

**A CHARACTERIZATION OF THE
EXTENDED CLAIM-EGALITARIAN SOLUTION***

M^a Carmen Marco**

WP-AD 93-03

* Thanks are due to C. Herrero for helpful comments. Any mistakes are my exclusive responsibility.

** Universidad de Alicante.

Editor: **Instituto Valenciano de
Investigaciones Económicas, S.A.**
Primera Edición Mayo 1993.
ISBN: 84-482-0178-7
Depósito Legal: V-1520-1993
Impreso por KEY, S.A., Valencia.
Cardenal Benlloch, 69, 46021-Valencia.
Impreso en España.

**A CHARACTERIZATION OF THE
EXTENDED CLAIM-EGALITARIAN SOLUTION**

M^a Carmen Marco Gil

A B S T R A C T

Some monotonicity conditions for bargaining problems with claims are presented. They are used in providing a characterization of the extended claim-egalitarian solution.

1.- INTRODUCTION

Bargaining problems with claims have been introduced in a recent paper by Chun and Thomson (1992). They propose a generalization of Nash's (1950) bargaining model by adding a third element to the disagreement point and the feasible set, namely, a point representing the claims of the agents, (also in terms of utilities). In this setting, a solution specifies exactly one feasible outcome for each triple of feasible set, disagreement point and claims point. As is usual in axiomatic bargaining theory, the traditional way of defending a solution concept relies on the properties satisfied by this solution, from a normative point of view.

We concentrate on the application of the so-called "equal-loss principle"⁽¹⁾ to the framework of bargaining with claims. In this way, a first solution concept arises in a natural way, namely, the *claim-egalitarian solution*, by equalizing losses from the claims point for all agents [see Bossert (1992a)]. This solution is the counterpart of the *equal-loss solution* in the classical bargaining problem [see Chun (1988)], which equalizes losses from the ideal point. In the same way as the equal-loss solution itself may fail to be individually rational for more than two agents, the claim-egalitarian solution may also present lack of

¹ The consideration of equal losses in utility from the ideal point gave rise to several bargaining solutions in the classical framework [see Yu (1973), Freimer and Yu (1976), Chun (1988), Chun and Peters (1991) and Herrero and Marco (1992a, 1992b)].

individual rationality. In consequence, it is natural to also consider the individually rational extension of the claim-egalitarian solution, namely, the *extended claim-egalitarian solution*, [see Bossert (1992a)], which turns out to be the counterpart of the *rational equal-loss solution* in the classical bargaining framework [see Herrero & Marco (1993)]. In Bossert (1992a), the behaviour of both the claim-egalitarian and the extended claim-egalitarian solutions, with respect to some monotonicity requirements is analyzed. Moreover, the existence of a characterization result in an unpublished paper [Bossert (1992b)], is mentioned.

In the present paper we formulate axioms specifying how the solution outcome should respond to certain changes, both in the feasible set and in the claims point. These axioms are different from those presented in Bossert (1992a). Moreover, by means of these requirements, together with some standard conditions, we provide an alternative characterization of the extended claim-egalitarian solution.

2.- PRELIMINARIES

A bargaining problem with claims is a triplet (S,d,c) , where $S \subseteq \mathbb{R}^n$, $d \in S$, and $c \in \mathbb{R}^n \setminus S$. \mathbb{R}^n is the utility space, S the feasible set, d the disagreement point and c the claims point. The agents could achieve any point in S if they agree on it unanimously, otherwise they will end up at d .

Let Σ^n the class of n -personal bargaining problems with claims (S,d,c) such that:

- (i) S is convex, closed and comprehensive⁽²⁾
- (ii) $\exists p \in \mathbb{R}_{++}^n, r \in \mathbb{R}$ such that $\forall x \in S, px \leq r$
- (iii) $\exists x \in S$ with $x \gg d$
- (iv) $c \notin S, c > d$

Sometimes, it is also required that c be weakly dominated by the ideal point of (S,d) [see Chun and Thomson (1992)]. The class we consider here coincides with that which appears in Bossert (1992a).

