

Gas and dust in the star-forming region ρ Oph A^{*,**,***}

The dust opacity exponent β and the gas-to-dust mass ratio $g2d$

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ABSTRACT

Aims. We aim at determining the spatial distribution of the gas and dust in star-forming regions and address their relative abundances in quantitative terms. We also examine the dust opacity exponent β for spatial and/or temporal variations.

Methods. Using mapping observations of the very dense ρ Oph A core, we examined standard 1D and non-standard 3D methods to analyse data of far-infrared and submillimetre (submm) continuum radiation. The resulting dust surface density distribution can be compared to that of the gas. The latter was derived from the analysis of accompanying molecular line emission, observed with *Herschel* from space and with APEX from the ground. As a gas tracer we used N_2H^+ , which is believed to be much less sensitive to freeze-out than CO and its isotopologues. Radiative transfer modelling of the N_2H^+ ($J = 3-2$) and ($J = 6-5$) lines with their hyperfine structure explicitly taken into account provides solutions for the spatial distribution of the column density $N(H_2)$, hence the surface density distribution of the gas.

Results. The gas-to-dust mass ratio is varying across the map, with very low values in the central regions around the core SM 1. The global average, ≈ 88 , is not far from the canonical value of 100, however. In ρ Oph A, the exponent β of the power-law description for the dust opacity exhibits a clear dependence on time, with high values of 2 for the envelope-dominated emission in starless Class-I sources to low values close to 0 for the disk-dominated emission in Class III objects. β assumes intermediate values for evolutionary classes in between.

Conclusions. Since β is primarily controlled by grain size, grain growth mostly occurs in circumstellar disks. The spatial segregation of gas and dust, seen in projection toward the core centre, probably implies that, like $C^{18}O$, also N_2H^+ is frozen onto the grains.

Key words. ISM: general – ISM: individual objects: rho Oph A – dust, extinction – ISM: abundances – stars: formation

1. Introduction

It is widely accepted that the gas-to-dust mass ratio ($g2d$) in our Galaxy has a value of about 100. Of course, this is an average value and it does, in particular, pertain to the diffuse interstellar medium (ISM). However, this value is also commonly adopted for dense cloud environments, such as star-forming regions, and the methods used to determine that parameter are described for instance by Kenyon et al. (1998), Draine (2003), and Vuong et al. (2003). Based on observations of CO isotopologues and stellar extinction values in the nearby star-forming regions in

Taurus and Ophiuchus, Frerking et al. (1982) established the still widely used molecular gas-dust relations, that is, $N(^X C^Y O) \propto A_V$, $A_V \lesssim 20$ mag, and $^{12}C^{16}O/H_2 \sim 8.5 \times 10^{-5}$. For higher A_V , saturation makes these relations less useful.

Young & Scoville (1991) discussed the high average $g2d$ of ~ 600 obtained for molecular clouds, where gas masses refer to $HI + H_2$. The latter was derived from CO observations and the dust masses were determined from IRAS observations. Furthermore, based on data for HI and HII regions, Spitzer (1978) quoted the rather wide range of 20 to 700 for this parameter. A value of about 450 was found by Liseau et al. (1995) for L 1688 using CS maps and 60 μm IRAS data. A high $g2d$ would also be consistent with the low oxygen abundance in ρ Oph A found by Liseau & Justtanont (2009). Figure 11 of Brinchmann et al. (2013), which is based on a large number of galaxies, supports this view on larger, extragalactic scales.

One of the reasons for these high $g2d$ values could be that large portions of the dust are at temperatures considerably lower than 30 K and, hence, remained undetected by IRAS (Young & Scoville 1991). However, at temperatures below about 25 K, the abundance of the dominant gas tracer, CO and its isotopologues, could also become highly diminished by freeze-out (e.g., Lippok et al. 2013, and references therein). One might therefore select spectral lines of a molecule that is seen in regions where CO is

* Based on observations with APEX, which is a 12 m diameter submillimetre telescope at 5100 m altitude on Llano Chajnantor in Chile. The telescope is operated by Onsala Space Observatory, Max-Planck-Institut für Radioastronomie (MPIfR), and European Southern Observatory (ESO).

** And also based on observations with *Herschel* which is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.

*** FITS files containing the data of Figs. 2, 11, 12, and 16–18 are available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/578/A131>

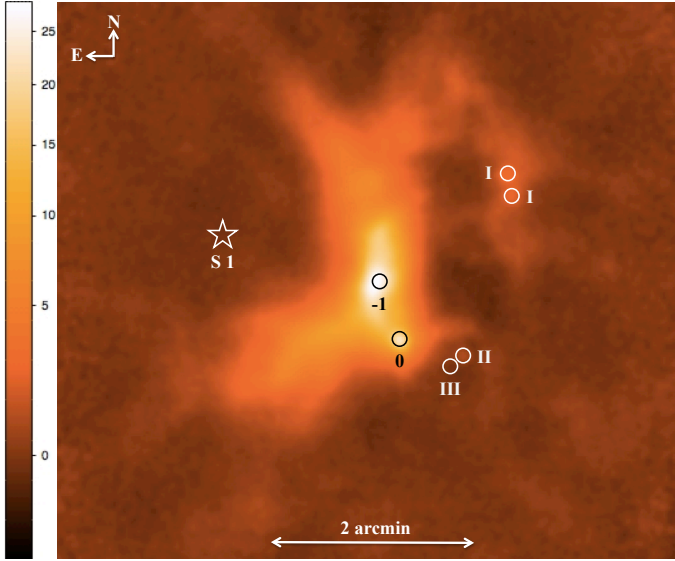


Fig. 1. Core ρ Oph A in the continuum at $350\ \mu\text{m}$, where the different evolutionary phases are identified. The position of the dominating radiative source S 1 is shown by the star symbol. The colour scale is in units of Jy beam^{-1} , with the circles corresponding to the beam size. The angular scale is shown at the bottom of the figure and the orientation in the sky in the upper left corner. The APEX maps of this paper have their origin at RA = $16^{\text{h}}26^{\text{m}}27^{\text{s}}.90$, Dec = $-24^{\circ}23'57''.00$ (J2000.0).

thought to be depleted. One such molecule is diazenylium, N_2H^+ (e.g., Caselli et al. 1999), which is formed from N_2 (which remains in the gas phase to somewhat lower temperatures than CO) and is removed from the gas phase mainly by CO (Bergin et al. 2002; Öberg et al. 2005). However, as pointed out by Bergin et al. (2002), even N_2H^+ (and N_2) may become depleted and thus leave very few molecular probes (perhaps only H_2D^+ , Brünken et al. 2014) to study the centres of the densest cores.

The rotational transitions ($J = 3-2$) and ($J = 6-5$) of N_2H^+ , at 280 GHz and 560 GHz and with upper level energies of 27 K and 94 K, respectively, could fulfil these requirements. In particular, the (1–0) line at 93 GHz, having an upper level energy similar to that of CO, has been widely used for dense interstellar clouds, including the ρ Oph A region (e.g., Di Francesco et al. 2004). However, E_1/k is only 4.5 K and at considerably higher temperatures, the population of the $J = 0$ and $J = 1$ levels changes only slowly and does as such not contribute much to the understanding of the overall excitation of the molecule.

Friesen et al. (2014) have used the Atacama Large Millimeter/submillimeter Array (ALMA) to observe ρ Oph A in the N_2H^+ (4–3) lines toward a small region ($<20'' \times 20''$), but the paper focused on the continuum data. There are no line profiles nor line maps shown for these data, which, according to Friesen et al. (2014), were either self-absorbed or resolved out by the interferometer. The authors also noted that line and continuum sources did not coincide, neither for SM 1 nor for SM 1N, a point of potential importance (see below, Sect. 4.4). The primary beam of these observations is smaller than the single-dish beams of our observations.

As revealed by pure-rotational H_2 line emission, relatively high temperatures, $\gtrsim 10^3$ K, are present in the interface regions toward the dominating radiation source S 1 (Fig. 1). In addition, Liseau et al. (1999) found extended [O I] $63\ \mu\text{m}$, [O I] $145\ \mu\text{m}$ and [C II] $157\ \mu\text{m}$ emission, which is indicative of temperatures in excess of 100 K. These phenomena probably refer to the outer

layers of the cloud. The N_2H^+ (6–5) line could be used to probe that temperature regime in a coherent map.

Already early on, the actively star-forming ρ Oph clouds attracted wide attention, largely because the nearest stellar cluster is forming there. This is the dominant star formation mode, in contrast to more isolated star formation as in the Taurus-Auriga clouds, for example, that is contributing only little to the stellar initial mass function (IMF) of the Galaxy. Not surprisingly therefore, a huge body of literature exists, and we refer to the review by Wilking et al. (2008) and also to a few recent specific papers on the distribution of molecular gas and icy grains (Shuping et al. 2000; Pontoppidan 2006; André et al. 2007; White et al. 2015). For these clouds in ρ Oph, the visual extinction can locally reach extremely high values ($\text{max } A_V > 10^2$ mag).

The nearby $3'$ (0.1 pc) ρ Oph A core (Loren et al. 1990) is unique in the sense that all phases of the earliest phases of stellar evolution are present in a very compact region (see Figs. 1 and 2) – from starless clumps, Class –1 (SM 1), via Class 0 (VLA 1623), Class I (GSS 30-1) and Class II (LFAM 3) to Class III (GSS 32) (see, e.g., Comeron et al. 1993; Bontemps et al. 2001; White et al. 2015). Potentially, this fact may make it possible to follow the time evolution of the dust in various locations in the core, including grain growth and changes in composition, such as ice coatings onto initially “bare” grains. Such a scenario could have considerable effect on theories of planetary formation (e.g., the location of the snow line in the circumstellar disks) and help to relax tight timescale requirements, particularly in the outer, less dense regions of the disks. The status of the current understanding of the dust evolution in disks has recently been summarized by Testi et al. (2014).

In this paper, we focus on the gas and dust contents of the nearby star-forming ρ Oph A core, observed in the far-infrared (FIR) and sub-millimeter spectral regions (submm). For the distance we adopt the accurately determined value with the Very Long Baseline Array (VLBA) by Loinard et al. (2008, viz. $D = 120.0^{+4.5}_{-4.2}$ pc). The organization is as follows: in Sect. 2, our mapping observations of freeze-out insensitive molecules are described. These observations have been obtained from space with *Herschel* (Pilbratt et al. 2010) and from the ground with APEX at 5100 m altitude. There, maps in the submm continuum have also been obtained. This section also describes the reduction of these data, and the results are presented in Sect. 3. These are discussed in Sect. 4, illustrating specifically the aspects of spectral line overlap and also of geometry in the radiative transfer problems. We compare the results obtained with tools widely in use with those arrived at with our own developments. The conclusions follow in Sect. 5.

2. Observations and data reduction

2.1. SHeFI-APEX-2 and Herschel-HIFI

2.1.1. APEX-2

The Atacama Pathfinder Experiment (APEX) is a 12 m single-dish telescope situated at 5100 m altitude in Chile. The pointing accuracy of the telescope has been determined at $2''$ (rms). We used the Swedish heterodyne facility instrument APEX-2 (Vassilev et al. 2008) for the raster-mapping observations of ρ Oph A in the $J = 3-2$ rotational transition of the N_2H^+ molecule. The central rest frequency is at 279 515.06711 MHz and the average zenith optical depth was 0.04. At 279.5 GHz, the beam size is $FWHM = 22''$, the main beam efficiency is $\eta_{\text{mb}} = 0.73$, and the LSB receiver temperature was 125 K. We used the

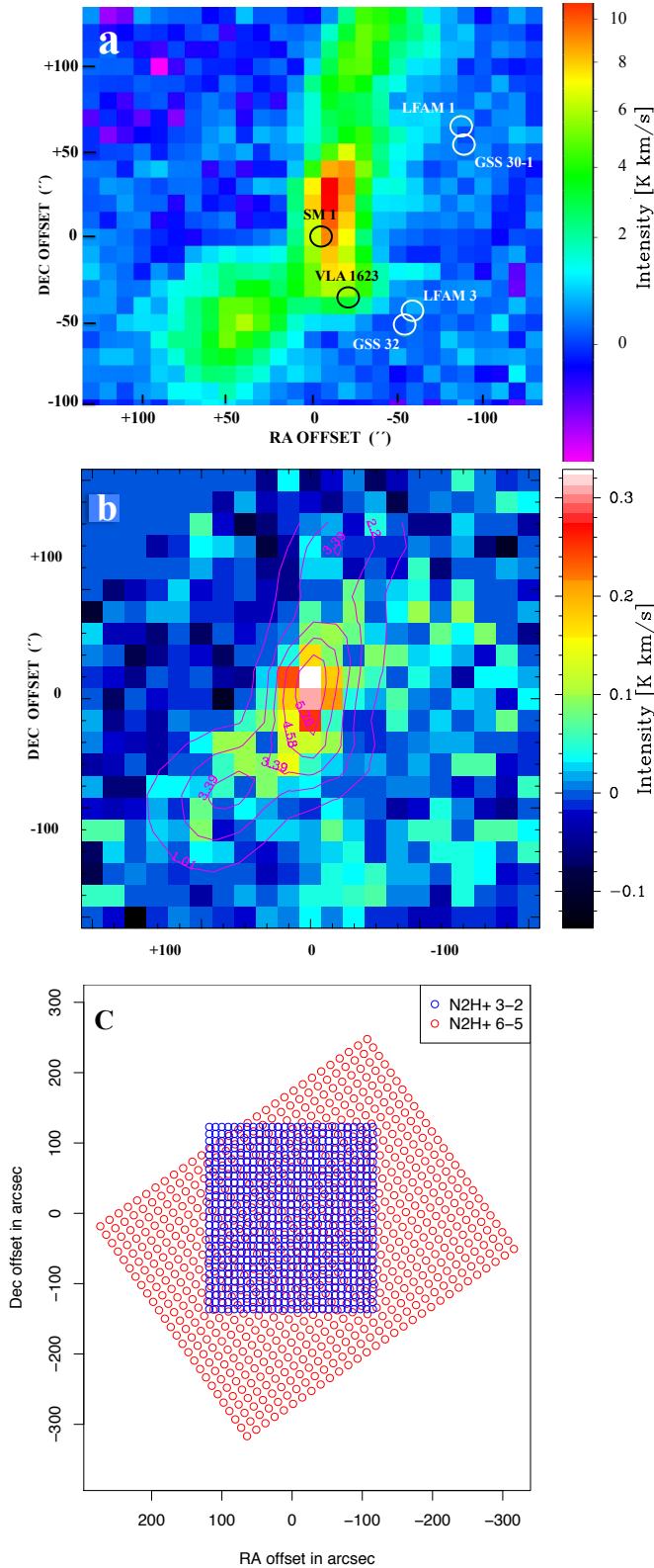


Fig. 2. **a)** Integrated intensity, $\int T_A dv$, of N_2H^+ (3–2) at 22'' resolution with APEX and with a sampling rate of 10''/pixel is shown in the upper panel. The positions of the SED-class sources of Fig. 1 are shown with their proper designations. **b)** *Herschel* map of the ρ Oph A core in the N_2H^+ (6–5) line that is rotated to align with the APEX data. The (6–5) map has a resolution of 38'' and is sampled at a rate of 16''/pixel. Superposed, and shown as contours, is the map in the (3–2) line at degraded resolution. **c)** Orientation of the maps in the sky.

Fast Fourier Transform Spectrometer with 73.6 kHz wide channels, resulting in a velocity resolution of 0.082 km s^{-1} per channel and a spectral coverage corresponding to 200 km s^{-1} . The data reduction involved the fitting and removal of the baselines and was made with the locally available software package *xs*¹.

