Assessing the influence of ITZ on the steady-state chloride diffusivity of concrete using a numerical model

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10 ABSTRACT

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12 In this study, the influence of the aggregate-cement paste interfacial transition zone (ITZ) on the steady-state 13 chloride diffusivity of mortars and concretes was examined using a semi-empirical, three-phase composite 14 sphere model. Mortars and concretes were modelled as three-phase composites consisting of the aggregate, bulk 15 cement paste and an inhomogeneous ITZ. The latter was divided into a series of homogenous concentric shell 16 elements of equal thickness. The initial porosity and cement gradients at the ITZ were first estimated from the 17 overall water/cement ratio (w_0/c). The evolution of the porosity, solid hydration products and remnants of 18 unreacted cement were then calculated from the hydration degree and local water/cement ratio (w/c) using 19 Powers' empirical model. Based on the Laplacian equation, an element transfer matrix was derived analytically 20 to predict the steady-state chloride diffusivity. The model was calibrated using available experimental data and 21 then applied to perform a sensitivity analysis to evaluate the effects of aggregate content, water/cement ratio, 22 curing period, ITZ width, maximum aggregate size and aggregate gradation on diffusivity. Some of these 23 variables are impractical to quantify by laboratory experimentation. Implications of the findings with regards to 24 the role of ITZ on mass transport properties are discussed.

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Keywords: Interfacial transition zone (A); diffusion (B); transport properties (B); microstructure (B); modeling
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32 **1. Introduction**

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34 The durability of most concrete structures is determined by their resistance to penetration of external deleterious 35 species, such as chloride ions. Thus, the ability to estimate the transport properties of a concrete from its mixture 36 proportions and microstructure is attractive, as it would assist the development of service life prediction models 37 and durability-based design codes. However, the microstructure of concrete is complex and its transport properties are influenced by many interacting parameters. This study aims to use a numerical model to explore 38 39 the relative influences of these parameters and to determine those having the most significant effect on the steady state chloride diffusivity of concrete. Chloride diffusion was selected as the transport process of interest 40 41 for this study because it is crucial to one of the most widespread and problematic deterioration processes 42 affecting concrete structures, chloride-induced reinforcement corrosion. This particular transport coefficient, i.e. 43 steady state chloride diffusivity as measured in a diffusion cell test, was selected because it is required in 44 mechanistic models of chloride transport that treat chloride ion diffusion and chloride binding separately, but it 45 is extremely time-consuming to measure on representatively thick concrete specimens [1].

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At the most basic level, concrete can be viewed as consisting of aggregate particles distributed in a continuous 47 48 cement paste matrix. Most aggregates used in concrete are dense compared with the paste and so are assumed to 49 allow negligible transport through them. However, the cement paste region surrounding each aggregate particle, 50 i.e. the ITZ, contains higher porosity and lower cement content relative to the bulk cement paste regions farther 51 away and is usually accorded a separate phase. The ITZ occupies a significant fraction of the total paste volume 52 in practical mortars and concretes, and so the property of this phase is expected to have an influence on the 53 overall behaviour of the composite. Indeed, modelling work has found that the ITZ forms an interconnected 54 network even for a modest width of 10-20µm [2], while experimental studies on mortars have observed an increase in the paste porosity due to the presence of the porous ITZs [3]. 55

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However, available experimental studies on mortars and concretes, where the aggregate content is systematically increased to change the ITZ volume fraction, do not provide a clear answer as to whether the ITZ has a significant effect on bulk transport properties [4]. For example, some studies have found that the ITZ has a significant influence on the chloride diffusivity [5, 6], while results from other studies seem to suggest otherwise [3, 7, 8]. These conflicting results from different sources underscore the difficulty in isolating the ITZ effect through experimental studies, where other important parameters that influence transport inevitably vary, whenpreparing and testing samples with different aggregate contents.

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Because a large number of related factors have the potential to influence transport properties, many experiments need to be carried out in order to understand their significance and interactions, and even so, may not be able to isolate all of these effects. In this study, a numerical model is first developed to estimate the chloride diffusivity of conventional concretes. The model is then used to carry out a sensitivity analysis to examine the significance of various parameters, in particular the influence of the ITZ on chloride diffusivity.

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71 **2. Modelling techniques**

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73 2.1. Overview

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75 The microstructure of concrete is inherently complex and variable, so some approximation is inevitable when 76 attempting to model its effect on bulk properties. In this study, we only consider the case of diffusion under 77 saturated and steady-state conditions. To simplify analysis, the aggregates are modelled as polydispersed spheres 78 and the ITZs as shells of certain width that extend from the aggregate particles. The volume fractions of the ITZ 79 and bulk paste are calculated from the ITZ width, aggregate content and size distribution. To model the 80 microstructure development, the initial distribution of cement particles from the aggregate surface is first 81 specified using an empirical equation with the overall water/cement ratio (w_0/c) and ITZ width as parameters 82 that define the shape of the gradient. A hydration model is then executed and the change in phase composition of 83 the ITZ and bulk paste is followed as hydration proceeds. After a desired hydration degree is achieved, the 84 capillary and gel porosity is calculated as a function of distance from the aggregate surface and converted into 85 diffusivity values using a previously derived relationship. These values are then used as inputs into the three-86 phase composite sphere model to estimate the diffusivity of the overall system comprised of the aggregate, ITZ 87 and bulk paste.