For any $(S,d,c) \in \Sigma^n$, we use $IR(S,d)$ to denote the set of individually rational points, that is, $IR(S,d) = \{x \in S \mid x \geq d\}$. $PO(S)$ will denote the set of Pareto optimal outcomes, and $WPO(S)$ the set of weakly

² $S \subseteq \mathbb{R}^n$ is comprehensive if, for all $x \in S$ and all $y \in \mathbb{R}^n$, $y < x$ implies $y \in S$. Notation for vector inequalities is $\geq, >, \gg$.

Pareto optimal outcomes, that is, $PO(S) = \{ x \in S \mid \text{if } y \geq x \Rightarrow y \notin S \}$ and $WPO(S) = \{ x \in S \mid \text{if } y \gg x \Rightarrow y \notin S \}$.

A solution on Σ^n is a function $F: \Sigma^n \longrightarrow \mathbb{R}^n$ such that $F(S,d,c) \in S$ for all $(S,d,c) \in \Sigma^n$.

Bossert (1992a) introduces the equal-loss principle for bargaining problems with claims, by means of two solution concepts, namely, the claim-egalitarian and the extended-claim egalitarian solutions.

Definition 1 [Bossert (1992a)]: For all $(S,d,c) \in \Sigma^n$, the claim-egalitarian solution, $E(S,d,c)$ is the weakly Pareto Optimal point in S such that $|c_i - y_i| = |c_j - y_j| \forall i, j \in N$.

Definition 2⁽³⁾: For all $(S,d,c) \in \Sigma^n$, the extended claim-egalitarian solution, $E^*(S,d,c)$ chooses the alternative:

$$E_i^*(S,d,c) = \begin{cases} d_i & \text{if } E_i(\bar{S},d,c) < d_i \\ E_i(\bar{S},d,c) & \text{if } E_i(\bar{S},d,c) \geq d_i \end{cases}$$

where \bar{S} stands for the comprehensive hull of the set $IR(S,d)$.

³ It is easy to check that this definition is equivalent to that appearing in Bossert (1992a).

The interpretation of the extended claim-egalitarian solution is the following: the agents' losses are equal with respect to their claims if doing this represents an agreement which is acceptable to all individuals. If it does not, it is because there are some agents that, at the claim-egalitarian solution are worse off than at the disagreement point. In this event, we will accept smaller losses for these agents, keeping them at their level of disagreement, and we will only level off losses with relation to the rest of the agents' claims. In this way, a compromise between the equal-loss principle and the possibility of agreement among the agents is found.

3.- CHARACTERIZATION OF E^* .

Consider the following axioms for bargaining problems with claims:

(WPO) *Weak Pareto Optimality*: $\forall (S,d,c) \in \Sigma^n, F(S,d,c) \in WPO(S)$.

(AN) *Anonymity*: $\forall (S,d,c) \in \Sigma^n$, and for all permutations $\pi: \{1, \dots, n\} \rightarrow \{1, \dots, n\}$ $F(\pi(S), \pi(d), \pi(c)) = \pi(F(S,d,c))$.

(T.INV) *Translation Invariance*: $\forall (S,d,c) \in \Sigma^n, \forall t \in \mathbb{R}^n$,
 $F(S+t, d+t, c+t) = F(S,d,c) + t$.

(CONT) *Continuity*: \forall sequences $\{(S^v, d^v, c^v)\}$ of elements of $\Sigma^n, \forall (S,d,c) \in \Sigma^n$, si S^v converges to S in the Hausdorff topology, $d^v = d$ y $c^v = c \forall v$, thus $F(S^v, d^v, c^v)$ converges to $F(S,d,c)$.

(B.D.D) *Boundedness*: $\forall (S,d,c) \in \Sigma^n, d \leq F(S,d,c) \leq c$

(ST.MON) *Strong Monotonicity*: $\forall (S,d,c), (S',d',c') \in \Sigma^n$, such that $S' \subset S$, $c' = c$, then $F(S',d',c') \leq F(S,d,c)$.

(R.ST.MON) *Rational Strong Monotonicity*: $\forall (S,d,c), (S',d',c') \in \Sigma^n$, such that $S' \subseteq S$, $d \leq d'$ and $c=c'$, if $F(S,d,c) \geq d'$, then $F(S',d',c') \leq F(S,d,c)$.

