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THE INCENTIVE EFFECTS OF PRIVATE PENSION PLANS

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### ABSTRACT

The proportion of workers covered by pensions has increased very substantially over the past two or three decades, and in particular the number of older workers with pensions continues to increase. During the same period, and especially in the past decade, the labor force participation of older workers has declined dramatically. These two trends may well be related. This paper examines the incentive effects of private pensions. We find that the provisions of pension plans provide very substantial incentives to terminate work at the current job after the age of early retirement and even greater incentives to leave after the age of normal retirement. It is not unusual for the reduction in pension benefit accrual after these retirement ages to equal the equivalent of a 30 percent reduction in wage earnings. In addition to a potentially large impact on labor force participation of older workers, pension plan provisions are likely to have important effects on labor mobility of younger workers.

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#### THE INCENTIVE EFFECTS OF PRIVATE PENSION PLANS

by

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The proportion of workers covered by pensions has increased very substantially over the past two or three decades, and in particular the number of older workers with pensions continues to increase. During the same period, and especially in the past decade, the labor force participation of older workers has declined dramatically. The juxtaposition of these two trends suggests the possibility that they may be related. In this paper, we examine the stipulations of private pension plans with a view to analyzing the incentive effects created by their provisions. We find that the provisions of pension plans provide very substantial incentives to terminate work at the current job after the age of early retirement and even greater incentives to leave after the age of normal retirement. While analysis of the plan provisions suggests a potentially large effect of pension plans on labor force participation, the evidence does not directly demonstrate that pension related work incentives did indeed cause workers to leave the labor force earlier. Such conclusions must rely on the association of individual retirement decisions with the provisions of individual pension plans - an analysis that must await data as yet held from public use. Nonetheless, examination of the structure of pension plans suggests the likelihood of a very sizeable effect of plan provisions on labor force participation. The analysis of plan provisions also allows inferences about the cost in pension benefits of job change. In addition, the examination of plan provisions allows consideration of the differential cost of pension plans for men versus women. The wide diversity of plans and the corresponding wide diversity of the pension related work incentives is a major theme of the paper.

In an earlier paper Kotlikoff and Wise (1984) emphasized the apparent inconsistency of pension accrual profiles with a spot market view of the labor market. The evidence in this paper, particularly the analysis of post normal retirement benefit accrual and supplemental benefit formulae, provides even stronger demonstration of the inconsistency. In contrast to the earlier paper which considered only a limited number of plans with earnings related benefit formulae, this paper includes the entire universe of defined benefit pension plans.

### I. Background

#### A. Vested Pension Benefit Accrual Profiles

Information on the value of annual vested accrued pension benefits for workers of different ages and with different amounts of service is useful for displaying a variety of pension incentive effects. Vested pension benefit accrual at age a, I(a), equals the difference between pension wealth at age a + 1, Pw(a + 1), and pension wealth at age a, Pw(a), accumulated to age a + 1 at the nominal interest rate r, i.e.:

(1) I(a) = Pw(a + 1) - Pw(a)(1 + r).

Pension wealth at age a is defined as the expected value of vested pension benefits discounted to age a. Intuitively Pw(a) can be thought of as the worker's pension bank account. If I(a) equals zero, the worker continuing

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employment with the plan sponsor at age a has exactly the same pension wealth at age a + 1 as an identically situated worker who terminates employment at age a. Pension accrual is thus the increment to pension wealth in excess of the return on the previously accumulated pension bank account. Throughout the paper we express pension accrual increments as a fraction of the worker's wage, W(a). Specifically R(a,t) denotes the ratio of I(a) to W(a) for a worker age a with t years of service.

The appendix presents formulae for pension benefit accrual for a very simple defined benefit pension plan, emphasizing the change in the formula at ages of full or partial vesting, at early retirement age, and after normal retirement. This analysis explains why many pension age-accrual profiles show sizeable discontinuities at vesting, and early and normal retirement. It is useful here to provide a brief summary of the implications of these formulae. The discontinuities in age accrual profiles associated with vesting are fairly obvious; in the case of cliff vesting (100 percent vesting occurring at a particular age) Pw(a) in (1) equals zero prior to the age of vesting and suddenly becomes positive at the full vesting age. Hence I(a) is zero prior to cliff vesting and rises to a positive value at the cliff vesting age, a\*; on the other hand, I(a\* + 1) is smaller than I(a\*) because it represents the difference in two pension wealth numbers, rather than simply the value of one (Pw(a\*)).

