

Validation of the Driving by Visual Angle car following model

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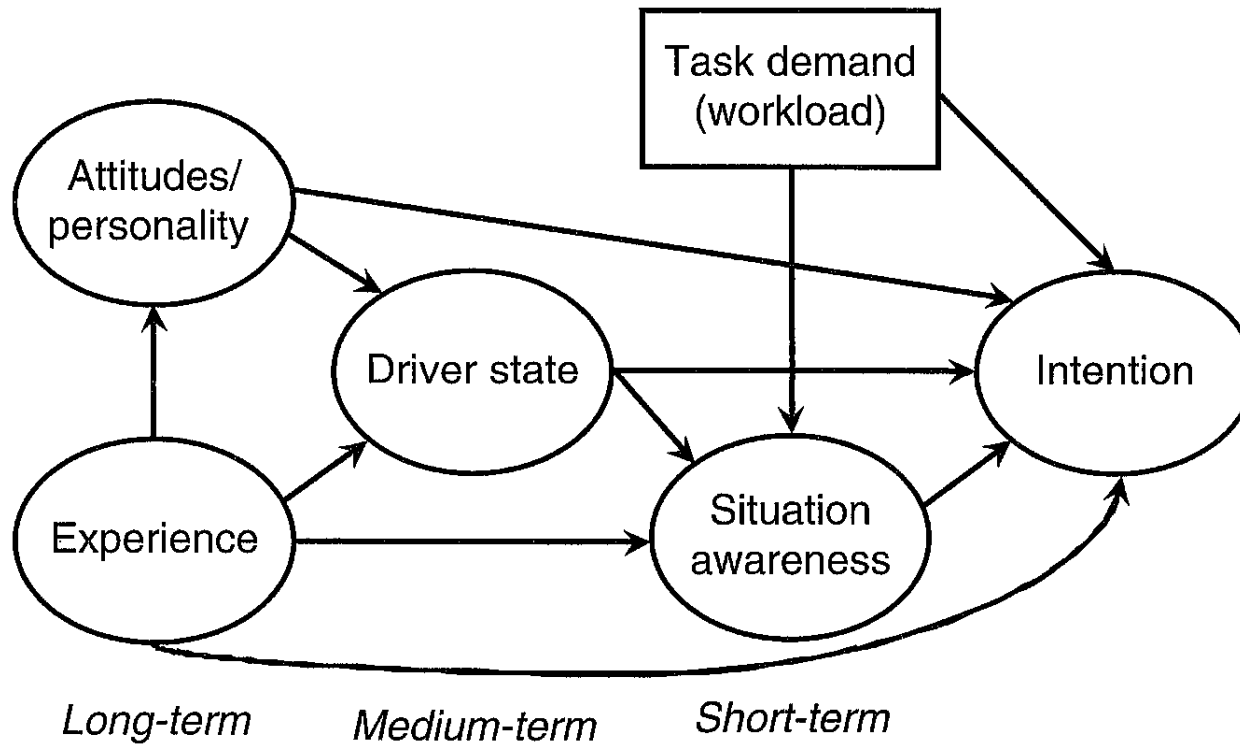


Why modelling car following?



Examples of models

Box-and-Arrow



Carsten (2007)



Examples of models

Cognitive architecture, production rules

(p decide-lc-lane1	==>
=goal>	=subgoal>
isa drive	isa check-lc
stage decide-lc	lane lane1
task lk	v =v
lane lane1	result =result
v =v	!push! =subgoal
fkind car	=goal>
fthw =thw	stage =result)
!eval! (< =thw *thw-pass*)	

(Salvucci, e.g. 2005)



Examples of models

Psychophysical controller for car following behavior

$$a_{t+1} = j \left(\frac{1}{\alpha_t} - \frac{1}{\alpha'} \right) + k \frac{d}{dt} \alpha_t$$

Anderson and Sauer (2007)

