A hybrid plasmonic waveguide for subwavelength confinement and long range propagation

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The emerging field of nano-photonics[1] addresses the challenge of manipulating light on scales much smaller than the wavelength although very few practical approaches exist at present. Surface plasmon polaritons (SPP)[2,3] are among the most promising candidates for subwavelength optics[3–10]. However, demonstrations of long-range SPPs have only achieved confinement comparable to that of conventional dielectric waveguides because of practical issues including optical losses and stringent fabrication demands[3,11–13]. We propose a new approach that integrates dielectric and plasmonic waveguiding. The hybrid waveguide consists of a dielectric nanowire separated from a metal surface by a nanoscale dielectric gap. The coupling between the plasmonic and waveguide modes across the gap allows 'capacitor-like' energy storage leading to effective subwavelength transmission. Hybrid SPPs can propagate large distances (40 μm - 150 μm) with strong confinement (λ^2/400 - λ^2/40). The approach is fully compatible with semiconductor fabrication techniques and hence, enables truly nanoscale semiconductor-based plasmonics and photonics.

The need for fast, compact and efficient light sources and detectors with high spatial and temporal resolution has motivated research into optical structures capable of guiding light with deep

subwavelength confinement. Photonic crystals[14–16] have been utilized to guide light, although fundamentally, the confinement is limited to the order of a wavelength in each direction. Subwavelength confinement along one dimension has been shown in all-dielectric coupled Silicon waveguides[17]. This geometry is of fundamental importance in nano-photonics, although the relatively large portion of energy propagating in the surrounding regions may restrict the compactness of the waveguide. On the other hand, plasmonic waveguides can provide subwavelength confinement by storing optical energy in electron oscillations within dissipative metallic regions[2–13,18]. This, however, leads to high optical loss, which is further exacerbated when high permittivity dielectric materials, such as semiconductors, are involved[18]. Consequently, semiconductor-based plasmonics faces a fundamental challenge at telecommunications and visible frequencies.

In this letter, we report a *hybrid plasmonic waveguide* capable of subwavelength confinement in two dimensions with low propagation loss. The hybrid mode can be strongly confined to sizes more than $100\times$ smaller than the area of a diffraction-limited spot, while maintaining propagation distances exceeding those of SPPs of the equivalent high permittivity dielectric-metal interface, which are only confined in one dimension. Moreover, by tuning the geometrical properties of this structure, we can increase the propagation distance up to millimeter range while still maintaining moderate confinement. This approach naturally extends the capabilities of both plasmonics and semiconductor photonics and can be applied to subwavelength laser devices, such as visible nano-lasers[20,21] and Tera-Hertz lasers[22] as well as optically integrated circuits[23].

The hybrid waveguide geometry, shown in Fig 1, consists of a high permittivity semicon-

ductor nanowire[19] ("cylinder waveguide") embedded in a low-permittivity dielectric near a metal surface ("SPP waveguide") [24]. In the following study, we vary the cylinder diameter, d, and dielectric gap width between the cylinder and the metal plane, h, to control the propagation distance, L_m, mode area, A_m, and electromagnetic field distribution of a single hybrid mode at the telecommunications wavelength, $\lambda = 1550$ nm. Figures 2a and 2b show the dependence of propagation distance and normalized mode area, respectively, on d and h using the finite element method (see Methods). For a large cylinder diameter and gap width ($d > 200$ nm, $h > 50$ nm), the hybrid waveguide supports a low loss cylinder-like mode with electromagnetic energy confined to the high-permittivity dielectric core (Fig 2c). Conversely, a small diameter cylinder ($d < 200$ nm) results in an SPP-like mode with very weak localization parallel to the metal surface and suffering loss comparable to that of uncoupled SPPs. At moderate cylinder diameters ($d \simeq 200$ nm), mode coupling results in a new hybrid mode that features both cylinder and SPP characteristics; namely, its electromagnetic energy is distributed over both the cylinder and adjacent metal-dielectric interface (Fig 2d). However, when reducing the gap towards the nanometer scale, the hybrid mode no longer displays characteristics of either the cylinder or the SPP mode; instead, it is strongly confined in two dimensions within the gap (Figs 2e and 2f). What is interesting here is that, despite this strong confinement, the hybrid mode's propagation length exceeds that of SPPs of the equivalent metal-semiconductor interface (Fig 2b).

