# MPRA <br> Munich Personal RePEc Archive 

# Non-linear adjustment in law of one price deviations and physical characteristics of goods 

Berka, Martin
Massey University, Department of Commerce

November 2006

Online at http://mpra.ub.uni-muenchen.de/8606/ MPRA Paper No. 8606, posted 07. November 2007 / 01:25

# Non-linear adjustment in law of one price deviations and physical characteristics of goods 

Martin Berka<br>Department of Commerce, Massey University*


#### Abstract

At the level of individual goods, heterogeneity in marginal transaction costs, proxied by price-to-weight and price-to-volume ratios, together with measures of pricing power within industries, explains a large part of the variation in thresholds of no-adjustment as well as in conditional half-life of law of one price deviations. Prices of goods that are more heavy or voluminous deviate further before becoming mean-reverting. Moreover, after becoming mean-reverting, prices of heavier (more voluminous) goods converge more slowly. Size of the market is also important in explaining threshold heterogeneity. These factors explain up to $60 \%$ of the variation in no-adjustment threshold estimates across 49 goods in US-Canada post Bretton Woods monthly CPI data.

These results open two avenues for the importance of marginal transaction costs in accounting for real exchange rate persistence: first through generating persistence in individual real exchange rate components, and second by accentuating persistence in the process aggregation of heterogeneous components (the "aggregation bias" of Imbs, et. al. 2005). They also highlight the relevance of theoretical modeling of transaction frictions for understanding real exchange rate persistence.

Keywords: Law of One Price Deviations, Real Exchange Rate Persistence, NonLinearities, transaction costs, Physical Weight, Physical Volume, Threshold Autregressive Models


JEL Classification: F36, F31

[^0]
## 1 Introduction

This paper shows that the non-linear behaviour of differences in prices of traded products between Canada and US is significantly related to the marginal shipping costs proxied by the physical characteristics of the products. Estimates of thresholds in law of one price deviations for goods are significantly negatively related to price-to-weight ratios and price-to-volume ratios of the same products. Size of the market is also important in explaining threshold heterogeneity: goods with smaller market shares tend to have wider thresholds. These factors explain up to $60 \%$ of the variation in threshold estimates. Furthermore, estimates of half-lives of convergence outside of said thresholds are also significantly negatively related to price-to-weight ratios and stowage factors. Not only do price differences of goods goods that are relatively heavier deviate further before becoming mean-reverting, price differences also persist longer outside of said thresholds.

These results suggest existence of two channels through which marginal shipping costs generate persistence in price deviations of traded goods: directly through "iceberg costs" and indirectly by affecting optimal decisions for the mode of transport. Due to the heterogeneity in the marginal shipping costs of traded goods, the two effects can be respectively detected in the heterogeneous thresholds of price deviations as well as in the heterogeneous conditional half-lifes. Consequently, detailed modeling of marginal shipping costs as an empirically important avenue for explaining persistence and volatility of price deviations ${ }^{1}$.

The empirical framework in this paper is based on the role that transaction costs play in impeding arbitrage. Many theories of international price deviations rely on the existence of sticky prices in an environment with real rigidities. Such theories explicitly assume limits to arbitrage, implying very large transaction costs. In the extreme case, markets in such models are segmented in the presence of local currency pricing by firms and households cannot arbitrage away price differences (e.g., Betts and Devereux (2000)). Trade and open macro models often link differences in prices to transportation frictions by assuming that a form of shipping costs is added to the price of the product at the point of origin (or,

[^1]equivalently, that a fraction of the product's value disappears in the course of transport). Even with market segmentation and pricing to market these theories frequently include a condition $p_{i t}=p_{i t}^{*} /(1-\tau)$ where $p_{i t}$ is a c.i.f. price of good $i$ at time $t$ in home country (measured at factory gates), $p^{*}$ is price of the same good abroad and $\tau$ is an iceberg shipping cost (Obstfeld \& Rogoff (2000), Novy (2006)). The above condition is observationally equivalent to arbitrage condition at the level of factory gate prices.

Hecksher (1916) showed the importance of arbitrage for sustainability of price deviations in his calculation of the "commodity points". In a modern application of that idea, Obstfeld and Taylor (1997) found that such commodity points were visible in the non-linearity of deviations in sectoral law of one price deviations when estimated by threshold-autoregressive (TAR) models. Their estimates of non-linear threshold are positively related to distance and exchange rate volatility, both measures of transaction costs. Zussmann (2002) finds that tariffs also determine the width of the no-arbitrage band. Imbs et. al. (2003) confirm these results and show existence of a similar relationship between transaction costs and conditional half-lives of deviations in prices outside the thresholds. All studies find heterogeneity across sectors in threshold estimates or estimates of conditional half-lives.

This paper argues that, at the level of individual goods, marginal shipping costs vary in proportion to the "relative value" of goods, i.e., their price-to-weight or price-to-volume ratios. The key insight is that physical characteristics of goods matter in shipment (the dependance of freight rates on weight and volume relative to their price has been documented by Hummels 1999, 2001). Ceteris paribus, trade friction create a smaller ad-valorem wedge for goods that are lighter or less voluminous relative to their price (high-valued products). Conversely, goods with large volume or weight relative to their price sustain larger deviations before the price difference justifies shipment ${ }^{2}$. To the extent that the heterogeneity in price deviations across goods and services contributes to the dynamics of aggregate real exchange rates (e.g., through the "aggregation effect" in Imbs et. al. (2005)), marginal shipping costs are also important for explaining the persistence and volatility components of the PPP puzzle.

[^2]The remainder of the paper is structured as follows: section 2 outlines the idea, section 3 discusses the data, section 4 presents the results and section 5 concludes.

## 2 Arbitrage

Many open macro (Novy 2006) and trade (Hummels and Skiba 2004) models imply that shipping costs and trade barriers lead to differences in prices of goods, at least at the dock level. Such condition is commonly expressed as $S P_{j, g}=P_{i, g}+A_{i, j, g}$ where $P_{i, g}$ is the local currency price of good $g$ in country $i, S$ the nominal exchange rate between $i$ and $j$ and $A_{i, j, g}$ the marginal transaction cost. $A_{i, j, g}$ is usually modeled as a constant consisting of marginal transport cost ${ }^{3}$ and marginal trade barrier (tariffs, etc.): $A_{i, j, g}=t+B$. It can be interpreted as the minimum price difference that makes arbitrage trade profitable between $i$ and $j$. In an environment with perfectly competitive transport sector using constant returns to scale technology and where sellers of goods have no pricing power, price differences in excess of marginal transaction costs would be arbitraged away:

$$
\begin{equation*}
-A_{i, j, g} \leq S P_{j, g}-P_{i, g} \leq A_{i, j, g} \tag{1}
\end{equation*}
$$

There are environments in which price differences can exceed marginal transaction costs, e.g., pricing power on the side of sellers, market segmentation, or non-constant returns to scale in transportation sector. Nevertheless, marginal transaction costs in any environment split the price-difference space into two regions: a region of no-arbitrage outlined by (1) and a region with some level of arbitrage where (1) does not hold. This implies a non-linearity in the behaviour of the observed price differences: a random walk process in the first region and mean reversion in the second region ${ }^{4}$.

It is well known that neither the marginal transport costs nor the tariff barriers are constant across goods and locations. Consequently, the random-walk and mean-reverting regions vary systematically - an implication explored before using threshold-autoregressive

[^3]models. Obstfeld and Taylor (1997), Zussman (2002), Imbs et. al. (2003) use distance, exchange rate volatility ${ }^{5}$, tariffs and non-tariff trade barriers as measures of transaction costs to identify variation in threshold estimates for bilateral real exchange rates.

At the level of an individual good $g$, transport costs also depend on good-specific physical characteristics. Hummels $(2001,2003)$ estimates the dependance of freight costs on physical weight of the goods across four modes of transport (air, ocean, truck and rail) using US Census data and Transborder Surface Trade Database. Weight-to-price ratios are highly positively significant in explaining the freight rates ${ }^{\sqrt{66}}$, more so than the distance of the shipment. To illustrate the implication for non-linearity of price-differences, let the total transport costs follow a flexible Cobb-Douglas form. Specifically, let the transport cost depend positively on the weight of a shipment $w_{g} q_{g}$, distance between locations $d_{i j}$, value of the shipment $P_{i g} q_{g}$ (insurance costs) and negatively on the total trade volume $M_{i j}$ between two locations ${ }^{77}: T_{i j g}=\left(w_{g} q_{g}\right)^{\alpha_{1}} d_{i j}^{\alpha_{2}}\left(P_{i g} q_{g}\right)^{\alpha_{3}} M_{i j}^{\alpha_{4}} . \quad \alpha_{k} \in(0,1) k=1, \ldots, 3 ; \alpha_{4} \in(-1,0)$ because doubling of distance, shipment size, etc., does not require doubling of resources used in transportation (decreasing returns to factor accumulation due to efficiency gains see Hummels (2001)). Condition (1) can then be expressed as a condition for good-specific real exchange rate with predictions about the determinants of the no-arbitrage bounds

$$
\begin{equation*}
1-\left(\frac{t_{i j g}}{P_{i g}}+\frac{B_{i j g}}{P_{i g}}\right) \leq \frac{S P_{j g}}{P_{i g}} \leq 1+\left(\frac{t_{i j g}}{P_{i g}}+\frac{B_{i j g}}{P_{i g}}\right) \tag{2}
\end{equation*}
$$

where $t_{i j g}=\alpha_{1} q_{g}^{\alpha_{1}+\alpha_{3}-1} w_{g}^{\alpha_{1}} d_{i j}^{\alpha_{2}} P_{i g}^{\alpha_{3}} M_{i j}^{\alpha_{4}}$ is the marginal transport cost. The assumptions on $\alpha$ s imply that bounds of inequality (2) are increasing in the physical characteristic of the good $w_{g}$ and decreasing in its price $P_{i g}$ as well as the aggregate trade volume $M_{i j}$. Through (2), heterogeneity of marginal transaction costs implies that the non-linearity in price differences is good-specific; wider threshold estimates for heavier, more distant products, or for goods between locations that see little mutual trade. Heterogeneity in thresholds of sectoral real exchange rate found by Obstfeld \& Taylor (1997) and Imbs, et. al. (2003) is a result of aggregation in good-specific non-linearities driven by heterogeneous

[^4]marginal transaction costs at the level of individual goods.

## 3 Data

I use disaggregated consumer price index data to measure price differences. This limits the type of questions the study can address as the data does not contain information about the absolute size of of price differences ${ }^{88}$. However, information about dynamic properties of price levels is fully preserved in the dynamics of price index data. Consequently, de-meaning of the price index dataset is harmless while de-trending it removes information about price dynamics. The CPI data in this study is de-meaned but not detrended. Properties of aggregate US-Canada exchange rates are summarized in tables 4, 5] and 6. We see that both nominal and real exchange rates are more stationary before Bretton Woods period. This is true for raw, linearly-detrended as well as HP-detrended series.

### 3.1 Price index dataset

The price index dataset contains disaggregated price series of 63 groups of goods and services in the United States and Canada between 1970:1 and 2000:8 (some series start after 1970), as well as the aggregate consumer price index and the nominal exchange rate. Choice of the country combination is guided by the availability of data at a level of disaggregation at which physical characteristics of products can be estimated as well as by the sufficient time-span of the monthly series. Data for matching categories was obtained from Bureau of Labor Statistics and Statistics Canada, respectively, and is all demeaned. 49 of the series represent goods and 14 service $^{99}$, covering $73.5 \%$ of the CPI overall (goods cover $24.1 \%$ and services $46.7 \%$ of the CPI, respectively ${ }^{10}$ ). Using the taxonomy of Lebow and Rudd (2001), $77 \%$ of durable goods, $70 \%$ of nondurable goods and $39 \%$ of services are included in the data (see table 1 in Appendix A.2).

[^5]
### 3.2 Physical weights dataset

The dataset of physical weights and individual prices for each good (or group) necessary in estimations using price-to-weight data is constructed using a following data-collection procedure ${ }^{[11]}$. When available, weights are obtained from statistical agencies or government bodies. Otherwise, manufacturers' associations are searched for average weights of particular goods or product groups. In a minority of cases when neither of the approaches works, weights are estimated as an average of the market's large manufacturer's product range (e.g., for watches, an average weight is set equal to a current average weight of a Timex watch). Average prices are obtained in a similar manner, with a search of US data sources preceding a search of Canadian data sources. Price level necessary to construct a price-toweight ratios across goods corresponds to an average USD price in year 2000. When a price is unavailable in 2000, the last available price is inflated by the CPI inflation rate of the relevant country. Weight (and price) data of groups of products (e.g., women's apparel) are computed as weighted averages of weights (and prices) of components using the expenditure shares from US urban average CPI in December 2001 as weights. The composition of all groups, data sources, as well as price and weight estimates are documented in table 2 in Appendix B.

### 3.3 Volume dataset

The dataset of physical volumes of is calculated indirectly using data on stowage factors from the German Transportation Information Service databas ${ }^{[12]}$. A stowage factor of a cargo is the ratio of weight to stowage space (the unit is ton $/ \mathrm{m}^{3}$ ) required under normal conditions, including all packaging. Consequently, the volume of a unit of the good can be calculated using the stowage factor and weight of a good. Because stowage factors for goods can vary depending on packaging, water contents, and compression, I use the average of all quoted stowage factors in calculating the volume of a good. I find stowage ratios for products that are not included in the German database from other sources. Table 3 in Appendix $\sqrt{B}$ documents the data sources.

[^6]
## 4 Empirical framework and results

The first part of this section estimates threshold-autoregressive (TAR) models on goodspecific real exchange rate data. The second part assesses the extent to which heterogeneity in marginal transaction costs explains heterogeneity of threshold estimates and conditional half-lifes. The discrete break in good-specific real exchange rates implied by equation (2) guides the choice of a discrete self-exciting TAR models ${ }^{133}$. The nature of the break driven by heterogeneity of $t_{i j g}$ across goods can be captured well by a highly disaggregated data on hand ${ }^{[14]}$. Logarithm of good-specific real exchange rate $z_{t}^{g}$ is used as the object of first-stage estimation: $z_{t}^{g}=p_{t}^{g}-p_{t}^{g *}+s_{t}$, where $t$ is a time index and $g$ is a good (service) index, $p$ and $p^{*}$ denote logarithm price indexes in US and Canada, respectively, and $s_{t}$ is the logarithm of the nominal exchange rate.