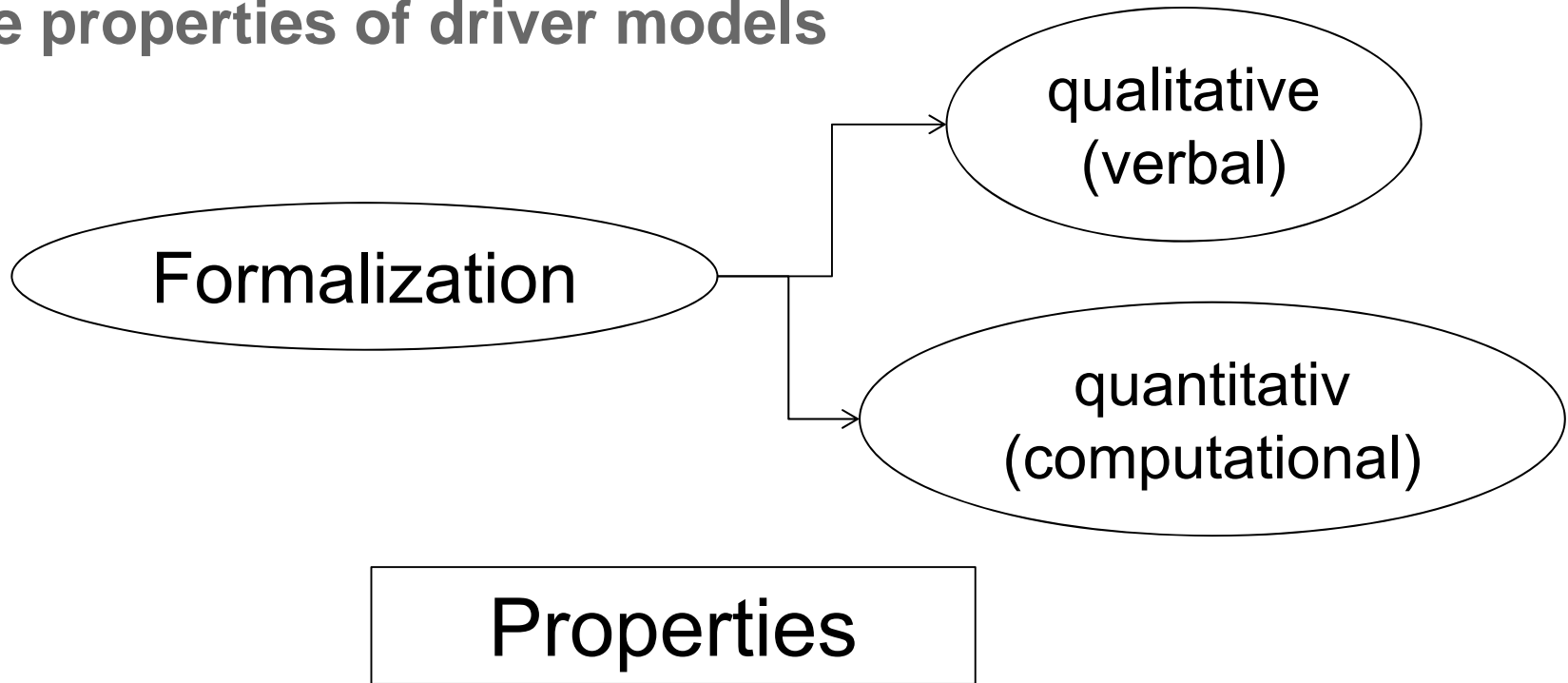


Some properties of driver models

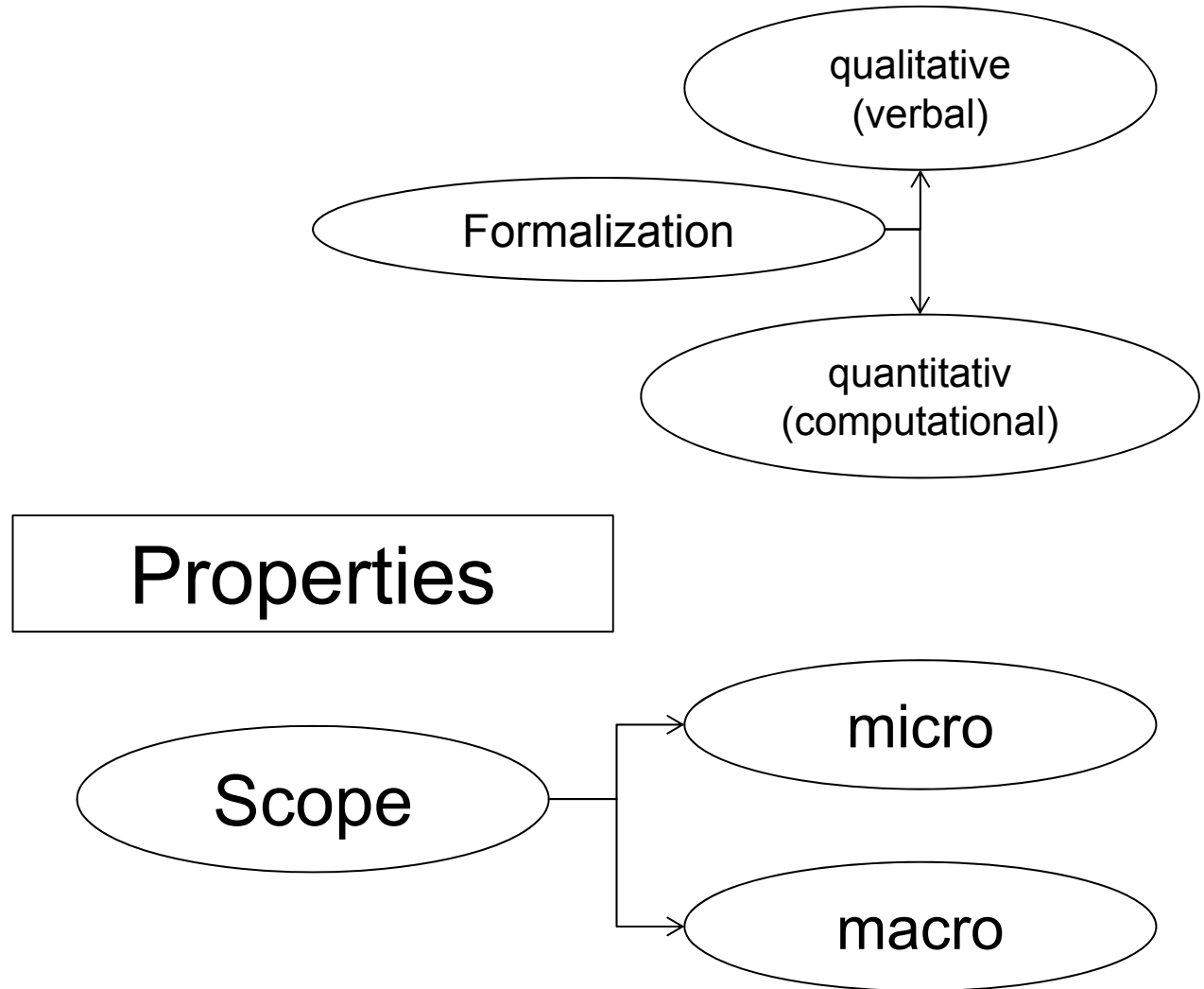
Properties



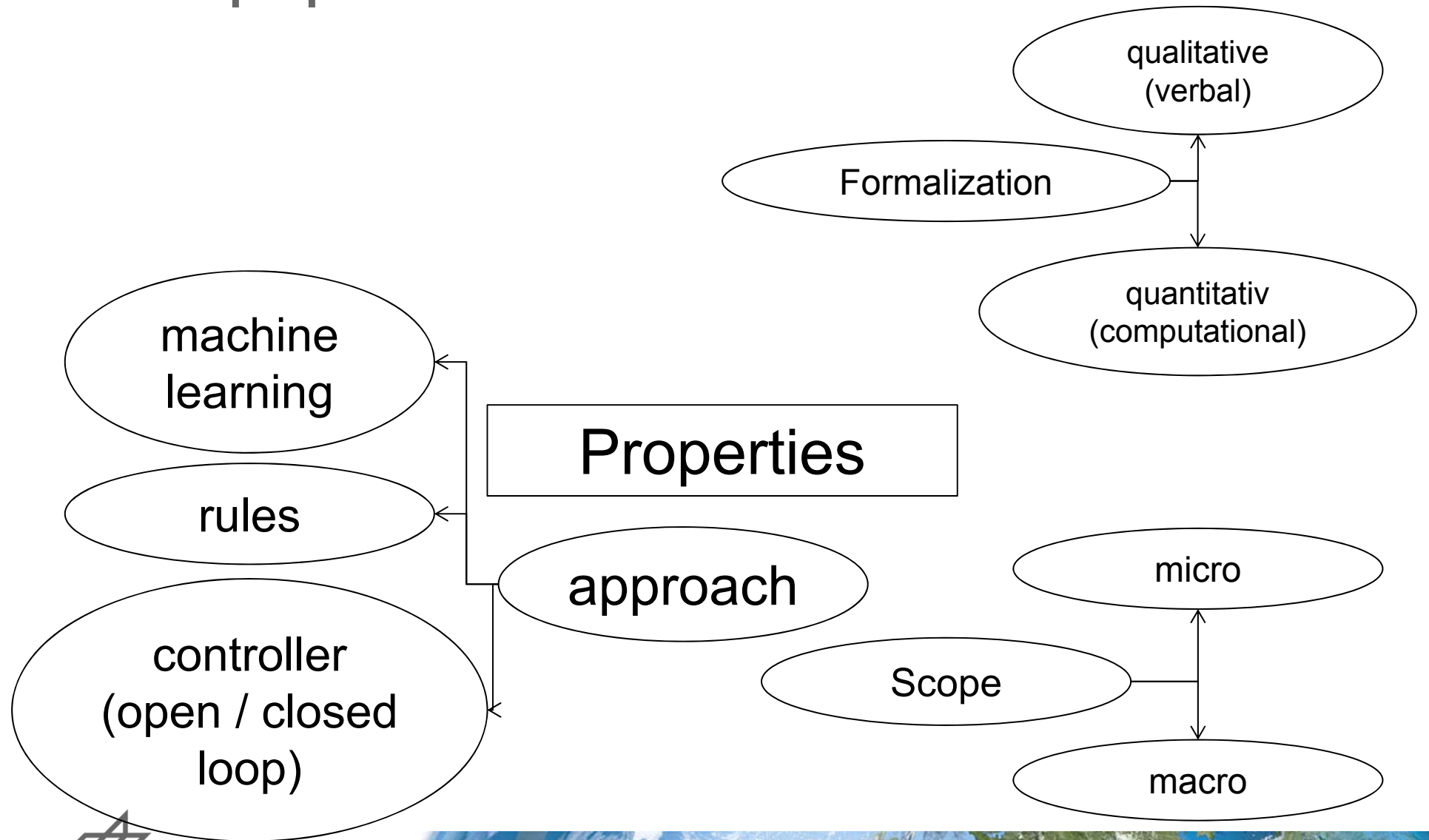
Some properties of driver models



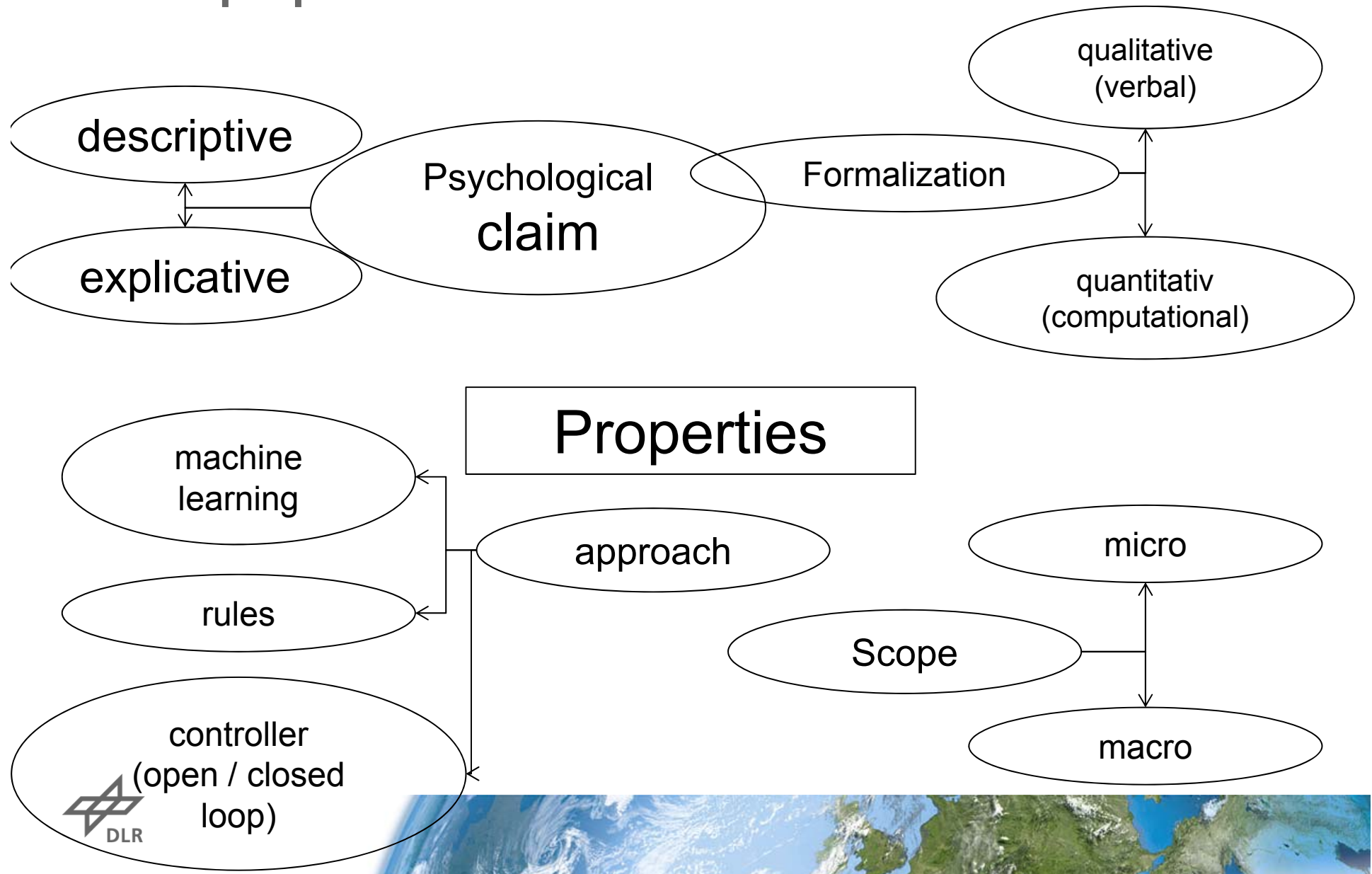
Some properties of driver models



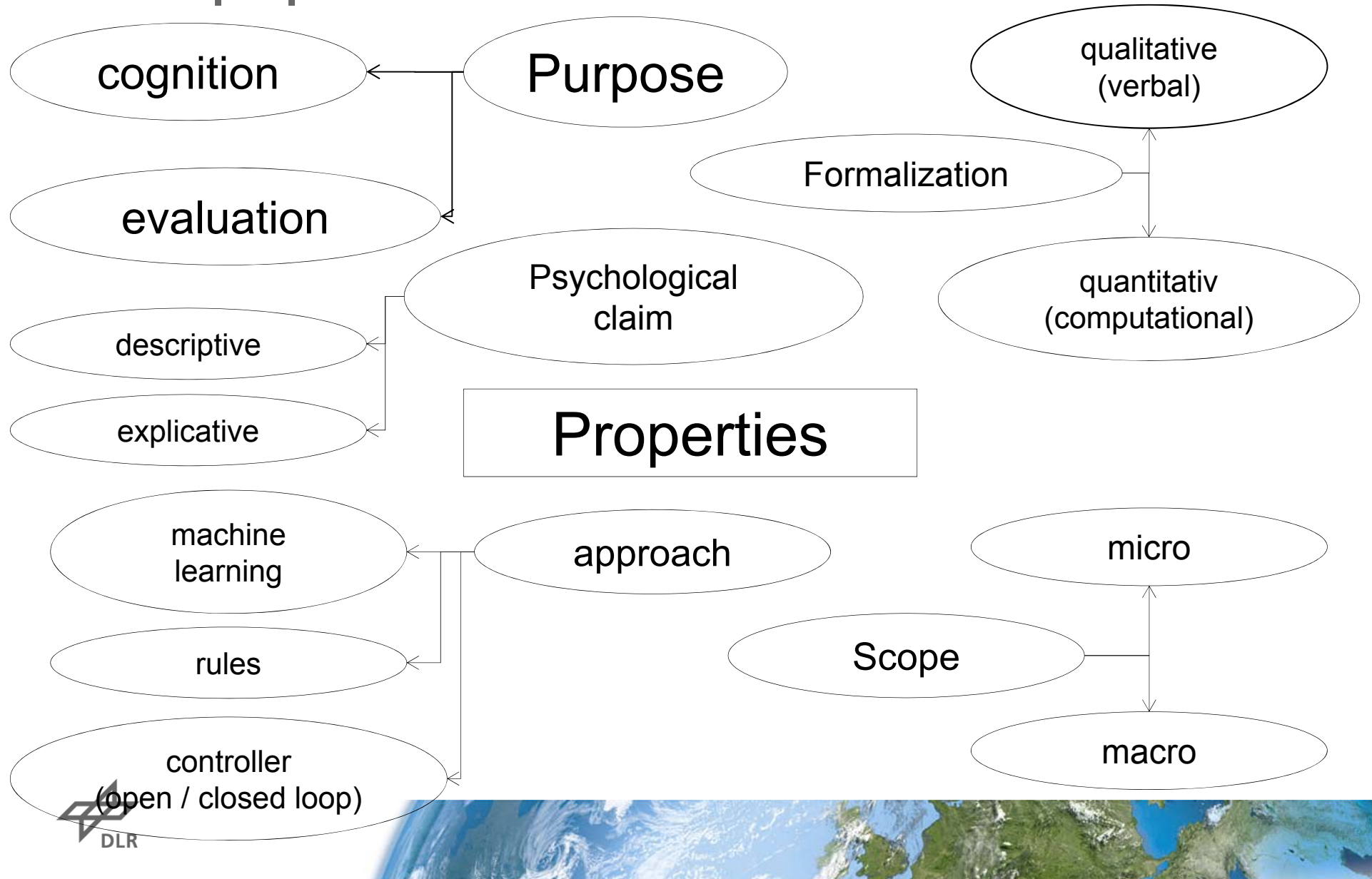
Some properties of driver models



