

Demographic Research a free, expedited, online journal of peer-reviewed research and commentary in the population sciences published by the Max Planck Institute for Demographic Research Konrad-Zuse Str. 1, D-18057 Rostock • GERMANY www.demographic-research.org

# VOLUME 17 ARTICLE 11, PAGES 301-338 

PUBLISHED 20 NOVEMBER 2007
http://www.demographic-research.org/Volumes/Vol17/11/
DOI: 10.4054/DemRes.2007.17.11
Research Article

# Stochastic forecast of the population of Poland, 2005-2050 

## Anna Matysiak

Beata Nowok

## © 2007 Matysiak \& Nowok

This open-access work is published under the terms of the Creative Commons Attribution NonCommercial License 2.0 Germany, which permits use, reproduction \& distribution in any medium for non-commercial purposes, provided the original author(s) and source are given credit. See http:// creativecommons.org/licenses/by-nc/2.0/de/

## Table of Contents

Introduction ..... 302
2 Method ..... 303
3 Forecast assumptions ..... 305
3.1 Jump-off population ..... 305
3.2 Fertility ..... 307
3.3 Mortality ..... 311
3.4 Net migration ..... 316
4 Forecast results ..... 322
4.1 Total population ..... 322
4.2 Age structure ..... 324
5 Sensitivity analysis ..... 328
6 Discussion ..... 330
7 Acknowledgements ..... 332
References ..... 333
Annex ..... 336

# Stochastic forecast of the population of Poland, 2005-2050 

Anna Matysiak ${ }^{1,2}$<br>Beata Nowok ${ }^{3}$


#### Abstract

Forecasting the population of Poland is very challenging. Firstly, the country has been undergoing rapid demographic changes. In the 1990s, they were influenced by the political, economic, and social consequences of the collapse of the communist regime. Since 2004 they have been shaped by Poland's entry into the European Union. Secondly, the availability of statistics for Poland on past trends is strongly limited. The resulting high uncertainty of future trends should be dealt with systematically, which is an essential part of the stochastic forecast presented in this paper. The forecast results show that with the probability of $81.8 \%$ the Polish population will decline during the next decades and Poland will face significant ageing as indicated by a rising old-age dependency-ratio. There is a probability of $50 \%$ that in 2050 the population will number between 25.7 and 36.5 million compared to 38.2 in 2004 and that there will be at least 64 persons aged $65+$ per 100 persons aged 19-64.


[^0]
## 1. Introduction

Ever since the beginning of the 1990s, Poland has been experiencing rapid changes in its demographic patterns. In terms of family formation, these are the postponement or even abandonment of marriage and childbearing, the spread of alternative living arrangements and rising numbers of marriages ending in divorce. As a consequence, the Period Total Female First-marriage Rate dropped from 0.90 in 1989 to 0.57 in 2004 and the Period Total Fertility Rate fell from 2.03 to 1.23 . Mortality patterns in Poland have also undergone a significant change. Life expectancy has been rising since 1992 following two decades of very modest improvement and a temporary increase in mortality at the beginning of the 1990s. It increased by 4 years for women and nearly 4.5 years for men over the 1992-2004 period. The major improvement has been observed for infants. In 2004, the infant mortality rate was less than half of that in 1989. As regards international migration, the limited mobility of the past arising from political restrictions has come to an end and today migration from and to Poland is contributing significantly to the volume of international migratory flows.

The process of demographic change in Poland has surely not ended yet. Although demographers have some expectations about the direction of future population developments in this country, a lot still remains uncertain. The uncertainty is growing owing to ongoing economic transformation in Poland, its entry into the EU, and the consequences of opening the national economy to highly competitive global markets. The ageing of Poland's population is an additional challenge. This process has already started and cannot be avoided. The higher percentage of the elderly will result in greater burdens on the working-age population in terms of financial support and care. Consequently, population ageing will affect the state of the country's public finances and its social security system. The direction of future demographic developments in Poland may depend significantly on whether or not the system undergoes the necessary reforms and the extent to which the state adjusts to the ongoing changes. The reforms need to be carefully planned, entailing detailed calculations of their costs and benefits. Qualitative experts' descriptions of the expected future do not suffice. Instead, a reliable population forecast is needed.

Since the beginning of the 1990s, several forecasts of the Polish population have been prepared. The most recent are a forecast of the Central Statistical Office (hereafter referred to as the CSO) for the years 2003-2030 (Bolesławski 2004), of the United Nations for the years 2005-2050 (UN 2004), and of Eurostat for the years 2005-2050 (EUROPOP2004). Each of them has three scenarios, of which one is perceived to be the most likely and the other two to show the magnitude of divergence from the most likely path if some of the fertility, mortality, or international migration parameters are changed. Thus, alternative variants are developed to capture the uncertainty about the
future developments in this country. The problem with this approach, however, is that no probability is attached to the scenarios. Nevertheless, for planning purposes it is crucial to know whether the given projection variant will be reached with a probability of $30 \%, 60 \%$ or $90 \%$ (Keilman and Pham 2004).

We deal with this problem by implementing a stochastic approach. As far as we know, this is the first time that a stochastic forecast for population of Poland is produced. Uncertainty about the future is taken into account by expressing assumptions on fertility, mortality, and migration in terms of their predictive probability distributions. This means that contrary to deterministic forecasts, we attach certain probabilities to certain scenarios. Random values from the assumed distributions for fertility, mortality, and migration are generated to produce a predictive probability distribution of population. The forecast results are presented in the form of median and prediction intervals. The forecast covers the 2005-2050 period.

The paper consists of six sections. After the introduction we provide a brief description of the method. The third section presents the concept of the jump-off population as well as forecast assumptions on fertility, mortality, and migration. Each sub-section begins with a description of the data sources available. The presentation of the forecast assumptions on vital events is accompanied by a description of their past trends and assumptions on uncertainty. Finally, our assumptions are compared to those of the CSO, UN, and Eurostat. The fourth section of the study presents the results of our forecast. Similarly to the assumptions, they are compared with the results obtained in other demographic forecasts for Poland. In the fifth section we show the impact of changes in the uncertainty assumptions on the forecast results. Finally, we summarize the paper and discuss the results referring to the condition of the Polish social security system.

## 2. Method

Similarly to other conventional population forecasts, the probabilistic forecast is based on the cohort-component model. The difference, however, is that instead of formulating alternative low and high scenarios, probabilistic forecasting requires the specification of prediction intervals for future age-specific vital rates and migration flows. The randomly selected rates and flows from these intervals then are used to derive the predictive distribution for the population numbers. Technically, this is achieved by running the cohort-component model several thousand of times.

In the literature, there are three methods of producing the predictive distributions for fertility, mortality, and migration: time-series extrapolation, expert judgement, and an analysis of past forecast errors (Alho and Spencer 2005, pp. 238-256, Keilman,

Pham, and Hetland 2002). In practice, a combination of at least two of these methods is used. The first method is based on statistical models fitted to historical data. However, it tends to give excessively wide predictive distributions due to difficulties in explaining variation in past trends. Therefore, expert judgment is used to correct the resulting prediction intervals. The last method is based on the extrapolation of errors made in past forecasts. Its drawback is that for some countries the forecasts dating far back into the past either are not well documented, not available, or simply non-existent.