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89 2.2. Three-phase composite sphere model

91 A three-phase composite sphere model shown in Fig. 1a is used to represent the concrete matrix, where the inner sphere is the aggregate phase with radius r_a , surrounded by a concentric ITZ shell of width $r_b - r_a$. The ITZ is 92 93 further subdivided into N concentric shell elements of equal thickness, where each shell element is composed of 94 unreacted cement, hydration products and pores. The aggregate and the ITZ shells are embedded in bulk paste 95 matrix of thickness $r_c - r_b$. The shell elements are assumed to be homogeneous and isotropic in composition and 96 transport property. The values of r_a , r_b and r_c are defined such that the volume fractions of the aggregates, ITZ 97 and bulk paste in the model match those values calculated for the actual sample (shown next). This approach of 98 homogenisation at the mesoscale is broadly similar to previous models such as the n-layered spherical inclusion 99 model that has been applied to study elasticity, thermoelasticity, electrical/thermal conductivity and ionic 100 diffusivity of composite materials [9-11]. However, unlike some effective medium based models, the ITZ is not 101 assumed here to be a single shell of uniform property, but the composition and diffusivity of each ITZ shell is 102 allowed to vary with distance from the aggregate surface and with the progress of hydration as shown in Fig. 1b.

103

To determine the volume fractions of the ITZ and bulk paste, the aggregate size distribution is required and this can either be generated from typical sieve analysis, or assumed to follow a particular gradation such as Fuller or Equal Volume Fraction (EVF) that represent the lower and upper bounds of typical aggregate gradation respectively [12]. This can be expressed as

108
$$p(D) = \frac{nD_{min}^{n}D_{max}^{n}}{(D_{max}^{n} - D_{min}^{n})D^{n+1}}$$
(1)

where p(D) is the probability density function for the aggregate distribution in terms of the number of aggregate particles, D is the diameter of aggregate particles, which varies between the minimum aggregate diameter D_{min} and the maximum aggregate diameter D_{max} , and n is a coefficient denoting the type of aggregate gradation (2.5 for Fuller gradation and 3 for EVF gradation).

113

The volume fraction of ITZ is then computed, taking into account the overlapping of ITZ shells in samples containing large aggregate contents. This is carried out analytically using the 'void exclusion probability' derived by Lu & Torquato [13] for the polydispersed spheres system, and as described in Bentz & Garboczi [10]. When applied to our case, the void exclusion probability is basically the volume fraction of the space not occupied by all the spheres and ITZ shells, i.e. fraction of the bulk paste. Accordingly, the ITZ volume fraction

119
$$f_i$$
 for an ITZ width of h can be expressed as

120
$$f_i = (1 - f_a)[1 - \exp(-\pi\rho(t_1h + t_2h^2 + t_3h^3))]$$
 (2)

where f_a is the aggregate volume fraction, ρ is the total number of aggregate particles per unit volume, and t_1 , t_2 and t_3 are coefficients defined in terms of the mean aggregate radius $\langle R \rangle$ and the mean square aggregate radius $\langle R^2 \rangle$, over the entire aggregate size distribution.

124
$$t_1 = \frac{4\langle R^2 \rangle}{1 - f_a}$$
(3a)

125
$$t_2 = \frac{4\langle R \rangle}{1 - f_a} + \frac{8\pi\rho\langle R^2 \rangle^2}{(1 - f_a)^2}$$
(3b)

126
$$t_{3} = \frac{4}{3(1-f_{a})} + \frac{16\pi\rho\langle R\rangle\langle R^{2}\rangle}{3(1-f_{a})^{2}} + \frac{64\lambda\pi^{2}\rho^{2}\langle R^{2}\rangle^{3}}{27(1-f_{a})^{3}}$$
(3c)

127 The parameter λ in Eq. (3c) is equal to 0, 2, or 3, depending on the approximation used in the derivation by Lu 128 & Torquato [13]. However, Garboczi & Bentz [10] observed that the value for λ does not make much 129 difference to the calculated ITZ volume fraction, and the best agreement with numerical simulation results was 130 obtained when $\lambda = 0$. Thus λ is taken as zero in this paper. Once the ITZ volume fraction is known, the 131 volume fraction of bulk paste f_m is obtained by simple subtraction.

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133 2.3. Microstructure and hydration model

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135 To model the microstructure development of the cement paste, we begin by specifying the initial distribution of 136 cement particles at the time of mixing. This was previously estimated by Crumbie [14] who measured the 137 distributions of unreacted cement, porosity and hydration products after various hydration times using 138 backscattered electron microscopy. From these, the initial distribution of the cement particles can be backcalculated and the results for concretes with different w_0/c ratios are reproduced in Fig. 2. Crumbie [14] found 139 140 that the ITZ width is between 20-30µm and that the porosity tends towards 100% at the interface. As expected, 141 the width of the ITZ appears to be related to the cement particle size, but is independent of the aggregate size and 142 w_0/c ratio, although the latter influences the gradient of the cement distribution.

