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# Interaction between vertical and horizontal tax competition: evidence and some theory

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## Abstract

The aim of this paper is to determine to what extent and how federal taxes affect local tax decisions. Testing the impact of an increase in the federal tax on horizontal tax competition with Canada-US data for 1984–1994, we find evidence that an increase in federal tax affects horizontal tax competition. The novelty of our approach is that it indirectly tests the effect of an increase in federal tax on provincial tax, by testing whether provincial reaction to an increase in neighboring tax changes according to the federal tax level. The test allows for control of yearly macroeconomic shocks by inserting dummies for each year. These are not used in the empirical literature on vertical tax competition because they would cause perfect collinearity with the federal tax.

**Keywords:** horizontal externality, vertical externality, tax competition, tax rate.

**JEL classification:** H21.

## 1 Introduction<sup>1</sup>

Federal tax is fixed in the cross section and does not normally vary by province or state. The literature regresses local tax rate on the federal tax rate as Besley and Rosen (1998) do, finding a positive coefficient. This method prevents checking for year effects, because the federal tax rate in a panel data set does not have a state dimension, and insertion of year effects results in an insignificant coefficient for the federal tax rate, which is a linear combination of year effects. The typical problem in these studies is that the federal tax-coefficient can be significant because it picks up yearly macroeconomic shocks. Esteller-Moré and Solé-Ollé (2001) analyzed the vertical externality for the US using a state average federal income tax rate instead of the marginal federal tax rate. The tax rate calculated in this way

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varies by state, so that the method is able to control for year effects. They also find a positive coefficient. Andersson et al. (2004) test the presence of vertical externality on income tax rates using data on the Swedish local and regional public sector for the period 1981-1990. In this case they are able to control for year fixed effects because their high jurisdiction tax level varies by counties, which are 24: they find a negative coefficient.

Interestingly, some recent studies put together horizontal and vertical fiscal externalities with contrasting results. Goodspeed (2000) used a data set with 13 OECD provinces for the period 1975–1984. A poverty index was used as a measure of intra-province mobility: the poorer the less mobile people are, the smaller is the horizontal externality. The author used local income tax as a dependent variable and found a negative sign for the federal tax rate and for the mobility index. Boadway and Hayashi (2001), using Canadian annual data for 1963–1996, tested horizontal and vertical tax competition by considering corporate taxes on businesses. They found a negative sign for the vertical externality and positive sign for the horizontal externality. Each estimate was for a single province or an average province. This result is confirmed by Karkalakos, Kotsogiannis (2007), who extend the previous work exploring fiscal interactions for all ten fiscal autonomous provincial governments. Revelli (2003) studied the non-metropolitan two-tier system of local government in England—comprising 34 counties and 238 districts—using per capita current expenditure for the financial year 2000/2001, disaggregated into various functions of interest. He found that horizontal externality disappears when a vertical externality coefficient is introduced, arguing that the only relevant externality is the last one. Interestingly, Devereux et al. (2007) found the opposite for the US using panel data for 1977–1997: vertical externality for cigarette and gasoline taxes was not significant if there was also a test for horizontal externality, which was significant. None of these studies, even if controlling for neighboring taxes, have checked for year effects. Finally Brulhart and Jametti (2006) use a local-regional panel data and build an income tax rate index for Switzerland for the years 1985, 1991, 1995 and 1998. They find a positive link between the tax chosen by the canton and that chosen by the municipality, and that vertical tax externality prevails over horizontal tax externality. They obtain this latter result by using an indirect estimate of the sum of these two externalities through a "smallness" index of the municipality. They can control for year effects because, as in Andersson et al. (2004), the high jurisdiction tax level varies by canton, of which there are 23 in their panel.

This study introduces year effects and estimates the effect of a change in federal tax on tax-competition behavior. If an increase in federal tax affects the tax-rate choice of a province after an increase in the tax rate on the same mobile tax base of a neighboring province, this means that there is a link between tax rates chosen at the federal and local levels on the same tax base. This test enables one to control for year effects, avoiding collinearity with the federal tax. Goodspeed (2002), extending some earlier results (Goodspeed, 2000), found that

the vertical externality affects the horizontal externality (measured through a poverty index; Goodspeed, 2000) in an income tax environment by offsetting it. In his study, differently from the present one, there was no check for year effects. Moreover, the present study uses tax rates rather than the ratio of tax revenue to GNP; it also does not estimate the horizontal externality, but the tax competition coefficient and interacts the independent tax variable (the mean of the taxes of the neighbors) with the federal tax variable. It finds that the federal tax rate affects the neighboring average tax rate in explaining the variance of a province's own tax rate.

The remainder of the paper is organized as follows: the second section reports an empirical test. Section 3 outlines a theoretical model and explains the empirical results. Section 4 concludes.