In order to produce a stochastic forecast for the population of Poland, we proceed as follows. Based on available data on past trends and on expert judgment we formulate point forecasts for age-specific fertility rates, age-specific mortality rates, and agespecific net migration flows. Unfortunately, an extrapolation of past trends and past forecast errors to produce the prediction intervals for Poland is not possible as long time-series and population forecasts dating far back into the past are not available. Therefore, we use an empirical specification of the error structure estimated by Alho and Spencer (2005) and the experts of the UPE project (European Commission 2005) ${ }^{4}$ for selected European countries and, when necessary, these estimates are further adjusted by expert judgments on the Polish conditions. The so-called scaled model for error (Alho and Spencer 2005) is used to approximate error structures. For each component of demographic change, uncertainty is assumed to increase with the forecast year. The uncertainty of age-specific mortality and fertility rates is treated in relative (logarithmic) terms. The scales of the model for error are constant over time. For fertility, the error increments are assumed to be uncorrelated. Therefore, the model can be interpreted as a random walk. For mortality, the autocorrelation of error increments is 0.05 and the model can be interpreted as a random walk with a random drift. The uncertainty of net migration is represented in absolute terms by using information on gross migration. The constant autocorrelation of error increments is assumed to be 0.3. As regards cross-correlation of errors across age, for fertility and mortality autoregressive ( $\mathrm{AR}(1)$ ) correlation of 0.95 is assumed. For migration dependence on age is deterministic and is given by a fixed distribution over age. Cross-correlation of errors between males and females is expected to be high. A level of 0.85 and 0.90 is applied to errors in mortality and net migration respectively. The variability of fertility, mortality, and migration is treated as independent of each other.

Thus, the future paths of the vital rates and international migration are specified by point forecasts and stochastic error terms. Using a cohort component model, 3000 simulations are run in order to propagate uncertainty from fertility, mortality, and net

[^1]migration to the future population number. For our computations, we use the computer program PEP (Program for Error Propagation) developed by Alho (n.d.) at the University of Joensuu.

## 3. Forecast assumptions

### 3.1 Jump-off population

The jump-off population of the forecast is the Polish population as of 31 December 2004, by sex and single years of age ( $0,1,2, \ldots, 100+$ ). According to the official estimates, based on the results of the last census (20 May 2002) and annual vital and migration registration data, the total population of Poland at that time amounted to 38.174 million.

The official annual population statistics in Poland suffer from serious conceptual drawbacks, however. At the national level, they capture the population permanently resident, i.e. persons registered for permanent stay in Poland. The problem with this is that there is a second type of residence, namely a temporary one. This residence should be recorded in the population register for each stay outside the permanent place of residence (in the country or abroad) exceeding two months. Thus, a person may have a temporary place of residence at the same time as having a permanent place of residence. Besides, there is no upper limit to the former. As a result, a number of people who are temporarily abroad in theory may have been living there already for a few years and they may treat the destination country as their new place of usual residence. These "emigrants" are included in the population of Poland unless they formally give up their permanent place of residence. At the same time, persons with a permanent place of residence abroad who live in Poland just temporarily are not included in the official population statistics. Foreigners who want to settle in Poland are treated as inhabitants of Poland after they have received a permanent residence permit, i.e. after having lived there without interruption for at least three years.

Thus, the concept used in the official statistics does not correspond with the internationally recommended concept of the usually resident population (see United Nations and Eurostat 1998, pp. 11-13). Note that it also differs from the definition of both the de jure and the de facto population ${ }^{5}$. Currently, Poland is an emigration country. Out-migration is usually under-registered, thus the figure for the Polish

[^2]population is larger than it would be according to the two internationally recognised concepts of population mentioned above. Another misleading factor is that the CSO labels differently defined populations with international terminology. The term de jure is applied to the permanently resident population. The term de facto population covers also only permanent residents of Poland, but at the sub-country level, persons with both a permanent and temporary place of residence in the country are counted as de facto residents at their temporary place of residence. Thus, in the terminology used by the CSO, at the country level the de jure and the de facto populations are equal.

The usually resident population was estimated for the first time in the 2002 Census and it has been the only one estimation so far. The usual residents of Poland were distinguished by applying the criterion that the individuals concerned stayed in Poland for at least 12 months. This means that persons who stayed in Poland for at least 12 months were included in the resident population and persons who were staying abroad for at least 12 months were excluded from the resident population. Therefore, the last census results allow for a comparison to be made between the permanent and the usually resident population as of 20 May 2002. The discrepancy between the two population groups is about 610000 persons $(1.6 \%$ of the total permanent population of Poland). There were 22700 persons who lived in Poland on a temporary basis for at least 12 months and 626000 permanent residents of Poland who were absent from the country for at least 12 months. As the information on emigrants can not be collected from the emigrants themselves, the reliability of the latter figure is questionable, e.g., families who left the country are not covered. Besides, the figures for permanent and usual residents include persons who could not have been enumerated by fieldwork for various reasons unfortunately unspecified and the basic information about them was obtained from the population register. The CSO (2003) estimated that about 730000 permanent residents were enumerated that way and the majority of them were also included in the usually resident population. The above comparison leads us to conclude that even if we ignore a possible underestimation of temporary emigration, there still is a difference between the usually and the permanently resident population.

Note that there is a strict connection between the population concept and the reliability of the vital rates, especially fertility rates. An application of the permanent residence concept causes a nominator-denominator bias. Only children born in Poland to mothers who are permanent residents of Poland are included in figures on births. Thus, children born abroad to permanent residents of Poland are not covered, but their mothers are included in the population at risk. Children born to temporary residents of Poland are not counted either.

Although the definition of permanent population has received criticism, we are forced to use data based on this concept. Data availability on the usually resident population is highly limited. The total number of the usually resident population on 20

May 2002 is not disaggregated by age and the appropriate migration data are missing. Additionally, note that the very change of the population concept from permanent, used by the CSO when producing annual population statistics, to usually resident, would not solve the existing data problem. It must be accompanied by a change in people's attitudes towards registration rules; these are usually not adhered to, in particular by people leaving the country.

Unfortunately, even if we use statistics on the permanent population instead of statistics on the usually resident population, uncertainty surrounding the figures still remains. The population number on 31 December 2000 adjusted after the 2002 Census suggests that 390000 permanent residents were not included compared with the data calculated by using the balancing equation of population change. The difference is tied up with undocumented migration. It covers persons who were deregistered from their permanent place of residence, but information about their new place of residence, which may be in the country or abroad, is missing, and who were not present in Poland during census enumeration. This may give raise to doubts on the reliability of the figures of 31 December 2004, although the bias should be lower as relatively short time elapsed since the last census. In addition, since the results of the post-enumeration survey are not easily accessible, we are not able to assess the quality of the census itself. In this situation, the uncertainty of the jump-off population should be taken into account in the forecast. Unfortunately, this can not be done since the current version of PEP does not allow for this source of uncertainty.

### 3.2 Fertility

Fertility assumptions for Poland are based on the observation of past trends in period age-specific fertility rates. Moreover, as Polish couples have been changing their fertility behaviour only since recently (implying high uncertainty as to any likely recuperation effect at older childbearing ages), we also analyse fertility trends in other European countries. We pay special attention to Spain and Italy. Similarly to Poland, the two countries have a strong Catholic tradition, a family orientation that is high, and family and labour market regulations that are considered to create serious constraints to the reconciliation between work and family (e.g. Muszyńska 2005, Kotowska et al. 2005). Fertility has reached lowest low levels in the two Mediterranean countries as well as in Poland (i.e. the Period Total Fertility Rate (hereinafter referred to as TFR) is below 1.35), but the process of decline in the former countries began much earlier than in the latter. Furthermore, in recent years a slight increase in the TFR of the aforementioned Mediterranean countries has been observed, and this observation may be the result of fertility postponement in the past.