(ST-c-MON) *Strong c-Monotonicity*: $\forall (S,d,c), (S',d',c') \in \Sigma^n$, for all $i \in N$, if $S = S'$, $d = d'$, $c'_i > c_i$, and $c'_j = c_j \quad \forall j \neq i$, then $F_i(S',d',c') \geq F_i(S,d,c)$ and $F_j(S',d',c') \leq F_j(S,d,c)$.

(C.MON) *Claims Point Monotonicity*: $\forall (S,d,c), (S',d',c') \in \Sigma^n$, such that $S=S'$, $d=d'$ and $c_j=c'_j \quad \forall j \neq i$, $c_i \geq c'_i$, then $F_i(S,d,c) \geq F_i(S',d',c')$.

WPO requires that there be no feasible alternative at which all agents are better off than they are at the solution outcome. AN says that the names of the agents do not affect the solution outcome. T.INV requires the choice of origin of the utility functions to be irrelevant. CONT implies that small variations in the opportunity set, with changes neither in the disagreement point nor in the claims point, cause small variations in the solution. B.D.D. requires that no agent may be worse off at the solution outcome than at the disagreement point, and also, that no agent may enjoy more utility at the solution outcome than that utility corresponding to her/his claim. WPO, AN, T.INV, CONT and B.D.D. are borrowed from Chun & Thomson (1992).

ST.MON means that, given an increase in the feasible set without any changes in the claims, no agent loses. This axiom is an adaptation of the property "*Strong Monotonicity other than the ideal point*" [introduced by Chun (1988) for the classical bargaining problem] to one of bargaining with claims. R.ST.MON says that if the set of agreements acceptable to all agents shifts, and if the agents' claims remain unchanged, nobody will benefit, unless the new disagreement point represents an improvement for

some individual as far as the solution to the initial problem is concerned. This axiom may be considered as a weak version of ST.MON.

ST-c-MON was introduced by Bossert (1992a). C.MON is a weakening of the axiom ST.c-MON. Our version requires that an increase in the utility level to which the agent has a claim should not damage him as long as the rest of the claims, the feasible set and the disagreement point remain fixed. This condition is an adaptation of the property "*Ideal Point Monotonicity*" [introduced by Chun (1988)], to one of bargaining with claims.

The next lemmata are used in our main result (Theorem 1):

Lemma 1: The extended claim-egalitarian solution satisfies rational strong monotonicity.

Proof: Let $(S,d,c), (S',d',c') \in \Sigma^n$ such that $S' \subseteq S$, $d \leq d'[1]$, $c = c'$ and $E^*(S,d,c) \geq d'$ [2].

Let $\bar{S} = \text{Com}[\text{IR}(S,d)]$, $\bar{S}' = \text{Com}[\text{IR}(S',d')]$, thus, considering $S' \subseteq S$ and inequality [1], we have $\bar{S}' \subseteq \bar{S}$. Bearing in mind that the claim-egalitarian solution E verifies strong Monotonicity (see Chun (1988)), we can apply this property to the pair $(\bar{S},d,c) (\bar{S}',d',c')$, concluding that

$$E(\bar{S}',d',c') \leq EL(\bar{S},d,c) \quad [3]$$

Let us analyze two possible cases:

(i) If $E_i(\bar{S}, d, c) \geq d_i \forall i \in N$, then $E_i^*(S, d, c) = E_i(\bar{S}, d, c) \forall i \in N$.

Furthermore,

$$E_i^*(S', d', c') = \begin{cases} E_i(\bar{S}', d', c') \leq E_i(\bar{S}, d, c) = E_i^*(S, d, c), \text{ by [3]} \\ d'_i \leq E_i^*(S, d, c), \text{ by [2]} \end{cases}$$

