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Lattice-based spatio-temporal ensemble prediction

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Abstract
With the rapidly increasing deployment of sensor networks, large amounts of time series data are generated. One of the main challenges when dealing with such data is performing accurate predictions in order to address a broad class of application problems, ranging from mobile broadband network (MBN) optimization to preventive maintenance. To this end, time series prediction has been widely addressed by the statistics community. Nevertheless, such approaches fail in performing well when the data are more context-dependent than history-dependent. In this paper, we investigate how latent attributes can be built upon the time series in order to define a spatio-temporal context for predictions. Moreover, such attributes are often hierarchical, leading to multiple potential contexts at different levels of granularity for performing a given prediction. In support of this scenario, we propose the Lattice-Based Spatio-Temporal Ensemble Prediction (LBSTEP) approach, which allows modeling the problem as a multidimensional spatio-temporal prediction. Given an ensemble prediction model, we propose a solution for determining the most appropriate spatio-temporal context that maximizes the global prediction metrics of a set of the time series. LBSTEP is evaluated with a real-world MBN dataset, which exemplifies the intended general application domain of time series data with a strong spatio-temporal component. The experimental results shows that the proposed contextual and multi-granular view of the prediction problem is effective, in terms of both several optimization metrics and the model calculation.

Keywords: Time series; prediction; spatio-temporal; ensemble; context; lattice; hierarchy; latent attributes

1. Introduction
Time series are one of the most prominent types of data nowadays. The massive increase of sensor network deployments, e.g., in smart cities, means that a tremendous number of time series are generated. To fully benefit from this potentially highly valuable data, one of the main challenges when dealing with the time series is performing an accurate estimation of the future values. Indeed, predicting time series allows addressing a broad class of application problems ranging from mobile broadband network (MBN) optimization to preventive maintenance.

The statistics community has addressed the time series prediction problem, a.k.a. forecasting, for decades. Multiple prediction strategies have been developed, ranging from well-known state of the art techniques, e.g., AutoRegressive...
Integrated Moving Average (ARIMA), which can deal with a broad range of prediction problems, to specific models, e.g., EGRV \(^1\), designed for accurate energy demand forecasts. Nevertheless, such approaches fail in performing well when data are more dependent on context than history, especially when the context is spatio-temporal. For instance, let us consider hourly aggregated traffic in an MBN. In this scenario, the context is the most important for performing accurate predictions. For instance, considering the type of the day, e.g., weekday or week-end, the hour of the day, as well as the node location might significantly impact the traffic load prediction, i.e., traffic will very likely be low in a shopping area during the night. The role of latent attributes, i.e., attributes that are built upon a given dataset, is most often decisive in the success of data mining or machine learning techniques\(^2\). From now we will call a context of a time series value a set of latent attributes values that spatially, temporally, etc., characterize this value.

In a previous work\(^3\), we have proposed STEP (Spatio-Temporal Ensemble Prediction), that starts considering this contextual aspect for unidimensional time series predictions. Roughly speaking, given a set of time series, each was considered separately and models were built for each hour and network node set. The proposed models were based on an ensemble strategy and are further extended in this paper. Nevertheless, attributes in a multidimensional context are often hierarchical. For instance, timestamps can be aggregated to hours that can further aggregated to either morning, afternoon, or night. Thus, considering that all attributes belonging to the context can be hierarchical, the main challenge is to determine which combination of levels is the best for achieving the most accurate prediction. Typically, STEP does not address this issue and forces the user to determine a priori this combination of levels of granularity.

In this paper, we go one step further by proposing LBSTEP (Lattice-Based Spatio-Temporal Ensemble Prediction), a multidimensional and multi-granular model for contextual attributes and investigate how to select the most appropriate models to perform the prediction. LBSTEP extends the STEP approach by (1) shifting from a single pre-defined context defined for unidimensional time series to varying contexts defined for unidimensional time series, (2) proposing new ensemble strategies for combining the separate predictions, (3) providing heuristics for selecting the optimal model, and (4) providing new quality measures to accordingly select the most appropriate contexts. LBSTEP is targeted at time series with a strong spatio-temporal component. It has been validated on a real MBN dataset and the results show the effectiveness of LBSTEP, both quantitatively and qualitatively.