In order to formulate fertility assumptions, we collected the time series of period age-specific fertility rates for Poland, Italy, and Spain. We had access to data on the Mediterranean countries by single age, covering the period of 1971-2000 (Spain) and 1950-2000 (Italy). The data stem from the Eurostat online database. Data collection for Poland was more complicated, requiring that we use different data sources and some interpolation procedures. A detailed description of the data sources used is presented in Table 1 in the Annex.

Before the economic transformation, Poland witnessed relatively high fertility by European standards. The TFR declined from 3 children per woman in the 1950s and oscillated around 2.2-2.3 in the 1970s and 1980s. The highest intensity of births was observed in the age group 20-24 and the mean age at childbirth was nearly 26 years at the end of the 1980s. After the fall of the communist regime, Poland experienced a major change in fertility patterns, reflected mainly in a drastic drop in fertility over the first six years of economic transformation and a further decline accompanied by a shift in birth intensities toward higher ages since the mid 1990s. As a result of these changes, the TFR decreased to 1.227 in 2004 (with the lowest value being 1.223 in 2003). In the meantime, the mean age at childbirth rose by nearly two years, to 27.9 . The intensity of fertility decline in urban areas was similar to that in rural areas. Starting from the lower level, the TFR in the former dropped to 1.107 in 2003. Only in 2004 did it increase for the first time since 1989 , to $1.124^{6}$. This may indicate a slight reversal of the negative trend in urban areas (implying a recuperation effect at older ages). Such a phenomenon has not been observed in rural areas so far; here the TFR is still continuously declining (1.421 in 2004).

A similar pattern of fertility decline was observed in the late 1970s and 1980s in Spain and Italy. Here, the TFR dropped from replacement level to around 1.3 within about 10 years. The downward trend continued for the next $8-10$ years, at a lower intensity however, and resulting in a TFR of 1.18 in Italy (1995) and of 1.15 in Spain (1998). Since then, a slightly rising tendency has been observed and in 2004 the countries reached a TFR of 1.33 and 1.32, respectively. This process was continuously accompanied by a shift in birth intensities toward higher ages and may indicate a recuperation effect. Although the process has probably not ended yet, its magnitude seems to be weak.

Based on past trends for Poland, Spain, and Italy, we assume that the negative trend in Poland will slightly reverse. The effect will be slower in the first two years of the forecast when we expect a minor rise in urban fertility but a continuing decline in

[^3]rural fertility. After 2006, the rise in TFR will accelerate as a consequence of childbearing recuperation at older ages. Nevertheless, we do not expect this increase to be strong. In our opinion, fertility will remain low due to serious constraints to the reconciliation between work and family, an existing lack of political will to introduce reforms to family policy and to integrate these reforms with other social and employment policies as well as rising competition in the labour market. Hence, our point forecast for the TFR is 1.35 in 2030 and beyond. This development will be accompanied by a further postponement of births. Therefore, we assume that the age distribution of fertility will resemble that of Spain or Italy today. This implies that the point forecast for the mean age at birth will rise to 30.5 in 2030 and remain constant afterwards. Technically, this is achieved by lowering the fertility rates in ages below 27.9 and raising the rates in ages above 27.9, using an exponential transformation (Alho 1998). The result is presented in Figure 1.

Figure 1: Period age-specific fertility rates, past and forecasted values


The uncertainty of our assumptions on fertility rates is described by a probability distribution around our point forecast. The key issue at this point is the calculation of the standard deviation. We do not have access to long time-series and forecasts dating far back into the past for Poland that would allow for its computation. For this reason, we use the estimates of relative errors in naive fertility forecasts, which assumes that future fertility is equal to the current value, calculated by Alho and Spencer (2005) for six European countries (Denmark, Finland, Iceland, the Netherlands, Norway, and Sweden) over the time span beginning between 1751 and 1900 and ending in 2000. Alho and Spencer (2005) determined that the median of the relative errors closely matches the error of the random walk with volatility of $0.06^{2}$. It might be arguable whether this estimate is appropriate for Poland. There are two reasons for which we claim that it is. First, the estimate by Alho and Spencer (2005) was calculated on a long time-series and not for one, but for a group of countries. Therefore it is even more robust than the one we could compute for Poland. Second, the period studied by the authors was characterized by high volatility in fertility, including both baby busts and booms. Given the long forecast period and the magnitude of change in fertility patterns over the last 15 years we have no grounds to expect that future developments in fertility in Poland will be less variable. Applying the estimates by Alho and Spencer (2005) yields $80 \%$ prediction intervals of [0.99, 1.82] in 2030 and [0.90, 2.01] in 2050. The prediction interval for 2050 is comparable to the corresponding interval of [0.9, 2.2] obtained for both Italy and Spain in the UPE project (European Commission 2005).

A comparison of our point forecast for the TFR with the assumptions of other available forecasts for the Polish population shows that only the CSO assumes the population to display lower fertility levels. The base scenario of the last CSO forecast from 2003 assumes a further decline in the TFR to 1.1 in 2010, followed by a rise to 1.2 in 2020. This is also the level at which the TFR is supposed to remain constant until 2030 according to the CSO. The other two forecasts, one by the UN and the other one by Eurostat, are much more optimistic. Whereas Eurostat claims that there will be a continuous drop in the TFR to 1.18 in the years 2006-2009 followed by a rise to 1.64 in 2034 with no change afterwards, the UN assumes a linear increase to nearly 1.8 in 2050 from the beginning of the forecast period. Nevertheless, although our point forecast differs from those of the CSO, UN, and Eurostat, our $80 \%$ prediction intervals cover the whole range of available forecasts and even allow for the possibility that fertility will fall further (Figure 2). Furthermore, based on our probabilistic model we can compute the probabilities with which the above mentioned forecasts overestimate the future TFR. These probabilities are: $31 \%$ for the CSO forecast in 2030, $71 \%$ for the Eurostat forecast in 2050 and $81 \%$ for the UN forecast in 2050. The probability that the TFR will fall below the value observed in 2004 is $38 \%$.

Figure 2: Period total fertility rate, past and forecasted values


### 3.3 Mortality

Similarly to fertility, mortality assumptions were based mainly on the observation of past trends. Detailed information on data sources and procedures used for calculating the required indicators is provided in Table 2 in the Annex. As a final outcome, we had at our disposal period age-specific mortality rates by sex for the 1950-2004 period. This indicator for ages up to 100, however, was available only for the 1971-2004 period (earlier data covered ages $0-80$ ). Moreover, the data on old-age mortality turned out to be relatively volatile for both women and men, irrespective of the data source used. For this reason, we replaced the old-age mortality rates by a linear extrapolation of the logarithm of mortality rates for ages 30-79. This resulted in mortality rate of 0.411 for women and 0.477 for men at age 100 .

In the post-war period, Poland experienced relatively strong improvement in mortality. Life expectancy at birth in the 1950s rose from 56.1 to 64.9 for men and from
61.7 to 70.6 for women. A rising tendency, although much weaker, was also observed in the 1960s. In the next two decades, the improvement came to a halt. While for women, life expectancy at birth increased by less than 2 years during this period, there was nearly no change for men. What is more, one even observed some temporary ups and downs in male life expectancy. These developments contributed to a further increase in the gender gap in mortality that was already widening in the 1960s (the gap in life expectancy grew from 5.6 years in 1960 to 8.7 in 1989). The fall of state socialism is marked by a sudden rise in mortality for all age groups. This phenomenon was, however, only a temporary one and since 1992 a continuous fall in mortality has been observed. As a result, female life expectancy increased by nearly 4 years (to 79.2 in 2004) and that for men rose by 4.5 years (to 70.7 in 2004) compared to 1991 . The improvement in mortality was strongest for infants. The infant mortality rate in 2004 was less than half of that in 1989.