144 Using the data from Crumbie [14], we can approximate the initial distribution of cement particles $f_c(r)$ with the

145 following equation:

146
$$f_{c}(r) = \begin{cases} f_{c,bulk} \sum_{j=1}^{4} (b_{j}/b_{0}) [(r-r_{a})/(r_{b}-r_{a})]^{j}, & r_{a} \le r < r_{b} \\ f_{c,bulk}, & r_{b} \le r \le r_{c} \end{cases}$$
(4)

where $f_{c,bulk}$ is the cement volume fraction in the bulk paste, r is the distance from the centre of the aggregate, r_a , r_b and r_c are as defined in Fig. 1b, b_0 is the sum of b_j (i.e. $b_0 = \sum b_j$) and b_j is a series of empirical

149 functions expressed in terms of w_0/c ratio, obtained from least squares analysis:

$$b_{1} = 4.670 - 5.228(w_{0}/c)$$

$$b_{2} = -10.569 + 12.700(w_{0}/c)$$

$$b_{3} = 9.950 - 12.195(w_{0}/c)$$

$$b_{4} = -3.397 + 4.195(w_{0}/c)$$
(5)

151

The volume fraction of cement in the bulk paste $f_{c,bulk}$ can be calculated from w_0/c ratio, cement density ρ_c and the volume fractions of the bulk paste and ITZ as follows. Consider that the total volume of cement in the composite sphere V_c is the sum of the volume of cement located in the ITZ, $V_{c,ITZ}$, and in the bulk cement paste, $V_{c,bulk}$, i.e.

156
$$V_c = V_{c,IIZ} + V_{c,bulk} = \frac{4\pi (r_c^3 - r_a^3)}{3[1 + \rho_c (w_0/c)]}$$
(6)

157 $V_{c,TTZ}$ can be obtained by integrating Eq. (4) from $r = r_a$ to r_b :

158
$$V_{c,ITZ} = \int_{r_a}^{r_b} 4\pi r^2 f_c(r) dr = 8\pi f_{c,bulk} \sum_{j=1}^4 \sum_{k=1}^3 \frac{b_j r_a^{(3-k)} (r_b - r_a)^k}{b_0 (j+k) [(k-1)!] [(3-k)!]}$$
(7)

159 and $V_{c,bulk}$ is the product of $f_{c,bulk}$ and the volume of the bulk paste:

160
$$V_{c,bulk} = \frac{4\pi (r_c^3 - r_b^3) f_{c,bulk}}{3}$$
 (8)

161 Substituting Eqs. (7) and (8) into Eq. (6) and solving for $f_{c,bulk}$ yields:

162
$$f_{c,bulk} = \frac{(r_c^3 - r_a^3)}{[1 + \rho_c(w_0/c)] \left[(r_c^3 - r_b^3) + 6\pi \sum_{j=1}^4 \sum_{k=1}^3 \frac{b_j r_a^{(3-k)} (r_b - r_a)^k}{b_0 (j+k)[(k-1)!][(3-k)!]} \right]}$$
(9)

Fig. 2 shows that the agreement between Eq. (4) and the data from Crumbie [14]. The correlation coefficients for the regression analysis are 0.9982 and 0.9978 for w_0/c ratio of 0.4 and 0.6 respectively. Note that this approach does not simulate the packing of individual cement grains on the aggregate surface. The cement particles are merely distributed to recreate the gradients measured by Crumbie [14] as a function of w_0/c ratio, but allowing us to treat the ITZ width as a freely variable parameter. With the initial cement distribution described, the local water/cement ratio (w/c) at any point in the ITZ and bulk paste can be determined as follows:

170
$$w/c = \frac{1 - f_c(r)}{\rho_c f_c(r)}$$
 (10)

171

After the initial distribution of the cement particles, simple empirical equations are used to model the hydration reactions between cement and water. The cement particles are allowed to hydrate and the change in phase composition of the ITZ shells and bulk paste is followed with the progress of hydration. The hydration of cement is assumed to occur via a dissolution and precipitation process, and the reaction rates are as described in the model by Parrot & Killoh [15]. In this approach, the rate of hydration of a particular clinker phase $R_{i,t}$ is expressed by a set of three equations below, where the lowest value of $R_{i,t}$ at any time is taken as the rate controlling step and used to calculate the instantaneous degree of hydration:

179 Nucleation and growth:
$$R_{i,t} = \frac{K_1}{N_1} (1 - \alpha_{i,t}) [-\ln(1 - \alpha_{i,t})]^{1 - N_1}$$
 (11a)

180 Diffusion:
$$R_{i,t} = \frac{K_2 (1 - \alpha_{i,t})^{2/3}}{1 - (1 - \alpha_{i,t})^{1/3}}$$
 (11b)

181 Formation of hydration shell:
$$R_{i,t} = K_3 (1 - \alpha_{i,t})^{N_3}$$
 (11c)

where $\alpha_{i,t}$ is the degree of hydration of clinker phase *i* (C₃S, C₂S, C₃A and C₄AF) at time *t* (in days) and K_1 , N_1 , K_2 , K_3 , and N_3 are empirical constants from Parrot & Killoh [15], as listed in Table 1. The degree of hydration at time $t + \Delta t$ is then expressed as:

185
$$\alpha_{i,t+\Delta t} = \alpha_{i,t} + \Delta t R_{i,t}$$
(12)

186 where Δt is the time interval for integration. The overall degree of hydration α is calculated as a weighted 187 average of the degrees of hydration of the clinker phases. For this study, hydration is assumed to occur at room 188 temperature so the effect of temperature on the rate constants is not considered, although this is possible in Parrot & Killoh's model. However the effect of water/cement ratio is accounted for by reducing the degree of hydration by a factor β as follows:

191
$$\beta = \begin{cases} [1+4.444(w/c) - 3.333\alpha]^4 \text{ for } \alpha > 1.333(w/c) \\ 1, \text{ for } \alpha \le 1.333(w/c) \end{cases}$$
(13)

