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## FEMALE LABOUR SUPPLY IN FARM HOUSEHOLDS: FARM AND OFF-FARM PARTICIPATION

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## Female Labour Supply in Farm Households: Farm and Off-Farm Participation

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## Abstract

In Ireland, with its relatively large farm sector, the numbers of farmer's wives who exercise the option of becoming "relastives assisting" is substantial. Using cross-section household data collected by ESRI in 1987, we analyse various models in which farmer's wives choose between farm work, off-farm paid work, and other (home production) activities. The explanatory variables include family characteristics, farm characteristics, and the wife's wage rate for off-farm work. We compare probit and logit type of models, and allow for wage rate endogeneity. The main finding according to all models is the very large sensitivity of off-farm participation with respect to the wage.

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## **1. Introduction**

A vast literature on the analysis of female labour supply has grown up in recent decades. But most studies in this literature exclude women whose husbands are self-employed or farmers.<sup>1</sup> The main reason for this exclusion is that such women may face different economic opportunities from others. They have an additional option of assisting on the family farm or business. Furthermore, the value of their time in this use is not conveniently summarised by a wage: by definition, relatives assisting are family members who do not receive a regular wage. This creates obvious difficulties in modelling the incentives facing them.

In many countries, the proportion of married women who have this additional option is low: their exclusion from studies in the UK or USA, for example, does not greatly affect the overall picture of married women's labour supply in those countries. But in Ireland the size of the self-employed sector, and more especially of the farm sector, is such that the issue is potentially important. Adjustment of farm labour supply to changes in the balance between farm and off-farm opportunities is of considerable relevance in the context of reforms of the Common Agricultural Policy and the reductions in agricultural output likely to be associated with the completion of the Uruguay round of GATT negotiations. It is clear from the general labour supply literature that women's labour supply may be more responsive than that of men, so that particular attention may need to be given to the labour supply of farm wives in this context.

This paper has three main aims.

 To establish the extent to which married women in Irish farm households exercise the option of becoming "relatives assisting" in farm work.

<sup>1</sup> See, for example, Killingsworth and Heckman's (1986) summary of the samples used in these various studies: the vast majority exclude women who are themselves self-employed, or whose husband is self-employed or a farmer.

- (2) To identify and analyse factors influencing farm wives' allocation of time between farm work, off-farm paid work, and other activities.
- (3) To explore the sensitivity of estimates of farm wives' labour supply elasticities with respect to model specifications and estimation procedures.

The paper is structured as follows. Section 2 deals with the first of these objectives, and outlines the nature of the data gathered in the ESRI Survey of Income Distribution, Poverty and Usage of State Services. A model of the decision between participation in farm work, off-farm employment and non-participation is outlined in section 3, together with the estimation procedures. Section 4 deals with the results, and considers the sensitivity of wage elasticities with respect to choices made in model specification and estimation.

## 2. Relatives assisting: a dying breed or a hidden army?

Estimates of the incidence of relatives assisting on family farms vary widely, as pointed out by Fahey (1990). Table 1 draws together information from the Census of Population, the Labour Force Survey, the EC Farm Structures Survey, and the ESRI Survey of Income Distribution, Poverty and Usage of State Services. The Census of Population and Labour Force Survey results suggest that the numbers engaged as relatives assisting have declined to very low levels. The Census of Population uses a "principal economic status" classification (PES). As Fahey points out, "PES data tend to discount the economic activity of women who see their primary role in terms of housework" (Fahey, 1990, p. 179). It is not surprising, therefore, that the Census figures show very low numbers classified as relatives assisting.

		Tota	ıl	Agricu	lture
Data source	Year	Male	Female	Male	Female
Census of Population	1971	50,800	8,100	-	-
Census of Population	1981	23,300	5,400	-	-
Labour Force Survey	1987	15,800	8,700	13,900	5,000
EC Farm Structures Survey (married women at work farming)	1979-80 in	-	-	-	94,300
ESRI Survey (married women at work farming as assisting relatives)	1987 in	-		-	38,300

Table 1: Alternative Estimates of Numbers of "Relatives Assisting"

The Labour Force Survey uses both a PES definition and an alternative definition (a labour force measure), under which persons who are engaged in activity for "pay, profit or family gain" for more than one hour per week are classified as economically active. The figures in Table 1 show that the numbers under the alternative definition in the 1987 Labour Force Survey are of the same order of magnitude as those for the PES definition in the 1981 Census of Population. On the basis of a closer comparison of the definitions within the 1983 Labour Force Survey, Fahey (1990) concludes that the numbers on a labour force definition are somewhat higher than those on a PES definition, but that the differences within agriculture are surprisingly small.

Sectoral studies of agriculture have shown quite different results. The EC Farm Structure survey<sup>2</sup> of 1979-80, found over 10 times as many women at work in agriculture as the 1981 Census; and almost 30 times as many married women at work in agriculture. Short-term and seasonal participation were included in this measure, but accounted for only a small proportion

<sup>2</sup> For a more detailed assessment of this data source see Fahey (1990) and O'Neill (1985).

of the total. The level of participation shown by this data source has fluctuated, giving rise to suspicions of measurement error, but these fluctuations have been at a high level relative to the Census and Labour Force Surveys.

Fahey's conclusion, based on comparisons within and between these surveys, and additional evidence from the study by Hannan and Katsioaouni (1977)<sup>3</sup>, is that the Labour Force Survey (and *a fortiori* the Census of Population) underestimates the numbers of farm wives engaged in farm work, while the figures in the Farm Structures Survey may be somewhat on the high side. Differences in concepts may play some role in creating the gap between the different estimates, but it is clear that there are also substantial biases involved. The reasons for such biases are outside the scope of the present paper; suffice it to say that difficulties in establishing the boundaries between farm work and other work, the preconceptions of enumerators, interviewers and respondents, shaped by general societal attitudes and the relative prestige accorded to different statuses have all been identified as possible contributors.<sup>4</sup>

The ESRI Survey of Income Distribution, Poverty and Usage of State Services, conducted in 1987, offers some new perspectives on this issue. Respondents answered questions about their main economic status in a way similar to that for the Labour Force Survey. But they were also asked separate questions about extent of farm work, irrespective of their answer to the question on principal economic status.<sup>5</sup> Those who stated that their principal status was home duties, but reported working more than an hour a week on the farm

**<sup>3</sup>** This additional evidence includes the fact that two-thirds of the farm husbands interviewed by Hannan and Katsioaouni stated that without the contribution of wives and younger children, some line of production would have to be dropped.

<sup>4</sup> Shortall (1990), for example, argues that the concentration on traditionally defined farm work obscures women's role.

<sup>5</sup> The key question, asked of every respondent, was "Do you own or operate any farm land, or assist with the running of a farm owned by a member of your family?". Follow up questions included the number of weeks of full-time work, and for part-time work, the number of weeks and weekly hours.

were reclassified to the status of relatives assisting.<sup>6</sup> This definition of "relatives assisting" in the ESRI survey produces a figure which is between that of the Farm Structure survey, which is suspected of being an over-estimate, and those of the Census of Population and Labour Force Surveys, which are suspected of being underestimates. It is this ESRI data which provides the basis for the analysis of farm wives choice of farm as against off-farm participation in the next section.