Given the trends described above, we expect that the improvement in mortality observed since 1992 will continue in the future. With time, however, the rates of decline will weaken, converging to those observed in the most developed countries of Europe. The slowdown in mortality improvement can be explained by the fact that the sudden drop in mortality during the 1992-2004 period was most probably the result of a rapid increase in living standards and the spread of a healthy life style. This trend will continue for some time as Poland's level of economic development will converge to the EU average. In our opinion there is, however, no reason to believe that in the long term life expectancy in Poland will increase faster than it has been observed so far in the most developed countries in Europe.

The initial annual rates of decline in mortality were estimated from the observed mortality rates for single years of age up to 80 for the 1992-2004 period. For ages over 80 the rates of decline were assumed to remain at the level they are in age 80. Due to a high variability across single ages the obtained rates of decline were further smoothed. Next, we assumed that the obtained rates of decline will decrease linearly until 2030 to reach the average rates of decline calculated for Austria, Denmark, Finland, France, Germany, Italy, the Netherlands, Norway, Sweden, Switzerland, and the United Kingdom for the last 30 years (European Commission 2005). The decline rates for ages $60-100$ in both Poland and the most developed European countries were much higher for women than for men. Since the gender gap in mortality in Poland is relatively high if compared to the EU- 15 countries we decided to avoid its further widening. For that reason we lowered the difference in the rates of decline calculated for Poland by increasing the male rates and lowering the female rates by one third of the difference. The resulting mortality rates are presented in Figures 3 and 4.

Figure 3: Mortality rates, past and forecasted values, males


Figure 4: Mortality rates, past and forecasted values, females


Similarly to fertility, our assumptions on mortality are uncertain. On the one hand, it seems quite plausible that the recent improvements in mortality will continue. This should happen as a consequence of technological progress in medicine, further prevention of diseases, and the spread of a healthier lifestyle. This effect should be particularly strong in Poland as it still has a lot to catch up with EU-15. On the other hand, whether mortality declines or not highly depends on the economic development of the country and the state of public health care. The latter currently is and may continue to remain in poor conditions if major reforms are not undertaken. This issue will become more urgent and more difficult to address in view of the ongoing process of population ageing. Moreover, we do not have an answer yet to the question whether or not there are limits to rising life expectancy, an issue that is subject to current debate (see Oeppen and Vaupel 2002, Olshansky, Carnes, and Cassel 1990, Vaupel 2005). This uncertainty is described by prediction intervals around our point forecast. Here too, we do neither have access to long time series nor to a large deal of long-term forecasts that would allow us to calculate the relative forecast errors. Therefore, we took the estimates by Alho and Spencer (2005) as the point of departure. They compared mortality rates in nine European countries (Austria, Denmark, France, Italy, the Netherlands, Norway, Sweden, Switzerland, and the United Kingdom) with a baseline forecast, assuming decline in mortality by the observations made in the past 15 years. Their period of analysis covered a time span ending in 2000 and starting at various dates, with the earliest being 1841 for the UK. They determined that the median of the relative errors closely matches the error of the random walk with a drift. The estimate by Alho and Spencer (2005) seemed plausible for Poland for the reasons given while describing the fertility assumptions. It is calculated on a long time-series, covering the period of a significant change in mortality patterns (including mortality revolution) and for a group of countries. Therefore, it is more robust than the one we could compute on a short time-series for one country only. The resulting $80 \%$ prediction intervals for life expectancy were, however, much narrower than the corrected model-based intervals for the countries in the UPE project (European Commission 2005) and did not even include the base scenarios of future life expectancy development prepared by other institutes. We have no grounds to claim that future developments in mortality in Poland are less uncertain than in other European countries and that some experts are entirely wrong about them. Hence, we adjusted the assumptions on uncertainty in line with the average standard deviation of life expectancy in the lead time in the UPE project (see Table 8 in European Commission 2005).

Figure 5: Life expectancy at birth, past and forecasted values, males


Figure 6: Life expectancy at birth, past and forecasted values, females


The magnitude of uncertainty as to the future mortality patterns is presented in form of $80 \%$ prediction intervals around the point forecast of the life expectancy derived from our assumptions on age-specific mortality rates. For men, this interval will be [73.0, 79.4] in 2030 and [74.8, 84.5] in 2050; for women it will be [81.3, 86.6] and [82.7, 91.0] (see Figures 5 and 6). In terms of the point forecast, this implies a rise in male life expectancy by 5.4 years until 2030 compared to $\mathrm{e}_{0}$ in 2004 and a climb by further 3.5 years until 2050 (which gives $\mathrm{e}_{0}$ of 76.1 in 2030 and 79.6 in 2050). The improvements will be slightly lower for women: the point forecast increases by 4.7 years by 2030 and another 2.8 years by 2050 (i.e. to the level of 83.9 and 86.7 respectively). This will contribute to a slight narrowing in the gender gap in life expectancy by 1.5 years (to 7 years).

A comparison of our assumptions on life expectancy with the assumptions of other available forecasts shows that our prediction intervals for men generally cover the most likely scenarios predicted by the UN and Eurostat, with the latter being closest to our point forecast. According to our probabilistic model, the institutions underestimate the life expectancy for men in 2050 with a probability of $73.6 \%$ and $55.4 \%$ respectively. The CSO predicts a much stronger rise in male life expectancy in the first decade, but thenafter the growth slows down and after 2020 the assumed $e_{0}$ is also covered by our prediction interval. Again, according to our model the male life expectancy in 2030 is underestimated by the CSO with probability of $27.0 \%$.

Contrary to our assumptions on male life expectancy, the assumptions on female life expectancy are more optimistic than those made by the UN and Eurostat. The values predicted by these institutions, particularly the UN, are covered by the lowest parts of our $80 \%$ prediction intervals. The CSO forecast on female life expectancy is closest to our point forecast. According to our stochastic model, the probabilities of underestimating the female life expectancy are: $77.2 \%$ (Eurostat in 2050), $80.7 \%$ (UN in 2050), and 63.6\% (the CSO in 2030).

### 3.4 Net migration

International migration is a component of population change that is the most difficult to forecast in general and in Poland in particular. Firstly, the Polish statistics on international migration flows are of very poor quality (Nowok forthcoming). Secondly, Poland's entry into the EU makes migration strongly dependent on political decisions, such as the timing of lifting restrictions on the free movement of labour for the citizens of the new Member States by the old EU-15, and the future economic development of Poland.

Official Polish statistics on international immigration and emigration flows cover permanent migration only. Permanent is understood literally, i.e. it refers to declared infinite duration of stay (for more details on the applied concept see Nowok forthcoming). The statistics available at the time of preparing the forecast (until reference year 2004) were produced on the basis of registration and deregistration forms that are filled out in the municipality when reporting a change in the place of permanent residence. Usually, however, people do not report their departure abroad. Thus, emigration is not covered in full and this is reflected in the population number obtained from the census count. The underestimation of Polish migration data is also evident when compared to the statistics reported by the EU countries that have a migration exchange with Poland (hereinafter referred to as partner countries) (Kupiszewska and Nowok forthcoming). However, note that these discrepancies largely result from differences in the definition of migration and migrants.