2.1.2. HIFI

The ($J = 6-5$) line of N_2H^+ was observed at the same time as our *Herschel* H_2O maps (2012, GT2_riseau_1). The observational details regarding the partial map data of 2010 (Table 1) that were obtained within the KPGT_evandish_1 programme were already described in detail by Bjerkeli et al. (2012). In their Fig. 1, offsets are relative to the (0, 0)-position at $\alpha_{2000} = 16^{\text{h}}26^{\text{m}}26^{\text{s}}.4$, $\delta_{2000} = -24^{\circ}24'31''$. The more extended mapping observations in 2012 were made on-the-fly, with a reference position 14' away. The data reduction was made within HIPE 10². For the final composite map, the zero-offset is at $\alpha_{2000} = 16^{\text{h}}26^{\text{m}}27^{\text{s}}.78$, $\delta_{2000} = -24^{\circ}23'50''.3$, which is slightly offset from the APEX origin by $(-1''.6, -6''.7)$ and which is smaller than the beam size at 559 GHz, that is, 38''. At this frequency in HIFI-band 1, the main beam efficiency³ is $\eta_{\text{mb}} = 0.63$.

2.2. LABOCA and SABOCA

The continuum observations were carried out with two bolometer multi-pixel cameras, viz. the Large Apex Bolometer Camera LABOCA (Siringo et al. 2009) and the Submillimetre Array, that is, SABOCA (Siringo et al. 2010). The effective operating frequencies correspond to $870 \mu\text{m}$ and $350 \mu\text{m}$, with about 150 and $50 \mu\text{m}$ wide filters, respectively⁴. The resolutions are 19''.5 and 7''.5, respectively. At the two wavelengths, the maps of ρ Oph A span almost $40' \times 40'$ and $8' \times 8'$, respectively (Fig. 3), and in both maps the centre coordinates are at $RA = 16^{\text{h}}26^{\text{m}}27^{\text{s}}.90$ and $Dec = -24^{\circ}23'57''.0$ for the epoch of J2000.0.

The 11'.4 circular field of view (FOV) of LABOCA is determined by the 295 bolometers, which are arranged with 36'' spacings in between them. The number of loosely spaced bolometers of SABOCA is 39 and its FOV is 1'.5. The FOV is under-sampled for both cameras and is filled by repetitive continuous scanning of the mapped region. For both LABOCA and SABOCA, the data reductions were made with CRUSH⁵. CRUSH uses the actual atmospheric opacities at the time of observation. For the two data sets, average zenith optical depths were 0.42 at $870 \mu\text{m}$ and 1.07 at $350 \mu\text{m}$, with a range of 0.55 to 1.20 for the latter.

3. Results

3.1. Spectral line data

The maps of main-beam corrected integrated intensity, $\int T_{\text{mb}} dv$, of N_2H^+ (6–5) and (3–2) are shown in Fig. 2. The mapping of the (6–5) line with HIFI was made at an angle with respect to the equatorial coordinate system, so that the map had to be rotated to be properly aligned with the APEX data (Fig. 2c). In Figs. 2a

¹ <ftp://yggdrasil.oso.chalmers.se/pub/xs/>

² *Herschel* interactive processing environment, see herschel.esac.esa.int/hipe/

³ Mueller et al. (2014): Release Note #1, HIFI-ICC-RP-2014-001, v1.1

⁴ <http://www.apex-telescope.org/instruments/>

⁵ <http://www.submm.caltech.edu/sharc/crush/download.htm>

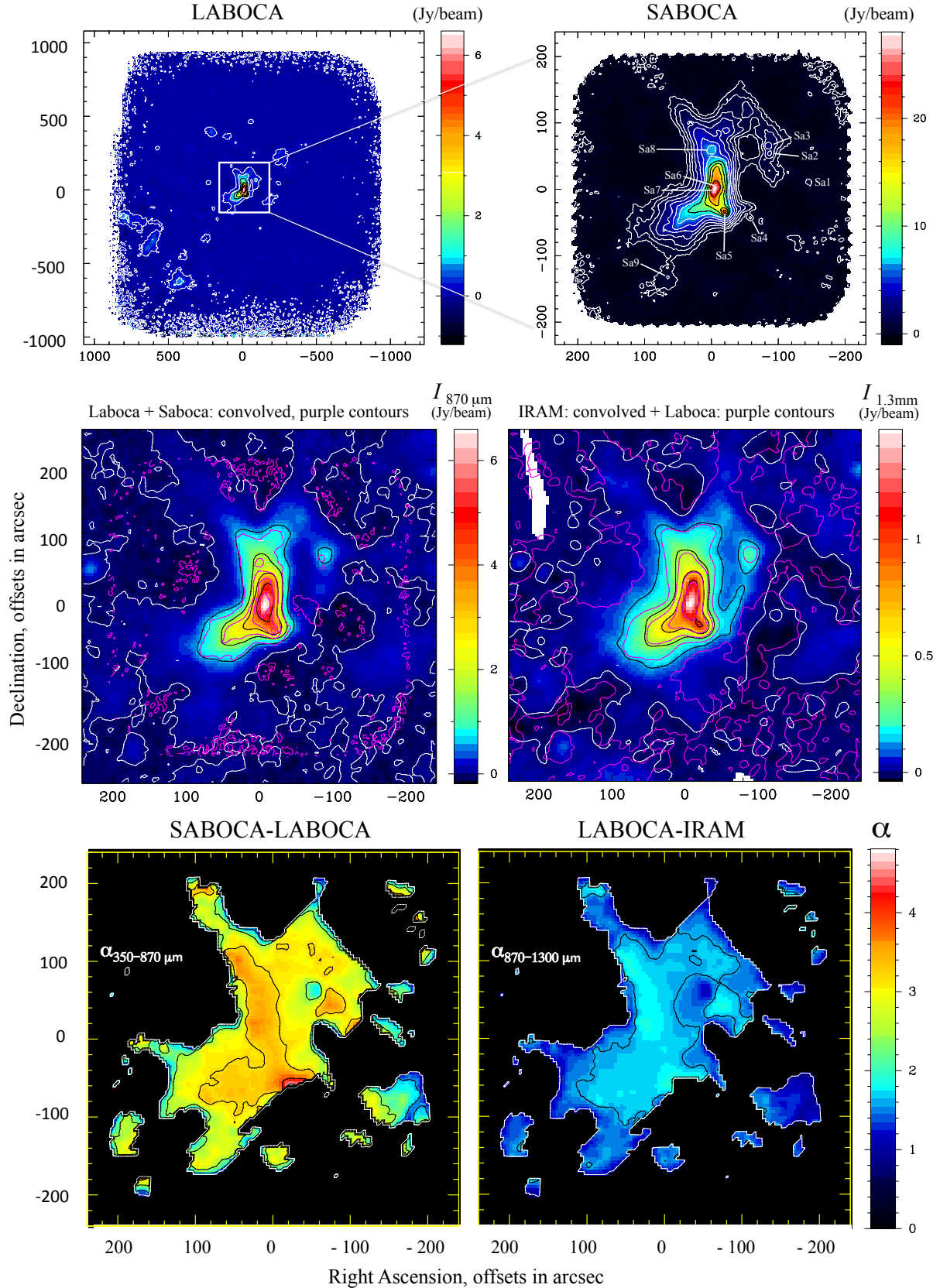


Fig. 3. *Top:* ρ Oph A observed at 870 μm with LABOCA (*left*) and at 350 μm with SABOCA (*right*). Offsets are in seconds of arc and units are in Jy/beam. The origin, (0,0), is the same as in Fig. 1 and the numbers refer to Table 2. *Middle:* SABOCA data (*left*, purple contours), degraded to the 19''5 resolution of the LABOCA map (in colour). The colours show the IRAM map (*right*) of Motte et al. (1998), convolved to 19''5 resolution, and shifted to the position of the LABOCA origin. The LABOCA data are shown as purple contours. *Bottom:* observed spectral index $\alpha = \Delta \log I_\nu / \Delta \log \nu$ for the wavebands 350 μm –870 μm (*left*) and 870 μm –1.3 mm (*right*).

Table 1. Log of observations.

Instrument	Prog/Obs ID ESO/ <i>Herschel</i>	Mode	Frequency (GHz)	Beam HPBW	Observing date yy–mm–dd	t_{int} (s)	Map dimension RA \times Dec	PA
APEX-2 ^a	090.F-9319(A)	N ₂ H ⁺ (3–2)	279.515067	22''	12–09–22 to 25	65160	4'26 \times 4'32	0°
HIFI ^b	1342204010 ^c	N ₂ H ⁺ (6–5)	558.957500	38''	10-09-01	6552	5'0 \times 2'0	35°
	1342251245 ^d				12-09-21	3608	5'8 \times 1'0	35°
	1342251246 ^e				12-09-21	5712	5'0 \times 2'0	125°
	1342251247 ^f				12-09-21	5712	5'0 \times 2'0	125°
	1342251429 ^g				12-09-26	3608	5'8 \times 1'0	35°
LABOCA ^a	090.F-9304(A)	Continuum	345	19''5	12–08–17	9298	38'3 \times 35'5	0°
SABOCA ^a	090.F-9304(B)	Continuum	852	7''5	12–08–22	20419	7'75 \times 7'85	0°

Notes. ^(a) Map offsets refer to $\alpha_{2000} = 16^{\text{h}}26^{\text{m}}27^{\text{s}}90$, $\delta_{2000} = -24^{\circ}23'57''.0$. ^(b) The HIFI data refer to OD 475 on 10-09-01 and OD 1221 on 12-09-16 and OD 1231 on 12-09-26, with a total integration time of 25192 s. ^(c) Observed centre coordinates are $\alpha_{2000} = 16^{\text{h}}26^{\text{m}}26^{\text{s}}38$, $\delta_{2000} = -24^{\circ}24'31''$; ^(d) $16^{\text{h}}26^{\text{m}}13^{\text{s}}79$, $-24^{\circ}22'31''$; ^(e) $16^{\text{h}}26^{\text{m}}21^{\text{s}}30$, $-24^{\circ}26'15''$; ^(f) $16^{\text{h}}26^{\text{m}}31^{\text{s}}73$, $-24^{\circ}22'47''$; ^(g) $16^{\text{h}}26^{\text{m}}38^{\text{s}}97$, $-24^{\circ}26'32''$.

and b, the shown pixel sizes correspond to the respective samplings, and in b, the superposed contours show the (3–2) data after convolution to the (6–5) resolution (38'').

3.2. Continuum data

The reduced data are shown in Fig. 3 for both LABOCA and SABOCA, where intensity units are Jy beam^{-1} . These intensity scales assume Gaussian beams given in Table 1, and in the figure, the contour levels for LABOCA are (1) –1.21, (2) 0.13, (3) 0.59, (4) 1.20, (5) 2.02, (6) 3.13, (7) 4.61, (8) 6.60 Jy beam^{-1} . For SABOCA, the corresponding contours are (1) –1.01, (2) 0.31, (3) 0.74, (4) 1.31, (5) 2.06, (6) 3.06, (7) 4.38, (8) 6.12, (9) 8.44, (10) 11.50, (11) 15.55, (12) 20.92, (13) 28.03 Jy beam^{-1} . The value of 1 Jy beam^{-1} corresponds to an intensity of about 100 MJy sr^{-1} for LABOCA and 600 MJy sr^{-1} for SABOCA, and with 1σ of the rms noise corresponding to 5 and 30 MJy sr^{-1} , respectively.

At the higher resolution of the SABOCA observations, individual sources can be identified, and their equatorial coordinates are presented in Table 2. The rms pointing accuracy of the APEX telescope is about 2''. The observed field at $350 \mu\text{m}$ is much smaller than that at $870 \mu\text{m}$ (Fig. 3). For quantitative applications, the SABOCA data have to be degraded to the appropriate LABOCA values, that is, 19''5, and re-sampled onto a 4'' grid. This is illustrated in the middle panels of Fig. 3, where SABOCA contours are shown superposed on the LABOCA intensities. In addition, the IRAM 1.3 mm data of Motte et al. (1998) are shown, also convolved to the 19''5 resolution of LABOCA and sampled onto the 4'' regular grid. For the comparison with the APEX results, the map of ρ Oph A was shifted to the same centre coordinates.

4. Discussion

We start our discussion with determining the physical parameters for the gas, in particular T_{kin} and $N(\text{H}_2)$, using spectral line maps of (presumably) optically thin emission, and C^{18}O has often been used to guarantee this. However, as shown by Liseau et al. (2010) on the basis of C^{18}O (3–2) and $^{13}\text{C}^{18}\text{O}$ (3–2) observations of ρ Oph A, optical depths do exceed unity even in the rare isotopologues of CO. In those cases, the observed radiation does not carry information about the entire core but is restricted to layers closer to the surface, leading to erroneous

Table 2. SABOCA objects at 7''5 resolution.

ID	RA (J2000) hh mm ss.sss	Dec (J2000) ° ' "	Compactness/source
Sa1	16 26 17.30	–24 23 46.5	diffuse, ISO-Oph 21
Sa2	16 26 21.53	–24 23 04.5	point, GSS 30-1
Sa3	16 26 21.75	–24 22 51.0	point, LFAM 1
Sa4	16 26 23.67	–24 24 39.8	point, LFAM 3
Sa5	16 26 26.42	–24 24 30.4	point, VLA 1623
Sa6	16 26 27.49	–24 23 56.2	diffuse, SM 1N
Sa7	16 26 27.52	–24 23 54.8	diffuse, SM 1
Sa8	16 26 27.74	–24 22 55.5	diffuse
Sa9	16 26 32.68	–24 26 09.8	diffuse

estimates of the overall temperature and density distribution. For instance, temperatures based on such observations are around the (for a dense core) surprisingly high value of $\sim 25 \text{ K}$. At temperatures below this, which are commonly encountered in dense cores, the CO gas will be depleted because of freeze-out of the molecules onto the surfaces of the accompanying grains. In contrast, N_2H^+ molecules remain in the gas phase down to much lower temperatures (Lippok et al. 2013, and references therein). Except for a few exceptions, only the (1–0) line and its hyperfine components have been observed and the analysis generally assumed thermodynamic equilibrium (LTE). Here, we make multi-transition analyses and treat the radiative transfer in non-LTE. The implications for our observations are described in the next section.

4.1. Gas temperature, opacity, and mass

For large numerical grids, the publicly available computer code radex (van der Tak et al. 2007) is very suitable. In its present form, the code is unable to properly handle the transfer in optically thick lines with extremely closely spaced transitions, however (the ‘‘line overlap’’ problem, Fig. 6). In addition, by construction, the code will not return the proper shapes of the lines. To surmount these difficulties, we used for the analysis an accelerated lambda iteration (ALI) code that takes line-overlap explicitly into account and also correctly computes the line profiles with which the observations can be compared directly.