Evidently, the gap provides the means to store electromagnetic energy leading to subwavelength optical guiding with low mode loss. (See animation in Supplementary On-Line Material.) This is further confirmed by resolving the electromagnetic energy density in more detail (Fig 3).

The proportion of the mode's energy residing within the gap is 15% for h=2 nm (Fig 2e) up to 20% for h=100 nm (Fig 2d), where we define the gap region as the area of low permittivity dielectric directly beneath the cylinder and above the metal. The strong energy confinement in the gap region occurs for two reasons: firstly, it arises from the continuity of the displacement field at the material interfaces, which leads to a strong normal electric field component in the gap[17]; and secondly, in both uncoupled SPP and cylinder geometries, the electric field components normal to material interfaces are dominant, amplifying the first effect. In fact, the dielectric discontinuity at the semiconductor/oxide interface produces a polarization charge[25] that interacts with the plasma oscillations of the metal/oxide interface; i.e. the gap region has an *effective optical capacitance*, similar to that of closely spaced metallic wire and plane.

In order to gain a deeper understanding, we analyzed the dependence of the hybrid mode's effective index, $n_{hyb}(d,h)$, on d and h. Figure 4a depicts the variation of the effective index for the same set of parameters as in Fig 2. Naturally, in the limits of cylinder-like and SPP-like modes, the effective index approaches that of a pure cylinder, $n_{cyl}(d)$, or an SPP, n_{spp}, mode (Fig 4a). At the same time, the hybrid mode's effective index is *always* larger than that of the underlying cylinder and SPP waveguide modes, indicating a behavior typical of a *coupled mode* system with mode "splitting" into symmetric and anti-symmetric hybrid modes[26,27] with effective indices, $n_{\pm}(d,h)$ (see Methods). Interestingly, the lower ('anti-symmetric') branch of the system is "cut-off" as the lower index hybrid mode cannot exist for effective indices, $n_{-}(d,h) < n_{spp}$. The high index ('symmetric') mode is the only bound solution in this geometry for a single mode cylinder waveguide. (Note that hybridization lifts the degeneracy of the cylinder's fundamental

mode and the second mode is cut-off when the coupling is strong.)

Using a coupled mode theory, we can describe the hybrid mode, to a first approximation, as a "superposition" of the cylinder waveguide (without the metallic region) and SPP waveguide (with no cylinder) modes,

$$\psi_{\pm}(d,h) = a_{\pm}(d,h)\psi_{cyl}(d) + b_{\pm}(d,h)\psi_{spp} \tag{1}$$

where $a_{\pm}(d,h)$ and $b_{\pm}(d,h) = \sqrt{1-|a_{\pm}(d,h)|^2}$ are the amplitudes of the constituent cylinder $\psi_{cyl}(d)$, and SPP, ψ_{spp}, modes respectively (see Methods). The square norm of the cylinder mode amplitude, $|a_{\pm}(d,h)|^2$ is a measure of the "character" of the hybrid mode, i.e., the degree to which the guided mode is cylinder-like (or SPP-like).

$$|a_{+}(d,h)|^2 = \frac{n_{hyb}(d,h) - n_{spp}}{(n_{hyb}(d,h) - n_{cyl}(d)) + (n_{hyb}(d,h) - n_{spp})} \tag{2}$$

In this respect, the mode is cylinder-like for $|a_{+}(d,h)|^2 > 0.5$ and SPP-like otherwise (Fig 3b). While the mode character predicts the transition between cylinder-like and SPP-like modes, it also correlates the point of strongest coupling, near $d = 200$ nm, with the minimum of both mode area and propagation distance (Fig 2). At the critical coupling diameter, d_c, the hybrid mode has equal SPP and cylinder characteristics ($|a_{+}(d,h)|^2 = 0.5$) corresponding to the condition $n_{cyl}(d) = n_{spp}$, indicating that polarization charge and plasma oscillations move in phase and maximize the effective optical capacitance of the waveguide. For $d \simeq d_c$, mode areas more than two orders of magnitude ($6 \times 10^{-3} A_0$) smaller than the diffraction limited area in free-space, $A_0 = \lambda^2/4$, are achievable (Fig 2a). As the gap width decreases further, $h \mapsto 0$, we can ex-

pect the reduction in mode area to continue with the propagation distance tending to that of a semiconductor-metal interface, subject to constraints of non-local effects when h is of the order of a few atomic monolayers.