Specification of a TAR model requires selection of a number of thresholds, number of autoregressive lags $p$ and of an optimal delay parameter $d_{p}$. I assume two thresholds ${ }^{155}$ for each good. As there is no a-priori reason for $t_{i j g}$ to have different effects in appreciation and depreciation, I assume symmetry: $\gamma_{1}^{g}=-\gamma_{2}^{g} \equiv \gamma^{g} \forall g$. The main model is a Band$\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ specified as:

$$
\Delta z_{t}^{g}= \begin{cases}\bar{\beta}^{g, \text { out }}\left(\bar{z}_{t}^{g}-\gamma^{g}\right)+e_{t}^{\text {out }} & \text { if } z_{t-d_{p}}^{g}>\gamma^{g}  \tag{3}\\ \bar{\beta}^{g, \text { in }} \bar{z}_{t}^{g}+e_{t}^{\text {in }} & \text { if } \gamma^{g} \geq z_{t-d_{p}}^{g} \geq-\gamma^{g} \\ \bar{\beta}^{g, \text { out }}\left(\bar{z}_{t}^{g}+\gamma^{g}\right)+e_{t}^{\text {out }} & \text { if }-\gamma^{g}>z_{t-d_{p}}^{g}\end{cases}
$$

where $\bar{z}_{t}$ is the vector of the appropriate lagged values of $z_{t}, e_{t}^{\text {out }} \sim \mathrm{N}\left(0, \sigma_{B}^{\text {out }}{ }^{2}\right)$ and $e_{t}^{\text {in }} \sim \mathrm{N}\left(0, \sigma_{B}^{\text {in }}{ }^{2}\right)$.

[^7]For robustness, Equilibrium-TAR (Eq-TAR) model is also estimated:

$$
\Delta z_{t}^{g}= \begin{cases}\bar{\beta}^{g, o u t} & \bar{z}_{t}^{g}+e_{t}^{o u t}  \tag{4}\\ \text { if } z_{t-d_{p}}^{g}>\gamma^{g} \\ \bar{\beta}^{g, \text { in }} \bar{z}_{t}^{g}+e_{t}^{i n} & \text { if } \gamma^{g} \geq z_{t-d_{p}}^{g} \geq-\gamma^{g} \\ \bar{\beta}^{g, o u t} \bar{z}_{t}^{g}+e_{t}^{o u t} & \text { if }-\gamma^{g}>z_{t-d_{p}}^{g}\end{cases}
$$

where $e_{t}^{\text {out }} \sim \mathrm{N}\left(0, \sigma_{E}^{\text {out }}{ }^{2}\right)$ and $e_{t}^{\text {in }} \sim \mathrm{N}\left(0, \sigma_{E}^{\text {in }}{ }^{2}\right)$. Because the identification of the thresholds relies on (2), both specifications assume no mean reversion of price difference between the thresholds (a restriction of $\bar{\beta}^{g, i n}=0$ ). The two specifications differ in their assumptions on mean-reversion of $z_{g}$ outside thresholds. Band-TAR assumes that price differences converge back to the no-arbitrage threshold, in line with equation (2). Eq-TAR assumes convergence back to the middle of the no-arbitrage band (mean). Hence, Band specification produces faster conditional convergence speeds. The results from both specifications are very similar. See Appendix A for details on estimation and testing of a TAR (2, p,d) model.

### 4.1 Non-linearities

Columns 4 and 5 of table 7 show that a vast majority of the series can not reject the $\mathrm{H}_{0}$ of unit root by either ADF or Philips-Perron tests ${ }^{16}$. Unit roots appear to be rejected for the more valuable series with the notable exception of foods. At the other extreme, data for many services and non-traded goods is not stationary even in their OLS point estimates. Tsay's test for threshold non-linearity ${ }^{[17}$ rejects linearity for 49 out of 63 series in favour of a TAR specification (column 3 of table 7). Therefore, threshold autoregressive models provide a better characteristic of price differences than linear models for the bulk of the series ${ }^{18}$. The non-linearities are distributed fairly evenly across all goods and services.

[^8]Space limitations require reporting of only general results. As is well known, model misspecification causes incorrectly long half-life estimates (Obstfeld \& Taylor 1997). This is highlighted in the reduction of an average half-life for all series with AR point estimates inside the unit circle from 126 months under $\operatorname{AR}(1)$ specification to 63 months under TAR (2,p,d). Slightly larger reductions are observed for goods (drop from 112 to 52 months on average) than services (drop from 202 to 123 months). Services and medical products have the longest AR half lifes, followed surprisingly by high-tech goods (PCs and audiovisual equipment - see tables 8 and 9). Price differences for cars, car parts, clothing and footwear are quickest in converging to mean. The conditional half lifes under TAR are calculated using impluse response functions, allowing them to exceed linear half-lifes. Vice goods, medical and chemical products, and marginally for cars, car parts, clothing and footwear all see a marginal increases in half-life while high-tech goods drop significantly. General findings also confirm - at a greater level of disaggregation than in Imbs et. al, (2003) and in a two-country setting - a positive correlation between AR half-life and threshold width, as well as between AR half-life and the reduction of half-life from AR to TAR specification (see figure 2). Slowly-reverting goods tend to have larger thresholds and larger drops in conditional persistence.

### 4.2 Determinants of thresholds

Arbitrage condition (2) predicts a relationship between the estimates of thresholds $\hat{\gamma}^{g}$ in equations (3) and (4) and good-specific determinants of marginal transaction costs. This guides a conjecture

$$
\begin{equation*}
\hat{\gamma}^{g}=\beta_{0}+\sum_{i=1}^{k} \beta_{i} y_{i}^{g}+\epsilon^{g} \tag{5}
\end{equation*}
$$

where $y_{g}^{i}$ is a vector of good-specific determinants of marginal transaction costs including measures of physical characteristics of goods (price-to-weight, price-to-volume ratios or stowage factors) and measures of trade barriers (tariffs). It also includes measures of price-setting power and market structure (market size proxy and industry concentration measures). The importance of physical characteristics for the marginal transport costs is explained in section 2 above. Tariffs are measured as an average tariff rate for the product
category in 1989, date approximately half way through the gradual tariff-reduction process under NAFTA ${ }^{19}$. With increasing returns to scale in production (e.g., in the presence of fixed costs), market size matters in profits. Larger markets are more attractive, lowering sellers' price-setting power. I include CPI expenditure shares across goods as a measure of the price-setting power. Market structure is obviously also directly relevant for pricesetting power of the firms. Herfindahl-Herschmann index from 1997 US Economic Census is included as a measure of pricing power due to individual market structure ${ }^{20}$. Finally, a dummy for tobacco is added to the right-hand side variables due to a complicated one-sided change in federal as well as provincial taxes in Canada in the spring of 1994 (see figures 3 and 4$)^{21}$.

Price-to-weight ratios are highly significant in explaining thresholds (column 2 of table 12). Heavier goods (relative to their value) with larger marginal transport costs have wider thresholds of no-arbitrage. A ten-fold increase in the price-to-weight ratio increases the threshold by 0.73 percentage points (i.e., widens the no-arbitrage band by 1.46 percentage points). Column 6 of table 12 examines a logarithmic specification, allowing the interpretation of the coefficient as an elasticity of threshold with respect to price-to-weight ratios ${ }^{222}$. Coefficient of $\log (P / W)$ is -1.46 and highly significant. Estimations with price-to-volume ratios have negative sign but are not significant. Specifications explain up to $46 \%$ of the variation in thresholds. These important new results show that at the individual goods, real exchange rate non-linearity is caused by good-specific characteristics that drive marginal transaction costs. Aggregation of these effects leads to heterogeneity in RER at sectoral level.

Measures of price-setting power are also important in explaining thresholds. Expenditure share is negatively related to threshold width (at $10 \%$ significance). A hypothesis

[^9]consistent with this finding is that of market size determining price-setting power, possibly because of a lower degree of monopoly power in larger markets. Tariffs and HerfindahlHerschmann index are not significant ${ }^{233}$.

### 4.2.1 Robustness of threshold regressions

Robustness of these results is confirmed with three methods: exclusion of goods with limited tradability, Tobit estimations allowing for linearity control and finally by a complete reestimation of TAR models in which thresholds are imposed to drop at the rate equal to the drop in US-Canada transport costs found in recent empirical literature.

First, threshold regressions are re-estimated while excluding goods that are known to have limited tradability. The second section of table 13 excludes natural gas and gasoline for which trade normally requires sophisticated and expensive distribution networks (pipelines), making physical characteristics poor measures of marginal transport costs. The third section of the same table also excludes alcoholic beverages whose licensing requirements make trade complicated within countries and much more so between countries. As expected, price-toweight and price-to-volume ratios are more significant than in the original specification.

Second, to control for linearity of the series equation (5) is re-estimated with Tobit estimator setting $\gamma^{g}=0$ for those goods for which I either can not reject linearity (second section of table 14), or can not reject linearity and reject stationarity (first section of table 14). In addition, in the third section of table 14 I re-estimate OLS using only the series for which linearity is rejected (these robustness checks follow Imbs. et. al. (2003)). The original results carry through in all cases, with an increase in significance of the expenditure weights.

Finally, $\operatorname{EQ}-\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ and BAND-TAR (2,p,d) models are re-estimated under the constraint that marginal transport costs have declined throughout the sample period. I use a direct estimate of Novy (2006) that Canada-US transport costs dropped by $39 \%$ between 1960 and $2002^{24}$. Table 15 shows the second-stage regression results based on the threshold estimates which incorporate such decline in transport costs between US and Canada. The

[^10]results are highly significant, explaining up to $60 \%$ of variation in thresholds. An increase in the size of the price-to-weight and expenditure share coefficients is seen in all specifications. This is not unexpected as thresholds now take into account the empirically documented decline in transport costs.

### 4.3 Determinants of conditional persistence

This section investigates the possibility that persistence of prices also depends on marginal transaction costs. The estimation is based on

$$
\begin{equation*}
\hat{h \hat{l}^{g}}=\delta_{0}+\sum_{i=1}^{k} \delta_{i} x_{i}^{g}+\nu^{g} \tag{6}
\end{equation*}
$$

where $h \hat{l}^{g}$ is the conditional half-life estimated by impulse response functions using TAR estimates from (3) and $x_{i}$ is a vector of explanatory variables. In addition to the determinants of transaction costs and measures of pricing-power included in $y_{i}$ a dummy variable for chilling is included in $x_{i}{ }^{25}$. Although many open macro models can generate persistence in relative prices, very few make predictions about the relationship between conditional convergence speeds and marginal transaction costs. Imbs et. al. (2003) establish that relationship empirically in a cross-country sectoral real exchange rate setting.

Persistence of price differences outside of the thresholds co-varies negatively with price-to-weight ratios as well as with the refrigeration requirements (table 16 summarizes initial results). Price differences for goods with larger marginal transaction costs (heavier goods) take longer to converge to the no-adjustment bound (the elasticity is approximately -0.2 ). This is likely caused by the importance of marginal transaction costs in the decision on the mode of transport. Hummels (2001b) estimates that, in bilateral US trade data, each day saved shipping is worth 0.8 percentage ad-valorem points for manufactured products. Larger average price differences for goods with bigger marginal transport costs then justify use of slower mode of transport ${ }^{26}$. On the other hand, more valuable goods are transported

[^11]more quickly, thus lowering their conditional half-life.

### 4.3.1 Robustness of persistence regressions

The above results are robust to various specifications. Exclusion of goods with poor tradability such as energies and alcoholic beverages increases the significance of the relationship (columns 3 to 6 of table 16). For the remaining products, conditional persistence of price differences is also highly significantly explained by their respective stowage factors (weight to packed volume ratios). Heavier goods (relative to their volume) again exhibit longer persistence.

The results also carry through to unconditional linear half-lifes, with similar level of significance (column 1 of table 17). Tobit estimations, performed in the same way as for threshold estimates, also confirm the results (columns 2-4). Tariffs are significant in explaining persistence, implying that the influence of the trade barriers is not limited to a constant price wedge. A possible reason for slower disappearance of higher-tariff goods may lie in lower trade volumes fir such goods. An additional marginal significance of HerfindahlHerschmann index in some Tobit regressions is particularly intriguing due to its negative sign which implies that price convergence is quicker in more concentrated industries. This somewhat counter-intuitive result may be caused by a larger degree of producer pricing in more concentrated industries. Expenditure shares enter with a negative sign (implying quicker conditional convergence for goods with larger markets) but are not significant. Results carry through in OLS specification that excludes linear series (columns 6 and 7), and OLS with linearity control (columns 8 and 9 ).

## 5 Conclusion

Physical characteristics of goods, through their importance in marginal transaction costs, explain a large part of the threshold non-linearity and conditional persistence of law-of-oneprice deviations. Visible at a sufficiently detailed level of disaggregation, this mechanism drives the heterogeneity at higher levels of aggregation such as the sectoral real exchange rates. In post-Bretton Woods US-Canada monthly data for 49 products and product groups,
heavier goods (relative to their price) see their price differences diverge further before becoming mean reverting (transport costs are higher for those goods because they are more difficult to move). Furthermore, after becoming mean reverting, price differences for heavier goods converge more slowly, possibly due to choice of slower mode of transport for goods with larger average price differences. Both mechanisms increase the unconditional persistence of the price differences of products with higher marginal transaction costs. While the relationship between physical characteristics of products and freight costs is not unknown, its implications for the behaviour of price differentials have not yet been explored.

This account of the heterogeneity in the behaviour of price differences also sheds light on the potential sources of the most formidable components of the purchasing power parity puzzle - the persistence of real exchange rates. Imbs, et. al. (2005b) show how the peculiar nature of aggregating heterogeneous real exchange rate components accentuates the persistence at the level of the aggregate real exchange rate. There is a discussion about whether such "aggregation bias" explains PPP puzzle (see also Chen and Engel (2004)). To the extent that a large part of the heterogeneity in real exchange rate components is accounted for by the heterogeneity in marginal transaction costs across goods, my study shows that persistence in real exchange rates - and hence the PPP puzzle - is driven by the composition of a trade basket at micro level. Consequently, economic models that take heterogeneity of marginal transaction costs into account may stand a better chance in explaining the puzzling persistence in aggregate real exchange rates. It would be interesting to further verify these results in a geographically larger dataset with heterogeneity of countries as well as locations (both within and between countries).

## 6 Acknowledgements

I would like to thank Michael B. Devereux, John F. Helliwell and James M. Nason for their support. I am also grateful for the discussions with Brian R. Copeland, Werner Antweiler as well as the participants of the INE/TARGET international workshop.