The upper level energy of the N_2H^+ (3–2) transition corresponds to nearly 28 K , close to previous estimates of the

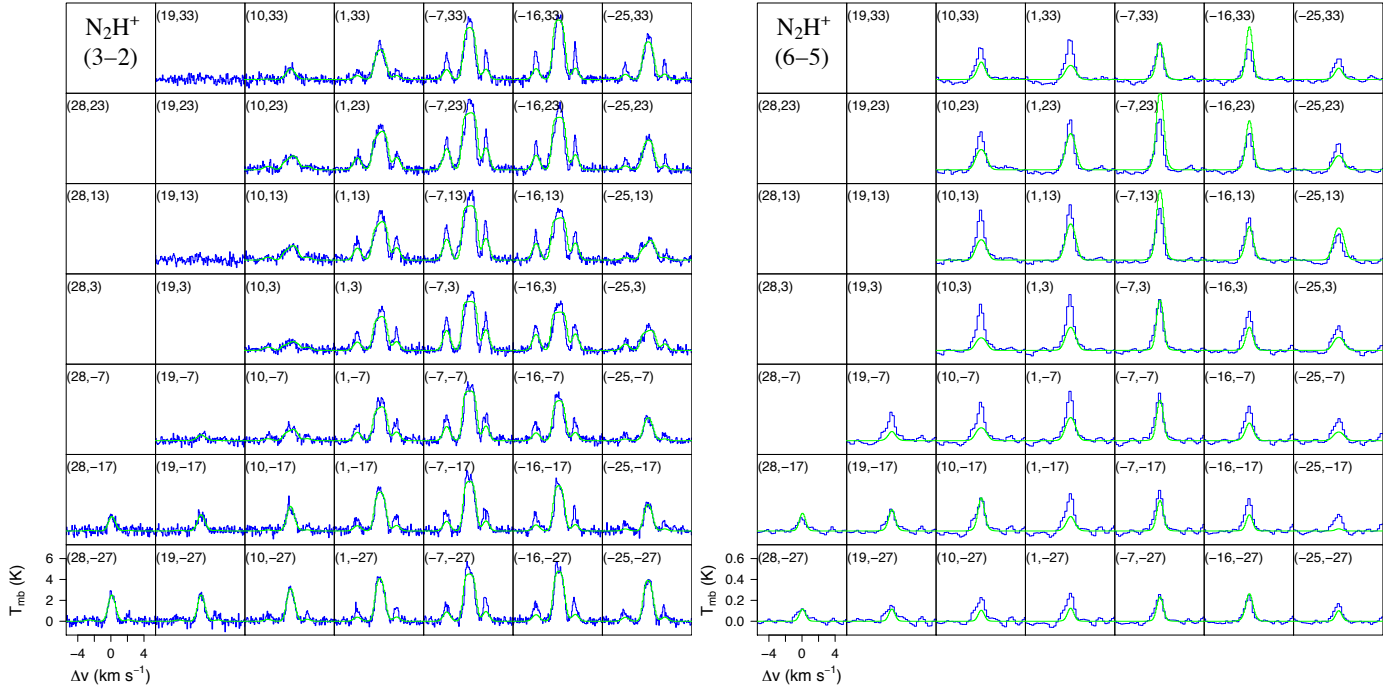


Fig. 4. Centre of the three sub-regions of the mapped area showing the best-fit models (green) for the observed (blue) N_2H^+ (3–2) and (6–5) line profiles (left and right, respectively). The radiative transfer with ALI takes the overlapping transitions of the 38 hyperfine components into account, with the frequencies of Pagani et al. (2009). In the small frames, the numbers in the upper left corners are equatorial offsets in arcsec from the map origin (0, 0). In the lower left frames, the scales are given for T_{mb} (K) and $\Delta v = v - v_{\text{LSR}}$ ($v_{\text{LSR}} = +3.5 \text{ km s}^{-1}$), respectively (Figs. 5 and 6).

kinetic gas temperature. The observed (3–2) lines exhibit the remarkable feature that the satellite lines reveal strengths that are almost similar to that of the main line (Fig. 4), that is, much stronger than expected for optically thin radiation in LTE (Fig. 6). In fact, this strongly suggests optically very thick emission in the overlapping components of the central, spectrally non-resolved, main line. This line anomaly is in contrast to the observed (6–5) line profile, which appears nearly Gaussian (however, the spectral resolution is lower). The $J = 6$ level is about 94 K above ground.

The Onsala ALI code (P. Bergman) is based on the work by Rybicki & Hummer (1991) and Rybicki & Hummer (1992) and the bench-marking has been reported by Maercker et al. (2008). It takes line overlap explicitly into account and, in the following, we use this program to model the multitude of hfs lines of N_2H^+ . The geometry is spherically symmetric, which needs to be kept in mind when comparing model line profiles with observed ones. Dust continua are included, but switched out in the simulated on-off observations presented below (zero baseline).

The radiative transfer in the hfs transitions with line overlap was computed using the energy levels that we derived from the frequencies presented by Pagani et al. (2009). The collisional de-excitation rate coefficients were adopted from Lique et al. (2015), who have calculated the rates for collisions with H_2 for the temperature range 5 to 70 K and for the lowest hfs levels. However, F. Lique kindly made available to us their entire results for upper energy levels up to $J_{\text{up}} = 7$ prior to publication. The computation of the inverse rates, that is, the collisional excitation rate coefficients, assumed thermal balance.

The region was divided into three parts: the north, centred on N2, the middle, centred on SM 1, and the southeast, centred on N6, where the N-nomenclature refers to the source designations by Di Francesco et al. (2004). However, only pixels with

$\geq 3\sigma$ integrated intensities in both the N_2H^+ (3–2) and (6–5) lines were included. These regions, assumed to be spherical, are about $75''$ in size, hence neighbouring regions are overlapping and radii are 0.02 pc ($6.75 \times 10^{16} \text{ cm}$). We kept the turbulent velocity constant throughout the core, that is, $v_{\text{turb}} = 0.25 \text{ km s}^{-1}$. After a number of initial trials spanning over a much larger parameter space, the ALI code was run on a finer grid around the most probable values, defined by $4.0 \leq \log n(\text{H}_2) \leq 7.0$ in steps of 0.2, $-11.0 \leq \log X(\text{N}_2\text{H}^+) \leq -8.0$ by 0.2 and $5 \leq T_{\text{kin}} \leq 50 \text{ K}$ by increments of 1 K, generating 11776 models. Among these, 2816 solutions were found that fit the observed intensity ratios within the observational errors. Using the individual line profiles, that is, both the shape and the absolute intensity, for both lines, N_2H^+ (3–2) and (6–5) from the same position (pixel), the best-fit ALI solution was selected for that pixel. As best-fit-estimator, we used sums of the residuals, where the higher frequency spectra were weighted more strongly to compensate for their overall lower intensities. In other words, we minimized $\sum_{3-2} (T_{\text{obs}} - T_{\text{ALI}})^2 + 10 \times \sum_{6-5} (T_{\text{obs}} - T_{\text{ALI}})^2$, resulting in a map of best-fit model profiles that, together with the observed ones, are displayed in Fig. 4.

In Fig. 5, the spatial distributions of the best-fit model parameters $N(\text{H}_2)$, T_{kin} , $n(\text{H}_2)$ and $X(\text{N}_2\text{H}^+)$ are shown. Values for the $10''$ pixels span two orders of magnitude in column density, $N(\text{H}_2)$. For the star $\rho \text{ Oph}$, Bohlin et al. (1978) determined the anomalous relation $N(\text{HI} + \text{H}_2)/E(B - V) = 15.4 \times 10^{21} \text{ atoms cm}^{-2} \text{ mag}^{-1}$. Since $R_V = A_V/E(B - V) = 5.5$, the gas-dust relation for $\rho \text{ Oph}$ reads $N(\text{H}_2) = 1.4 \times 10^{21} A_V \text{ cm}^{-2}$. Using this calibration also for the core, the ALI results over $30''$ scales would imply the surprisingly low visual extinction, A_V , through $\rho \text{ Oph A}$ of about 100 mag or lower. Average column densities of a few times 10^{22} cm^{-2} are in accord with previous determinations.

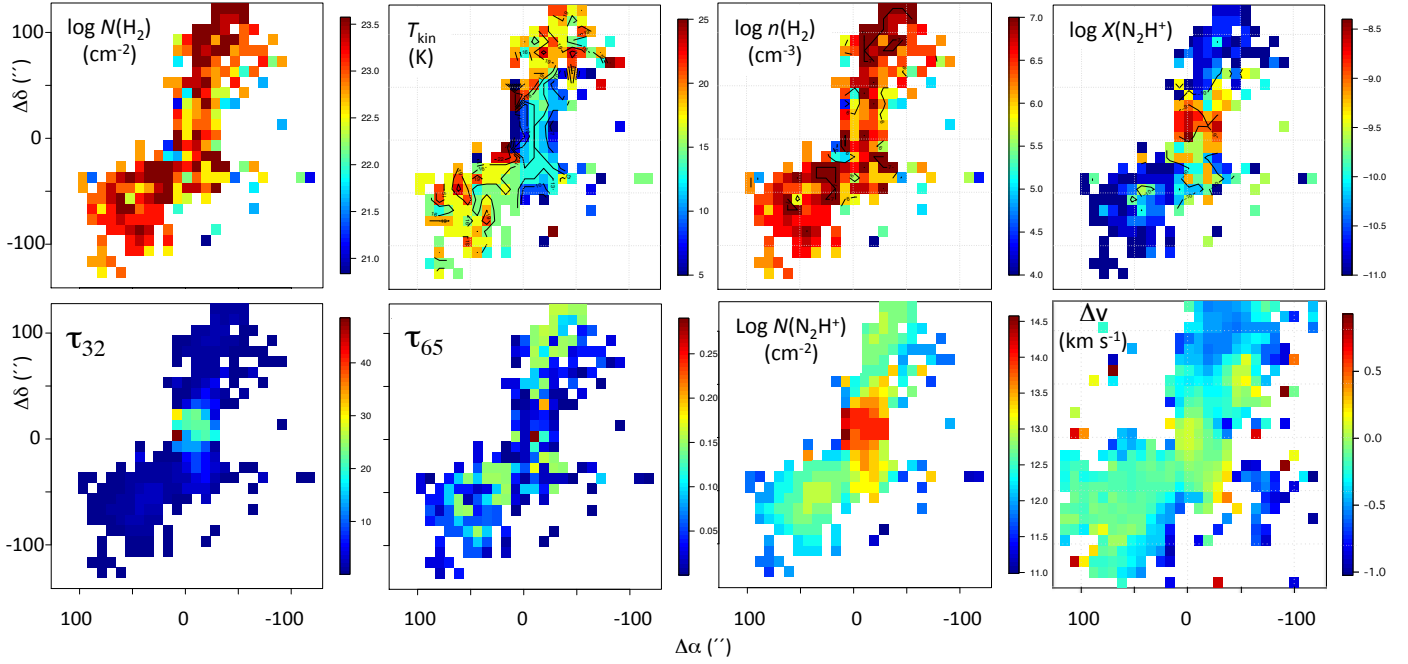


Fig. 5. Best-fit parameters from the ALI modelling of the observed N_2H^+ maps, yielding results as shown in Fig. 4. Modelled data use an intensity threshold of 3σ of the rms noise for both lines. *Upper row: from left to right*, spatial distributions for the gas column density, $N(H_2)$, the kinetic gas temperature, T_{kin} , the gas volume density, $n(H_2)$ and the relative molecular abundance, $X(N_2H^+) = n(N_2H^+)/n(H_2)$. *Lower row: from left to right*, spatial distributions for the line centre optical depth of the (3–2) and (6–5) lines, the N_2H^+ column density, $N(N_2H^+)$, and the residuals of the radial velocity fits Δv in $km\ s^{-1}$. Spatial scales are in arcsec and the colour coding is given by the vertical bars next to each frame.

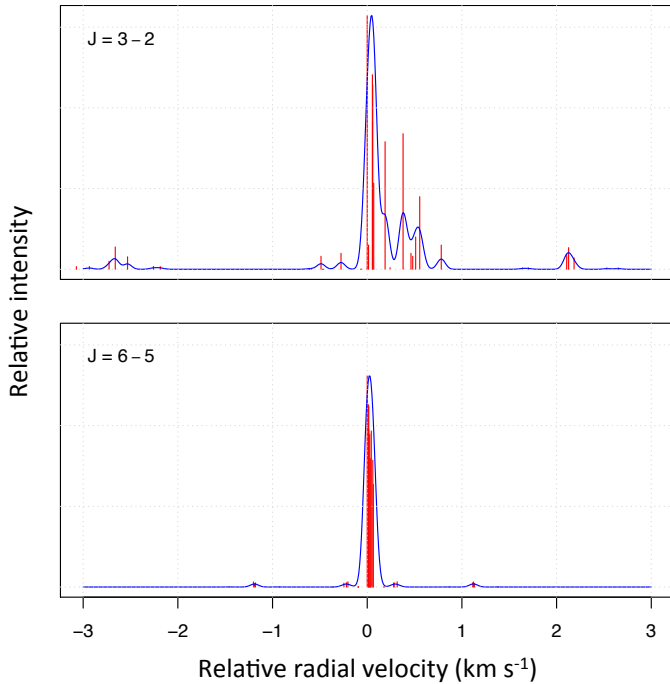


Fig. 6. Hyperfine line strengths (red vertical bars) for the $J = 3-2$ (*upper panel*) and $J = 6-5$ (*lower panel*) transitions. The blue curves are theoretical profiles for an optical depth of 0.1 and a line width of $0.1\ km\ s^{-1}$, scaled to the same maximum amplitude as the LTE line strengths.

Kinetic gas temperatures are about 10–13 K in the central regions, but 17–19 K in the north, and 16–19 K in the southeast. Overall, these temperatures are lower than what has been determined before (e.g., [Bergman et al. 2011](#), and references therein).

The relative abundance, $X(N_2H^+) = N(N_2H^+)/N(H_2)$ appears to peak in the central part, where $\log X(N_2H^+) = -9.0 \pm 0.2$, whereas $X(N_2H^+)$ is generally lower than 10^{-10} in the outer regions. There, derived overall gas volume densities, $n(H_2)$, are around $10^6\ cm^{-3}$, which would be in accord with what might be required by some models of the dust opacity (see below, Sect. 4.4.2). Toward SM 1, and on much smaller scales, [Friesen et al. \(2014\)](#) estimated densities in excess of $10^9\ cm^{-3}$.

As expected, optical depths in the centre of the (3–2) main line are high, explaining the low contrast between main and satellite components (Fig. 5). In contrast, the (6–5) lines are optically thin, which is supported by their observed Gaussian line shapes. The figure also shows the distribution of the radial velocity residuals, $\Delta v = v_0 - v_{LSR}$, where v_0 is the observed central velocity and $v_{LSR} = +3.5\ km\ s^{-1}$. Locally, velocity shifts are lower than $0.2\ km\ s^{-1}$, which is much lower than the assumed turbulent velocity of the gas ($0.6\ km\ s^{-1}$). On much larger scales, $>40'$, [Liseau et al. \(1995\)](#) derived a NW-SE radial velocity gradient of about $1\ km\ s^{-1}\ pc^{-1}$. For the limited extent of the region studied here, this has only a negligible effect on the line transfer.