Another discontinuity in I(a) occurs, for most plans, at early retirement. This discontinuity occurs for plans that reduce early retirement benefits using a formula that is less than actuarially fair, and the lower the reduction the greater the decline in I(a). To see this note that prior to the early retirement age Pw(a) is not influenced by the early retirement reduction

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rate since workers are assumed to start collecting their vested benefits at the most lucrative date, which is almost invariably the age of early retirement; taking benefits at early retirement generally provides a larger present value of vested pension benefits accrued up to this age than opting to begin collecting these accrued benefits later. This reflects the use by pension plans of reduction rates in computing early retirement benefits that are typically lower than the actuarial rate. While Pw(a) and I(a) are independent of the reduction rate prior to early retirement, they are both functions of the reduction factor after early retirement. The smaller the reduction factor, the closer Pw(a) will be to  $\dot{P}w(a + 1)$ , holding other factors constant, and the smaller will be I(a). This is important since the reduction factors of most plans are fairly small providing substantially less than an actuarial reduction.

A second, more fundamental reason for smaller increments after the early retirement age involves discounting. Prior to early retirement an extra dollar of benefits has a higher present value in the Pw(a + 1) formula than in the Pw(a) formula because at age a + 1 the worker is one year closer to receipt of these additional benefits than at age a. After the early retirement age benefits are available immediately and, ignoring the worker's shortening life span, an extra dollar of benefits at age a + 1 has the same present value as an extra dollar at age a. Stated differently, after early retirement there is no special advantage from raising benefits next year over this year because, like additional benefits earned next year, additional benefits earned this year become available immediately. This lack of discounting after benefits are available raises Pw(a) relative to Pw(a + 1) which implies a smaller annual pension accrual, I(a), and smaller values of R(a,t).

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A third factor leading to a drop in I(a) at early retirement is the shorter life span during which benefits will be collected if retirement from the Olan is postponed. This factor does not enter into the calculus for I(a) prior to early retirement because, conditional on reaching early retirement, both Pw(a + 1) and Pw(a) are based on the same potential lifespan of the worker.

Each of these three factors also plays a role in the significant decline in I(a) at normal retirement. Most pension plans do not increase annual benefits for workers electing to postpone receipt of pensions in years after normal retirement. This implicit zero reduction rate means a smaller value of incremental accrued benefits. The second factor involved in the drop in I(a)after early retirement is the change in discounting of Pw(a) relative to Pw(a + 1). This feature continues after normal retirement as well because benefits remain immediately available. Finally, beyond the normal retirement age there is a more rapid reduction in expected lifespan and, therefore, in the expected duration of benefit receipt if the worker postpones retiring. This feature also lowers I(a).(See Appendix).

While these three features help explain low and even negative values of I(a) after normal retirement, other provisions produce sharp declines in I(a) at normal retirement. According to data in the 1979 BLS Level of Benefits Survey 23 percent of covered workers are enrolled in plans that do not credit service at all after normal retirement. Another 30 percent of covered workers are in plans that provide limited credit after normal retirement, and the remaining pension participants are in plans that credit all service during all years after normal retirement. Plans that provide limited credit typically credit service until the worker reaches a specified age, about age 70 on average.

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Once plans stop crediting service they either (1) commence benefit payments immediately regardless of the recipient's work status, (2) defer pension benefits until the worker actually retires, or (3) defer payment until retirement, but actuarially increase the benefit. Of the participants in the plans that provide no or limited credit, 15 percent receive immediate payments, 76 percent receive deferred payments with no actuarial increase, and the rest receive deferred payments with an actuarial increase.

## B. <u>Implication of Pension Accrual Discontinuities for Viewing Lebor</u> Market Equilibrium

If the labor market exhibits spot market equilibrium, I(a) plus the worker's non-pension compensation at age a, W(a), equals the worker's marginal product at age a, M(a):

(2) M(a) = W(a) + I(a).