## Appendix

## A Specification and estimation of a TAR

Specification and estimation of $\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ proceeds in three steps ${ }^{27}$ that are repeated for all 63 series: selection of an appropriate lag-structure $p$ for the linear model, selection of the delay parameter $d$, and finally estimation and testing of the non-linear model. Specifically:

1. With monthly data, up to 12 lags are considered. Examination of the partial autocorrelogram (Granger and Teräsvirta (1993)) narrows the potential candidates, of which I choose a combination with the lowest Akaike information criterion (or Schwarz Bayesian information criterion) as long as the residuals are not serially correlated and are normally distributed ${ }^{28}$. Appropriate model specification is important at this stage because omitted autocorrelation may lead to rejection of the the linear model and in general complicate interpretation of test results (Kilian and Taylor (2003)).
2. Given the lag structure $p$ and the set of feasible values of the delay parameter $d \in$ $\{1,2, \ldots, 12\}$ ), optimal $d_{p}$ is selected by a procedure suggested in Tsay (1989):

$$
\hat{F}\left(p, d_{p}\right)=\max _{\nu \in S} \hat{F}(p, \nu)
$$

where $\hat{F}$ is the F-statistic described in the Appendix A.2. This procedure selects the value of the delay parameter which gives the most significant result in testing for a non-linearity. P-values of the optimal $d_{p}$ can then also be used as a general nonparametric test of non-linearity.
3. Given optimal $p$ and $d_{p}$, parametric maximum likelihood estimation procedure according to Obstfeld and Taylor (1997) (who follow Fanizza (1990), Balke and Fomby (1997) and Prakash (1996)) obtains $\hat{\gamma}$ and $\hat{\beta}$. Practically, the procedure is a best-

[^12]fit grid search for a threshold parameter $\gamma$ that maximizes the log-likelihood ratio $L L R=2\left(L_{a}-L_{0}\right)$ where
\[

$$
\begin{aligned}
L_{a}\left(\beta_{\text {in }}, \beta_{\text {out }}, \sigma_{\text {in }}, \sigma_{\text {out }}, \gamma\right)= & -\frac{1}{2} n_{\text {in }}\left[\log (2 \pi)+\log \left[\frac{\sum_{I_{\text {in }}} e_{t, \text { in }}^{2}}{n_{\text {in }}-2}\right]+\frac{n_{\text {in }}-2}{n_{\text {in }}}\right] \\
& -\frac{1}{2} n_{\text {out }}\left[\log (2 \pi)+\log \left[\frac{\sum_{I_{\text {out }}} e_{t, \text { out }}}{n_{\text {out }}-2}\right]+\frac{n_{\text {out }}-2}{n_{\text {out }}}\right] \\
L_{0}(\beta, \sigma)= & -\frac{1}{2} n\left[\log (2 \pi)+\log \left[\frac{\sum e_{t}^{2}}{n-2}\right]+\frac{n-2}{n}\right] \\
\text { where } e_{t, \text { in }}= & \Delta z_{t, \text { in }}-\beta_{\text {in }} \bar{z}_{t, \text { in }} \\
e_{t, \text { out }}= & \Delta z_{t, \text { out }}-\beta_{\text {out }} \overline{\bar{z}}_{t, \text { out }} \\
\text { and } e_{t}= & \Delta z_{t}-\beta \bar{z}_{t}
\end{aligned}
$$
\]

Choices of $\gamma$ with less than 10 observation above the threshold are not considered due to excessive sample bias. Estimates of $\hat{\beta}$ are used in computing conditional half-life of convergence (using impulse response functions) ${ }^{29}$.
4. Two tests are used to assess the non-linear TAR against the linear alternative: likelihood ratio test and Tsay's general nonparametric F-test. Likelihood ratio test uses a statistic obtained during the grid-search. However, this statistic does not follow the asymptotic $\chi^{2}$ distribution in a non-linear model because the threshold parameter $\gamma$ is not identified under $H_{0}$ of linearity. Hence, a Monte Carlo simulation of 5000 draws is used to obtain p-values of the LLR statistic. Tsay's general nonparametric F-test uses the minimal p-value of two F-statistics: one from an arranged regression using ascending ordering of the case data, another with descending orderings of the case data.

## A. 1 Log-likelihood ratio test

Log likelihood ratio $(L L R)$ tests the likelihood that the non-linear model describes the data better than the linear autoregressive model. The statistic is computed during the TAR $(2, \mathrm{p}, \mathrm{d})$ estimation, and measures the difference between log-likelihoods of an optimal

[^13]$\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ and a corresponding $\mathrm{AR}(\mathrm{p})$ model. $L L R$ statistic of a non-linear model does not follow the usual $\chi^{2}$ distribution because the parameters of the nonlinear alternative are not identified under $H_{0}$ of linearity (Granger and Teräsvirta (1993)). There exists more than one set of restrictions which makes a $\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ model linear. Monte Carlo simulation is used to obtain an empirical distribution of $L L R$ for all goods and from it compute the empirical p-values of $L L R$ statistics Tables 10 and 11 provide empirical p-values of the hypothesis that a $\operatorname{TAR}(2, \mathrm{p}, \mathrm{d})$ is better than $\mathrm{AR}(\mathrm{p})$ for EQ-TAR and BAND-TAR models, respectively. At $10 \%$ significance level, LLR test results imply that TAR $(2, \mathrm{p}, \mathrm{d})$ is a better model than the linear $\mathrm{AR}(\mathrm{p})$ for $40 \%$ of series ( $30 \%$ in Equilibrium TAR).

## A. 2 Tsay's F-test for non-linearity

The F-test for non-linearity consists of several steps. First, data is arranged into cases of $\left(\Delta z_{t}, 1, z_{t-1}, \ldots, z_{t-k}\right)$ such that $k \in M$ where M is a set of all relevant lags as determined in stage 1 of the model-specification (see previous section). Second, these cases are arranged in ascending order according to $z_{t-d}$ where $d$ is the threshold delay parameter ${ }^{[30]}$ (see Tsay (1986), Obstfeld and Taylor (1997)). Third, an arranged autoregression is run on the ordered case data using recursive least squares:

$$
\begin{equation*}
\Delta z_{t}=\sum_{k \in M}^{k^{\max }} \alpha_{k} z_{t-k}+u_{t} \tag{7}
\end{equation*}
$$

Recursive least square technique provides predictive residuals which are then used in Tsay's nonlinearity test. The recursive estimates are updated as follows (see Tsay (1986), Tong (1990), Ertel and Fowlkes (1976)):

$$
\begin{aligned}
\hat{\beta}_{m+1} & =\hat{\beta}_{m}+K_{m+1}\left[\Delta z_{m+1}-\beta_{m} \bar{z}_{m}\right] \\
K_{m+1} & =P_{m} \bar{z}_{m+1} / D_{m+1} \\
D_{m+1} & =1+\bar{z}_{m+1}^{\prime} P_{m+1} \bar{z}_{m+1} \\
P_{m+1} & =\left(I-P_{m} \frac{\bar{z}_{m+1} \bar{z}_{m+1}^{\prime}}{D_{m+1}}\right) P_{m}
\end{aligned}
$$

[^14]where $m$ denotes a case, $\bar{z}_{m}$ is a vector of all RHS variables in equation (7) (hence $\beta=$ $\left(\alpha_{1} \ldots \alpha_{\left.\left.k_{\max }\right)^{\prime}\right)}\right)$ and I is an identity matrix. The recursion is initiated by a regular OLS on the first $b$ cases where $b=n / 10+p, n$ is the total number of observations and $p$ is the number of elements in $M^{31]}$. The first $b$ cases are then scrapped. The predictive ( $\hat{a}_{m}$ ) and standardized predictive ( $\hat{e}_{m}$ ) residuals are obtained as: $\hat{a}_{m+1}=\Delta z_{m+1}-\beta_{m} \bar{z}_{m}$ and $\hat{e}_{m+1}=\hat{a}_{m+1} / \sqrt{D_{m+1}}$.

Fourth, standardized predictive residuals are regressed on the RHS variables.

$$
\begin{align*}
\hat{e}_{m} & =\sum_{k \in M}^{k^{m a x}} \gamma_{k} z_{m-k}+\epsilon_{m} \\
F & =\frac{\left(\sum \hat{e}_{t}^{2}-\sum \epsilon_{t}^{2}\right) /(p+1)}{\sum \epsilon_{t}^{2} /(n-d-b-p-h)} \tag{8}
\end{align*}
$$

The F-statistic follows an F distribution with $p+1$ and $n-d-b-p-h$ degrees of freedom where $h \equiv \max \{1, p+1-d\}$.

Intuitively, a threshold implies a parameter change in the arranged autoregression (7) at the threshold level. Therefore, while predictive residuals will be orthogonal to the regressors for the cases that fall below the threshold, they will become biased above the threshold, destroying the orthogonality with the regressors. Such regime change then leads to a rejection of orthogonality and can be tested by the F-statistic (8). Rejection of orthogonality implies a rejection of a linear AR model for a non-linear TAR alternative.

[^15]Table 1: Coverage of CPI by the data.
Relative importance of components in the Consumer Price Indexes (1999-2000 weights): U.S. city average,
December 2001. Bold series are not included in the dataset.

| Item | CPI-U | CPI-W | Item | CPI-U | CPI-W |
| :---: | :---: | :---: | :---: | :---: | :---: |
| All items | 100.000 | 100.000 | Gas (piped) and electricity | 3.466 | 3.778 |
| Food and beverages | 15.719 | 17.229 | Electricity | 2.521 | 2.762 |
| Food | 14.688 | 16.228 | Utility natural gas service | . 945 | 1.017 |
| Food at home | 8.468 | 9.798 | Water and sewer and trash collection services | . 857 | . 873 |
| Cereals and bakery products | 1.298 | 1.468 | Water and sewerage maintenance | . 633 | . 660 |
| Cereals and cereal products | . 444 | . 525 | Garbage and trash collection | . 224 | . 213 |
| Flour and prepared flour mixes | . 058 | . 070 | Household furnishings and operations | 4.840 | 4.101 |
| Breakfast cereal | . 249 | . 278 | Window \& floor coverings \& other linens | . 289 | . 254 |
| Rice, pasta, cornmeal | . 137 | . 177 | Furniture and bedding | 1.051 | . 955 |
| Bakery products | . 854 | . 944 | Bedroom furniture | . 306 | . 284 |
| Meats, poultry, fish, and eggs | 2.271 | 2.831 | Living room, kitchen, \& dining room furniture | . 555 | . 495 |
| Meats, poultry, and fish | 2.178 | 2.712 | Other furniture | . 181 | . 154 |
| Meats | 1.450 | 1.832 | Unsampled furniture | . 010 | . 021 |
| Beef and veal | . 693 | . 868 | Appliances | . 364 | .416 |
| Uncooked ground beef | . 255 | . 334 | Major appliances | . 199 | . 226 |
| Uncooked beef roasts | . 115 | . 132 | Other appliances | . 151 | . 176 |
| Uncooked beef steaks | . 278 | . 351 | Unsampled appliances | . 013 | . 015 |
| Uncooked other beef and veal | . 045 | . 051 | Other household equip. \& furnishings | . 806 | . 565 |
| Pork | . 468 | . 610 | Tools, hardware, outdoor eq. \& supplies | . 649 | . 595 |
| Bacon, breakfast sausage, \& rel. products | . 148 | . 190 | Housekeeping supplies | . 862 | . 959 |
| Ham | . 104 | . 132 | Household cleaning products | . 392 | . 459 |
| Pork chops | . 112 | . 156 | Household paper products | . 200 | . 221 |
| Other pork including roasts and picnics | . 105 | . 132 | Miscellaneous household products | . 270 | . 279 |
| Other meats | . 289 | . 355 | Household operations | . 820 | . 357 |
| Poultry | . 414 | . 518 | Apparel | 4.399 | 4.831 |
| Chicken | . 329 | . 423 | Men's and boys' apparel | 1.122 | 1.243 |
| Other poultry including turkey | . 085 | . 095 | Men's apparel | . 880 | . 927 |
| Fish and seafood | . 314 | . 362 | Men's suits, sport coats, and outerwear | . 201 | . 189 |
| Fresh fish and seafood | . 187 | . 219 | Men's furnishings | . 191 | . 196 |
| Processed fish and seafood | . 126 | . 143 | Men's shirts and sweaters | . 263 | . 279 |
| Eggs | . 093 | . 119 | Men's pants and shorts | . 203 | . 241 |
| Dairy and related products | . 916 | 1.021 | Unsampled men's apparel | . 021 | . 023 |
| Fruits and vegetables | 1.204 | 1.307 | Boys' apparel | . 242 | . 316 |
| Fresh fruits and vegetables | . 928 | . 995 | Women's and girls' apparel | 1.807 | 1.864 |
| Fresh fruits | . 466 | . 490 | Women's apparel | 1.515 | 1.504 |
| Apples | . 084 | . 095 | Women's outerwear | . 108 | . 111 |
| Bananas | . 088 | . 100 | Women's dresses | . 214 | . 247 |
| Citrus fruits | . 079 | . 085 | Women's suits and separates | . 762 | . 712 |
| Other fresh fruits | . 215 | . 210 | Women's underwear, nightwear, sportswear | . 400 | . 399 |
| Fresh vegetables | . 462 | . 505 | Unsampled women's apparel | . 032 | . 036 |
| Potatoes | . 080 | . 092 | Girls' apparel | . 292 | . 360 |
| Lettuce | . 059 | . 066 | Footwear | . 874 | 1.165 |
| Tomatoes | . 094 | . 109 | Men's footwear | . 290 | . 416 |
| Other fresh vegetables | . 230 | . 238 | Boys' and girls' footwear | . 177 | . 269 |
| Processed fruits and vegetables | . 276 | . 312 | Women's footwear | . 407 | . 480 |
| Nonalc. beverages and bev. materials | . 967 | 1.132 | Infants' and toddlers' apparel | . 203 | . 256 |
| Juices and nonalcoholic drinks | . 710 | . 853 | Jewelry and watches | . 394 | . 303 |
| Carbonated drinks | . 364 | . 468 | Watches | . 058 | . 057 |
| Frozen noncarbonated juices and drinks | . 036 | . 039 | Jewelry | . 336 | . 245 |
| Nonfrozen noncarbonated juices and drinks | . 310 | . 346 | Transportation | 17.055 | 19.393 |
| Beverage materials including coffee and tea | . 257 | . 280 | Private transportation | 15.845 | 18.452 |
| Coffee | . 100 | . 105 | New and used motor vehicles | 8.614 | 10.145 |
| Other beverage materials including tea | . 157 | . 174 | New vehicles | 5.083 | 4.897 |
| Other food at home | 1.811 | 2.038 | Used cars and trucks | 2.195 | 4.099 |
| Sugar and sweets | . 315 | . 339 | Leased cars and trucks | 1.061 | . 925 |
| Sugar and artificial sweeteners | . 056 | . 069 | Car and truck rental | . 120 | . 085 |
| Candy and chewing gum | . 200 | . 207 | Unsampled new \& used motor veh. | . 155 | . 140 |
| Other sweets | . 059 | . 063 | Motor fuel | 2.564 | 3.153 |
| Fats and oils | . 265 | . 316 | Gasoline (all types) | 2.536 | 3.120 |
| Butter and margarine | . 090 | . 103 | Other motor fuels | . 028 | . 033 |
| Salad dressing | . 076 | . 089 | Motor vehicle parts and equipment | . 421 | . 530 |
| Other fats and oils including peanut butter | . 098 | . 125 | Tires | . 234 | . 262 |
| Other foods | 1.232 | 1.383 | Vehicle accessories other than tires | . 187 | . 268 |
| Food away from home | 6.220 | 6.430 | Motor vehicle maintenance and repair | 1.400 | 1.438 |
| Full service meals and snacks | 2.649 | 2.198 | Motor vehicle body work | . 082 | . 077 |
| Limited service meals and snacks | 2.741 | 3.354 | Motor vehicle maintenance and servicing | . 478 | . 475 |
| Food at employee sites and schools | . 296 | . 375 | Motor vehicle repair | . 821 | . 868 |
| Food - vending mach. \& mobile vendors | . 151 | . 229 | Unsampled service policies | . 020 | . 019 |
| Other food away from home | . 383 | . 275 | Motor vehicle insurance | 2.288 | 2.679 |
| Alcoholic beverages | 1.031 | 1.001 | Motor vehicle fees | . 558 | . 506 |
| Alcoholic beverages at home | . 682 | . 709 | Public transportation | 1.211 | . 941 |
| Beer, ale, and other malt beverages at home | . 352 | . 469 | Airline fare | . 761 | . 508 |
| Distilled spirits at home | . 109 | . 102 | Other intercity transportation | . 187 | . 124 |
| Wine at home | . 221 | . 139 | Intracity transportation | . 256 | . 300 |
| Alcoholic beverages away from home | . 348 | . 292 | Unsampled public transportation | . 006 | . 008 |
| Housing | 40.873 | 38.141 | Medical care | 5.810 | 4.620 |
| Shelter | 31.522 | 29.212 | Medical care commodities | 1.377 | 1.006 |
| Rent of primary residence | 6.421 | 8.395 | Prescription drugs and medical supplies | . 959 | . 680 |
| Lodging away from home | 2.702 | 1.523 | Nonprescription drugs and medical supplies | . 418 | . 326 |
| Housing at school, excluding board | . 241 | . 176 | Internal \& respiratory over-the-counter drugs | . 304 | . 250 |
| Other lodg. away from home incl. hotels | 2.461 | 1.347 | Nonprescription medical equip. \& supplies | . 114 | . 076 |
| Owners' equivalent rent of primary residence | 22.046 | 18.980 | Medical care services | 4.434 | 3.614 |
| Tenants' and household insurance | . 353 | . 314 | Professional services | 2.784 | 2.245 |
| Fuels and utilities | 4.511 | 4.829 | Physicians' services | 1.503 | 1.280 |
| Fuels | 3.654 | 3.955 | Dental services | . 747 | . 584 |
| Fuel oil and other fuels | . 188 | . 177 | Eyeglasses and eye care | . 288 | . 240 |
| Fuel oil | . 121 | . 105 | Services by other medical professionals | . 247 | . 142 |
| Other household fuels | . 068 | . 072 | 1 Hospital and related services | 1.353 | 1.092 |