192

As the cement hydrates, the originally water-filled spaces (capillary pores) become progressively filled with hydration products due to increase in total solids volume. However, the main hydration product (C-S-H) also contains pores, i.e gel pores, and these will increase in volume as hydration continues. According to Powers & Brownyard's [16] model (as summarised by Hansen [17]), the volume fractions of capillary f_{cap} and gel pores f_{gel} are related to the water/cement ratio and the degree of hydration, hence the total porosity f_p is:

198
$$f_p = f_{cap} + f_{gel} = \frac{(w/c) - 0.36\alpha}{(w/c) + 0.32} + \frac{0.19\alpha}{(w/c) + 0.32}$$
(14)

199

Note that the above equation was derived using specific values of chemical and physical bound water, and 200 201 chemical shrinkage for the hydration of typical Portland cements under room temperature conditions [17]. Thus, 202 the equation is likely to be less accurate for other systems such as those containing supplementary cementitious materials. Assuming that the hydration products are deposited close to the cement from which they are formed, 203 204 this equation can then be used to calculate the porosity of the ITZ shells and bulk paste at any location and time, 205 from the local water/cement ratio (Eq. 10) and degree of hydration (Eq. 12). Fig. 3 shows an example of the 206 simulated distributions of unreacted cement, capillary and gel pores, and hydration products for a concrete at 0.4 207 w_0/c ratio that has hydrated for 28 days.

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209 2.4. Calculation of chloride diffusivity

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Initially, the ITZ contains a higher water/cement ratio and more porosity than the bulk paste. As the cement hydrates, the porosity is reduced throughout, but remains higher in the ITZ. The previous section described how the porosity can be quantified as a function of distance from the aggregate surface at any time during hydration. The next step is to apply these results to define the diffusivities of the ITZ shells and bulk paste in our composite model (Fig. 1b). 216 Zheng & Zhou [18] presented a semi-empirical equation for the steady-state chloride diffusivity of Portland 217 cement pastes, which was derived by considering the cement paste as consisting of impermeable solids and pore 218 space. By introducing a hypothetical homogeneous medium of non-zero diffusivity and applying the effective 219 medium model described in Koelman & de Kuijper [19], the chloride diffusivity of the cement paste was shown 220 to be a function of the porosity and the diffusivity of chloride ions in the pore solution:

221
$$D_{cp} = \frac{2f_p^{2.75}D_p}{f_p^{1.75}(3-f_p) + 14.4(1-f_p)^{2.75}}$$
(15)

where D_{cp} and D_{p} are the chloride diffusivity of the cement paste and the pore solution respectively. The 222 exponents for porosity are derived from percolation theory [19, 20] and the value 14.4 is a fitting parameter from 223 224 two sets of experimental data for ASTM Type 1 cement pastes with w_0/c ratios ranging from 0.4 to 0.8 [18]. 225 We note that D_p is the only non-measurable parameter in the model and needs to be calibrated with 226 experimental results from neat cement pastes. D_p accounts for pore geometry effects and physico-chemical 227 interactions, and so should be significantly lower than the diffusivity of chloride ions in bulk water $(=2.0\times10^{-1})^{-1}$ ${}^{9}m^{2}/s$ at 20°C) [21]. Eq. (15) has been further tested on three independent sets of experimental data showing 228 reasonably good agreement [18]. It also appears to fit both experimental data obtained by using simple diffusion 229 230 cells or electro-migration.

231

Once the ITZ shells and bulk paste have been assigned with their respective diffusivities, the final step in the model is to derive the effective diffusivity of the composite sphere model by applying a concentration gradient in the radial direction and using a transfer matrix method [9]. For steady-state diffusion, the chloride content $C(r, \phi, \theta)$ in a homogeneous and isotropic medium should satisfy the following governing equation [22]:

$$236 \qquad \nabla^2 C(r, \varphi, \theta) = 0 \tag{16}$$

where ∇^2 is the Laplacian operator in spherical polar coordinates with the origin at the common centre of the spheres; r, φ and θ are the distance from the centre, and the polar and azimuthal angles respectively.

239
$$\nabla^{2} = \frac{1}{r^{2}} \frac{\partial}{\partial r} \left(r^{2} \frac{\partial}{\partial r} \right) + \frac{1}{r^{2} \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial}{\partial \theta} \right) + \frac{1}{r^{2} \sin^{2} \theta} \frac{\partial^{2}}{\partial \varphi^{2}}$$
(17)

240 The aggregate phase is assumed to have zero diffusivity so the radial flux $q(r, \varphi, \theta)$ at the aggregate surface 241 $(r = r_a)$ and at the outer boundary of the composite sphere $(r = r_c)$ can be written as:

242
$$q(r_a, \varphi, \theta) = 0 \text{ and } q(r_c, \varphi, \theta) = \overline{q}_{N+1} \cos \theta$$
 (18)

From the governing Eq. 16 and the boundary conditions in Eq. 18, it can be shown that the general solution for the chloride content and corresponding radial flux in the *i*-th homogeneous spherical shell element are in the form of [22]:

246
$$C(r,\varphi,\varphi) = \left(A_{1i}r + \frac{A_{2i}}{r^2}\right)\cos\theta \text{ and } q(r,\varphi,\varphi) = -\overline{D}_i\left(A_{1i} - \frac{2A_{2i}}{r^3}\right)\cos\theta$$
 (19)

where A_{1i} and A_{2i} are constants that can be determined from the boundary conditions. If the chloride content and radial chloride flux at $r = r_i$ are expressed as $\overline{C_i} \cos \theta$ and $\overline{q_i} \cos \theta$ respectively, substitution of $r = r_i$ and $r = r_{i+1}$ into Eq. 19 yields:

250
$$\overline{C}_{i} = \left(A_{1i}r_{i} + \frac{A_{2i}}{r_{i}^{2}}\right) \text{ and } \overline{q}_{i} = -\overline{D}_{i}\left(A_{1i} - \frac{2A_{2i}}{r_{i}^{3}}\right)$$
(20a)

251
$$\overline{C}_{i+1} = \left(A_{1i}r_{i+1} + \frac{A_{2i}}{r_{i+1}^2}\right) \text{ and } \overline{q}_{i+1} = -\overline{D}_i \left(A_{1i} - \frac{2A_{2i}}{r_{i+1}^3}\right)$$
 (20b)

252 By rearranging Eq. 20 and eliminating A_{1i} and A_{2i} , \overline{C}_{i+1} and \overline{q}_{i+1} can be expressed in terms of \overline{C}_i and \overline{q}_i as:

253
$$\left\{ \begin{matrix} \overline{C}_{i+1} \\ \overline{q}_{i+1} \end{matrix} \right\} = \left[t^i\right] \left\{ \begin{matrix} \overline{C}_i \\ \overline{q}_i \end{matrix} \right\}$$
(21)

254 where $[t_i]$ is a 2×2 element transfer matrix and its four elements are as follows:

255
$$t_{11}^{i} = \frac{r_{i}^{3} + 2r_{i+1}^{3}}{3r_{i}r_{i+1}^{2}}, t_{12}^{i} = \frac{r_{i}^{3} - r_{i+1}^{3}}{3\overline{D}_{i}r_{i+1}^{2}}, t_{21}^{i} = \frac{2\overline{D}_{i}(r_{i}^{3} - r_{i+1}^{3})}{3r_{i}r_{i+1}^{3}}, t_{22}^{i} = \frac{2r_{i}^{3} + r_{i+1}^{3}}{3r_{i+1}^{3}}$$
(22)

By iterating Eq. 22, one can then derive an equation that relates \overline{C}_{N+1} and \overline{q}_{N+1} to \overline{C}_1 and \overline{q}_1 according to the principle of transfer matrix method [23]:

258
$$\left\{ \begin{matrix} \overline{C}_{N+1} \\ \overline{q}_{N+1} \end{matrix} \right\} = [T] \left\{ \begin{matrix} \overline{C}_1 \\ \overline{q}_1 \end{matrix} \right\}$$
(23)

259 where the global transfer matrix [T] is:

260
$$[T] = \prod_{i=1}^{N+1} [t^{(N+2-i)}]$$
 (24)

261 It follows from the boundary condition (Eq. 18) that $\overline{q}_1 = 0$ and thus:

262
$$\overline{q}_{N+1} = \frac{T_{21}\overline{C}_{N+1}}{T_{11}}$$
 (25)

– 10 –

263 If the composite sphere model is considered as a monolithic homogeneous medium with an effective diffusivity 264 D_{con} , it is easily shown that:

$$265 \qquad \overline{q}_{N+1} = -\frac{D_{con}\overline{C}_{N+1}}{r_c}$$
(26)

Finally, by comparing Eq. (25) with Eq. (26), it follows that:

267
$$D_{con} = -\frac{T_{21}r_c}{T_{11}}$$
 (27)

268

269 To apply Eq. (27), it is first necessary to evaluate the effect of the number of ITZ shells, N on the simulation. 270 Obviously, dividing the ITZ into more elements will improve accuracy of the simulation, but at the cost of 271 longer computation time. Fig. 4 shows the effect of N on the calculated diffusivity ratio D_{con}/D_p for concretes 272 with total aggregate volume fraction ranging from 0.2 to 0.8. The simulated concrete has a $w_0/c = 0.5$, aggregate size = 0.15-16mm (Fuller gradation), $h = 35 \mu m$ and curing period of 28 days. It can be seen from Fig. 273 274 4 that in all cases, D_{con}/D_p increases with N up to about N=5. For N>5, D_{con}/D_p achieves a relatively 275 stable value, which suggests that the minimum number of ITZ elements required is about six. As a conservative 276 estimate, we will use N = 10 for all subsequent simulations.

277

278 **3. Results**

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280 3.1. Comparison with previous experimental results

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282 In this section, we compare the simulated diffusivities from the proposed model with two sets of experimental 283 results found in the literature. The first set, from Delagrave et al. [3], consists of three series of mortars. Series 1 was made of French OPC (CPA-CEM I 42.5) at 0.38 w_0/c ratio and 0.3-3mm natural siliceous sand at 0%, 284 285 19% and 57% volume fractions. 10mm thick samples were cured in saturated lime solution for 28 days and then vacuum saturated in a simulated pore solution (0.08M KOH, 0.025M NaOH). The samples were then tested 286 287 using a two-compartment diffusion cell similar to the one described by Chatterji & Kawamura [24], containing 288 0.35M NaCl in the simulated pore solution in the upstream compartment. Chloride concentration in the 289 downstream compartment was periodically measured for 15 months and the effective diffusion coefficient was 290 obtained from the steady-state regime according to Fick's first law. Mortars from Series 2 were made of ASTM 291 Type I cement at 0.45 w_0/c ratio, while mortars from Series 3 were made of ASTM Type III cement at 0.25 w_0/c ratio. Both contained 0.15-0.6mm crushed siliceous sand at 0%, 30% and 50% volume fractions. 15mm 292 293 thick samples from both series were cured in saturated lime solution for 3 months then vacuum-saturated in 294 deionised water and tested using a migration cell technique similar to the one described by Buenfeld & El-Belbol 295 [25]. The upstream compartment of the migration cell was filled with a 0.5M NaCl in 0.3M NaOH solution, and 296 a 10V potential was applied across the cell. The chloride concentration in the downstream compartment was 297 monitored for 3 weeks and the migration coefficient was obtained from the steady-state regime according to the 298 Nernst-Plank equation.