The current study is based on official statistics on net migration (immigration minus emigration). These statistics have been corrected by using a post-census adjustment of the population number and statistics produced by the main EU destination countries. The net migration figures, which are calculated as a difference between immigration and emigration, are equal to the net migration figures obtained as residual values of annual population change and natural increase for all years except 2000. The post-census adjustment was applied to the total population number on 31 December 2000. Provided that the census count and registration figures for births and deaths are accurate, the adjustment difference covers net migration accrued over the whole intercensal period. We therefore distributed it among the years 1989-2000. The distribution was carried out on the basis of the average share of net migration in a given year in a cumulative net migration for the whole period. Net migration was calculated for migration exchange with Germany, the Netherlands, and Sweden, using the statistics reported by these countries. Even if the migration exchange with Germany is much higher than with the Netherlands and Sweden (the other two most important partner countries for which data are available), we did not rely on the German data only, because they cover all stays exceeding one week. This is short a stay to qualify a movement as migration. The distribution reflects the undocumented migration wave that took place during the first years following the transformation of the political system in Poland in 1989. Besides, note that the cumulative official net migration figure for the 1989-2000 period (192000) was less than half of the value of our post-census correction (390000). The average relative increase of net migration due to applied adjustments for the period 1995-2000 was used to correct the values of net migration for 2001-2004, calculated from the Polish official statistics on immigration and emigration. An additional correction was applied to the figure for 2004, the first year of Poland's membership in the EU (since 1 May 2004). According to the European main
partner countries for which data were available (Germany, the Netherlands, Spain, and Sweden), their positive migration balance with Poland on average doubled. Polish data showed an opposite trend, i.e. an increase in net migration compared to the previous year. The adjustment was introduced on the basis of the assumption that the bias of net migration data is connected mainly to the emigration component and thereby to the migration exchange with the destination countries of migrants from Poland.

The age pattern of both immigration and emigration obtained from the Polish statistics (2004, by single age, and 1999-2003 by 5 year age groups, interpolated by the Karup-King method) was unrealistic, and this additionally lowers the quality of the Polish data on international migration flows. Therefore, the initial age pattern of net migration was derived on the basis of data on immigration and emigration by the country of previous and next residence respectively produced by the main partner countries. The average of the age pattern of the migration exchange with the following countries in 2004 was used: Germany, Austria, the Netherlands, Italy, Spain, and Sweden. However, starting from age 80, zero migration was assumed.

The low reliability of the statistics on international migration flows available for Poland hinders an analysis of historical trends. However, some general and characteristic features can be distinguished. During the pre-transition period (19501988), the population movement was constrained by political factors and responded to fluctuating restrictions. Migration reached a significant level only in some exceptional cases and only specific categories of migrants were involved, e.g. ethnic Germans and Polish Jews. The sudden increase in migration outflow took place after the collapse of state socialism in 1989, when people started to move abroad freely. Following a period of high intensity of migratory movements, net migration was rather stable and oscillated between -14000 and $-20000(-28000$ and -46000 after our correction), with the minimum level reached in 2000, most probably connected to the deterioration of the economic situation in Poland.

Owing to Poland's entry into the EU, the future trend of international migration depends largely on the political decisions made by individual EU-15 Member States regarding the free movement of labour. The turning points in that respect are defined by the transitional arrangements set out in the Treaty of Accession of 2003. The transitional period (1 May 2004-30 April 2011) is divided into three distinct phases, according to the " 2 - plus 3 - plus 2 " formula. The first 2-year period ended on 30 April 2006. During this period, the three countries that opened their labour markets, namely Ireland, Sweden, and the United Kingdom, recorded an increase in immigration from the new Member States. On 1 May 2006, four additional countries ended the restrictions: Finland, Greece, Portugal, and Spain. The next verifications of the restrictions will take place in April 2009. All countries are obliged to end all constraints by 2011. The German government has already announced that it wants to prevent the
uncontrolled inflow of cheap labour, in particular from Poland and the Czech Republic, for as long as possible. A similar decision was taken by Austria. For the other countries we have to make arbitrary assumptions on the date of opening their labour markets, based on the prevailing attitudes to foreign labour in these states. Thus, we assume that in 2009 all other countries except France will abandon the transition period. Besides, we assume that the removal of restrictions will result in a temporary increase in outmigration, in particular when Germany, currently the main destination country of Polish emigrants, opens its labour market. In general, we are of the opinion that Poland will follow the footsteps of Portugal and Ireland following their entry into the EU. This analogy is build on the basis of similarities in terms of an economic gap between the new Member State and the "old" EU. Therefore, net migration in Poland will first drop due to the dominating outflow to more affluent countries that have opened their labour markets. A minimum level of -88500 will be reached in 2011 and 2012, i.e. in the years directly following the transition period for the free movement of workers. At the same time, the gradual improvement in the economic situation and the increasing relative attractiveness of Poland will result in an inflow of migrants, especially from the former Soviet Union countries. The immigration flow will then take precedence and in the long run Poland will become an immigration country. We assume that this will happen around 2025. In 2050, a level of 30000 net migrants will be reached.

The assumed convergence of net migration to the EU pattern refers also to the age structure of net migrants. The initial age pattern will change linearly to adjust to the average EU pattern estimated in the UPE project, based on data from Austria, Belgium, Denmark, Iceland, Netherlands, Norway, Sweden, and Switzerland (European Commission 2005). This age pattern, reached in 2030, will remain constant for the rest of the forecast period. The number of net migrants by age is presented in Figure 7 for males and in Figure 8 for females. The sex structure is kept constant over the whole forecast period at the average level of the years 2000-2004 (the calculations are based on the Polish registration statistics). The share of males and females are $51 \%$ and $49 \%$ respectively.

Figure 7: Net migrants by age, males


Figure 8: Net migrants by age, females


All of our assumptions are based on a judgmental view. Therefore, the uncertainty surrounding future net migration in Poland is of great importance. The unpredictable pace of future economic development in Poland, dependency on the EU-15 countries' decisions on access to their labour markets and the poor quality of Polish statistics on international migration suggest that the uncertainty is higher than in the most of the countries studied in the UPE project (see Table 10 in European Commission 2005). We assume that in terms of uncertainty of net migration Poland is comparable to Greece and Portugal, for which the highest standard deviation per thousand of the jump-off population was set ( $6 \%$ at the end of the forecast period). For the latter two states, as for Poland, the data situation is known to be very problematic (Breem and Thierry 2006, Cantisani and Greco 2006). In addition, in both Greece and Portugal past development of net migration was relatively volatile. Thus, we have no grounds to claim than the future net migration in Poland will be less or more uncertain. Therefore we assume the standard deviation of net migration at the end of the forecast period to be $6 \%$ of the jump-off population. As a result the $80 \%$ prediction interval in 2050 is [263 530; 323 530]. The interval for all forecast years is presented in Figure 9. The corresponding $80 \%$ prediction interval for the cumulative net migration during the whole forecast period is [-8 $304000 ; 6286000]$. It is symmetric around the median of 1009000 . The probability that the net impact of international migration on population number of Poland until 2050 will be positive is equal to $43 \%$.

The future overall trend of net migration is very similar to that assumed by Eurostat in its projection, but the discrepancies still persist. They refer to the minimum level of net migration reached before the trend changes (-59 000 in the baseline Eurostat scenario compared to our point forecast of -88500 ) and the pace of the increasing trend. The target levels of net migration in 2050 are very close to each other. The differences in the net migration level result to some extent from differences in the figure for the jump-off net migration, since the correction introduced by us is larger than that applied by Eurostat. However, since 2008 the base variant of the Eurostat projection is within the $80 \%$ prediction interval of our forecast.

The UN and CSO consider only one variant of the future non-zero net migration pattern. Their assumptions are not comparable to the other two forecasts. The UN assumes constant net migration at the level of -16 000 and the CSO assumes a decline to -24000 in 2010 and then a gradual increase to -16000 in 2030 (projection lead time). These assumptions are highly questionable. Firstly, they are based on an underestimated registration number of net migrants and secondly, possible changes connected with Poland's entry into the EU are not taken into account.

