with sinusoidally varying  $\alpha$  and  $\phi$  excitations.

The open loop steady state response tests and the frequency response tests with  $\theta_o$ ,  $\theta_s$  and  $\theta_c$  excitations were performed on configuration 5 ('supersoft' flexure without tip weight) only. The aim was to obtain experimental rotor response data at combinations of nondimensional flapping frequency (P) and advance ratio ( $\mu$ ) not previously tested. Frequency response tests with  $\alpha$  and  $\phi$  excitations were conducted with both configurations 1 and 5 since this type of testing was initiated during this phase of the research program. Closed loop frequency response tests with  $\alpha$  and  $\phi$  excitations were meant to complement similar closed loop Phase 2 data with swashplate excitations ( $\theta_o$ ,  $\theta_s$ , and  $\theta_c$ ) and thus only configuration 1 was considered.



Since exactly the same types of tests were performed during the whirl and wind tunnel activities, it is possible to summarize the total test program in one table (Table III). The summary contains the rotor configurations and conditions tested for each of the three types of tests as well as the data acquired.

### DISCUSSION OF TEST RESULTS

As has been the case with previous phases of this research program, the test activity was quite successful and resulted in a large amount of experimental data. With the exception of rotor frequency response with respect to  $\alpha$  and  $\phi$ , the results are essentially the same as those obtained during the Phase 1 and Phase 2 programs. Improvements in test techniques and data analysis methods indicated by the previous experience and the addition of a shaft bending moment measurement have changed the type of data and the presentation slightly.

In the following discussion, the results from the three types of tests will be presented separately. In the interest of brevity, the details regarding the test procedures and data analysis methods which are common to the Phase 1 and Phase 2 programs will be referenced wherever possible. Emphasis will be placed on those tests and results which were initiated during the current phase of the program.

#### Open Loop Steady State Tests

These tests consisted of exciting the rotor with steady  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  and  $\alpha$  excitations at various rotor rotational speeds and forward velocities. Each of the four excitations was applied independently at several magnitudes in order to obtain data from which linear rotor shaft, hub flapping and blade flapping moment derivatives and lift derivatives could be determined. All of the rotor moment response data for the steady state tests were determined by a harmonic analysis (over 40 rotor cycles) of digitized analog signals. The collective pitch, cyclic pitch and angle of attack angles were measured by linear potentiometers, the outputs of which were recorded with a steady data sampling system.

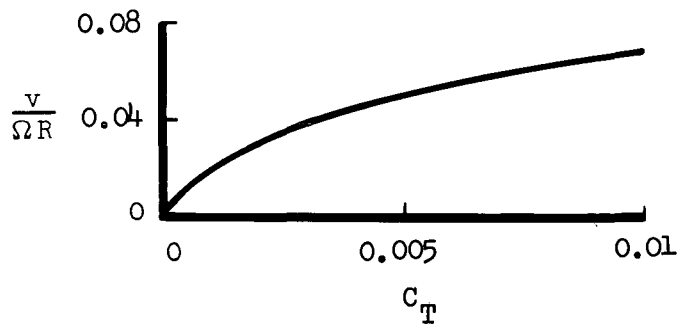
TABLE III  
HIGH ADVANCE RATIO RESEARCH PROGRAM PHASE 3 TEST CONDITIONS

Type of Test	Config	$\gamma$	RPM	$\mu$	P	Excitations	Excitation Frequencies	Data Acquired				
Open Loop Steady State Response	5	5	1000	0	1.125	$\theta_o, \theta_s$	0	Steady rotor shaft and hub moments and lift. Radially distributed blade flap bending moments				
				0.27 0.36 0.51 0.60 0.72 0.75 0.81	1.15	$\theta_o, \theta_s, \theta_c, \alpha$						
			550	0	1.28	$\theta_o, \theta_s, \theta_c, \alpha$						
				0.41 0.56 0.79 0.92	1.15	$\theta_o, \theta_s, \theta_c$						
				0.27 0.36 0.51 0.60	1.15	$\alpha, \phi$						
			550	5	850	0			1.28	$\theta_o, \theta_s, \theta_c$	0 $\rightarrow$ 32 Hz	Rotor transfer functions
						0.41 0.79 0.92			1.28	$\alpha, \phi$		
						0.28 0.38 0.54 0.64			1.33	$\alpha, \phi$		
			550	5	800	0			1.56	$\alpha, \phi$	0 $\rightarrow$ 14 Hz	Closed loop transfer functions
						0.41 0.56 0.78 0.93			1.33	$\phi$ $\alpha$		
0.28 0.38 0.54 0.64	1.33	$\phi$ $\alpha$										

\* Closed Loop Control System Configuration (A = 0.5, I = 0,  $\Delta$  = 0 deg)

The steady state whirl test ( $\mu = 0$ ) results indicate that the induced inflow has both a linear and a non-linear effect on the rotor response. The variation of rotor thrust with collective pitch at  $\mu = 0$  clearly demonstrates the non-linear influence. For example, experimental rotor thrust versus collective pitch for configuration 5 at three rotor speeds is presented in Figure 2. At low thrust levels the reduction in the effective blade angle of attack due to the inflow is very non-linear, generating a corresponding non-linear thrust- $\theta_0$  relationship. At higher thrust levels the inflow tends to be approximately linear. This inflow characteristic is easily understood from simple momentum theory from which it can be shown that for  $\mu = 0$

$$\frac{v}{\Omega R} = \sqrt{\frac{C_T}{2}} \quad (1)$$



A similar non-linear characteristic at low thrust levels can also be seen in Figure 3 where the rotor hub pitching ( $M_H$ ) and rolling ( $L_H$ ) moments due to longitudinal cyclic pitch ( $\theta_s$ ) are plotted for three thrust levels at  $\mu = 0$  and a rotor speed of 550 rpm. These data also demonstrate the effect that the inflow has upon the linear rotor moment response; namely a reduction in the magnitude of the derivative.

In the current presentation the resolved rotor hub moments are designated  $M_H$  and  $L_H$ . In previous related documentation (References 1 and 2)  $M_H$  was symbolized as  $M_R$  (3.3 in.) and  $L_H$  as  $L_R$  (3.3 in.).

The swashplate of the model was designed to permit independent excitation of longitudinal and lateral cyclic pitch. In order to demonstrate that this was in fact the case, the rotor was excited with  $\theta_c$  at  $\mu = 0$ . Figure 4 shows the rotor response which was generated. A comparison of the moments (with

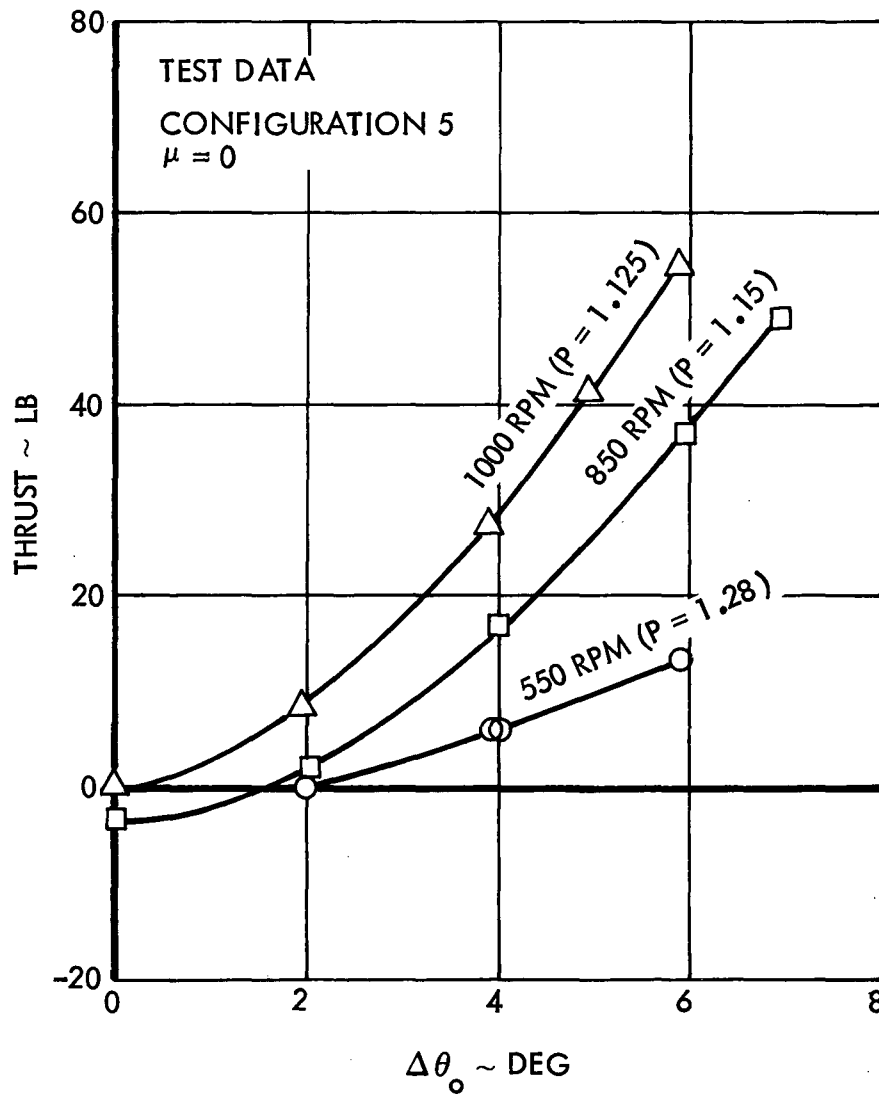


Figure 2. Rotor Thrust Versus Collective Pitch at  $\mu = 0$ , Configuration 5

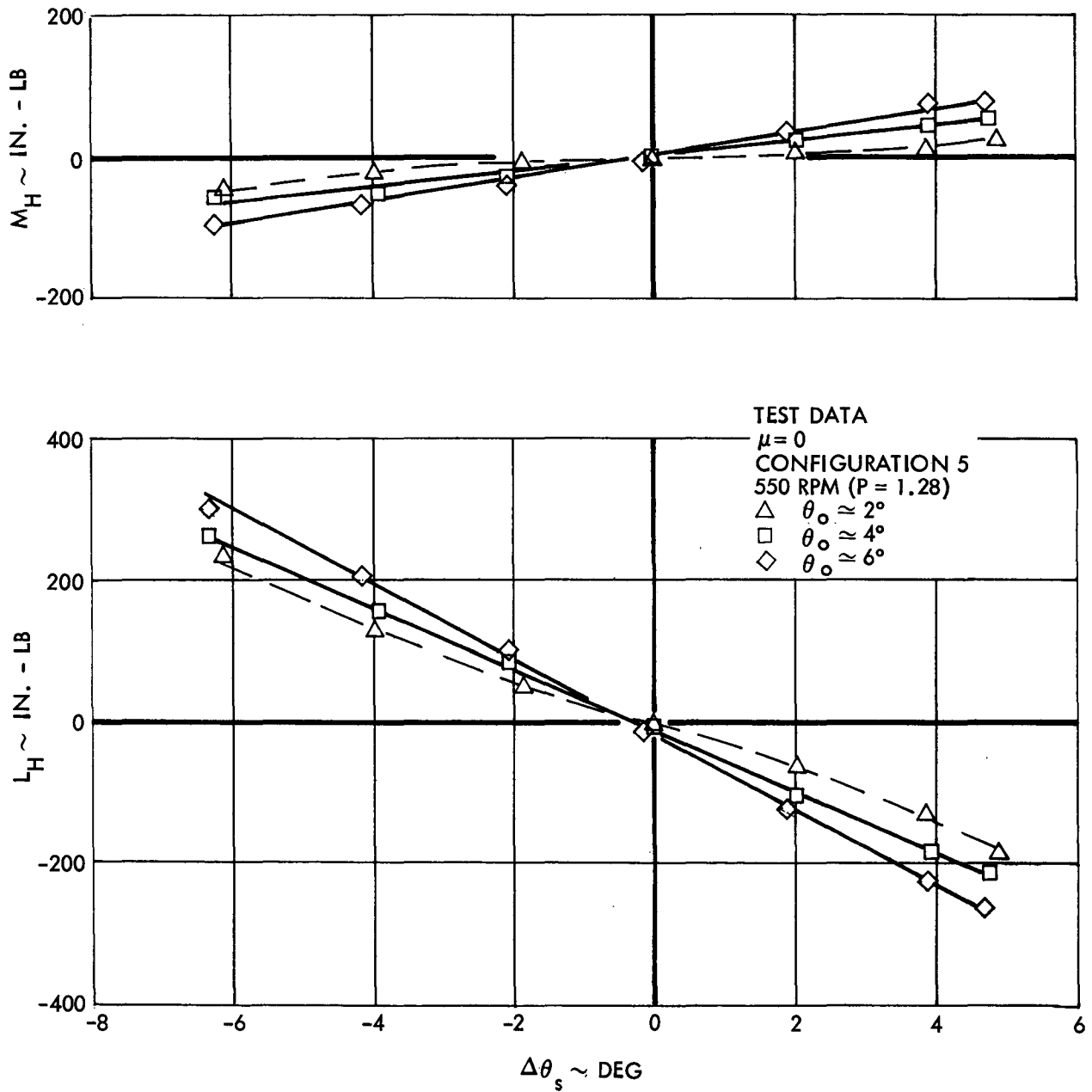


Figure 3. Rotor Hub Moment Response to Longitudinal Cyclic Pitch,  $\mu = 0$ , Configuration 5, 550 RPM ( $P = 1.28$ )

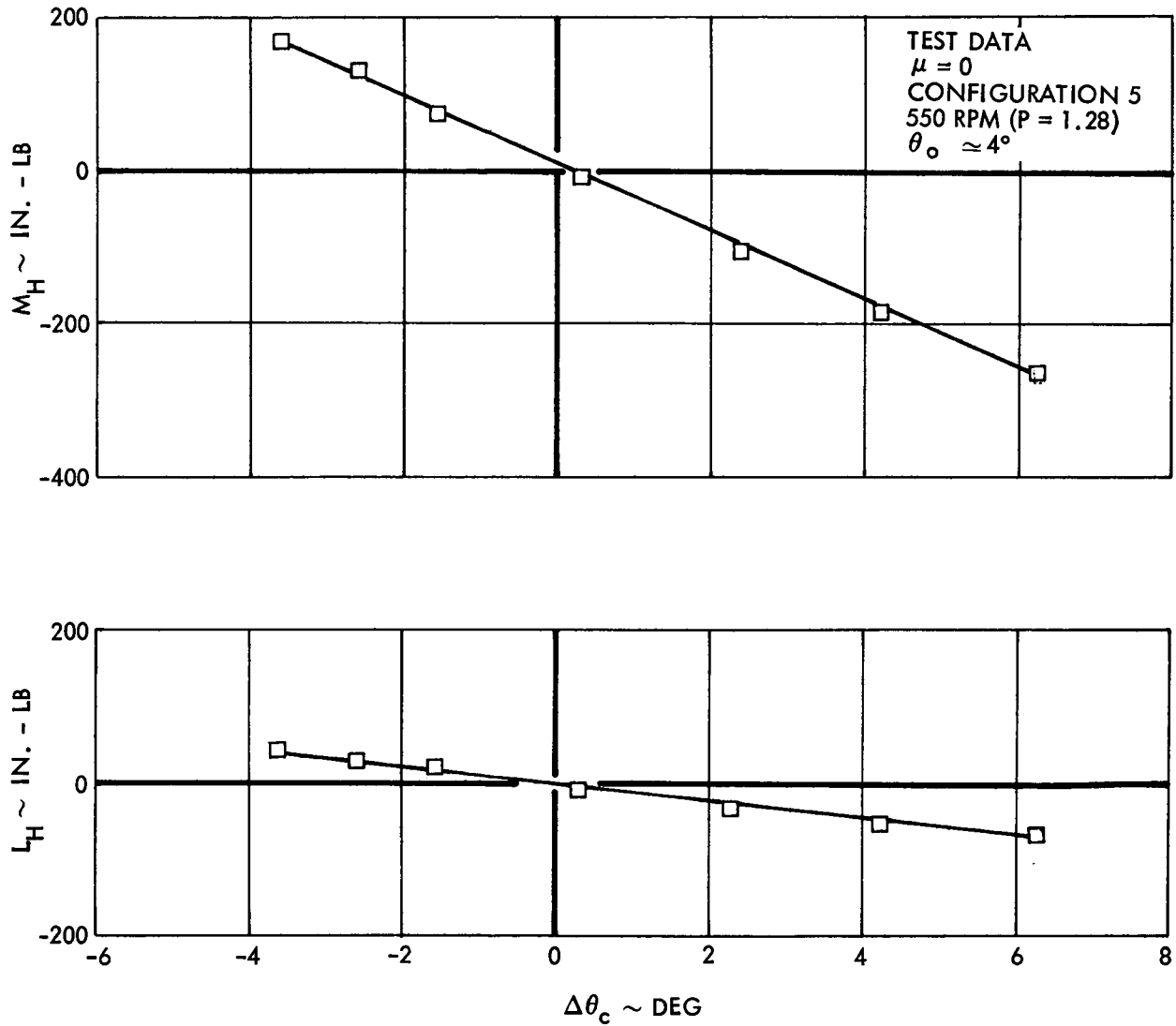


Figure 4. Rotor Hub Moment Response to Lateral Cyclic Pitch,  $\mu = 0$ , Configuration 5, 550 RPM (P = 1.28)

$\theta_0 = 4^\circ$ ) in Figures 3 and 4 confirms the symmetry of the open loop cyclic controls.

The rotor response to  $\theta_s$  at 850 rpm (first flap mode frequency  $P = 1.15$ ) is shown in Figure 5 and the response at 1,000 rpm ( $P = 1.125$ ) in Figure 6. The characteristics of the curves are generally the same as those previously discussed.

Figure 7 presents a summary of the linear hub moment response to longitudinal cyclic pitch for  $\mu = 0$ . The results are presented in terms of the total hub moment derivative

$$\text{HUB MOMENT (HM)} = \sqrt{M_H^2 + L_H^2} \quad (2)$$

and its phase angle of response measured from  $\psi = 0^\circ$

$$\text{PHASE} = \text{ARCTAN} \left( - \frac{L_H}{M_H} \right) \quad (3)$$

plotted versus rotor rotational speed. Noteworthy characteristics include anticipated increases in the magnitude and phase angle of response with decreasing flap frequency ( $P$ ) and the larger magnitude of response at the higher rotor thrust level. The ratio of the steady hub moment derivative to the steady shaft moment (SM) derivative is also shown in Figure 7. The shaft moment data will be thoroughly discussed later in this section. Suffice it for now to note the reduction in the ratio of hub moment to shaft moment with increased rotor speed.

The individual hub and shaft moment derivatives used to generate the data in Figure 7, i.e.,

$$\frac{\partial M}{\partial \theta_s^H}, \frac{\partial L}{\partial \theta_s^H}, \frac{\partial M}{\partial \theta_s^S}, \frac{\partial L}{\partial \theta_s^S} \quad (4)$$

were determined using a linear least squares curve fit. All of the steady state data at  $\mu = 0$  are tabulated in Appendix A. The derivatives from the least squares curve fit and the deviation of each individual data point from the statistical line are also listed.

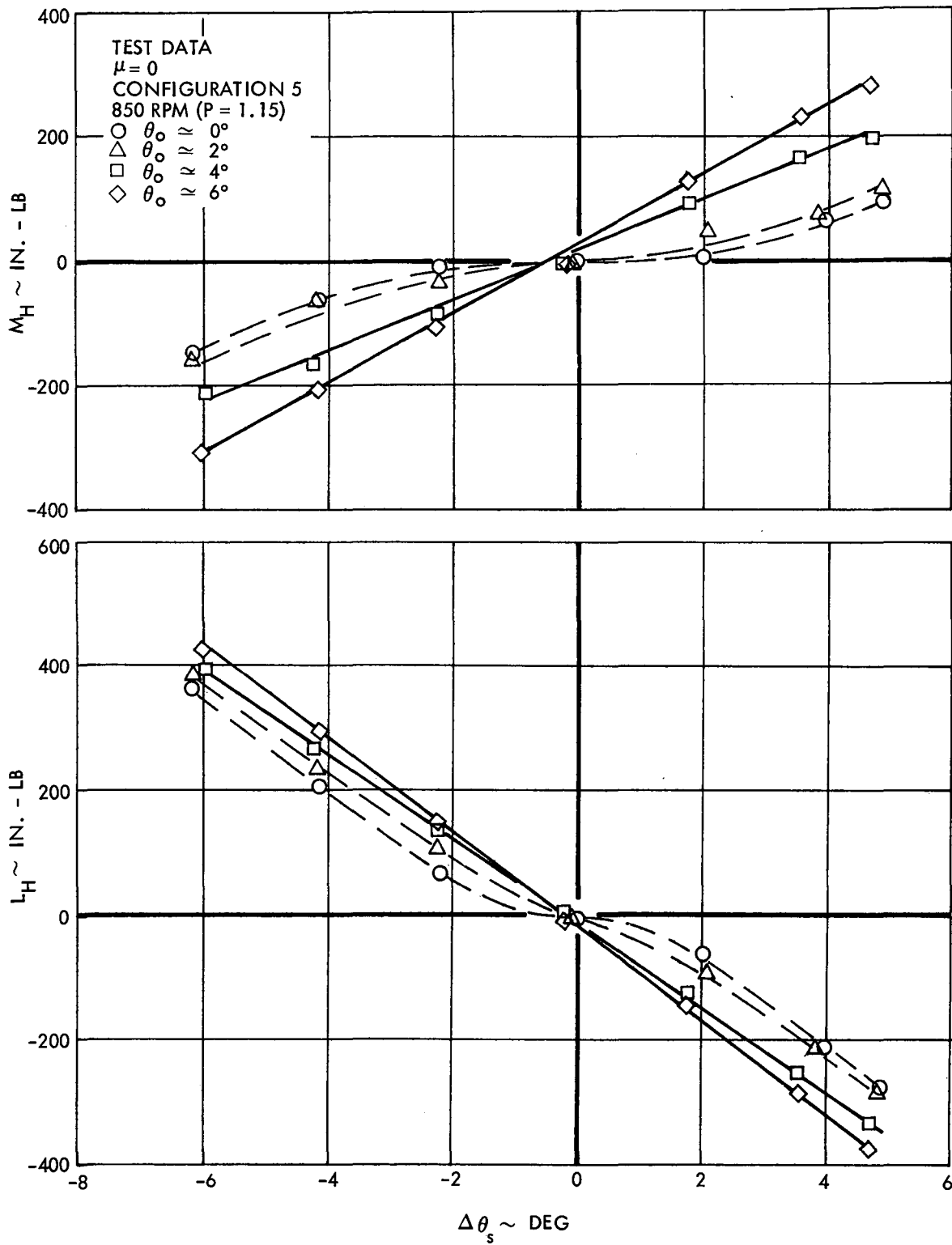


Figure 5. Rotor Hub Moment Response to  $\theta_s$ ,  $\mu = 0$ , Configuration 5, 850 RPM ( $P = 1.15$ )





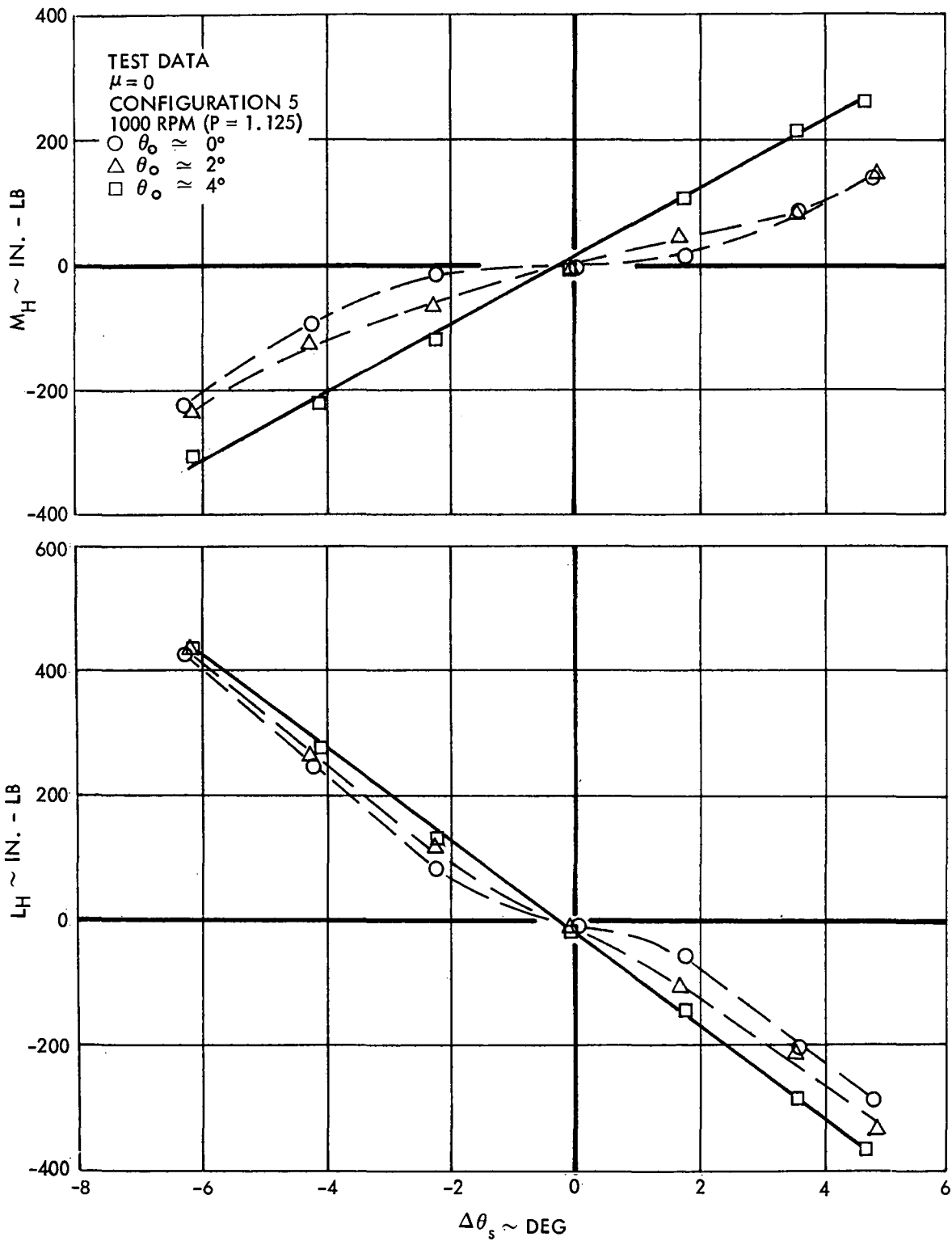


Figure 6. Rotor Hub Moment Response to  $\theta_s$ ,  $\mu = 0$ , Configuration 5, 1000 RPM ( $P = 1.125$ )

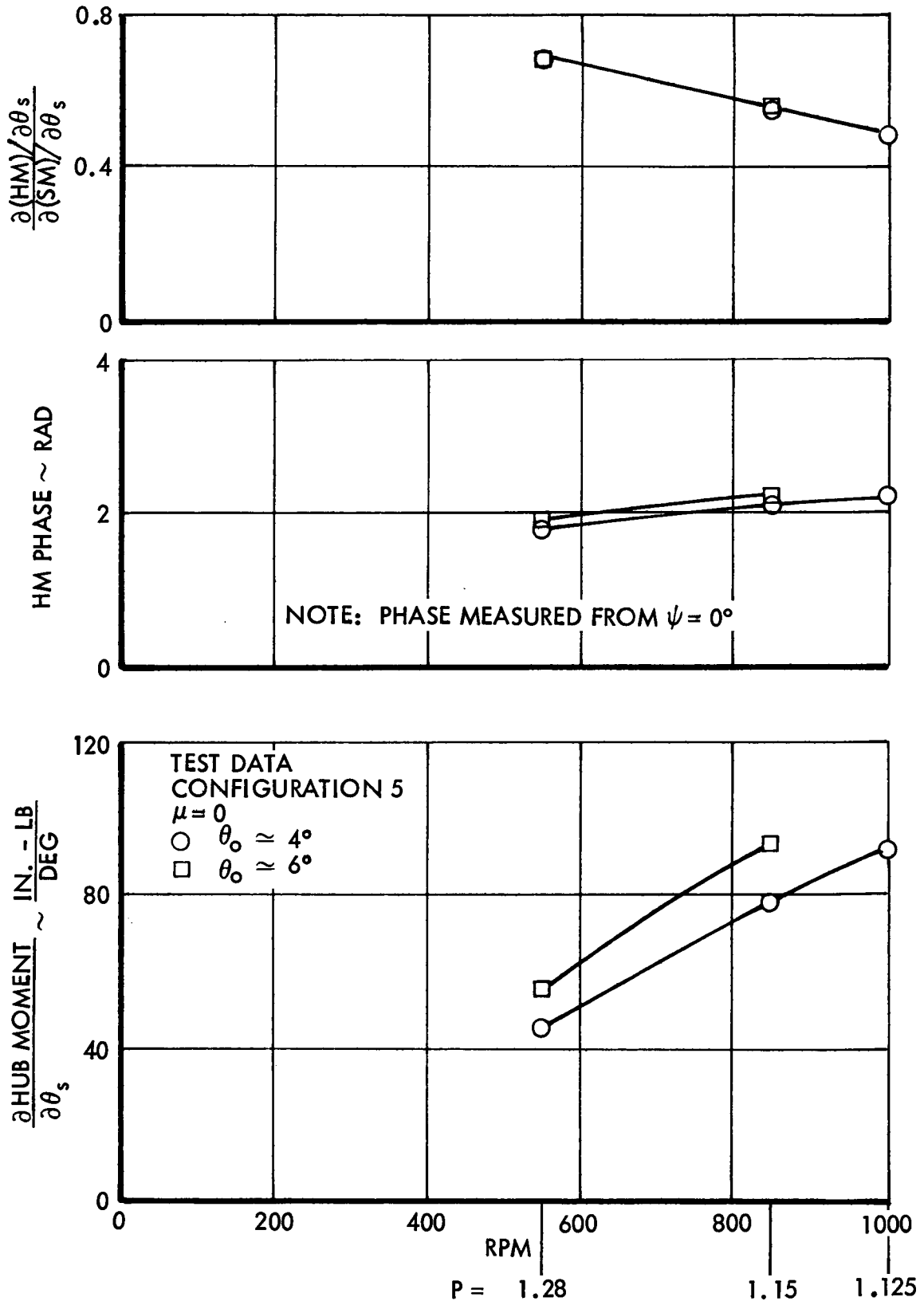


Figure 7. Linear Rotor Hub and Shaft Moment Derivatives with Respect to  $\theta_s$  for  $\mu = 0$

Forward flight data were acquired at rotor speeds of 550 and 850 rpm. The test procedure was the same as that used during the Phase 1 test (Reference 1). Briefly this means that the rotor was disturbed from a trim state with either a  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  or an  $\alpha$  excitation. Each excitation was applied independently at several magnitudes. The rotor was nominally unloaded and the aerodynamic environment was linear (low tip Mach number and blade angles below stall values).

An example of the quality (and linearity) of the data is shown in Figure 8. The measured rotor hub pitching and rolling moments are plotted versus collective pitch for a rotor rotational speed of 550 rpm and advance ratios ranging from 0.41 to 0.92. The data manifest very little scatter and the slopes of the curves are very definitely linear. The expected increase in the magnitude of the response with increased  $\mu$  is noted.

As indicated previously, the rotor shaft moment was measured during the Phase 3 test program (it was not measured during the Phase 1 and Phase 2 tests). A rotating signal aligned with blades 1 and 3 ( $\psi = 0^\circ$  and  $180^\circ$ ) was recorded on tape and harmonically analyzed at  $1\Omega$  to determine the steady pitching ( $M_s$ ) and rolling ( $L_s$ ) components of the total shaft moment. An example of these data for the conditions shown in the previous figure are shown in Figure 9. It can be seen that the linearity of the shaft moment data and the hub moment data are approximately the same.

Despite the consistency between shaft and hub moment results indicated by Figure 8 and 9 it is important to recognize several sources of inexactness in the shaft moment data. First, the accuracy of the calculation of the harmonic components  $M_s$  and  $L_s$  depends upon the accuracy of the rotor frequency,  $\Omega$ . As demonstrated in Appendix A of Reference 2, very small errors in frequency can generate significant errors in the magnitude and phase of the harmonic components. The most likely source of error in  $\Omega$  is caused by slight variations in the rotor speed during the test. The analytical procedure for calculating  $\Omega$  from the experimental data (i.e. counting rpm blips) can also introduce slight errors. It is noted that an imprecise value of  $\Omega$  does not affect the values of  $M_H$  and  $L_H$  because they are resolved signals and therefore the steady component of the harmonic analyses. It is further noted that  $M_H$

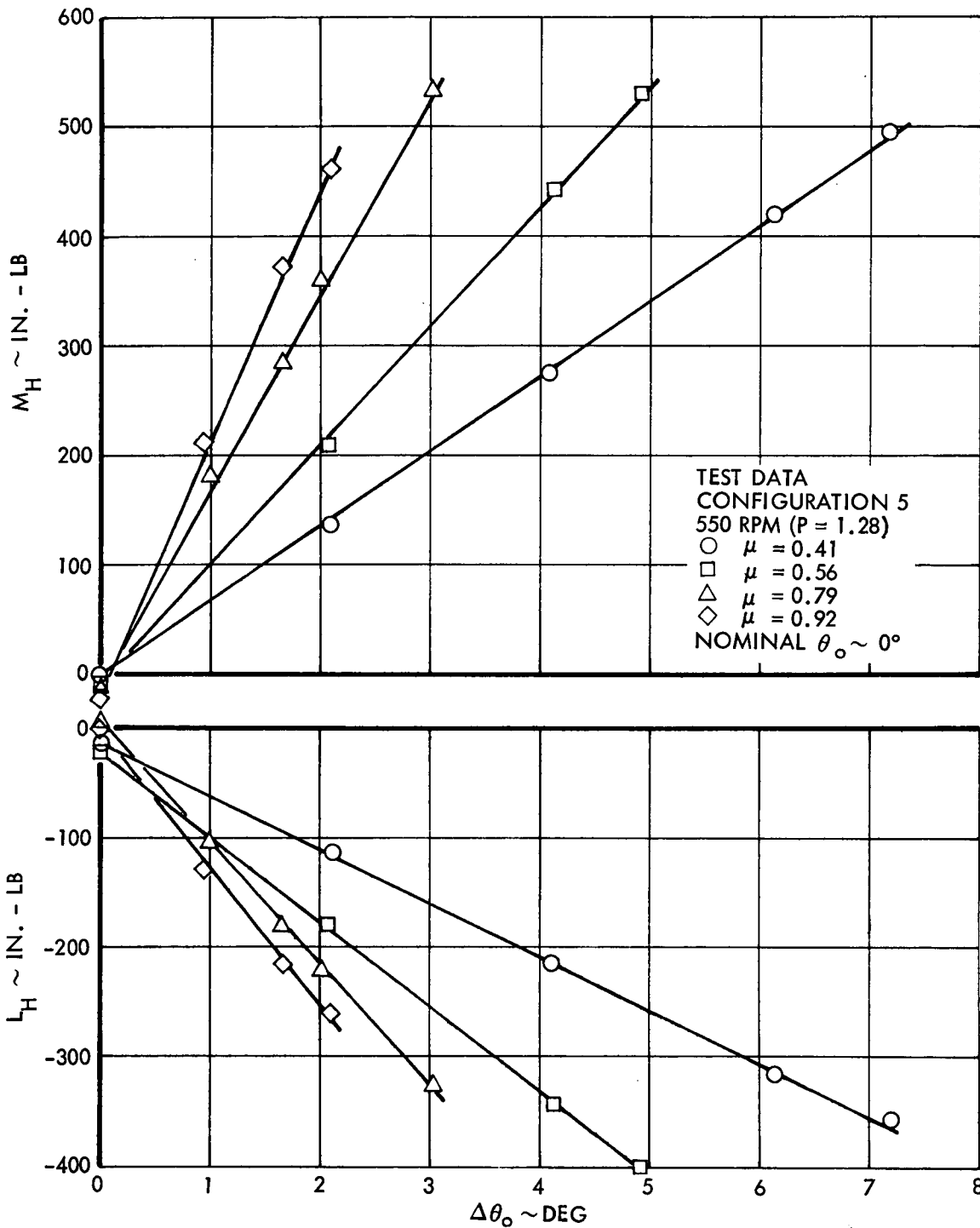


Figure 8. Rotor Hub Moment Response to Collective Pitch, Configuration 5, 550 RPM (P = 1.28)

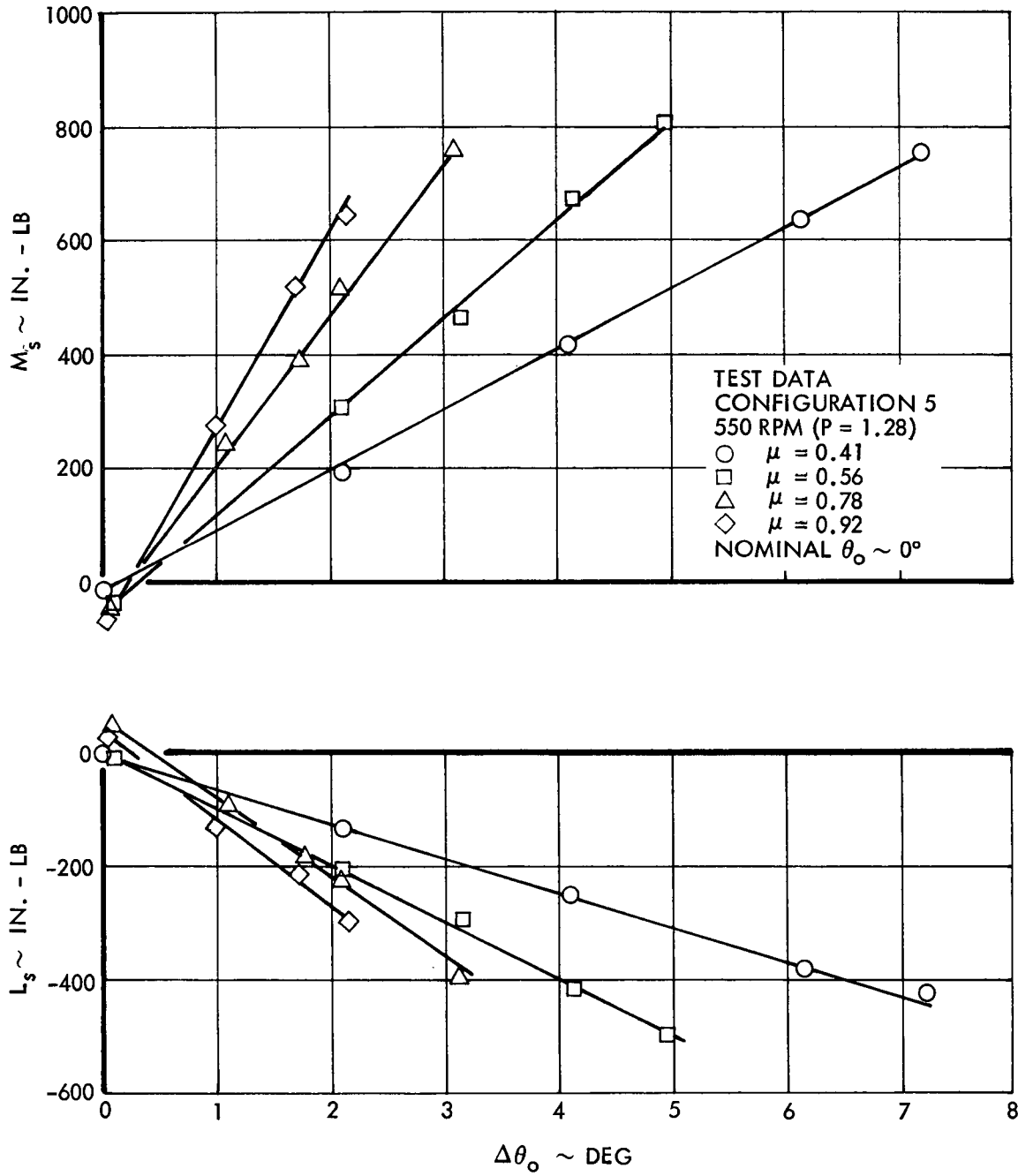
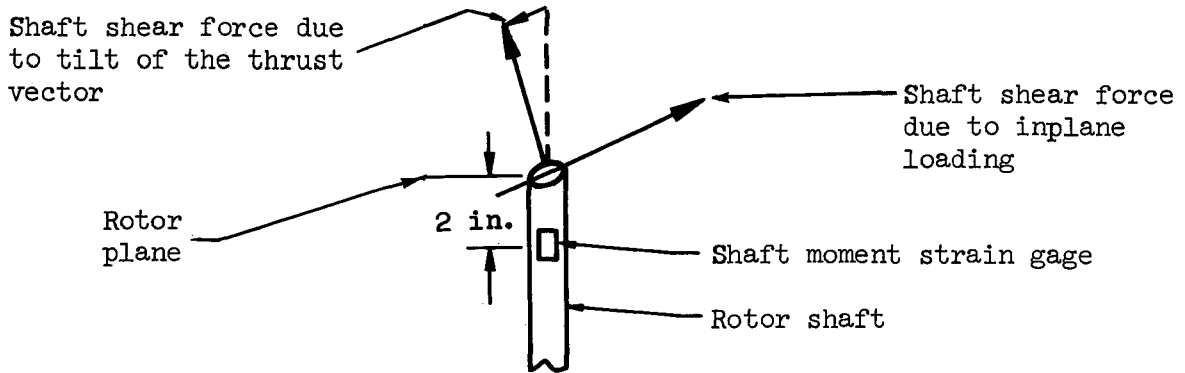


Figure 9. Rotor Shaft Moment Response to Collective Pitch, Configuration 5, 550 RPM (P = 1.28)

and  $L_H$  are calculated from the response of all four blades, whereas  $M_S$  and  $L_S$  are influenced by only blades 1 and 3.

Two other factors which influence shaft moments are the shear loads at the center of rotation due to inplane loading and the tilt of the thrust vector. These do not affect the hub flap moments. They do, however, contribute to the measured shaft moment because the shaft bending strain gage is located approximately two inches below the plane of the rotor, viz,



Although each of these three effects are minor,

- maximum error in  $\Omega$      $\sim 0.2\%$
- maximum shaft moment     $\sim 10$  in.-lb  
due to inplane shear  
forces
- maximum shaft moment     $\sim 20$  in.-lb  
due to tilt of thrust  
vector

they do introduce scatter into the shaft moment results. This will be evident in the following presentation of data.

All of the steady state rotor moment response data are conveniently summarized in subsequent curves as total moment derivatives and their phase angles of response (measured relative to  $\psi = 0^\circ$ ).

$$\text{PHASE ANGLE} = \text{ARCTAN} \left( \frac{-L}{-H} \right) \quad (5)$$

The derivatives are calculated using a linear least squares curve fit. The data used in their determination plus the calculated values of the shaft and hub moment derivatives and the deviation of each datum from the statistical curves are tabulated in Appendix A.

The rotor response to collective pitch is shown in Figure 10 for the two tested rotor speeds, 550 rpm and 850 rpm, which correspond to blade first flap mode natural frequencies of  $1.28\Omega$  and  $1.15\Omega$ . The total hub moment derivative, its phase angle of response and the ratio of the magnitudes of hub moment and shaft moment derivatives are plotted versus advance ratio. Shaft moment phase is approximately the same as hub moment phase and thus is not shown. The characteristics of the curves are similar to previous experimental results (References 1 and 2). That is, the magnitude of the response derivative increases with increased advance ratio and decreased flap frequency. Noteworthy also is the nearly constant phase angle of response over the tested advance ratio range for both rotor speeds. As discussed earlier in this section, the shaft moment data are subject to contamination by shear loads and rpm variations which accounts for the scatter in the

$$\frac{\partial HM / \partial \theta_0}{\partial SM / \partial \theta_0} \quad (6)$$

curves.

The results of the steady state tests with longitudinal and lateral cyclic pitch excitations are shown in Figures 11 and 12.

There was one steady state test condition which yielded a non-linear rotor moment response. It was with configuration 5 at 550 rpm and  $\mu = 0.41$  with an  $\alpha$ -excitation. The data are plotted in Figure 13. This non-linear behavior suggests that induced inflow is still an important consideration even at advance ratios as high as  $\mu = 0.40$ .

The test results with steady state angle of attack variations are presented in Figure 14. A change in sign of the hub roll moment derivative at  $\mu = 0.27$  (850 rpm) is indicated by the phase angle of response varying from less than to greater than  $\pi$  radians. This characteristic was also observed during high

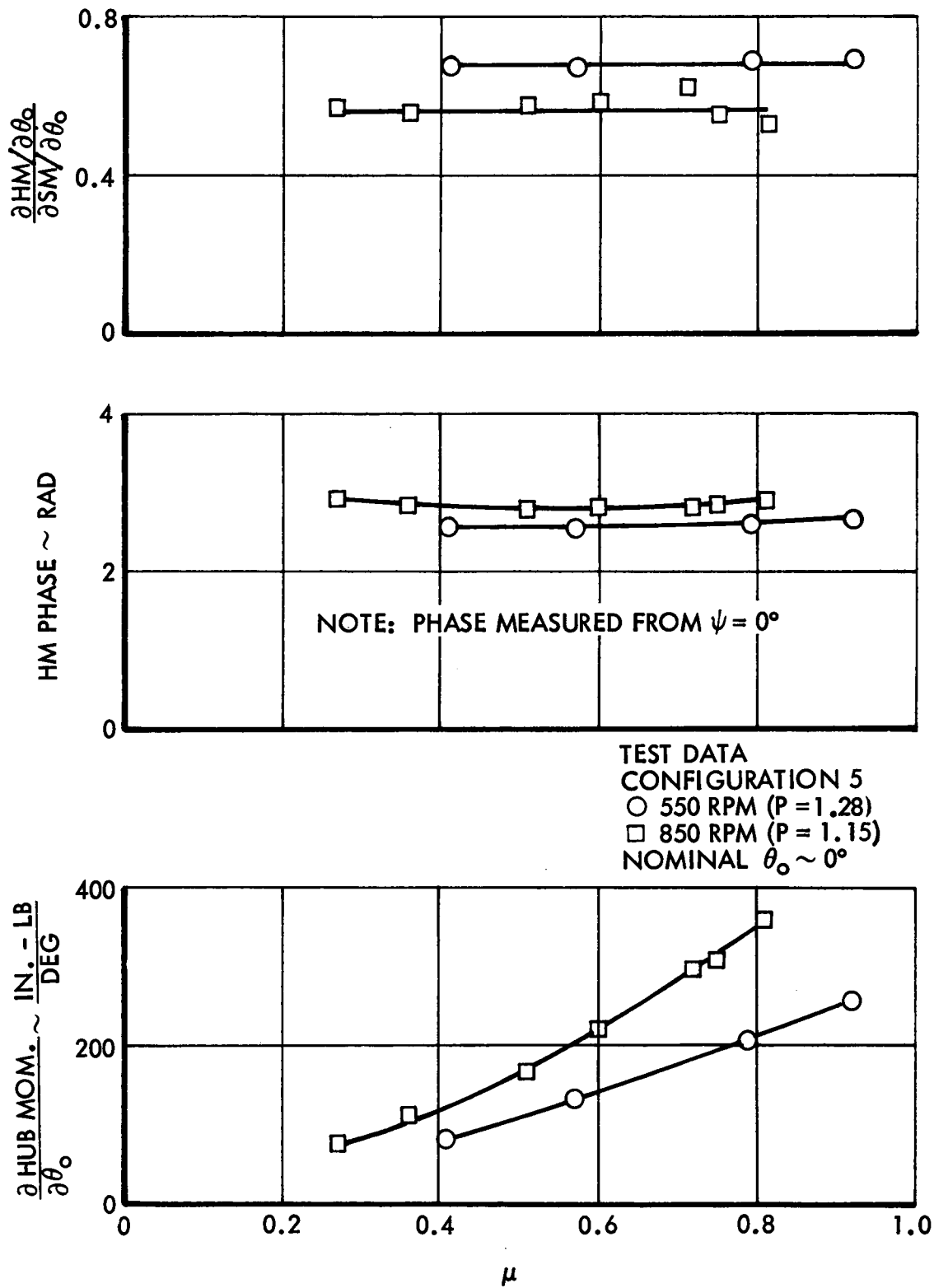
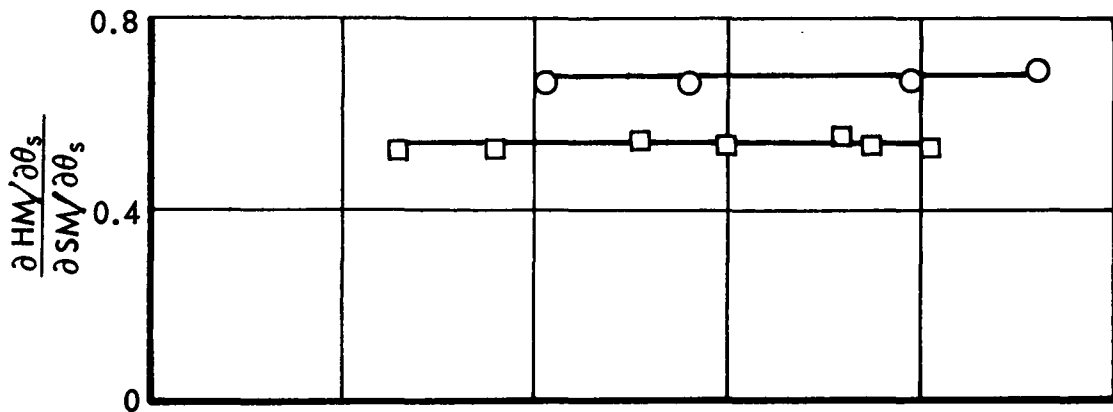
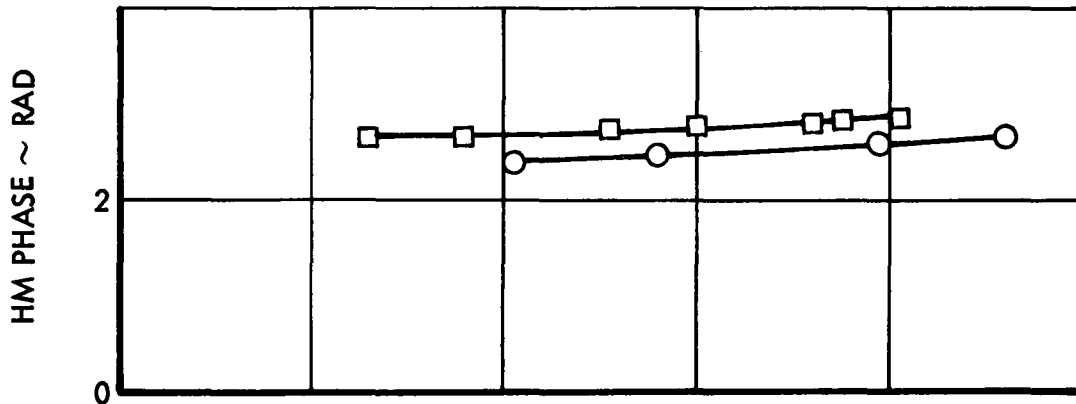


Figure 10. Rotor Hub and Shaft Moment Derivatives with Respect to  $\theta_0$ , Configuration 5





NOTE: PHASE MEASURED FROM  $\psi = 0^\circ$



TEST DATA  
 CONFIGURATION 5  
 ○ 550 RPM (P = 1.28)  
 □ 850 RPM (P = 1.15)  
 NOMINAL  $\theta_s \sim 0^\circ \rightarrow 1^\circ$

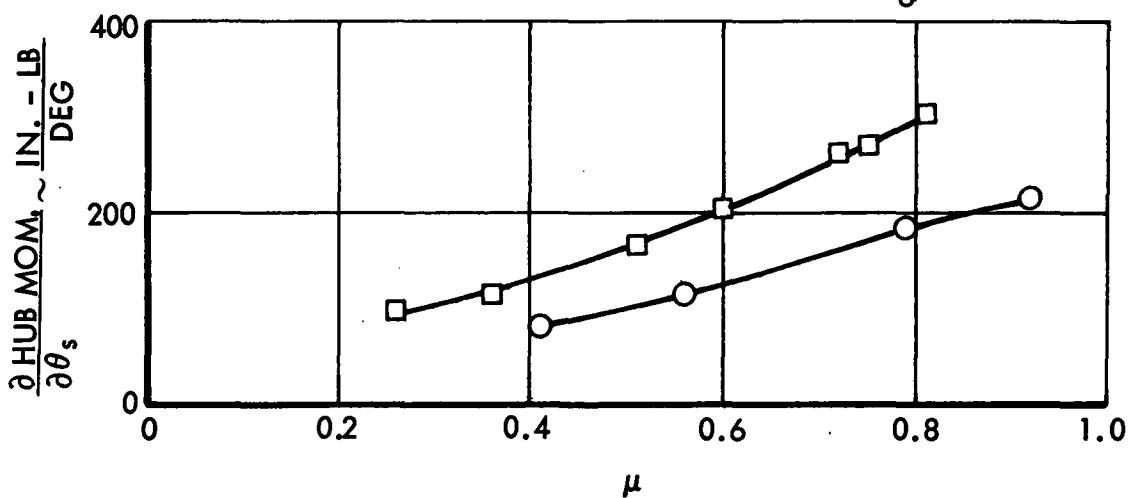
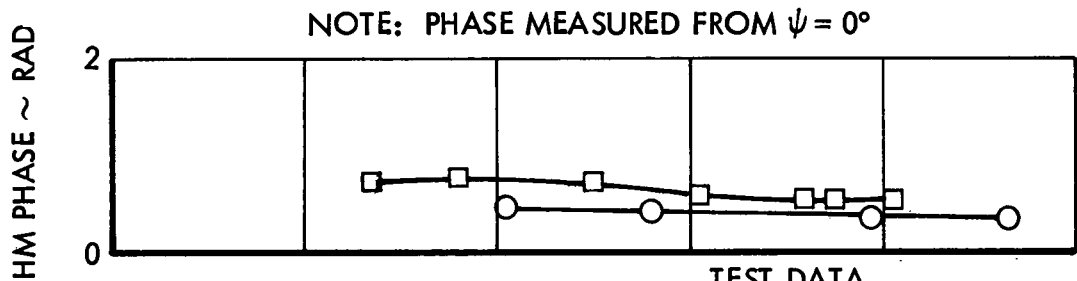
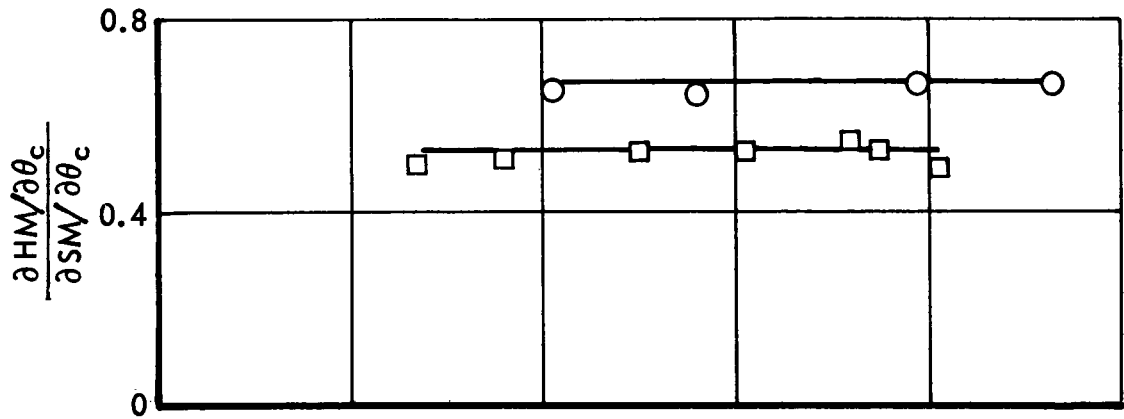


Figure 11. Rotor Hub and Shaft Moment Derivatives with Respect to  $\theta_s$ , Configuration 5



TEST DATA  
 CONFIGURATION 5  
 ○ 550 RPM (P = 1.28)  
 □ 850 RPM (P = 1.15)  
 NOMINAL  $\theta_o \sim 0^\circ \rightarrow 1^\circ$

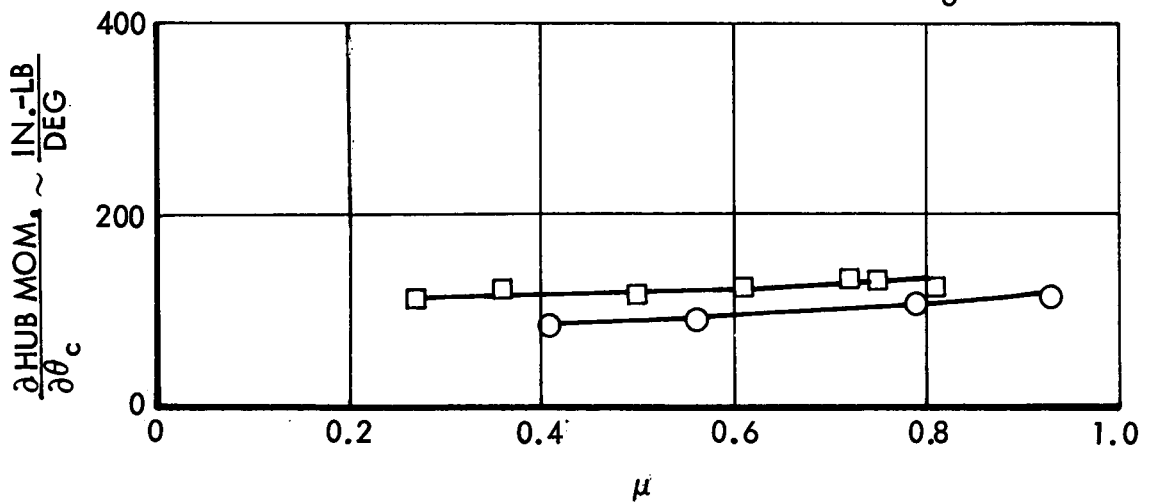


Figure 12. Rotor Hub and Shaft Moment Derivatives with Respect to  $\theta_c$ , Configuration 5

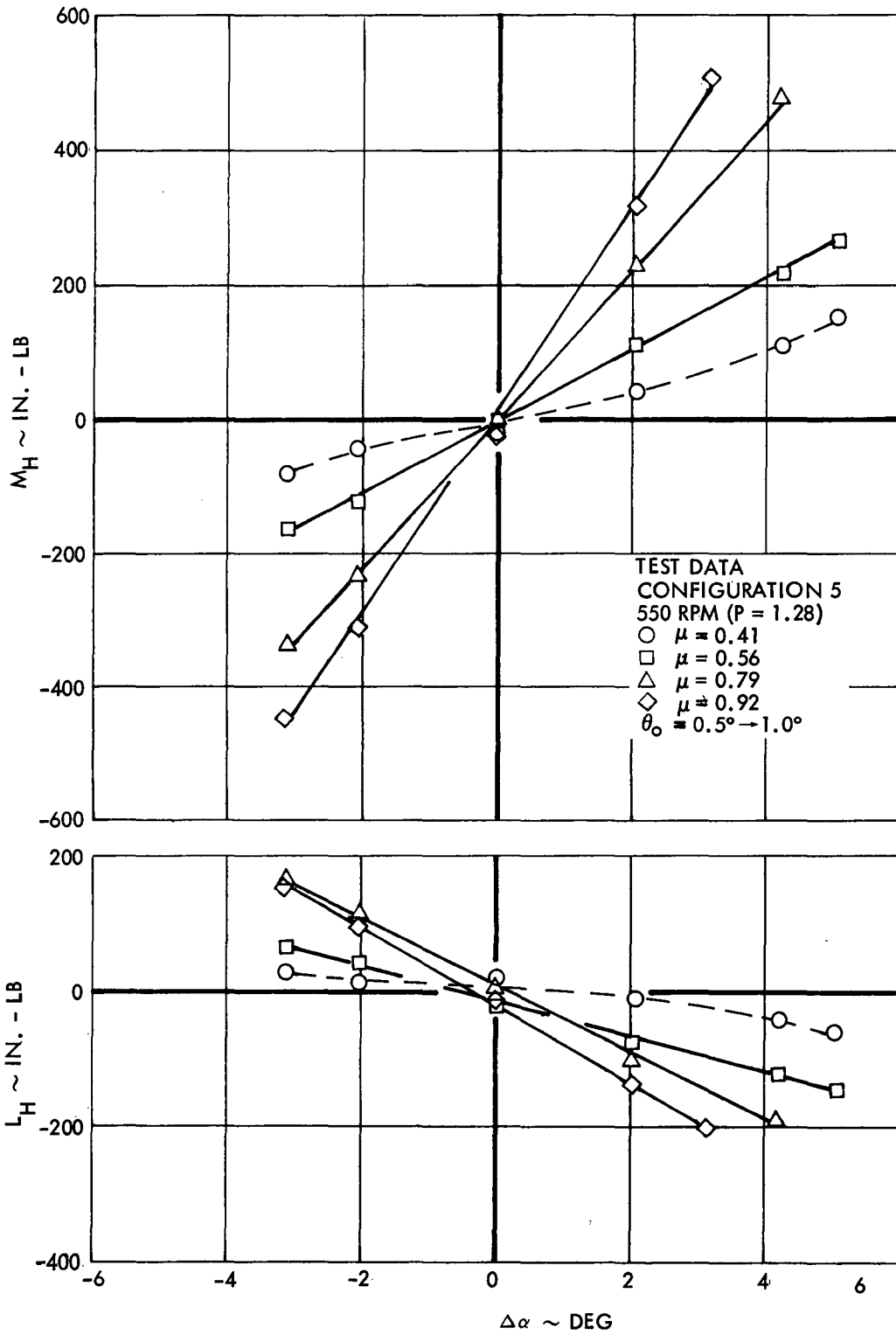
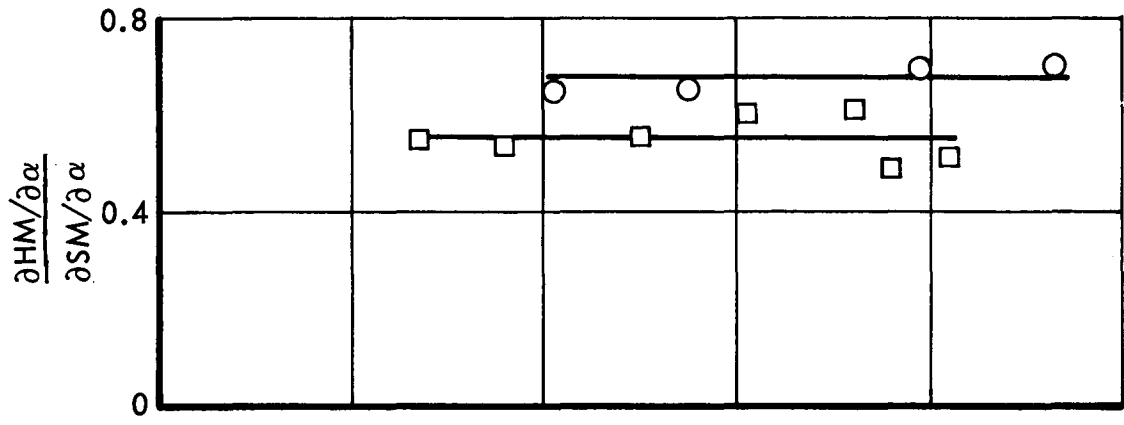
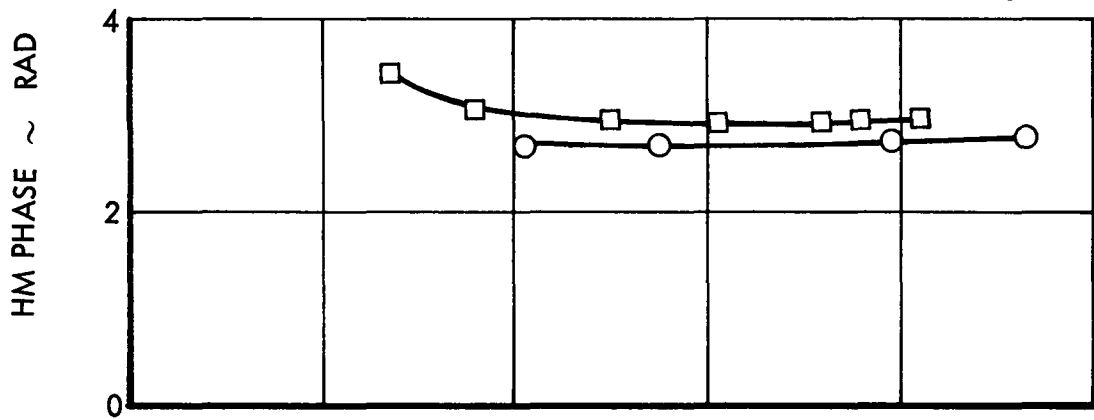


Figure 13. Rotor Hub Moment Response to  $\alpha$ , Configuration 5, 550 RPM (P = 1.28)



NOTE: PHASE MEASURED FROM  $\psi = 0^\circ$



TEST DATA  
 CONFIGURATION 5  
 ○ 550 RPM (P = 1.28)  
 □ 850 RPM (P = 1.15)  
 NOMINAL  $\theta_0 \sim 0^\circ \rightarrow 1^\circ$

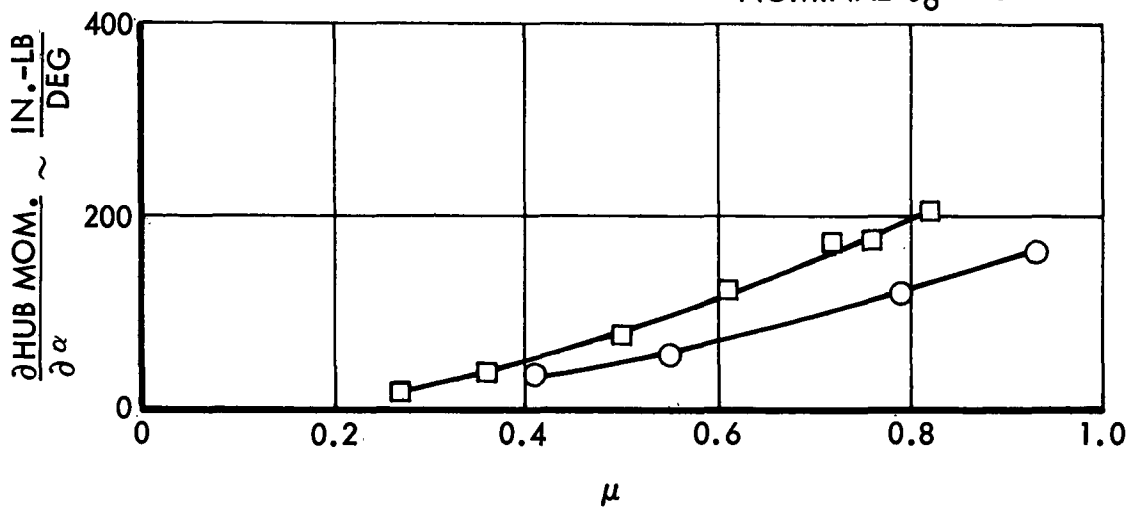


Figure 14. Rotor Hub and Shaft Moment Response Derivatives with Respect to  $\alpha$ , Configuration 5

rpm ( $P = 1.17$ ) steady state  $\alpha$ -tests of configuration 1 (Reference 2), and is thought to be caused by induced inflow.

The rotor lift which was generated during the application of  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  and  $\alpha$  disturbances is summarized in Figure 15. The lift is expressed in terms of blade loading coefficient ( $C_T/\sigma$ ) derivatives versus advance ratio. The slight negative lift generated by lateral cyclic pitch at high advance ratios was not previously discovered experimentally. It is probable that it would have been if a least squares linear curve fit of the test data had been used rather than a hand faired curve fit. It is noted that a simple theoretical model incorporating a two mode approximation for blade flapping and periodic aerodynamic spring, damping and excitation functions also predicts this characteristic. All of the lift data from which these derivatives were calculated are listed in Appendix A, as are the deviations of each data point from the curve fit line.

The harmonic content of a single blade flapping moment has also been extracted from the steady state test data. The digitized analog output of a flap strain gage located at 3.3 inches from the center of rotation of blade 1 has been Fourier analyzed at harmonic frequencies up to  $4\Omega$ . Typical results of this analysis are shown in Figure 16, where the derivatives with respect to  $\theta_o$  are plotted versus  $\mu$  for the 850 rpm tests. Similar data for all the steady state test conditions are plotted in Appendix A. The experimental data from which the derivatives were calculated are also tabulated therein.

The total blade flapping moment is expressed as

$$\begin{aligned}
 M_{\beta} (\text{@ } r = 3.3 \text{ in.}) = & M_{\beta_o} - M_{\beta_{1c}} \cos \psi - M_{\beta_{1s}} \sin \psi \\
 & - M_{\beta_{2c}} \cos 2\psi - M_{\beta_{2s}} \sin 2\psi \\
 & - M_{\beta_{3c}} \cos 3\psi - M_{\beta_{3s}} \sin 3\psi \\
 & - M_{\beta_{4c}} \cos 4\psi - M_{\beta_{4s}} \sin 4\psi
 \end{aligned} \tag{7}$$

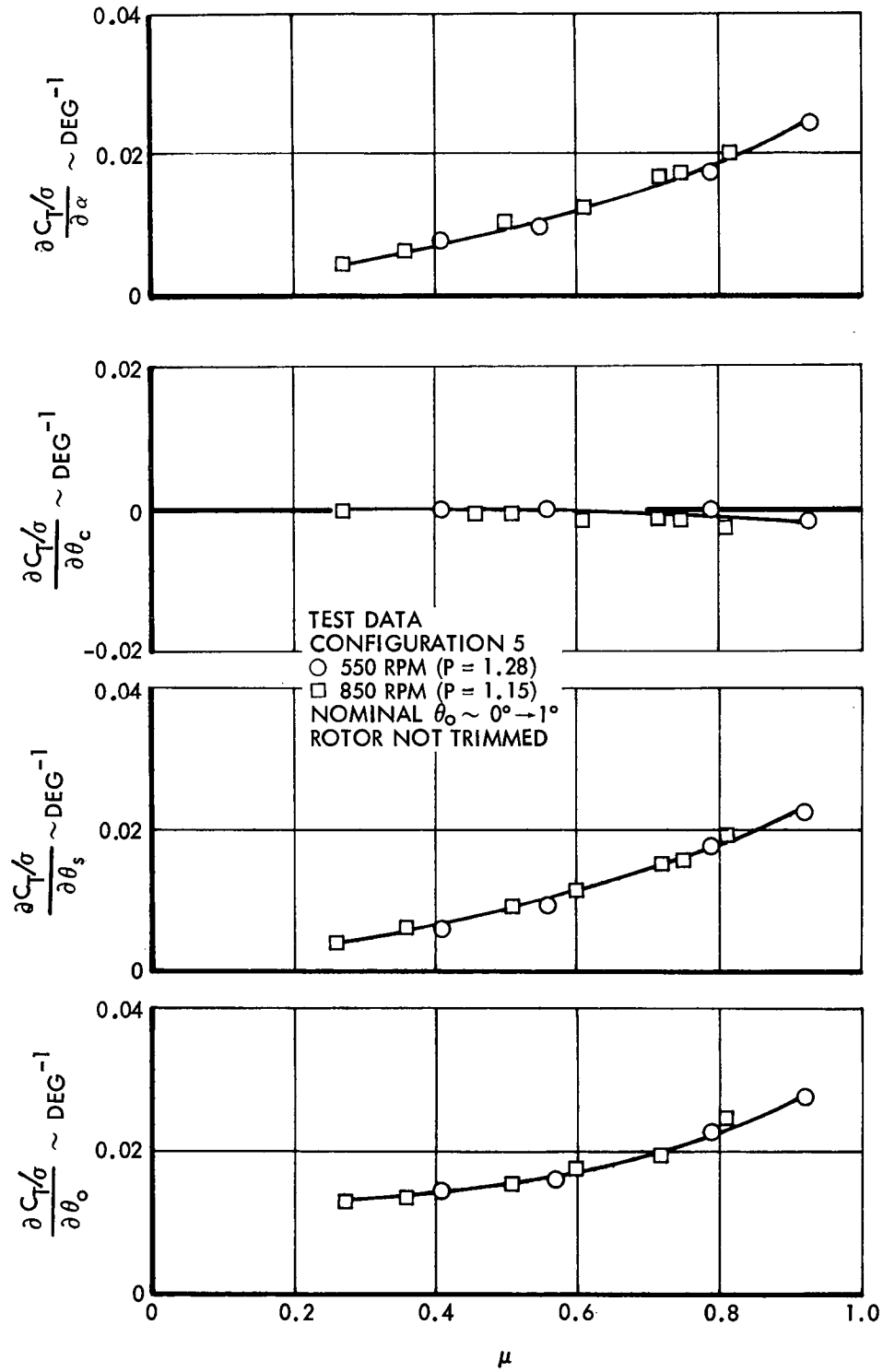


Figure 15. Rotor Lift Derivatives Versus  $\mu$

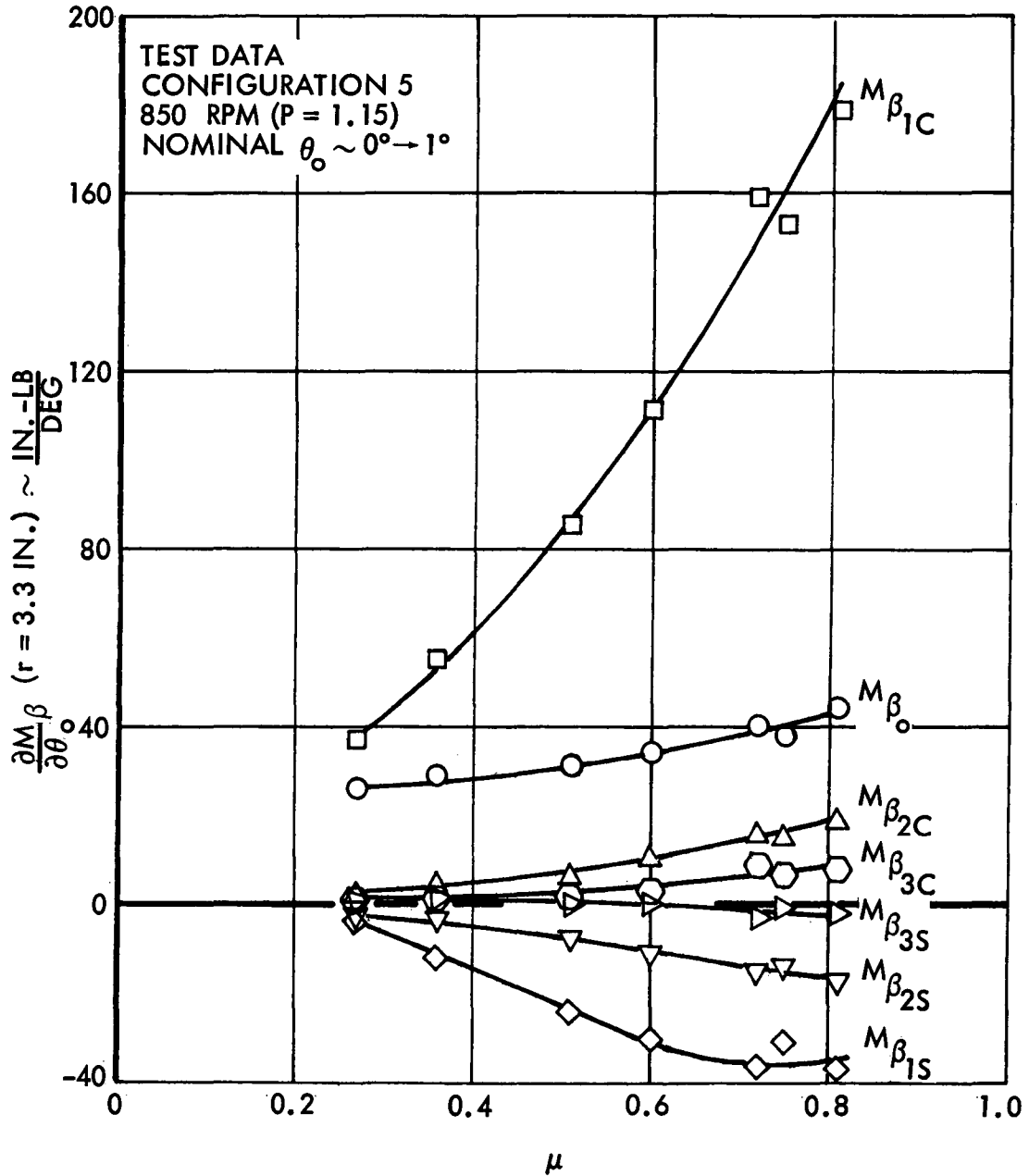


Figure 16. Harmonic Content of Blade Flapping, Configuration 5, 850 RPM (P = 1.15), Steady  $\theta_0$  Excitation

The data indicate that the blade 1-per-rev response is dominant over the tested advance ratio range and that the strength of the higher harmonic flapping increases with advance ratio. This latter characteristic is expected since it coincides with a corresponding increase in the higher harmonic aerodynamic excitations (Reference 1). The 4-per-rev harmonic of the blade flapping moment derivative was not plotted since it was approximately zero for all tested conditions.

A cursory examination of Figure 16 reveals an anomaly in the data taken at  $\mu = 0.72$  and  $0.75$ . One's first inclination might be to attribute the inflection to scatter and simply fair a curve through the data (as has been done). This may be totally valid because the tests at  $\mu = 0.75$  and  $\mu = 0.81$  were performed at the end of the wind tunnel program and those up to and including  $\mu = 0.72$  at the beginning of the test. It is conceivable (though not a certainty) that deadbands in the controls and/or the flapping stiffness (as affected by the feathering bearing slop) could have changed sufficiently to generate scatter of the magnitude indicated. The fact that the derivatives of Figure 16 are based upon data from one blade must also be considered. The hub moment derivatives previously presented (which are a function of the flapping of all 4 blades) display a much milder curvature at  $\mu \sim 0.75$ . It is logical to expect that the overall effect of slop and deadband would be reduced if four blade motions are averaged.

It is also possible that the characteristic is natural. Work by Dr. Robert A. Ormiston and Mr. David A. Peters of AMRDL (Ames Directorate), reported in Reference 3, indicates that an inflection in the derivative curves should occur at  $\mu \sim 0.8$  due to inflow. Their results, however, suggest that the perturbation should occur over an advance ratio span of  $\sim 0.3$  rather than the 0.05 width seen in Figure 16.

Plans are currently underway to re-enter the tunnel with the High Advance Ratio Model to conduct high lift testing. At that time data will be obtained which will resolve the peculiarity just described.

The rotor blade one-per-rev (1P) bending moment distribution has also been determined by harmonically analyzing the radially distributed flapping bending moments. Flap moments were measured at



$$r = 3.3 \text{ in. (} x = 0.073 \text{)}$$

$$r = 13.15 \text{ in. (} x = 0.293 \text{)}$$

$$r = 22.3 \text{ in. (} x = 0.49 \text{)}$$

on blade No. 1 and their 1P derivatives with respect to  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  and  $\alpha$  calculated. These were then nondimensionalized by one-half the shaft moment derivative (i.e., blade moment derivative at  $x = 0$ ) to obtain a nondimensional distribution. The results at  $\mu = 0$  for a  $\theta_s$ -excitation are plotted in Figure 17. Data for the three tested rotor speeds are presented. Both the magnitude and phase of the moments are shown as a function of nondimensional radial position ( $x$ ). For a constant shaft moment the data show a decrease in the outboard flap bending moments with increased rotor rotational speed. The reason for this is that the internal loading in the structure is a function of the flapping displacement which decreases at higher rotor speeds (for a constant airload) because of increased centrifugal force. The linearity of the distributions and the nearly constant phase angle of response (with radial position) suggests that the 1P airload is concentrated over an outboard expanse of the blade.

The blade bending moment distributions for all of the forward flight test conditions and excitations have been calculated. The curves and a tabulation of the test data used to calculate the derivatives are presented in Appendix A. The forward flight distributions are very similar to those shown in Figure 17. The radial blade bending moments are not significantly affected by either advance ratio or type of excitation.

#### Open Loop Frequency Response Tests (Swashplate Excitations)

Open loop frequency response tests with  $\theta_o$ ,  $\theta_s$  and  $\theta_c$  excitations were conducted with configuration 5 only. The test procedures and data analysis techniques were the same as those used during the Phase 2 program (Reference 2). The problem of support stand resonance, which affected some of the Phase 2 data in the frequency range 6 to 10 Hz, was not evident (either visually or from accelerometer measurements) during these Phase 3 tests. There are probably two reasons for this. First, the magnitude of the viscous damping of

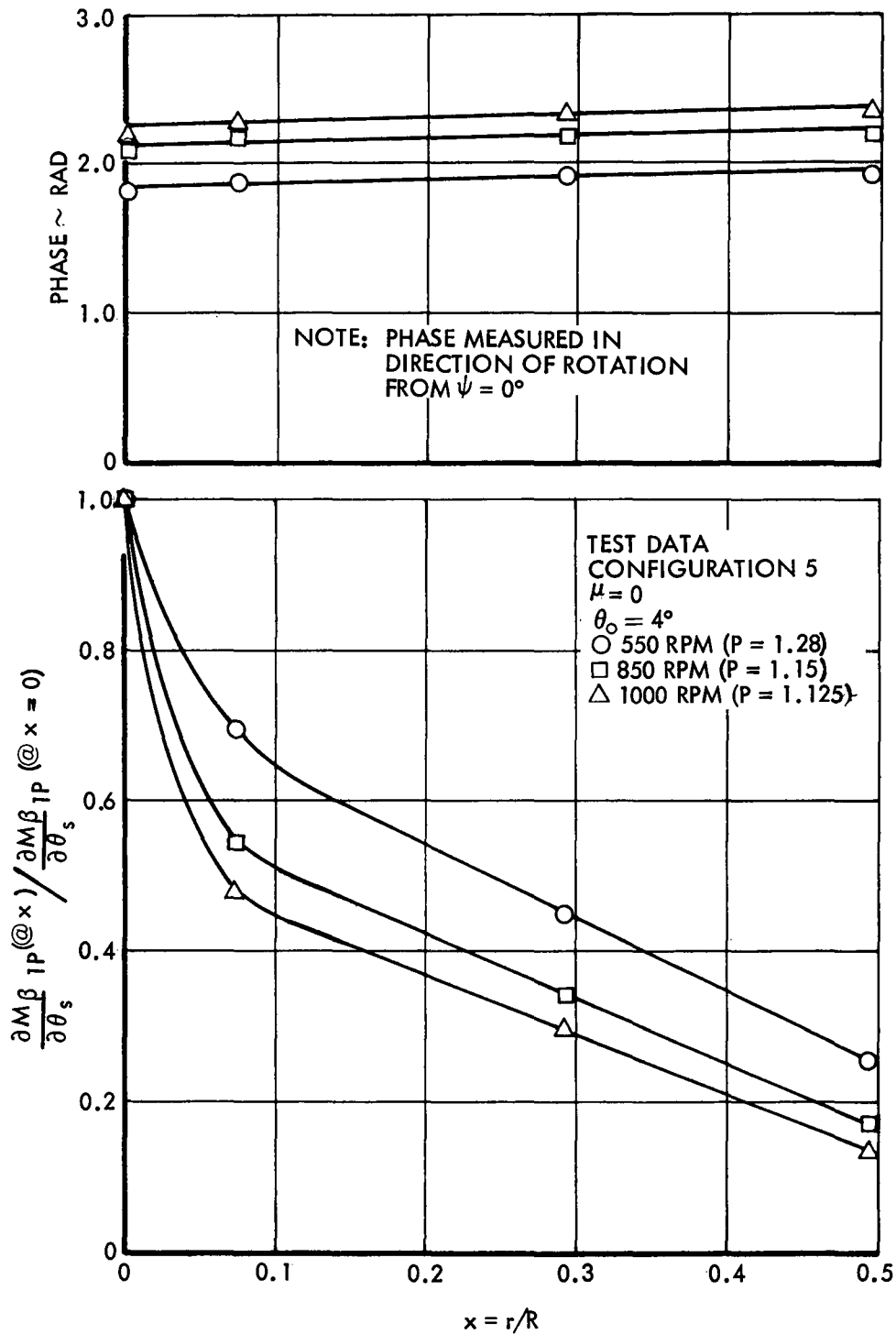


Figure 17. One-Per-Rev Blade Radial Flap Bending Moment Distribution at  $\mu = 0$

the model pitch motion was increased above the previous value. Secondly, the softer rotor hub configuration may have actually added to the damping of the body mode and/or changed the relative magnitudes and phases of the motions (eigenvectors) in the mode.

There was one problem which was encountered with high frequency sinusoidal cyclic pitch excitations. The gyroscopic inertia moments which were generated in one swashplate axis by excitations in the other axis, aggravated by a servo natural frequency of approximately 40 Hz, produced coupling between longitudinal and lateral cyclic pitch. The degree of coupling was a nonlinear function of the excitation frequency ( $\omega$ ) and a linear function of the swashplate rotational frequency ( $\Omega$ ). Because of this it was reasoned that the coupling was caused by the near resonance response of the servo to the gyroscopic excitation rather than a simple overpowering of the actuator. Typical  $\theta_c/\theta_s$  and  $\theta_s/\theta_c$  couplings are shown in Figure 18.

Correcting the test data to obtain hub moment pitch and roll frequency response with respect to pure  $\theta_s$  and  $\theta_c$  excitations was relatively simple. It consisted of forming a complex second order linear system from moment and cyclic pitch data during the  $\theta_s$  and  $\theta_c$  tests which were conducted at the same excitation frequency, i.e.,

$$\begin{aligned} \theta_{s1} \frac{\partial M_{H1}}{\partial \theta_s} + \theta_{c1} \frac{\partial M_{H1}}{\partial \theta_c} &= M_{H1} \\ \theta_{s2} \frac{\partial M_{H2}}{\partial \theta_s} + \theta_{c2} \frac{\partial M_{H2}}{\partial \theta_c} &= M_{H2} \end{aligned} \quad (8)$$

The subscript 1 refers to data obtained when  $\theta_s$  was the intended excitation and the subscript 2 when  $\theta_c$  was the principal excitation. Premultiplying Eq. 8 by the inverse of the  $\theta$ -matrix yields the following linear system which is solved simultaneously to obtain the moment derivatives.

$$\begin{pmatrix} \frac{\partial M_{H1}}{\partial \theta_s} \\ \frac{\partial M_{H2}}{\partial \theta_c} \end{pmatrix} \begin{bmatrix} \theta_{s1} & \theta_{c1} \\ \theta_{s2} & \theta_{c2} \end{bmatrix}^{-1} = \begin{pmatrix} M_{H1} \\ M_{H2} \end{pmatrix} \quad (9)$$

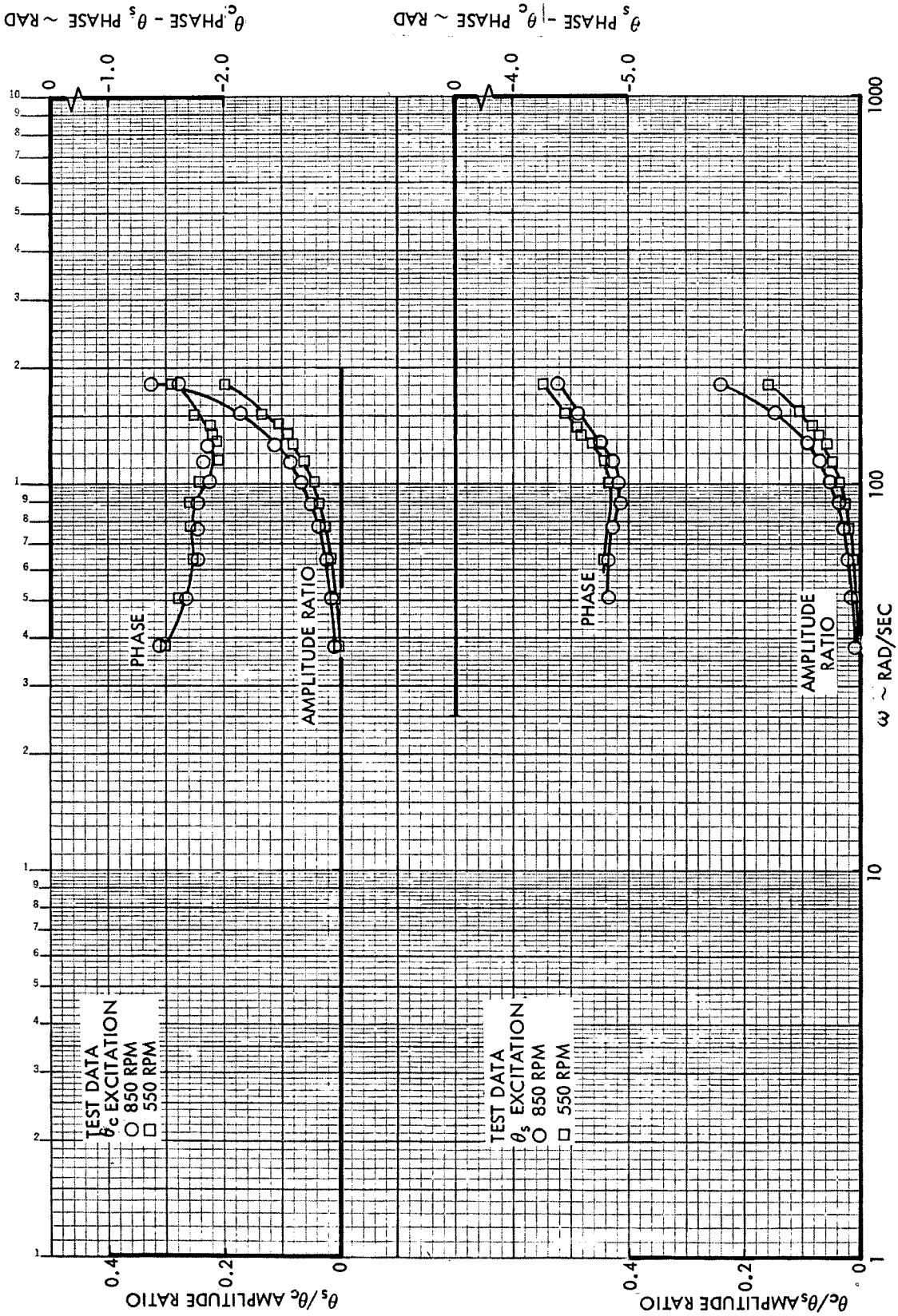


Figure 18. Cyclic Pitch Coupling at High Excitation Frequencies

Since the numbers are complex, the amplitude ratio and phase lag between the moment and the cyclic pitch are obtained directly. Most of  $\theta_s$  and  $\theta_c$  tests were conducted at identical frequencies. For the few tests that were not, interpolated values were used to generate one of the two linear equations. Since both  $\theta_c$  and  $\theta_s$  tests were not performed in hover, symmetry in the coupling was assumed.

It is noted that the frequency response data presented in Reference 2 were not corrected for the cyclic pitch coupling (the problem was not recognized at the time). The maximum excitation frequency for those tests was 22 Hz and the three tested rotor speeds were 300, 550, and 800 rpm. Based upon Figure 18, the probable coupling which existed at 22 Hz was

- 300 rpm - 4.78% coupling
- 550 rpm - 8.75% coupling
- 800 rpm - 12% coupling.

The maximum correction applied to the Phase 3 data at  $\omega = 22$  Hz and 850 rpm was  $\sim 1$  dB and  $\sim 5^\circ$  phase. It is therefore concluded that the corrections to the Phase 2,  $\theta_s$  and  $\theta_c$  frequency response data would have been within experimental error.

The experimental open loop rotor transfer functions with respect to swashplate excitations for configuration 5 are approximately the same as those determined for configuration 1 during the Phase 2 test. In general, the rotor response peaked when the excitation frequency was in resonance with the blade rotating first flap bending mode natural frequency. As shown in Figure 19, this occurred twice; when  $\omega = (P - 1)\Omega$  and  $\omega = (P + 1)\Omega$ . The cited example presents the hub pitch moment frequency response to collective pitch at an advance ratio of  $\mu = 0.41$  and a rotor speed of 550 rpm. The amplitude ratio  $M_H/\theta_o$  is expressed in decibels (dB)

$$\text{dB} = 20 \text{ LOG}_{10} (\text{amplitude ratio}) \quad (10)$$

and has the dimensions in.-lb/deg. The phase lag of  $M_H$  relative to  $\theta_o$  is expressed in degrees in the range  $-180^\circ \rightarrow +180^\circ$ . The measured hub roll

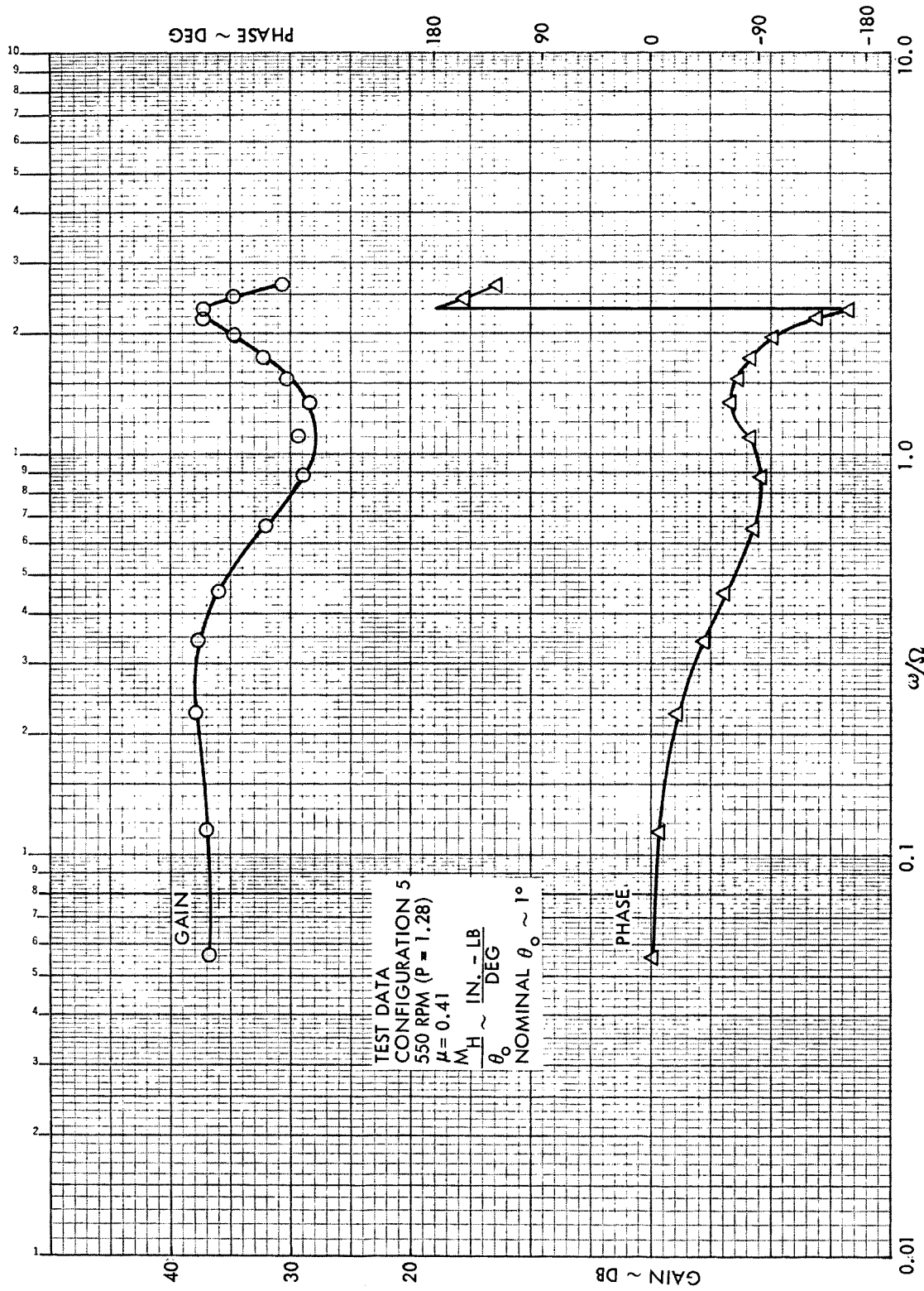


Figure 19. Rotor Hub Pitch Moment Frequency Response to  $\theta_0$ ,  $\mu = 0.41$ , Configuration 5, 550 RPM (P = 1.28)

moment frequency response to  $\theta_0$  for the same test condition is shown in Figure 20. The dissimilarity of the  $M_H$  and  $L_H$  gain curves indicates that the rotor phase angle of response, i.e.,

$$\text{PHASE ANGLE OF RESPONSE} = \text{TAN}^{-1} \left( \frac{-L_H}{-M_H} \right) \quad (11)$$

varies with the excitation frequency.

It is noted that the rotor moment transfer functions presented in this report have the dimensions in.-lb/deg. In Reference 2 the moments were non-dimensionalized by an analytically determined rotor stiffness ( $K_\theta$ ) and presented in the form of fore-aft ( $a_1$ ) and lateral ( $b_1$ ) rotor angular displacements. This approach was not used for the current presentation because the assumption that a single value of  $K_\theta$  is sufficient for all test conditions at a constant rotor speed is not totally valid. The procedure by which  $K_\theta$  was reduced to account for the radially offset hub moment measurement is also suspect. The transfer functions in Reference 2 can be converted to the dimensions in.-lb/deg by simply adding

$$20 \text{ LOG}_{10} K_\theta \quad (12)$$

to the gain values which have the units deg/deg.  $K_\theta$  values for the Phase 2 data are listed in Table IV of Reference 2. For those who would prefer to nondimensionalize the Phase 3 hub moment data,  $20 \text{ LOG}_{10} K_\theta$  must be subtracted from the gains with the dimensions in.-lb./deg.  $K_\theta$  values for configuration 5 which are calculated from first flap bending mode moments and deflections (see Section 7 of Reference 1) are

<u>RPM</u>	<u><math>K_\theta</math> (@ 3.3 in.)</u>
1000	125 in-lb/deg
850	123
550	120

An increase in the damping of blade flapping with increased advance ratio was revealed by the measured hub moment frequency response. Examples of data which demonstrate this characteristic are contained in the next four curves.

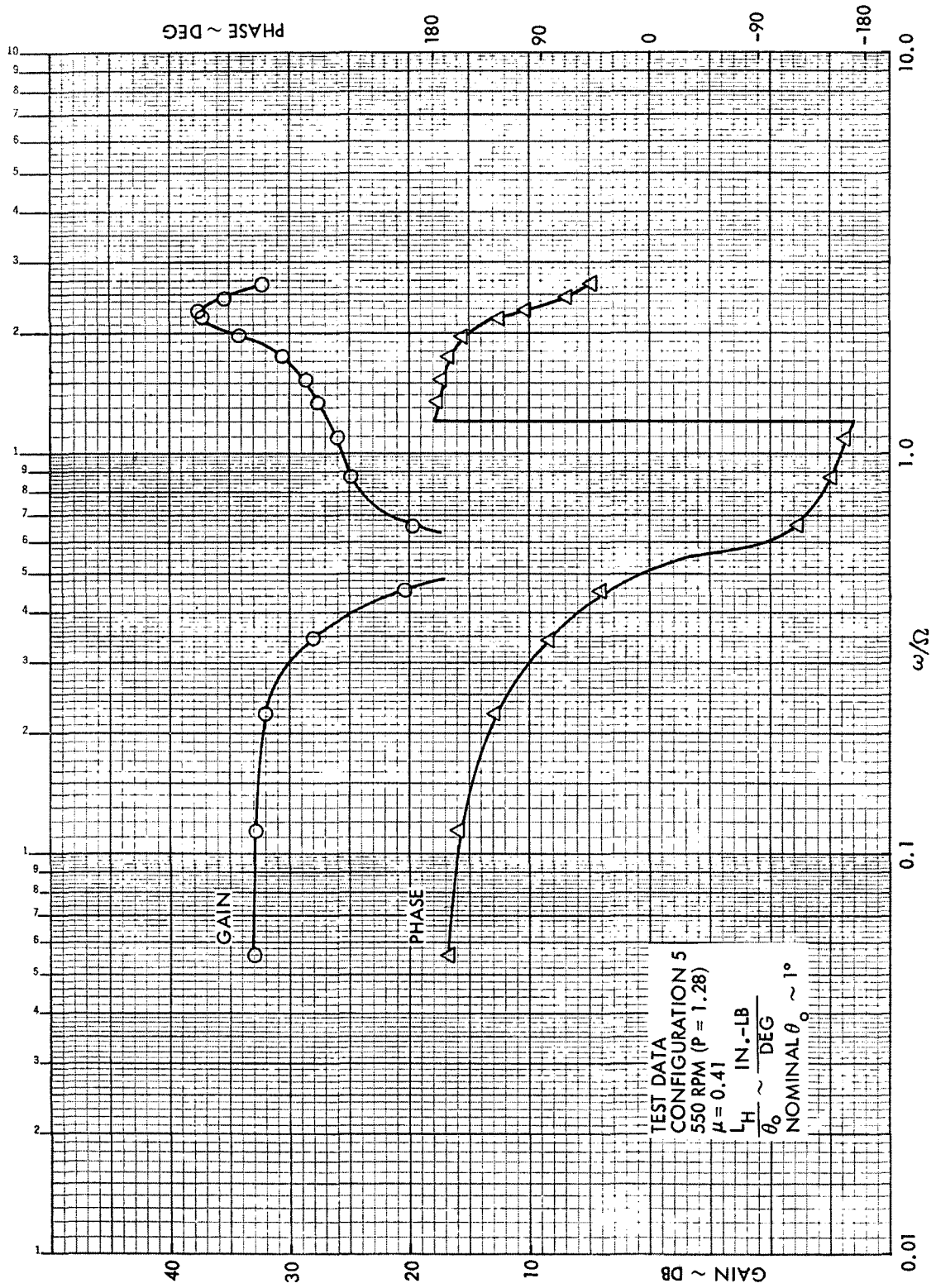


Figure 20. Rotor Hub Roll Moment Frequency Response to  $\theta_0$ ,  $\mu = 0.41$ , Configuration 5, 550 RPM (P = 1.28)



Figures 21 and 22 present the rotor hub moment frequency response to longitudinal cyclic pitch at  $\mu = 0$  and a rotor speed of 850 rpm. Similar transfer functions are plotted in Figures 23 and 24 at  $\mu = 0.27$ . The increase in flap damping is indicated by both the gain and the phase curves. The reduced peaking of the low frequency hub pitch moment response at  $\mu = 0.27$  as compared with the response at  $\mu = 0$  is indicative of greater damping. Also the rate of change in phase lag with excitation frequency of both the pitch and roll response is smaller at  $\mu = 0.27$  than at  $\mu = 0$ . This trend is also characteristic of increased damping.

