

This PDF is a selection from a published volume from the National Bureau of Economic Research

Volume Title: NBER International Seminar on Macroeconomics 2007

Volume Author/Editor: Richard Clarida and Francesco Giavazzi, organizers

Volume Publisher: University of Chicago Press

ISSN: 1932-8796

Volume URL: <http://www.nber.org/books/clar07-1>

Conference Date: June 15-16, 2007

Publication Date: January 2009

Chapter Title: International Portfolios with Supply, Demand and Redistributive Shocks

Chapter Author: Nicolas Coeurdacier, Robert Kollmann, Philippe Martin

Chapter URL: <http://www.nber.org/chapters/c3009>

Chapter pages in book: (231 - 263)

---

## International Portfolios with Supply, Demand, and Redistributive Shocks

**Nicolas Coeurdacier**, *London Business School and CEPR*

**Robert Kollmann**, *ECARES, Université Libre de Bruxelles, Université Paris XII and CEPR*

**Philippe Martin**, *Université Paris I Panthéon Sorbonne, Paris School of Economics and CEPR*

### 5.1 Introduction

In the past twenty years, international capital flows have increased to unprecedented levels for both bonds and stocks. Gross external financial positions now exceed 100 percent of gross domestic product (GDP) for major industrialized countries, so that variations in exchange rates and asset returns may generate sizable wealth transfers between countries. For industrialized countries, international portfolios are long in foreign currency and short in domestic currency, so that the depreciation of a country's exchange rate generates a net external capital gain, (i.e., a positive wealth transfer from the rest of the world). Strikingly, though, home bias in equity portfolios remains sizable, despite the fact that the most legal and technological impediments to international trade in assets have been eliminated among industrialized countries. Lane and Milesi-Ferretti (2003, 2005, 2006, 2007), Tille (2005), Gourinchas and Rey (2005), and Lane and Shambaugh (2007) have recently documented these facts (see also tables 5A.1 and 5A.2 in the appendix).

The goal of this paper is to explain these facts. For this purpose, a general equilibrium model with two countries (Home and Foreign) and two goods is used. There is international trade in Home and Foreign stocks and bonds. The model assumes *consumption* home bias, in accordance with the fact that the bulk of consumption consists of local goods. Three exogenous disturbances are assumed: shocks to endowments, to the distribution of income between labor and capital (redistributive shocks), and to the relative world demand for Home versus Foreign goods. The relative demand shocks can reflect changes in preferences or in the quality or number of varieties of Home/Foreign goods.

Existing models of portfolio choice are generally unable to explain the international portfolio facts. We argue that one of the main reasons for

this is that the prior literature has focused on supply shocks. When faced with a negative supply shock in the Home country—which triggers a Home real exchange rate appreciation—the optimal portfolio should generate an increase in Home net external financial income, in order to finance an increase in Home net imports and thus stabilize Home consumption. With just supply shocks, the optimal Home portfolio is hence biased towards *Foreign* equity: Foreign equity is a better hedge for Home output shocks than Home equity (the Foreign equity return exceeds the Home equity return when Home output is low). Note also that a model with just supply shocks predicts that a country whose exchange rate appreciates experiences a capital gain on its external assets (i.e., a wealth transfer from the rest of the world); in practice, however, industrialized countries that experience an exchange rate appreciation suffer a capital loss on their external assets.

We show that the introduction of redistributive shocks and of relative demand shocks allows us to generate equity home bias, and external valuation effects (effects of exchange rate and asset price fluctuations on external positions) that are broadly consistent with the empirical evidence. Contrary to most of the related literature, we allow for trade in two bonds, denominated in Home and Foreign goods, respectively. The financial market is (effectively) complete (up to a first-order approximation of the equilibrium condition) when there are just two types of shocks; the market is incomplete with the three simultaneous types of shocks.

Intuitively, a redistributive shock (a shock that increases dividends of domestic firms while reducing domestic labor income) can be hedged by holding stocks of local firms, the home bias observed in the data. We show that, given equity home bias, it is efficient for each agent to go long in foreign currency bonds and short in domestic currency bonds, in order to hedge relative demand shocks. For example, when faced with a negative relative demand shock for Home goods—which worsens Home terms of trade—a bond portfolio that is short in Home good bonds and long in Foreign good bonds generates an external capital gain for the Home household, which allows the Home country to stabilize its consumption by allowing it to increase its imports. The optimal bond portfolio thus produces a wealth transfer toward the country that experiences a depreciation of its real exchange rate, which is in line with actual valuation effects (see previous discussion). We show that a plausibly calibrated model with *simultaneous* supply, demand, and redistributive shocks produces realistic equity and bond positions, and that it captures the external valuation effects observed for industrialized countries.

Interestingly, the assumption here that there are bonds denominated in local and in foreign goods helps to explain *equity* home bias, as terms of trade movements can be hedged by holding bonds. In our model, international risk sharing occurs both through equity and bond holdings.

In the next section, we review the related literature and point to differences with the present analysis. Section 5.3 describes the model setup. Section 5.4 solves for optimal portfolios under complete markets. Section 5.5 considers incomplete markets; we provide closed-form solutions for portfolios under incomplete markets, using the method developed by Devereux and Sutherland (2006) and calibrate our model to analyze its quantitative properties.

## 5.2 Related Literature

Since the well-known paper of French and Poterba (1991) that documented equity home bias, various forms of cross-country heterogeneity among investors have been analyzed in order to explain international portfolio holdings. Indeed, without heterogeneity, all investors would, in equilibrium, hold the same portfolio of worldwide assets, and thus no bias toward local assets would exist (see Lewis (1999) for a survey). In the present paper, we abstract from barriers to international capital movements and assume that any investor can purchase any security without transaction costs. In other words, each investor faces the same investment opportunity set; this is, admittedly, a strong assumption, but our result would be reinforced if we assumed costs of buying foreign securities.<sup>1</sup> However, we assume that consumers have a greater preference for the locally produced good than for the imported good (consumption home bias). Empirically, the bulk of consumption consists of locally produced goods (see Kollmann 2006b). Consumption home bias implies that the (consumption-based) real exchange rate fluctuates in response to supply and demand shocks. A recent literature has discussed possible links between the financial and real home biases; in particular, Obstfeld and Rogoff (2000) have argued that consumption home bias (due to trade costs for goods) can solve the equity home bias puzzle.

Uppal (1993), Coeurdacier (2005), Kollmann (2006a, 2006b) and Obstfeld (2007) study portfolio choice in models with consumption home bias; in those settings, there are just output shocks, and the only traded assets are domestic and foreign stocks. Those models can only generate equity home bias when the substitution elasticity between domestic and imported goods is (roughly speaking) smaller than unity. Intuitively, a

country that receives a negative output shock experiences an improvement of its terms of trade; when the substitution elasticity between local and imported goods is low, then the terms of trade improvement are so strong that the return on local equity rises compared to the return on foreign equity; thus, local equity has a high (relative) return in states of the world in which the country's output is low; this makes holding local equity attractive, and induces investors to mainly invest their wealth in local stocks. By contrast, when the substitution elasticity exceeds unity, then the relative return on local equity drops when local output falls, and hence foreign equity is a better hedge for output fluctuations. Hence, a model with just supply shocks only generates equity home bias under the condition that a negative local output shock *raises* the relative return on local equity. Essentially, in such a model, equity home bias only arises when a country's relative equity return is highly positively correlated with its terms of trade (and, hence, with its real exchange rate). Yet empirically, the correlation between relative equity returns and real exchange rate changes is close to zero (see van Wincoop and Warnock 2006). Our model here reproduces this low correlation, yet it also generates realistic equity home bias. This is due to the fact that (as mentioned previously) our model assumes trade in stocks and in two *bonds*, denominated in the home and the foreign goods, respectively.<sup>2</sup> In our setting, bonds are essentially used to hedge real exchange rate risk, a feature that we view as realistic. Moreover, we assume relative demand shocks and redistributive shocks, in addition to the more standard supply shocks. Those new shocks break the close link between terms of trade movements and relative equity returns.

Another strand of literature related to our paper analyzes the impact of nontradable labor income on equity home bias. According to this literature, the presence of labor income either worsens the home bias in equities puzzle (Brainard and Tobin 1991; Baxter and Jermann 1997) or helps explain it (Bottazzi, Pesenti, and van Wincoop 1996; Julliard 2002 and 2004; Engel and Matsumoto 2006). In the models discussed by these authors, the composition of equity portfolios hinges on the correlation between equity returns and wages; as households seek to hedge their human capital risk, they only hold local equity if local stock returns are negatively correlated with labor income (Bottazzi, Pesenti, and van Wincoop 1996; Engel and Matsumoto 2006).<sup>3</sup> In our paper, labor income and equity returns are partially disconnected due to redistributive shocks from labor to capital (or dividends). There are two main differ-

ences that set our paper apart from the existing theoretical literature on the role of labor income in international portfolio choice. First, as already mentioned, we allow for two differentiated (tradable) goods and two differentiated bonds.<sup>4</sup> Due to the availability of bonds, the direction of the equity bias is not pinned down by the correlation between equity returns and wages. This can produce drastically different equity portfolios compared to the existing literature. The intuition for our result can be simply exposed in a situation where there are only output (endowment) shocks and redistributive shocks. In that case, the model here predicts full equity home bias for any stochastic structure of the two types of shock; households fully hold the local equity to insure themselves against redistributive shocks. Output shocks are hedged using positions in Home and Foreign bonds, as supply shocks affect the return difference between the two bonds (by altering terms of trade).

A second difference is that while most existing theoretical models assume that an equity portfolio exists that perfectly mimics wage returns (a case of perfect spanning and complete markets), we here allow for market incompleteness. This is important because complete markets models counterfactually predict perfect correlation between the ratio of home to foreign marginal utilities of consumption and the real exchange rate (the well-known consumption-real exchange rate anomaly; see Kollmann 1991, 1995, 1996; Backus and Smith 1993). As recently documented by Corsetti, Dedola, and Leduc (2008) and Benigno and Thoenissen (2006), the correlation between relative consumption and the real exchange is low in the data (see also Chari, Kehoe, and McGrattan 2002). While Corsetti, Dedola, and Leduc (2008) (or Kollmann 1995, 1996) tackle the puzzle by restricting the menu of assets, we adopt here a different strategy by increasing the number of shocks to obtain incomplete markets.