## 2 The empirical test

We use a Canada<sup>2</sup>–US data set for 1984–1994 to estimate if there is any significant strategic link between federal and provincial taxation when tax is levied on the same tax base. In the literature this has been carried out by regressing the local tax rate on the federal tax rate (Besley and Rosen, 1998). It should be noted that the federal tax coefficient can be significant because it picks up a year, or trend effect. On first glance at our data, it seems that both situations are particularly true. Fig. 1 shows trends, normalized by province, for Canadian provincial, federal and mean neighboring taxes on cigarettes, expressed in 1989 US\$. The three variables are well correlated for every province and trend up to 1993. From 91 to 93 there was a strong federal no-smoking policy and federal taxes increased, followed by provincial taxes as well. In 1994, federal tax was drastically cut to counteract smuggling from the US; almost all provinces adopted the cut. We conclude that the federal tax effect cannot be estimated by omitting year effects, which also allow for control for the trend effect.<sup>3</sup>

We split the sample into two subsamples. One subsample is relative to the years when the federal tax on cigarettes, expressed in 1989 US\$, is low (this the period 1984–1990 and 1994 when the federal tax was less than 0.462 per pack of 20 cigarettes) and the other subsample relates to the years when the federal tax on cigarettes is high (it is the period 1991–1993: the federal tax was larger than 0.894 per pack of 20 cigarettes). To understand whether there are some regularities in the tax-rates relations of the subsamples considered, we regress each province's own tax on the average of the neighboring Canadian taxes and interact this coefficient with a dummy equal to 1 for the high federal tax subsample and control for the time trend. Table 2 shows that the tax competition coefficient is

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<sup>2</sup>We excluded the three territories of Nunavut, Northwest Territories and Yukon because they represent a very small part of Canada in terms of population, income and tax base.

<sup>3</sup>A trend variable is a linear combination of the dummies for year effects.

lower when the federal tax is high (0.3522-0.1431) than when it is low (0.3522): the interaction coefficient is negative (-0.1431).

This preliminary check suggests that the provincial tax reaction to a change in the mean neighboring provincial tax changes according to the federal tax level, supporting the idea that the federal tax matters in provincial tax decisions. If the federal authority intervenes by introducing a central tax, it affects the local welfare and the choice of the provincial tax, and thus the tax-rate response to an increase in tax rate in a neighboring province. The next sections investigate this issue in more detail.

## 2.1 Estimation Strategy

To isolate the independent impact of the neighboring tax rates on Canadian provincial tax, the other variables that might affect the provincial tax rates must be taken into account. Therefore, we control for the US neighboring tax rates. Moreover the provincial tax rate on goods depends on several other types of variables. Provincial taxation may be influenced by the economic and demographic environment. We controlled for this by using socioeconomic variables (see data appendix). For all of these variables we computed the corresponding mean variable for the neighboring Canadian provinces and neighboring US states for each Canadian province. The political party of the provincial government may also affect the tax-rate level: we divided the Canadian party system into three main groups: the conservative-progressive group, which is right wing; the liberal group, which is center; and the left wing group, comprising the Democratic-Progressives, the Quebec party and the Social Credit party. We then build two dummies accounting for the premier of the province being liberal or conservative-progressive. Finally, we have dichotomous variables to control for province and year effects. We check the effect of federal tax on the tax competition coefficient by estimating the following equation on the entire data set:

$$t_{st} = \alpha_s + \beta_t + \gamma_1 h_{st} + \gamma_2 v_t h_{st} + \gamma_3 m_{st} + \theta x_{st} + \epsilon_{st} \quad (1)$$

where:  $t_{st}$  is the tax rate for province  $s$  and year  $t$ ;  $\alpha_s$  is the province fixed effect;  $h_{st}$  is the tax-rate average for the provinces neighboring province  $s$  in year  $t$ ;  $v_t$  is the federal tax rate in year  $t$ ;  $m_{st}$  is the tax-rate average of the US states neighboring province  $s$  in year  $t$ ;  $x_{st}$  is a vector of the province-specific time-varying variables  $POP_{st}$ ,  $CHILD_{st}$ ,  $AGED_{st}$ ,  $GRANT_{st}$ ,  $UNEMP_{st}$ ,  $INC$ ,  $INC^2$ ; the corresponding Canadian and US neighboring variables for  $INC_{st}$  and  $INC_{st}^2$  computed respectively as  $h_{st}$  and  $m_{st}$ ; the dummies for the premier of the province being liberal or conservative-progressive and  $\epsilon_{st}$  is the error term.

Note that  $\gamma_1 + \gamma_2 \bar{v}_t$  is the slope of the tax-rate reaction function for a given mean of the federal tax. After the results of the preliminary check reported in the previous section, we may want to test  $\gamma_2 < 0$ : an increase in the federal tax rate decreases the coefficient of the tax-rate reaction function.

### 2.1.1 Instrumentation

The mean Canadian neighboring tax rate and its interactions are endogenous, because they can also be influenced by the Canadian provinces. The mean neighboring US tax rate,  $m_{st}$  may clearly be endogenous: the US rate mean may also be influenced by the Canadian provinces.