If the high frequency portions of the transfer functions at the two advance ratios are now compared, it is seen that the gain and phase curves are nearly identical or varying at the same rate. It is known that the decrease in the low frequency response is caused by induced inflow. It is suspected, therefore, that the induced velocity only has an influence on the rotor response at low frequencies. For the example shown the inflow has an effect only up to  $\omega/\Omega \sim 0.2$ .

Another feature of the 850 rpm frequency response data which is notable is a broad fluctuation in the hub moment gain curves centered at  $\omega/\Omega \sim 0.8$ . Examples of the response are shown in Figures 25 and 26 in which the hub moment transfer functions with respect to collective pitch at  $\mu = 0.27$  are plotted. The characteristic in question is manifested by a peak in the pitch moment and a depression in the roll moment gain curves. It is suspected that this characteristic is caused by a mild involvement of the second flap bending mode in the response. The variations are the most prevalent when the moments are at a low level and the control input is collective pitch. If the dynamic response of the second flap mode is assumed to be relatively invariant with the tested aerodynamic environment, its influence on the total response would lessen at increased moments because of the decibel presentation.

All of the rotor hub moment frequency response data with respect to  $\theta_o$ ,  $\theta_s$  and  $\theta_c$  control inputs for configuration 5 (as delineated in Table III) are contained in Appendix B. The results are presented graphically in curves exactly like those just discussed. The experimental hub moment transfer

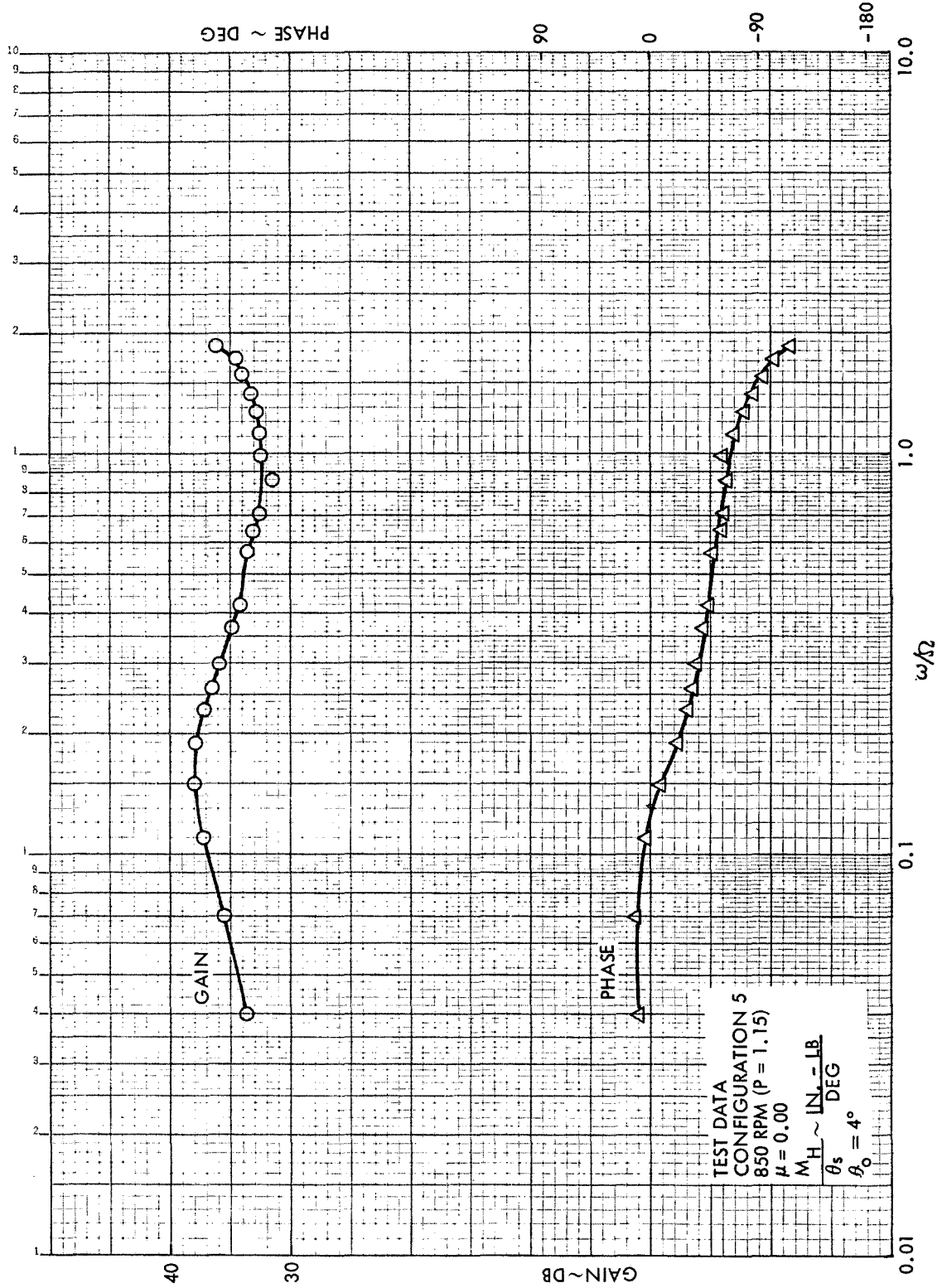


Figure 21. Rotor Hub Pitch Moment Frequency Response to  $\theta_s$ ,  $\mu = 0$ , Configuration 5, 850 RPM (P = 1.15)

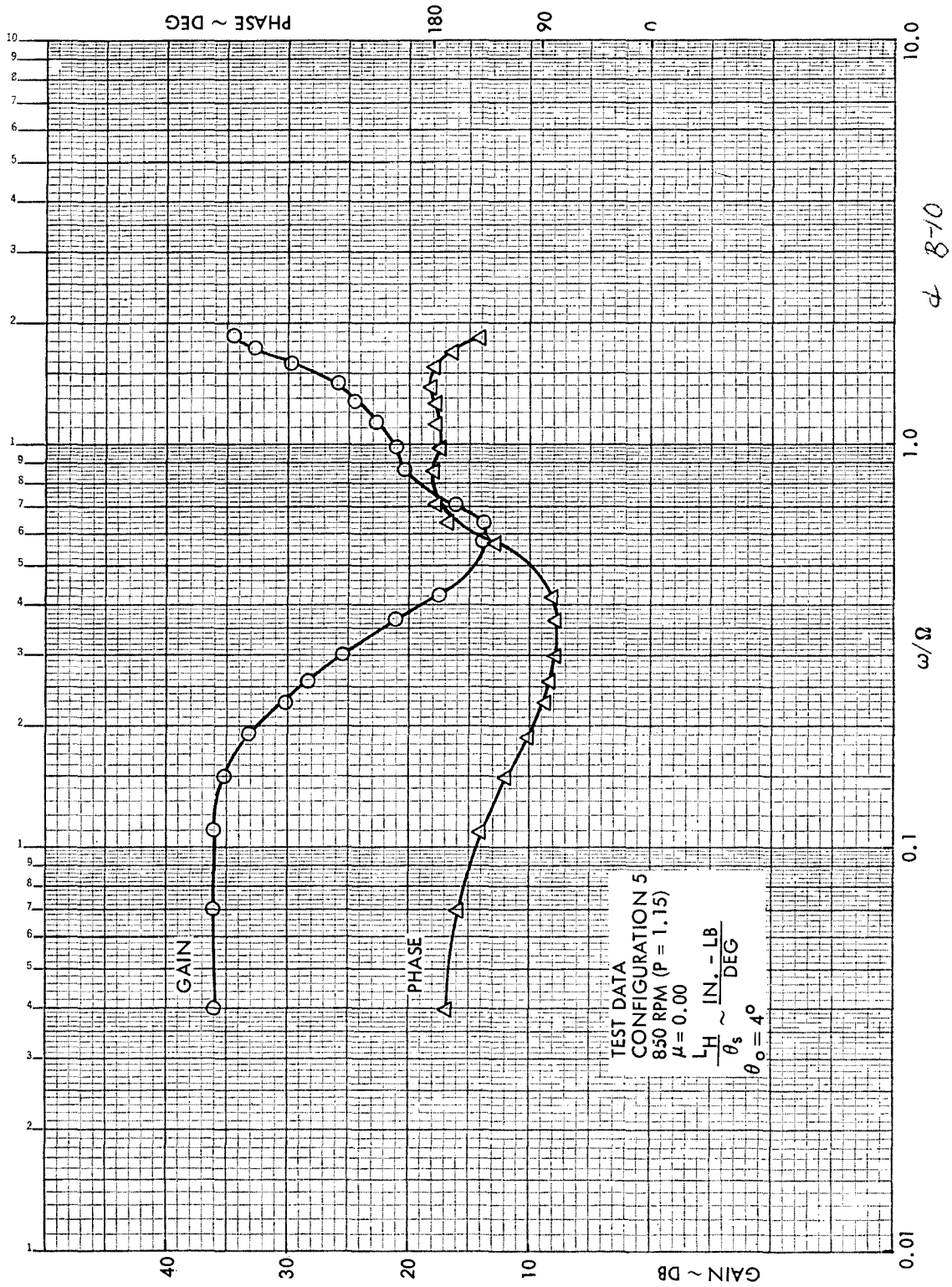


Figure 22. Rotor Hub Roll Moment Frequency Response to  $\theta_s$ ,  $\mu = 0$ , Configuration 5, 850 RPM ( $P = 1.15$ )

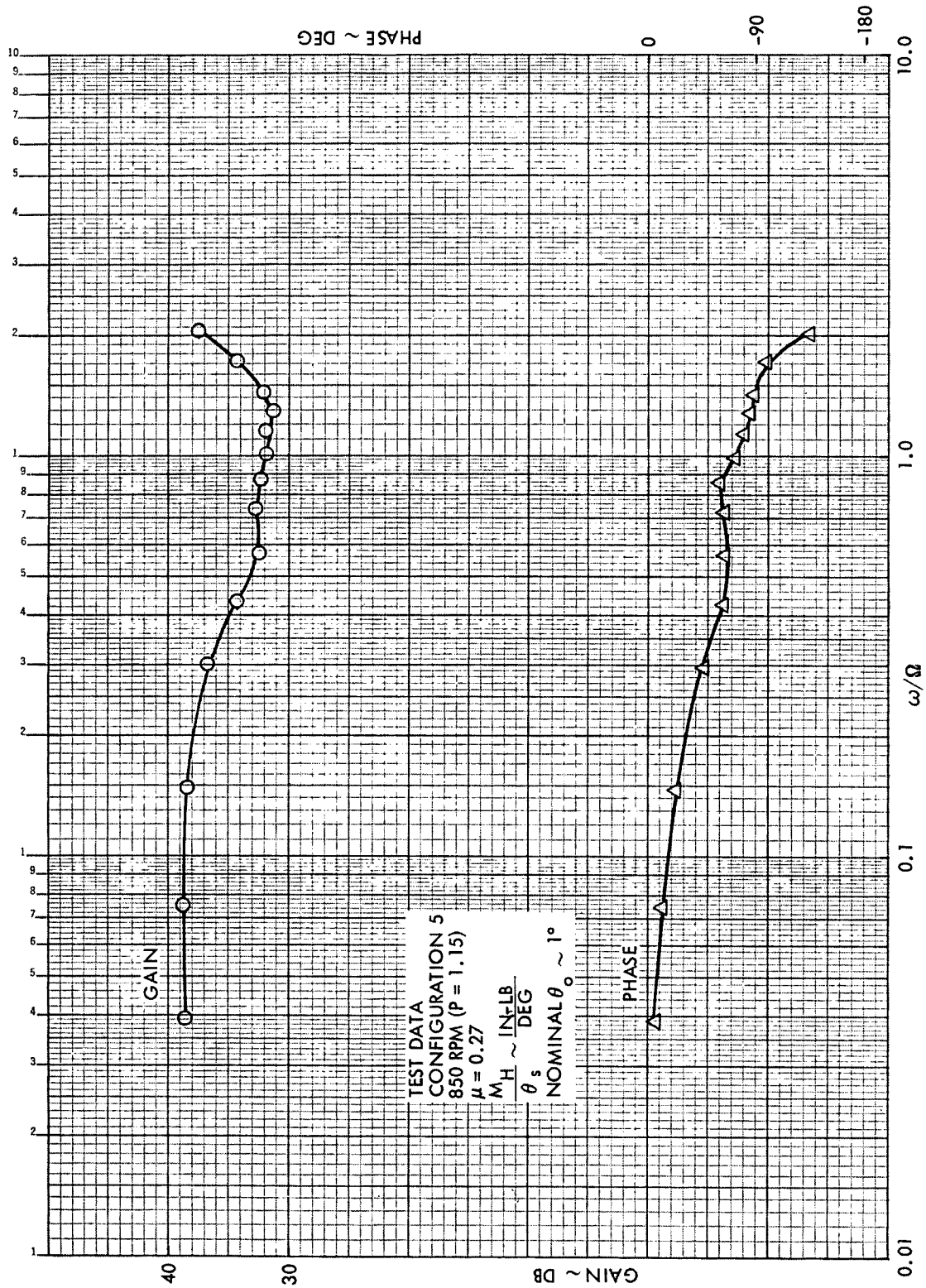


Figure 23. Rotor Hub Pitch Moment Frequency Response to  $\theta_s$ ,  $\mu = 0.27$ , Configuration 5, 850 RPM (P = 1.15)

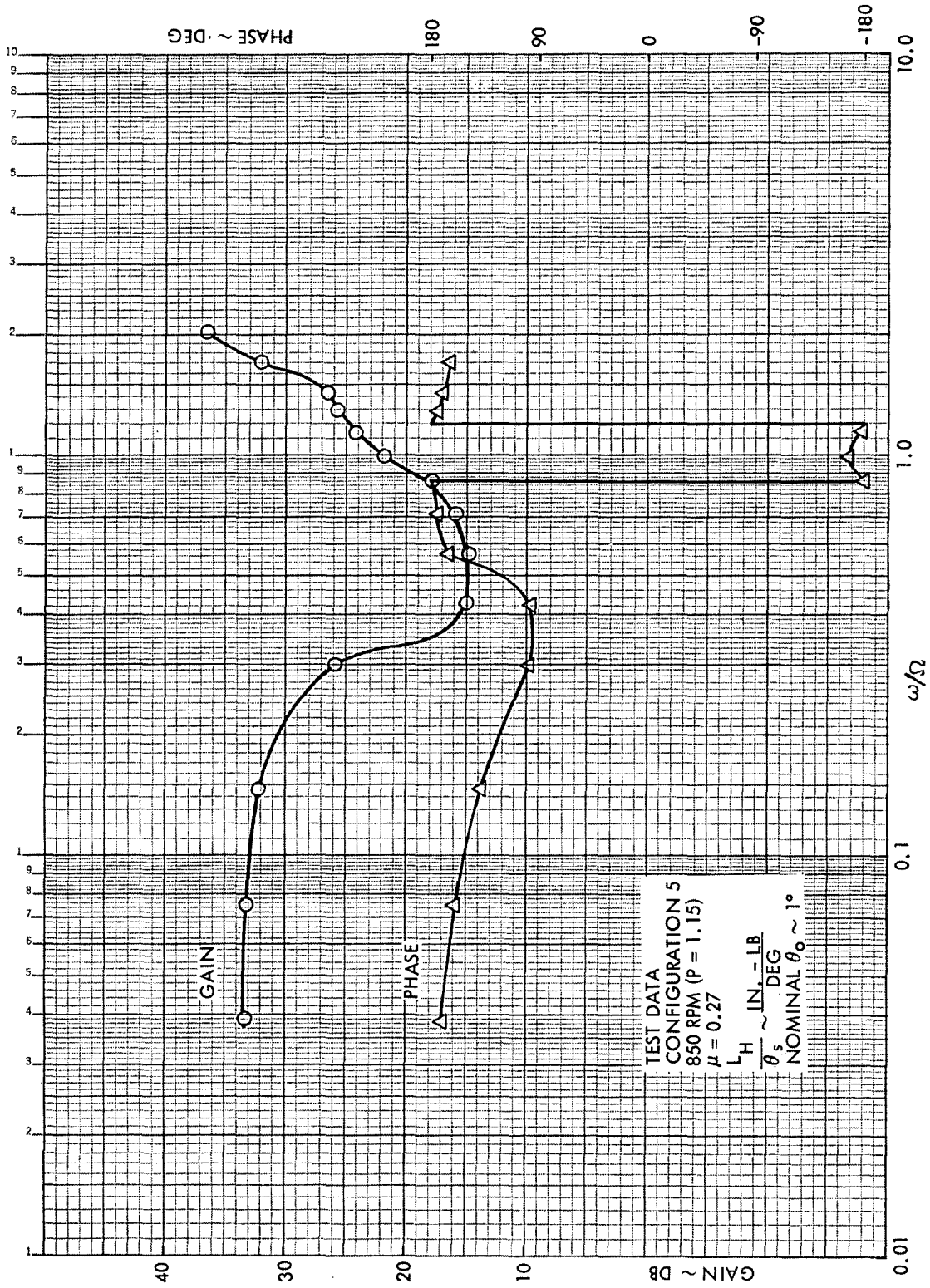


Figure 24. Rotor Hub Roll Moment Frequency Response to  $\theta_s$ ,  $\mu = 0.27$ , Configuration 5, 850 RPM ( $\mu = 1.15$ )

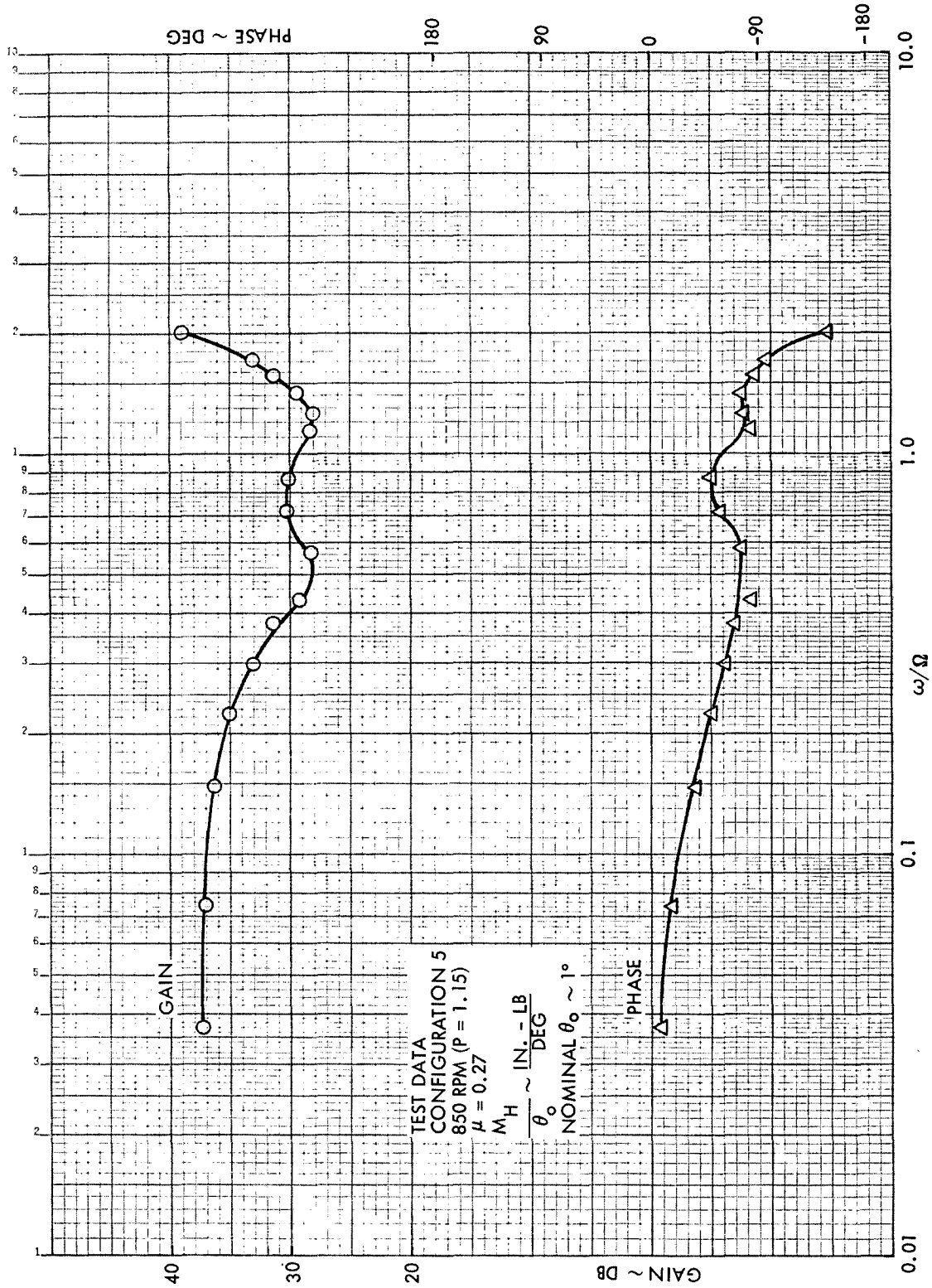


Figure 25. Rotor Hub Pitch Moment Frequency Response to  $\theta_0$ ,  $\mu = 0.27$ , Configuration 5, 850 RPM (P = 1.15)

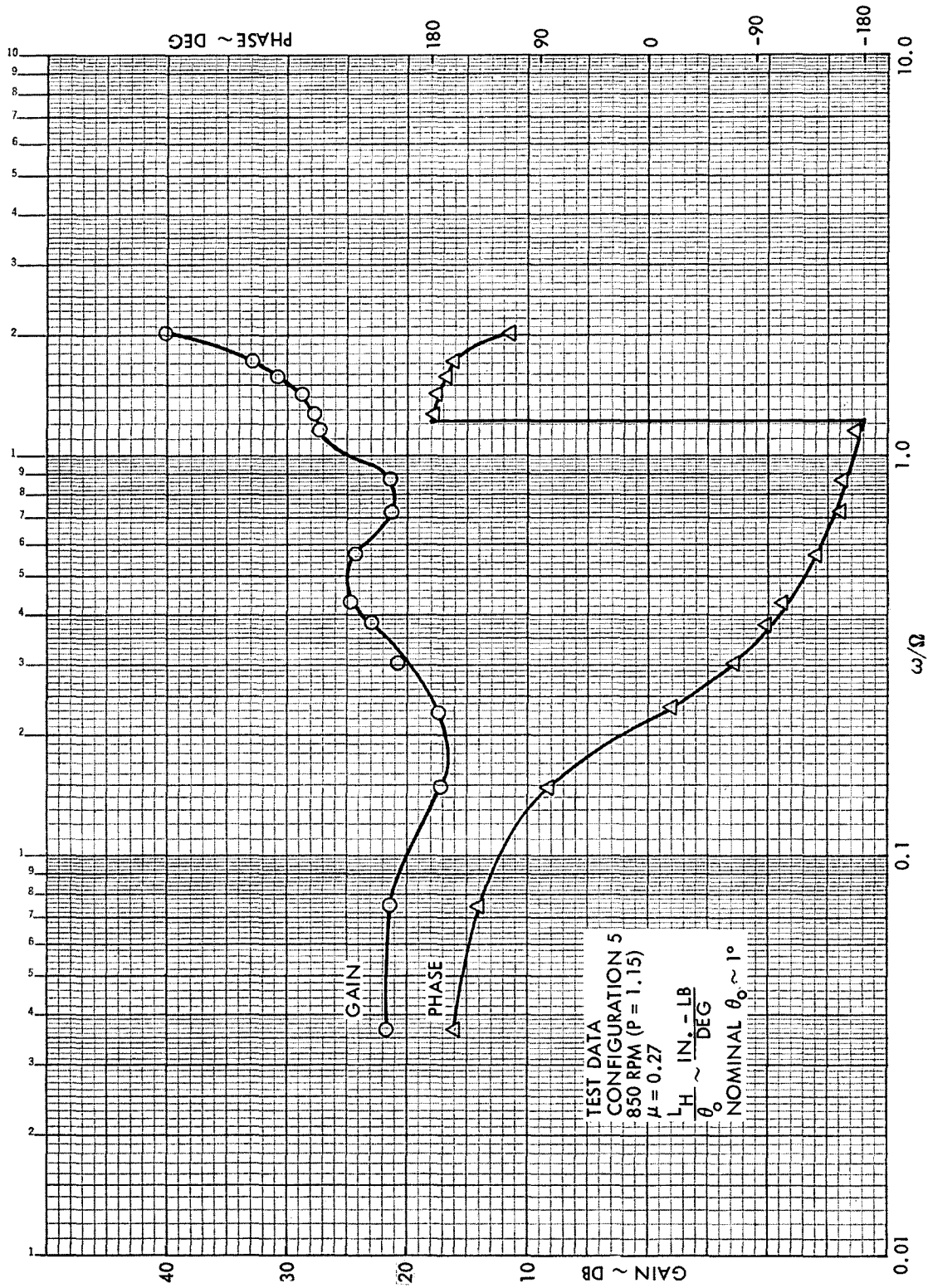


Figure 26. Rotor Hub Roll Moment Frequency Response to  $\theta_0$ ,  $\mu = 0.27$ , Configuration 5, 850 RPM ( $P = 1.15$ )



functions have also been adjusted to the center of rotation and converted to a coefficient form. These results (including phase lag) are tabulated as a function of excitation frequency, rotor speed, and advance ratio.

#### Open Loop Frequency Response Tests (Rotor Shaft Excitations)

Experimental rotor frequency response with respect to shaft pitch ( $\alpha$ ) and roll ( $\phi$ ) excitations had not been acquired during previous phases of the High Advance Ratio Research Program. Therefore, both configuration 1 (soft flexure, no tip weight) and configuration 5 ('supersoft' flexure, no tip weight) were tested. The test conditions ( $\Omega, \mu$ ) for configuration 1 are compatible with those considered during the Phase 2 program. All configuration 5 test conditions (i.e., with  $\theta_o, \theta_s, \theta_c, \alpha$  and  $\phi$  excitations) are identical.

The test technique for the  $\alpha$  and  $\phi$  frequency response experiments was the same as for the swashplate excitations. That is, the hydraulic actuators which restrained the model in pitch and roll were driven (one at a time) with a sine wave function generator at discrete frequencies ranging from 0.5 Hz to 14 Hz. The magnitude of the input was adjusted according to the rotor response. Flexure bending moment endurance limits were respected at all times. The maximum allowable angular travel in both pitch and roll, as dictated by mechanical interference, was  $\pm 5^\circ$ .

The experimental rotor frequency response data with respect to  $\alpha$  are not of a quality comparable to the results for swashplate excitations. The primary reason for this is the large moment of inertia of the body about the pitch pivot. When the model was oscillated at high frequencies the resulting large inertia forces generated bending of the support structure. Since the pitch angular position was deduced from the actuator ram position, elastic deformations were not accounted for in the measurement.

In general the frequency response data with respect to  $\phi$  are more reliable than those with respect to  $\alpha$ . The model moment of inertia about the roll axis was considerably less than the inertia about the pitch axis. Also, the pitch damper was installed during the roll tests which helped to minimize unprogrammed pitch vibrations. All of the data that are suspected of being



contaminated by elastic deformations and/or support vibrations are noted as such in the presentation of the test results.

Before the experimental rotor transfer functions are discussed, it is important to recognize the content of the excitations which the rotor experiences when the shaft is oscillated. As discussed in Section 3, the pivots about which the model pitched and rolled were located below the plane of the rotor. Therefore, in addition to the angular excitations of the rotor generated by shaft variations, i.e.,

$$\begin{aligned}
 \alpha &= \alpha_0 \sin \omega t & \phi &= \phi_0 \sin \omega t \\
 \dot{\alpha} &= \alpha_0 \omega \cos \omega t & \dot{\phi} &= \phi_0 \omega \cos \omega t \\
 \ddot{\alpha} &= -\alpha_0 \omega^2 \sin \omega t & \ddot{\phi} &= -\phi_0 \omega^2 \sin \omega t
 \end{aligned}
 \tag{13}$$

there are also linear velocity ( $\dot{\eta}$ ) and acceleration ( $\ddot{\eta}$ ) excitations, e.g.,

$$\begin{aligned}
 \dot{\eta} &= l\dot{\alpha} \\
 \ddot{\eta} &= l\ddot{\alpha}
 \end{aligned}
 \tag{14}$$

$l$  is the distance from the pitch pivot to the rotor hub. In the curves which will be presented, the transfer functions are labeled as being with respect to  $\alpha$  and  $\phi$  where it is understood that the total excitation is not merely the angular displacement but the composite of the linear and angular displacements, rates and accelerations.

Several curves which illustrate the nature of the experimental rotor frequency response with respect to shaft pitch and roll are discussed below. The reader is referred to Appendix C for graphical and tabular presentations of all the test data (including those presented in the main body of this report).

The experiments conducted at  $\mu = 0$  provide a good basis for evaluating the effect of support stand vibrations on the rotor data. Because the response of the rotor to the displacement,  $\alpha$ , is zero when  $\mu = 0$ , the transfer functions with respect to  $\alpha$  and  $\phi$  oscillations should be symmetrical. Rotor hub moment frequency response data at  $\mu = 0$  with  $\alpha$  and  $\phi$  excitations are shown in Figures 27 to 30. In the first two plots the pitch and roll response to  $\alpha$  are presented. In the next two figures the same responses to a  $\phi$  excitation are shown. The conditions for the two tests are identical (configuration 5, rotor speed = 850 rpm and  $\theta_0 = 4^\circ$ ). Comparisons of  $M_H/\alpha$  with  $L_H/\phi$  and  $L_H/\alpha$

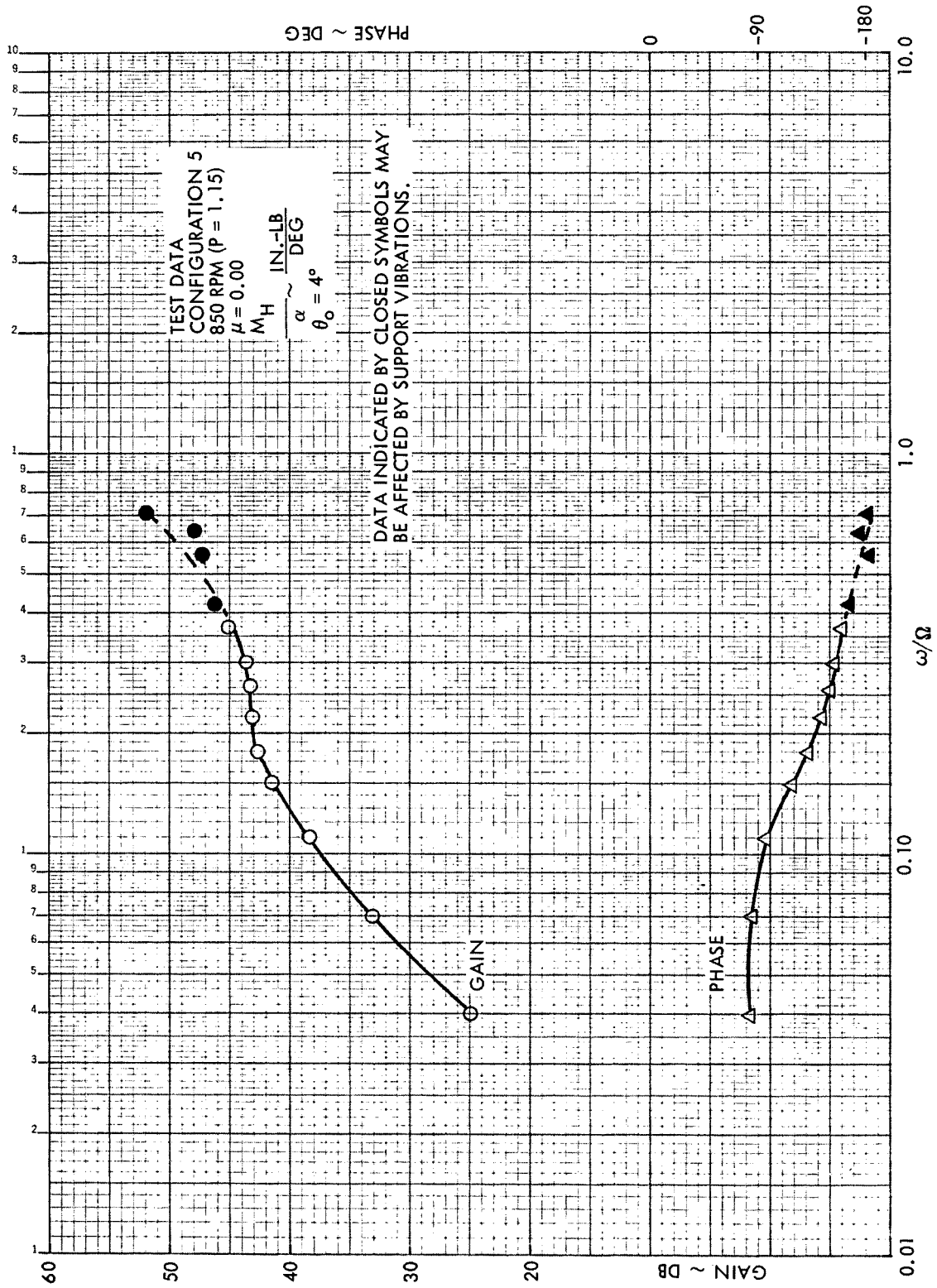


Figure 27. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0$ , 850 RPM (P = 1.15)

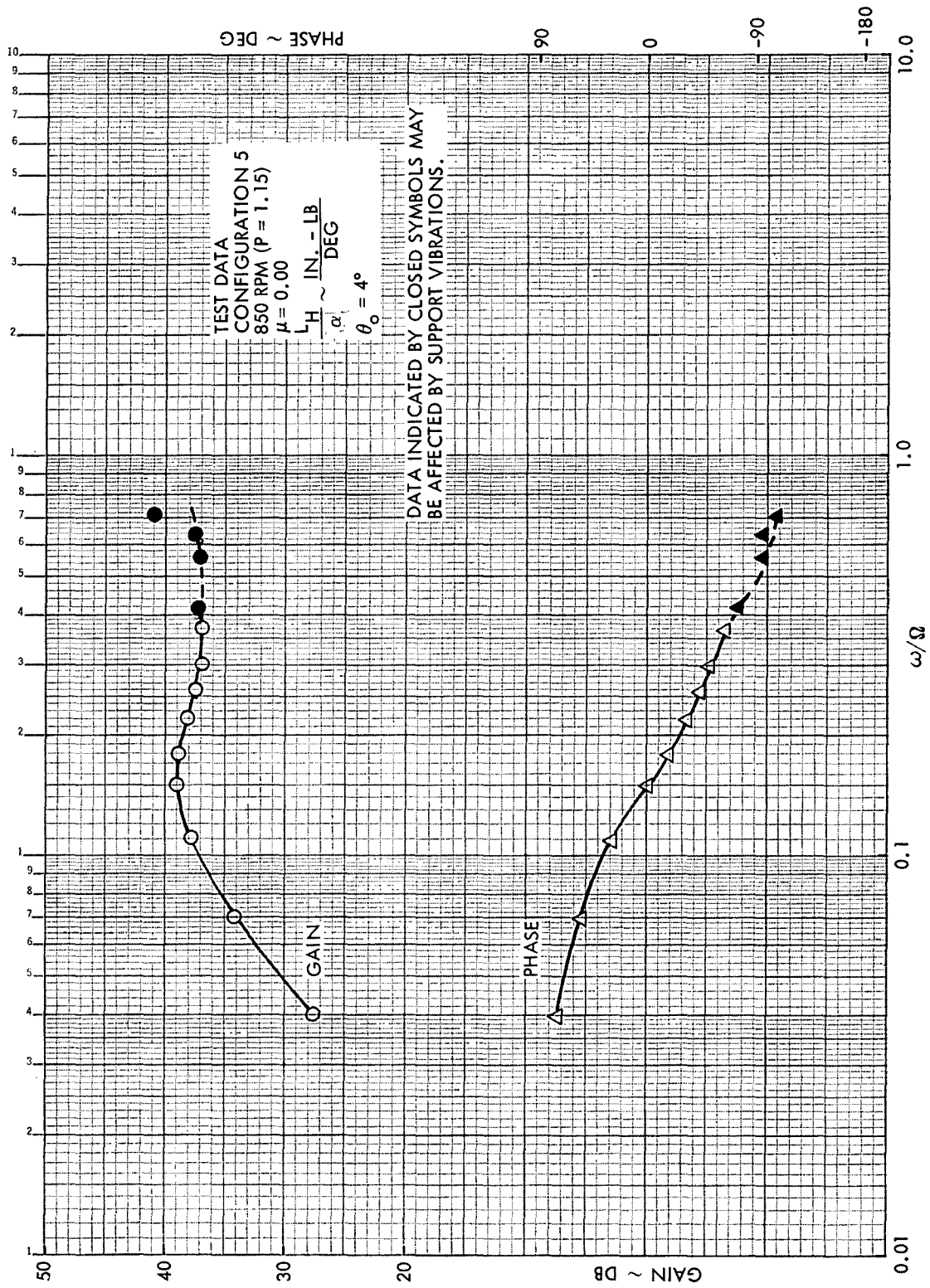


Figure 28. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0$ , 850 RPM (P = 1.15)

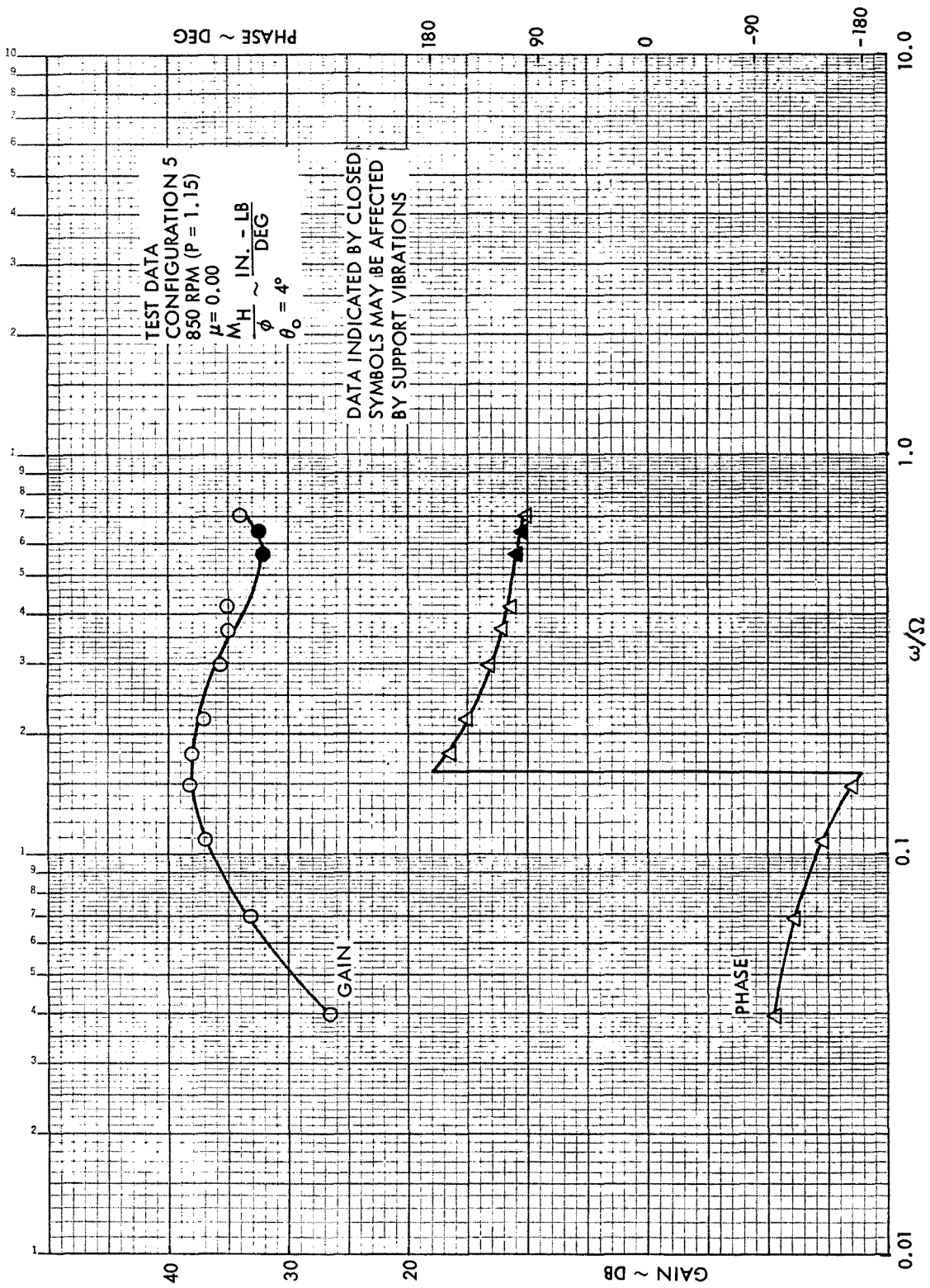


Figure 29. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0$ , 850 RPM (P = 1.15)

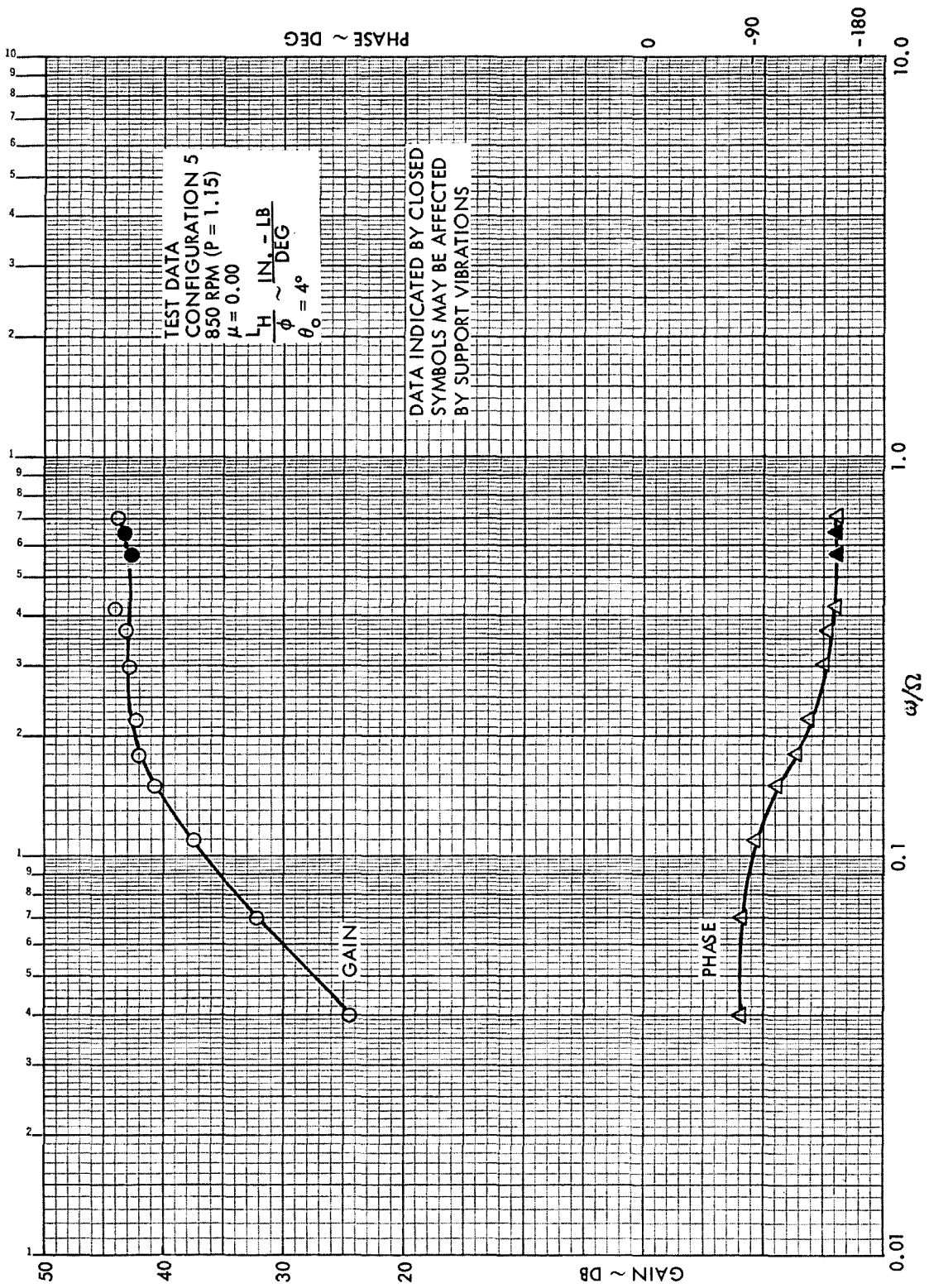


Figure 30. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0$ , 850 RPM ( $P = 1.15$ )

with  $M_H/\phi$  reveal that the responses are approximately symmetric up to an excitation frequency of  $\omega \sim 0.3 \Omega$ . The gain values generally agree to within 1 dB and phase discrepancies are almost undetectable. As the frequency ratio increases, however, the disagreement also increases until at  $\omega/\Omega = 0.7$  the responses are divergent by 7 to 8 dB in gain and  $30^\circ$  in phase. As has been discussed previously, the roll frequency response data are considered more reliable than the pitch results.

The characteristics of the experimental data at  $\mu = 0$  are quite informative. Consider, for example, the hub moment roll response to a shaft roll oscillation,  $L_H/\phi$  (Figure 30). When the excitation frequency is small the response is low. This is due to the fact that the roll rate ( $\dot{\phi}$ ) and roll acceleration ( $\ddot{\phi}$ ) are small. The rotor, of course, does not respond to roll position at any advance ratio. The  $90^\circ$  phase lag at the low frequencies indicates the primary rotor excitation is due to  $\dot{\phi}$ . Since the response and excitation are in phase, the excitation is of aerodynamic origin. As the excitation frequency increases the magnitude of both  $\dot{\phi}$  and  $\ddot{\phi}$  increase for a constant  $\phi$ , thus generating the higher rotor response.

The hub pitch moment response to  $\phi$  at  $\mu = 0$  is shown in Figure 29. Again, at low excitation frequencies the phase lag is  $90^\circ$ . In this case the primary disturbance is the gyroscopic excitation due to  $\dot{\phi}$ . The peaking of the pitch response at  $\omega/\Omega \sim 0.15$  is caused by the resonant response of the rotor at its natural flapping frequency.

Experimental rotor frequency response with respect to shaft roll oscillations in forward flight are shown in Figures 31 through 34. Hub pitch and roll moment data at two advance ratios ( $\mu = 0.27$  and  $\mu = 0.51$ ) are presented for configuration 5 at a rotor speed of 850 rpm. The rotor response is not affected by roll position ( $\phi$ ) and the inertia excitations due to  $\dot{\phi}$  and  $\ddot{\phi}$  are independent of  $\mu$  at a constant excitation frequency. Therefore, the differences between the transfer functions at the two advance ratios must be due to a change in aerodynamic excitation; the primary excitation (ignoring unsteady effects) is caused by the steady roll rate,  $\dot{\phi}$ . From the data shown it can be seen that increased forward speed generates a slight reduction in the hub

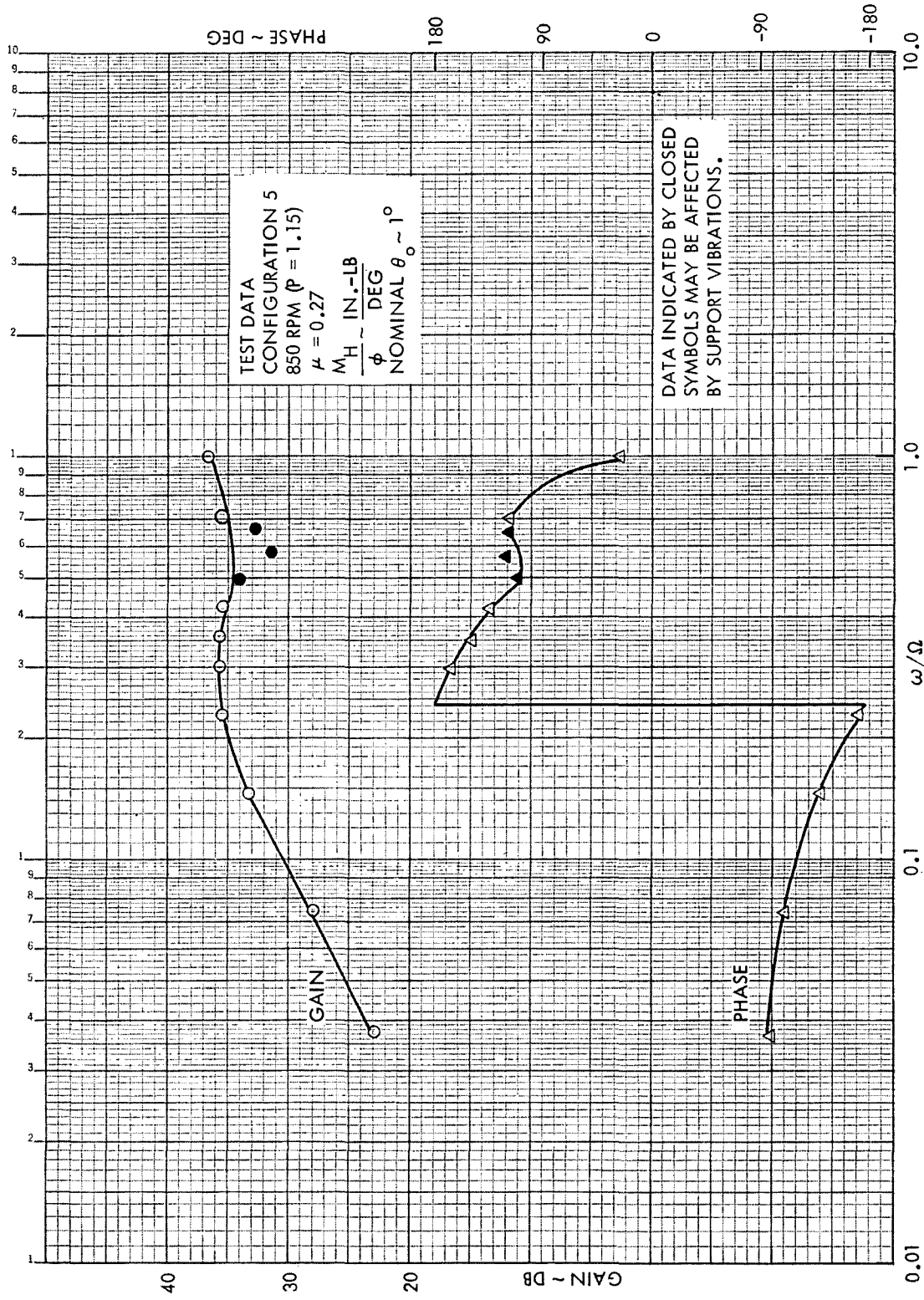


Figure 31. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)



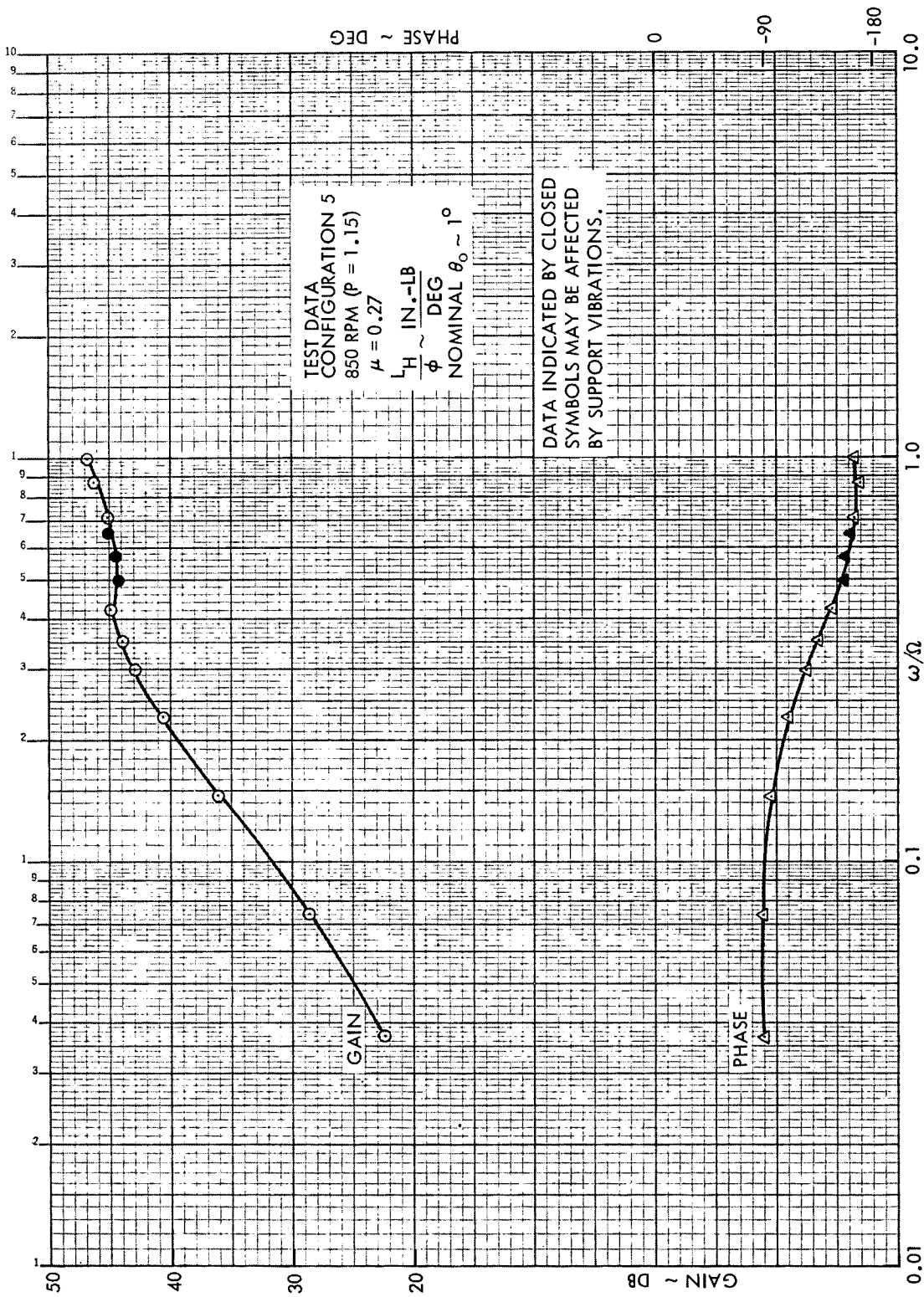


Figure 32. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )



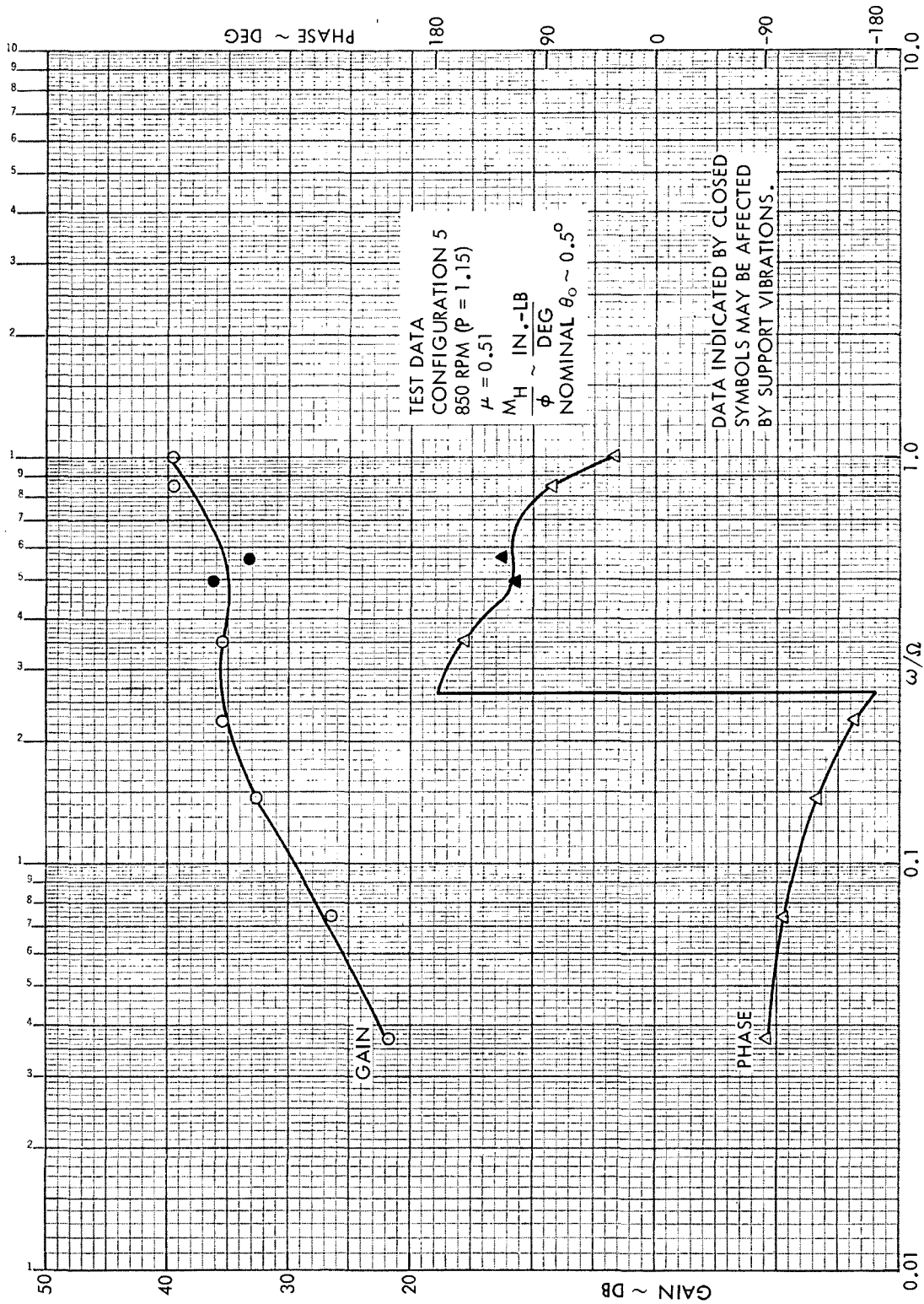


Figure 33. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )

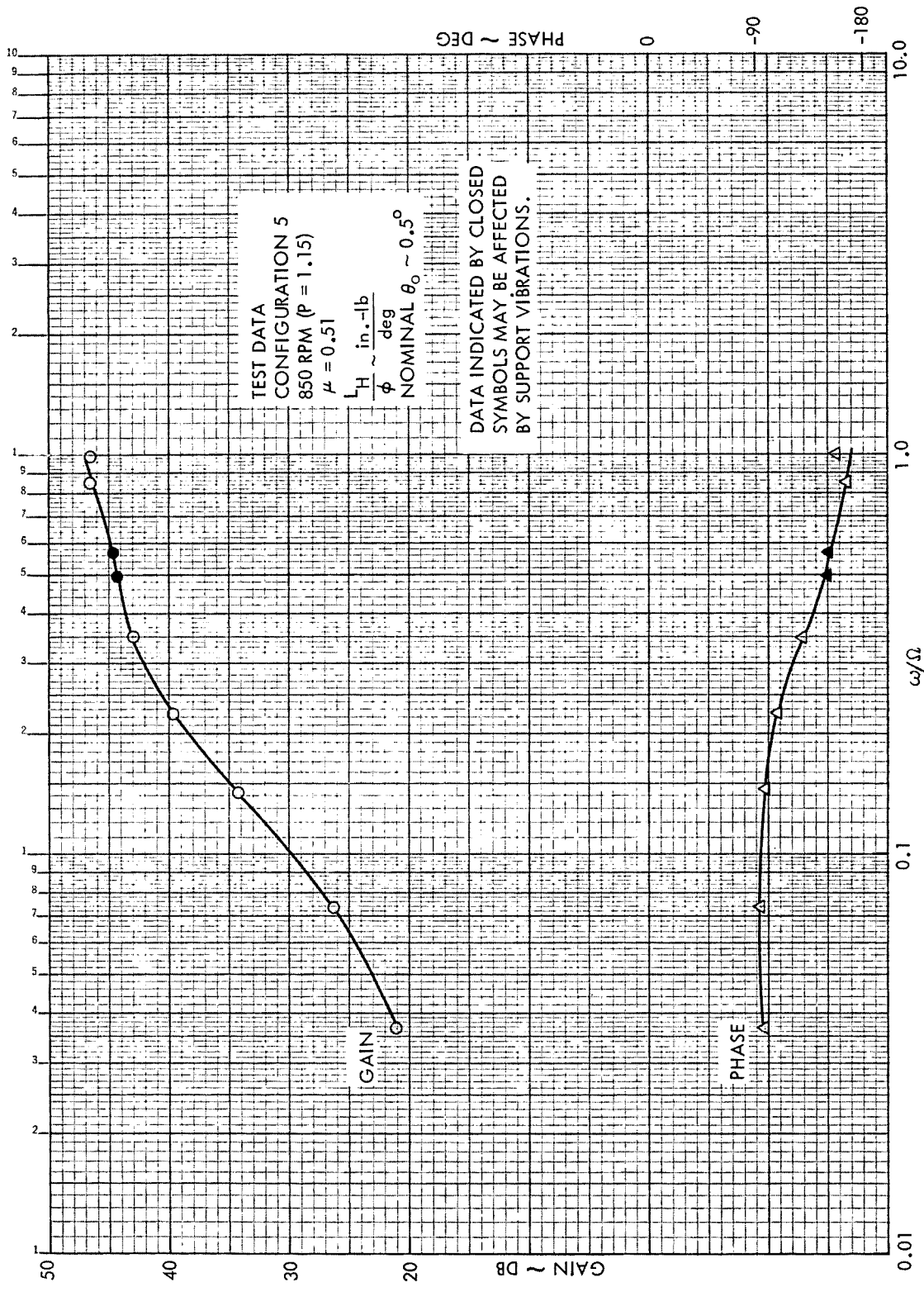


Figure 34. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)

moment response up to an excitation frequency of  $\omega \sim 0.5 \Omega$ . At higher frequencies the transfer functions are the same. The phase lag of the response is also affected only slightly over the tested excitation frequency range.

Rotor frequency response to  $\alpha$  is plotted in Figures 35 through 38 at the same test conditions (i.e., configuration 5, 850 rpm  $\mu = 0.27$  and  $\mu = 0.51$ ). By comparing similar response data at the two advance ratios, the aerodynamic effect of forward speed is seen. Based upon the roll frequency response results it is probable that most of the increased response at the higher advance ratio is due to  $\alpha$  rather than  $\dot{\alpha}$ . It is noted, however, that the aerodynamic excitation of blade flapping by  $\dot{\alpha}$  and  $\dot{\phi}$  are not identical.

#### Closed Loop Frequency Response Tests (Rotor Shaft Excitations)

A major portion of the Phase 2 study was spent in determining the dynamic characteristics of hingeless rotors equipped with hub moment feedback controls. The model control system is electronic and consists of two decoupled first order lag filters which have variable gains and time constants. The resolved rotor hub pitching and rolling moments constitute the feedback signals to the control filters. The control system outputs, in turn, drive the longitudinal and lateral cyclic pitch actuators. For a complete description of the closed loop system, the reader is referred to Section 3 of Reference 2.

In order to further evaluate the first order lag feedback control system, several closed loop tests were conducted during the Phase 3 program. The object of the experiments was to determine the effectiveness of the electronic control device in alleviating the rotor response to the external disturbances generated by shaft motion. One rotor and control system configuration was considered, i.e.,

Rotor Configuration 1 ( $\gamma = 5.0$ )

800 rpm ( $P = 1.33$ )

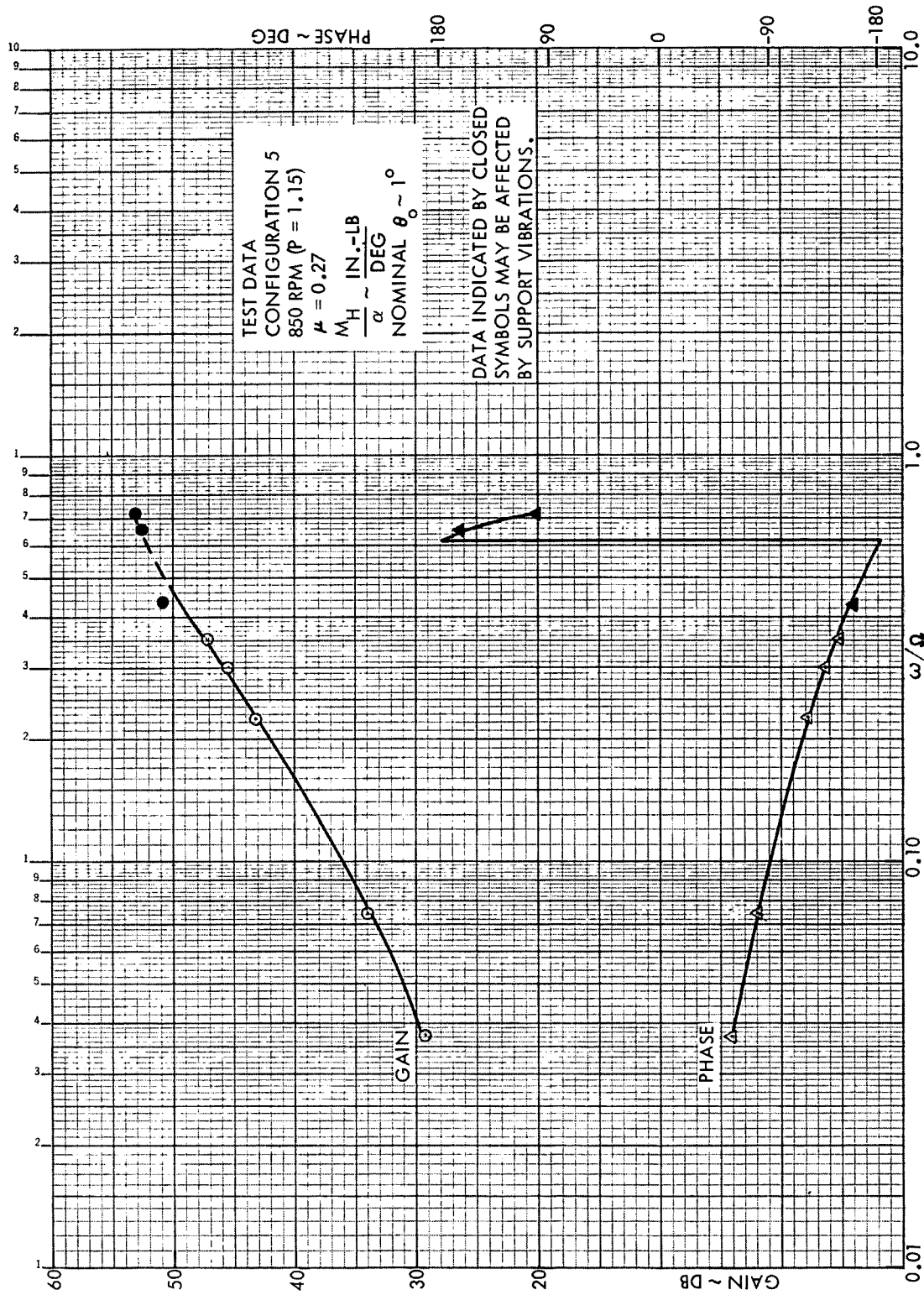


Figure 35. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )

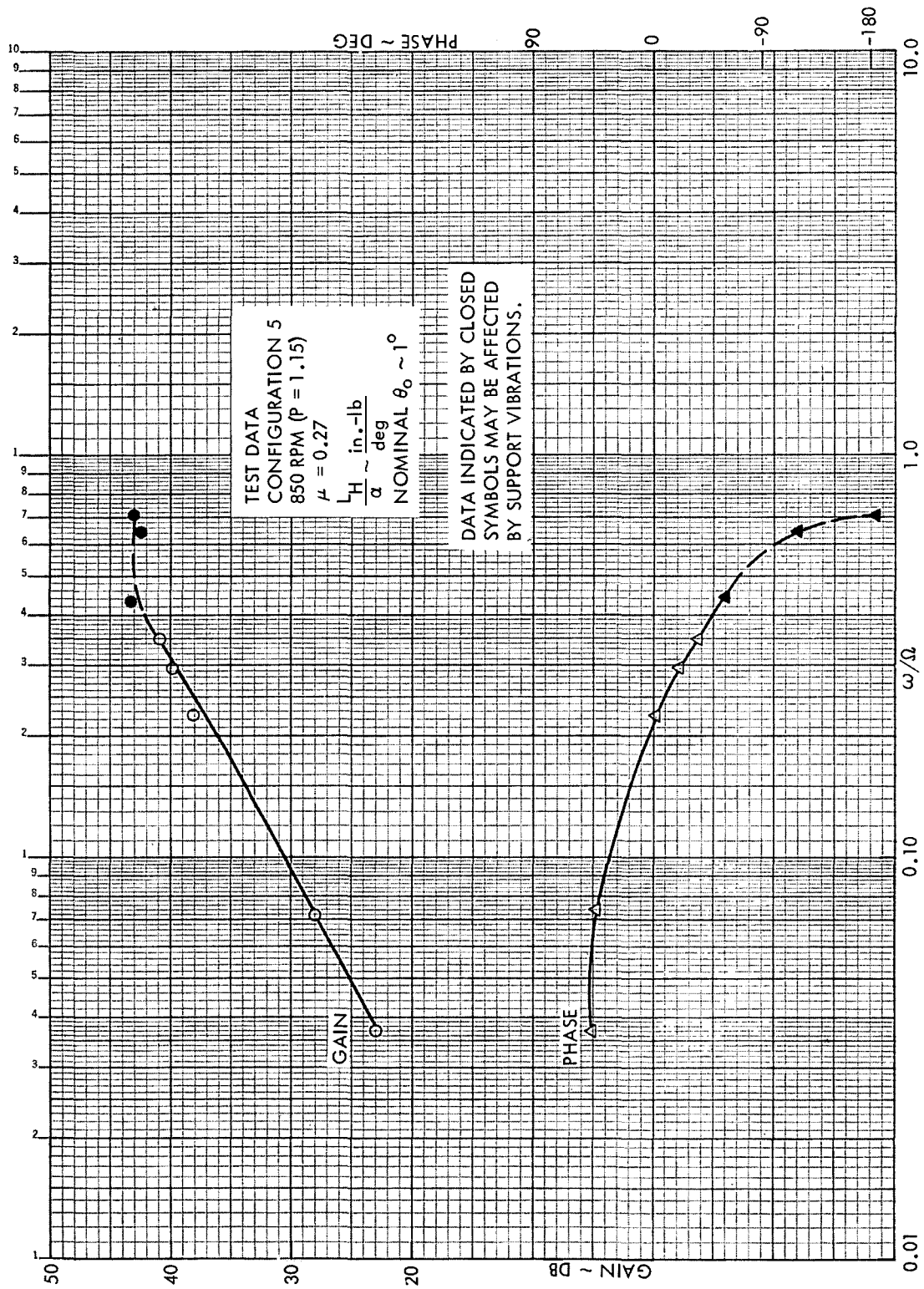


Figure 36. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )

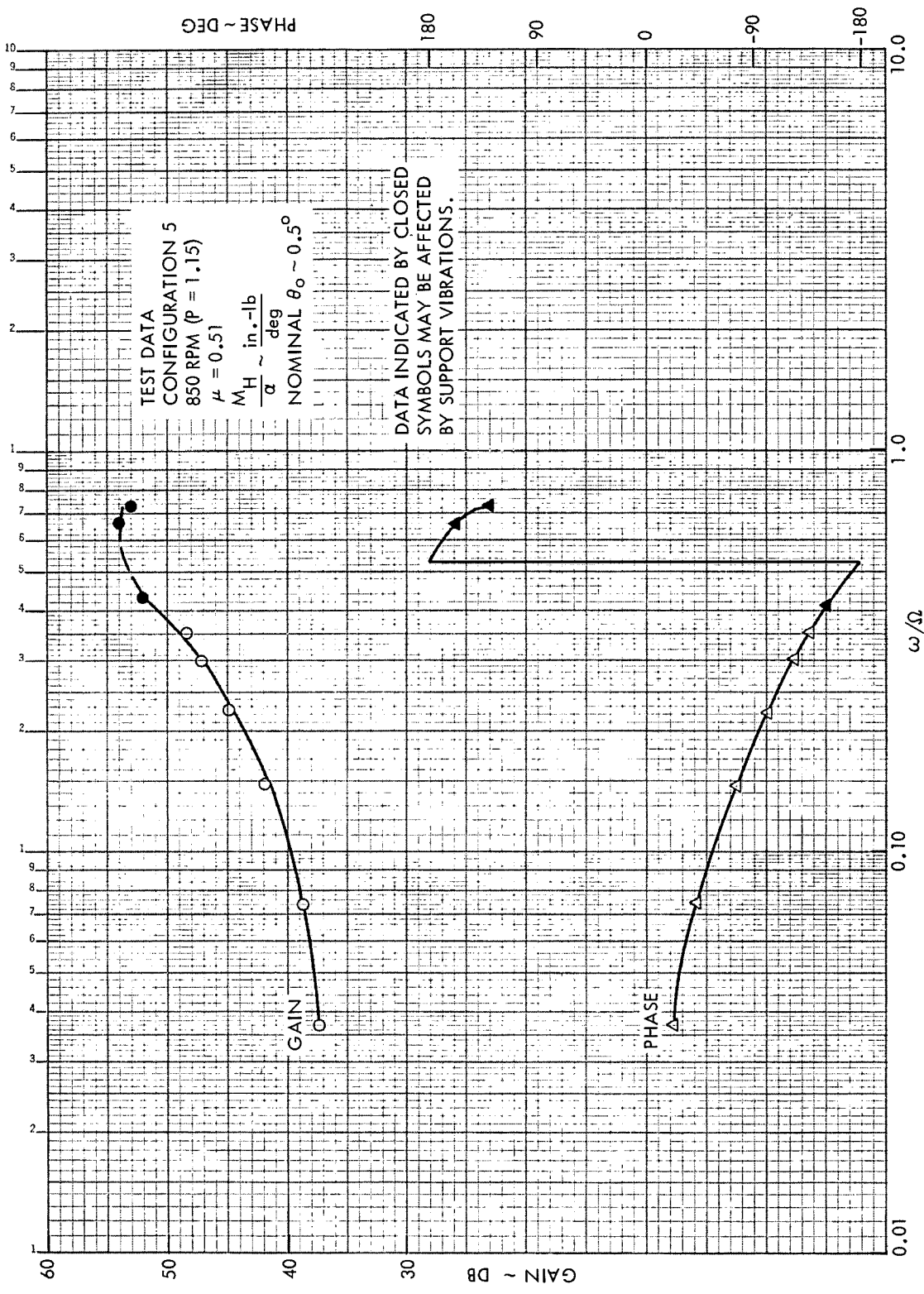


Figure 37. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )

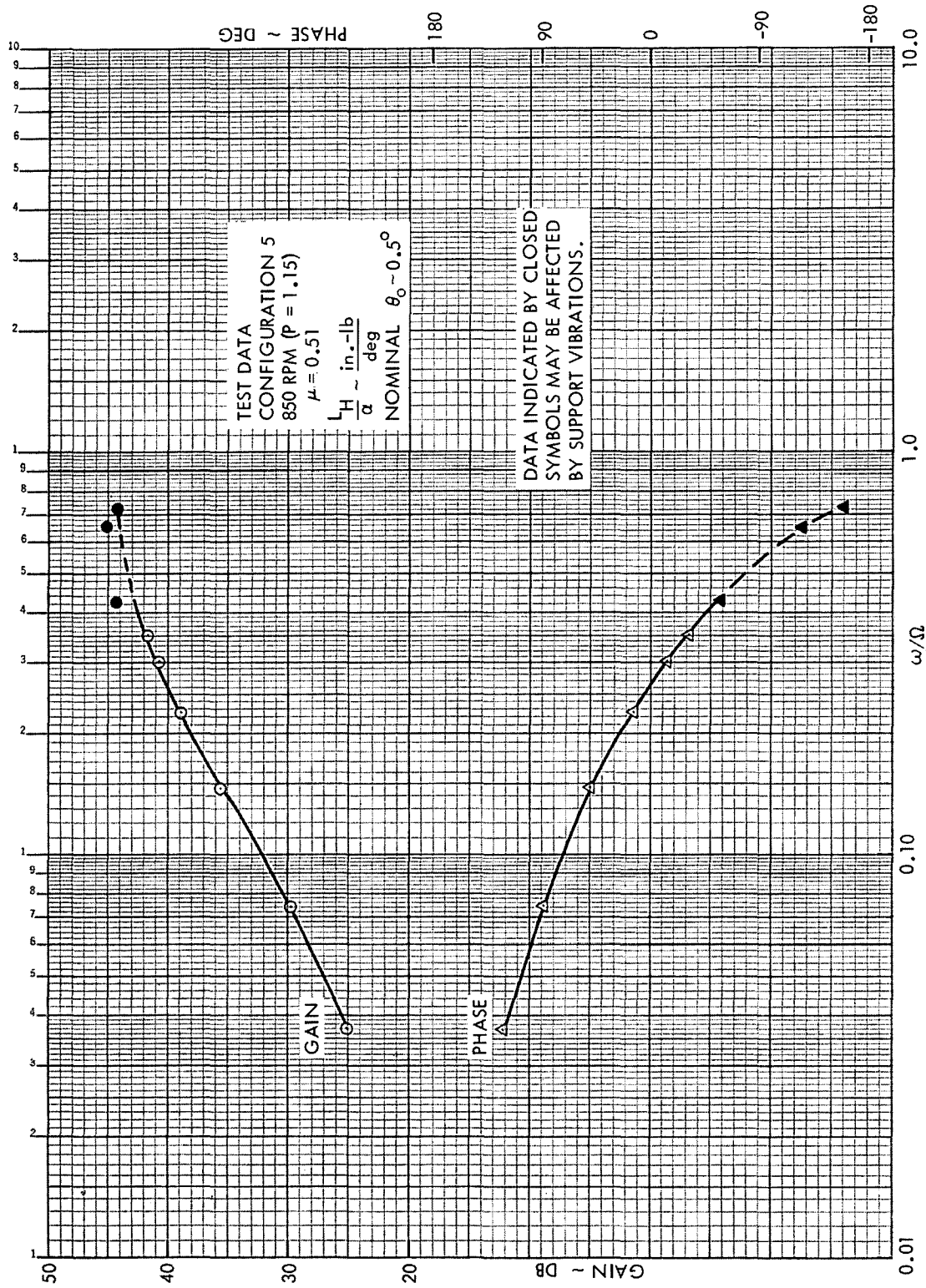


Figure 38. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )



## Control System Parameters

$$A = 0.5$$

$$L = 0$$

$$\Delta = 0 \text{ deg}$$

$$\Gamma = 0 \text{ deg}$$

The closed loop rotor hub moment frequency response to shaft roll at  $\mu = 0$  is presented in Figures 39 and 40. A comparison of these data with similar open loop results (i.e., Figures C33 and C34) indicates the feedback control system is mildly effective in alleviating the external disturbance at low excitation frequencies and ineffective or even deteriorating at higher frequencies. These characteristics are consistent with similar Phase 2 test results where a collective pitch excitation comprised the external disturbance of the closed loop system.

Closed loop frequency response test results at  $\mu = 0.28$  are shown in Figures 41 and 42. For these data the excitation was shaft pitch. Generally the rotor characteristics are the same as those obtained at  $\mu = 0$ . The effectiveness of the control system at low frequencies is somewhat greater, however. (Comparable open loop data are plotted in Figures C25 and C26.) This is simply due to the fact that the rotor open loop response to  $\alpha$  at  $\mu = 0.28$  is greater than the response to  $\phi$  at  $\mu = 0$  and thus there is more moment response to relieve. The peaking of the closed loop response at  $\omega/\Omega \sim 0.23$  is the result of a natural mode associated with the feedback control system.



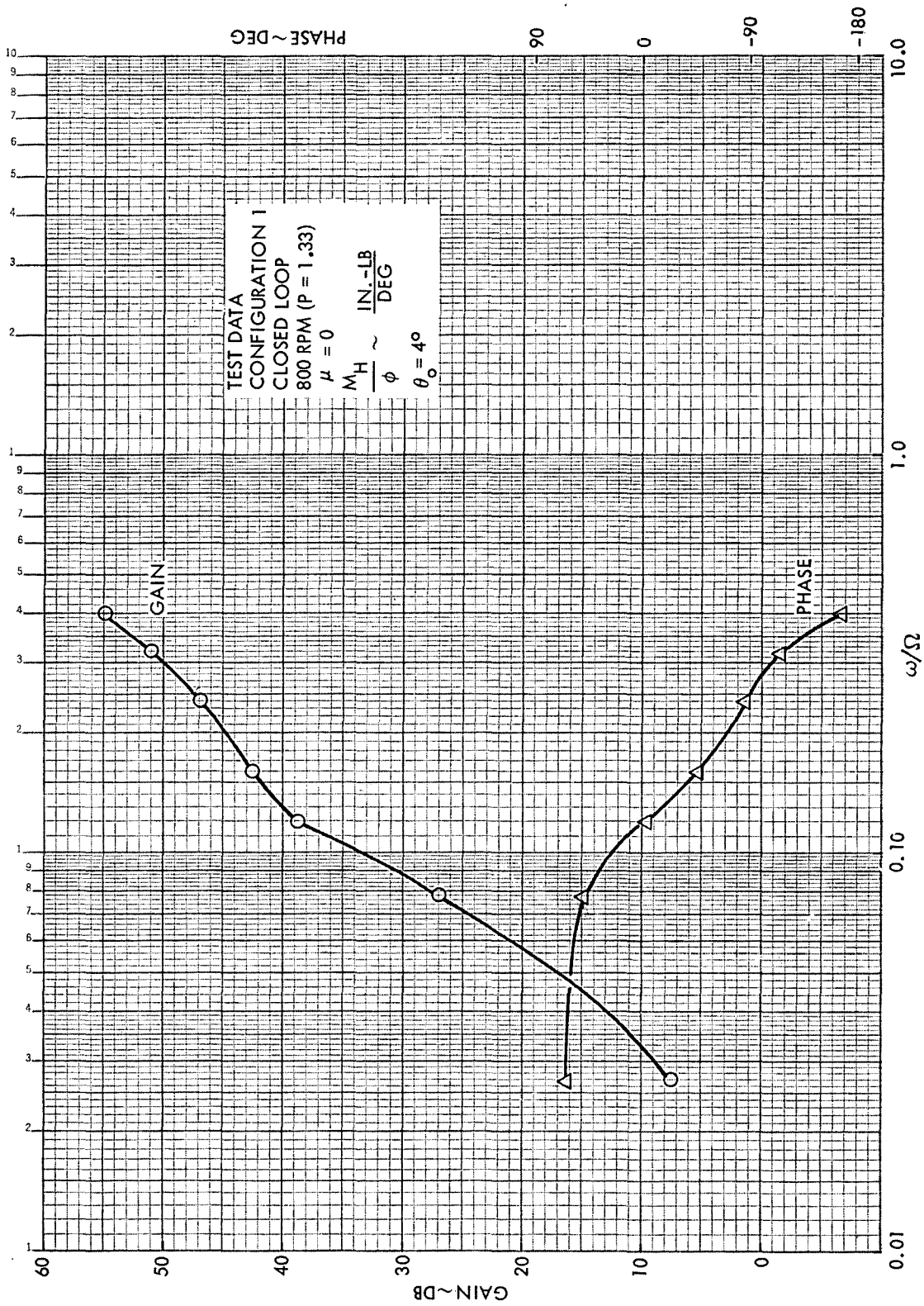


Figure 39. Closed Loop Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0$ , 800 RPM (P = 1.33); (A = 0.5, L = 0,  $\Delta = \Gamma = 0^\circ$ )

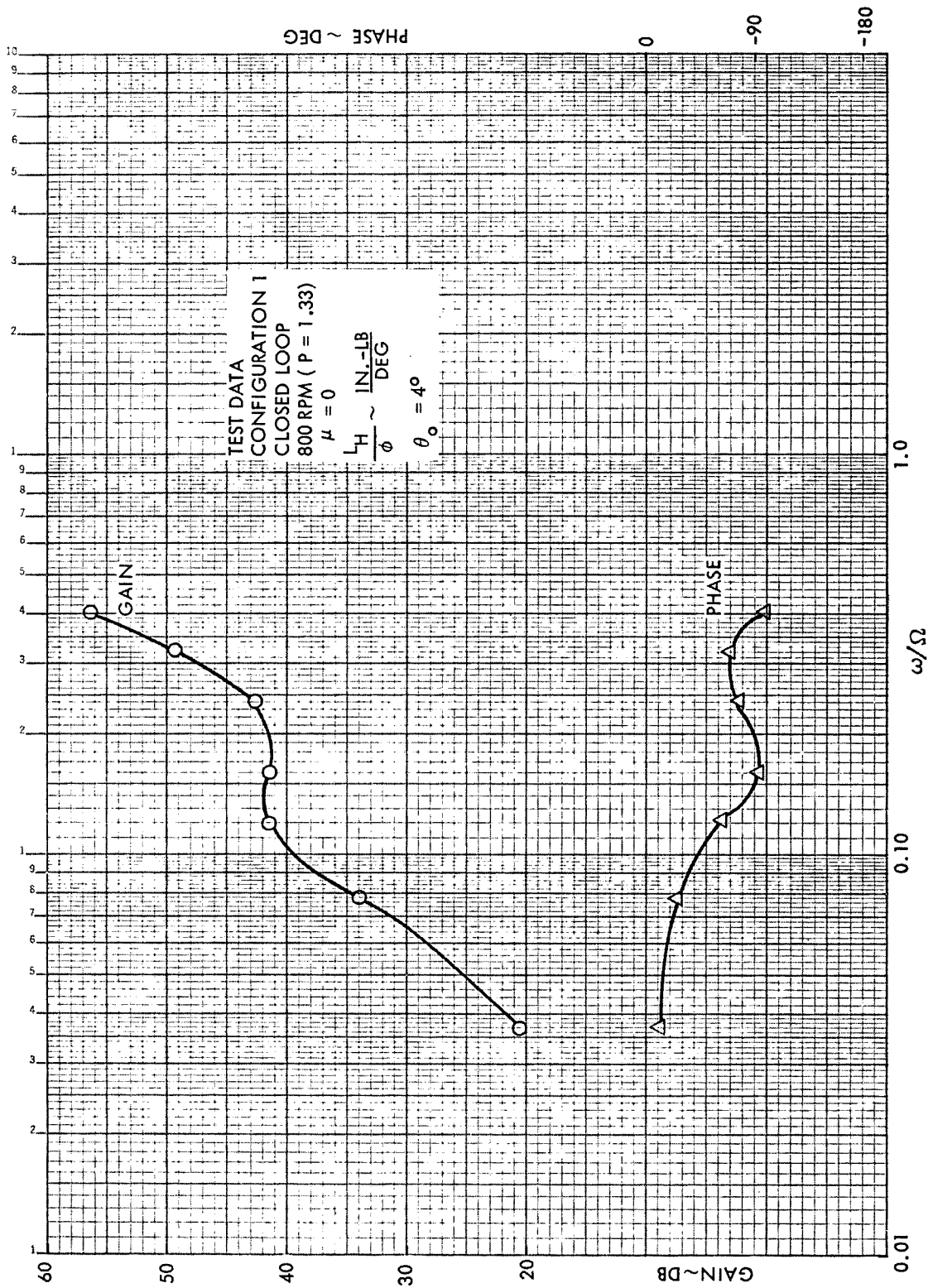


Figure 40. Closed Loop Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0$ , 800 RPM (P = 1.33), (A = 0.5, I = 0,  $\Delta = \Gamma = 0^\circ$ )

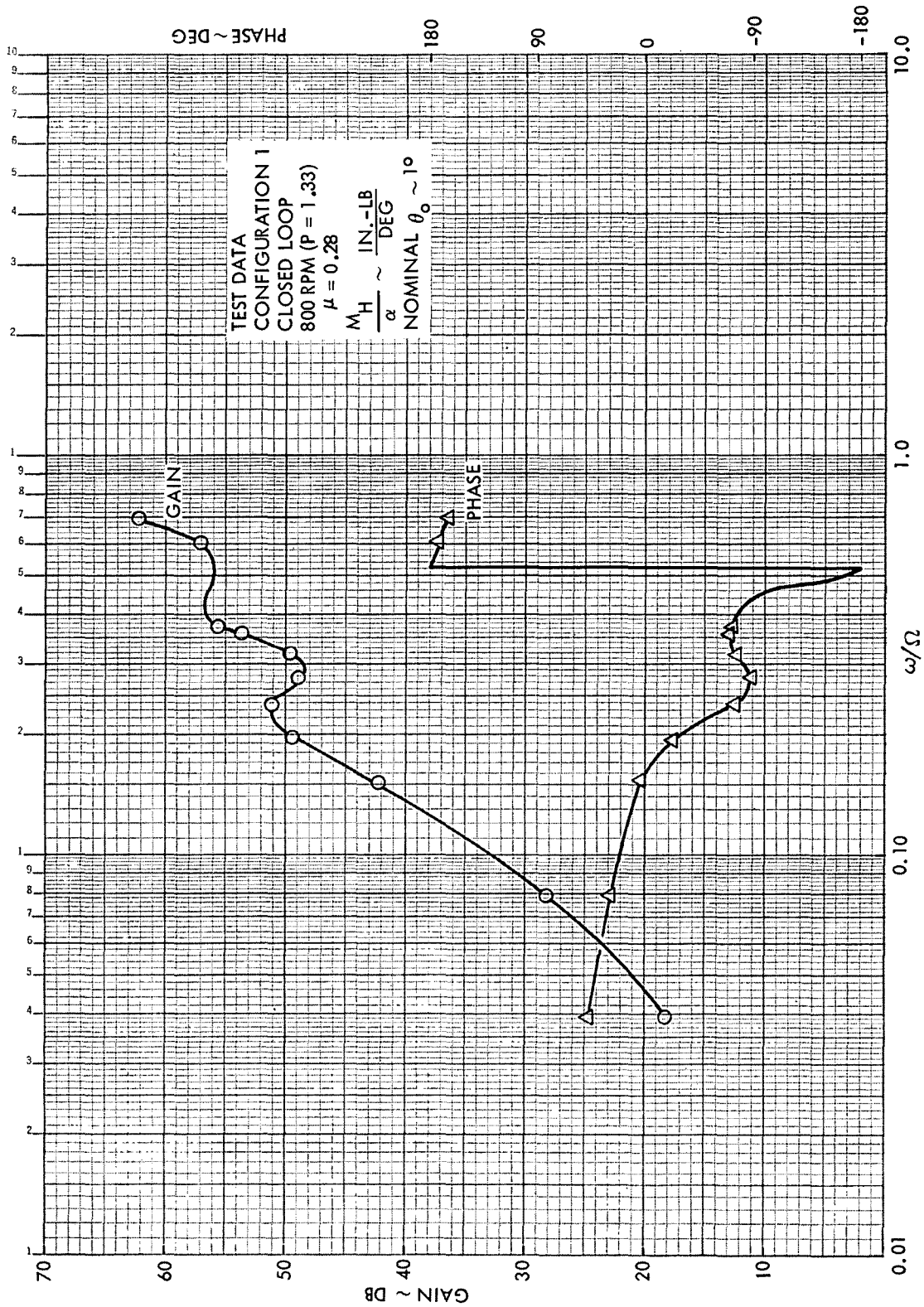


Figure 41. Closed Loop Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.28$ , 800 RPM (P = 1.33), (A = 0.5, L = 0,  $\Delta = \Gamma = 0^\circ$ )

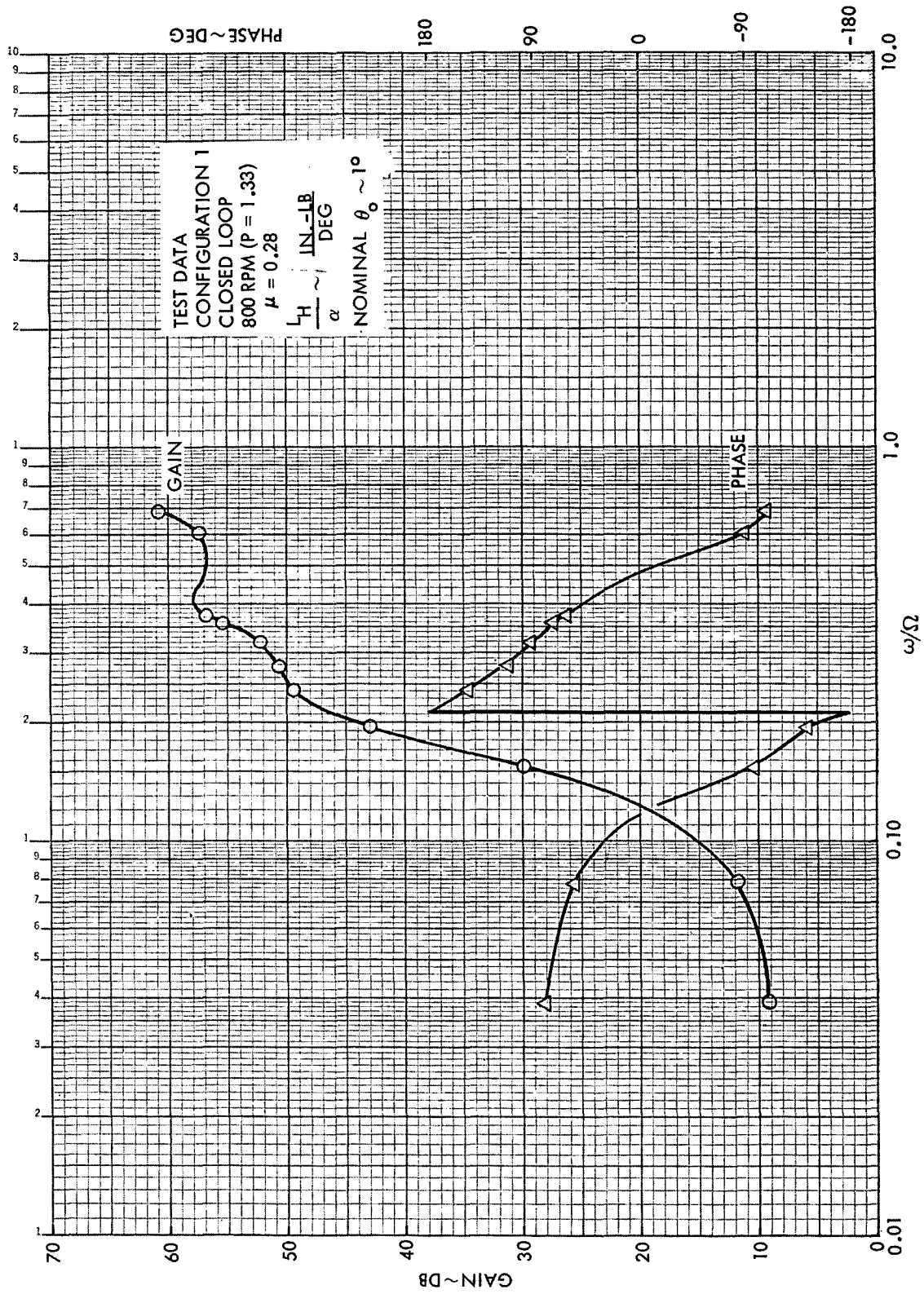


Figure 42. Closed Loop Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.28$ , 800 RPM (P = 1.33) (A = 0.5, L = 0,  $\Delta = \Gamma = 0^\circ$ )

## SECTION 6

## COMPARISON OF THEORETICAL AND EXPERIMENTAL DATA

An important part of the Lockheed/AMRDL High Advance Ratio Research Program has been the evaluation of a simple rotor theory by comparing analytical and experimental data. The correlation effort, previous results of which are reported in References 1 and 2, has been continued during the Phase 3 program. The open loop rotor frequency response to shaft pitch and roll constitute the data which were correlated for the current study.

THEORY

The mathematical rotor model is completely defined in Section 7 of Reference 2. It consists of four untwisted rigid blades which flap individually and inelastically about a centrally arranged flapping hinge. Each blade is restrained by a hypothetical spring which is selected so that the rigid blade flapping frequency is identical to the first flap mode natural frequency of the elastic blade being simulated. Steady state aerodynamic theory is used and the effects of blade stall, Mach number and deviations from a uniform induced velocity field are ignored. Reversed flow is totally accounted for resulting in equations which are valid over the complete advance ratio range,  $\mu = 0 \rightarrow \infty$ .

The flapping equations of motion in Reference 2 do not include shaft pitch and roll forcing functions. The mass moment acting on the  $i^{\text{th}}$  blade of a four-bladed rotor due to steady pitch and roll angular rates and accelerations is

$$\frac{M_Y i}{R^4 \rho a_c^2} = \frac{2}{\gamma} \left\{ \cos \left[ \psi + (i-1) \frac{\pi}{2} \right] (2\Omega \dot{\phi} + \ddot{\alpha}) + \sin \left[ \psi + (i-1) \frac{\pi}{2} \right] (-2\Omega \dot{\alpha} + \ddot{\phi}) \right\} \quad (15)$$

The aerodynamic moment is

$$\frac{M_Y}{R^4 \rho a \frac{c}{2}} \ddot{\beta}_i = \Omega \dot{\phi} m_{\dot{\phi}} \left[ \psi + (i-1) \frac{\pi}{2} \right] + \Omega \dot{\alpha} m_{\dot{\alpha}} \left[ \psi + (i-1) \frac{\pi}{2} \right] \quad (16)$$

where  $i = 1, 2, 3$  or  $4$ ,

$$\left. \begin{aligned} m_{\dot{\alpha}}(\psi) &= \cos(\psi) C(\psi) \\ m_{\dot{\phi}}(\psi) &= \sin(\psi) C(\psi) \end{aligned} \right\} \quad (17)$$

and  $C(\psi)$  is the periodic aerodynamic damping of blade flapping. Combining equations (15) and (16) with the flapping equations of motion (i.e., equation (1) of Reference 2) yields

$$\begin{aligned} & \frac{2}{\gamma} \ddot{\beta}_i + \Omega \dot{\beta}_i C \left[ \psi + (i-1) \frac{\pi}{2} \right] + \Omega^2 \beta_i \left\{ \frac{2}{\gamma} P^2 + K \left[ \psi + (i-1) \frac{\pi}{2} \right] \right\} \\ &= \alpha \Omega^2 m_{\alpha} \left[ \psi + (i-1) \frac{\pi}{2} \right] + \Omega^2 \left\{ \theta_o + \theta_s \sin \left[ \psi + (i-1) \frac{\pi}{2} \right] \right. \\ &+ \left. \theta_c \cos \left[ \psi + (i-1) \frac{\pi}{2} \right] \right\} m_{\theta_o} \left[ \psi + (i-1) \frac{\pi}{2} \right] \\ &+ \frac{2}{\gamma} \left\{ \cos \left[ \psi + (i-1) \frac{\pi}{2} \right] (2\Omega \dot{\phi} + \ddot{\alpha}) + \sin \left[ \psi + (i-1) \frac{\pi}{2} \right] (-2\Omega \dot{\alpha} + \ddot{\phi}) \right\} \\ &+ \Omega \dot{\phi} m_{\dot{\phi}} \left[ \psi + (i-1) \frac{\pi}{2} \right] + \Omega \dot{\alpha} m_{\dot{\alpha}} \left[ \psi + (i-1) \frac{\pi}{2} \right] \end{aligned} \quad (18)$$

Equation (18) was solved using the techniques described in Section 7 of Reference 2 to obtain rotor transfer functions with respect to rotor shaft pitch and roll oscillations.