Figure 5 shows a parametric plot of normalized mode area, A_m/A_0, versus normalized propagation distance, L_m/λ, for a variety of plasmonic waveguides. Note that this plot is independent of a waveguide's structural parameters allowing a fair comparison of waveguide geometries. Furthermore, by retaining the absolute values of L_m and A_m this representation provides a more powerful comparative tool than a single-valued figure of merit[30], such as $\simeq L_m/\sqrt{A_m}$. Each trajectory in Fig 5 represents a plasmonic waveguide over the range of a structural parameter; here, we compare the hybrid waveguide with dielectric clad metal NWs[4–6] and metal clad dielectric NWs[5,6]. Waveguides with the best performance have trajectories towards the top left of the plot. Clearly, the hybrid waveguide out-performs the other geometries considered by at least an order of magnitude in propagation length for comparable mode areas. We have also compared the hybrid waveguide with other plasmonic waveguides including wedge and groove structures. (See supplementary online material.) In these cases, the hybrid waveguide also shows longer propagation distances for similar degrees of confinement.

In conclusion, we have proposed a new approach for low-loss deep subwavelength light transport. By controlling the hybridization of the fundamental mode of a dielectric cylinder with the SPP of a dielectric/metal interface, we can simultaneously achieve subwavelength confinement and long propagation. We have further shown that the new hybrid waveguide is superior to

other plasmonic waveguides in the literature. Our hybrid approach enables the integration of high gain semiconductor materials and plasmonics and therefore, it may lead to the implementation of waveguide loss compensation techniques[8,18] as well as other schemes for actively manipulating truly nano-scale optical fields. The potential for single mode operation in conjunction with deep subwavelength mode sizes and long propagation lengths suggests application to subwavelength devices, such as visible nano-lasers and Tera-Hertz lasers as well as optically integrated circuits[20–23].

Methods

Coupled Mode Theory

Coupled mode theory describes the mode hybridization of two uncoupled modes using a 2 dimensional matrix representation. A linear superposition of basis vectors, which here represent the uncoupled SPP (i.e. without cylinder) and one of the degenerate cylinder (i.e. without metallic region) waveguide fundamental modes, defines two possible hybrid modes; $\psi_{\pm}(d,h) = a_{\pm}(d,h)\psi_{cyl}(d) + b_{\pm}(d,h)\psi_{spp}$, where $a_{\pm}(d,h)$ and $b_{\pm}(d,h)$ are the amplitudes of the constituent cylinder $\psi_{cyl}(d) = \{\ 1 \quad 0\ \}^T$ and SPP $\psi_{spp} = \{\ 0 \quad 1\ \}^T$ basis modes respectively. All modes may be characterized in terms of an effective index, which is proportional to the real part of its eigenvalue quantifying the phase velocity in the direction of propagation, $\hat{z}$ (Fig 1). The magnitude of the in plane surface plasmon wavevector, $k_{spp} = n_{spp}k_0$ corresponds to an effective index $n_{spp} = \sqrt{\varepsilon_m\varepsilon_d/(\varepsilon_m + \varepsilon_d)}$ (black broken line in Fig 4a)[2], where k_0 is the free space wavenumber. The effective index of the fundamental cylinder mode, $n_{cyl}(d)$, is calculated using standard analytical means[29] (solid black line in Fig 4a). The modes of the coupled system are characterized by the

system of equations,

$$\begin{pmatrix} n_{cyl}(d) & V(h,d) \\ V(h,d) & n_{sp} \end{pmatrix} \begin{pmatrix} a_{\pm}(d,h) \\ \sqrt{1-|a_{\pm}(d,h)|^2} \end{pmatrix} = n_{\pm}(d,h) \begin{pmatrix} a_{\pm}(d,h) \\ \sqrt{1-|a_{\pm}(d,h)|^2} \end{pmatrix} \tag{3}$$

where $V(d,h)$ is the coupling strength between cylinder and SPP modes and mode amplitude normalization implies $b_{\pm}(d,h) = \sqrt{1-|a_{\pm}(d,h)|^2}$. The mode labels reflect the quadratic nature of the characteristic equation of the coupled mode theory, whose solutions are $n_{\pm} = \bar{n}(d) \pm \Delta(d,h)$, where $\bar{n} = (n_{cyl}(d) + n_{spp})/2$ and $\Delta(d,h)^2 = (n_{cyl} - n_{spp})^2/4 + V(d,h)^2$. The mode amplitude $|a_{\pm}(d,h)|^2$ provides a measure of the "character" of the hybrid mode (Fig 4b), i.e., the degree to which the guided mode is "cylinder-like" (or for $1-|a_{\pm}(d,h)|^2$; "SPP-like"), and is given by,

$$|a_{\pm}(d,h)|^2 = \frac{V(d,h)^2}{(n_{+}(d,h) - n_{cyl}(d))^2 + V(d,h)^2} \tag{4}$$