(ii) If $\exists i \in N$ such that $E_i(\bar{S}, d, c) \geq d_i$ and $j \in N$ such that $E_j(\bar{S}, d, c) < d_j$. Let $Q = \{ i \in N \mid E_i(\bar{S}, d, c) \geq d_i \}$. Then $\forall i \in Q$ we can obtain $E_i^*(S', d', c') \leq E_i^*(S, d, c)$ by reasoning in the same way as in (i) for $Q \subset N$. $\forall j \in N \setminus Q$, we will have $E_j(\bar{S}, d, c) < d_j$, and $E_j^*(S, d, c) = d_j$. Considering [1] and [2] we obtain $d'_j = d_j \forall j \in N \setminus Q$, and bearing in mind [3], we get $E_j(\bar{S}', d', c') < d_j = d'_j$. Therefore, $E_j^*(S', d', c') = d'_j = d_j$. ■

As a direct consequence of Theorem 2 in Bossert (1992a), we get:

Lemma 2: The extended claim-egalitarian solution satisfies claims point monotonicity.

Now we can present our main result:

Theorem 1: The extended claim-egalitarian solution is the only one in Σ^n satisfying Weak Pareto Optimality, Anonymity, Translation Invariance, Boundedness, Rational Strong Monotonicity, Claims Point Monotonicity, and Continuity.

Proof: Obviously, E^* satisfies WPO, AN, T.INV, B.D.D. and CONT. Furthermore, it verifies ST.R.MON and C.MON (Lemmas 1 and 2). In order to prove uniqueness let F be a solution that verifies all the axioms, and consider a problem $(S,d,c) \in \sum^n$ such that $WPO(S)=PO(S)$.

We will distinguish between two cases:

(i) If $E(S,d,c) \in IR(S,d)$, because of T.INV we can assume $c=(1,\dots,1)$. Let $E^*(S,d,c)=x$, $S^1 = \text{Com}\{x\}^{(4)}$, $d^1 \leq d / d_i^1 = d_j^1 \forall i,j$. By WPO and SY we will have $F(S^1,d^1,c) = x$. Given that F verifies B.D.D, we can apply ST.R.MON twice to the pairs $(S^1,d^1,c),(S,d^1,c)$ and $(S,d^1,c),(S,d,c)$ in order to conclude $F(S,d,c)=x$.

(ii) If $E(S,d,c) \notin IR(S,d)$ we will apply mathematical induction. We will use Q to denote $\{i \in N / E_i(S,d) \geq d_i\}$

(ii)-(a) Let $P = N/Q = \{j\}$.

If $n=2$, we assume $j=2$ by AN. We now take $c_1=1$ by T.INV, we then have $E^*(S,d,c) = (x_1,d_2)$. Once again by T.INV we assume that $d_2 = x_1$, so $E^*(S,d,c) = (x_1,x_2) = x$, with $x_1 = x_2$. Let c' such that $c'_1 = c_1$ and $c'_2 = c_1$, so by (i) $F(S,d,c') = x$ and applying B.D.D. and C.MON we will have $F_2(S,d,c) = x_2$ and now, by WPO $F_1(S,d,c) = x_1 \Rightarrow F(S,d,c) = x$.

⁴ Com (A) stands for the comprehensive hull of set A. CoCom (A) stands for the Convex and comprehensive hull of set A.

If $n \geq 3$, we assume that $j=n$ by AN. We now take $c_i = 1 \forall i \neq n$ by T.INV, so $E^*(S,d,c) = (x_1, x_2, \dots, x_{n-1}, d_n)$ with $x_1 = x_2 = \dots = x_{n-1}$. Once again by T.INV we assume $d_n = x_1$, thus $E^*(S,d,c) = (x_1, \dots, x_n) = x$. Let d' so that $d' \leq d$ and $d'_i = d'_k \forall i, k \in Q$, $d'_j = d_j$. Let $c' = (1, \dots, 1)$ and $S' = \text{CoCom} \{ x, (d'_1, d'_2, \dots, d'_{n-1}, a_n(S,d)) \}$. Thus $F(S,d',c') = x$ by (i). Applying C.MON on (S,d',c') and (S,d',c) we will have $F_n(S,d',c) \leq x_n$ and by B.D.D. we get $F_n(S,d',c) = x_n$. By ST.R.MON on the pair (S,d',c) and (S',d',c) we will have that $F(S,d',c) \leq F(S',d',c)$ and by B.D.D, $F_n(S',d',c) = x_n$. Now by AN and WPO on (S',d',c) we conclude that $F_i(S',d',c) = x_i \forall i \in Q \Rightarrow F(S',d',c) = x$. Applying ST.R.MON twice to the pairs $(S',d',c), (S,d',c)$ and $(S,d',c), (S,d,c)$ we get $F(S,d,c) = x$.