#### CORRELATION RESULTS

Only experimental data for configuration 1 have been compared with theoretical data. Typical correlation results are shown in Figures 43 through 48. The measured test derivatives have been nondimensionalized by the rotor stiffness,  $K_{\theta}$ , in order to obtain data which are compatible with the theoretical

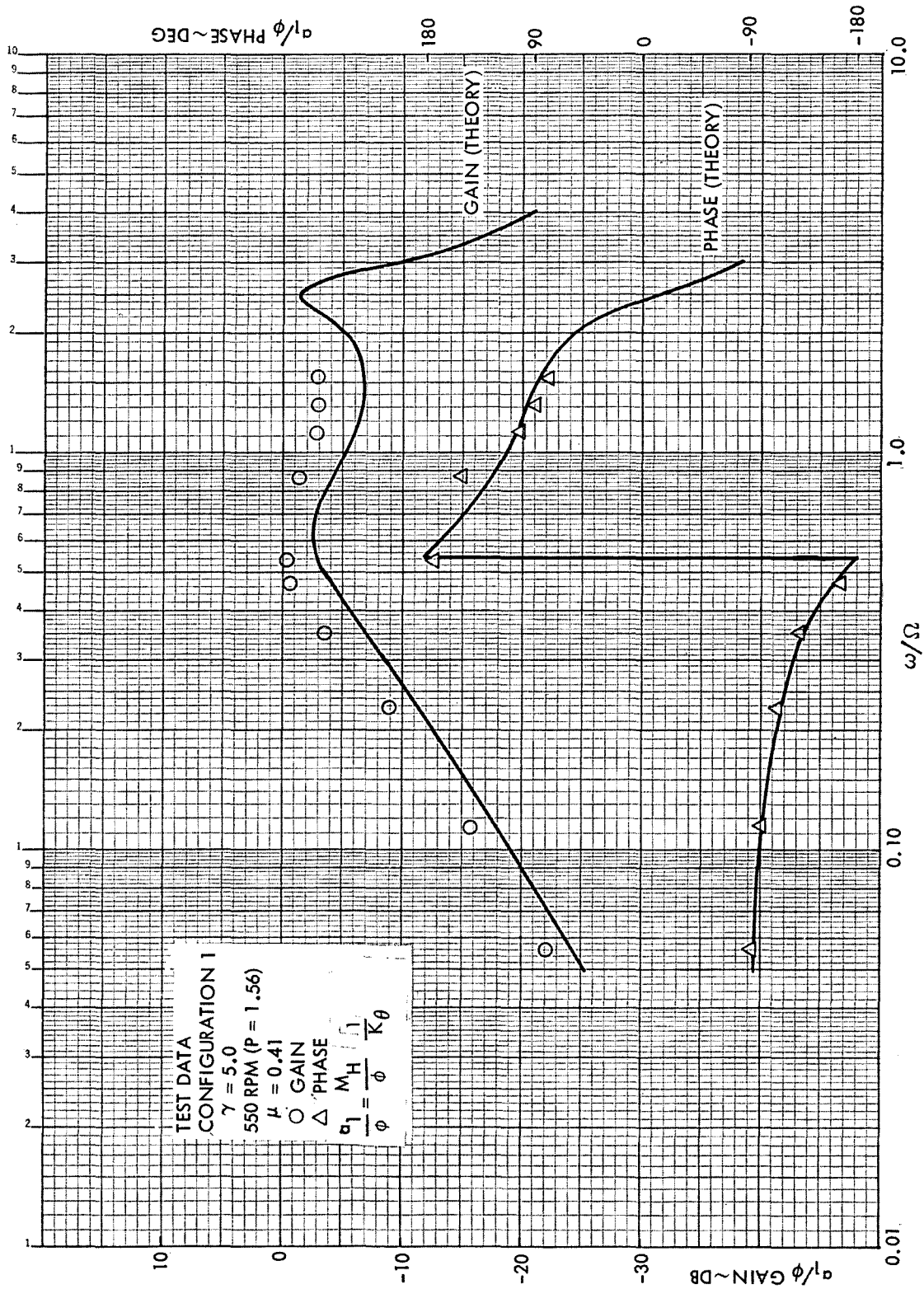


Figure 43. Comparison of Experimental and Theoretical Data, Rotor Longitudinal Frequency Response to  $\phi$ , Configuration 1,  $\mu = 0.41$ , 550 RPM ( $P = 1.56$ )



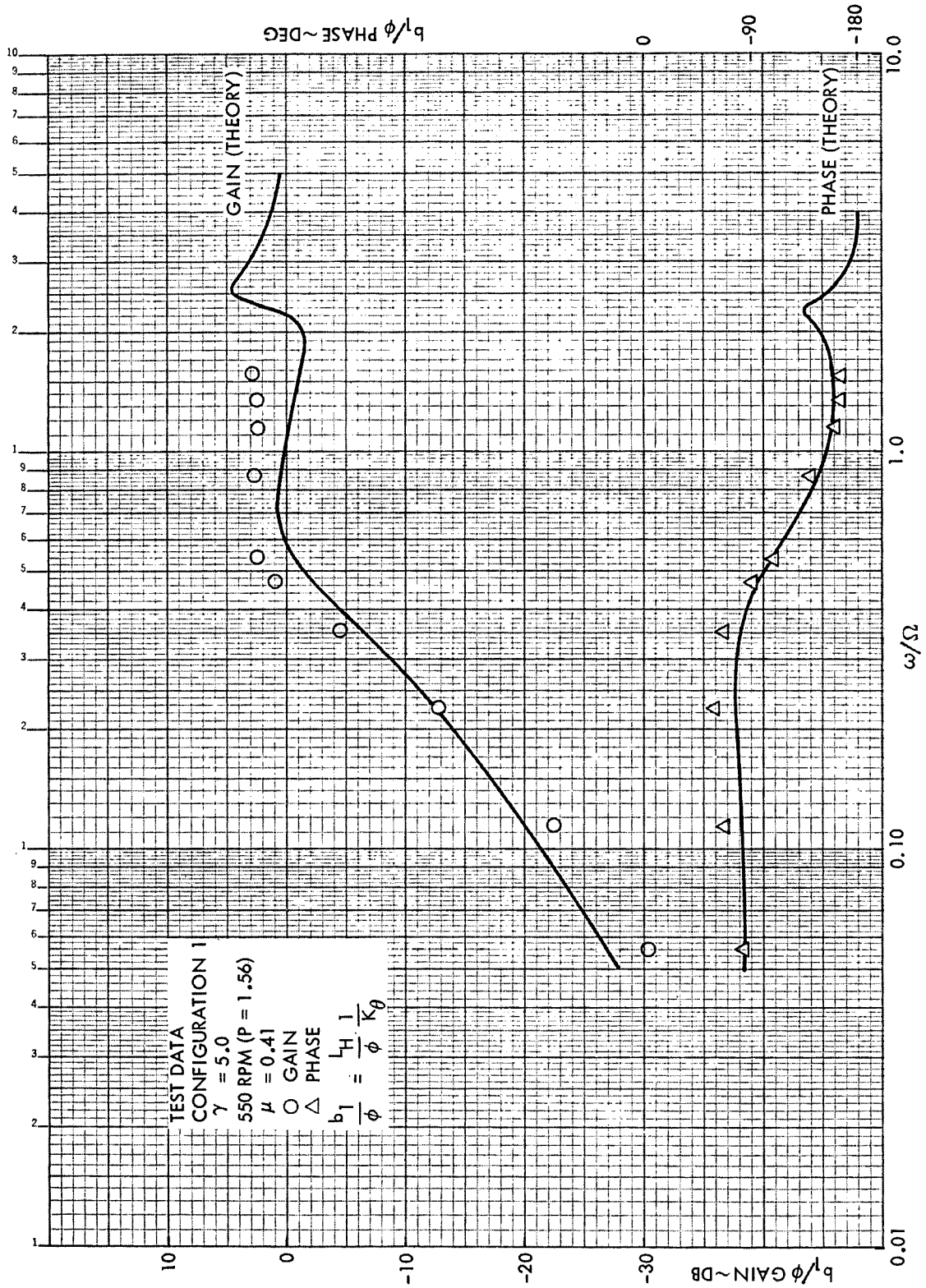


Figure 44. Comparison of Experimental and Theoretical Data, Rotor Lateral Frequency Response to  $\phi$ , Configuration 1,  $\mu = 0.41$ , 550 RPM ( $P = 1.56$ )



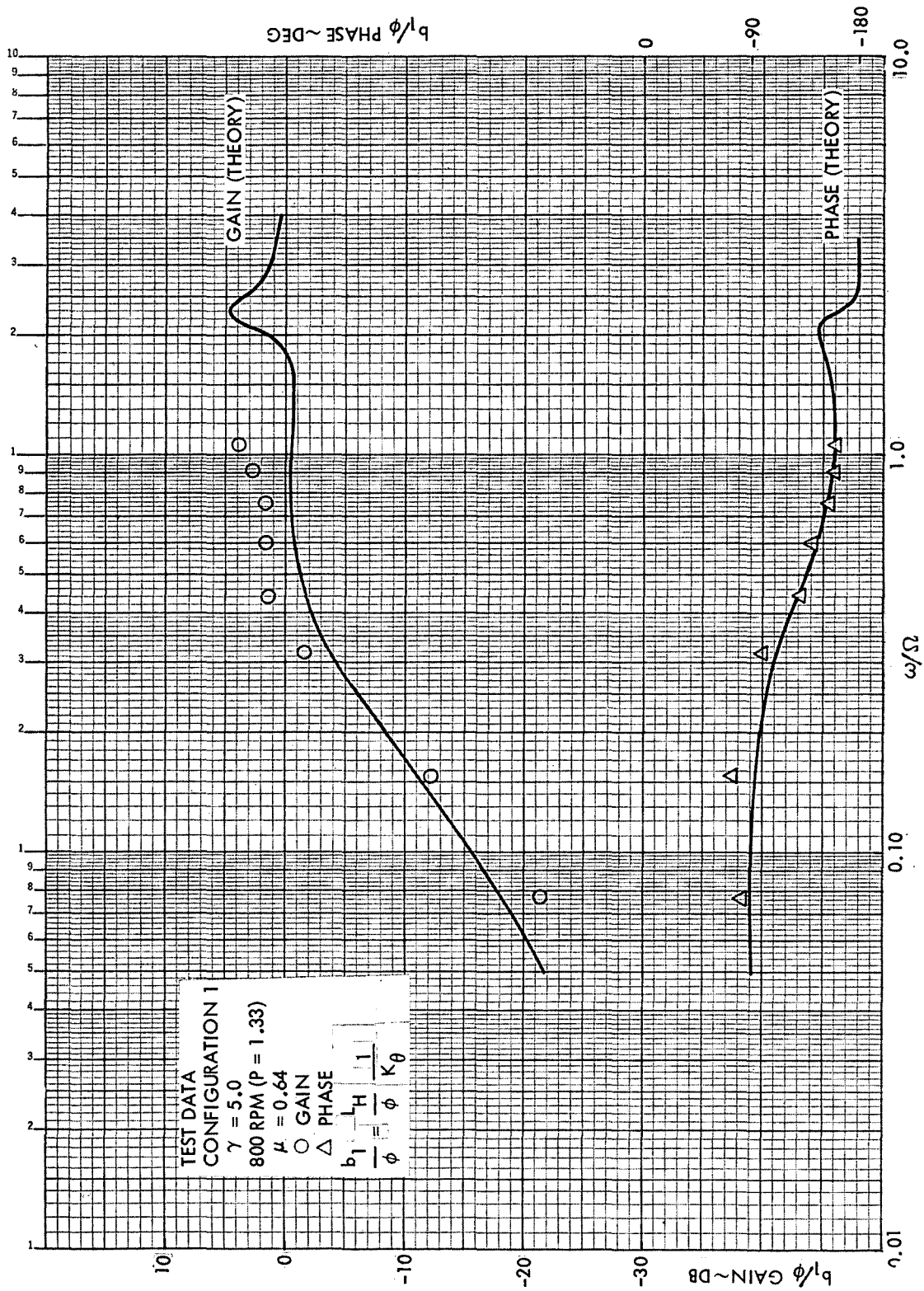


Figure 45. Comparison of Experimental and Theoretical Data, Rotor Lateral Frequency Response to  $\phi$ , Configuration 1,  $\mu = 0.64$ , 800 RPM ( $P = 1.33$ )

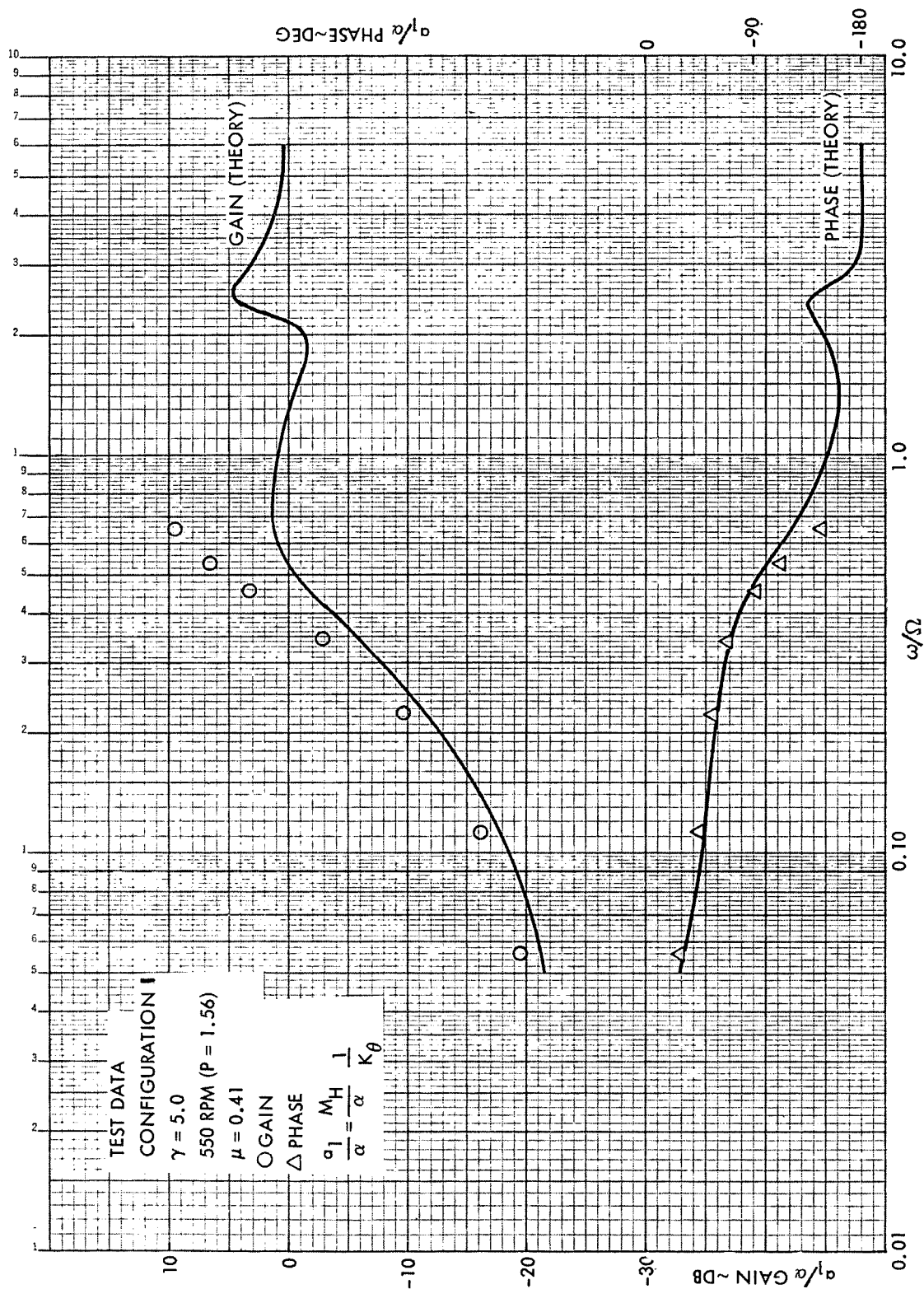


Figure 46. Comparison of Experimental and Theoretical Data, Rotor Longitudinal Frequency Response to  $\alpha$ , Configuration 1,  $\mu = 0.41$ , 550 RPM ( $P = 1.56$ )

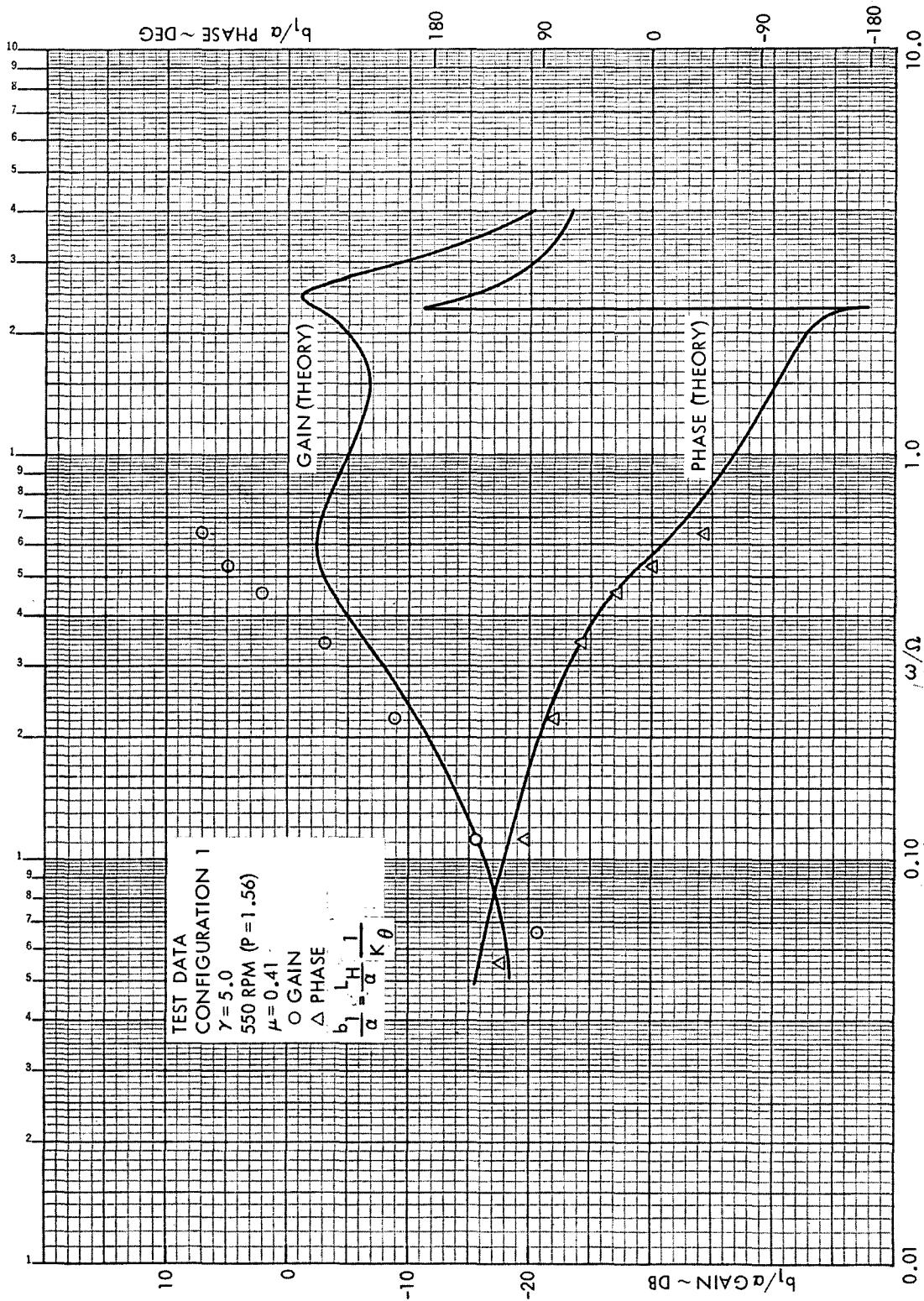


Figure 47. Comparison of Experimental and Theoretical Data, Rotor Lateral Frequency Response to  $\alpha$ , Configuration 1,  $\mu = 0.41$ , 550 RPM ( $P = 1.56$ )

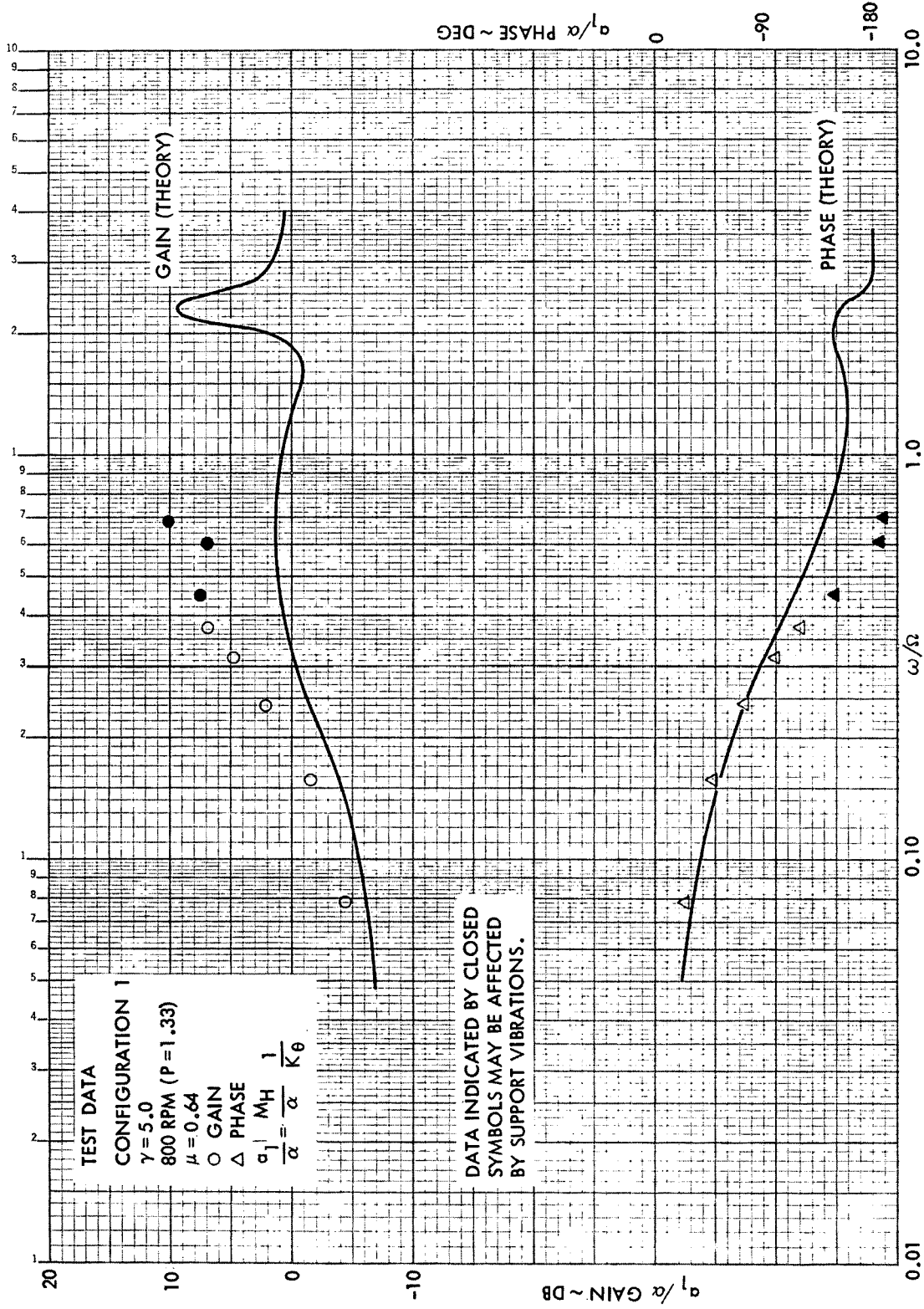


Figure 48. Comparison of Experimental and Theoretical Data, Rotor Longitudinal Frequency Response to  $\alpha$ , Configuration 1,  $\mu = 0.64$ , 800 RPM ( $P = 1.33$ )

results.  $K_{\theta}$  varies with rotor rotational speed and blade structural stiffness (Reference 1). For the data presented,  $K_{\theta} = 327$  in.-lb/deg at 550 rpm and  $K_{\theta} = 348$  in.-lb/deg at 800 rpm.

Without discussing Figures 43 through 48 individually, the following observations are offered concerning the correlation results. With the exception of the absolute gains, good agreement exists between theoretical and experimental frequency response to shaft roll. It is probable that the discrepancies in the magnitudes of the derivatives are due to the procedure by which the test data were nondimensionalized as much as the theory itself. It is highly unlikely that a single value of  $K_{\theta}$  (which is based upon the first flap mode response at  $\mu = 0$ ) is valid for all excitation frequencies and forward speeds.

The correlation results for shaft pitch oscillations are not quite as good as for shaft roll. Agreement does exist at low excitation frequencies for both gain and phase data. At higher frequencies, however, the experimental data exhibit greater peaking and more phase lag than the theory. This implies that the actual rotor flap damping is less than that predicted theoretically. The experimental frequency response data for shaft roll excitations also manifest this characteristic to a lesser degree. It is noted that similar correlations of frequency response to swashplate excitations (Reference 2) also suggested that the actual flap damping was less than that predicted analytically.

## SECTION 7

## CONCLUDING REMARKS

The third phase of the Lockheed/AMRDL "High Advance Ratio Research Program" was primarily an experimental activity. The hingeless rotor data bank established during the earlier two phases of the program was expanded by testing a larger advance ratio/flap frequency ( $\mu/P$ ) envelope and by determining rotor frequency response to shaft pitch and roll for the first time.

The  $\mu/P$  envelope for which rotor response data with respect to steady  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$ , and  $\alpha$  excitations are available was extended to include  $P = 1.125$  at  $\mu = 0$ ,  $P = 1.15$  for  $\mu = 0 \rightarrow 0.82$  and  $P = 1.28$  for  $\mu = 0 \rightarrow 0.92$ . The analysis of these steady state data included determining steady rotor hub moment, shaft moment and lift derivatives. The rotor rotating blade flap bending moments at three radial positions ( $x = 0.073, 0.293, 0.49$ ) were also harmonically analyzed and response derivatives calculated. The characteristics of the data generally agree with previous test results. Variations in the rotor response with changes in flap frequency and advance ratio were as anticipated. Test results at  $\mu = 0$  with low and moderate rotor lift levels clearly demonstrate the linear and nonlinear effects of induced inflow.

The rotor frequency response data bank with  $\theta_o$ ,  $\theta_s$  and  $\theta_c$  excitations was expanded to include  $P = 1.15$  for  $\mu = 0 \rightarrow 0.60$  and  $P = 1.28$  for  $\mu = 0 \rightarrow 0.92$ . These newly acquired transfer functions have the same characteristics as similar Phase 2 data. The rotor response was a maximum when the excitation frequency was in resonance with the blade first flap bending mode natural frequency. A mild involvement of the blade second flap bending mode in the response was noted at several test conditions. The frequency response characteristics also indicate that the damping of the blade flapping motion increases with advance ratio and that induced inflow is an important consideration only at low excitation frequencies.

Experimental rotor transfer functions with respect to shaft pitching ( $\alpha$ ) and rolling ( $\phi$ ) oscillations were obtained for nondimensional flap frequencies ranging from  $P = 1.15 \rightarrow 1.56$  and advance ratios from  $\mu = 0 \rightarrow$  to  $0.93$ . The data indicate that the major part of the rotor response is caused by the inertial and gyroscopic excitations. Aerodynamic excitations due to  $\dot{\alpha}$  and  $\dot{\phi}$  are comparatively weak and the aerodynamic excitation due to  $\alpha$  is only a factor at low frequencies.

Several closed loop frequency tests with  $\alpha$  and  $\phi$  excitations were also conducted to further evaluate the Phase 2 hub moment feedback control system. The closed loop response characteristics were approximately the same as those previously obtained. That is, the control network was only effective in reducing the rotor response to the shaft excitations at very low frequencies.

Selected experimental rotor transfer functions with  $\alpha$  and  $\phi$  excitations were compared with theoretical results in order to assess the validity of the mathematical model. The rigid blade flapping theory agreed reasonably well with the test results, a finding which is consistent with previous correlation efforts.

The hingeless rotor data bank, which has been formed by testing the 7 1/2-foot diameter Lockheed/AMRDL rotor model is characterized by low nominal rotor lift levels. A follow-on effort which is currently in the planning stages will involve testing the model at high rotor lifts. The testing will be open loop and include both steady response and frequency response. These results will greatly compliment the existing data by defining the conditions where the linear rotor derivatives are valid.

## SECTION 8

## REFERENCES

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## APPENDIX A

## EXPERIMENTAL STEADY STATE ROTOR RESPONSE DATA

The data used to calculate the steady lift and moment derivatives presented in Section 5 of this report are tabulated herein. Measured values of  $\Omega$ ,  $\mu$ ,  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$ ,  $\alpha$ ,  $M_H$ ,  $L_H$ ,  $M_S$ ,  $L_S$  and LIFT are listed in Table IV for each test point. For each data set, where one of the four excitations was varied while the other three were held constant, a linear least squares curve fit of the five responses was used to determine steady derivatives. These are noted in the tabulations as slopes. The deviation of each datum from the statistical line was also calculated and is labeled an error. The errors are useful as a quick check of the linearity of the data.

All of the rotating blade bending moment data are listed in Table V. Derivatives were also determined from these data with a linear least squares curve fit. They are plotted in Figures A1 through A12. The one-per-rev blade bending moment distributions are used in Appendices B and C to transfer hub moment frequency response data to the rotor shaft centerline.

TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5

$\Omega$ rad sec	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$I_H$			$M_S$			$I_S$			$LIFT$	
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag lb	Slope lb deg
57.6	0.0	1.98	-0.03	0.23	0.0	-4	*	-5	*	-3	*	-5	*	0	0	-2	0	0	-2
57.6	0.0	1.96	2.03	0.22	0.0	6		-64		12		-96		1	1	1		1	1
57.5	0.0	1.98	3.86	0.22	0.0	11		-130		17		-191		3	3	1		3	1
57.5	0.0	1.98	4.89	0.22	0.0	23		-188		38		-275		0	0	-1		0	-1
57.6	0.0	1.98	-1.85	0.23	0.0	-8		49		-9		81		2	2	1		2	1
57.5	0.0	1.98	-3.98	0.23	0.0	-21		125		-31		189		3	3	1		3	1
57.5	0.0	1.98	-6.12	0.23	0.0	-47		233		-63		344		6	6	-2		6	-2
57.4	0.0	3.94	0.03	0.23	0.0	-1	10	-8	-44	4	16	4	-14	4	6	0	0	4	0
57.5	0.0	3.94	2.04	0.22	0.0	22		-106		32		-158		1	1	-10		1	-1
57.5	0.0	3.94	3.90	0.22	0.0	43		-188		65		-273		5	5	-6		5	-6
57.4	0.0	3.94	4.76	0.22	0.0	52		-215		71		-316		-3	-3	6		-3	6
57.6	0.0	3.94	-2.07	0.23	0.0	-29		81		-41		128		-7	-7	13		-7	13
57.5	0.0	3.94	-3.92	0.23	0.0	-52		156		-2		233		-7	-7	1		-7	1
57.4	0.0	3.94	-6.31	0.23	0.0	-54		260		-2		381		8	8	-6		8	-6
57.4	0.0	5.90	-0.16	0.23	0.0	-4	17	-12	-52	0	26	-6	-14	0	13	0	0	13	0
57.3	0.0	5.90	1.89	0.22	0.0	38		-123		59		-181		3	3	-11		3	-11
57.2	0.0	5.90	3.90	0.22	0.0	75		-227		121		-325		13	13	-2		13	-2
57.2	0.0	5.90	4.70	0.22	0.0	79		-265		121		-383		-6	-6	0		-6	0
57.3	0.0	5.90	-2.07	0.22	0.0	-40		98		-9		151		-13	-13	21		-13	21
57.2	0.0	5.90	-4.16	0.22	0.0	-67		204		0		299		0	0	11		0	11
57.2	0.0	5.90	-6.31	0.22	0.0	-67		299		6		432		9	9	-19		9	-19
57.5	0.0	3.99	-0.10	0.30	0.0	-8		-9		-4		-13		-7	-7	5		-7	5
57.4	0.0	3.99	-0.11	2.37	0.0	-105		-33		-4		-80		-13	-13	1		-13	1
57.4	0.0	3.99	-0.10	4.21	0.0	-184		-53		-4		-269		-5	-5	-3		-5	-3
57.3	0.0	4.00	-0.09	6.24	0.0	-265		-67		7		-385		13	13	-108		13	-108
57.4	0.0	4.00	-0.09	-1.56	0.0	76		20		3		26		1	1	26		1	26
57.3	0.0	3.99	-0.11	-3.62	0.0	170		40		1		252		-3	-3	66		-3	66
57.4	0.0	3.99	-0.12	-2.59	0.0	132		29		1		41		15	15	41		15	41
89.0	0.0	0.02	-0.05	0.15	0.0	-4	2	-6	-3	-2	6	1	-4	1	-2	-2	-2	-2	0
89.5	0.0	2.04	-0.05	0.14	0.0	3		-7		3		-6		3	3	-6		3	-6
88.2	0.0	4.00	-0.04	0.13	0.0	6		-12		4		0		21	21	0		21	0
88.6	0.0	5.86	-0.02	0.12	0.0	3		-28		-5		-13		18	18	-46		18	-46
89.3	0.0	6.92	-0.01	0.12	0.0	20		-25		1		-39		47	47	-10		47	-10
89.0	0.0	0.01	-0.03	0.14	0.0	-3	*	-7	*	2	*	-8	*	2	2	-8	*	2	-8
89.0	0.0	0.01	2.01	0.14	0.0	6		-65		17		-128		17	17	-128		17	-128
89.1	0.0	0.01	3.98	0.14	0.0	64		-211		48		-398		48	48	-398		48	-398
89.0	0.0	0.01	4.69	0.14	0.0	95		-277		68		-534		-2	-2	68		-2	68
89.9	0.0	0.01	-2.21	0.15	0.0	-11		66		-8		157		-8	-8	157		-8	157
88.8	0.0	0.01	-4.14	0.15	0.0	-63		206		-57		400		-57	-57	400		-57	400
88.6	0.0	0.01	-6.18	0.14	0.0	-147		362		-248		665		-248	-248	665		-248	665
88.6	0.0	2.00	-0.09	0.14	0.0	-3	*	-5	*	1	*	-1	*	1	1	-1	*	1	-1
88.7	0.0	2.00	2.09	0.13	0.0	40		-94		95		-202		95	95	-202		95	-202
88.6	0.0	2.00	3.84	0.13	0.0	73		-211		133		-406		133	133	-406		133	-406
89.5	0.0	2.00	4.87	0.13	0.0	117		-286		209		-539		209	209	-539		209	-539
88.7	0.0	2.00	-2.23	0.14	0.0	-35		108		-57		224		-57	-57	224		-57	224
88.6	0.0	2.00	-4.19	0.14	0.0	-63		232		-109		441		-109	-109	441		-109	441
88.4	0.0	2.00	-6.17	0.13	0.0	-160		384		-279		699		-279	-279	699		-279	699

\* Nonlinear



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$L_H$			$M_S$			$L_S$			$LIFT$		
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag lb	Slope lb deg	Error lb
88.6	0.0	4.00	-0.23	0.12	0.0	-6	40	-9	3	-67	1	-8	70	-20	15	-10	17	0	-3	
88.5	0.0	3.95	1.77	0.12	0.0	90		7	-128	6	169		16	-246	-5	18	-2	-2		
88.4	0.0	3.99	3.55	0.12	0.0	164		11	-254	1	307		29	-458	4	21	0	0		
88.3	0.0	3.99	4.72	0.12	0.0	194		-6	-335	-2	339		-21	-616	-10	24	4	4		
88.5	0.0	4.00	-2.24	0.13	0.0	-86		-9	134	-3	-141		-12	274	20	24	-3	-3		
88.4	0.0	4.00	-4.22	0.13	0.0	-164		-9	264	-6	-274		-6	492	-7	20	0	0		
88.0	0.0	4.00	-5.97	0.13	0.0	-211		14	393	5	-376		15	705	-10	24	4	4		
85.8	0.0	5.92	-0.19	0.12	0.0	-5	56	-17	-11	-75	-4	2	99	-23	-11	38	0	-1		
85.0	0.0	5.92	1.76	0.11	0.0	125		5	-148	5	240		21	-276	0	38	-2	-2		
82.9	0.0	5.92	3.58	0.11	0.0	230		9	-287	2	430		31	-509	15	40	0	0		
88.7	0.0	5.92	4.70	0.11	0.0	281		-2	-378	-5	481		-29	-701	-24	41	2	2		
88.9	0.0	5.92	-2.24	0.12	0.0	-106		-3	145	1	-185		-7	289	21	37	-2	-2		
88.9	0.0	5.92	-4.13	0.13	0.0	-206		2	294	7	-362		3	545	20	39	0	0		
88.7	0.0	5.92	-6.03	0.14	0.0	-309		5	423	-6	-550		3	752	-32	42	0	0		
104.8	0.0	0.01	-0.01	0.14	0.0	-7	3	0	-8	-3	-2	9	2	-9	2	13	*	3		
104.9	0.0	1.97	-0.01	0.14	0.0	-2		-1	-10	2	12		-3	-11	7	21				
104.9	0.0	3.93	0.0	0.12	0.0	8		2	-16	2	31		0	-33	-1	40				
104.3	0.0	5.92	0.01	0.11	0.0	11		1	-24	0	50		0	-44	2	67				
104.8	0.0	4.95	0.02	0.10	0.0	9		0	-24	-3	42		1	-43	-4	54				
105.3	0.0	0.0	0.02	0.12	0.0	-6	*		-10	*	8	*		-9	*	13	0	1		
105.3	0.0	0.0	1.75	0.12	0.0	15			-58		30			-163		15		2		
105.4	0.0	0.0	3.58	0.12	0.0	87			-205		178			-454		13		0		
105.3	0.0	0.0	4.77	0.07	0.0	139			-289		299			-604		12		-2		
105.5	0.0	0.0	-2.24	0.09	0.0	-17			83		-34			226		12		0		
105.3	0.0	0.0	-4.23	0.09	0.0	-95			245		-172			541		10		1		
105.4	0.0	0.0	-6.29	0.10	0.0	-223			428		-419			850		9		1		
105.3	0.0	2.00	-0.08	0.25	0.0	-6	*		-11	*	-7	*		-18		20	0	-6		
105.4	0.0	2.00	1.66	0.25	0.0	45			-105		106			-246		21		-5		
105.2	0.0	2.00	3.53	0.25	0.0	81			-214		154			-469		27		2		
105.2	0.0	2.00	4.82	0.25	0.0	147			-337		307			-687		31		6		
105.4	0.0	2.00	-2.27	0.27	0.0	-64			117		-128			299		22		-4		
105.3	0.0	2.00	-4.27	0.26	0.0	-125			261		-258			564		29		2		
105.2	0.0	2.00	-6.17	0.26	0.0	-235			437		-464			865		31		4		
105.5	0.0	3.97	-0.07	0.24	0.0	-7	54	-13	-19	-74	0	-4	107	-37	11	40	0	-5		
105.6	0.0	3.97	1.75	0.24	0.0	104		1	-146	7	227			-331	-17	42		-2		
105.5	0.0	3.97	3.54	0.24	0.0	216		15	-286	0	433			-606	-20	44		1		
105.6	0.0	3.97	4.66	0.24	0.0	262		1	-368	0	519			-746	11	48		5		
105.7	0.0	3.97	-2.23	0.26	0.0	-119		-8	131	-10	-225			331	40	42		-4		
105.7	0.0	3.97	-4.10	0.26	0.0	-221		-8	273	-6	-406			598	23	43		-3		
105.5	0.0	3.97	-6.13	0.26	0.0	-306		16	437	9	-608			846	-38	54		7		
57.6	C.41	0.0	0.03	0.78	0.0	2	69	4	-9	-46	0	-14	107	7	3	4	9	0		
57.8	0.41	2.10	0.03	0.78	0.0	139		-4	-104		193			-133	-3	22		0		
57.8	0.41	4.09	0.03	0.78	0.0	279		0	-209	-3	416			-254	-5	40		0		
57.5	0.41	6.15	0.03	0.78	0.0	423		0	-296	-4	635			-382	-9	58		0		
57.5	C.41	7.21	0.03	0.78	0.0	499		3	-336	4	753			-424	12	67		0		

\* Nonlinear



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$L_H$			$M_S$			$L_S$			$LIFT$			
						Mag in-lb	Error in-lb	Slope deg	Mag in-lb	Error in-lb	Slope deg	Mag in-lb	Error in-lb	Slope deg	Mag in-lb	Error in-lb	Slope deg	Mag lb	Error lb	Slope deg	Mag lb
57.8	0.40	0.98	-1.05	0.80	0.0	-16	5	61	-5	-1	-56	1	-31	89	-2	31	-87	-2	8	0	0
57.6	0.41	0.98	0.94	0.78	0.0	116	5	-106	8	-232	8	152	4	-144	18	15	18	18	15	0	0
57.7	0.42	0.98	2.99	0.78	0.0	239	2	-232	-2	311	-20	-368	-20	-368	-27	25	-27	25	0	0	0
57.7	0.42	0.98	5.03	0.78	0.0	359	-2	-403	-4	528	14	-521	14	-521	15	34	15	34	0	0	0
57.5	0.40	0.98	-5.32	0.80	0.0	-275	-4	241	2	-403	2	-403	7	398	-10	-10	-10	-10	1	1	1
57.5	0.40	0.98	-7.08	0.80	0.0	-374	4	333	-5	-570	-3	512	-3	512	-24	-16	-24	-24	1	1	1
57.7	0.41	0.98	-1.06	0.80	0.0	-4	8	-79	8	-1	-35	-1	-24	23	5	5	23	5	0	0	0
57.6	0.41	0.98	-1.06	2.51	0.0	-140	6	-69	-8	-224	-4	-86	-4	-86	-6	7	-6	7	0	0	0
57.6	0.42	0.98	-1.06	4.38	0.0	-301	-8	-144	-9	-444	-7	-227	-7	-227	-20	7	-20	7	0	0	0
57.6	0.42	0.98	-1.06	6.30	0.0	-440	4	-194	17	-645	15	-315	15	-315	23	5	23	5	0	0	0
57.8	0.41	0.98	-1.06	-1.42	0.0	150	-13	89	-4	225	-10	186	-10	186	-3	8	-3	8	0	0	0
57.9	0.41	0.97	-1.06	-3.53	0.0	323	-7	183	6	472	-8	346	-8	346	13	7	13	7	0	0	0
57.9	0.41	0.97	-1.06	-5.40	0.0	488	11	254	4	714	4	460	17	460	1	8	1	8	0	0	0
57.9	0.41	0.97	-1.06	0.74	0.0	-21	23	*	*	*	*	*	*	*	62	7	*	5	1	1	1
58.1	0.41	0.97	-1.06	0.74	2.06	41	-7	-7	6	-16	-74	-3	-36	170	8	-12	-98	-6	6	1	1
57.8	0.57	2.09	0.06	1.08	0.0	214	-2	-165	2	308	-2	-207	-2	-207	3	25	3	25	1	1	1
57.9	0.56	4.14	0.06	1.08	0.0	447	5	-323	-4	671	-4	418	12	-418	-7	48	-7	48	0	0	0
57.9	0.56	4.94	0.06	1.08	0.0	535	6	-380	-3	802	7	-496	7	-496	-6	57	-6	57	1	1	1
57.9	0.56	3.13	0.06	1.08	0.0	317	-14	-235	9	463	-24	-294	17	36	-1	36	-1	36	-1	-1	-1
57.8	0.56	1.15	0.80	0.86	0.0	219	27	-156	-72	-10	33	201	7	22	22	6	22	6	1	1	1
57.9	0.56	1.15	2.85	0.86	0.0	370	-9	-291	3	549	-15	-410	-15	-410	-1	33	-1	33	-1	-1	-1
58.0	0.56	1.15	3.84	0.86	0.0	463	-6	-361	4	698	-2	-507	4	698	9	41	9	41	1	1	1
57.4	0.55	1.15	-3.40	0.86	0.0	-208	-18	160	3	-325	3	-325	7	-6	-6	1	-6	1	1	1	1
57.4	0.55	1.15	-5.58	0.86	0.0	-383	6	316	-6	-17	-134	-7	46	-65	17	9	-18	9	0	0	0
57.5	0.56	1.15	-1.31	0.86	0.0	0	-89	2	3	-38	-4	-241	-4	-241	-7	8	-7	8	0	0	0
57.5	0.56	1.15	-1.31	2.55	0.0	-151	6	-61	-4	-128	-4	-241	-4	-241	-14	8	-14	8	0	0	0
57.5	0.56	1.15	-1.31	4.49	0.0	-339	-13	-128	1	-509	1	-509	9	-238	17	8	-238	17	8	0	0
57.5	0.56	1.15	-1.31	5.49	0.0	-413	3	-157	10	-620	9	-620	29	173	-25	9	-25	9	1	1	1
57.7	0.55	1.15	-1.31	-1.35	0.0	211	16	70	-23	314	29	359	-21	359	21	7	21	7	-1	-1	-1
57.7	0.55	1.15	-1.31	-3.46	0.0	368	-16	189	15	546	-2	403	3	403	3	8	3	8	0	0	0
57.7	0.55	1.15	-1.31	-4.40	0.0	469	1	215	6	695	-4	-24	2	18	-12	22	-12	22	0	0	0
57.7	0.55	1.14	-1.30	1.08	0.0	0	53	2	-13	-25	-4	-24	83	2	18	-32	7	9	6	0	0
57.9	0.56	1.14	-1.30	1.08	2.06	112	4	-66	-5	150	6	-53	2	-53	-12	22	-12	22	0	0	0
58.1	0.55	1.14	-1.30	1.08	4.22	217	-6	-111	3	315	-8	-108	6	-108	3	37	3	37	0	0	0
58.2	0.55	1.14	-1.30	1.08	5.05	269	3	-133	2	397	5	-130	7	42	7	42	7	42	0	0	0
57.8	0.55	1.14	-1.30	1.08	-2.06	-120	-8	48	7	-213	-16	98	7	-4	-4	0	-4	0	0	0	0
57.8	0.55	1.14	-1.30	1.08	-3.11	-162	5	65	-2	-272	12	128	3	-10	-10	0	-10	0	0	0	0
57.4	0.79	0.08	-0.37	0.99	0.0	-10	-5	12	-105	2	-40	7	48	-145	-10	5	-145	-10	5	0	0
57.6	0.79	1.09	-0.37	0.99	0.0	184	8	-96	0	241	10	-91	10	-91	1	20	1	20	1	1	1
57.9	0.78	2.10	-0.37	0.99	0.0	363	7	-207	-5	516	19	-227	12	33	12	33	12	33	0	0	0
57.9	0.79	3.12	-0.37	0.99	0.0	536	-4	-306	4	757	-8	-397	-10	-397	-10	47	-10	47	0	0	0
57.4	0.79	1.75	-0.37	0.99	0.0	288	-6	-167	-2	391	-14	-185	-14	-185	3	27	3	27	1	1	1

\* Nonlinear



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$L_H$			$M_S$			$L_S$			$LIFT$		
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag lb	Slope deg	Error lb
57.2	0.79	0.56	-0.87	1.29	0.0	-31	160	-7	10	-98	11	-74	235	-27	42	-130	3	10	11	0
57.3	0.79	0.56	0.03	1.29	0.0	139	19	-97	170	-7	170	6	-104	-29	20	1	20	1	1	1
58.0	0.79	0.55	1.99	1.29	0.0	426	-7	-283	0	633	9	-312	18	39	3	-5	-1	0	0	0
57.6	0.79	0.55	-2.08	1.29	0.0	-224	-7	115	-3	-334	3	-4	203	10	-14	0	0	0	0	0
57.5	0.79	0.55	-3.10	1.29	0.0	-378	2	217	-2	-553	16	343	10	-14	0	0	0	0	0	0
57.7	0.79	0.55	-0.97	1.29	0.0	-14	-104	19	-7	-38	-16	-44	-153	21	34	-64	7	7	0	0
57.5	0.79	0.55	-0.97	2.38	0.0	-156	-10	-35	-62	2	-362	2	-26	-8	6	0	6	6	0	0
57.5	0.80	0.55	-0.97	3.21	0.0	-235	-3	-62	-83	17	-513	2	-26	-8	6	0	6	6	0	0
57.6	0.79	0.55	-0.95	4.17	0.0	-340	-9	-83	179	-12	243	29	158	29	158	-10	7	0	0	0
57.6	0.79	0.55	-0.95	-2.79	0.0	375	-14	163	-1	544	-17	312	1	6	0	0	6	0	0	0
57.7	0.79	0.55	-0.95	-3.87	0.0	496	-5	219	14	721	14	721	14	9	7	14	9	7	14	0
57.6	0.79	0.55	-0.95	1.13	0.0	-4	112	-4	9	-47	-4	-36	164	-8	49	-60	0	7	11	-2
57.9	0.79	0.55	-0.95	1.13	2.05	228	-3	-91	-73	6	306	-3	-73	-1	29	-3	29	-3	3	3
58.3	0.78	0.55	-0.95	1.13	4.21	477	4	-181	6	671	7	199	2	59	2	59	2	59	2	3
57.7	0.79	0.55	-0.95	1.13	-2.05	-234	-4	113	3	-374	0	-174	0	-13	174	1	-13	174	1	1
57.8	0.79	0.55	-0.95	1.13	-3.10	-341	7	162	2	-525	13	238	2	-24	2	-24	2	-24	2	2
57.6	0.92	0.04	-0.25	1.35	0.0	-24	231	-6	-2	-116	4	-67	340	-8	27	-150	13	10	17	0
57.7	0.92	0.99	-0.25	1.35	0.0	211	9	-124	-7	275	11	-133	11	-133	26	0	26	0	0	0
58.0	0.92	1.15	-0.25	1.34	0.0	462	-8	-247	5	645	-14	-298	-5	45	0	45	0	0	0	0
58.0	0.92	1.71	-0.25	1.35	0.0	373	5	-204	-3	520	11	-214	13	39	0	39	0	0	0	0
57.8	0.92	0.55	-0.78	1.35	0.0	5	188	-14	-13	-102	6	-21	272	-19	24	-146	-2	11	13	-2
58.0	0.92	0.55	0.15	1.35	0.0	206	12	-124	-10	260	10	-145	10	-145	26	0	26	0	0	0
57.9	0.92	0.55	1.46	1.35	0.0	438	-3	-243	4	607	0	-310	7	43	0	43	0	0	0	0
57.6	0.93	0.55	-0.81	1.35	0.0	-2	-110	1	-11	-41	4	-33	-163	-9	26	-70	13	10	-1	0
57.6	0.93	0.55	-0.81	2.10	0.0	-64	20	-56	-20	-11	-120	26	-48	-15	11	0	11	0	0	0
57.5	0.93	0.55	-0.81	3.03	0.0	-200	-14	-80	3	-314	-17	-100	-1	9	0	9	0	0	0	0
57.5	0.93	0.55	-0.81	4.00	0.0	-305	-12	-113	10	-462	-7	-154	13	6	0	6	0	0	0	0
57.6	0.92	0.55	-0.78	0.13	0.0	158	25	25	-9	317	26	94	-11	13	1	13	1	1	1	1
57.6	0.92	0.55	-0.78	-0.80	0.0	234	-2	64	-9	169	-9	169	-2	14	1	14	1	1	1	1
57.5	0.92	0.55	-0.78	-2.83	0.0	442	-16	169	13	648	-9	323	10	15	-1	15	-1	1	1	1
57.5	0.93	0.55	-0.78	1.44	0.0	-23	-32	-10	-55	2	-59	221	-47	21	-65	3	10	15	-5	0
57.9	0.92	0.55	-0.78	1.44	2.05	316	-5	-125	0	429	-12	-133	-12	45	0	45	0	0	0	0
58.2	0.91	0.55	-0.79	1.44	3.16	509	20	-187	1	721	34	-189	34	66	3	66	3	3	3	3
57.6	0.92	0.55	-0.78	1.44	-2.05	-305	-3	100	0	-471	-6	150	3	-16	0	-16	0	0	0	0
57.7	0.92	0.55	-0.78	1.44	-3.12	-445	20	157	-1	-672	30	214	-4	-30	2	-30	2	2	2	2
88.9	0.27	-0.03	0.15	0.44	0.05	-4	75	4	-1	-16	-1	-38	132	9	-3	-21	-8	0	19	0
88.9	0.27	2.07	0.17	0.44	0.06	145	-4	-30	-3	226	-6	-55	-6	39	3	39	3	3	3	3
88.8	0.27	4.01	0.17	0.44	0.06	292	-2	-66	-3	481	-8	-124	-8	75	0	75	0	0	0	0
88.9	0.27	6.17	0.17	0.44	0.07	446	-8	-96	2	769	-6	-153	-8	115	0	115	0	0	0	0
88.7	0.27	7.16	0.17	0.44	0.07	538	9	-113	1	917	11	-146	20	135	0	135	0	0	0	0
88.8	0.26	1.04	-0.54	0.73	0.06	-20	87	19	-11	-46	4	-89	14	-10	-93	29	15	6	0	0
88.9	0.27	1.04	1.49	0.73	0.07	151	13	-102	7	252	24	-229	24	27	0	27	0	0	0	0
88.9	0.27	1.04	3.59	0.73	0.06	331	12	-217	-11	597	28	-434	-30	39	1	39	1	1	1	1
88.7	0.26	1.04	5.66	0.73	0.07	474	-24	-297	4	867	-39	-568	-29	48	0	48	0	0	0	0
88.7	0.26	1.04	-2.70	0.74	0.05	-231	-6	76	-6	-473	-19	204	-21	2	0	2	0	0	0	0
88.8	0.26	1.04	-4.88	0.74	0.04	-429	-14	186	2	-816	-8	380	-7	-11	0	-11	0	0	0	0



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$		$L_H$		$M_S$		$L_S$		LIFT						
						Mag in-lb	Error in-lb	Slope in-lb deg	Mag in-lb	Error in-lb	Slope in-lb deg	Mag in-lb	Error in-lb	Slope in-lb deg	Mag lb	Error lb	Slope lb deg			
88.7	0.27	1.04	-0.67	0.73	0.06	-3	-84	37	-4	-75	10	-72	-163	23	8	-155	-24	15	0	0
88.7	0.27	1.04	-0.67	2.78	0.05	-211	-164	3	-164	4	-440	4	-440	-9	-330	-4	-4	14	0	0
88.8	0.27	1.04	-0.67	4.70	0.05	-396	-310	-20	-310	2	-744	2	-744	0	-625	1	13	17	1	1
89.0	0.26	1.04	-0.67	-1.34	0.07	126	111	-8	111	-30	231	-12	289	-14	632	23	18	18	1	1
89.0	0.26	1.04	-0.67	-3.25	0.07	285	-10	-285	1	542	1	542	-14	632	23	18	18	1	1	1
88.9	0.26	1.04	-0.67	-4.78	0.07	422	-2	413	-2	817	15	817	11	837	-10	17	-10	17	-1	-1
89.0	0.27	1.11	-1.36	0.13	2.10	22	17	-7	16	5	2	9	31	-11	51	8	-9	38	7	-1
89.1	0.27	1.11	-1.36	0.13	4.26	68	3	3	21	3	92	0	78	5	57	-8	-8	55	5	0
89.3	0.26	1.10	-1.36	0.13	5.10	80	1	31	31	113	3	113	0	78	6	61	6	61	1	1
88.9	0.27	1.10	-1.35	0.13	-2.06	-31	10	-13	-13	-8	-91	18	3	18	3	-9	11	11	1	1
88.8	0.27	1.10	-1.35	0.13	-3.07	-63	-6	-3	-3	7	-152	-12	11	-12	11	7	3	3	0	0
89.1	0.36	-0.04	-0.56	0.28	0.04	5	5	106	-15	-34	0	-18	193	6	-26	-9	11	11	0	0
89.1	0.36	2.06	-0.56	0.31	0.05	211	-11	-86	-86	0	367	-12	-129	-12	-129	-9	11	55	1	1
89.2	0.36	4.07	-0.56	0.31	0.05	440	5	-156	-156	5	773	6	-230	6	-230	1	98	0	0	0
89.0	0.36	1.24	-1.80	0.31	0.04	-22	8	-2	-2	-52	-7	-72	195	-6	30	-105	21	27	9	1
89.2	0.36	1.24	-1.67	0.31	0.05	222	20	-110	-110	1	399	1	399	35	-217	-6	46	0	0	0
89.5	0.36	1.24	2.48	0.31	0.05	413	-12	-219	-219	2	766	2	766	-7	-439	-7	65	0	0	0
89.2	0.36	1.24	-3.76	0.31	0.03	-264	-26	112	112	3	-510	3	-510	-59	247	21	7	-2	-2	-2
89.2	0.35	1.24	-6.23	0.30	0.04	-490	10	240	240	0	-900	36	466	36	466	-19	-13	1	1	1
89.4	0.36	1.24	-1.67	0.31	0.05	-8	-91	10	-1	-83	1	-66	-170	-15	21	-165	-6	27	-1	0
89.3	0.36	1.24	-1.67	2.19	0.04	-188	1	-151	-151	7	-380	7	-380	-9	-285	2	25	0	0	0
89.2	0.36	1.24	-1.67	4.14	0.04	-374	-8	-321	-321	1	-690	14	-609	14	-609	2	22	0	0	0
89.5	0.36	1.24	-1.67	-1.85	0.05	182	5	159	159	-18	322	5	377	5	377	-6	31	1	1	1
89.4	0.36	1.24	-1.66	-4.26	0.05	388	-8	388	388	10	734	10	734	5	788	5	32	1	1	1
89.3	0.36	1.24	-1.66	0.43	0.04	-4	34	-5	-8	-2	-62	2	63	-5	20	-3	-17	28	0	0
89.3	0.36	1.24	-1.66	0.43	2.10	69	-3	-14	-14	0	69	0	69	-5	-4	1	49	1	1	1
89.7	0.36	1.24	-1.66	0.44	4.26	138	-8	-12	-12	6	193	6	193	-17	0	11	72	0	0	0
90.0	0.36	1.24	-1.66	0.43	5.09	186	12	-25	-25	-6	284	21	-31	21	-31	-17	82	1	1	1
88.9	0.36	1.24	-1.66	0.43	-1.98	-75	-7	-8	-8	-1	-191	-1	-191	-7	5	-2	7	0	0	0
88.8	0.36	1.24	-1.66	0.43	-3.07	-95	10	-5	-5	-55	2	-44	274	-11	7	-12	-3	1	1	1
89.0	0.51	1.02	-0.89	0.41	0.04	-4	159	-5	-2	-55	2	-44	274	-11	7	-12	-3	1	1	1
89.1	0.51	1.05	-0.89	0.41	0.05	161	-3	-3	-61	1	241	1	241	-9	-90	1	35	-1	-1	-1
89.1	0.51	2.05	-0.89	0.41	0.05	323	1	-113	-113	2	527	2	527	3	-171	10	58	0	0	0
89.1	0.51	3.14	-0.89	0.43	0.04	458	2	-176	-176	-2	827	5	-288	5	-288	-9	84	1	1	1
88.6	0.51	-0.98	-0.87	0.43	0.04	-153	5	49	49	-2	-295	12	95	12	95	-7	7	1	1	1
88.7	0.51	0.43	-1.20	0.67	0.04	0	155	19	-26	-65	0	-45	279	12	-25	-127	-3	18	1	1
88.9	0.51	0.43	-0.20	0.57	0.04	144	7	-92	-92	8	215	8	215	-24	-173	-15	31	0	0	0
89.0	0.51	0.43	0.84	0.67	0.05	278	-19	-150	-150	8	488	8	488	-24	-285	5	44	-1	-1	-1
89.2	0.51	0.43	1.77	0.66	0.05	443	1	-225	-225	-6	793	21	-410	21	-410	-3	59	0	0	0
88.7	0.51	0.43	-2.21	0.57	0.02	-169	6	39	39	-7	-345	-7	-345	-7	20	4	4	1	1	1
88.6	0.50	0.43	-3.43	0.57	0.04	-370	-1	117	117	-1	-672	8	259	8	259	7	-13	1	1	1
89.3	0.50	0.43	-3.86	0.67	0.04	-439	-8	147	147	0	-802	-2	288	-2	288	-19	-21	-1	-1	-1



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$I_H$			$M_S$			$I_S$			LIFT		
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb
89.5	0.50	0.43	-1.25	0.57	0.05	11	-89	26	-28	-78	-5	-29	-168	25	-32	-149	36	20	-1	3
89.3	0.51	0.43	-1.25	1.51	0.04	-76	-95	14	-95	-7	-176	20	-159	20	-159	-20	18	2		
89.4	0.51	0.43	-1.25	2.50	0.02	-186	-164	-7	-164	10	-363	1	-294	1	-294	-8	15	1		
89.3	0.51	0.43	-1.25	3.30	0.03	-270	-218	-20	-218	10	-520	-23	-369	36	-369	36	12	-3		
89.5	0.50	0.43	-1.25	1.39	0.05	168	127	-11	127	-11	273	-19	283	-11	283	20	20	1		
89.5	0.50	0.43	-1.24	3.40	0.05	336	305	11	305	11	627	-2	616	22	616	22	20	-2		
89.4	0.50	0.43	-1.24	0.62	0.03	-7	73	-7	73	-5	-14	3	-72	127	-20	-14	-4	20	15	-1
89.7	0.50	0.43	-1.22	0.62	2.09	149	-1	-1	-36	1	202	-8	-53	6	-53	6	48	-3		
90.2	0.50	0.42	-1.23	0.62	4.25	306	-3	-3	-61	4	480	-4	-105	-1	-105	-1	84	1		
89.5	0.50	0.42	-1.23	0.63	5.08	374	5	5	-79	-3	605	15	-125	-4	-125	-4	95	1		
88.2	0.51	0.42	-1.24	0.63	-2.01	-142	7	7	13	-7	-299	11	21	-3	21	-3	-8	1		
88.2	0.51	0.42	-1.24	0.63	-3.06	-227	-1	-1	39	5	-438	6	43	-2	43	-2	-24	1		
89.0	0.60	-0.01	-0.98	0.58	0.05	-11	213	-7	3	-70	3	-57	363	-11	7	-119	12	26	1	
89.2	0.61	1.01	-0.98	0.58	0.05	202	-13	-13	-67	4	304	-19	-105	10	-105	10	39	-1		
89.4	0.60	2.10	-0.98	0.58	0.05	440	-7	-7	-145	2	717	-2	-218	27	-218	27	68	0		
89.3	0.60	2.44	-0.98	0.58	0.05	527	7	7	-172	-2	846	4	-310	-25	-310	-25	78	0		
88.9	0.61	0.46	-0.98	0.58	0.05	117	20	20	-39	-6	151	27	-62	-13	-62	-13	28	2		
89.3	0.60	0.46	-1.51	0.73	0.05	-8	190	15	-11	-74	5	-67	351	16	-1	-148	1	17	17	
89.5	0.60	0.46	-0.51	0.73	0.05	165	-2	-2	-78	3	243	-25	-145	3	-145	3	30	-3		
89.7	0.60	0.46	0.48	0.73	0.05	346	-9	-9	-153	2	604	-12	-290	4	-290	4	49	-1		
90.0	0.60	0.46	1.39	0.73	0.05	527	-2	-2	-222	15	951	15	-430	1	-430	1	68	2		
89.3	0.61	0.46	-2.18	0.73	0.05	-135	15	15	37	-6	-305	14	90	-11	90	-11	5	1		
89.3	0.60	0.46	-3.50	0.73	0.04	-419	-18	-18	147	6	-790	-7	304	7	304	7	-18	0		
89.5	0.61	0.46	-1.47	0.73	0.05	-15	-105	9	-2	-73	6	-78	-195	2	21	-148	17	-2		
89.3	0.61	0.46	-1.47	1.74	0.04	-115	15	15	-88	-6	-249	28	-171	-29	-171	-29	15	1		
89.3	0.61	0.46	-1.47	2.66	0.05	-243	-17	-17	-143	6	-474	-18	-254	24	-254	24	11	-1		
89.5	0.60	0.46	-1.47	1.22	0.05	176	-4	-4	120	-14	279	-22	267	-28	267	-28	19	0		
89.3	0.60	0.46	-1.47	-3.15	0.05	381	-2	-2	283	8	687	9	599	19	599	19	23	0		
88.0	0.61	0.47	-1.46	1.60	0.02	26	120	-11	-13	-28	4	8	201	-21	-12	-32	-10	17	18	-4
88.7	0.61	0.46	-1.44	1.61	2.08	275	-9	-9	-69	-3	428	-17	-77	5	-77	5	56	-3		
89.0	0.61	0.46	-1.44	1.62	3.54	471	11	11	-100	5	761	22	-133	-4	-133	-4	90	4		
88.1	0.61	0.46	-1.46	1.62	-2.03	-203	8	8	44	-4	-376	8	41	-10	41	-10	-15	2		
88.3	0.61	0.46	-1.46	1.62	-3.08	-336	1	1	83	6	-586	9	91	6	-34	6	-34	1		
88.8	0.72	0.02	-1.28	1.68	0.03	13	282	12	1	-92	-5	-15	461	19	0	-108	0	18	28	1
89.0	0.72	1.04	-1.28	1.68	0.03	288	1	1	-88	1	432	-4	-97	3	-97	3	46	0		
89.1	0.72	1.50	-1.28	1.68	0.03	424	6	6	-130	0	671	22	-147	2	-147	2	60	1		
88.8	0.72	0.62	-1.28	1.68	0.03	153	-17	-17	-45	4	201	-41	-55	0	-55	0	31	-3		
88.7	0.72	-0.09	-1.29	1.69	0.02	-314	-1	-1	110	2	-543	4	135	5	-13	5	-13	1		
88.7	0.72	0.03	-1.28	1.68	0.02	8	250	24	0	-88	-11	-25	457	30	0	-125	-17	16	22	1
89.0	0.72	0.03	-0.12	1.68	0.03	284	9	9	-96	-4	470	-5	-151	-9	-151	-9	43	1		
89.2	0.71	0.03	0.71	1.68	0.03	465	-17	-17	-157	8	847	-7	-237	10	-237	10	60	0		
88.6	0.72	0.03	-2.26	1.70	0.02	-259	2	2	95	-2	-511	-9	111	-17	111	-17	-5	0		
88.6	0.72	0.03	-2.70	1.70	0.02	-389	-18	-18	144	9	-712	-8	202	19	-15	19	-15	0		



TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\frac{\Omega}{\text{rad}} / \frac{\text{sec}}$	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$M_S$			$L_S$			$LIFT$				
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag lb	Slope lb deg	Error lb		
88.8	0.72	0.03	-1.31	1.72	0.03	-20	-116	8	9	-70	1	-69	2	13	-144	14	14	-2	0
88.9	0.72	0.03	-1.31	2.78	0.03	-145	5	-73	-6	-275	9	-275	9	-158	16	13	13	1	1
88.8	0.72	0.03	-1.31	3.69	0.02	-279	-22	-124	6	-480	-12	-266	7	-266	7	9	9	-1	-1
88.8	0.71	0.03	-1.31	0.78	0.03	94	12	80	6	112	-7	161	14	15	14	15	15	-2	-2
89.0	0.71	0.03	-1.31	-0.30	0.03	235	27	136	-14	358	22	295	22	22	-7	22	22	3	3
88.9	0.71	0.03	-1.31	-1.74	0.02	345	-30	260	8	612	-15	509	1	20	24	20	24	-2	-2
88.7	0.72	0.03	-1.31	1.85	0.02	-20	168	1	1	-35	-10	-70	9	-7	-35	0	15	-4	-4
89.3	0.71	0.03	-1.31	1.86	2.07	318	-6	-63	-6	479	-13	-62	13	66	13	66	-2	-2	-2
89.6	0.71	0.03	-1.31	1.86	3.05	500	4	-91	6	782	6	-119	-9	95	66	95	3	3	3
89.0	0.72	0.03	-1.31	1.84	-2.03	-367	1	88	8	-657	-7	67	0	-28	0	-28	2	2	2
88.4	0.75	-0.04	0.29	2.17	0.00	-189	2	42	-2	-355	5	30	1	-4	1	-4	1	1	1
89.4	0.75	-0.04	0.29	2.17	0.00	-29	297	-21	52	-84	2	-91	-41	113	-124	3	0	0	0
89.6	0.75	0.44	0.29	2.17	0.00	148	13	4	-6	230	19	35	19	35	-9	0	0	0	0
89.9	0.75	0.99	0.29	2.17	0.00	319	21	-37	41	-29	-4	-29	41	-29	-4	0	0	0	0
90.3	0.75	1.45	0.29	2.17	0.00	422	-12	-71	3	739	-20	-79	-20	-79	3	0	0	0	0
89.8	0.75	-0.52	0.28	2.17	0.00	-170	-19	94	4	-347	-36	171	-36	171	8	0	0	0	0
90.0	0.75	-1.12	0.28	2.17	0.00	-311	18	139	-1	-599	37	229	37	229	-8	0	0	0	0
88.9	0.75	0.51	-0.59	1.46	0.00	21	259	0	1	-79	1	-1	483	0	38	-140	23	1	1
89.3	0.75	0.51	-0.42	1.46	0.00	283	0	-80	-2	492	5	-121	5	-121	-6	44	2	2	2
89.0	0.75	0.51	-1.06	1.46	0.00	-106	-6	46	7	-247	-19	105	-19	105	12	5	-3	-3	-3
89.0	0.75	0.51	-1.69	1.46	0.00	-251	13	84	-5	-516	17	156	17	156	-26	-5	1	1	1
89.6	0.74	0.51	-0.51	2.18	1.46	0.00	-398	-7	128	-68	1	-772	-3	261	10	-16	1	1	1
89.1	0.75	0.51	-0.51	1.62	0.00	-6	-113	-16	-8	-8	-11	-64	-43	5	-134	8	19	-2	-2
89.1	0.75	0.51	-0.51	2.68	0.00	-109	1	-71	-1	-245	2	-110	2	-110	0	15	-1	-1	-1
89.1	0.75	0.51	-0.51	3.33	0.00	-196	-13	-105	9	-392	-6	-180	-6	-180	18	14	-1	-1	-1
88.3	0.75	0.51	-0.51	0.67	0.00	152	35	72	5	229	46	166	46	166	8	24	3	3	3
89.6	0.74	0.51	-0.51	-0.32	0.00	263	34	122	-13	449	55	264	55	264	-26	25	2	2	2
89.3	0.74	0.51	-0.51	-1.33	0.00	329	-14	209	6	582	-29	457	-29	457	32	24	-2	-2	-2
89.2	0.74	0.51	-0.51	-1.33	0.00	315	-27	210	6	586	-25	419	-25	419	-7	24	-2	-2	-2
89.0	0.81	0.06	-0.13	1.72	0.00	-46	-7	-3	-91	-5	-138	-25	3	-155	-3	17	36	-2	-2
89.2	0.81	0.58	-0.14	1.72	0.00	151	9	-57	3	228	11	-80	11	-80	-4	34	-3	-3	-3
89.4	0.80	1.13	-0.14	1.73	0.00	326	-8	-99	2	552	-13	-147	-13	-147	13	57	0	0	0
89.6	0.80	1.57	-0.14	1.73	0.00	489	2	-140	8	856	12	-231	12	-231	-3	75	2	2	2
89.0	0.81	-0.45	-0.14	1.73	0.00	-210	7	35	-8	-427	8	62	8	62	-22	0	0	0	0
89.1	0.81	-1.06	-0.14	1.72	0.00	-434	-4	105	7	-816	6	196	6	196	17	-20	2	2	2
89.1	0.81	0.51	-0.65	1.74	0.00	-39	-26	-4	4	-84	-48	26	-48	26	19	19	-4	-4	-4
89.3	0.81	0.51	-0.12	1.73	0.00	150	9	-58	-6	226	12	-86	12	-86	-3	36	-2	-2	-2
89.5	0.81	0.51	0.40	1.72	0.00	272	-20	-93	3	443	-55	-205	-55	-205	-37	55	-2	-2	-2
89.6	0.81	0.51	0.83	1.72	0.00	442	25	-137	-4	758	64	-219	64	-219	19	67	2	2	2
88.7	0.82	0.51	-1.25	1.72	0.00	-180	7	47	5	-400	6	98	6	98	-2	4	-2	-2	-2
89.0	0.81	0.51	-1.77	1.73	0.00	-352	-14	99	12	-710	-19	209	-19	209	24	-8	0	0	0
89.1	0.81	0.51	-2.24	1.73	0.00	-454	20	112	-14	-909	39	236	-14	-909	-24	-18	3	3	3





TABLE IV  
EXPERIMENTAL STEADY ROTOR RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$ , CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_H$			$L_H$			$M_s$			$L_s$			LIFT		
						Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag in-lb	Slope in-lb deg	Error in-lb	Mag lb	Slope lb deg	Error lb
89.1	0.81	0.51	-0.59	1.72	0.0	9	-109	-9	-12	-65	-9	-34	-220	-32	-9	-140	15	24	-4	-1
89.1	0.81	0.51	-0.59	2.24	0.0	-35	-10	4	-50	-11	-125	-9	-6	-83	-28	21	-28	21	1	1
89.1	0.81	0.51	-0.59	3.39	0.0	-174	39	-10	-107	6	330	76	-6	-180	36	18	36	18	1	1
89.3	0.81	0.51	-0.59	0.56	0.0	184	-10	116	72	-11	479	21	291	195	15	31	15	31	1	1
89.4	0.81	0.51	-0.59	-0.37	0.0	235	-13	191	116	11	587	-51	448	23	-19	35	-19	35	2	2
89.1	0.82	0.51	-0.59	-1.19	0.0	321	171	-2	-7	-35	-11	65	354	-10	23	7	21	-1	-1	-1
89.1	0.76	0.49	-0.47	1.56	0.0	55	171	-2	-7	-35	-11	65	354	-10	23	7	21	-1	-1	-1
89.4	0.75	0.49	-0.47	1.56	1.05	222	-15	-15	-35	-2	470	23	-31	-31	-17	52	2	2	0	0
89.0	0.75	0.48	-0.47	1.56	1.57	410	15	-60	-60	6	767	-5	-36	-36	14	78	2	2	2	2
87.9	0.76	0.49	-0.47	1.57	-1.04	-130	-10	-10	46	6	-325	-32	76	7	7	7	7	7	7	7
89.3	0.75	0.49	-0.47	1.57	-1.52	-260	12	12	72	1	-580	24	104	1	-20	1	-20	1	1	1
89.2	0.82	0.49	-0.69	1.57	0.0	30	202	15	6	-33	-16	8	392	7	52	14	23	29	29	29
89.7	0.82	0.49	-0.69	1.57	1.01	204	-15	-15	-13	-1	430	33	-40	-41	53	-41	53	-2	-2	-2
89.7	0.82	0.49	-0.69	1.56	1.65	355	7	7	-26	7	628	-21	0	32	77	32	77	3	3	3
88.1	0.83	0.49	-0.70	1.57	-1.02	-206	-14	-14	64	8	-443	-44	123	-44	14	14	-44	14	0	0
88.2	0.83	0.49	-0.70	1.57	-1.74	-330	7	7	81	1	-656	25	145	25	-2	-2	-24	-24	1	1



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5

$\Omega$ rad/sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta}$ @ r = 22.3 in.			$M_{\beta}$ @ r = 13.15 in.			$M_{\beta}$ @ r = 3.3 in. ~ in.-lb					
						in.-lb			in.-lb			in.-lb					
						$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_{2c}}$	$M_{\beta_{2s}}$	$M_{\beta_{3c}}$
57.6	0.0	1.98	-0.03	0.23	0.0	34	0	0	54	0	0	-7	0	0	0	0	0
57.5	0.0	1.98	2.03	0.22	0.0	35	3	-10	56	5	-18	-4	7	-28	-2	-1	0
57.5	0.0	1.98	3.86	0.22	0.0	38	4	-22	59	7	-41	0	10	-62	-4	0	0
57.5	0.0	1.98	4.98	0.22	0.0	36	8	-33	60	13	-60	0	18	-90	-5	1	0
57.5	0.0	1.98	-1.85	0.23	0.0	35	-2	9	56	-3	18	-5	-5	27	0	0	0
57.5	0.0	1.98	-3.98	0.23	0.0	37	-6	23	59	-10	43	0	-14	64	-4	0	0
57.5	0.0	1.98	-6.12	0.23	0.0	38	-12	43	61	-20	79	2	-28	118	-5	-2	-1
57.5	0.0	3.84	0.03	0.23	0.0	42	0	0	67	0	0	10	1	-1	0	0	0
57.5	0.0	3.84	2.07	0.22	0.0	43	6	-18	68	10	-32	10	15	-50	-1	0	0
57.5	0.0	3.84	3.90	0.22	0.0	44	11	-32	70	19	-60	15	28	-90	-6	-4	0
57.5	0.0	3.94	4.75	0.22	0.0	45	12	-37	72	21	-69	18	30	-104	-8	0	0
57.6	0.0	3.94	-2.07	0.23	0.0	43	-6	15	67	-11	28	10	-16	42	0	0	0
57.5	0.0	3.94	-3.92	0.23	0.0	44	-11	28	69	-20	53	12	-28	79	-6	-5	0
57.5	0.0	3.94	-5.31	0.23	0.0	46	-15	47	75	-26	87	22	-38	130	-6	-6	0
57.4	0.0	5.90	-0.16	0.23	0.0	52	0	-1	82	0	-1	30	0	-3	0	-2	0
57.3	0.0	5.90	1.83	0.22	0.0	53	9	-21	84	16	-38	32	24	-58	0	-1	1
57.2	0.0	5.90	3.90	0.22	0.0	54	15	-38	86	32	-71	36	48	-108	-2	-3	0
57.2	0.0	5.90	4.70	0.22	0.0	54	18	-46	87	32	-85	37	49	-128	-5	-2	0
57.3	0.0	5.70	-2.07	0.22	0.0	52	-8	17	83	-14	33	31	-22	50	0	-1	0
57.2	0.0	5.70	-4.14	0.22	0.0	53	-14	36	85	-25	68	35	-39	103	-2	-2	0
57.2	0.0	5.90	-6.31	0.22	0.0	53	-22	53	87	-39	99	37	-57	148	-9	-9	0
57.5	0.0	3.99	-0.10	0.30	0.0	43	0	0	67	-1	-1	11	-2	-2	0	0	0
57.4	0.0	3.99	-0.11	2.37	0.0	43	-17	-6	67	-33	-11	11	-50	-17	1	0	0
57.3	0.0	3.99	-0.10	4.21	0.0	45	-31	-12	71	-59	-21	16	-89	-31	6	3	1
57.2	0.0	5.00	-0.09	6.24	0.0	47	-46	-17	76	-86	-29	24	-129	-42	6	7	0
57.1	0.0	5.00	-0.09	-1.56	0.0	43	13	4	67	25	9	11	38	13	1	0	0
57.3	0.0	3.99	-0.11	-3.62	0.0	44	20	12	70	56	21	15	84	29	5	3	0
57.4	0.0	3.99	-0.12	-2.59	0.0	44	23	8	69	43	15	12	65	20	1	2	0
88.0	0.0	0.02	-0.05	0.15	0.0	37	0	0	68	0	0	-3	0	0	-2	0	0
88.0	0.0	2.04	-0.05	0.14	0.0	41	1	0	73	2	0	2	2	0	-2	0	0
88.2	0.0	5.00	-0.04	0.13	0.0	51	2	-1	90	3	-1	22	4	-3	-1	0	0
88.3	0.0	5.96	-0.02	0.12	0.0	64	1	-4	113	2	-6	50	3	-10	0	0	-1
88.3	0.0	6.92	-0.01	0.12	0.0	71	4	-3	126	7	-5	66	11	-8	-1	-2	-1
89.0	0.0	0.01	-0.02	0.14	0.0	38	0	0	68	0	0	-2	0	-2	0	0	0
89.0	0.0	0.01	2.01	0.14	0.0	37	2	-8	65	4	-17	-6	6	-29	0	0	0
89.1	0.0	0.01	3.98	0.14	0.0	36	9	-32	64	15	-64	-7	21	-103	-1	0	1
89.0	0.0	0.01	4.89	0.14	0.0	35	12	-42	63	21	-86	-9	30	-139	-1	0	2
88.9	0.0	0.01	-2.21	0.15	0.0	37	-2	10	66	-3	22	-6	-4	35	-2	0	-1
88.9	0.0	0.01	-4.14	0.15	0.0	34	-13	31	64	-23	64	-8	-35	102	0	0	-3
88.5	0.0	0.01	-6.18	0.14	0.0	35	-23	54	63	-54	110	-9	-83	175	1	1	-3
88.3	0.0	2.00	-0.09	0.14	0.0	41	0	0	74	0	0	2	0	-1	-2	0	0
88.3	0.0	2.00	2.02	0.13	0.0	37	9	-14	72	18	-28	11	27	-46	-2	-3	1
88.6	0.0	2.00	3.84	0.13	0.0	42	15	-31	77	28	-63	14	42	-102	-4	0	1
88.5	0.0	2.00	4.87	0.13	0.0	43	24	-42	79	44	-85	14	67	-136	-5	-4	3
88.7	0.0	2.00	-2.23	0.14	0.0	41	-6	16	75	-11	33	5	-18	54	-2	0	0
88.6	0.0	2.00	-4.12	0.14	0.0	44	-14	34	80	-25	71	12	-37	113	-6	-3	-1
88.4	0.0	2.00	-6.17	0.13	0.0	45	-32	56	82	-60	115	14	-92	184	-3	-5	-2



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M\beta @ r = 22.3 \text{ in.}$				$M\beta @ r = 13.15 \text{ in.}$				$M\beta @ r = 3.3 \text{ in.} \sim \text{in.-lb}$					
						in.-lb		in.-lb		in.-lb		in.-lb		in.-lb		in.-lb		in.-lb	
						$M\beta_{1o}$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_{1o}$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_{1o}$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_{2o}$	$M\beta_{2c}$	$M\beta_{2s}$	$M\beta_{3o}$	$M\beta_{3c}$
89.5	0.0	4.00	-0.23	0.12	0.0	51	0	1	90	0	2	-2	2	-1	0	0			
89.5	0.0	3.99	1.77	0.12	0.0	52	16	-17	92	31	-35	50	-58	-1	0	1			
89.5	0.0	3.99	3.55	0.12	0.0	53	31	-35	95	60	-71	94	-115	-4	0	2			
89.5	0.0	3.99	4.72	0.12	0.0	55	36	-47	98	68	-97	106	-156	-8	0	1			
89.5	0.0	4.00	-2.24	0.13	0.0	52	-14	19	91	-27	41	-44	66	-2	0	-2			
89.5	0.0	4.00	-6.22	0.13	0.0	53	-28	38	95	-55	79	-87	125	-6	0	-5			
89.5	0.0	4.00	-5.97	0.13	0.0	56	-40	55	100	-77	116	-120	184	-1	-6	-6			
89.5	0.0	5.92	-0.19	0.12	0.0	64	0	-1	113	0	-2	49	0	0	0	0			
89.5	0.0	5.92	1.76	0.11	0.0	66	22	-20	114	44	-40	69	-65	-1	-2	1			
89.5	0.0	5.92	3.58	0.11	0.0	66	41	-38	116	81	-80	129	-128	-1	0	3			
89.5	0.0	3.92	4.70	0.11	0.0	57	47	-55	119	93	-112	146	-180	-4	0	4			
89.5	0.0	5.92	-2.24	0.12	0.0	63	-16	20	112	-33	45	-55	71	-2	-1	-3			
89.5	0.0	5.92	-4.13	0.13	0.0	64	-33	42	115	-63	89	-110	140	-3	-6	-7			
89.5	0.0	5.92	-6.03	0.14	0.0	56	-53	58	119	-107	123	-168	196	-2	-9	-9			
105.8	0.0	0.01	-0.01	0.14	0.0	38	0	0	78	0	0	0	-1	-1	0	0			
104.3	0.0	1.97	-0.01	0.14	0.0	41	0	0	84	1	0	2	-1	0	0	0			
104.3	0.0	3.93	0.0	0.12	0.0	52	2	-2	101	3	-2	20	6	-5	-2	0			
103.3	0.0	5.92	0.01	0.11	0.0	65	3	-2	125	6	-4	48	9	-7	-1	-3			
104.8	0.0	4.95	0.02	0.10	0.0	59	2	-2	114	4	-3	35	8	-8	0	-1			
105.3	0.0	0.0	0.02	0.12	0.0	39	0	0	79	0	0	0	0	-1	-3	0			
105.3	0.0	0.0	1.75	0.12	0.0	32	3	-7	72	6	-17	0	10	-30	0	2			
105.4	0.0	0.0	3.58	0.12	0.0	34	17	-26	73	33	-57	-4	52	-96	0	4			
105.4	0.0	0.0	4.77	0.07	0.0	35	27	-36	73	55	-79	-7	85	-132	0	6			
105.5	0.0	0.0	-2.24	0.09	0.0	36	-4	11	75	-7	26	-7	-10	43	-1	-1			
105.3	0.0	0.0	-4.23	0.09	0.0	36	-17	33	74	-34	74	-9	-52	120	1	0			
105.4	0.0	0.0	-6.29	0.10	0.0	36	-41	55	73	-84	121	-10	-123	202	2	0			
105.3	0.0	2.00	-0.08	0.25	0.0	43	0	0	85	0	0	3	0	-2	-1	0			
105.4	0.0	2.00	1.66	0.25	0.0	43	8	-12	85	17	-27	0	27	-47	0	0			
105.2	0.0	2.00	3.53	0.25	0.0	46	15	-27	89	30	-60	6	45	-100	-2	0			
105.2	0.0	2.00	4.82	0.25	0.0	48	29	-42	93	58	-92	11	88	-154	3	1			
105.4	0.0	2.00	-2.27	0.27	0.0	44	-10	16	87	-19	36	2	-31	61	-1	7			
105.4	0.0	2.00	-4.27	0.26	0.0	47	-23	34	92	-47	76	9	-71	126	-8	0			
105.2	0.0	2.00	-6.17	0.26	0.0	47	-43	55	94	-88	123	12	-131	206	-1	-3			
105.5	0.0	3.97	-0.07	0.24	0.0	53	0	-1	102	0	-2	21	0	-6	0	0			
105.6	0.0	3.97	1.75	0.24	0.0	53	17	-18	103	35	-39	21	58	-66	0	1			
105.5	0.0	3.97	3.54	0.24	0.0	55	35	-35	106	72	-78	24	116	-132	0	5			
105.7	0.0	3.97	4.66	0.24	0.0	56	44	-45	109	91	-100	28	141	-169	0	8			
105.7	0.0	3.97	-2.23	0.26	0.0	53	-16	17	103	-35	40	21	-58	66	1	-2			
105.7	0.0	3.97	-4.10	0.26	0.0	54	-33	36	105	-69	81	24	-110	133	-3	-3			
105.5	0.0	3.97	-6.13	0.26	0.0	57	-52	53	114	-110	119	35	-167	201	-4	-10			



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\frac{\Omega}{\text{rad/sec}}$	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta} @ r = 22.3 \text{ in.}$			$M_{\beta} @ r = 13.15 \text{ in.}$			$M_{\beta} @ r = 3.3 \text{ in.} \sim \text{in.-lb}$						
						in.-lb			in.-lb			in.-lb			in.-lb			
						$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_{2s}}$
57.6	0.41	0.0	0.03	0.78	0.0	15	-2	1	36	0	2	0	1	3	0	6	-4	0
57.8	0.41	2.10	0.03	0.78	0.0	30	17	-0	66	60	-22	44	70	-38	0	-9	2	0
57.8	0.41	7.06	0.03	0.78	0.0	45	40	-20	95	85	-47	87	145	-79	3	-24	6	0
57.5	0.41	6.15	0.03	0.78	0.0	60	64	-32	125	133	-73	133	223	-124	5	-37	8	3
57.5	0.41	7.21	0.03	0.78	0.0	68	78	-36	141	160	-83	157	267	-140	13	-44	3	0
57.8	0.40	0.68	-1.05	0.80	0.0	21	-5	2	45	-5	4	11	-4	7	5	6	-3	0
57.6	0.41	0.98	0.94	0.78	0.0	26	15	-11	57	35	-25	25	61	-42	-4	-6	-1	0
57.7	0.42	0.98	2.99	0.76	0.0	31	32	-31	67	59	-67	48	114	-112	-19	-13	-1	-1
57.7	0.42	0.98	5.03	0.78	0.0	36	54	-45	80	114	-96	68	188	-161	-24	-31	2	-3
57.5	0.40	0.68	-5.32	0.80	0.0	9	-48	37	19	-93	76	-30	-145	127	20	35	-7	0
57.5	0.40	0.68	-7.08	0.80	0.0	5	-67	49	9	-131	101	-46	-206	167	27	47	-9	0
57.7	0.41	0.68	-1.06	0.80	0.0	21	-3	2	44	-2	4	7	-1	9	-2	6	-2	-1
57.6	0.41	0.68	-1.06	2.51	0.0	19	-22	-9	43	-42	-19	8	-67	-31	-2	17	-3	-1
57.6	0.42	0.68	-1.06	4.38	0.0	18	-45	-24	41	-89	-50	6	-142	-82	-10	32	-4	0
57.6	0.42	0.68	-1.06	6.30	0.0	16	-66	-34	38	-132	-70	3	-213	-113	-11	45	-5	0
57.8	0.41	0.68	-1.06	-1.42	0.0	22	15	18	46	37	37	10	67	63	9	-5	-2	0
57.8	0.41	0.67	-1.06	-3.53	0.0	23	37	37	47	94	75	10	146	123	19	-16	-2	0
57.8	0.41	0.67	-1.06	-5.40	0.0	25	62	50	49	134	102	12	228	166	20	-30	-1	1
57.9	0.41	0.67	-1.06	0.74	0.0	20	-7	6	43	-9	12	7	-12	21	2	7	-2	-1
58.1	0.41	0.67	-1.06	0.74	2.06	26	1	4	57	10	5	5	22	20	7	1	-2	0
58.2	0.41	0.67	-1.06	0.74	4.22	34	11	2	74	30	-1	57	55	-4	6	-3	-2	0
58.0	0.41	0.67	-1.06	0.74	5.05	36	17	1	80	62	-4	67	75	-11	8	-5	-2	0
57.7	0.40	0.67	-1.06	0.74	-2.07	14	-10	4	31	-15	9	-10	-25	18	2	10	-4	1
57.7	0.40	0.67	-1.06	0.74	-3.11	11	-15	4	23	-18	12	-24	-44	24	-1	16	-4	0
57.6	0.57	0.01	0.06	1.08	0.0	16	-5	2	37	-5	3	1	-8	4	0	13	-5	0
57.8	0.57	2.09	0.03	1.08	0.0	32	28	-14	69	53	-35	50	108	-60	1	-10	-1	-1
57.9	0.56	4.14	0.06	1.08	0.0	49	64	-32	104	137	-77	104	233	-134	7	-36	3	0
57.9	0.56	5.94	0.06	1.08	0.0	55	78	-38	117	166	-93	125	281	-161	12	-44	4	0
57.9	0.56	3.13	0.06	1.08	0.0	41	44	-21	86	96	-53	76	163	-92	5	-23	0	0
57.8	0.56	1.15	0.80	0.85	0.0	29	29	-12	63	66	-31	40	112	-54	-2	-12	-1	-1
57.9	0.56	1.15	2.85	0.86	0.0	36	53	-29	78	115	-70	65	192	-121	-14	-28	0	-2
58.0	0.56	1.14	3.84	0.86	0.0	39	67	-36	87	145	-87	91	244	-151	-15	-38	1	-2
57.6	0.55	1.15	-3.40	0.86	0.0	13	-38	24	26	-74	51	-15	-116	85	16	35	-6	0
57.6	0.55	1.15	-5.58	0.86	0.0	5	-66	44	8	-131	96	-48	-210	162	29	54	-9	2
57.6	0.54	1.14	-1.31	0.86	0.0	21	-3	4	45	-2	7	10	-1	13	5	9	-4	0
57.5	0.56	1.15	-1.31	2.59	0.0	20	-25	-7	43	-47	-15	9	-74	-26	0	25	-5	0
57.5	0.56	1.15	-1.31	4.65	0.0	18	-52	-20	42	-103	-42	8	-167	-70	-8	46	-6	1
57.5	0.56	1.15	-1.31	5.49	0.0	18	-63	-25	41	-127	-52	7	-205	-86	-8	54	-7	2
57.5	0.56	1.15	-1.31	1.35	0.0	23	24	18	48	56	34	13	59	57	13	-10	-3	0
57.7	0.55	1.15	-1.31	-3.46	0.0	23	44	39	45	98	78	8	169	127	26	-24	-2	1
57.7	0.55	1.15	-1.31	-4.40	0.0	24	58	46	46	128	89	10	219	144	29	-35	-1	2
57.7	0.55	1.14	-1.30	1.08	0.0	21	-4	2	46	-4	3	12	-3	6	5	10	-4	0
57.9	0.56	1.14	-1.30	1.08	2.06	30	11	-1	64	30	-3	43	54	-17	11	0	-3	0
58.1	0.55	1.14	-1.30	1.08	4.22	39	26	-3	84	63	-19	75	110	-35	16	-5	-2	0
58.2	0.55	1.14	-1.30	1.08	5.05	41	33	-3	91	78	-21	88	136	-41	16	-7	-1	1
57.8	0.55	1.14	-1.30	1.08	-2.06	12	-22	7	26	-43	18	-18	-65	33	1	24	-6	0
57.8	0.55	1.14	-1.30	1.08	-3.11	8	-28	6	17	-55	23	-32	-89	43	-2	29	-6	-1



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_0$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_0$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta}$ @ r = 22.3 in. in.-lb			$M_{\beta}$ @ r = 13.15 in. in.-lb			$M_{\beta}$ @ r = 3.3 in. ~ in.-lb						
						$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_0}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_{2c}}$	$M_{\beta_{2s}}$	$M_{\beta_{3c}}$	$M_{\beta_{3s}}$
57.4	0.79	0.08	-0.37	0.99	0.0	16	-6	6	36	-2	12	0	-14	21	2	26	-9	0
57.6	0.79	1.09	-0.37	0.99	0.0	24	21	-3	55	50	-14	32	86	-25	12	0	-5	1
57.9	0.78	2.10	-0.37	0.99	0.0	33	48	-15	74	105	-41	61	181	-70	16	-19	-2	0
57.9	0.79	3.12	-0.37	0.99	0.0	42	72	-29	92	155	-74	53	265	-127	18	-41	1	2
57.4	0.79	1.78	-0.37	0.99	0.0	30	37	-13	67	83	-35	50	141	-59	9	-13	-3	0
57.2	0.79	0.56	-0.87	1.29	0.0	13	-10	6	36	-16	6	9	-24	15	5	27	-8	1
57.3	0.79	0.56	0.03	1.29	0.0	20	15	-5	51	38	-17	30	65	-29	3	11	-8	0
58.0	0.79	0.55	1.09	1.29	0.0	31	60	-19	75	133	-51	69	226	-90	4	-25	-2	0
57.6	0.79	0.55	-2.08	1.29	0.0	12	-38	18	25	-76	39	-22	-123	66	9	47	-10	4
57.5	0.79	0.55	-3.10	1.29	0.0	7	-62	30	13	-125	66	-42	-205	111	13	67	-13	4
57.7	0.79	0.55	-0.97	1.29	0.0	18	-6	5	40	-8	8	4	-13	13	13	20	-6	6
57.5	0.79	0.55	-0.97	2.38	0.0	18	-26	-1	39	-51	-4	0	-84	-8	-1	41	-10	1
57.5	0.80	0.55	-0.97	3.21	0.0	17	-52	-10	38	-105	-23	-2	-175	-39	-4	49	-11	2
57.5	0.79	0.55	-0.95	-0.53	0.0	19	19	19	41	45	34	3	78	58	16	-1	-5	0
57.6	0.79	0.55	-0.95	-2.79	0.0	19	44	34	40	98	68	2	171	115	33	-22	-2	0
57.7	0.79	0.55	-0.95	-3.87	0.0	19	60	45	40	133	89	5	225	148	45	-38	0	3
57.6	0.79	0.55	-0.95	1.13	0.0	18	-5	7	40	-7	12	3	-11	21	8	23	-8	2
57.9	0.79	0.55	-0.95	1.13	2.05	29	28	-3	67	64	-14	51	110	-21	19	-1	-5	2
58.3	0.78	0.55	-0.95	1.13	4.21	41	63	-10	100	140	-36	112	239	-61	36	-21	-1	3
57.7	0.79	0.55	-0.95	1.13	-2.05	7	-40	16	14	-81	38	-40	-135	64	-7	48	-12	0
57.9	0.79	0.55	-0.95	1.13	3.10	2	-56	22	0	-114	52	-65	-191	87	-13	59	-13	1
57.6	0.92	0.04	-0.25	1.35	0.0	17	-9	4	39	-15	8	3	-26	15	1	33	-10	1
57.7	0.92	0.99	-0.25	1.35	0.0	25	23	-8	59	55	-23	39	96	-37	11	1	-6	2
58.0	0.92	2.15	-0.25	1.34	0.0	35	59	-21	83	131	-54	80	225	-91	21	-28	-2	4
58.0	0.92	1.71	-0.25	1.35	0.0	31	47	-14	74	106	-38	65	182	-64	18	-12	-4	2
57.8	0.92	0.55	-0.78	1.35	0.0	18	-5	5	42	-5	7	9	-9	12	14	26	-9	4
58.0	0.92	0.55	0.15	1.35	0.0	24	23	-9	58	55	-25	38	94	-40	5	0	-7	1
57.9	0.92	0.55	1.46	1.35	0.0	31	57	-21	77	125	-53	73	213	-88	3	-22	-4	0
57.6	0.92	0.55	-1.82	1.35	0.0	13	-33	17	29	-63	33	-14	-103	54	11	47	-11	4
57.6	0.93	0.55	-0.81	2.10	0.0	19	-14	-1	44	-24	-8	10	-39	-15	2	34	-10	3
57.5	0.93	0.55	-0.81	3.03	0.0	19	-32	-7	41	-53	-19	6	-106	-34	-5	49	-13	2
57.5	0.93	0.55	-0.81	4.00	0.0	18	-46	-14	40	-93	-32	1	-156	-55	-12	63	-14	4
57.6	0.92	0.55	-0.78	0.13	0.0	19	15	11	45	38	20	14	65	37	17	5	-6	2
57.5	0.92	0.55	-0.78	-0.80	0.0	19	25	19	45	59	36	15	101	61	26	-4	-5	3
57.5	0.92	0.55	-0.78	-2.83	0.0	20	53	34	45	118	69	17	205	117	42	-32	-2	5
57.5	0.93	0.55	-0.78	1.44	0.0	18	-7	4	42	-11	5	7	-18	9	9	29	-9	3
57.9	0.92	0.55	-0.78	1.44	2.05	32	39	-11	80	89	-26	78	155	-42	27	-9	-5	6
58.2	0.91	0.55	-0.78	1.44	3.16	41	67	-11	104	149	-36	122	258	-59	38	-24	-2	5
57.5	0.92	0.55	-0.78	1.44	-2.05	7	-50	16	10	-101	36	-50	-170	56	-5	61	-14	3
57.7	0.92	0.55	-0.78	1.44	-3.12	0	-70	22	-8	-145	50	-84	-246	80	-9	76	-16	5
88.9	0.27	-0.03	0.15	0.44	0.05	20	-5	1	52	-3	4	-8	-3	6	-2	2	-3	0
88.9	0.27	2.07	0.17	0.44	0.06	34	15	1	94	37	0	38	67	0	1	-3	0	1
88.8	0.27	4.01	0.17	0.44	0.06	50	35	-1	117	79	-9	74	146	-16	-14	-6	-3	4
88.9	0.27	6.17	0.17	0.44	0.07	68	57	0	157	125	-11	150	218	-24	8	-13	2	4
88.7	0.27	7.16	0.17	0.44	0.07	77	68	2	175	150	-6	177	260	-17	12	-15	2	4