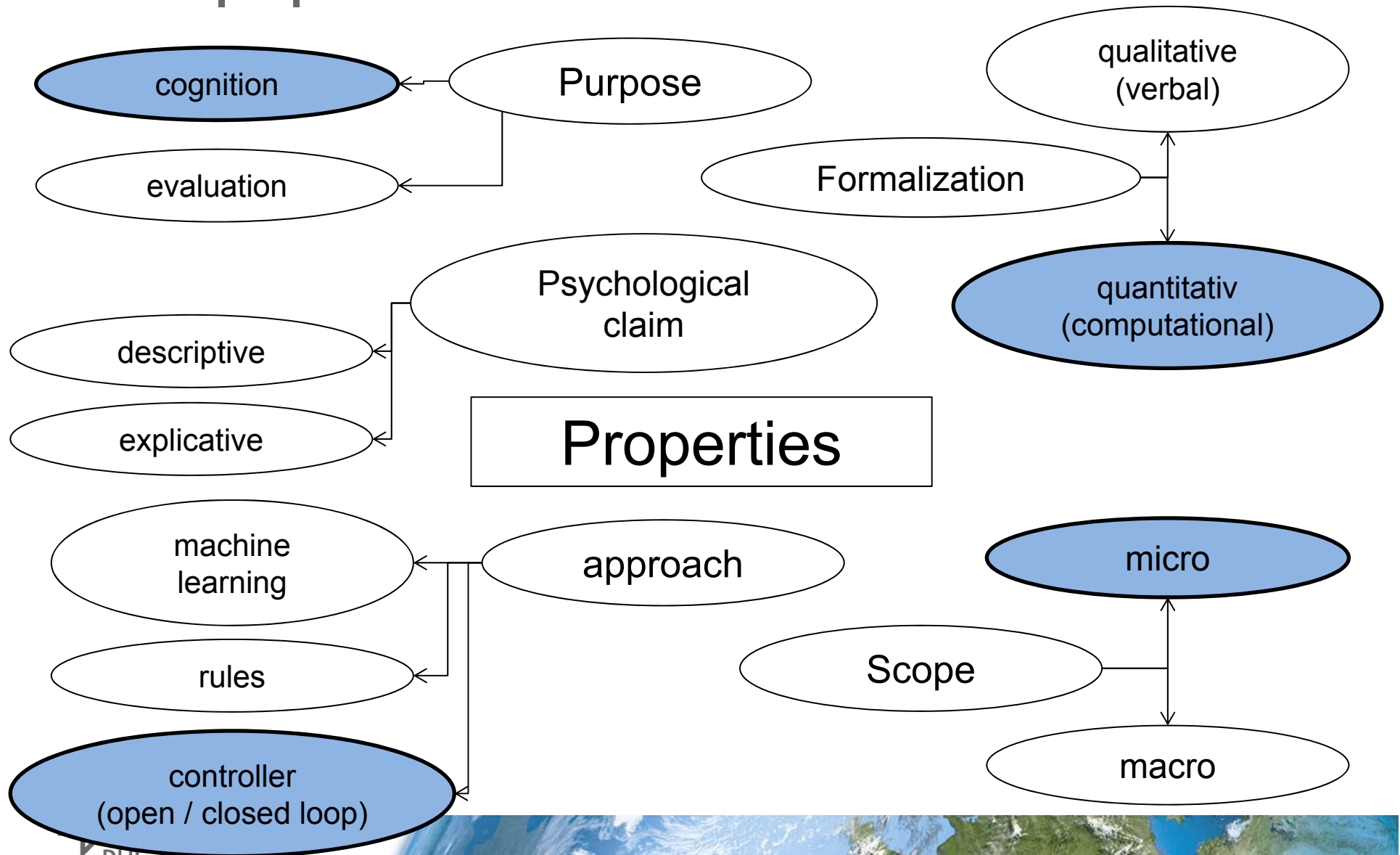
Some properties of driver models



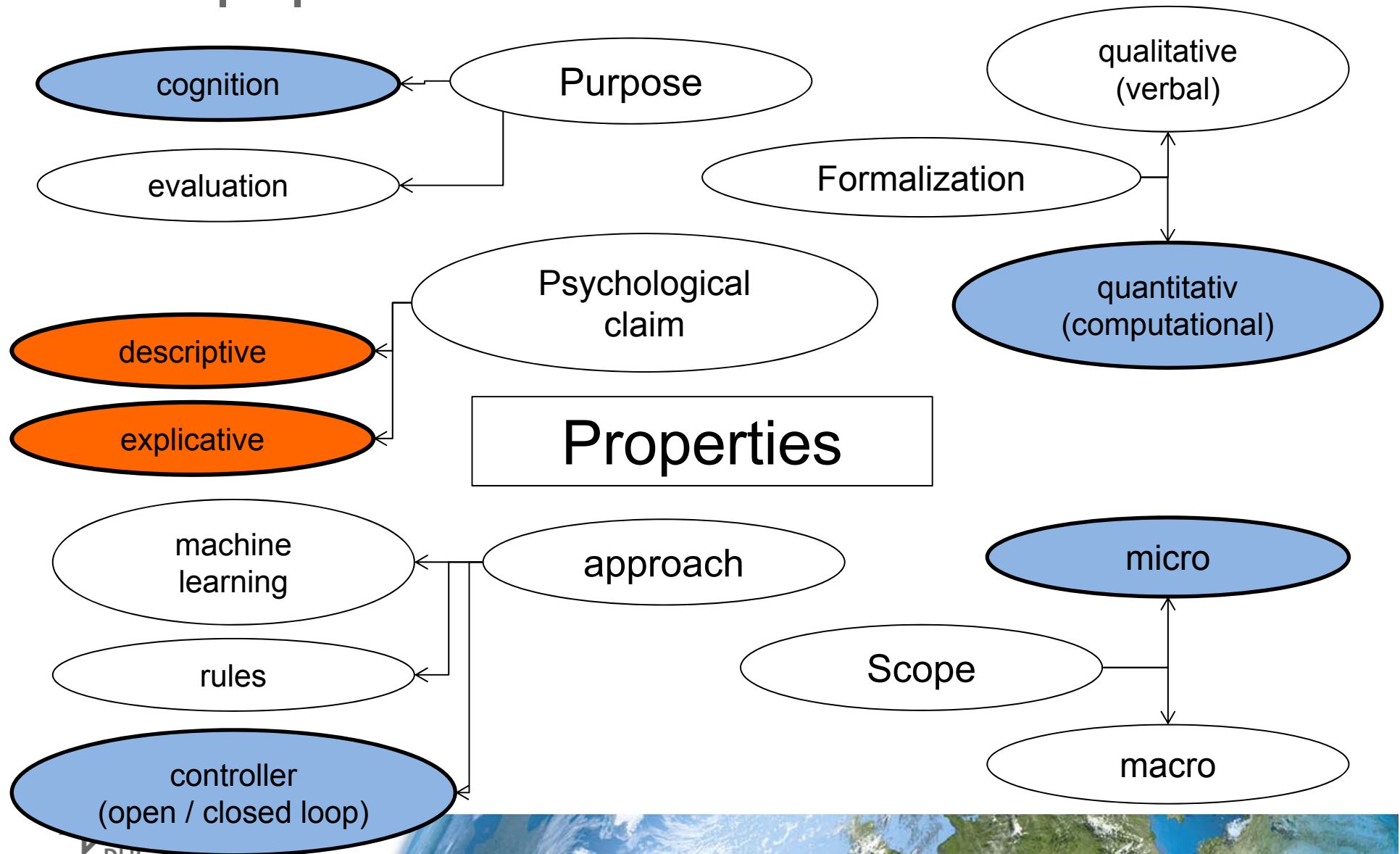
Some properties of driver models



Some properties of driver models



Some properties of driver models



Why modelling car following?

basic driving task

- essential for higher cognition driver models
- comparatively easy modelling of a driving task