The theoretical literature on external valuation effects is more recent and has focused on their impact on current account adjustment. See, for example, Tille (2005); Blanchard, Giavazzi, and Sa (2005), and Ghironi, Lee, and Rebucci (2007). Ghironi, Lee, and Rebucci (2007) have a richer dynamic business cycle model (with endogenous labor and production) than the present paper. However, they assume that international financial transactions are costly and restricted to stocks. In their model, steady state equity portfolios are pinned down by costs to holding foreign stocks. By contrast, our model assumes trade in stocks and bonds in a frictionless financial market.

### 5.3 Setup of the Model

#### 5.3.1 Goods and Preferences

We consider a two-period ( $t = 0, 1$ ) endowment economy. There are two symmetric countries, Home ( $H$ ) and Foreign ( $F$ ), each with a representative household. Each country produces one good. There is no output (and no consumption) at  $t = 0$ , but agents trade financial claims (stocks and bonds) at date 0. In period 1, country  $i = H, F$  receives an exogenous endowment  $y_i$  of good  $i$ . Equation  $E_0(y_i) = 1$  hold for both countries, where  $E_0$  is the conditional expectation operator, given date  $t = 0$  information. Once stochastic endowments are realized, households consume using their financial and labor incomes.

The country  $i$  household has these preferences:

$$U_i = E_0 \left[ \frac{C_i^{1-\sigma}}{1-\sigma} \right], \quad (1)$$

where  $C_i$  is an aggregate consumption index in period 1. Like much of the literature, we take the coefficient of relative risk aversion to be greater than unity:  $\sigma > 1$ . Variable  $C_i$ , for  $i = H, F$  is given by:

$$C_H = [a^{1/\phi}(\Psi_H c_H^H)^{(\phi-1)/\phi} + (1-a)^{1/\phi}(\Psi_F c_F^H)^{(\phi-1)/\phi}]^{\phi/(\phi-1)} \quad (2)$$

$$C_F = [a^{1/\phi}(\Psi_F c_F^F)^{(\phi-1)/\phi} + (1-a)^{1/\phi}(\Psi_H c_H^F)^{(\phi-1)/\phi}]^{\phi/(\phi-1)} \quad (3)$$

where  $c_j^i$  is country  $i$ 's consumption of the good from country  $j$ . The elasticity of substitution between the two goods is  $\phi$ .  $\Psi_i$ ,  $i = H, F$  with  $E_0(\Psi_i) = 1$  is an exogenous worldwide shock to the (relative) preference for the country  $i$  good. To be more illustrative we call this shock an iPod shock. Note that the shock  $\Psi_i$  can also have a more supply-oriented interpretation, as a shock to the quality of good  $i$ . In a model with love for variety of the Dixit-Stiglitz type, the shock could also reflect a change in the number of differentiated good varieties produced by country  $i$ . Broda and Weinstein (2007) report that electronics, records, and tapes is the product group that has the largest quality/new goods bias in the consumer price index (CPI). Hence, our choice of name.

We assume a preference bias for local goods,  $1/2 < a < 1$ . Note that in the special Cobb-Douglas case ( $\phi = 1$ ),  $a$  is the share of consumption spending devoted to the local good.

The welfare-based consumer price indices that correspond to these preferences are:

$$P_H = \left[ a \left( \frac{p_H}{\Psi_H} \right)^{1-\phi} + (1-a) \left( \frac{p_F}{\Psi_F} \right)^{1-\phi} \right]^{1/(1-\phi)} \quad (4)$$

$$P_F = \left[ (1-a) \left( \frac{p_H}{\Psi_H} \right)^{1-\phi} + a \left( \frac{p_F}{\Psi_F} \right)^{1-\phi} \right]^{1/(1-\phi)}, \quad (5)$$

where  $p_H$  and  $p_F$  are the prices of good H and F, respectively. Note that the welfare-based CPIs indices may differ from empirical CPIs, if the empirical measures do not capture changes in preferences (or in the quality/number of varieties).

Resource constraints are given by:

$$c_H^H + c_H^F = y_H \quad (6)$$

$$c_F^F + c_F^H = y_F. \quad (7)$$

We denote Home terms of trade; that is, the relative price of the Home good in terms of the Foreign good, by  $q$ :

$$q \equiv \frac{p_H}{p_F}. \quad (8)$$

### 5.3.2 Financial Markets

There is trade in stocks and bonds, in period 0. Each stock represents a share in one of the future endowments. The supply of each type of share is normalized at unity. An exogenous fraction  $k_i$  of the country  $i$  endowment  $y_i$  accrues to shareholders, while a fraction  $(1 - k_i)$  is received by the local household. Hence,  $(1 - k_i)p_i y_i$  can be interpreted as country  $i$  labor income. There is a bond denominated in the Home good, and a bond denominated in the Foreign good. Buying one unit of the Home (Foreign) bond in period 0 gives one unit of the Home (Foreign) good at  $t = 1$ . Both bonds are in zero net supply.

Each household fully owns the local stock at birth, and has zero initial foreign assets. The country  $i$  household thus faces the following budget constraint, at  $t = 0$ :

$$p_s S_i^j + p_s S_j^i + b_i^j + b_j^i = p_s, \quad \text{with } j \neq i \quad (9)$$

where  $S_j^i$  is the number of shares of stock  $j$  held by country  $i$ , at the end of period 0, while  $b_j^i$  represents claims (held by  $i$ ) to future unconditional payments of good  $j$ . The share price is  $p_s$  (identical for both stocks due to symmetry).<sup>5</sup>



Market clearing in asset markets requires:  $S_H^H + S_H^F = S_F^F + S_F^H = 1$  and  $b_H^H + b_H^F = b_F^F + b_F^H = 0$ . Symmetry of preferences and shock distributions implies that equilibrium portfolios are symmetric:  $S_H^H = S_F^F$ ,  $S_H^F = S_F^H$ ,  $b_H^H = b_F^F$  and  $b_H^F = b_F^H$ . In what follows, we denote a country's holdings of local stock by  $S$ , and its holdings of bonds denominated in its local good by  $b$ . The pair  $(S; b)$  thus describes portfolios. The expression  $S > 1/2$  means that there is equity home bias;  $b < 0$  means that a country issues bonds denominated in its local good, and that the country is lending in units of the foreign good.

Finally, we define a country's net foreign currency position (FCP) as its holdings of assets denominated in foreign good units, net of the country's liabilities denominated in foreign good. Up to a first-order approximation,  $p_s = \bar{k}$  holds, where  $\bar{k} \equiv E_0(k_i)$  is the expected capital share. Hence,

$$FCP = \bar{k}(1 - S) - b. \quad (10)$$

Empirically,  $FCP$  is positive for industrialized countries (as explained in section 5.1). Note that, in the model,  $FCP$  equals the expected payment of foreign currency (foreign good) received by a country in period 1. Symmetry entails that if a country is long in foreign currency ( $FCP > 0$ ), then the country has a short position of the same amount in its own currency (good). A positive  $FCP$  means that, ceteris paribus, a 1 percent worsening of a country's terms of trade ( $q$ ) generates an increase in the country's net external income that represents  $FCP$  percent of its expected GDP.

## 5.4 Characterization of World Equilibrium with Complete Markets

To build up intuition, we first characterize the equilibrium in settings in which the number of shocks equals the number of assets. In these settings, the asset structure supports a complete markets allocation, up to a first-order approximation of the equilibrium conditions. (Throughout the following discussions we refer to those settings as "complete markets" settings although, strictly speaking, completeness only holds up to a linear approximation.)

### 5.4.1 Efficient Consumption and Terms-of-Trade

When markets are complete, the equilibrium allocation is Pareto efficient, so that it corresponds to the allocation chosen by a social planner

who maximizes the sum of countries' utilities, subject to the resource constraints (6) and (7):

$$\max_{\{c_H^H, c_F^H, c_H^F, c_F^F\}} \frac{C_H^{1-\sigma}}{1-\sigma} + \frac{C_F^{1-\sigma}}{1-\sigma}. \tag{11}$$

We obtain the following first-order conditions for consumption:

$$\begin{aligned} c_H^H &= a\Psi_H^{\phi-1}\lambda_H^{-\phi}C_H^{1-\sigma\phi} & c_H^F &= (1-a)\Psi_H^{\phi-1}\lambda_H^{-\phi}C_F^{1-\sigma\phi} \\ c_F^H &= (1-a)\Psi_F^{\phi-1}\lambda_F^{-\phi}C_H^{1-\sigma\phi} & c_F^F &= a\Psi_F^{\phi-1}\lambda_F^{-\phi}C_F^{1-\sigma\phi} \end{aligned} \tag{12}$$

where  $\lambda_H$  and  $\lambda_F$  are the multipliers on the Home and Foreign market clearing conditions (6) and (7), respectively. The decentralized equilibrium is such that Home terms of trade  $q \equiv p_H/p_F$  equal the ratio of multipliers:  $\lambda_H/\lambda_F = q$ . Hence, using the market clearing conditions (6) and (7), we get:

$$c_H^H + c_H^F = \Psi_H^{\phi-1}p_H^{-\phi}[aC_H^{1-\sigma\phi} + (1-a)C_F^{1-\sigma\phi}] = y_H \tag{13}$$

$$c_F^F + c_F^H = \Psi_F^{\phi-1}p_F^{-\phi}[aC_F^{1-\sigma\phi} + (1-a)C_H^{1-\sigma\phi}] = y_F. \tag{14}$$

Taking the ratio of these expressions and defining

$$\Omega(x) = \frac{1+x\left(\frac{1-a}{a}\right)}{x+\left(\frac{1-a}{a}\right)}$$

gives:

$$q^{-\phi}\left(\frac{\Psi_H}{\Psi_F}\right)^{\phi-1}\Omega\left[\left(\frac{C_F}{C_H}\right)^{1-\sigma\phi}\right] = \frac{y_H}{y_F}. \tag{15}$$