4.2. Dust temperature, opacity, and mass

4.2.1. Point-source fitting of the spectral energy distribution (SED)

The fluxes of several point sources in the field were extracted and corrected for the underlying cloud emission. Their SEDs were determined assuming modified blackbody emission, where the adjustable parameter β is the power-law exponent of the frequency dependence of the flux in the Rayleigh-Jeans regime (see Appendix A). The fitting results are presented in Table 3 and shown in Fig. 7. These suggest a temporal evolution of the parameter β , in the sense that the FIR/submm SEDs become

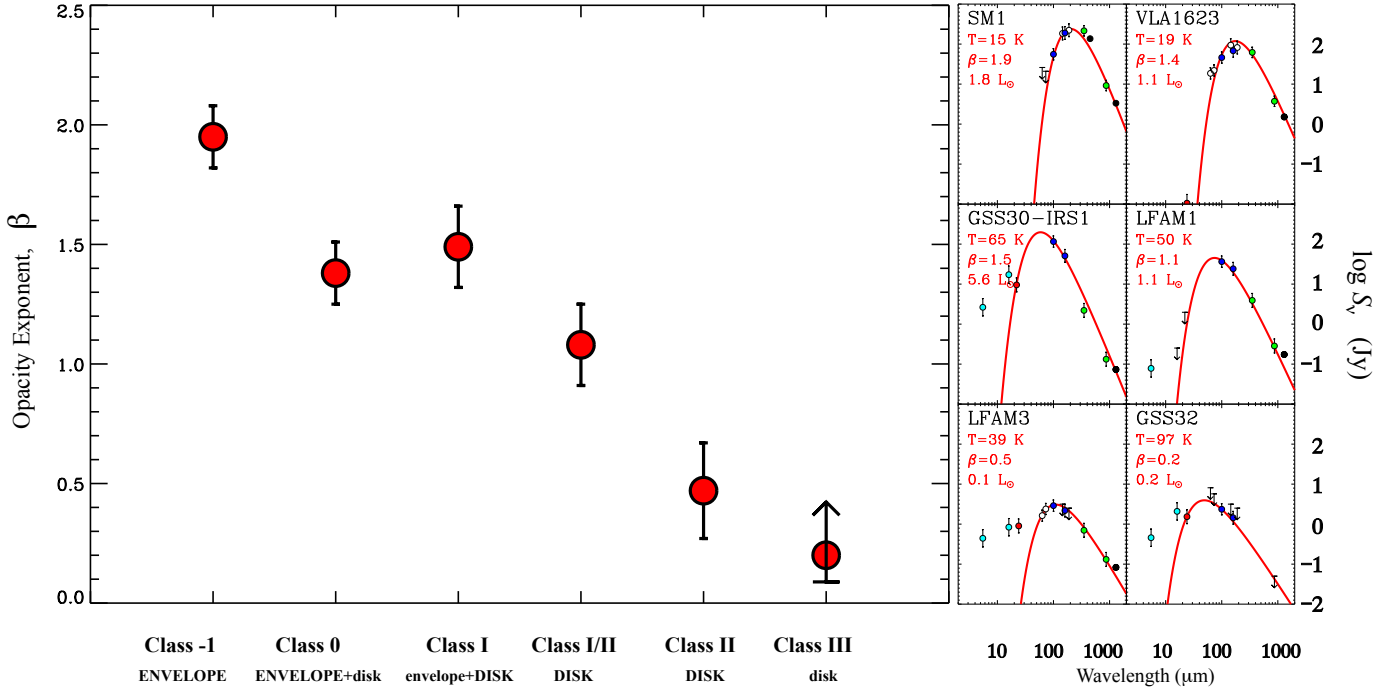


Fig. 7. *Left:* time evolution of the opacity exponent β , where $\kappa_r \propto \gamma^\beta$, and the values are derived from the fits to the adjacent SEDs. *Right:* SEDs of the point sources SM 1, VLA 1623, GSS 30-IRS1, LFAM 1, LFAM 3 AND GSS 32, belonging to different evolutionary classes (see Fig. 2). The β -values decrease from 2 for the starless dense dust core SM 1 to 0.2 for the visible T Tauri star GSS 32. Colour coding of the symbols is light blue: ISO-CVF 5.5 μm and 16 μm . Red: WISE 22 μm or *Spitzer* 24 μm . Blue: *Herschel*-PACS 100 μm and 160 μm . White: PACS-spectra at 63, 73, 145 and 189 μm . Green: APEX 350 and 870 μm . Black refers to literature data: [Wilson et al. \(1999, 450 \$\mu\text{m}\$ \)](#) and [Motte et al. \(1998, 1.3 mm\)](#).

Table 3. SED-fitting result for sources at different evolutionary stages.

Source	T_{dust} [K]	β	Type
SM1 ^a	15 \pm 1	1.95 \pm 0.13	Class -1
VLA1623	19 \pm 2	1.38 \pm 0.14	Class 0
GSS 30-IRS1	65 \pm 4	1.49 \pm 0.17	Class I
LFAM 1	51 \pm 6	1.08 \pm 0.17	Class I
LFAM 3	39 \pm 3	0.47 \pm 0.21	Class II
GSS 32	96 \pm 18	≥ 0.2	Class III

Notes. ^(a) [Ward-Thompson et al. \(1989\)](#) determined $T_{\text{dust}} = 15 \pm 5$ K and $\beta = 2.2 \pm 0.3$.

increasingly flatter with time. At early times, Class -1 and Class 0, the FIR/submm emission is entirely dominated by the envelope, whereas at the later stages, the envelope emission has essentially vanished and is dominated by the disk or the remnants of it (Class III). A mixture of these two dust-emission components is exhibited by the objects in between (Class I and II). The value of β is presumably dominated by the size distribution of the dust grains (e.g., [Miyake & Nakagawa 1993](#); [Kruegel & Siebenmorgen 1994](#)).

To examine the β -dependence on the size a of (spherical) grains, we performed Mie-calculations ([Min et al. 2003](#)) using laboratory measurements for a few typical grain materials (Fig. 8). This plot is qualitatively similar to Fig. 4 of [Testi et al. \(2014\)](#) for young disks, but here, β has been calculated for the wavelength region 200 μm to 1.3 mm instead, and it falls into the interval $0.0 \leq \beta \leq 2.5$. The power-law exponent p has been varied within the range $-5.0 \leq p \leq -2.0$, and where

$dn(a) \propto a^p da$. As expected, the β -dependence on chemical composition decreases with increasing p , that is, grain size, and these larger grains are found around the Class II and III objects, viz. LFAM 3 and GSS 32, respectively, with $a \geq 100$ μm . In contrast, the very small grains are found predominantly around the probably youngest object, that is, the starless clump SM 1 (Class -1). Around the Class 0 to I sources VLA 1623, GSS 30 IRS1 and LFAM 1, sizes would fall roughly within $0.1 \leq a \leq 10$ μm .

Therefore, the observed time dependence suggests that grain growth mainly occurs in the protoplanetary disks, with only little enrichment of large grains in the parental cloud. However, the precise dating of these events is difficult, but they probably fall within the range of some thousand years (starless cores, Class -1) to some megayears (near the ZAMS, Class III). If our observational results apply to currently adopted pre-main-sequence timescales (e.g., [Evans et al. 2009](#)), then $\beta(t)$ can be fit by a (broken) power law, $\beta \sim t^{-\gamma}$, where $\gamma (< 10^5 \text{ yr}) \sim 0.04$ and $\gamma (\geq 10^5 \text{ yr}) \sim 0.5$ to 0.6, respectively. If β scales inversely with grain size/mass, this may be consistent with stochastic processes in a turbulent medium (see also [Blum 2004](#)). Apparently, very little happens up to some 10^5 years. Thereafter, grain growth seems to occur at a faster rate.

Needless to say, it would be very valuable to extend this type of analysis to other star-forming regions, both for better statistics, but above all also for the comparison among different environments. β -evolution around young sources has recently been found elsewhere, but generally only for a single object at a time or, in one case, for two sources ([Testi et al. 2014](#), and references therein). However, the very compactness (0.05 pc $\sim 10^4$ AU) of an entire star-forming region in combination with the multitude of objects of different type as discussed here, makes the present study of ρ Oph A unique.

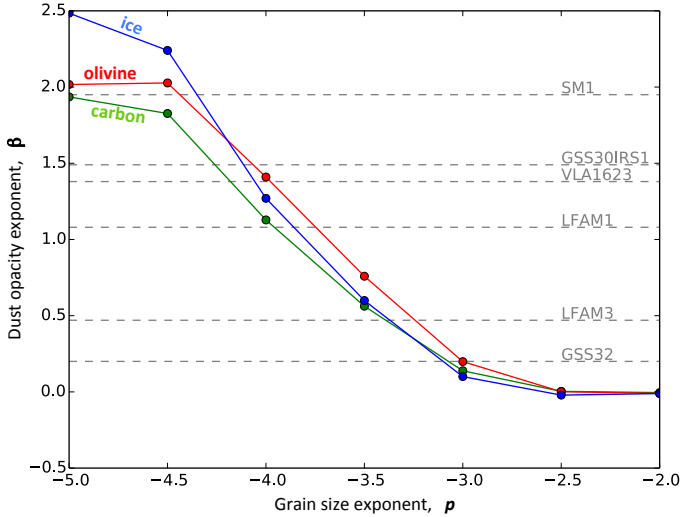


Fig. 8. Grain size exponent p , defined through $dn(a) \propto a^p da$ for spherical grains of size a , as a function of the grain opacity exponent β for the wavelength range $200 \mu\text{m}$ to 1.3 mm , and where $\kappa_\nu \propto \nu^\beta$. The curves for three different materials are shown, viz. for amorphous ice (H_2O , blue: Bertie et al. 1968), amorphous silicates (MgFeSiO_4 , red: Jaeger et al. 1994) and amorphous carbon (C, green: Blanco et al. 1991). The values of β determined from observations are shown as dashed lines, referring to the sources of Table 3 and identified to the right.

As for SM 1, these results refer to source scales of some 10^3 AU . On smaller scales, that is, a few 10^2 AU , SM 1 appears to have fragmented into smaller pieces (Nakamura et al. 2012). This may be expected on the basis of current theoretical models of star formation (Lomax et al. 2014, and references therein). However, using ALMA at higher resolution, Friesen et al. (2014) found no evidence for substructures down to scales of some 10 AU .

4.2.2. Extended dust emission

The methods for estimating dust emissions from point and extended sources differ only slightly (e.g., Andre et al. 1993), and in Appendix A, we present the analysis of our submm data assuming conventional methods, again for the purpose of comparison with other works. We did not, however, as is often done, assume a single dust temperature nor a single power law exponent β of the frequency dependence of the dust opacity, nor a single normalization value at some fiducial frequency. Instead, we intend to exploit observations at, at least, three frequencies to determine the spatial distribution of the dust temperature, the dust optical depth, and the absolute grain mass opacity. However, from the observed spectral index $\alpha = \Delta \log I_\nu / \Delta \log \nu$ for the wavebands $350 \mu\text{m}$ – $870 \mu\text{m}$ and $870 \mu\text{m}$ – 1.3 mm , respectively, it is apparent that the APEX data are internally consistent, but appeared incompatible with the IRAM data (Fig. 3). Whereas α generally is >2 for the Saboca-Laboca maps, as one would expect for thermal emission in the Rayleigh-Jeans (RJ) regime, the index is <2 everywhere for the Laboca-IRAM data. We have to conclude that the relative calibration of the LABOCA and SABOCA maps is good, but that the LABOCA and IRAM data suffer from inter-calibration uncertainties, and the latter were therefore not used in our analysis (see Appendix A).

With I_ν obtained from observation, the right-hand side of Eq. (A.2) contains two unknowns. For the interpretation of observations of molecular clouds, it has been common to assume ad hoc values for κ_ν and T_d . In addition, one also assumes that the

run of κ with ν is given by a power law, with an exponent β , that is, $\kappa_\nu \propto \nu^\beta$. For thermal emission in the RJ-regime, β would be related to the spectral index α , given by $\beta = \alpha - 2$, and for spherical Mie particles, β takes values between 0 and 2 (e.g., Emerson 1988), but values lower than 0 and greater than 2 are possible when the proper physics of non-perfect crystalline material are included (Meny et al. 2007). The use of the β -relation for mass estimates requires the normalization at some fiducial frequency (cf. Hildebrand 1983). In many cases, the normalization value of the opacity incorporates an assumed g_{2d} of 100 (Beckwith et al. 2000, and references therein).

The normalization is commonly taken from published works on dust opacity computations. However, by using these theoretical results directly, one circumvents the necessity of specifying β -values, which can change from one frequency band to another. Instead, one would wish to determine how these might vary spatially across a cloud, which might tell us something about the cloud dust properties. Potential problems include noise fluctuations and calibration uncertainties, and gradients in density and/or temperature along the line of sight (LOS) that may lead to non-convergence/inconsistent κ -values. Similar would apply to derived β -values, when one assumes that $\kappa(\nu)$ is given by a single power law of index β (e.g., Juvela et al. 2013). The accuracy of our results below is limited to twice the statistical error of the intensity I_ν at each frequency ν . However, the largest uncertainty comes from the absolute value of the opacity.

As an example, we chose the work by Ossenkopf & Henning (1994), which provides dust mass opacities for conditions thought to prevail in dense molecular clouds. Processes of coagulation are considered and the steady state is reached typically after some 10^5 years, which is most likely younger than the ages of molecular clouds. The initial state consists of bare grains, distributed in size as in the diffuse ISM (viz. “MRN-distribution”, Mathis et al. 1977)⁶. With time, these grains grow in size by acquiring ice mantles of various thickness and opacities, between the wavelengths of $1 \mu\text{m}$ and 1.3 mm , are provided for a range in environmental density, from $n(\text{H}) = 0$ to 10^8 cm^{-3} .

Shown below, in Sect. 4.2.4 (Fig. 16), are the results for fixing the opacity curve, that is, No. 22 in Table 4. The distribution of the dust temperature exhibits an average value of 19 K . Although temperatures are around 20 K in most parts of the map, regions with $T_d > 25 \text{ K}$ exist along a north-south ridge, in addition to a couple of localized shocked regions, near VLA 1623 and GSS 30 (cf. Fig. 1). The dust optical depth at $350 \mu\text{m}$, $\tau_{350 \mu\text{m}}$, is much lower than unity, justifying a posteriori the assumption of low optical depth. This is then of course also simultaneously justified for the LABOCA data ($\max \tau_{870 \mu\text{m}} = 0.005$).

A major drawback of the presented analysis is that it ignores the details of the processes that are heating the observed dust. In other words, the energy balance equation is not solved, which neglects the existence of gradients in density and radiation field strength, and hence temperature, in the source. These shortcomings are considered in the physical models described below, which are two 3D radiative transfer models that follow two different approaches. Regarding spatial coverage, these models are complementary, meaning that model I provides a larger, global view and model II focuses on the central regions of ρ Oph A.

⁶ Comparing mass absorption coefficients for MRN dust of Draine (2003) with those of Ossenkopf & Henning (1994) indicates some differences: Draine (2003) lists values of $\kappa_{350 \mu\text{m}} = 1.92 \text{ cm}^2 \text{ g}^{-1}$ and $\kappa_{850 \mu\text{m}} = 0.383 \text{ cm}^2 \text{ g}^{-1}$. The corresponding data by Ossenkopf & Henning (1994) are $\geq 3.64 \text{ cm}^2 \text{ g}^{-1}$ and $\geq 0.70 \text{ cm}^2 \text{ g}^{-1}$, respectively.

Table 4. Dust masses for opacities from Ossenkopf & Henning (1994).

κ curve	Ice coating	$n(\text{H})$ (cm^{-3})	β_{theo} 350–870 μm	Average T_{d} (K)	$100 M_{\text{d}}$ (M_{\odot})
1	no ice	0	1.84	21.06	15.92
2		10^5	1.50	45.88	3.28
3		10^6	1.28	81.44	0.81
4		10^7	1.12	107.06	0.23
5		10^8	1.05	112.52	0.14
6	thin	0	1.89	19.38	10.54
7		10^5	1.86	20.16	7.42
8		10^6	1.86	20.10	5.79
9		10^7	1.86	20.00	4.97
19		10^8	1.86	20.24	4.66
20	thick	0	1.89	20.36	7.69
21		10^5	1.89	19.36	6.17
22		10^6	1.89	19.43	5.52
23		10^7	1.89	19.44	5.41
24		10^8	1.92	18.91	5.61

Table 5. Stellar parameters used in model I.

Parameter	S 1	HD 147889
M (M_{\odot})	6	12
R (R_{\odot})	3	7
T_{eff} (K)	17 000	22 000
$\log g$ (in dyn cm^{-2})	4.0	4.0
v_{turb} (km s^{-1})	2.0	2.0

4.2.3. 3D dust modelling: Model I

Model I uses the code RADMC-3D⁷ developed by Dullemond and benchmarked by Pinte et al. (2009). The model consists of a low-density widespread cloud medium, the high-density core ρ Oph A with the dust clump SM 1, the two point sources VLA 1623 and GSS 30, and the two early-type stars S 1 (B 4) and HD 147889 (B 2.5), each with its own PDR bubble. These are the main energy sources in the model, providing the heating of the dust. The stellar SEDs are based on Kurucz ATLAS 9 model atmospheres with the parameters of Table 5.

In detail, the model assumes a high-density core of radius 0.045 pc that is embedded in a low-density cloud. The early-type stars S 1 and HD 147889 generate two PDRs, viz. west and east of the dense core, with respective radii of 0.06 pc and 0.5 pc. The bright B2 star HD 147889 is situated more than half a parsec away to the southwest and behind the cloud (Liseau et al. 1999). Together, these stellar radiation sources are heating the dust of ρ Oph A from the outside. By comparison, internal heating sources are essentially negligible.