Section 2 presents a running example that is used throughout the rest of the paper. Section 3 introduces the definitions while Section 4 presents the models for the multidimensional contexts. Our LBSTEP approach is developed in Section 5 and validated in Section 6. Finally, related work is discussed in Section 7 and some conclusions and perspectives are drawn in Section 8.

2. Running example

A Mobile Broadband Network (MBN) is composed of nodes (cells), each providing coverage for a limited area. Constant MBN development requires additional node deployment which creates overlapping areas and allows network optimization\(^4\). MBN traffic varies a lot, reaching the maximum network load levels only for a limited time. MBN operators monitor many network parameters, e.g., the number of active users, traffic served by the node, etc. Collected MBN data can be used for network optimization, i.e., some network nodes can potentially be turned off during low load periods. Due to operational costs, it is infeasible to optimize MBNs based on only the current traffic level. Instead, MBN load prediction must be considered to achieve good network optimization\(^5\). Figure 1a provides hourly traffic measurements in MBs for a single node for 6 consecutive days. During the hours when the node carries less than 30 MB, the node can potentially be turned off. In Figure 1b, 24 consecutive Saturday traffic measurements of the selected node are provided. The dashed line shows traffic load changes. The straight line at 30MB splits traffic into two node load levels, i.e., unfilled triangles present when the traffic load is high and the node should remain turned on, and filled green triangles indicate low traffic periods when the node potentially could be turned off. We notice that MBN energy potentially could be saved between 2AM and 9AM on Saturday. Considering this observation, some questions naturally arise: (1) “Is this behavior observable for this network node only?”, (2) “Is the behavior observable every Saturday, on weekdays, or week-end days?”, and more generally (3) “Can a spatio-temporal context be extracted such that records belonging to this context will share the same behavior and benefit from a single prediction model?”. This paper provides a way to efficiently answer such questions.
3. Data definitions

A time series collection $T$ is defined as a set of time series $T = \{TS_1, \ldots, TS_n\}$ such that each $TS_i$ is an ordered M-sequence $TS_i = (E_{i1}, \ldots, E_{im})$ where $E_{ij}$ is the most recent event. An event $E_{ij}$ is a pair $E_{ij} = (T_j, val_j)$ meaning that the time series $TS_i$ had a value of $val_j$ at time $T_j$. For simplicity of exposition, we assume that the time series are regularly sampled (as is typical for time series) and have no missing values or noise. These assumptions typically hold for critical systems, like MBNs, being continuously monitored. In case they do not hold, cleansing techniques have to be applied; however, such cleansing techniques are orthogonal to the approach presented in this paper, and thus beyond the scope of the paper. On top of this time series definition, latent attributes, $A_1, \ldots, A_k$, can be derived from time series to depict a more sophisticated view of the raw data. To do so, we define a uniform structure for the input as $Data = [T, A_1, A_2, \ldots, A_k, V]$ which extends the pair definition of the time series event. A tuple $d = [t, a_1, a_2, \ldots, a_k, v]$ in the $Data$ has three main parts, i.e., the temporal dimension $T$, attributes $A_1, A_2, \ldots, A_k$, and the monitored value $V$ in the system. Each attribute $A_i$ is assumed to be equipped with a hierarchy, denoted by $H_i = H^1_i, \ldots, ALL_i$. The number of levels in the hierarchy $H_i$ is given by $SizeA_i$. To identify which attribute values are aggregated when forming different hierarchy levels, we use the function $Desc$. The results of the $Desc(H^\text{destination}_j, a^\text{source}_j)$ are attribute values at hierarchy level $H^\text{destination}_j$ that form attribute $a^\text{source}_j$ value. $T$ represents the absolute discrete times of the start of the monitored periods. The temporal attribute $T$ allows ordering tuples, e.g., $d'$ has occurred before $d''$ if $t' < t''$. Additional operations such as filtering continuous records or time series construction can be performed based on $T$. Attributes $A_1, \ldots, A_k$ represent the set of $k$ latent and contextual attributes that will be used during the prediction. We assume that at least one attribute represents spatial details. A combination of the time attribute $t$ and domain specific attributes $a_1, \ldots, a_k$ uniquely identifies the value $v$. As described previously, $T$ is the absolute discrete time. The temporal dimension $T$ can be viewed as linear or cyclic. Cyclic time represents reoccurring time cycles of the temporal element, e.g., seven days in the week, etc. We assume functions $p_1(t), \ldots, p_j(t)$ that can project cycles and be new attributes $A_1$, e.g., attribute $A_2 = p_1(t)$ is the projection of seven days and attribute $A_3 = p_2(t)$ is the projection of 24 hours of the day.