When markets are complete, the ratio of Home to Foreign marginal utilities of aggregate consumption is linked to the consumption-based real exchange rate by the following familiar condition:

$$\left(\frac{C_H}{C_F}\right)^{-\sigma} = \frac{P_H}{P_F}. \tag{16}$$

Hence, any shock that raises Home aggregate consumption relative to Foreign aggregate consumption must be associated with a Home real exchange rate depreciation. Thus, under complete markets:

$$q^{-\phi}\left(\frac{\Psi_H}{\Psi_F}\right)^{\phi-1}\Omega\left[\left(\frac{P_H}{P_F}\right)^{1/\sigma-\phi}\right] = \frac{y_H}{y_F}. \tag{17}$$

### 5.4.2 Budget Constraints

Recall that each household holds shares  $S$  and  $1 - S$  of local and foreign stocks, respectively, while  $b$  denotes his or her holding of bonds denominated in his or her local good; also, the stock  $j$  dividend is  $k_j p_j y_j$ . The period 1 budget constraints of countries  $H$  and  $F$  are thus:

$$P_H C_H = S k_H p_H y_H + (1 - S) k_F p_F y_F + p_H b - p_F b + (1 - k_H) p_H y_H \quad (18)$$

$$P_F C_F = (1 - S) k_H p_H y_H + S k_F p_F y_F - p_H b + p_F b + (1 - k_F) p_F y_F. \quad (19)$$

These constraints imply:

$$P_H C_H - P_F C_F = (2S - 1)(k_H p_H y_H - k_F p_F y_F) + 2b(p_H - p_F) + (1 - k_H) p_H y_H - (1 - k_F) p_F y_F, \quad (20)$$

which says that the difference between countries' consumption spending equals the difference between their incomes.

### 5.4.3 Log-Linearization of the Model

Henceforth, we write  $y \equiv y_H / y_F$ ,  $\Psi \equiv \Psi_H / \Psi_F$ , and  $k \equiv k_H / k_F$  to denote relative outputs, preference shocks, and capital shares. We log-linearize the model around the symmetric deterministic steady state where  $y$ ,  $\Psi$ , and  $k$  equal unity, and use  $\hat{x} \equiv \log(x/\bar{x})$  to denote the log deviation of a variable  $x$  from its steady state value  $\bar{x}$ .

The log-linearization of the Home country's welfare-based real exchange  $\widehat{RER}_{WB} \equiv P_H / P_F$  gives:

$$\widehat{RER}_{WB} = \frac{\widehat{P}_H}{\widehat{P}_F} = (2a - 1)(\hat{q} - \hat{\Psi}). \quad (21)$$

It is important to notice that the real exchange rate observed by the statistician might be different from the welfare-based real exchange rate since preference or quality changes are very imperfectly measured. We denote by  $RER$  the real exchange rate measure derived from CPI measures that do not capture taste or quality changes so that:  $(RER)^\wedge = (2a - 1)\hat{q}$ .

Log-linearizing (17) and (21) implies:

$$\begin{aligned} \hat{y} &= - \left\{ \phi \left[ 1 - (2a - 1)^2 \right] + (2a - 1)^2 \frac{1}{\sigma} \right\} (\hat{q} - \hat{\Psi}) - \hat{\Psi} \\ &\equiv -\lambda \hat{q} + (\lambda - 1) \hat{\Psi}, \end{aligned} \quad (22)$$

where  $\lambda \equiv \phi[1 - (2a - 1)^2] + (2a - 1)^2/\sigma$ . Note that  $\lambda > 0$  as  $1/2 < a < 1$ . It follows from (22), that the equilibrium relative price is:

$$\hat{q} = -\frac{1}{\lambda}\hat{y} + \frac{\lambda - 1}{\lambda}\hat{\Psi} \tag{23}$$

As expected, Home terms-of-trade ( $q$ ) are decreasing in relative Home output  $\hat{y}$  (with an elasticity  $-1/\lambda$ ). Home terms of trade are increasing in the relative demand (iPod) shock  $\Psi$  if and only if  $\lambda > 1$ ; roughly speaking, this is the case when the substitution elasticity between Home and Foreign goods,  $\phi$ , is larger than unity. The reason why the sign of the response of terms of trade to the relative iPod shock  $\Psi$  depends on the substitution elasticity is the following: the relative supply of good  $H$  in efficiency units is  $\Psi y$ , while the relative price of one efficiency unit of good  $H$  (in efficiency units of good  $F$ ) is  $q/\Psi$ . Hence, a positive relative iPod shock both induces an increase in the (relative) supply of good  $H$ , in efficiency units, and an increase in demand. While the first effect reduces the relative price (not adjusted for efficiency units) with an elasticity of  $1/\lambda$ , the second effect increases the relative price with a unit elasticity. When demand is sufficiently elastic (so that  $\lambda$  exceeds unity), then the demand effect dominates and the relative price (unadjusted for efficiency units) increases with the relative iPod shock.

We next log-linearize equation (20); using (21) and (16) we obtain:

$$\begin{aligned} \widehat{P_H C_H} - \widehat{P_F C_F} &= \left(1 - \frac{1}{\sigma}\right) \underbrace{(2a - 1)(\hat{q} - \hat{\Psi})}_{RER_{WB}} \tag{24} \\ &= \bar{k}(2S - 1)(\hat{q} + \hat{k} + \hat{y}) + 2b\hat{q} + (1 + \bar{k})\left(\hat{q} + \hat{y} - \frac{\bar{k}}{1 - \bar{k}}\hat{k}\right). \end{aligned}$$

The first equality shows the Pareto optimal reaction of relative consumption spending to a change of the welfare-based real exchange rate. This reaction depends on the coefficient of relative risk aversion. In a Pareto efficient equilibrium, a shock that appreciates the (welfare-based) real exchange rate of country  $H$ , induces an increase in country  $H$  relative consumption spending when  $\sigma > 1$  (as assumed in the analysis here). The risk-sharing condition (16) shows that when the (welfare-based) real exchange rate appreciates by 1 percent, then relative aggregate country  $H$  consumption ( $C_H/C_F$ ) decreases by  $1/\sigma$  percent. Hence, efficient relative consumption spending by  $H$  ( $P_H C_H/P_F C_F$ ) increases by  $(1 - 1/\sigma)$  percent. The expression to the right of the second equal sign in (24) shows the change in country  $H$  relative income (compared to the in-

come of  $F$ ) necessary to obtain the Pareto optimal allocation. Given  $\sigma > 1$ , the efficient portfolio has to be such that a real appreciation (welfare based) is associated with an increase in relative spending and income.

The financial market is effectively complete (up to a first-order approximation) when there exists a pair  $(S, b)$  such that (23) and the second equation in (24) both hold for arbitrary realizations of the relative shocks  $\hat{y}, \hat{\Psi}, \hat{k}$ . Clearly, the market can only be complete when there are (at most) two relative shocks.

#### 5.4.4 Complete Markets Examples

We now solve for equilibrium portfolios in economies with just two (relative) shocks. In these economies, markets are effectively complete (perfect spanning).

**Output and iPod Shocks** We start with a situation with just relative supply (output) and iPod shocks  $\hat{y}, \hat{\Psi}$ . The following portfolio  $(S, b)$  ensures that (23) and (24) hold for arbitrary realizations of  $\hat{y}$  and  $\hat{\Psi}$ :

$$S = 1/2 \left[ 1 - \frac{(2a-1)(1-1/\sigma)}{\bar{k}} - \frac{1-\bar{k}}{\bar{k}} \right]; \quad b = 0. \quad (25)$$

Note that the correlation between shocks does not matter for the equilibrium portfolio, as long as the correlation is not perfect (this also holds in the other complete markets examples discussed following). The local equity share depends on three terms. The first term,  $1/2$ , represents the diversification motive in a single-good world with zero labor income, as analyzed by Lucas (1982): in such a world, equity portfolios are fully diversified. The second term,  $-1/2[(2a-1)/\bar{k}][(1-1/\sigma)/(\lambda-1)]$ , represents the hedging of real exchange rate risk, as analyzed, i.a., in Coourdacier (2005), Kollmann (2006b), Obstfeld (2007), and van Wincoop and Warnock (2006); this term is negative (i.e., it generates foreign equity bias), when the substitution elasticity between goods,  $\phi$ , is (roughly speaking) larger than unity (so that  $\lambda > 1$ ).<sup>6</sup> When there is no consumption home bias ( $a = 1/2$ ), the real exchange rate is constant and the second term disappears. The third term,  $-1/2[(1-\bar{k})/\bar{k}]$ , represents the foreign equity bias in a single-good world with labor income and a constant capital share, so that labor and capital incomes are perfectly positively correlated (see Baxter and Jerman 1997); in such a world, foreign equity bias emerges as labor income and is less closely correlated with foreign equity returns than with domestic returns.

With just supply and iPod shocks, bonds are not useful for the hedging of terms of trade risk, as the latter is hedged using stocks; hence,  $b = 0$ .

Thus, this case shares the difficulties of the previous literature to explain equity home bias. It makes clear that in order to get more realistic portfolios, one needs a shock that eliminates the perfect correlation between relative dividends and the real exchange rate, as well as the perfect correlation between labor and capital incomes. We next analyze such a shock, namely a redistributive shock.

**Output and Redistributive Shocks** We now analyze a situation with just relative output and capital share (redistributive) shocks,  $\hat{y}$  and  $\hat{k}$ . It follows from (23) and (24) that, in this case, the equilibrium portfolio is:

$$S = 1; b = \frac{1}{2} [(2a - 1)(1 - 1/\sigma) + \lambda - 1]. \quad (26)$$

Hence, full equity home bias ( $S = 1$ ) appears for all preference parameters and any stochastic structure of the two shocks. By contrast, the previous literature on portfolio choice in models with labor income and a variable labor/capital share (e.g., Botazzi, Pesenti, and van Wincoop 1996) argued that equity home bias only arises when output and the capital share are sufficiently negatively correlated. Note that, in contrast to most of that literature, we here consider a world with multiple goods and the possibility to share risk using bonds.