Under the spot market assumption workers always receive M(a) regardless of the firm or its pension plan. If I(a) is smaller in one firm that another, W(a) must be larger in the firm with the smaller value of I(a) to insure equality of total annual compensation across firms. Since in a spot market equilibrium workers can freely move from one firm to another and firms can freely fire any worker demanding more than M(a), only accrued vested benefits will have any economic value; if the value of this year's pension benefits reflected anything other than those to which the worker had legal title, either the worker or the employer would have an incentive to terminate the employment relationship. Note that the terms in (1) incorporate the spot market free mobility assumption in that workers are assumed to choose the most advantageous date to start collecting previously accumulated benefits since "retiring" for purposes of

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collecting a pension from one firm does not preclude subsequent work in another firm paying M(a).

Obviously, if W(a) is a smooth function of age, and I(a) exhibits sharp discontinuities, M(a) must exhibit sharp discontinuities at these same ages to satisfy (2). Casual empiricism suggests that W(a) changes smoothly with age, or at least does not abruptly change precisely at ages when I(a) exhibits sharp changes. There is also no reason to believe that M(a) abruptly changes with age to satisfy (2); hence the sizeable discontinuities reported here in the I(a)profile appear strikingly at odds with the spot market condition (2).

## C. Calculating Vested Benefit Accrual Profiles

This study calculates accrual profiles for 2342 of the 2492 plans identified by the ELS as useable.<sup>2</sup> Throughout the paper we focus on the age profiles of the ratios of I(a) to W(a); i.e., we express the pension increments at age a as a fraction of the wage at age a. We utilize the survey's weights in presenting various average accrual profiles. The weights reflect the plan's fraction of total pension participants. To construct accrual profiles for plans which base their benefits on earnings we used a set of industry- and occupationspecific cross section age earnings profiles estimated from CPS data. Longitudinal age earnings profiles were obtained by assuming 6 percent overall growth in wages and adding to this the wage growth by age estimated by the CPS cross section data. Kotlikoff and Wise (1984) describe these estimates in detail. In the analysis here we assume that wage earnings after age 65 remain constant in nominal dollars. Our actuarial calculations employ a 9 percent nominal interest rate and use a unisex mortality table, which represents an

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average of male and female mortality probabilities. Unlike the simple formulae in the appendix, our calculations take account of the worker's survival probabilities prior to retirement as well as after retirement.

The BLS Level of Benefits Survey contains highly detailed information concerning the sampled pension plans' vesting provisions, requirements for early and normal retirement, the specifics of their normal and supplemental benefit formulae, and the crediting of service and payment of benefits for those working beyond the normal retirement age.

There is a very considerable amount of diversity in the particular provisions of private plans which generate sizeable differences in vested pension benefit accrual. Many seemingly minor features of a plan can have very important effects on benefit accrual. For example, consider a stipulation that service is credited for only 25 years in a plan that permits early retirement at 62. For a worker hired at age 30 the accrual at age 55 will decline sharply to zero and remain at zero until the early retirement age. Without this ceiling on credited service, accrual between ages 55 and 62 could be very sizeable; the weighted average ratio of pension accrual to the wage is roughly 15 percent in our sample of plans with age 62 early retirement. Other examples of very important "details" of pension provisions are age and service requirements for supplemental benefits, ceilings on the amount by which social security benefits can be used to offset pension benefits, maximum values of pension benefits, discontinuous changes by age in the rate of benefit reduction for early retirement, and maximum ages for plan participation. Each of these features, as well as numerous others not mentioned, can produce sharp discontinuities in I(a) at ages other than the ages of vesting, early retirement, and normal retirement.

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Our calculations take into account each of the seemingly "minor" as well as major pension provisions included in the data.

The considerable variation in plan features within industry and occupation and, consequently, accrual profiles raises several important issues about the functioning of U.S. labor market. First, equally productive workers are likely to face very different incentives to change jobs or retire because of pension plans. Second, the heterogeneity in accrual profiles across plans suggests that equally productive workers in the same industry and occupation, but in different plans, may be receiving quite different amounts of total compensation both on an annual and on a lifetime basis. Third, equally productive workers of different sexes or ages who join the same pension plan in a firm at the same time are likely to receive very different labor remuneration, even if the quality and quantity of their labor supply is equivalent. Fourth, the complex calculations required to compute the accrual of vested benefits and, therefore, the compensation one is currently receiving, calls into question the understanding of pension compensation both on the part of employers and workers.