extremely useful for design of assistance systems

lacking so far

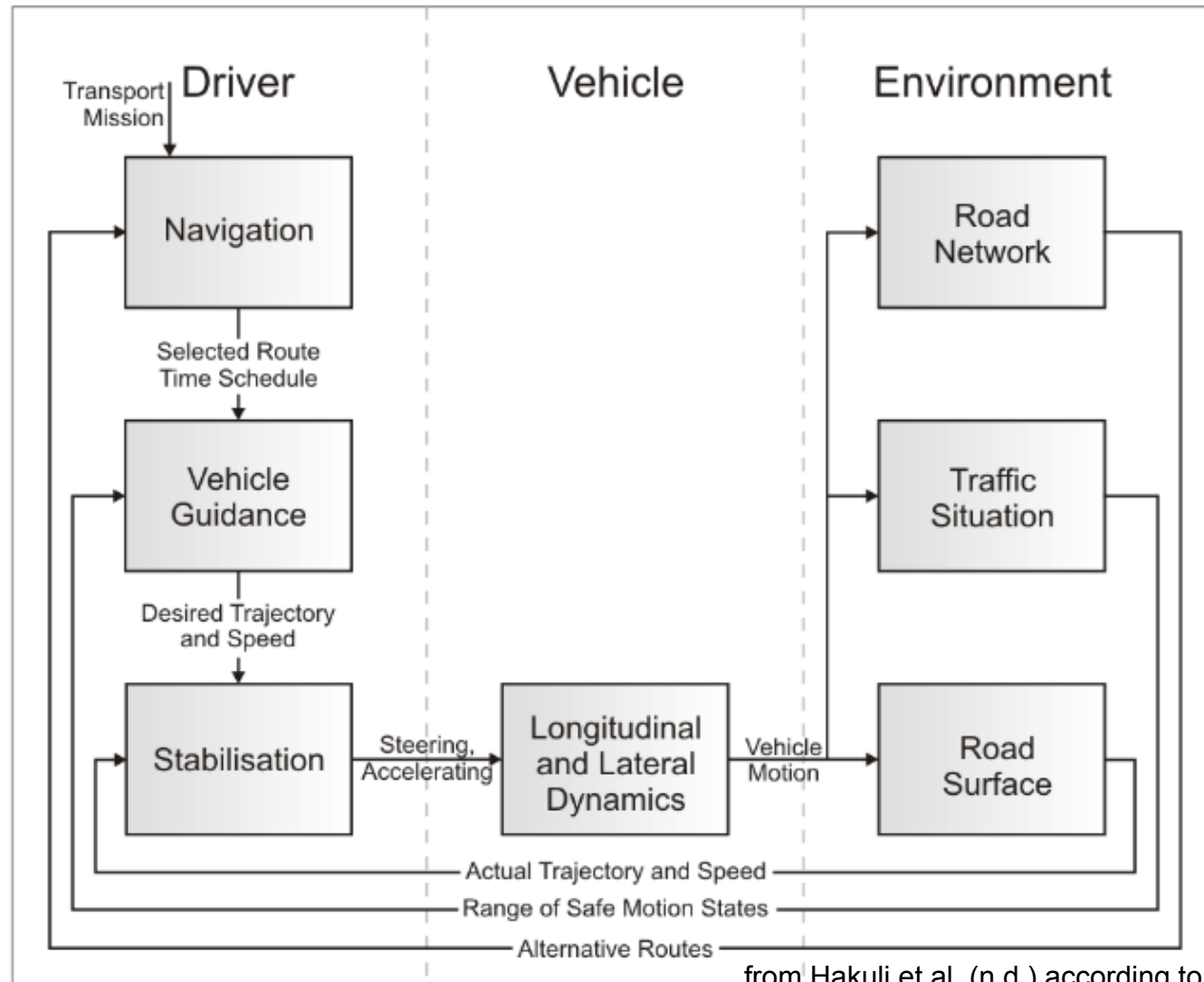
- good data on individual car-following behavior
- systematic evaluation of models on this data

we contribute to close that gap

- data for individual drivers
- from real traffic with instrumented vehicle
- systematic variation of road type (city, highway, country)



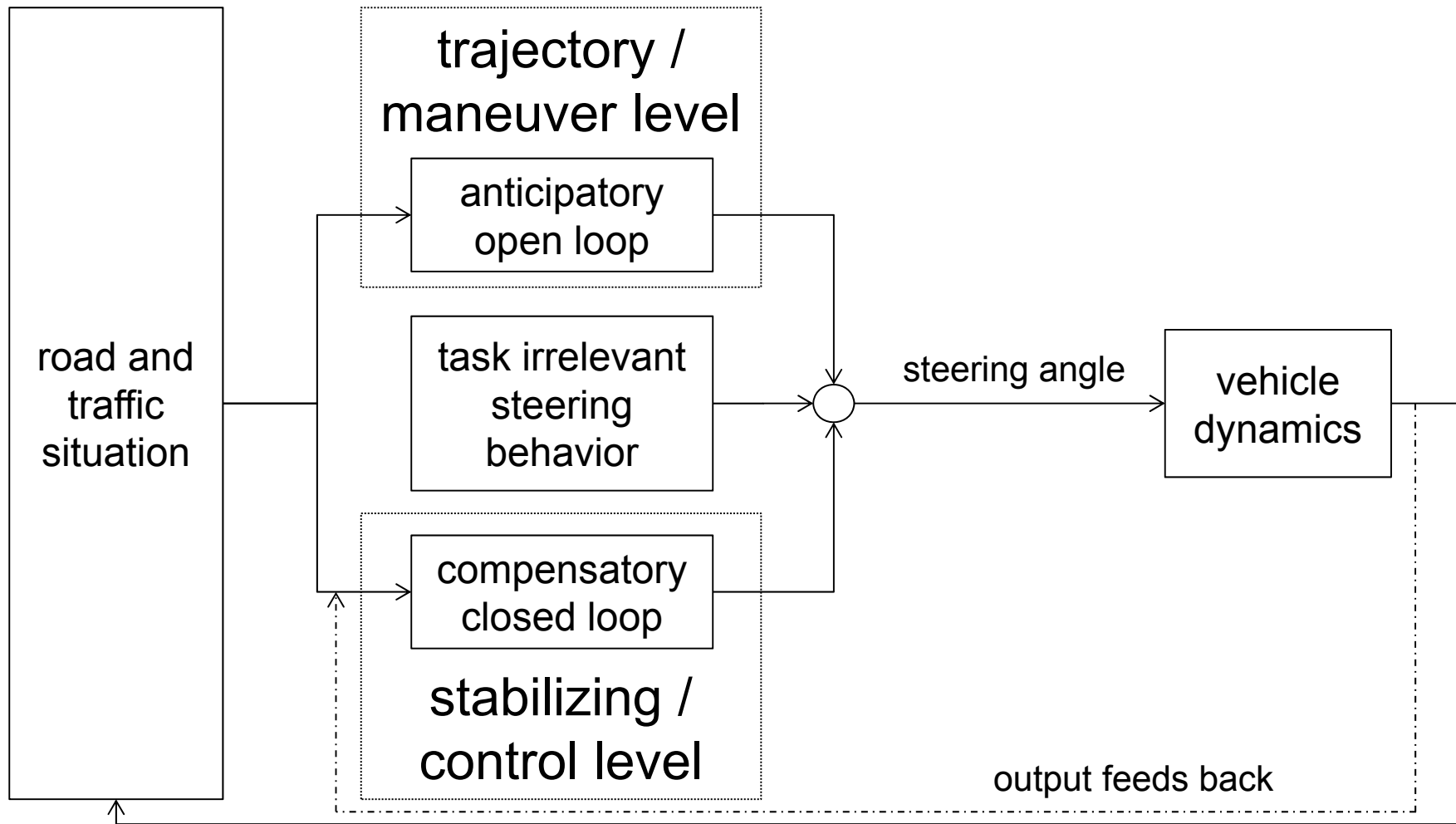
Basic driving tasks



from Hakuli et al. (n.d.) according to Donges (1982)



Control level of driving



adapted from Donges (1978)



A very simple car following model

$$a_t = s \left(v_{VF_{t-T}} - v_{FF_{t-T}} \right)$$

with

$a(t)$ = acceleration at time t ,

$v_{VF_{t-T}}$ = velocity lead vehicle one timestep ago,

$v_{FF_{t-T}}$ = velocity following vehicle one timestep ago,

s = free parameter

Pipes (1953)



A very simple car following model

$$a_t = s(v_{VF_{t-T}} - v_{FF_{t-T}})$$

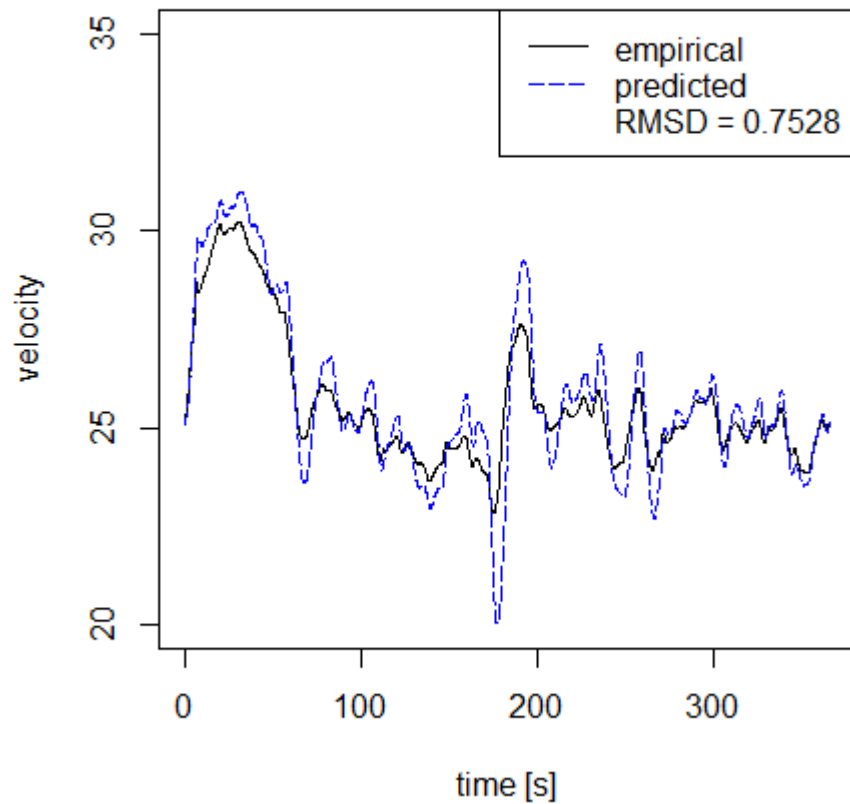
basic algorithm

1. choose a start parameter for s
2. take values for leading vehicle from data
3. take first value for following vehicle from data
4. compute prediction for the next time step by using the predicted a
5. do so until the end of the vector
6. compute error metric
7. test next parameter, until the error metric is at a minimum