**Example 1.** Consider Figure 2 and the spatial network attribute Location. The Location attribute has three hierarchy levels, i.e., $SizeA_{\text{Location}}=3$, that are Node, Site, and ALL. Referring to Figure 2, $Desc(\text{Location}^{node}, \text{site}_1) = \{\text{node}_10024, \text{node}_10025, \text{node}_10029\}$. In our running example, we consider three attributes, i.e., Location, Day, and ToD (short for Time of Day). We now define hierarchies for the remaining attributes Day and ToD. The Day hierarchy has three levels, i.e., Day, Day-type, and ALL, where Day level is the day of the week, Day-type splits days into weekdays or weekend days, and ALL aggregates all days. The ToD hierarchy has three levels Hour, Hour-type, and ALL, i.e., Hour is the hour of the day, Hour-type aggregates similar time hours, e.g., night, day, etc. hours, and ALL aggregates all hours.
Discretization. Data measurements come in different formats and depend on the inspected system, e.g., values might be represented as real numbers or text. Prediction of the precise absolute values is not always required and sometimes optimization instead relies on the predicted discrete class. The simple discretization technique presented in [2] was based on a defined threshold, thus only two classes Low and High could be used. In the current paper, we use a more general discretization function $Disc(v) = Class$, where $v$ is the value to be discretized and $Class$ is the discrete class. The $Disc$ function is not limited by the number of different classes.

Example 2. Let us consider MBN traffic data where $v$ denotes the traffic in MB carried over a single hour at a selected node, stored as real numbers. Our task requires predicting only a few possible network node states, e.g., Low, Median, and High, and does not require accurate prediction of traffic values. Predicted Low traffic nodes can potentially be turned off without a major loss in the Quality of Service (QoS) in the MBN.

We want to discretize traffic equal to $v=74$ MB carried at node node_10024 during the first Saturday hour, see Figure 1a. To discretize traffic values, we use a classification table defined as traffic ranges and names of the traffic classes (traffic load), e.g., $[0, 30, \text{Low}], [30, 500, \text{Median}], \text{and } [500, \infty, \text{High}]$. Using the discretization function we classify $v$ as $Disc(v) = Disc(74) = \text{Median}$.

4. Lattice-based contexts

Similarly to data cubes, combinations of levels of granularity form a lattice, e.g., see Figure 3. We now formally define this lattice and the concept of a context.

Lattice Construction. The following partial order allows us to consider a lattice representation. Let a lattice element, $e$, be defined as a combination of $k$ hierarchy levels, i.e., $e = (H^0_i, \ldots, H^k_i)$, where $H^0_i$ is a level in the hierarchy $H_i$. We define the partial order between two lattice elements $e = (H^0_i, \ldots, H^k_i)$ and $e' = (H^0_{i'}, \ldots, H^k_{i'})$ as:

$$e \preceq e' \iff \forall i = 1 \ldots k: H^0_i \lesssim H^0_{i'}.$$

Example 3. Let us consider the two lattice elements, $e = (\text{Node}, \text{Day}, \text{Hour})$ and $e' = (\text{Node}, \text{Day}, \text{Hour\_type})$. Both are at the lowest levels of the Location and the Day hierarchies. Since $\text{Hour} \preceq \text{Hour\_type}$, we have that $e \preceq e'$. The complete lattice for the Location, Day, and ToD hierarchies is provided in Figure 3. Lattice elements are uniquely identified by ID numbers for easier later referencing.