#### II. Pension Accrual Profiles for Percent of Earnings Plans

Percent of earnings plans are discussed in this section and flat (non earnings related) plans in the next. Variation in pension accrual profiles by early and normal retirement ages is discussed first, followed by a discussion of the wide variation among plans holding early and normal retirement ages fixed. Next we consider the effect of social security offset provisions and also examine accrual profiles by industry and by occupation. Then the effects of alternative post-normal-retirement provision are discussed. Finally there is an

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analysis of the effects on accrual profiles of early and normal retirement supplements. The cost in pension wealth of job change is discussed in section IV. Section V describes the differences in the pension cost of hiring women versus men.

# A. The Decline in Pension Wealth Accrual at Early and Normal

## Retirement Ages

Average accrual profiles for the percent of earnings plans with 10-year cliff vesting are shown in table 1 by early and normal retirement ages. Three of these average profiles corresponding to plans with the respective early and normal retirement ages --55-55, 55-65, 65-65--are graphed in figure 1. In this and subsequent figures and tables, annual accrued pension benefits are expressed as a ratio of the wage. The graph depicts the very substantial declines in the rate of pension wealth accrual at several critical ages. The first is the age of normal retirement, which equals the age of early retirement for plans with no early retirement option. Second, there is also a sharp decline in the rate of accrual at the age of early retirement, but this decline is substantially lower than the decline at the normal retirement age.<sup>3</sup> Third, there is a very substantial decline between ages 65 and 66 in the average accrual rate no matter what the ages of early and normal retirement.

The actual declines in average accrual rates at these critical ages indicated in table 1 are highlighted in table 2. The ages of early and normal retirement are identical in columns 1, 4, 6, and 8 of the table with respective retirement ages of 55, 60, 62, and 65. At these ages the accrual rates as a percent of wages decline from .26 to 0, .27 to -.06, .25 to -.13, and .21 to -.19 respectively. Thus, at these ages the total annual compensation (wage plus

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				+		+		<u> </u>
Early Ret.	55	55	55	60	60	62	62	65
Normal Ret.	55	60	65	60	65	62	65	65
No. of Plans	152	115	513	78	53	19	8	50
Age								
40	.244	.111	.071	.034	.047	.038	.054	.036
41	.045	.022	.013	.007	.010	.016	•009	.010
42	.051	<b>.02</b> 6	.016	.008	•011	.017	.010	.011
43	.058	.029	.018	.010	.013	.120	•011	.012
44	.066	•033	<b>.02</b> 0	.011	•015	.029	.013	.014
45	•075	<b>.03</b> 6	•023	.013	.017	.036	.013	•016
46	.085	.043	<b>.</b> 026	.016	.019	.042	•015	<b>.</b> 018
47	•0 <del>9</del> 7	<b>.05</b> 0	.031	.028	•022	.047	.017	.021
48	.110	•057	<b>.</b> 035	.039	.025	.054	•019	.024
49	.124	•064	•040	.056	.029	.060	.021	.027
50	.141	•077	<b>.</b> 046	.065	.034	.068	.023	.031
51	.159	•072	•052	.084	.040	.077	<b>.02</b> 6	.033
52	<b>.</b> 180	.087	.062	.091	.050	.090	.028	.043
53	.204	•099	.072	.105	<b>.06</b> 0	.101	.032	.050
54	<b>.</b> 231	<b>.</b> 113	.083	.117	•068	.114	.035	.055
55	<b>.</b> 261	.130	.097	.149	.082	.128	.039	.065
56	003	.100	.068	.170	.094	.144	•0 <b>3</b> 6	.068
57	012	.111	•072	.192	.107	.162	.039	.076
58	020	<b>.</b> 118	•076	.224	<b>.</b> 127	. 184	•044	.089
59	028	.129	•077	.241	.146	.208	•048	.105
60	038	.143	•079	.269	.167	.241	<b>.</b> 054	.118
61	048	090	•068	061	.113	.220	<b>.</b> 059	.128
62	058	091	.064	091	<b>.</b> 115	.248	<b>.06</b> 6	.145
63	067	091	•056	114	.114	130	•017	.163
64	076	092	<b>.</b> 053	-,121	.114	136	.012	<b>.</b> 186
<b>6</b> 5	<b>-</b> .085	094	.044	121	.112	-,144	.006	.211
66	292	169	152	138	088	266	081	194
67	294	174	162	155	115	-,263	<b>08</b> 0	204
68	295	<b>-</b> .179	171	171	142	260	079	213
69	296	182	179	184	162	258	078	<b>2</b> 21
70	297	184	186	196	182	255	-,077	234