Table 2 shows how the sample used in the econometric analysis was arrived at. A total of 511 farm households contained a married woman, but only 418 of these were aged under 65 and married to the person mainly responsible for the farm. Missing data led to the exclusion of a further 23 cases, leaving a sample of 395 cases for analysis.

Table 2:	Definition of	of Sample	of Farm	Wives
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Inclusion criterion	N excluded	N remaining
Total number of farm households	0	670
Married woman in farm household	159	511
Married woman is aged under 65	55	456
Husband is person mainly responsible for farm	38	418
Full individual questionnaire for woman	23	395

Source: ESRI Survey of Income Distribution, Poverty and Usage of State Services, 1987.

Of the 395 remaining cases, 44 women (11.1 per cent) were engaged in paid off-farm employment, 159 (40.3 per cent) were classified as relatives assisting with farm work, with the remaining 192 (48.6 per cent) engaged in neither of these activities. A description of the variables used in the analysis is given in Appendix A, with sample statistics in Appendix B.

More detailed information on weeks and hours of work is available for about 85 per cent of those classified as relatives assisting. Of these, about 80 per cent were found to have worked for 40 weeks or more in the year; and less than 8 per cent worked fewer than 13 weeks.

<sup>6</sup> Most of those reclassified in this way worked substantially more than the minimum hours.

Combining information on weeks worked and hours worked per week, we constructed a measure of annual labour input. Taking a value of 48 weeks at 40 hours as a measure of a full year's work, we found that 11 per cent worked as relatives assisting for a full year, 26 per cent worked between a half-year and a full year, and a further 38 per cent worked the equivalent of between a quarter-year and a half-year. Thus, for the vast majority of those classified as relatives assisting, their role involved a substantial time commitment rather than simply a seasonal one.<sup>7</sup>

Of the 44 women working in paid employment, only 1 worked for less than 20 hours per week, and over 70 per cent worked for at least 30 hours per week. This suggests that either the opportunities for part-time work were extremely limited, or the fixed costs associated with employment (such as travel to work, and some element of childcare costs) discouraged the choice of such arrangements.

<sup>7</sup> Interviews were conducted between February and September 1987. Some women who had only a short, seasonal involvement in farm work may not have classified themselves as relatives assisting because of the timing of the interview; but the group identified here, as indicated by the extra information on weeks of work, does not include many such women.

## 3. Analysis of female labour supply in farm households

## 3.1 Models

#### Basic Model

Our focus in this section is on the labour supply behaviour of farm wives. As noted earlier, the labour supply of this group is rendered more complex by the fact that they may allocate time to farm activities, as well as to off-farm employment, home production and leisure. The data collected in the ESRI survey are not sufficiently detailed to support a full structural model along the lines of the household production models surveyed by Gronau (1986). A structural model would include a production function (in this case, for farm output), with the time spent by a farm wife as relative assisting figuring as one form of labour input, substitutable against other labour and non-labour inputs. Here a simpler approach is adopted, with farm characteristics (farm size, soil type and farm system) being treated as factors which shift the productivity of labour inputs. These factors are treated as exogenous, as well as the off-farm labour supply of the husband. The main endogenous variable is an index D indicating the woman's type of economic activity:

D=1: the woman has a formal job and receives a wage (employed)

D=2: the woman works on the farm (relative assisting)

D=0: the woman is neither an employee, nor a relative assisting (non-participant)

The value of D indicates the main activity. In principle, it is possible that individuals might combine farm work and off-farm employment. But the data show that very few women combine farm work and off-farm work, so that D can be treated as having one and only one value. A wage rate is observed if and only if D=1. The natural logarithm of the wife's gross (i.e., pre-tax) hourly wage rate is denoted by W.

We want to find out what determines D, with emphasis on economic factors such as W. W is treated separately from the other variables, because of the observability problem (it is not observed unless D=1) and because of possible endogeneity. We therefore also include a wage equation. A so-called "random utility" model can capture the main features of interest. The complete model for individual i is as follows:

$$U_{ij} = A_{ij} + u_{ij} \quad (j = 0, 1, 2) \tag{1}$$

$$D_i = j$$
 if and only if  $U_{ij} \ge U_{ik}$ ,  $k = 0, 1, 2$  (2)

$$A_{ij} = X_i' \beta_j + \gamma_j W_i \quad (j = 1, 2); \quad A_{i0} = 0$$
(3)

$$W_i = Z_i' \alpha + v_i \tag{4}$$

$$u_{i0} = 0; \quad (u_{i1}, u_{i2}, v_i | X_i, Z_i) \sim N_3(0, \Sigma)$$
(5)

Thus, if  $\gamma_1 = \gamma_2 = 0$ , (1) through (3) yield the familiar multinomial probit model with three alternatives (see, for example, Maddala, 1983). By means of normalisation,  $\Sigma(1,1)=\Sigma(2,2)=1$ . Because only the differences  $U_{ij}$  - $U_{ik}$  are identified, the normalisation  $U_{i0} = 0$  is necessary for identification.

The covariance matrix  $\Sigma$  can be a full matrix. There seems to be no economic reasons for setting  $\Sigma(1,2)$  equal to zero. In particular, if we imposed  $\Sigma(1,2)=0$  and then rewrite the model with a different normalisation such as  $U_{i1} = 0$ , we would obtain a transformed covariance matrix with a non-zero element in place of  $\Sigma(1,2)$  (the covariance between  $-u_{i1}$  and  $u_{i2} - u_{i1}$  is nonzero if the covariance between  $u_{i1}$  and  $u_{i2}$  is zero).

If we ignore labour market constraints leading to involuntary unemployment,  $U_{i1}$  can be interpreted as the difference between utility of employment and utility of non-participation. The term  $\gamma_1 W_i$  thus reflects the impact on utility of the difference between earnings and returns of non-participation (i.e. home production). It might also pick up some taste shifter effect, however. Since the wife's contribution to farm output is not observed, returns to activity as a relative assisting are not measured. The term  $\gamma_2 W_i$  may to some extent pick up the part of difference between farm earnings and returns of home production not captured by other regressors such as farm size and type. Again it may also reflect a pure taste shifter effect. Given the information in the data, the two cannot be disentangled.

Setting  $\Sigma(1,3)=\Sigma(2,3)=0$  boils down to assuming that W is exogenous. Unobserved characteristics not included in X or Z may however lead to correlation between  $v_i$  and the  $u_{ij}$ 's. Therefore, we shall at least try to estimate the model with a full covariance matrix  $\Sigma$ , although, for practical purposes, it may still be necessary to impose zero restrictions.

The vectors of exogenous variables X and Z may partly overlap. Throughout the paper, we shall assume that X contains at least one variable which is not in Z (e.g. characteristics of the farm or family composition) and that Z contains at least one variable which is not in X (e.g. the woman's education level). These two conditions are sufficient for (non-parametric) identification of the model, even if no restrictions on  $\Sigma$  are imposed. It is clear that the latter of the two, which is the hardest to defend from an economic point of view, cannot be omitted, unless restrictions on  $\Sigma$  are imposed instead.