The exploited grain opacities are shown in Fig. 9, and in ρ Oph A, individual sources contribute to the total modelled dust mass of $10.4 \times 10^{-2} M_{\odot}$ as follows: the core with 7, SM 1 with 1.7, VLA 1623 with 0.9, and GSS 30 with 0.8 in units of $10^{-2} M_{\odot}$. A match to the PDR around HD 147889 assumes $0.04 M_{\odot}$ of dust (see Fig. 10). Based on C^{18}O and other molecules (Paper II, in prep.), the density profile is given by $\rho \propto r^{-1.5}$ for ρ Oph A globally and by $\rho \propto r^{-2}$ for SM 1 locally.

⁷ <http://www.ita.uni-heidelberg.de/dullemond/software/radmc-3d/>

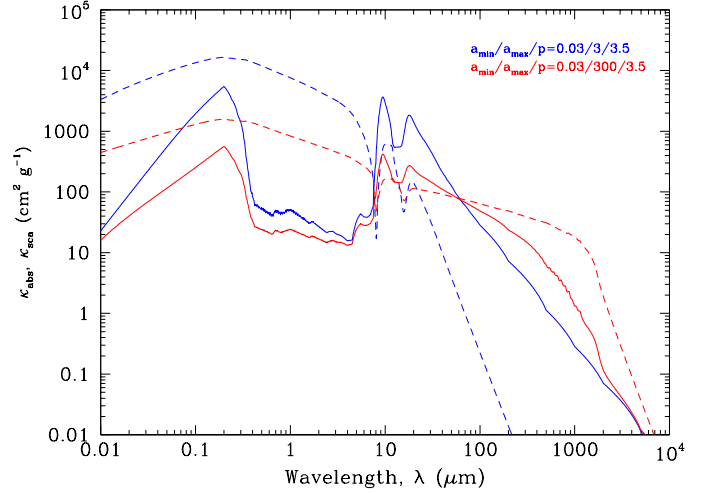


Fig. 9. Extinction curves used for Model I, where the mass extinction coefficient is given by $\kappa_{\text{ext}}(\lambda) = \kappa_{\text{abs}}(\lambda) + \kappa_{\text{sca}}(\lambda)$. Solid lines are for mass absorption coefficients κ_{abs} and dashes are for the scattering, κ_{sca} . The curves are based on the optical constants provided by Jaeger et al. (1994) and by Dorschner et al. (1995) for two grain populations. The adopted grain size distributions have an exponent $p = 3.5$, and minimal sizes are $a_{\text{min}} = 0.03 \mu\text{m}$ for both. The largest sizes are $a_{\text{max}} = 3 \mu\text{m}$ (blue) and $a_{\text{max}} = 300 \mu\text{m}$ (red).

In the model, the stellar object S 1 (Chini 1981, B5)⁸ is situated off-centre in a low-density bubble of radius 0.06 pc that is filled with $7 \times 10^{-4} M_{\odot}$ of $0.1 \mu\text{m}$ sized carbon particles⁹ (Dorschner et al. 1995). These small particles scatter the short-wavelength radiation extremely well, and this is needed to account for the observed intensity distribution in the near- and mid-IR. However, some finite, non-zero filling of the bubble is also required for numerical reasons. For an assumed $q2d = 100$, the total mass from model I of the entire ρ Oph A core is $23.7 M_{\odot}$ (Fig. 11).

As already mentioned, we used RADMC-3D to solve for the temperature distribution, which is shown along two different cuts on the right-hand side of Fig. 10. Obviously, the grain temperature also depends on its size, and the distributions for the three groups of grains are shown individually. For μm - and mm -size grains, temperatures of the dust amount to 10–30 K near the dense core SM 1. These model results can be used to generate synthetic images of ρ Oph A. These are shown in Fig. 12, together with the observations at six wavelengths, from the mid-infrared to the submm. Evidently, model I reproduces the observed intensity distributions very well, in particular the large-scale features.

4.2.4. 3D dust modelling: Model II

Thermal equilibrium models

The modelling follows the procedure outlined by Juvela et al. (2011), which starts by deducing the $350 \mu\text{m}$ optical

⁸ This is a binary (B4+K, Gagné et al. 2004). The magnetic B star (Andre et al. 1991) is also a bright source of X-ray emission (Hamaguchi et al. 2003; Gagné et al. 2004).

⁹ For $M/L = 4.6 \times 10^{-3}$ of an equivalent single star, the blow-out grain size is larger than $50 \mu\text{m}$, and radiation pressure would empty the 12 000 AU region of carbonaceous particles of size $0.1 \mu\text{m}$ within 3500 years. The likely existence of an intense stellar wind, exerting additional outward momentum, would shorten this timescale even further.

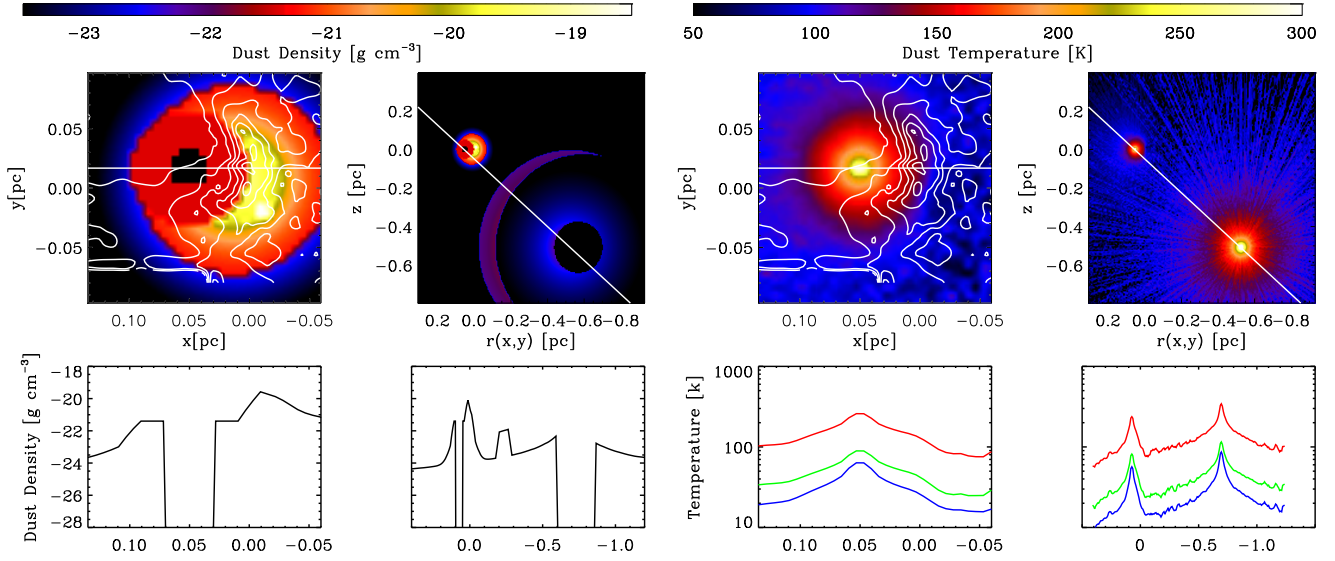


Fig. 10. Left panels: density distribution of model I. With the logarithmic colour bars on top, a 2D distribution is shown to the left that lies in a plane containing the star S 1 and the centre of the main core SM 1, and to the right the entire model, also containing HD 147889. The panels below show the cuts along the straight white lines. White contours refer to the C^{18}O (3–2) measurements by Liseau et al. (2010). Right panel: resulting temperature distribution of model I, with similar format as for the density distribution. The different colours in the frames below refer to the temperatures of the various dust constituents. Red: Very small grains (VSGs) and polycyclic aromatic hydrocarbons (PAHs). Green: grains with sizes between $0.03\text{--}3\ \mu\text{m}$. Blue: grains whose sizes extend up to $300\ \mu\text{m}$.

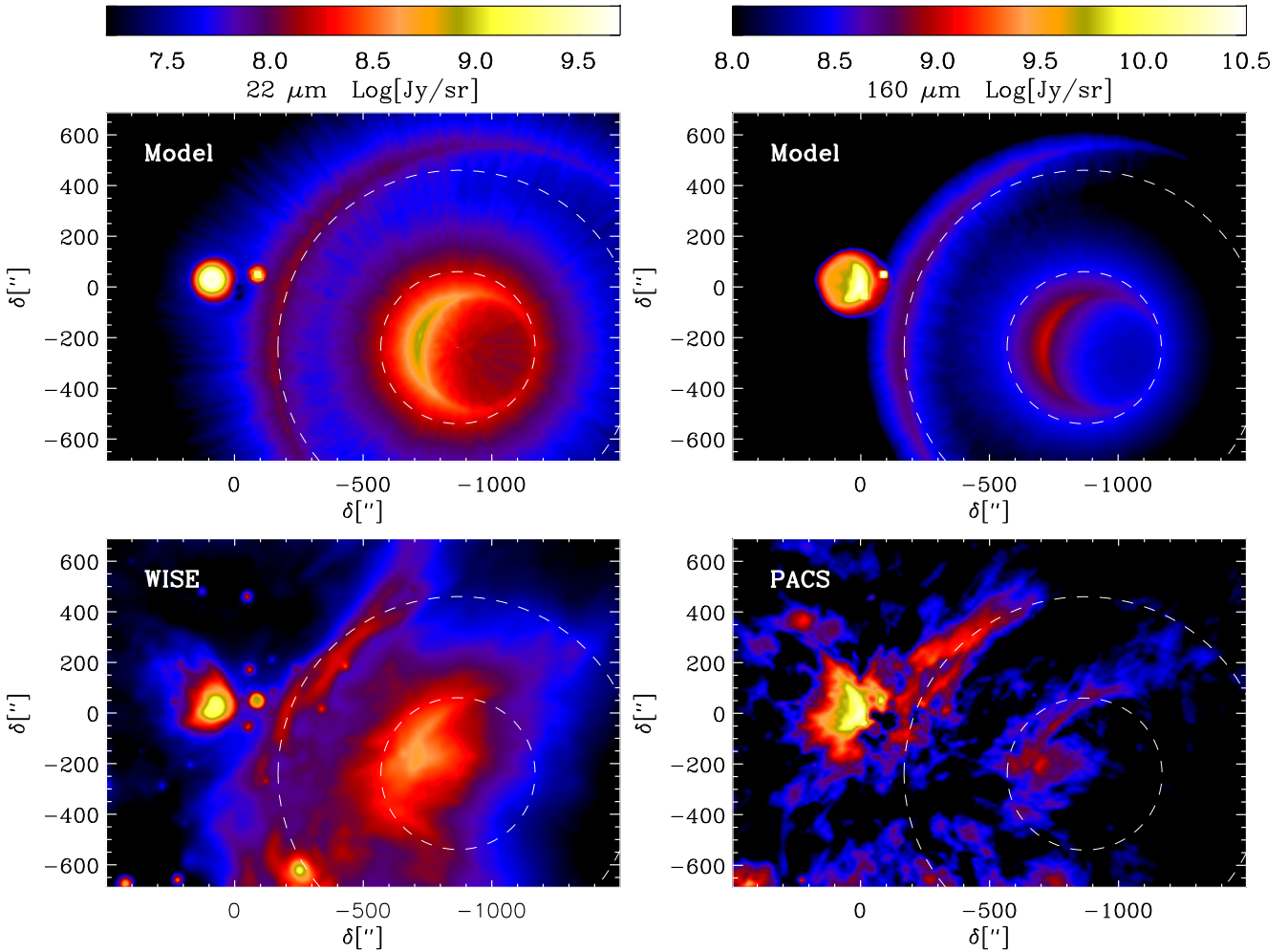


Fig. 11. Images of the full 3D dust model I at $22\ \mu\text{m}$ and $160\ \mu\text{m}$ for the entire ρ Oph A core. Upper panel: synthetic images at $22\ \mu\text{m}$ and $160\ \mu\text{m}$. Lower panel: observations with WISE ($22\ \mu\text{m}$, left) and PACS ($160\ \mu\text{m}$, right).

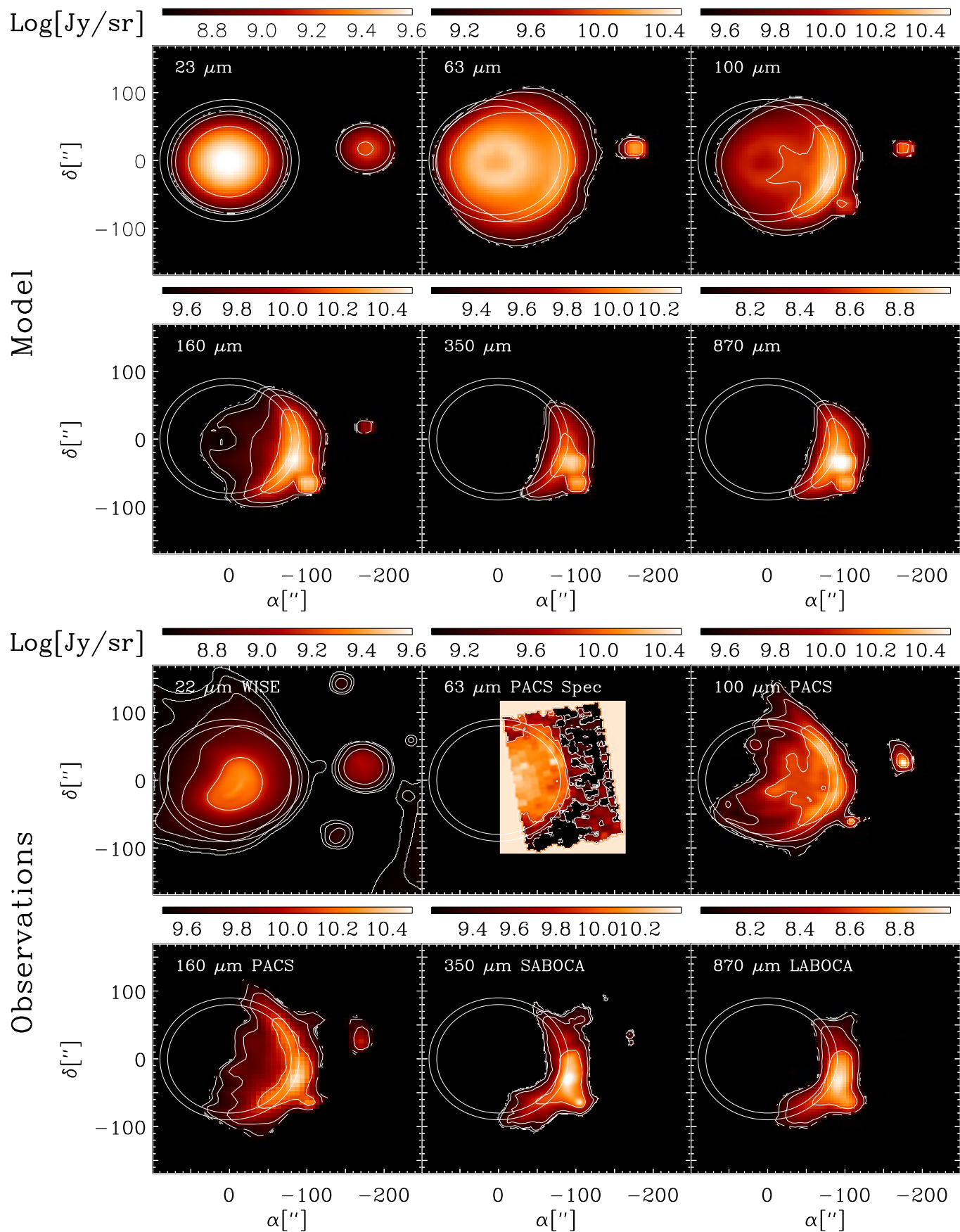


Fig. 12. *Top panels:* synthetic images of ρ Oph A that were generated from the results of model I. Continuum wavelengths are 22, 63, 100, 160, 350, and 870 μm . The logarithmic scales are in units of Jy sr^{-1} and given along the colour bars atop each frame. *Bottom panels:* displayed observations taken from WISE (22 μm), *Herschel*-PACS (63, 100 and 160 μm), and APEX (350 and 870 μm).