Context definition. Lattice elements represent the hierarchy levels at which attributes are processed. Each hierarchy level contains multiple attribute values. A context is defined as an instance of different attribute values from the hierarchy levels of a given lattice element. Considering a lattice element, $e = (H^0_i, \ldots, H^k_i)$, a combination of attribute values forms a context of $e$, denoted by context $= (a_1, \ldots, a_k)$, such that $\forall i = 1 \ldots k, a_i \in \text{Dom}(H^i)$. Tuple selection that matches a specific context $= (a_1, \ldots, a_k)$ is done by $\text{Data}\_\text{context} = \{(t, a_1, a_2, \ldots, a_k, v)|a_i \in \text{Desc}(H^i, a_i) \land \ldots \land a_k \in \text{Desc}(H^k, a_k)\}$.
Example 4. We illustrate how a context is constructed for the lattice element \( e = (\text{Site}, \text{Day}, \text{Hour}) \), the highlighted lattice element in Figure 3. The attribute values site_1, Monday, and 1 are selected from their respective hierarchies Site, Day, and Hour. For the selected attribute values we construct a context instance context = (site_1, Monday, 1). The tuples that form the context satisfy Data_{context} = \{ \text{loc} \mid \text{loc} \in \text{Desc}(H_{\text{Node}}^{\text{Location}}, \text{site}_1) \land \text{day} \in \text{Desc}(H_{\text{Day}}^{\text{Day}}, \text{Monday}) \land \text{tod} \in \text{Desc}(H_{\text{ToD}}^{\text{ToD}}, 1) \} and are shaded. For clarity, the attribute values that do not match the context are white-boxed in Figure 4.

5. Lattice-based spatio-temporal prediction

The STEP approach proposed in\(^3\) is based on model training and predictions of a single fixed and predefined context, i.e., context[node, hour]. In this paper we propose LBSTEP which is a more general prediction approach based on contexts defined for the lattice elements. We split Data at time \( t' \) into training data Data\_T where \( t < t' \) and evaluation data Data\_E where \( t \geq t' \). Before introducing the approach itself, we first start by presenting the evaluation metrics that will allow assessing the quality of the prediction.

**Prediction evaluation metrics** For model evaluation we use the standard qualitative metrics\(^5\), i.e., accuracy, recall, precision, and F-measure, which are calculated separately for each discrete class. The standard metrics do not show the real model performance for the purpose of MBN optimization, i.e., a high accuracy score does not guarantee high utility. Therefore, to estimate the possible energy savings in the MBN we define a utility score using \#TruePositive and \#FalsePositive. \#TruePositive shows the correct predictions when the specific network part (node, site) potentially can be turned off and \#FalsePositive represents the wrong predictions, i.e., the network part that will be turned off although it really should not have been. This will lead to an instant "re-turning-on" of the mistakenly turned off network part, which causes an additional (penalty) energy consumption for turning back on. To evaluate the possible energy savings score of the selected class Class, we use Utility_{Class} = \#TruePositive - \text{wrongPenalty} \ast \#FalsePositive, where \text{wrongPenalty} is the penalty score for incorrect prediction. These evaluation metrics are calculated, aggregated, and provided for every lattice element.
Example 5. Consider that the MBN traffic load levels predicted at a specific node is \(v_p = \{\text{Low, Low, Low, High, Low}\}\). The actual traffic monitored for 5 consecutive periods is \(v_c = \{10, 10, 100, 10, 10\}\) for the same node. If MBN optimization is performed using \(v_p\), the node will be turned off for the whole period, while it should not have been turned off for period 3. Such an incorrectly predicted traffic load will require the turned off node to be turned on again. MBN equipment turning on and off is inefficient and requires additional energy consumption. Therefore, to estimate the real utility, we use \(\text{wrongPenalty} = 2\) for the wrong predictions, i.e., \(\text{Utility}_{\text{Low}} = 4 - 2 * 1 = 2\), and the network could be optimized for 2 time units only. As shown, high prediction accuracy score does not guarantee high utility value.

**LBSTEP approach** For data with schema \([T, A_1, \ldots, A_k, V]\), we want to build a model \(M\) that can predict future values of \(v\). From a probabilistic point of view, \(M\) should be a good approximation of the probability distribution \(p*(V|A_1, \ldots, A_k, Data_T)\). We assume that (1) \(p*(V|A_1, \ldots, A_k, Data_T)\) is a good approximation of the true probability distribution \(p(V|A_1, \ldots, A_k)\) and (2) \(p(V|A_1, \ldots, A_k)\) is stationary, i.e., it does not evolve over time. As stated in\(^6\), ensemble methods have shown to be more efficient, accurate, and diverse than single method approaches. For these reasons, model \(M(A_1, \ldots, A_k, Data_T)\) is composed of \(n\) separate models, \(M_1, \ldots, M_n\), which are then combined using a function \(M(A_1, \ldots, A_k, Data_T) = \text{Agg}(M_1, \ldots, M_n)\) to provide a single ensemble prediction. We now describe how models are built using the lattice, lattice elements and the contexts defined in Section 4. Models are trained for each context. Using cross-validation\(^3\), accuracy is calculated for every discrete class, model \(M_i\), and contextual data \(Data_{\text{context}}\), i.e.,