(ii)-(b) If $p = \text{cardinal of } P$ is k , we assume that $F(S,d,c) = x$ where $x = \text{EL}^*(S,d,c)$.

(ii)-(c) Let now $p=k+1$. Assume that $j \in P$ $j = 1, 2, \dots, k+1$ by AN. We take $c_i = 1 \forall i \in Q$ by T.INV, so $E^*(S,d,c) = (d_1, d_2, \dots, d_{k+1}, x_{k+2}, \dots, x_n)$ with $x_{k+2} = \dots = x_n$. Once more by T.INV we assume $d_j = x_1 \forall j \in P$, therefore, $E^*(S,d,c) = (x_1, \dots, x_n) = x$. Let d' such that $d' \leq d$, and $d'_i = d'_k \forall i, k \in Q$, $d'_j = d_j \forall j \in P$. Let c^j such that $c_i^j = 1 \forall i \in Q$, $c_j^j = 1$ for $j \in P$ and $c_k^j = c_k$ for $k \neq j$, $k \in P$. Finally, let $S' = \text{CoCom} \{ x, (a_1, d'_{N/(1)}), (d'_1, a_2, d'_{N/(1,2)}), \dots, (d'_1, \dots, d'_k, a_{k+1}, d'_Q) \}$. Thus, by way of the induction hypothesis [(ii)-(b)], we can conclude that $F(S,d',c^j) = x \forall j = 1, \dots, k+1$. We now take the pairs $(S,d',c^j) (S,d',c) \forall j \in P$ and by applying C.MON and B.D.D

we will have $F_j(S, d', c) = d_j = x_j \quad \forall j \in P$. By ST.R.MON on (S, d', c) and (S', d', c) , $F(S', d', c) \leq F(S, d', c)$ and, again, by B.D.D, $F_j(S', d', c) = x_j \quad \forall j \in P$. Now, by AN and WPO on (S', d', c) , $F_i(S', d', c) = x_i \quad \forall i \in Q \Rightarrow F(S', d', c) = x$. By applying ST.R.MON twice to pairs $(S', d', c), (S, d', c)$ and $(S, d', c), (S, d, c)$ we conclude that $F(S, d, c) = x$.

Finally, for an arbitrary element of Σ^n , we apply CONT. ■

REFERENCES

- W. Bossert (1992a) "Monotonic Solutions for Bargaining Problems with Claims". *Economics Letters* 39, 395-399.
- W. Bossert (1992b) "An Alternative solution to Bargaining Problems with Claims". *Mathematical Social Sciences* (forthcoming)
- Y. Chun (1988) "The Equal-Loss Principle for Bargaining Problems". *Economics Letters* 26, 103-106.
- Y. Chun & H. Peters (1991) "The Lexicographic Equal-Loss Solution" . *Mathematical Social Sciences* 22, 151-161.
- Y. Chun & W.Thomson (1992) "Bargaining Problems with Claims". *Mathematical Social Sciences* 24, 19-33.
- M. Freimer & P.L. Yu (1976) "Some New Results on Compromise Solutions for Group Decision Problems" . *Management Science* 22, 6, 936-946.
- C. Herrero & M.C. Marco (1992a) "A Note on the Equal-Loss Principle for Bargaining Problems" . A Discusión, WP-AD-92-02.
- C. Herrero & M.C. Marco (1992b) "Rational Equal-Loss Solutions for Bargaining Problems" . *Mathematical Social Sciences* (forthcoming).
- J.F. Nash (1950) "The Bargaining Problem". *Econometrica* 18, 155-162.
- P.L. Yu (1973) "A Class of Decisions for Group Decision Problems". *Management Science* 19, 18, 688-693.