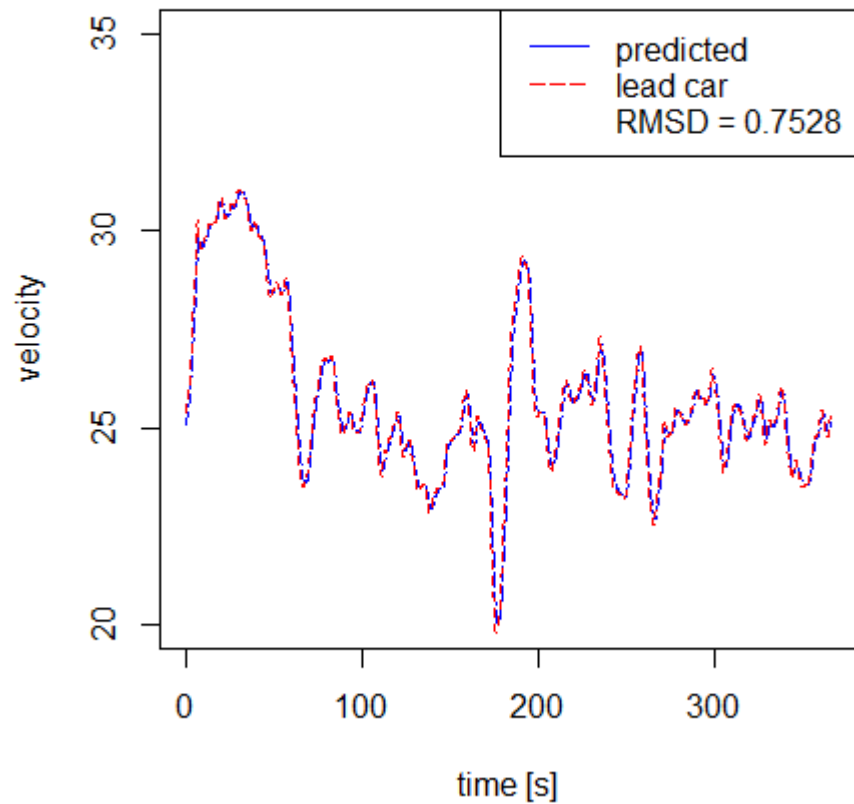


A very simple car following model

empirical vs predicted velocity, $s = 1$

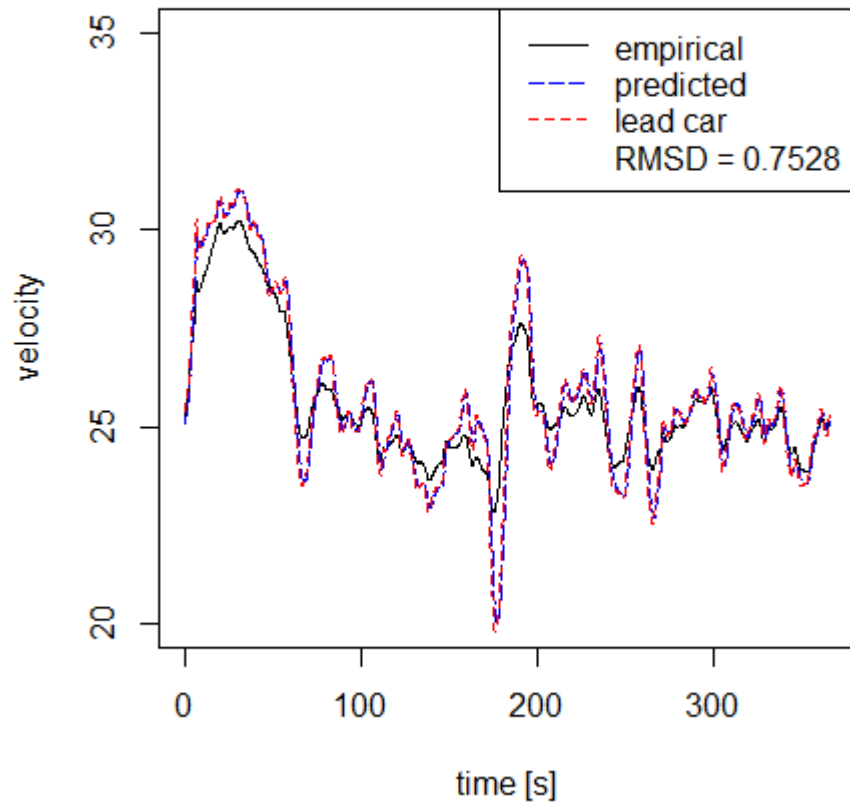


predicted velocity vs lead car, $s = 1$

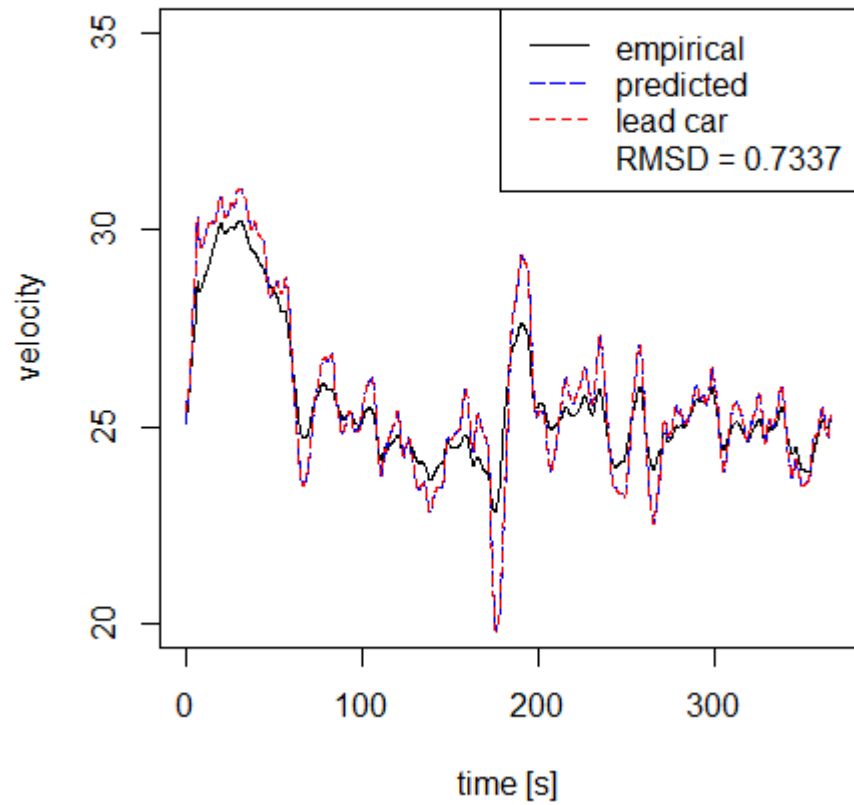


A very simple car following model

all together, $s = 1$



all together, $s = 9.22$



The Gipps model

$$v_{t+\tau} = b^{max} + \sqrt{(b^{max})^2 \cdot \tau^2 - b^{max} \cdot (2 \cdot [d_t + d^{min}] - v_{FF_t} \cdot \tau - \frac{v_{VF_t}^2}{b^{est}})}$$

with

Gipps (1981)

b^{max} = most severe braking of the driver,

b^{est} = estimated braking of the leading vehicle,

d^{min} = safety distance,

d_t = velocity of leading vehicle at time t ,

τ = apparent reaction time, a constant for all vehicles,

$v_{VF_{t-\tau}}$ = velocity lead vehicle one timestep ago,

$v_{FF_{t-\tau}}$ = velocity following vehicle one timestep ago



The Helly model

$$a_t = j \cdot (d_{t-T} - d'_t) + k \cdot (v_{VF_{t-T}} - v_{FF_{t-T}})$$

with

$$d'_t = s + r \cdot v_{FF_t},$$

s = safety distance,

$v_{VF_{t-T}}$ = velocity lead vehicle one timestep ago,

$v_{FF_{t-T}}$ = velocity following vehicle one timestep ago,

r = weight factor,

T = time step

Helly (1959)



The Driving-by-Visual-Angle model

$$a_{t+1} = j \cdot \left(\frac{1}{\alpha_t} - \frac{1}{\alpha'} \right) + k \cdot \frac{d}{dt} a$$

with

$$\alpha' = 2 \cdot \operatorname{atan} \left(\frac{w}{THW \cdot v_{FF_t}} \right)$$

and

α_t = visual angle,

α' = desired visual angle,

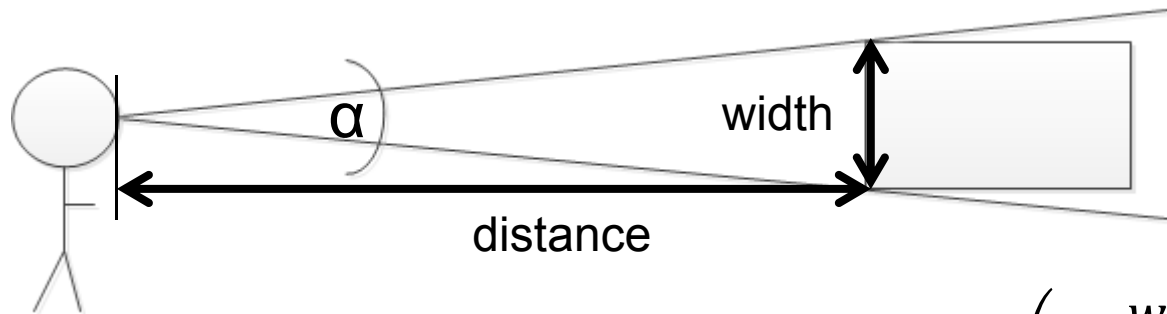
w = width of lead car,

THW = timegap,

v_{FF_t} = velocity lead car

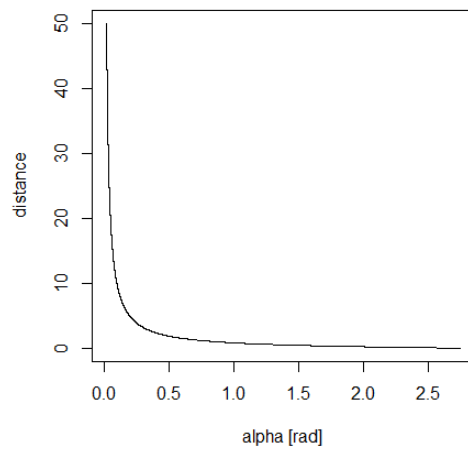


The Driving-by-Visual-Angle model

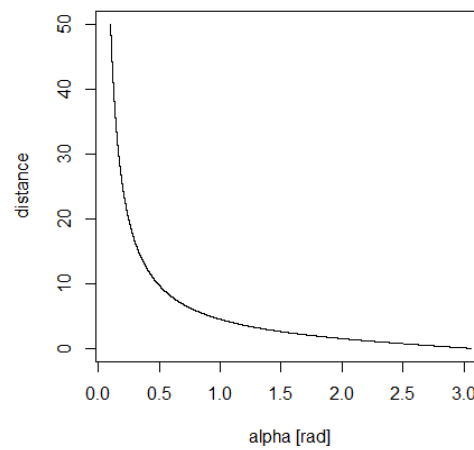


$$\alpha = 2 * \operatorname{atan} \left(\frac{\text{width}}{2 * \text{distance}} \right) \approx \frac{\text{width}}{\text{distance}}$$

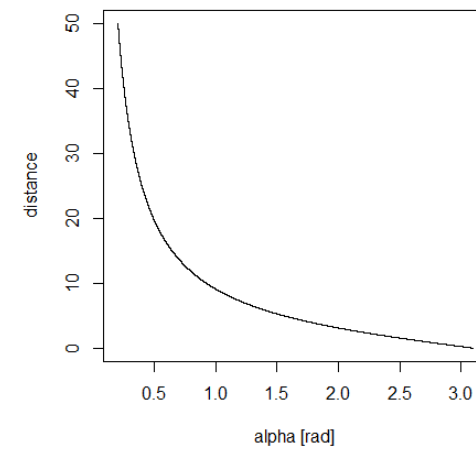
alpha vs distance, width = 1



alpha vs distance, width = 5



alpha vs distance, width = 10



Helly's model vs. DVA

Helly

$$a_{t+1} = j(d_t - d'_t) + k(v_{LV_t} - v_{FV_t})$$

DVA

$$\begin{aligned} a_{t+1} &= j \left(\frac{1}{\alpha_t} - \frac{1}{\alpha'_t} \right) + k \frac{d}{dt} \alpha \\ &= j \frac{1}{w} (d_t - d'_t) + (-k) \left(w \left(\frac{d_{t-1} - d_t}{d_t^2} \right) \right) \end{aligned}$$



Validation methods

driving simulator: often sinusoidal speed profiles

- disadvantage: might be too artificial

real driving data: cameras, induction loops etc.