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING-RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\Omega$ rad sec	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M\beta @ r = 22.3 \text{ in.}$			$M\beta @ r = 13.15 \text{ in.}$			$M\beta @ r = 3.3 \text{ in.} \sim \text{in.-lb}$						
						in.-lb			in.-lb			in.-lb						
						$M\beta_o$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_o$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_o$	$M\beta_{1c}$	$M\beta_{1s}$	$M\beta_{2c}$	$M\beta_{2s}$	$M\beta_{3c}$	$M\beta_{3s}$
88.8	0.26	1.04	-0.54	0.73	0.06	27	-5	0	66	-7	0	17	-9	1	-1	2	0	0
88.9	0.27	1.04	1.49	0.73	0.07	31	17	-9	76	44	-23	28	77	-41	-3	-3	1	1
88.9	0.27	1.04	3.59	0.73	0.06	34	42	-22	84	97	-51	47	170	-89	-5	-12	3	3
88.9	0.26	1.04	5.66	0.73	0.07	37	61	-28	91	140	-66	58	246	-120	-6	-18	4	4
88.7	0.26	1.04	-2.70	0.74	0.05	22	-34	9	55	-70	20	3	-117	38	0	10	-3	-1
88.8	0.26	1.04	-4.88	0.74	0.04	18	-63	19	45	-133	44	-14	-224	80	0	18	-3	-4
88.7	0.27	1.04	-0.67	0.73	0.06	26	-3	2	65	-3	4	16	-3	8	0	1	0	1
88.7	0.27	1.04	-0.67	2.78	0.05	24	-26	-22	63	-56	-50	12	-96	-87	-4	1	0	0
88.8	0.27	1.04	-0.67	4.70	0.05	21	-46	-43	59	-103	-100	12	-179	-175	-8	2	0	-2
89.0	0.26	1.04	-0.67	-1.34	0.07	29	10	17	49	31	39	18	58	70	1	0	-1	0
89.0	0.26	1.04	-0.67	-3.25	0.07	30	24	42	71	65	57	20	123	169	8	0	-2	3
88.9	0.26	1.04	-0.67	-4.78	0.07	32	41	60	72	104	136	21	194	236	8	0	0	3
89.0	0.27	1.11	-1.36	0.13	2.10	34	0	6	96	4	11	41	11	16	3	2	0	0
89.1	0.27	1.11	-1.36	0.13	4.26	39	5	9	100	17	14	63	35	19	1	0	1	1
89.3	0.26	1.10	-1.35	0.13	5.10	41	6	10	105	20	17	71	40	24	4	0	0	0
88.9	0.27	1.10	-1.35	0.13	-2.06	28	-6	0	65	-9	0	6	-12	0	2	3	-1	2
88.8	0.27	1.10	-1.35	0.13	-3.07	25	-11	0	59	-19	1	-2	-29	3	0	4	-2	0
89.1	0.36	-	-0.56	0.28	0.04	24	-5	2	60	-3	1	3	2	2	-1	4	-2	0
89.1	0.36	2.06	-0.56	0.31	0.05	42	21	-2	102	58	-13	63	113	-25	5	-4	1	0
89.2	0.36	4.07	-0.56	0.31	0.05	59	50	-4	141	122	-23	121	228	-47	13	-12	2	5
89.0	0.36	1.24	-1.90	0.31	0.04	31	-9	4	76	-11	7	25	-11	7	5	4	0	1
89.2	0.36	1.24	0.39	0.31	0.05	37	22	-7	92	60	-21	50	116	-41	1	-6	1	1
89.5	0.36	1.24	2.48	0.31	0.05	42	46	-19	106	114	-51	73	213	-95	0	-14	4	1
89.2	0.36	1.24	-3.76	0.31	0.03	26	-41	16	61	-84	35	0	-138	57	6	17	-3	0
89.2	0.35	1.24	-6.23	0.30	0.04	20	-70	28	46	-151	65	-24	-256	114	11	28	-5	-1
89.4	0.36	1.24	-1.67	0.31	0.05	32	-7	4	77	-7	6	25	-5	7	4	4	0	1
89.2	0.36	1.24	-1.67	2.10	0.04	29	-27	-17	73	-57	-41	22	-90	-76	1	10	-1	0
89.2	0.36	1.24	-1.67	4.14	0.04	27	-47	-39	68	-104	-94	16	-174	-171	-5	14	-2	0
89.2	0.36	1.24	-1.67	-1.85	0.05	34	15	26	92	46	56	22	92	98	8	0	-1	0
89.4	0.36	1.24	-1.66	-4.26	0.05	36	36	58	85	98	129	35	187	222	18	-3	-1	3
89.3	0.36	1.24	-1.66	0.43	0.04	32	-6	4	78	-5	5	27	-1	5	6	1	0	0
89.3	0.36	1.24	-1.66	0.43	2.10	38	0	5	94	12	5	54	33	4	4	1	0	0
89.7	0.36	1.24	-1.66	0.44	4.26	44	6	9	111	28	9	83	64	8	8	0	0	0
90.0	0.36	1.24	-1.66	0.43	5.09	46	12	9	119	42	6	95	89	0	7	-1	0	0
88.9	0.36	1.24	-1.66	0.43	-1.98	26	-14	0	62	-27	0	1	-36	2	2	8	-1	0
88.8	0.36	1.24	-1.66	0.43	-3.07	23	-16	0	52	-30	0	-11	-49	2	-1	9	-2	0
89.0	0.51	0.02	-0.89	0.41	0.04	24	-8	5	61	-7	7	4	-6	10	1	11	-4	0
89.1	0.51	0.05	-0.89	0.41	0.05	33	12	3	82	41	-4	35	83	-14	6	1	-1	0
89.1	0.51	2.05	-0.89	0.41	0.05	42	31	0	103	87	-16	67	169	-36	12	-5	0	0
89.1	0.51	3.14	-0.89	0.43	0.04	51	52	-2	125	136	-31	100	259	-67	20	-12	1	2
88.6	0.51	-	-0.87	0.43	0.04	15	-26	7	40	-52	18	-25	-86	30	-5	20	-6	0
88.7	0.51	0.13	-1.20	0.67	0.04	26	-8	3	66	-6	2	11	-2	0	3	10	-3	0
88.9	0.51	0.43	-0.70	0.67	0.04	30	9	-1	76	34	-14	28	70	-31	2	3	-1	0
89.0	0.51	0.43	0.84	0.67	0.05	33	26	-5	86	75	-27	45	146	-55	2	-3	0	-2
89.2	0.51	0.43	1.77	0.66	0.05	37	45	-10	96	121	-42	61	229	-84	2	-11	1	-1
88.7	0.51	0.43	-2.21	0.67	0.04	21	-29	9	54	-57	19	-7	-93	31	5	18	-4	3
88.6	0.50	0.43	-3.43	0.67	0.04	17	-53	13	41	-114	34	-28	-195	61	6	29	-5	3



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\frac{\Omega}{\text{rad}} / \text{sec}$	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta} @ r = 22.3 \text{ in.}$				$M_{\beta} @ r = 13.15 \text{ in.}$				$M_{\beta} @ r = 3.3 \text{ in.} \sim \text{in.-lb}$					
						in.-lb		in.-lb		in.-lb		in.-lb		in.-lb		in.-lb		in.-lb	
						$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_{2c}}$	$M_{\beta_{2s}}$
89.3	0.50	0.43	-3.86	0.57	0.04	15	-61	12	36	-135	37	-38	-234	68	0	33	-7	3	
89.5	0.50	0.43	-1.25	0.47	0.05	26	-7	3	66	-5	1	11	0	0	3	9	-2	2	
89.3	0.51	0.43	-1.25	1.51	0.04	25	-16	-6	64	-27	-23	11	-39	-40	0	14	-4	1	
89.4	0.51	0.43	-1.25	2.50	0.02	24	-27	-18	62	-56	-43	6	-92	-80	-3	19	-3	3	
89.3	0.51	0.43	-1.25	3.30	0.03	23	-37	-25	60	-91	-58	3	-137	-104	-6	23	-3	4	
89.5	0.50	0.43	-1.39	1.39	0.05	28	10	25	69	39	49	16	80	83	3	-1	-1	-1	
89.5	0.50	0.43	-1.24	-3.44	0.05	30	28	50	72	85	105	17	165	179	22	-1	-1	0	
89.4	0.50	0.43	-1.24	0.62	0.03	21	-9	4	61	-10	5	16	-10	5	2	10	-2	1	
89.7	0.50	0.43	-1.22	0.62	2.09	33	6	8	83	35	6	51	66	2	9	14	13	2	
90.2	0.50	0.42	-1.23	0.62	4.25	42	23	13	112	76	3	51	154	-11	18	1	-1	0	
89.5	0.50	0.42	-1.23	0.63	5.08	45	31	14	121	95	1	107	188	-15	22	1	0	1	
88.2	0.51	0.42	-1.24	0.63	-2.01	18	-22	0	44	-46	6	-22	-77	13	-1	17	-4	2	
88.2	0.51	0.42	-1.24	0.63	-3.06	13	-32	0	32	-69	7	-35	-123	11	-5	20	-7	2	
85.0	0.50	-0.01	-0.98	0.58	0.05	24	-10	6	59	-11	9	2	-12	13	2	15	-2	0	
89.2	0.61	1.01	-0.98	0.58	0.05	32	13	5	81	48	-3	36	98	-13	14	5	0	0	
89.4	0.60	2.10	-0.98	0.58	0.05	43	40	2	106	115	-17	75	223	-41	25	-6	4	0	
89.3	0.60	2.44	-0.98	0.58	0.05	47	51	-1	114	138	-30	87	264	-65	28	-12	3	0	
88.9	0.61	0.46	-0.98	0.57	0.05	28	2	5	70	21	2	20	48	0	11	8	-2	1	
89.3	0.60	0.46	-1.51	0.73	0.05	26	-11	5	64	-13	7	9	-14	8	5	15	-2	1	
89.5	0.60	0.46	-0.51	0.73	0.05	31	9	0	75	36	-9	33	74	-8	24	6	0	0	
89.7	0.60	0.46	0.48	0.73	0.05	34	30	-2	87	90	-25	49	175	-52	8	-1	0	0	
90.0	0.60	0.46	1.39	0.73	0.05	38	52	-6	100	144	-40	71	274	-83	11	-10	2	-1	
89.3	0.61	0.46	-2.18	0.73	0.05	23	-26	7	55	-49	16	-5	-80	25	4	21	-4	2	
89.3	0.60	0.46	-3.50	0.73	0.05	16	-61	15	37	-132	43	-36	-229	76	5	35	-6	5	
89.5	0.61	0.46	-1.47	0.73	0.05	25	-11	8	63	-13	11	12	-15	14	12	12	-2	2	
89.3	0.61	0.46	-1.67	1.74	0.04	25	-22	-6	62	-61	-19	24	-61	-37	-1	21	-3	1	
89.5	0.61	0.46	-1.47	2.65	0.05	23	-36	-15	58	-76	-35	14	-130	-69	-2	32	-3	2	
88.0	0.60	0.46	-1.47	1.22	0.05	28	9	26	68	40	48	49	86	81	10	18	-1	0	
89.3	0.60	0.46	-1.47	-3.15	0.05	30	30	51	71	93	103	21	185	174	31	-2	1	0	
88.0	0.61	0.47	-1.46	1.60	0.02	26	-6	5	65	-1	6	7	6	10	7	17	-3	2	
88.7	0.61	0.47	-1.44	1.61	2.08	36	19	8	92	64	-1	58	142	-10	21	6	3	0	
89.0	0.61	0.46	-1.44	1.62	3.54	41	39	11	112	113	-6	100	244	-27	38	0	4	1	
89.1	0.61	0.46	-1.45	1.62	-2.03	16	-31	3	84	-65	14	-40	-126	34	-6	27	-11	5	
89.3	0.61	0.46	-1.46	1.62	-3.08	10	-44	3	24	-98	20	-67	-196	49	-17	33	-12	5	
88.8	0.72	0.02	-1.28	1.68	0.03	22	-6	9	58	-5	10	0	-4	19	20	16	-3	6	
89.0	0.72	1.04	-1.28	1.68	0.03	31	21	6	81	66	-3	29	145	-13	25	11	0	-1	
89.1	0.72	1.50	-1.28	1.68	0.03	36	37	3	93	104	-13	60	225	-31	32	3	5	0	
88.8	0.72	0.22	-1.28	1.68	0.03	27	6	6	69	27	2	18	65	2	17	16	-2	0	
88.7	0.72	-1.09	-1.29	1.69	0.02	11	-45	12	32	-98	31	-46	-193	64	-12	45	-19	6	
89.0	0.72	0.03	-0.12	1.68	0.02	22	-8	7	58	-8	9	-1	-11	19	4	26	-6	1	
89.2	0.71	0.03	-0.12	1.68	0.03	27	22	4	74	68	-8	33	146	-24	16	13	-4	-2	
88.6	0.72	0.03	-2.26	1.70	0.02	17	-42	0	87	120	-22	57	254	-51	19	6	2	-8	
88.6	0.72	0.03	-2.70	1.70	0.03	13	-56	15	35	-124	37	-46	-243	77	0	49	-16	11	
88.8	0.72	0.03	-1.31	1.72	0.03	22	-12	8	56	-18	12	-7	-30	23	5	27	-5	0	
88.9	0.72	0.03	-1.31	2.78	0.03	21	-26	-3	55	-52	-11	-7	-100	-25	36	-9	3	3	
88.9	0.72	0.03	-1.31	3.69	0.02	19	-40	-12	52	-87	-29	-13	-172	-60	-10	45	-14	5	



TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\frac{\Omega}{\text{rad}} / \text{sec}$	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta} @ r = 22.3 \text{ in.}$			$M_{\beta} @ r = 13.15 \text{ in.}$			$M_{\beta} @ r = 3.3 \text{ in.} \sim \text{in.-lb}$					
						in.-lb			in.-lb			in.-lb					
						$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_o}$	$M_{\beta_{1c}}$	$M_{\beta_{1s}}$	$M_{\beta_{2c}}$	$M_{\beta_{2s}}$	$M_{\beta_{3c}}$
89.0	0.71	0.03	-1.31	0.78	0.03	23	0	17	58	12	33	33	65	12	21	-4	-1
89.0	0.71	0.03	-1.31	-0.30	0.03	24	15	28	63	52	52	7	119	99	23	13	-1
88.9	0.71	0.03	-1.31	-1.74	0.03	24	29	43	61	87	86	5	196	159	39	-2	0
88.7	0.72	0.03	-1.31	1.85	0.02	21	-12	6	57	-18	10	-3	-29	18	4	27	-7
89.3	0.71	0.03	-1.31	1.86	2.07	30	21	12	87	69	4	60	152	-1	35	16	2
89.6	0.71	0.03	-1.31	1.86	3.09	36	40	12	105	116	-2	97	250	-15	45	8	-1
89.0	0.72	0.03	-1.31	1.84	-2.03	11	-50	5	26	-114	21	-63	-228	45	-20	43	10
88.8	0.72	0.03	-1.31	1.85	-0.99	17	-30	5	43	-64	14	-31	-125	33	-5	34	6
89.4	0.75	-0.04	0.29	2.17	0.0	18	-8	12	43	-8	20	-11	-7	30	1	19	0
89.6	0.75	0.44	0.29	2.17	0.0	24	11	9	58	41	9	10	82	11	9	11	-2
89.9	0.75	0.99	0.29	2.17	0.0	29	30	10	72	88	3	33	170	-2	18	5	0
90.3	0.75	1.45	0.29	2.17	0.0	34	42	6	82	117	-5	47	222	-15	22	0	0
89.8	0.75	-0.52	0.28	2.17	0.0	15	-24	12	33	-48	27	-28	-80	45	-6	28	0
90.0	0.75	-1.12	0.28	2.17	0.0	10	-41	13	21	-90	34	-47	-156	61	-13	34	2
88.9	0.75	0.51	-0.59	1.46	0.0	23	-2	6	51	5	6	0	18	7	18	5	1
89.3	0.75	0.51	0.42	1.46	0.0	27	27	2	67	79	-11	28	153	-25	13	7	0
89.0	0.75	0.51	-1.06	1.46	0.0	19	-19	10	43	-34	18	-14	-50	26	1	25	-1
89.0	0.75	0.51	-1.69	1.46	0.0	19	-35	7	36	-74	19	-28	-125	34	-6	31	2
89.1	0.75	0.51	-2.18	1.46	0.0	15	-53	12	28	-116	33	-41	-200	57	-4	38	5
89.1	0.75	0.51	-0.51	1.62	0.0	22	-5	5	50	-2	3	-1	3	1	2	20	-5
89.1	0.75	0.51	-0.51	2.68	0.0	21	-17	-3	49	-30	-16	-2	-46	-33	-3	26	0
89.1	0.75	0.51	-0.51	3.33	0.0	21	-26	-9	47	-53	-29	-7	-86	-55	-9	29	1
89.3	0.75	0.51	-0.51	0.67	0.0	23	10	18	54	40	29	7	81	47	14	12	-4
89.6	0.74	0.51	-0.51	-0.52	0.0	24	23	25	56	71	43	11	138	72	18	5	0
89.3	0.74	0.51	-0.51	-1.33	0.0	26	27	36	57	83	71	9	161	123	26	5	-1
89.2	0.74	0.51	-0.51	-1.33	0.0	25	28	34	56	83	67	7	163	112	25	2	0
89.0	0.81	0.06	-0.13	1.72	0.0	21	-9	4	47	-12	1	-5	-15	1	0	25	-8
89.2	0.81	0.58	-0.14	1.72	0.0	26	12	2	62	43	-9	17	86	-19	10	15	0
89.4	0.80	1.13	-0.14	1.73	0.0	30	30	2	75	89	-15	41	173	-34	21	7	0
89.0	0.81	-0.45	-0.14	1.73	0.0	17	-27	4	35	-57	8	-26	-98	14	-11	30	-1
89.1	0.81	-1.06	-0.14	1.72	0.0	10	-54	8	19	-122	25	-51	-217	47	-19	45	4
89.1	0.81	0.51	-0.65	1.74	0.0	23	-9	4	50	-11	2	-3	-11	2	4	21	-7
89.3	0.81	0.51	-0.12	1.73	0.0	25	11	2	60	42	-10	18	86	-22	12	16	0
89.5	0.81	0.51	0.40	1.72	0.0	27	26	2	68	75	-25	33	146	-51	17	4	-3
89.6	0.81	0.51	0.83	1.72	0.0	29	45	0	78	125	-24	54	238	-48	19	4	0
88.7	0.82	0.51	-1.25	1.72	0.0	20	-26	7	41	-54	13	-18	-90	21	-1	33	-11
89.0	0.81	0.51	-1.77	1.73	0.0	18	-46	10	31	-101	29	-35	-179	46	-6	39	5
89.1	0.81	0.51	-2.24	1.73	0.0	21	-57	11	38	-129	27	-58	-242	45	-14	42	-16
89.1	0.81	0.51	-0.59	1.72	0.0	23	-3	3	52	3	0	2	14	-2	5	22	-7
89.1	0.81	0.51	-0.59	2.24	0.0	23	-8	0	52	-10	-10	0	-9	-22	-2	23	0
89.1	0.81	0.51	-0.59	3.39	0.0	22	-23	-9	49	-48	-29	-3	-78	-55	-6	30	-11
89.3	0.81	0.51	-0.59	0.56	0.0	24	16	20	57	55	32	14	111	54	19	13	-2
89.4	0.81	0.51	-0.59	-0.37	0.0	24	24	25	58	75	46	15	146	78	25	7	-1
89.1	0.82	0.51	-0.59	-1.19	0.0	26	29	31	58	85	66	12	165	119	23	7	-2





TABLE V  
 HARMONIC CONTENT OF THE BLADE FLAPPING RESPONSE TO  $\theta_o$ ,  $\theta_s$ ,  $\theta_c$  AND  $\alpha$  AT THREE RADIAL POSITIONS, CONFIGURATION 5 (Continued)

$\frac{\Omega}{\text{rad}} \frac{\text{sec}}{\text{sec}}$	$\mu$	$\theta_o$ deg	$\theta_s$ deg	$\theta_c$ deg	$\alpha$ deg	$M_{\beta} @ r = 22.3 \text{ in.}$			$M_{\beta} @ r = 13.15 \text{ in.}$			$M_{\beta} @ r = 3.3 \text{ in.} \sim \text{in.-lb}$						
						$M_{\beta_o}$	$M_{\beta_{lc}}$	$M_{\beta_{ls}}$	$M_{\beta_o}$	$M_{\beta_{lc}}$	$M_{\beta_{ls}}$	$M_{\beta_c}$	$M_{\beta_{lc}}$	$M_{\beta_{ls}}$	$M_{\beta_{2c}}$	$M_{\beta_{2s}}$	$M_{\beta_{3c}}$	$M_{\beta_{3s}}$
89.1	0.76	0.49	-0.47	1.56	0.0	23	1	7	53	16	6	9	38	6	8	18	-5	0
89.4	0.75	0.49	-0.47	1.56	1.05	29	25	10	72	77	1	45	150	-4	22	10	-2	0
89.0	0.75	0.48	-0.47	1.56	1.97	33	42	11	88	121	2	75	231	-3	28	7	2	-1
87.9	0.76	0.49	-0.47	1.57	-1.04	19	-22	6	37	-43	13	-20	-72	21	-7	26	-10	1
89.3	0.75	0.49	-0.47	1.57	-1.92	14	-36	4	23	-81	17	-45	-145	30	-18	28	-13	2
89.2	0.82	0.49	-0.69	1.57	0.0	23	-1	9	51	8	10	7	24	15	10	19	-5	0
89.7	0.82	0.49	-0.69	1.57	1.01	28	24	6	71	72	-2	44	140	-9	25	4	-1	-1
89.7	0.82	0.49	-0.69	1.56	1.65	29	33	12	81	100	6	68	194	5	36	9	1	-1
88.1	0.83	0.49	-0.70	1.57	-1.02	18	-29	9	34	-61	19	-25	-104	30	-7	32	-13	2
98.2	0.83	0.49	-0.70	1.57	-1.74	15	-42	7	22	-95	21	-48	-167	36	-17	35	-17	6



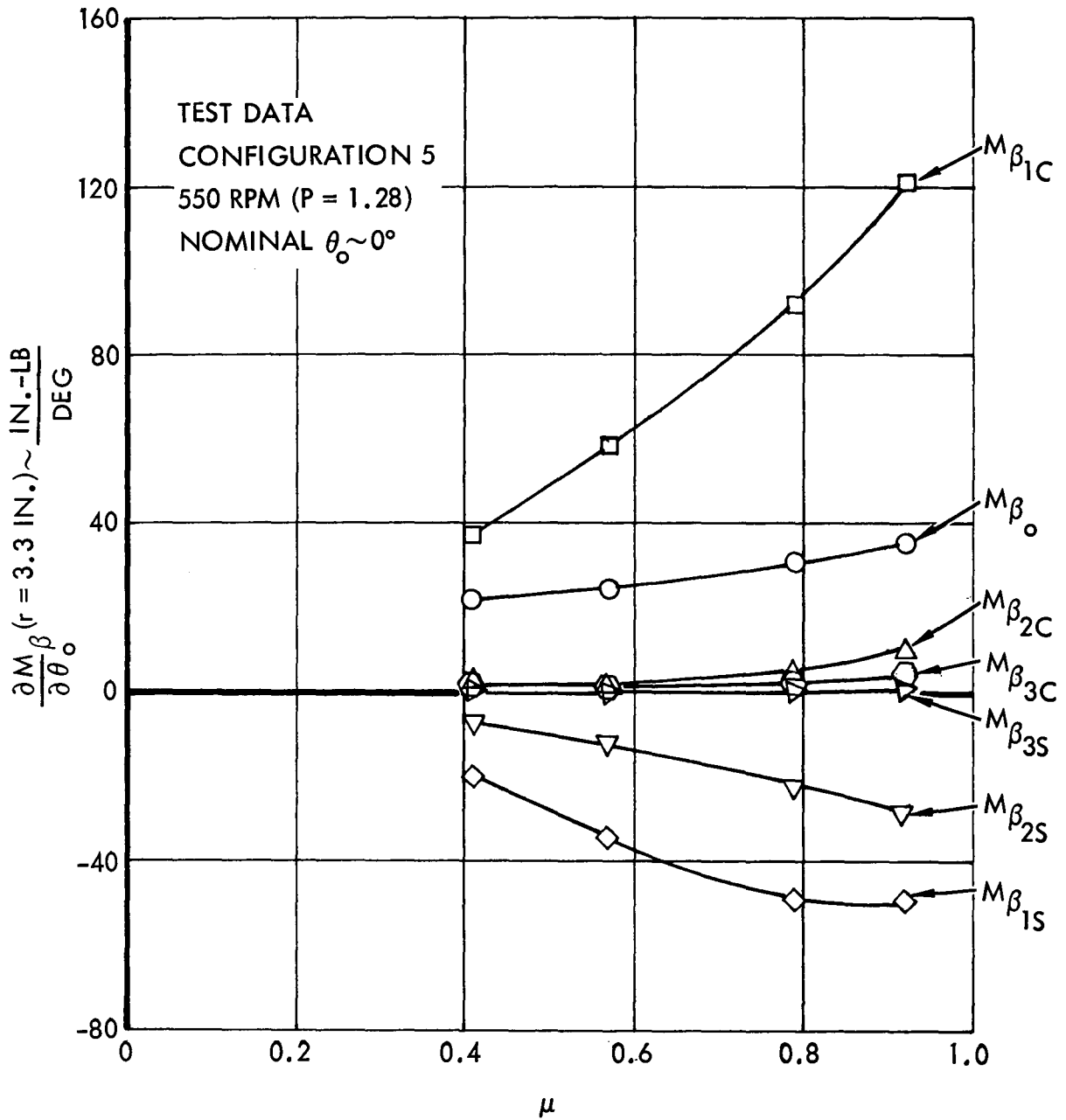


Figure A1. Harmonic Content of Blade Flapping, Configuration 5, 550 RPM (P = 1.28), Steady  $\theta_0$  Excitation

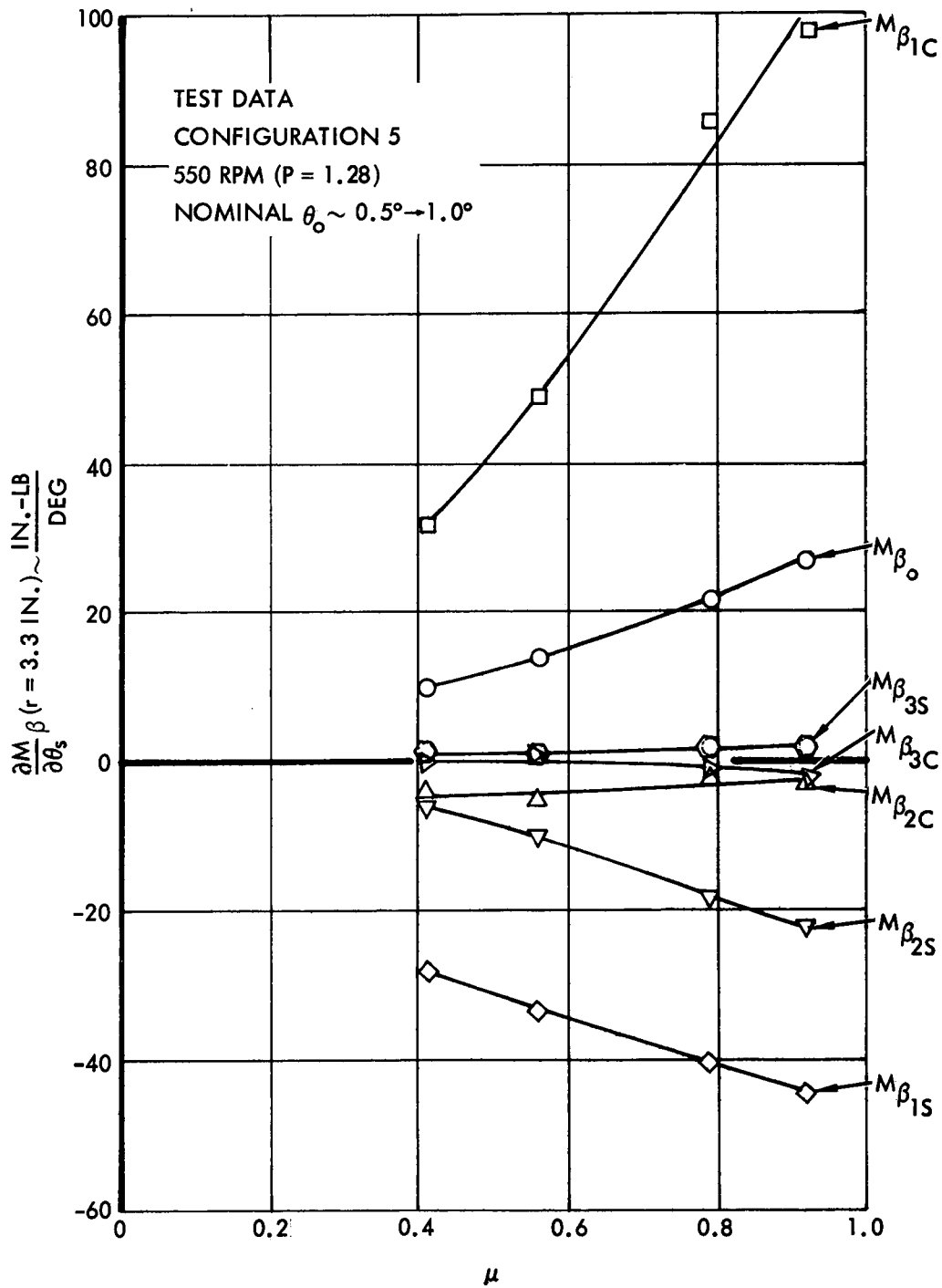


Figure A2. Harmonic Content of Blade Flapping, Configuration 5, 550 RPM (P = 1.28), Steady  $\theta_s$  Excitation



TEST DATA  
 CONFIGURATION 5  
 550 RPM (P = 1.28)  
 NOMINAL  $\theta_o \sim 0.5^\circ \rightarrow 1.0^\circ$

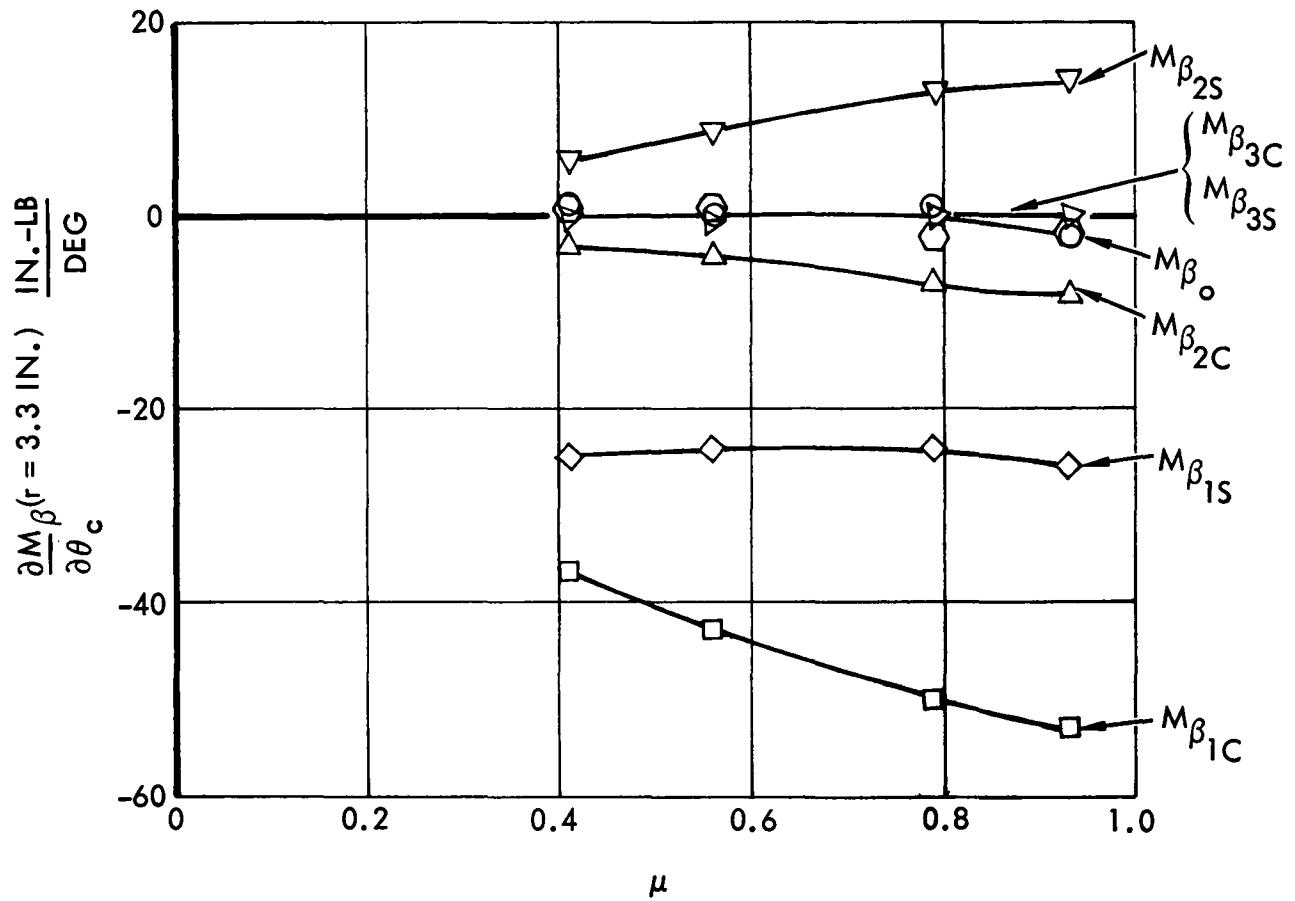


Figure A3. Harmonic Content of Blade Flapping, Configuration 5, 550 RPM (P = 1.28), Steady  $\theta_c$  Excitation

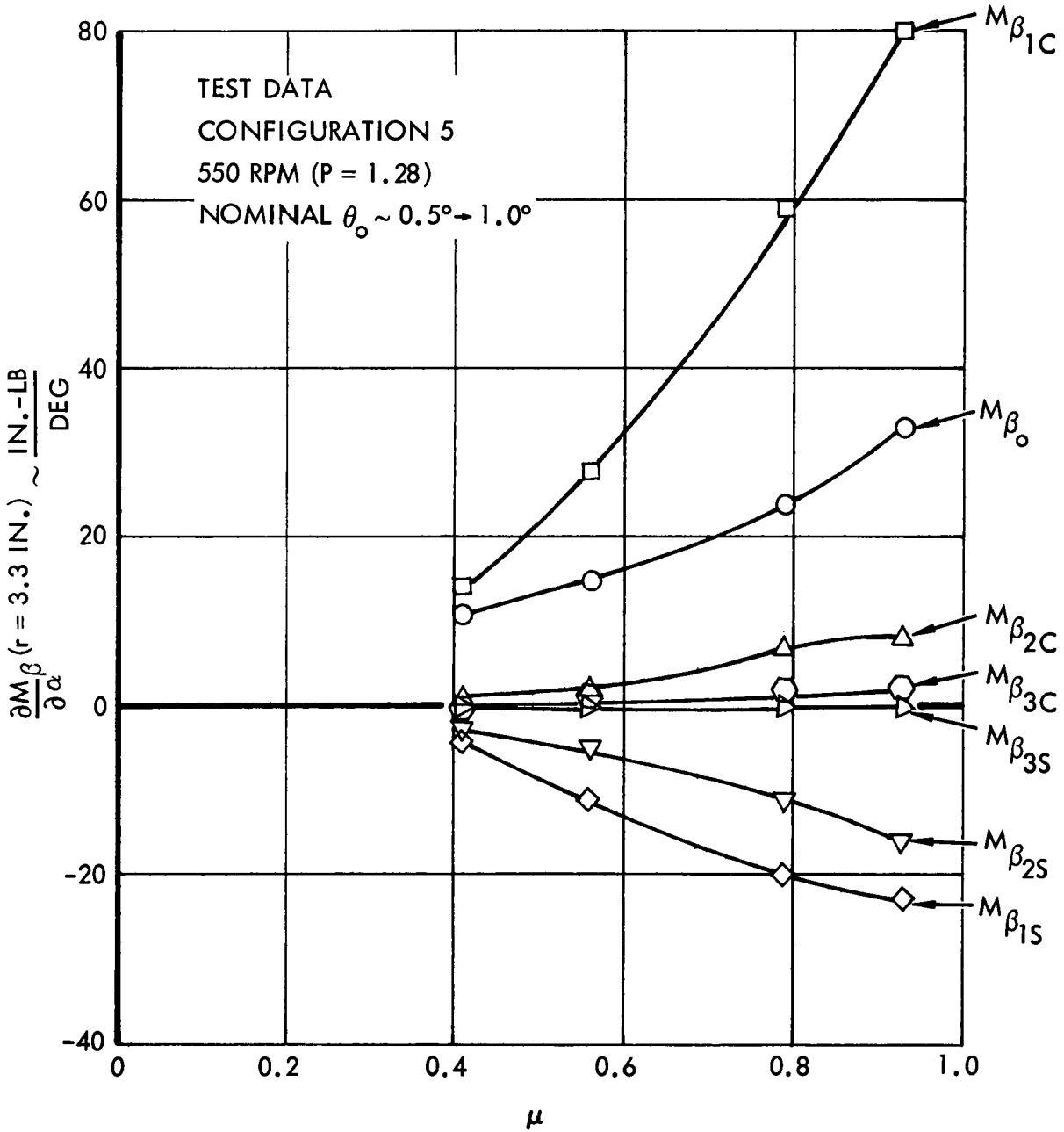


Figure A4. Harmonic Content of Blade Flapping, Configuration 5, 550 RPM (P = 1.28), Steady  $\alpha$  Excitation

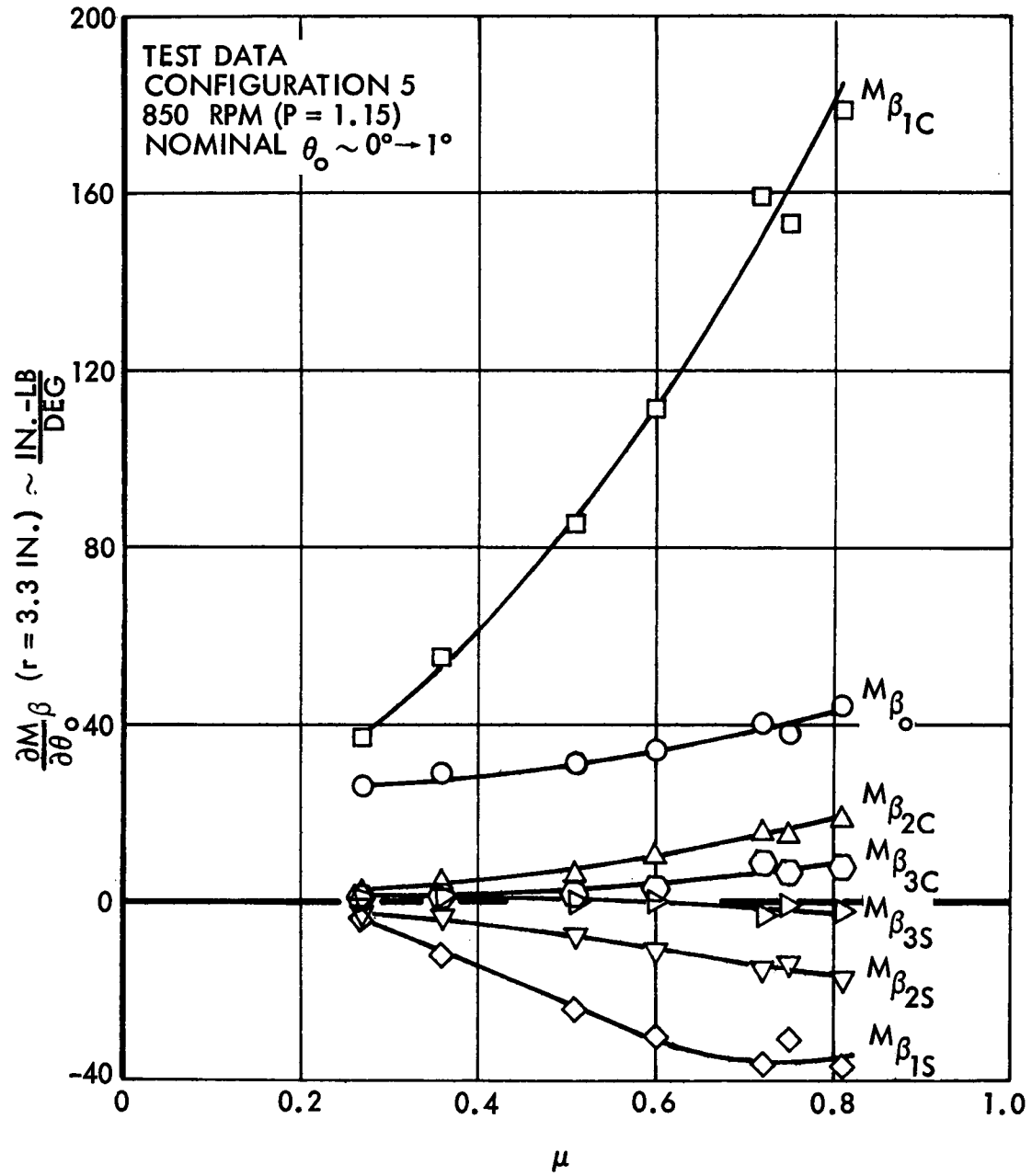


Figure A5. Harmonic Content of Blade Flapping, Configuration 5, 550 RPM (P = 1.15), Steady  $\theta_0$  Excitation

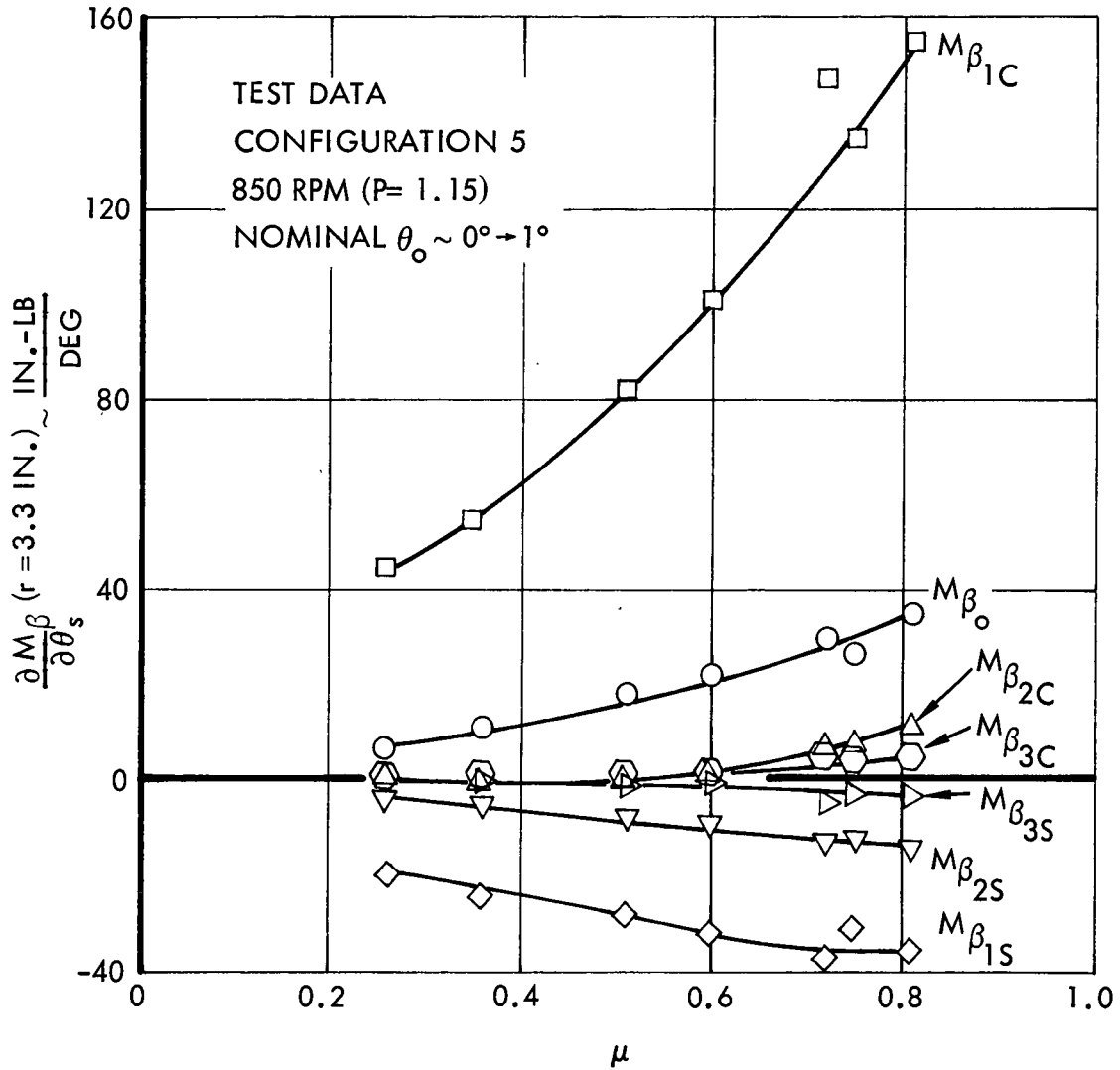


Figure A6. Harmonic Content of Blade Flapping, Configuration 5, 850 RPM (P = 1.15), Steady  $\theta_s$  Excitation

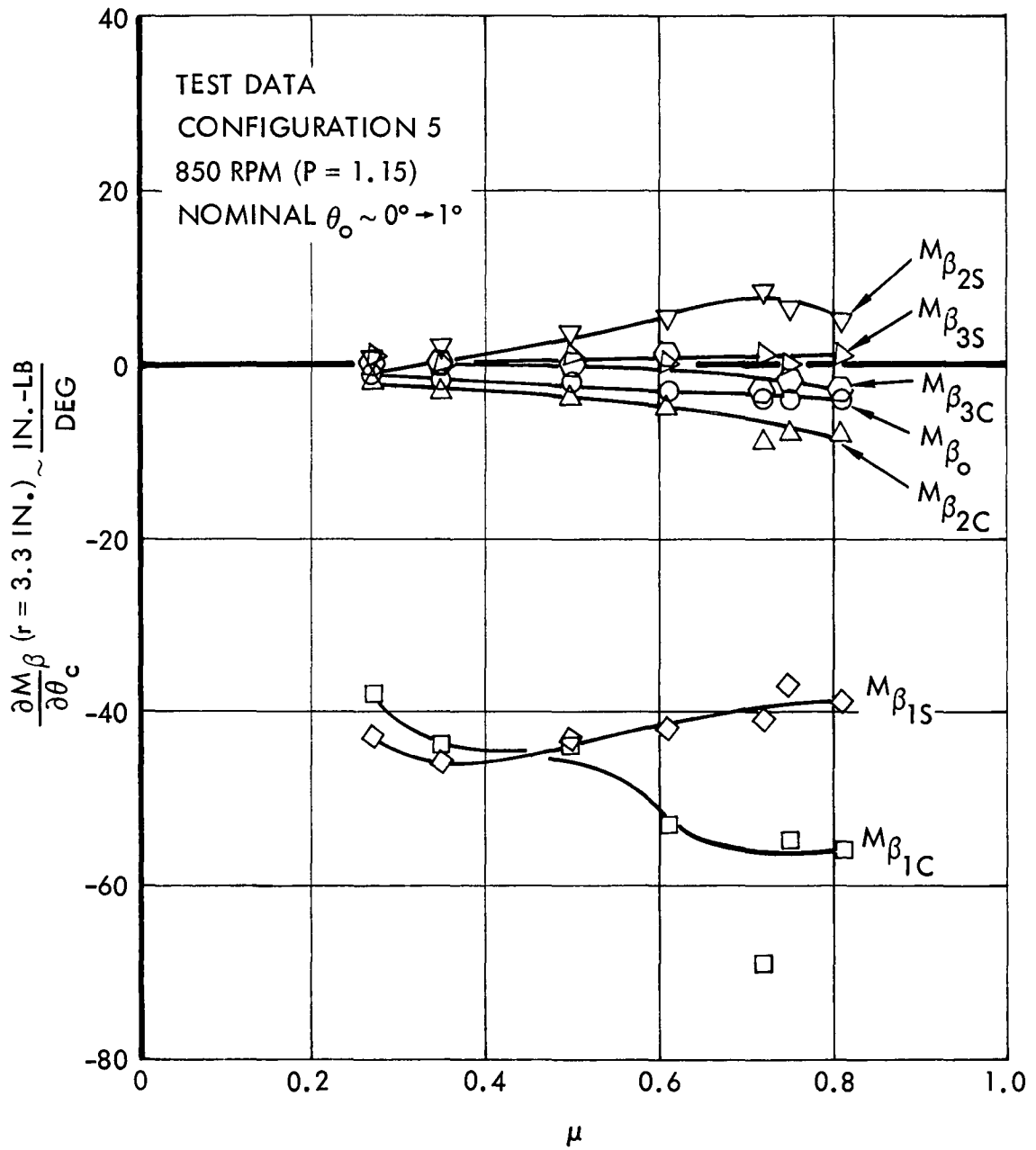


Figure A7. Harmonic Content of Blade Flapping, Configuration 5, 850 RPM (P = 1.15), Steady  $\theta_c$  Excitation



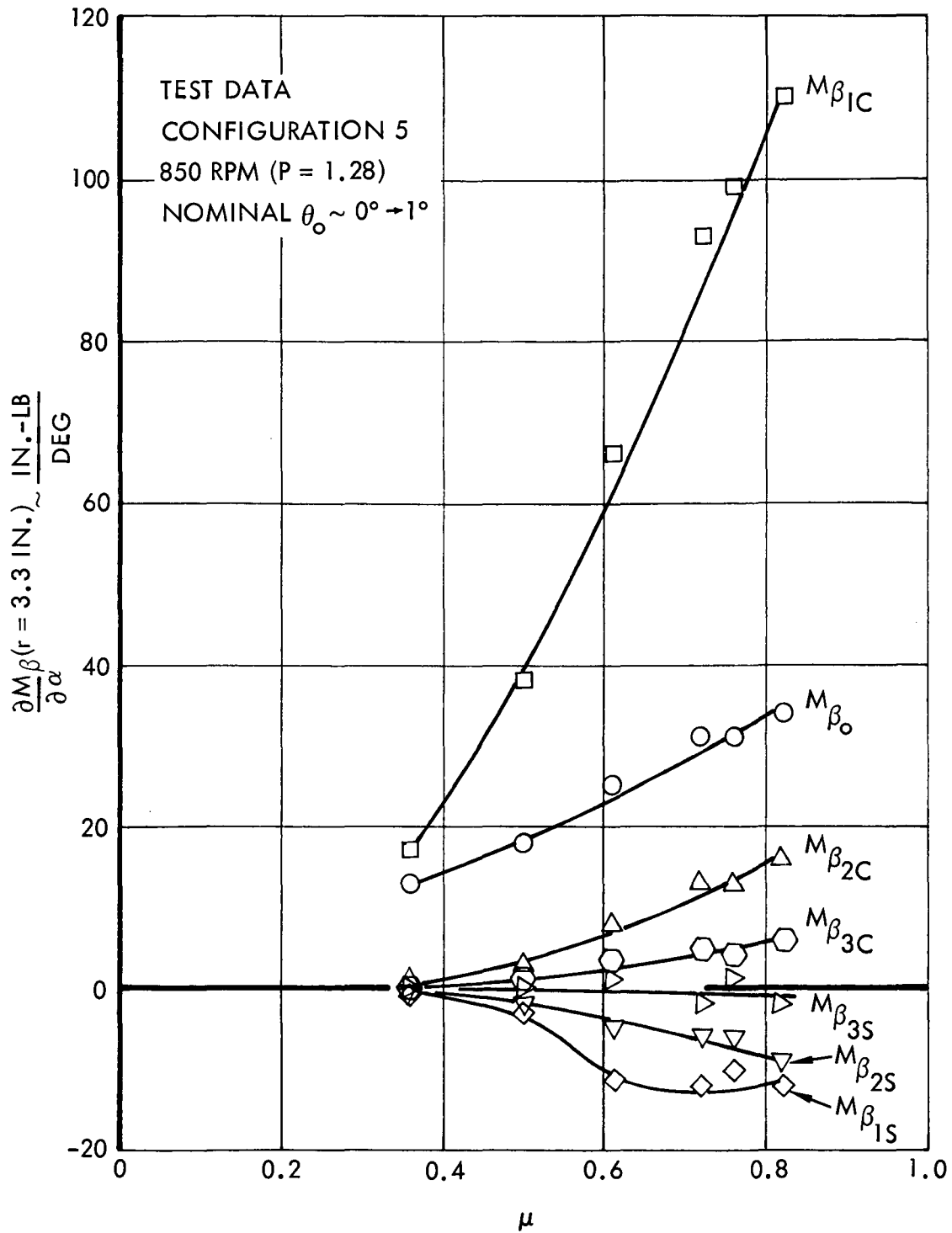


Figure A8. Harmonic Content of Blade Flapping, Configuration 5, 850 RPM (P = 1.15), Steady  $\alpha$  Excitation

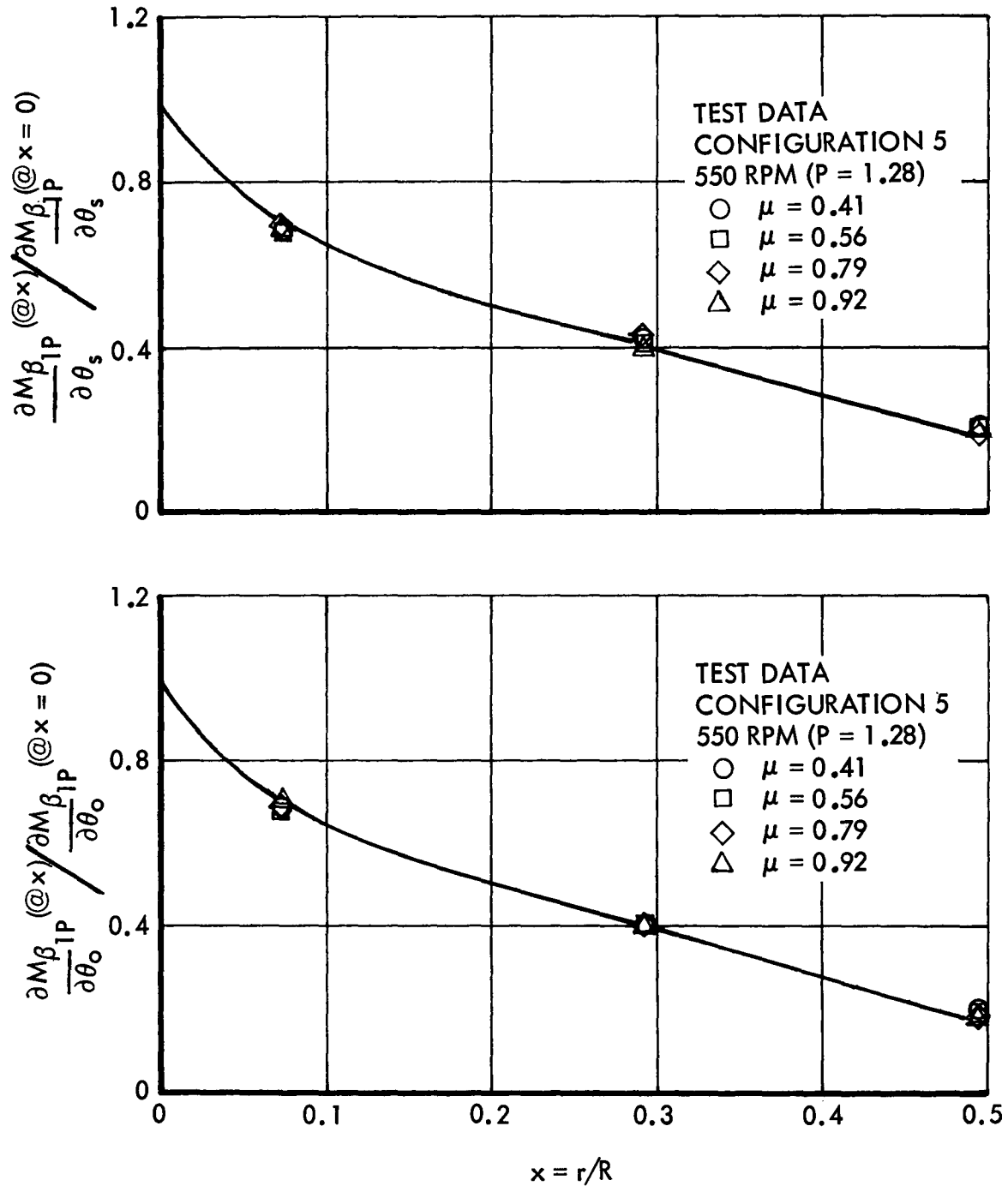


Figure A9. One-Per-Rev Blade Radial Flap Bending Moment Distribution Configuration 5, 550 RPM (P = 1.28),  $\theta_o$  and  $\theta_s$  Excitations

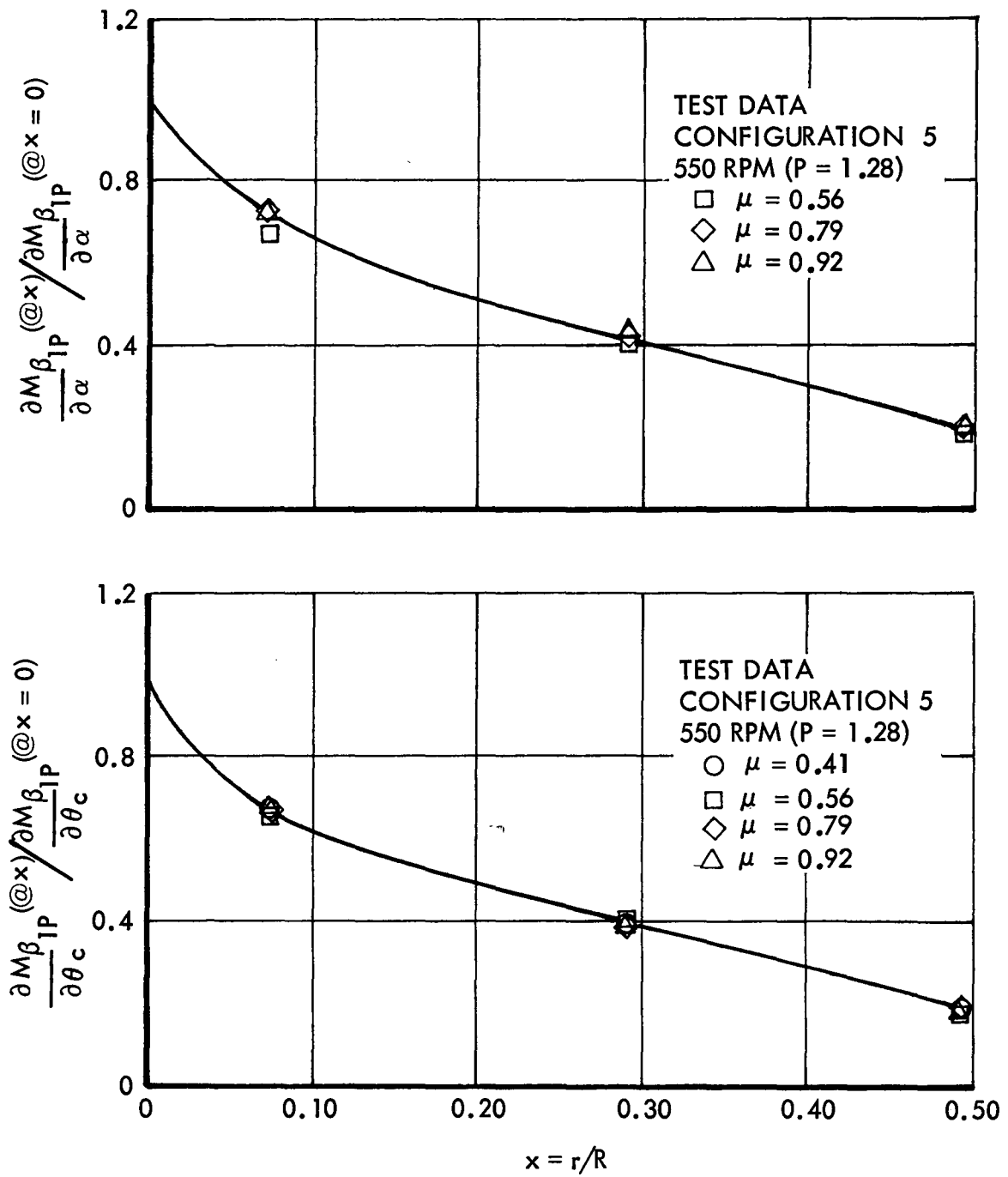


Figure A10. One-Per-Rev Blade Radial Flap Bending Moment Distribution Configuration 5, 550 RPM (P = 1.28),  $\theta_c$  and  $\alpha$  Excitations

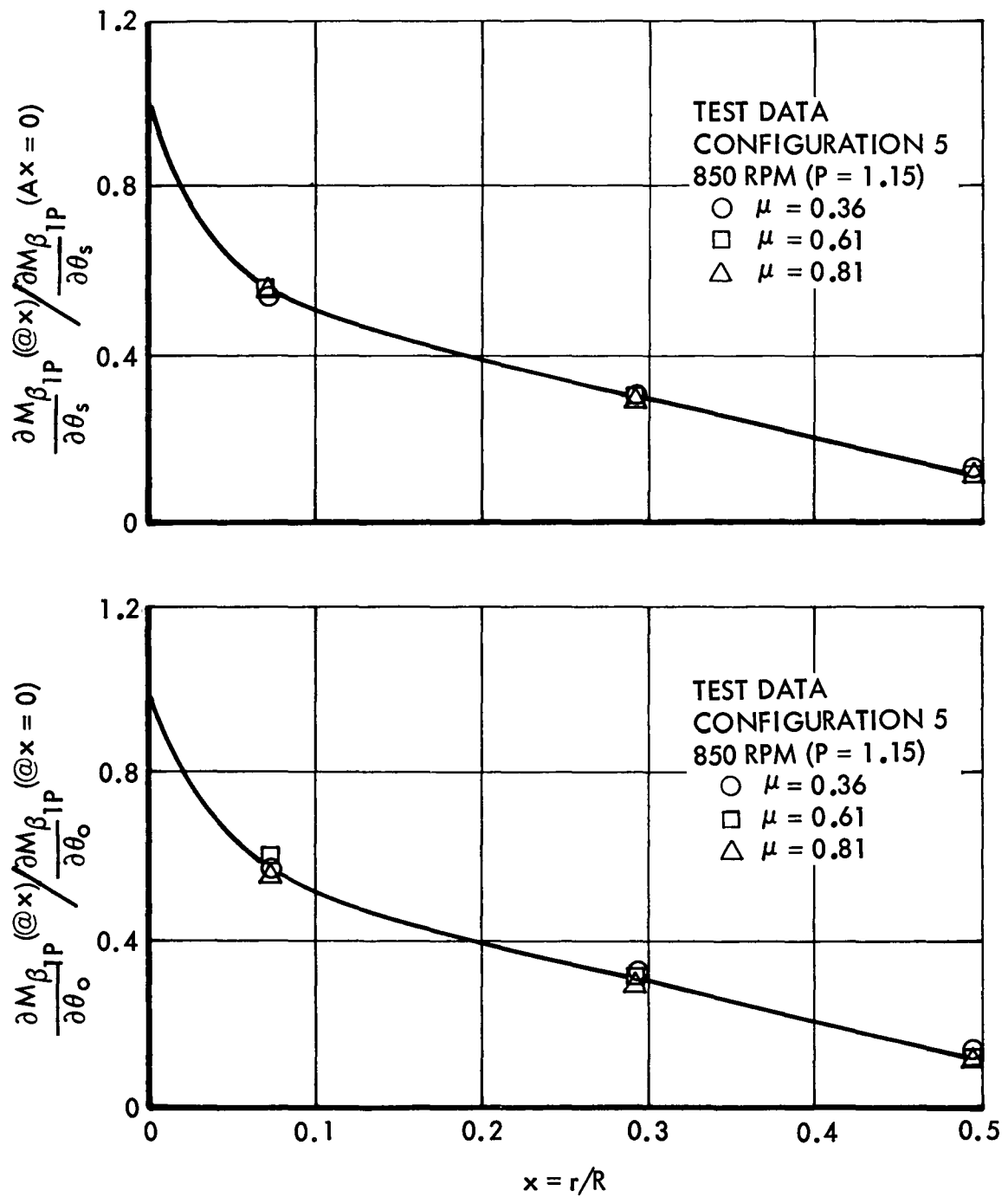


Figure All. One-Per-Rev Blade Radial Flap Bending Moment Distribution Configuration 5, 850 RPM (P = 1.15),  $\theta_o$  and  $\theta_s$  Excitations

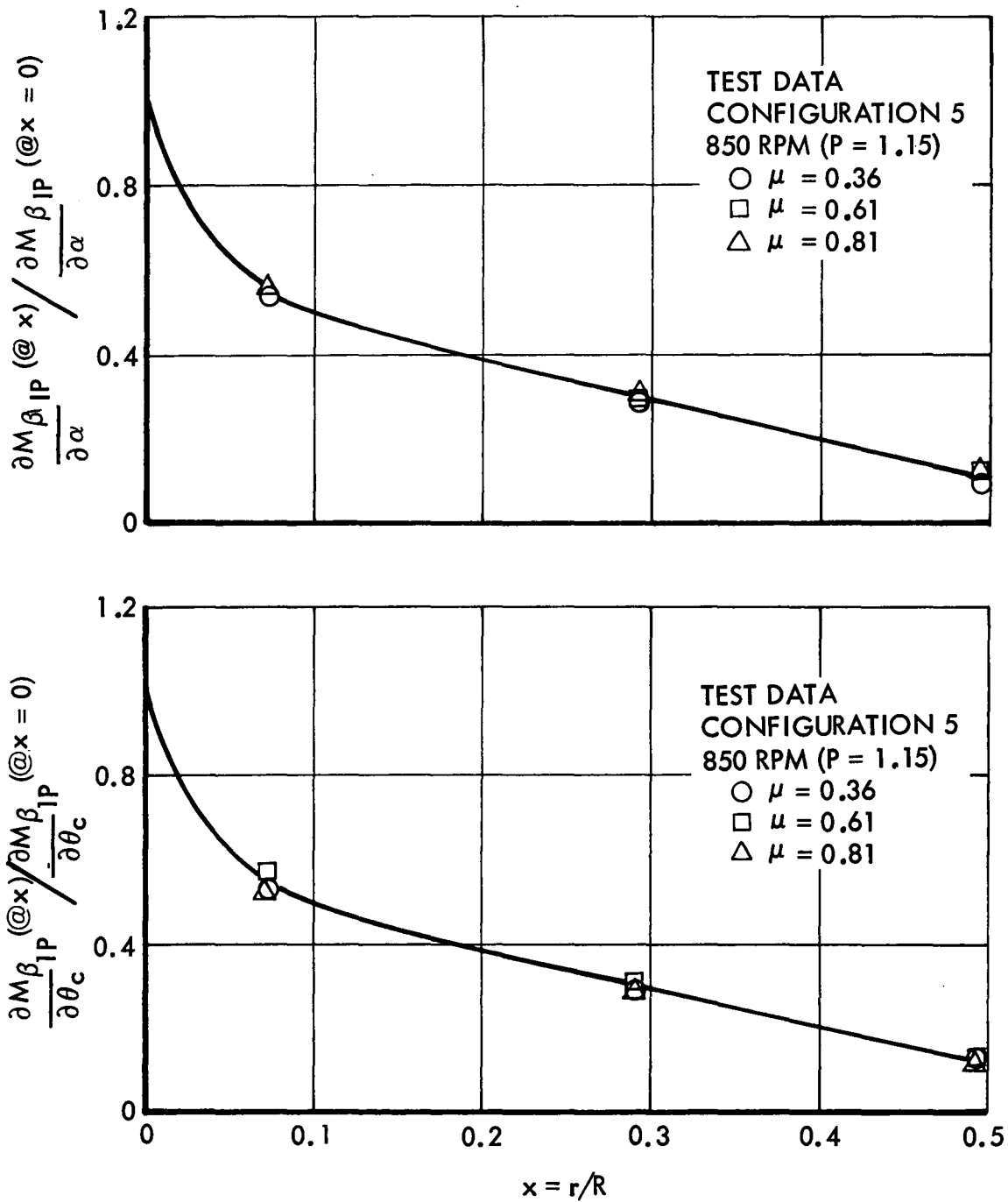


Figure A12. One-Per-Rev Blade Radial Flap Bending Moment Distribution Configuration 5, 850 RPM (P = 1.15),  $\theta_c$  and  $\alpha$  Excitations

## APPENDIX B

EXPERIMENTAL ROTOR FREQUENCY RESPONSE DATA ( $\theta_o$ ,  $\theta_s$  AND  $\theta_c$  EXCITATIONS)

All of the Phase 3 rotor transfer functions with respect to  $\theta_o$ ,  $\theta_s$  and  $\theta_c$  are contained in this appendix. The hub moment frequency response is plotted (in Figures B1 through B46) as it was in the main body of this report. The hub moment data have also been transferred to the shaft centerline, nondimensionalized and tabulated (Tables VI, VII and VIII). The procedure by which this was accomplished is fully described in Appendix C. The reader is reminded that the nominal rotor lift is approximately zero for all of these data.

TABLE VI  
 ROTOR MOMENT FREQUENCY RESPONSE TO COLLECTIVE  
 PITCH, CONFIGURATION 5

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_0 a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_0 a \sigma}$	$c_l$ Phase (rad)	
850/1.15	0.27	3.26	0.027	0.0200	-0.152	0.0033	-3.499	
		6.63	0.075	0.0192	-0.304	0.0032	-3.836	
		13.14	0.148	0.0178	-0.601	0.0020	-4.847	
		26.96	0.304	0.0120	-1.072	0.0029	-1.275	
		20.16	0.227	0.0151	-0.890	0.0020	-0.316	
		33.78	0.381	0.0098	-1.204	0.0037	-1.752	
		38.70	0.436	0.0077	-1.430	0.0046	-1.970	
		50.72	0.571	0.0069	-1.314	0.0043	-2.467	
		64.23	0.725	0.0086	-0.994	0.0032	-2.835	
		77.98	0.880	0.0085	-0.874	0.0031	-2.839	
	101.60	1.145	0.0070	-1.411	0.0061	-3.003		
	114.16	1.287	0.0068	-1.366	0.0065	-3.191		
	127.04	1.434	0.0079	-1.369	0.0072	-3.269		
	153.10	1.727	0.0121	-1.661	0.0115	-3.473		
	141.58	1.598	0.0100	-1.516	0.0094	-3.368		
	180.35	2.037	0.0241	-2.597	0.0272	-4.309		
	0.36		3.25	0.036	0.0303	-0.139	0.0085	-3.414
			6.58	0.074	0.0296	-0.271	0.0080	-3.697
			13.16	0.147	0.0283	-0.551	0.0063	-4.314
			20.22	0.226	0.0250	-0.836	0.0038	-5.101
26.83			0.300	0.0210	-1.057	0.0023	-0.040	
33.50			0.374	0.0171	-1.226	0.0028	-1.182	
37.78			0.421	0.0148	-1.343	0.0039	-1.567	
50.67			0.565	0.0137	-1.010	0.0040	-2.525	
57.51			0.641	0.0123	-1.194	0.0047	-2.515	
63.49			0.714	0.0097	-1.226	0.0055	-2.678	
76.61		0.859	0.0102	-1.083	0.0056	-2.862		
102.90		1.154	0.0089	-1.441	0.0086	-3.109		
113.29		1.270	0.0087	-1.403	0.0087	-3.239		
127.20		1.427	0.0108	-1.386	0.0097	-3.273		
140.44		1.574	0.0136	-1.532	0.0115	-3.337		
153.10		1.714	0.0160	-1.672	0.0157	-3.326		
166.58		1.865	0.0218	-1.975	0.0227	-3.625		
180.14		2.016	0.0283	-2.435	0.0301	-4.046		
196.35		2.159	0.0307	-3.464	0.0316	-4.888		
207.64		2.323	0.0215	-4.302	0.0206	-5.059		

TABLE VI

ROTOR MOMENT FREQUENCY RESPONSE TO COLLECTIVE  
PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_0 a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_0 a \sigma}$	$c_l$ Phase (rad)		
850/1.15	0.51	3.26	0.037	0.0443	-0.164	0.0116	-3.472		
		6.55	0.073	0.0433	-0.310	0.0110	-3.765		
		13.01	0.146	0.0414	-0.601	0.0092	-4.397		
		26.48	0.297	0.0305	-1.154	0.0048	-6.197		
		50.56	0.566	0.0159	-1.042	0.0050	-2.259		
		63.45	0.710	0.0153	-1.338	0.0069	-2.342		
		76.85	0.860	0.0145	-1.297	0.0077	-2.608		
		101.57	1.138	0.0109	-1.550	0.0120	-3.099		
		114.91	1.288	0.0135	-1.424	0.0131	-3.324		
		126.17	1.412	0.0167	-1.576	0.0143	-3.463		
		139.26	1.558	0.0206	-1.801	0.0171	-3.589		
		152.73	1.708	0.0259	-2.034	0.0232	-3.718		
		179.01	2.003	0.0403	-2.879	0.0424	-4.518		
		164.66	1.838	0.0351	-2.245	0.0343	-3.917		
		206.41	2.302	0.0173	-4.293	0.0252	-5.685		
		194.17	2.179	0.0351	-3.893	0.0404	-5.472		
			0.60	3.26	0.037	0.0556	-0.175	0.0156	-3.466
				6.54	0.074	0.0553	-0.323	0.0151	-3.758
				12.96	0.146	0.0520	-0.626	0.0125	-4.361
13.00	0.146			0.0512	-0.632	0.0124	-4.365		
26.59	0.299			0.0368	-1.216	0.0057	-6.032		
37.60	0.422			0.0225	-1.622	0.0058	-1.345		
50.33	0.566			0.0168	-1.587	0.0069	-2.055		
19.85	0.223			0.0452	-0.948	0.0085	-5.101		
63.40	0.712			0.0173	-1.441	0.0076	-2.321		
76.57	0.860			0.0162	-1.386	0.0090	-2.538		
88.42	0.992			0.0152	-1.620	0.0127	-2.747		
101.61	1.140			0.0124	-1.489	0.0152	-3.092		
113.87	1.278			0.0159	-1.416	0.0160	-3.356		
126.48	1.420			0.0204	-1.571	0.0171	-3.474		
139.82	1.569			0.0251	-1.808	0.0206	-3.587		
152.80	1.716			0.0310	-2.034	0.0277	-3.740		
179.32	2.012			0.0608	-3.012	0.0621	-4.646		
194.89	2.188			0.0397	-3.982	0.0454	-5.572		



TABLE VI  
 ROTOR MOMENT FREQUENCY RESPONSE TO COLLECTIVE  
 PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_0 a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_0 a \sigma}$	$c_l$ Phase (rad)		
550/1.28	0.41	3.27	0.056	0.0356	-0.067	0.0230	-3.337		
		6.62	0.114	0.0370	-0.147	0.0223	-3.553		
		13.08	0.225	0.0408	-0.398	0.0201	-4.065		
		26.53	0.455	0.0330	-1.105	0.0054	-5.584		
		20.09	0.344	0.0399	-0.803	0.0132	-4.797		
		38.29	0.659	0.0204	-1.493	0.0049	-2.133		
		50.87	0.879	0.0145	-1.628	0.0090	-2.652		
		63.65	1.099	0.0154	-1.437	0.0100	-2.858		
		77.57	1.336	0.0137	-1.190	0.0123	-3.226		
		88.72	1.528	0.0170	-1.239	0.0136	-3.310		
		101.44	1.744	0.0213	-1.455	0.0171	-3.361		
		114.83	1.973	0.0282	-1.808	0.0254	-3.578		
		127.35	2.187	0.0378	-2.426	0.0370	-4.119		
		142.93	2.453	0.0283	-3.562	0.0300	-5.100		
		133.24	2.285	0.0383	-2.865	0.0387	-4.509		
		154.30	2.646	0.0180	-4.049	0.0206	-5.462		
			0.79	6.61	0.115	0.0974	-0.228	0.0544	-3.620
				13.07	0.227	0.1022	-0.546	0.0484	-4.200
				20.18	0.351	0.0933	-0.992	0.0320	-4.955
				26.74	0.465	0.0725	-1.327	0.0154	-5.661
38.02	0.661			0.0431	-1.749	0.0091	-1.606		
50.25	0.873			0.0254	-1.810	0.0173	-2.416		
63.30	1.100			0.0233	-1.571	0.0224	-2.677		
77.30	1.343			0.0247	-1.193	0.0286	-3.170		
89.05	1.550			0.0334	-1.302	0.0281	-3.325		
100.60	1.748			0.0416	-1.522	0.0343	-3.378		
114.24	1.986			0.0541	-1.968	0.0497	-3.692		
127.04	2.209			0.0703	-2.608	0.0684	-4.263		
132.62	2.309			0.0668	-3.024	0.0671	-4.643		
140.44	2.443			0.0511	-3.501	0.0533	-5.055		
153.10	2.664			0.0318	-4.023	0.0355	-5.483		
179.73	3.127			0.0117	-4.879	0.0126	-6.111		



TABLE VI

 ROTOR MOMENT FREQUENCY RESPONSE TO COLLECTIVE  
 PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_0 a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_0 a \sigma}$	$c_l$ Phase (rad)
550/1.28	0.92	3.26	0.056	0.1307	-0.123	0.0621	-3.385
		6.62	0.114	0.1294	-0.262	0.0597	-3.652
		12.97	0.224	0.1302	-0.587	0.0519	-4.231
		19.92	0.344	0.1177	-1.009	0.0340	-4.967
		26.44	0.457	0.0935	-1.331	0.0173	-5.753
		31.26	0.540	0.0763	-1.501	0.0102	-0.235
		37.96	0.657	0.0530	-1.716	0.0118	-1.655
		50.52	0.871	0.0312	-1.662	0.0204	-2.453
		63.47	1.054	0.0290	-1.582	0.0291	-2.651
		76.23	1.314	0.0299	-1.196	0.0364	-3.132
		88.75	1.520	0.0411	-1.337	0.0353	-3.373
		101.51	1.751	0.0510	-1.592	0.0414	-3.438
		114.49	1.977	0.0653	-1.940	0.0567	-3.662
		127.45	2.202	0.0806	-2.631	0.0764	-4.274
		132.84	2.255	0.0774	-3.001	0.0755	-4.606
		120.33	2.077	0.0742	-2.199	0.0673	-3.880
		152.51	2.634	0.0404	-3.960	0.0443	-5.428
		179.52	3.059	0.0151	-4.845	0.0156	-6.051

TABLE VII

 ROTOR MOMENT FREQUENCY RESPONSE TO LONGITUDINAL  
 CYCLIC PITCH, CONFIGURATION 5

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_s a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_s a \sigma}$	$c_l$ Phase (rad)
850/1.15	0	3.52	0.040	0.0130	-6.108	0.0168	-3.331
		6.55	0.074	0.0161	-6.080	0.0171	-3.549
		9.73	0.111	0.0196	-6.190	0.0173	-3.844
		13.02	0.149	0.0213	-0.146	0.0154	-4.214
		16.37	0.188	0.0211	-0.380	0.0121	-4.547
		19.94	0.229	0.0192	-0.549	0.0086	-4.786
		23.13	0.262	0.0179	-0.625	0.0069	-4.847
		26.49	0.298	0.0167	-0.697	0.0051	-4.936
		33.03	0.372	0.0146	-0.792	0.0030	-4.961
		37.76	0.424	0.0138	-0.844	0.0020	-4.900
		50.25	0.565	0.0129	-0.908	0.0011	-3.991
		57.27	0.643	0.0121	-0.995	0.0013	-3.354
		63.11	0.709	0.0115	-1.051	0.0017	-3.190
		76.51	0.858	0.0102	-1.148	0.0028	-3.108
		88.30	0.991	0.0112	-1.033	0.0030	-3.252
		101.02	1.132	0.0116	-1.236	0.0037	-3.151
		113.70	1.274	0.0117	-1.365	0.0046	-3.150
		126.17	1.414	0.0123	-1.473	0.0053	-3.113
		139.69	1.565	0.0134	-1.629	0.0083	-3.153
		152.51	1.723	0.0143	-1.799	0.0115	-3.454
165.26	1.862	0.0172	-2.009	0.0141	-3.835		
0.27		3.50	0.039	0.0231	-0.091	0.0123	-3.317
		6.65	0.075	0.0231	-0.189	0.0122	-3.515
		13.05	0.147	0.0228	-0.406	0.0108	-3.897
		26.57	0.300	0.0183	-0.835	0.0053	-4.573
		38.03	0.429	0.0136	-1.067	0.0015	-4.589
		50.74	0.572	0.0112	-1.120	0.0015	-3.387
		63.75	0.719	0.0116	-1.124	0.0017	-3.249
		76.66	0.864	0.0112	-1.036	0.0021	-3.139
		89.45	1.009	0.0108	-1.251	0.0033	-2.907
		101.11	1.141	0.0106	-1.383	0.0044	-3.111
		114.95	1.298	0.0102	-1.470	0.0051	-3.251
		126.94	1.433	0.0107	-1.536	0.0057	-3.304
		152.58	1.723	0.0139	-1.737	0.0107	-3.443
		180.97	2.043	0.0207	-2.342	0.0179	-4.058

TABLE VII

ROTOR MOMENT FREQUENCY RESPONSE TO LONGITUDINAL  
CYCLIC PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_s a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_s a \sigma}$	$c_l$ Phase (rad)		
850/1.15	0.36	3.54	0.040	0.0285	-0.080	0.0142	-3.312		
		6.59	0.074	0.0279	-0.217	0.0135	-3.538		
		13.09	0.147	0.0272	-0.439	0.0116	-3.938		
		26.90	0.302	0.0216	-0.909	0.0053	-4.641		
		37.19	0.417	0.0154	-1.182	0.0010	-4.810		
		50.74	0.569	0.0152	-1.082	0.0014	-3.512		
		69.58	0.778	0.0123	-1.284	0.0027	-2.854		
		83.38	0.928	0.0110	-1.343	0.0037	-2.854		
		95.17	1.060	0.0104	-1.435	0.0049	-2.964		
		109.16	1.215	0.0100	-1.463	0.0059	-3.163		
		120.05	1.335	0.0099	-1.493	0.0061	-3.134		
		127.45	1.425	0.0106	-1.501	0.0069	-3.150		
		159.80	1.792	0.0165	-1.799	0.0135	-3.597		
			0.51	3.53	0.039	0.0370	-0.099	0.0155	-3.342
				6.55	0.073	0.0361	-0.236	0.0146	-3.584
13.07	0.146			0.0352	-0.495	0.0126	-4.022		
26.50	0.296			0.0277	-1.007	0.0057	-4.949		
38.00	0.425			0.0175	-1.366	0.0009	-0.767		
50.61	0.566			0.0139	-1.341	0.0022	-2.410		
64.00	0.715			0.0142	-1.321	0.0027	-2.536		
77.25	0.862			0.0129	-1.272	0.0037	-2.692		
88.90	0.992			0.0118	-1.404	0.0052	-2.718		
100.72	1.122			0.0104	-1.419	0.0066	-2.998		
114.28	1.273			0.0107	-1.350	0.0071	-3.142		
126.27	1.407			0.0124	-1.383	0.0077	-3.219		
139.57	1.571			0.0149	-1.527	0.0101	-3.175		
152.06	1.710			0.0174	-1.645	0.0140	-3.335		
179.52	2.017			0.0287	-2.265	0.0257	-3.973		
206.68	2.322	0.0245	-3.457	0.0227	-5.185				
	0.60	3.28	0.037	0.0453	-0.143	0.0173	-3.387		
		6.55	0.073	0.0449	-0.271	0.0167	-3.619		
		13.02	0.146	0.0433	-0.545	0.0143	-4.079		
		26.30	0.295	0.0326	-1.072	0.0061	-5.085		
		33.21	0.372	0.0253	-1.271	0.0023	-5.664		
		38.00	0.425	0.0197	-1.411	0.0010	-1.115		
50.61	0.566	0.0138	-1.319	0.0030	-2.528				

TABLE VII

ROTOR MOMENT FREQUENCY RESPONSE TO LONGITUDINAL  
CYCLIC PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_{sa} \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_{sa} \sigma}$	$c_l$ Phase (rad)		
850/1.15	0.60	63.96	0.716	0.0154	-1.355	0.0035	-2.428		
		76.27	0.854	0.0138	-1.306	0.0045	-2.574		
		88.47	0.991	0.0122	-1.456	0.0067	-2.683		
		101.21	1.134	0.0106	-1.406	0.0085	-3.005		
		113.58	1.276	0.0119	-1.318	0.0086	-3.174		
		126.42	1.417	0.0139	-1.364	0.0090	-3.210		
		139.32	1.562	0.0160	-1.503	0.0114	-3.158		
		152.21	1.707	0.0187	-1.642	0.0153	-3.335		
		178.81	2.006	0.0299	-2.172	0.0271	-3.849		
550/1.28	0	3.25	0.057	0.0085	-5.778	0.0235	-3.163		
		6.52	0.113	0.0149	-5.570	0.0274	-3.244		
		9.79	0.169	0.0250	-5.657	0.0329	-3.491		
		13.03	0.225	0.0339	-6.010	0.0347	-3.904		
		16.47	0.284	0.0361	-0.141	0.0285	-4.345		
		19.95	0.343	0.0331	-0.429	0.0203	-4.624		
		26.52	0.456	0.0270	-0.699	0.0109	-4.797		
		33.14	0.568	0.0234	-0.847	0.0063	-4.717		
		37.67	0.645	0.0217	-0.929	0.0044	-4.531		
		50.09	0.859	0.0204	-1.046	0.0036	-3.931		
		57.21	0.979	0.0188	-1.159	0.0045	-3.506		
		63.06	1.107	0.0179	-1.247	0.0056	-3.393		
		76.33	1.426	0.0171	-1.456	0.0086	-3.394		
		88.50	1.650	0.0174	-1.507	0.0102	-3.600		
		100.56	1.873	0.0214	-1.840	0.0144	-3.710		
		114.08	2.051	0.0258	-2.198	0.0197	-3.995		
		126.27	2.221	0.0272	-2.669	0.0227	-4.434		
		140.38	2.469	0.0213	-3.312	0.0206	-4.935		
		152.66	2.683	0.0146	-3.937	0.0162	-5.517		
			0.41	3.28	0.056	0.0346	-0.036	0.0294	-3.305
				6.55	0.113	0.0364	-0.085	0.0295	-3.484
13.16	0.227			0.0417	-0.295	0.0285	-3.932		
26.50	0.457			0.0364	-1.010	0.0115	-4.570		
19.80	0.341			0.0429	-0.668	0.0215	-4.499		
38.18	0.657			0.0234	-1.307	0.0007	-3.491		
44.60	0.775			0.0218	-1.273	0.0027	-3.167		
50.62	0.869			0.0179	-1.346	0.0054	-2.844		
62.92	1.080			0.0188	-1.367	0.0070	-2.989		
77.42	1.327			0.0182	-1.349	0.0102	-3.221		

TABLE VII

ROTOR MOMENT FREQUENCY RESPONSE TO LONGITUDINAL  
CYCLIC PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_s a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_s a \sigma}$	$c_l$ Phase (rad)
550/1.28	0.41	89.18	1.527	0.0197	-1.431	0.0125	-3.317
		102.37	1.753	0.0235	-1.616	0.0164	-3.465
		114.41	1.957	0.0287	-1.880	0.0226	-3.676
		127.19	2.221	0.0414	-2.585	0.0378	-4.324
		140.00	2.438	0.0313	-3.459	0.0316	-5.185
		133.12	2.316	0.0396	-2.995	0.0379	-4.726
		153.70	2.674	0.0165	-3.972	0.0187	-5.628
		179.01	3.113	0.0050	-4.226	0.0089	-5.964
	0.79	6.60	0.114	0.0761	-0.204	0.0461	-3.596
		13.01	0.226	0.0822	-0.504	0.0425	-4.132
		20.09	0.349	0.0759	-0.939	0.0293	-4.818
		26.38	0.458	0.0615	-1.260	0.0158	-5.377
		31.23	0.542	0.0513	-1.424	0.0083	-5.904
		37.87	0.658	0.0379	-1.619	0.0047	-1.130
		50.54	0.877	0.0216	-1.639	0.0118	-2.452
		63.30	1.100	0.0217	-1.557	0.0164	-2.704
		76.53	1.329	0.0224	-1.286	0.0206	-3.166
		88.50	1.537	0.0295	-1.368	0.0214	-3.302
		101.51	1.763	0.0374	-1.623	0.0284	-3.418
		113.74	1.974	0.0450	-1.977	0.0377	-3.726
		127.14	2.207	0.0595	-2.657	0.0555	-4.352
		132.17	2.295	0.0575	-3.025	0.0559	-4.708
		139.69	2.427	0.0460	-3.510	0.0470	-5.173
		152.58	2.650	0.0269	-3.989	0.0301	-5.585
		179.52	3.118	0.0072	-4.549	0.0114	-6.108
		0.92	6.60	0.114	0.0984	-0.252	0.0492
	12.91		0.222	0.1024	-0.557	0.0439	-4.166
	20.08		0.346	0.0916	-0.985	0.0295	-4.877
	26.37		0.454	0.0738	-1.293	0.0155	-5.521
	31.26		0.539	0.0619	-1.447	0.0087	-6.129
	37.97		0.654	0.0432	-1.671	0.0069	-1.380
	50.96		0.877	0.0275	-1.606	0.0138	-2.419
	63.22		1.089	0.0245	-1.600	0.0208	-2.658
	76.59		1.317	0.0254	-1.283	0.0262	-3.165
	88.15		1.517	0.0327	-1.392	0.0251	-3.380
	100.98		1.739	0.0416	-1.640	0.0311	-3.463
114.74	1.976		0.0519	-2.053	0.0427	-3.793	
126.43	2.178		0.0629	-2.647	0.0567	-4.333	
140.94	2.425		0.0477	-3.509	0.0466	-5.106	
152.66	2.626		0.0322	-3.963	0.0354	-5.507	
180.35	3.103		0.0075	-4.727	0.0119	-6.128	

TABLE VIII  
 ROTOR MOMENT FREQUENCY RESPONSE TO LATERAL CYCLIC  
 PITCH, CONFIGURATION 5

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_c a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_c a \sigma}$	$c_l$ Phase (rad)		
850/1.15	0.27	3.26	0.037	0.0202	-3.361	0.0201	-3.162		
		6.60	0.074	0.0197	-3.594	0.0213	-3.207		
		13.02	0.146	0.0170	-4.045	0.0237	-3.388		
		26.49	0.298	0.0079	-4.845	0.0226	-3.938		
		37.75	0.425	0.0026	-4.966	0.0175	-4.271		
		50.37	0.567	0.0015	-4.152	0.0136	-4.465		
		63.62	0.715	0.0022	-3.714	0.0107	-4.553		
		76.72	0.863	0.0035	-3.447	0.0093	-4.545		
		101.41	1.140	0.0036	-3.448	0.0095	-4.680		
		114.91	1.292	0.0044	-3.405	0.0099	-4.780		
		126.73	1.424	0.0055	-3.457	0.0102	-4.862		
		153.10	1.722	0.0083	-3.693	0.0113	-5.089		
		182.02	2.048	0.0148	-4.221	0.0176	-5.604		
			0.36	3.26	0.037	0.0218	-3.357	0.0203	-3.159
				6.65	0.075	0.0210	-3.562	0.0212	-3.200
12.94	0.146			0.0184	-3.982	0.0233	-3.362		
26.33	0.297			0.0093	-4.773	0.0231	-3.873		
37.95	0.427			0.0032	-4.997	0.0186	-4.209		
50.77	0.571			0.0015	-4.238	0.0152	-4.440		
63.98	0.720			0.0025	-3.764	0.0123	-4.577		
77.28	0.870			0.0039	-3.542	0.0103	-4.634		
101.83	1.146			0.0037	-3.526	0.0095	-4.771		
115.33	1.298			0.0046	-3.504	0.0095	-4.831		
127.14	1.430			0.0056	-3.577	0.0100	-4.884		
152.80	1.719			0.0085	-3.769	0.0118	-5.138		
	0.51			3.24	0.036	0.0228	-3.372	0.0203	-3.144
				6.57	0.074	0.0223	-3.575	0.0212	-3.184
				13.11	0.147	0.0194	-4.016	0.0236	-3.342
		26.52	0.297	0.0099	-4.800	0.0236	-3.842		
		37.62	0.422	0.0036	-4.948	0.0193	-4.130		
		50.46	0.565	0.0015	-4.380	0.0160	-4.364		

TABLE VIII

ROTOR MOMENT FREQUENCY RESPONSE TO LATERAL CYCLIC  
PITCH, CONFIGURATION (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\theta_c a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\theta_c a \sigma}$	$c_l$ Phase (rad)
850/1.15	0.51	64.09	0.716	0.0022	-3.824	0.0133	-4.507
		76.81	0.858	0.0037	-3.549	0.0116	-4.590
		88.75	0.992	0.0034	-3.553	0.0112	-4.676
		100.89	1.126	0.0038	-3.554	0.0104	-4.788
		114.07	1.280	0.0049	-3.511	0.0100	-4.857
		126.38	1.417	0.0060	-3.614	0.0101	-4.928
		140.00	1.568	0.0070	-3.680	0.0110	-5.021
		152.73	1.709	0.0085	-3.850	0.0115	-5.105
		178.91	2.001	0.0147	-4.341	0.0182	-5.616
	206.96	2.314	0.0125	-5.679	0.0117	-0.285	
	0.60	3.26	0.036	0.0271	-3.357	0.0189	-3.134
		6.58	0.074	0.0257	-3.581	0.0205	-3.146
		12.88	0.144	0.0228	-3.999	0.0234	-3.281
		26.41	0.296	0.0118	-4.782	0.0242	-3.806
		33.27	0.373	0.0069	-5.008	0.0215	-4.010
		37.94	0.425	0.0042	-4.985	0.0197	-4.106
		50.13	0.561	0.0020	-4.670	0.0164	-4.324
		63.39	0.709	0.0024	-3.972	0.0140	-4.454
		76.85	0.860	0.0037	-3.685	0.0124	-4.540
101.74		1.139	0.0040	-3.436	0.0110	-4.777	
113.83	1.274	0.0054	-3.452	0.0107	-4.857		
127.09	1.422	0.0065	-3.586	0.0106	-4.929		
140.00	1.566	0.0075	-3.672	0.0112	-5.029		
152.80	1.711	0.0090	-3.874	0.0117	-5.126		
172.71	1.933	0.0142	-4.256	0.0165	-5.535		
550/1.28	0.41	3.26	0.056	0.0360	-3.311	0.0216	-3.074
		6.55	0.113	0.0361	-3.505	0.0243	-3.041
		12.99	0.225	0.0349	-3.953	0.0327	-3.194
		26.58	0.460	0.0150	-4.964	0.0345	-4.032
		20.07	0.347	0.0264	-4.561	0.0386	-3.641
		38.12	0.660	0.0042	-4.862	0.0242	-4.389
		43.87	0.759	0.0041	-4.399	0.0220	-4.446
		50.96	0.882	0.0035	-3.848	0.0187	-4.566
		64.10	1.109	0.0053	-3.648	0.0157	-4.664
		76.79	1.329	0.0077	-3.448	0.0146	-4.735
		89.30	1.545	0.0097	-3.517	0.0154	-4.821
		101.64	1.758	0.0129	-3.611	0.0175	-4.958
		114.20	1.975	0.0181	-3.804	0.0212	-5.192



TABLE VIII

ROTOR MOMENT FREQUENCY RESPONSE TO LATERAL CYCLIC  
PITCH, CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{a\sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{a\sigma}$	$c_l$ Phase (rad)	
550/1.28	0.41	128.44	2.220	0.0293	-4.475	0.0291	-5.861	
		140.69	2.434	0.0264	-5.272	0.0223	-0.347	
		134.09	2.315	0.0306	-4.849	0.0282	-6.237	
		153.33	2.646	0.0185	-5.666	0.0167	-0.637	
		180.24	3.108	0.0085	-6.234	0.0051	-1.292	
	0.79	6.50	0.113	0.0524	-3.536	0.0251	-2.909	
		13.05	0.227	0.0490	-4.002	0.0362	-3.091	
		20.10	0.349	0.0360	-4.564	0.0429	-3.546	
		26.41	0.459	0.0219	-4.897	0.0390	-3.903	
		31.25	0.543	0.0144	-4.998	0.0343	-4.092	
		37.68	0.655	0.0088	-4.997	0.0294	-4.251	
		50.54	0.880	0.0033	-4.658	0.0248	-4.452	
		63.49	1.103	0.0044	-3.458	0.0218	-4.620	
		76.66	1.332	0.0100	-3.269	0.0196	-4.780	
		89.15	1.549	0.0136	-3.492	0.0209	-4.870	
		101.41	1.760	0.0188	-3.667	0.0236	-5.042	
		113.83	1.974	0.0253	-3.996	0.0277	-5.355	
		126.78	2.199	0.0379	-4.627	0.0358	-6.005	
		132.73	2.302	0.0395	-5.021	0.0344	-0.120	
		140.25	2.434	0.0327	-5.486	0.0259	-0.570	
		152.36	2.643	0.0217	-5.909	0.0175	-0.927	
		178.91	3.107	0.0084	-0.436	0.0040	-2.226	
		0.92	6.50	0.112	0.0575	-3.553	0.0253	-2.901
			13.07	0.225	0.0524	-4.020	0.0365	-3.096
	20.00		0.343	0.0376	-4.543	0.0420	-3.530	
	26.67		0.458	0.0228	-4.876	0.0386	-3.883	
	31.26		0.535	0.0155	-4.964	0.0350	-4.054	
	37.74		0.648	0.0095	-4.848	0.0300	-4.197	
	50.78		0.872	0.0043	-4.595	0.0262	-4.427	
	63.42		1.091	0.0046	-3.617	0.0234	-4.623	
	76.66		1.321	0.0103	-3.361	0.0206	-4.774	
	88.77		1.528	0.0139	-3.521	0.0209	-4.870	
	100.44		1.730	0.0190	-3.674	0.0239	-5.025	
	114.20		1.967	0.0289	-4.038	0.0304	-5.362	
	126.32		2.176	0.0378	-4.663	0.0348	-6.006	
	140.69		2.425	0.0330	-5.610	0.0249	-0.662	
152.51	2.626		0.0236	-6.035	0.0188	-1.064		
179.83	3.098		0.0089	-0.568	0.0052	-2.478		

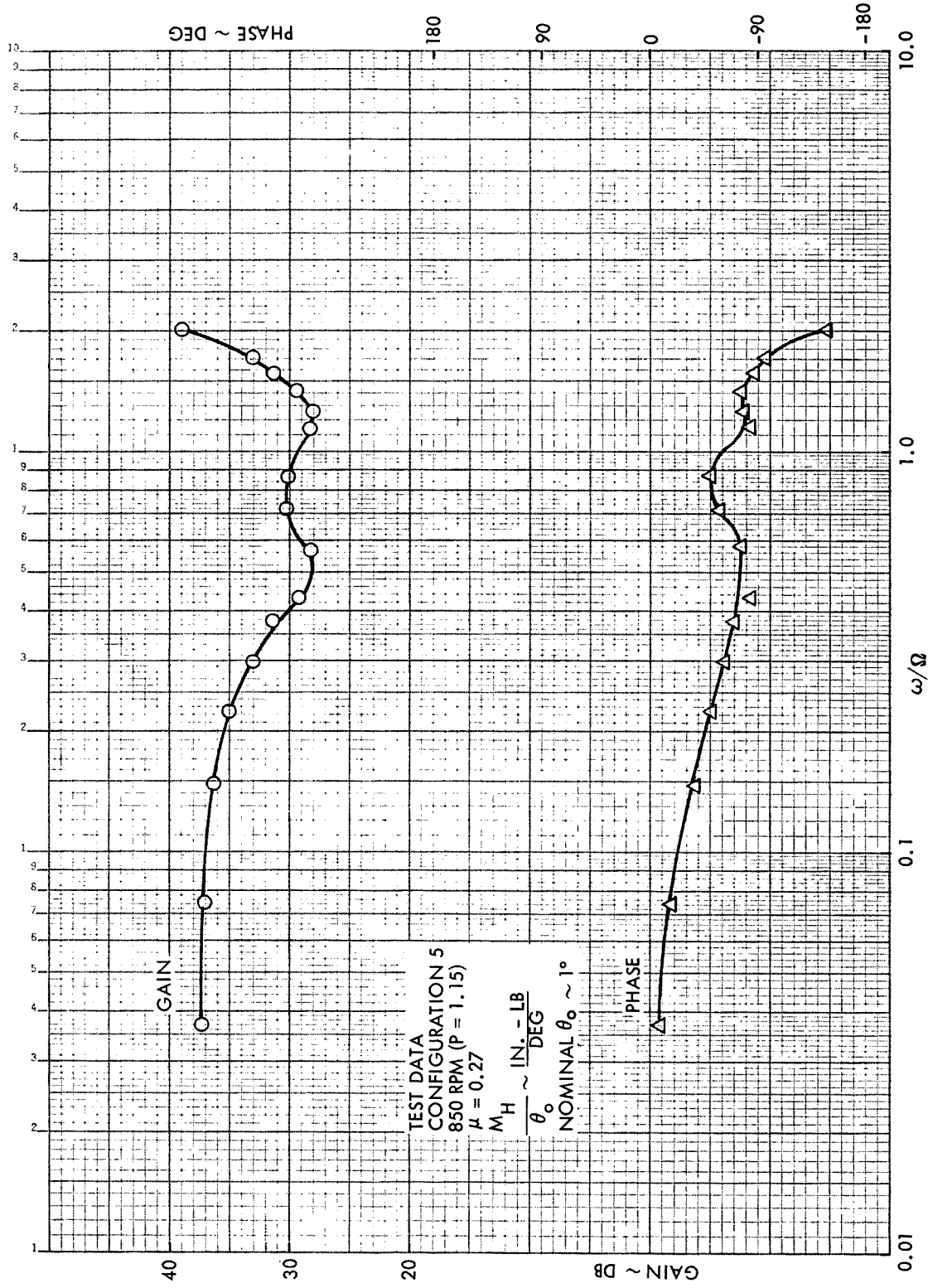


Figure B1. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)