| Item | CPI-U | CPI-W | Item | CPI-U | CPI-W |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Hospital services | 1.271 | 1.075 | Cigarettes | . 864 | 1.360 |
| Nursing homes and adult daycare | . 082 | . 017 | Tobacco products other than cigarettes | . 057 | . 073 |
| Health Insurance | . 297 | . 276 | Unsampled tobacco and smoking prods | . 007 | . 008 |
| Recreation | 6.019 | 5.649 | Personal care | 3.384 | 3.059 |
| Video and audio | 1.645 | 1.803 | Personal care products | . 706 | . 815 |
| Televisions | . 150 | . 157 | Hair, dental, shaving, \& pers. care | . 374 | . 434 |
| Cable television | . 928 | 1.034 | Cosmetics, perfume, bath, nail preps | . 327 | . 374 |
| Other video equipment | . 055 | . 064 | Unsampled personal care products | . 005 | . 006 |
| Video casset., discs, \& other media incl. rental | . 148 | . 182 | Personal care services | . 901 | . 900 |
| Audio equipment | . 117 | . 131 | Miscellaneous personal services | 1.562 | 1.161 |
| Audio discs, tapes and other media | . 147 | . 159 | Miscellaneous personal goods | . 215 | . 183 |
| Unsampled video and audio | . 099 | . 076 | Special aggregate indexes |  |  |
| Pets, pet products and services | . 711 | . 703 | All items | 100.000 | 100.000 |
| Sporting goods | . 628 | . 728 | Commodities | 41.300 | 45.559 |
| Sports vehicles including bicycles | . 286 | . 413 | Commodities less food and beverages | 25.582 | 28.330 |
| Sports equipment | . 333 | . 309 | Nondurables less food and beverages | 13.493 | 14.685 |
| Unsampled sporting goods | . 009 | . 006 | Nondurables less food, bev. \& apparel | 9.094 | 9.854 |
| Photography | . 241 | . 215 | Durables | 12.089 | 13.645 |
| Photographic equipment and supplies | . 110 | . 092 | Services | 58.700 | 54.441 |
| Photographers and film processing | . 129 | . 122 | Rent of shelter | 31.169 | 28.898 |
| Unsampled photography | . 001 | . 001 | Transportation services | 6.638 | 6.573 |
| Other recreational goods | . 497 | . 512 | Other services | 10.963 | 10.033 |
| Toys | . 360 | . 399 | All items less food | 85.312 | 83.772 |
| Sewing machines, fabric and supplies | . 058 | . 052 | All items less shelter | 68.478 | 70.788 |
| Music instruments and accessories | . 062 | . 049 | All items less medical care | 94.190 | 95.380 |
| Unsampled recreation commodities | . 016 | . 012 | Commodities less food | 26.612 | 29.331 |
| Recreation services | 1.861 | 1.364 | Nondurables less food | 14.524 | 15.687 |
| Recreational reading materials | . 436 | . 324 | Nondurables less food and apparel | 10.125 | 10.855 |
| Newspapers and magazines | . 265 | . 210 | Nondurables | 29.212 | 31.915 |
| Recreational books | . 170 | . 114 | Nondurables less food | 14.524 | 15.687 |
| Unsampled recreational reading materials | . 001 | . 000 | Nondurables less food and apparel | 10.125 | 10.855 |
| Education and communication | 5.813 | 5.637 | Nondurables | 29.212 | 31.915 |
| Education | 2.726 | 2.382 | Apparel less footwear | 3.525 | 3.666 |
| Educational books and supplies | . 220 | . 203 | Services less rent of shelter | 27.531 | 25.543 |
| Tuition, other school fees, and childcare | 2.506 | 2.178 | Services less medical care services | 54.266 | 50.827 |
| College tuition and fees | 1.162 | . 877 | Energy | 6.218 | 7.109 |
| Elementary \& high school tuition \& fees | . 338 | . 258 | All items less energy | 93.782 | 92.891 |
| Child care and nursery school | . 840 | . 895 | All items less food and energy | 79.094 | 76.663 |
| Technical \& business sch. tuition \& fees | . 084 | . 077 | Commodities less food \& energy | 23.860 | 26.001 |
| Unsampled tuition, fees, \& childcare | . 083 | . 071 | Energy commodities | 2.752 | 3.330 |
| Communication | 3.087 | 3.255 | Services less energy services | 55.234 | 50.663 |
| Other goods and services | 4.312 | 4.499 | Domestically produced farm food | 7.099 | 8.204 |
| Tobacco and smoking products | . 928 | 1.441 | Utilities and public transportation | 8.785 | 9.217 |

* CPI-U are weights for BLS series "CPI, All Urban Consumers". CPI-W are weights for BLS series "CPI, Urban Wage

Earners and Clerical Workers.
Constructing the price and weight, and volume datasets

| item | Table 2: Data sources on weights and prices |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | unit | price | curr. | weight $(\mathrm{kg})$ | $\begin{gathered} \mathrm{p} / \mathrm{w} \\ (\mathrm{USD} / \mathrm{kg}) \end{gathered}$ | note |
| Apples | kg | 2.57 | CND | 1 | 1.7 | 05/00-05/01 average, Statcan Table 326-0012 |
| Audio equipment | stereo unit | 150 | USD | 6 | 25 | www.jandr.com (the largest retailer in US), includes packaging |
| Beef | ground, 1 kg | 4.63 | CND | 1 | 3.06 | 05/00-05/01 average, Statcan Table 326-0012 |
| Beer | six pack | 5.40 | USD | 2.30 | 2.35 | See Grossmann \& Markowitz (1999) |
| Car purchase | car | 24,923 | USD | 1326.13 | 18.79 | 1996 avg. extrapolated to 2000, American Automobile Manufacturers' Association 1996 |
| Car parts | tire | 100 | USD | 10 | 10 |  |
| Cheese | kg | 8.69 | USD | 1 | 8.69 | Avg. of American processed cheese (Series APU0000710211) and Cheddar cheese (Series APU0000710212) BLS, 2001 average monthly |
| Clothes |  |  |  |  |  |  |
| Clothes (men) | basket\# | USD |  |  | 50.52 | U.S. Department of Commerce, 2000 |
| Clothes (women) | basket\# | USD |  |  | 52.93 | U.S. Department of Commerce, 2000 |
| Coffee | roast, 300 g | 3.27 | CND | 0.3 | 7.20 | 05/00-05/01 average, Statcan Table 326-0012 |
| Educ. books \& supplies |  |  |  |  |  |  |
| Eggs | dozen | 1.91 | CND | 0.73 | 1.74 | 05/00-05/01 average, Statcan Table 326-0012 weight: a $30-$ dozen egg container weighs 47 lb . |
| Electricity | 500 kWh | 48.55 | USD | - | - | BLS, average 2001 price (Series APU000072621) |
| Fats and oils | basket* | 1.81 | USD | 0.598 | 3.68 | StatCan, Avg price in Calgary in Nov 2001 for Salad dressing, avg. price in NYC, Feb 2001 |
| Fish and seafood | basket ${ }^{+}$ | 2.85 | USD | 1 | 2.85 | Fish processing industry data, wholesale prices. |
| Flour | 2.5 kg | 3.37 | CND | 2.50 | 0.89 | 05/00-05/01 average, Statcan Table 326-0012 |
| Footwear |  |  |  |  |  |  |
| Footwear (men) | pair, avg of casual and athletic | 46.50 | USD | 0.73 | 63.70 |  |
| Footwear (women) | pair, athletic | 43.88 | USD | 0.56 | 81.00 |  |
| Fuel oil | liter | 0.34 | USD | 0.86 | 0.39 | Avg price, BLS 2001, Series APU000072511 |
| Furniture | bed | 200 | CND | 46.7 | 4.3 | IKEA |
| Gas | $1000 \mathrm{ft}^{3}$ | 7.45 | USD | 18.16 | 0.41 | Avg price for year 2000, Energy Information Administration, Natural Gas Monthly, Jan 2002 |
| Gasoline | liter | 0.38 | USD | 0.70 | 0.54 | Avg. price, BLS, 2001, Series APU000074714 |
| House chemicals | 75 oz pack of laundry deterg. | 2.30 | USD | 2.13 | 1.16 | 1997 NYC price extrapolated into 2001 |
| Jewelry | - |  |  |  |  |  |
| Laundry appliances | washer | 887 | USD | 158.9 | 5.58 | 2002 avg. price for Maytag |
| Liquor <br> Medical care products | 750 ml whiskey | 11.74 | USD | 0.75 | 15.65 | BLS avg. price for 1986, adjusted by CPI inflation (series APU0000720211) |
| Non-prescription med. |  |  |  |  |  |  |
| Pants | pair, jeans, avg. | 50.18 | USD | 1.36 | 36.86 | Parsley \& Wei (2001) and US Department of Commerce, avg. price 01/00-07/00 |
| PC | unit | 1000 | USD | 20 | 50 | Dell.com average price in 2002. |
| Personal care products Photo equipment | a basket ${ }^{1}$ | 12.58 | CND | 8.31 | 2.77 | 05/00-05/01 average, Statcan Table 326-0012 |
| Pork | kg, chops | 9.29 | CND | 1 | 6.14 | 05/00-05/01 average, Statcan Table 326-0012 |
| Potatoes | 4.54 kg | 3.83 | CND | 4.54 | 0.56 | 05/00-05/01 average, Statcan Table 326-0012 |
| Poultry | kg | 4.45 | CND | 1 | 2.94 | 05/00-05/01 average, Statcan Table 326-0012 |
| Prescription medicine | \% |  |  |  |  |  |
| Sport equipment | basket\% | 99.67 | USD | 2.10 | 65.00 | http://www.usolympicteam.com/sports2/ih/az equip.html |
| Sport vehicles | bicycle | 225 | USD | 15 | 15.00 |  |
| Sugar | 11 b | 0.43 | USD | 0.45 | 0.95 | BLS avg. price for 2001 (Series APU0000715212) |
| Tobacco | 200 cigs | 37.78 | CND | 0.25 | 99.80 | 05/00-05/01 average, Statcan Table 326-0012 |
| Toys | basket | 31.33 | USD | 2.55 | 13.19 | average of 5 age-group categories from Toys'R'Us 2001. |
| Video equipment | basket** | 226.67 | USD | 8.73 | 25.96 | from J\&R website, the largest US retailer, includes packaging. |
| Watches | piece | 50 | USD | 0.2 | 250 | Timex website avg. price, weight approximated |
| Wine | liter | 5.96 | USD | 1.3 | 4.58 | BLS avg. price, 2001 (series APU0000720311) |
| Fresh fruits | basket | 19.36 | USD | 8 | 2.42 | BLS avg. price, 2001 |
| Reading materials | book | 30 | USD | 0.5 | 60 |  |
| Tomatoes | kg | 2.90 | USD | 1 | 2.9 | BLS avg. price, 2001 (series APU0000712311) |