Eq. (4) can be rewritten in the form presented in the main text (see Eq. (2)) using the solution for $n_{+}(d,h)$ and then equating $n_{hyb}(d,h) = n_{+}(d,h)$.

Definition of Mode Area, A_m and Propagation Length, L_m

The modal area, A_m, is defined as the ratio of the total mode energy and the peak energy density such that,

$$A_m = \frac{W_m}{\max\{W(\mathbf{r})\}} = \frac{1}{\max\{W(\mathbf{r})\}} \iint_{-\infty}^{\infty} W(\mathbf{r}) d^2\mathbf{r} \tag{5}$$

where W_m and $W(\mathbf{r})$ are the electromagnetic energy and energy density respectively (per unit length along the direction of propagation).

$$W(\mathbf{r}) = \frac{1}{2}\left(\frac{d(\varepsilon(\mathbf{r})\omega)}{d\omega}|E(\mathbf{r})|^2 + \mu_0|H(\mathbf{r})|^2\right) \tag{6}$$

While this provides a fair measure of the confinement, the proportion of a mode's energy that propagates within A_m ultimately depends on the field distribution. Generally this is not arbitrarily quantifiable. In the current system for $d = 200$ nm we have estimated this proportion to be more than 25 % for $h = 2$ nm (Fig 2e) up to more than 60 % for $h = 100$ nm (Fig 2d). When interpreting these results, it is useful to note that the value of A_m is also the area of a uniform field distribution carrying the same energy density as the optical mode in question.

In the text, the normalized energy density, $W(\mathbf{r})A_0/W_m$ is plotted in Fig 4. This neatly emphasizes the reciprocal relationship of the peak normalized energy density and the normalized mode area, A_m/A_0.

The propagation length, $L_m = 1/(2\text{Im}\{k_{hyb}(d,h)\})$, where $k_{hyb}(d,h)$ is the complex mode wavevector component in the propagation direction.

Numerical Calculations

The hybrid mode's complex effective index, $n_+(d,h)$, was calculated using the commercial finite element package FEMLab from COMSOL. The eigenvalue solver was used to find modes of the hybrid waveguide. The effective index and propagation distance were determined from the real and imaginary parts of the eigenvalue. The extremities of the calculation region were given scattering properties to mimic the necessary open boundary conditions. A convergence analysis was conducted to ensure that the real and imaginary parts of the effective indices varied by less than 1 %. This corresponded to a calculation region between 4λ and 12λ in the $\hat{x}$-direction and 4λ in the $\hat{y}$-direction, depending upon the diameter, d and gap width, h. ($\lambda = 1550$ nm is the free-

space wavelength.) Convergence of the numerical solution, for asymptotic values of d and h, with analytical solutions (cf. Fig 5) indicates that the meshing, boundary conditions and associated calculation parameters were sound. Rapid convergence was achieved by using the uncoupled cylinder (i.e. without metallic region) effective index as an initial guess for large d followed by successive refinement of the resulting solution for decreasing values of d for each value of h considered.