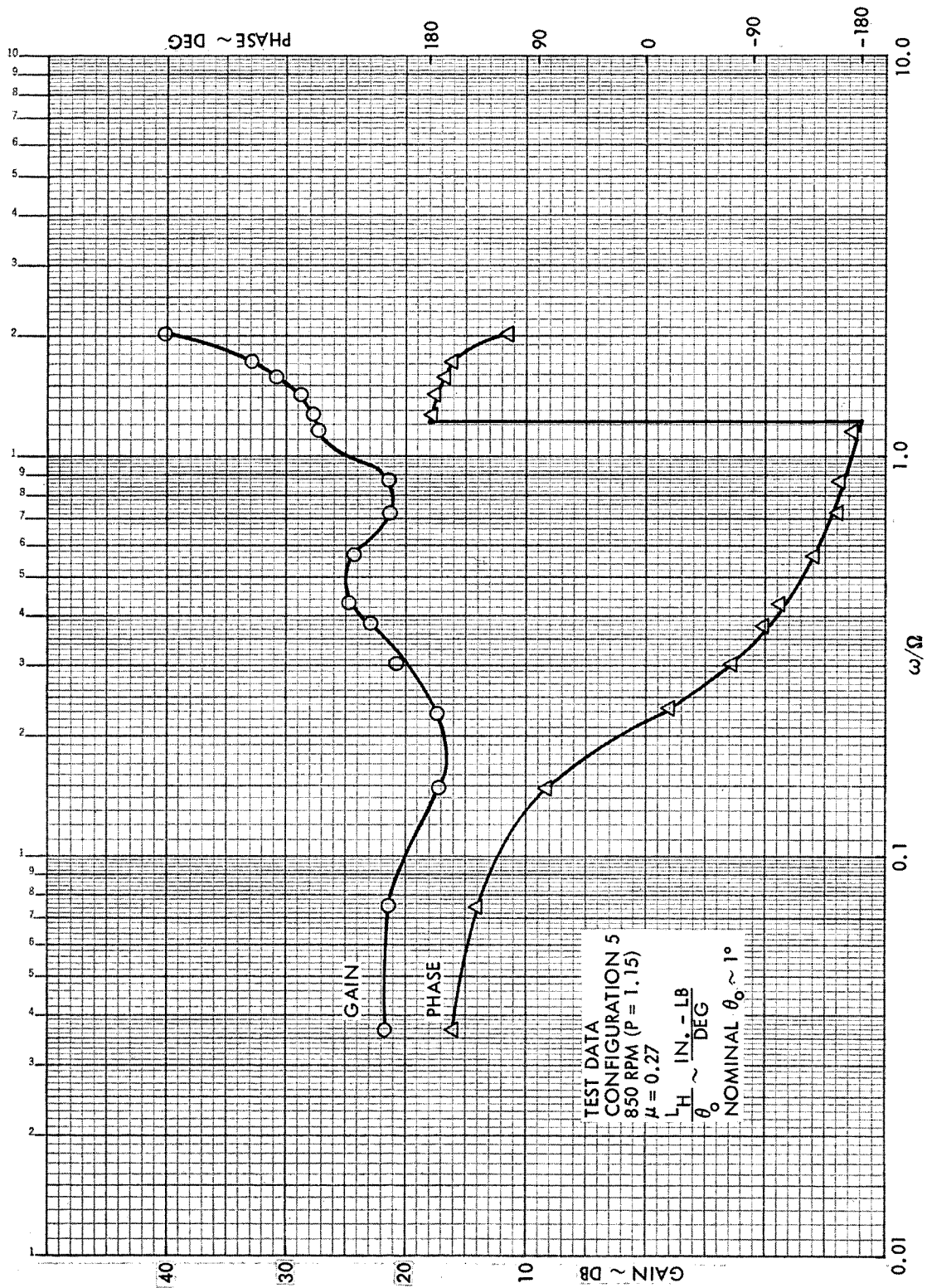


Figure B2. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)

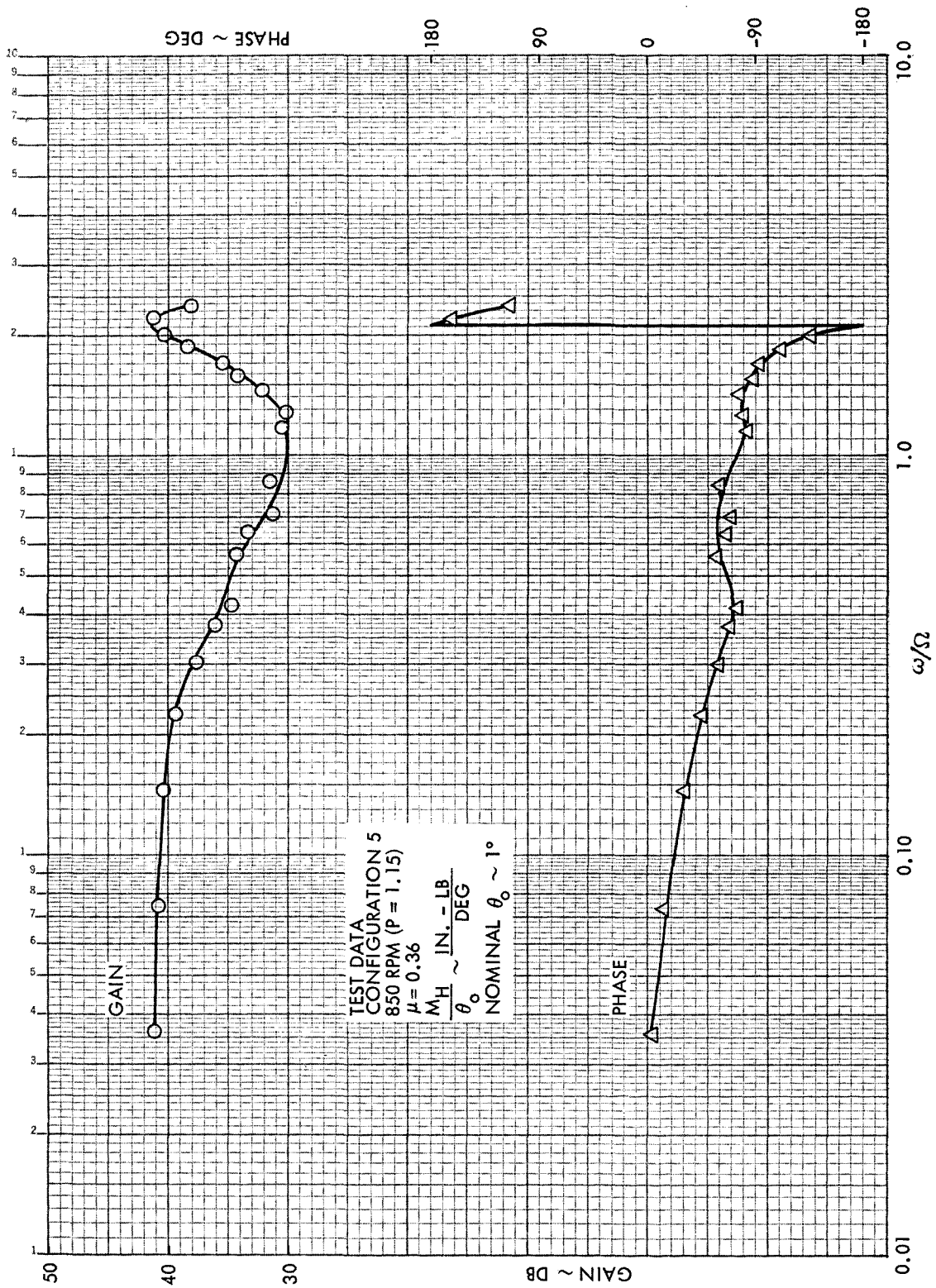


Figure B3. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)

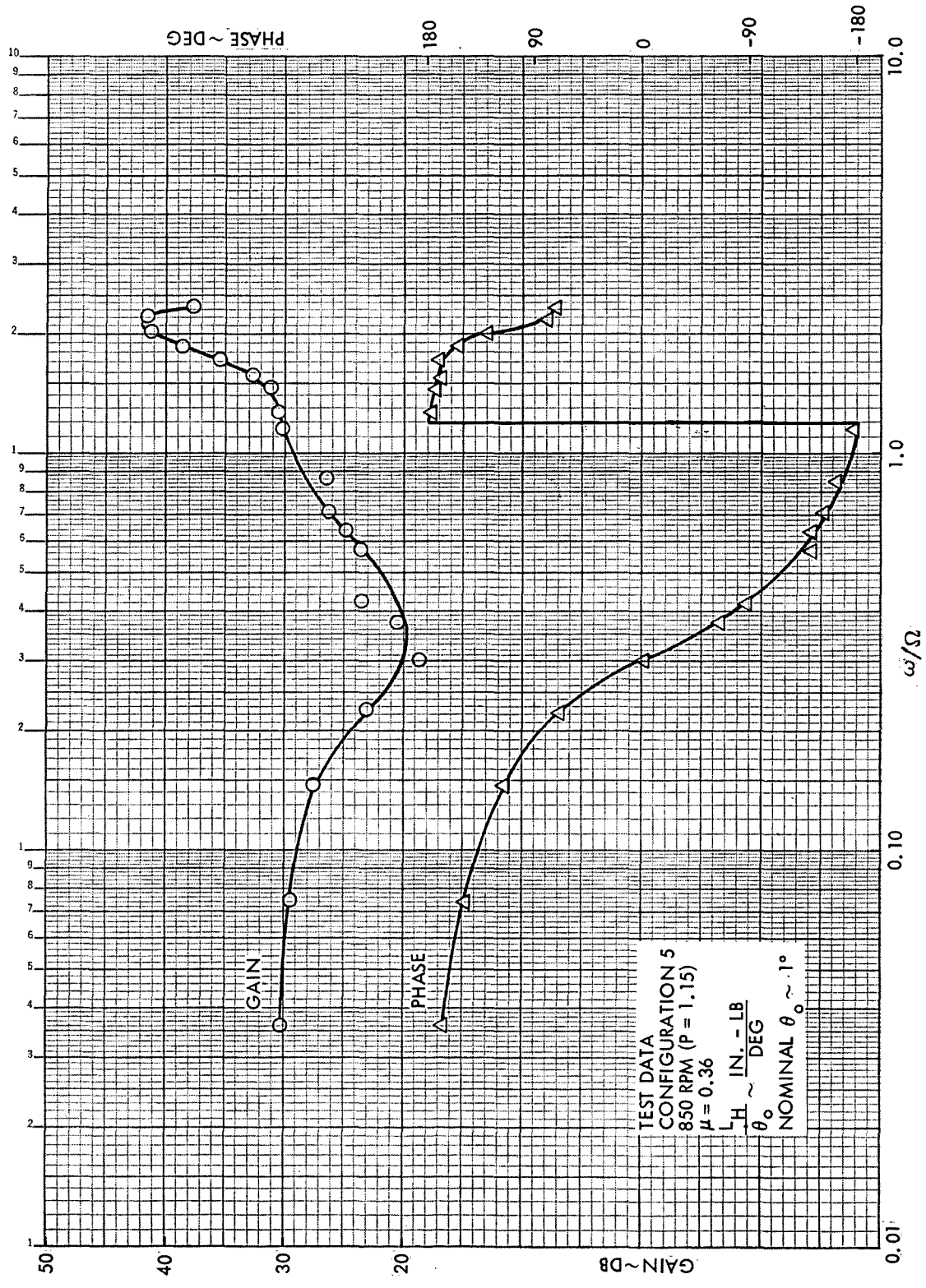


Figure B4. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)

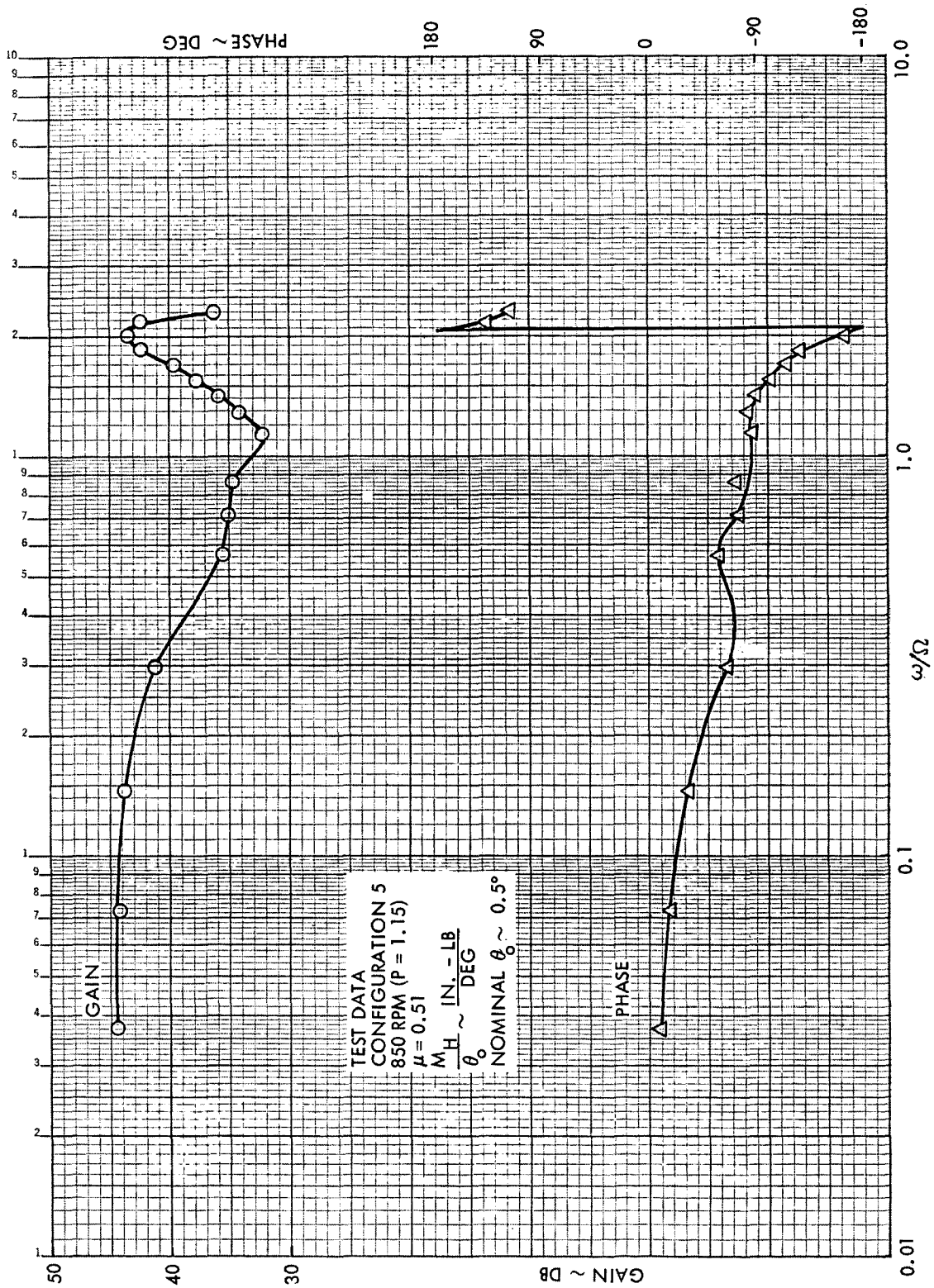


Figure B5. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)



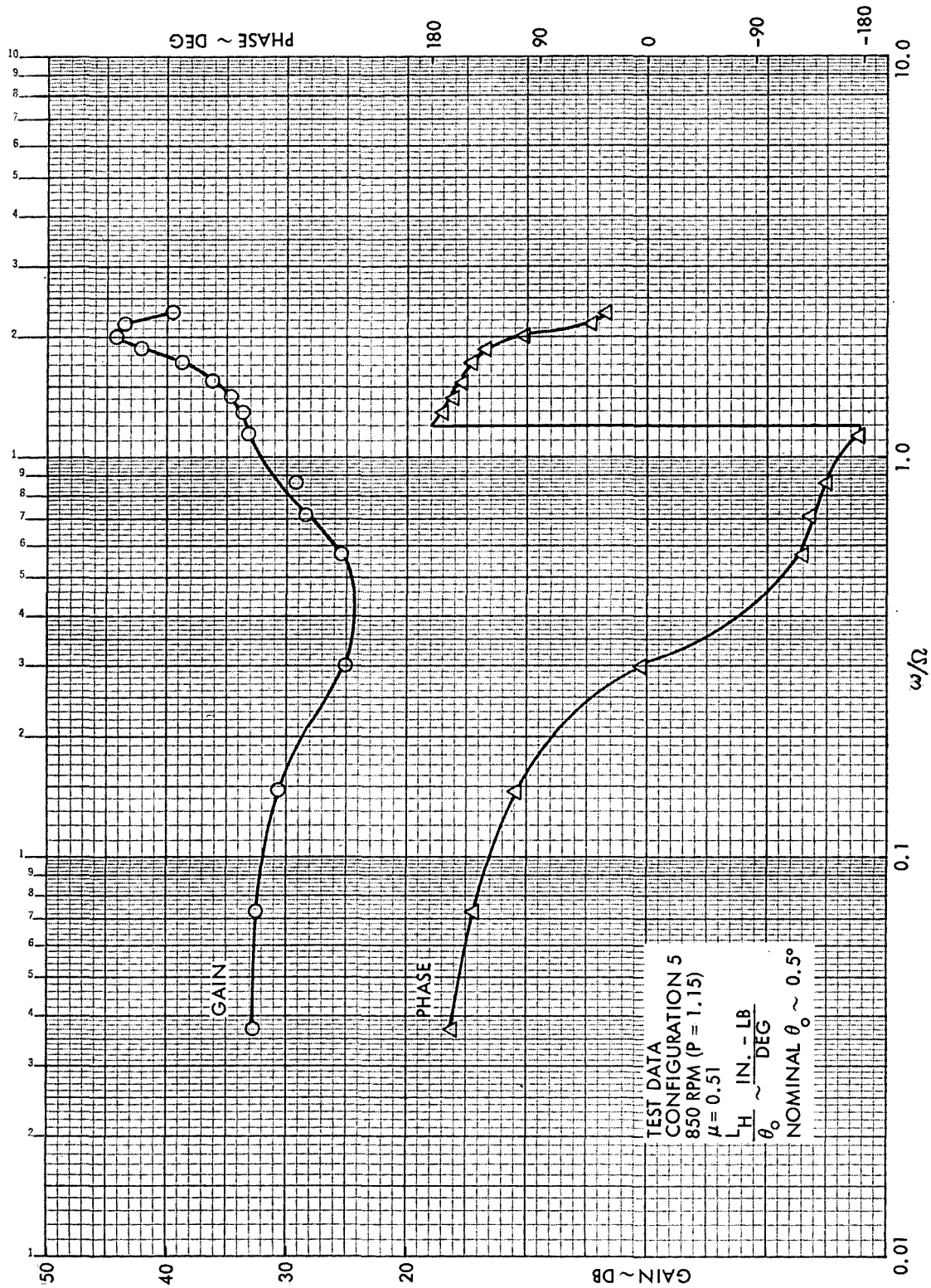


Figure B6. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5, # = 0.51, 850 RPM ( $P = 1.15$ )



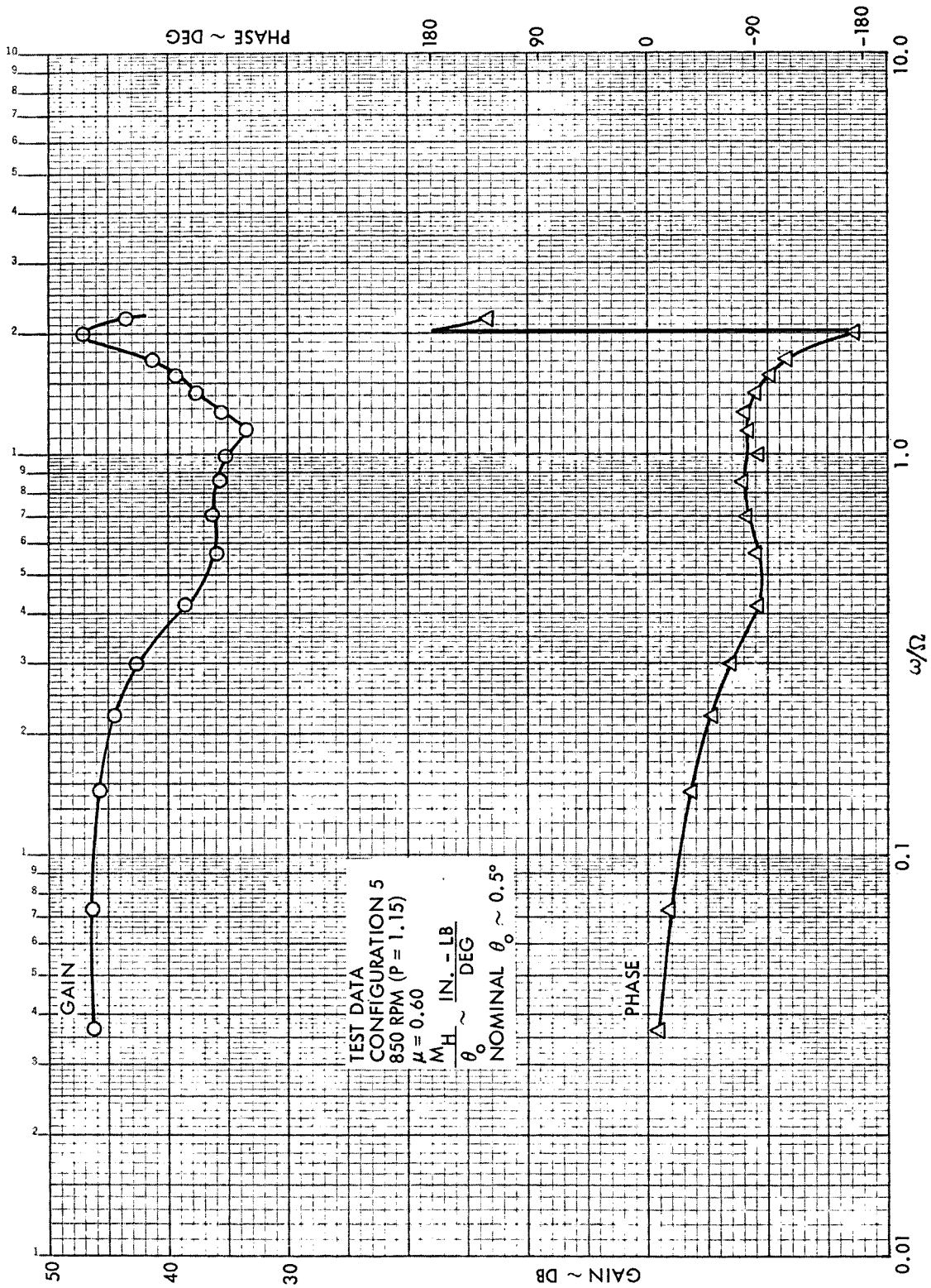


Figure B7. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )



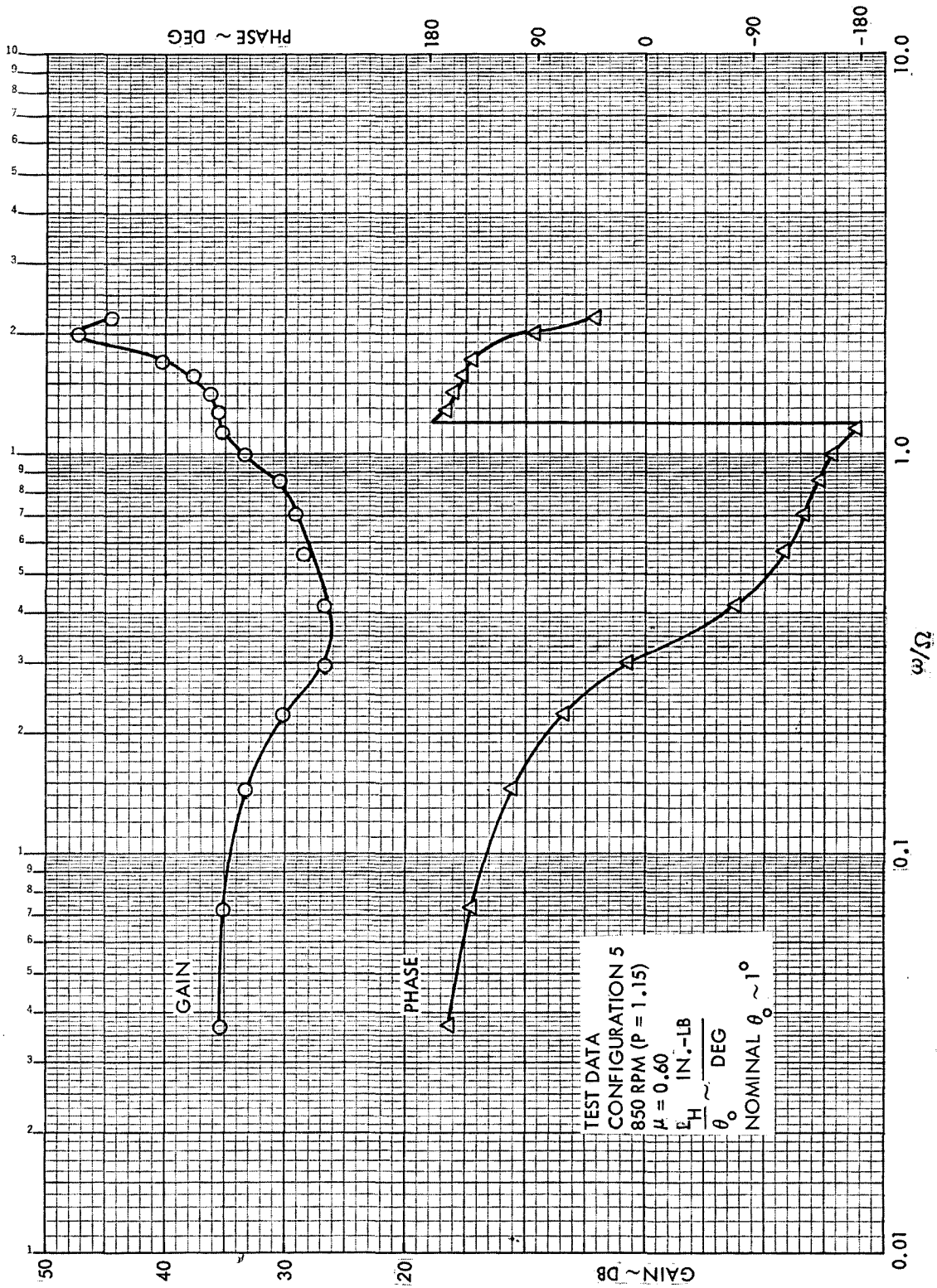


Figure B8. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM (P = 1.15)



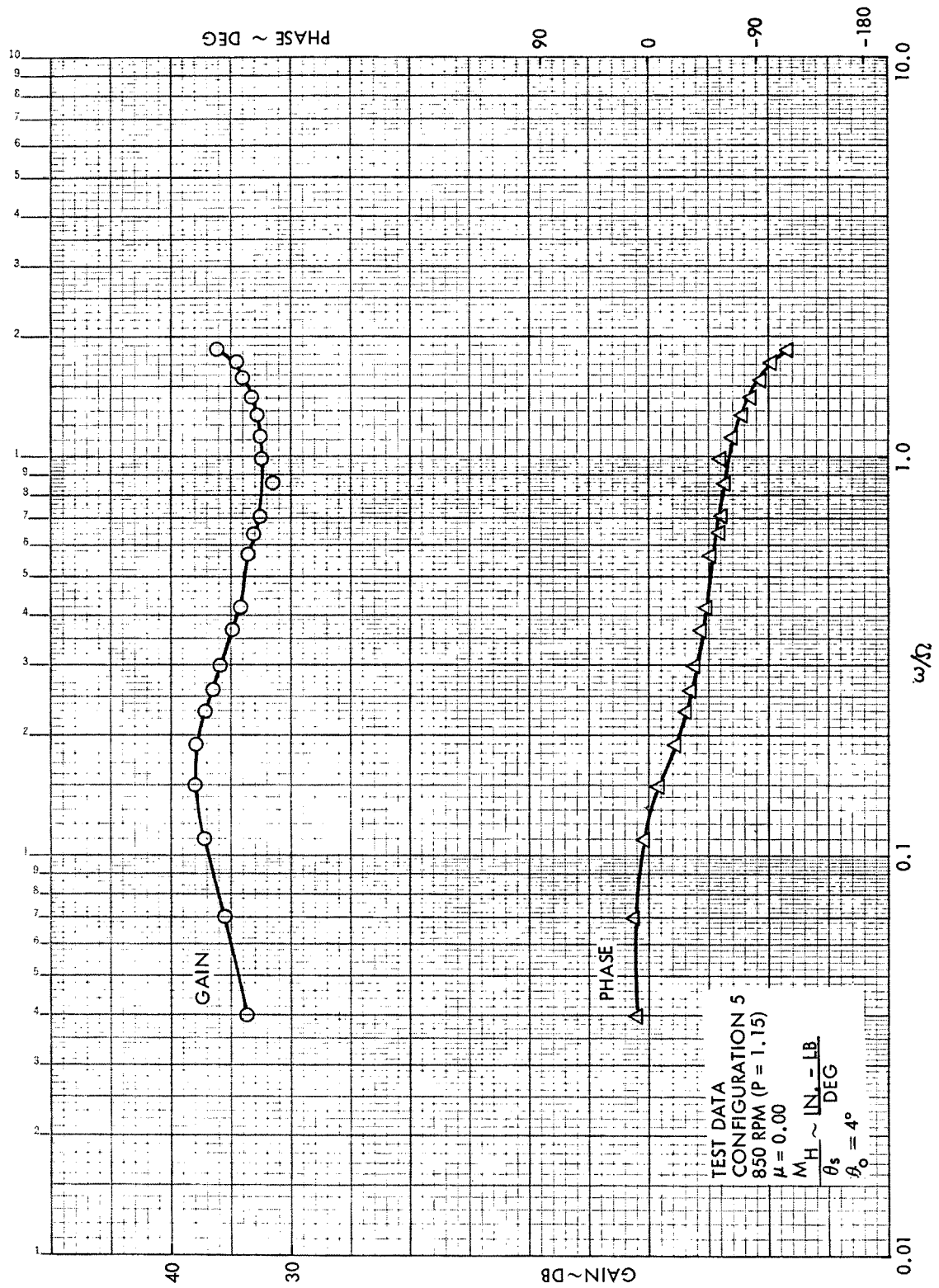


Figure B9. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.0$ , 850 RPM (P = 1.15)

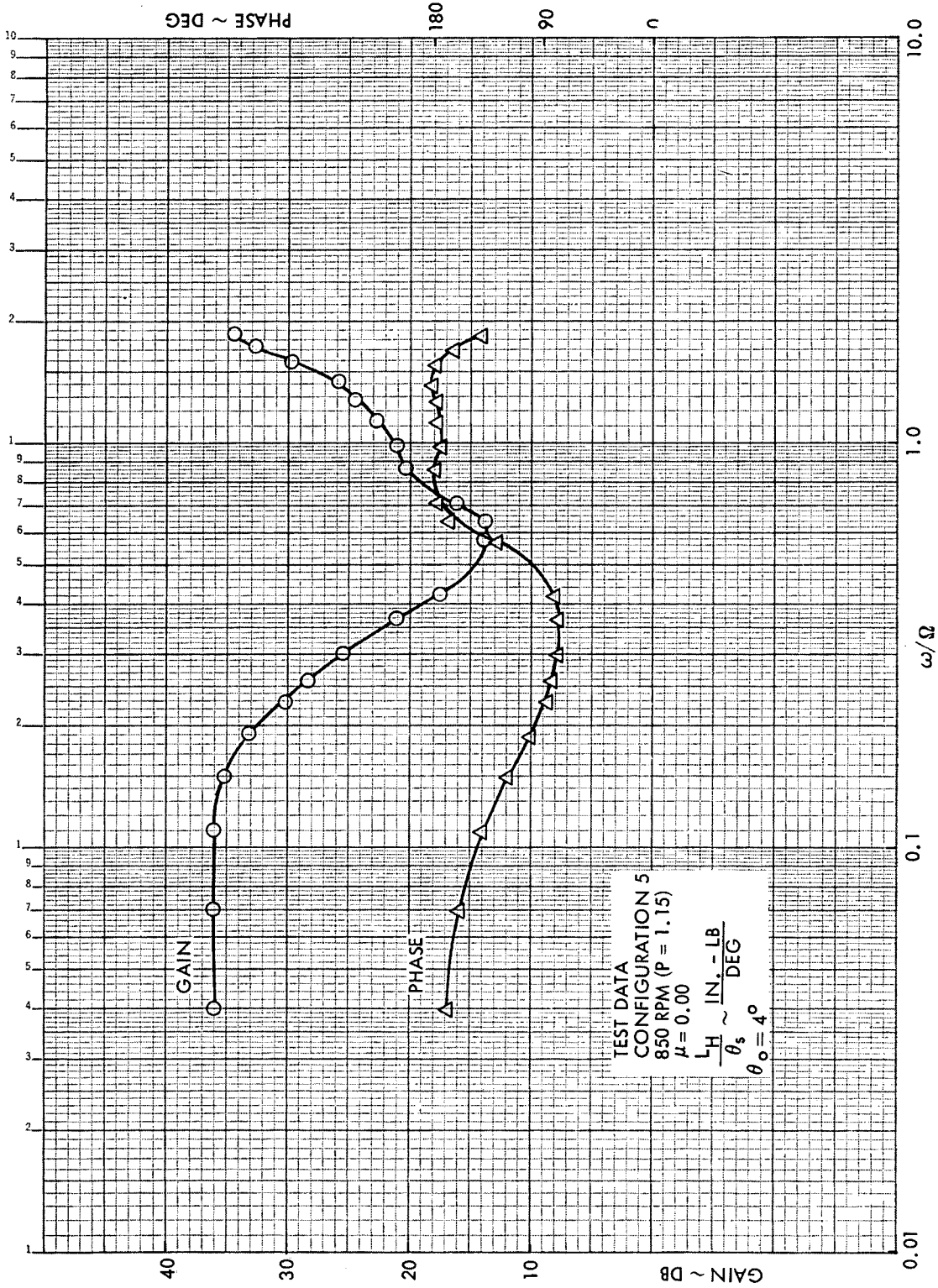


Figure B10. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.00$ , 850 RPM (P = 1.15)

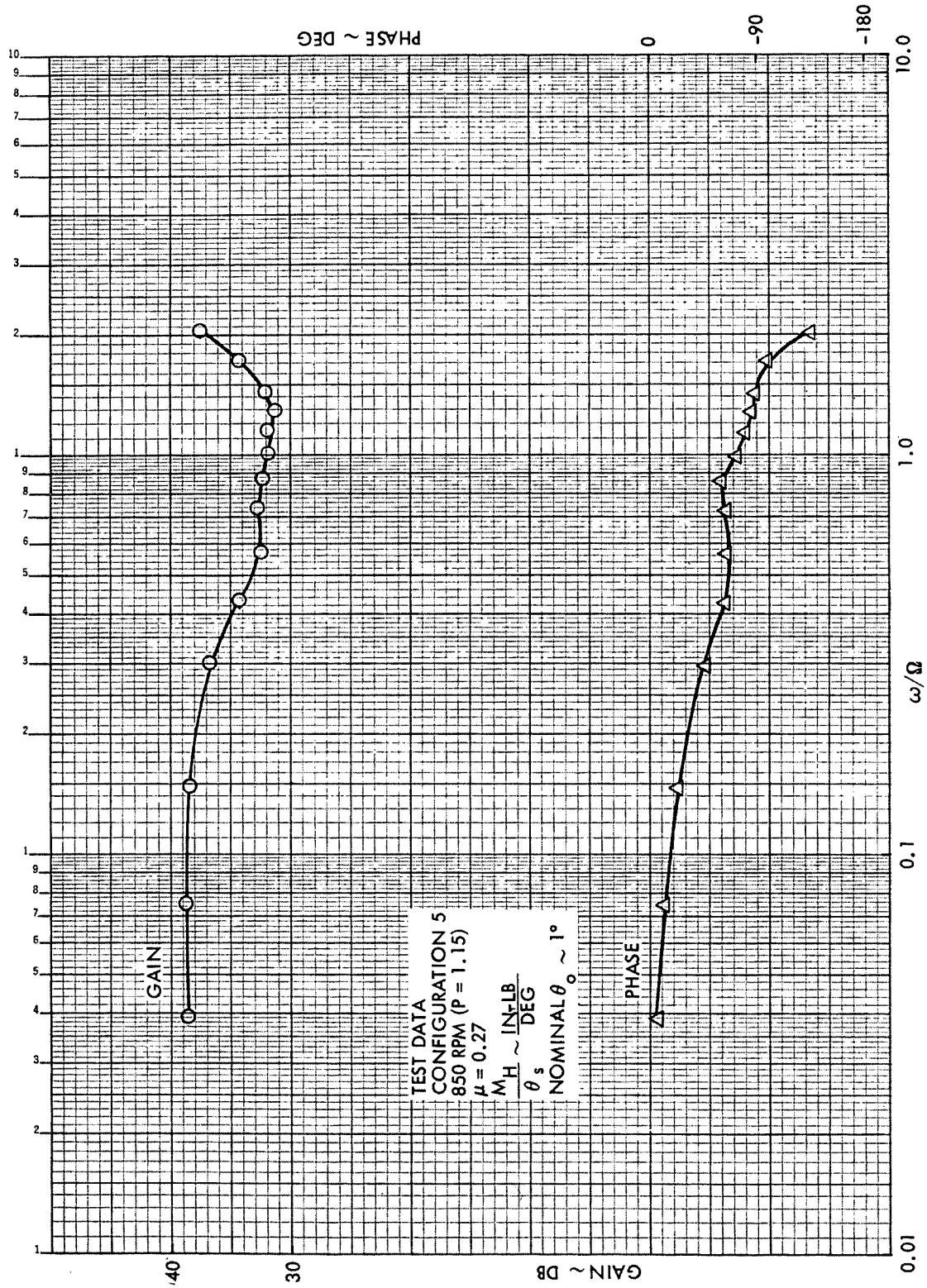


Figure B11. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )

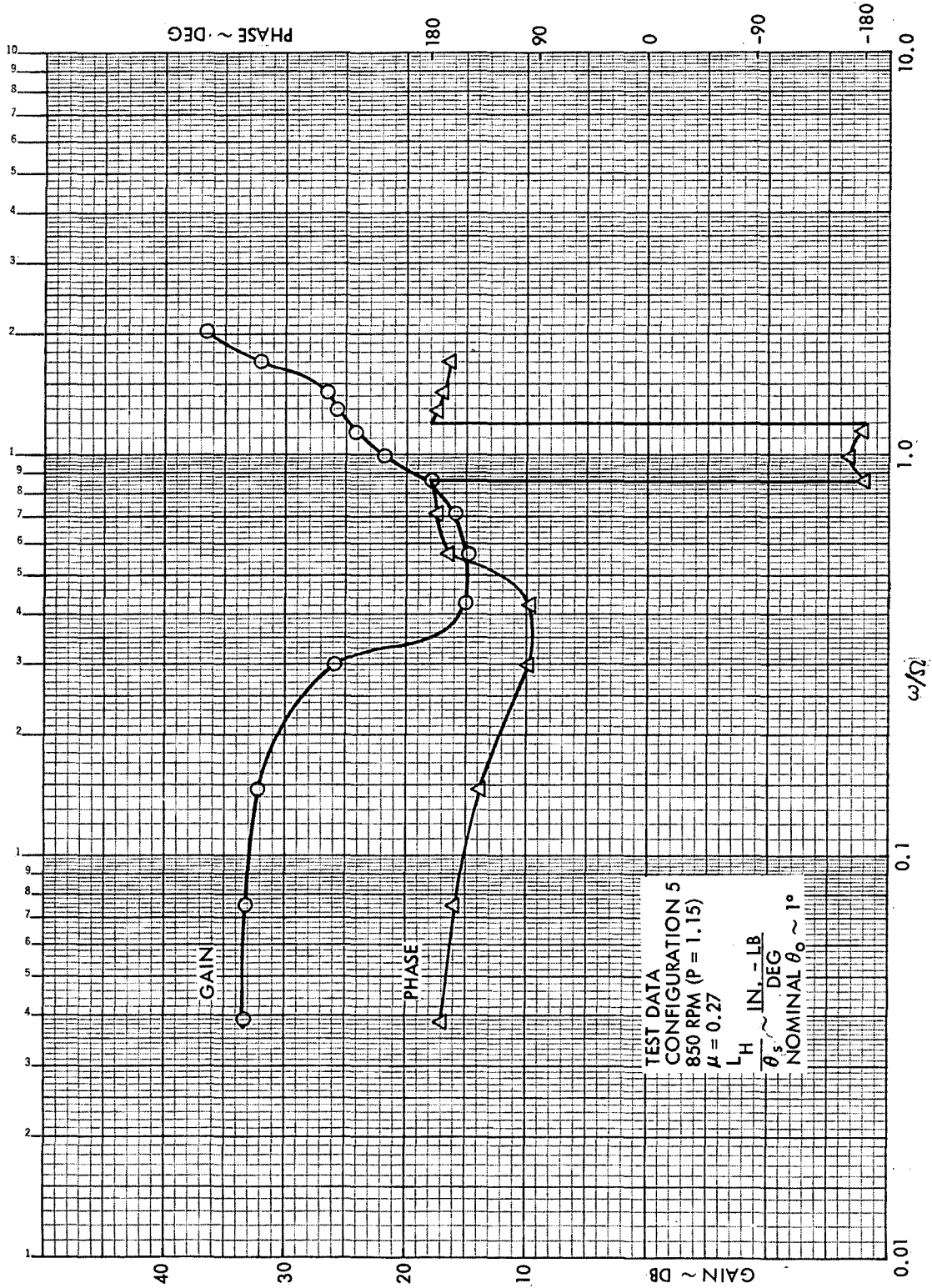


Figure B12. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)

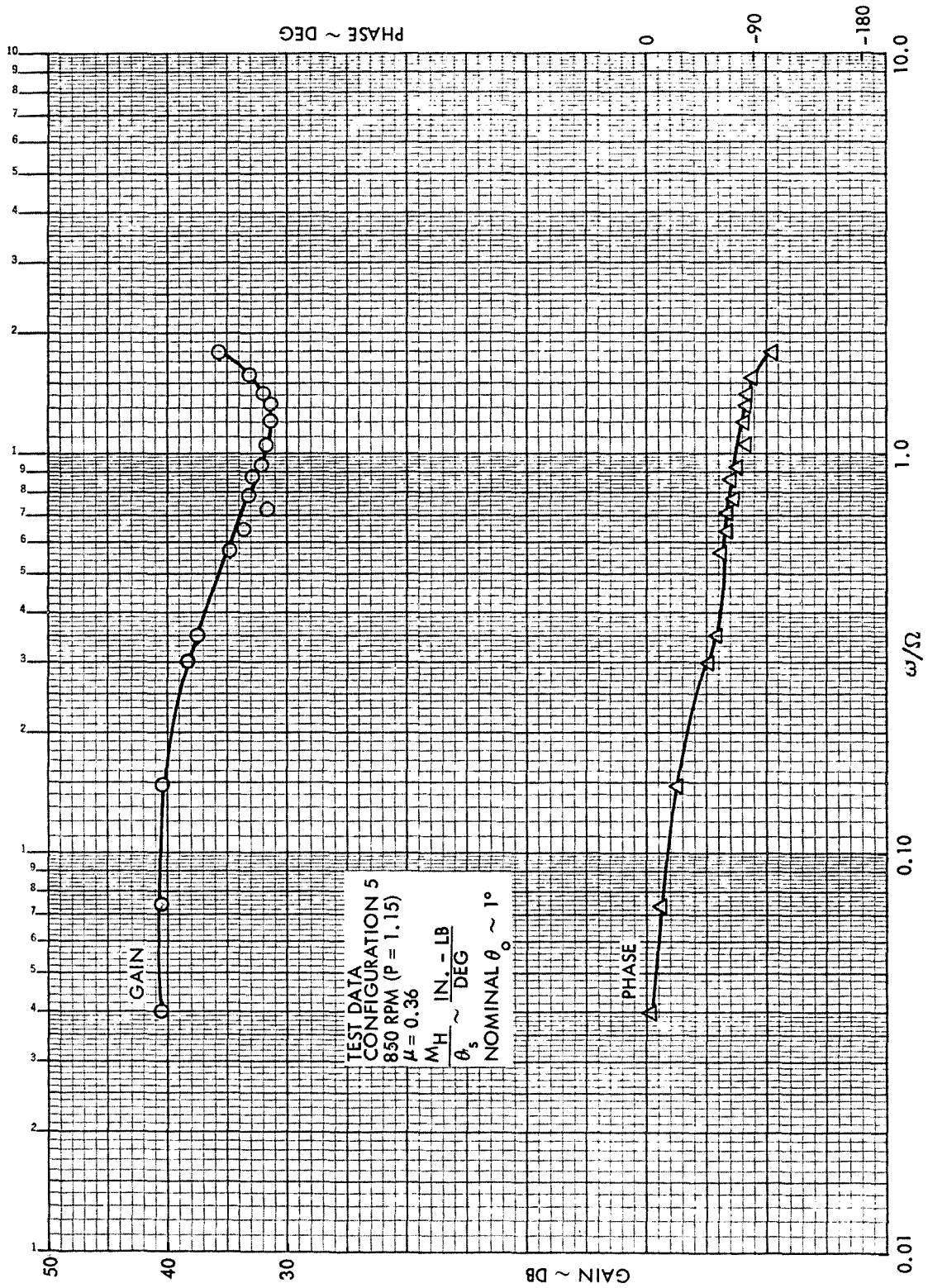


Figure B13. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)





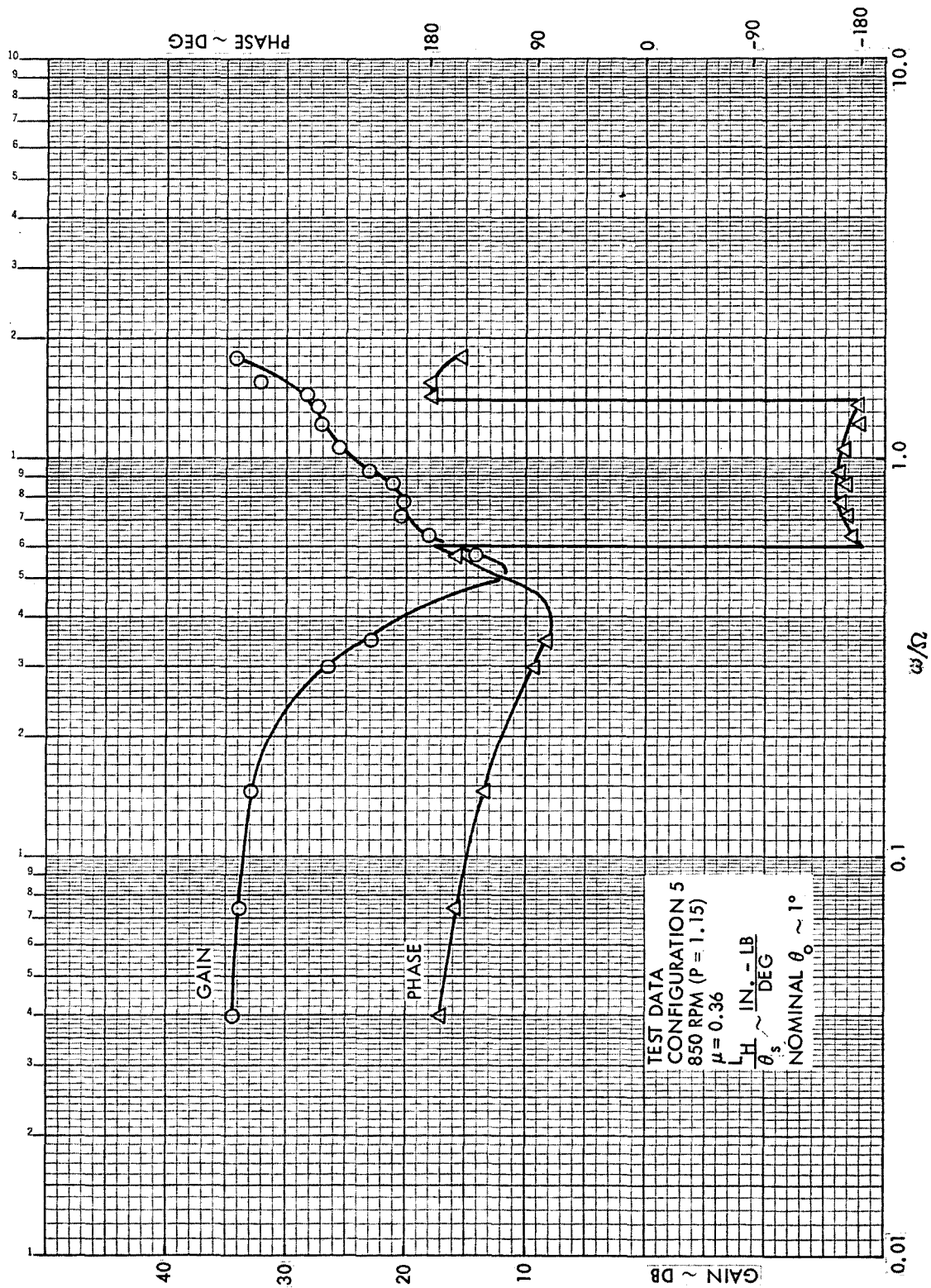


Figure B14. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM ( $P = 1.15$ )

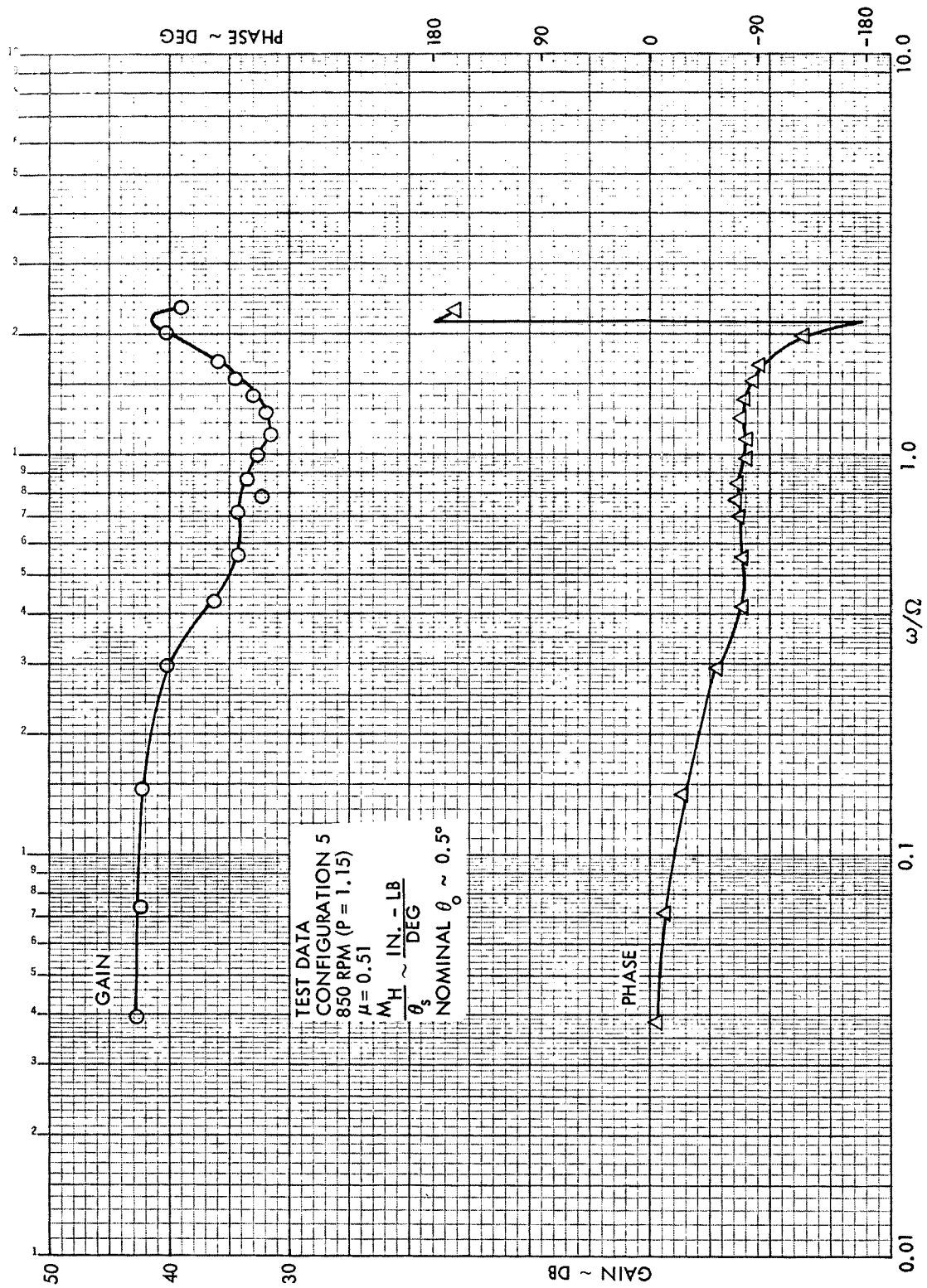


Figure B15. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)



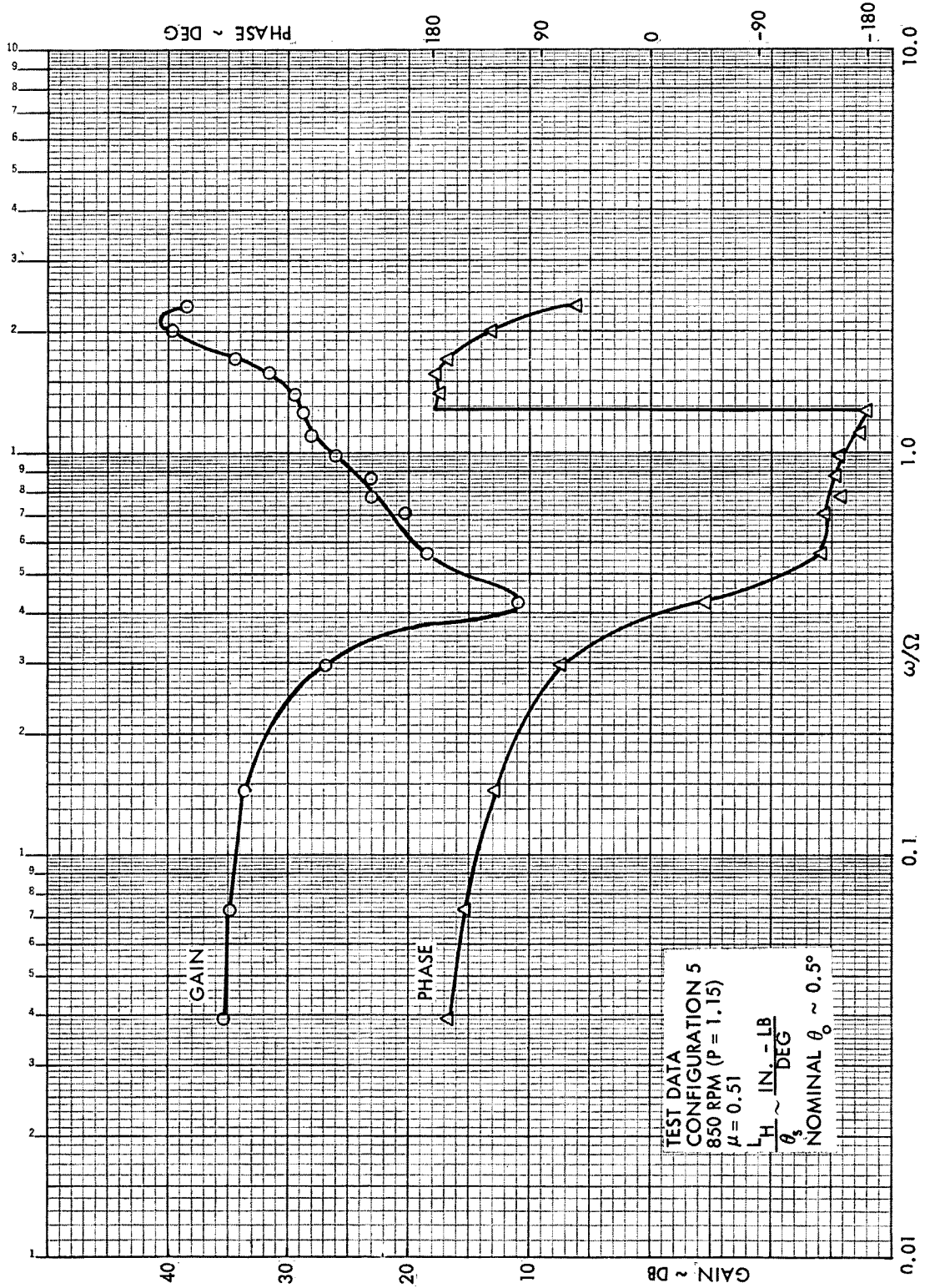


Figure B16. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)

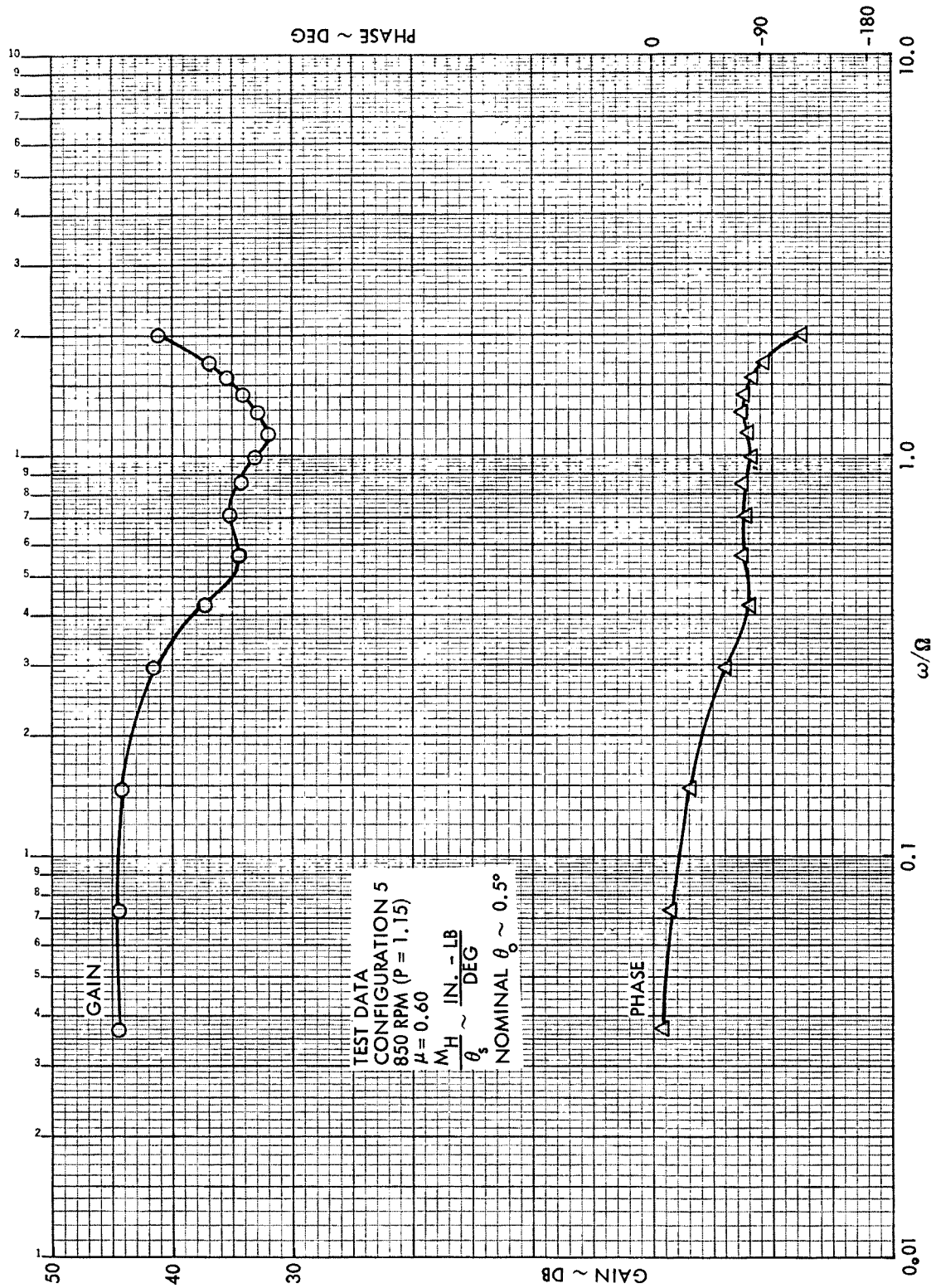


Figure B17. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )

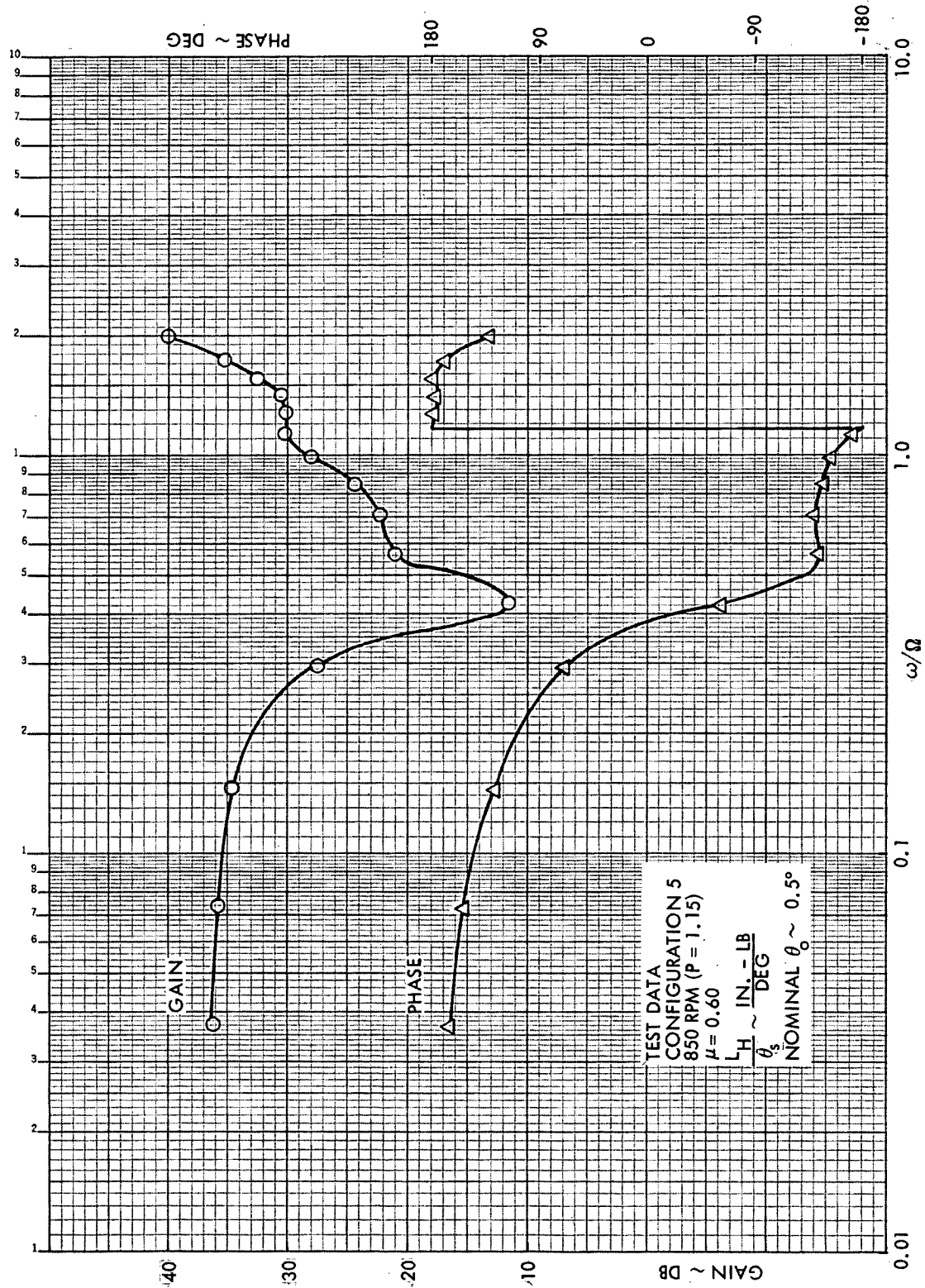


Figure B18. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )

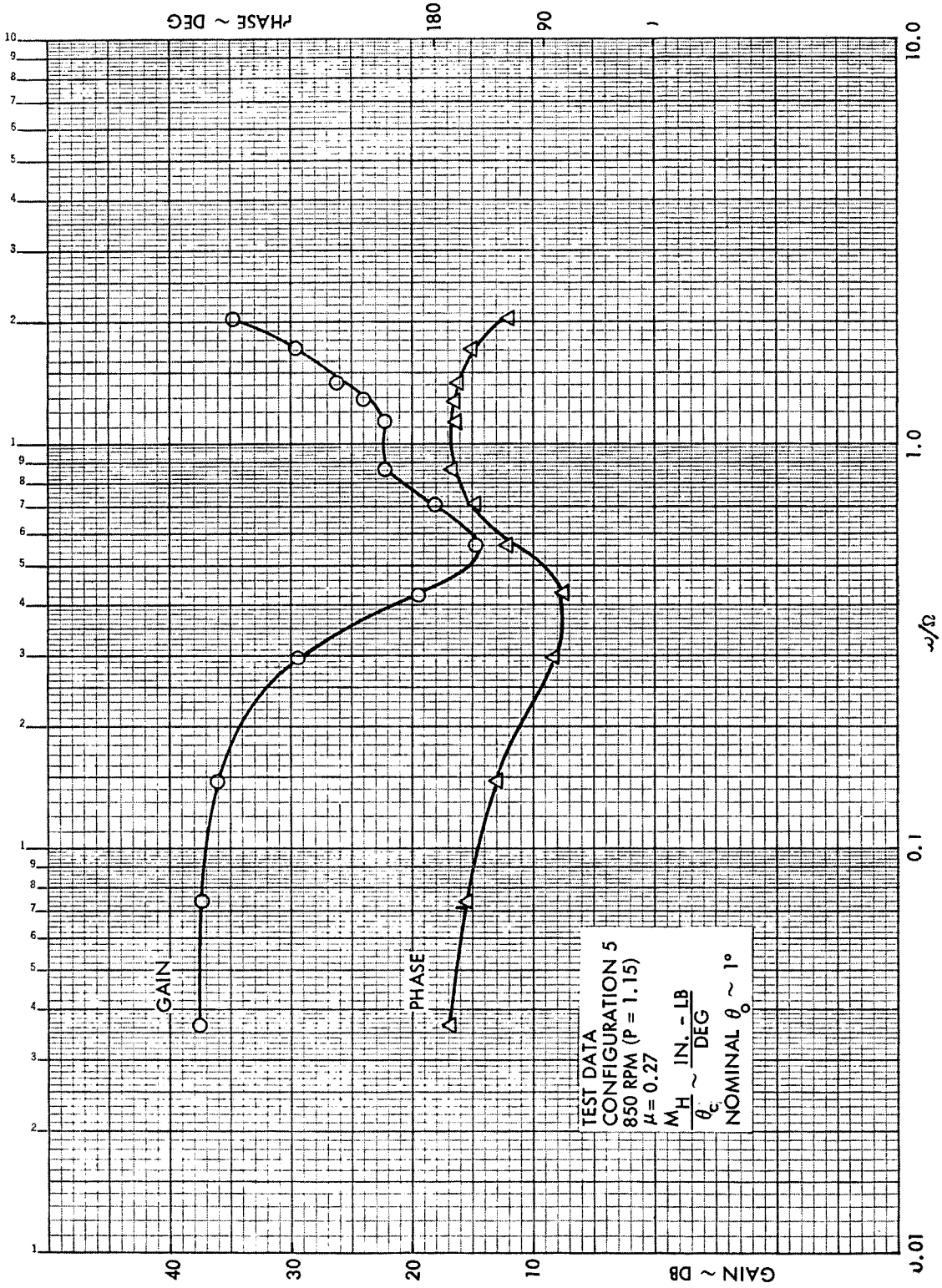


Figure B19. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)

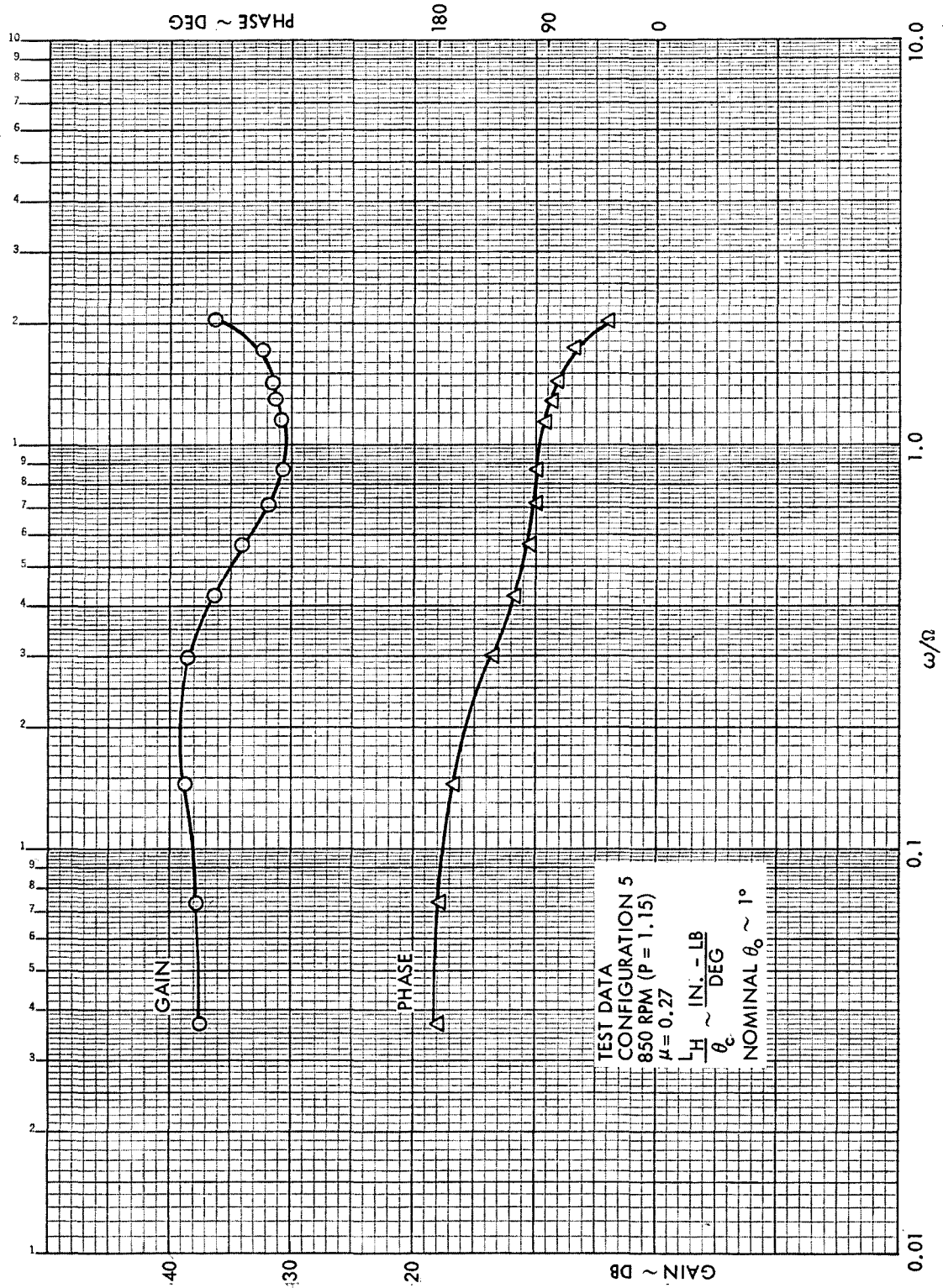
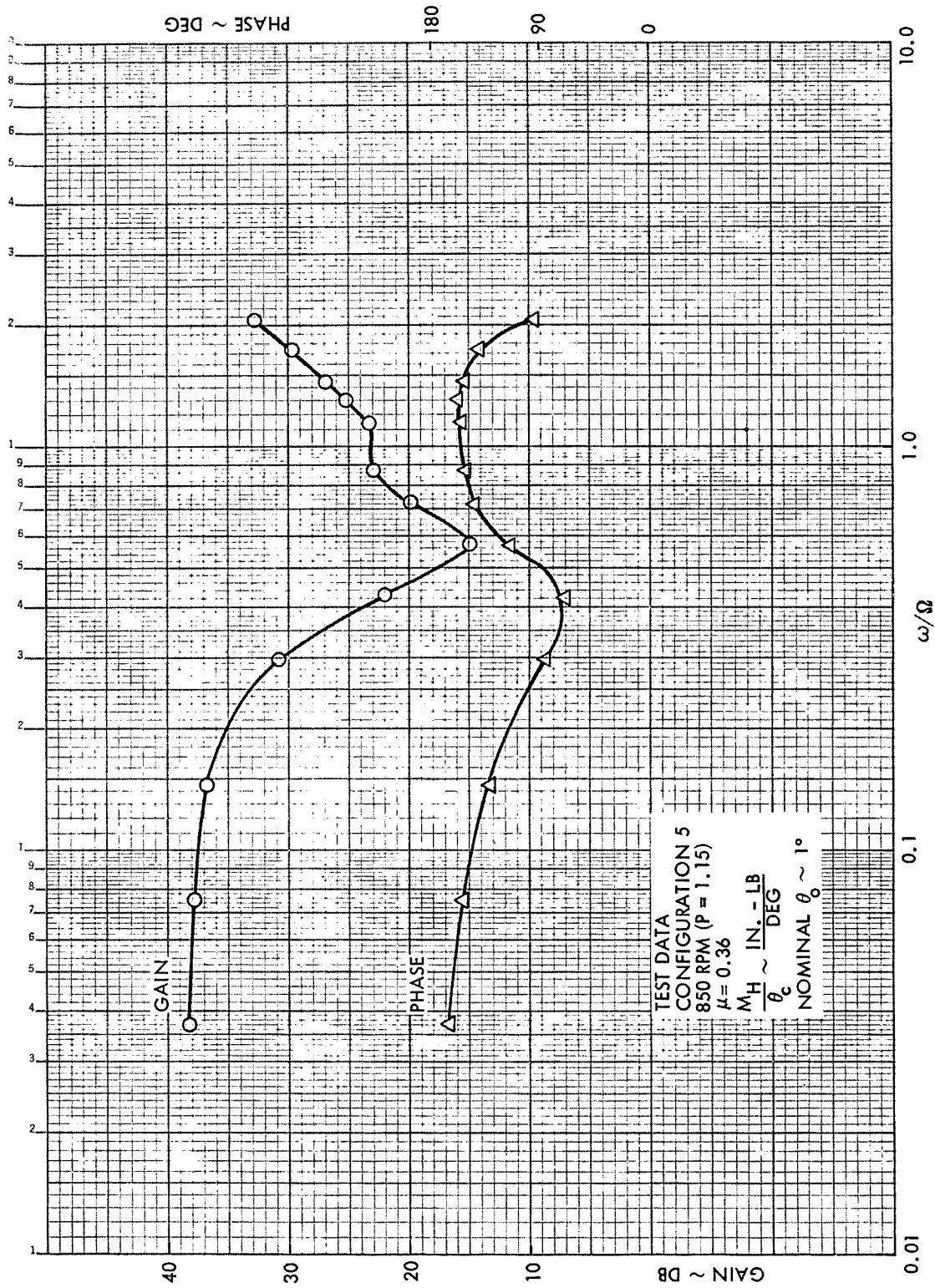


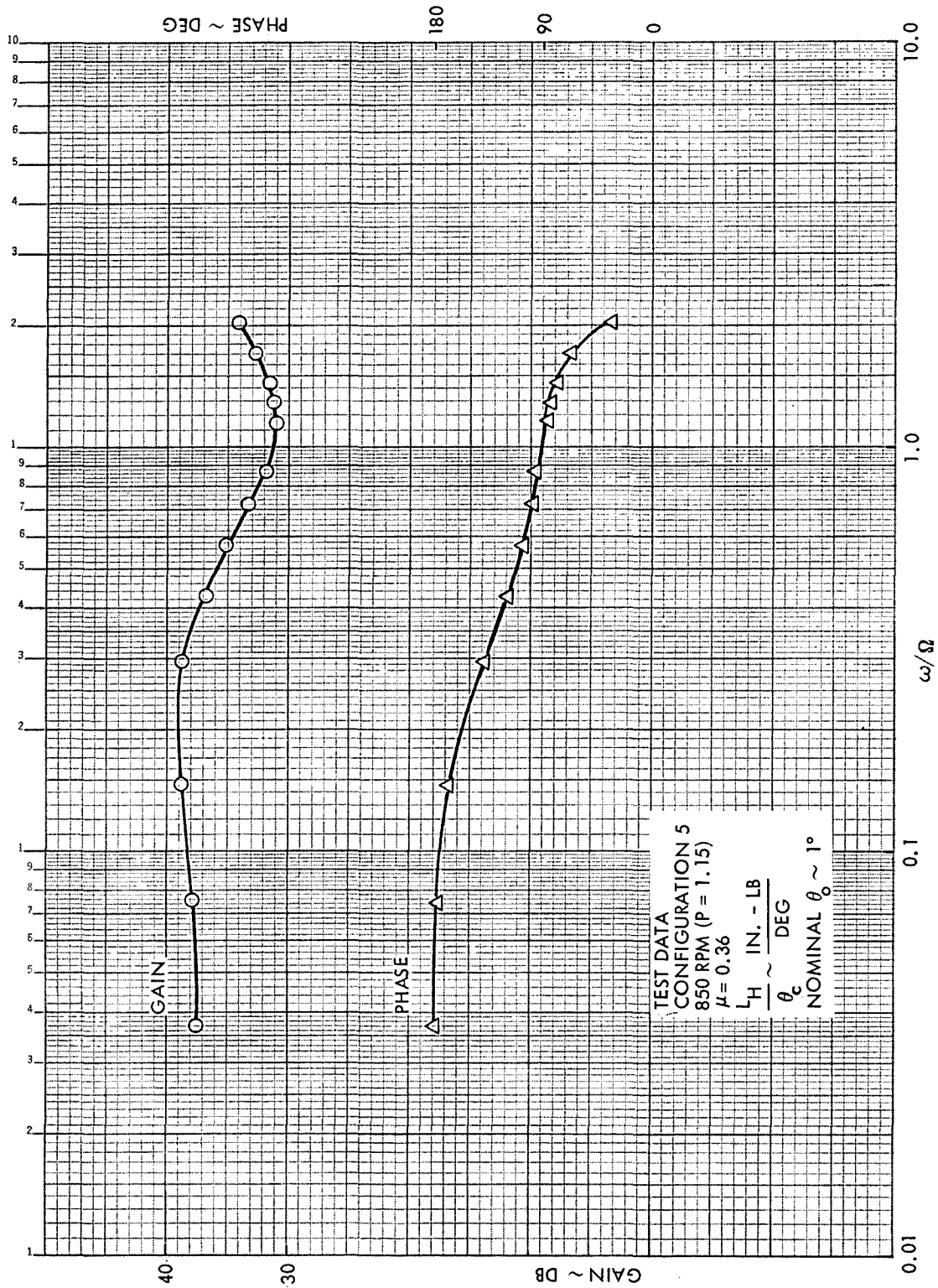
Figure B20. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM (P = 1.15)



TEST DATA  
 CONFIGURATION 5  
 850 RPM (P = 1.15)  
 $\mu = 0.36$   
 $\frac{MH}{\theta_c} \sim \frac{IN.-LB}{DEG}$   
 NOMINAL  $\theta_c \sim 1^\circ$

Figure B21. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)





TEST DATA  
 CONFIGURATION 5  
 850 RPM (P = 1.15)  
 $\mu = 0.36$   
 $L_H \sim \frac{IN. - LB}{\theta_c}$   
 NOMINAL  $\theta_0 \sim 1^\circ$

Figure B22. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)

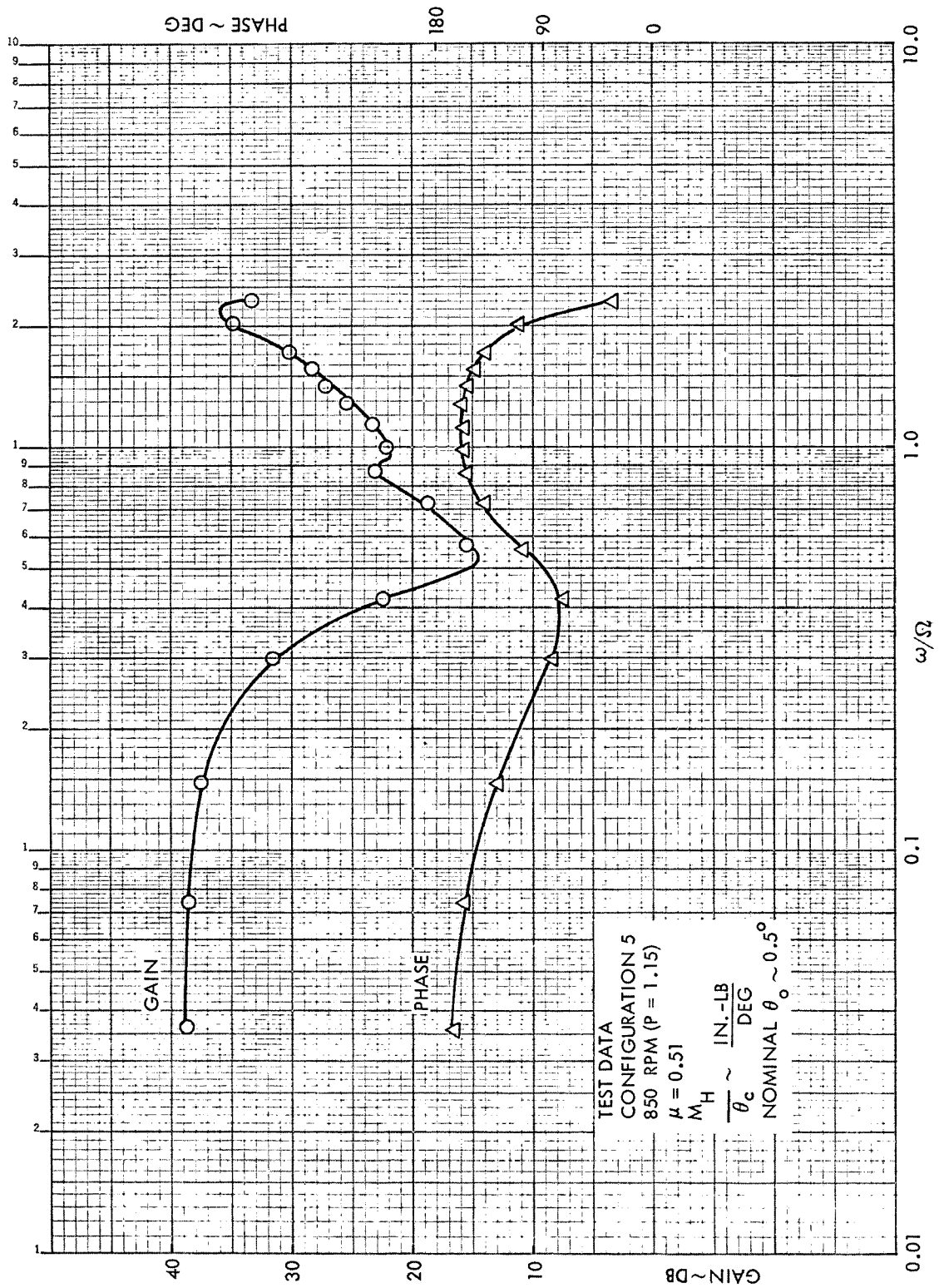
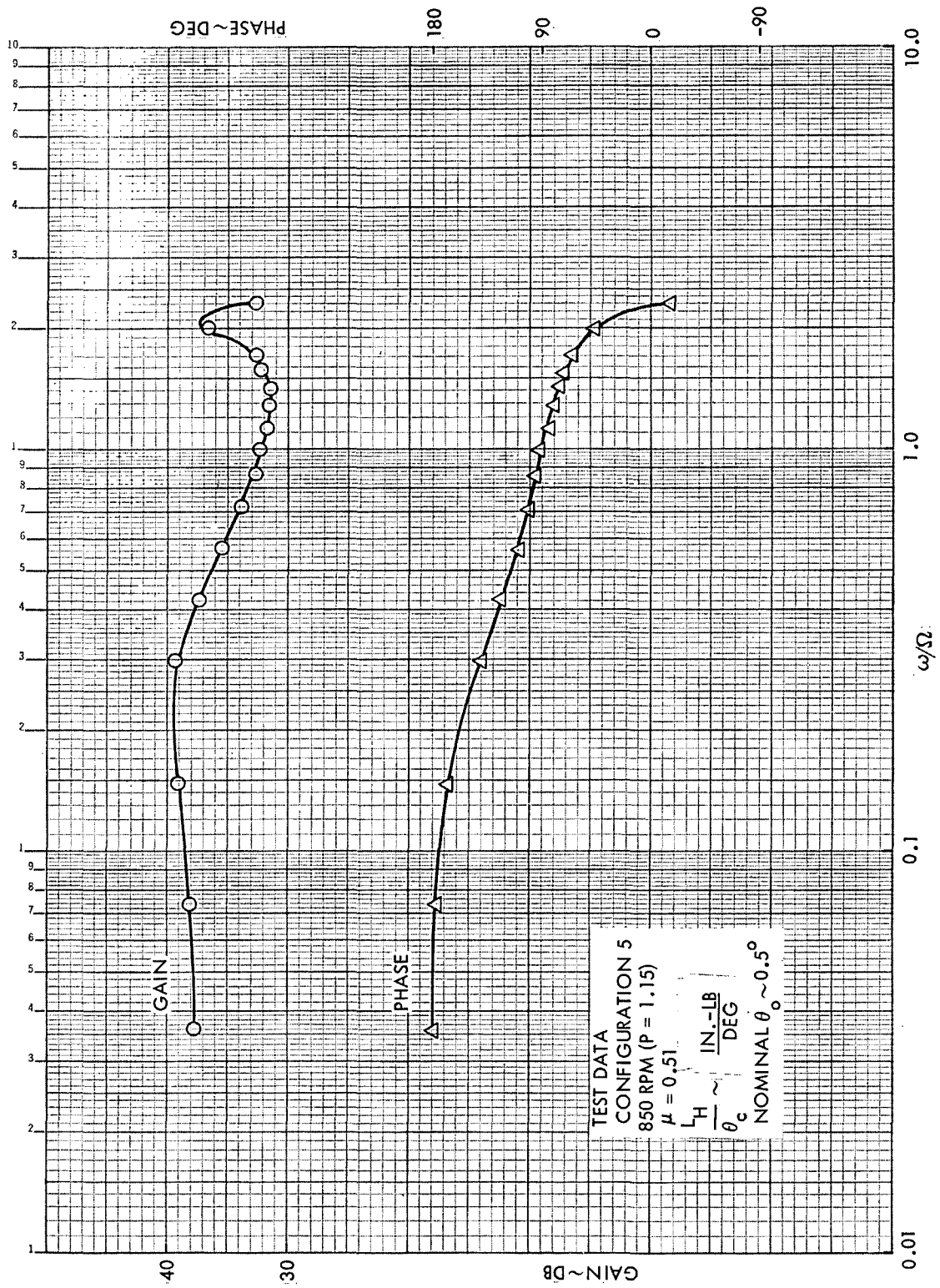


Figure B23. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)





TEST DATA  
 CONFIGURATION 5  
 850 RPM (P = 1.15)  
 $\mu = 0.51$   
 $\frac{L_H}{\theta_c} \sim \frac{\text{IN.-LB}}{\text{DEG}}$   
 NOMINAL  $\theta_0 \sim 0.5^\circ$

Figure B24. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM (P = 1.15)

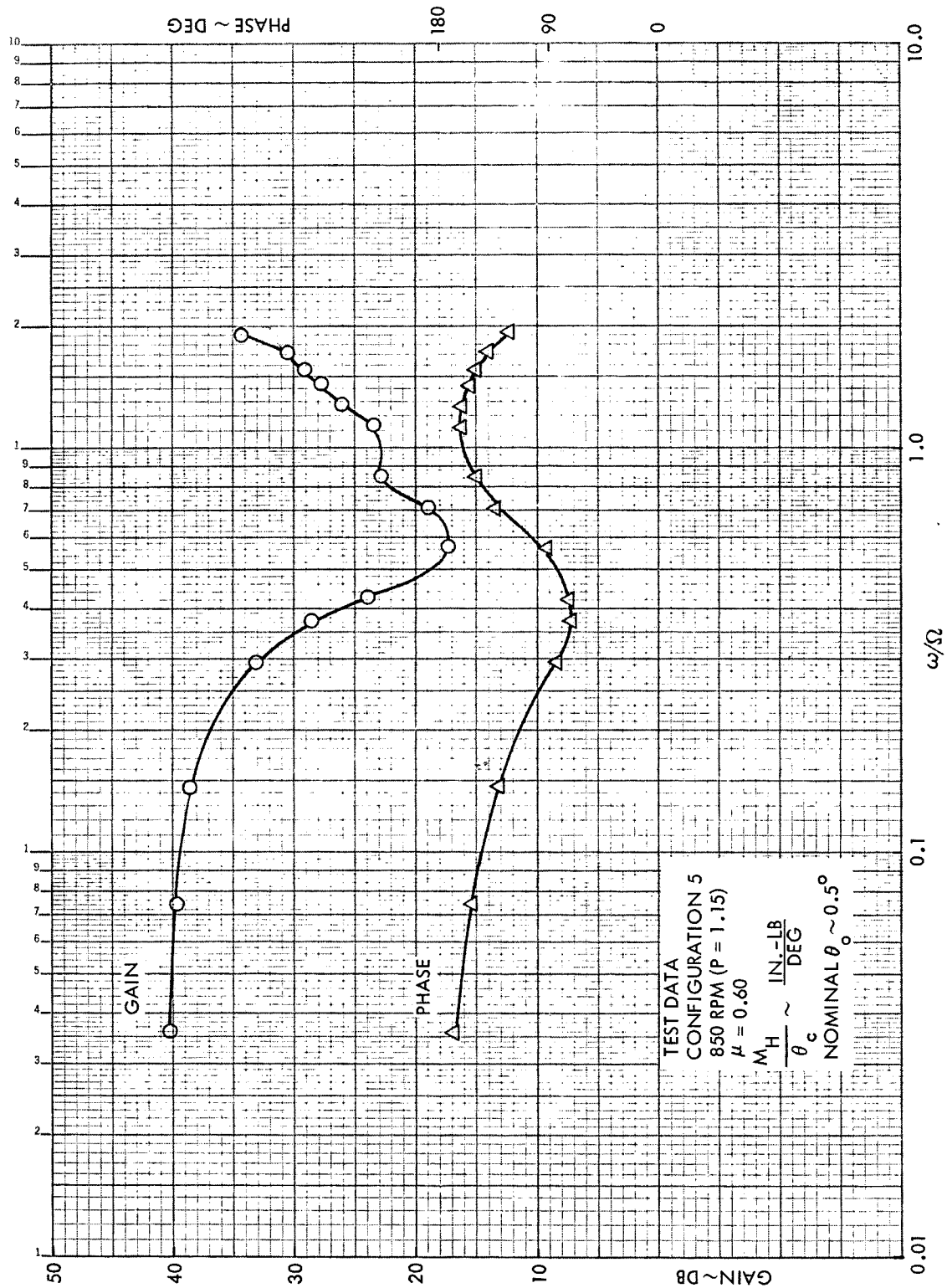


Figure B25. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM (P = 1.15)

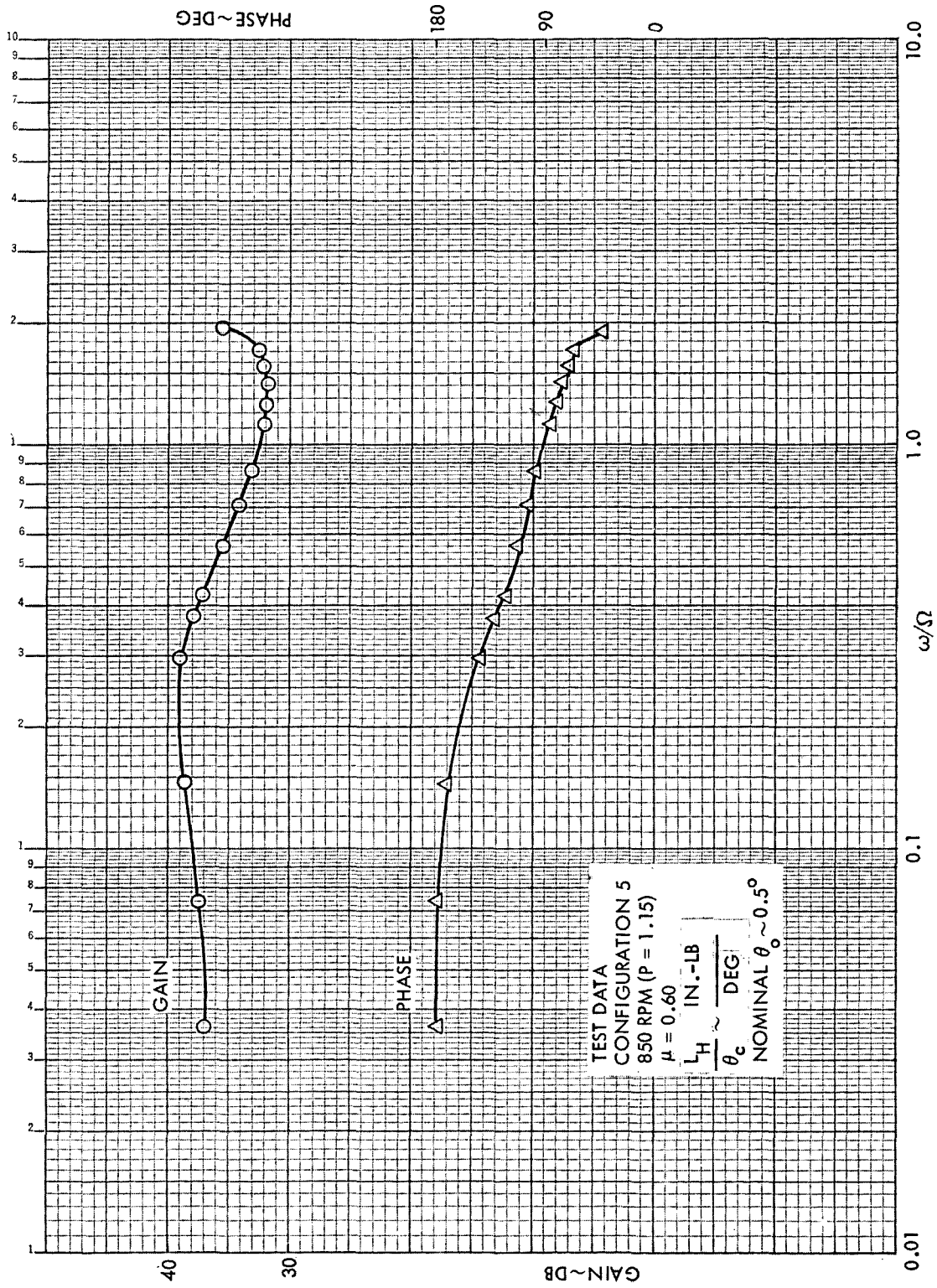


Figure B26. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )

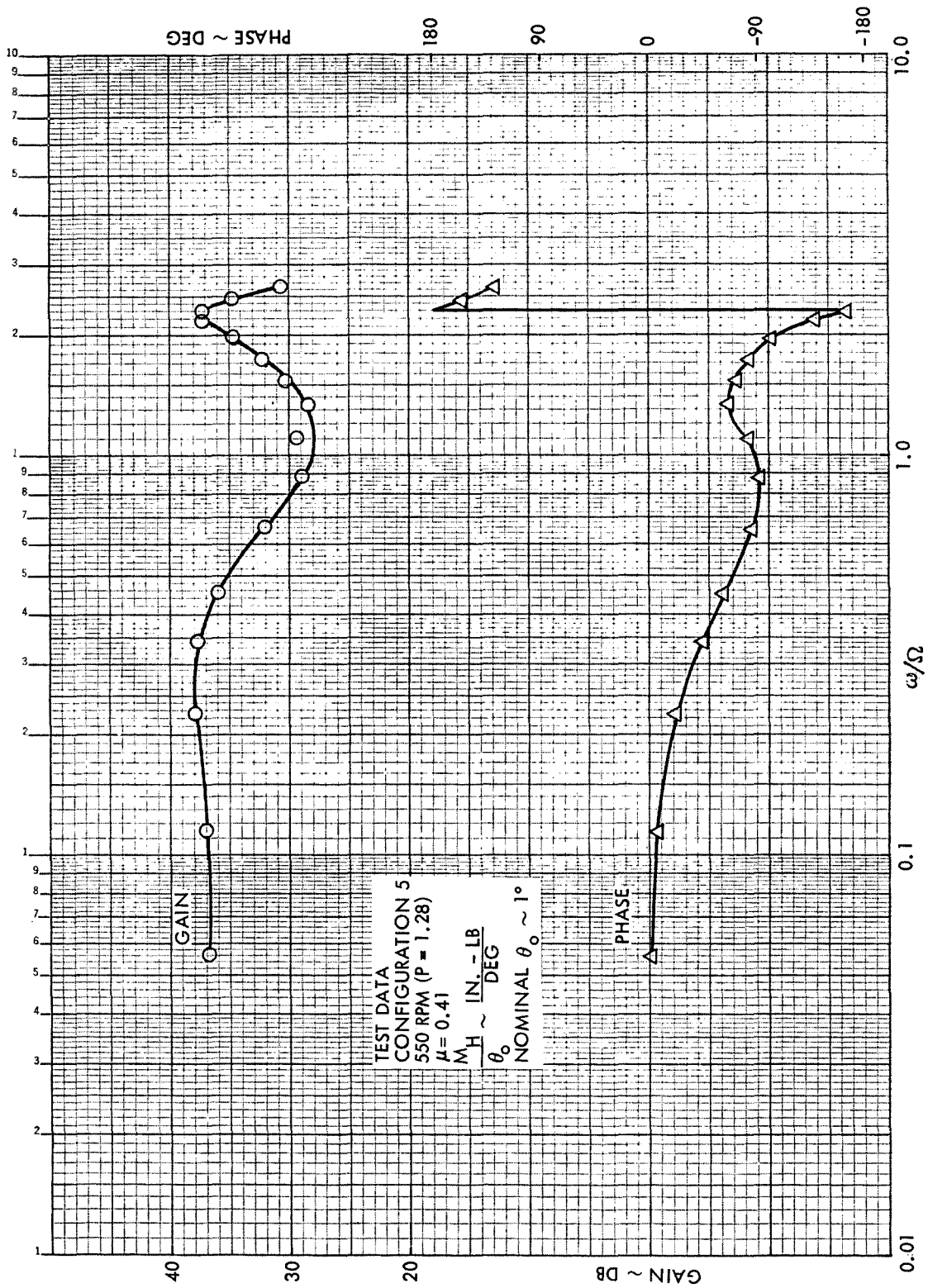


Figure B27. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM (P = 1.28)