\# Men's basket: coats, blazers, trousers,


 a VCR, and a camcorder
Table 3: Data sources on volume
wage volume

|  |  | p | factor | $\left(\mathrm{m}^{3}\right)$ | (USD/m ${ }^{3}$ ) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total RER-CPI |  |  |  |  |  |  |
| Apples | kg | 2.57 | 2.622 | 0.003 | 647.4 | boxes, http://www.tis-gdv.de/tis e/ware/obst/apfel/apfel.htm |
| Audio equipment | stereo unit | 150 | 5.495 | 0.055 | 2730 | http://www.jr.com/JRProductPage.process? Product=3967701 |
| Beef | ground, 1 kg | 4.63 | 1 | 0.001 | 3057.8 | http://www.tis-gdv.de/tis e/ware/fleisch/gekuehlt/gekuehlt.htm |
| Beer | six pack | 5.40 | 1.556 | 0.004 | 1508.9 | http://www.tis-gdv.de/tis e/ware/lebensmi/bier/bier.htm |
| Car purchase | car | 24,923 | 8.399 | 11.138 | 2237.7 | http://www.fordvehicles.com/Cars/focus/features/specdimensions/ |
| Car parts | tire | 100 | 4.041 | 0.04 | 2474.6 | http://amchouston.home.att.net/stowage factors.htm |
| Cheese | kg | 8.69 | 1.397 | 0.001 | 6222 | http://www.tis-gdv.de/tis e/ware/milchpro/kaese/kaese.htm |
| Clothes |  |  |  |  |  |  |
| Clothes (men) | basket \# |  | 4.728 |  | 10686.4 | http://www.tis-gdv.de/tis e/ware/textil/konfektion/konfektion.htm |
| Clothes (women) | basket ${ }^{\text {\# }}$ |  | 4.728 |  | 11208.1 | http://www.tis-gdv.de/tis e/ware/textil/konfektion/konfektion.htm |
| Coffee | roast, 300g | 3.27 | 1.961 | 0.001 | 3671.3 | Rodrigues et. al. (2003) |
| Educ. books \& supplies Eggs | dozen | 1.91 | 2.755 | 0.002 | 630.7 | measure |
| Electricity | 500 kWh | 48.55 |  | 0.002 | 630.7 | - |
| Fats and oils | basket* | 1.81 | 1.25 | - | 2944 | German transportation database source for each component |
| Fish and seafood | basket ${ }^{+}$ | 2.85 | 1.85 | - | 1537.8 | German transportation database source for most components |
| Flour | 2.5 kg | 3.37 | 1.33 | 0.003 | 669.4 | http://amchouston.home.att.net/stowage factors.htm |
| Footwear |  |  |  |  |  |  |
| Footwear (men) | pair, avg of casual and athletic | 46.50 | 21.918 | 0.016 | 2906.3 | Mens shoe box 14-3/4" $\times 10-1 / 8^{\prime \prime} \times 5-5 / 8^{\prime \prime}$ |
| Footwear (women) | pair, athletic | 43.88 | 28.351 | 0.014 | 2857.1 |  |
| Fuel oil | liter | 0.34 | 1.163 | 0.001 | 338 |  |
| Furniture | bed | 200 | 4.73 | 0.22 | 909.1 | http://www.ikea-usa.com/webapp/wcs/stores/servlet/... <br> ...ProductDisplay?catalogId=10101\&storeId=12\&productId=32145\&... <br> $\ldots$...angId $=-1$ \&parentCats $=10103 * 10144$ |
| Gas | $1000 \mathrm{ft}^{3}$ | 7.45 | 1559.298 | 28.317 | 0.3 |  |
| Gasoline | liter | 0.38 | 1.434 | 0.001 | 337 |  |
| House chemicals | 75 oz pack of laundry deterg. | 2.30 | 10.591 | 0.021 | 109.5 | measurement |
| Jewelry |  |  |  |  |  |  |
| Laundry appliances | washer | 887 | 4.506 | 0.716 | 1238.8 | http://www.maytag.com/products/images/products/dmsearcywash.pdf |
| Liquor <br> Medical care products | 750 ml whiskey | 11.74 | 1.75 | 0.001 | 8944.8 | http://www.tis-gdv.de/tis e/ware/genuss/rum/rum.htm |
| Non-prescription med. |  |  |  |  |  |  |
| Pants | pair, jeans, avg. | 50.18 | 3.57 | 0005 | 10328 | http://www.tis-gdv.de/tis e/ware/textil/konfektion/konfektion.htm |
| PC | unit | 1000 | 25 | 0.5 | 2000 | http://www.shipit.co.uk/Overseas Removals Companies Volumes.htm |
| Personal care products Photo equipment | a basket ${ }^{1}$ | 12.58 | 8.664 | 0.024 | 346.2 | measurement of basket items |
| Pork | kg, chops | 9.29 |  | 1 | 6.14 |  |
| Potatoes | 4.54 kg | 3.83 | 1.7 | 0.002 | 3609.1 | http://www.tis-gdv.de/tis e/ware/gemuese/kartoffe/kartoffe.htm |
| Poultry | kg | 4.45 | 1 | 0.005 | 557.1 | assume same volume as beef |
| Prescription medicine | - |  |  |  |  |  |
| Sport equipment | basket ${ }^{\text {\# }}$ | 99.67 | 23.61 | 0.036 | 2753.3 | various sources for items \# |
| Sport vehicles | bicycle | 225 | 17.864 | 0.268 | 839.7 | http://www.crateworks.com/frameset.html?page=features |
| Sugar | 11 b | 0.43 | 1.354 | 0.001 | 699.5 | http://www.tis-gdv.de/tis e/ware/zucker/weiszuck/weiszuck.htm |
| Tobacco | 200 cigs | 37.78 | 0.002 | 6 | 13861 | http://www.discount-cigarettes-online.biz/templates/faq.php |
| Toys | basket | 31.33 | . | 0.2 | 156.7 | guess |
| Video equipment | basket* | 226.67 | 0.044 | 5 | 5191.4 | http://www.tis-gdv.de/tis e/ware/maschinen/unterhaltung/unterhaltung.htm |
| Watches | piece | 50 | , | 0.0012 | 41667 | dims: $20 \times 10 \times 5 \mathrm{~cm}$, volume direct |
| Wine | liter | 5.96 19.36 | 1.175 | 0.0015 | 3973.3 | same stowage factor as liquor |
| Fresh fruits | basket | 19.36 | 2.95 | 0.024 | 820.3 | German transportation database source for each component |
| Reading materials | book | 30 | 1.78 | 0.001 | 33707.9 | http://www.tis-gdv.de/tis e/ware/papier/zeitung/zeitung.htm |
| Tomatoes | kg | 2.90 | 2.373 | 0.002 | 1221.9 | http://www.tis-gdv.de/tis e/ware/gemuese/tomaten/tomaten.htm |

Basket composition identical to that of above table. Additional data sources: \#Sports basket contains ski boots (http://www.snowshack.com/head-bootbag.html), skis and bindings (http://www.snowshack.com/salomon-equipe-2pr-skibag.html), tennis racquet, basketball (http://experts.about.com/q/2551/1184149.htm), golf set (11pc, length $44 \mathrm{in}=111 \mathrm{~cm}$ ), dozen golf balls (http://www.overstock.com/cgi-bin/d2.cgi?PAGE=PROFRAME\&PROD ID=676397), hockey stick (http://www.unleash.com/picks/sportinggoods/topsportinggoodshockeysticks.asp), hockey skates ( $15-\mathrm{in} \quad \mathrm{x} \quad 9$-in $\mathrm{x} \quad 15$-in bag), and inline skates and hockey helmet http://secure1.esportspartners.com/store-redskins/main detail.cfm?nCategoryID=4\&nObjGroupID=134\&nProductID=56453

## References

[1] American Automobile Manufacturers' Association. Motor Vehicles Facts and Figures. AAMA, Washington, D.C., 1996.
[2] Anindya Banerjee, Massimiliano Marcellino, and Chiara Osbat. Some cautions on the use of panel methods for integrated series of macro-economic data. manuscript, July 2001.
[3] Caroline Betts and Michael B. Devereux. Exchange rate dynamics in a model of pricing-to-market. Journal of International Economics, 50(1):215-244, February 2000.
[4] Fabian Bornhorst. On the use of panel unit root tests on cross-sectionally dependent data: an application to PPP. Working Paper ECO 2003/24, European University Institute, November 2003.
[5] Ariel Burstein, Joao C. Neves, and Sergio Rebelo. Distribution costs and real exchange rate dynamics during exchange-rate-based stabilizations. Journal of Monetary Economics, 50:1189-1214, September 2003.
[6] Shiu-Sheng Chen and Charles Engel. Does "aggregation bias" explain the PPP puzzle? Working Paper 10304, NBER, February 2004.
[7] Mario Crucini, Chris Telmer, and Marios Zachariadis. Dispersion in real exchange rates. Mimeo, Vanderbilt University, Carnegie Mellon University, Ohio State University, February 2000.
[8] Mario Crucini, Chris Telmer, and Marios Zachariadis. Understanding European real exchange rates. American Economic Review, 95(3):724-738, June 2005.
[9] James E. Ertel and Edward B. Fowlkes. Some algorithms for linear splines and piecewise linear regression. Journal of the American Statistical Association, 71:640-648, 1976.
[10] C.W.J. Granger and Timo Teräsvirta. Modelling Nonlinear Economic Relationships. Oxford University Press, Oxford, 1993.
[11] Michael Grossmann and Sarah Markowiz. Alcohol regulation and violence on college campuses. Working Paper 7129, NBER, May 1999.
[12] Jonathan Gruber, Anindya Sen, and Mark Stabile. Estimating price elasticities when there is smuggling: the sensitivity of smoking to price in Canada. Working Paper 8962, NBER, May 2002.
[13] Bruce Hansen. Inference in TAR models. Studies in Nonlinear Dynamics and Econometrics, 2(1):1-14, April 1997.
[14] David Hummels. Have international transportation costs declined? University of Chicago, July 1999.
[15] David Hummels. Time as a trade barrier. Purdue University, July 2001.
[16] David Hummels. Towards a geography of trade costs. University of Chicago, September 2001.
[17] David Hummels and Alexandre Skiba. Shipping the good apples out? An empirical confirmation of the Alchian-Allen conjecture. Journal of Political Economy, 112:13841402, 2004.
[18] Jean Imbs, Haroon Mumtaz, Morten O. Ravn, and Helene Rey. Non linearites and real exchange rate dynamics. Journal of the European Economic Association, 1(2-3):639649, April May 2003.
[19] Jean Imbs, Haroon Mumtaz, Morten O. Ravn, and Helene Rey. Aggregation bias does explain the PPP puzzle. Discussion Paper 5237, CEPR, September 2005.
[20] Jean Imbs, Haroon Mumtaz, Morten O. Ravn, and Helene Rey. PPP strikes back: Aggregation and the real exchange rate. Quarterly Journal of Economics, forthcoming, 2005.
[21] Lutz Kilian and Mark P. Taylor. Why is it so difficult to beat the random walk forecast of exchange rates? Journal of International Economics, 60:87-107, May 2003.
[22] David E. Lebow and Jeremy B. Rudd. Measurement error in the consumer price index: Where do we stand? Finance and Economic Discussion Papers 61, The Federal Reserve Board, December 2001.
[23] Johan Lyhagen. Why not use standard panel unit root tests for testing PPP. Working Papers Series in Economics and Finance 413, Stockholm School of Economics, December 2000 .
[24] Dennis Novy. Is the iceberg melting less quickly? international trade costs after world war ii. University of Cambridge manuscript, July 2006.
[25] Dennis Novy. Trade costs in a model of pricing-to-market. University of Cambridge manuscript, July 2006.
[26] Maurice Obstfeld and Alan M. Taylor. Nonlinear aspects of goods-market arbitrage and adjustment: Heckschers commodity points revisited. Journal of the Japanese and International Economics, (11):441-479, 1997.
[27] Paul G. J. O'Connel. The overvaluation of purchasing power parity. Journal of International Economics, 44:1-19, 1998.
[28] David H. Papell. Searching for stationarity: Purchasing power parity under the current float. Journal of International Economics, (43):313-332, 1997.
[29] Melissa A. A. Rodrigues, Maria Lucia A. Borges, Adriana S. Franca, Leandro S. Oliveira, and Paulo C. Correa. Evaluation of physical characteristics of coffee during roasting. Manuscript, December 2003.
[30] Timo Teräsvirta. Specification, estimation and evaluation of smooth transition autoregressive models. Journal of the American Statistical Association, 89(425):208-218, March 1994.
[31] Howell Tong. Non-linear Time Series: A Dynamic Systems Approach. Clarendon Press, Oxford, 1990.
[32] Ruey S. Tsay. Nonlinearity tests for time series. Biometrika, 73(2):461-466, August 1986.
[33] Ruey S. Tsay. Testing and modeling threshold autoregressive processes. Journal of the American Statisctical Association, 84(405):231-240, March 1989.
[34] Asaf Zussman. Limits to arbitrage: Trading frictions and deviations from purchasing power parity. Manuscript, December 2002.

## C Figures

Figure 1: Some prices in NYC, February 2001


Figure 2: Thresholds and Half Lives



Figure 3: Drop in Canadian Tobacco taxes, 1994

| Province | Year; tax rate, \$ |  | Date of change |
| :---: | :---: | :---: | :---: |
|  | 1993 | 1994 |  |
| Provinces where <br> provincial taxes were <br> cut |  |  |  |
| Quebec | $29.61$ | 8.61 | February 1994* |
| New Brunswick | $29.45$ | $15.45$ | February 1994 |
| Ontario | $28.85$ | $9.65$ | February 1994† |
| Prince Edward Island | $35.45$ | $21.20$ | March 1994 $\ddagger$ |
| Nova Scotia | $29.45$ | $15.45$ | April 1994 |
| Provinces where provincial taxes were not cut |  |  |  |
| Newfoundland | 36.41 | 31.41 | NA§ |
| Manitoba | 31.85 | 26.85 | NA |
| Saskatchewan | 31.85 | 26.85 | NA |
| Alberta | 29.85 | 24.85 | NA |
| British Columbia | 37.85 | 32.85 | NA |

*The tax rate in Quebec subsequently increased, reaching $\$ 10.81$ in May 1995.
+The tax rate in Ontario subsequently increased, reaching $\$ 10.85$ in February 1995.
$\neq$ The tax rate in PEI was further reduced to $\$ 19.20$ in June 1994.
§NA = not applicable.

