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Original Citation:

Gallana, Luca; Fraternali, Federico; Iovieno, Michele; Fosson, Sophie Marie; Magli, Enrico; Opher, Merav; Richardson, John D.; Tordella, Daniela (2016). *Voyager 2 solar plasma and magnetic field spectral analysis for intermediate data sparsity*. In: [JOURNAL OF GEOPHYSICAL RESEARCH. SPACE PHYSICS](#), vol. 121 n. 5, pp. 3905-3919. - ISSN 2169-9380

Availability:

This version is available at : <http://porto.polito.it/2649633/> since: September 2016

Publisher:

American Geophysical Union

Published version:

DOI:[10.1002/2015JA021830](https://doi.org/10.1002/2015JA021830)

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Supporting Information for "Voyager 2 solar plasma and magnetic field spectral analysis for intermediate data sparsity"

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Introduction

This supporting information document is to give information about the software we use for the spectral estimation from gapped Voyager datasets. All the software is made of Fortran90 routines, except the *compressed sensing* method which is implemented in the Matlab environment (the complete script is reported below). All the Fortran routines can be downloaded from our research group website <http://areeweb.polito.it/ricerca/philofluidsoftware.html>, where one can also find detailed instruction for the use of the codes. In the following we report a list of the routines and a brief description.

Fortran routine for the generation of synthetic datasets

This code can be used to generate synthetic turbulence datasets from imposed spectral properties. Uniformly distributed random phases are chosen before the inverse transform operation is performed. The code makes use of the C06GBF, C06FBB, C06FAF routines from the NAG library (not open-source). Another small Fortran routine is provided to project the same gap distribution of the Voyagers data onto the synthetic sequences.

Fortran routine for data interpolation and computation of the two-points correlations

This code reads the plasma and magnetic field data, computes average quantities, magnetic field in Alfvén variables and average plasma parameters. Following, the two-point correlation functions are computed, after linear interpolation of the data on a uniform time grid with the same Δt as the spacecraft data. A subroutine is dedicated to find

the best alignment with the original points in order to reduce errors when spectra are computed. The full correlation tensors can be computed (autocorrelations and cross correlations of velocity and magnetic field). To deal with large data sets, this code can be used with multiple threads by the *OpenMP* interface.

Fortran routines for computation of power spectra

This routines compute the power spectral density (PSD) of all the field components either from the correlation functions or directly from reconstructed datasets. The codes use the *dffti*, *dfftf*, *dfftb* routines from the FFTPack libraries (open source, see <http://www.netlib.org/fftpack/> for further details). Different subroutines are also included for spectral smoothing.

Fortran routines for averaged spectra from data subsets

This code can be used to compute averaged spectra. From the total period analyzed, different "continuous" subsets are identified. A continuous subset is defined as a sequence of data containing gaps below a certain threshold (called T_g , see the main text), which is an input parameter of the code. Given this threshold, the number of continuous subsets is uniquely identified. These sequences are linearly interpolated (if $T_g > \Delta t_{sampling}$) on a uniform time grid and the Fourier transform is computed. Before the FFT is performed, some techniques may be applied, such as data windowing (Hann or Welch windows) or detrending. All the computed spectra are then averaged. The codes use the *dffti*, *dfftf*, *dfftb* routines from the FFTPack libraries.

Fortran routines for the maximum likelihood recovery

This set of five routines implement the maximum likelihood recovery method published by Rybicki & Press (1982). This code is derived from routines published on their webpage <http://www.lanl.gov/DLDSTP/fast/> which we modified to apply to the Voyager solar wind datas. The method reconstructs the data with a minimum variance recovery plus a stochastic component. So, the resulting reconstruction is constrained by the data where the data are present, while it is stochastic in the gaps, with the same second order statistical properties of the data. Since the recovery is not deterministic, different realizations can be obtained. The reconstruction is based on a correlation function, which has to be given as an input. We use the correlation function $\rho(\tau)$ computed from linearly interpolated data. Since the code involves operations such as eigenvalue/eigenvector computation of the correlation matrix, as well as matrix inversions, the correlation function has to be quite smooth. This requirement holds for lag times τ below a certain threshold τ_{max} so only data segments of size below τ_{max} can be recovered at a time. For this reason the input dataset is split into subsets. Since usually the biggest gap is shorter than τ_{max} , the entire dataset can be reconstructed. The user can choose to recover the global dataset or only some subset of it. Parameters of the code are related to the segmentation, for the details we refer to the software user guide in our group webpage. This code uses the *DSYSV*, *DGEMV*, *DSYTRF*, *DSYTRI* routines from the LAPACK libraries (open source).