The predicted full equity home bias reflects the fact that holding local equity insulates household income from capital share shocks; this is important, as the efficient consumption allocation does not depend on those shocks. Intuitively, capital share shocks entail that domestic equity returns are high when domestic labor income is low (and vice versa); this makes holding local equity attractive. Note that this mechanism operates even when the unconditional correlation between labor and capital income is positive. (The unconditional correlation is positive when output shocks are sufficiently volatile, compared to capital share shocks.)

More generally, any shock that takes away resources from consumers and redistributes them to firms would have the same effect on portfolios as the capital share shocks discussed in this section. The working paper version of this paper shows that a model with output shocks and shocks to government purchases generates the same portfolio as the model with output and capital share shocks.

Once capital share shocks have been hedged by holding local equity, the remaining output risk can be hedged using the bond portfolio; this

is so because output shocks induce terms of trade movements that affect the difference between the returns on Home and Foreign good bonds. When  $S = 1$  holds, then a country's net imports equal its net foreign bond income, as can readily be seen from the budget constraints (18) and (19). For country  $H$ :  $(P_H/p_F)C_H - qy_H = (q-1)b$ . In an efficient equilibrium, a positive shock to Home output always worsens the Home terms of trade ( $q$ ); when the elasticity of substitution between  $H$  and  $F$  goods is high, then Home net imports fall, in an efficient equilibrium. For low substitution elasticities, by contrast, net imports rise.<sup>7</sup> There exists a threshold value of the substitution elasticity between Home and Foreign goods  $\phi$  for which net imports are unaffected by output shocks; that threshold is roughly equal to unity—it is given by the value of  $\phi$  for which the right-hand side of the equation that determines  $b$  (see [26]) is zero.<sup>8</sup>

The variable  $b$  is positive (negative) when a domestic output increase lowers (raises) net imports. When  $\phi$  exceeds the threshold, each country thus goes long in local-good bonds (and short in foreign-good bonds): this ensures that an increase in the local endowment (which lowers the country's terms of trade) triggers a capital loss on the country's bond portfolio, which induces the country to lower its net imports, as prescribed by efficient international risk sharing. By contrast, for low values of  $\phi$ , the country goes short in local good bonds; the terms of trade worsening that results from a positive domestic output shock then leads to a capital gain that allows the country to finance the efficient increase in its net imports.

Empirically, industrialized countries have a positive (gross) foreign currency position,  $FCP > 0$  (as was discussed previously). In the setting with just output and capital share shocks, we have:

$$FCP \equiv \bar{k}(1 - S) - b = -b. \quad (27)$$

Therefore, the main conclusion is that redistributive shocks provide a strong incentive to hold local equity. However, in a world with just supply and redistributive shocks, the predicted foreign currency position is realistic ( $FCP > 0$ ) only for low substitution elasticities, namely for values of  $\phi$  roughly smaller than unity, such that  $\lambda < 1$  holds (as can be seen from [26]). (For  $\lambda > 1$ , by contrast, investors are long in local good bonds and short in foreign good bonds, so that a terms of trade depreciation is associated with a wealth transfer from the country to the rest of the world.) Note that  $\lambda < 1$  implies that a positive shock to a country's output worsens its terms of trade so strongly that the relative *value*

of the country's output, at market prices ( $qy$ ) drops (see [23]). Such a (relative) immiserizing growth effect seems implausible, at least among industrialized economies. We thus conclude that, in the model with just supply and redistributive shocks,  $FCP > 0$  and realistic valuation effects only obtain for implausible parameter configurations.

**iPod and Redistributive Shocks** When there are just iPod and capital share shocks ( $\hat{\Psi}, \hat{k}$ ), the model generates full equity home bias; it furthermore yields a positive foreign currency position (FCP) when  $\lambda > 1$ . The equilibrium portfolio with just  $\hat{\Psi}, \hat{k}$ , shocks is:

$$S = 1; b = -\frac{1}{2} - \frac{1}{2} \frac{(2a-1)(1-1/\sigma)}{\lambda-1}. \quad (28)$$

As before, capital share shocks are hedged by holding local equity ( $S = 1$ ). The iPod risk is hedged using bonds. The bond position is structured in such a manner that external capital gains/losses track changes in efficient consumption spending induced by iPod shocks. A positive relative iPod shock (increase in  $\Psi = \Psi_H/\Psi_F$ ) depreciates the Home real exchange rate (welfare based), as:  $\widehat{RER}_{WB} = (2a-1)(\hat{q} - \hat{\Psi}) = -1/\lambda(2a-1)\hat{\Psi}$ ; this induces a decrease in relative country  $H$  consumption spending (assuming  $\sigma > 1$ ; see [24]). Following this relative demand shock, country  $H$  terms of trade appreciate when  $\lambda > 1$ ; that is, when the elasticity of substitution is, roughly speaking, greater than unity (see [23]). When  $\lambda > 1$  holds, country  $H$  thus experiences a decrease in its efficient relative consumption spending in states of the world in which its terms of trade improve; in order to finance efficient consumption spending, the country thus goes short in local-good bonds ( $b < 0$ ); as a result, the gross foreign currency position is positive ( $FCP > 0$ ).<sup>9</sup>

Hence, a combination of demand and redistributive shocks helps to reproduce the broad facts presented in the introduction: home bias in stocks, and a long position in foreign currency (short position in domestic currency).

## 5.5 Characterization of World Equilibrium with Incomplete Markets

### 5.5.1 Analytical Results

**Solution Method** Complete markets provide a simple and useful benchmark for analyzing international portfolio behavior. However, the



complete markets assumption has some unrealistic implications; for example, it implies that ratios of Home to Foreign marginal utilities of consumption are perfectly correlated with real exchange rates; that prediction is rejected by the data (e.g., Kollmann 1991, 1995, 1996; Backus and Smith 1993). We now assume that the world economy is subjected to the three (relative) shocks simultaneously, so that markets are incomplete.

The solution methods developed by Coeurdacier (2005), Devereux and Sutherland (2006), and Tille and van Wincoop (2007) allow us to compute equilibrium portfolios in economies with incomplete markets. Those methods solve for portfolios that satisfy a second-order accurate approximation of household Euler equations for the four assets:

$$0 = E_0[m_i(p_F - p_H)] = E_0\left[m_i\left(\frac{k_j p_j y_j}{p_s} - p_H\right)\right] \text{ for } j = \{H, F\}, \quad (29)$$

where  $m_i = U'(C_i)/P_i$  is the marginal utility of household  $i$  dividend by its CPI. Rewriting (29) in relative terms, we get:

$$0 = E_0\left[(m_i - m_j)\left(\frac{k_j p_j y_j}{p_s} - p_H\right)\right] \text{ for } j = \{H, F\} \quad (30)$$

$$0 = E_0[(m_i - m_j)(p_F - p_H)]. \quad (31)$$

Equation (30) can be stated as:  $E_0(m \cdot ER) = 0$ , where  $m = m_i - m_j$  is the cross-country difference of stochastic discount factors, while  $ER$  is the vector of excess returns on the two stocks and the Foreign bond (relative to the return of the Home-good bond):

$$ER = \begin{pmatrix} \frac{k_H p_H y_H}{p_s} - p_H \\ \frac{k_F p_F y_F}{p_s} - p_H \\ p_F - p_H \end{pmatrix}.$$

A second-order accurate approximation of this condition is given by  $E_0(\hat{m} \widehat{ER}) = 0$ , where  $\hat{m}$  and  $\widehat{ER}$  are first-order accurate.<sup>10</sup>

The equilibrium portfolio is computed in a two-step approach:

1. For a given portfolio  $(S, b)$ , the budget constraint (18), the first-order condition that prescribes equalization of marginal rates of substitution between the two goods to terms of trade, and the goods market clearing conditions ([6], [7]) are solved for  $m$  and  $ER$ . A linear approximation gives:  $\hat{m} = A(S, b)\xi$  and  $\widehat{ER} = B(S, b)\xi$ , where  $\xi = [y_{H'} y_{F'} k_{H'} k_{F'} \Psi_{H'} \Psi_{F'}]'$

is the vector of exogenous variables;  $A(S, b)$  and  $B(S, b)$  are vectors/matrices (of dimensions  $[1 \times 6]$  and  $[3 \times 6]$ , respectively) that are functions of  $S$  and  $b$ .

2. Determination of the values of  $S$  and  $b$  for which  $E_o(\hat{m}\widehat{ER}) = 0$  holds; that is,  $B(S, b)\Sigma A(S, b) = 0$ , where  $\Sigma = E_o[\xi\xi']$  is the covariance matrix of exogenous disturbances.