If this is a structural model, a simple OLS estimate of (1) would suffer from endogeneity bias: the error term  $\epsilon_{st}$  would be correlated with the error terms of the other simultaneous equations of the system. The endogeneity bias arises from the fact that we are dealing with simultaneous equations. We use the two-stage least squares method: first we estimate the reduced forms of the endogenous variables and then substitute their fitted values into (1). The residuals of this last equation are corrected using the actual values of the endogenous variables.<sup>4</sup>

We instrumented the mean Canadian neighboring tax rate  $h_{st}$  with the neighboring Canadian variables for  $AGED_{st}$ ,  $v_t h_{st}$  firstly with  $AGED_{st}$  and  $UNEMP_{st}$ , interacted with  $v_t$  and secondly with  $AGED_{st}$  and  $UNEMP_{st}$ , interacted with  $FED UNEMP_t$ .<sup>5</sup> Finally, we instrumented the mean US neighboring tax rate with the US neighboring variables for  $POP_{st}$

In a reduced-form equation, the tax rate on cigarettes is reasonably linked to the size of the population: this variable influences the available tax base and the cost of public goods. Moreover, the age structure influences taxation according to the relative preference for social policies. It is reasonable to think that these neighboring variables do not affect the provincial tax rate on cigarettes. The economic cycle is also important in determining the tax rate level, and this is captured by  $UNEMP_{st}$ .

We finally have 4 instruments, and therefore Eq. (1), which has three endogenous variables, is identified.

Moreover, in the second-stage equation we also control for demographic variables  $POP_{st}$ ,  $CHILD_{st}$ ,  $AGED_{st}$  and variables controlling for the economic cycle like  $GRANT_{st}$ ,  $UNEMP_{st}$ ,  $INC_{st}$  and  $INC_{st}^2$ .

Spatial error dependence may arise when the error includes some omitted variables not captured in the covariates, which are themselves spatially dependent. If the spatial dependence is ignored the estimation may be biased (Brueckner, 2001; Brueckner and Saavedra, 2001). We deal with this problem by controlling

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<sup>4</sup>The two-stage least squares strategy would deliver residuals using the fitted values of the endogenous variables. Since we are estimating a structural model, we are interested in the residuals using the actual values of the endogenous variables.

We execute the procedure using the *ivreg2* command of STATA, which already gives the corrected residuals with the actual values of the endogenous variables.

<sup>5</sup>In the first case we estimate a Stackelberg model where the federal government moves first and the provinces follow, which implies an exogenous federal tax; in the second case the federal government moves simultaneously with the provincial governments and therefore the federal tax is endogenous. Keen and Kotsogiannis (2002) explore differences in statics-comparative results between the two models.

for a variable proxying the neighboring economic environment: the neighboring Canadian variables for  $INC_{st}$  and its square, and symmetric variables for the neighboring US states. If those variables are omitted, they may generate a spurious correlation between a province's own tax and the neighboring tax or other exogenous covariates.

After performing the two-stage least squares regressions, we test the validity of the instruments using the Hansen  $J$ -test,<sup>6</sup> the minimized value of the GMM criterion function. The joint null hypothesis is that the excluded instruments are valid instruments, i.e., uncorrelated with the error term, and that they are correctly excluded from the estimated equation. Under the null, the test statistic is distributed as  $\chi^2$  in the number of overidentifying restrictions.

## 2.2 Results

Table 3 first reports a simple OLS regression (column 1) that tests for vertical and horizontal externalities: the coefficients are both positive and significant at the 1% level. In this regression we control for province effects and take account of trends or macroeconomic shocks using federal GDP and deficit. When we instrument the Canadian and US average neighboring taxes (column 2), the federal tax is not significant and the overidentification test is not satisfactory ( $P = 0.42$ ). Column 3 shows a specification whereby the federal tax is instrumented with the federal unemployment. The federal tax coefficient increases, becoming significant at the 10% level and the overidentification test is worse ( $P = 0.22$ ). This means that the instruments are not good, or that the specification is not correct because some variable correlated with the instruments is missing. We opt for the second argument and estimate a model with year effects, dropping the federal tax coefficient. We adopt a specification whereby the federal tax is interacted with the mean of the neighboring taxes. Specifically (Table 4) we estimate the horizontal tax-competition coefficient:  $\gamma_1 + \gamma_2 \bar{v}_t$ . This is the slope of the tax-rate reaction function, and the interesting coefficient is  $\gamma_2$ .

In Table 4  $\gamma_2 = -3.51$  is negative and significant at the 1% level, meaning that an increase in federal tax decreases the tax reaction to an increase in the mean of the neighboring taxes. Finally, the overidentification test greatly improves ( $P = 0.76$ ), supporting the idea that the interaction term and the year effects were really missing variables. We also checked a model assuming the federal

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<sup>6</sup>The Hansen-Sargan test is a test of overidentifying restrictions. For the efficient GMM estimator, the test statistic is Hansen's  $J$ -statistic, the minimized value of the GMM criterion function. For the 2SLS estimator, the test statistic is Sargan's statistic, typically calculated as  $N \times R^2$  from a regression of the IV residuals on the full set of instruments. The  $J$ -statistic is consistent in the presence of heteroskedasticity; Sargan's statistic is not. Since we use the command "robust" and therefore assume the presence of heteroskedasticity, which is quite common in a panel for a federal nation such as Canada, we use, as STATA does, Hansen's  $J$ -statistic, which allows observations to be correlated within groups.

tax as endogenous, instrumenting the federal tax interaction with the federal unemployment, and the result did not change (column 2 of table 4)

### 3 Making sense of the results

Consider a federation with two provinces and a federal government maximizing their welfare functions. One mobile good is produced using one input with a constant return to scale technology. The good is taxed according to the destination principle. Using the same technology a good not mobile is also produced. This good is not taxed. The production cost of the two goods is normalized to 1. When the destination principle (people pay tax where they consume the good) holds, cross-border shopping for the taxed good may occur.