Figure 4: Effects of tobacco tax change


## D Tables

Table 4: Long run properties of exchange rates

|  | Sample: 1947:1-2000:8 |  |  | Sample: 1947:1-1969:12 |  |  | Sample: 1970:1-2000:8 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NER | RER | Rel. CPI | NER | RER | Rel. CPI | NER | RER | Rel. CPI |
| Lags $^{0}$ | 1 | 11 | 13 | 6 | 12 | 13 | 1 | 11 | 13 |
| ADF stat. ${ }^{1}$ | 0.057 | -0.923 | $-1.923^{*}$ | -0.667 | -1.195 | -1.444 | 0.471 | -0.614 | -1.495 |
| ADF stat. $^{2}$ | 0.067 | -0.884 | -1.931 | -1.545 | -2.083 | $-3.19^{* *}$ | -0.225 | -0.881 | -1.882 |
| ADF stat. $^{3}$ | $-16.6^{* * *}$ | $-5.4^{* * *}$ | $-5.5^{* * *}$ | $-9.9^{* * *}$ | $-3.35^{* *}$ | $-4.2^{* * *}$ | $-12.6^{* * *}$ | $-4.2^{* * *}$ | $-4.0^{* * *}$ |
| Half life $^{4}$ | $-(1.001)$ | $-(1.0014)$ | 146.4 | 74.2 | 27.3 | 10.5 | 14145 | $-(1.0015)$ | 140 |

Table 5: Long run properties of linearly detrended exchange rates

|  | Sample: 1947:1-2000:8 |  | Sample: $1947: 1-1969: 12$ |  |  | Sample: 1970:1-2000:8 |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NER | RER | Rel. CPI | NER | RER | Rel. CPI | NER | RER | Rel. CPI |
| Lags $^{0}$ | 11 | 1 | 13 | 13 | 12 | 12 | 11 | 13 | 13 |
| ADF stat. $^{1}$ | $-2.93^{* * *}$ | $-2.09^{* *}$ | $-2.26^{* * *}$ | $-2.57^{* * *}$ | $-3.22^{* * *}$ | $-2.11^{* *}$ | $-1.87^{*}$ | $-1.74^{*}$ | $-1.98^{* *}$ |
| ADF stat. $^{2}$ | $-2.93^{* *}$ | -2.09 | -2.25 | $-2.74^{*}$ | $3.37^{* *}$ | -2.1 | -1.86 | -1.72 | -1.99 |
| ADF stat. $^{3}$ | $-6.01^{* * *}$ | $-5.3^{* * *}$ | $-5.35^{* * *}$ | $-4.39^{* * *}$ | $-3.35^{* *}$ | $-3.95^{* * *}$ | $-4.48^{* * *}$ | $-4.16^{* * *}$ | $-4.3^{* * *}$ |
| Half life $^{4}$ | 98.7 | 64.1 | 128 | 66 | 15.4 | 13 | 154.3 | 228.3 | 321.9 |

Table 6: Long run properties of HP-detrended exchange rates

|  | Sample: 1947:1-2000:8 |  | Sample: 1947:1-1969:12 |  |  | Sample: 1970:1-2000:8 |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NER | RER | Rel. CPI | NER | RER | Rel. CPI | NER | RER | Rel. CPI |
| Lags $^{0}$ | 11 | 11 | 13 | 15 | 13 | 13 | 12 | 11 | 17 |
| ADF stat. $^{1}$ | $-8.2^{* * *}$ | $-7.4^{* * *}$ | $-7.8^{* * *}$ | $-4^{* * *}$ | $-4.6^{* * *}$ | $-5.3^{* * *}$ | $-5.4^{* * *}$ | $-5.9^{* * *}$ | $-5.6^{* * *}$ |
| ADF stat. $^{2}$ | $-8.2^{* * *}$ | $-7.4^{* * *}$ | $-7.9^{* * *}$ | $-4^{* * *}$ | $-4.6^{* * *}$ | $-5.3^{* * *}$ | $-5.4^{* * *}$ | $-5.9^{* * *}$ | $-5.6^{* * *}$ |
| ADF stat. $^{3}$ | $-9.2^{* * *}$ | $-8.6^{* * *}$ | $7.5^{* * *}$ | $-6^{* * *}$ | $-5.7^{* * *}$ | $-5.1^{* * *}$ | $-5.9^{* * *}$ | $-5.8^{* * *}$ | $-5.8^{* * *}$ |
| Half life $^{4}$ | 5 | 4.5 | 4.9 | 5 | 4.3 | 3.2 | 4.9 | 4.6 | 5.9 |

[^16]Table 7: Long run properties: ADF and half-life convergence

|  | obs | Tsay's non-linear test $\left(\mathrm{p}\right.$-value) ${ }^{1}$ | ADF p-value ${ }^{2}$ | Philips-Perron ${ }^{2}$ | half-life $_{A}$ | half-life ${ }_{B}^{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Apples | 367 | 0.000 | 0.000 | 0.000 | 5 | 6 |
| Audio equipment | 189 | 0.018 | 0.919 | 0.935 | 182 | - |
| Beef | 358 | 0.000 | 0.159 | 0.383 | 20 | 29 |
| Beer | 367 | 0.026 | 0.606 | 0.595 | 114 | - |
| Car purchase | 367 | 0.118 | 0.093 | 0.114 | 19 | 27 |
| Car maintenance | 265 | - | 0.953 | 0.954 | 1216 | - |
| Car parts | 118 | 0.066 | 0.111 | 0.133 | 22 | - |
| Cheese | 189 | - | 0.968 | 0.952 | - | - |
| Clothes | 224 | 0.125 | 0.438 | 0.514 | 26 | 83 |
| Clothes (men) | 224 | 0.097 | 0.545 | 0.593 | 34 | 265 |
| Clothes (women) | 224 | 0.132 | 0.182 | 0.337 | 15 | 26 |
| Coffee | 358 | 0.003 | 0.840 | 0.778 | 130 | - |
| Educat. books \& supplies | 71 | 0.011 | 0.936 | 0.937 | 119 | - |
| Eggs | 367 | 0.016 | 0.000 | 0.000 | 5 | 6 |
| Electricity | 367 | 0.191 | 0.670 | 0.643 | 107 | - |
| Fats and oils | 142 | 0.003 | 0.618 | 0.572 | 35 | - |
| Fish and seafood | 190 | 0.134 | 0.916 | 0.907 | 175 | - |
| Flour | 274 | 0.084 | 0.382 | 0.345 | 40 | 258 |
| Footwear | 367 | 0.007 | 0.076 | 0.124 | 21 | 31 |
| Footwear (men) | 190 | 0.166 | 0.230 | 0.338 | 15 | 27 |
| Footwear (women) | 274 | 0.010 | 0.157 | 0.375 | 19 | 32 |
| Fuel oil | 334 | 0.001 | 0.416 | 0.454 | 39 | 117 |
| Furniture | 370 | 0.020 | 0.619 | 0.625 | 59 | 804 |
| Gas | 367 | 0.010 | 0.124 | 0.095 | 16 | 21 |
| Gasoline | 367 | 0.079 | 0.422 | 0.467 | 43 | 132 |
| House chemicals | 367 | - | 0.978 | 0.962 | - | - |
| Jewelry | 118 | 0.008 | 0.340 | 0.335 | 21 | - |
| Laundry appliances | 190 | 0.194 | 0.851 | 0.846 | 94 | - |
| Liquor | 274 | 0.153 | 0.797 | 0.733 | 103 | - |
| Medical care products | 266 | - | 0.987 | 0.982 | - | - |
| Non-prescription medicine | 167 | 0.031 | 0.882 | 0.859 | 132 | - |
| Pants | 274 | 0.117 | 0.000 | 0.124 | 11 | 14 |
| PC | 35 | 0.259 | 0.398 | 0.394 | 6 | 519 |
| Personal care products | 358 | 0.215 | 0.000 | 0.884 | 338 | - |
| Photo equipment | 190 | - | 0.947 | 0.947 | 579 | - |
| Pork | 266 | - | 0.404 | 0.531 | 23 | 45 |
| Potatoes | 270 | 0.000 | 0.000 | 0.000 | 4 | 4 |
| Poultry | 367 | 0.058 | 0.016 | 0.049 | 14 | 17 |
| Prescription medicine | 190 | 0.004 | 0.993 | 0.988 | - | - |
| Sport equipment | 266 | 0.067 | 0.476 | 0.464 | 37 | 200 |
| Sport vehicles | 266 | 0.000 | 0.435 | 0.445 | 48 | - |
| Sugar | 142 | 0.041 | 0.704 | 0.697 | 39 | - |
| Tobacco | 178 | - | 0.964 | 0.951 | - | - |
| Toys | 190 | 0.093 | 0.000 | 0.569 | 31 | 622 |
| Video equipment | 58 | 0.118 | 0.614 | 0.569 | 10 | - |
| Watches | 94 | 0.014 | 0.001 | 0.003 | 2 | 3 |
| Wine | 331 | 0.086 | 0.439 | 0.422 | 69 | - |
| Airfare | 367 | 0.054 | 0.000 | 0.000 | 5 | 5 |
| Cable TV | 201 | 0.049 | 0.752 | 0.785 | 45 | - |
| Car insurance | 367 | 0.009 | 0.533 | 0.450 | 43 | 132 |
| Child care | 117 | - | 0.991 | 0.990 | 451 | - |
| Dental services | 367 | - | 0.985 | 0.994 | 260 | - |
| Fresh fruits | 367 | - | 0.859 | 0.911 | 77 | - |
| Intra-city transport | 273 | 0.202 | 0.431 | 0.426 | 32 | 102 |
| Margarine | 367 | 0.094 | 0.296 | 0.286 | 31 | 60 |
| Medical services | 189 | - | 0.975 | 0.976 | 438 | - |
| Reading materials | 273 | 0.010 | 0.000 | 0.607 | 48 | - |
| Rent | 367 | 0.030 | 0.976 | 0.962 | 1195 | - |
| Restaurant meals | 367 | 0.082 | 0.870 | 0.771 | 117 | - |
| Shelter | 265 | 0.000 | 0.000 | 0.934 | 509 | - |
| Tomatoes | 367 | 0.033 | 0.002 | 0.051 | 8 | 9 |
| Tuition | 273 | 0.001 | 0.000 | 0.014 | 44 | 779 |
| Water and sewerage | 330 | 0.089 | 0.816 | 0.803 | 120 | - |

${ }^{1}$ Test requires stationarity. ${ }^{2}$ McKinnon asymptotic p-values. ${ }^{3}$ After correcting for small-sample bias in AR(1)

Table 8: EQ-TAR Summary

|  | STD | AR(1) <br> half life | TAR(2,1,1) <br> threshold | TAR(2,1,1) <br> half life | AR(p) <br> half life | TAR(2,p,d) <br> threshold | TAR(2,p,d) <br> half life |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Foods | 0.147 | 45 | 0.144 | 34 | 41 | 0.083 | 58 |
| Vice goods | 0.188 | 72 | 0.115 | 79 | 91 | 0.134 | 105 |
| Clothing and footwear | 0.075 | 20 | 0.035 | 21 | 26 | 0.041 | 19 |
| Tech stuff | 0.085 | 156 | 0.077 | 45 | 540 | 0.063 | 38 |
| Fuels | 0.149 | 51 | 0.109 | 45 | 50 | 0.070 | 48 |
| Medical and chemical | 0.146 | 235 | 0.194 | 100 | 244 | 0.131 | 90 |
| Cars and car parts | 0.074 | 20 | 0.039 | 19 | 27 | 0.046 | 23 |
| Laundry appliances | 0.099 | 94 | 0.134 | 26 | 98 | 0.154 | 25 |
| Furniture | 0.092 | 59 | 0.125 | 30 | 67 | 0.145 | 34 |
| Services | 0.133 |  |  |  | 224 | 0.054 | 241 |
| CPI-RER | 0.111 |  | 0.071 |  | 162 | 0.012 | 213 |

Table 9: BAND-TAR Summary

|  | STD |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | AR(1) <br> half life | TAR $(2,1,1)$ <br> threshold | TAR $(2,1,1)$ <br> half life | AR(p) <br> half life | TAR(2,p,d) <br> threshold | TAR $(2, \mathrm{p}, \mathrm{d})$ <br> half life |  |
| Foods | 0.147 | 45 | 0.146 | 22 | 41 | 0.083 | 29 |
| Vice goods | 0.188 | 72 | 0.149 | 70 | 55 | 0.144 | 149 |
| Clothing and footwear | 0.075 | 20 | 0.027 | 23 | 26 | 0.022 | 31 |
| Tech stuff | 0.085 | 156 | 0.079 | 33 | 540 | 0.063 | 27 |
| Fuels | 0.149 | 51 | 0.097 | 43 | 50 | 0.069 | 50 |
| Medical and chemical | 0.146 | 235 | 0.193 | 332 | 244 | 0.105 | 527 |
| Cars and car parts | 0.074 | 20 | 0.039 | 22 | 27 | 0.035 | 26 |
| Laundry appliances | 0.099 | 94 | 0.074 | 111 | 98 | 0.154 | 45 |
| Furniture | 0.092 | 59 | 0.127 | 43 | 67 | 0.145 | 60 |
| Services | 0.133 |  |  |  | 224 | 0.065 | 160 |
| CPI-RER | 0.111 |  | 0.071 | 1733 | 162 | 0.012 | 193 |

Table 10: EQ-TAR(2,p,d) results

|  | LLR | $\begin{gathered} \mathrm{TAR}(2, \mathrm{p}, \mathrm{~d}) \\ \text { threshold } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { TAR(2,p,d) } \\ & \text { halflife } \end{aligned}$ | $\begin{gathered} \mathrm{p} \text {-value } \\ \text { (old, } 600 \text { ) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| Total RER-CPI | -9.1 | 0.012 | 213 | 0.056 |
| Apples | 20.9 | 0.073 | 6 | 0.126 |
| Audio equipment | 12.6 | 0.078 | 115 | 0.103 |
| Beef | 13.4 | 0.039 | 23 | 0.235 |
| Beer | 1.8 | 0.041 | 113 | 0.260 |
| Car purchase | 2.9 | 0.022 | 25 | 0.278 |
| Car maintenance | -1.9 | 0.086 | 470 | 0.114 |
| Car parts | 1 | 0.070 | 20 | 0.425 |
| Cheese | -2.7 | 0.081 | 563 | 0.113 |
| Clothes | 1 | 0.084 | 21 | 0.201 |
| Clothes (men) | -11.8 | 0.132 | 8 | 0.189 |
| Clothes (women) | -7.1 | 0.009 | 23 | 0.270 |
| Coffee | 1.3 | 0.223 |  | 0.070 |
| Educational books and supplies | 1.4 | 0.116 | 9 | 0.131 |
| Eggs | -1.9 | 0.034 | 7 | 0.414 |
| Electricity | 1.4 | 0.059 | 79 | 0.218 |
| Fats and oils | 2.7 | 0.033 | 53 | 0.211 |
| Fish and seafood | -2.1 | 0.152 | 27 | 0.107 |
| Flour | 20.5 | 0.157 | 27 | 0.124 |
| Footwear | -6.3 | 0.006 | 34 | 0.192 |
| Footwear (men) | -2.4 | 0.019 | 22 | 0.367 |
| Footwear (women) | -13.4 | 0.020 | 13 | 0.214 |
| Fuel oil | 4.1 | 0.112 | 45 | 0.204 |
| Furniture | 10.4 | 0.145 | 34 | 0.194 |
| Gas | 44.5 | 0.043 | 18 | 0.029 |
| Gasoline | 28.3 | 0.064 | 48 | 0.190 |
| House chemicals | -1.3 | 0.166 |  | 0.152 |
| Jewelry | -2.1 | 0.080 | 18 | 0.386 |
| Laundry appliances | -2.2 | 0.154 | 25 | 0.185 |
| Liquor | -4.1 | 0.012 | 86 | 0.075 |
| Medical care products | -4.9 | 0.027 |  | 0.091 |
| Non-prescription medicine | 2 | 0.150 | 42 | 0.143 |
| Pants | -5.1 | 0.016 | 11 | 0.327 |
| PC | -1.4 | 0.018 | 18 | 0.000 |
| Personal care products | -3.2 | 0.263 | 138 | 0.211 |
| Photo equipment | -1.1 | 0.202 | 37 | 0.114 |
| Pork | -3.6 | 0.013 | 15 | 0.288 |
| Potatoes | 1.3 | 0.065 | 14 | 0.356 |
| Poultry | 20.5 | 0.086 | 15 | 0.103 |
| Prescription medicine | -3.7 | 0.047 |  | 0.077 |
| Sport equipment | -4.3 | 0.055 | 49 | 0.183 |
| Sport vehicles | 43.1 | 0.183 | 11 | 0.066 |
| Sugar | 1.6 | 0.030 | 23 | 0.410 |
| Tobacco | 106.8 | 0.301 | 172 | 0 |
| Toys | 10.8 | 0.145 | 18 | 0.201 |
| Video equipment | 5.9 | 0.012 | 18 | 0.177 |
| Watches | -5.2 | 0.007 | 3 | 0.332 |
| Wine | 30.1 | 0.230 | 47 | 0.029 |
| Airfare | -2.3 | 0.015 | 11 |  |
| Cable TV | 22.1 | 0.042 | 51 |  |
| Car insurance | 23.2 | 0.025 | 48 |  |
| Child care | 10.1 | 0.018 |  |  |
| Dental services | 9.4 | 0.046 |  |  |
| Fresh fruits | -12.5 | 0.051 | 11 |  |
| Intra-city transport | 4.9 | 0.036 | 51 |  |
| Margarine | 0.9 | 0.117 | 15 |  |
| Medical services | 0.3 | 0.161 |  |  |
| Reading materials | -2.2 | 0.017 | 48 |  |
| Rent | -3.3 | 0.016 | 1066 |  |
| Restaurant meals | 5 | 0.040 | 63 |  |
| Shelter | -2.2 | 0.033 | 146 |  |
| Tomatoes | -28.5 | 0.042 | 6 |  |
| Tuition | -0.05 | 0.017 | 17 |  |
| Water and sewerage | -2.7 | 0.114 | 75 |  |

LLR test p-values obtained by Monte Carlo simulation, 5000 iterations.