## Alternative Models

A number of variants and generalisations of the basic model described above are possible. In order to determine the sensitivity of the results with respect to distributional and functional form assumptions, it seems worthwile to estimate some of these alternatives. The relatively small number of observations makes a more general treatment, semi- or semi-non-parametric estimation, infeasible.

The alternatives which we shall consider are the following:

#### (A) Multinomial Logit, exogenous wage rates

Replace (5) by:

$$u_{i,v} \in V$$
,  $(j = 0, 1, 2)$ ;  $v_i \in N(0, \sigma_v^2)$ ,  $u_{i0}, u_{i1}, u_{i2}, v_i$  independent (5')

Here EV denotes the (standard) extreme value distribution underlying the multinomial logit model (cf. McFadden, 1974). For given W, the choice probabilities are the familiar multinomial logit probabilities:

$$P(D_i = j | X_i, Z_i, W_i) = \frac{\exp(A_{ij})}{\sum_{k} \exp(A_{ik})}$$
(6)

#### (B) Multinomial Logit, endogenous wage rates

The specification given above does not allow for endogeneity of W. It can however easily be generalised such that it does, without essentially complicating the estimation procedure. This is achieved by replacing (5') by

$$v_i \sim N(0, \sigma_v^2) \tag{7}$$

$$u_{ij} - \mu_j v_i | v_i \sim EV, \quad j = 0, 1, 2, \quad \mu_0 = 0 \tag{8}$$

$$u_{i0}|v_i, u_{i1}|v_i, u_{i2}|v_i$$
 independent (9)

If  $\mu_j \neq 0$ ,  $u_{ij}$  and  $v_i$  are not independent.  $\mu_1$  and  $\mu_2$  are parameters to be estimated. The expression for the conditional choice probabilities which generalises (6) becomes

$$P(D = j | X, Z, W) = \frac{\exp(A_j + \mu_j v)}{\sum_k \exp(A_k + \mu_k v)} \quad \text{with} \quad v = W - Z' \alpha$$
<sup>(6')</sup>

This thus boils down to adding the residual of the wage equation to the systematic part of the  $U_{ij}$ 's, with coefficients  $\mu_j$ .

#### (C) Non-linearities

The impact of exogenous variables and W on  $U_{ij}$  may be non-linear. Obviously, if this only concerns observed exogenous variables, it is straightforward to allow for, including nonlinear transformations of these variables in X. The situation is slightly more complicated if the impact of W is non-linear. We may, for example, want to use a Box-Cox transformation and replace (3) by:

$$A_{ij} = X_i'\beta_j + \gamma_j \frac{(\exp(\lambda W) - 1)}{\lambda} \quad (j = 1, 2); \quad A_{i0} = 0$$
(3')

For  $\lambda \to 0$ , we again get the model with the log wage W. For  $\lambda = 1$  the wage itself is included. In general, any  $\lambda \in \Re$  is possible, although many people often assume that  $\lambda \in [0, 1]$ . This generalisation can be incorporated in the basic multinomial probit model, as well as in the multinomial logit variants. As will be seen below, the non-linearities make ML-estimation more difficult, but does not complicate a simulation-based estimation procedure.

#### 3.2 Estimation procedures

The basic model can be estimated in several ways. Apart from ML- estimation, we discuss some alternative estimators, which can also be used to estimate the alternative models.

#### ML-estimation of the basic model

This is straightforward. The likelihood contributions can be written as follows, distinguishing the case that W is observed (D=1) and the case that W is not observed (D=2 or D=0). The index i is suppressed.

D=1, observed log wage W:

(10)

 $L = f_{v}(v)P(-u_{1} < -A_{1}, u_{2} - u_{1} < A_{1} - A_{2}|v),$ where v = W - Z' and  $A_{j} = X_{i}'\beta + \gamma W$ 

Here  $f_v$  denotes the marginal density of v, which is univariate normal  $N(0, \sigma_v^2)$ . The conditional probability in (10) is bivariate normal and therefore easy to compute, because of the simultaneous normality of  $(u_1, u_2, v)$ .

D=2, wage rate not observed:

$$L = P[u_2 + \gamma_2 v > -X'\beta_2 - \gamma_2 Z'\alpha, u_2 - u_1 + (\gamma_2 - \gamma_1)v > X'(\beta_1 - \beta_2) + (\gamma_1 - \gamma_2)Z'\alpha]$$
(11)

Again, this is a bivariate normal probability which can easily be computed. For D=0, an analagous expression can be given.

ML-estimation of the full model, not imposing restrictions on  $\Sigma$ , yields estimates of all the parameters, including those in  $\Sigma$ . If restrictions on  $\Sigma$  are imposed, the estimates of  $\alpha$ ,  $\beta$  and  $\gamma$  will only be consistent under the null that the restrictions are true. Thus, accounting for simultaneity implies the need to estimate more parameters. In this type of models, this can sometimes be avoided using a two step estimation procedure:

#### Two-step estimation of the basic model

Step 1: Estimate  $\alpha$ , using the familiar Heckman procedure (add a reduced form participation equation to the wage equation to correct for selectivity bias). This yields an estimate a of  $\alpha$ . In principle, the estimate of  $\alpha$  will not be consistent given the complete model: According to the complete model, participation is determined by two separate equations, and this is approximated by one reduced form participation equation. However, in practice the asymptotic bias will be quite small.

Step 2: Replace  $W_i$  in (3) by its prediction  $Z_i$ 'a and estimate the resulting multinomial probit model. This solves the problem that  $W_i$  is sometimes unobserved. Moreover, although  $W_i$  may be correlated with  $u_{ij}$ , its predicted systematic part  $Z_i$ 'a will in general be (asymptotically) uncorrelated with  $u_{ij}$ . Thus, the estimator remains consistent if there is simultaneity.

Although this may seem a feasible and computationally attractive procedure, it also creates a new problem: Note that substituting (3) and (4) into (10) yields

$$U_{ij} = X_i'\beta_j + \gamma_j Z_i'\alpha + u_{ij} + \gamma_j v_i (j = 0, 1, 2)$$
(12)

$$D_i = j$$
 if and only if  $U_{ij} > U_{ik}$ ,  $k = 0, 1, 2$  (13)

The second step implies replacing  $Z_i'\alpha$  by  $Z_i'a$  and estimating (12) and (13) as a multinomial probit model. This implies a normalisation different from the original one  $(\Sigma(1,1)=\Sigma(2,2)=1)$ : If  $V\{u_{ii}\}=1$ , then, in general,  $V\{u_{ii}+\gamma_iv_i\} \neq 1$ . The estimates of  $\beta$  thus have

to be rescaled. This is easy if it is assumed that  $Cov\{v_i, u_{ij}\}=0$ . Otherwise, however, it requires estimating these covariances. For similar reasons, the estimated covariance between the two errors in the two equations of (12) is not the same as  $Cov\{u_{i1}, u_{i2}\}$ .

The two-step procedure thus suffers from several drawbacks. The assumptions needed for consistency are just as strong as for ML (We need normality and homoskedasticity of  $v_i$  to obtain normality and homoskedasticity of the errors in (12)). Obtaining consistent estimates of the standard errors, taking into account that  $\alpha$  is replaced by a, requires extra computations.