We model the interaction between the federal government and the province as a Stackelberg game (Boadway et al., 1998; Keen and Kotsogiannis, 2002). Let  $i = 1, 2$  index the two provinces. In the first stage, the central government chooses the federal tax  $T$  by maximizing its welfare, and in the second stage each province chooses its tax rate  $t_i$ , by maximizing its own welfare, given the federal tax choice. Each citizen in province  $i$  has  $m_i + 1$  units of endowments; she uses one unit to pay the net of tax price of the taxed good, with inelastic demand equal to 1. With the remaining units she pays taxes on the mobile good and consumes the other good. Each citizen can move to buy the mobile good in the province where it is cheaper, bearing a transport cost  $\delta$  per unit of distance  $d$ . We solve the model by backward induction.

#### 3.1 The consumer decision

Let  $t_i$  be the specific unit tax on the mobile good, levied by province  $i$ . Assume that  $t_1 > t_2$ . The consumer in province 1 decides where to buy the good according to her net surplus. If the customer buys in province 1, she pays  $t_1$  plus the production cost. If the customer crosses the border and buys in province 2, she pays  $d + t_2$  plus the production cost. Therefore consumer in province 1 will shop from province 2 until:

$$d_1\delta + t_2 = t_1,$$

then:

$$d_1 = \frac{t_1 - t_2}{\delta}, \tag{2}$$

where  $d_1$  is the distance from the border of the consumer in province 1, who is indifferent between shopping in province 1 or cross the border and shopping in province 2. Moreover, since consumers in 1 are uniformly distributed on  $[0, 1]$ ,  $k$



is also the number of residents in province 1, buying goods from province 2, for a given  $t_1 - t_2$ .

If  $t_1 \leq t_2$ , analogously we obtain:

$$d_2 = \frac{t_2 - t_1}{\delta}, \quad (3)$$

where  $d_2$  is the distance from the border of the consumer in province 2, who is indifferent between shopping in province 2 or cross the border and shop in province 1.  $d_2$  is also the number of residents in 2, buying from province 1, for a given  $t_2 - t_1$ .

Finally, if  $t_1 > t_2$ :

$$B_1 = 1 - d_1, \quad (4)$$

and if  $t_1 \leq t_2$ :

$$B_1 = 1 + d_2, \quad (5)$$

where  $B_1$  is the tax base faced by province 1, whose population is normalized to 1. We can simplify the notation by defining:

$$n(t_1, t_2) = \begin{cases} -d_1 & \text{if } t_1 > t_2 \\ d_2 & \text{if } t_1 \leq t_2. \end{cases} \quad (6)$$

It follows that:

$$B_1 = 1 + n(t_1, t_2), \quad (7)$$

and:

$$B_2 = 1 - n(t_1, t_2), \quad (8)$$

where  $n$  is the incoming or outgoing mobile tax-base quota depending on which tax regime we are dealing with.

### 3.2 The province problem

At the second stage province  $i$  maximizes the following function:

$$W_i = \ln \left( 1 - \frac{t_i - t_j}{\delta} \right) t_i + \ln (m_i - T - t_i) + \gamma(1) \ln u, \quad (9)$$

with  $i \neq j$ . The first term is the utility from revenue collected by the province taxing the good; the second term is the utility for the representative citizen, from consumption of the good not taxed, after paying federal and provincial tax and buying the taxed good in her province; the third term is the utility from consumption of the taxed good,  $x$  with  $\gamma(x) = 1$  if  $x \geq 1$  and  $\gamma(x) = 0$  if  $x < 1$  and finally  $u > 1$ .<sup>7</sup> These assumptions imply that the demand for the good  $x$  is inelastic and equal to one. (See appendix only for the referee)

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<sup>7</sup>For a general theory on utility with models of discrete choice see Peitz (1995).

Provincial taxation of the mobile good is distorted by the *mobility incentive* and the presence of a *higher layer of government*. In particular, if the province tax rate on the good  $x$  is equal to  $t_i$ , tax revenue for province  $i$  is equal to  $t_i \left(1 - \frac{t_i - t_j}{\delta}\right)$ , but the burden for taxpayers (in terms of forgone consumption of the other good) is equal to  $(m_i - T - t_i)$ , because taxpayers bear also the federal tax  $T$ . Note that (9) implies that the province cares about revenue and the indirect utility of a representative citizen buying the taxed good in her province. In particular the second term of (9) implies that the larger  $t_i$  and/or  $T$ , the smaller the utility from the endowment quota available to buy the other good.