**Equilibrium Portfolios** Devereux and Sutherland (2006) provide a closed-form solution for the equilibrium portfolio. Under incomplete markets, the portfolio depends on the correlation between shocks. We first focus on the simplest case where the three relative shocks are uncorrelated (section 5.5.3 extends the analysis to correlated shocks); one can show that then the optimal portfolio is given by:

$$S = 1 - \frac{1}{2\bar{k}} \frac{2a(\phi - 1)\sigma_y^2\sigma_\Psi^2[(2a - 1)(1 - 1/\sigma) + \lambda - 1]}{2a(\phi - 1)(\lambda - 1)(\sigma_y^2 + \sigma_k^2)\sigma_\Psi^2 + \sigma_y^2\sigma_k^2} \tag{32}$$

$$b = \frac{1}{2} \frac{[(2a - 1)(1 - 1/\sigma) + \lambda - 1][\sigma_y^2 - 2a(\phi - 1)\sigma_\Psi^2]\sigma_k^2}{2a(\phi - 1)(\lambda - 1)(\sigma_y^2 + \sigma_k^2)\sigma_\Psi^2 + \sigma_y^2\sigma_k^2}$$

where  $\sigma_y = std(\hat{y})$ ,  $\sigma_\Psi = std(\hat{\Psi})$ , and  $\sigma_k = std(\hat{k})$  are the standard deviations of the (relative) supply, iPod, and redistributive shocks, respectively. Note that eliminating one of the shocks (setting one of the standard deviations to zero) brings us back to the complete markets situations analyzed in the preceding section. The local equity position can be rewritten as:

$$S = \frac{1}{2} - \frac{1}{2\bar{k}} \frac{2a(2a - 1)(\phi - 1)(1 - 1/\sigma)\sigma_y^2\sigma_\Psi^2}{2a(\phi - 1)(\lambda - 1)(\sigma_y^2 + \sigma_k^2)\sigma_\Psi^2 + \sigma_y^2\sigma_k^2} \tag{33}$$

$$+ \frac{1}{2\bar{k}} \frac{[2a(\phi - 1)(\lambda - 1)\sigma_\Psi^2 + \sigma_y^2]\sigma_k^2}{2a(\phi - 1)(\lambda - 1)(\sigma_y^2 + \sigma_k^2)\sigma_\Psi^2 + \sigma_y^2\sigma_k^2} - \frac{1 - \bar{k}}{2\bar{k}}$$

The equity portfolio depends on four terms. The first term (1/2) reflects the diversification motive in a single-good world with zero labor income. The second term represents the hedging of real exchange rate risk, which we discussed already in the complete market case (see section 5.4.4). Real exchange rate hedging is now more complex, because of the larger number of shocks. The second term tends to generate a foreign equity bias for sufficiently high substitution elasticities ( $\phi > 1$ ).<sup>11</sup> Again, this term disappears when preferences are identical across countries (no consumption home bias,  $a = 1/2$ ), as then the real exchange rate is con-

stant. The third term comes from the redistributive shock and it tends to induce a Home bias in stocks. When the redistributive shock is sufficiently large (more precisely when  $\sigma_k^2$  is large relative to  $\sigma_\psi^2$  and  $\sigma_y^2$ ), then there always is equity home bias,  $S > 1/2$ . The last term, again, represents the foreign equity bias in a single-good world with labor income, in which the labor share is fixed (so that labor and capital incomes are perfectly positively correlated).

Note also that with a substitution elasticity of unity ( $\phi = 1$ ), full Home bias ( $S = 1$ ) is obtained for all configurations of parameters as long as the variance of the distribution shock  $\sigma_k^2$  is not zero.

The local-good bond position can be rewritten as:

$$b = -\bar{k}(1 - S) \frac{\sigma_k^2}{\sigma_\psi^2} \left[ \frac{\sigma_\psi^2}{\sigma_y^2} - \frac{1}{2a(\phi - 1)} \right] \quad (34)$$

where  $S$  is given by (33).

Equation (34) shows the relative importance of the demand and supply shocks for the structure of the bond portfolio. For a substitution elasticity larger than 1 and interior portfolios ( $0 < S < 1$ ), agents go short on local good bonds ( $b < 0$ ) and long on foreign-good bonds when iPod shocks are large enough relative to supply shocks. Intuitively, a negative iPod shock that deteriorates a country's terms of trade also deteriorates its relative output (evaluated at market prices); the shock can thus be hedged by holding Foreign bonds (whose relative return rises when domestic terms of trade worsen).

In the economy with the three types of shocks, the foreign currency position is:

$$FCP = (1 - S)\bar{k} - b = (1 - S)\bar{k} \left\{ 1 + \frac{\sigma_k^2}{\sigma_\psi^2} \left[ \frac{\sigma_\psi^2}{\sigma_y^2} - \frac{1}{2a(\phi - 1)} \right] \right\}, \quad (35)$$

which is strictly positive as long as there is no full home bias ( $S < 1$ ) in stocks and supply shocks are not too large compared to the iPod shocks.

### 5.5.2 Quantitative Analysis with Incomplete Markets

**Calibration** In this section, we calibrate the incomplete markets model with supply, demand, and redistributive shocks. The mean capital share across G7 countries is 40 percent, hence we set  $\bar{k} = 0.4$ .<sup>12</sup> We computed standard deviations of annual rates of change for real GDP growth and capital shares, for each G7 country (1972 through 2003). Across the G7 countries, the mean standard deviations of (rates of change of) real GDP and the capital shares are 1.91 percent and 2.34 percent, respectively.

Equilibrium portfolios under incomplete markets depend on the standard deviations of the relative supply, capital share, and iPod shocks,  $y \equiv y_H/y_F$ ,  $k \equiv k_H/k_F$  and  $\Psi \equiv \Psi_H/\Psi_F$ . We computed a country's relative real GDP and capital share, compared to a geometric average of the remaining G7 countries' GDPs and the capital shares (1972 through 2003).<sup>13</sup> Relative outputs and capital shares undergo highly persistent fluctuations. The mean value (across G7 countries) of standard deviations of annual growth rate of relative GDPs is 1.59 percent. For relative capital shares the corresponding mean standard deviation is 2.39 percent.<sup>14</sup> For all countries, the relative capital share is more volatile than relative GDP. In the calibrated model, we therefore set  $std(y_t) = 1.91\%$ ,  $std(k_t) = 2.34\%$ ,  $\sigma_y \equiv std(\hat{y}) = 1.59\%$ ,  $\sigma_k \equiv std(\hat{k}) = 2.39\%$ .

As mentioned before, iPod shocks can have several interpretations, and their quantification is less easy than that of the other two shocks. Under one interpretation, iPod shocks reflect quality changes and/or changes in the number of varieties produced by a country. Recent empirical evidence at a very disaggregated level by Broda and Weinstein (2007) suggests that quality/varieties changes are an important phenomenon. In the model here, portfolios and other endogenous variables only depend on the relative iPod shock. We experiment with two values for the volatility of relative iPod shocks,  $\sigma_\psi \equiv std(\hat{\Psi}) = 1$  percent, and  $\sigma_\psi = 2$  percent; that is, in one case the iPod shock is less volatile than relative output, while in the other case, it is slightly more volatile than relative output. We also report results for the case where  $std(\hat{\Psi}) = 0$ . In that case, there are only supply and capital share shocks, and markets are complete.

Across G7 countries, the mean imports/GDP ratio (1972 through 2003) is 20 percent. Hence, we set  $a = 0.8$ .

The substitution elasticity  $\phi$  equals the price elasticity of foreign trade flows. A wide range of empirical estimates of  $\phi$  has been reported. Hooper and Marquez (1995) survey a large number of time-series studies that estimated (long run) price elasticities of aggregate trade flows for the United States, Japan, Germany, the United Kingdom, and Canada; the median estimates (post-Bretton Woods era) for those countries are 0.97, 0.80, 0.57, 0.6, and 1.01, respectively. The median estimate across the five countries is 0.88. We here consider a range of values of  $\phi$ :  $\phi = 0.6, 0.9, 1.5, 2$ . That range encompasses most values of  $\phi$  that have been assumed in recent quantitative macro/finance models; see, for example, Kollmann (2006b), Heathcote and Perri (2002), and Chari, Kehoe, and McGrattan (2002), who have set  $\phi$  at 0.6, 0.9, and 1.5, respectively.

Estimates of  $\sigma$  in the range of 2 (or greater) are common for industri-

**Table 5.1**  
Parameter values

Substitution elasticity	Risk aversion	Spending share local goods	Mean capital share	Std relative output	Std relative capital share	Std relative iPod shock
$\phi$	$\sigma$	$a$	$\bar{k}$	$\sigma_y$	$\sigma_k$	$\sigma_\psi$
0.6 to 2	2	0.8	0.4	1.59%	2.39%	1 to 2%

alized countries (e.g., Barrionuevo 1992); in the quantitative experiments to follow, the risk aversion parameter is hence set at  $\sigma = 2$ .

Table 5.1 summarizes the parameter values used in the simulation.

**Numerical results** Table 5.2 reports numerical results. Columns (1) and (2) list the standard deviation of the relative iPod shock and the elasticity of substitution. Columns (3) through (8) show model predictions.

We report the locally held equity share ( $S$ ), holdings of local-good bonds ( $b$ ), and the foreign currency position ( $FCP = [1 - S] \bar{k} - b$ ) (see columns [3] through [5]). In addition, we report three statistics that describe the behavior of equity returns and the real exchange rate (columns [6] through [8]): the cross-country correlation of equity returns;<sup>15</sup> the covariance of the measured real exchange ( $\widehat{RER}$ ) with the cross-country equity returns differential ( $\widehat{R}_H - \widehat{R}_F = \bar{k}_H p_H y_H - \bar{k}_F p_F y_F$ ) normalized by the variance of the returns differential, that is,  $cov(\widehat{R}_H - \widehat{R}_F, \widehat{RER}) / var(\widehat{R}_H - \widehat{R}_F)$ ; the correlation between (measured) relative aggregate consumption and the (measured) real exchange rate. The last two statistics are based on CPIs, real exchange rates, and aggregate consumption measures that do not take into account preference of quality changes ( $\hat{\Psi}$ ); this is again motivated by the fact that empirical CPI and real consumption measures do not (or only very partially) capture quality/variety changes (see Broda and Weinstein 2007). Also, purely psychological demand shocks are not reflected in official consumption data.