- disadvantage: dirty data, absolutely no control over situation

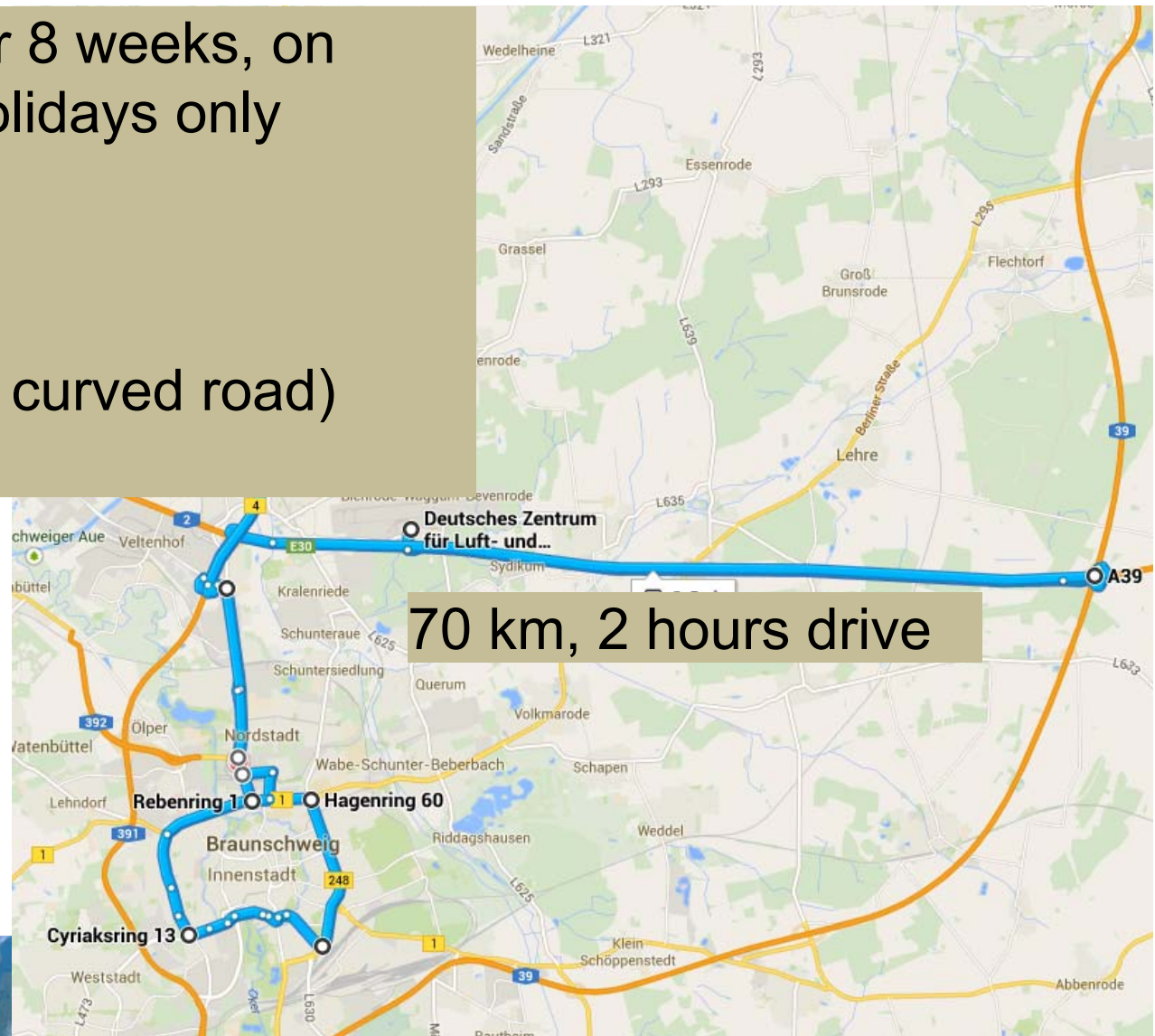


Methods

12 participants over 8 weeks, on Sundays / public holidays only

road types:

- highway
- city (straight and curved road)
- country

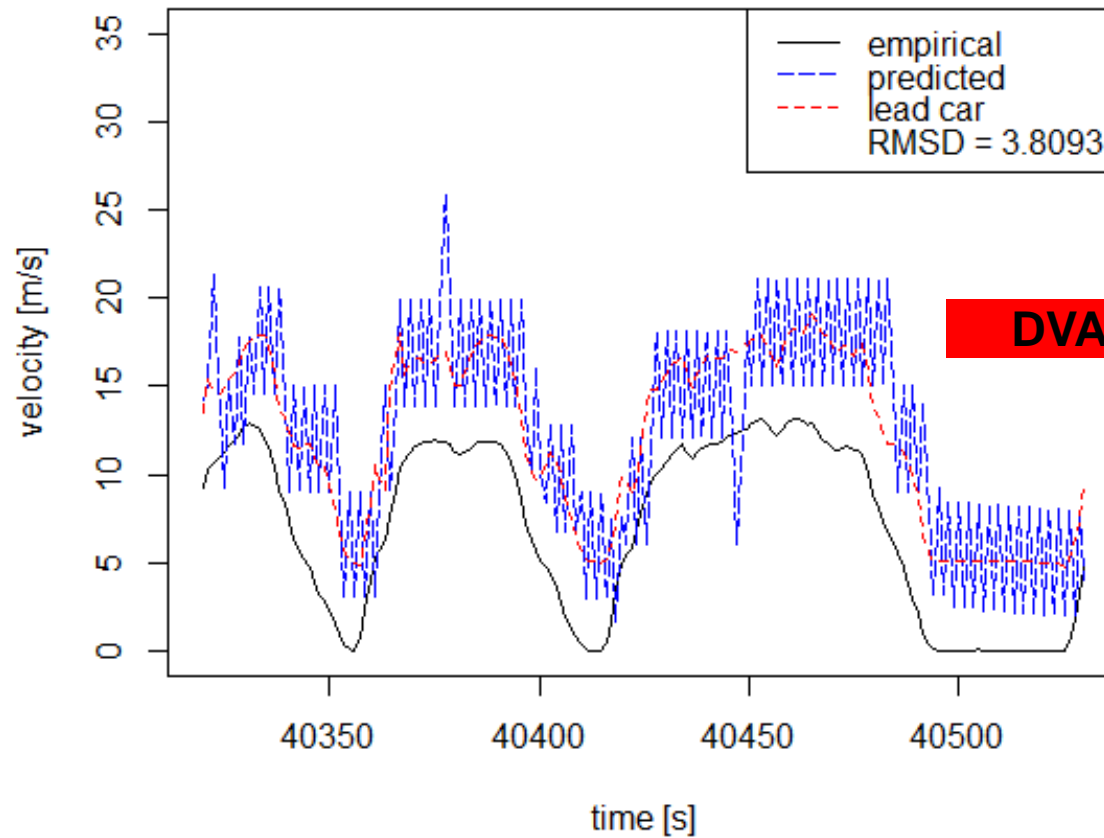


Methods



Predictions unoptimized

DVA unoptimized, subj 2, city ring

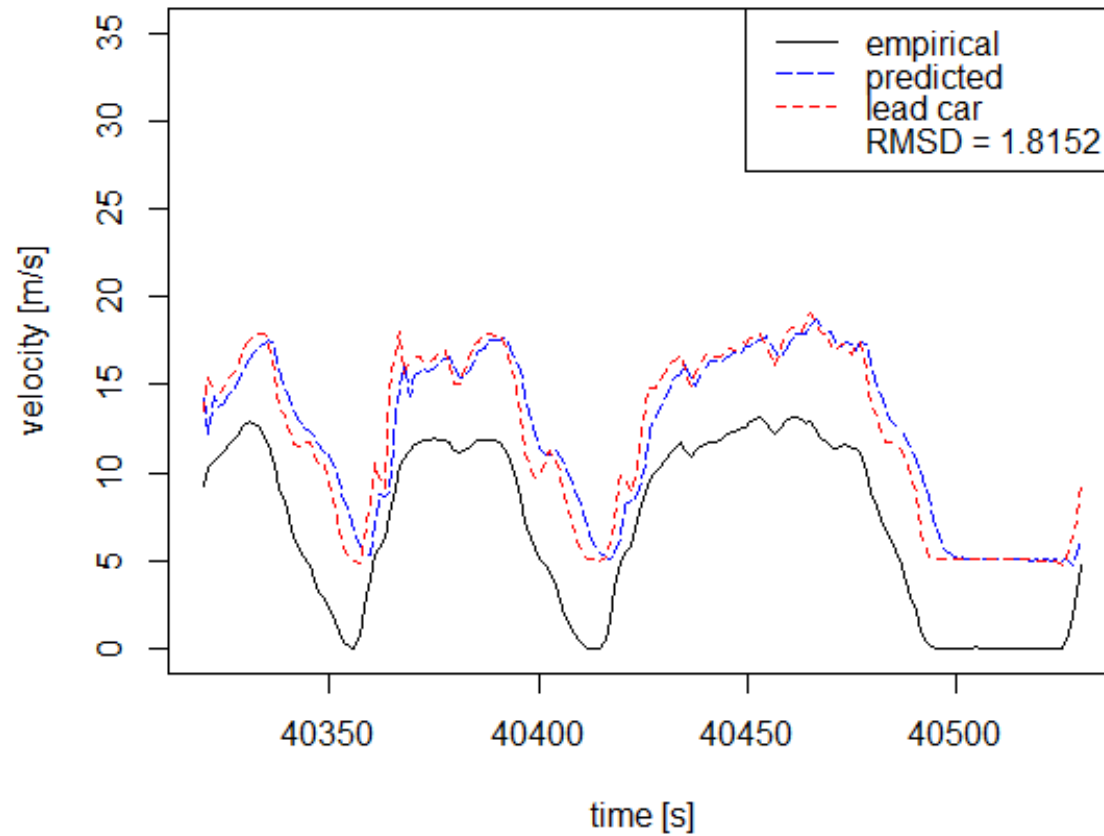


DVA is unstable!