299

The second set of data is from Yang & Su [26], who tested mortars made of ASTM Type I cement at a w_0/c ratio of 0.40. The mortars contained 0.15-4.75mm sand at 0%, 10%, 20%, 30% and 40% volume fractions. After demoulding, the 50mm thick samples were cured in water for 12 months and then vacuum saturated in deionised water. The samples were tested using a migration cell similar to the one described earlier, except that a higher 60V potential was used.

305

To apply the proposed model, the ITZ width, h and the chloride diffusivity in the pore solution, D_p need to be 306 307 predetermined. The ITZ width is known to be related to the cement particle size, and typical values of 20 to 308 50µm have been reported in the literature. Thus, the lower and upper bounds for the simulation can be made by 309 taking h equal to 20 and 50 μ m respectively. In well-hydrated and very dense systems, the ITZ may be very 310 small or even non-existent, so we will simulate the case of a thin ITZ (5µm) for comparison. The chloride 311 diffusivity in the pore solution D_{a} , however, is dependent on many factors such as the materials and mix 312 proportions, hydration degree, test conditions and pore structure. Unfortunately, there is a lack of data to 313 quantify this relationship, so D_p can only be determined by fitting results of neat pastes. This produces the following D_n values: $2.8 \times 10^{-11} \text{m}^2/\text{s}$, $9.5 \times 10^{-11} \text{m}^2/\text{s}$ and $1.9 \times 10^{-11} \text{m}^2/\text{s}$ for Series 1, 2 and 3 respectively [3] and 314 6.2×10^{-11} m²/s for the samples from Yang & Su [26]. As expected, D_p is significantly lower than the diffusivity 315 in bulk water or in simulated pore solutions ($\sim 10^{-10} \text{m}^2/\text{s}$) [27]. 316

318 Fig. 5 compares the numerical simulations with experimental results, which are plotted against aggregate volume 319 fraction. Note that the actual aggregate size distribution and cement composition from the original references 320 were used as inputs to the proposed model. The measured diffusivities range slightly over one order of magnitude, between 1×10^{-13} and 4.5×10^{-12} m²/s. The results show that in all cases, the diffusivity decreases with 321 322 increase in aggregate volume fraction. For samples with w_0/c ratio of 0.38, 0.40 and 0.45 (Figs. 5a, b & d), the 323 measured diffusivities seem to agree well with the estimated values when the ITZ width is taken to be equal to 324 20µm. The errors are between -5% and +3%, except in one instance ($w_0/c = 0.38$, $f_a = 0.55$) where the 325 diffusivity is under-estimated by 26%. For samples with w_0/c ratio of 0.25 (Fig. 5d), the agreement between 326 the measured diffusivity values and the estimated values appear to be reasonable when a smaller ITZ width of 5μ m is assumed. However, the discrepancy here is higher than the previous case, that is -12% and +18% for 327 328 $f_a = 0.3$ and 0.5 respectively. Nevertheless, the smaller ITZ width is consistent with the expectation for this mix, 329 which has the lowest w_0/c ratio.

330

332

A sensitivity analysis was carried out using the proposed model to examine the relative influence of w_0/c ratio, curing period, ITZ width and aggregate volume fraction, size and gradation. We plotted the ratio D_{con}/D_p against aggregate volume fraction for four test cases as described in Table 2, which were designed to examine the effect of changing a particular variable on the simulated diffusivity ratio. Results are shown on separate plots for each test case in Fig. 6, plotted on the same scale to facilitate comparison. The percentage change in D_{con}/D_p due to varying each parameter at the simulated range is also given in Table 3.

339

For all cases, the diffusivity decreases significantly with the increase in aggregate content and samples with large w_0/c ratio and short curing age show the highest change in D_{con}/D_p ratio. For instance, increasing the aggregate content from 0 to 60% decreases the D_{con}/D_p ratio by a factor of three for 0.6 w_0/c , and by a factor of two for 0.4 w_0/c ratio. Fig. 6a shows that a reduction in w_0/c ratio will also cause a significant reduction in D_{con}/D_p , as expected. However, this effect decreases at high aggregate contents. At 0% aggregate, D_{con}/D_p for 345 0.6 w_0/c ratio is about three times that for 0.4 w_0/c ratio, while at 60% aggregate, D_{con}/D_p for 0.6 w_0/c 346 ratio is about twice that for 0.4 w_0/c ratio.