At the first stage the federal government solves the following problem:

$$\text{Max}_T \ln 2T + \sum_{i=1}^2 \ln \left(1 - \frac{t_i^* - t_j^*}{\delta}\right) t_i^* + \sum_{i=1}^2 \ln (m_i - T - t_i^*)$$

Where  $t_i^*$  and  $t_j^*$  are second stage tax rates equilibrium. Notice that a subgame perfect equilibrium must necessarily deliver:

$$\frac{t_i - t_j}{\delta} < 1 \quad (10)$$

and

$$m_i - T - t_i > 0. \quad (11)$$

### 3.3 The reaction function

Let us explore the second stage first order conditions. Province  $i$  chooses  $t_i$ , which maximizes (9), obtaining the following first order condition:

$$\frac{dW_i}{dt_i} = \frac{\delta - 2t_i + t_j}{\delta t_i - t_i^2 + t_i t_j} - \frac{1}{m_i - T - t_i} = 0, \quad (12)$$

it follows:

$$(\delta - 2t_i + t_j)(m_i - T - t_i) - (\delta - t_i + t_j)t_i = 0, \quad (13)$$

Implicitly differentiating (13) with respect to  $t_i$  and  $t_j$  and defining  $A = T + 2t_i - m_i$ :

$$\frac{dt_i}{dt_j} = \frac{A}{2(A + t_i - t_j - \delta)} > 0. \quad (14)$$

*Proof:* (10) and (11) imply that if (13) holds then:

$$\delta - 2t_i + t_j > 0 \quad (15)$$

Moreover, since  $\delta - 2t_i + t_j < \delta - t_i + t_j$ , then, when (13) holds  $m_i - T - t_i > t_i$ , which is:

$$A = 2t_i + T - m_i < 0. \quad (16)$$

Finally using (15) and (11):

$$A + t_i - t_j - \delta = 2t_i - t_j - \delta - (m_i - T - t_i) < 0. \quad (17)$$

Use of (16) and (17) implies the sign of (14).

Implicit differentiation with respect to  $t_i$  and  $T$  of (13) gives:

$$\frac{dt_i}{dT} = -\frac{\delta - 2t_i + t_j}{2(A + t_i - t_j - \delta)}. \quad (18)$$

Since we know from above that  $A + t_i - t_j - \delta < 0$ , and from (15) we know that the numerator of (18) is positive, then  $\frac{dt_i}{dT} > 0$ .

How does the existence of a federal tax on the same tax base affect the reaction function of one province with respect to the other province tax rate? To answer this question we must compute the following derivative of (14) with respect to  $T$ , at the second stage tax-rates equilibrium:

$$\frac{dt_i}{dt_j dT} = \frac{(t_i - t_j - \delta) \left(1 + 2\frac{dt_i}{dT}\right) - A \left(\frac{dt_i}{dT} - \frac{dt_j}{dT}\right)}{2(A + t_i - t_j - \delta)^2} < 0.$$

This holds in the symmetric case ( $m_1 = m_2$ ) and also in the asymmetric case ( $m_1 \neq m_2$ ) if the distance between  $m_1$  and  $m_2$  is not too big.

## 4 Conclusions

We have tested the impact of an increase in federal tax on tax competition, providing evidence that an increase in federal tax affects tax competition, since provinces behave differently after an increase in federal tax. Federal tax matters, because it affects the welfare of the province: that is, it decreases the sensitivity of the province tax to a change in tax of the neighboring provinces.

The novelty of this approach is that one can indirectly test the effect of an increase in federal tax on the provincial tax by controlling for yearly macroeconomic shocks, which are not used in the standard empirical literature because they would be perfectly collinear with the federal tax. We accordingly test the coefficient of the variable for the interaction between federal tax and the mean of the neighboring taxes. The paper developed a test using a data set for Canada and US running from 1984 to 1994 for specific cigarette taxes.

Several extensions of this work are possible. On the empirical side, it would be useful to collect data on border densities and border lengths. It is likely that

each state fixes its tax rate, being aware of the neighboring rates, where population density near the border and the length of the border are greater. From a theoretical point of view, it would be interesting to explore the political economy reasons that could determine the ambiguous sign of the vertical externality reported previously in the literature: friendly provinces could decide to sustain the federal authority's decision to increase the federal tax by decreasing their own, while other, non-friendly provinces could do the opposite.

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## 5 Data Appendix

$t_{st}$  Canadian cigarette tax rate, for province  $s$  in year  $t$ , divided by the Canadian CPI and the Canada-US PPP index; these rates are provided by the Finance departments of the ten considered provinces and are expressed in Canadian dollars per pack of 20 cigarettes.

### 5.1 Endogenous variables

$v_t$  is the federal Canadian cigarette tax rate. This is from the National Clearinghouse on Tobacco and Health for Canada.

$h_{st}$  is the mean of the tax rates in year  $t$  of the Canadian provinces bordering on province  $s$ , divided by the Canadian CPI and the Canada-US PPP index.

$m_{st}$  mean of the tax rates of the US states bordering on province  $s$  in year  $t$ , divided by the US CPI. The tax rates on cigarettes for the United States are taken from <http://www.library.unt.edu/gpo/acir/acir.html>: cigarette tax rates are expressed in US dollars per pack of 20 cigarettes.

## 5.2 Demographic and economic variables

$POP_{st}$  is the number of persons in province  $s$  in year  $t$ . It is taken from [www.statcan.ca](http://www.statcan.ca) for Canada and [www.census.gov](http://www.census.gov) for the US.

$CHILD$  is the ratio of individuals aged 5–17 years to the total population of province  $s$  in year  $t$ , taken from [www.statcan.ca](http://www.statcan.ca) for Canada.

$AGED_{st}$  is the ratio of individuals of over 65 years of age to the total population of province  $s$  in year  $t$ , taken from [www.statcan.ca](http://www.statcan.ca) for Canada and [www.census.gov](http://www.census.gov) for the US.