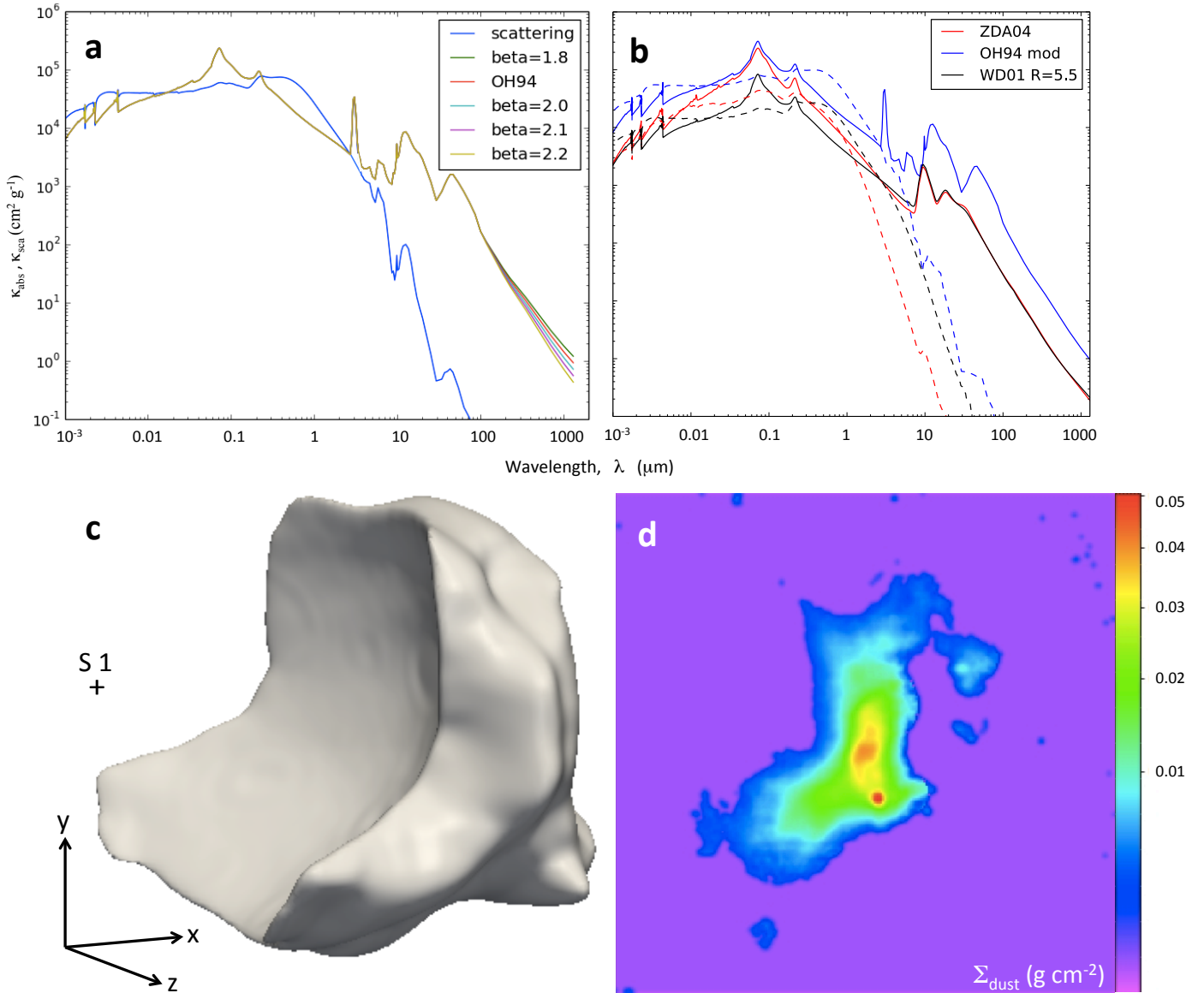


Fig. 13. **a)** Modification of the extinction curves of Ossenkopf & Henning (1994, OH94) for various grain sizes and β -values (see the text). The extinction coefficients K_{abs} and K_{scat} of model Milky Way A for $R_V = 5.5$ of Weingartner & Draine (2001) match at $1 \mu\text{m}$. **b)** The extinction curves of Zubko et al. (2004, ZDA04 in red) and Weingartner & Draine (2001, WD01 in black). The modified curve of Ossenkopf & Henning (1994) is shown in blue (OH94 mod). Solid lines depict mass absorption, dashed lines scattering. **c)** Structure of model II, where the isodensity surface corresponds to 20 percent of the highest density. The surface encloses approximately 30 percent of the total mass of the core. The LOS is along the negative z -axis, i.e. the axis pointing towards the observer. In the sky, right ascension is along the negative x -axis and declination along the positive y -axis. The dominating heating source S 1 is situated near the focus of the paraboloid low-density region. **d)** The surface density distribution of the dust, Σ_{dust} in g cm^{-2} , for model II.3, i.e. for the extinction curve (Weingartner & Draine 2001, $R_V = 5.5$ with PAHs).

depth distribution for a fixed $\beta = 2$ from the observed APEX ($350 \mu\text{m}$ and $870 \mu\text{m}$) maps. The optical depth map is used to set the column density distribution of the model. However, the LOS density distribution is not directly constrained by the observations. We assumed a Gaussian distribution with a FWHM of 0.05 pc towards the densest part of the core, increasing up to 0.07 pc towards the low-density regions. With these values the LOS extent of the core is similar to its plane-of-sky dimensions. The resulting 3D density distribution was further modified to include a cavity around the S 1 star. The cavity was modelled as a paraboloid with the star S 1 at the focus. Inside the cavity the density was set to 10^{-5} times the highest density of the model core. The models represent a box with a size of 0.225 pc at a distance of 120 pc and use 256^3 cells, yielding a resolution of

approximately 180 AU , or $1''.5$. The three-dimensional density distribution and the plane-of-sky surface density distribution are illustrated in the bottom left and right panels of Fig. 13, respectively.

The model was embedded in an interstellar radiation field with intensity three times that of the solar neighbourhood. However, irradiation of the core was dominated by the individual stars, mainly S 1 and HD 147889. The stellar object S 1 was modelled as a 16000 K , $L = 1100 L_{\odot}$ blackbody, while HD 147889 was given a temperature of 20000 K and luminosity $L = 4500 L_{\odot}$. Because HD 147889 is more than 0.5 pc away from the dense parts of the core compared to less than 0.1 pc for S 1, the latter is the main heating source in most parts of the model core. In addition, the model included two deeply

embedded stellar objects with luminosities of approximately $2 L_{\odot}$, but these do not have any significant effect on the radiation field except in their immediate surroundings. The radiative transfer calculations were made using the CRT program (Lunntila & Juvela 2012). The program calculates the dust temperature taking into account the dust self-absorption and heating, and integrates along the LOS to produce maps of dust FIR emission. For comparison with observations, the synthetic maps were convolved with Gaussian kernels corresponding to the APEX beam sizes.

We have calculated grids of models with varying dust properties and density scaling, but keeping the same radiation sources and the three-dimensional density distribution. In model II.1 we adopted the mass extinction from curve No. 22 in Table 4, taken from Ossenkopf & Henning (1994); however, the opacities are given only for wavelengths $\lambda \geq 1.0 \mu\text{m}$ and no information is given about scattering properties. Therefore, for the shorter wavelength extinction, the model *Milky Way A* for $R_V = 5.5$ of Weingartner & Draine (2001) was used, matched to the former at the wavelength of $1.0 \mu\text{m}$. The scattering properties were obtained by assuming the same albedo and scattering asymmetry parameter as in the Weingartner & Draine (2001) $R_V = 5.5$ model. To study the effect of β , in addition to the unmodified $\beta \approx 1.9$ dust, we used models where the extinction curve at wavelengths $\lambda \geq 100 \mu\text{m}$ was modified by multiplying the Ossenkopf & Henning (1994) absorption cross-sections by $(\lambda/100 \mu\text{m})^a$ with $a = -0.1, 0.1, 0.2,$ and 0.3 , corresponding approximately to $\beta = 1.8, 2.0, 2.1,$ and 2.2 . The extinction curves are shown in Figs. 13a and b. The peak dust surface density was varied in eight steps between $0.00501 \text{ g cm}^{-2}$ and 0.0130 g cm^{-2} .

In model II.1, the best fit was obtained with $\beta = 2.0$ and a peak dust surface density $\Sigma_{\text{dust}} = 0.010 \text{ g cm}^{-2}$. Dust models with lower β predict a too high $870 \mu\text{m}$ to $350 \mu\text{m}$ brightness ratio. Assuming a gas-to-dust mass ratio of 100, the mass of the main part of the core (defined as having at least 5% of the peak surface density and corresponding roughly to the extent that was used for the 1D analysis in Sect. 4.2.2) is $7.3 M_{\odot}$. The mass included in the whole simulated region is approximately 20 percent higher. Although the best models fit the observed $350 \mu\text{m}$ and $870 \mu\text{m}$ intensity within approximately 20 percent, none of the models is successful in reproducing the $100 \mu\text{m}$ and $160 \mu\text{m}$ *Herschel*-PACS observations. The calculated surface brightness is at least a factor of two higher than observed. In particular, it is difficult to simultaneously produce the relatively high brightness at $350 \mu\text{m}$ and the low observed intensity in the PACS bands. Figure 14 shows the comparison between the simulated maps from the best-fit model II.1 and the *Herschel*-PACS $100 \mu\text{m}$ and $160 \mu\text{m}$, and the SABOCA $350 \mu\text{m}$, and LABOCA $870 \mu\text{m}$ maps. To study the effects of numerical resolution on the results, we increased the resolution by a factor of four, that is, to a cell size of $0.0002 \text{ pc} = 45 \text{ AU}$. The differences between lower and higher resolution were lower than 10% everywhere and lower than 2% where the processes were active. In the following, we therefore ran the models with the lower resolution to keep the computations tractable.

In model II.2 we have chosen BARE-GR-S of Zubko et al. (2004, Table 7) as our basic dust opacities¹⁰. As with model II.1, we ran simulations with modified dust models with different values of β . The modifications of the extinction law were similar to model II.1, except that the changes were applied at wavelengths $\lambda > 20 \mu\text{m}$. In addition to the standard $\beta \approx 2.0$ model

we used $\beta = 1.5, 1.8, 2.1,$ and 2.2 . The density scaling was varied with nine steps corresponding to peak dust surface densities (at $1''5$ scale) between 0.0197 g cm^{-2} and 0.0985 g cm^{-2} . As the Zubko et al. (2004) dust models have much lower sub-mm opacities than the dust used in model II.1, in both cases the models span a similar range of $350 \mu\text{m}$ optical depths. The best-fit II.2 model has a peak dust surface density $\Sigma_{\text{dust}} = 0.0498 \text{ g cm}^{-2}$ and $\beta = 2.1$. Modified dust with a steeper sub-mm extinction law matches the $870 \mu\text{m}$ to $350 \mu\text{m}$ brightness ratio better than the original dust model in this case as well. Using the same A_V -to-gas mass ratio as in the BARE-GR-S model of Zubko et al. (2004) for our modified $\beta = 2.1$ dust, the total mass of the best-fit model is $59.1 M_{\odot}$, where a $g2d = 161$ has been assumed.

In all models, the amount of dust in the cavity is very low, resulting in a visual extinction between the exciting source S 1 and the inner edge of the cavity of $A_V = 3 \times 10^{-3} \text{ mag}$. The extinction toward the observer is less well constrained, but model II.2 gives $A_V \lesssim 15 \text{ mag}$, with similar values for the others. This value compares very well with the $A_V = 12.5 \text{ mag}$ determined by Ward-Thompson et al. (1989) from the H_2O -ice absorption feature at $3.1 \mu\text{m}$, and the range $A_V = 11$ to 13 mag , for $R_V = 5.5$, based on the X-ray analysis by Vuong et al. (2003).

Non-equilibrium models

Models II.1 and II.2 assume that the dust grains are in thermal equilibrium with the local radiation field. However, absorption of a single high-energy photon can heat a very small dust grain to a high temperature. Absorbed energy is therefore reradiated more in the infrared than in the sub-mm (see, e.g., Draine 2003). To examine whether an accurate calculation of the emission from very small grains changes the results, model II.3 uses the dust model *Milky Way A* for $R_V = 5.5$ of Weingartner & Draine (2001) but does not assume thermal equilibrium. Because these calculations are much more time-consuming, only three different density scalings were used with this dust model. At wavelengths $\lambda > 200 \mu\text{m}$ the calculated emission from the best-fit model is almost identical to the best-fit model II.2. At $100 \mu\text{m}$ and $160 \mu\text{m}$, model II.3 produces slightly lower fluxes as shown in Fig. 15, but the discrepancy between the model and *Herschel*-PACS observations remains large. The best-fit model has a peak dust surface density of $\Sigma_{\text{dust}} = 0.0491 \text{ g cm}^{-2}$ and, using a gas-to-dust mass ratio of 105.1, a mass of $38.0 M_{\odot}$.

The LOS mass-averaged dust temperature, T_{dust} , and the $350 \mu\text{m}$ optical depth, $\tau_{350 \mu\text{m}}$, from the best-fit 1D model (see Sect. 4.2.2) and the three 3D models II.1, II.2, and II.3 are shown in Fig. 16. The results from all three 3D models are similar. Their LOS optical depths agree within 20 percent and the calculated dust temperatures only differ by approximately 1 to 2 K. The large differences in calculated masses are caused mostly by the widely varying sub-mm opacities and, to a smaller degree, by the gas-to-dust mass ratios of the dust models. The LOS average temperature through the dense core is between 18 and 20 K, but along the borders of the low-density cavity around the S 1 star the temperature rises to 25–30 K. Results from the 1D model show much larger variations in temperature, although the average value is similar. The $350 \mu\text{m}$ optical depths from the 1D analysis are approximately 30% lower.

4.3. The $g2d$ in ρ Oph A

Table 6 compares the results of different approaches to the dust modelling. Derived absolute masses can vary quite substantially,

¹⁰ These opacities do not require any ad hoc adjustments of the silicon or other abundances (see the discussion by Draine 2009).