F

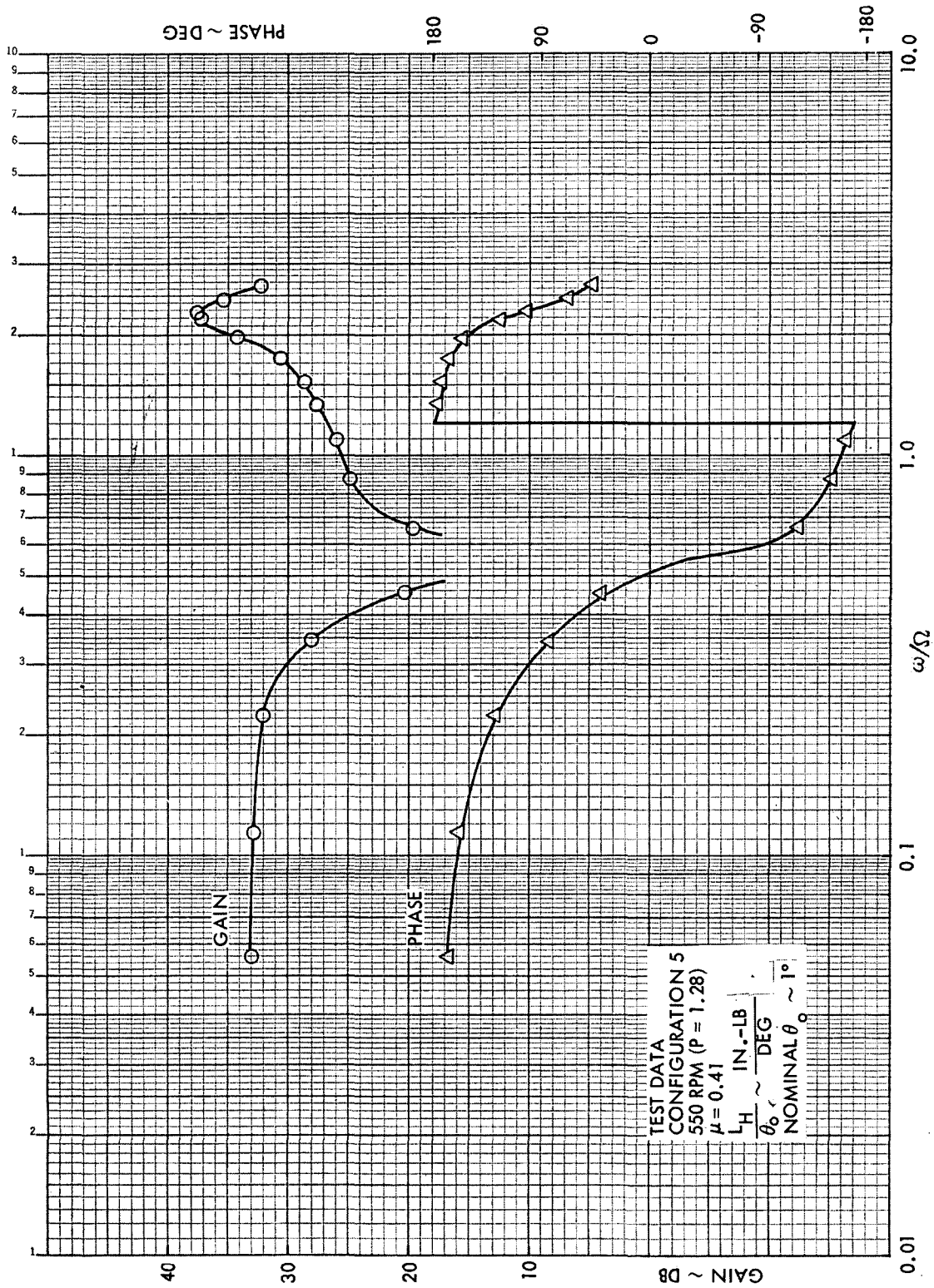


Figure B28. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM ( $P = 1.28$ )



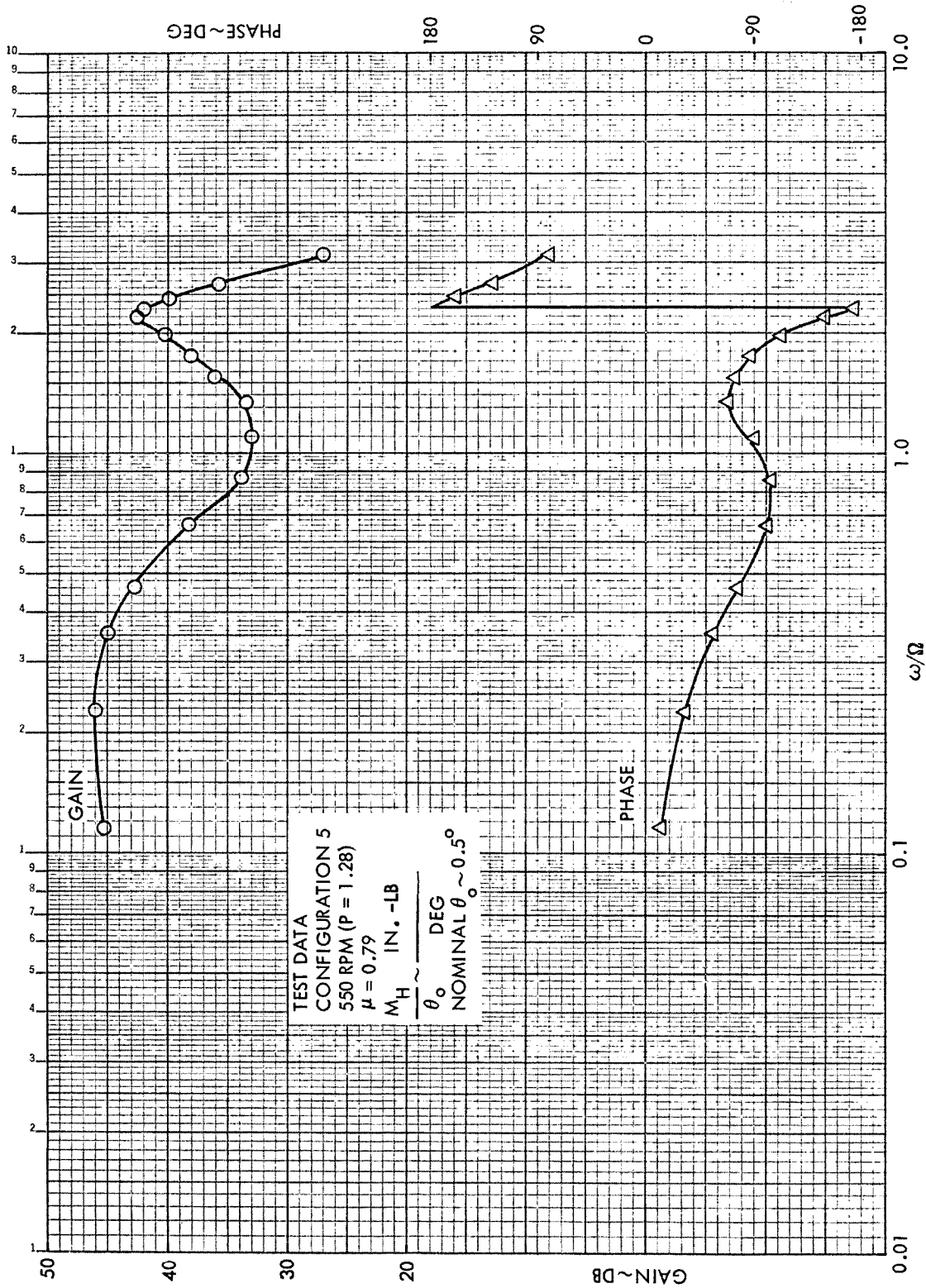


Figure B29. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM ( $P = 1.28$ )



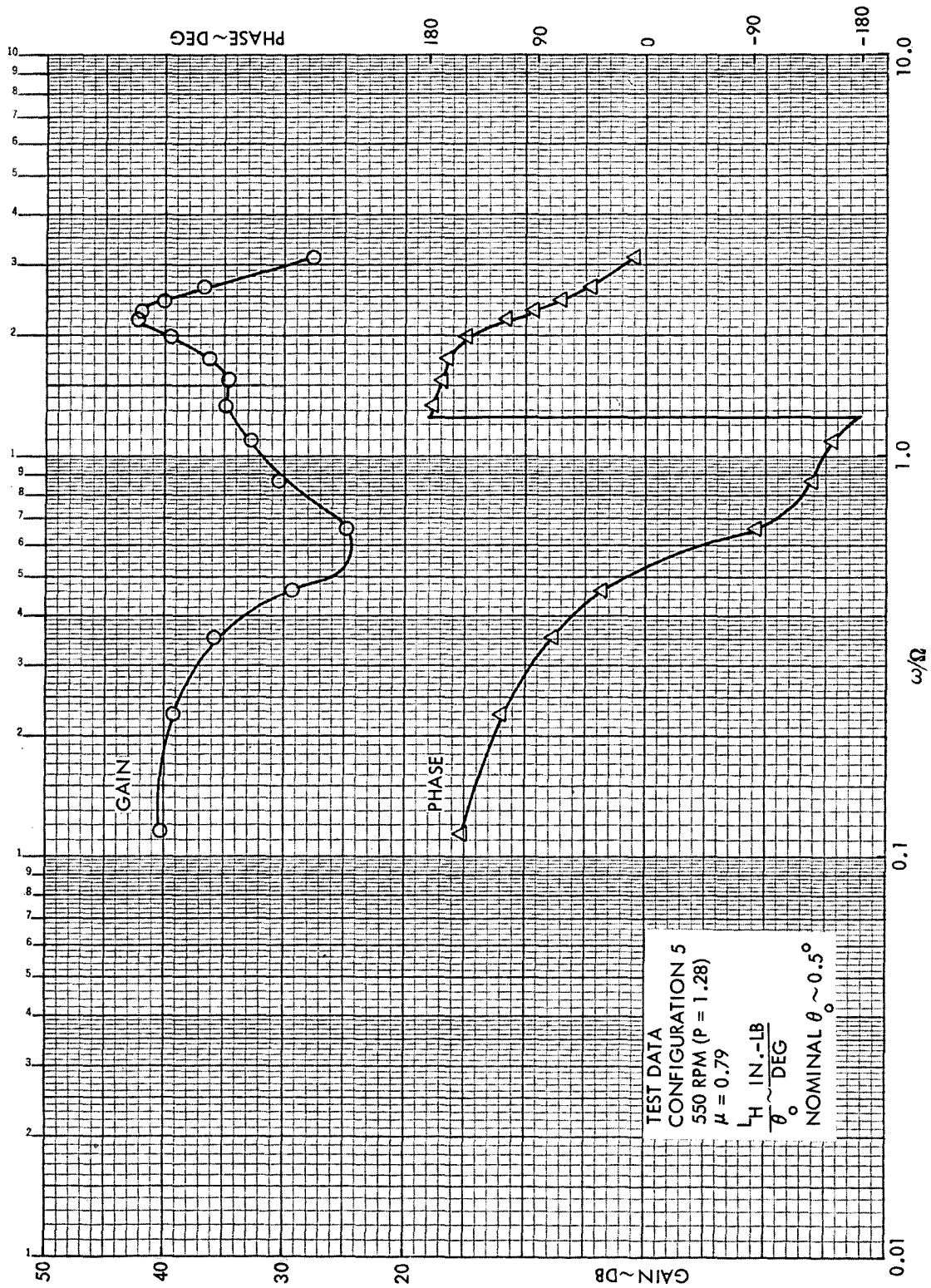


Figure B30. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM (P = 1.28)

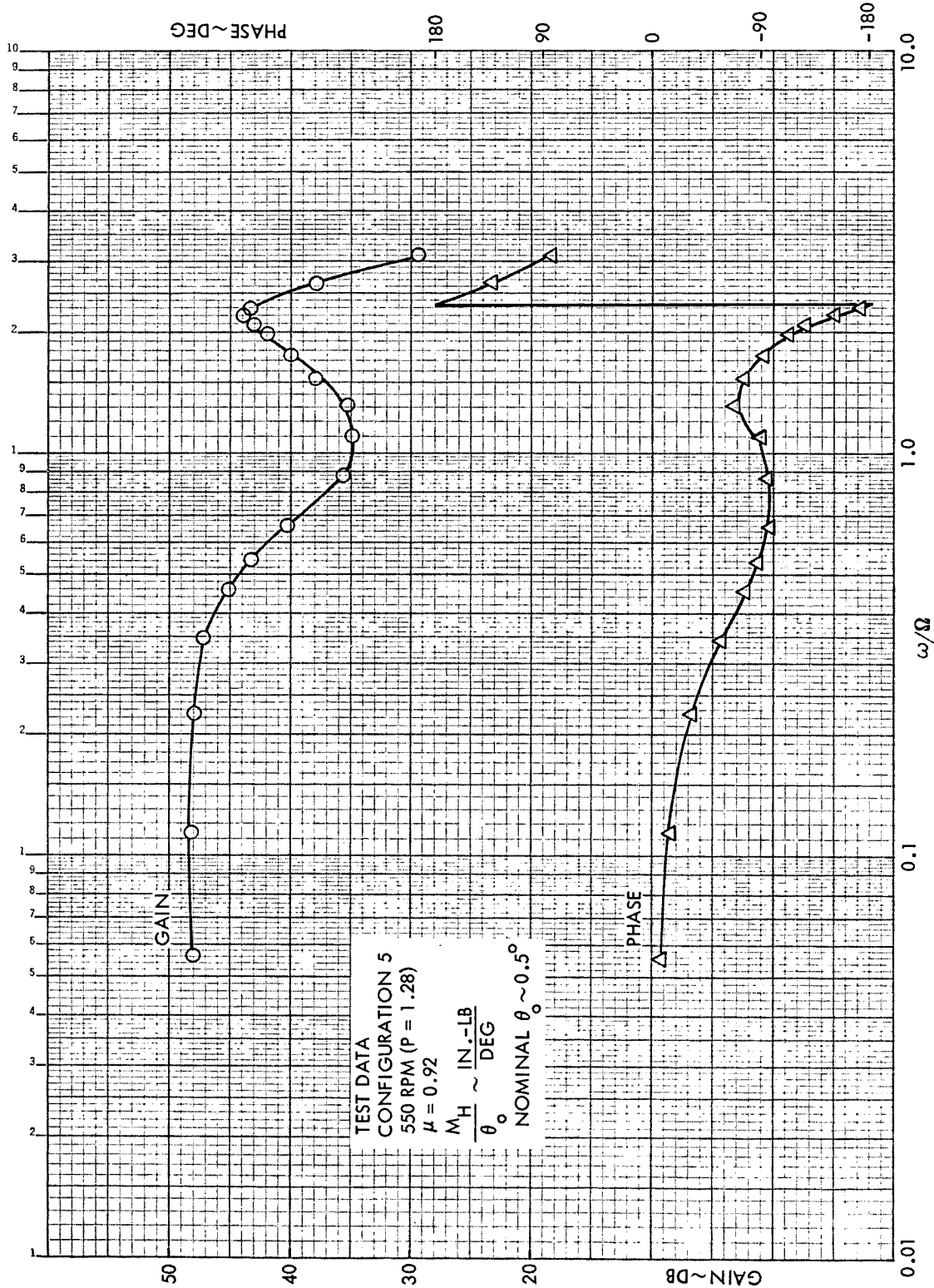


Figure B31. Rotor Hub Pitch Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM (P = 1.28)



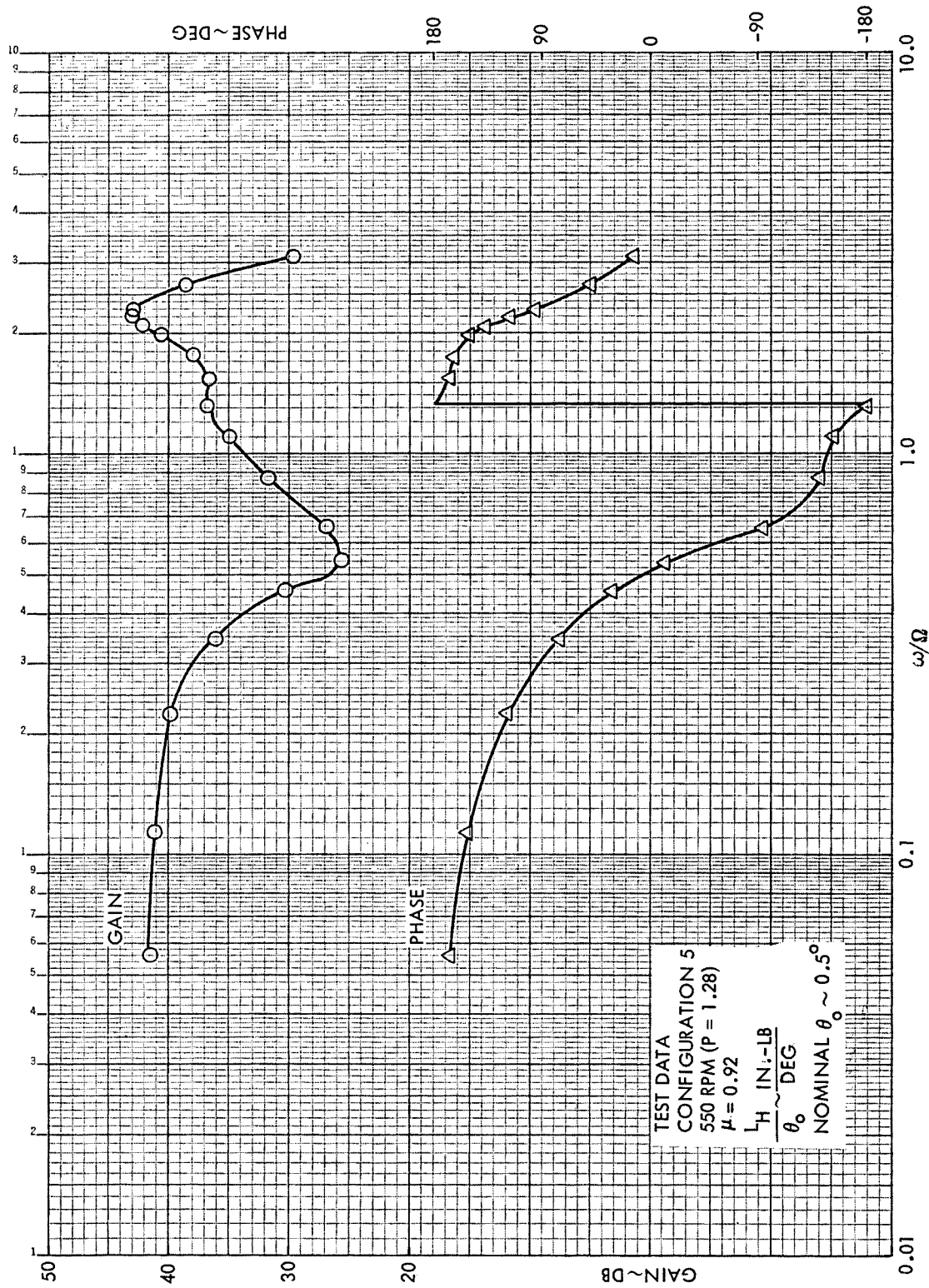
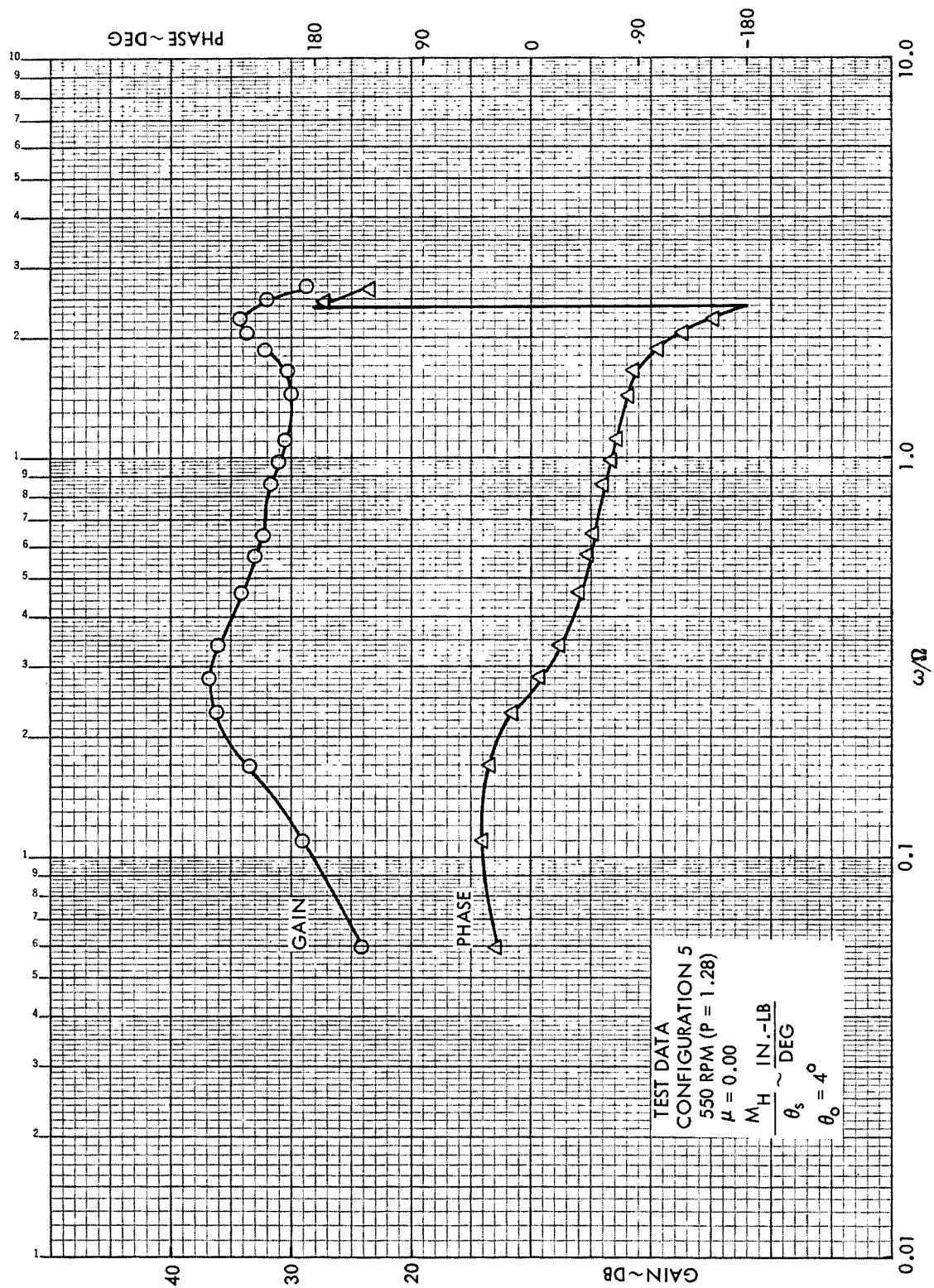


Figure B32. Rotor Hub Roll Moment Frequency Response to Collective Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM (P = 1.28)



TEST DATA  
 CONFIGURATION 5  
 550 RPM (P = 1.28)  
 $\mu = 0.00$   
 $M_H \sim \text{IN.-LB}$   
 $\theta_s \sim \text{DEG}$   
 $\theta_0 = 4^\circ$

Figure B33. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.0$ , 550 RPM (P = 1.28)

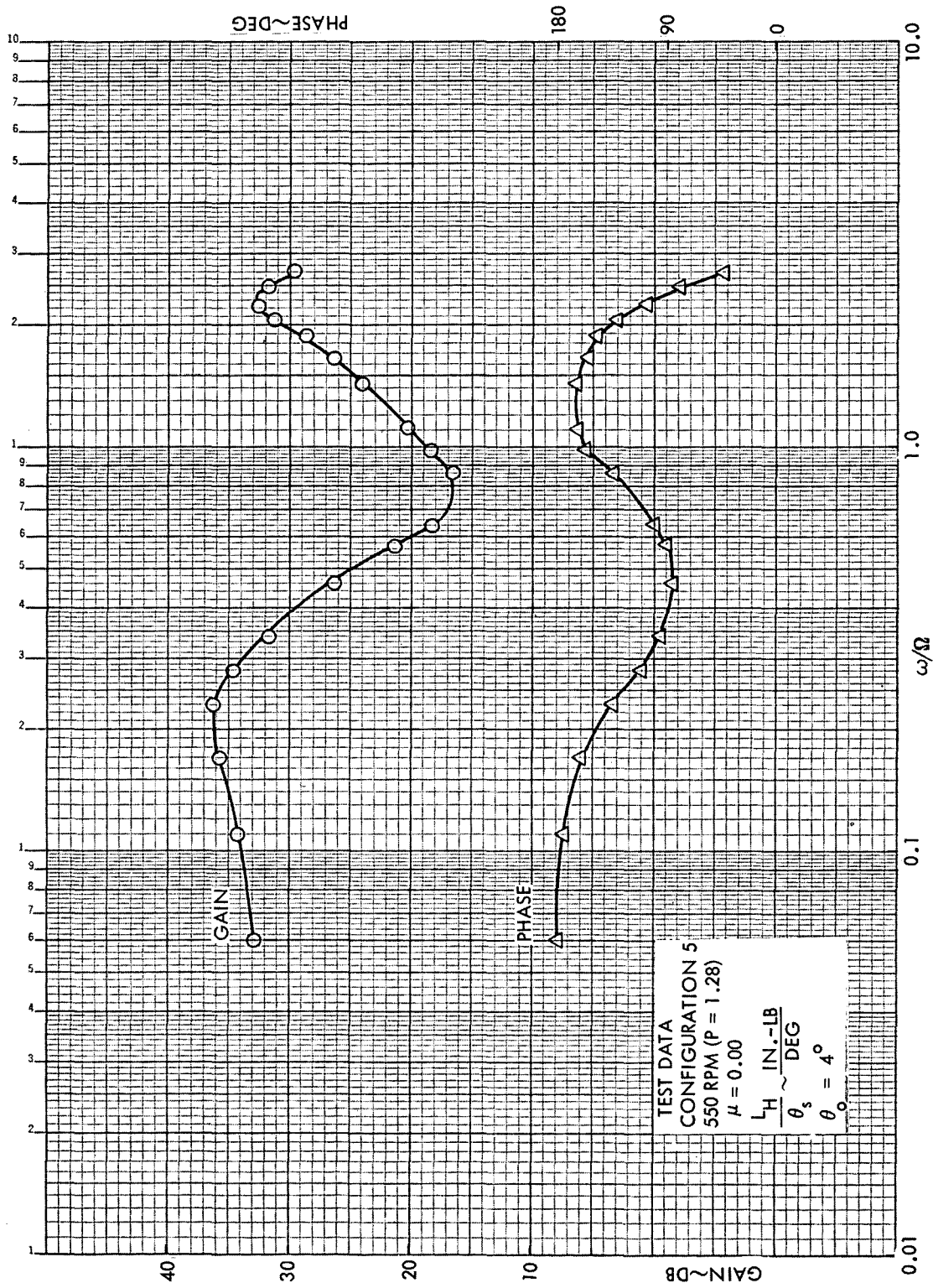


Figure B34. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.0$ , 550 RPM (P = 1.28)

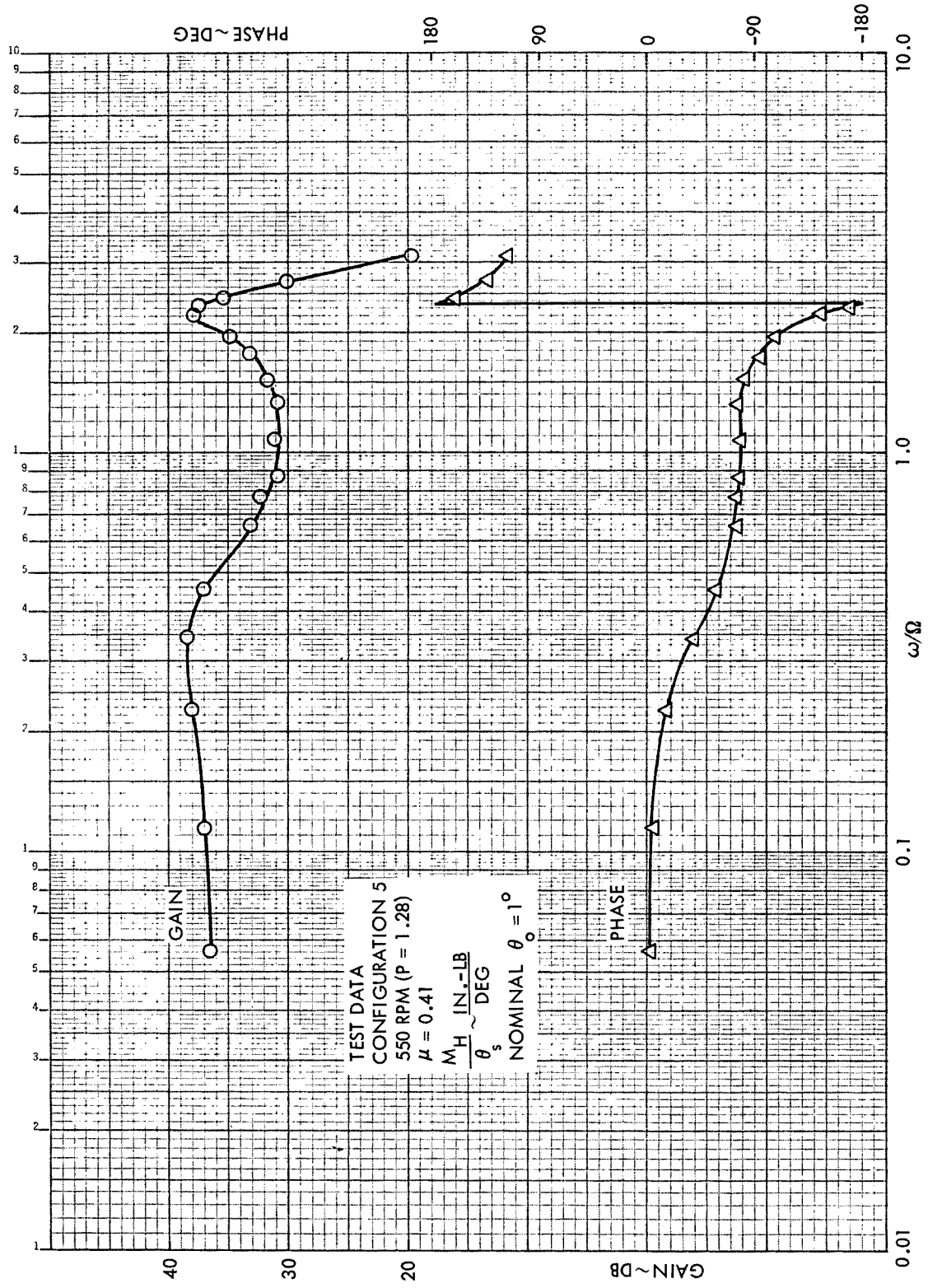


Figure B35. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM (P = 1.28)

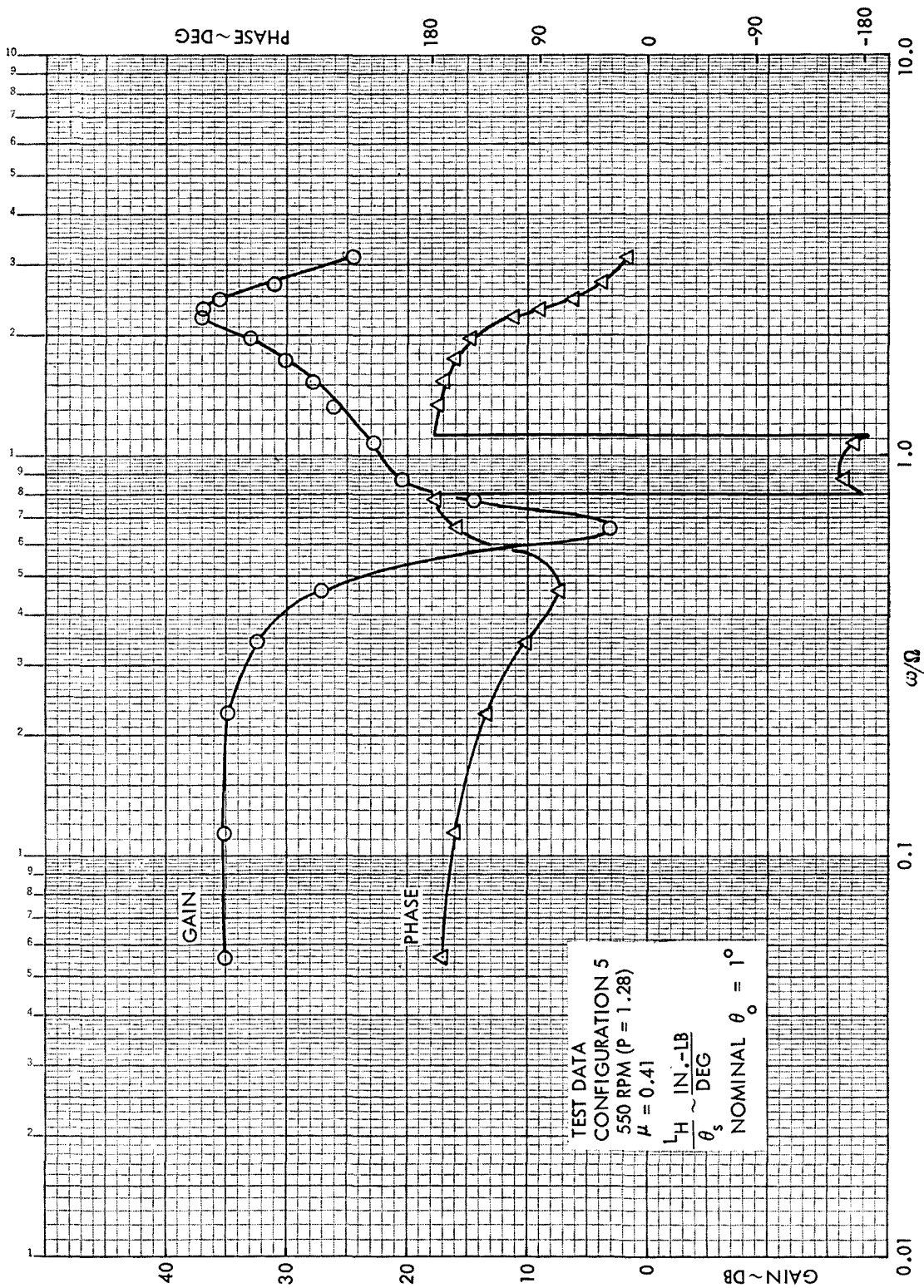


Figure B36. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM (P = 1.28)

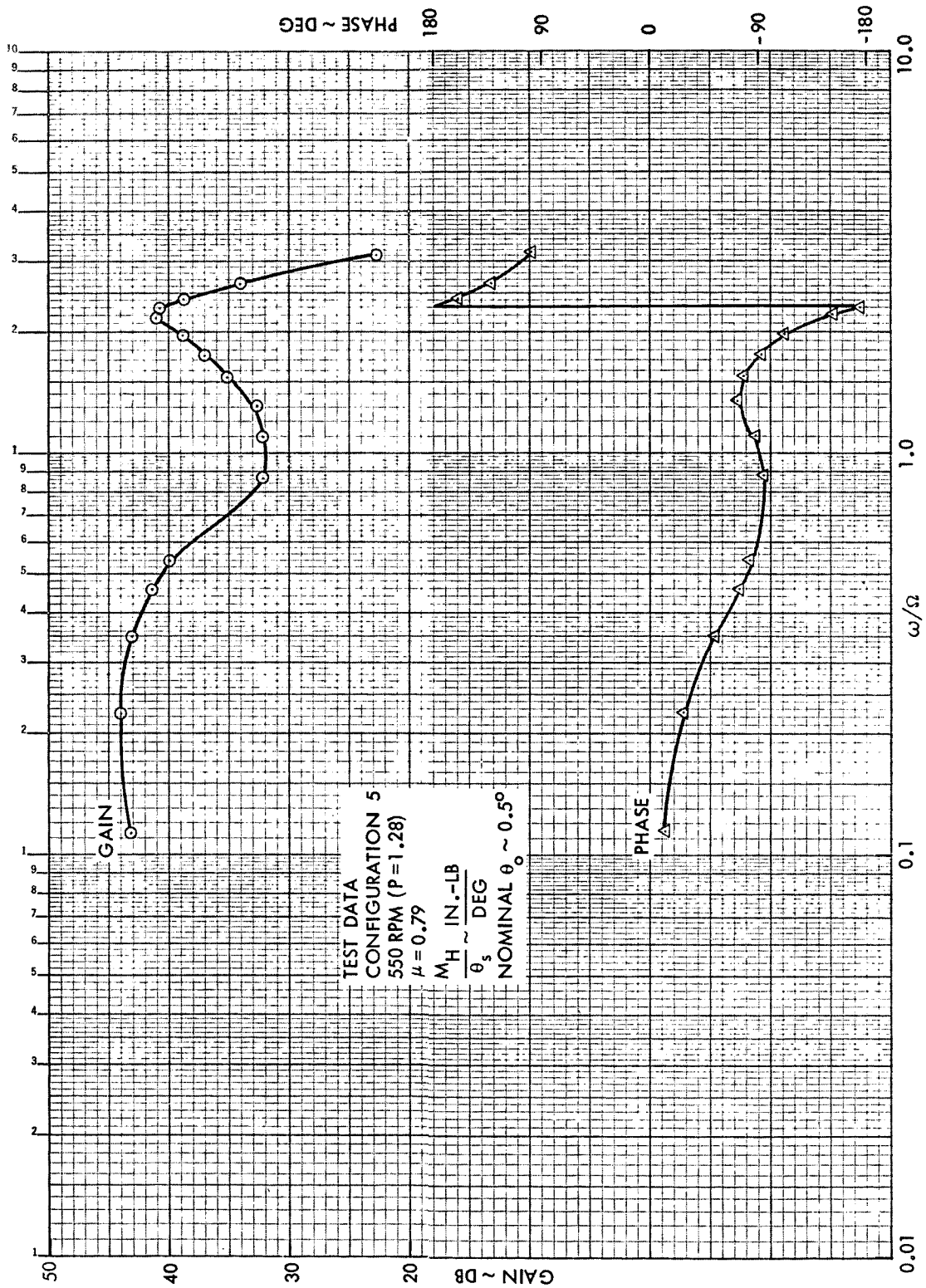


Figure B37. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM ( $P = 1.28$ )



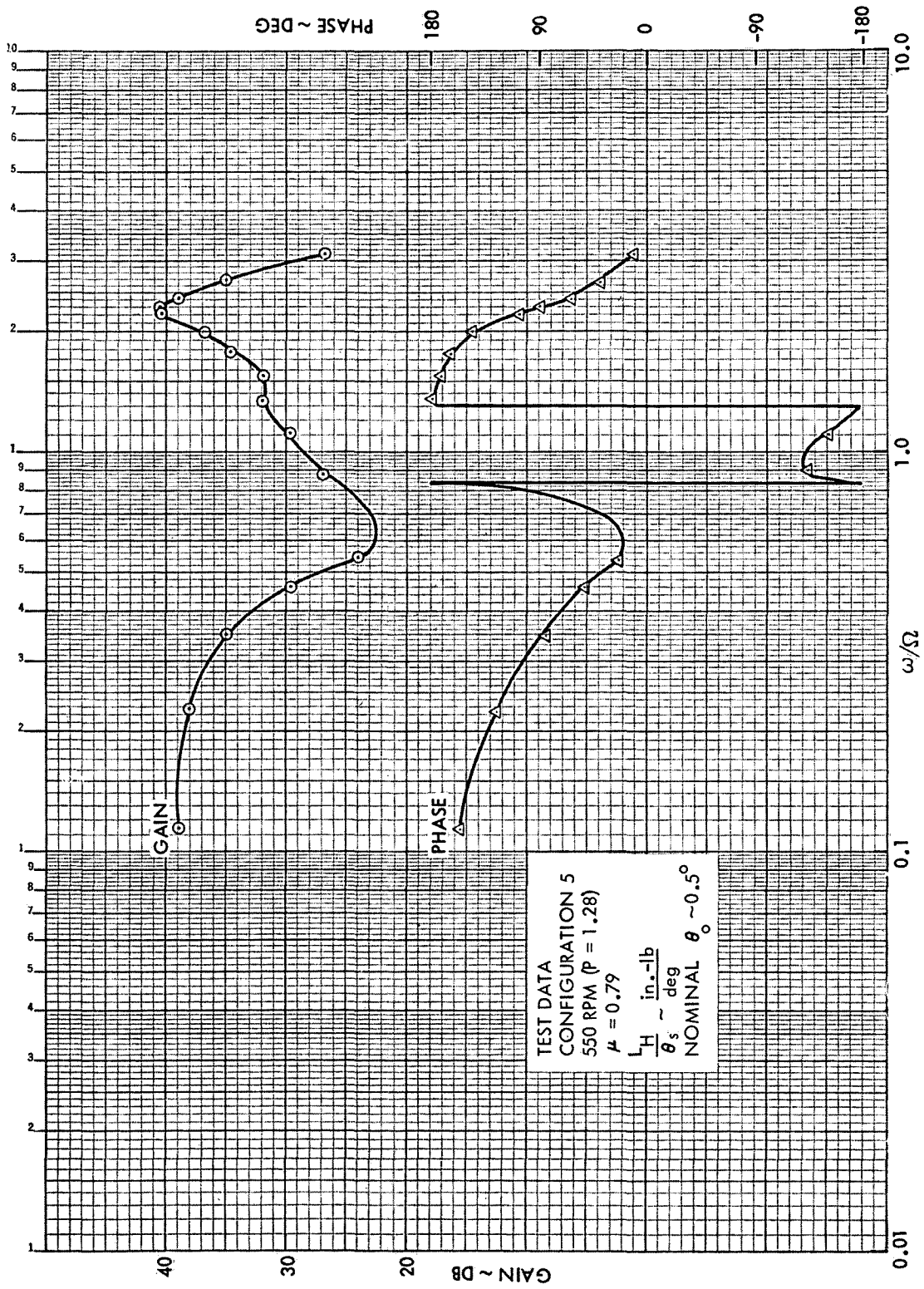


Figure B38. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM ( $P = 1.28$ )

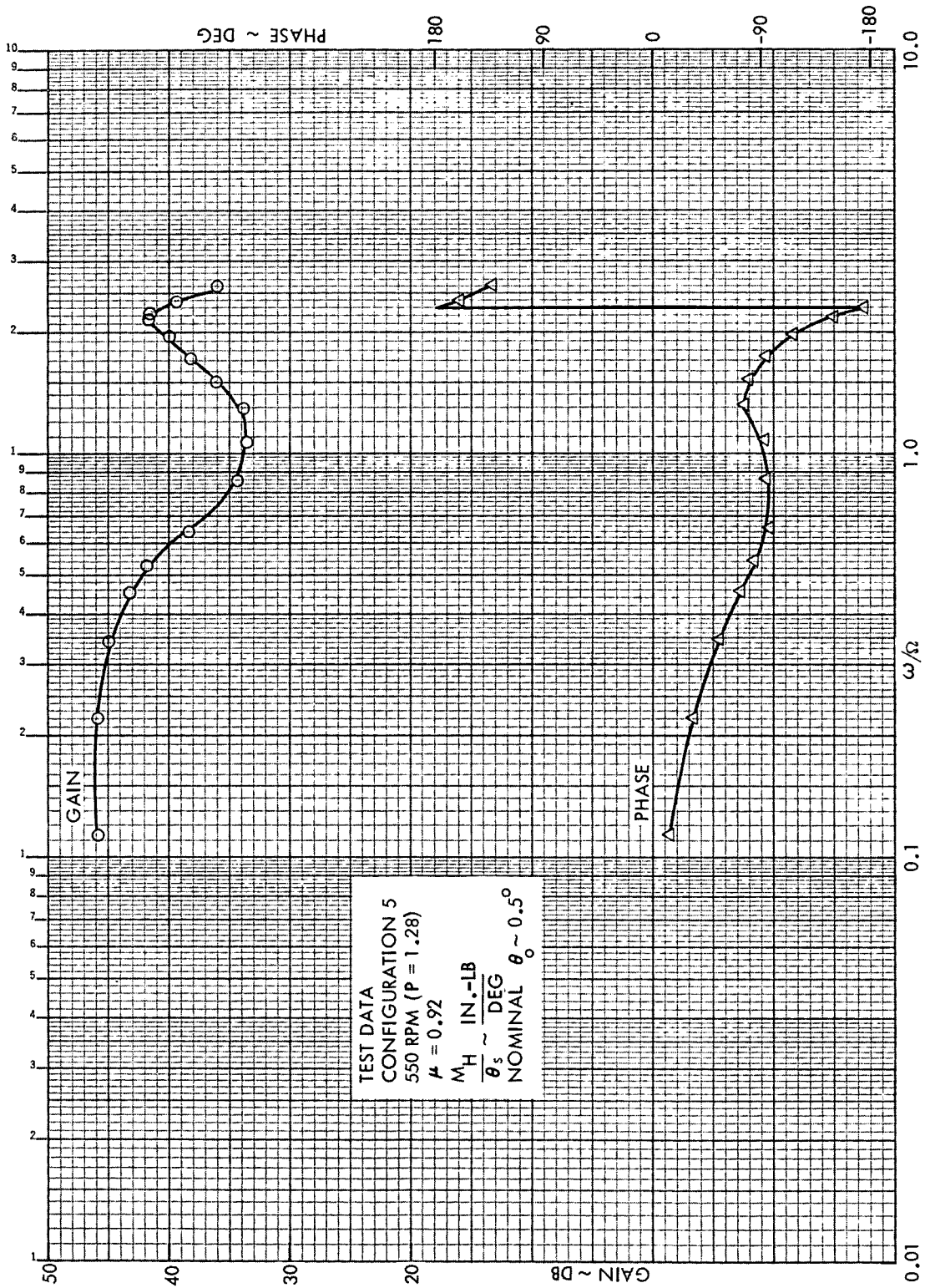


Figure B39. Rotor Hub Pitch Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM (P = 1.28)



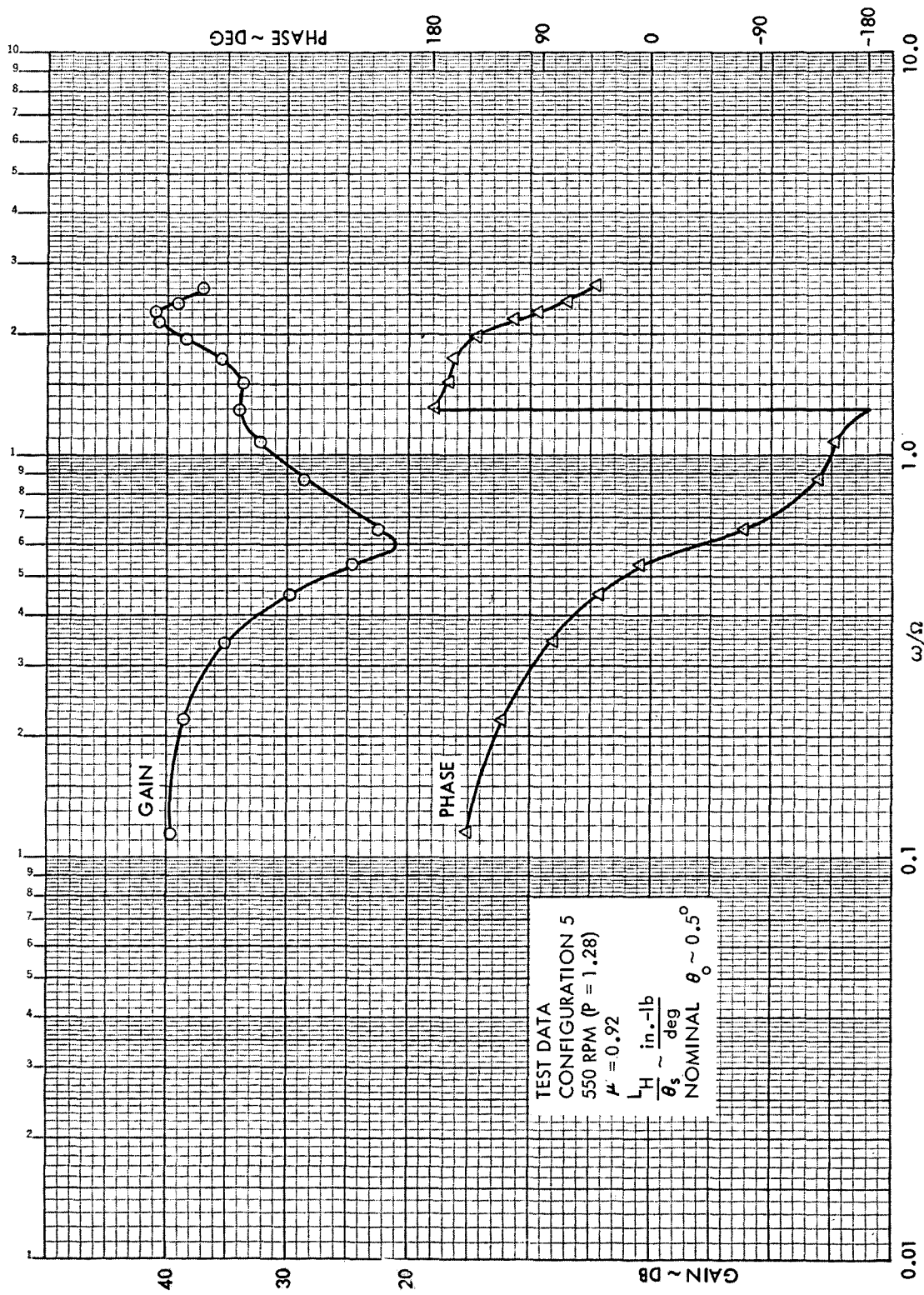


Figure B40. Rotor Hub Roll Moment Frequency Response to Longitudinal Cyclic Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM ( $P = 1.28$ )



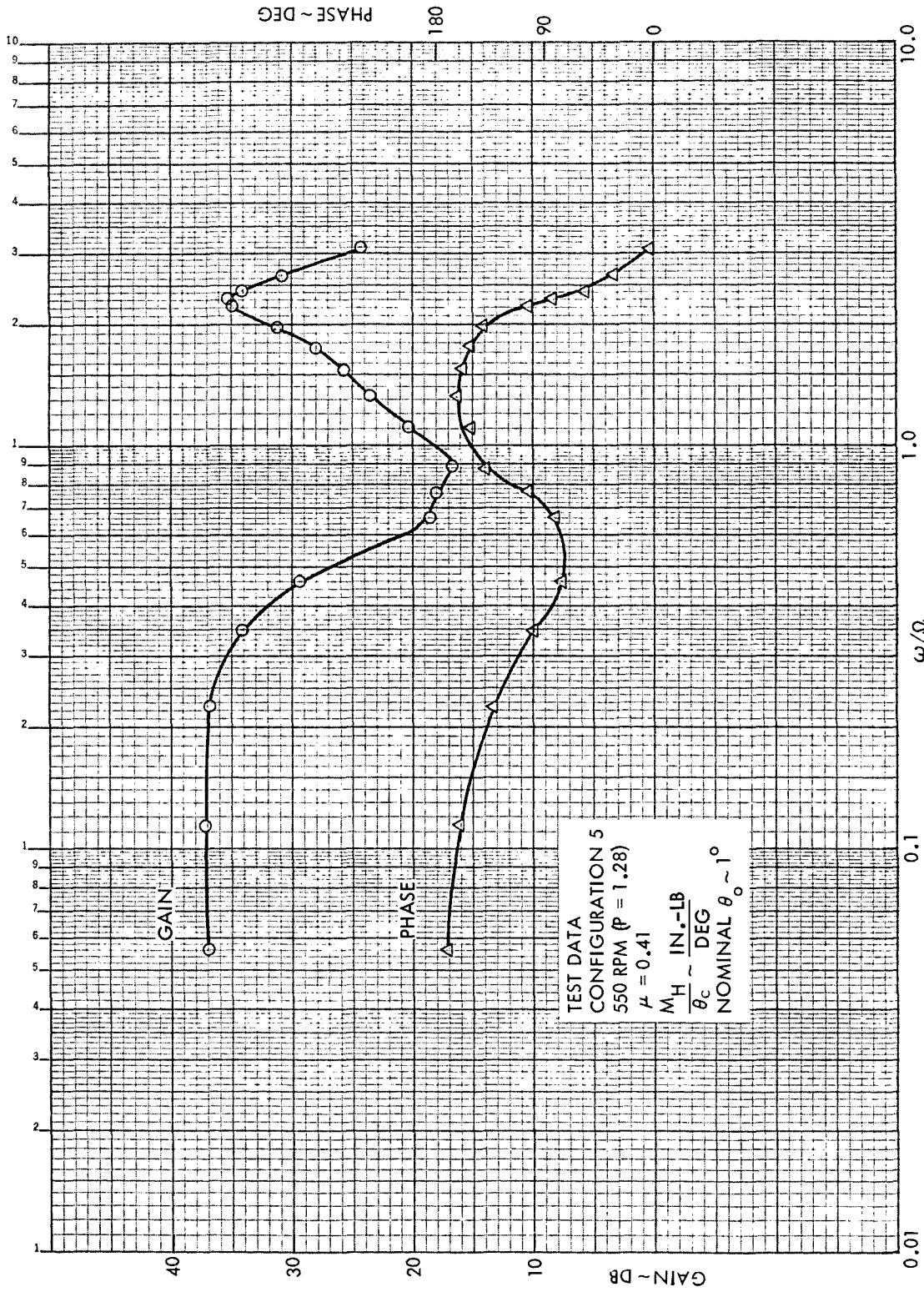
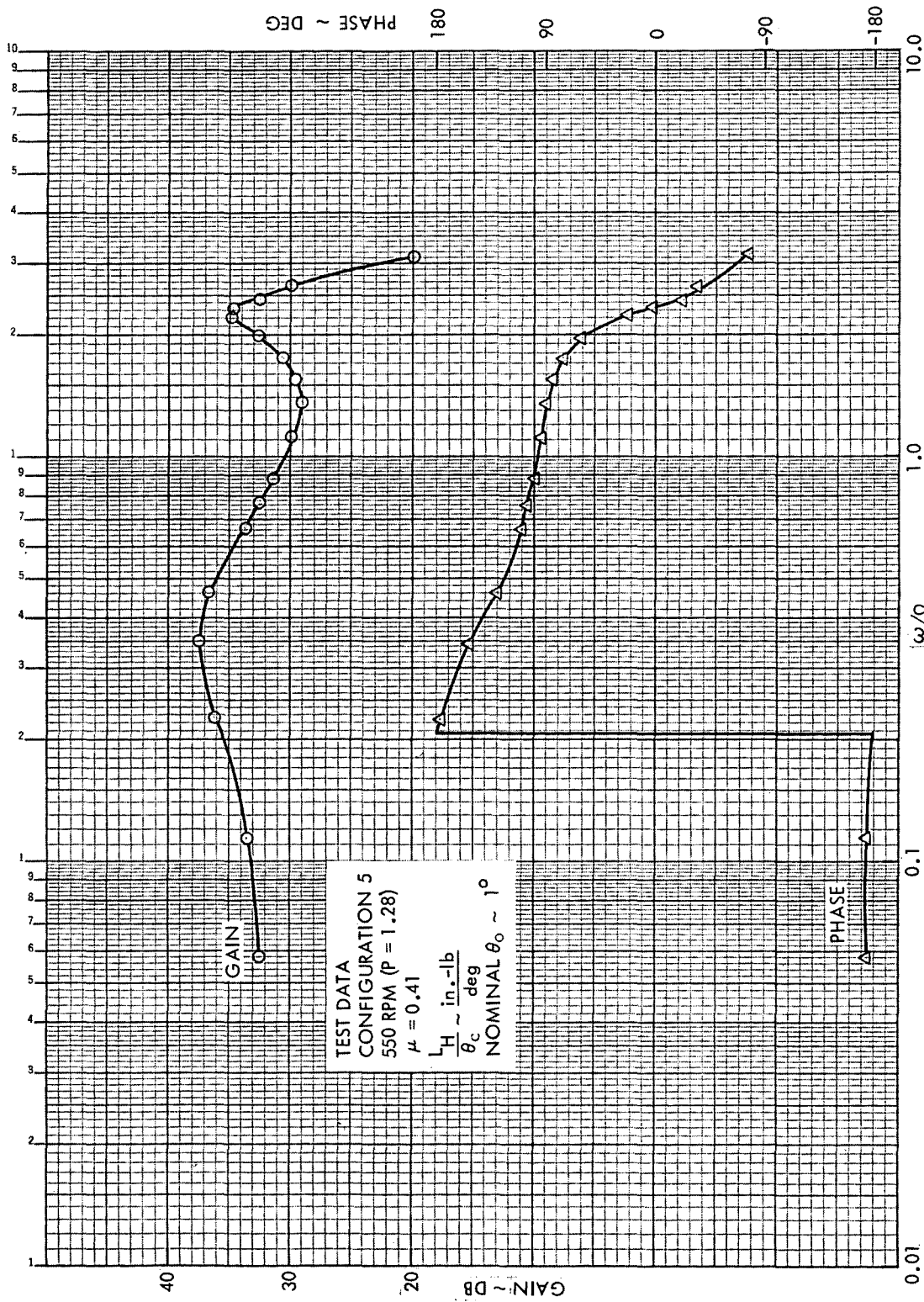


Figure B41. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM ( $P = 1.28$ )



TEST DATA  
 CONFIGURATION 5  
 550 RPM (P = 1.28)  
 $\mu = 0.41$   
 $L/H \sim \frac{\text{in.} \cdot \text{lb}}{\theta_c \text{ deg}}$   
 NOMINAL  $\theta_0 \sim 1^\circ$

Figure B42. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.41$ , 550 RPM (P = 1.28)



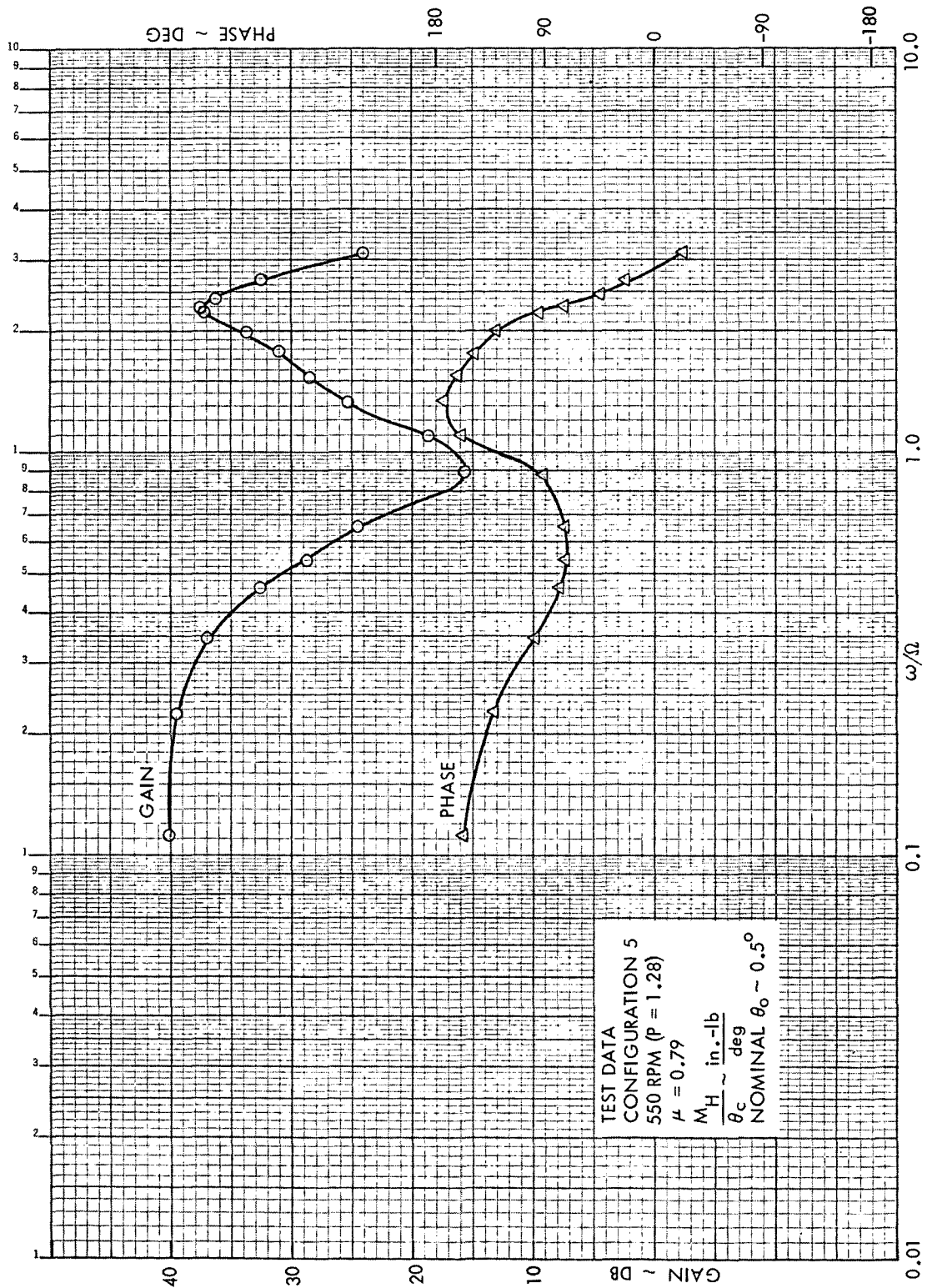


Figure B43. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM ( $P = 1.28$ )

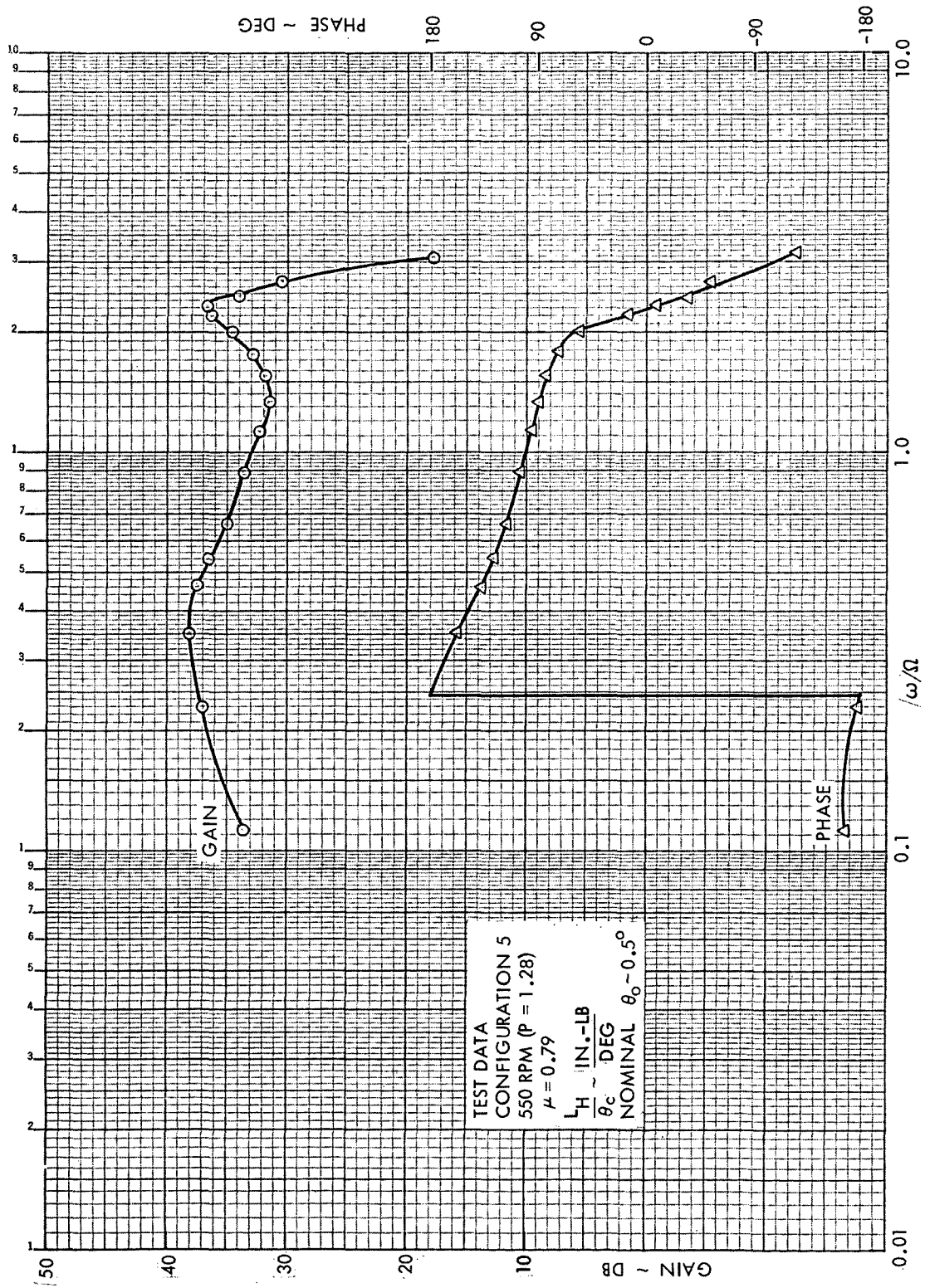


Figure B44. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.79$ , 550 RPM (P = 1.28)

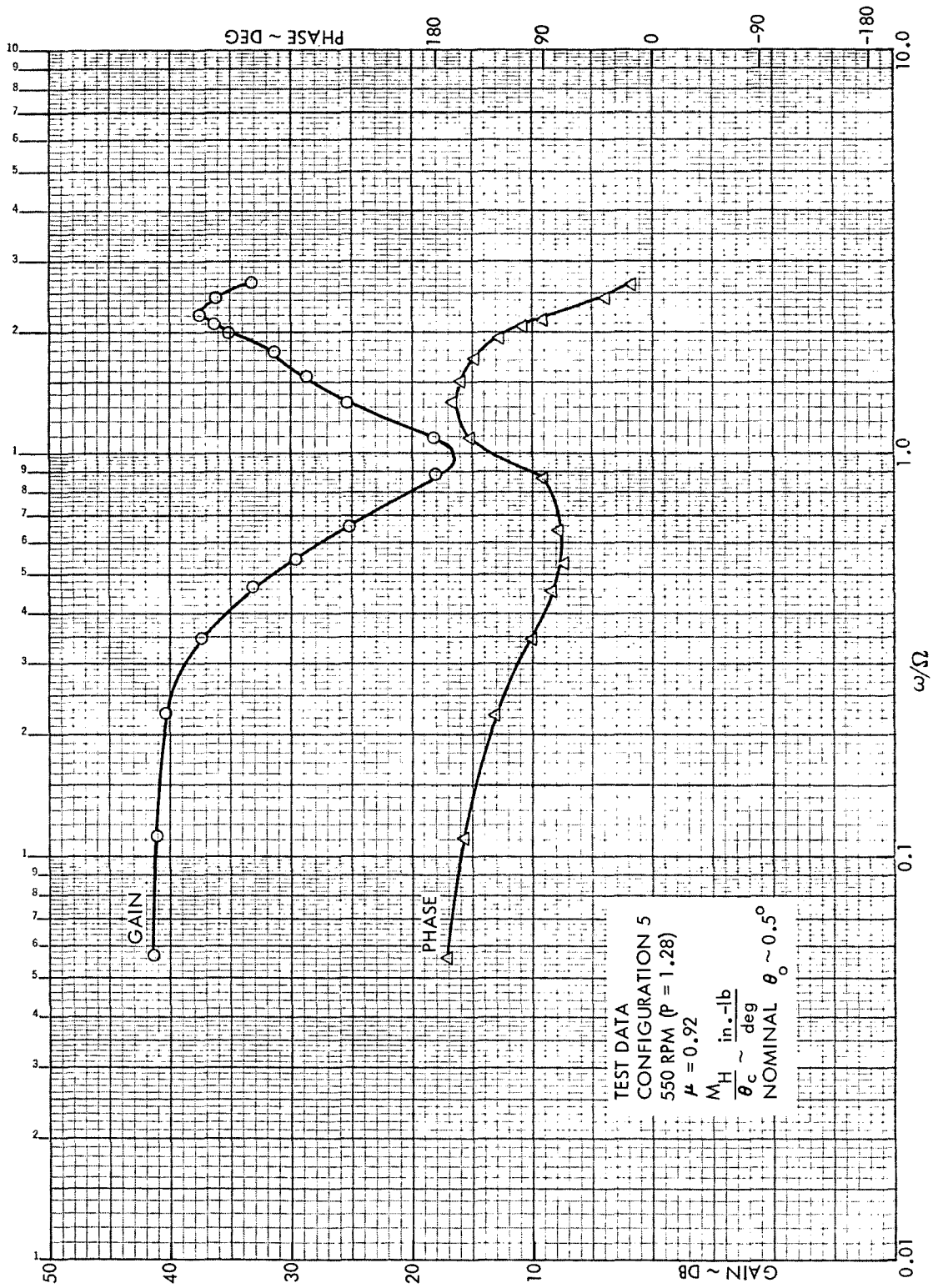


Figure B45. Rotor Hub Pitch Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM ( $P = 1.28$ )



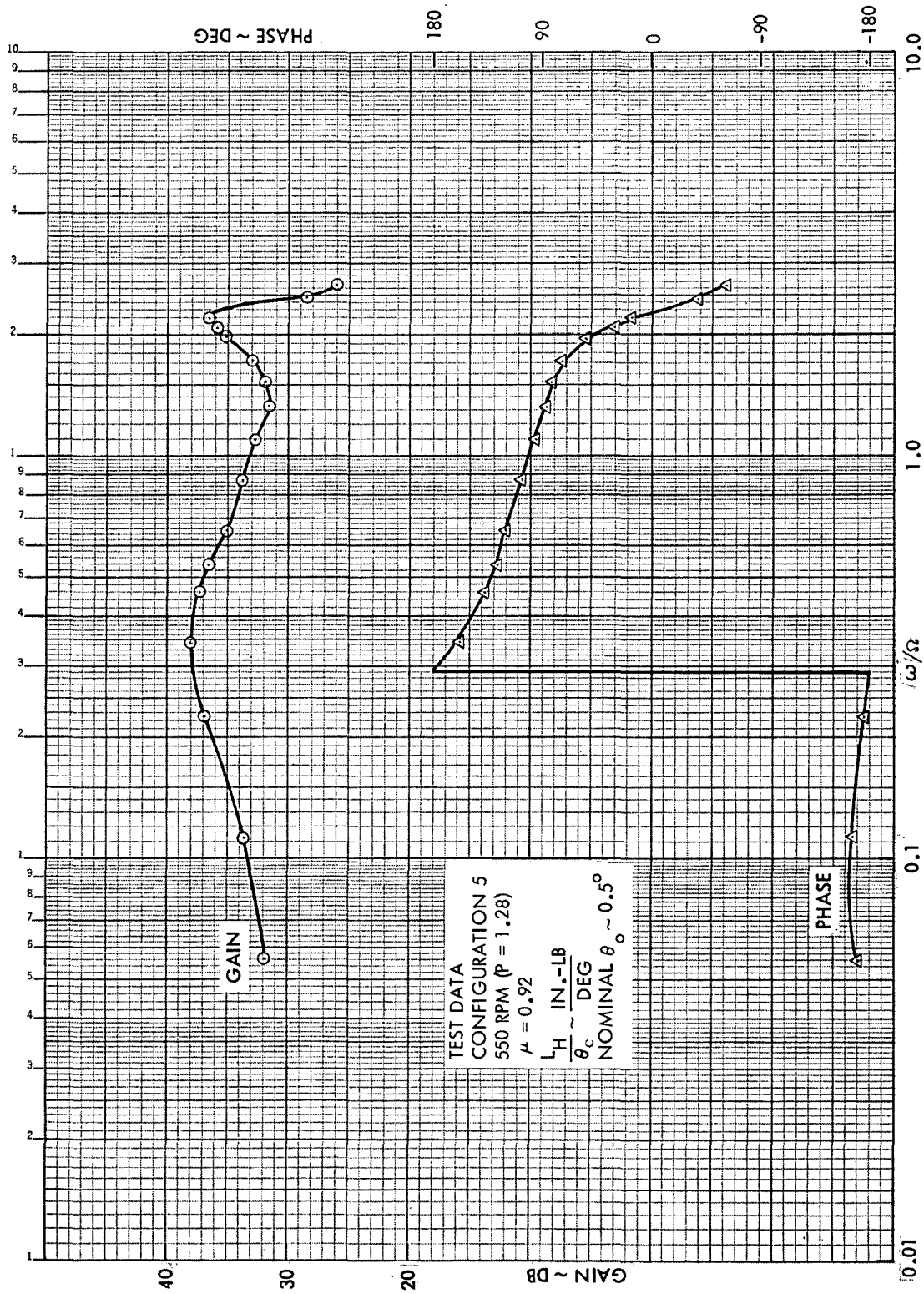


Figure B46. Rotor Hub Roll Moment Frequency Response to Lateral Cyclic Pitch, Configuration 5,  $\mu = 0.92$ , 550 RPM ( $P = 1.28$ )

## APPENDIX C

## EXPERIMENTAL ROTOR FREQUENCY RESPONSE DATA (ROTOR SHAFT EXCITATIONS)

All of the rotor transfer functions with respect to shaft pitch ( $\alpha$ ) and roll ( $\phi$ ), which were acquired during the Phase 3 test, are contained in this appendix. The hub moment frequency response data, with the dimensions, in.-lb/deg, are plotted in Figures C1 through C54. These derivatives have also been transferred to the center of rotation, converted to coefficient form and tabulated (Tables IX through XII). The amplification factors ( $k$ ) used to transfer the configuration 5 hub moment derivatives to the shaft centerline are based on the experimental one-per-rev blade bending moment distributions plotted in Appendix A. The amplification factors for configuration 1 are analytically determined as described in Reference 1 (page 84). The values of  $k$  used are summarized below:

Configuration	RPM	$k$
1	800	1.235
	550	1.17
5	850	1.785
	550	1.43

The equations used to nondimensionalize the data are:

$$\frac{c_m}{a\sigma} = \frac{kM_H}{\pi R^3 \rho (\Omega R)^2 a\sigma}$$

$$\frac{c_l}{a\sigma} = \frac{kL_H}{\pi R^3 \rho (\Omega R)^2 a\sigma}$$

where  $a = 5.73$  and  $\rho = 0.002324$  slugs/ft<sup>3</sup> are assumed.

The tabulated phase lags are expressed in radians in the range  $0 \rightarrow -2\pi$ . It is noted that the nominal rotor lift is approximately zero for all of the data presented herein.



TABLE IX  
 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT PITCH  
 CONFIGURATION 5

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\alpha a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\alpha a \sigma}$	$c_l$ Phase (rad)		
850/1.15	0	3.26	0.037	0.0048	-1.448	0.0064	-5.005		
		6.52	0.073	0.0122	-1.474	0.0136	-5.346		
		9.70	0.109	0.0226	-1.674	0.0208	-5.761		
		13.08	0.147	0.0320	-2.045	0.0239	-6.266		
		16.31	0.184	0.0364	-2.294	0.0234	-0.323		
		19.87	0.223	0.0387	-2.495	0.0217	-0.605		
		23.02	0.258	0.0397	-2.605	0.0199	-0.774		
		26.37	0.296	0.0422	-2.679	0.0189	-0.900		
		33.03	0.371	0.0485	-2.801	0.0187	-1.128		
		*37.61	0.422	0.0571	-2.913	0.0194	-1.336		
		*50.29	0.564	0.0626	-3.150	0.0191	-1.670		
		*57.01	0.641	0.0675	-3.050	0.0199	-1.674		
		*63.21	0.712	0.1068	-3.174	0.0299	-1.877		
		0.27	0.27	3.31	0.037	0.0078	-0.997	0.0038	-5.395
				6.57	0.074	0.0135	-1.421	0.0070	-5.443
20.01	0.224			0.0387	-2.133	0.0219	-0.002		
26.39	0.296			0.0502	-2.388	0.0266	-0.367		
31.23	0.350			0.0604	-2.567	0.0297	-0.653		
*38.23	0.429			0.0937	-2.781	0.0402	-1.066		
*57.73	0.647			0.1109	-3.404	0.0369	-2.098		
*63.74	0.715	0.1199	-4.513	0.0385	-3.205				
0.36	0.36	3.26	0.037	0.0099	-0.677	0.0032	-4.986		
		6.61	0.074	0.0141	-1.204	0.0056	-5.124		
		20.07	0.225	0.0397	-2.000	0.0216	-6.153		
		26.53	0.298	0.0526	-2.293	0.0266	-0.312		
		31.24	0.351	0.0638	-2.495	0.0308	-0.593		
		*37.96	0.427	0.0979	-2.727	0.0424	-1.024		
		*57.68	0.648	0.1147	-3.382	0.0411	-2.077		
*63.44	0.713	0.1256	-4.441	0.0428	-3.141				

\*These data may be affected by support vibrations.

TABLE IX

ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT PITCH,  
CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\alpha a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\alpha a \sigma}$	$c_l$ Phase (rad)
850/1.15	0.51	3.26	0.037	0.0206	-0.382	0.0049	-4.157
		6.55	0.074	0.0235	-0.752	0.0084	-4.740
		12.98	0.146	0.0339	-1.310	0.0161	-5.425
		19.82	0.223	0.0476	-1.793	0.0236	-6.027
		26.80	0.301	0.0617	-2.184	0.0296	-0.267
		31.26	0.351	0.0729	-2.397	0.0330	-0.565
		*38.12	0.429	0.1094	-2.661	0.0449	-1.005
		*58.35	0.657	0.1372	-3.487	0.0483	-2.195
		*64.23	0.722	0.1227	-4.041	0.0441	-2.806
	0.60	3.26	0.037	0.0306	-0.323	0.0072	-3.922
		6.58	0.074	0.0340	-0.673	0.0103	-4.540
		12.81	0.144	0.0420	-1.229	0.0157	-5.212
		20.20	0.228	0.0566	-1.737	0.0239	-5.998
		26.64	0.300	0.0691	-2.107	0.0291	-0.230
		33.07	0.373	0.0876	-2.386	0.0348	-0.653
		*37.74	0.425	0.1167	-2.602	0.0452	-0.993
		*58.17	0.654	0.1359	-3.676	0.0459	-2.438
		*64.04	0.721	0.1335	-3.876	0.0438	-2.701
	550/1.28	0	3.28	0.057	0.0058	-1.191	0.0125
6.54			0.113	0.0182	-1.080	0.0282	-5.119
9.73			0.169	0.0407	-1.256	0.0489	-5.483
12.97			0.225	0.0748	-1.688	0.0732	-6.043
16.31			0.284	0.0873	-2.153	0.0722	-0.288
19.80			0.344	0.0396	-2.453	0.0524	-0.546
23.02			0.401	0.0902	-2.604	0.0558	-0.857
26.46			0.461	0.0915	-2.701	0.0510	-1.015
*33.00			0.574	0.1010	-2.823	0.0482	-1.236
*37.52			0.653	0.1185	-2.922	0.0512	-1.438
*44.02			0.766	0.0908	-3.197	0.0385	-1.749
*50.30			0.875	0.1043	-3.178	0.0436	-1.823
*57.27			0.956	0.1346	-3.049	0.0511	-1.899
*63.00			1.059	0.2000	-3.178	0.0743	-2.062

\*These data may be affected by support vibrations.

TABLE X  
 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT ROLL,  
 CONFIGURATION 5

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\phi a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\phi a \sigma}$	$c_l$ Phase (rad)		
850/1.15	0	3.26	0.027	0.0056	-1.844	0.0044	-1.426		
		6.54	0.074	0.0122	-2.154	0.0110	-1.445		
		9.74	0.110	0.0134	-2.554	0.0202	-1.638		
		12.87	0.145	0.0219	-2.989	0.0289	-1.933		
		16.31	0.184	0.0214	-3.402	0.0337	-2.245		
		19.93	0.225	0.0191	-3.648	0.0349	-2.429		
		26.52	0.299	0.0162	-3.974	0.0363	-2.631		
		32.97	0.371	0.0152	-4.173	0.0385	-2.726		
		37.48	0.421	0.0154	-4.292	0.0423	-2.814		
		*50.31	0.566	0.0108	-4.378	0.0366	-2.806		
		*57.41	0.646	0.0112	-4.454	0.0390	-2.815		
		63.00	0.709	0.0134	-4.516	0.0416	-2.832		
		0.27		3.26	0.027	0.0038	-1.722	0.0036	-1.599
				6.63	0.074	0.0067	-1.953	0.0074	-1.572
				13.02	0.146	0.0125	-2.462	0.0174	-1.695
26.73	0.299			0.0164	-3.420	0.0382	-2.218		
37.83	0.423			0.0160	-3.979	0.0475	-2.564		
*50.64	0.569			0.0099	-4.205	0.0447	-2.746		
63.54	0.713			0.0161	-4.247	0.0487	-2.876		
77.06	0.864			0.0258	-4.730	0.0559	-2.984		
89.02	0.997			0.0184	-5.848	0.0594	-2.854		
20.17	0.227			0.0158	-3.003	0.0293	-1.963		
31.25	0.351			0.0159	-3.700	0.0429	-2.382		
*44.07	0.496			0.0134	-4.380	0.0436	-2.763		
*57.60	0.650			0.0117	-4.229	0.0489	-2.826		
0.36				3.26	0.027	0.0034	-1.652	0.0034	-1.641
				6.56	0.074	0.0064	-1.932	0.0067	-1.603
		13.04	0.147	0.0115	-2.365	0.0158	-1.729		
		20.25	0.228	0.0157	-2.929	0.0277	-1.945		
		26.64	0.300	0.0165	-3.313	0.0361	-2.175		
		31.26	0.352	0.0146	-3.550	0.0396	-2.319		
		38.02	0.427	0.0140	-3.946	0.0452	-2.525		
		*44.17	0.496	0.0125	-4.274	0.0409	-2.695		
		*50.82	0.570	0.0103	-4.172	0.0441	-2.696		
		*57.76	0.648	0.0097	-4.160	0.0468	-2.763		
		63.76	0.715	0.0160	-4.273	0.0504	-2.829		
		77.40	0.868	0.0238	-4.792	0.0549	-2.958		

\*These data may be affected by support vibrations.



TABLE X

ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT ROLL,  
CONFIGURATION 5 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\phi a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\phi a \sigma}$	$c_l$ Phase (rad)	
850/1.15	0.51	3.26	0.037	0.0033	-1.630	0.0031	-1.651	
		5.60	0.074	0.0057	-1.873	0.0055	-1.630	
		12.93	0.145	0.0113	-2.370	0.0141	-1.702	
		20.05	0.224	0.0161	-2.888	0.0263	-1.902	
		31.23	0.350	0.0155	-3.585	0.0379	-2.279	
		*44.21	0.495	0.0172	-4.342	0.0445	-2.650	
		*50.76	0.567	0.0122	-4.122	0.0467	-2.651	
		76.85	0.855	0.0252	-4.807	0.0585	-2.935	
		89.02	1.000	0.0259	-5.718	0.0572	-2.728	
		0.60	3.26	0.036	0.0034	-1.285	0.0030	-1.865
			6.53	0.073	0.0061	-1.861	0.0065	-1.647
			12.98	0.145	0.0131	-2.385	0.0150	-1.684
	20.08		0.224	0.0176	-2.909	0.0258	-1.896	
	26.86		0.300	0.0195	-3.364	0.0348	-2.132	
	31.24		0.348	0.0194	-3.678	0.0398	-2.292	
	31.26		0.348	0.0194	-3.652	0.0395	-2.285	
	38.03		0.427	0.0195	-4.124	0.0459	-2.517	
	*44.22		0.496	0.0132	-4.754	0.0404	-2.683	
	*50.35		0.564	0.0118	-4.118	0.0452	-2.644	
	*57.42		0.643	0.0149	-4.247	0.0495	-2.731	
	63.26		0.707	0.0183	-5.199	0.0473	-2.840	
	76.76	0.856	0.0110	-5.200	0.0542	-2.843		
	88.80	0.990	0.0107	-5.325	0.0642	-2.859		
	350/1.28	0	3.26	0.056	0.0123	-1.755	0.0056	-1.158
6.52			0.112	0.0278	-1.971	0.0178	-1.017	
9.70			0.167	0.0506	-2.335	0.0432	-1.191	
13.03			0.224	0.0711	-2.961	0.0779	-1.702	
16.26			0.278	0.0655	-3.490	0.0861	-2.176	
19.83			0.340	0.0550	-3.803	0.0829	-2.452	
26.55			0.453	0.0413	-4.111	0.0777	-2.672	
33.07			0.563	0.0366	-4.285	0.0788	-2.765	
37.73			0.641	0.0365	-4.458	0.0862	-2.865	
*43.92			0.758	0.0253	-4.530	0.0640	-2.869	
*50.23			0.865	0.0261	-4.550	0.0721	-2.832	
*57.22			0.984	0.0262	-4.621	0.0761	-2.836	
62.96			1.081	0.0284	-4.609	0.0801	-2.831	

\*These data may be affected by support vibrations.

TABLE XI  
 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT PITCH,  
 CONFIGURATION 1

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\alpha a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\alpha a \sigma}$	$c_l$ Phase (rad)
800/1.33	0.28	3.27	0.039	0.0087	-0.777	0.0058	-4.320
		6.54	0.078	0.0140	-1.127	0.0119	-4.967
		13.05	0.155	0.0299	-1.409	0.0260	-5.254
		19.92	0.226	0.0557	-1.684	0.0454	-5.651
		26.50	0.314	0.0896	-2.008	0.0669	-6.117
		31.23	0.371	0.1196	-2.279	0.0830	-0.205
		*37.92	0.450	0.1871	-2.740	0.1134	-0.800
		*50.48	0.559	0.1684	-3.443	0.0904	-1.737
		*63.49	0.752	0.2140	-3.922	0.0948	-2.355
	0.38	3.26	0.039	0.0129	-0.517	0.0069	-4.278
		6.60	0.078	0.0176	-0.846	0.0125	-4.660
		13.07	0.155	0.0329	-1.229	0.0262	-5.108
		19.95	0.237	0.0601	-1.554	0.0458	-5.562
		26.55	0.316	0.0959	-1.928	0.0675	-6.055
		31.23	0.373	0.1271	-2.208	0.0835	-0.140
		*38.25	0.458	0.1435	-2.747	0.0856	-0.768
		*50.51	0.604	0.1526	-3.505	0.0802	-1.757
		0.54	3.26	0.039	0.0278	-0.312	0.0149
	6.61		0.079	0.0312	-0.558	0.0185	-4.182
	13.04		0.155	0.0472	-0.979	0.0320	-4.809
	20.01		0.239	0.0770	-1.383	0.0522	-5.373
	26.60		0.317	0.1141	-1.809	0.0726	-5.926
	31.26		0.373	0.1461	-2.120	0.0878	-0.044
	*38.10		0.454	0.1650	-2.654	0.0907	-0.687
	*50.42		0.601	0.1557	-3.449	0.0788	-1.711
	*57.59		0.687	0.2083	-4.009	0.0952	-2.391
	0.64	3.26	0.039	0.0398	-0.221	0.0210	-3.590
		6.56	0.078	0.0444	-0.438	0.0249	-3.978
		13.09	0.156	0.0619	-0.852	0.0377	-4.638
		20.05	0.239	0.0943	-1.310	0.0576	-5.280
		26.31	0.314	0.1291	-1.749	0.0760	-5.849
		31.29	0.373	0.1635	-2.092	0.0918	-0.004
		*37.86	0.451	0.1750	-2.578	0.0918	-0.590
*50.37		0.601	0.1631	-3.281	0.0807	-1.536	
*57.73		0.689	0.2329	-3.285	0.1043	-1.660	
*64.66	0.771	0.2814	-4.111	0.1253	-2.564		

\*These data may be affected by support vibrations.