Figure 9: $\quad$ Net migration, past and forecasted values


## 4. Forecast results

### 4.1 Total population

Figure 10 contains the median, first and third quartiles, and first and ninth deciles of the predictive distribution of the population of Poland until 2050. It is clear that the Polish population is most likely to decline from the current 38.2 million to 35.2 million in 2030 and to 31.2 million in 2050, as indicated by the median. This downward trend will be observed from the beginning of the forecast period. The $50 \%$ prediction interval places the Polish population between [32.3, 37.8] million in 2030 and [25.7, 36.5] million in 2050. The $80 \%$ prediction interval is much wider, it ranges from the very low values of 29.8 to 40.4 in 2030 and from 21.0 million to 41.6 million in 2050. Hence, with a probability of $18.2 \%$ the Polish population in 2050 will be higher than in 2004.

The medium forecasts of the total population by the CSO, UN, and Eurostat are nearly fully covered by the $50 \%$ prediction intervals obtained by us. However, they all give higher population numbers than our point forecast.

The CSO predicts the total Polish population to be 35.9 million in 2030, which is about 0.7 million higher than the median in our forecast. Since our point forecast on fertility places the TFR at a higher level than in the forecast by the CSO and since the assumptions on mortality for 2030 are quite similar, this difference results from different assumptions on migration. Indeed, in our point forecasts we definitely expect a much higher out-migration than the CSO does. The probability, calculated based on our stochastic model, that the CSO overestimates the population number in 2030 is $57.2 \%$.

Figure 10: Total population, past and forecasted values


Note: The total population forecasted by the UN is predicted on 1 July each year

The base variant by Eurostat places the total population on a level similar to our point forecast in the first forecast years, until around 2017. Thenafter, it begins to predict higher values and in 2050 it yields 33.5 million of inhabitants, i.e. 2.3 million more than our point forecast. This difference is probably mainly a consequence of the fact that Eurostat's assumptions on fertility are much more optimistic than ours. The probability that Eurostat overpredicts the total population in 2050 is $61.0 \%$.

The UN medium scenario yields the highest differences in comparison to our point forecast in the first forecast years, until around 2030. This gap results probably from higher assumptions on fertility and lower out-migration. Thenafter the difference decreases but still the population is predicted to be 31.9 million in 2050 , that is by 0.7 million higher than in our point forecast. According to our probabilistic model the population in 2050 is overestimated with a probability of $53.1 \%$.

### 4.2 Age structure

Along with the decline in its total population, Poland will face rapid population ageing. This process will not only be the result of low fertility and rising life expectancy but also of rolling demographic booms and busts. As a consequence, the median age of the population will rise from 35.7 in 2004 to 47.5 in 2030 and 52.9 in 2050 (according to our point forecast).

Table 1: Median age of the $1^{\text {st }}, 5^{\text {th }}$ and $9^{\text {th }}$ decile of the forecasted population

|  | $1^{\text {st }}$ decile | $5^{\text {th }}$ decile | $9^{\text {th }}$ decile |
| :--- | :---: | :---: | :---: |
| 2004 | - | 35.7 | - |
| 2030 | 49.8 | 47.5 | 45.5 |
| 2050 | 59.7 | 52.9 | 48.0 |

The change in the age structure of the population will be reflected in a gradual decline in the number of children aged 0-6 and at school age (aged 7-18) over the whole forecast period (with the exception of the years 2008-2011 in the case of the younger group). The working-age population (aged 19-64) will continuously decrease from 2011 onwards. Only in the case of the elderly (65+) will we observe a constant increase. A remarkable feature of these changes will be a significant rise in the number of oldestold $(80+)$ until the end of 2043. This has already been observed in EU-15 on a large scale during the last decades, but has not yet taken place to such an extent in the new member states. The general overview of these changes is graphed in the age pyramids (see Figure 11). The border of the dark grey area stands for the lower bound of the $80 \%$ prediction interval, whereas the border of the black area represents the upper bound. The absolute uncertainty, expressed as the width of the prediction interval, is highest in the young ages and around the peak ages of international migration. In a relative sense, i.e. the uncertainty defined by the width of the prediction interval as a ratio of the median, it is greatest in young and very old (95+) ages. Nevertheless, even if the future
age structure of the population is as indicated by the ninth decile of the forecast, the age pyramid will remain of regressive shape.

Figure 11: Future age structure of the population (ages 0-99), median and $\mathbf{8 0}$ \% prediction intervals



lower bound of the $80 \%$ prediction interval
median
upper bound of the $80 \%$ prediction interval

The process of population ageing is reflected also in a detailed analysis of population composition by age (see Figure 12). The main absolute changes in the population share refer to people aged 65-79 and at mobile productive age (19-44). The fraction of the former increases by 11.9 percentage points (from $10.6 \%$ up to $22.5 \%$ ) and that of the latter decreases by $11.4 \%$ percentage points (from $38.4 \%$ down to $27 \%$ ). The most substantial relative change in the share takes place in the oldest-old age group $(80+)$, which grows nearly fourfold. As a result, the fraction of the combined group of the elderly ( $65+$ ) increases from $13.3 \%$ to $33.2 \%$. Due to the assumed eventual rise in fertility rates, the decline in the share of children aged 0-6 is relatively small, lower than that for children at school age (7-18), in both absolute and relative terms.

Figure 12: Age structure of the population


Year

The pressure on the economy of population ageing can be described by the socalled old age dependency ratio (OADR). The OADR analysed in this study is defined as the size of population aged 65 and above, divided by the working age population (19-
64). However, one needs to take into account that this measure does not reflect the exact burden placed by the dependant elderly on the working population due to variations in employment participation and eligibility to social benefits. The dynamics of the OADR presented in Figure 13 (median with an $80 \%$ prediction interval) reflect clearly a dramatic process of population ageing, which is connected with a substantial increase in the financial burden posed on the working age population.

Figure 13: Old-age dependency ratio (OADR), past and forecasted values


Year

Over the forecast period, the OADR more than triples. According to our point forecast, it increases from $21 \%$ in the first years of the forecast to $42 \%$ in 2030 and $64 \%$ in 2050. The probability that the OADR will more than double until 2050 is equal to $97 \%$. As the ninth decile for 2050 indicates, there is a probability of $10 \%$ that the future demographic development will bring us to the level higher than $94 \%$.

## 5. Sensitivity analysis

While formulating the uncertainty assumptions on vital rates and migration flows we used the estimates by Alho and Spencer (2005) and the experts involved in the UPE project (European Commission 2005). If these assumptions are not appropriate for Poland our forecasted population numbers and related probabilities are incorrect. Therefore, in order to assess the possible specification error we conducted a sensitivity analysis. The initial uncertainty parameters were increased and decreased by 10, 20, and $30 \%$ separately for fertility, mortality, and net migration. The resulting total population numbers were compared with total population numbers obtained using the basic parameters.