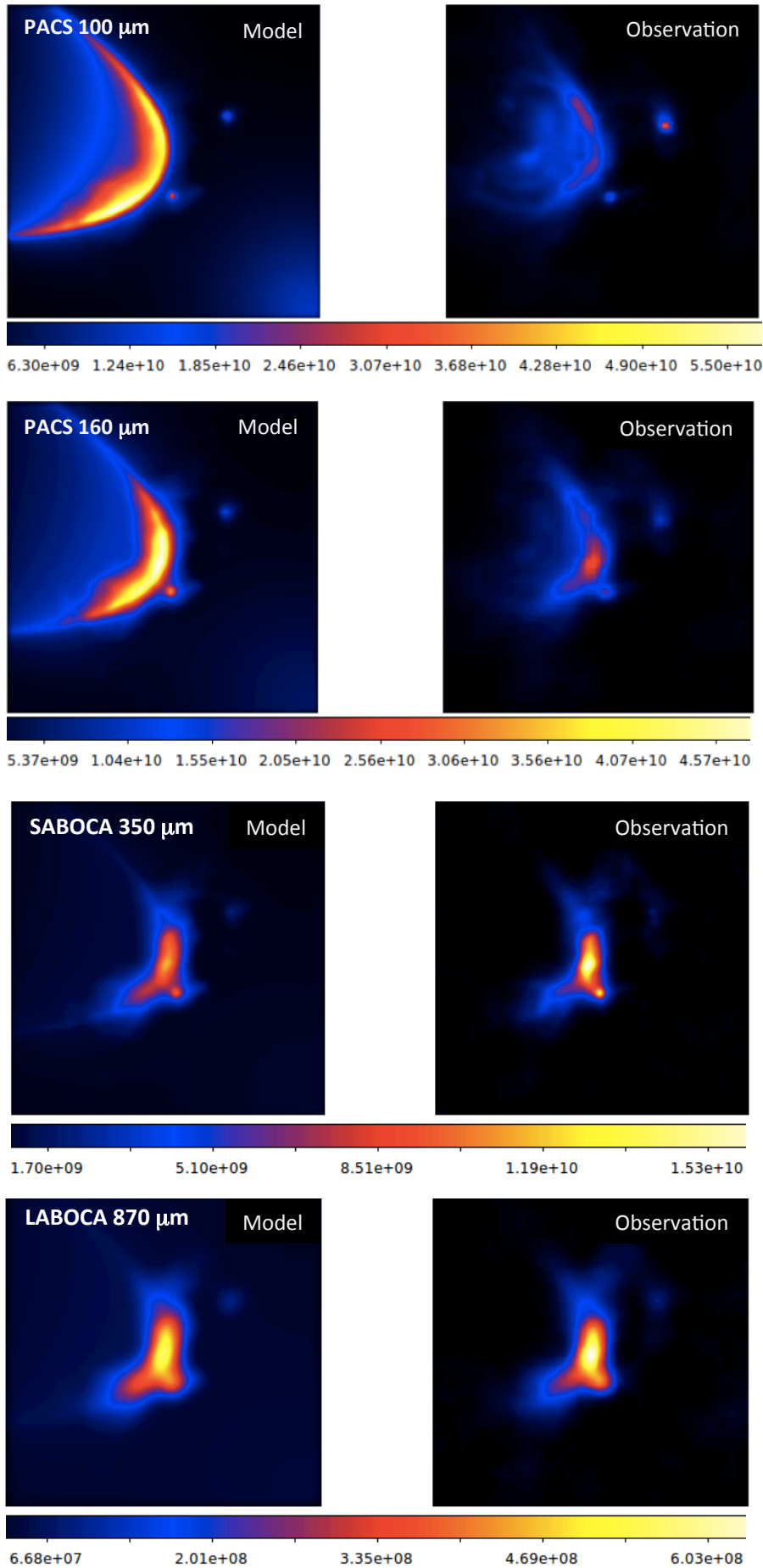


Fig. 14. Results from model II.1, comparing modelling results (*left*) with the observations (*right*). From top to bottom PACS 100 μm , PACS 160 μm , SABOCA 350 μm , and LABOCA 870 μm , where intensity units are Jy sr^{-1} . Including the PAH opacities did not improve the models at the FIR wavelengths, where the models over-predict the intensities observed by *Herschel*. In contrast, the agreement between models and APEX observations in the submm is very satisfactory, within better than 20%.

Table 6. Assumed submm/mm dust opacities, normalized to $g2d = 100$.

Opacity reference	$\kappa_{350\mu\text{m}}$ ($\text{cm}^2 \text{g}^{-1}$)	$\kappa_{870\mu\text{m}}$ ($\text{cm}^2 \text{g}^{-1}$)	$\kappa_{1.3\text{mm}}$ ($\text{cm}^2 \text{g}^{-1}$)	M^a (M_\odot)	$(\kappa M)/(\kappa_0 M_0)$ 350, 870, 1300 μm	Note
1D-models						
This work (M_0, κ_0)	11.78	2.148	0.9621	5.5	1.0, 1.0, 1.0	$T = 10\text{--}50 \text{ K}$, OH No. 22, $\beta = 1.89$
Johnstone et al. (2000)	...	1.0 ^{a,b}	...	8.1 (5.2)	0.7 (0.4)	$T = \text{const.} = 20 \text{ K}$ ($T = 13\text{--}42 \text{ K}$)
André et al. (2007)	0.5 ^a	7.5	0.5	$T = \text{const.} = 12 \text{ or } =20 \text{ K}$
3D-models						
Model I ^c	2.87	0.406	0.1846	10.4	0.5, 0.4, 0.4	MgFeSi grains for $a_{\text{max}} = 3 \mu\text{m}$
Model II.1 ^d	11.17	1.825	0.8206	7.3	1.3, 1.1, 1.1	Modified OH No. 22, i.e., $\beta = 1.99$
Model II.2 ^e	2.05	0.376	0.1886	36.7	1.2, 1.2, 1.3	Mass for $g2d = 100$
Model II.3 ^f	2.00	0.393	0.2073	36.2	1.1, 1.2, 1.4	$R_V = 5.5$ and PAHs

Notes. ^(a) For the ρ Oph A core with assumed gas-to-dust mass ratio of $g2d = 100$. ^(b) Refers to $850 \mu\text{m}$. ^(c) Opacities from Jaeger et al. (1994), Dorschner et al. (1995). ^(d) Modified Curve No. 22 of Ossenkopf & Henning (1994) using submm- $\beta = 1.99$, but normalized at $100 \mu\text{m}$, i.e. $\beta_{350\text{--}100\mu\text{m}} = 2.18$. ^(e) $M = 59.1 M_\odot$: unmodified BARE-GR-S assumes $g2d = 161$ (Zubko et al. 2004). ^(f) $M = 38.0 M_\odot$: $R_V = 5.5$ curve of Weingartner & Draine (2001) that includes PAHs assumes $g2d = 105.1$.

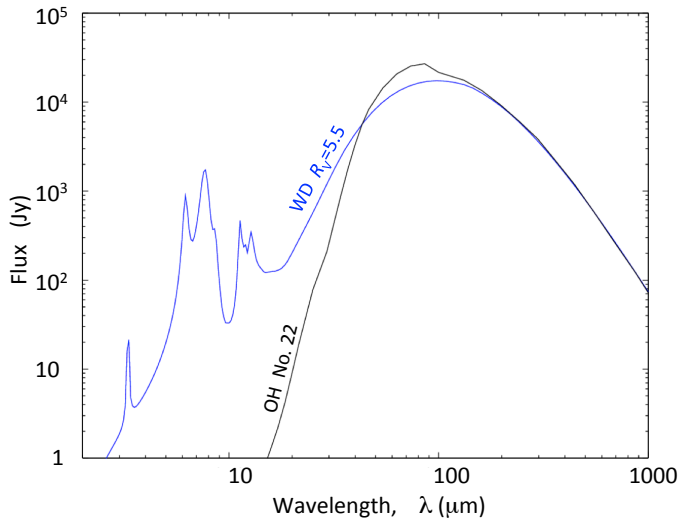


Fig. 15. SEDs of ρ Oph A. For models II.1 (black) and II.3 (blue), the emerging specific intensity has been integrated over the core ρ Oph A that is displayed in Fig. 13d. The thermal equilibrium model II.1 uses the extinction curve as modified by Ossenkopf & Henning (1994). The non-equilibrium model II.3 uses that of Weingartner & Draine (2001) for $R_V = 5.5$, which includes the PAHs, and where by comparison, the 100 and $160 \mu\text{m}$ fluxes are reduced.

from 5 to $40 M_\odot$. However, opacity-weighted, normalized masses agree to within 10% of each other, with an average value of 1.1 over an interval of 0.4 to 1.4.

To determine the absolute gas-to-dust mass ratio, $g2d$, is therefore not a trivial task. For example, if we choose the result of the non-equilibrium model 2.III, the map average is only slightly sub-canonical, $g2d = 88$ (Fig. 17). This value would directly agree with that derived from X-ray work by Vuong et al. (2003), who found $g2d = 95 - 80$ within the range $R_V = 4\text{--}6$ ¹¹.

However, on scales of the individual sub-regions, this number would not be truly representative: over tens of seconds of arc, $g2d$ takes median values of 145^{+144}_{-105} around N 2 in the north,

¹¹ Other parameters include the metallicity $Z/Z_\odot = 0.9\text{--}1.0$ and the minimum grain size $a_{\text{min}} = 0.025\text{--}0.07 \mu\text{m}$.

of 14^{+28}_{-10} in the central regions of SM 1, and of 104^{+97}_{-43} in the southeast, near N 6. Taken literally, local $g2d$ values in ρ Oph A imply fractions of the dust mass from lower than 0.5% to more than 10%. In particular, the deviating, low values around the core SM 1 were already remarked upon by Bergman et al. (2011).

To bring the central $g2d$ into line with the widely accepted value of 100 would require the downward adjustment of the derived gas mass by a factor of ten. This is not a realistic option on the basis of the ALI modelling, however, and must be discarded. Similarly, reducing the dust mass by an order of magnitude would result in $g2d$ of several thousand in the north and southeast, an option that is not convincing either. On the other hand, an uneven projected distribution of gas and dust may be a solution. In Fig. 18, maps of gas and dust at $7''$ resolution are displayed, from which it becomes apparent that the continuum radiation peaks at positions offset from those of the gas. A low $g2d$ would naturally result.

4.4. Distribution of gas and dust in ρ Oph A

The $\text{C}^{18}\text{O}(3\text{--}2)$ line and the LABOCA continuum band are close in frequency, at about $850 \mu\text{m}$ wavelength, and the maps of both have been observed with the same telescope (APEX), meaning that these data share the same angular resolution of $\sim 20''$. Our SABOCA continuum map at $350 \mu\text{m}$ has also been obtained with APEX, albeit at the higher resolution of $7''$. Both APEX continuum maps share the same offset centre and internally agree excellently well (Sect. 4.2). The nominal offset of the $\text{C}^{18}\text{O}(3\text{--}2)$ map (Liseau et al. 2010) is at $(-45''.1, +3''.0)$, which was applied to the line data to align with the continuum maps. As already mentioned, the pointing accuracy of the APEX telescope is $2''$ rms.

We applied the program IMAGINE, which is based on an in-house developed algorithm (Rydbbeck 2008), to the spatially oversampled $\text{C}^{18}\text{O}(3\text{--}2)$ data. The number of noise channels in the line spectra, in each positional pixel, is large, which allows an accurate description of the statistics of the noise distribution. In addition, the spectra have a high signal-to-noise ratio. These properties of the data are used by IMAGINE to deconvolve high-quality data, increasing the resolution by up to a factor of three. The deconvolved $\text{C}^{18}\text{O}(3\text{--}2)$ map of the integrated

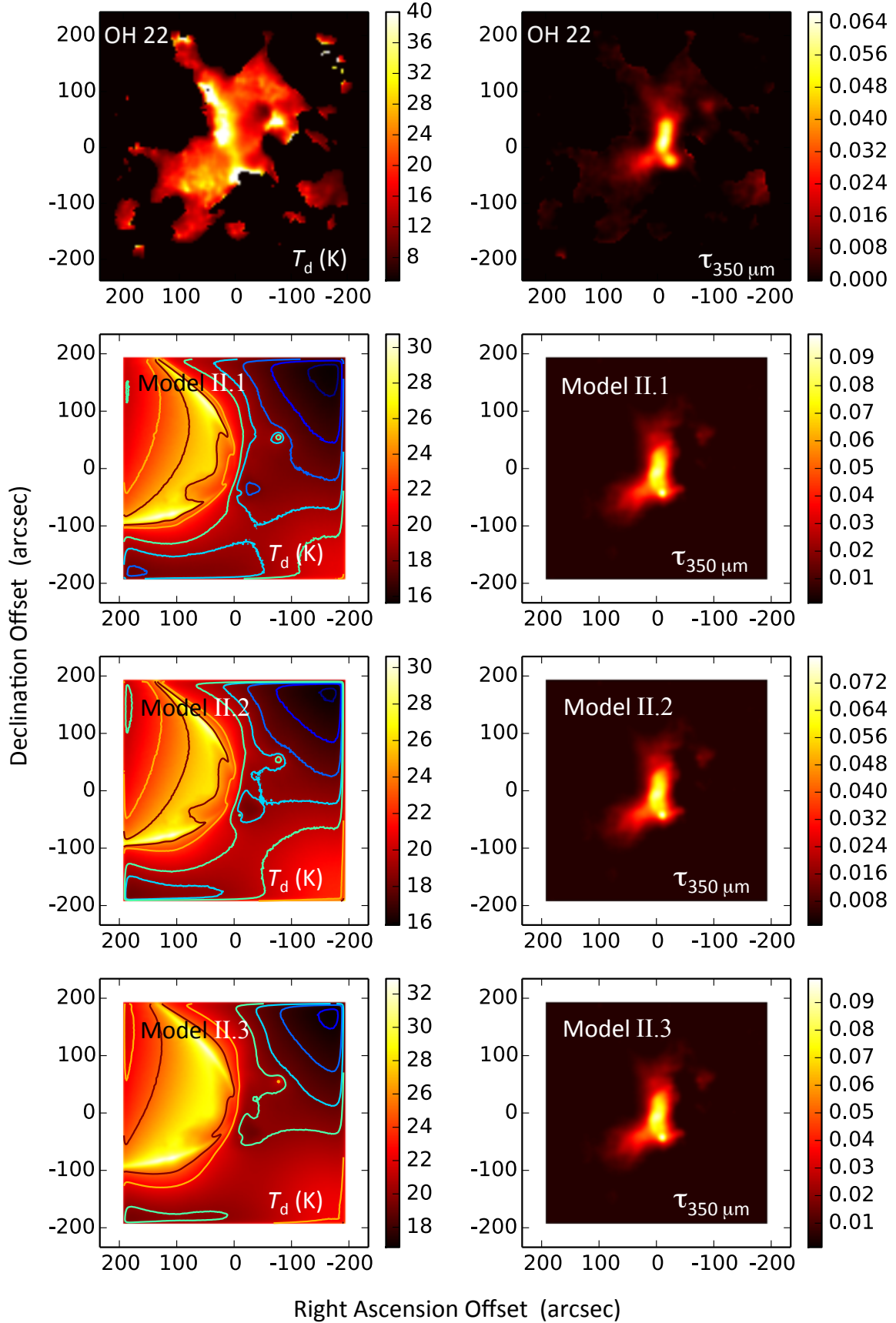


Fig. 16. Distributions of dust temperature (*left*) and 350 μm optical depth (*right*). *Top*: 1D model using opacity curve No. 22 of Ossenkopf & Henning (1994, Table B.1), where $\beta = 1.89$. *Second from above*: 3D model (cf. Fig. 13) accounting for gradients in the core and using a slightly modified curve No. 22 with $\beta = 1.99$ (model II.1). The contours correspond to 16, 17, 18, 19, 20, 25, and 30 K. *Second from below*: same 3D model geometry, but with the opacity curve of Zubko et al. (2004) that includes PAHs and for $\beta = 2.1$ (model II.2, see the text). *Bottom*: model II.3 has the same geometry as before, but uses opacities from Weingartner & Draine (2001) for $R_v = 5.5$ and PAHs (see Fig. 13).