TABLE XI

 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT PITCH,  
 CONFIGURATION 1 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\alpha a \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\alpha a \sigma}$	$c_l$ Phase (rad)
550/1.56	0.41	3.26	0.056	0.0146	-0.482	0.0130	-4.122
		6.57	0.113	0.0213	-0.768	0.0230	-4.502
		13.05	0.224	0.0454	-1.002	0.0507	-4.887
		20.01	0.344	0.0982	-1.211	0.0991	-5.274
		26.76	0.459	0.2017	-1.593	0.1798	-5.812
		31.26	0.535	0.2950	-1.984	0.2438	-0.001
		38.00	0.649	0.4241	-2.563	0.3107	-0.744
	0.56	3.27	0.056	0.0258	-0.292	0.0232	-3.720
		6.57	0.113	0.0320	-0.531	0.0312	-4.137
		13.08	0.226	0.0575	-0.835	0.0582	-4.678
		20.11	0.347	0.1169	-1.126	0.1108	-5.164
		26.67	0.460	0.2226	-1.542	0.1896	-5.738
		31.23	0.529	0.3165	-1.958	0.2503	-6.251
		37.84	0.654	0.4455	-2.548	0.3167	-0.686
	58.13	1.011	0.4227	-3.372	0.2491	-1.861	
	0.78	3.26	0.056	0.0511	-0.201	0.0445	-3.513
		6.60	0.114	0.0593	-0.359	0.0524	-3.830
		13.05	0.226	0.0889	-0.654	0.0782	-4.393
		19.96	0.345	0.1602	-0.999	0.1332	-4.964
		26.55	0.459	0.2798	-1.499	0.2141	-5.653
		31.26	0.540	0.3752	-1.952	0.2684	-6.215
		38.08	0.657	0.4970	-2.569	0.3217	-0.683
	57.90	0.998	0.4644	-3.393	0.2631	-1.836	
	0.93	3.27	0.056	0.0742	-0.164	0.0594	-3.471
		6.60	0.114	0.0835	-0.293	0.0668	-3.733
		12.93	0.224	0.1132	-0.551	0.0896	-4.246
		20.08	0.347	0.1991	-0.949	0.1494	-4.900
		26.60	0.460	0.3234	-1.486	0.2267	-5.630
31.24		0.540	0.4125	-1.949	0.2732	-6.204	
37.92		0.656	0.5500	-2.555	0.3409	-0.655	

TABLE XII  
 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT ROLL,  
 CONFIGURATION 1

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\phi \alpha \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\phi \alpha \sigma}$	$c_l$ Phase (rad)	
800/1.33	0	3.27	0.039	0.0079	-1.675	0.0033	-1.236	
		6.50	0.078	0.0159	-1.776	0.0082	-1.043	
		12.88	0.154	0.0397	-2.081	0.0299	-1.023	
		19.72	0.235	0.0723	-2.762	0.0767	-1.550	
		22.99	0.274	0.0784	-3.163	0.0931	-1.894	
		26.31	0.313	0.0733	-3.481	0.0978	-2.184	
		30.05	0.358	0.0658	-3.755	0.0974	-2.407	
		33.10	0.394	0.0591	-3.934	0.0958	-2.539	
		37.49	0.447	0.0542	-4.125	0.0969	-2.709	
		49.88	0.596	0.0397	-4.200	0.0809	-2.745	
		57.02	0.681	0.0357	-4.334	0.0827	-2.790	
	63.20	0.755	0.0349	-4.384	0.0852	-2.809		
	0.28	3.26	0.039	0.0058	-1.680	0.0038	-1.534	
		6.80	0.081	0.0122	-1.802	0.0079	-1.365	
		12.98	0.155	0.0256	-2.132	0.0200	-1.325	
		26.61	0.319	0.0549	-2.993	0.0699	-1.759	
		38.09	0.457	0.0548	-3.841	0.1010	-2.379	
		50.78	0.609	0.0485	-3.944	0.0982	-2.589	
		63.49	0.758	0.0407	-4.548	0.0962	-2.849	
		77.28	0.924	0.0315	-4.723	0.1010	-2.880	
		89.00	1.063	0.0305	-4.830	0.1124	-2.891	
		0.64	6.54	0.078	0.0131	-1.806	0.0063	-1.415
			13.18	0.157	0.0281	-2.151	0.0181	-1.278
	26.70		0.319	0.0566	-3.059	0.0631	-1.731	
	37.19		0.444	0.0552	-3.852	0.0833	-2.282	
	50.79		0.605	0.0487	-3.887	0.0904	-2.468	
	63.78		0.761	0.0401	-4.574	0.0904	-2.720	
	76.59		0.914	0.0367	-4.799	0.1011	-2.779	
	88.84		1.059	0.0346	-4.970	0.1164	-2.814	
	550/1.56	0	3.26	0.057	0.0119	-1.615	0.0035	-1.038
			12.92	0.224	0.0635	-1.866	0.0401	-0.699
			16.30	0.283	0.0953	-2.035	0.0711	-0.803
			19.83	0.344	0.1380	-2.305	0.1211	-1.024
22.94			0.398	0.1820	-2.638	0.1781	-1.316	
26.27			0.456	0.2093	-3.099	0.2286	-1.737	
32.93			0.572	0.1761	-3.743	0.2288	-2.331	

TABLE XII  
 ROTOR MOMENT FREQUENCY RESPONSE TO SHAFT ROLL,  
 CONFIGURATION 1 (Continued)

rpm/P	$\mu$	$\omega$ (rad/sec)	$\frac{\omega}{\Omega}$	$\frac{c_m}{\phi \alpha \sigma}$	$c_m$ Phase (rad)	$\frac{c_l}{\phi \alpha \sigma}$	$c_l$ Phase (rad)
550/1.56	0	37.67	0.654	0.1509	-4.077	0.2204	-2.620
		50.07	0.869	0.1064	-4.223	0.1728	-2.709
		57.18	0.991	0.0943	-4.364	0.1691	-2.771
		63.25	1.096	0.0832	-4.408	0.1661	-2.775
	0.41	3.26	0.056	0.0108	-1.653	0.0042	-1.462
		6.66	0.115	0.0225	-1.760	0.0103	-1.199
		13.29	0.228	0.0499	-1.993	0.0319	-1.029
		20.54	0.352	0.0921	-2.365	0.0820	-1.159
		27.25	0.467	0.1322	-2.923	0.1541	-1.586
		31.27	0.535	0.1341	-3.298	0.1828	-1.919
		50.80	0.866	0.1198	-3.692	0.1894	-2.459
		64.40	1.115	0.1004	-4.535	0.1815	-2.834
		76.94	1.331	0.0991	-4.782	0.1850	-2.905
		89.15	1.546	0.1000	-4.947	0.1939	-2.891
	0.56	3.26	0.057	0.0109	-1.663	0.0038	-1.476
		6.61	0.115	0.0232	-1.775	0.0094	-1.145
		13.18	0.228	0.0512	-2.014	0.0303	-0.977
		20.16	0.349	0.0927	-2.405	0.0791	-1.133
		26.86	0.465	0.1297	-2.967	0.1457	-1.573
		31.27	0.543	0.1305	-3.369	0.1738	-1.921
		50.74	0.880	0.1176	-3.679	0.1845	-2.406
		64.09	1.111	0.1053	-4.549	0.1839	-2.790
		77.21	1.327	0.1032	-4.814	0.1902	-2.881
		89.10	1.541	0.1010	-4.977	0.2006	-2.875
	0.93	3.26	0.057	0.0112	-1.476	0.0041	-2.143
		6.57	0.114	0.0245	-1.704	0.0067	-1.283
		13.12	0.228	0.0555	-2.006	0.0259	-0.888
		20.03	0.348	0.0996	-2.492	0.0767	-1.095
		26.70	0.463	0.1286	-3.098	0.1358	-1.594
		31.25	0.541	0.1254	-3.485	0.1571	-1.923
		50.68	0.878	0.0964	-3.736	0.1660	-2.358
		64.17	1.112	0.1053	-4.553	0.1750	-2.685
		77.06	1.334	0.1099	-4.899	0.1841	-2.782
		89.07	1.542	0.1090	-5.111	0.2073	-2.739



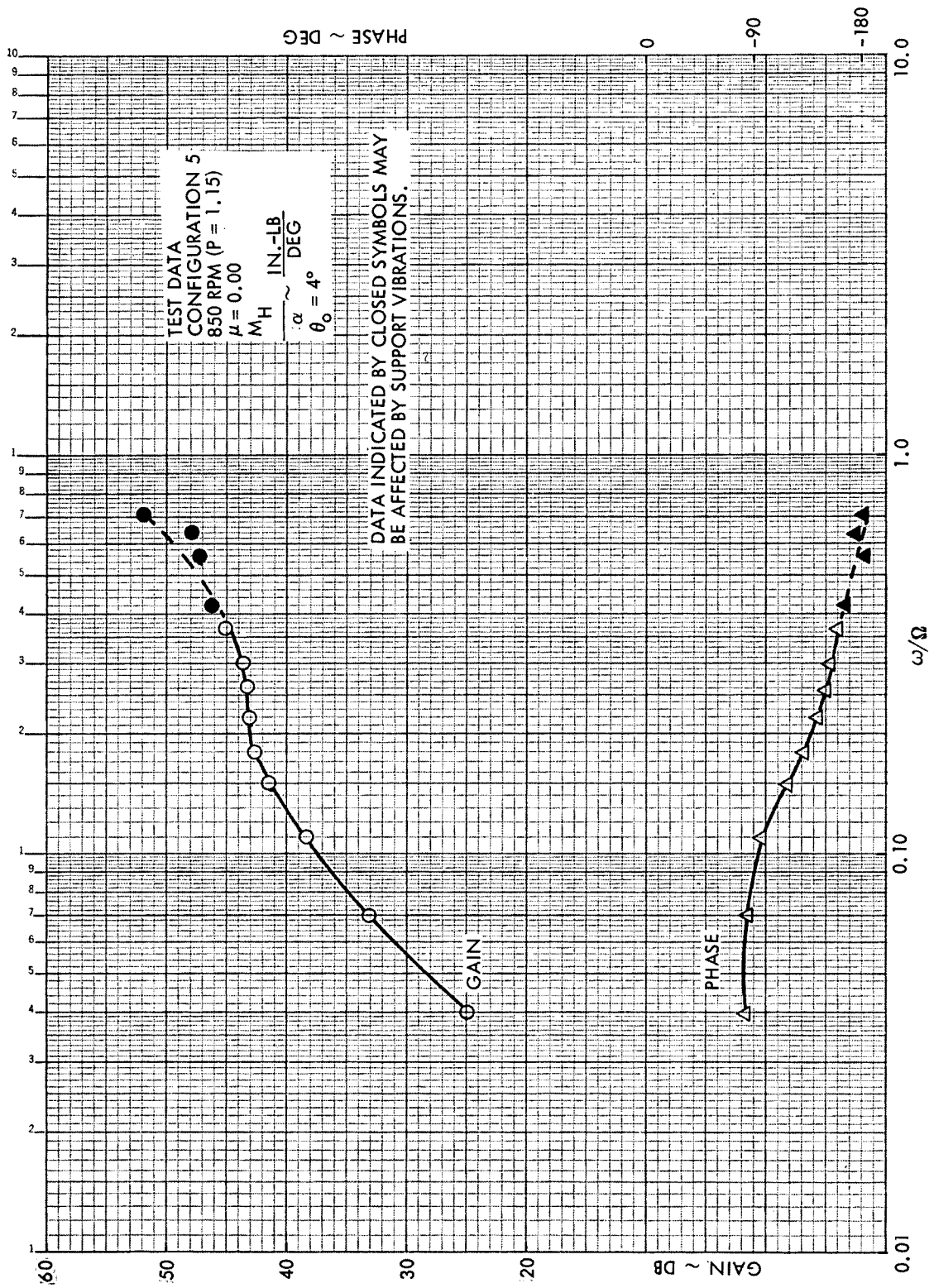


Figure C1. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.0$ , 850 RPM (P = 1.15)

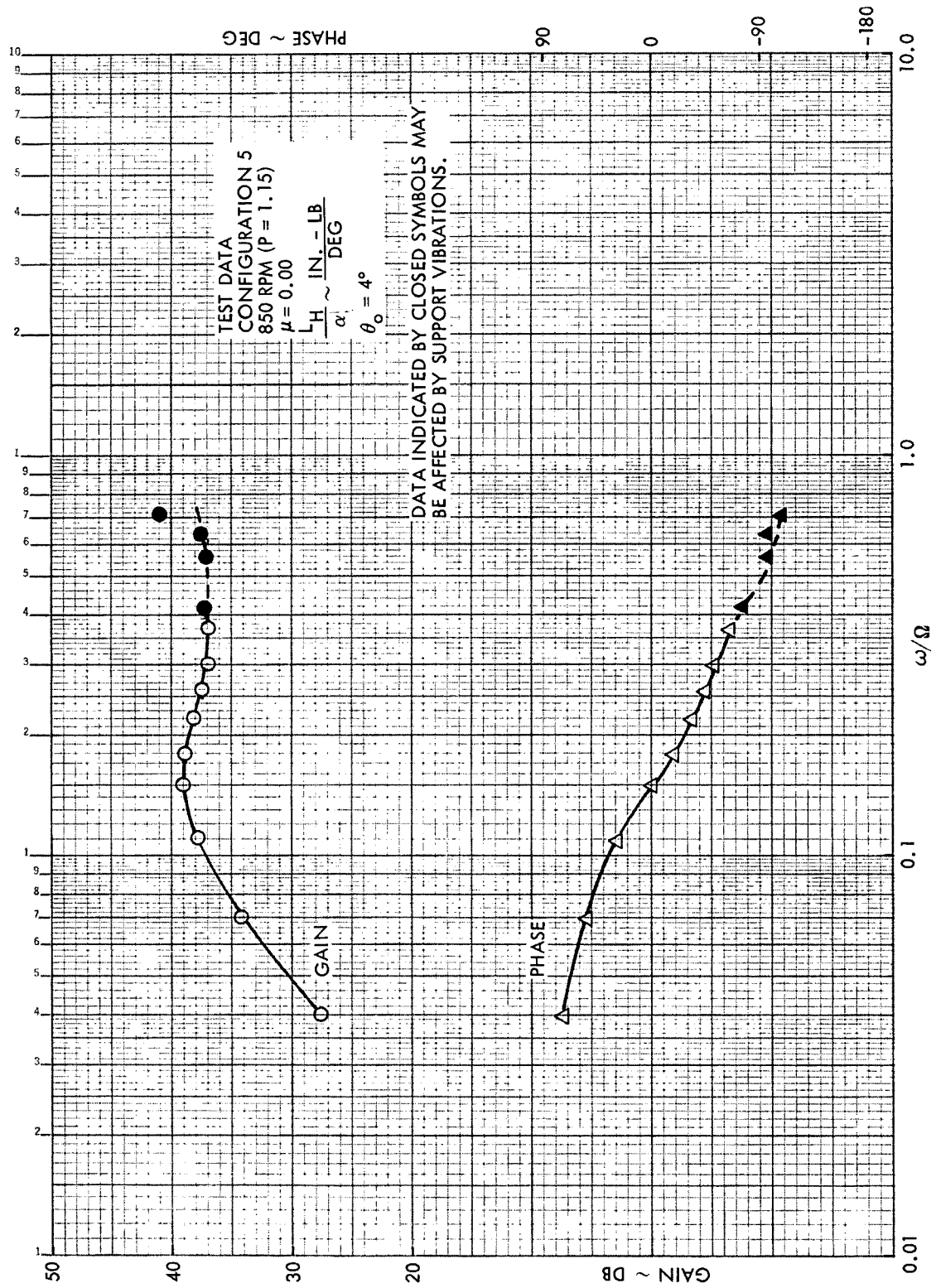


Figure C2, Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.00$ , 850 RPM (P = 1.15)

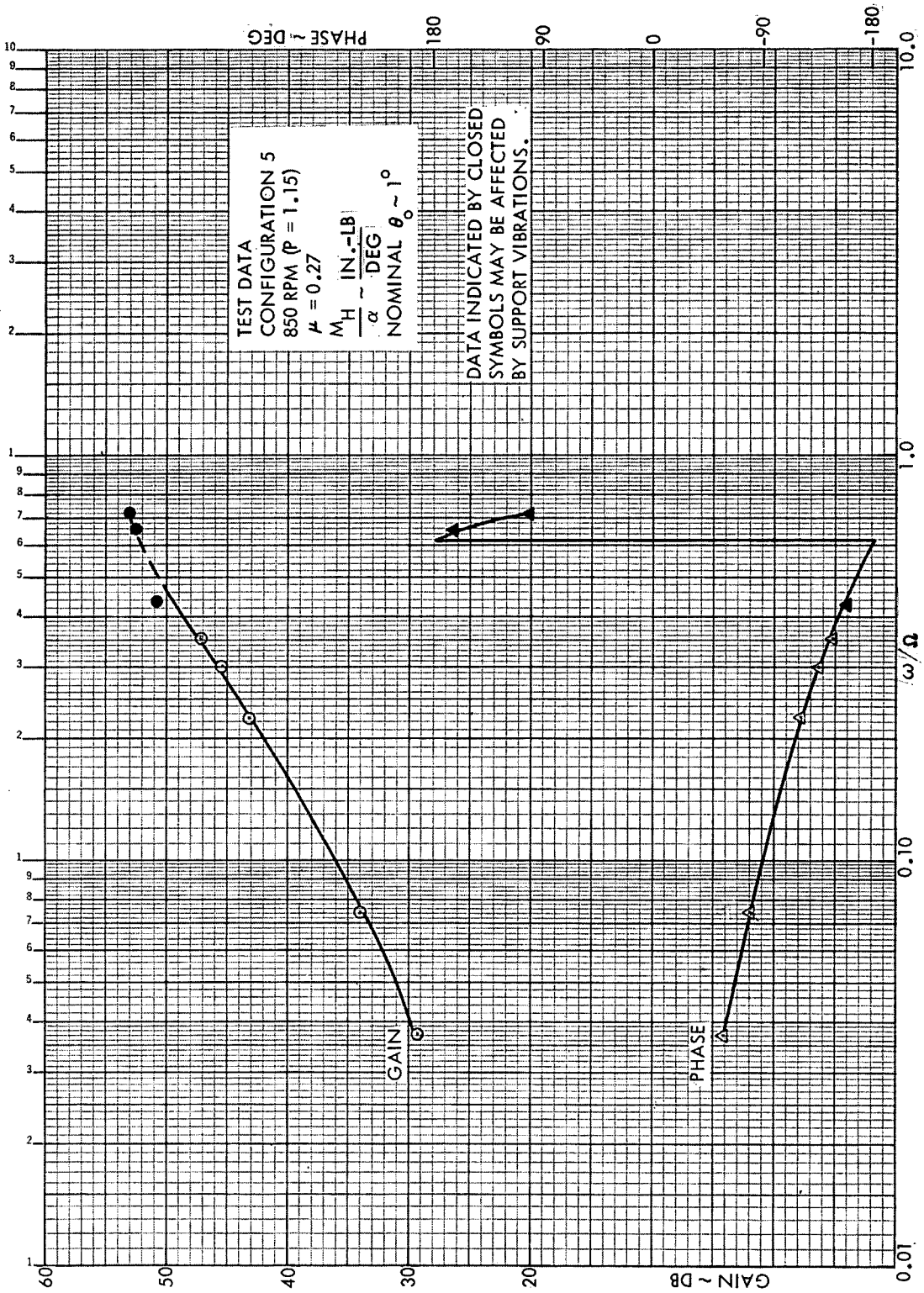


Figure C3. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $\mu = 1.15$ )

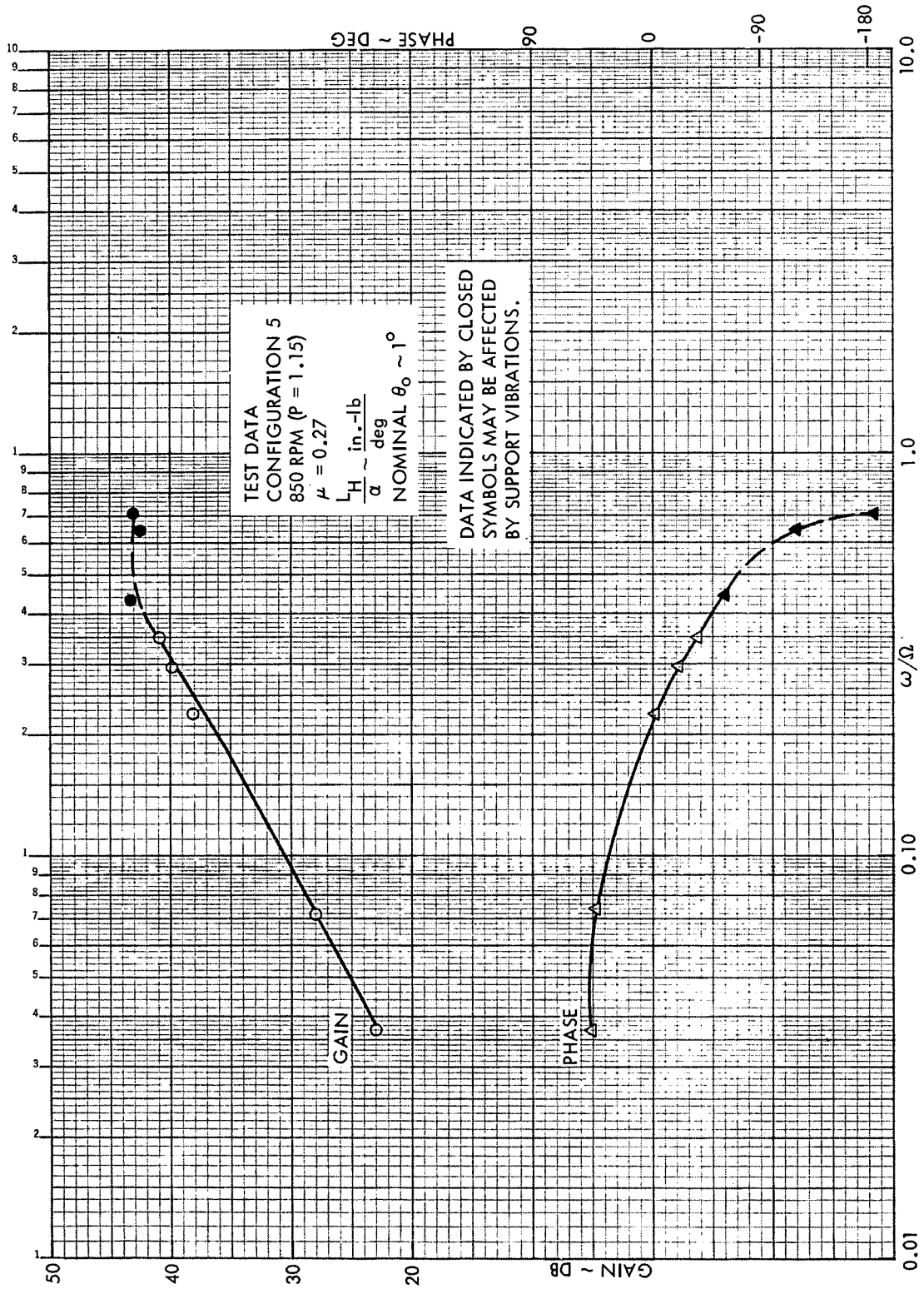


Figure C4. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )

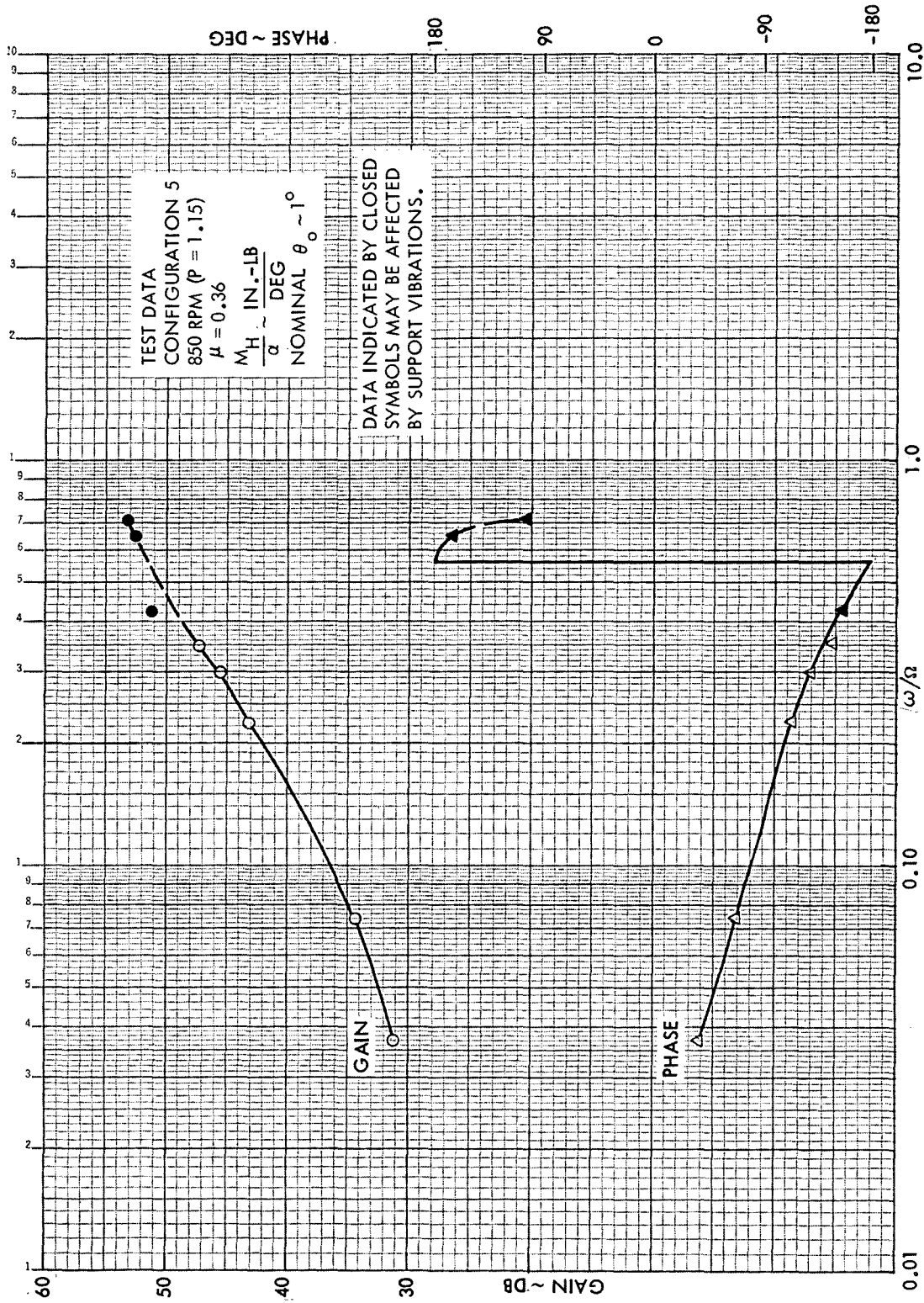


Figure C5. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM (P = 1.15)

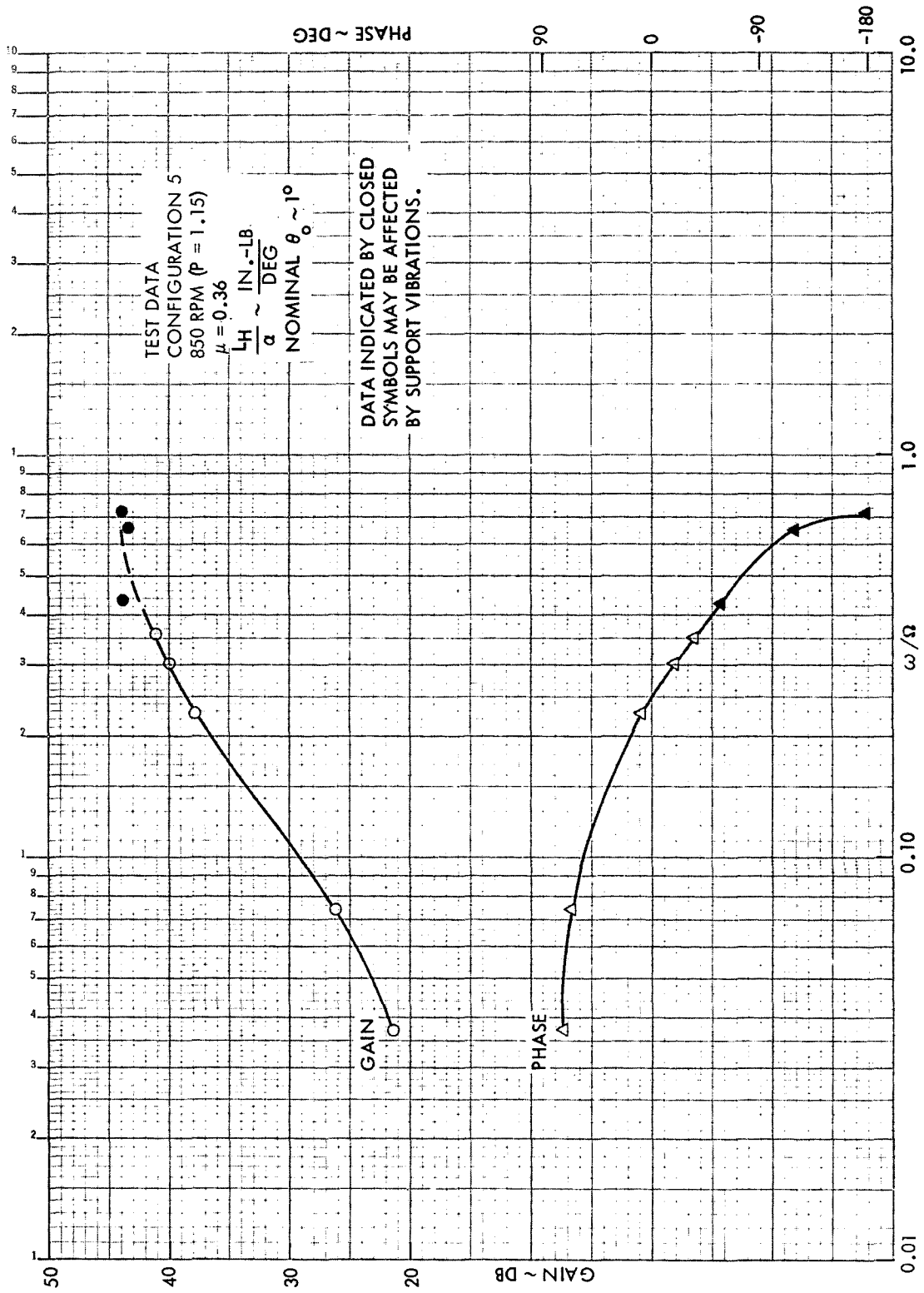


Figure C6. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.36$ , 850 RPM ( $P = 1.15$ )



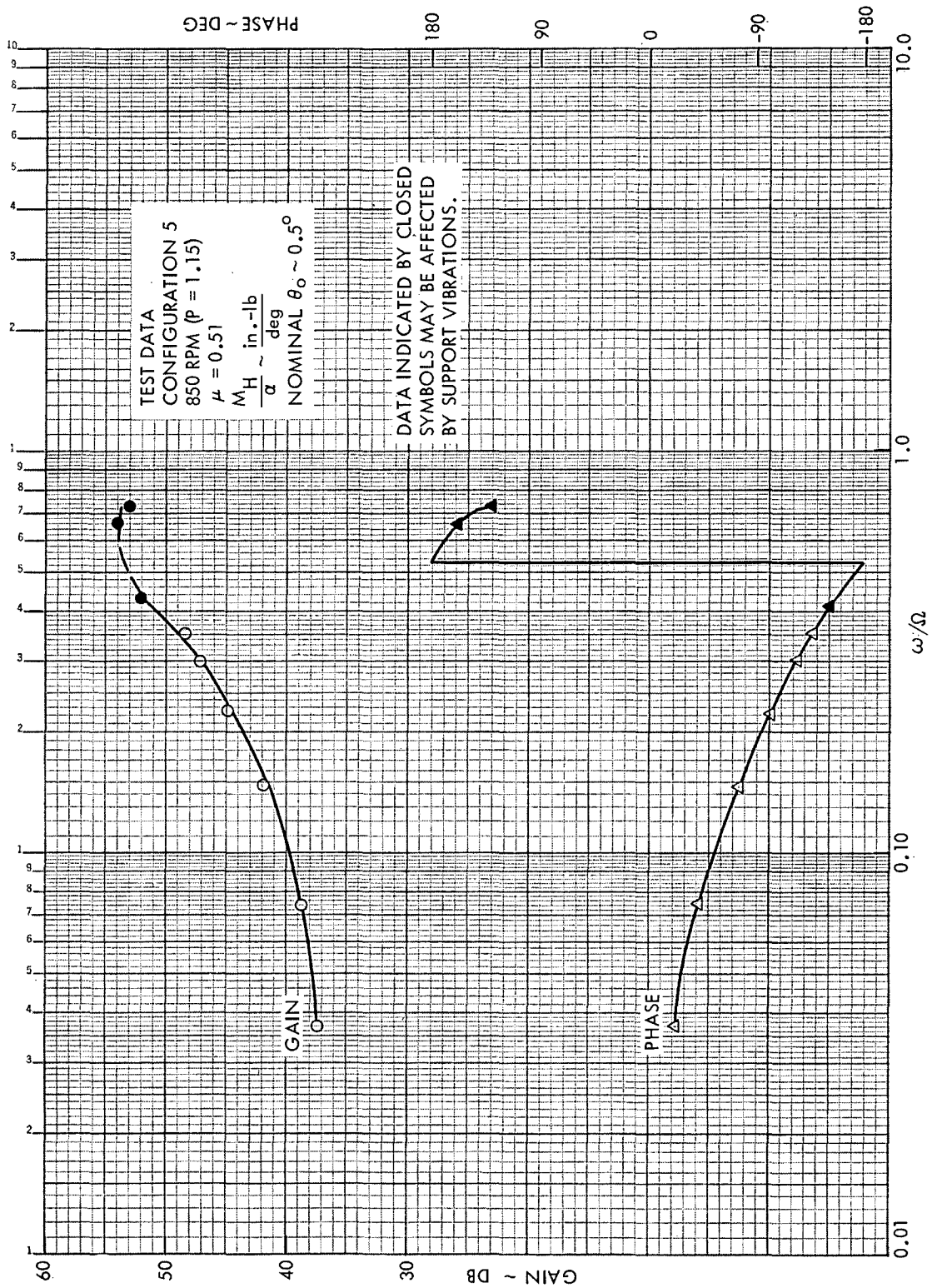


Figure C7. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )

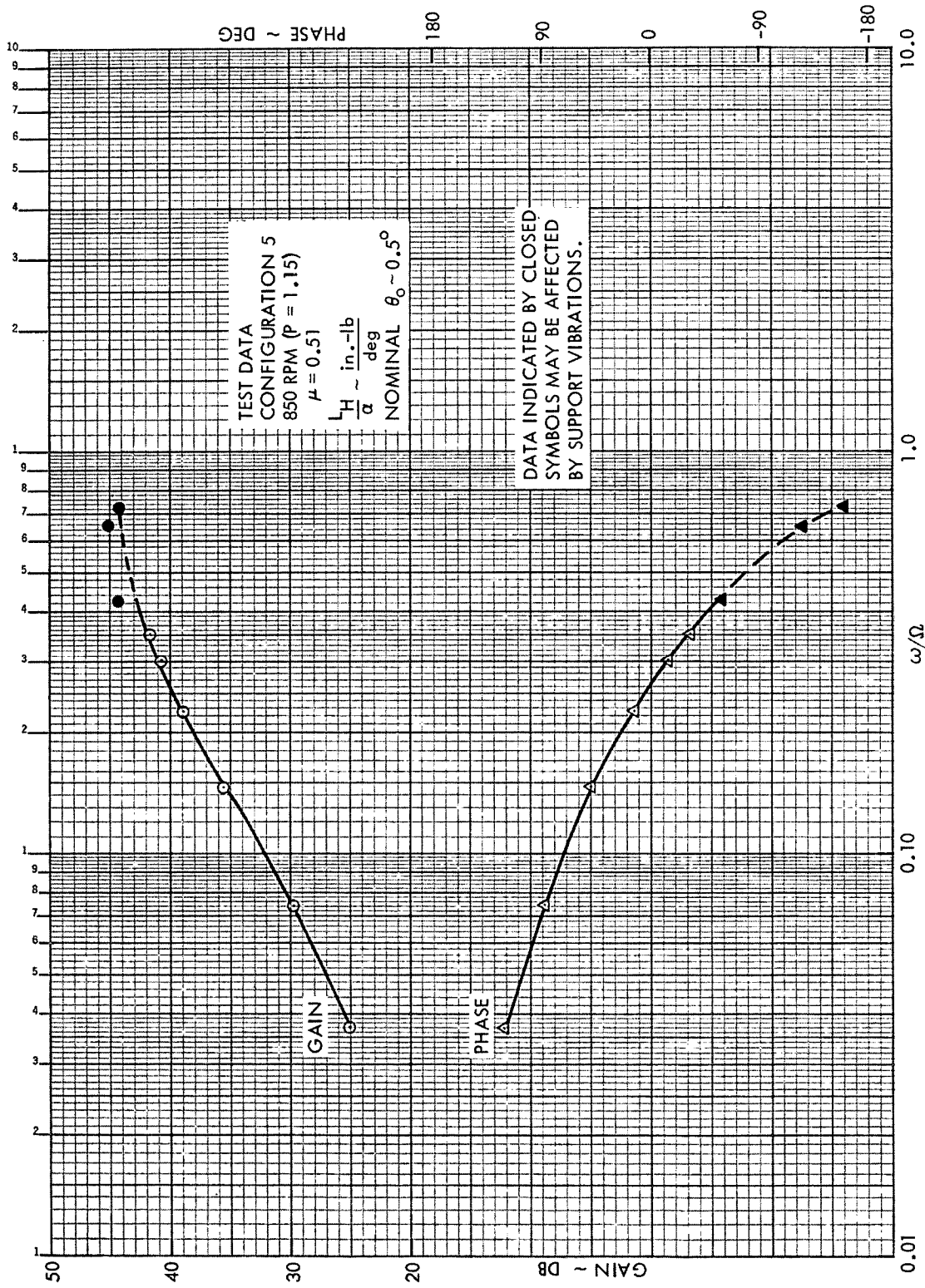


Figure C8. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )



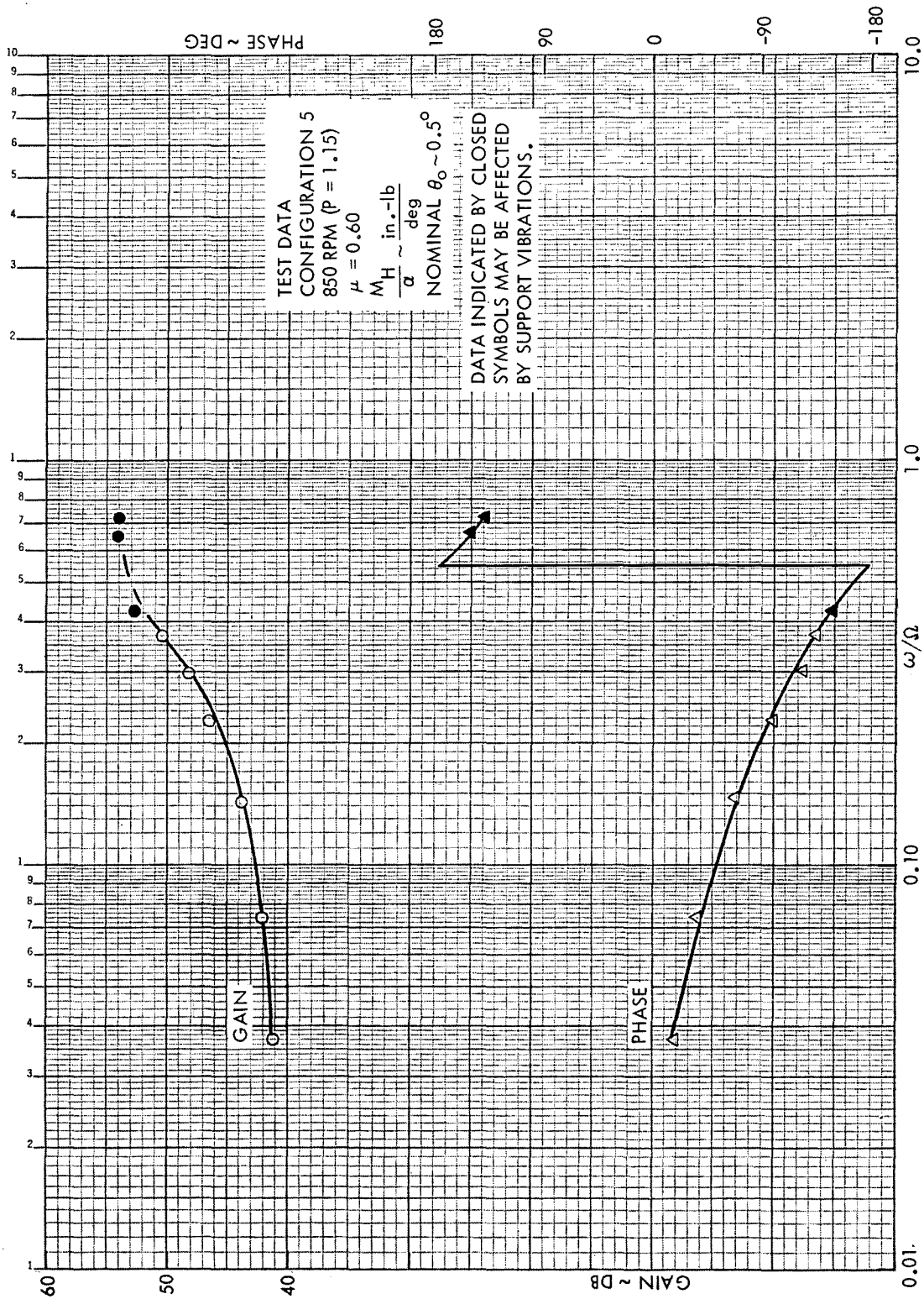


Figure C9. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM (P = 1.15)

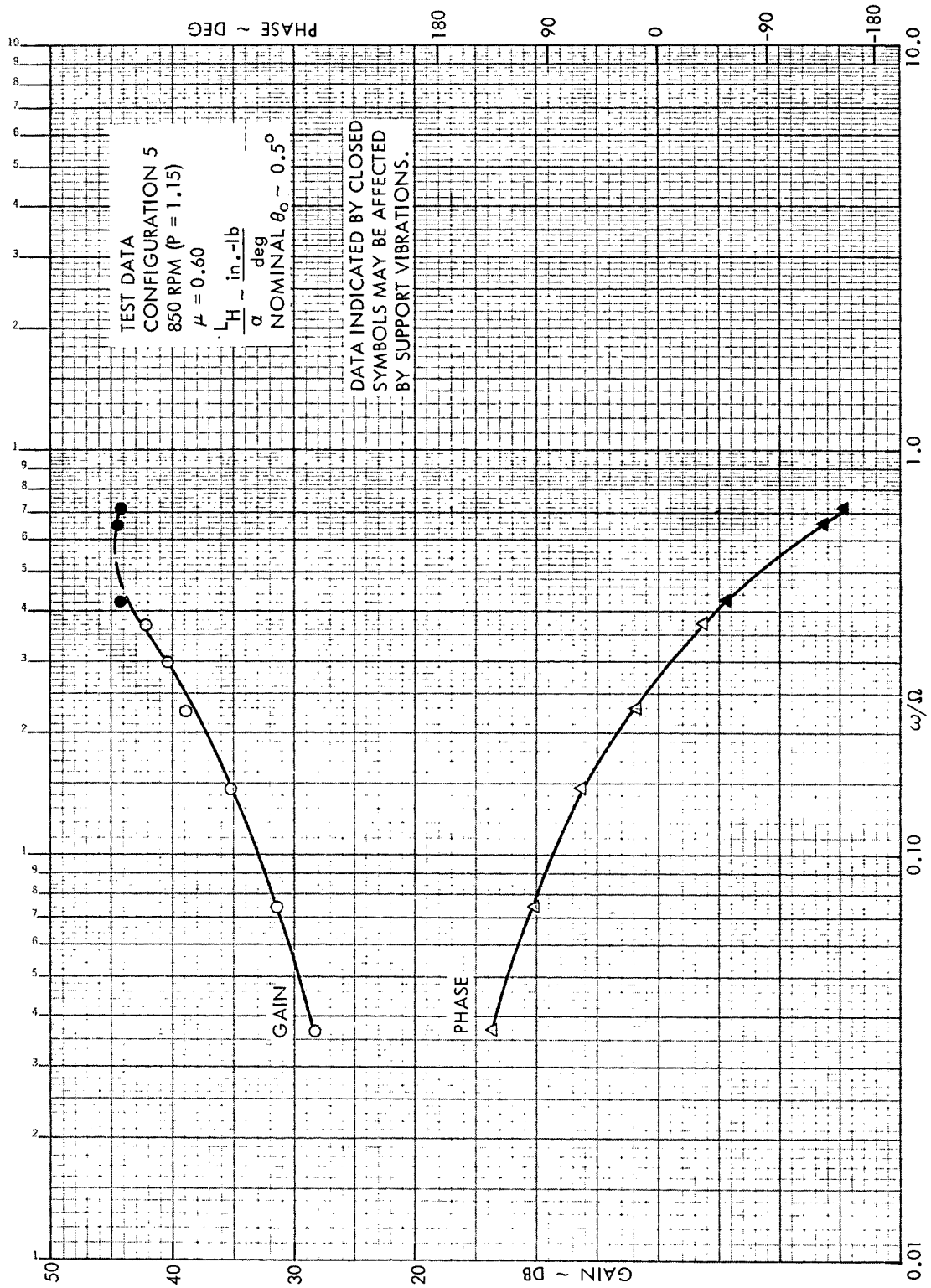


Figure C10. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )

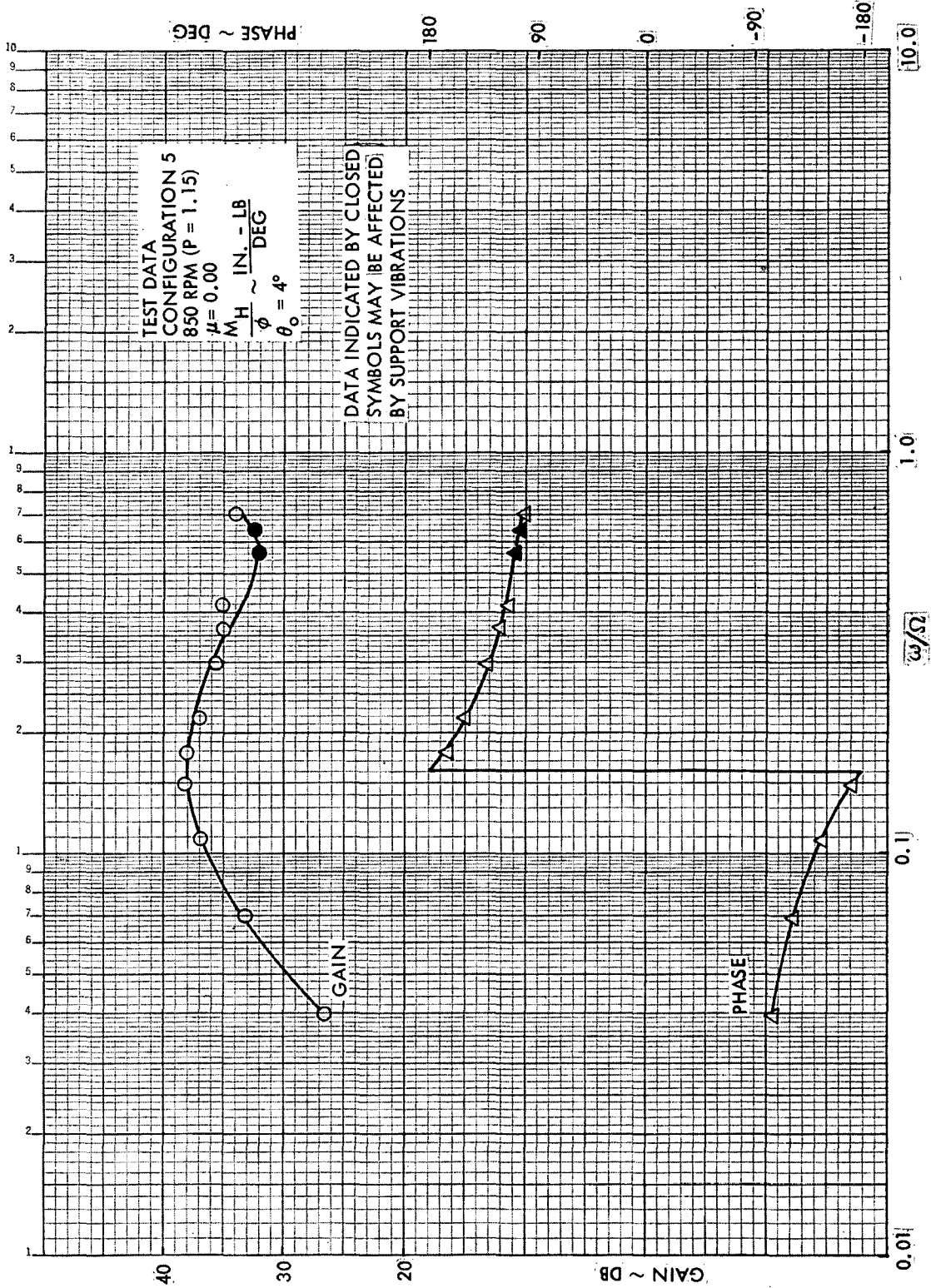


Figure C11. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.0$ , 850 RPM ( $\mu = 1.15$ )

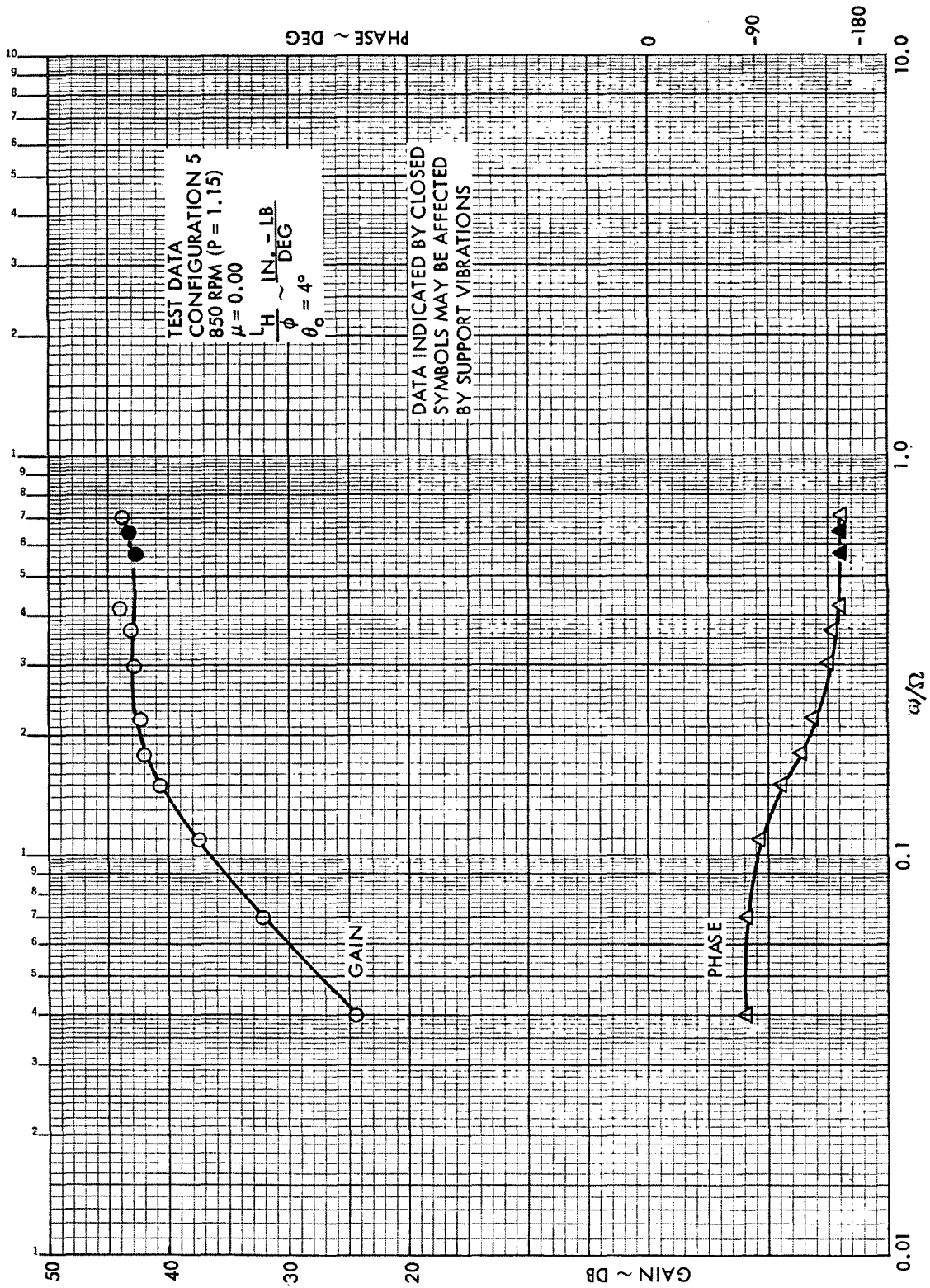


Figure C12. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.0$ , 850 RPM (P = 1.15)

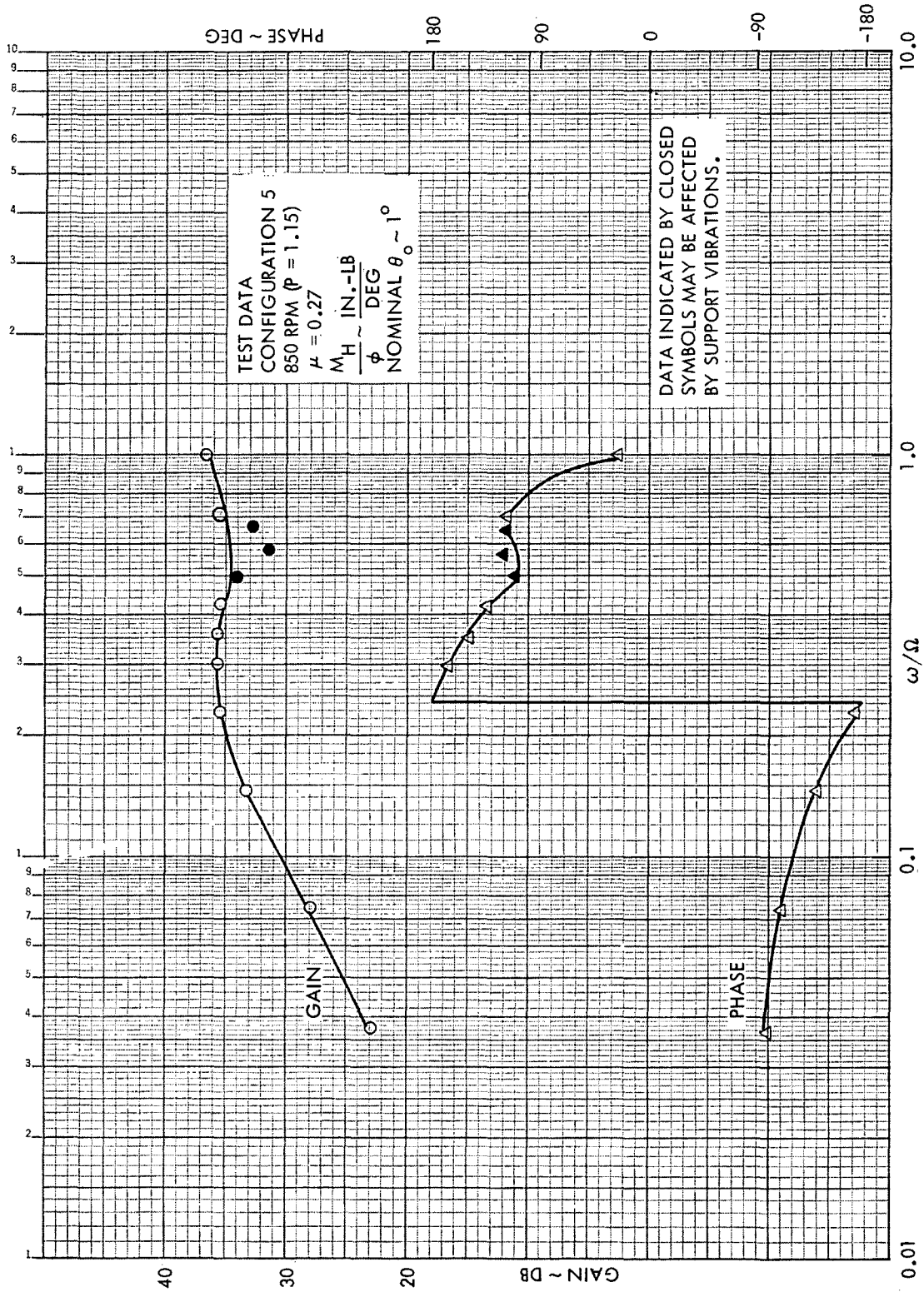


Figure C13. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $\mu = 1.15$ )

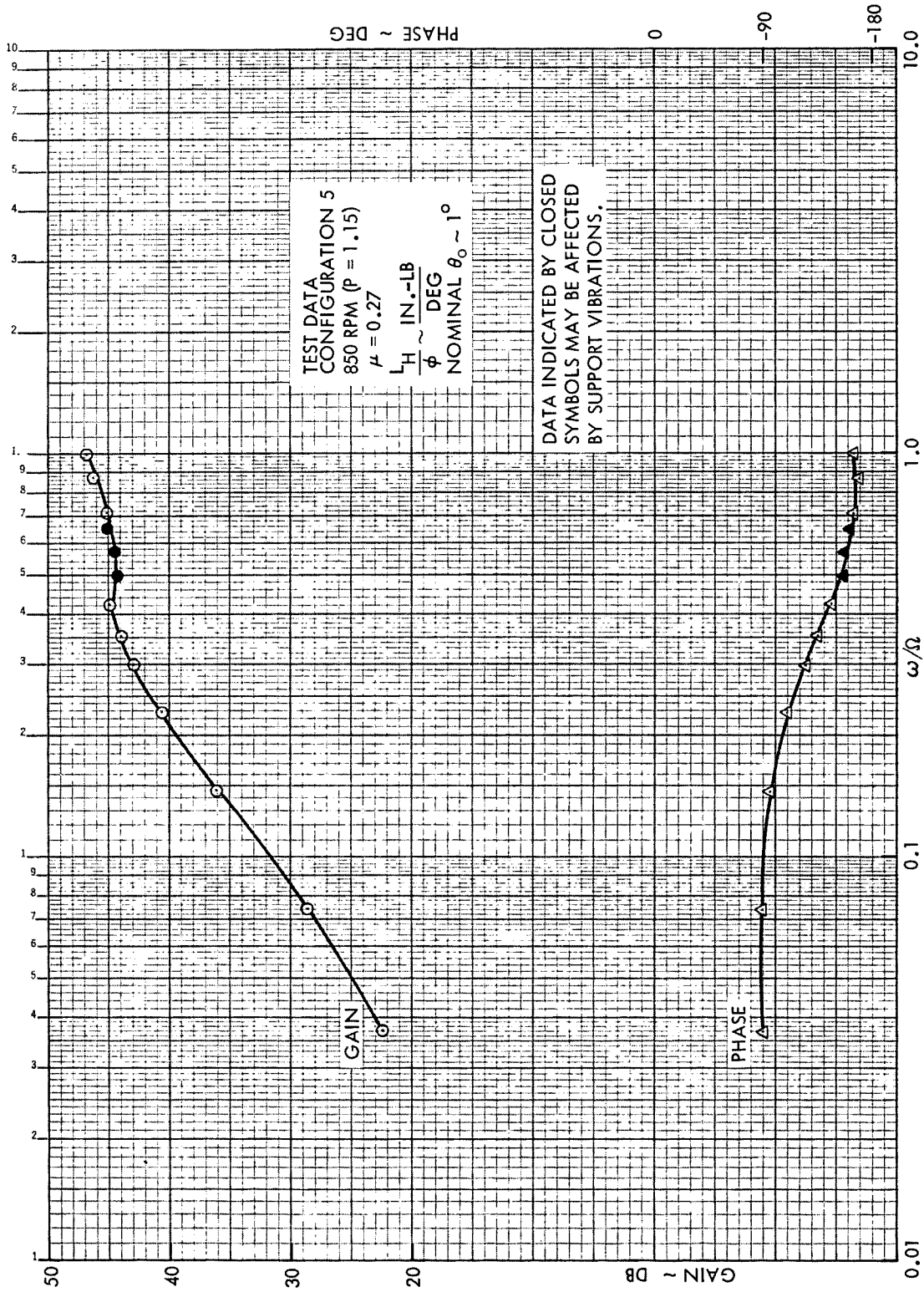


Figure C14. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.27$ , 850 RPM ( $P = 1.15$ )



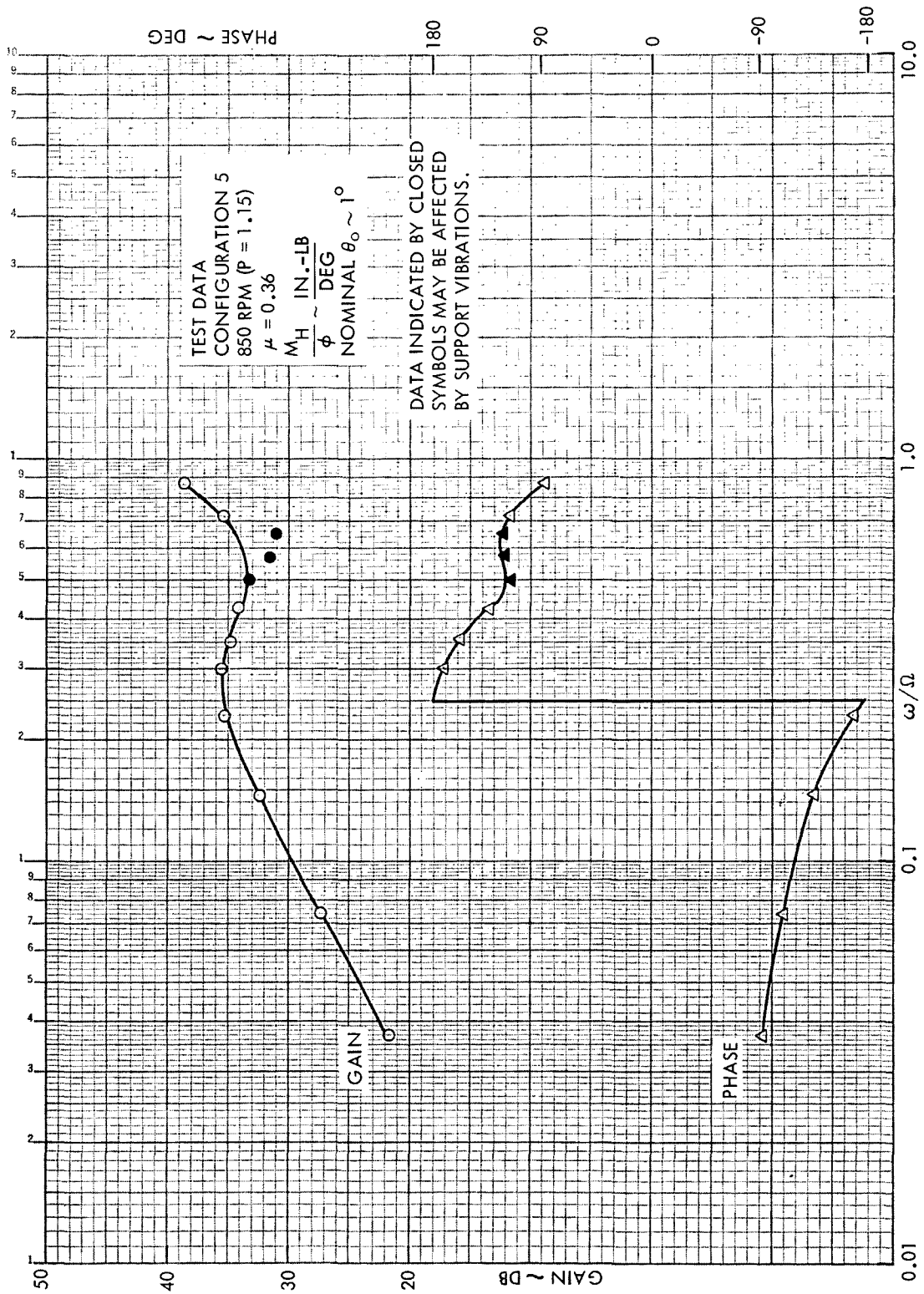


Figure C15. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.36$ , 850 RPM ( $P = 1.15$ )



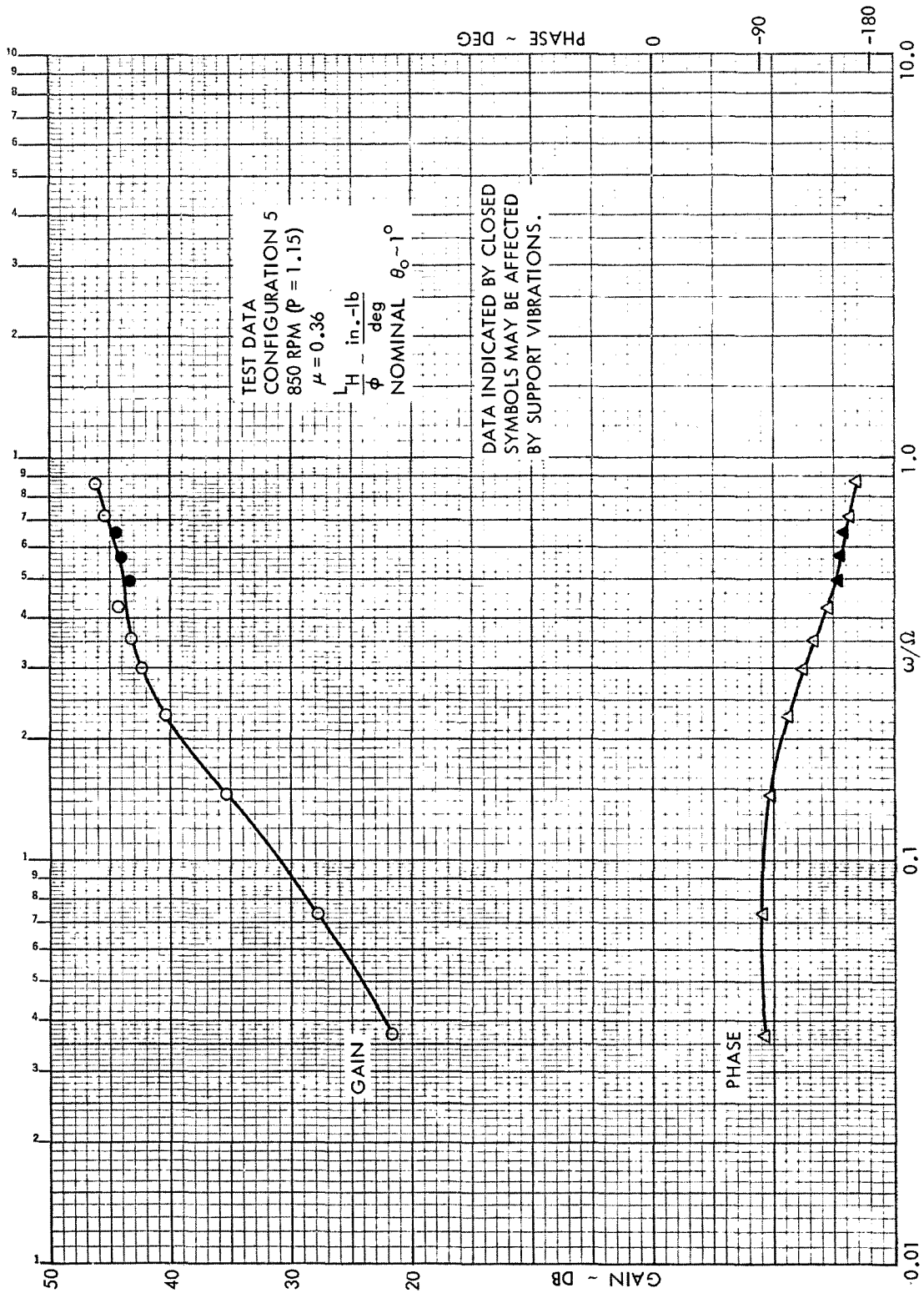


Figure C16. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.36$ , 850 RPM ( $P = 1.15$ )



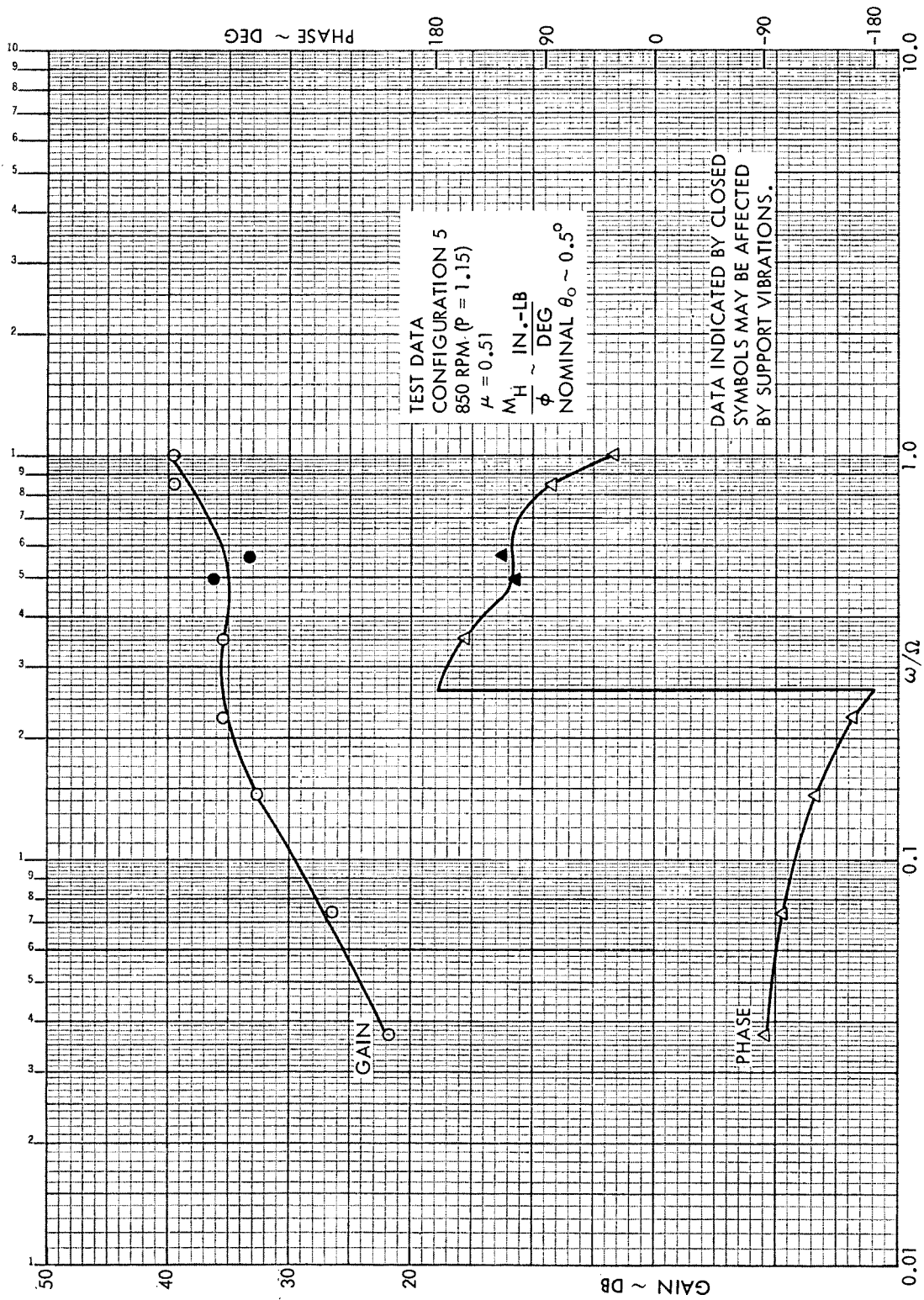


Figure C17. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )

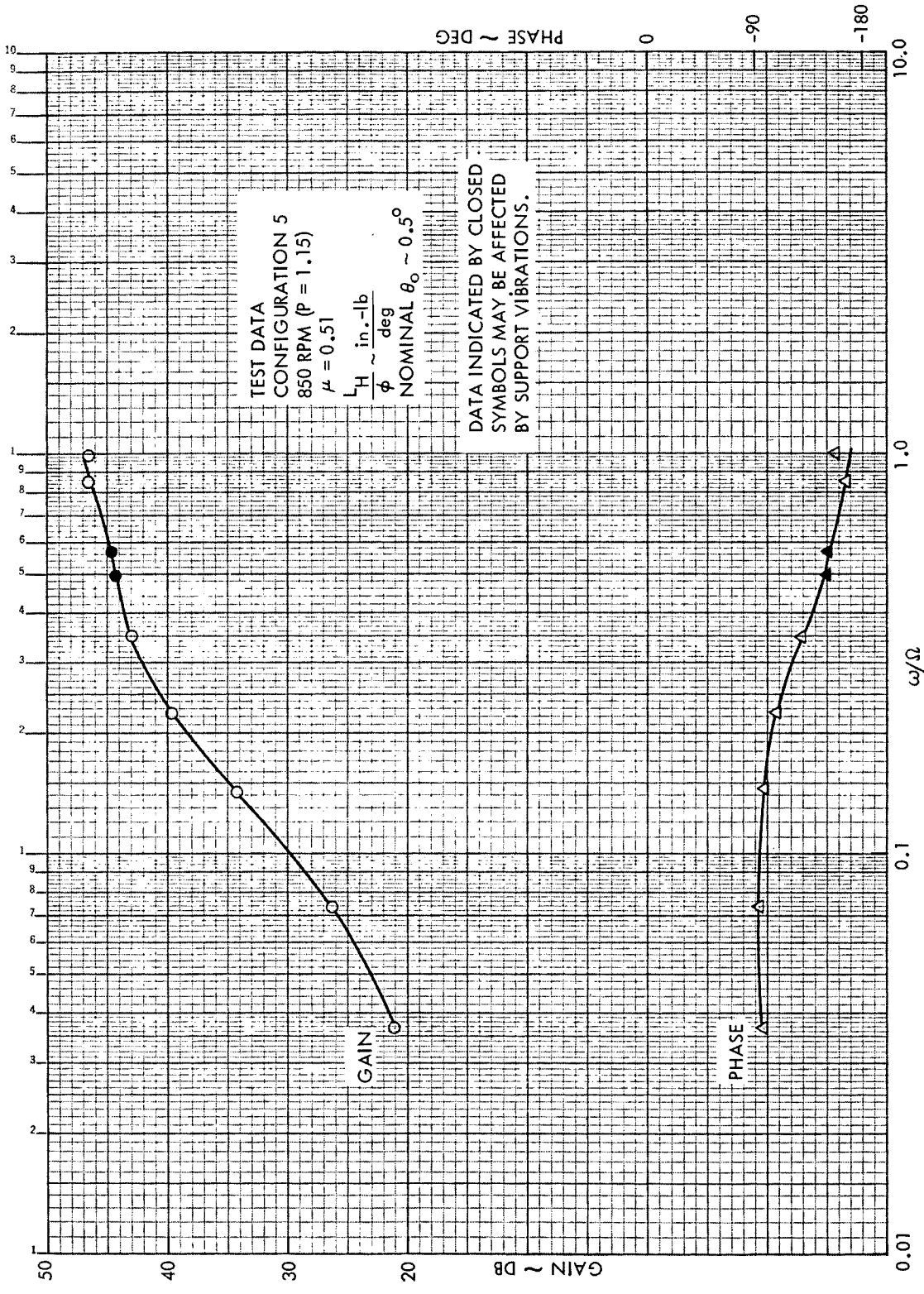


Figure C18. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.51$ , 850 RPM ( $P = 1.15$ )

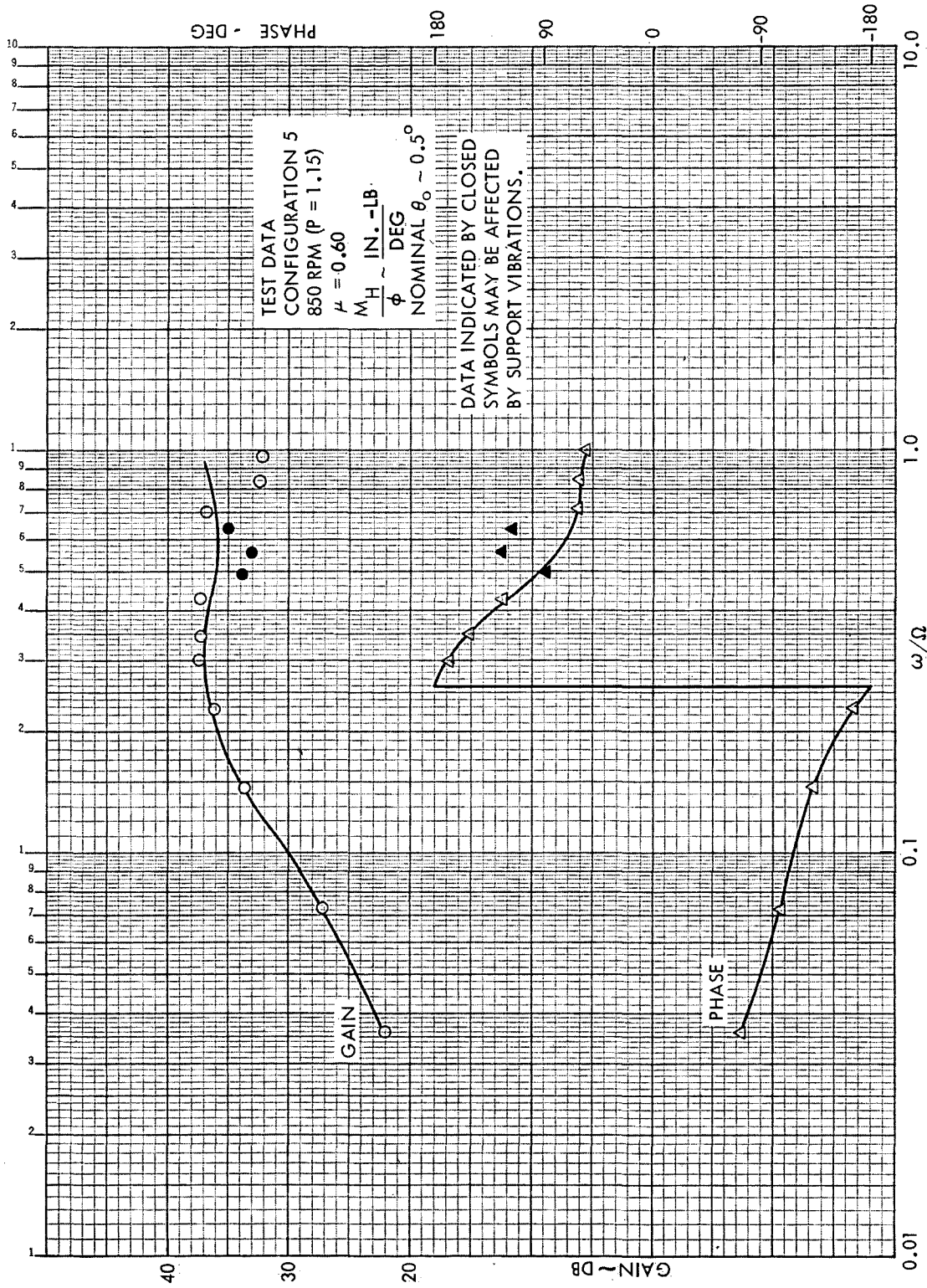


Figure C19. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.60$ , 850 RPM (P = 1.15)

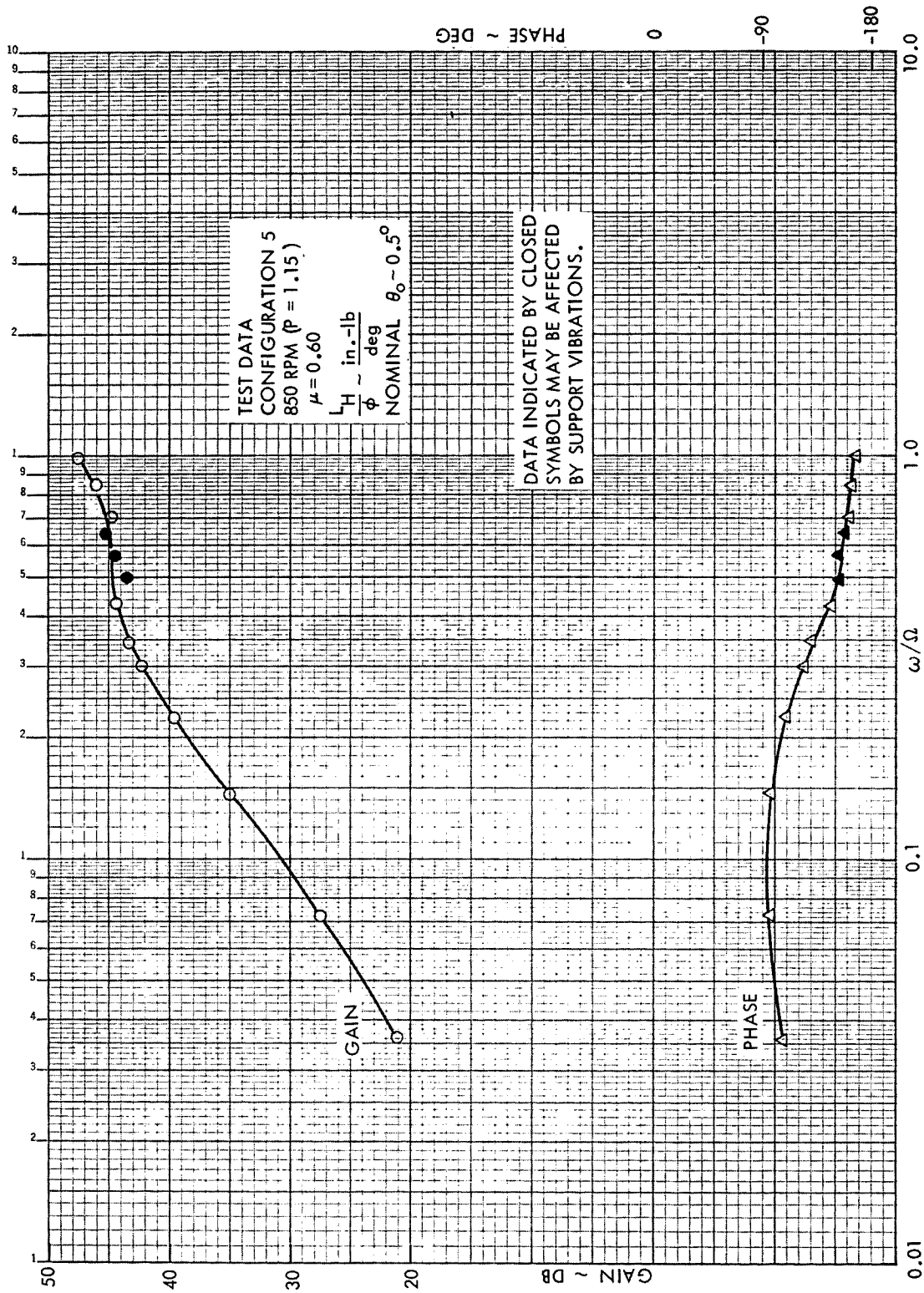


Figure C20. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.60$ , 850 RPM ( $P = 1.15$ )

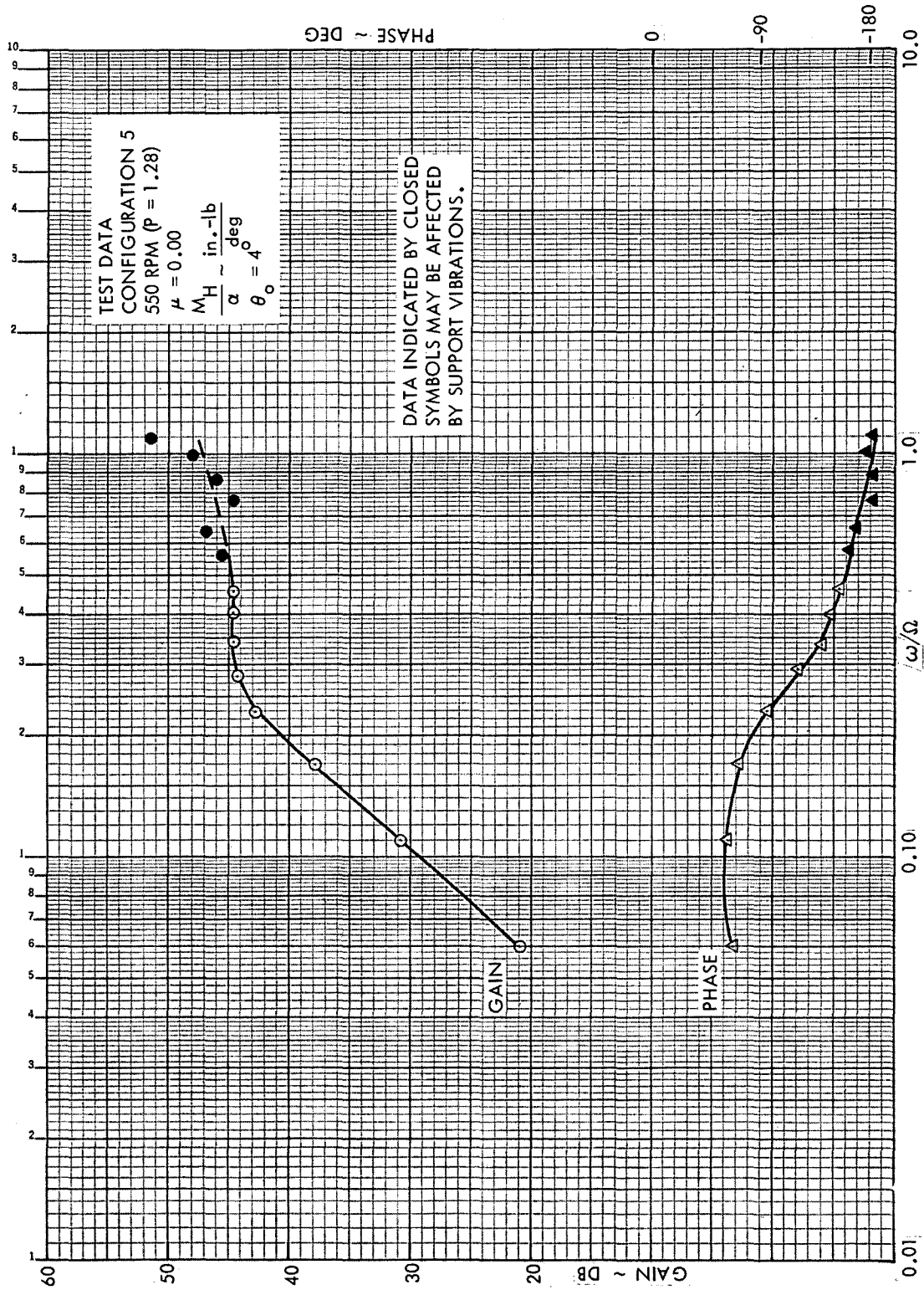


Figure C21. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.0$ , 550 RPM ( $P = 1.28$ )

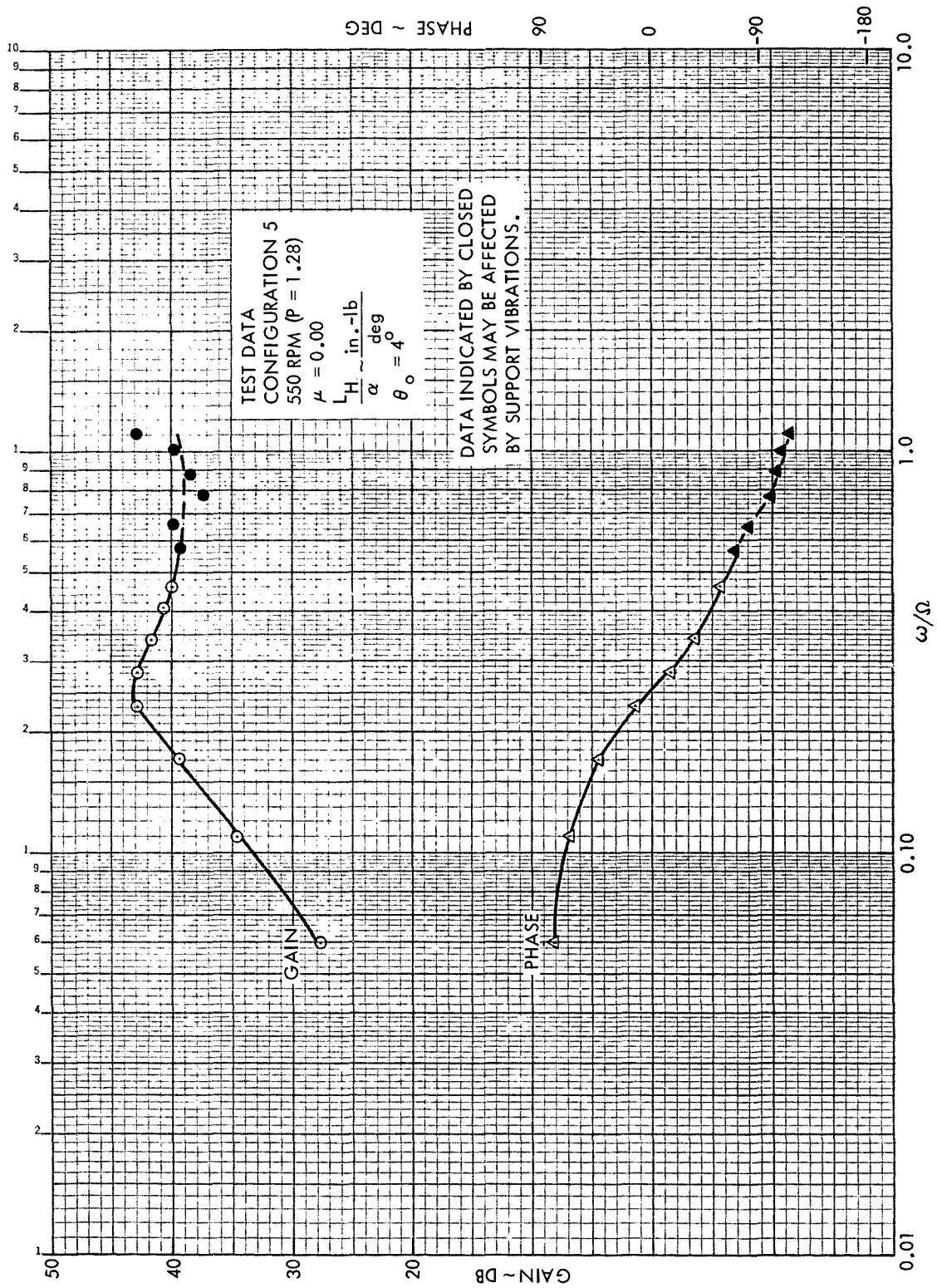


Figure C22. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 5,  $\mu = 0.00$ , 550 RPM ( $P = 1.28$ )



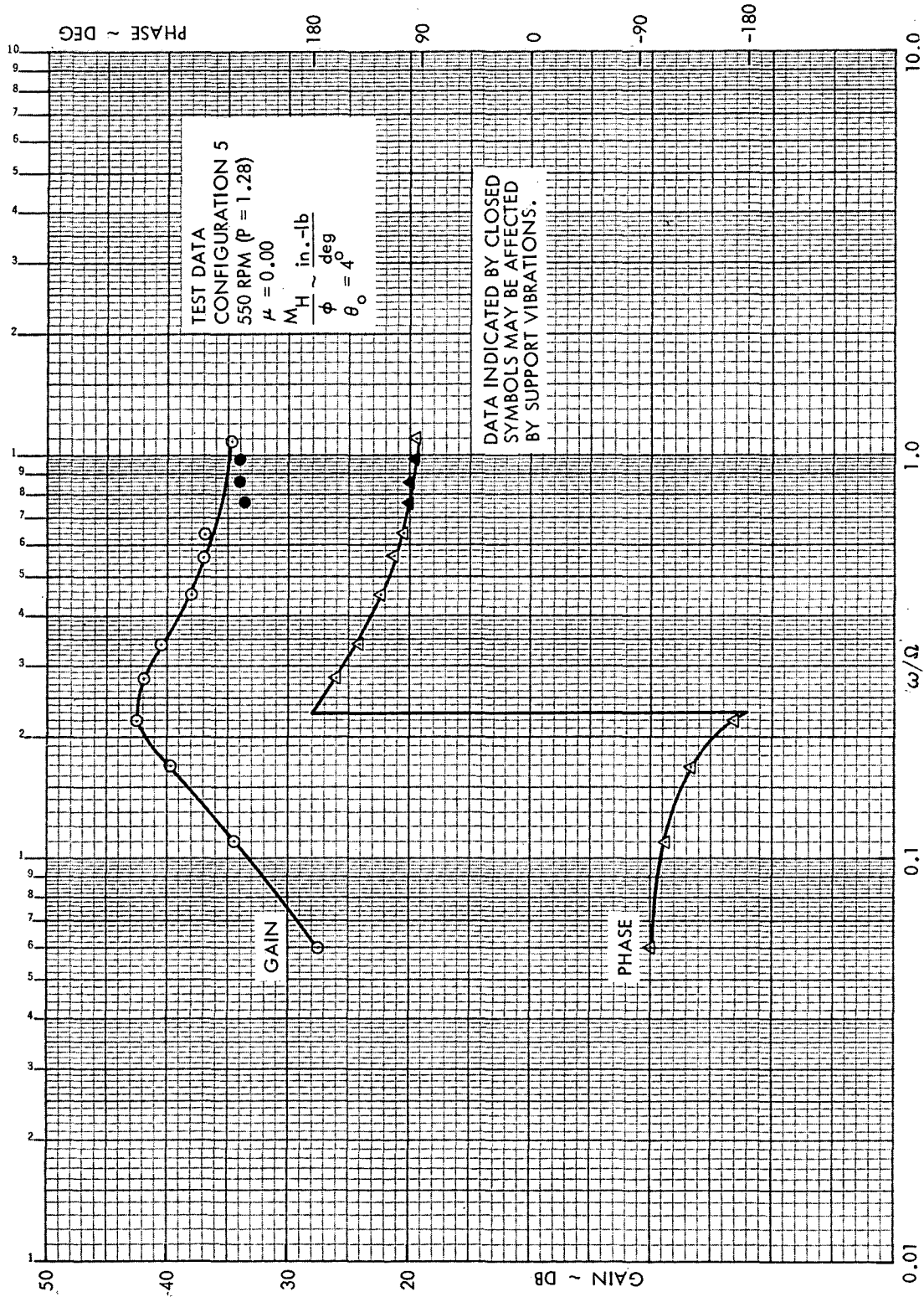


Figure C23. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.00$ , 550 RPM ( $\mu = 1.28$ )

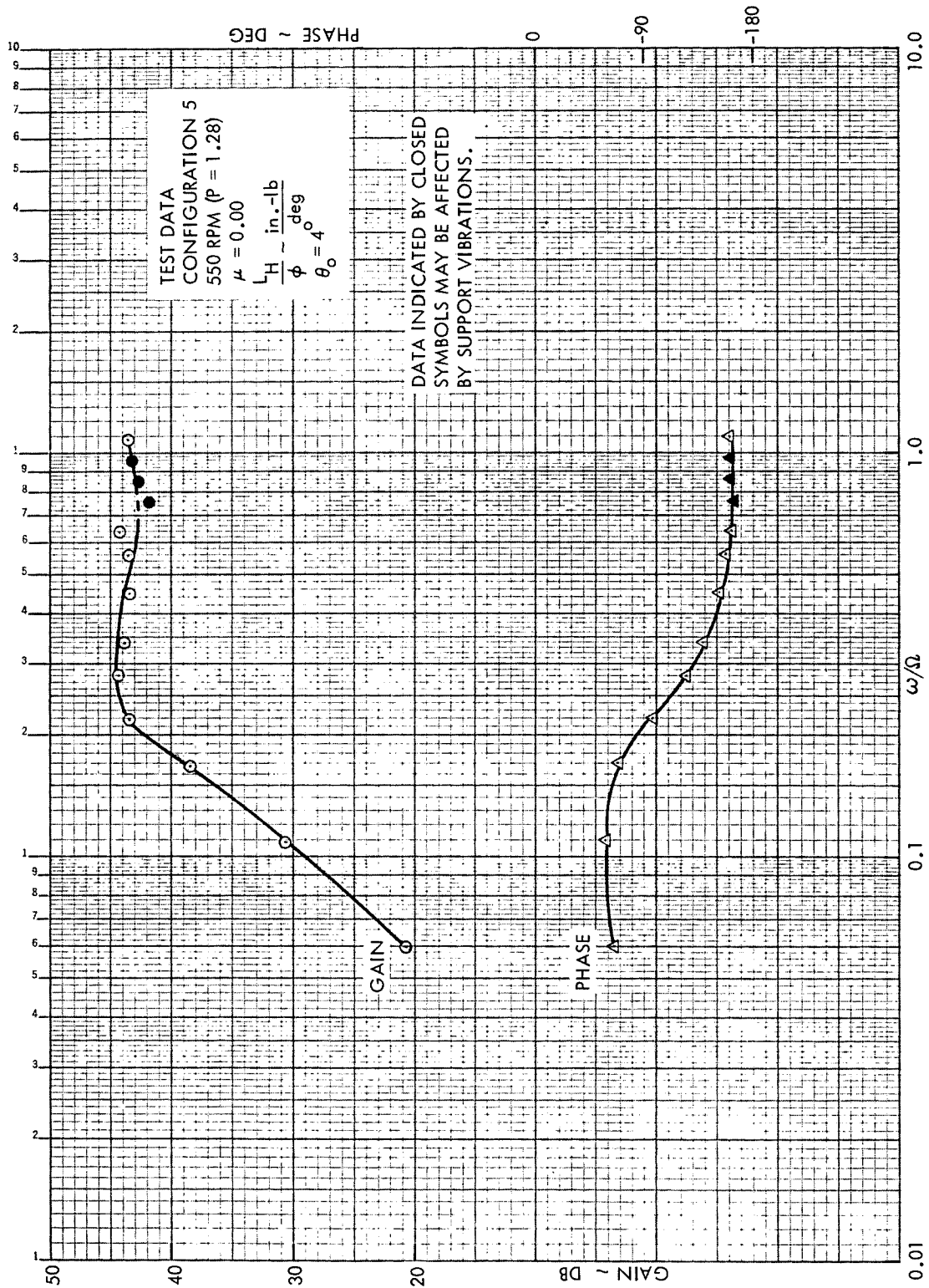


Figure C24. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 5,  $\mu = 0.00$ , 550 RPM ( $P = 1.28$ )



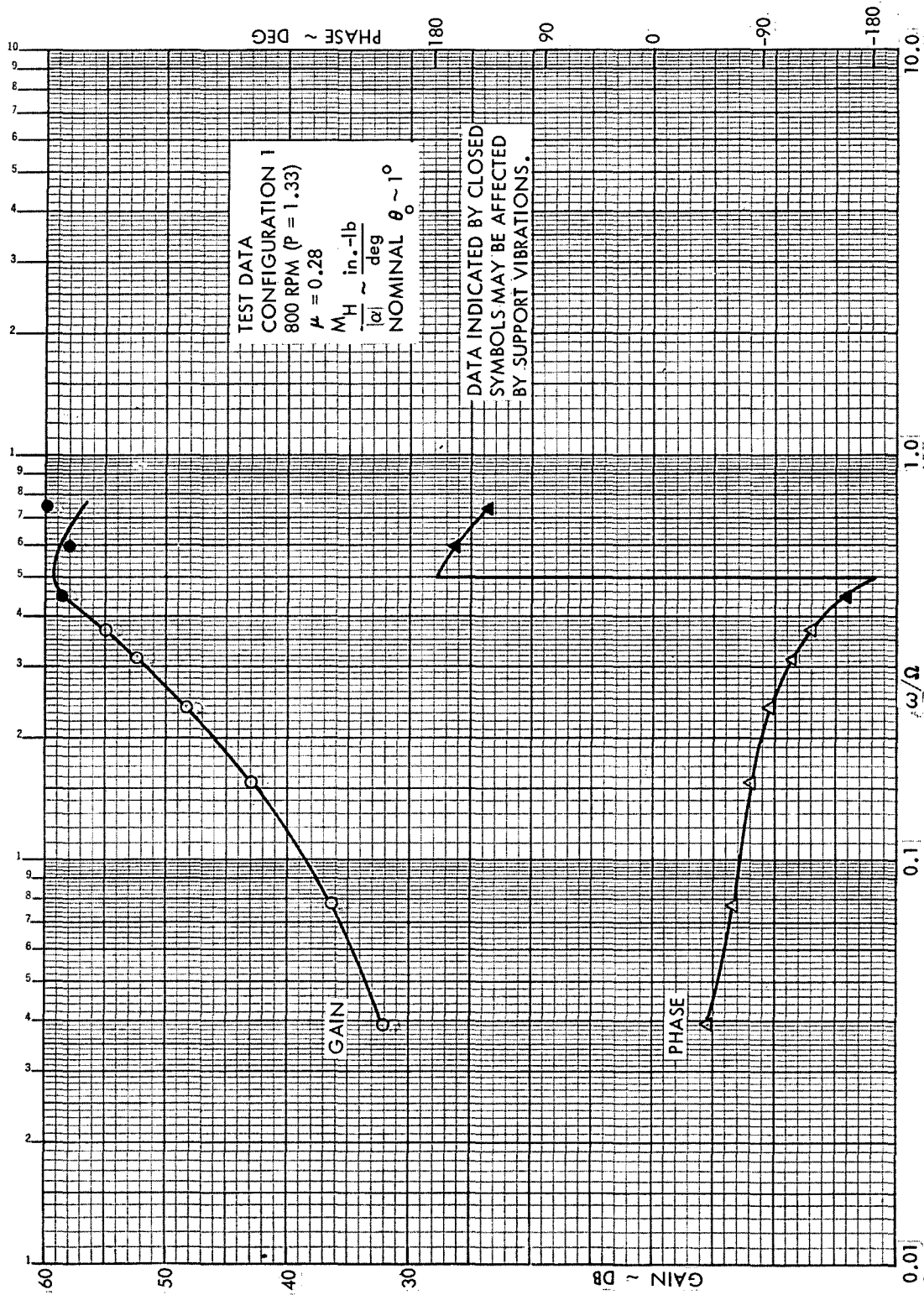


Figure C25. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.28$ , 800 RPM ( $P = 1.33$ )

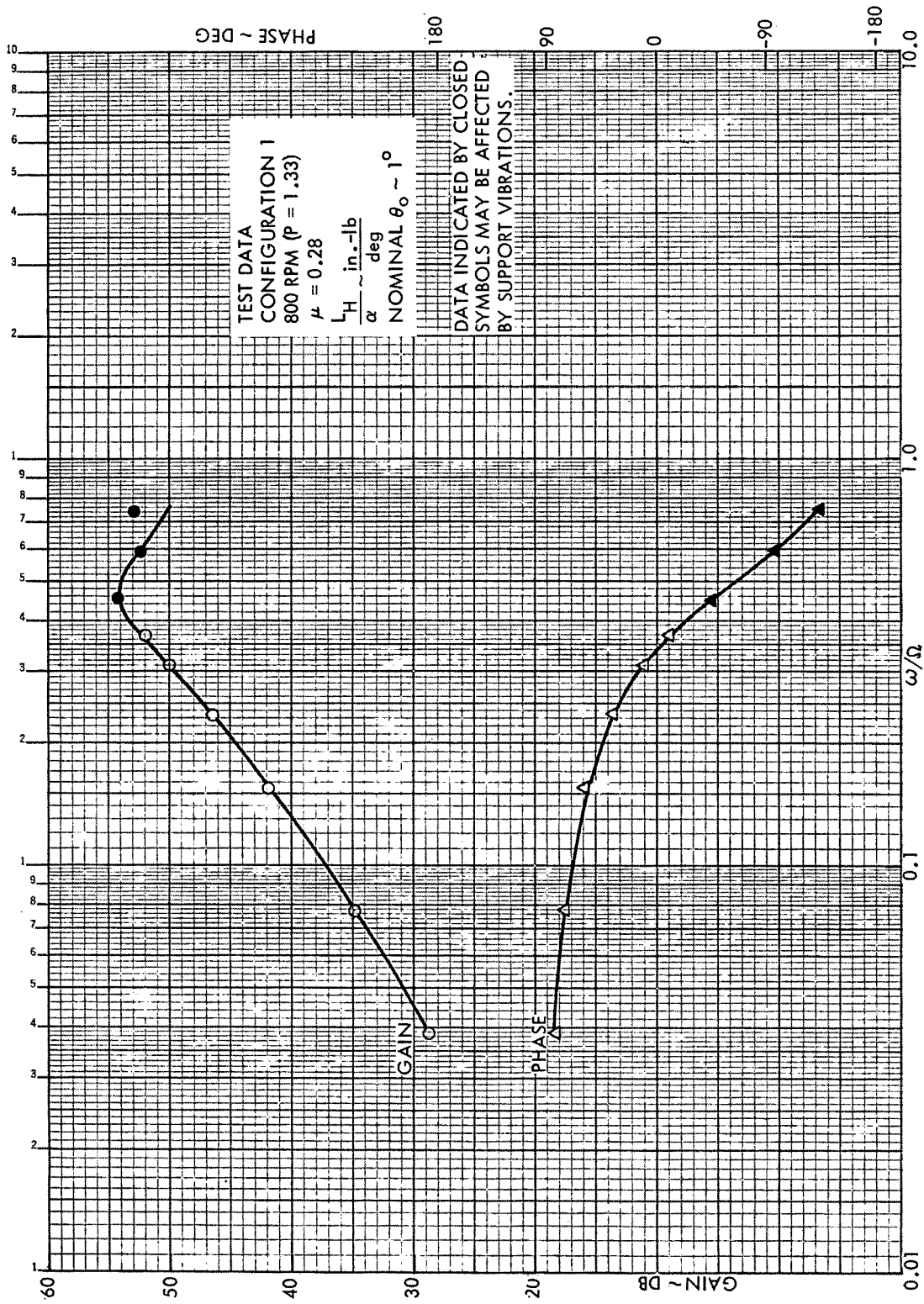


Figure C26. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.28$ , 800 RPM ( $P = 1.33$ )

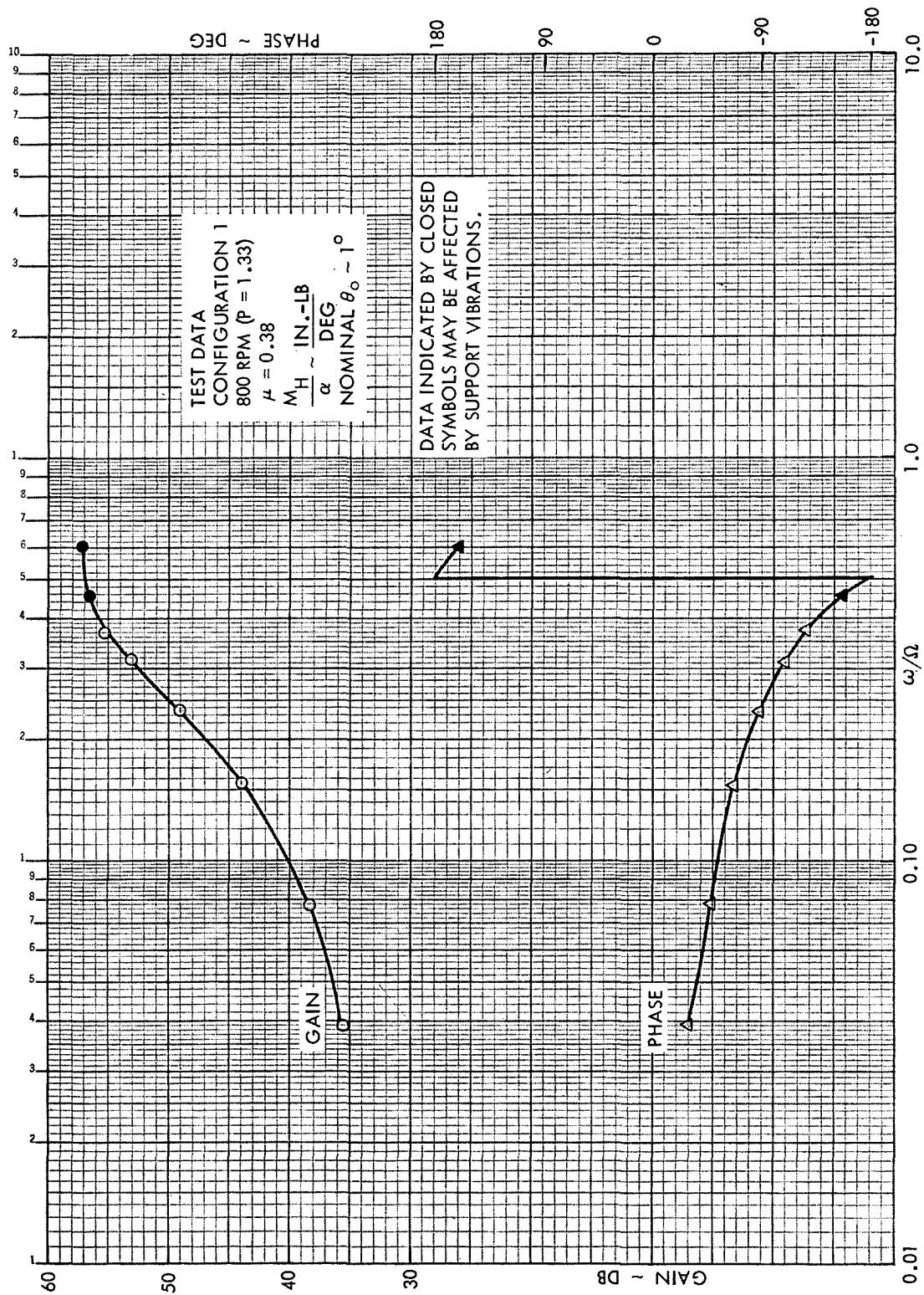


Figure C27. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.38$ , 800 RPM ( $P = 1.33$ )

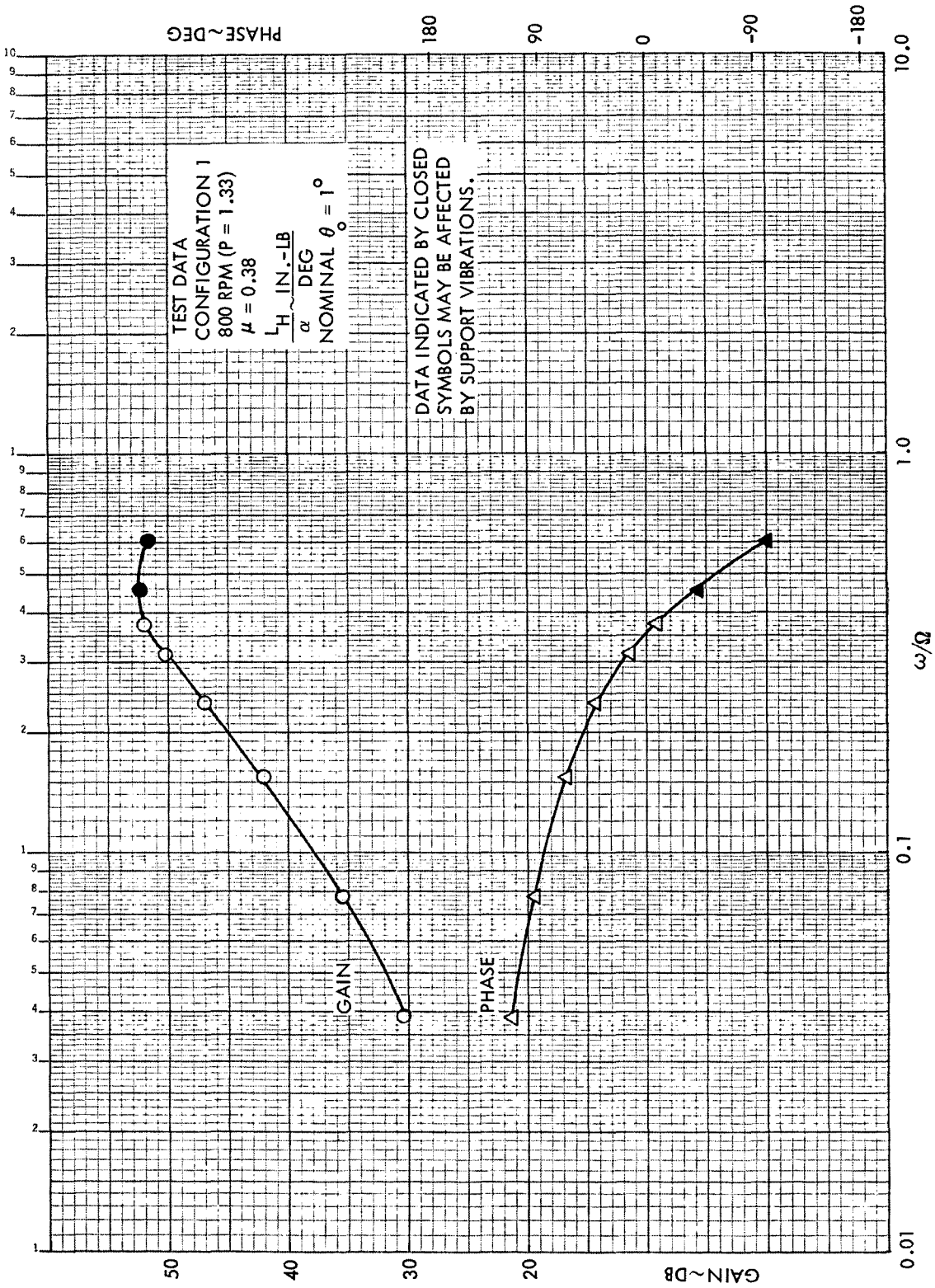


Figure C28. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.38$ , 800 RPM (P = 1.33)