Markets are complete when there are no iPod shocks ( $\sigma_\psi = 0$ ). A 100 percent equity home bias ( $S = 1$ ) is then obtained, and countries hold a long position in local-good bonds if  $\phi > 1$ . In the model versions with  $\phi > 1$ , the long position in home currency is sizable (it amounts to 22 percent of expected output, when  $\phi = 1.5$ ). This is just a restatement of the puzzle presented before; with supply shocks and redistributive shocks only, the model is unable to reproduce a long position in foreign currency for an elasticity of substitution larger than 1. Introducing iPod

**Table 5.2**  
Numerical results

Std iPod $\sigma_\psi$	Substitution elasticity $\phi$	Local equity position S	Bond position b	Foreign currency position FCP	Correlation equity returns	$\frac{cov(\widehat{R}_H - \widehat{R}_F, RER)}{var(\widehat{R}_H - \widehat{R}_F)}$	Correlation (Cons., RER)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
0	0.6	1.00	-0.08	0.06	0.67	0.28	-1.00
1%	0.6	0.98	-0.07	0.08	0.66	0.30	-0.79
2%	0.6	0.95	-0.08	0.10	0.62	0.35	-0.53
0	0.9	1.00	0.03	-0.03	0.69	0.10	-1.00
1%	0.9	1.00	0.03	-0.03	0.69	0.11	-0.96
2%	0.9	1.01	0.03	-0.03	0.68	0.13	-0.85
0	1.5	1.00	0.22	-0.22	0.69	-0.02	-1.00
1%	1.5	0.92	0.14	-0.11	0.69	-0.05	-0.60
2%	1.5	0.75	-0.05	0.14	0.69	-0.08	-0.56
0	2	1.00	0.38	-0.38	0.66	-0.05	-1.00
1%	2	0.81	0.10	-0.02	0.67	-0.07	-0.43
2%	2	0.60	-0.21	0.37	0.66	-0.05	-0.53

shocks reduces the equity home bias, and holdings of local-good bonds, when the substitution elasticity exceeds unity. For example, when  $\phi = 1.5$ , and  $\sigma_\psi = 2$  percent, the model predicts that 75 percent of equity is locally owned, and that countries go short in local-good bonds; the overall foreign good claim is positive,  $FCP = 0.14$ ; that value implies that an exogenous unexpected 10 percent worsening of a country's terms of trade would generate a capital gain that represents 1.4 percent ( $= 0.10 \times 0.14$ ) of (expected) output. We think of this calibration as a plausible benchmark case.

Kollmann (2006b) reports external equity liabilities (defined as the sum of portfolio equity and FDI liabilities) of Organization for Economic Cooperation and Development (OECD) economies in 2003 (data source: IMF international investment positions database). The U.S. foreign equity liabilities amounted to 37 percent of U.S. GDP. Among G7 countries, foreign equity liabilities represented between 12 percent (Italy) and 78 percent (U.K.) of domestic GDP. Assuming that the domestic capital stock is about three times larger than annual GDP, these figures suggest that between 74 percent and 96 percent of the capital stocks located in G7 countries were owned by local investors in 2003. The predicted locally held equity share in the three-shocks model is thus broadly consistent with G7 data.

The cross-country correlations of equity returns given in table 5.2 range between 0.6 and 0.7. The model thus matches the high correlation of stock returns across G7 countries, 0.63.<sup>16</sup> This high correlation reflects the high positive correlation of output and capital share shocks across countries;<sup>17</sup> it also reflects terms of trade movements (Cole and Obstfeld 1991; Pavlova and Rigobon 2004): a positive output shock at home raises the relative price of the foreign good—hence, it raises stock returns in both countries.

The finance literature has shown that real exchange rate fluctuations generate a hedging motive in portfolio choice. Van Wincoop and Warnock (2006) discuss a partial equilibrium model, without labor income, in which the only assets are Home and Foreign stocks. In that model, equity home bias is an increasing function of the covariance-variance ratio between the real exchange rate ( $\widehat{REER}$ ), on the equity return differential  $\widehat{R}_H - \widehat{R}_F$  discussed previously ( $cov[\widehat{R}_H - \widehat{R}_F, \widehat{REER}] / var[\widehat{R}_H - \widehat{R}_F]$ ); when this covariance-variance ratio is zero, then equity home bias is zero (i.e., equity portfolios are perfectly diversified:  $S = 1/2$ ). Van Wincoop and Warnock (2006) document that empirically, the covariance-variance ratio is close to zero;<sup>18</sup> they thus conclude that the “portfolio

home bias associated with hedging real exchange rate risk is essentially zero" (p. 11). Simple general equilibrium models driven by supply shocks (without demand or redistributive shocks) can only generate equity home bias, if the implied covariance-variance ratio is much larger than that observed in the data. As discussed previously, in the model here, capital share shocks create a powerful motive for holding local equity; those shocks induce equity return fluctuation that are disconnected from real exchange rate movements. Also, in the setting here, bonds can be used for hedging real exchange rate risk. This enables the present model to simultaneously generate a realistic equity home bias, *and* to generate a covariance-variance ratio that is close to zero (see column [6] in table 5.2).

Van Wincoop and Warnock (2006) also discuss a model with trade in stocks and in Home and Foreign bonds; when there are neither capital share nor iPod shocks, the degree of equity home bias depends on a covariance-variance ratio based on components of excess equity returns and of the real exchange rate that are orthogonal to exchange rate movements; empirically, that conditional covariance-variance ratio is essentially zero. In the present model, the conditional covariance-variance ratio is exactly zero.

Under complete markets, the risk sharing condition (16) implies that, up to a linear approximation, relative aggregate consumption is perfectly negatively correlated with the (welfare-based) real exchange rate; see Kollmann (1991, 1995), and Backus and Smith (1993). Empirically, the consumption-real exchange correlation is close to zero (mean correlation for G7 countries: 0.04 [1972 through 2003]).

Incomplete markets break the perfect correlation between relative consumption and the welfare-based real exchange rate; iPod shocks further weaken the link between measured relative consumption and the measured real exchange rate, when empirical CPI and real consumption measures do not (or only partially) capture quality/variety changes. However, in the model here, the predicted correlation between (measured) relative consumption and the (measured) RER remains too large (in absolute value), compared to the data (see table 5.2, column [8]). For the specifications where we obtain the most realistic foreign asset positions, the correlation is around  $-0.5$  (e.g., when  $\phi = 1.5$  and  $\sigma_\psi = 2$  percent, the consumption-real exchange rate correlation is  $-0.56$ ). So even though we are going in the right direction, we cannot quantitatively reproduce the low consumption-real exchange rate correlation observed in the data.



We have also studied more in detail how our results vary with the substitution elasticity  $\phi$ . When the standard deviation of the iPod shock has an intermediate value of 1.5 percent, our results are quite robust to setting  $\phi$  at values in the range up to 4 or 5; that is, at values that are much larger than those generally used in macro/finance models (but closer to elasticities often used in the trade literature). The equity home bias never falls below 60 percent. We have also checked that our results are quite insensitive to changes in the risk aversion coefficient (a higher coefficient of risk aversion raises slightly foreign stock and bond holdings).

### 5.5.3 *Correlated Shocks*

In this section, we consider model variants with correlated relative shocks. Under complete markets, equilibrium portfolios do not depend on shock correlations. When markets are incomplete, by contrast, the correlation structure affects portfolios (markets remain incomplete, as long as the correlation between shocks is not 100 percent). In what follows, we thus assume a setting with all three shocks (incomplete markets). We first consider a case in which relative supply and redistributive shocks are correlated (but independent of iPod shocks).

**Correlation Between Supply and Redistributive Shocks** In the *Handbook of Macroeconomics*, Rotemberg and Woodford (1999) report several measures of the correlation between output and the labor share. They conclude that the labor share is weakly countercyclical; in other terms, the capital share is weakly positively correlated with output.<sup>19</sup> In the model here, equilibrium portfolios depend on the correlation between *relative* (Home versus Foreign) output and the relative capital share. Across G7 countries (1972 through 2003), the mean correlation between annual growth rates of relative GDP and relative capital shares is about 20 percent.<sup>20</sup> For the United States, the correlation is close to zero.

When there is a nonzero correlation between (relative) supply and redistributive shocks, the equilibrium portfolio is given by equation (36) in the appendix. As in the zero-correlation case, stock holdings can again be decomposed into four terms that capture different diversification/hedging motives, but these terms are now more complex. The real exchange rate hedging motive (see second term in [36]) becomes stronger. Intuitively, the covariance between equity returns and output is higher when output is positively correlated with the capital share; as a result, the covariance between the real exchange rate and equity returns is lower

(when  $\phi > 1$ ), which pushes toward less equity home bias.<sup>21</sup> Also, with a procyclical capital share, wages are more stable, which dampens the incentive to hedge wage fluctuations through the holding of domestic stocks (see the third term in [36]).

This helps to understand why a positive correlation between shocks reduces somewhat the degree of equity home bias, as can be seen from table 5.3, where we consider model variants in which the correlation between (relative) supply and capital share shocks are set at 0, 0.2, and 0.4, respectively. (Table 5.3 assumes  $\phi = 1.5$  and  $\sigma_\psi = 2\%$ ; all remaining parameters are set at the same values as in table 5.2.) For example, when the shock correlation is 0.2 (the mean empirical correlation for G7 countries), then 68 percent of stocks are held locally (compared to 75 percent in the zero-correlation case).

The predicted Foreign Currency Position ( $FCP = (1 - S)\bar{k} - b$ ) remains positive, which is consistent with the data. In fact, FCP tends to be larger, the higher the correlation between output and capital share shocks; this mainly reflects the fact that equity home bias is lower when the correlation is higher.

**Correlation between Supply and iPod Shocks** Finally, we consider a setting in which (relative) supply and iPod shocks are correlated. Under the interpretation of iPod shocks as pure preference shocks, there is no reason to think that these two shocks are correlated. However, if iPod shocks represent changes in the quality of goods (or in the number of varieties), one may believe that the two shocks are somewhat related. For example, when labor productivity rises because of human capital accumulation, this could both increase output and the quality of goods (or give an incentive to introduce new varieties). The equilibrium portfolio under correlated supply and iPod shocks is given in the appendix (equation [38]).

There are no precise empirical estimates of the correlation between output and quality/varieties changes. Broda and Weinstein (2007) report that, for the United States, the net creation of product varieties is procyclical and that the destruction of varieties is countercyclical. At a highly disaggregated product group level, the correlation between the net rate of creation of product varieties and the growth of consumption and of sales ranges roughly between 0.1 and 0.4.