#### Simulated Maximum Likelihood

Exact ML-estimation of the basic model is straightforward because the probabilities in (10) and (11) are bivariate normal. In the alternative models, (11) contains either a convolution of a normal and an extreme value distribution (the multinomial logit case), or a non-linear function of two normals (in case of non-linearity). In both cases, it remains easy to compute the probability in (10), since the second factor treats v as known. Problems arise with (11). Note that (11) can be replaced by

$$L = \int_{-\infty}^{\infty} f_{\nu}(\nu) P[u_{2} > -X'\beta_{2} - \gamma_{2}(Z'\alpha + \nu), u_{2} - u_{1} > X'(\beta_{1} - \beta_{2}) + (\gamma_{1} - \gamma_{2})(Z'\alpha + \nu)|\nu| d\nu$$
  
=  $E\{P[D = 2|\nu]\}$  (11')

where the expectation is taken with respect to v. In all variants of the model, P[D = 2|v] is easy to compute, but the expectation is not, except for the basic model. One way to approximate the expectation in (11') is to replace it by a simulated mean, using R independent draws of v:

$$La = \frac{1}{R} \sum_{r=1}^{R} P[D = 2|v_r]$$
(14)

For large R, La approximates L, because of the law of large numbers. Instead of maximising the exact likelihood, the approximate likelihood can be maximised, in which for the

observations with D=2, L is replaced by La (and similarly for those with D=0). The resulting estimator is known as Simulated Maximum Likelihood (SML). See Lerman and Manski (1981) or Gourieroux and Monfort (1990). For fixed R, the estimator is inconsistent. If R tends to infinity with the number of observations, the estimator is consistent. Moreover, provided that draws for different indivdiuals are independent, ML and SML will be asymptotically equivalent as  $R/\sqrt{N} \rightarrow \infty$ , where N is the number of observations (cf. Gourieroux and Monfort, 1990).

### Using Complementary Data

A problem with the estimation procedures described above is the lack of data on wage rates. In the data set to be used, containing farmer's wives only, no more than 44 women have a formal job. Instead of estimating  $\alpha$  and  $\sigma_{\nu}$  from these 44 observations only, it is possible to use the full data set of married women to estimate a wage equation. The implicit assumption, that the wages of farmer's wives are determined in the same way as wages of other married women, seems a reasonable one. Estimates for  $\alpha$  and  $\sigma_{v}$  based on the whole data set are given in Callan (1991). The sample used there contains 1712 married women, 324 of whom are employed with observed wage rate. We use results corrected for selectivity bias (Column 3 of Table 1, Callan, 1991). Thus, instead of estimating all the parameters simultaneously, an alternative approach is to assume that  $\alpha$  and  $\sigma_{\nu}$  are equal to the Callan (1991) estimates and estimate the other parameters. In principle, the standard errors have to be corrected for the fact that  $\alpha$  and  $\sigma_{v}$  are replaced by their estimates. We present the uncorrected standard error estimates, which thus may be biased downwards. This problem does not seem to be too serious, because of the relatively large number of observations used to estimate  $\alpha$  and  $\sigma_{v}$ . Estimation results based on a wage equation which includes only the farmers' wives in the present sample, reported below, provide a check on this procedure. The alternative wage equation estimates are available on request.

Some idea of the reliability of this procedure can also be gained by testing the structural stability of the wage equation over the full sample as against two sub-samples: the 44 farm wives and 282 non-farm wives. As expected, least squares estimates show that structural stability of the wage equation as between the full sample and sub-samples of farm and non-farm wives is not rejected.

## **4.Results**

## 4.1 Parameter estimates

Maximum likelihood estimates of the basic model are set out in Table 3. The table contains three sets of estimates. In the first two, the parameters  $\alpha$  and  $\sigma_{\nu}$  in the wage equation are not estimated, but set equal to the estimates based on a larger data set (cf. Callan, 1991, Table 1, column 3). The first set is based on the assumption that  $\Sigma$  is a diagonal matrix, and thus imposes exogeneity of W. The second set of estimates shows the consequences of relaxing the conditions on  $\Sigma$ .

The estimates of the correlation coefficients are very imprecise. An upper-bound on  $\rho(1,2)$  had to be imposed to ensure that  $\Sigma$  is positive definite. Thus no standard error for the estimate of  $\rho(1,2)$  could be computed. The standard errors for the other correlation coefficients are huge and suggest that, from a practical point of view, there is no point in estimating  $\Sigma$  with the data at hand, even though the model is identified in theory. However, a likelihood ratio test based on the restricted and unrestricted likelihoods clearly rejects diagonality of  $\Sigma$ .

	1	I		11	III		
	parameter	std error	parameter	std error	parameter	std error	
Correlations							
$rho(u_1, u_2)$			0.8418*		0.8651*	-	
$rho(u_1,v)$			-0.1400	0.5160	-0.4148	0.9189	
$rho(u_2,v)$			0.2154	0.5960	-0.3813	1.1444	
Employment vs	Non-particip	ation					
constant	-1.5520	28.5576	-5.1307	21.5148	-8.2709	20.0414	
log age	2.8984	15.8265	3.8290	11.8012	5.3926	10.9743	
log 2 age	-0.7368	2.1759	-0.6944	1.5992	-0.8456	1.485	
young 0-4	-0.4424	0.3857	-0.2324	0.2715	-0.1850	0.2394	
log fam siz	-0.1965	0.3343	0.0421	0.2400	0.2113	0.240	
reg unemprt	-3.6089	5.3385	-5.4829	3.4848	-7.3556	2.895	
log inc hus	-0.0494		-0.0060	0.0466	0.0231	0.0411	
log farm siz	-0.1707	0.1561	-0.0299	0.1130	0.0974	0.1169	
dum cattle	0.2980	0.2688	0.2981	0.1803	0.1775	0.161	
dum soil1	0.1969	0.2636	0.2816	0.1822	0.2793	0.1569	
dum soil3	-0.0938	0.5170	0.1374	0.3051	0.3664	0.2840	
dum debt os	-0.5881	1.4633	-1.2659	1.0453	-1.5612	0.9062	
log debt os	0.1229	0.1633	0.1862	0.1181	0.2133	0.1009	
log wage rt	1.0072	0.2651	0.7561	0.2831	0.2471	0.1367	
Relative Assisti	ng vs. Non-pa	rticipation					
constant	-38.4688	25.4719	-19.5815	20.5113	-10.7054	22.7200	
log age	20.9443	13.7976	11.4184	11.1279	6.6039	12.3199	
log 2 age	-2.8089	1.8460	-1.6224	1.4900	-0.9926	1.6439	
young 0-4	0.0123	0.2597	-0.1665	0.2367	-0.1846	0.2379	
log fam siz	0.4252	0.2486	0.3016	0.2227	0.2543	0.2160	
reg unemprt	-9.3229	3.2719	-8.0377	2.7582	-7.4016	2.6798	
log inc hus	0.0708	0.0417	0.0452	0.0381	0.0307	0.0398	
log farmsiz	0.2227	0.1175	0.1435	0.1008	0.1222	0.1056	
dum cattle	0.1368	0.1536	0.1667	0.1392	0.1557	0.1390	
dum soil 1	0.3217	0.1704	0.3094	0.1499	0.2832	0.1586	
dum soil 3	0.4928	0.2210	0.4452	0.2140	0.4184	0.2136	
dum debt os	-1.7462	0.7641	-1.7663	0.7138	-1.6596	0.8286	
log debt os	0.2217	0.0865	0.2316	0.0809	0.2227	0.0940	
log wage rt	-0.7501	0.4190	-0.2078	0.3192	0.1331	0.437	
log likelihood		-307.57		-297.83		-290.21	