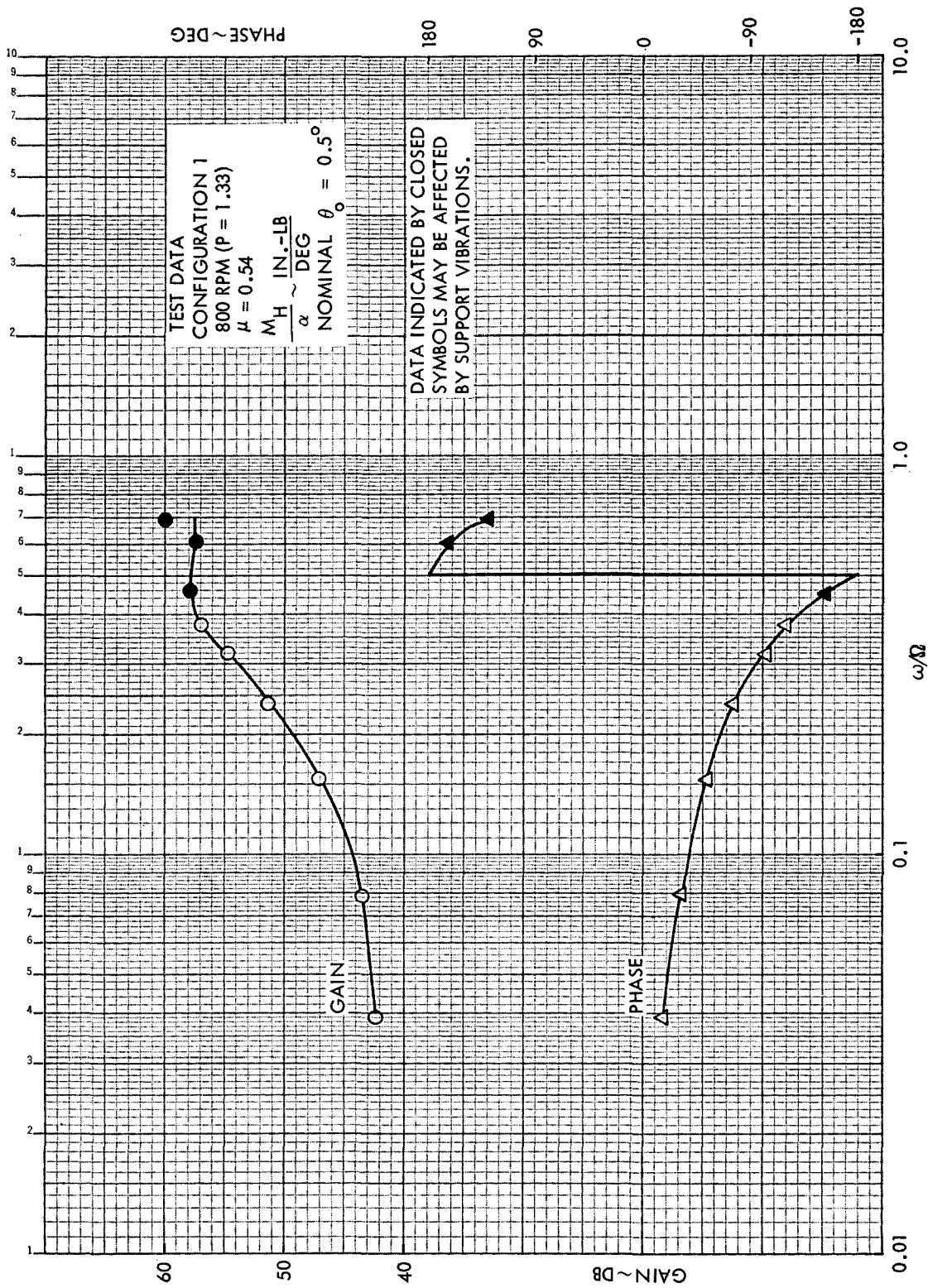


Figure C29. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.54$ , 800 RPM ( $P = 1.33$ )

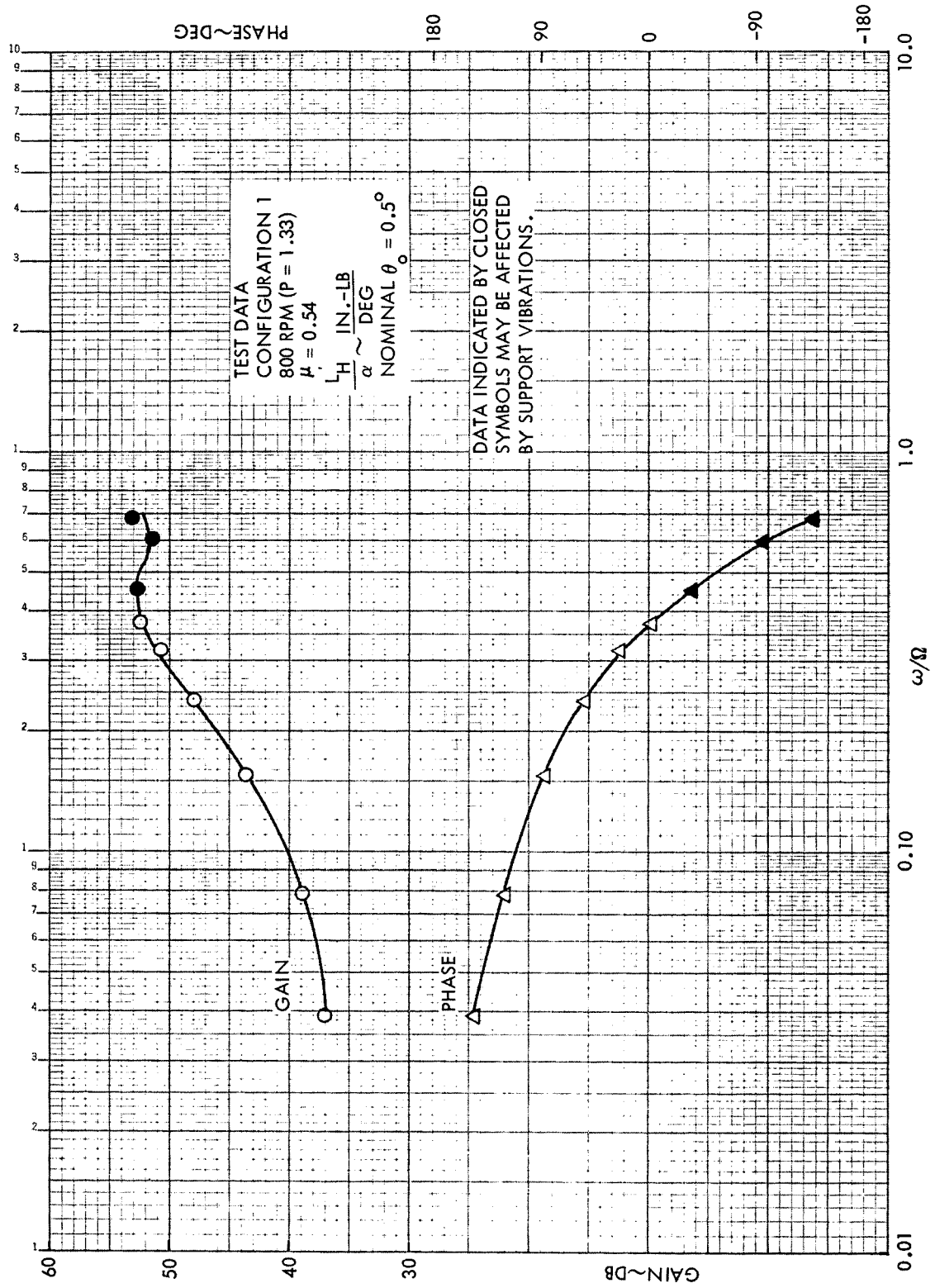


Figure C30. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.54$ , 800 RPM (P = 1.33)



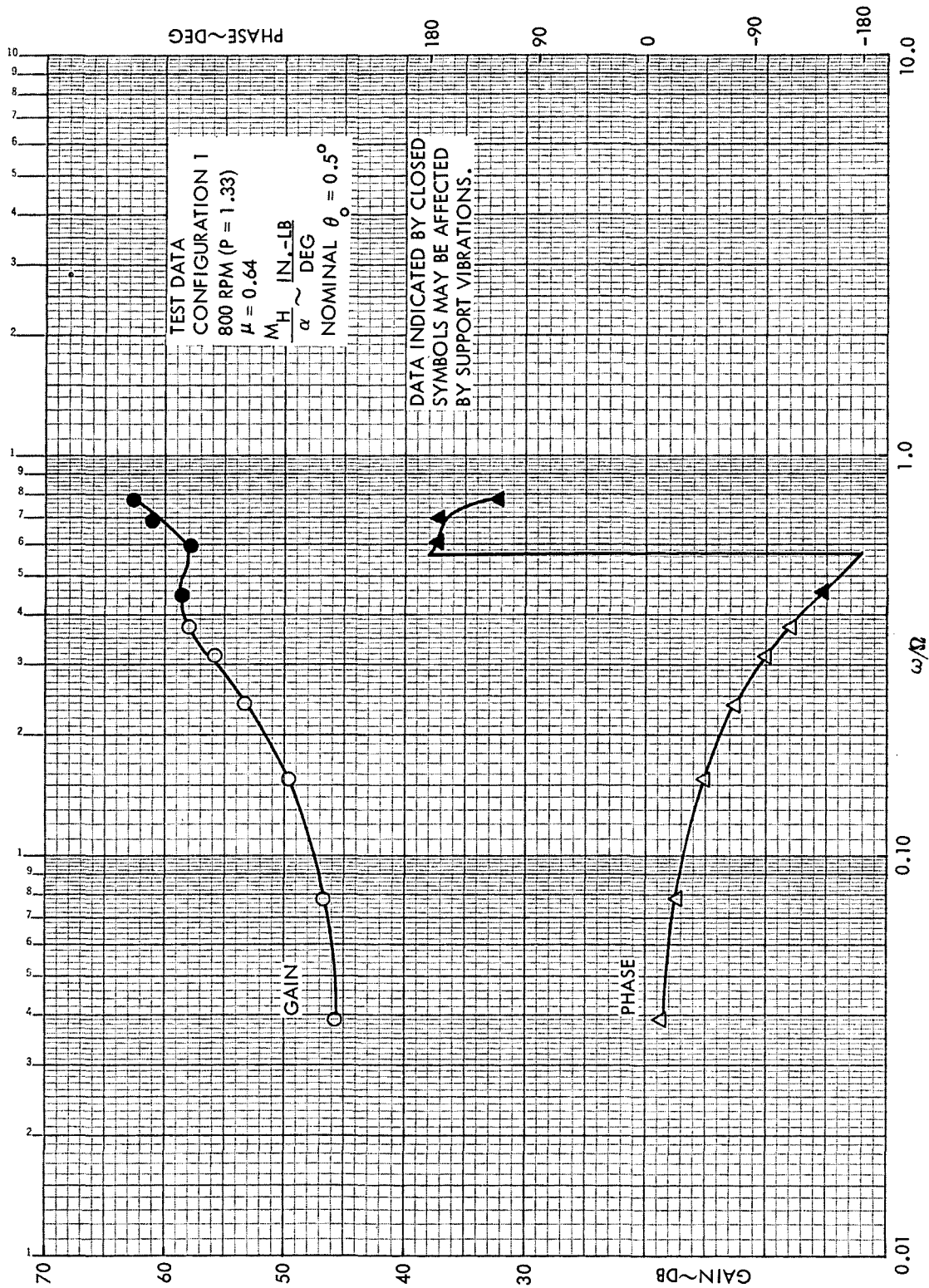


Figure C31. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.64$ , 800 RPM ( $P = 1.33$ )

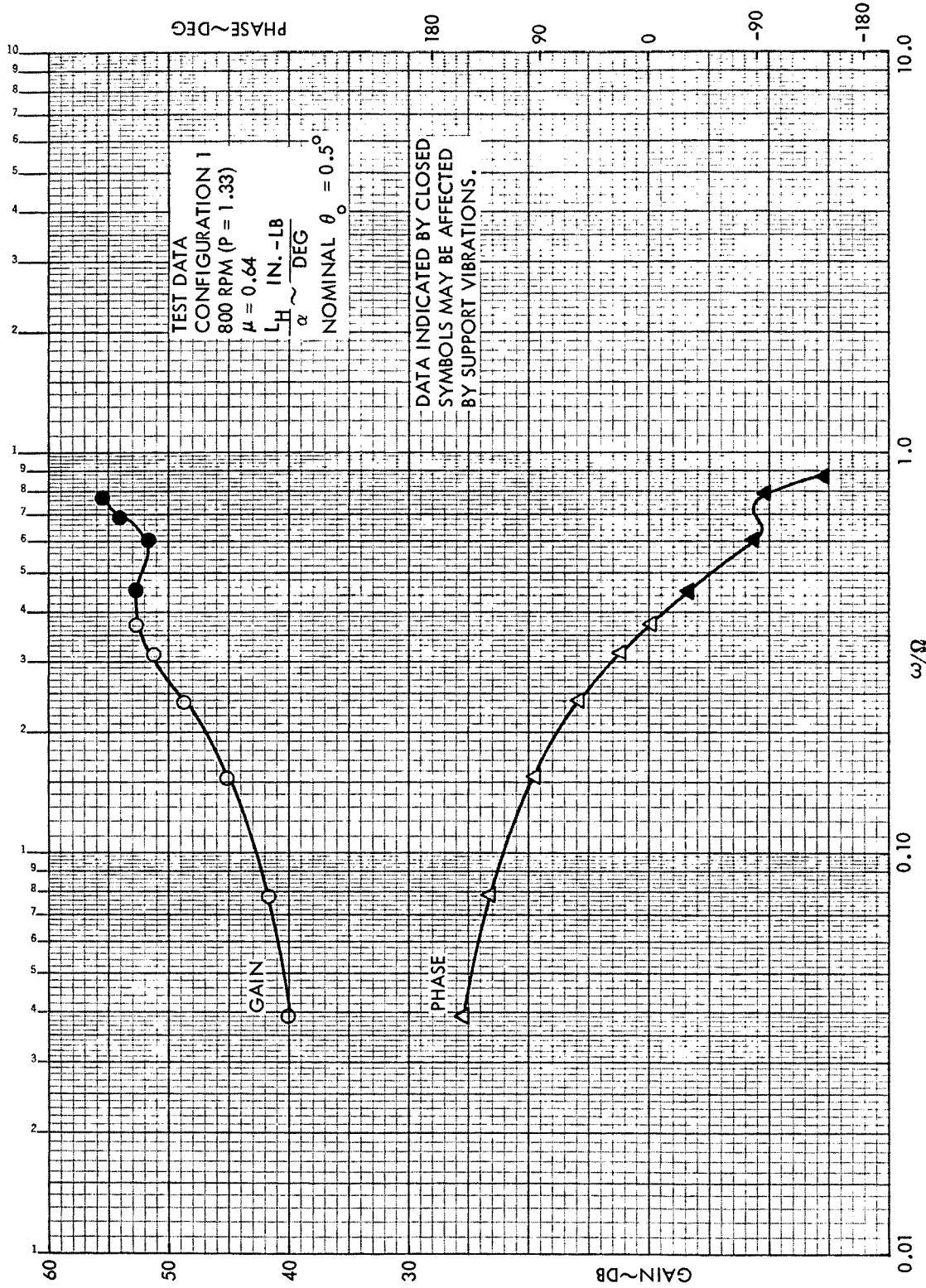


Figure C32. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.64$ , 800 RPM (P = 1.33)



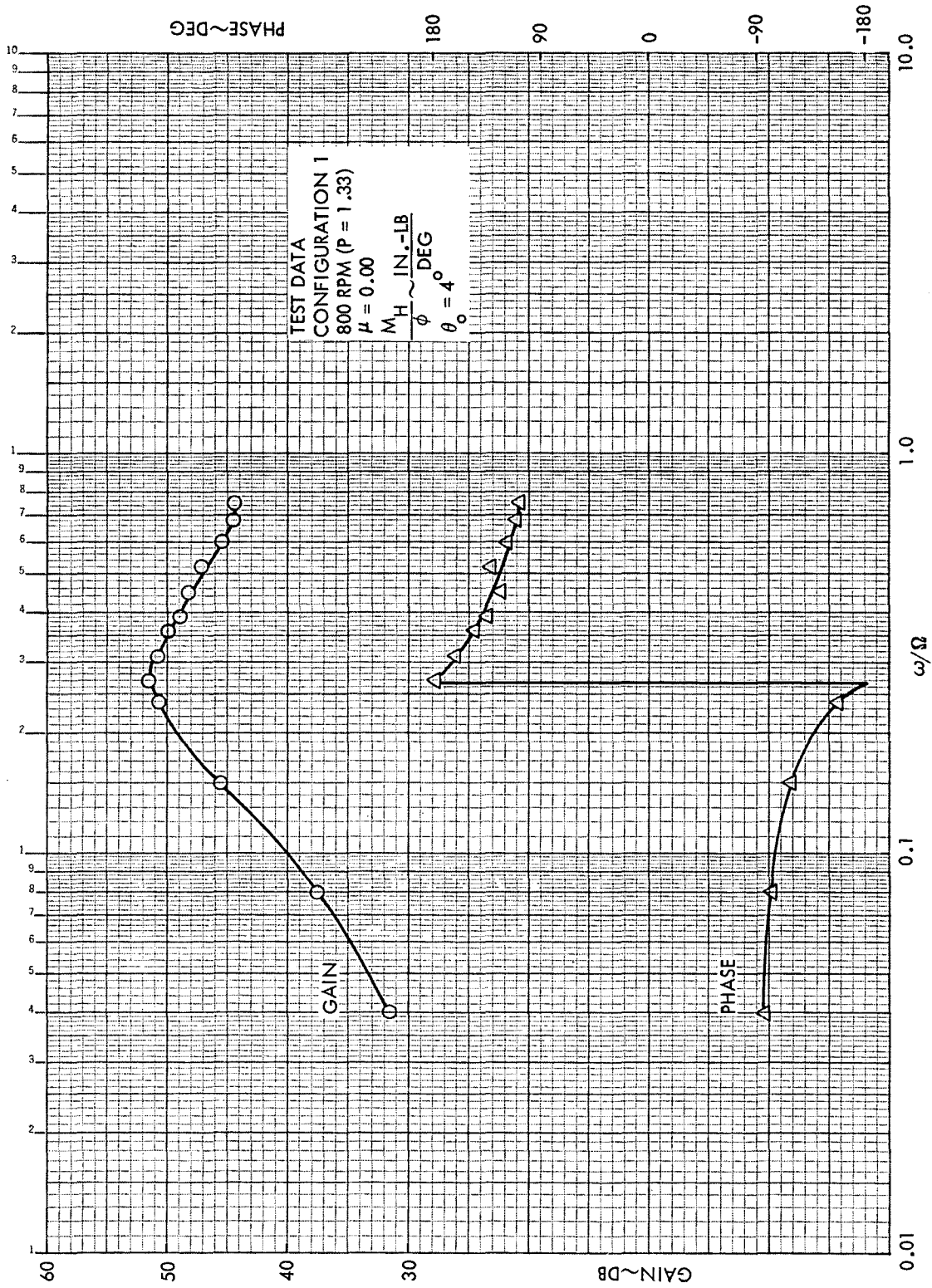


Figure C33. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.00$ , 800 RPM (P = 1.33)



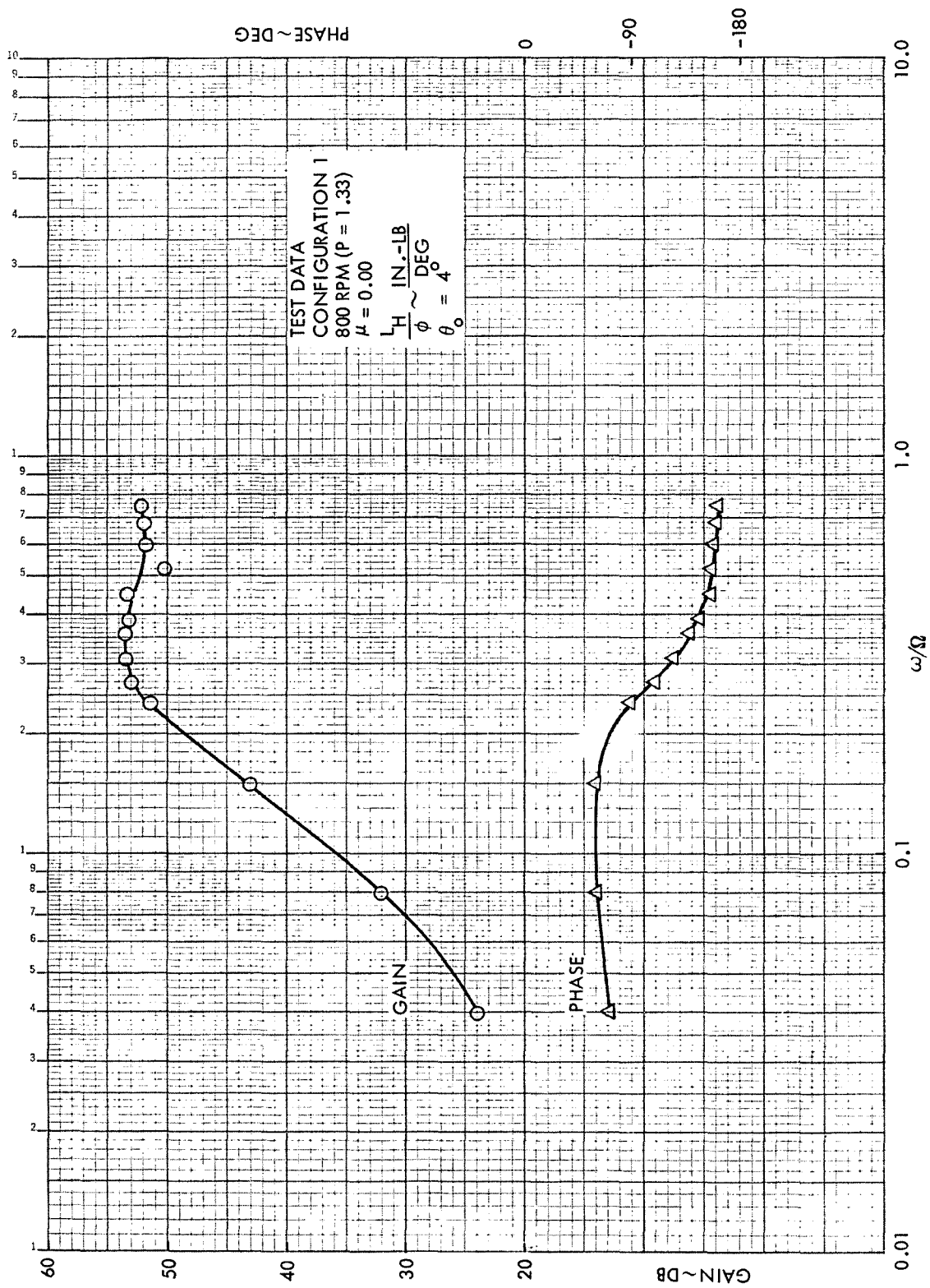


Figure C34. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.00$ , 800 RPM ( $P = 1.33$ )

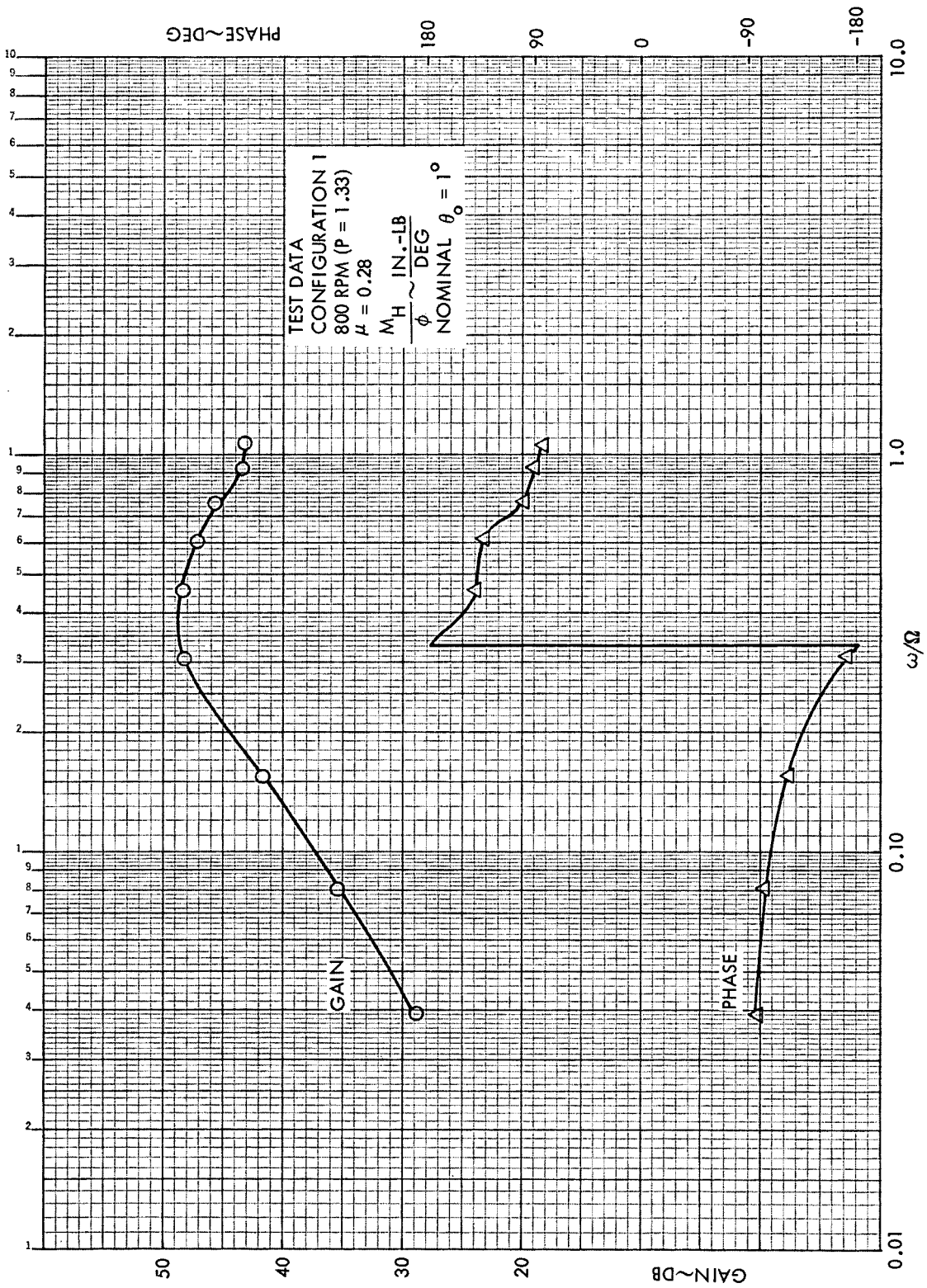


Figure C35. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.28$ , 800 RPM ( $\mu = 1.33$ )

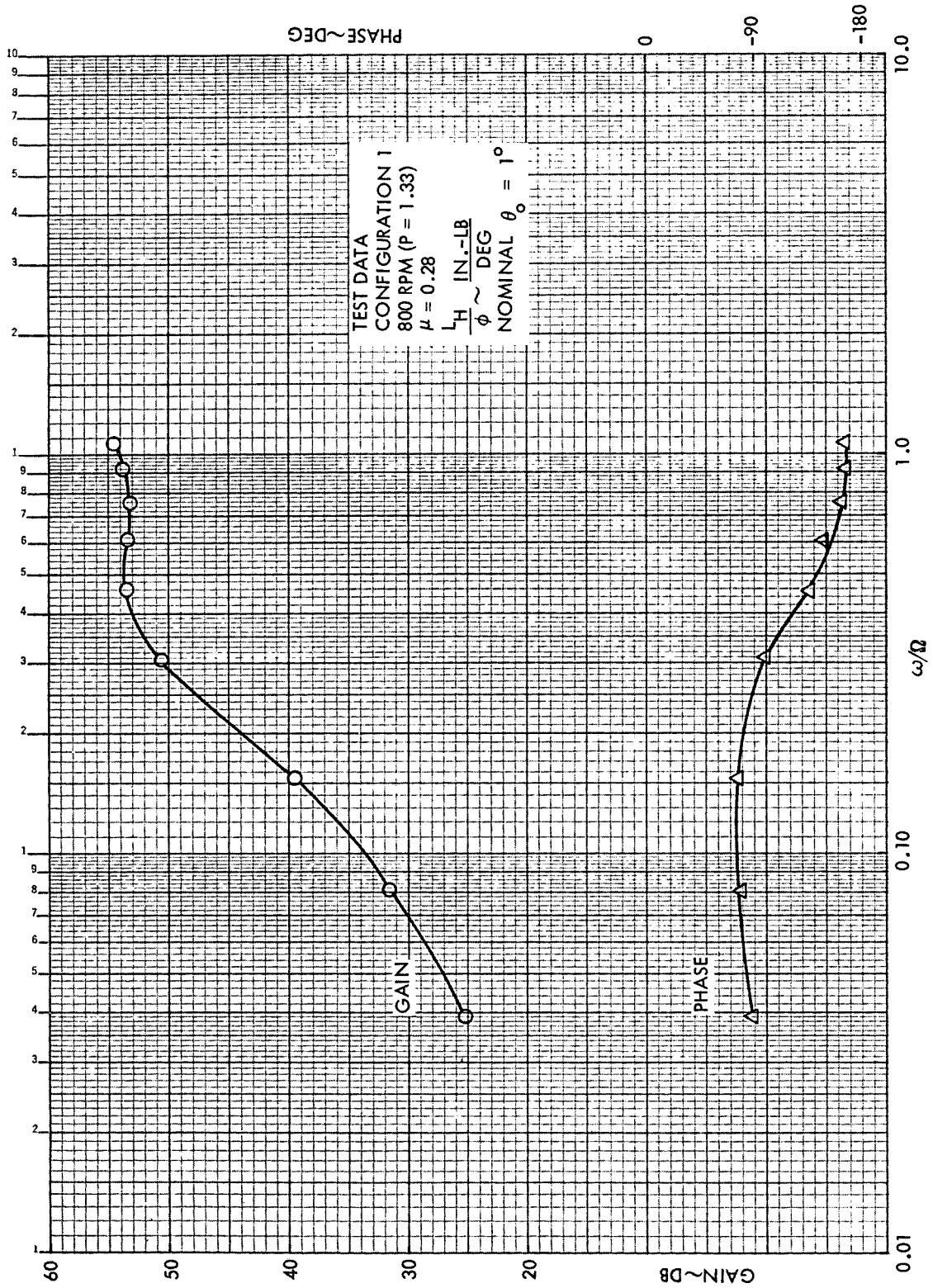


Figure C36. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.28$ , 800 RPM ( $P = 1.33$ )

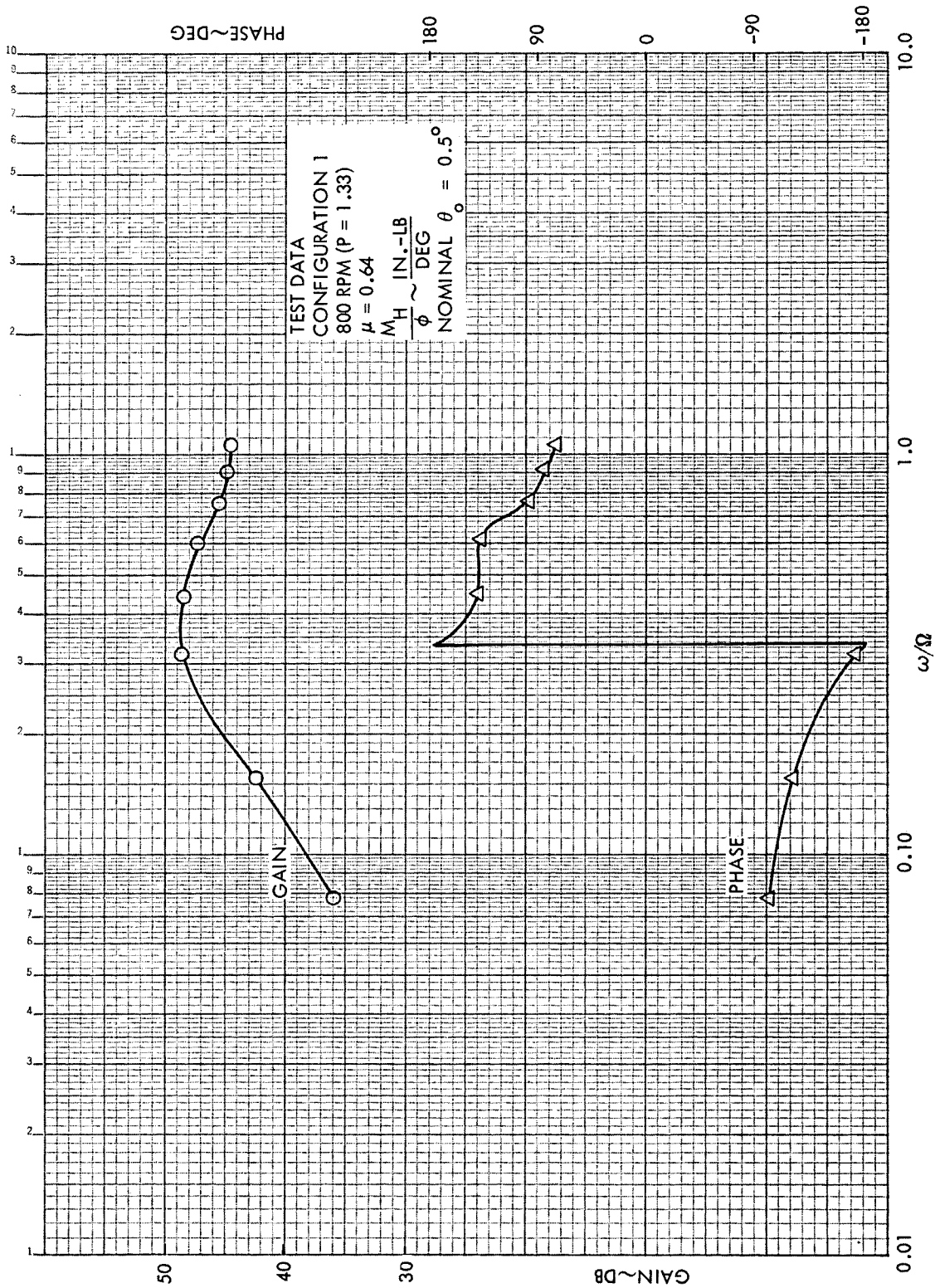


Figure C37. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.64$ , 800 RPM ( $P = 1.33$ )

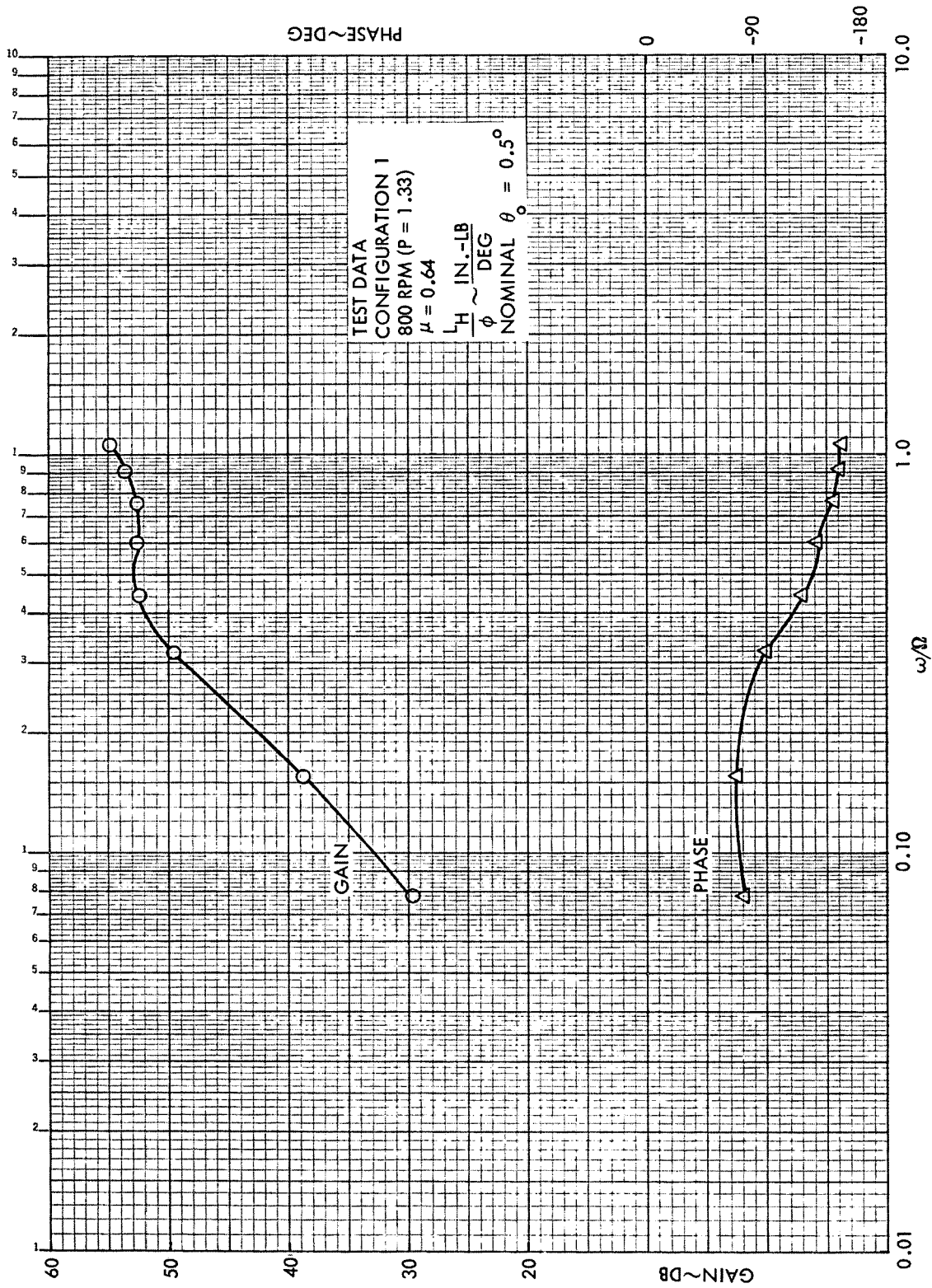


Figure C38. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.64$ , 800 RPM ( $P = 1.33$ )



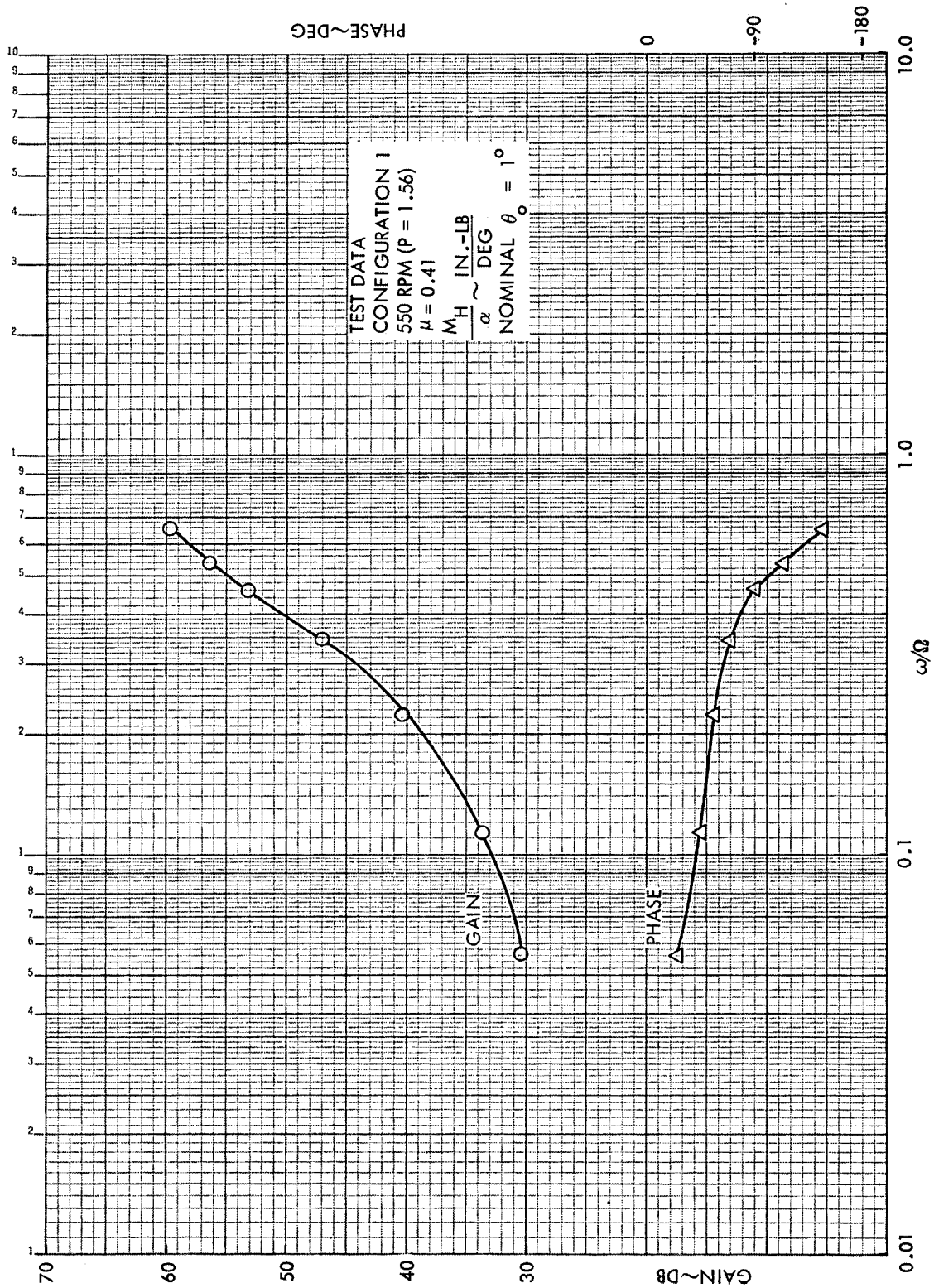


Figure C39. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.41$ , 550 RPM ( $P = 1.56$ )

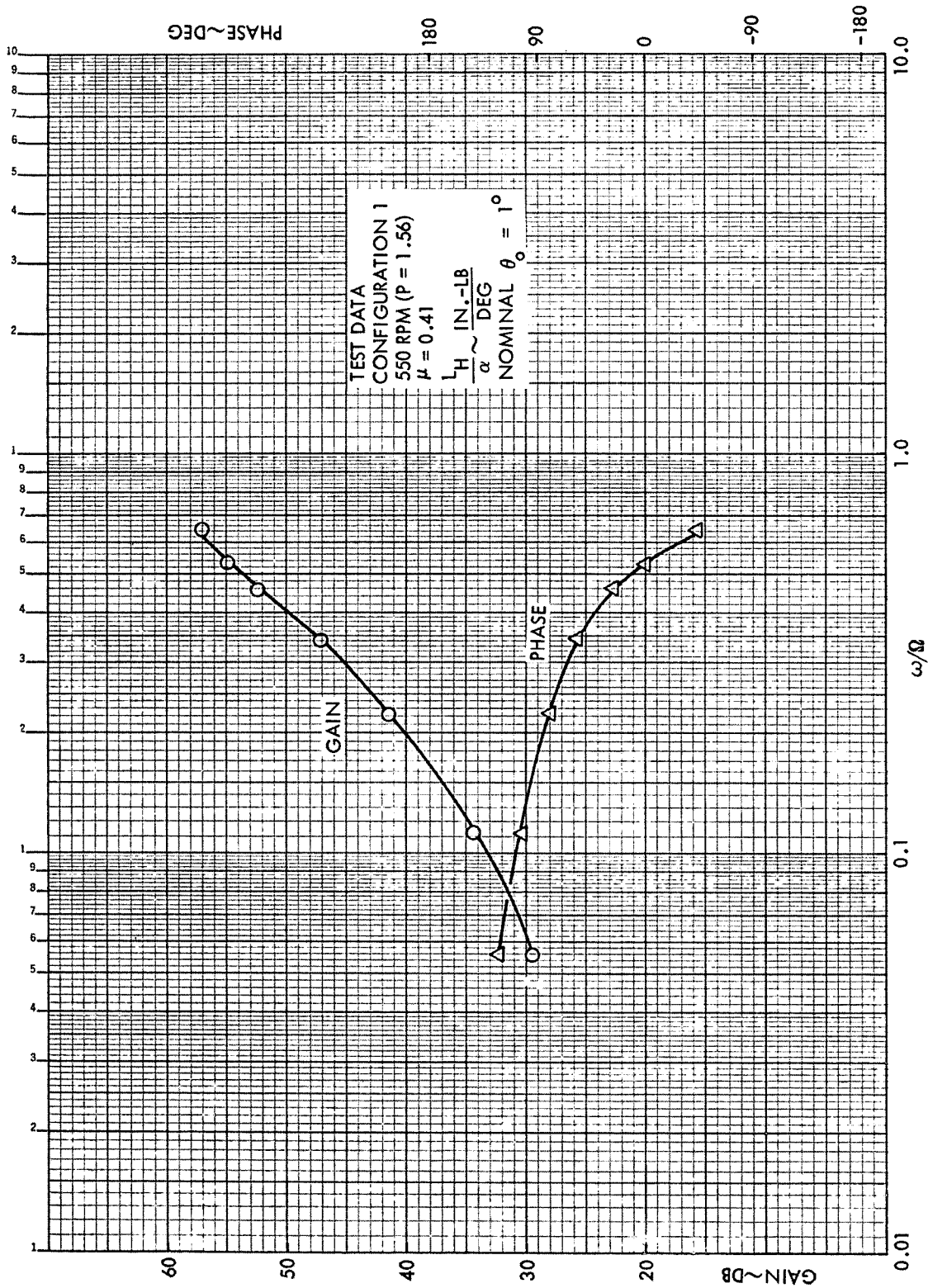


Figure C40. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.41$ , 550 RPM (P = 1.56)



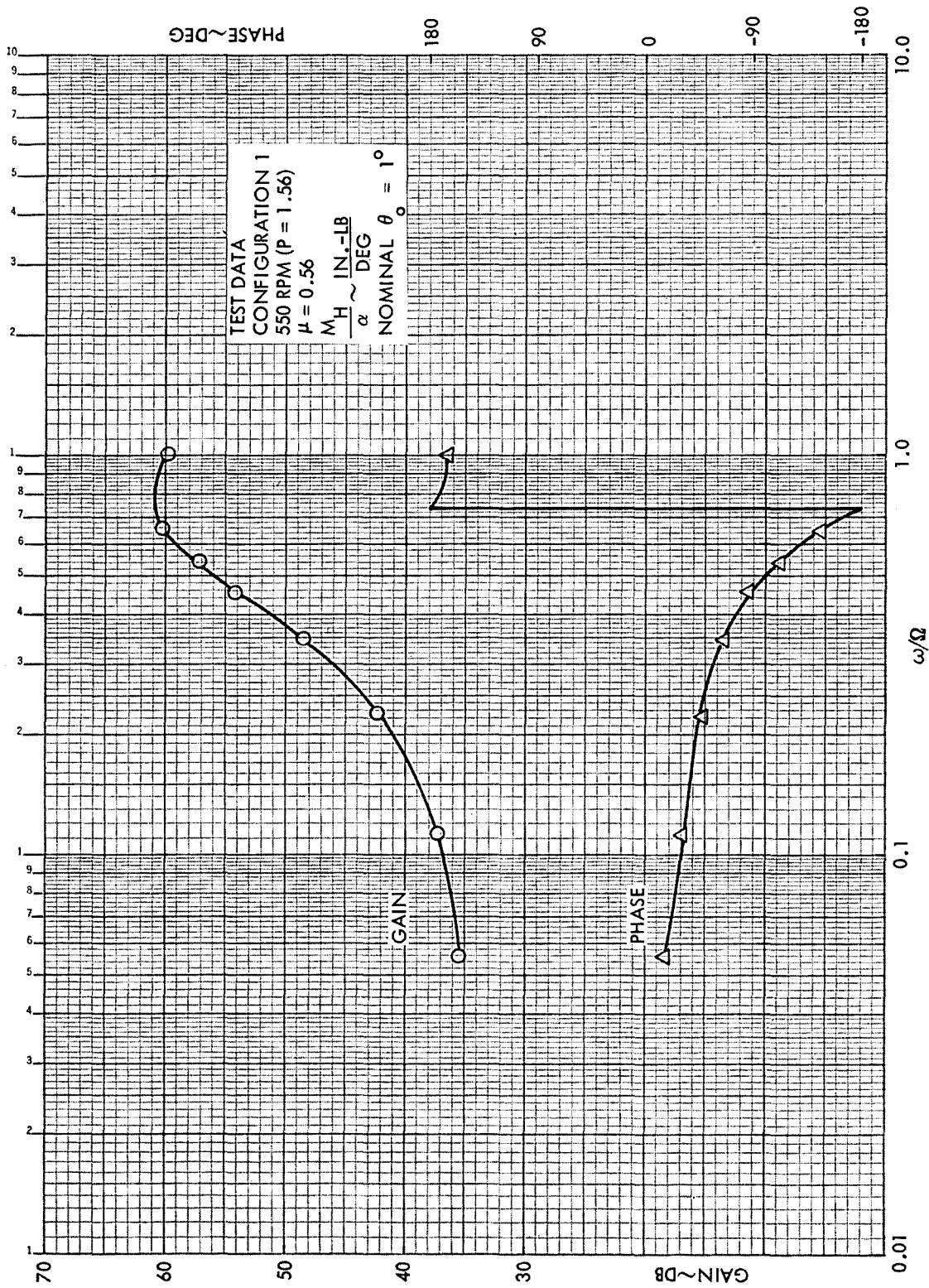


Figure C41. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.56$ , 550 RPM (P = 1.56)

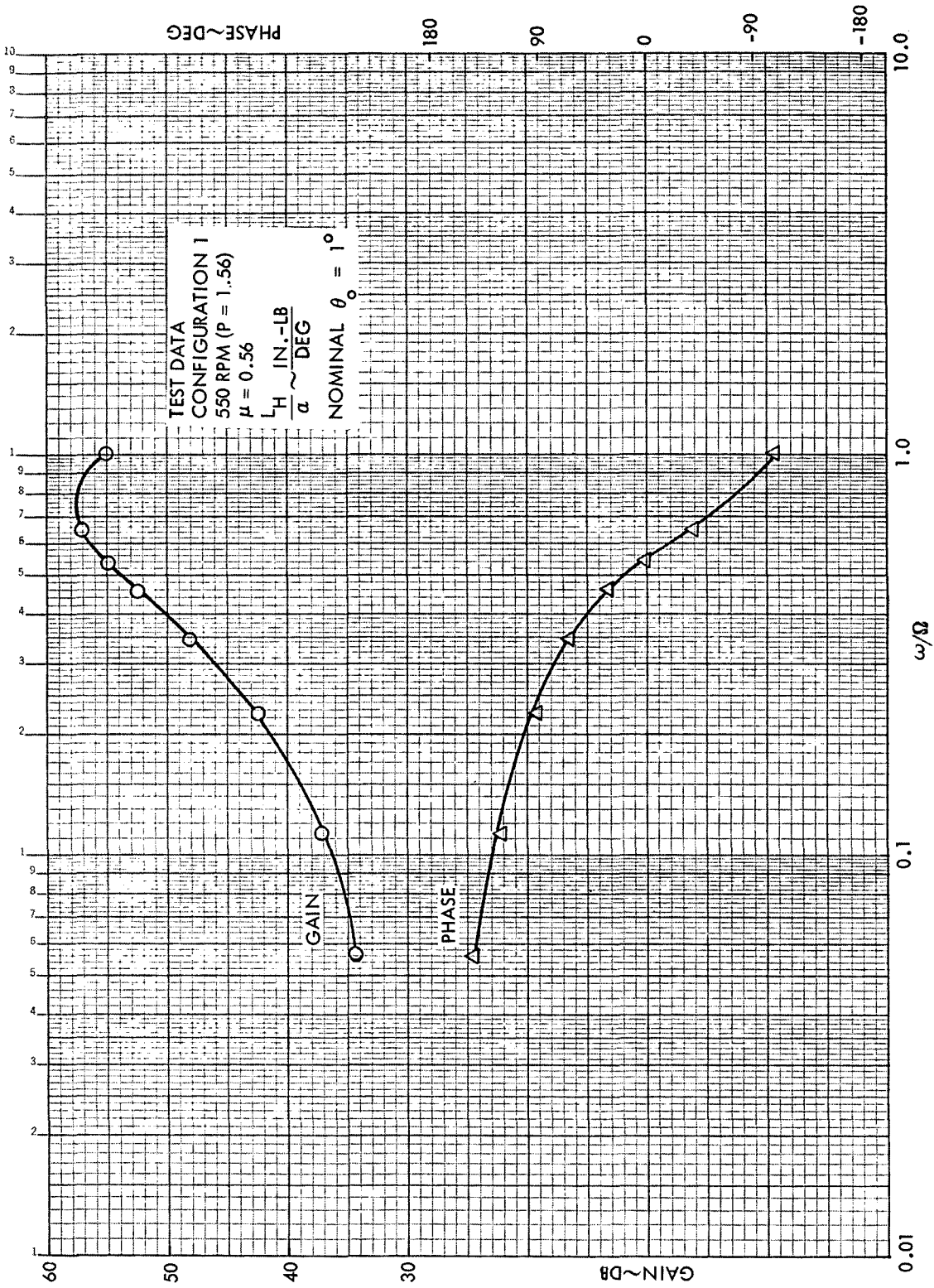


Figure C42. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.56$ , 550 RPM ( $P = 1.56$ )

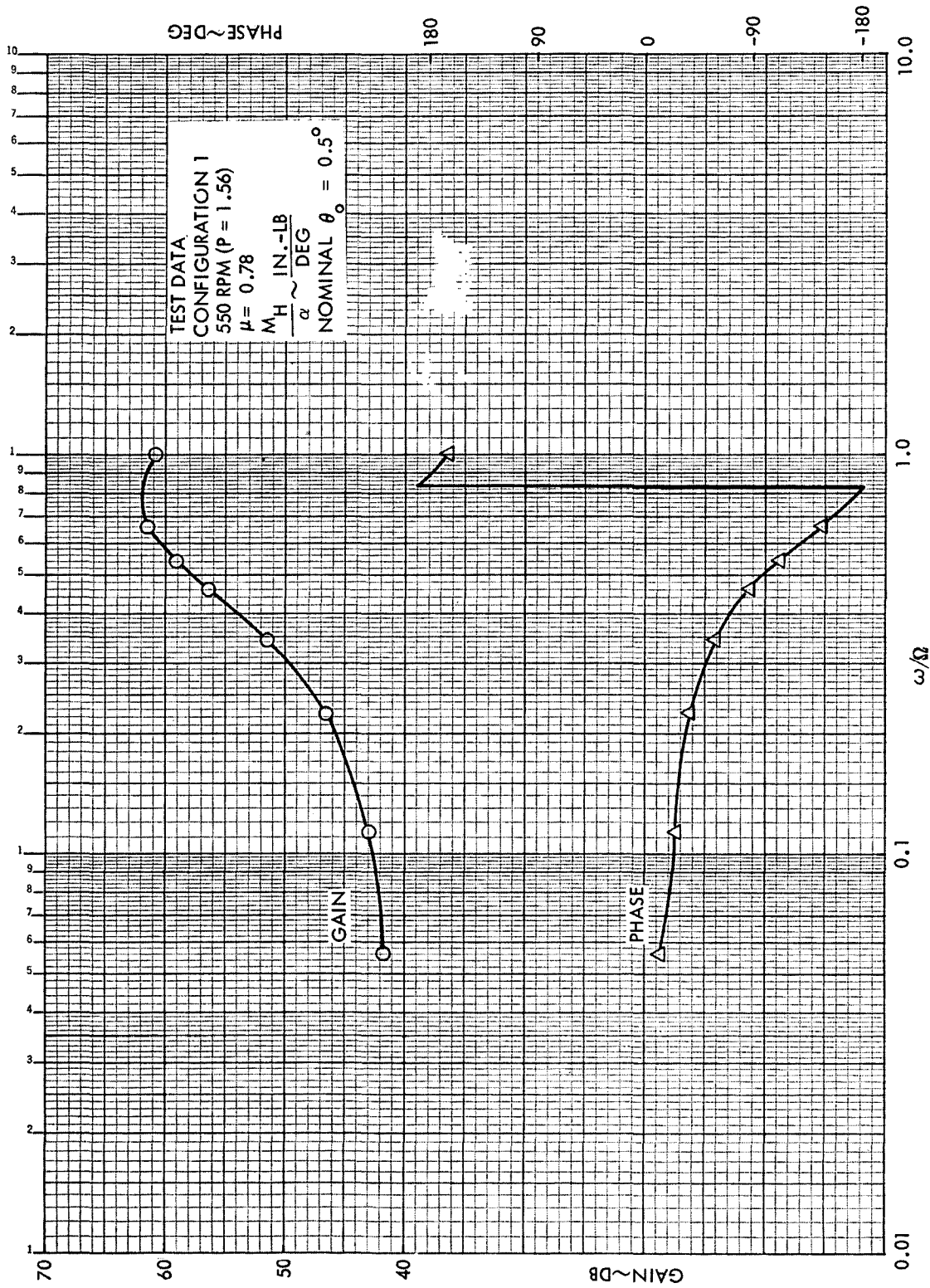


Figure C43. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.78$ , 550 RPM (P = 1.56)

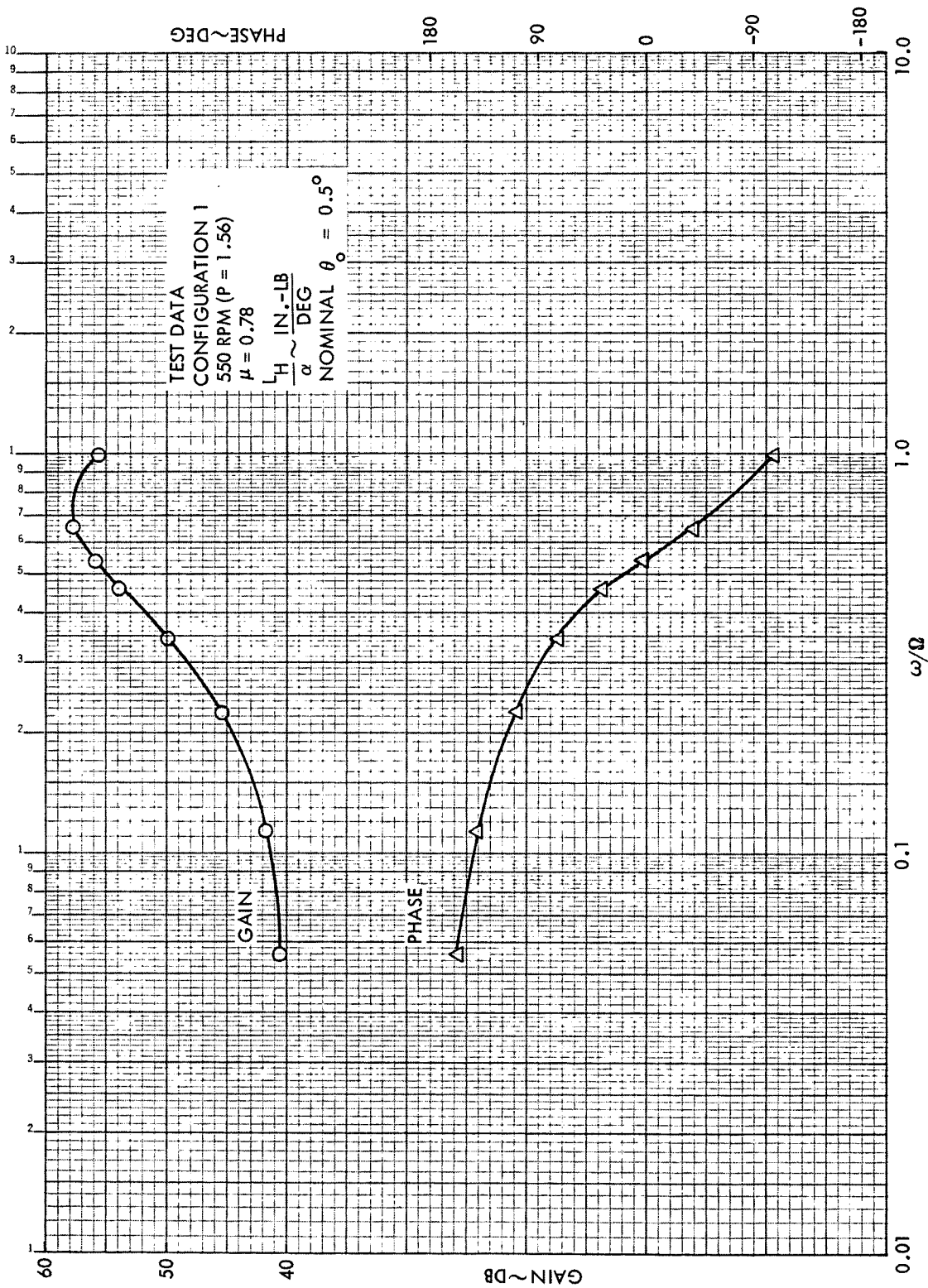


Figure C44. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.78$ , 550 RPM (P = 1.56)

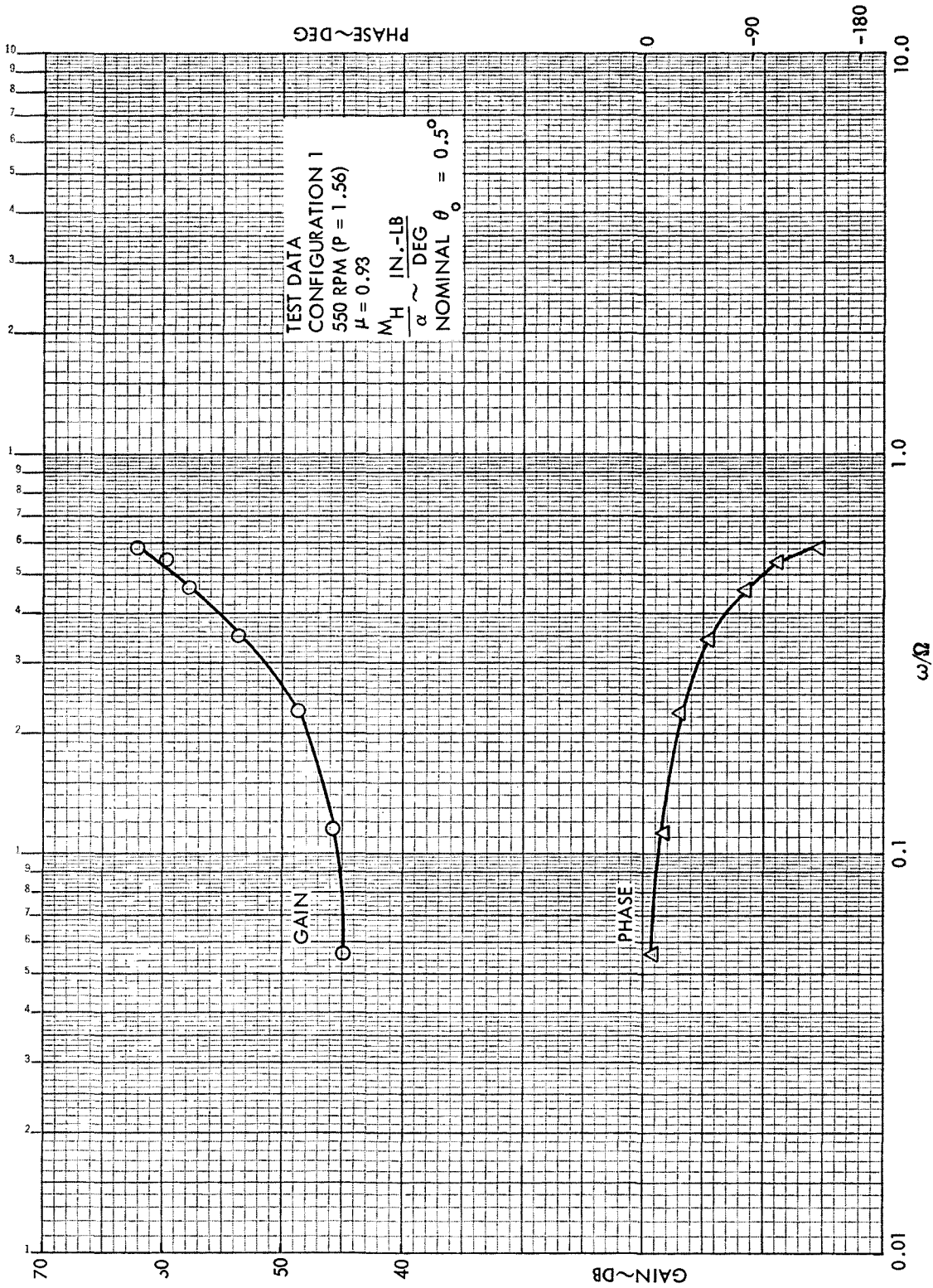


Figure C45. Rotor Hub Pitch Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.93$ , 550 RPM (P = 1.56)

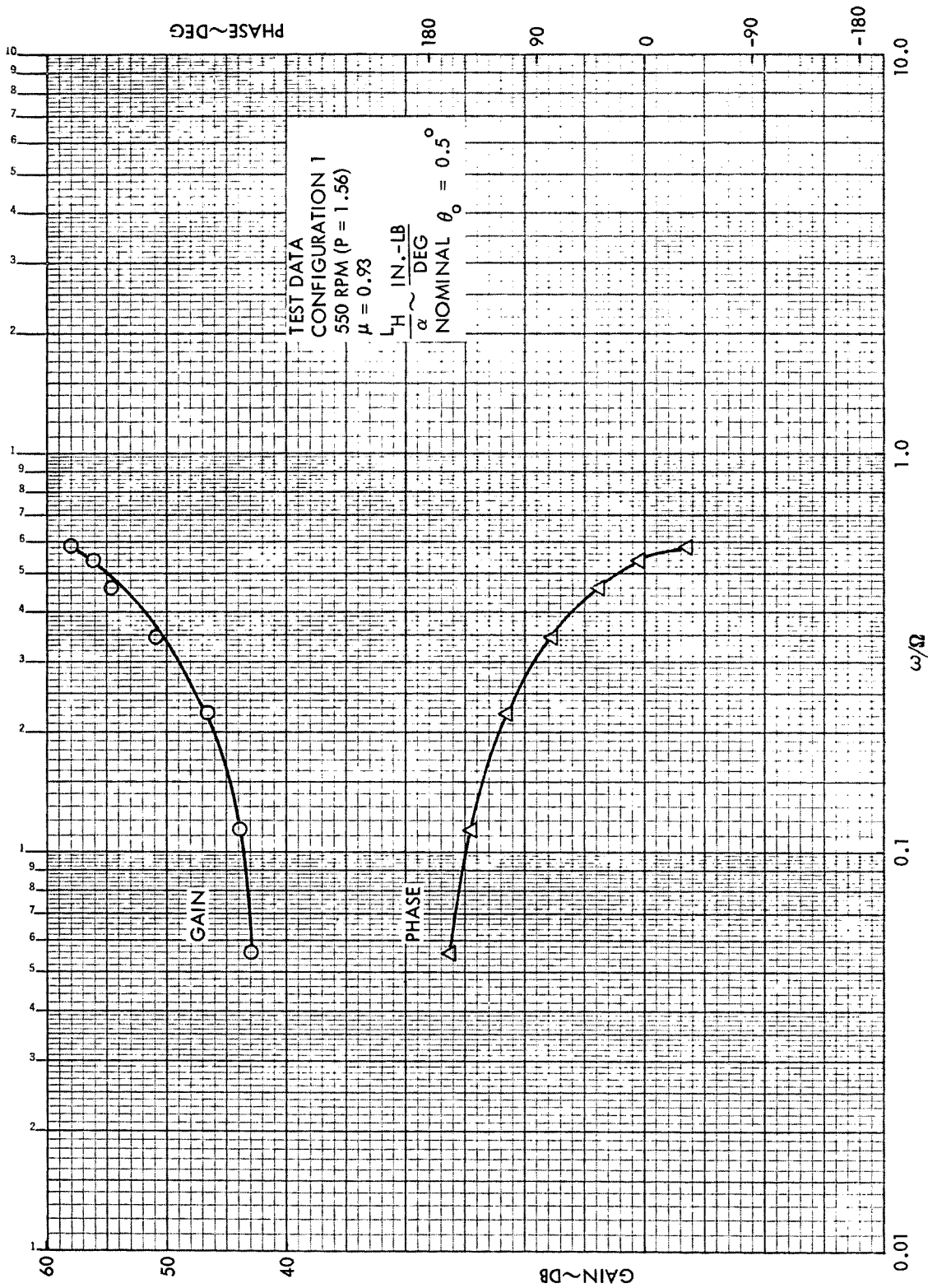


Figure C46. Rotor Hub Roll Moment Frequency Response to Shaft Pitch, Configuration 1,  $\mu = 0.93$ , 550 RPM ( $P = 1.56$ )



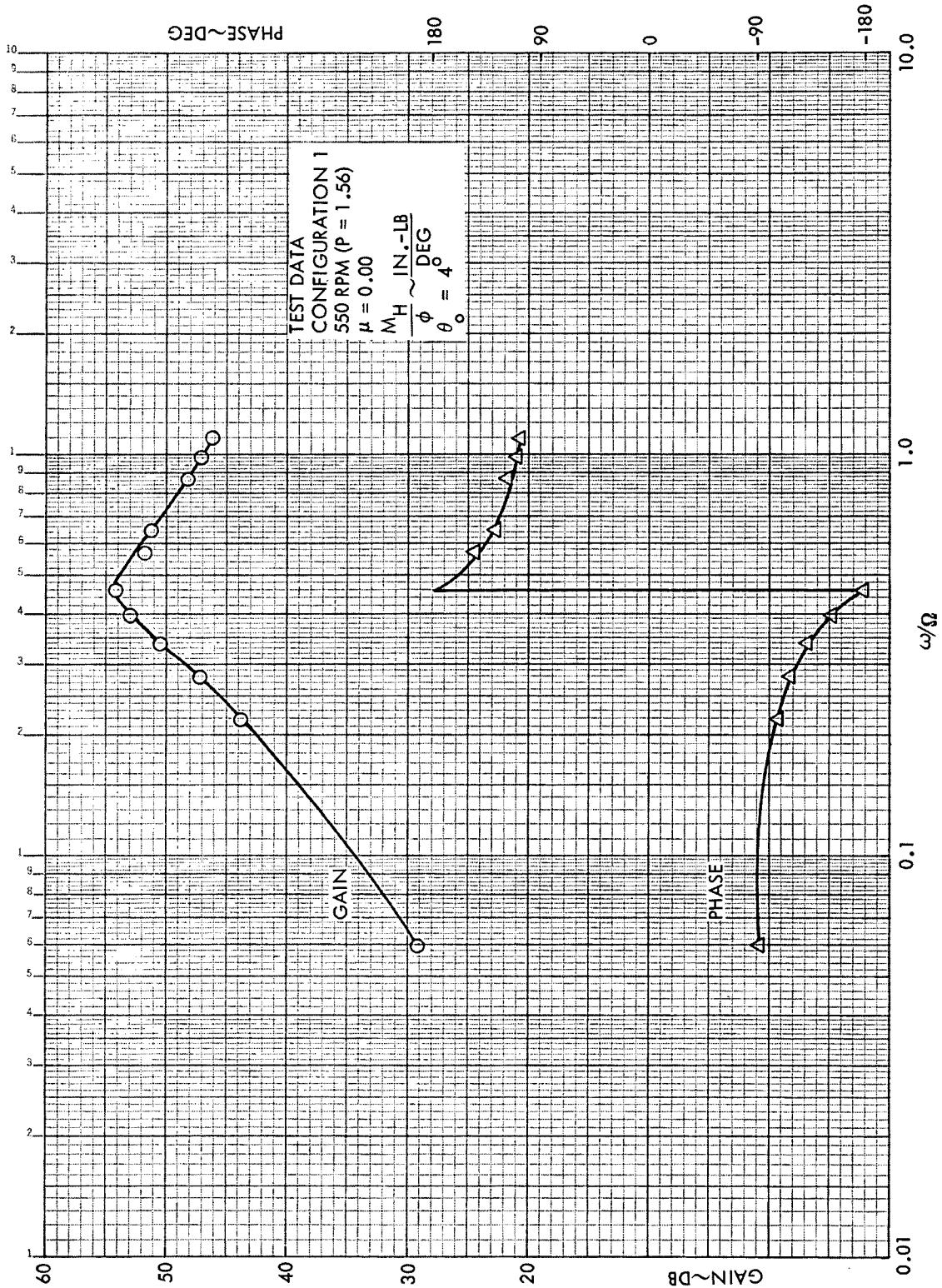


Figure C47. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.0$ , 550 RPM ( $P = 1.56$ )

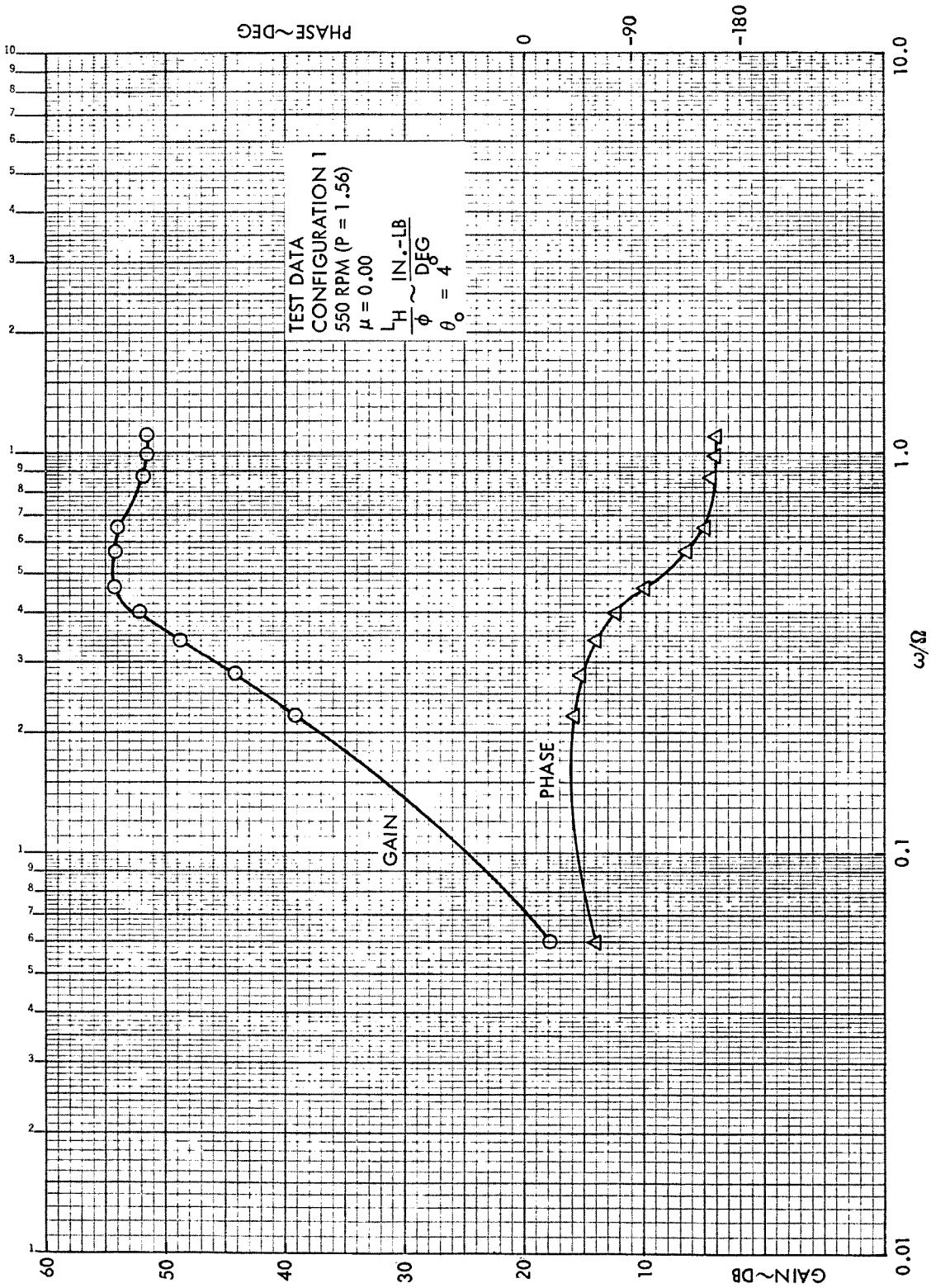


Figure C48. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.0$ , 550 RPM (P = 1.56)



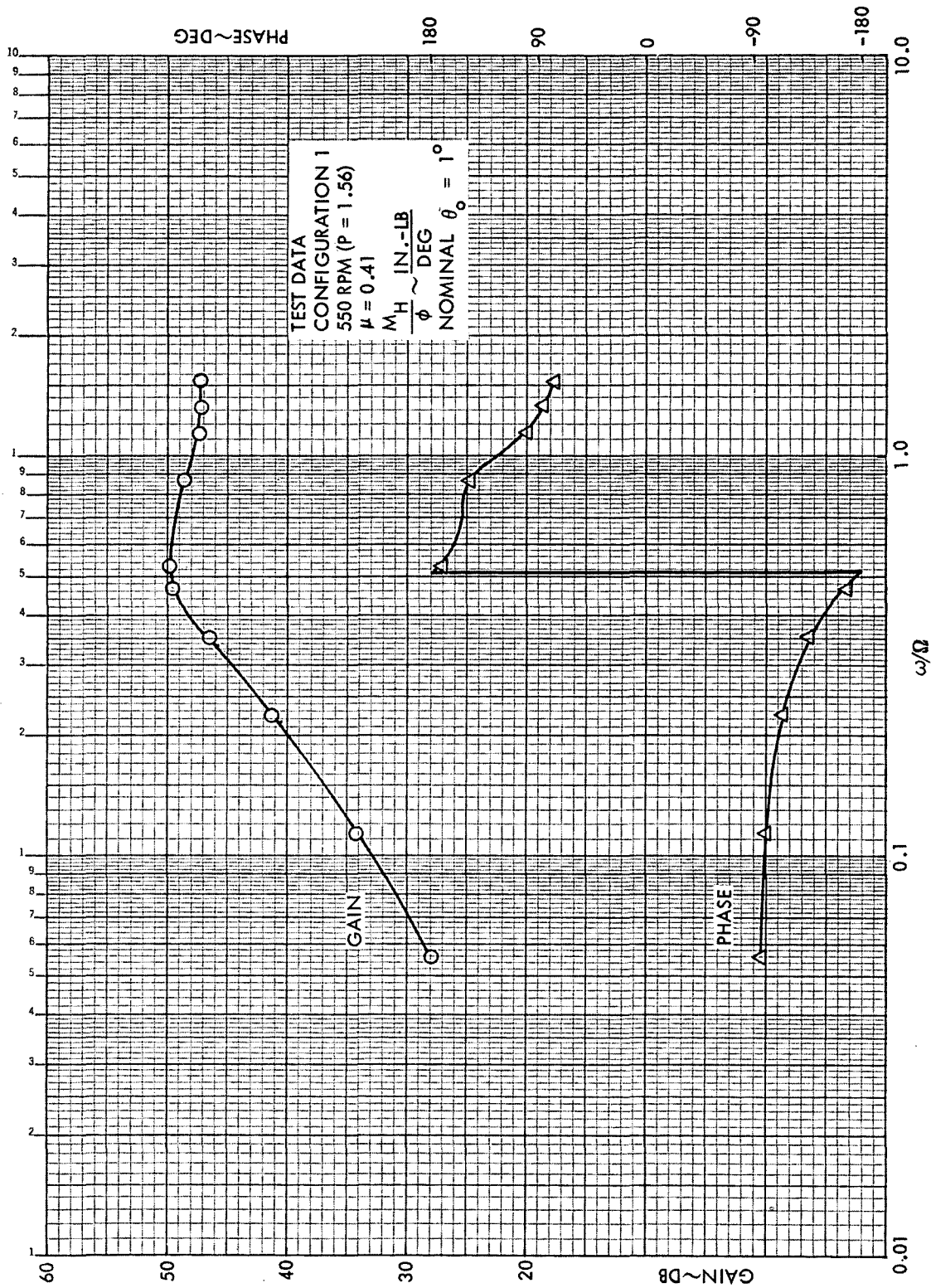


Figure C49. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.41$ , 550 RPM ( $\mu = 1.56$ )

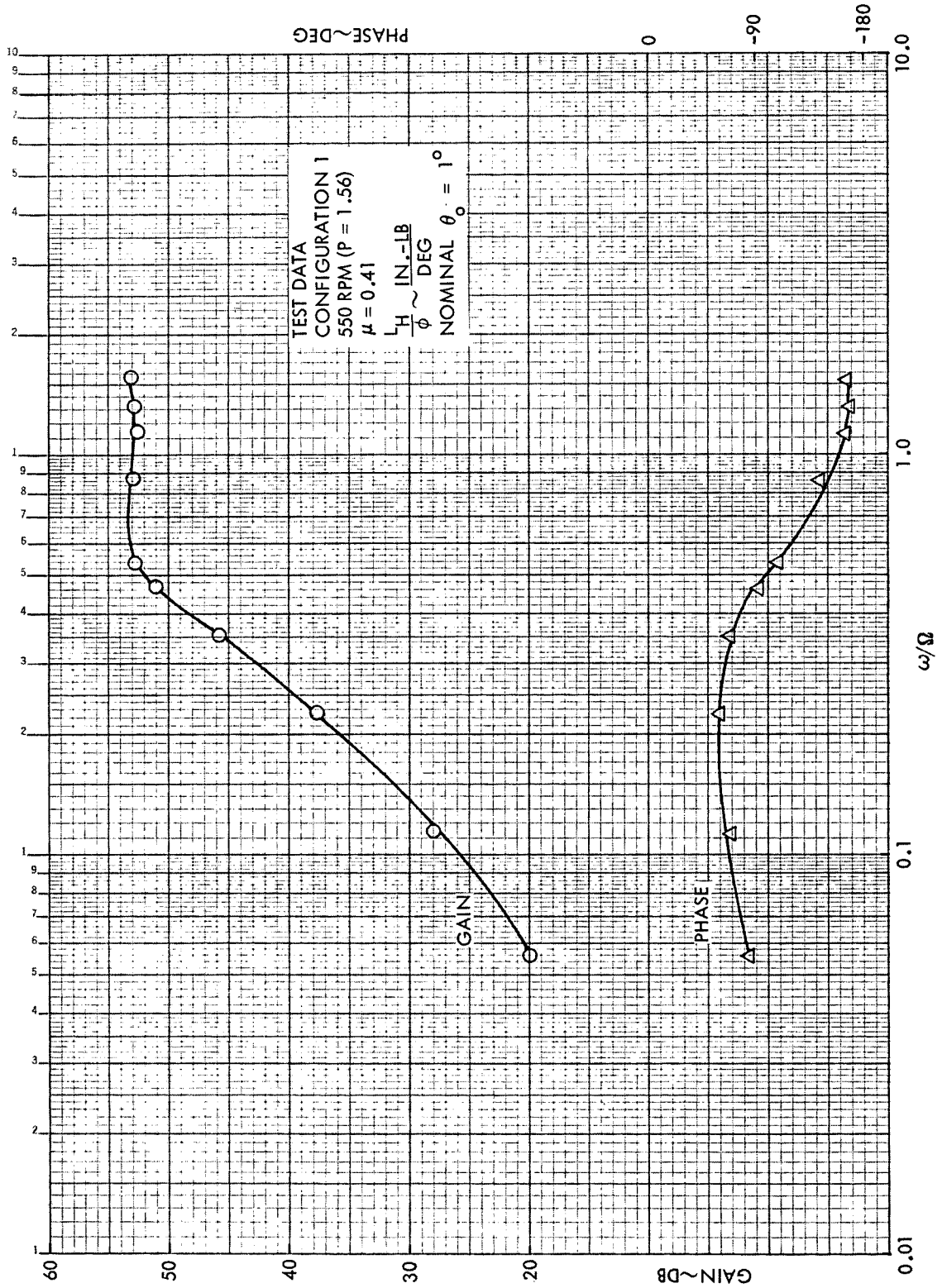


Figure C50. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.41$ , 550 RPM (P = 1.56)

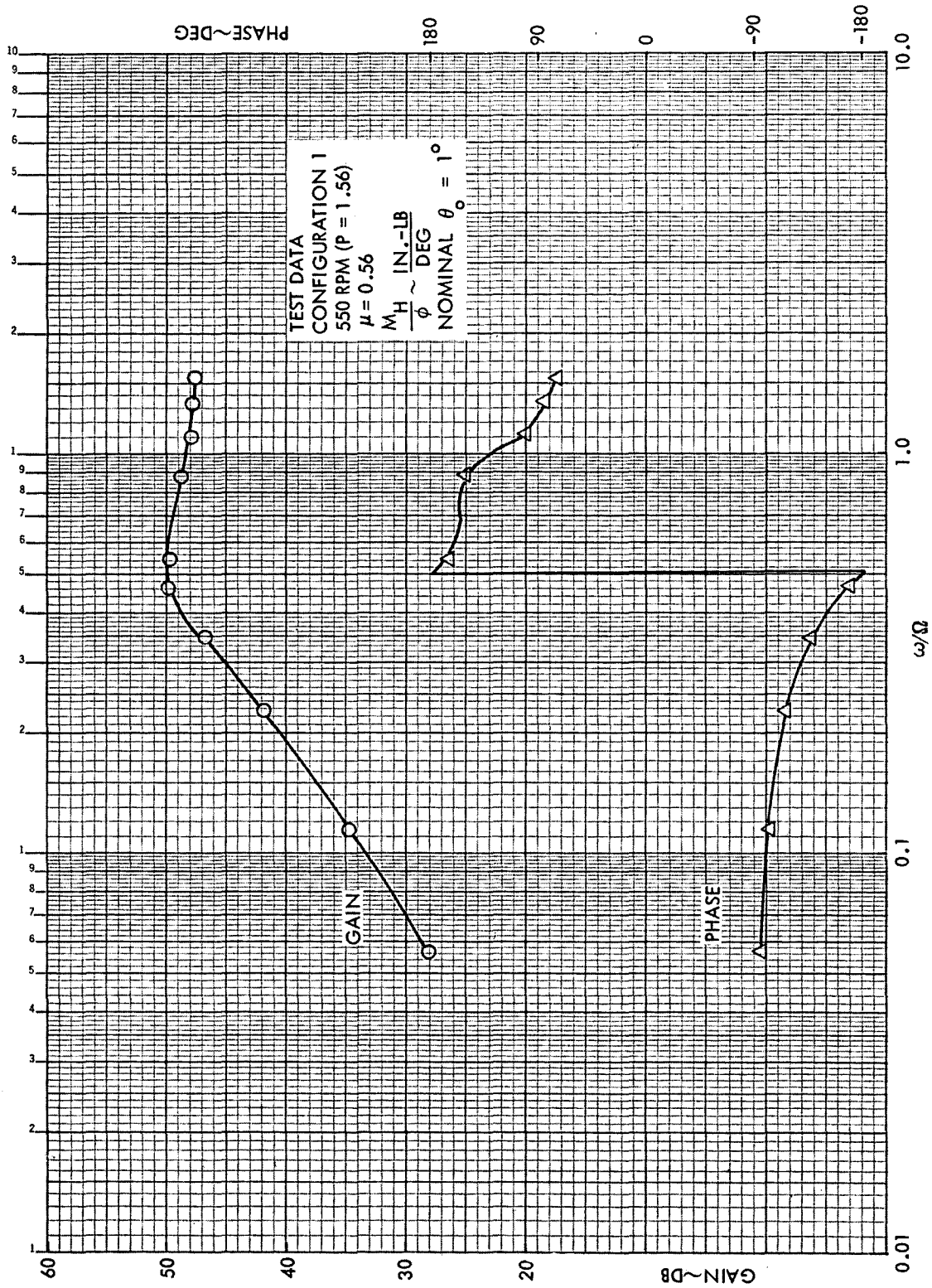


Figure C51. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.56$ , 550 RPM (P = 1.56)

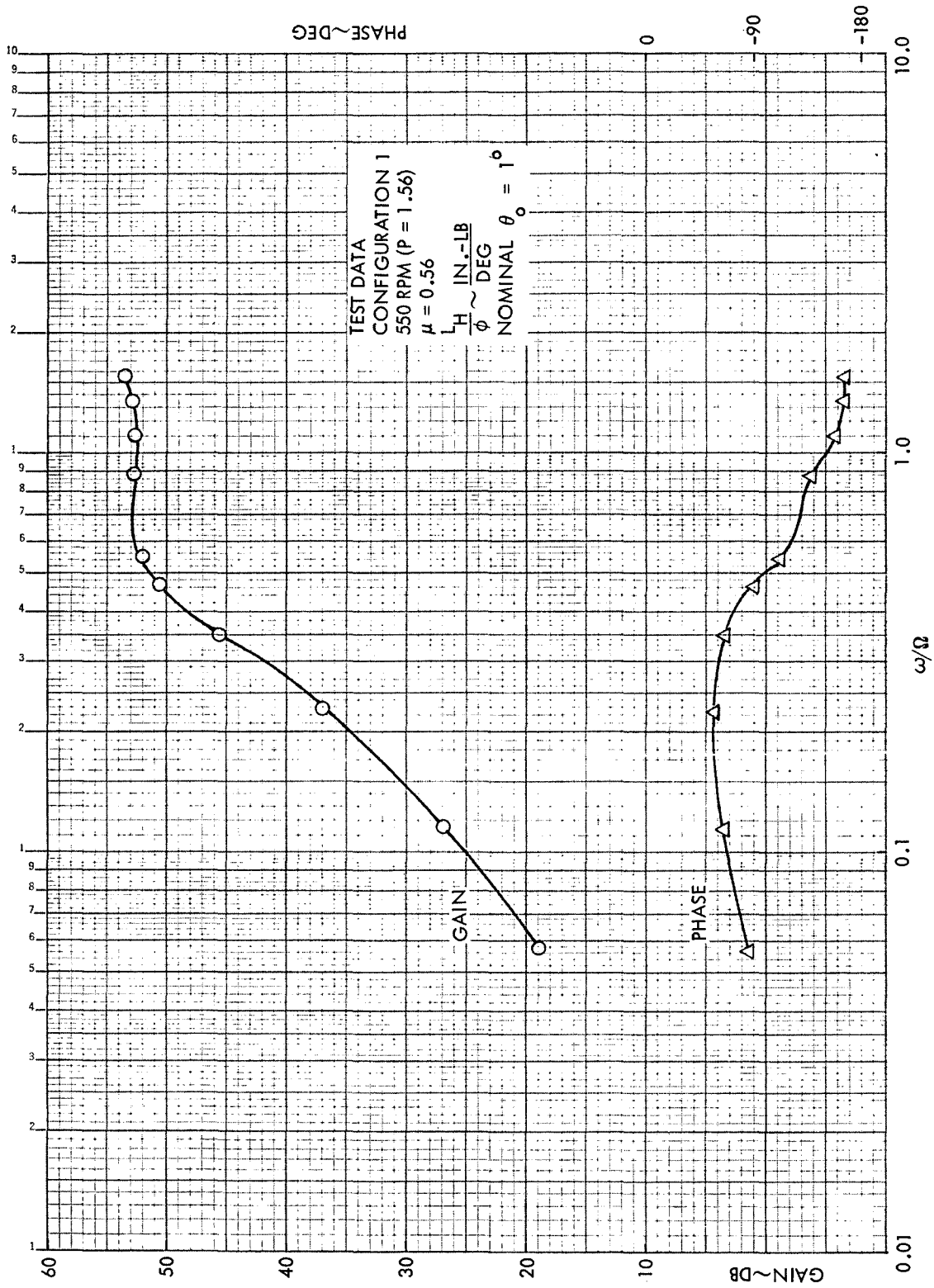


Figure C52. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.56$ , 550 RPM ( $\mu = 1.56$ )

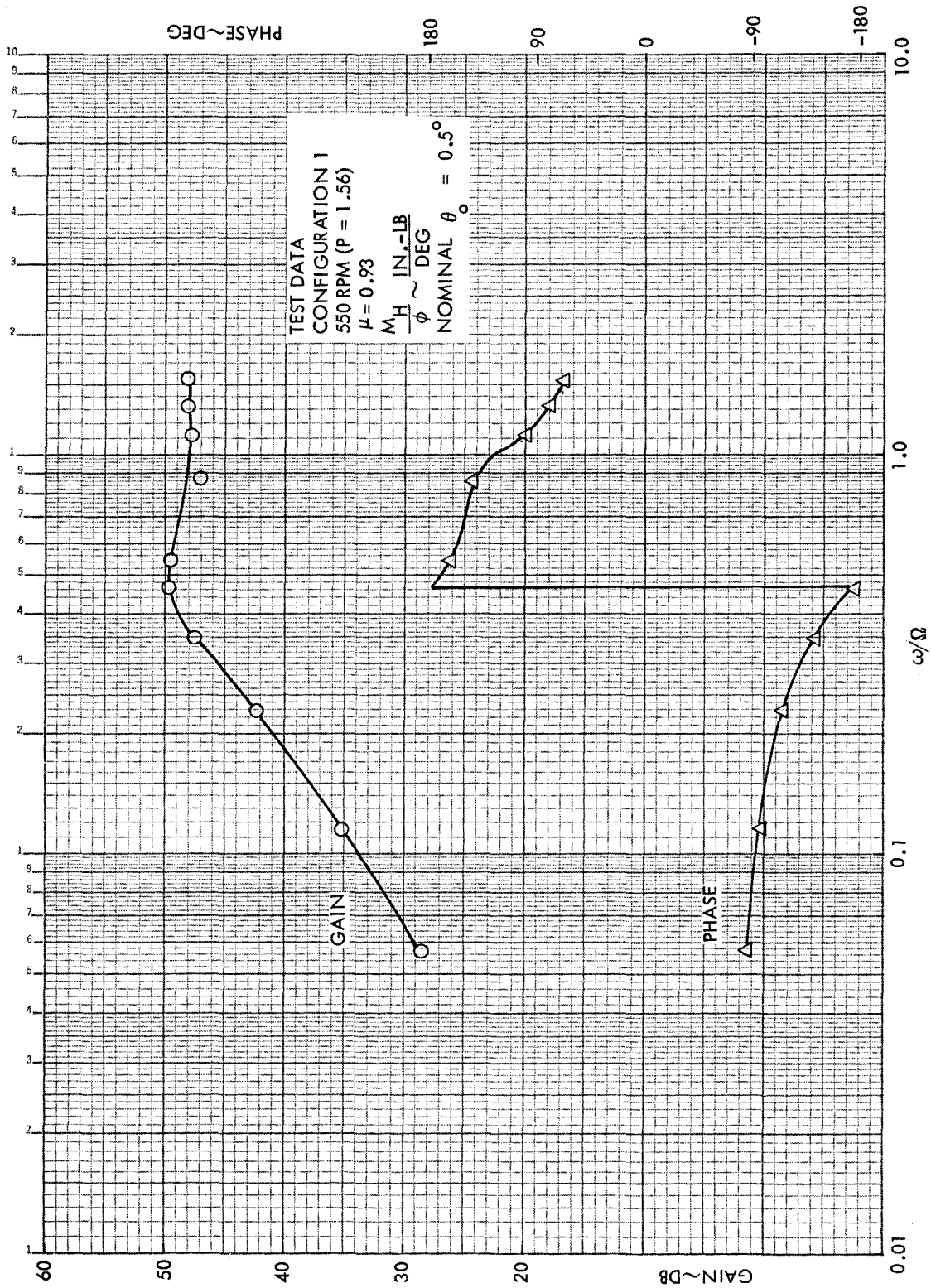


Figure C53. Rotor Hub Pitch Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.93$ , 550 RPM (P = 1.56)

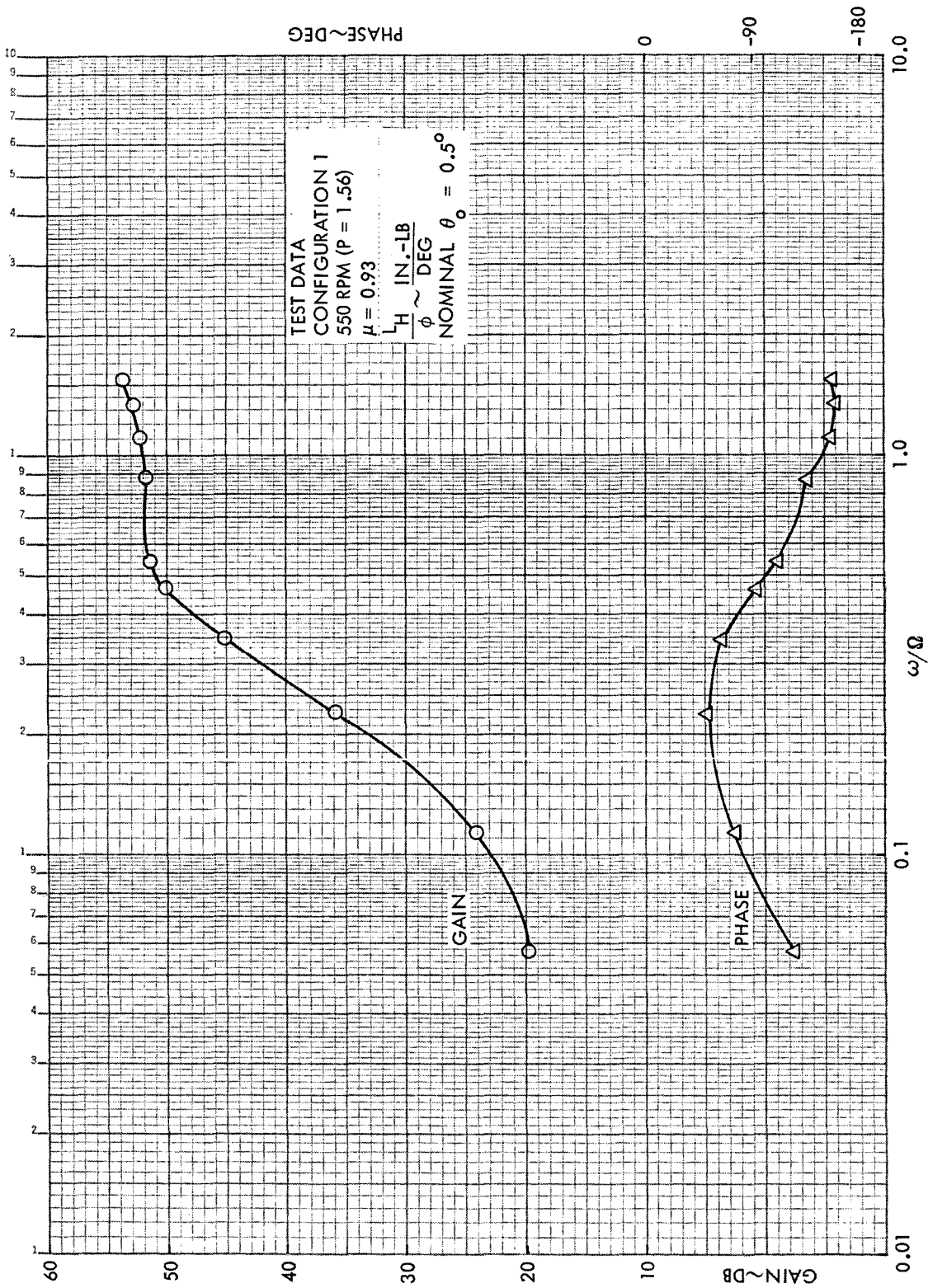


Figure C54. Rotor Hub Roll Moment Frequency Response to Shaft Roll, Configuration 1,  $\mu = 0.93$ , 550 RPM (P = 1.56)