Table 11: BAND-TAR (2,p,d) results

|  | LLR | $\begin{gathered} \mathrm{TAR}(2, \mathrm{p}, \mathrm{~d}) \\ \text { threshold } \end{gathered}$ | $\begin{gathered} \text { TAR(2,p,d) } \\ \text { halflife } \end{gathered}$ | p-value |
| :---: | :---: | :---: | :---: | :---: |
| Total RER-CPI | -9 | 0.012 | 193 | 0.057 |
| Apples | 23 | 0.073 | 6 | 0.094 |
| Audio equipment | 13 | 0.076 | 86 | 0.087 |
| Beef | 15.1 | 0.039 | 23 | 0.243 |
| Beer | 1.3 | 0.041 | 144 | 0.179 |
| Car purchase | 1.2 | 0.022 | 30 | 0.249 |
| Car maintenance | -1.9 | 0.167 | 58 | 0.110 |
| Car parts | 6.5 | 0.048 | 21 | 0.446 |
| Cheese | -1 | 0.163 | 24 | 0.106 |
| Clothes | -2.2 | 0.087 | 36 | 0.208 |
| Clothes (men) | -11.8 | 0.010 | 46 | 0.182 |
| Clothes (women) | -7.3 | 0.009 | 24 | 0.229 |
| Coffee | 1.4 | 0.225 | 107 | 0.071 |
| Educational books and supplies | -1.7 | 0.116 | 22 | 0.090 |
| Eggs | -4 | 0.033 | 8 | 0.413 |
| Electricity | 2.5 | 0.055 | 71 | 0.211 |
| Fats and oils | 3.1 | 0.033 | 49 | 0.185 |
| Fish and seafood | -2.5 | 0.126 | 50 | 0.107 |
| Flour | 17.3 | 0.157 | 48 | 0.230 |
| Footwear | -6.6 | 0.006 | 35 | 0.164 |
| Footwear (men) | -3 | 0.006 | 22 | 0.365 |
| Footwear (women) | -14.1 | 0.020 | 39 | 0.212 |
| Fuel oil | 5.9 | 0.112 | 48 | 0.206 |
| Furniture | 10.4 | 0.145 | 60 | 0.165 |
| Gas | 41.9 | 0.043 | 28 | 0.088 |
| Gasoline | 28.7 | 0.064 | 51 | 0.134 |
| House chemicals | -1.3 | 0.125 | 188 | 0.192 |
| Jewelry | -1.3 | 0.029 | 17 | 0.398 |
| Laundry appliances | -2.3 | 0.154 | 45 | 0.194 |
| Liquor | -4.1 | 0.012 | 86 | 0.1 |
| Medical care products | -4.9 | 0.027 | 9634 | 0.079 |
| Non-prescription medicine | 0.9 | 0.150 | 101 | 0.144 |
| Pants | -5.6 | 0.016 | 13 | 0.291 |
| PC | -1.6 | 0.018 | 22 | 0.000 |
| Personal care products | -2.2 | 0.177 | 165 | 0.236 |
| Photo equipment | 1.2 | 0.202 | 5 | 0.0104 |
| Pork | -3.6 | 0.013 | 15 | 0.286 |
| Potatoes | -0.6 | 0.065 | 14 | 0.175 |
| Poultry | 18.6 | 0.086 | 34 | 0.296 |
| Prescription medicine | -4 | 0.047 | 1655 | 0.064 |
| Sport equipment | -5.6 | 0.009 | 50 | 0.224 |
| Sport vehicles | 40.5 | 0.183 | 13 | 0.085 |
| Sugar | 2.7 | 0.030 | 21 | 0.375 |
| Tobacco | 107.5 | 0.303 | 106 | 0.000 |
| Toys | 8.7 | 0.120 | 161 | 0.211 |
| Video equipment | 5.6 | 0.012 | 20 | 0.169 |
| Watches | -3.4 | 0.008 | 3 | 0.273 |
| Wine | 27 | 0.230 | 409 | 0.090 |
| Airfare | -2.4 | 0.015 | 11 | 0.319 |
| Cable TV | 22.4 | 0.042 | 50 | 0.077 |
| Car insurance | 23.2 | 0.025 | 51 | 0.141 |
| Child care | 10 | 0.019 | 461 | 0.164 |
| Dental services | 8.4 | 0.046 |  | 0.161 |
| Fresh fruits | -13 | 0.051 | 11 | 0.324 |
| Intra-city transport | 5.2 | 0.061 | 60 | 0.191 |
| Margarine | 1 | 0.054 | 32 | 0.247 |
| Medical services | 0.9 | 0.166 | 165 | 0.170 |
| Reading materials | -2.4 | 0.017 | 51 | 0.102 |
| Rent | -3.1 | 0.016 | 542 | 0.121 |
| Restaurant meals | 5.1 | 0.040 | 68 | 0.053 |
| Shelter | -1.7 | 0.033 | 119 | 0.041 |
| Tomatoes | -28.5 | 0.042 | 6 | 0.443 |
| Tuition | 1.3 | 0.028 | 18 | 0.431 |
| Water and sewerage | -1.6 | 0.114 | 76 | 0.239 |

LLR test p-values obtained by Monte Carlo simulation, 5000 iterations.

Table 12: Threshold regressions

| dep. var. | $\begin{gathered} 1 \\ \operatorname{Thr}_{B} \end{gathered}$ | $\begin{gathered} 2 \\ \operatorname{Thr}_{B} \end{gathered}$ | $\begin{gathered} 3 \\ \mathrm{Thr}_{B} \end{gathered}$ | $\begin{gathered} 4 \\ \operatorname{Thr}_{B} \end{gathered}$ | $\begin{gathered} 5 \\ \operatorname{Thr}_{B} \end{gathered}$ | $\begin{gathered} 6 \\ \operatorname{Thr}_{B} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cnst | $8.7^{* * *}$ | 11*** | $8.7{ }^{* * *}$ | 7.8 ${ }^{* * *}$ | 10*** | 10*** |
|  | (0.000) | (0.000) | (0.000) | (0.000) | (0.000) | (0.000) |
| $\mathrm{P} / \mathrm{W}$ | -0.036 | -0.073 ${ }^{* * *}$ | -0.061 ${ }^{* * *}$ | - | -0.17 ${ }^{* * *}$ | - |
|  | (0.168) | (0.006) | (0.008) |  | (0.002) |  |
| $\mathrm{P} / \mathrm{W}^{2}$ | (0.168) | (0.006) | (0.008) | - | 0.0005 ${ }^{* *}$ | - |
|  |  |  |  |  | (0.021) |  |
| $\log (\mathrm{P} / \mathrm{W})$ | - | - | - | - | - | $\begin{gathered} -1.46^{* * *} \\ (0.01) \end{gathered}$ |
| $\mathrm{P} / \mathrm{V}$ | - | - | - | -0.0001 | - | - |
|  |  |  |  | (0.11) |  |  |
| $\mathrm{D}_{t o b}$ | - | $29^{* * *}$ | $28^{* * *}$ | 24*** | 32 ${ }^{* * *}$ | $27^{* * *}$ |
|  |  | (0.001) | (0.000) | (0.001) | (0.000) | (0.000) |
| tariff | - | -14.5 | - | - | - |  |
|  |  | (0.6) |  |  |  |  |
| CPI weight | - | -2.2* | - | - | - | - |
|  |  | (0.098) |  |  |  |  |
| Herfindahl | - | 0.001 | - | - | - | - |
|  |  | (0.57) |  |  |  |  |
| $\mathrm{R}^{2}$ | 0.05 | 0.46 | 0.37 | 0.29 | 0.46 | 0.35 |
| F-stat | 0.17 | 0.003 | 0.002 | 0.002 | 0.000 | 0.000 |
| N | 41 | 34 | 41 | 41 | 41 | 41 |

p-values in parentheses. $\mathrm{A}^{*} \sim 10 \%,^{* *} 5 \%$ and ${ }^{* * *} 1 \%$ signifi-
cance.

Table 13: Threshold regressions - robustness

|  | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| dep. var. | $\operatorname{Thr}_{B, N T}$ | $\operatorname{Thr}_{B, N T}$ | $\operatorname{Thr}_{B, N T E}$ | $\operatorname{Thr}_{B, N T E}$ | $\operatorname{Thr}_{B, N T A E}$ | $\operatorname{Thr}_{B, N T A E}$ |
| Cnst | $\mathbf{8 . 6 8}^{* * *}$ | $\mathbf{8 . 4 2}^{* * *}$ | $\mathbf{8 . 9}^{* * *}$ | $\mathbf{7 . 9}^{* * *}$ | $\mathbf{8 . 7}^{* * *}$ | $\mathbf{7 . 7}^{* * *}$ |
|  | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ | $(0.000)$ |
| P/W | $\mathbf{- 0 . 0 5 9 ^ { * * }}$ | - | $\mathbf{- 0 . 0 6 4}^{* * *}$ | - | $\mathbf{- 0 . 0 6 2}^{* * *}$ | - |
|  | $(0.013)$ |  | $(0.008)$ |  | $(0.006)$ | - |
| P/V | - | $\mathbf{- 0 . 0 0 0 2}^{* *}$ | - | $\mathbf{- 0 . 0 0 0 1 2}$ |  |  |
|  |  | $(0.052)$ |  | $(0.107)$ | - | $\mathbf{- 0 . 0 0 0 1}^{*}$ |
| $\mathrm{R}^{2}$ | 0.16 | 0.1 | 0.18 | 0.07 | 0.21 | $(0.10)$ |
| F-stat | 0.013 | 0.05 | 0.008 | 0.048 | 0.006 | 0.08 |
| N | 2.36 | 2.48 | 38 | 38 | 35 | 35 |

$\overline{\text { p-values in parentheses. } \mathrm{A}^{*} \sim 10 \%,{ }^{* *} 5 \% \text { and }{ }^{* * *} 1 \% \text { significance. } " N T " \text { is a regression excluding }}$ tobacco due to a large discrete jump in its relative price in 1994 following a tax change. "NTE" excludes tobacco and energies (gasoline, natural gas). "NTAE" excludes tobacco, alcohol (liquor, beer, wine) and energies (gasoline, natural gas)

Table 14: Threshold regressions

|  | Tobit |  |  |  |  |  | OLS, Non-linear series only |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Non-linear only |  |  | Non-lin. \& Stationary |  |  |  |  |  |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 0 |
| Const. | 7.6 ${ }^{*}$ | $8.6{ }^{* * *}$ | $10^{* * *}$ | $12^{* * *}$ | $10^{* * *}$ | $11^{* * *}$ | 11** | $\mathbf{9}^{* * *}$ | $10^{* * *}$ |
|  | (0.06) | (0.00) | (0.000) | (0.00) | (0.00) | (0.00) | (0.02) | (0.00) | (0.00) |
| P/W | -0.062* | -0.058** | -0.17** | -0.076 ${ }^{* * *}$ | -0.067 ${ }^{* * *}$ | -0.18*** | -0.066** | -0.05** | -0.14** |
|  | (0.06) | (0.036) | (0.022) | (0.003) | (0.004) | (0.001) | (0.026) | (0.042) | (0.048) |
| $(\mathrm{P} / \mathrm{W})^{2}$ | - | - | 0.0006* | - | - | 0.0006** | - | - | 0.0004 |
|  |  |  | (0.057) |  |  | (0.013) |  |  | (0.17) |
| CPI ${ }^{\text {weight }}$ | -6.46* | -5.92** | -5.8** | -3.08** | -2.4** | -2.2* | -1.8 | - | - |
|  | (0.07) | (0.045) | (0.037) | (0.034) | (0.05) | (0.056) | (0.2) |  |  |
| Tariff | 10.6 | - | - | -14.4 | - | - | -3.1 | - | - |
|  | (0.78) |  |  | (0.59) |  |  | (0.93) |  |  |
| Herfindahl | 0.001 | - | - | -0.00048 | - | - | -0.002 | - | - |
|  | (0.72) |  |  | (0.80) |  |  | (0.53) |  |  |
| $\mathrm{D}_{\text {tob }}$ | 34*** | 35*** | $35^{* * *}$ | $33^{* * *}$ | 30*** | $35^{* * *}$ | $29^{* *}$ | 26*** | $30^{* * *}$ |
|  | (0.00) | (0.00) | (0.00) | (0.00) | (0.00) | (0.00) | (0.013) | (0.00) | (0.00) |
| N | 34 | 41 | 41 | 34 | 41 | 41 | 23 | 30 | 30 |
| LogL or R ${ }^{2}$ | 17.3 | 28.3 | 30.1 | 42.6 | 53.7 | 56.8 | 0.5 | 0.39 | 0.43 |
| LR $\chi^{2}$ or F-prob | 16.3 | 19.6 | 23.4 | 21.3 | 21.8 | 28.2 | 0.023 | 0.012 | 0.002 |

$\overline{\text { p-values in parentheses. } \mathrm{A}^{*} \sim \text { sig. at } 10 \%,{ }^{* *} \text { at } 5 \% \text { and }{ }^{* * *} \text { at } 1 \% \text {. }{ }^{~} \mathrm{D}_{\text {tob }} \text { " is a dummy variable }}$
(= 1 for tobacco) due to a large discrete jump in its relative price in 1994 following a tax change.