Figure 14: Total population, various uncertainty of fertility (a), mortality (b), and net migration (c)


Figure 14: (continued) Total population, various uncertainty of fertility (a), mortality (b), and net migration (c)

c)


The sensitivity analysis revealed a negligible impact of changes in relative errors of mortality on forecasted population size (see Figure 14b). In the case of fertility, modification of uncertainty assumptions resulted in a small but visible change in the ninth decile of the predictive distribution of the total population (see Figure 14a). Relative to the results obtained using the basic uncertainty parameters in 2050 its value increased by 1.2 million when the relative error was enlarged by $30 \%$ and decreased by 0.8 million when the relative error was reduced by $30 \%$. The lower $80 \%$ prediction interval of the total population changed negligibly. The change in the upper interval values and no change in the lower interval values is to be explained by a threefold difference in the number of women aged 15-49 between the intervals. Contrary to fertility and mortality the forecast results are quite sensitive to the changes in net migration uncertainty, both at the lower and upper $80 \%$ prediction interval (see Figure 14 c ). After increasing the standard deviation of net migration at the end of the forecast period (per thousand of the jump-off population) by $30 \%$, the $80 \%$ prediction interval for total population in 2050 became by 5.3 million wider than the prediction interval obtained using the basic assumptions on uncertainty. Furthermore, the population size at the ninth decile of this enlarged predictive distribution is almost impossible to be reached under the assumption of low uncertainty of future net migration flows.

Based on the results of the sensitivity analysis we conclude that the results of our forecast are robust as regards the effects of fertility and mortality on total population numbers. This is not as much the case as regards international migration. Taking into account the low quality of the Polish migration data and the high uncertainty on the future migration flows it is, however, hardly possible to produce an adequate migration forecast.

## 6. Discussion

No one can say with certainty what the demographic development in Poland of the future will look like, but compared to other existing forecasts for Poland prepared conventionally, we have quantified the uncertainty we should expect. The analysis of the historical forecast errors for Poland is limited, however, by the lack of long timeseries data. Thus we had to rely on the experience of other countries. We have assumed that future uncertainty is at least as high as it was in the past for other European countries that possess appropriate data. This uncertainty is higher than usually believed by demographic forecasters. Even under these assumptions, it is highly probable that the population of Poland will decline in future and that a further advancement in population ageing is inevitable. This process will have severe implications on the financial conditions of the social security system and the state of public finance. Policy
makers should be aware of it and take appropriate measures. Although Poland has already made a big step forward reforming the non-agricultural old-age pension scheme, there are still some elements of the social security system that require changes.

The reform of the non-agricultural old-age pension system took place in 1999. The previous "pay-as-you-go" system has been gradually replaced by a new one, entirely based on individual retirement accounts. The pension formula in the new system depends on the accumulated capital and life expectancy at the time of retirement. Hence, the system is actuarially neutral (it does not generate debt exceeding that which it can finance without the necessity of raising contributions) and creates incentives to delay withdrawal from the labour market (Góra 2005). Furthermore, in parallel to the introduction of the new system, the law limiting the early retirement privileges was passed. Altogether, the reforms are expected to lower the expenditures on old-age pensions. According to the projections carried out by the Ageing Working Group of the Economic Policy Committee the expenditures on the public and private mandatory oldage and early pensions will fall from the current relatively high level of $10.1 \%$ to $7.9 \%$ of GDP in 2050, which will be one of the lowest levels in EU-25 (Economic Policy Committee and European Commission 2006). Note, however, that recently some amendments to the legislation on non-agricultural old-age pension system have been adopted that indicate a step backwards. They loosen the restrictions on early retirement, delaying the complete revocation of early retirement and granting early retirement privileges to some occupational groups.

Apart from the successful reform of the Polish non-agricultural old-age pension scheme some elements of the social security system still require reforms. These are agricultural pension scheme, the disability, health care, and long-term care. The basic problem with the agricultural pension scheme is that only around $6 \%$ of the expenditures on pensions is covered from the contributions. The rest is financed from the state budget. The reason is the flat contribution rate, fixed at $30 \%$ of the minimum old-age pension for owners of small and low-income as well as large and profitable farms. As regards disability benefits, the percentage of the persons currently entitled to them in Poland is highest among the OECD countries (OECD 2003). Although some measures directed at limiting the entitlements to disability benefits have been already implemented, the system still requires to be adjusted to the reform of the old-age pension system. According to the law passed recently the disability pensioner who reaches the retirement age is automatically entitled to an old-age pension that is at least as high as the previously received disability pension. However, due to the reform of the old-age pension system, the average disability pension will exceed the average old-age pension in the future. This will create incentives to apply for a disability pension before retirement. As regards the health-care and long-term care in Poland, the Ageing Working Group of the Economic Policy Committee projects relatively slight increases
in expenditures, if compared to other EU countries (by 0.9-1.7 for health care and 0-0.2 for long-term care depending on the scenario assumptions) (Economic Policy Committee and European Commission 2006). However, apart from the level of spending, one has to take into account the relation between the demand and supply. Currently, formal care for the elderly is hardly available and care is to a large extent provided by family members, hindering the labour force participation of women (Wóycicka and Rurarz 2007). Taking into account the expected upward trend in the share of the oldest-old, the declining propensity to form multi-person households (Abramowska 2005) and the necessity to increase the currently low female employment, a discussion on the development of long-term care is required.

In sum, a comprehensive redesign of the old-age pension system in Poland was an important step to safeguard the future economic, budgetary, and social consequences of population ageing. The response to the demographic challenge has still, however, to be completed. Considerable improvements need to be made to other parts of the social security system. These include disability, health-care, long-term care, and agricultural pension scheme. Moreover, an additional challenge is posed by the difficult labour market situation. The employment rates are exceptionally low, especially among the young and people at pre-retirement age. As revealed in this study, a further advancement in population ageing is inevitable, thus the government will have to tackle these problems. Furthermore, it will also have to face the problem of availability and quality of demographic statistics in Poland.

## 7. Acknowledgements

The first version of the forecast was prepared during our stay at the Max Planck Institute for Demographic Research as fellows in the European Doctoral School of Demography. The work was continued when Anna Matysiak was participating in the International Max Planck Research School for Demography and later was supported by the Foundation for Polish Science, and Beata Nowok was a PhD candidate based at the Netherlands Interdisciplinary Demographic Institute. We are very grateful to Juha Alho for his valuable teaching within the EDSD course on Modelling, simulation and forecasting. We also appreciate the suggestions made by anonymous reviewers and comments on an earlier version of this paper by Marek Kupiszewski and Heiner Maier. Finally, we would like to thank Susann Backer for language editing.

## References

Abramowska, A. (2005). Projekcja liczby osób starszych wymagających opieki w Polsce. Internal Research Report. Warsaw: Warsaw School of Economics, Institute for Statistics and Demography.

Alho, J. (1998). Stochastic Forecast of the Lithuanian Population 2001-2050. Research Report P98-1023-R. Joensuu: University of Joensuu, Department of Statistics.

Alho, J., and B. Spencer (2005). Statistical Demography and Forecasting. New York: Springer Science + Business Media.

Alho, J. (n.d.) PEP - Program for Error Propagation (tutorial). Retrieved April 4, 2006, from http://joyx.joensuu.fi/~ek/pep/userpep.htm

Bolesławski, L. (2004). Demographic projection of Poland 2003-2030. Warsaw: Central Statistical Office.

Breem, Y. and X. Thierry (2006). Country report: Portugal. In M. Poulain, N. Perrin, and A. Singleton (Eds.), THESIM: Towards Harmonised European Statistics on International Migration (pp. 591-598). Louvain-la-Neuve: Presses universitaires de Louvain.

Cantisani, G. and V. Greco (2006). Country report: Greece. In M. Poulain, N. Perrin, and A. Singleton (Eds.), THESIM: Towards Harmonised European Statistics on International Migration (pp. 437-446). Louvain-la-Neuve: Presses universitaires de Louvain.

Central Statistical Office, Population Indicators Database, http://www.stat.gov.pl/ dane_spol-gosp/ludnosc/index.htm

Central Statistical Office (2003). Migracje zagraniczne ludności 2002. Warsaw: Central Statistical Office.