Table 1. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting, by early and normal retirement age.<sup>a</sup>

a. Plans with early or normal retirement supplements are excluded.



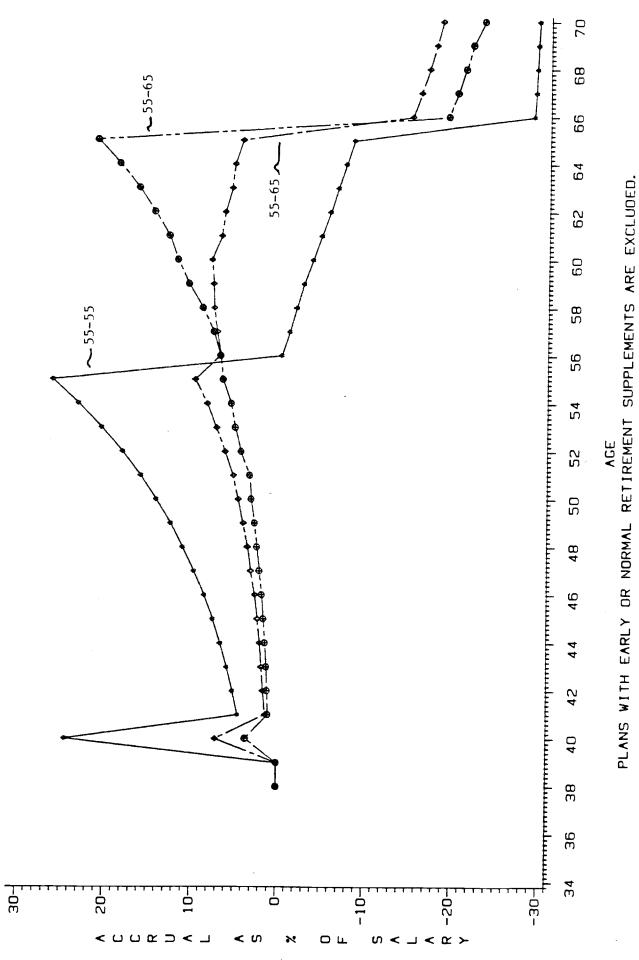


Table	2.
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		Ear	ly and	Normal F	Retiremer	it Age		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Age	55	55	55	60	60	62	62	65
vãe	<b>5</b> 5	60	65	60	65	62	65	65
40	.244	.111	.071	.034	.047	.038	.054	<b>.03</b> 6
55 56	.261 003	•130 •100	.097 .068					
50 51		.143 090	Ī	.269 061	.167 .113			
52 53						.248 130	.066 .017	
65 66	085 292	094 169	•044 - •152	121 138	.112 088	144 266	.006 081	•211 -•194
70	<b>-,2</b> 97	184	186	196	182	<del>-</del> .255	077	234
-66	<b>2</b> 0	8	19	2	20	12	8	40

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pension accrual) from working declines by 21 percent, 26 percent, 30 percent, and 33 percent respectively. Surely then the incentive to continue work with the current employer past these ages is very substantially reduced.

In instances where early and normal retirement ages do not coincide, there is also a very substantial decline in the ratio of pension accrual to the wage at the age of normal retirement. For example, among plans with early retirement at 55 and normal retirement at 60 the decline is from .14 to -.09. There is also a decline at the age of early retirement for these plans, although it is considerably less substantial than the decline at the age of normal retirement. For example, of plans with early retirement at 55 and normal retirement at 65 the decline at 55 is from .10 to .07, while at 65 the decline is from .04 to -.15.