Table 15: Threshold regressions (estimates with drop in transport costs)

|  | Tobit |  |  |  |  |  | OLS, Non-linear series only |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Non-linear only |  |  | Non-linear and Stationary |  |  |  |  |  |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| Cnst | $9^{* *}$ | $11^{* * *}$ | $12^{* * *}$ | $13^{* * *}$ | $11^{* * *}$ | $13^{* * *}$ | $13.5{ }^{* * *}$ | $13^{* * *}$ | $11^{* * *}$ |
|  | (0.045) | (0.00) | (0.00) | (0.00) | (0.00) | (0.00) | (0.007) | (0.00) | (0.00) |
| P/W | -0.071** | -0.067** | -0.19*** | -0.085 ${ }^{* * *}$ | -0.076*** | -0.2 ${ }^{* * *}$ | -0.077 ${ }^{* * *}$ | -0.06** | -0.06** |
|  | (0.039) | (0.025) | (0.010) | (0.003) | (0.003) | (0.001) | (0.009) | (0.018) | (0.018) |
| $(\mathrm{P} / \mathrm{W})^{2}$ | (0.039) | (0.025) | 0.0006* | - |  | 0.0006** | ) | (0.018) | 0.0004 |
|  |  |  | (0.061) |  |  | (0.013) |  |  | (0.174) |
| CPI ${ }^{\text {weight }}$ | -9.2 ${ }^{* *}$ | -8.84** | -7.8** | -3.8** | -3.2** | $-3^{* *}$ | -10.6** | -8.4** | - |
|  | (0.043) | (0.02) | (0.025) | (0.018) | (0.029) | (0.029) | (0.023) | (0.032) |  |
| tariff | 11.1 |  |  | -14.6 | - | - | -5.1 | - | - |
|  | (0.78) |  |  | (0.62) |  |  | (0.88) |  |  |
| Herfindahl | 0.002 | - | - | 0.0001 | - | - | 0.0033 | - | - |
|  | (0.60) |  |  | (0.96) |  |  | (0.31) |  |  |
| $\mathrm{D}_{\text {tob }}$ | $37^{* * *}$ | 40*** | $44^{* * *}$ | $34^{* * *}$ | $33^{* * *}$ | $38^{* * *}$ | $34^{* * *}$ | $36^{* * *}$ | 32*** |
|  | (0.003) | (0.00) | (0.00) | (0.00) | (0.00) | (0.00) | (0.004) | (0.00) | (0.00) |
| N | 34 | 41 | 41 | 34 | 41 | 41 | 23 | 30 | 30 |
| LogL or $\mathrm{R}^{2}$ | 18.5 | 26.2 | 28 | 39.3 | 49.3 | 52.5 | 0.61 | 0.47 | 0.41 |
| LR $\chi^{2}$ or F-prob | 16.3 | 21.8 | 25.4 | 21.2 | 21.8 | 28.19 | 0.004 | 0.000 | 0.003 |

( $=1$ for tobacco) due to a large discrete jump in its relative price in 1994 following a tax change.

Table 16: Half life regressions

| dep. var. | $\begin{gathered} 1 \\ \mathrm{hl}_{B} \end{gathered}$ | $\begin{gathered} 2 \\ \mathrm{hl}_{B, N T} \\ \hline \end{gathered}$ | $\begin{gathered} 3 \\ \mathrm{hl}_{B, N T A E} \\ \hline \end{gathered}$ | $\begin{gathered} 4 \\ \mathrm{hl}_{B, N T A E} \\ \hline \end{gathered}$ | $\begin{gathered} 5 \\ \mathrm{hl}_{B, N T A E} \\ \hline \end{gathered}$ | $\begin{gathered} 6 \\ \mathrm{hl}_{B, N T A E} \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cnst | 60*** | $\mathbf{7 9}^{* * *}$ | 62 ${ }^{* * *}$ | 34*** | 40*** | $50^{* * *}$ |
|  | (0.002) | (0.000) | (0.000) | (0.000) | (0.000) | (0.000) |
| P/W | -0.5* | -0.45* | -0.31* | - | -0.27* | -0.33** |
|  | (0.06) | (0.096) | (0.074) |  | (0.085) | (0.036) |
| Stow. factor | - | - | - | 1.18** | $1.3{ }^{* * *}$ | 1.14** |
|  |  |  |  | (0.017) | (0.008) | (0.019) |
| $\mathrm{D}_{\text {chill }}$ | -66** | -54* | -37** | - | - | -28 |
|  | (0.027) | (0.066) | (0.045) |  |  | (0.11) |
| tariff | $\begin{gathered} 468^{*} \\ (0.085) \end{gathered}$ | - |  | - | - | (11) |
| $\mathrm{R}^{2}$ | 0.18 | 0.12 | 0.16 | 0.16 | 0.24 | 0.30 |
| F-stat(prob) | 0.058 | 0.086 | 0.063 | 0.017 | 0.013 | 0.011 |
| N | 41 | 40 | 35 | 35 | 35 | 35 |

p-values in parentheses. $\mathrm{A}^{*} \sim 10 \%,{ }^{* *} 5 \%$ and ${ }^{* * *} 1 \%$ significance. " $N T$ " is a regression excluding tobacco due to a large discrete jump in its relative price in 1994 following a tax change. " ${ }_{N T A E}$ " is a regression excluding tobacco, alcohol and energies (the latter two due to poor tradability). Stowage factor is a ratio of weight to stowage space of a product, measured in ton $/ \mathrm{m}^{3}$. " $\mathrm{D}_{\text {chill }}$ " is a dummy variable $=1$ for beef, cheese, eggs, fish and seafood, poultry, fresh fruits, margarine and tomatoes.

Table 17: Half-life regressions, robustness

|  | AR(p) | Conditional half-lives |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Tobit |  |  | OLS, Non-lin series only |  | OLS, Lin. control |  |
|  |  | Non-lin only | Non-lin | Station. |  |  |  |  |
| Cnst | 1 | 2 | 3 | 4 | 6 | 7 | 8 | 9 |
|  | 104*** | 85* | $120^{* * *}$ | $85^{* * *}$ | $117^{*}$ | $57^{* *}$ | $\mathbf{9 6}^{* * *}$ | 66** |
|  | (0.001) | (0.080) | (0.001) | (0.002) | (0.057) | (0.02) | (0.005) | (0.002) |
| P/W | -0.51* | -0.61* | -0.69** | -0.55** | -0.64* | -0.5* | -0.62** | -0.5* |
|  | (0.081) | (0.099) | (0.015) | (0.052) | (0.085) | (0.094) | (0.046) | (0.06) |
| CPI ${ }^{\text {weight }}$ | -4.32 | -72.8* | -28 | - | -51 $(0.36)$ | - | -6.3 | - |
|  | (0.76) | (0.089) | (0.13) |  | (0.36) |  | (0.69) |  |
| tariff | -0.5 | 666 | 502 | 639** | 790 | 712** | 440 | 456* |
|  | (0.42) | (0.13) | (0.11) | (0.045) | (0.36) | (0.052) | (0.20) | (0.098) |
| Herfindahl | -0.02 | -0.34 | -0.046* | -0.035* | -0.038 |  | -0.02 | (0) |
|  | (0.33) | (0.32) | (0.066) | (0.096) | (0.36) |  | (0.38) |  |
| $\mathrm{D}_{\text {tob }}$ | - | 171 | 133 | - | 107 | - | 70 | - |
|  |  | (0.156) | (0.12) |  | (0.42) |  | (0.43) |  |
| $\mathrm{D}_{\text {chill }}$ | - | -77.2 | -85.7 ${ }^{* *}$ | -78.5** | -111.5* | $-87^{* *}$ | -77* | -68** |
|  |  | (0.136) | $(0.025)$ | (0.044) | (0.056) | (0.019) | (0.065) | (0.024) |
| N | 31 | 34 | 34 | 34 | 23 | 30 | 34 | 41 |
| $\mathrm{R}^{2}$, LogL | 0.16 | -143 | -181 | -183 | 0.32 | 0.25 | 0.24 | 0.19 |
| F-prob, LR $\chi^{2}$ |  | 9.7 | 12.9 | 8.57 | 0.33 | 0.055 | 0.37 | 0.099 | due to a large discrete jump in its relative price in 1994 following a tax change. " $\mathrm{D}_{\text {chill" }}$ is a chilling dummy $=1$ for items requiring refrigeration. "Linearity control" includes a dummy $=1$ for series that can not reject linearity.


[^0]:    *Private Bag 102 904, Auckland, New Zealand, ph: +649-414-0800 ext 9474, fax: +649-441-8177, email: m.berka@massey.ac.nz

[^1]:    ${ }^{1}$ To the extent that this heterogeneity is important for our understanding of the persistence in the deviations of real exchange rates (see the "aggregation bias" discussion: Imbs et. al. (2004), (2005), Chen and Engel (2004)), this result contributes to our understanding of PPP puzzle as well.

[^2]:    ${ }^{2}$ For example, a $10 \%$ difference in price of a PC between downtown and a suburb may offset the transport costs to a more distant location. But a $10 \%$ price difference of a less valuable good - e.g., an equally-sized bag of potatoes - may be insufficient to justify the transport from an equally far-away location.

[^3]:    ${ }^{3}$ Transport costs also matter through their importance in distribution. Burstein et. al. (2003) find distribution margins can account for up to $60 \%$ of price differences between US and some latin-American countries.
    ${ }^{4}$ Such non-linearity also exists in the presence of other reasons for trade.

[^4]:    ${ }^{5}$ Through the effects of uncertainty in a fixed-cost environment.
    ${ }^{6}$ Regressions in Hummels (2001) contain up to half million datapoints
    ${ }^{7}$ Bigger trade routes justify use of larger vessels, longer trains, etc.

[^5]:    ${ }^{8}$ See Crucini, Telmer and Zachariadis (2005) for a price level analysis that documents widespread law of one price violations (hence mean does not equal parity) across the EU.
    ${ }^{9}$ The services are included only to allow an indirect check of data consistency. Lack of tradability of services in this dataset lead one to expect wider threshold estimates than for goods.
    ${ }^{10}$ Source: CPI all urban consumers, Bureau of Labor Statistics, December 2001. Some of the groups are a subset of other groups - all such double accounts are accounted for in this reported measure.

[^6]:    ${ }^{11}$ This data can not be obtained from a single source.
    ${ }^{12}$ A website run by the German Insurance Association http://www.tis-gdv.de/tis e/ware/inhalt.html

[^7]:    ${ }^{13}$ Self-exciting threshold autoregressive (SETAR) models can be thought of as a combination of several (typically two) regimes which differ in the degree of stationarity they impose on the series. The decision on which regime shall the variable observe depends on a position of a control variable - in "self-exciting" models this is just a lagged value of the examined series.
    ${ }^{14}$ Aggregation would make smooth threshold autoregressive models more appropriate. Smooth threshold autoregressive models are a fluid combination of a non-stationary and a stationary regime akin to a string. A larger deviation of the RER rises with the weight placed on the stationary regime relative to the nonstationary one. Therefore, reversion occurs for any deviation and its strength rises in the size of the deviation (see Tong (1990), Granger and Teräsvirta (1993) for reference on non-linear time series analysis).
    ${ }^{15}$ One threshold following sufficient appreciation, another one after depreciation.

[^8]:    ${ }^{16}$ Both tests take into account the appropriate lag structure chosen by analyzing the partial autocorrelation function.
    ${ }^{17}$ With two symmetric thresholds, Tsay's test (Tsay 1986) is more appropriate than Hansen's (1997) single-threshold non-linearity test (Tsay's the test is described in Appendix A.2).
    ${ }^{18}$ The precision with which we can conclude non-linearity or non-stationarity depends on the length and breadth of the sample as well as on whether the test statistic controls for the serial correlation of the error terms. O'Connel (1998) shows how failure to account for serial correlation leads to serious size distortions. Papell (1997) shows that various panel datasets provide stronger rejection of the unit root hypothesis than a similar time-series analyses. While panels improve the power of unit root tests, they suffer from series of other problems (see, e.g., Lyhagen (2000), Bornhorst (2003), Banerjee et. al. (2001)). In addition, power of unit root tests drops further when the underlying DGP is not linear.

[^9]:    ${ }^{19}$ For groups of goods, a weighted average tariff computed using CPI weights of constituent products is computed.
    ${ }^{20}$ Value-added based index is used. Data is available from http://www.census.gov/epcd/www/concentration.html.
    ${ }^{21}$ Due to an increase in smuggling of cigarettes, Canadian federal and provincial governments lowered cigarette taxes, leading to a structural break in tobacco price differences. The tax drop occurred at different times, and in different amounts, in different Canadian provinces (figure 3, see Gruber et. al. (2002)) for details), making it impossible to remove this outlier point from aggregate Canadian tobacco price index. The enormous jump in the tobacco real exchange rate (figure 4) is interpreted as a non-linearity by the TAR estimation and causes a mis-specified threshold estimate for tobacco.
    ${ }^{22}$ Equation (2) is in levels while TAR estimates relate to $\log (R E R)$.

[^10]:    ${ }^{23}$ Obstfeld and Taylor (1997) and Imbs et. al. (2003) also report insignificance of tariffs.
    ${ }^{24}$ This overall decline rate is pro-rated to the sample length, and the thresholds are forced to decline at this rate for all series over their sample period.

[^11]:    ${ }^{25}$ The variables equals 1 for goods requiring refrigeration in transport. The hypothesis is that the cost of refrigeration would require quicker transport, lowering conditional half-life.
    ${ }^{26}$ This may also be a consequence of partial substitution into cheaper but slower transport modes for goods that have larger marginal transport costs (here identified by their physical characteristics).

[^12]:    ${ }^{27}$ See Granger and Teräsvirta (1993), Teräsvirta(1994), Tsay (1986), Tsay(1989).
    ${ }^{28}$ Selected combination is tested for residual serial correlation using Breusch-Goodfrey LM test and by examining the Q-statistic, and for the residual normality using Lomnicki-Jarque-Berra statistic. Residual normality is frequently rejected which can be result of the sample size. Most of the time, these criteria select the same model.

[^13]:    ${ }^{29}$ For $p=1$, half-life $=-\frac{\log (2)}{\log \left(1+\hat{\beta}^{* g}\right)}$ where $\hat{\beta}^{* g}$ is Kendall's bias-adjusted slope coefficient: $\hat{\beta}^{* g}=\frac{n \beta+1}{n-3}$.

[^14]:    ${ }^{30}$ Cases are analyzed in an ordered fashion because of the lack of knowledge of the position of a threshold ex-ante.

[^15]:    ${ }^{31}$ Therefore $P_{b}=\left(\bar{z}_{b}^{\prime} \bar{z}_{b}{ }^{-1}\right)$.

[^16]:    All series are demeaned and in logarithms.
    ${ }^{0}$ Lags may vary for ADF tests in differences, depending on the PACF criteria.
    ${ }^{1}$ Augmented Dickey-Fuller test in levels, no intercept, no trend.
    ${ }^{2}$ Augmented Dickey-Fuller test in levels, with intercept, no trend.
    ${ }^{3}$ Augmented Dickey-Fuller test in differences, with intercept, no trend.
    ${ }^{4} \mathrm{AR}(1)$ half-life is calculated without a constant.