 Table 3:
 ML-estimates of the Basic Model

Notes: I:  $\Sigma$  diagonal, wage equation estimates from Callan (1991) II:  $\Sigma$  free, wage equation estimates from Callan (1991)

III:  $\Sigma$  free, wage equation estimated simultaneously

\* upper bound imposed because  $\Sigma$  must be positive definite

In the third column the wage equation estimates from Callan (1991) are not used. Instead, observed wage rates in the sample of farm wives (for the 44 women with a formal job) are used to estimate the wage equation simultaneously with the rest of the model. According to a likelihood ratio test, relaxing the restrictions that  $\alpha$  and  $\sigma_v$  are equal to the Callan (1991) values does not yield significant improvement. Moreover, standard errors in column 3 are close enough to those in column 2 to suggest that the problem of underestimating standard errors in the "complementary data" procedure is not a serious one. Thus, from this point on, we confine our attention to estimates which use the wage equation from Callan (1991).

The sets of estimates for the parameters  $\beta_1$ ,  $\gamma_1$ ,  $\beta_2$  and  $\gamma_2$  are not too different. In the equation determining the choice between non-participation and employment, only the log wage rate is significant (at the 5% level), with the expected positive sign. In the equation determining the choice between non-participation and relative assisting, some significance levels tend to vary. Significance levels for the first estimator, which imposes most constraints, are not systematically larger than for the second estimator. The general conclusions are comparable. The main difference concerns the estimated impact of the wage rate. In both cases the effect is negative, but its magnitude and significance level vary.

Since the likelihood ratio test suggests that some of the error correlations are non-zero, we concentrate in discussing the equation dealing with relatives assisting as against non-participation, on the second panel. Two variables dealing with farm debt are significant: a negative coefficient on a dummy for whether or not there is any debt, offset by a positive coefficient on the log of the amount outstanding. Since the amounts of debt outstanding are in practice quite large, the net effect is that debt has a positive and increasing effect on participation as a relative assisting. While there is a potential endogeneity in this area, debt overhang can also be the result of exogenous shocks such as those which pushed farm incomes to low levels in the mid-1980s. It seems from these estimates that one response to such debt overhang could have been to increase labour input by becoming a relative assisting.

Farm wives are also more likely to participate as relatives assisting on larger farms, though this is significant only at the (one-sided) 10 per cent level. Standard production function considerations would lead to such an effect: one would expect the marginal product of labour to rise with farm size. The other statistically significant coefficients are somewhat more difficult to interpret: there is a positive coefficient on both soil type 1 (the most fertile soils) and soil type 3 (the least fertile), as well as on the regional unemployment rate. The coefficient on the regional unemployment rate is heavily influenced by observations for one region: Donegal/North-West. A dummy for this region (or its exclusion) seems, from some additional analysis, to lead to the expected negative effect of the regional unemployment rate on farm wive's participation in the paid labour market, with the influence on participation assisting becoming insignificantly different from zero.

In Table 4, we present the results of a two step estimation procedure, again based on the wage equation estimates for the full sample set out in Callan (1991). The selection equations are estimated as a multinomial probit model, and, as discussed above, the estimates should be rescaled to compare them with those in Table 3. Without actually carrying out the rescaling procedure in too much detail (and without correcting standard errors), some conclusions can still be drawn. Again, all parameters in the employment versus non-participation equation are insignificant, except for the log wage rate. The sign of  $\gamma_1$  is again positive, but the magnitude of the effect according is somewhat out of line with the other estimates. This cannot be explained by rescaling. The estimates in the middle panel of Table 3 imply that  $V\{u_1 + \gamma_1 \nu\} \approx 1.08$ , so the estimate of  $\gamma_1$  should be rescaled from 1.88 to 1.95. However, the rescaling factor depends on the very inaccurate estimate of  $Cov\{u_1,v\}$ .

For the relative assisting versus non-participation parameters, the parameter corresponding to the log of the wage becomes significantly negative. This suggests that women who are able to command a high wage either tend to participate in paid employment,

or else to work in the home, but not to participate as relatives assisting. Otherwise, parameter estimates and significance levels largely correspond to those in Table 3. Rescaling hardly plays a role here, because of the small absolute value of  $\gamma_2$  in the second panel of Table 3.

	Employment vs Non-po	Employment vs Non-particpation		
	parameter	std error	parameter	std error
constant	6.5562	28.2595	37.2201	23.7837
log age	-2.9400	15.7309	20.7167	12.8653
log 2 age	0.1368	2.1651	-2.8113	1.7206
young 0-4	-0.3859	0.3937	-0.0302	0.2485
log fam siz	-0.1293	0.3430	0.3928	0.2334
reg unemprt	0.1259	5.2837	-9.7230	2.9241
log inc hus	-0.0754	0.0733	0.0698	0.0392
log farmsiz	-0.2295	0.1604	0.2195	0.1080
dum cattle	0.2759	0.2555	0.1437	0.1461
dum soil 1	0.1255	0.2585	0.3304	0.1603
dum soil 3	-0.1182	0.5629	0.4814	0.2093
dum debt os	-0.5709	1.3458	-1.7445	0.6978
log debt os	0.1122	0.1530	0.2238	0.0787
log wage rt	1.8895	0.3347	-0.9191	0.3692
log likelihood	-303.03			

 Table 4:
 Two-step Estimates of Basic Model

Notes: Predicted wages for all, using wage equation estimates from Callan (1991).

In Table 5, we present the simulated maximum likelihood estimates of the basic model, for various choices of R, i.e. the number of draws of v per observation. Diagonality of  $\Sigma$  has been imposed, and the wage equation estimates of Callan (1991) have been implemented. Thus the estimates in Table 5 should approximate those in the left panel of Table 3, and the only reason for including Table 5 is to see how good the approximation is for different values of R. Apparently, differences in estimates as well as standard errors are not very large. Standard errors tend to be somewhat underestimated. Somewhat surprisingly, the difference between the results for R=5 and those for R=50 are smaller than the differences between the exact ML results and those with R=50. R=50 thus seems to yield reasonable results. Therefore, R=50 will also be used in the alternative models, in which comparison with exact ML is computationally intractable.