$UNEMP_{st}$  is the unemployment rate for province  $s$  in year  $t$ , taken from [www.statcan.ca](http://www.statcan.ca) for Canada and from [www.stats.bls.gov](http://www.stats.bls.gov) for the US.

$INC_{st}$  is the per-capita income for province  $s$  in year  $t$  divided by the CPI and PPP index. Income data were taken from [www.statcan.ca](http://www.statcan.ca).

$GRANT_{st}$  is the federal grant-in-aid over GDP for province  $s$  in year  $t$ . Federal grant-in-aid data for Canada were taken from [www.statcan.ca](http://www.statcan.ca).

$PROG - CONS_{st}$  is dummy=1 if the premier of the province is Progressive Conservatives, taken from <http://www.swishweb.com/Politics/Canada>.

$LIBERAL_{st}$  dummy=1 if the premier of the province of Liberal Party, taken from <http://www.swishweb.com/Politics/Canada>.

$FED GDP$  is the federal GDP for year  $t$  divided by the CPI and PPP index, taken from [www.statcan.ca](http://www.statcan.ca).

$FED UNEMP$  is the federal unemployment for year  $t$ , taken from [www.statcan.ca](http://www.statcan.ca).

$FED DEFICIT$  is the federal deficit for year  $t$ , taken from [www.statcan.ca](http://www.statcan.ca).

The PPP (Parity Purchasing Power) index for Canada-US was downloaded from the OECD web site.

The US CPI was taken from the Statistical Abstracts of the United States (2000).

The Canadian CPI was taken from <http://www.statcan.ca>.

## 5.3 The neighboring variables

A neighboring Canadian variable for province  $s$  in year  $t$  is computed as the mean of the variable in all the Canadian provinces neighboring province  $s$  in year  $t$ . The neighboring Canadian  $x$  variable is defined as:  $C NEIGH x$ .

A neighboring United States variable for province  $s$  in year  $t$  is computed as the mean of the variable in all the US states neighboring province  $s$  in year  $t$ . The neighboring United States  $x$  variable is defined as:  $US NEIGH x$ .

An example: suppose there are four neighboring provinces (defined as  $n = 2, 3, 4, 5$ ), then the neighboring Canadian  $x_{st}$  variable for province 1 in year  $t$  would be:

$$C NEIGH x_{1t} = \frac{\sum_{s \in n} x_{st}}{4}.$$

## 6 Appendix only for the attention of the referee

The citizen buying the taxed good in her province solves the following problem:

$$\begin{aligned} \max_{x,y} u(x, y) &= \ln y + \gamma(x) \ln u \\ \text{s.t. : } m_i + 1 &= (1 + t_i + T)x + y \end{aligned} \quad (19)$$

Notice that by assumption if  $x \geq 1$  then  $\gamma(x) = 1$ , implying that the solution of the optimization problem is  $x = 1$ ; substituting the budget constraint with  $x = 1$  in the utility function:

$$v(1, m_i - t_i - T) = \ln(m_i - t_i - T) + \ln u. \quad (20)$$

By assumption if  $x < 1$  then  $\gamma(x) = 0$ , implying that the solution of the optimization problem is  $x = 0$ ; substituting the budget constraint with  $x = 0$  in the utility function:

$$v(0, m_i + 1) = \ln(m_i + 1). \quad (21)$$

The last step to solve (19) is comparing (20) with (21):

$$v(1, m_i - t_i - T) > v(0, m_i + 1) \text{ if and only if } 1 + t_i + T < \frac{(u - 1)(m_i + 1)}{u}. \quad (22)$$

Condition (22) must be satisfied if a subgame perfect equilibrium,  $T, t_1, t_2$ , with positive revenues holds. Hence the citizen buying the good in her province chooses:

$$y = m_i - t_i - T$$

and

$$x = 1.$$

**Table 1: Summary Statistics**

Variable	Observations	Mean	Std. Dev.	Min	Max
TAX (province unit cigarette tax, 1989 US\$)	110	0.8057	0.2962	0.2121	1.5347
C NEIGH TAX (neighboring Canadian province average unit cigarette tax, 1989 US\$)	110	0.7778	0.2417	0.2121	1.3254
FED TAX (Federal unit cigarette tax, 1989 US\$)	110	0.5505	0.2297	0.2277	0.9236
US NEIGH TAX (neighboring US state unit cigarette tax, 1989 US\$)	110	0.2075	0.1174	0	0.3947
POP *10 <sup>-7</sup> (province population)	110	0.2718	0.3110	0.0127	1.0828
UNEMP (unemployment rate)	110	11.4873	3.7242	5	21
AGED (proportion of population over 65)	110	0.1147	0.0163	0.0751	0.1443
CHILD (proportion of population between 5-17)	110	0.1920	0.0171	0.1693	0.2533
INC*10 <sup>-3</sup> (province income per capita in 1989 US\$)	110	13.2187	1.9920	9.4915	17.0063
GRANT (federal grants divided by provincial population)	110	0.0011	0.0005	0.0004	0.0020
C NEIGH UNEMP (neighboring Canadian province average unemployment rate)	110	10.9308	2.4546	6.25	15.50
US NEIGH UNEMP (neighboring US state average unemployment rate)	110	4.8178	2.6718	0	8.64
C NEIGH POP (neighboring Canadian province average population)	110	3060374	1942044	423817	7207302
US NEIGH POP (neighboring US state average population)	110	2474501	3165001	0	11100000
C NEIGH AGED (neighboring Canadian province average proportion of population over 65)	110	0.1133	0.0131	0.0751	0.1351
US NEIGH AGED (neighboring US state average proportion of population over 65)	110	0.1034	0.0522	0	0.1396
C NEIGH INC *10 <sup>-3</sup> (neighboring Canadian province average income per capita)	110	13.4088	1.3908	10.0837	15.8977
US NEIGH INC *10 <sup>-3</sup> (neighboring US state average income per capita)	110	12.7175	6.5527	0	19.2380
FED GDP (Federal GDP in 1989 million US \$)	110	476244	30031	423106	535407
FED UNEMP (Federal unemployment rate)	110	9.7273	1.3761	8	11
FED DEFICIT (federal deficit in 1989 million US \$)	110	-23471	3535	-29763	-17926
PROG-CONS dummy =1 if the Premier of the province is Progressive Conservative	110	0.4182	0.4955	0	1
LIBERAL dummy =1 if the Premier of the province is of the Liberal Party	110	0.3445	0.4777	0	1