Finally, in all cases there is a substantial decline in the rate of pension accrual between ages 65 and 66. The effective reduction in compensation ranges from 8 percent to 40 percent of the wage rate except for plans with early and normal retirement at 60, in which case the decline is from -.12 to -.14. Thus while the stipulations of plans vary tremendously, these plans, on average, seem to provide a substantial inducement to retirement after age 65, no matter what the inducement before this age.

The figure and the table also show a large variation in average pension accrual at 40, the age of cliff vesting. It is highest, on average, for plans with early and normal retirement at 55 and lowest, on average, for plans with early and normal retirement at 65. As mentioned, because the early retirement reduction is typically less than actuarially fair, pension wealth is generally greatest if benefits are taken at the age of early retirement. Thus the accrued

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wealth at the age of vesting is usually calculated by discounting benefits from the age of early retirement, assuming that the worker could begin to collect benefits at that age. Figure 1, for example, shows a vesting spike of almost 25 percent of earnings for 55-55 plans, 7 percent of earnings for 55-65 plans, and about 4 percent of earnings for 65-65 plans.

In summary, it seems apparent that continuation in the labor force after the age of normal retirement and sometimes early retirement as well typically involves a substantial reduction in compensation because of the very large declines in the rate of pension wealth accrual. After the age of 65, there is typically a substantial loss in pension accrual, no matter what the ages of early and normal retirement. And, the sharp changes in average pension accrual at particular ages provides rather strong prima facia evidence against annual spot market clearing; neither wages nor marginal products appear to adjust at these critical ages to meet the spot market equilibrium condition written in (1).

#### B. Variation Among Plans

Even among plans with the same early and normal retirement ages there is wide variation in accrual rates at each age, particularly after the age of early retirement. To demonstrate this fact, average accrual rates for the 513 plans of table 1 with early retirement at 55 and normal retirement at 65, together with median, maximum, minimum and upper and lower 5 percentile levels, are shown in table 3. The lower 5 percentile points for any age group for example is that accrual rate such that 5 percent of plans have accruals below that level. The upper 5 percentile point is defined analogously. Consider the accrual ratio at vesting. While the average vesting ratio for this smaple is

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	Weighted Average Accrual Ratios	Median Accrual Ratios	Minimum Accrual Ratios	Max1mum Accrua1 Rat1os	Lowest 5th Percen- tile	Largest 5th Percen- tile
No. of Plans	513	513	513	513	513	513
Age	+					
40	.071	.021	0	.383	0	<b>.</b> 201
41	.013	.012	025	.071	0	.036
42	•016	.013	025	<b>.08</b> 0	0	.041
43	.018	.014	027	.091	0	<b>.04</b> 6
44	.020	.016	026	<b>.</b> 103	0	.052
45	.023	.019	029	.116	0	•058
46	<b>.</b> 026	.023	028	<b>.13</b> 1	0	•066
47	.031	.028	024	.162	0	.076
48	•034	<b>.</b> 032	020	.167	0	.083
49	.040	.039	020	.188	0	.093
50	.046	.046	011	.212	0	.106
51	۵5 <u>2</u> و05	<b>.</b> 052	<b>-</b> .020	.240	0	.119
52	•062	<b>"0</b> 61	019	.270	0	.140
53	.072	.072	<b>-</b> _015	.305	0	.157
54	•083	.083	<b>-</b> •015	.344	0	<b>.</b> 180
55	.097	.100	005	.405	0	.208
56	<b>.06</b> 8	.075	065	.424	0	.165
57	.072	.079	-,063	<b>.3</b> 63	0	<b>.</b> 171
58	.076	.083	051	.248	0	.183
59	<b>077</b>	.083	046	.286	<b>0</b> 006	.190
60	.079	.086	<b>-</b> •064	.345	014	.204
61	.068	.074	156	.339	<del>-</del> .038	.181
62	•064	<b>.</b> 068	154	.325	<b>0</b> 50	.190
63	•056	•062	192	.310	-,115	<b>.</b> 191
64	•053	<b>.0</b> 60	221	.460	119	.210
65	.044	.052	<b>32</b> 3	.326	148	<b>.2</b> 05
66	<b>-.</b> 152	136	558	.121	- <u>-</u> 203	
67	<b></b> 162	159	550	.060	406	0
68	171	179	-,541	.043	-,412	0
69	<b>1</b> 79	190	534	.029	414	0
70	<b></b> 186	197	618	.014	424	0