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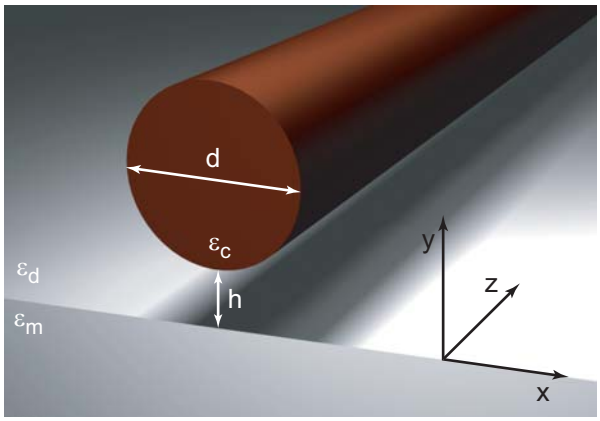
d
ε_c
ε_d
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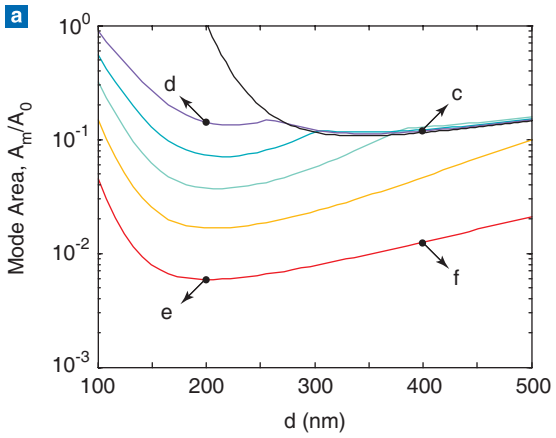