**Notes:** Figures are means, standard deviations, minimum and maximum, based on annual data for the years 1984-1994, inclusive, for the following ten Canadian provinces: Alberta, Ontario, British Columbia Saskatchewan, Newfoundland, Prince Edward Island, Nova Scotia, New Brunswick, Quebec, Manitoba (110 observations).



**Table 2: Federal tax and horizontal tax competition in Canada.**  
**Dependent variable: *province cigarette tax (specific unit tax), 1984-1994.***

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C NEIGH TAX	.3522 ( 3.00)***
C NEIGH TAX* dummy HIGH FED TAX	-.1431 (2.25)**
year	.0356 (3.90)***
constant	-70.1863 (3.88)***
Observations	110
Prob>F	0.0000
Adj R-squared	0.4538
R-squared	0.4689

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\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%

**Notes:** We splitted the sample into two subsamples, according to the federal tax. A dummy for the high federal tax years (91-92-93) is interacted with the tax-competition coefficient. Numbers in parenthesis are t-statistics (with robust standard errors). Variables are defined in table 1 and described in detail in the data appendix.

**Table 3: Federal tax (specific unit tax) on cigarettes.**  
**Dependent variable: province cigarette tax (specific unit tax), 1984-1994.**

	(1)	(2)	(3)
FEDERAL TAX	0.4238 (2.77)***	-0.4535 (1.18)	0.5895 (1.88)*
C NEIGH TAX	0.6703 (4.15)***	2.1426 (3.85)***	1.2342 (3.87)***
US NEIGH TAX	-1.0645 (1.47)	-0.2016 (0.13)	-1.4502 (1.32)
GRANT	-3.6760 (1.89)*	-8.6016 (2.09)**	-5.6438 (1.97)**
CHILD	-13.6136 (3.08)***	-22.8735 (2.22)**	-15.2912 (2.19)**
POP*10 <sup>-7</sup>	-3.5072 (2.17)**	-7.5599 (2.42)**	-6.1711 (3.06)***
AGED	-30.9564 (2.65)***	-47.1480 (3.45)***	-60.8151 (4.64)***
UNEMP	0.0897 (4.40)***	0.1226 (3.42)***	0.0848 (3.12)***
INC*10 <sup>-3</sup>	-0.8301 (2.99)***	-0.5658 (1.40)	-0.6562 (2.03)**
INC <sup>2</sup>	3.2214 (2.82)***	1.9725 (1.23)	2.3197 (1.79)*
US NEIGH INC*10 <sup>-3</sup>	0.9915 (2.59)**	-0.4729 (0.63)	0.0093 (0.02)
US NEIGH INC <sup>2</sup>	-2.7648 (2.28)**	1.9245 (0.80)	0.3906 (0.22)
C NEIGH INC*10 <sup>-3</sup>	-1.1967 (3.32)***	-1.4903 (3.07)***	-1.4173 (3.86)***
C NEIGH INC <sup>2</sup>	4.5712 (3.13)***	5.6150 (3.11)***	5.2452 (3.68)***
LIBERAL	-0.0525 (0.79)	-0.1731 (1.40)	-0.1521 (1.99)**
PROG-CONS	0.0162 (0.32)	-0.1083 (1.19)	-0.0754 (1.16)
GDP*10 <sup>-6</sup>	4.91 (3.36)***	4.57 (2.25)**	9.39 (4.21)***
DEFICIT*10 <sup>-6</sup>	15.9 (2.53)**	-0.460 (0.05)	8.63 (1.41)
Constant	7.9213 (2.22)**	23.1268 (2.63)***	17.6042 (3.30)***
Observations	110	110	110
Centered R-squared	0.8121	0.5037	0.7304
Uncentered R-squared		0.9414	0.9682
Hansen J statistic (overid)		0.4244	0.2382