Council of Europe (2005). Recent demographic developments in Europe 2004. Strasbourg: Council of Europe Publishing.

Economic Policy Committee and European Commission (DG ECFIN) (2006). The impact of ageing on public expenditure projections for the EU-25 Member States on pensions, health care, long-term care, education and unemployment transfers (2004-2050). European Economy. Special Report. No. 1. 2006. Luxembourg: Office for Official Publications of the EC. http://ec.europa.eu/economy_finance/ publications/european_economy/2006/eespecialreport0106_en.htm

European Commission (2005). Changing Population of Europe: Uncertain Future, UPE (final project report). Luxembourg: Office for Official Publications of the EC.

Eurostat, online database (Population/Social conditions, Population, Population projections), http://europa.eu.int/comm/eurostat/

Eurostat (2005). EU25 population rises until 2025, then falls. Eurostat press release 448/2005 of 8 April 2005.

Góra, M. (2005). Pension expenditure as the part of GDP: Social security vs. economic growth. Discussion Paper No.265. Project on Intergenerational Equity. Hitotsubashi: Institute of Economic Research, Hitotsubashi University.

Kannisto-Thatcher Database on Old Age Mortality (n.d.). Max Planck Institute for Demographic Research. Retrieved April 4, 2006, from http://www.demogr. mpg.de/

Keilman, N., D. Q. Pham, and A. Hetland (2002). Why population forecasts should be probabilistic - illustrated by the case of Norway. Demographic Research, 6(15), 409-454.

Keilman, N., and D. Q. Pham (2004). Empirical errors and predicted errors in fertility, mortality and migration forecast in the European Economic Area, Discussion Paper No 386, Statistics Norway, Social and Demographic Research.

Kotowska, I. E., A. Matysiak, M. Muszyńska, and A. Abramowska (2005). Work and Parenthood. Comparative Report and Summary Policy Implications. Research report for the European Commission prepared within the DIALOG Project, Work package: Work and Parenthood.

Kupiszewska, D., and B. Nowok (forthcoming). Comparability of statistics on international migration flows in the European Union. In J. Raymer, and F. Willekens (Eds.), The estimation of international migration in Europe: Data, models and estimates. Chichester: Wiley.

Marciniak, G. (1999). Symulacje zmian wzorca płodności do 2005r. Studia Demograficzne, 2(136).

Muszyńska, M. (2005). Structural and cultural determinants of fertility in Europe. PhD thesis. Warsaw: Warsaw School of Economics, Institute of Statistics and Demography.

Nowok, B. (forthcoming). Evolution of international migration statistics in selected Central European countries. In J. Raymer, and F. Willekens (Eds.), The
estimation of international migration in Europe: Data, models and estimates. Chichester: Wiley.

OECD (2003). Transforming Disability into Ability. Policies Promoting Work and Income Security for Disabled People. Paris: OECD.

Oeppen, J., and J. W. Vaupel (2002). Broken limits to life expectancy. Science, 296(5570), 1029-1031.

Olshansky, S. J., B. A. Carnes, and C. Cassel (1990). In search of Methuselah: Estimating the upper limits to human longevity. Science, 250(4981), 634-640.

Shryock, H. S., and J. S. Siegel (1976). The methods and materials of demography. New York: Academic Press.

UPE (2004). A forecast of the population of Europe 2004-2050, http://www.stat.fi/ tup/euupe/

United Nations and Eurostat (1998). Recommendations for the 2000 censuses of population and housing in the ECE region. Statistical Standards and Studies No. 49. New York and Geneva: United Nations.

United Nations (2004).World Population Prospects: The 2004 Revision Database, http://esa.un.org/unpp/

Vaupel, J.W. (2005). The biodemography of aging. In L. W. Waite (Ed.), Aging, health, and public policy: demographic and economic perspectives (pp.48-62). New York: Population Council. (Supplement: Population and Development Review, 30, 2004).

Wóycicka, I., and R. Rurarz (2007). Świadczenie opieki. In I. E. Kotowska, S. Sztanderska, and I. Wóycicka (Eds.). Aktywność zawodowa i edukacyjna a obowiazki rodzinne $w$ Polsce $w$ świetle badań empirycznych, Warsaw: Wydawnictwo Scholar.

## Annex

Table 1: Data sources for fertility indicators for Poland

| Indicator | Period | Data source | Notes |
| :---: | :---: | :---: | :---: |
| Period Total Fertility Rate (TFR) | 1960-1994 | Council of Europe |  |
|  | 1995-2004 | Eurostat online database |  |
| Mean age at childbirth | 1960-1994 | Council of Europe |  |
|  | 1995-2004 | Eurostat online database |  |
| Period age-specific fertility rates (in completed ages*) | 1971-1989 | Council of Europe | 5-year age groups reconstructed into single ages, using gamma distribution (see Marciniak 1999) |
|  | 1990-1996 | Central Statistical Office of Poland | calculated from annual number of births and total population |
|  | 1997-2004 | Eurostat online database | single ages |

[^4]Table 2: Data sources for mortality indicators for Poland

| Indicator | Period | Data source | Notes |
| :--- | :--- | :--- | :--- |
| Age-specific mortality rates <br> (in reached ages) | $1950-1989$ | Central Statistical <br> Office of Poland | probabilities of dying for ages 0- <br> 80 (in 5-year age groups) <br> converted into age-specific <br> mortality rates and interpolated <br> into single ages by Karup-King <br> method (Shryock and Siegel <br> 1976) |
|  |  |  | Eurostat online <br> database |
|  | $1990-2004$ | calculated from annual number of <br> deaths and total population |  |
|  | $1971-2004$ | Kannisto- <br> Thatcher <br> Database | for ages 80+ (in single ages) |
| Life expectancy at birth | $1950-2004$ | Central Statistical <br> Office of Poland |  |
|  |  |  |  |


[^0]:    ${ }^{1}$ The authors are listed in alphabetical order.
    ${ }^{2}$ PhD candidate and Research Assistant, Institute of Statistics and Demography, Warsaw School of Economics, Warsaw. E-mail: amatys@sgh.waw.pl.
    ${ }^{3} \mathrm{PhD}$ candidate, Population Research Centre, University of Groningen, Groningen; Netherlands Interdisciplinary Demographic Institute. E-mail: nowok@nidi.nl.

[^1]:    ${ }^{4}$ The UPE project (Changing Population of Europe: Uncertain Future) was funded by the EU Commission within the Fifth Framework Programme (HPSE-CT-2001-00095) (see UPE 2004). The objective of the project was to develop and implement stochastic forecasting in order to improve the quantification of uncertainty of future demographic trends. Stochastic forecasts were prepared for the old EU-15 countries, Iceland, Norway, and Switzerland.

[^2]:    ${ }^{5}$ A de facto population consists of all individuals present in the area regardless of their usual place of residence. A de jure population covers all persons having the right to legal residence in the area and normally living in it. Very often the concept of usual residence is referred to as though it is synonymous with the concept of de jure residence.

[^3]:    ${ }^{6}$ Assuming that the TFR is an estimate of a rate of an underlying Poisson process (sum of independent Poisson processes with parameters equal to age-specific fertility rates) the hypothesis that the increase in TFR in urban areas in 2004 as compared to 2003 is insignificant was rejected at p -value $=0.000$. An increase in fertility in urban areas resulted in a rise in TFR at the country level from 1.223 to 1.227 at $p$-value $=0.039$.

[^4]:    *The age-specific fertility rates in completed ages are automatically converted by PEP into age-specific fertility rates in reached ages