		SML ntr=5		SML, tr=10		SML, ntr=50	
	parameter	std error	parameter	std error	parameter	std error	
Employment v	s. Non-partic	ripation					
constant	2.36	51 28.1003				28.6542	
log age	0.794	41 15.5490	2.2396			15.8843	
log 2 age	-0.43						
young 0-4	-0.384						
log fam siz	-0.18.						
reg unemprt	-4.584	14 5.2224	-3.3139				
log inc hus	-0.04	53 0.0658	-0.0585	0.067	-0.0505	0.0681	
log farmsiz	-0.16	0.1473	-0.2018	0.159	-0.1692	0.1569	
dum cattle	0.264	43 0.2583	0.3077	0.272	.3 0.3104	0.2712	
dum soil 1	0.21	0.2551	0.1777	0.266	0 0.1998	0.2650	
dum soil 3	-0.12	0.4889	-0.1331	0.527	9 -0.1061	0.5197	
dum debt os	-0.700	1.3986	-0.6600	) 1.440	-0.6012	1.4574	
log debt os	0.134	45 0.1563	0.1330	0.160	0.1235	0.1625	
log wage rt	0.910	66 0.2357	1.0881	0.267	9 1.0498	0.2676	
μ1							
Relative Assist	ing vs. Non-	participation					
constant	-38.154	48 24.5328	-35.2080	24.703	-35.1564	24.8541	
log age	20.66	13.2163	18.9576	13.339	6 19.0147	13.4452	
log 2 age	-2.77	12 1.7640	-2.5326	1.782	-2.5439	1.7975	
young 0-4	-0.003	0.2579	-0.0146	0.251	2 0.0052	0.2547	
log fam siz	0.41	0.2412	0.4145	0.241	1 0.4099	0.2419	
reg unemprt	-8.729	2.9313	-8.5765	3.050	-8.5976	3.1010	
log inc hus	0.070	0.0402	0.0710	0.040			
log farmsiz	0.223	0.1109	0.2104	0.115	8 0.2016	0.1126	
dum cattle	0.15	0.1507	0.1479	0.148	4 0.1407	0.1498	
dum soil 1	0.308	0.1628	0.3233	0.165	4 0.3033	0.1647	
dum soil 3	0.504	0.2164	0.5024	0.217	2 0.4916	0.2166	
dum debt os	-1.630	<b>62</b> 0.7674	-1.7089		-		
log debt os	0.208	0.0867	0.2149	0.085	6 0.2189	0.0849	
log wage rt	-0.64	0.2608	-0.5369	0.335	7 -0.5906	0.3828	
μ <sub>2</sub>							
log likelihood		-308,19		-308.10		-308.06	

 Table 5:
 Simulated Maximum Likelihood Estimation of the Basic Model

Simulated maximum likelihood estimates for the multinomial logit version of the model are given in Table 6. In each case, we use the estimates of the wage equation from Callan (1991). The left two panels impose independence of the three error terms in the selection part of the model from the error in the wage equation. The estimates are based upon 10 and 50 draws per observation, and the differences between the two sets are quite small. In the last set, correlation between  $(u_0,u_1,u_2)$  and v is allowed for. A likelihood ratio test rejects the null  $\mu_1 = \mu_2 = 0$ , implying that W is endogenous. However, the estimates of the  $\mu_j$  seem rather inaccurate, and the separate hypotheses  $\mu_j = 0$  (j=1,2) cannot be rejected at the 5 per cent level. This finding corresponds to what was found in the multinominal probit model.

Qualitative conclusions from the estimates of the selection equations remain largely the same as those from the basic model. Choosing between employment and non-participation is only significantly affected by the wage. The wage rate coefficients are of similar magnitude as those in Tables 1 and 3 if appropriately rescaled (which now means dividing by  $[\pi^2/3 + \mu_1^2 \sigma_v^2]^{1/2}$ ).

		SML		SML,		ML,
	ntr = 1()			tr=50		r = 50
	exoge	nous wages	exoge	nous wages	endogen	ous wages
	parameter	std error	parameter	std error	parameter	std error
Employment v.	s. Non-partic	ipation				
constant	3.744	48 50.6004	4 -0.5685	49.970	6.6639	
log age	1.788	32 28.149	4.0720	27.837	7 -1.2672	29.1924
log 2 age	-0.864				3 -0.3928	
young 0-4	-0.768		-0.8145	0.691	3 -0.7978	0.7108
log fam siz	-0.221					
reg unemprt	-8.389	96 9.737	-8.8252			9.9763
log inc hus	-0.116				4 -0.1198	
log farmsiz	-0.286	63 0.2914	4 -0.2279			0.3102
dum cattle	0.534	48 0.501	0.5253	0.498	0.6645	0.5253
dum soil 1	0.367	0.491	6 0.4060			
dum soil 3	-0.064	43 0.878	-0.0468	0.8622	-0.2569	0.9605
dum debt os	-1.754	17 2.596	-1.5793	2.645	7 -2.0795	2.8486
log debt os	0.308	0.290	0.2840	0.295		
log wage rt	1.921	0.536	1.8632	0.541	7 3.3383	0.7052
μ1					-1.5347	1.1901
Relative Assist	ting vs. Non-p	participation				
constant	-56.039	41.208	4 -55.2370	41.3292	2 -58.5993	42.6530
log age	30.653		30.2962	22.3200	5 33.3290	23.1006
log 2 age	-4.147	2.965	-4.1033	2.979	-4.6065	3.0917
young 0-4	-0.076	0.423	-0.0617	0.4270	0 -0.2057	0.4480
log fam siz	0.608	0.396	0.6000			0.4174
reg unemprt	-14.819	5.1040	-14.7112	5.1550	0 -17.2112	5.7360
log inc hus	0.109	0.067	8 0.1013	0.0668	8 0.1174	0.0718
log farmsiz	0.338	0.191	0.3251	0.1853	3 0.3495	0.1977
dum cattle	0.269	0.247	0.2586	0.248	0.3152	0.2677
dum soil 1	0.554	16 0.274	0.5249	0.2718	8 0.6241	0.3030
dum soil 3	0.846	0.3630	0.8253	0.3615	5 0.8367	0.3874
dum debt os	-3.159	1.2712	-3.1749	1.2654	4 -3.5091	1.3883
log debt os	0.401				5 0.4491	0.1595
log wage rt	-0.708		-0.7361	0.6323	3 -1.1872	0.6708
$\mu_2$					2.5565	1.8212
log likelihood		-307.72	2	-306.64	4	-299.50

Finally, some non-linear models are estimated, using (3') instead of (3). Some of the insignificant regressors have been removed. For comparison, estimates for the basic linear model with the reduced set of regressors is also given.

The estimates for the Box-Cox parameter appears to be quite large (larger than 1), but also may be very imprecise. In the basic version of the model, the t-value of  $\lambda$  suggests that it is not significantly different from 0 at any reasonable level. On the other hand, a likelihood ratio test, based on comparing the likelihood values of the first two panels in Table 7, suggests that the Box-Cox transformation does yield significant improvement. In the multinomial logit case, in which we have also allowed for correlation between v and the u<sub>j</sub>'s, the estimate differs significantly from 0 at the 10 per cent level, but the standard error is quite large. Moreover, the presence of the Box-Cox transformation makes estimating  $\gamma_1$  and  $\gamma_2$  much harder. The standard errors increase and significance levels drop strongly. Estimates of the correlation structure (i.e.,  $\mu_1$  and  $\mu_2$ ) are substantially affected. However, the parameter estimates for the other regressors in the selection equation are not much changed.