PUBLISHED ISSUES

FIRST PERIOD

- 1 "A Metatheorem on the Uniqueness of a Solution"
T. Fujimoto, C. Herrero. 1984.
- 2 "Comparing Solution of Equation Systems Involving Semipositive Operators"
T. Fujimoto, C. Herrero, A. Villar. February 1985.
- 3 "Static and Dynamic Implementation of Lindahl Equilibrium"
F. Vega-Redondo. December 1984.
- 4 "Efficiency and Non-linear Pricing in Nonconvex Environments with Externalities"
F. Vega-Redondo. December 1984.
- 5 "A Locally Stable Auctioneer Mechanism with Implications for the Stability of General Equilibrium Concepts"
F. Vega-Redondo. February 1985.
- 6 "Quantity Constraints as a Potential Source of Market Inestability: A General Model of Market Dynamics"
F. Vega-Redondo. March 1985.
- 7 "Increasing Returns to Scale and External Economies in Input-Output Analysis"
T. Fujimoto, A. Villar. 1985.
- 8 "Irregular Leontief-Straffa Systems and Price-Vector Behaviour"
I. Jimenez-Raneda / J.A. Silva. 1985.
- 9 "Equivalence Between Solvability and Strictly Semimonotonicity for Some Systems Involving Z-Functions"
C. Herrero, J.A. Silva. 1985.
- 10 "Equilibrium in a Non-Linear Leontief Model"
C. Herrero, A. Villar. 1985.
- 11 "Models of Unemployment, Persistent, Fair and Efficient Schemes for its Rationing"
F. Vega-Redondo. 1986.
- 12 "Non-Linear Models without the Monotonicity of Input Functions"
T. Fujimoto, A. Villar. 1986.
- 13 "The Perron-Frobenius Theorem for Set Valued Mappings"
T. Fujimoto, C. Herrero. 1986.
- 14 "The Consumption of Food in Time: Hall's Life Cycle Permanent Income Assumptions and Other Models"
F. Antoñazas. 1986.
- 15 "General Leontief Models in Abstract Spaces"
T. Fujimoto, C. Herrero, A. Villar. 1986.

- 16 "Equivalent Conditions on Solvability for Non-Linear Leontief Systems"
J.A. Silva. 1986.
- 17 "A Weak Generalization of the Frobenius Theorem"
J.A. Silva. 1986
- 18 "On the Fair Distribution of a Cake in Presence of Externalities"
A. Villar. 1987.
- 19 "Reasonable Conjectures and the Kinked Demand Curve"
L.C. Corchón. 1987.
- 20 "A Proof of the Frobenius Theorem by Using Game Theory"
B. Subiza. 1987.
- 21 "On Distributing a Bundle of Goods Fairly"
A. Villar. 1987.
- 22 "On the Solvability of Complementarity Problems Involving Vo-Mappings and its Applications to Some Economic Models"
C. Herrero, A. Villar. 1987.
- 23 "Semipositive Inverse Matrices"
J.E. Peris. 1987.
- 24 "Complementary Problems and Economic Analysis: Three Applications"
C. Herrero, A. Villar. 1987.
- 25 "On the Solvability of Joint-Production Leontief Models"
J.E. Peris, A. Villar. 1987.
- 26 "A Characterization of Weak-Monotone Matrices"
J.E. Peris, B. Subiza. 1988.
- 27 "Intertemporal Rules with Variable Speed of Adjustment: An Application to U.K. Manufacturing Employment"
M. Burgess, J. Dolado. 1988.
- 28 "Orthogonality Test with De-Trended Data's Interpreting Monte Carlo Results using Nager Expansions"
A. Banerjee, J. Dolado, J.W. Galbraith. 1988.
- 29 "On Lindahl Equilibria and Incentive Compatibility"
L.C. Corchón. 1988.
- 30 "Exploiting some Properties of Continuous Mappings: Lindahl Equilibria and Welfare Egalitaria Allocations in Presence of Externalities"
C. Herrero, A. Villar. 1988.
- 31 "Smoothness of Policy Function in Growth Models with Recursive Preferences"
A.M. Gallego. 1990.
- 32 "On Natural Selection in Oligopolistic Markets"
L.C. Corchón. 1990.

- 33 "Consequences of the Manipulation of Lindahl Correspondence: An Example"
C. Bevía, J.V. LLinares, V. Romero, T. Rubio. 1990.
- 34 "Egalitarian Allocations in the Presence of Consumption Externalities"
C. Herrero, A. Villar. 1990.