\[
\text{Acc}_{\text{Class}}(M_i, Data_{\text{context}}) = \frac{\sum_{d_i \in Data_{\text{context}}} |M_i(Data_{\text{context}} \setminus d_i) = \text{Disc}(d_i)|}{\sum_{d_i \in Data_{\text{context}}} |\text{Class} = \text{Disc}(d_i)|},
\]

where \(|M_i(Data_{\text{context}} \setminus d_i)|\) is the class predicted by model \(M_i\) on \(Data_{\text{context}} \setminus d_i\), and \(|M_i(Data_{\text{context}} \setminus d_i) = \text{Disc}(d_i)|\) is equal to 1 if prediction is correct, 0 otherwise. Correct prediction of the specific class, \(|\text{Class} = \text{Disc}(d_i)|\) is equal to 1 if correct, 0 otherwise.

Example 6. We describe cross-validation, accuracy calculation, and traffic classification for the context \(\text{context}_{\text{Disc}, \text{Mon}, 1}\), see Figure 4, and the single model \(M_{\text{Min}}\). Three traffic classes, Low (below 30 MB), Median (between 30 and 500 MB), and High (above 500 MB), are used. Model \(M_{\text{Min}}\) returns the smallest traffic value of the provided data, i.e., \(M_{\text{Min}}(384, 13, 2.1) = 2.1\). In Table 1 we provide the accuracy calculation steps, where the first column is contextual data, and the second and third columns represent cross-validation. The value predicted by model \(M_{\text{Min}}\) (column four) is discretized (column five) and compared with the discretized actual value (column six). Model \(M_{\text{Min}}\) predicted class Low with \(\text{Acc}_{\text{Low}} = 2/2\), and the median class was predicted once while in fact it was Low, therefore \(\text{Acc}_{\text{Median}} = 0/1\). Total accuracy for the model is \(\text{Total Acc}_{\text{Min}} = 2/3\), i.e., two classes out of three where correct. The trained model \(M_{\text{Min}}\) for the selected context will predict \(\text{Prediction}_{\text{Min}} = \text{Low}\) class. We assume that the individual models are the following: \(M_{\text{Min}}\) gives the minimum, \(M_{\text{Max}}\) gives the maximum, \(M_{\text{Avg}}\) gives the average, and \(M_{\text{Med}}\) gives the set median. Model accuracies and weights, along with model predictions are provided in Table 2 for a larger training data set. Accuracies are provided for every class of the model. Model aggregation is extended by using weighted models \(w_M\). \(\text{Total Acc}_{\text{Min}}\) shows the total accuracy for the model \(M_i\), e.g., the model \(M_{\text{Min}}\) was the most accurate among the 4 models. \(\text{Prediction}_{\text{Min}}\) is the class predicted by the model \(M_i\), e.g., model \(M_{\text{Min}}\) will predict class Low.

We now describe how individual predictions are combined. To do so, let us assume that the accuracies are known for the models \(M_1, \ldots, M_n\) trained on \(Data_{\text{context}}\). Aggregation of several models into a single ensemble model \(M\) is not
In this paper, we explore and compare four ensemble aggregation strategies, \textit{AggS}, described below. We note that the main focus of the paper is the lattice-based context framework, not the aggregation strategies, and thus even more advanced aggregation strategies are left for future work. If several different candidate classes are selected, the higher predicted Class is the one predicted.