	Prot Σ diag		and the second	Probit Σ diagonal		MNL Σ free	
	parameter	std error	parameter	std error	parameter	std error	
Employment v.	s. Non-participa	tion					
constant	7.0599	2.1930	8.2346	2.2557	13.3875	5.0081	
log age	-2.0777	0.4846	-2.2392	0.5149	-4.0000	1.1003	
log fam siz	-0.3144	0.2879	-0.2449	0.2831	-0.2565	0.6241	
reg unemprt	-4.8511	4.6312	-3.5653	4.7360	-5.2794	10.0095	
log inc hus	-0.0401	0.0674	-0.0546	0.0754	-0.0928	0.1895	
log farmsiz	-0.1572	0.1505	-0.0960	0.1500	-0.2990	0.3305	
dum cattle					1.0798	0.5465	
dum soil 1					0.6218	0.6101	
dum soil 3					-0.2463	1.1627	
dum debt os	-0.5889	1.2734	-0.3406	1.3828	-2.5753	3.6584	
log debt os	0.1299	0.1436	0.0982	0.1579	0.4092	0.4203	
log wage rt	1.0197	0.2257	0.0013	0.0060	0.3851	0.5123	
μ					0.6885	1.2741	
Relative Assist	ting vs. Non-part	ticipation					
constant	-0.8589	1.9324	-1.2786	1.8461	1.9188	5.1076	
log age	0.2010	0.4054	0.2321	0.4034	-0.7436	1.0961	
log fam siz	0.5574	0.1901	0.5316	0.1881	1.1374	0.5167	
reg unemprt	-7.5412	2.8189	-7.3607	2.7497	-21.3859	8.8599	
log inc hus	0.0828	0.0386	0.0846	0.0396	0.2001	0.1123	
log farmsiz	0.1819	0.1068	0.1854	0.1072	0.5172	0.3105	
dum cattle					0.3856	0.3976	
dum soil 1					0.8342	0.4498	
dum soil 3					1.4064	0.6841	
dum debt os	-1.5083	0.7288	-1.5796	0.7475	-5.0084	1.9879	
log debt os	0.1911	0.0826	0.2020	0.0852	0.6574	0.2396	
log wage rt	-0.3467	0.3032	-0.0014	0.0056	-0.0932	0.2216	
μ <sub>2</sub>					5.1312	1.8794	
Box-Cox para	meter		3.6759	2.3650	1.2906	0.7545	
log likelihood:	d: -316.13		-308.89		-295.38		

 Table 7:
 Simulated Maximum Likelihood (R=25) Estimation of Linear and Non-Linear Models

## **4.2 Evaluation of results**

In order to get some insight in the implications of the parameter estimates for the wage rate sensitivity of the choice between non-participation, formal employment, and relative assisting, we computed the estimated probabilities of the three states as a function of the wage rate, for someone whose other (own, husband's, household's and farm characteristics) are equal to the average in the sample. The results for eight sets of parameter estimates are presented in Figure 1.

In general, the probability of formal employment increases with the wage, whereas the probability of relative assisting decreases with the wage. This corresponds to the estimated wage parameter in the employment equation. Note that a positive wage rate coefficient in the employment vs non- participation equation also implies a negative effect of potential wages on the probability of relative assisting. This effect may dominate the (often small and insignificant) wage effect through the relative assisting vs non- participation equation.

Although the direction of the effect is the same in all models, its magnitude varies a lot. For the basic model with diagonal covariance matrix, simulated ML and ML yield very similar results. This appears to be the case even for smaller values of R than the one (R=50) depicted. The two step estimates however suggest a much larger sensitivity. The graph for the SML estimates of the multinomial logit model with exogenous wage rates is again quite similar to the ML or SML basic model results.

The model extensions which allow for wage rate endogeneity or non-linearity through a Box-Cox transformation, yield quite different patterns, suggesting a larger wage rate sensitivity estimates. In calculating the probabilities for these simultaneous models, the correlation between the errors has been ignored. This may explain part of the differences.

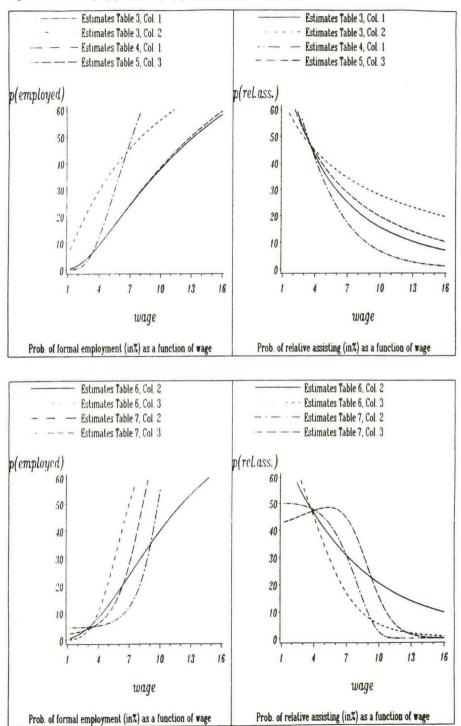


Figure 1: Sensitivity of probability of participation to wage rate

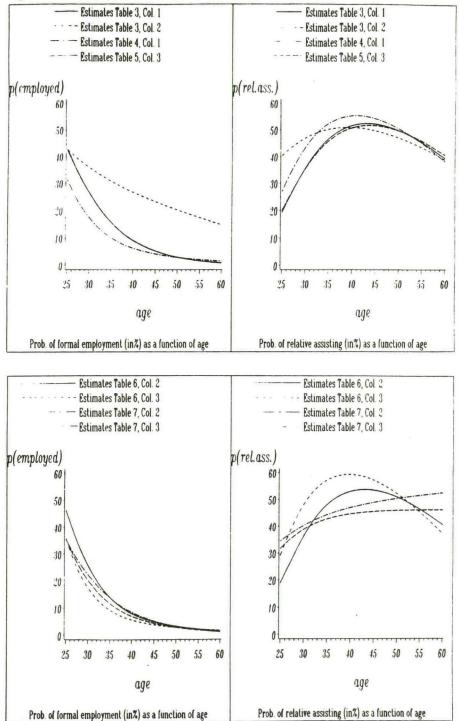


Figure 2: Sensitivity of probability of participation to age

In Figure 2, similar graphs are drawn as a function of age, for a fixed value of the wage rate (£2.95 per hour). The probability of formal employment decreases with age, whereas the probability of relative assisting is increasing at most ages, and, according to most of the results, decreasing at higher ages. The differences between the various graphs tend to be somewhat smaller than in Figure 1. In particular, the ML and SML results for the basic model are again quite similar.

Figures 1 and 2 are based on point estimates of the relevant parameters, and do not reveal the uncertainty due to the fact that parameters are replaced by their estimates. Therefore, we have also computed some asymptotic confidence intervals for wage rate elasticities. These elasticities are intricate nonlinear functions of the estimated parameters. Therefore, instead of using the delta method, we have used simulations to obtain the confidence intervals, as in Van Soest (1992). This boils down to drawing from the estimated asymptotic distribution of the parameter estimator, and look at the distribution of resulting elasticities. This method avoids the need to take derivatives and works well as long as the elasticities are differentiable functions of the parameters.