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Matlab script for compressed sensing spectral estimation

The following Matlab script implements the *compressed sensing* algorithm for the power spectrum estimation. The numerical solution is obtained by the SPGL1 solver (<https://www.math.ucdavis.edu/~mpf/spgl1/>) in the Fourier framework. This script is for a three-components field.

```
clear all
close all
clc

%addpath spgl1-1.8/
dd=load('dati_U_hires_2008.0_2008.2.txt');
% file format: [time(s), U1, U2, U2]
tot_run=1; % =n splits the data in n segments
and computes averaged output
sigma=0.01;% noise parameter for bpdn
step=192; % data sampling time (sec)

nn=size(dd,1); % change nn if you want to
%read only the first nn point of file

d(:,1)=dd(1:nn,1)- dd(1,1);
d(:,2)=dd(1:nn,2)-mean( dd(1:nn,2) );
d(:,3)=dd(1:nn,3)-mean( dd(1:nn,3) );
d(:,4)=dd(1:nn,4)-mean( dd(1:nn,4) );

time=zeros(1,size(d,1));
time(1)=1;
for h=2:nn
gap(h-1)=round((d(h,1)-d(h-1,1))/step);
time(h)=time(h-1)+gap(h-1);
end

L=floor((floor(max(time)/tot_run))/2)*2
% L must be even
Vr=zeros(L/2, tot_run);
Vt=zeros(L/2, tot_run);
Vn=zeros(L/2, tot_run);

Vr_recovered=zeros(L, tot_run);

K=zeros(tot_run,1);
for run=1:tot_run
disp(run);
[~,ei]=min(abs(time-(L*(run-1)+1)));
[~,es]=min(abs(time-run*L));
window=[ei:es];
r=time(window)-time(window(1))+1;
K(run)=length(window);

% BASIS PURSUIT DENOISE

opA = @(x,mode) partialFourier(r,L,x,mode);
```

```
% This is now "A"
opts = spgSetParms('verbosity',0);
z = spg_bpdn(opA,d(window,2),sigma, opts);
% if one want to use bp instead of bpdn
%z = spg_bp(opA,d(window,2), opts);
% power spectrum
Vr(:,run)=K(run)*step*(abs(z(1:L/2))).^2;
z = spg_bpdn(opA,d(window,3),sigma, opts);
%to check the correct recovery of input points
inverset2=ifft(z)*sqrt(L);
inverset1=partialFourier(r,L,z,1);
Vt(:,run)=K(run)*step*(abs(z(1:L/2))).^2;
z = spg_bpdn(opA,d(window,4),sigma, opts);
Vn(:,run)=K(run)*step*(abs(z(1:L/2))).^2;
clear r

end

figure(1),hold on
plot(time(1:end),inverset1,'ob')
plot(time(1:end),d(:,3),'+r')
plot(time(end):-1:1,inverset2,'+c')

f=[1:L/2]'/(step*L) %frequencies
Vr_mean=sum(Vr,2)/sum(K);
Vt_mean=sum(Vt,2)/sum(K);
Vn_mean=sum(Vn,2)/sum(K);
BP=[f, 2*Vr_mean, 2*Vt_mean, 2*Vn_mean, ...
2*(Vr_mean+Vt_mean+Vn_mean)];

%save('OUTPUT_CS.txt','BP', '-ascii');
figure(2)
loglog(BP(:,1), BP(:,5),'*r')
xlabel('f (Hz)');
ylabel('PSD |U|');
```

Correlations from lacunous datasets

Figure 1 shows the two-time correlations obtained from the synthetic dataset *Synt1* to which the same gaps of Voyager 2 data (1979, DOY 1–180) have been applied. The presence of gaps produces oscillations in the number of the couples of data available for the computation of the correlation, which in turn generate spurious oscillations in the correlation function. An interpolation is able to significantly reduce this effect.

As a consequence of the bias in the computation of the correlations, the spectrum becomes flatter. Table 1 shows the spectral exponents obtained from the Blackman-Tukey (BT) method (with and without prewhitening). The use of a prewhitening filter can improve the results of the BT method, especially in the high-frequency range, but the spectra are still affected by spurious peaks and biased values of the spectral index (see table 1). However, the values $k = 0.6$ suggested in the literature does not yield the best result, and there is no way to determine *a priori* a suitable value.