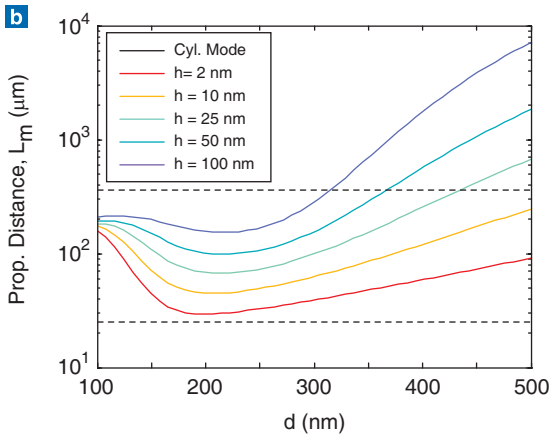
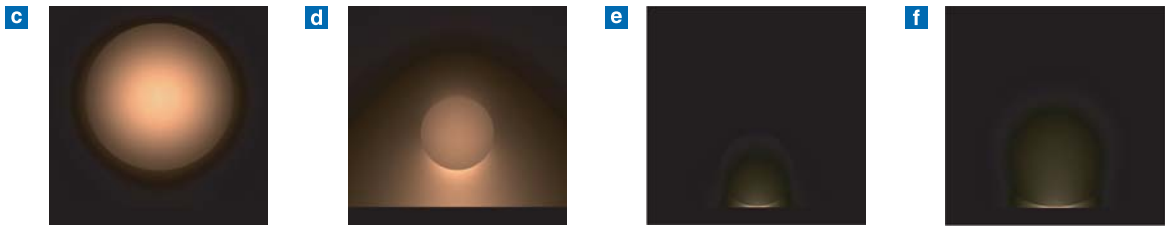
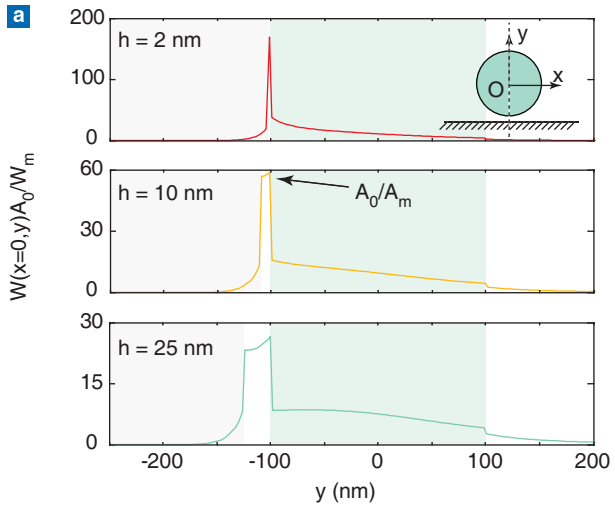
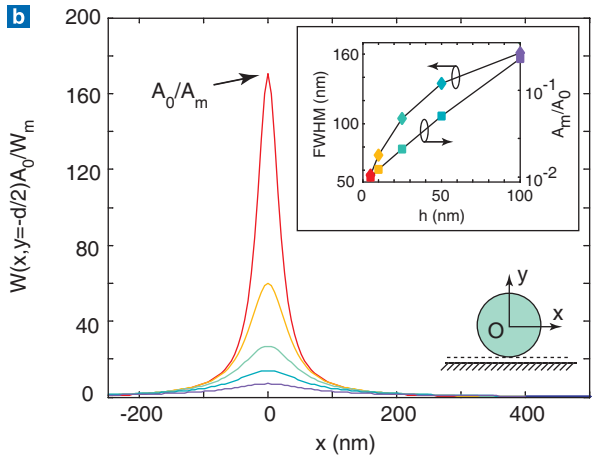
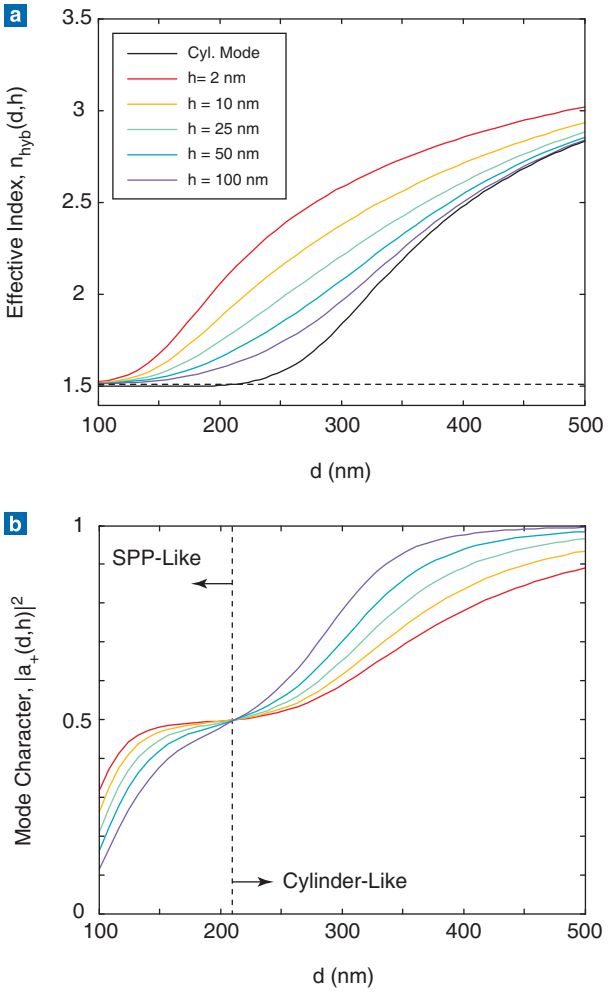