1. As in \textsuperscript{3}, we consider that ensemble prediction will select the model \( M_i \in M_1,\ldots, M_n \) with the highest \( \text{TotalAcc}_M \).
2. We consider only the \textit{frequency of Prediction}_\( M_i \), i.e., the most common predicted class is selected as the prediction. This is special case of aggregation strategy \textsuperscript{3}, where all weights are equal, \( w_{M_i} = 1 \).
3. We consider \textit{Prediction}_\( M_i \) and weight \( w_i \) for every model \( M_i \), i.e., we calculate \( \sum_{\text{Class}} w_{M_i} \) for every predicted \textit{Class}. Prediction is the \textit{Class} with the highest \( \sum_{\text{Class}} \).
4. We consider weights \( w_{M_i} \), predicted classes \textit{Prediction}_\( M_i \), and total accuracies \( \text{TotalAcc}_M \) for prediction. The highest \( \sum_{\text{Class}} w_{M_i} \ast \text{TotalAcc}_M \) shows which \textit{Class} is predicted.

\textbf{Example 7.} Using the presented prediction strategies and the accuracies in Table 2, we predict traffic load classes.

1. The highest \( \text{TotalAcc}_M \) is for model \( M_1 \), so model \( M \) will predict class Low as predicted by model \( M_1 \).
2. The models \( M_i \) predict 3 different classes. The most common predicted class is Low, therefore we will predict class Low.
3. For the provided weights, \( \sum_{\text{Low}} = 0.9 \), \( \sum_{\text{Median}} = 1 \), and \( \sum_{\text{High}} = 0.8 \), therefore \( M \) will predict class Median.
4. For the provided weights, \( \sum_{\text{Low}} = 6.4 \), \( \sum_{\text{Median}} = 6 \), and \( \sum_{\text{High}} = 5.6 \), therefore \( M \) will predict class Low.

\textbf{Greedy heuristic} Estimation of the optimal lattice element requires calculating accuracies of all lattice elements. Complex prediction models coupled with a potentially high number of lattice elements might be inefficient and too time consuming. To increase efficiency of the optimal lattice element selection, we propose a greedy heuristic. We start at the bottom element of the lattice (parent element). Iteratively, we estimate accuracies of the child elements and proceed with the single child with the highest accuracy, if accuracy is higher than the parent, otherwise we stop.

\textbf{Example 8.} Consider the lattice structure in Figure 4 and lattice element accuracies, i.e., \( \text{Acc(ID=1)}=0.75 \), \( \text{Acc(ID=2)}=0.74 \), \( \text{Acc(ID=3)}=0.72 \), \( \text{Acc(ID=4)}=0.77 \), \( \text{Acc(ID=7)}=0.74 \), \( \text{Acc(ID=9)}=0.72 \), \( \text{Acc(ID=10)}=0.73 \), \( \text{Acc(ID=1)}<\text{Acc(ID=4)} \), therefore we proceed with the child elements of lattice element \textit{ID}=4. Since child elements provide lower accuracy, we stop at element \textit{ID}=4.

\textbf{6. Experimental evaluation}

We consider an MBN of 660 nodes and 5 weeks of consecutively monitored traffic. The data did not contain noise, and it was regularly sampled. Missing records, which make up 0.3\% of the total dataset, are generated using the average of the neighboring existing values. LBSTEP is evaluated using both qualitative and quantitative measures: the prediction model construction time and the model size. To our knowledge, no other context-based prediction strategy than STEP can serve as competitor to LBSTEP. Additionally, we experiment how the weights and the voting function affect the performance. We consider the same four models, i.e., \( M_{\text{Min}}, M_{\text{Max}}, M_{\text{Avg}}, M_{\text{Med}} \), for ensemble prediction as
The models were trained on the first four weeks and then evaluated on the last one. The considered lattice and the underlying dimensions are shown in Figure 3. In the following figures, $ID$ of the lattice element is shown in x axis (see Figure 3), while the y axis represents various statistical measures. Traffic discretization implies that the number of traffic classes is not fixed. Network can be potentially optimized when traffic is low. Experiments were performed on an Intel i7 2.67GHz PC with 4GB RAM running Windows7 64-bit. LBSTEP has been implemented and tested with Java JDK 1.7 using 2GB RAM.