\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%

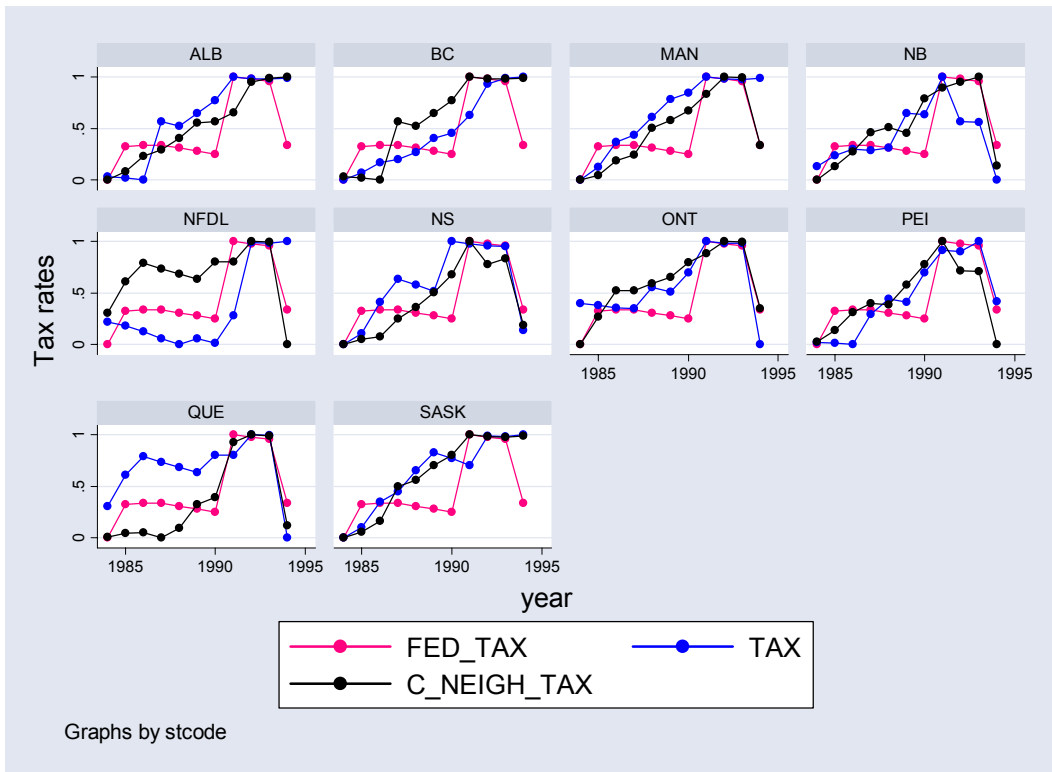
**Notes:** Column (1) presents OLS estimates of the parameters of equation (1), column (2) is a two stage least squares estimate where C NEIGH TAX is instrumented and column (3) presents as well a 2SLS estimate where both C NEIGH TAX and FED TAX are instrumented. Numbers in parenthesis are t-statistics for the column (1) and z-statistics for column (2) and (3), with robust standard errors. Variables are defined in table 1 and described in detail in the data appendix.

**Table 4: The impact of federal tax on horizontal tax competition.****Dependent variable: *province cigarette tax (specific unit tax), 1984-1994.***

	(1)	(2)
C NEIGH TAX	2.5991 (2.72)***	4.0504 (1.94)*
C NEIGH TAX * FED TAX	-3.5144 (2.80)***	-5.8663 (1.97)**
US NEIGH TAX	-1.0637 (0.79)	-3.5116 (1.34)
GRANT	-7.3861 (3.37)***	-6.9936 (2.48)**
CHILD	-9.8944 (1.67)*	-12.3094 (1.20)
POP*10 <sup>-7</sup>	-4.9865 (3.61)***	-4.8764 (2.61)***
AGED	-39.7100 (3.30)***	-37.0020 (2.08)**
UNEMP	0.0872 (3.76)***	0.0994 (2.40)**
INC*10 <sup>-3</sup>	-0.5921 (2.03)**	-0.4365 (1.32)
INC <sup>2</sup>	2.1018 (1.76)*	1.4562 (1.10)
US NEIGH INC*10 <sup>-3</sup>	0.4739 (0.81)	0.1198 (0.17)
US NEIGH INC <sup>2</sup>	-1.0756 (0.56)	0.2519 (0.11)
C NEIGH INC*10 <sup>-3</sup>	-1.1684 (3.48)***	-1.2181 (2.47)**
C NEIGH INC <sup>2</sup>	4.1917 (3.07)***	4.4510 (2.15)**
LIBERAL	-0.0603 (0.99)	-0.0746 (0.79)
PROG-CONS	-0.0002 (0.00)	0.0579 (0.62)
Constant	12.8172 (3.61)***	14.5301 (2.61)***
Observations	110	110
Centered R-squared	0.8057	0.6600
Uncentered R-squared	0.9771	0.9598
Hansen J statistic (overid)	0.7617	0.7179

\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%

**Notes:** Column (1) presents a two stages least squares estimate of the parameters of equation (1) where in the interaction C NEIGH TAX\*FED TAX only C NEIGH TAX is instrumented; in column (2) both C NEIGH TAX and FED TAX are instrumented. Numbers in parenthesis are z-statistics (with robust standard errors). Variables are defined in table 1 and described in detail in the data appendix.



**Fig. 1:** tax-rate trends; tax rates normalized by provinces.