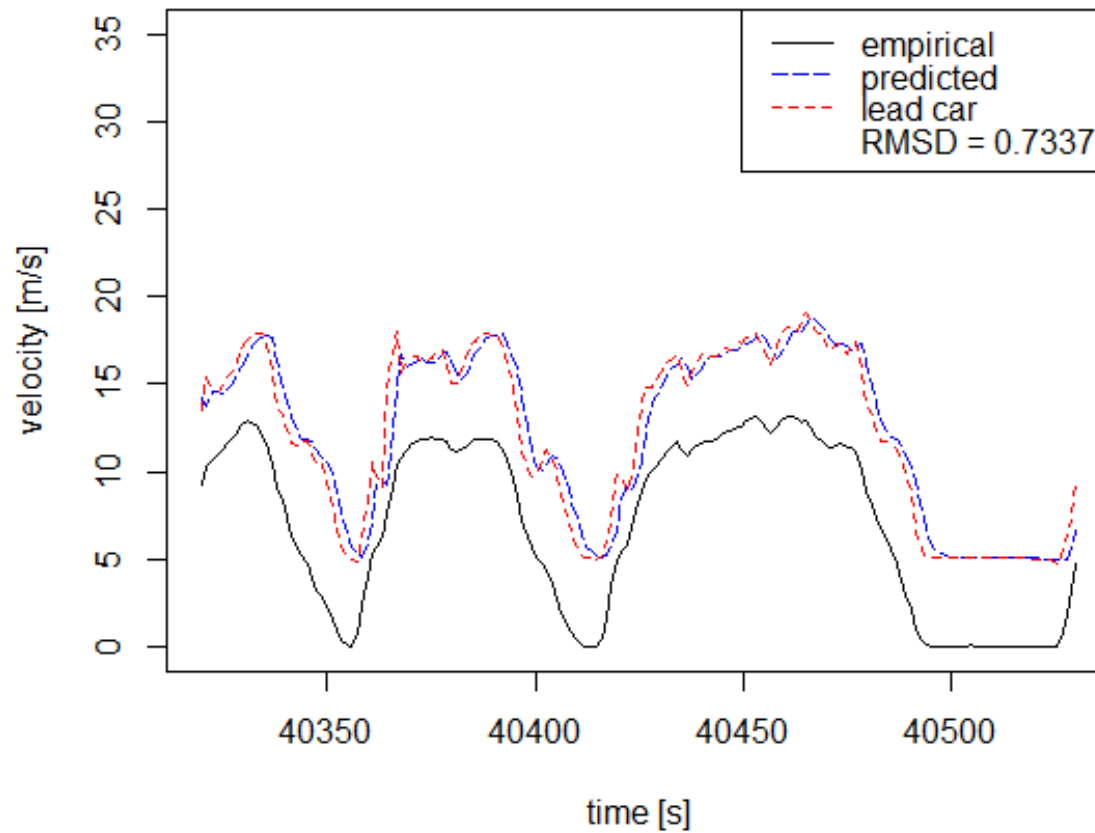
Predictions unoptimized

Gipps unoptimized, subj 2, city ring

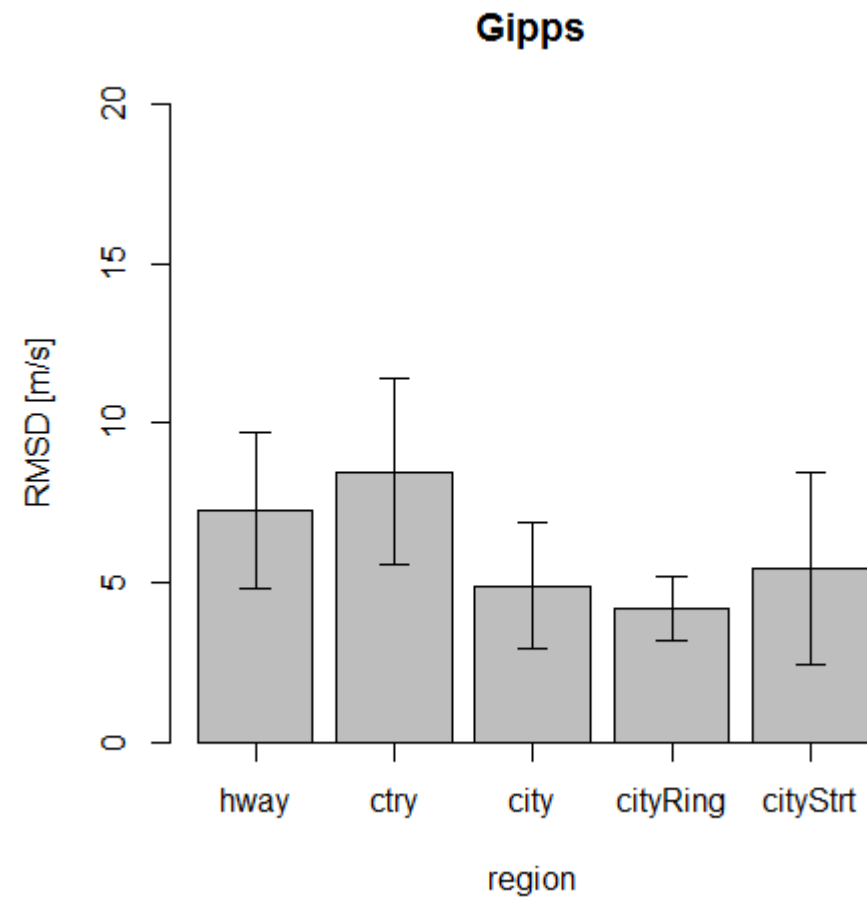
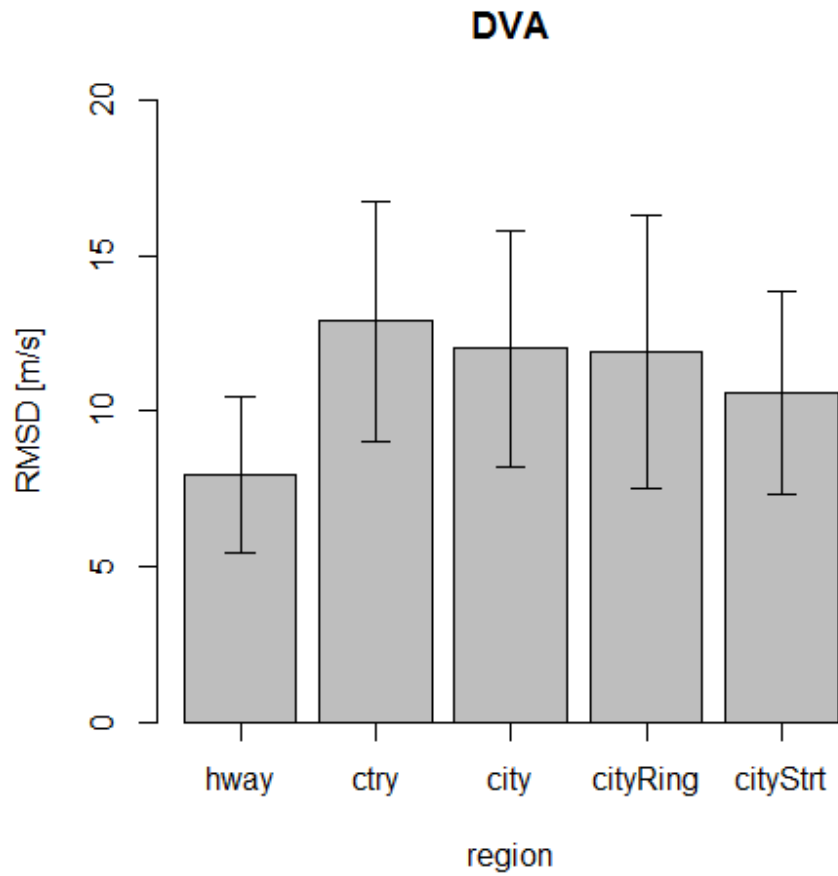


Predictions unoptimized

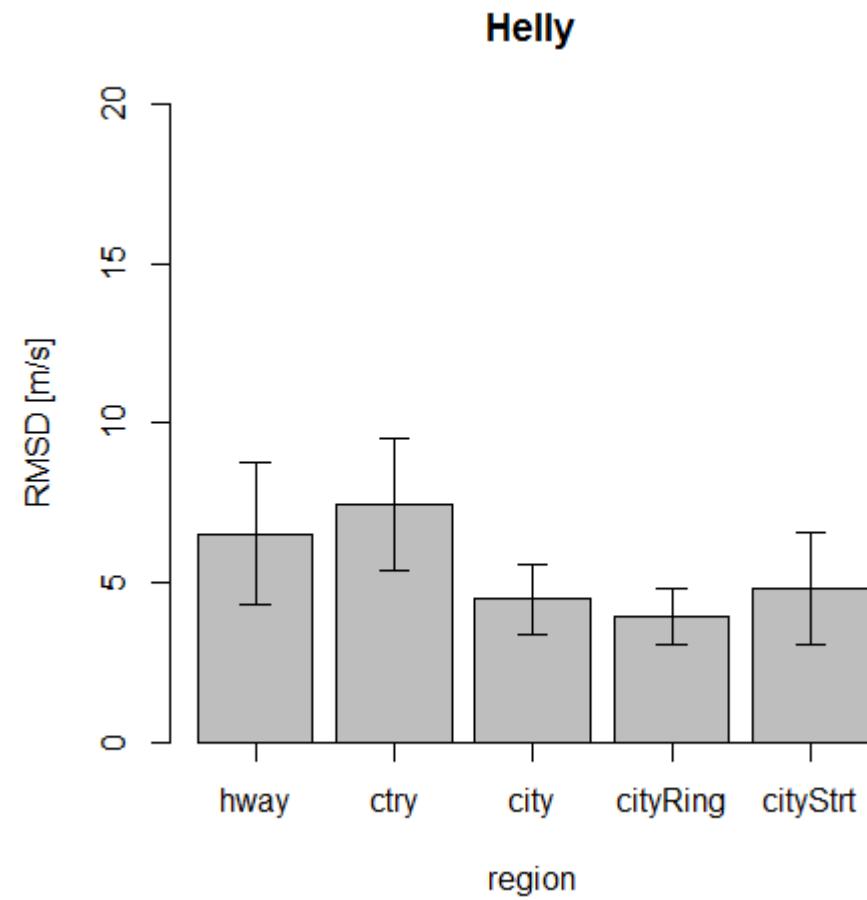
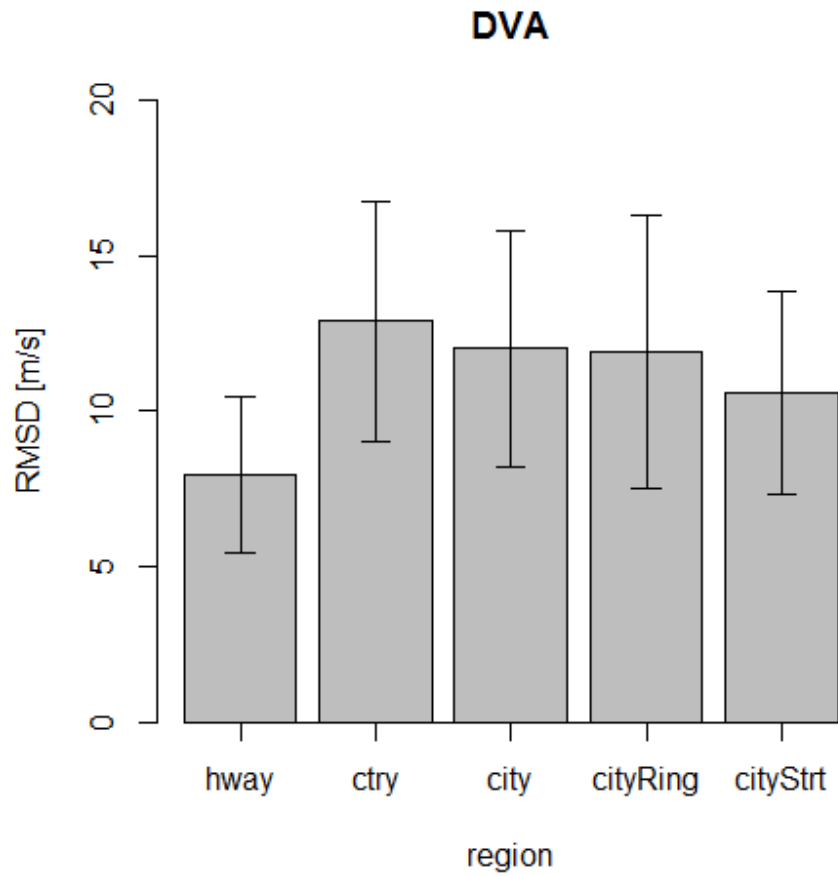
Helly unoptimized, subj 2, city ring