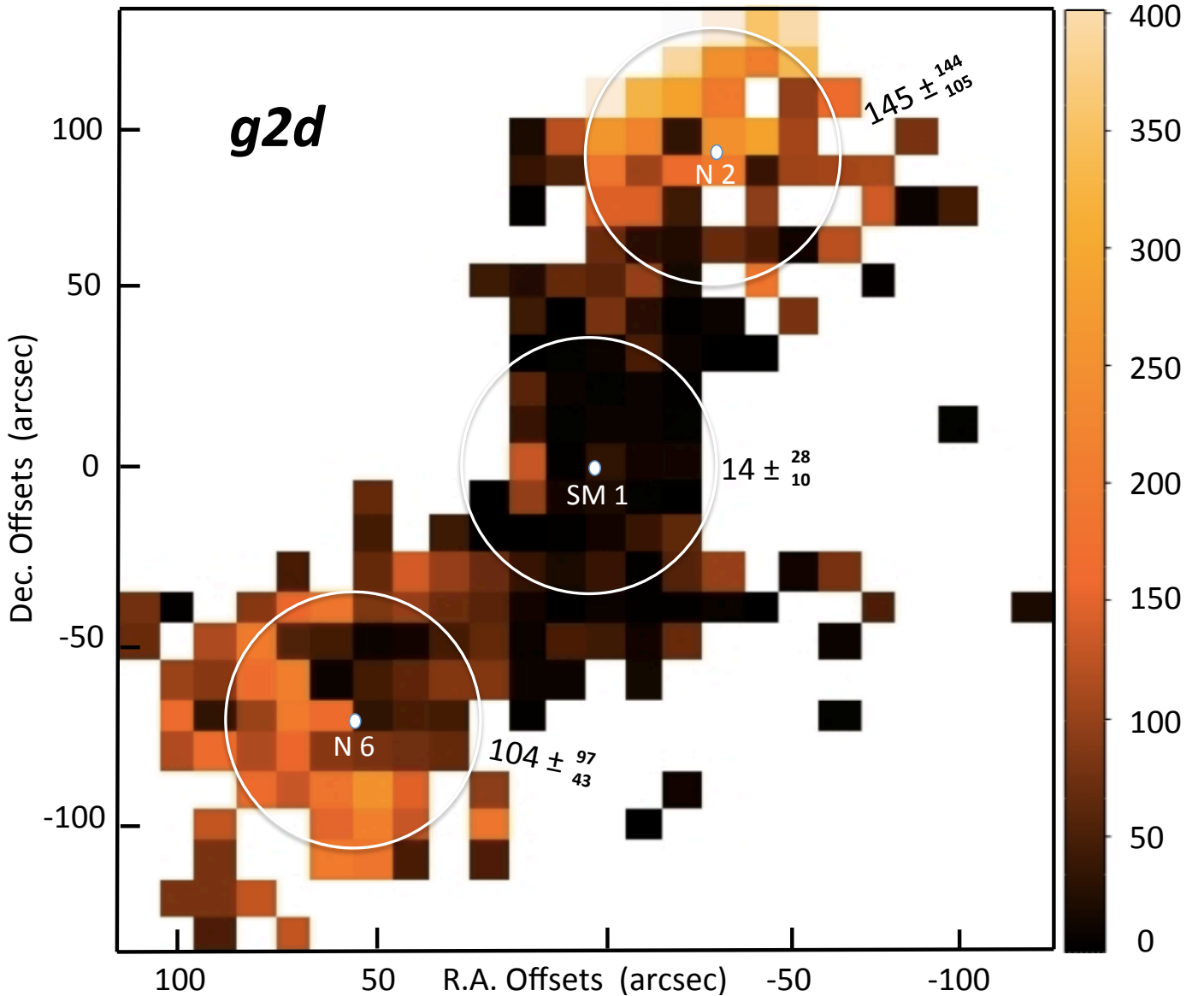


Fig. 17. Distribution of the gas-to-dust ratio, $g2d$, in ρ Oph A. The gas mass estimate is based on the N_2H^+ data and that of the dust on model II.3. The median values and their absolute deviations have been calculated inside the white circles around the sources in the north, N 2, the centre, SM 1, and the south, N 6 (see Di Francesco et al. 2004). On the other hand, the average refers to all pixels of the map, with the result $g2d_{ave} = 88$.

line intensity $\int T_A d\nu$ for the gas has then effectively the same resolution as the $350 \mu\text{m}$ continuum data for the dust (Fig. 18). It is gratifying to notice that the point source VLA 1623, which is detected in both data sets, is at the same position in both maps. Furthermore, as a final sanity check, we degraded the high-resolution result with the APEX beam at $850 \mu\text{m}$, and this procedure did indeed recover the observed (input) map. We are therefore confident that any differences in the intensity distributions and on spatial scales exceeding 3σ ($=6''$) of the pointing accuracy are real.

This gas-dust dichotomy is not immediately apparent in the presented maps involving N_2H^+ , since these have a much lower resolution, governed by the ($J = 6-5$) observations with the roughly $40''$ -beam of *Herschel*. However, the ($3-2$) data have been obtained with APEX and for the same coordinates as the LA-/SABOCA maps. Using IMAGINE for the N_2H^+ ($3-2$) map then yields a similar resolution as the SABOCA image and the sharpened $C^{18}O$ ($3-2$) map. The result is shown in the right panel of Fig. 18. The clear offset, by $12''$, between the continuum

source VLA 1623 and an intensity peak in N_2H^+ is at first astonishing. Similar mismatches are also found elsewhere in these images, and they have also been noticed by others (Di Francesco et al. 2004; Friesen et al. 2014). We therefore conclude that the spatial non-coincidence between molecular gas and dust is real. However, since the N_2H^+ emission ridge is much narrower than that in $C^{18}O$, a depression in the distribution is not evidenced by the present image. This may require data at higher resolution.

From Fig. 18, it is immediately evident that the dust continuum and the molecular line emission have different spatial distributions in the sky. Maximum line emission in $C^{18}O$ ($3-2$) is observed in a ridge closest to the stellar heating source S 1, whereas the continuum is mostly pronounced offset to the west, where all dust models, both 1D and 3D, indicate dust temperatures $T_{dust} \geq 20$ K. In contrast, the spectral line analysis points toward gas temperatures that are clearly much lower than twenty Kelvin (see also, e.g., Stamatellos et al. 2007). This might effectively have created the “hole” of the $C^{18}O$ emission, which might be due to depletion of the CO gas onto the dust. At $T_{kin} < 25$ K,

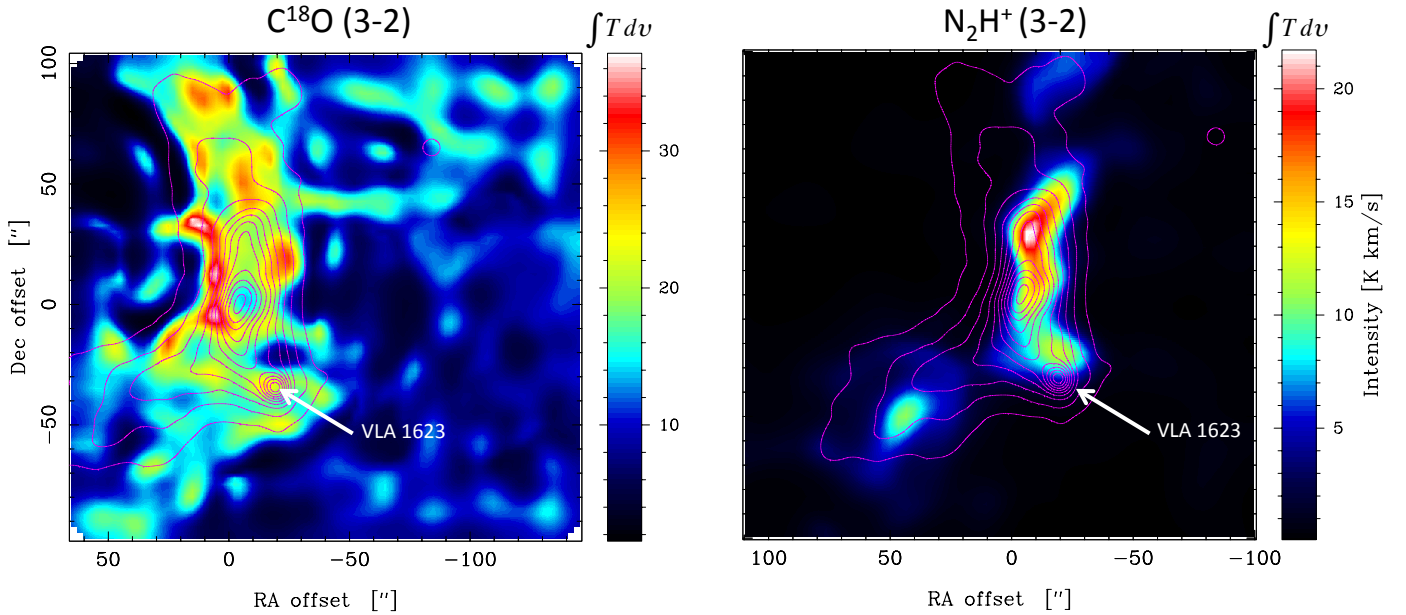


Fig. 18. *Left:* C^{18}O (3–2) map at $850\ \mu\text{m}$, deconvolved to the same resolution ($7''$) as that of the SABOCA $350\ \mu\text{m}$ continuum data, shown as contours (from 2.5 to 30 in increments of 2.5 Jy/beam). The Class 0 source VLA 1623 is clearly present in both the line and the continuum data. *Right:* same as the left frame, but for N_2H^+ (3–2) line and $350\ \mu\text{m}$ continuum radiation. The colour coding of the line intensity is given by the bar next to each image.

carbon monoxide is mostly frozen out (Sandford & Allamandola 1993; Öberg et al. 2005), whereas diazenylium is possibly much less affected because it mainly remains in the gas phase. It is not clear, however, how N_2H^+ would react at temperatures even below 15 K (Öberg et al. 2005). A selective freeze-out scenario would not explain the low $g2d$ that is based on N_2H^+ observations. On the other hand, if all molecules are frozen out, there would be no contradiction¹².

5. Conclusions

In the FIR/submm, observed point sources exhibit a dependence of the dust parameter β on evolutionary status (SED class), $\beta = \beta(t)$. Values decrease monotonically with age. For the pre-stellar core SM 1, the continuum emission is entirely dominated by the thick envelope and $\beta = 2$, whereas in pre-main-sequence stellar objects of Class III, the envelope is lost and the emission originates only from the circumstellar disk, $\beta \sim 0$. Objects of intermediate type display intermediate β -values. If not merely a matter of contrast, this may imply that grain growth primarily occurs in the protoplanetary disks, not in the natal cloud cores, since low values of β are ascribed to large grains.

ρ Oph A is exposed to uneven irradiation by stellar sources, heating the core primarily from the outside. We examined different dust emission models, including both 1D and 3D geometries, without and with thermal balance and with non-equilibrium conditions. Mass estimates span a factor of seven, but do agree to within a factor of two when proper weighting by the absolute mass opacity κ_ν is applied.

To model the observed gas emission in N_2H^+ lines, best-fit solutions were obtained by combing a multi-dimensional parameter space. These provided excellent fits to the spatial distribution of the line intensity and the line shape. Combining

the results for the gas with those for the dust yielded a global gas-to-dust mass ratio that is only slightly sub-canonical, $g2d = 88$. However, on local scales, this hardly applies anywhere, with ratios much higher than 10^2 in the north and south and significantly lower than that in the central regions. There, gas and dust appear to be spatially segregated. At high angular resolution, a hole of C^{18}O (3–2) emission is accompanied by maximum emission in the dust continuum. At lower resolution, this may result in a misleading $g2d$, and perhaps indicate that N_2H^+ is frozen out as well.

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Appendix A: Estimation of dust masses in homogenous and isothermal media

The modification we made to the commonly adopted procedure is based on the fact that we do not a priori assume only a single dust temperature and grain opacity. Rather, these quantities are parameters to be fit iteratively by comparison with submillimetre observations. The value of the optical depth at any frequency is obtained and tested a posteriori. The specific intensity I_ν , in $\text{erg cm}^{-2} \text{s}^{-1} \text{Hz}^{-1} \text{sr}^{-1}$, along the LOS of optically thin thermal emission from dust particles can be written as

$$I_\nu = \int \kappa_\nu n_d m_d B_\nu(T_d) ds, \quad \tau_\nu \ll 1, \quad (\text{A.1})$$

¹² Sandford et al. (1993) found evidence for frozen H_2 in the ρ Oph cloud. However, this result was retracted in 2000, *Sci.*, 287, 976.

where κ_ν is the dust mass opacity, in $\text{cm}^2 \text{g}^{-1}$, at the frequency ν , in Hz, n_d is the volume density of dust particles, in cm^{-3} , m_d is the mass of a dust grain, in g, and $B_\nu(T_d)$ is the Planck function, in $\text{erg cm}^{-2} \text{s}^{-1} \text{Hz}^{-1} \text{sr}^{-1}$, at ν and for the dust temperature T_d , in Kelvin.

For constant κ_ν , m_d and T_d along a ray, the integral is only over the volume density n_d , meaning that it is the column density of dust grains, $\int n_d ds = N_d$. The surface density of dust particles is $\Sigma_d = m_d N_d$. Identification in Eq. (A.1) yields

$$\Sigma_d = \frac{I_\nu}{\kappa_\nu B_\nu(T_d)}. \quad (\text{A.2})$$

From Eq. (A.2) it is apparent that the optical depth through the dust is given by

$$\tau_\nu = \kappa_\nu \Sigma_d. \quad (\text{A.3})$$

The assumption that $\tau_\nu \ll 1$ will have to be justified a posteriori. Applying Eq. (A.2) to observations I_{ν_1} at a given frequency ν_1 , together with κ_{ν_1} from a particular opacity curve ($j = 1, 2, 3, \dots$), yields a multitude ($i = 1, 2, 3, \dots$) of solutions for both Σ_d and T_d , that is,

$$\Sigma_d(i, j) = \frac{I_{\nu_1}}{\kappa_{\nu_1}(j) B_{\nu_1}[T_d(i, j)]}. \quad (\text{A.4})$$

This multitude is limited by the range of examined temperatures, viz. $T_d = 4$ to 2000 K, where the first value refers to the average equilibrium temperature of grains irradiated by the interstellar radiation field in the solar neighbourhood¹³ and the second to approximate dust evaporation temperatures. Similarly, the number of discretized temperature values, $T_d(i, j)$, that need to be computed is ultimately limited by the measuring accuracy of I_ν .

This multitude can be further reduced, in fact to unity, since, for any given opacity curve, only one value of T_d (and Σ_d) will simultaneously satisfy Eq. (A.2) for data at another frequency, for example, I_{ν_2} , viz.

$$\Delta I_{\nu_2}(j) = I_{\nu_2}^{\text{obs}} - \Sigma_d(i, j) \kappa_{\nu_2}(j) B_{\nu_2}[T_d(i, j)], \quad (\text{A.5})$$

where we let $\Delta I_{\nu_2}(j) \rightarrow 0$. Equation (A.5) yields for each opacity curve, designated by j , a unique solution for $T_d(j)$ and $\Sigma_d(j)$. It only remains to select the correct κ -curve. Minimization of the data for a third frequency, I_{ν_3} , could in principle be used to achieve this. Hence

$$\Delta \kappa_{\nu_3}(j) = \kappa_{\nu_3}(j) - \frac{I_{\nu_3}}{\Sigma_d(j) B_{\nu_3}[T_d(j)]}. \quad (\text{A.6})$$

Minimizing $\Delta \kappa_\nu$, then provides the unique solution for the temperature T_d , the surface density Σ_d and the opacity law of the dust, $\kappa = \kappa(\nu)$. Finally, the assumption of low optical depth at the different frequencies of this solution is then verified a posteriori (Eq. (A.3)).

The column density of the gas, $N_g = N(\text{H})$, needs to be determined from other observations. This, finally, leads to the gas-to-dust mass ratio from

$$g2d = \frac{\mu m_{\text{H}} N_g}{\Sigma_d}, \quad (\text{A.7})$$

where $\mu = 2.4$ is the mean molecular weight. The derived dust opacity curve has been computed for a particular volume density of the gas, $n^g(\text{H})$ and this ought to be consistent with that

determined from the spectral line fitting, $n^g(\text{H})$. The spatial averaging is done over each pixel, so that the total dust mass, M_d , is then obtained from the summation of the surface density per pixel over all pixels.

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¹³ For ρ Oph A, the (anisotropic) radiation field is more intense by two orders of magnitude (Liseau et al. 1999).

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