		Wage rate = Ir£10						
		_	Decile ci	ut-offs			Decile c	ut-offs
	Median	Mean	10th	90th	Median	Mean	10th	90th
Result	s in table 3,	col. 1:						
NP	0.285	0.197	-0.437	0.668	-0.924	-1.067	-2.288	-0.171
E	2.845	2.908	2.051	3.813	2.437	2.513	1.830	3.387
RA	-1.692	-1.688	-2.744	-0.556	-4.035	-4.091	-6.875	-1.382
Result	s in table 3,	col. 2:						
NP	-0.608	-0.627	-1.595	0.443	-1.531	-1.700	-3.588	0.080
E	1.239	1.241	0.801	1.589	1.178	1.163	0.830	1.543
RA	-0.739	-0.764	-1.216	-0.339	-1.542	-1.643	-2.570	-0.881
Result	s in table 4,	col. 1:						
NP	-0.607	-0.536	-1.777	0.530	-4.537	-5.169	-8.840	-1.545
E	4.420	4.433	2.755	6.156	2.072	2.304	1.058	3.700
RA	-2.276	-2.538	-4.145	-0.957	-7.653	-8.096	-13.404	-3.338
Result	s in table 5,	col. 3:						
NP	0.089	0.063	-0.611	0.672	-0.957	-1.183	-2.763	-0.023
E	2.954	2.982	1.964	4.114	2.554	2.632	1.593	3.717
RA	-1.331	-1.397	-2.552	-0.502	-3.050	-3.337	-6.351	-1.136
	s in table 6,							
NP	0.148	0.021	-0.812	0.666	-1.092	-1.374	-3.236	0.095
E	2.901	2.957	2.029	4.054	2.909	2.833	1.408	4.229
RA	-1.214	-1.318	-2.453	-0.352	-3.247	-3.314	-5.473	-1.321
	s in table 6,		2.155	0.002	5.2 11	0.011	5.115	1.021
NP	-0.365	-0.419	-1.540	0.512	-5.229	-5.473	-8.774	-2.775
E	-0.363	4.822	3.494	6.177	1.999	2.171	1.041	3.650
RA	-2.211	-2.307	-3.627	-1.328	-8.035	-8.363	-11.611	-5.142
	s in table 7,		-5.027	-120	0.0.0	0.50.7	11.011	
NP	0.164	0.278	0.003	0.802	0.003	-2.804	-12.717	0.593
E	0.164	0.278	0.005	1.950	4.642	-3.069	0.026	9.682
RA	-0.238	-0.417	-1.170	-0.004	-2.670	-93.736	-96.675	-0.007
	s in table 7,		-1.170	-0.004	-2.070	23.150	70.015	-0.007
	and a second second		4 202	0 400	12 050	20.240	56 510	1 257
NP	-0.725	-1.355	-4.303	0.498	-13.858	-20.249	-56.512	-1.257
E	3.954	3.023	-3.433	6.258	2.460 -12.783	-2.169	-28.467	6.107
RA	-0.739	-0.880	-2.843	1.066	-12.783	-14.181	-30.490	0.059

Table 8: Wage Rate Elasticities

Notes: NP: non-participation, E: formal employment, RA: relative assisting.

The results in Table 8 are all based on 100 draws. Of the 100 resulting elasticities, we present the median, the mean, and the first and ninth decile. In some cases, the drawn parameter values are such that the probability of a certain state becomes very small. In that case the (absolute) value of the elasticity can be extremely large. To reduce the impact of this type of outliers, it seems better to look at the median than at the mean. The latter two can be interpreted as an approximate 80% two-sided confidence interval. We computed elasticities at two levels of the wage rate, Ir£5 and Ir£10. Our calculations are based on the same sets of estimates as those used in Figure 1.

Parameter estimates for the non-linear models seem to be quite inaccurate, and elasticities vary wildly. One of the reasons is that estimates of state probabilities are sometimes quite small. The number of observations is probably too small to let the asymptotics work well. Using bootstrapping might be an alternative.

For the other models, results seem more reliable. Again, SML and ML based results for the basic model are quite similar, and similar to the basic multinomial logit results with exogenous wage rates. The wage rate elasticity of formal employment is significantly positive (at the one sided 10% level), and may take on values between 1.5 and 4. The wage rate elasticity of relative assisting is significantly negative, but the confidence intervals are quite large. The sign of the wage elasticity of non-participating is not unambiguously determined.

## 5. Conclusions

While Census and Labour Force Survey data suggest that the numbers of relatives assisting on family farms have declined to very low levels, more detailed sectoral investigations suggest otherwise. Evidence from the ESRI survey confirms that the status of relative assisting on family farms is indeed a numerically important one. Particular attention may need to be given to this area in the annual Labour Force Survey. Econometric analysis of farm wives' labour supply found certain similarities to that of other married women. The wage determination process seemed to be similar; and those who could command high wages were more likely to be found in employment. The factors influencing the choice between non-participation and participation as a relative assisting were more difficult to identify: the small sample size does not help. But physical characteristics such as farm size and soil type seemed to have a role, together with economic considerations such as the level of debt outstanding. As regards participation in the paid labour market, however, it is clear that the role of wages is central.

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# Appendix A: Variable descriptions

log AGE	log of (woman's age at last birthday)
log 2 AGE	square of log AGE
YOUNG 0_4	dummy: =1 when woman has a child aged less than 4
FAM SIZ	family size = 2 + number of dependant children, as defined by
	conditions for receipt of child benefit
REG UNEMPRT	regional unemployment rate
log INC HUS	log of (husband's off-farm employment income (£/week) +1)
	Note: Income from farming is not included, because it is impossible
	to separate the return to husbands and wives when both are working
	on the farm.
FARMSIZ	farm size in acres
dum CATTLE	dummy: =1 when farm system is cattle
dum SOIL 3	dummy: =1 when soil type = 3 (least fertile)
dum SOIL 1	dummy: =1 when soil type = 1 (most fertile)
dum DEBT OS	dummy: =1 when farm debt outstanding is positive
log DEBT OS	log of (amount of debt outstanding +1)
log WAGE RT	log of (gross hourly wage rate)

	Non-participants		Employ	Employees		ssisting
	Mean	Std dev	Mean	Std dev	Mean	Std dev
AGE	48.7	9.8	39.6	9.8	46.7	9.3
YOUNG 0_4	0.20	0.40	0.34	0.48	0.25	0.43
FAM SIZ	1.57	1.66	2.07	1.89	2.23	1.91
<b>REG UE RT</b>	16.6	2.81	15.7	2.69	15.8	2.44
INC HUS	22.95	59.58	22.63	81.98	39.8	98.17
FARMSIZ	61.3	46.1	71.9	51.6	65.3	44.2
dum SOIL 1	0.27	0.44	0.41	0.50	0.36	0.48
dum SOIL 3	0.14	0.35	0.09	0.29	0.18	0.39
dum DEBT OS	0.20	0.40	0.48	0.51	0.27	0.45
<b>DEBT OS*</b>	8092	12299	14068	13894	14392	18369
WAGE RT	-	-	6.66	4.24	-	-

# **Appendix B: Sample characteristics**

\* statistics for those with positive debt

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