SECOND PERIOD

- WP-AD 90-01 "Vector Mappings with Diagonal Images"
C. Herrero, A. Villar. December 1990.
- WP-AD 90-02 "Langrangean Conditions for General Optimization Problems with Applications to Consumer Problems"
J.M. Gutierrez, C. Herrero. December 1990.
- WP-AD 90-03 "Doubly Implementing the Ratio Correspondence with a 'Natural' Mechanism"
L.C. Corchón, S. Wilkie. December 1990.
- WP-AD 90-04 "Monopoly Experimentation"
L. Samuelson, L.S. Mirman, A. Urbano. December 1990.
- WP-AD 90-05 "Monopolistic Competition : Equilibrium and Optimality"
L.C. Corchón. December 1990.
- WP-AD 91-01 "A Characterization of Acyclic Preferences on Countable Sets"
C. Herrero, B. Subiza. May 1991.
- WP-AD 91-02 "First-Best, Second-Best and Principal-Agent Problems"
J. Lopez-Cuñat, J.A. Silva. May 1991.
- WP-AD 91-03 "Market Equilibrium with Nonconvex Technologies"
A. Villar. May 1991.
- WP-AD 91-04 "A Note on Tax Evasion"
L.C. Corchón. June 1991.
- WP-AD 91-05 "Oligopolistic Competition Among Groups"
L.C. Corchón. June 1991.
- WP-AD 91-06 "Mixed Pricing in Oligopoly with Consumer Switching Costs"
A.J. Padilla. June 1991.
- WP-AD 91-07 "Duopoly Experimentation: Cournot and Bertrand Competition"
M.D. Alepuz, A. Urbano. December 1991.
- WP-AD 91-08 "Competition and Culture in the Evolution of Economic Behavior: A Simple Example"
F. Vega-Redondo. December 1991.
- WP-AD 91-09 "Fixed Price and Quality Signals"
L.C. Corchón. December 1991.
- WP-AD 91-10 "Technological Change and Market Structure: An Evolutionary Approach"
F. Vega-Redondo. December 1991.

- WP-AD 91-11 "A 'Classical' General Equilibrium Model"
A. Villar. December 1991.
- WP-AD 91-12 "Robust Implementation under Alternative Information Structures"
L.C. Corchón, I. Ortuño. December 1991.
- WP-AD 92-01 "Inspections in Models of Adverse Selection"
I. Ortuño. May 1992.
- WP-AD 92-02 "A Note on the Equal-Loss Principle for Bargaining Problems"
C. Herrero, M.C. Marco. May 1992.
- WP-AD 92-03 "Numerical Representation of Partial Orderings"
C. Herrero, B. Subiza. July 1992.
- WP-AD 92-04 "Differentiability of the Value Function in Stochastic Models"
A.M. Gallego. July 1992.
- WP-AD 92-05 "Individually Rational Equal Loss Principle for Bargaining Problems"
C. Herrero, M.C. Marco. November 1992.
- WP-AD 92-06 "On the Non-Cooperative Foundations of Cooperative Bargaining"
L.C. Corchón, K. Ritzberger. November 1992.
- WP-AD 92-07 "Maximal Elements of Non Necessarily Acyclic Binary Relations"
J.E. Peris, B. Subiza. December 1992.
- WP-AD 92-08 "Non-Bayesian Learning Under Imprecise Perceptions"
F. Vega-Redondo. December 1992.
- WP-AD 92-09 "Distribution of Income and Aggregation of Demand"
F. Marhuenda. December 1992.
- WP-AD 92-10 "Multilevel Evolution in Games"
J. Canals, F. Vega-Redondo. December 1992.
- WP-AD 93-01 "Introspection and Equilibrium Selection in 2x2 Matrix Games"
G. Olcina, A. Urbano. May 1993.
- WP-AD 93-02 "Credible Implementation"
B. Chakravorti, L. Corchón, S. Wilkie. May 1993.
- WP-AD 93-03 "A Characterization of the Extended Claim-Egalitarian Solution"
M.C. Marco. May 1993.