347

For samples with equal w_0/c ratio and aggregate content, D_{con}/D_p decreases with the increase in curing age (Fig. 6b) and this effect is again more pronounced at low aggregate contents. When the sample is cured longer, the effect of further hydration on D_{con}/D_p becomes smaller. This is probably due to the fact that the rate of hydration and pore filling is higher at early ages and that the difference in porosity between the ITZ and the bulk cement paste becomes smaller as hydration proceeds.

353

At equal w_0/c ratio and curing age, increasing the ITZ width results in a small increase in D_{con}/D_p (Fig. 6c). Using a smaller aggregate size and finer gradation (the EVF compared with the Fuller) also increases D_{con}/D_p slightly (Fig. 6d). Nevertheless, comparing Figs. 6 (c & d) with Figs. 6 (a & b), it is evident that the effect of ITZ width and aggregate size on the diffusivity is small compared with aggregate content, w_0/c ratio and curing age.

550

359 **4. Discussion**

360

The proposed model has several limitations due to the approximations used in its development. Although its agreement with some experimental data appears to be good, it is only strictly valid within the assumptions used and is not expected to be generally applicable. The model contains several empirical relationships and requires calibration with experimental data, which also limits its ability to predict the properties of in-situ concrete. Nevertheless, as stated in the Introduction, our main objective here is to use the model to investigate how different parameters affect the diffusivity, which would otherwise be difficult to ascertain from experiments.

367

368 Obviously, real mortars and concretes are far more complicated than the three-phase model presented here. Real 369 aggregate particles are not spheres, and therefore have a larger specific surface and create more ITZ than 370 spherical aggregate particles at the same volume fraction. However, this approximation is not likely to have a 371 huge influence on the estimated diffusivities, as evident from our simulations (Figs. 6c & d).

373 Some studies have shown that the ITZ width is related to the median size of cement particles used. Our model 374 does not simulate the packing of individual cement particles, but it treats the ITZ width as a variable so that we are not restricted here. In addition, the modelled ITZ is not a single shell of uniform property, but has gradients 375 376 extending out to its width, which depends on the initial mixture proportions and evolves with hydration. 377 However, the real ITZ microstructure is spatially variable, its width and microstructural gradients are not 378 exhibited uniformly around each and every aggregate particle. Although its average property taken over many 379 locations shows well-defined gradients, its local property is highly variable. The mobility of calcium ions in 380 solution results in preferential nucleation and growth of calcium hydroxide on the aggregate surface, so that the porosity of the ITZ in many locations may be very low due to the presence of these deposits [28]. In our model, 381 382 this effect is not captured because our approach assumes that the hydration products are always deposited close to the cement from which they form. Bleeding effects may also increase the porosity in other locations. Arguably, 383 384 mapping an averaged property onto every aggregate particle may be a conservative approach, and this merits 385 further investigation.

386

387 Mortars and concretes also contain entrapped or entrained air voids, which are often assumed to play a negligible role in mass transport since they appear isolated, and so can simply be treated as inclusions that dilute the paste 388 389 matrix. Large air voids would also have their associated ITZs, and in certain cases, may be packed very close to 390 aggregate particles. These void-paste ITZs are potentially more porous than the aggregate-paste ITZs, since 391 aggregates can absorb some excess water in the fresh state and release it later for hydration of the surrounding 392 paste. Modelling work by Bentz et al. [29] found that increasing the amount of empty air voids from 0 to 10% 393 caused a small decrease in chloride diffusivity of concrete, suggesting that the dilution effect is more dominant. 394 However, unlike aggregate particles, air voids may not be treated as inclusions with zero conductivity depending 395 on their degree of saturation. Samples exposed to water for long periods may have air voids that are saturated 396 with water. We do not know if these effects are significant or may cancel out, as there has been no systematic 397 experimental study to establish the effect of saturated air voids on diffusivity.

398

399 Structures in service are often cracked due to loading and drying shrinkage, but modelling microcracks and its 400 effect on transport properties is extremely challenging. For samples with high aggregate contents, these localised 401 microcracks could become interconnected, thereby potentially compounding any effect of the ITZ. However, 402 there are some experimental and theoretical studies that show that microcracking has very little effect on diffusion compared with pressure-induced flow [4, 30, 31]. This is because permeability is influenced by pore size, while diffusivity is more dependent on the total porosity, which is not significantly increased by the microcracks.

406

In modelling the transport process, we assumed that all pores are saturated and that the only transport mechanism occurring is diffusion in the steady-state regime, where free and bound chlorides are already in equilibrium. Furthermore, we assumed that chloride diffusion occurs in both capillary and gel pores. This is an approximation because it is reasonable to expect that the larger capillary pores would play a dominating role at early ages. When these become filled with hydration products at later ages, diffusion would then occur via the smaller gel pores.

413

414 Previous modelling and experimental studies, for example Winslow et al., 1994, have shown that ITZ percolates 415 in samples with high aggregate contents. Our model does not explicitly address this, although it takes the ITZ 416 into account. However, whether or not ITZ percolation influences the composite property depends on the 417 contrast between the ITZ property and that of the bulk matrix [32, 33]. Fig. 7 shows the calculated diffusivity 418 ratio between the ITZ and bulk paste, D_{ITZ} / D_{bulk} , for a range of aggregate contents and ITZ widths, for a concrete with w_0/c ratio of 0.6. The ITZ diffusivity is taken as the average diffusivity of all the ITZ shell 419 420 elements. It can be observed that the D_{ITZ} / D_{bulk} ratio increases with aggregate content and ITZ width, but is no 421 more than five in the most extreme case. This contrast is considered low, and is not expected to have a 422 significant effect on the overall property.