In table 5.3, we report model prediction for output-iPod shock correlations of 0, 0.2, and 0.4.<sup>22</sup> It again appears that our main results are robust. A positive correlation between productivity and iPod shocks lowers

**Table 5.3**  
Numerical results: Model variants with correlated shocks

Correlation of shocks	Local equity position S	Bond position $b$	Foreign currency position FCP	Correlation equity returns	$\frac{cov(\widehat{R}_H - \widehat{R}_F, \widehat{RER})}{var(\widehat{R}_H - \widehat{R}_F)}$	Correlation (Cons., RER)
$\frac{\sigma_{y^k}}{\sigma_y}$ : output/distribution						
0	0.75	-0.05	0.14	0.69	-0.09	-0.56
0.2	0.68	-0.08	0.21	0.68	-0.15	-0.56
0.4	0.59	-0.14	0.31	0.65	-0.20	-0.56
$\frac{\sigma_{y^\psi}}{\sigma_y}$ : output/iPod						
0	0.75	-0.05	0.14	0.69	-0.09	-0.56
0.2	0.71	-0.05	0.16	0.70	-0.10	-0.47
0.4	0.66	-0.05	0.18	0.70	-0.12	-0.37

somewhat the Home bias in stocks, but increases the Foreign Currency Position.<sup>23</sup>

## 5.6 Conclusion

This paper has shown that a model with supply, demand, and redistributive shocks can help to understand the structure of international portfolios and associated valuation effects. This is in contrast to standard models that focus on supply shocks as the main source of uncertainty.

Our analysis could be extended in several directions. It would be interesting to model more closely the relation between goods supply and the capital share. This could, for example, be done by introducing sticky prices. With nominal rigidities, productivity shocks generate a procyclical capital share. It would also be interesting to model in greater detail the relation between supply and demand shocks, especially when we interpret the latter as shocks to the quality or the number of varieties of traded goods. Here, one might follow Corsetti, Martin, and Pesenti (2007), who show that terms of trade react differently to productivity shocks that affect the unit cost of goods production, and to productivity shocks that affect the cost of creating new varieties. One can also speculate that, in a model with imperfect competition, shocks to the degree of competition and to markups would combine the properties of redistributive and relative demand shocks, and thus help to produce realistic international portfolios, as such shocks likewise redistribute income between capital and labor. We leave those extensions for future research.

## Acknowledgments

This paper has been prepared for the NBER International Seminar on Macroeconomics (ISOM) conference (June 2007). We thank Francesco Giavazzi, Fabio Ghironi, and Refet Gurkaynak for their advice. For useful discussions and suggestions, we are also grateful to Alan Sutherland, Cédric Tille, and to workshop participants at University of Leuven, the Bundesbank, the Konstanz Seminar on Monetary Theory and Policy, and at the Annual Meeting of the Society for Economic Dynamics. Robert Kollmann thanks ECARES and the Belgian National Bank for financial support. Philippe Martin thanks Institut Universitaire de France for financial support. Correspondence to: Robert Kollmann, ECARES, Université Libre de Bruxelles, CP 114, 50 Av Franklin D. Roosevelt, B-1050 Brussels, Belgium.

## Notes

1. See Martin and Rey (2004, 2006); Heathcote and Perri (2004); Coourdacier and Guibaud (2005); Coourdacier (2005); Tille and van Wincoop (2007).
2. Pavlova and Rigobon (2004) also present a two-country model with trade in stocks and in differentiated bonds, but they exclusively focus on complete markets, and do not analyze portfolio choices.
3. Lustig and van Nieuwerburgh (2005) argue that, empirically, physical and human capital returns are negatively correlated.
4. Engel and Matsumoto (2006) also allow for trade in home and foreign bonds.
5. Bond prices are also identical due to symmetry.
6. Recall that we assume  $\sigma > 1$ .
7. For example, it is easy to see that when the substitution elasticity is infinite, then the country that receives a higher output ships a fraction of the additional output to the other country when there is efficient risk sharing; hence, the country that receives the higher output lowers its net imports. When the two goods are imperfect substitutes, then term of trade worsen, which dampens the fall in net imports (the relative price of imports rises).
8. When  $\sigma = 1$  the threshold value of is:  $\phi = 1$ .
9. Note that the model with just  $\hat{\psi}$ ,  $\hat{k}$  shocks may generate  $b < 0$  even when  $\lambda < 1$  holds. For example, this is the case when  $\sigma$  is sufficiently close to unity; then relative efficient consumption spending is essentially unaffected by a positive relative iPod shock; Home terms of trade worsen when  $\lambda < 1$ , and thus, the relative value (at market prices) of the Home endowment drops; hence, the H household needs to obtain a net external capital gain on its bond portfolio in order to finance its (essentially) unchanged relative consumption spending. In this case too, the country thus goes short in local good bonds.
10. All approximations are taken around the equilibrium of a deterministic economy in which the exogenous variables are set at the mean values assumed in the stochastic model; note that  $m = 0$  and  $ER = 0$  in the deterministic economy.
11. Again, for  $\phi > 1$ , foreign stocks give higher returns when the Home (welfare-based) real exchange rate appreciates, leading to some foreign bias in equities.
12. We measure a country's capital share as  $1 - (\text{compensation of employees})/(\text{GDP} - \text{indirect taxes})$ , using annual data from OECD National Accounts.
13. The weights are based on countries' time-averaged shares in G7 nominal GDP.
14. The standard deviations of relative GDP growth rates for the United States, Japan, Germany, France, United Kingdom, Italy, and Canada are 1.7 percent, 2.1 percent, 1.2 percent, 1.44 percent, 1.5 percent, 1.6 percent, and 1.5 percent, respectively. The corresponding standard deviations of growth rates of relative capital shares are 2.1 percent, 2.5 percent, 1.6 percent, 2.0 percent, 3.7 percent, 1.9 percent, 2.8 percent.
15. The correlation pertains to equity returns expressed in terms of the Home good.
16. For each G7 country, we computed the correlation between the Home real equity return and the foreign (rest-of G7) equity return, where (as in the theoretical model), all returns are expressed in units of Home GDP. The mean Home-Foreign equity return correlation is 0.63 (based on annual MSCI returns for 1972 through 1994).

17. Among the model predictions shown in table 5.2, only the cross-country correlation of equity returns depends on the cross-country correlations of output and of the capital share. In accordance with the mean statistics across G7 countries discussed previously, we set the standard deviations of output and the capital share in each country at 1.91 percent and 2.34 percent, respectively. The implied cross-country correlations of output and the capital share are 0.65 and 0.47, respectively.

18. For the United States vis-à-vis twenty-one other OECD countries, the covariance-variance ratio is 0.11.

19. A possible explanation for a procyclical capital share is given by Gali (1999), who argues that, when prices are sticky, productivity shocks reduce labor demand and employment, and raise the labor share in the short run. This is the mechanism at work in Engel and Matsumoto's (2004) two-country portfolio choice model with monopolistic competition.

20. The construction of the relative output and capital share series is discussed previously. The correlations for the individual G7 countries are: United States: -0.04; Japan: 0.05; Germany: 0.27; France: -0.03; United Kingdom: 0.22; Italy: 0.75; Canada: 0.44.

21. Table 5.3 shows that the covariance-variance ratio  $cov(\widehat{R}_H - \widehat{R}_F, RER) / var(\widehat{R}_H - \widehat{R}_F)$  is lower, the higher the correlation between the (relative) supply and redistributive shocks.

22. We again assume  $\phi = 1.5$  and  $\sigma_\psi = 2$  percent; all remaining parameters are set at the same values as in table 5.2.

23. The relationship between the output-iPod shock correlation and home bias in stocks is nonmonotonic: for higher correlations,  $S$  rises ( $S$  converges toward 1 as the correlation approaches unity).

## References

- Backus, D., and G. W., Smith. 1993. Consumption and real exchange rates in dynamic economies with non-traded goods. *Journal of International Economics* 35 (3-4): 297-316.
- Barrionuevo, J. 1992. Asset prices in the international economy. Ph.D. Dissertation, Economics Department, University of Chicago.
- Baxter, M., and U. Jermann. 1997. The international portfolio diversification is worse than you think. *American Economic Review* 87 (1): 170-80.
- Benigno, G., and C. Thoenissen. 2006. Consumption and real exchange rates with incomplete markets and non-traded goods. Centre for Economic Policy Research, Working Paper no. 5580.
- Blanchard, O., F. Giavazzi, and F. Sa. 2005. International investors, the U.S. current account, and the dollar. *Brookings Papers on Economic Activity*, Issue no. 1: 1-65.
- Bottazzi, L., P. Pesenti, and E. van Wincoop. 1996. Wages, profits, and the international portfolio puzzle. *European Economic Review* 40 (2): 219-54.
- Brainard, W., and J. Tobin. 1991. On the internationalization of portfolios. Discussion Paper, Cowles Foundation.
- Broda, C., and D. Weinstein. 2007. Product creation and destruction: Evidence and price implications. NBER Working Paper no. 13041. Cambridge, MA: National Bureau of Economic Research, April.