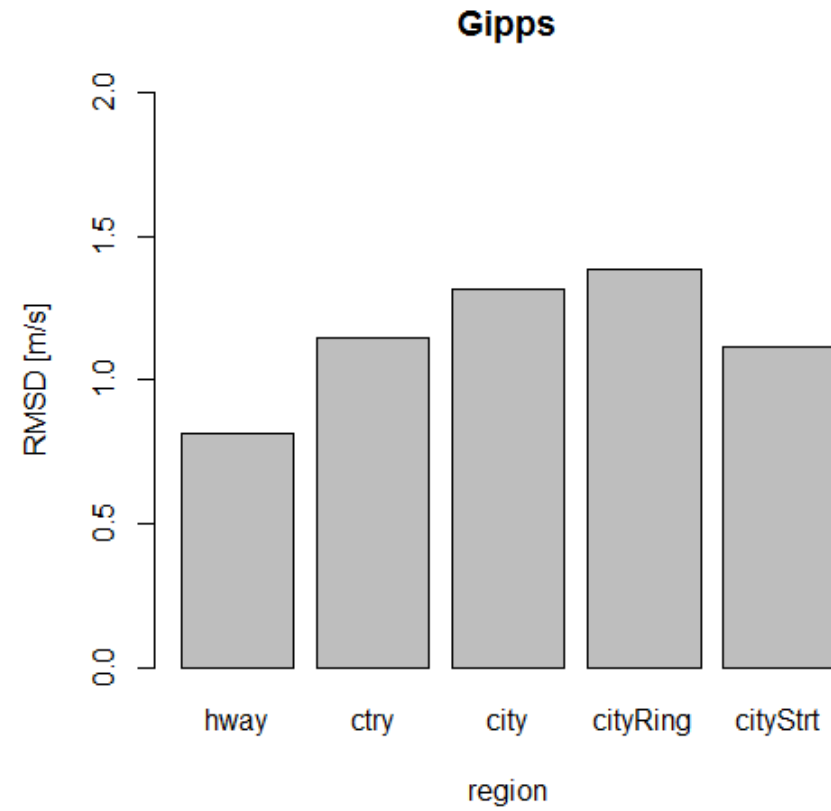
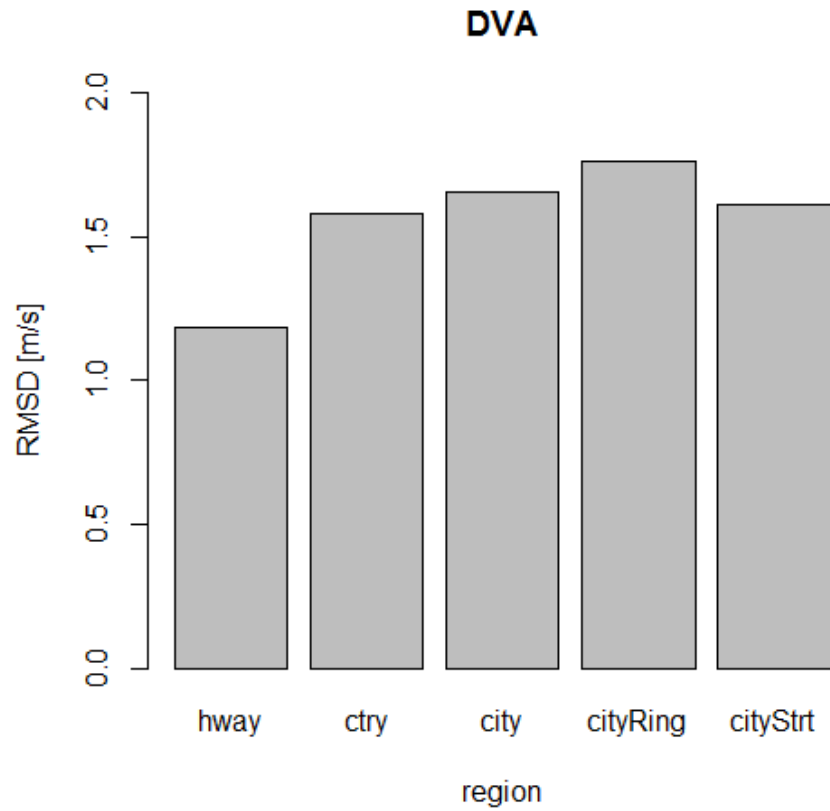
Results constrained, distance



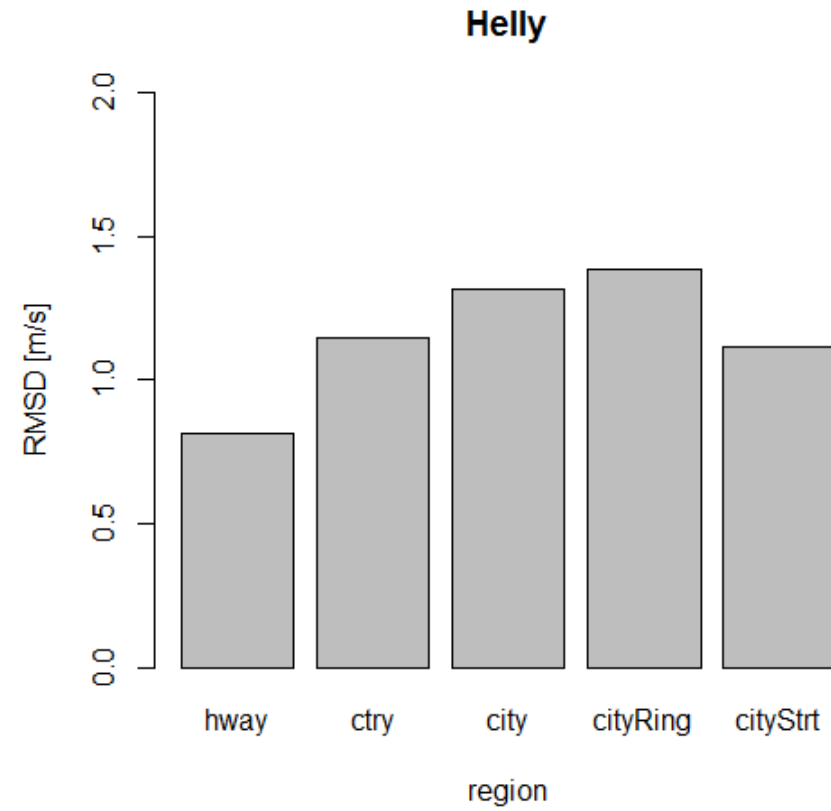
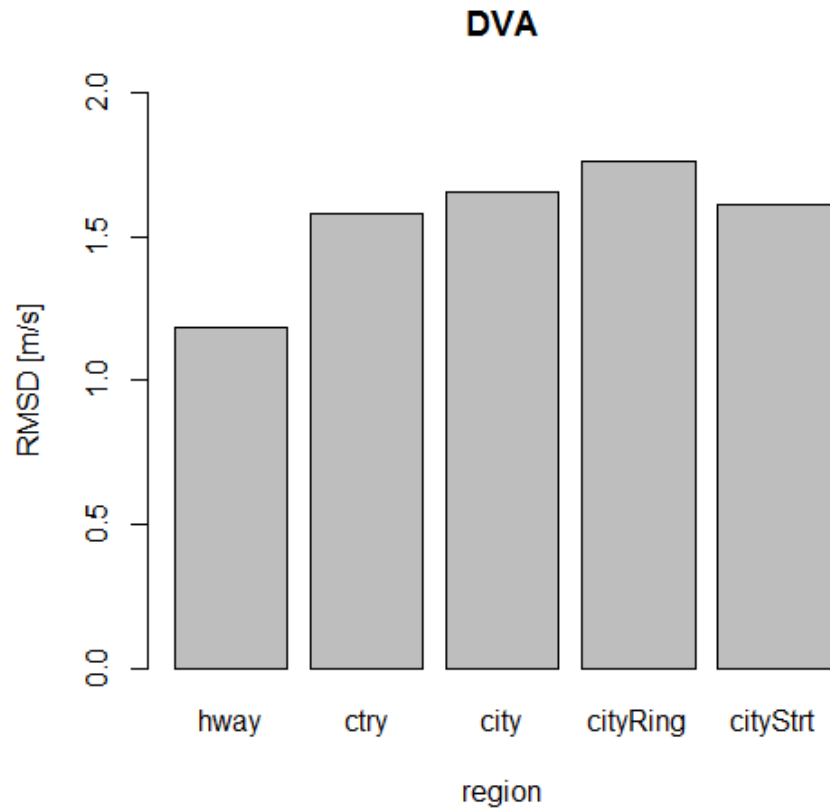
Results constrained, distance



Results unconstrained, speed



Results unconstrained, speed



Discussion

DVA does not hold its promises

- a few psychophysical additions doesn't make it psychologically plausible!
- unstable controller?

degree of psychology in car following controllers

- non-trivial question
- depends a lot on handling of parameters

interaction of parameters and optimization algorithm

- some algorithms are more sensitive to starting parameters than others



Outlook and Lessons Learned

systematic evaluation

- more models
- different driving simulators
- possibly new data collection in the field with better sensors

parameter

- other optimization algorithms
- windowing
- maximum likelihood methods
- bootstrapping
- grid search

more computational power / less precision

- more efficient code
- cluster
- less optimized parameters



Literature

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