**Optimal context** Lattice construction depends on the number of attributes, levels in the hierarchies, and the size of the Data. The discretization function $Desc$ is defined using a threshold of 105 MB (the median traffic value of 5 weeks of traffic), i.e., class Low represents traffic below 105 MB, class High traffic above. For the initial optimal context selection, weights for single models are set to $w_{Min} = 0.5$, $w_{Max} = 0.5$, $w_{Avg} = 1$, and $w_{Med} = 1$. We calculate qualitative measures, i.e., accuracy, precision, recall, utility, and F-measure for all lattice elements. The three selected measurements (accuracy, utility, and F-measure) are provided for the four ensemble strategies in Figures 5a, 5b, 5c. Only 2 lines are visible since performance of the models is similar and graph lines overlap.

We test the influence of the discretization function by using different threshold values equal to 48 MB (1/3 of the traffic) and 205 MB (2/3 of the traffic). Models are consistent and give the best statistical results for the same lattice element, i.e., the highest scores are detected for the lattice element $ID = 3$.

**Optimal weights** We have already identified that the optimal lattice element for the predictions is element $ID = 3$. We now focus on the weight optimization for the ensemble strategies $Agg_{s3}$ and $Agg_{s4}$. The estimated optimal weights are provided in Table 3. For weight optimization we consider a two class discretization function and thresholds equal to 48MB, 105MB, and 205MB. We check which weight combination gives the best accuracy (short A), utility (short U), and F-measure (short F) results, i.e., the single models are assigned weights $w_i$ in the range [0,1] with a step size of 0.1. The utility score is calculated with two penalty scores $wrongPenalty = 1$ (short U1) and $wrongPenalty = 2$ (short U2). Use of different $wrongPenalty$ scores allows simulating different network designs and technical details of the equipment installed in the MBN.

Different thresholds require different weights to get the best performance. Weights can be optimized according to user preferences aiming for the best accuracy, utility, or F-measure. For the inspected thresholds, ensemble strategy $Agg_{s3}$ has constant high weights for models $M_{Avg}$ and $M_{Med}$. Weights for strategy $Agg_{s4}$ vary for every threshold and every qualitative measure, therefore no standard rules can be defined for weights. We elect the best ensemble.

### Table 3. Optimized weights for models $M_{Min}, M_{Max}, M_{Avg}, M_{Med}$

<table>
<thead>
<tr>
<th>Threshold=48</th>
<th>Threshold=105</th>
<th>Threshold=205</th>
</tr>
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<tr>
<td>$Agg_{s3}$</td>
<td>$Agg_{s4}$</td>
<td>$Agg_{s4}$</td>
</tr>
<tr>
<td>$M_{Min}$</td>
<td>$M_{Max}$</td>
<td>$M_{Avg}$</td>
</tr>
<tr>
<td>A</td>
<td>0.1, 0.1</td>
<td>0.9, 1</td>
</tr>
<tr>
<td>T/1</td>
<td>0.1, 0.1</td>
<td>0.9, 1</td>
</tr>
<tr>
<td>T/2</td>
<td>0.1, 0.1</td>
<td>0.9, 1</td>
</tr>
<tr>
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<td>0.9, 1</td>
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<td>$M_{Max}$</td>
<td>$M_{Avg}$</td>
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<tr>
<td>T/1</td>
<td>0.5, 0.1</td>
<td>0.1, 1</td>
</tr>
<tr>
<td>T/2</td>
<td>0.5, 0.1</td>
<td>0.1, 1</td>
</tr>
<tr>
<td>$F$</td>
<td>0.8, 0.2</td>
<td>0.1, 1</td>
</tr>
</tbody>
</table>
strategy by comparing statistical measures for all lattice elements. Ensemble strategy $AggS3$ shows the highest sum of accuracy, utility with $wrongPenalty = 1$, and F-measure. Ensemble strategies $AggS1$ and $AggS4$ shows similar results to strategy $AggS3$, while ensemble strategy $AggS2$ has lower scores.

**Quantitative evaluation** We evaluate model construction using two criteria, *i.e.*, time and physical model size stored using Serializable functionality for ensemble strategy $AggS3$ with threshold 30MB. The main factor that affects the size of the trained models and time required for the model construction for the specific lattice element is $SizeE$, which defines the number of different contexts. For the lattice element $ID=1$ in total $SizeE_{node, Day, Hour} = 110880$ contexts will be trained, while for element $ID=4$ $SizeE_{node, Day, Hour, type} = 18480$. The model construction time and disk space are provided in Figure 6a. Default information stored in prediction models takes a constant size, therefore the real size of the model can be estimated by subtracting 35.5 MB. Both time and disk space are higher for the lattice elements containing more different contexts.