- Chan, K., V. M. Covrig, and L. K. Ng. 2005. What determines the domestic and foreign bias? Evidence from mutual fund equity allocations worldwide. *Journal of Finance* 60 (3): 1495–1534.
- Chari, V. V., P. Kehoe, and E. McGrattan. 2002. Can sticky price models generate volatile and persistent real exchange rates? *Review of Economic Studies* 69 (3): 533–63.
- Coourdacier, N. 2005. Do trade costs in goods markets lead to home bias in equities? ESSEC Working Paper DR 06014.
- Coourdacier, N., and S. Guibaud. 2005. A dynamic equilibrium model of imperfectly integrated financial markets. Working Paper PSE, 2005-24. Ecole normale supérieure.
- Cole, H., and M. Obstfeld. 1991. Commodity trade and international risk sharing: How much do financial markets matter? *Journal of Monetary Economics* 28 (1): 3–24.
- Corsetti, G., L. Dedola, and S. Leduc. 2008. International risk-sharing and the transmission of productivity shocks. *Review of Economic Studies* 75: 443–73.
- Corsetti, G., P. Martin, and P. Pesenti. 2007. Productivity, terms of trade, and the “home market effect.” *Journal of International Economics* 73 (1): 99–127.
- Devereux, M., and A. Sutherland. 2006. Solving for country portfolios in open economy macro models. Centre for Economic Policy Research Working Paper no. DP5966.
- Engel, C., and A. Matsumoto. 2004. Portfolio choice in a monetary open-economy DSGE model. University of Wisconsin and International Monetary Fund. Working Paper.
- Engel, C., and A. Matsumoto. 2006. Portfolio choice in a monetary open-economy DSGE model. NBER Working Paper no. 12214. Cambridge, MA: National Bureau of Economic Research, May.
- French, K., and J. Poterba. 1991. Investor diversification and international equity markets. *American Economic Review* 81 (2): 222–26.
- Gali, J. 1999. Technology, employment, and the business cycle: Do technology shocks explain aggregate fluctuations? *American Economic Review* 89 (1): 249–71.
- Ghironi, F., Lee, J., and A. Rebucci. 2007. The valuation channel of external adjustment. NBER Working Paper no. 12937. Cambridge, MA: National Bureau of Economic Research, February.
- Gourinchas, P.-O., and H. Rey. 2005. International financial adjustment. NBER Working Paper no. 11155. National Bureau of Economic Research, February.
- Heathcote, J., and F. Perri. 2002. Financial autarky and international business cycles. *Journal of Monetary Economics* 49 (3): 601–27.
- . 2004. Financial globalization and real regionalization. *Journal of Economic Theory* 119: 207–43.
- Hooper, P., and J. Marquez. 1995. Exchange rates, prices, and external adjustment in the United States and Japan. *Understanding interdependence*, In ed. P. Kenen, 107–68. Princeton, NJ: Princeton University Press.
- Julliard, C. 2002. International portfolio diversification is not worse than you think. Princeton University.
- . 2004. Human capital and international portfolio choice. Princeton University. Secondary Job Market Paper, October.

Kollmann, R. 1991. *Essays on international business cycles*. Ph.D. dissertation. Economics Department, University of Chicago.

———. 1995. Consumption, real exchange rates, and the structure of international asset markets. *Journal of International Money and Finance* 14: 191–211.

———. 1996. Incomplete asset markets and the cross-country consumption correlation puzzle. *Journal of Economic Dynamics and Control* 20 (5): 945–62.

———. 2006a. A dynamic general equilibrium model of international portfolio holdings: Comment. *Econometrica* 74 (1): 269–73.

———. 2006b. International portfolio equilibrium and the current account. Centre for Economic Policy Research Working Paper no. 5512.

Lane, P., and G. M. Milesi-Feretti. 2003. International financial integration. IMF Working Paper no. WP/03/86. Washington, D.C.: International Monetary Fund.

———. 2005. A global perspective on external positions. International Institute of Informatics and Systems (IIIS) Discussion Paper 79, Trinity College Dublin.

———. 2006. The external wealth of nations mark II. IMF Working Paper no. 06-69. Washington, D.C.: International Monetary Fund.

———. 2007. Europe and global imbalances. *Economic Policy* 22 (51): 519–73.

Lane, P., and J. Shambaugh. 2007. Financial exchange rates and international currency exposures. NBER Working Paper no. 13433. Cambridge, MA: National Bureau of Economic Research, September.

Lewis, K. 1999. Explaining home bias in equities and consumption. *Journal of Economic Literature* 37: 571–608.

Lucas, R. 1982. Interest rates and currency prices in a two-country world. *Journal of Monetary Economics* 10 (3): 335–59.

Lustig, H., and S. Van Nieuwerburgh. 2005. The returns on human capital: Good news on Wall Street is bad news on main street. NBER Working Paper no. 11564. Cambridge, MA: National Bureau of Economic Research, August.

Martin, P., and H. Rey. 2004. Financial supermarkets: Size matters for asset trade. *Journal of International Economics* 64, 335–61.

———. 2006. Globalization and emerging markets: With or without crash? *American Economic Review* 96 (December): 1631–51.

Obstfeld, M. 2007. International risk sharing and the costs of trade. The Ohlin Lectures, Stockholm School of Economics. 23–24 May, Stockholm, Sweden.

Obstfeld, M., and K. Rogoff. 2000. The six major puzzles in international macroeconomics: Is there a common cause? In *NBER macroeconomics annual, 2000* ed. Bernanke and K. S. Rogoff, 339–90. Cambridge, MA: MIT Press.

Pavlova, A., and R. Rigobon. 2004. Asset prices and exchange rates. *Review of Financial Studies*.

Rotemberg, J., and M. Woodford. 1999. The cyclical behavior of prices and costs. In *Handbook of Macroeconomics*, vol. 1C ed. J. B. Taylor and M. Woodford, 1051–1135. North Holland: Elsevier.



Tille, C. 2005. Financial integration and the wealth effect of exchange rate fluctuations. Federal Reserve Bank of New York Staff Report 226.

Tille, C., and E. van Wincoop. 2007. International capital flows. NBER Working Paper no. 12856. Cambridge, MA: National Bureau of Economic Research, January.

Uppal, R. 1993. A general equilibrium model of international portfolio choice. *Journal of Finance* 48 (2): 529–53.

van Wincoop, E., and F. Warnock. 2006. Is home bias in assets related to home bias in goods? NBER Working Paper no. 12728. Cambridge, MA: National Bureau of Economic Research, December.

## Appendix

### *Stylized Facts on International Portfolios*

**Table 5A.1**  
Home bias in equity portfolios

Country	(1) Country's share in world market capitalization (%)	(2) Share of domestic stocks in the aggregate portfolio (%)	(3) Share of domestic stocks in investment funds portfolios (%)	(4) Portfolio home bias $= \log \left( \frac{\text{column 3}}{\text{column 2}} \right)$
United States	47.8	88.7	85.5	0.62
United Kingdom	8.1	77	43.1	2.25
Japan	11.3	89.5	71.8	2.06
France	4.3	79.8	55.3	2.92
Germany	4.0	61.3	33.5	2.72
Canada	2.4	84	27.0	3.55
Italy	2.2	67.3	35.4	3.42
Switzerland	2.2	45.6	21.0	3.03
Netherlands	2.0	43.6	19.5	3.03
Spain	1.4	86	36.0	4.11
Australia	1.2	71.7	18.2	4.09

Sources: Chan, Covrig, and Ng (2005), CPIS data.

Notes: Column 2 measures the share of domestic stocks in countries portfolios in 2001 for the biggest market capitalization. Column 3 measures the share of domestic stocks in a representative sample of mutual funds, averaged over the period 1999–2000.

**Table 5A.2**  
 Currency exposure of international portfolios in 2005 (percent of country's GDP)

Country	Net external position	Net domestic currency position	Net U.S. dollar position	Net other currencies position
China	12.5	-28.3	29.2	11.6
Euro Area	-15.0	-65.5	16.8	34.5
Japan	35.9	-26.9	38.5	21.9
United States	-21.5	-74.8	-74.8	53.4

Source: Lane and Milesi-Feretti (2006b).

### Model Variants with Correlated Shocks: Equilibrium Portfolios

In the case of a nonzero correlation between relative output and capital share shocks, the equilibrium portfolio is:

$$S = \frac{1}{2} - \frac{1}{2\bar{k}} \frac{2a(2a-1)(\phi-1)(1-1/\sigma)\sigma_{\Psi}^2(\sigma_y^2 + \sigma_{y,k})}{2a(\phi-1)(\lambda-1)(\sigma_y^2 + 2\sigma_{y,k} + \sigma_k^2)\sigma_{\Psi}^2 + \sigma_y^2\sigma_k^2 - \sigma_{y,k}^2} \quad (36)$$

$$+ \frac{1}{2\bar{k}} \frac{2a(\phi-1)(\lambda-1)\sigma_{\Psi}^2(\sigma_k^2 + \sigma_{y,k}) + \sigma_y^2\sigma_k^2 - \sigma_{y,k}^2}{2a(\phi-1)(\lambda-1)(\sigma_y^2 + 2\sigma_{y,k} + \sigma_k^2)\sigma_{\Psi}^2 + \sigma_y^2\sigma_k^2 - \sigma_{y,k}^2} - \frac{1-\bar{k}}{2\bar{k}}$$

$$b = -\bar{k}(1-S) \frac{\sigma_k^2}{\sigma_{\Psi}^2} \frac{1}{1 + \frac{\sigma_{y,k}}{\sigma_y^2}} \left[ \frac{\sigma_{\Psi}^2}{\sigma_y^2} \left( 1 + \frac{\sigma_{y,k}}{\sigma_k^2} \right) - \frac{1 - \left( \frac{\sigma_{y,k}}{\sigma_y\sigma_k} \right)^2}{2a(\phi-1)} \right] \quad (37)$$

where  $\sigma_{y,k}$  is the covariance between  $\hat{y}$  and  $\hat{k}$ .

In the case of a nonzero correlation between relative output and iPod shocks, the optimal portfolio is:

$$S = 1 - \frac{1}{2\bar{k}} \quad (38)$$

$$\times \frac{2a(\phi-1)(\sigma_{\Psi}^2\sigma_y^2 - \sigma_{y,\Psi}^2)[(2a-1)(1-1/\sigma) + \lambda - 1]}{2a(\phi-1)(\lambda-1)[\sigma_{\Psi}^2(\sigma_y^2 + \sigma_k^2) - \sigma_{y,\Psi}^2] + \sigma_y^2\sigma_k^2 - \sigma_k^2\sigma_{y,\Psi}[\lambda - 1 + 2a(\phi-1)]}$$

$$b = -\bar{k}(1-S)\sigma_k^2 \left[ \frac{2a(\phi-1)(\sigma_{\Psi}^2 + \sigma_{y,\Psi}) - (\sigma_y^2 + \sigma_{y,\Psi})}{2a(\phi-1)(\sigma_{\Psi}^2\sigma_y^2 - \sigma_{y,\Psi}^2)} \right]$$

where  $\sigma_{y,\Psi}$  is the covariance between  $\hat{y}$  and  $\hat{\Psi}$ .