a
Mode Area, A_m/A_0
10^0
10^{-1}
10^{-2}
10^{-3}
100
200
300
400
500
d (nm)
d
c
e
f


b
Prop. Distance, L_m (μm)
10^4
10^3
10^2
10^1
Cyl. Mode
h= 2 nm
h = 10 nm
h = 25 nm
h = 50 nm
h = 100 nm
100
200
300
400
500
d (nm)


c
d
e
f


a
h = 2 nm
h = 10 nm
h = 25 nm
A0/Am
y
x
O
W(x=0,y)A0/Wm
y (nm)


b
A0/Am
FWHM (nm)
Am/A0
h (nm)
y
x
O
W(x,y=-d/2)A0/Wm
x (nm)


a
Effective Index, $n_{hyb}(d,h)$
3.5
3
2.5
2
1.5
100
200
300
400
500
d (nm)
Cyl. Mode
h= 2 nm
h = 10 nm
h = 25 nm
h = 50 nm
h = 100 nm
b
Mode Character, $|a_+(d,h)|^2$
1
0.5
0
SPP-Like
Cylinder-Like
d (nm)

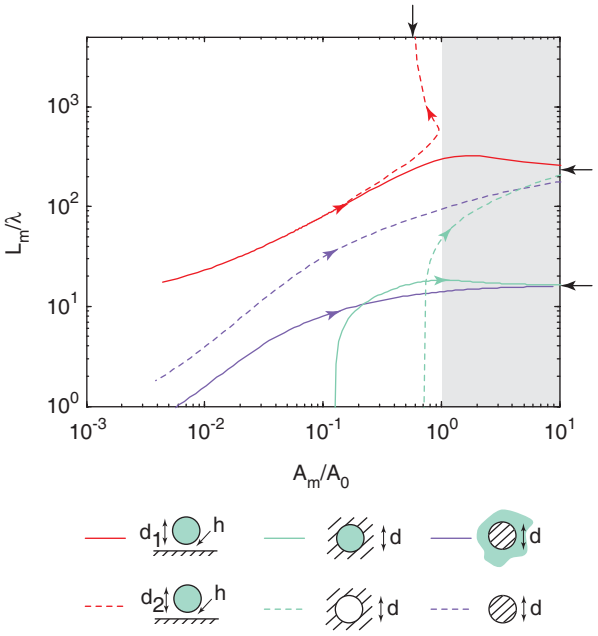

L_m/λ
10^3
10^2
10^1
10^0
10^{-3}
10^{-2}
10^{-1}
10^0
10^1
A_m/A_0
d_1
h
d
d_2
h
d
d

Figure 1 **The hybrid optical waveguide.** A dielectric cylindrical nanowire[19] of permittivity ε_c and diameter d is separated from a metallic half-space of permittivity ε_m by a nanoscale dielectric gap of permittivity ε_d and width h. The upper medium is dielectric of permittivity ε_d. In this letter, $\varepsilon_c = 12.25$ (GaAs) and $\varepsilon_d = 2.25$ (SiO_2) at the telecommunications wavelength $\lambda = 1550$ nm. The metallic region is Silver with a permittivity $-129 + 3.3i$[28]. The center of the cylinder defines the origin ($x = y = 0$).

Figure 2 **Propagation distance, mode area and field distributions of the hybrid mode.** **a** mode area, A_m/A_0, (See Eq. (5)) versus cylinder diameter, d, and gap width, h (colored lines), compared with the mode area of a pure cylinder mode (black line). **b** the hybrid mode's propagation distance (colored lines), compared with those of pure SPP modes at metal/oxide (upper broken black line) and metal/semiconductor (lower broken black line) interfaces. The lower panels show the electromagnetic energy density distributions for **c**, $[d, h] = [400, 100]$ nm; **d**, $[d, h] = [200, 100]$ nm; **e**, $[d, h] = [200, 2]$ nm; and **f**, $[d, h] = [400, 2]$ nm. The legend in **b** applies throughout this letter.

Figure 3 **Confinement in the dielectric gap region in the x and y directions.** **a** normalized energy density along $x = 0$ (broken line in inset) shows the confinement in the low index dielectric region (no shading). The shaded gray and green areas represent the metal and semiconductor regions respectively. **b** the energy density along $y = -d/2$ (broken line in lower right inset) also shows subwavelength localization. The upper right inset shows the

FWHM of the mode along $y = -d/2$ and the normalized mode area, A_m/A_0, as a function of h.

Figure 4 The hybridization of the dielectric cylinder and SPP modes as modeled by coupled-mode theory. **a** The effective index of the hybrid waveguide for a range of gap widths, h, and cylinder diameters, d, (colored lines) compared with the analytical effective indices of pure cylinder, $n_{cyl}(d)$,[29] (black solid line) and pure SPP, n_{spp}, (black broken line) modes. (See Methods.) **b** The cylinder mode character determined from Eqn. 2. When $|a_{\pm}(d,h)|^2 > 0.5$ the mode is "cylinder-like" and when $|a_{\pm}(d,h)|^2 < 0.5$, the mode is "SPP-like". Maximum coupling occurs near $d = 200$ nm where the hybrid mode consists of equal proportions of cylinder and SPP modes, i.e. $|a_{\pm}(d,h)|^2 = 0.5$.

Figure 5 Normalized mode area versus normalized propagation distance enables a comparison of various plasmonic waveguides. Here we compare the hybrid mode (red lines) with dielectric clad Silver NWs[4–6] (blue lines) and Silver clad dielectric NWs[5,6] (green lines). The permittivities of the NW waveguides are ε_d (broken lines) and ε_c (solid lines). A trajectory shows a range of one structural parameter: $h = [1, 10^4]$ nm, $d_1 = 200$ nm and $d_2 = 215$ nm for the hybrid mode. (d_1 and d_2 correspond to two possible asymptotic solutions as $h \mapsto \infty$); $d = [10^1, 10^4]$ nm for the NW waveguides. Arrows indicate increasing waveguide parameter. Black arrows on the right show asymptotic values for the propagation distances of SPPs at Oxide/Silver and Semiconductor/Silver interfaces. The black arrow on top is the mode area for the d_2 hybrid mode for $h \mapsto \infty$.