**Greedy heuristic validation** We evaluate the greedy heuristic for prediction correctness and efficiency in terms of required time with 10 discretization functions defined using thresholds evenly distributed in the range 30 to 300 MB. The heuristic gives the correct result if the lattice element selected by the heuristic is the lattice element with highest accuracy. The greedy heuristic is 100% correct and provides the highest accuracy lattice element in all 10 cases. Use of the heuristic provides approx. 20% time savings, since accuracies of the most costly lattice elements $ID=1...4$ are always evaluated, see Figure 6a.

**LBSTEP vs ARIMA vs STEP** We compare our proposed LBSTEP approach with other prediction strategies, *i.e.*, the state of the art forecasting technique ARIMA and the single context approach STEP. We use the R package for ARIMA times series forecasting. ARIMA is tested with the same setup, *i.e.*, four weeks used for training and one week for evaluation. ARIMA models show lower accuracy since most of the nodes are predicted to have High traffic, see Figure 6b. In addition, only the first ARIMA predictions actually vary and later the predictions become constant. This conservative ARIMA approach does not guarantee any energy savings for lower threshold values, see Figure 6c. We compare our previously proposed STEP, based on a fixed context[node, hour], and our multiple context LBSTEP. The STEP context[node, hour] in the lattice would be represented by the lattice element $element_{node, ALL, Hour}$ (ID=8) and ensemble strategy 1. As we have shown, $elements_{node, ALL, Hour}$ is not the optimal lattice element for prediction results and ensemble strategy 1 is not optimal. Considering the optimal lattice element, *i.e.*, $ID=3$, and the optimal ensemble strategy 3, we improve accuracy of the STEP approach by 1-2% for various thresholds, which is enough to give valuable energy savings.

7. Related work

Prediction and forecasting has been used for various applications. Traffic trends in mobile networks can be estimated using forecasting techniques. In [7], Cisco presents a forecasting model, trained on a list of parameters specific for the mobile networks, *e.g.*, density of the mobile users, active user time per hour, traffic generated within active period, other mobile network specific information. Even if this model is suitable for long term traffic predictions, *e.g.*, one year period, and gives abstract traffic trend in the network, it is useless when considering MBN optimization based on short term traffic load.
Context-based predictions have been analyzed in the past. Predictions using data cubes where dimensional attributes are equipped with hierarchies have been addressed in\(^8\). Multiple context-based predictions and use cases are presented in\(^9\). Context-based predictions are presented in\(^10\), where the authors present prediction using the context as well as future context prediction. In\(^11\), the authors consider factors that affects the accuracy of context use for predictions. Relations between similar users allows assuming that the users might share the same context\(^12\). In STEP\(^3\), models are built for the fixed context[node, hour] and afterward used for predictions. In the current paper, we extend model construction using multiple contexts defined by the lattice. Additionally, we propose a solution that can deal with more complex hierarchy types and multiple contexts.

Spatio-temporal predictions can be based on monitoring users and collecting spatial information, e.g., when and where users move. Expansion and the use of mobile devices made user tracking simple. In\(^13\), contextual information is used as the solution supporting computations. The possibility to predict user movement using historical data as well as to perform network optimization has been presented in the papers\(^14\)\(^15\). Constant position tracking of every mobile user is costly, both in data size and position estimation. Therefore, the current paper instead considers MBN optimization using the aggregated traffic information at every network element.

8. Conclusion and future work

This paper investigated spatio-temporal time series prediction considering contextual data. We presented LBSTEP which significantly extends our previously approach STEP by (1) the use of multidimensional prediction models, (2) the use of several ensemble strategies, and (3) a domain specific evaluation metric, i.e., MBN possible energy savings. Multiple contexts levels are presented as lattice elements. The experimental results show that LBSTEP’s multidimensional prediction models improve all qualitative metrics for hierarchical data.

LBSTEP can be extended in several directions. First, more complex multidimensional models can be used for a single ensemble prediction model. Second, hierarchies can be automatically built for achieving better prediction results. Third, LBSTEP can be extended to handle concept drift.

References