423

424 The sensitivity analysis shows that the aggregate volume fraction, w_0/c ratio, and curing age are the most 425 significant parameters, while the ITZ width, aggregate size and aggregate gradation have less influence on 426 diffusivity. This finding agrees well with the study by Bentz et al. [29]. It suggests that the changes in total paste 427 volume and total porosity due to mix design and curing have a more significant effect on diffusivity. Increasing 428 aggregate content produces more ITZ, but this is accompanied by a decrease in total porosity because more paste 429 is replaced by the non-porous aggregate particles. At constant aggregate content, increasing the ITZ width or 430 using a finer aggregate size creates more porous ITZ, but this is balanced by a denser bulk paste (lower w/c431 ratio) as a result of water conservation in the mix. These effects tend to cancel each other so that the overall 432 influence of the ITZ width and aggregate size is negligible within the range examined. Therefore, the influence
433 of ITZ on the overall diffusivity is not significant, despite it being on average more porous and itself having a
434 diffusivity that is several times that of the bulk paste.

435

436 **5. Conclusions**

437

In this study, a numerical method for estimating the steady-state chloride diffusivity of mortars and concretes 438 439 was presented. Mortars and concretes were approximated as three-phase composites representing the non-porous aggregate, bulk cement paste and an inhomogeneous ITZ. The model was calibrated using experimental data and 440 441 then applied to examine the influence of several parameters on diffusivity. It was found that the chloride 442 diffusivity decreases with increase in aggregate volume fraction, curing period and maximum aggregate diameter, 443 but increases with increase in w_0/c ratio and ITZ width. The most significant parameters however, were the 444 aggregate content, w_0/c ratio and curing age, which control the total porosity of the composite. The net effect 445 of the ITZ on the overall diffusivity was actually small, although its porosity and local diffusivity are higher than those of the bulk paste. This indicates that diffusivity is governed by the volume fraction and microgeometry of 446 the entire pore structure within the cement paste, and not just that within the porous ITZ. 447

448

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450

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- 545 Type 1 cement cured for 28 days.
- 546

547 Table 1 Parameters used for calculating the hydration of clinker phases for ordinary Portland cement as a

548 function of time, from Parott & Killoh [15]

Parameter	Clinker phase				
	Alite	Belite	Aluminate	Ferrite	
K_1	1.5	0.5	1.0	0.37	
N_1	0.7	1.0	0.85	0.7	
<i>K</i> ₂	0.05	0.006	0.04	0.015	
<i>K</i> ₃	1.1	0.2	1.0	0.4	
N_3	3.3	5.0	3.2	3.7	

550

551 Table 2 Experimental design for sensitivity analysis

Test case	Simulation parameters					
	w_0/c	Curing period, t (d)	ITZ width, <i>h</i> (µm)	Aggregate D_{max} (mm) & gradation	Aggregate fraction, f_a	
(a)	0.4, 0.5, 0.6	28	35	16 (Fuller)	0-0.6	
(b)	0.5	3, 7, 14, 28, 56	35	16 (Fuller)	0-0.6	
(c)	0.5	28	5, 10, 20, 35, 50	16 (Fuller)	0-0.6	
(d)	0.5	28	35	8, 16, 32 (Fuller) 16 (EVF)	0-0.6	

552

553

Table 3 Results from the sensitivity analysis showing the percentage change in D_{con}/D_p

	Domonotor	Simulated manage	Percentage change in D_{con}/D_p		
Parameter		Simulated range —	$f_a = 0$	<i>f</i> _{<i>a</i>} =0.6	
1.	w_0/c ratio	0.4 to 0.6	+ 186	+ 134	
2.	Curing period	3 to 56 days	- 59	- 42	
3.	ITZ width	5 to 50µm	0	+ 27	
4.	Aggregate volume fraction	0 to 0.6	- 1	- 153	
5.	Maximum aggregate diameter	8 to 32mm	0	- 14	
6.	Aggregate gradation	EVF to Fuller	0	+ 19	

555



Fig. 1 Schematics of the three-phase composite sphere model used to represent concrete. The various dimensionsand notations used in the model are shown.



560 Fig. 2 Initial distribution of cement particles from aggregate surface at different water/cement ratios. Data is

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564 aggregate size: 0.15-16mm, $h=25\mu m$)



Fig. 4 Effect of the number of ITZ elements on the calculated diffusivity ratio D_{con}/D_p for various aggregate volume fractions, f_a ($w_0/c = 0.50$, ITZ width = 35µm, curing period = 28 days, aggregate gradation = 0.15-16mm, Fuller). The simulation shows that N = 10 is sufficient to obtain representative results.





(a) Series 1 w_0/c 0.38 (from Delagrave et al [3])

(b) Series 2 w_0/c 0.45 (from Delagrave et al [3])



(c) Series 3 w_0/c 0.25 (from Delagrave et al [3])



570 Fig. 5 Comparison between the numerical simulation results with experimental results of Delagrave et al. [3] and

⁵⁷¹ Yang & Su [26].



Fig. 6 Results from sensitivity analysis showing the effect of a) w_0/c ratio, b) curing period, c) ITZ width and d) aggregate maximum size and gradation, on the simulated D_{con}/D_p



576 Fig. 7 Effect of ITZ width and aggregate content on D_{ITZ}/D_{bulk} ratio for a concrete with w_0/c 0.6 and ASTM

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