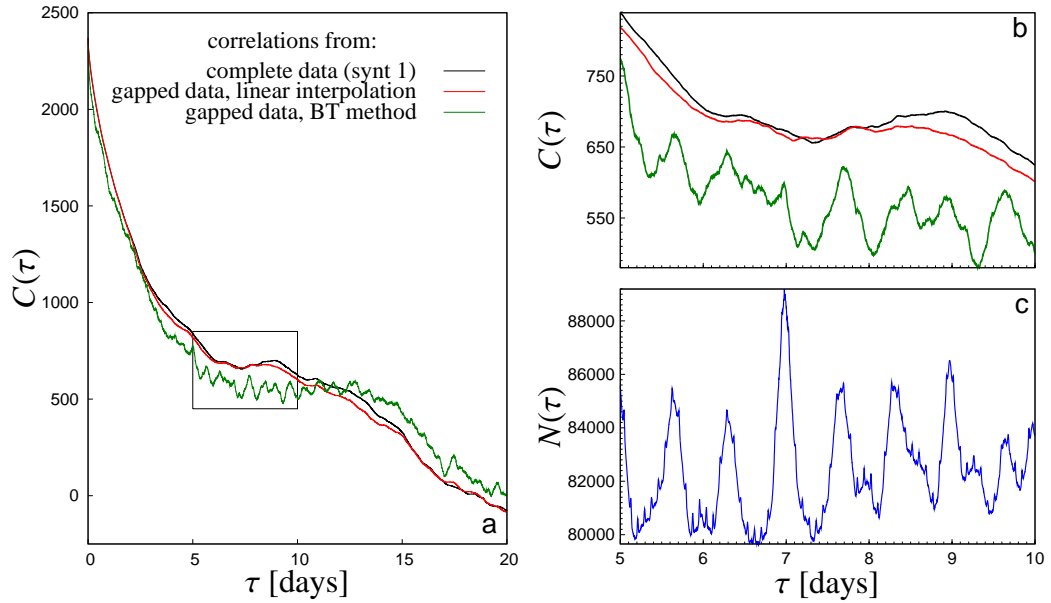


Figure 1. Influence of the missing data on the computation of the correlation. (a, b) Two-point correlation function computed from synthetic data. Black curve: correlations computed from the complete data-set *Synt1* (without any gap). Red curves: correlations computed from the gapped dataset after linear interpolation (the same gap distribution as in V2 data has been applied to the synthetic data-set). Green curves: correlations computed with the BT method (as in [Matthaeus & Goldstein [1982]]). The rectangle in panel (a) evidences the 5-days period shown in panel (b) to highlight the differences between the two approaches and the correct result. (c) The number $N(\tau)$ of available pairs $(X(t), X(t + \tau))$ of data at lag τ is shown in the same range as panel (b). The fluctuations of N , due to the presence of gaps, have a large influence on the correlation function and, therefore, on any method with uses the correlations to compute the spectra.

Table 1. Spectral slopes from different correlation methods and different values of prewhitening parameter k for the **Synt1** and **Synt2** datasets.

<i>Synt 1</i> dataset						
f [Hz]	original	corr+lin. interp	BT, k = 0.00	BT, k = 0.60	BT, k = 0.80	BT, k = 0.99
$10^{-5} \div 5 \cdot 10^{-4}$	-1.66±0.004	-1.70±0.005	-1.41±0.005	-1.48±0.005	-1.66±0.005	-1.77±0.003
$5 \cdot 10^{-4} \div 5 \cdot 10^{-3}$	-1.67±0.003	-1.70±0.003	-1.03±0.001	-2.01±0.001	-1.98±0.001	-1.77±0.002
<i>Synt 2</i> dataset						
f [Hz]	original	corr+lin. interp	BT, k = 0.00	BT, k = 0.60	BT, k = 0.80	BT, k = 0.99
$10^{-5} \div 5 \cdot 10^{-4}$	-1.70±0.005	-1.75±0.003	-1.44±0.005	-1.51±0.005	-1.66±0.005	-1.80±0.003
$5 \cdot 10^{-4} \div 5 \cdot 10^{-3}$	-3.15±0.002	-3.05±0.004	-0.88±0.002	-2.11±0.003	-2.39±0.003	-2.49±0.001