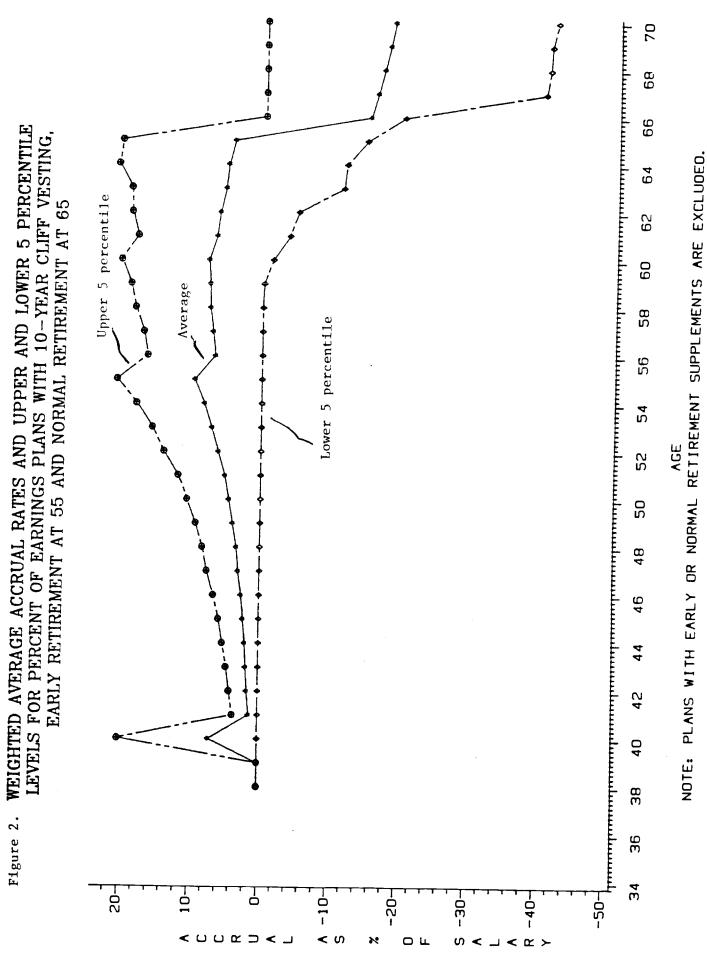
Table 3. Dispersion of accrual ratios for table 1 plans with age 55 early retirement and age 65 normal retirement. .071, the median is .021, the maximum is .383, and the minimum is 0. The ratio at the lowest 5th percentile is 0, while it is .201 for the largest 5th percentile. A similarly large dispersion in annual accrual ratios is indicated for each of the ages 40 through 70. Weighted average accrual rates together with upper and lower 5 percentile levels are graphed in figure 2. While the average accrual rates between ages 55 and 65 are positive, for many plans the rates by 65 are very negative. Thus it is important to base judgements about the labor force participation incentive effects of pension plans not simply on the basis of average accrual rates.

Additional evidence of the variability of pension accrued profiles is obtained by comparing profiles of particular plans. Figure 3 plots the accrual profiles of four of the sample's 30 largest plans. Plan 1 exhibits a 29 percent vesting spike, a reduction of 30 percentage points in the accrual ratio at age 55 and a further major reduction at age 65 from -.063 to -.351. In contrast the vesting spike is only 4 percent for plan 2 in the figure. This plan also exhibits no major reduction in the accrual ratio at early retirement and only a minor reduction at normal retirement. Plan 3's vesting spike is much less than that of plan 1, but the drop off of the accrual ratio at age 55 is very much larger than that in plan 1. This plan also exhibits extremely sharp changes in accrual ratios at ages 60, and 63. Plan 4 exhibits even greater discontinuities in the accrual profile. Thus the plans' incentive effects on labor force participation also vary widely.

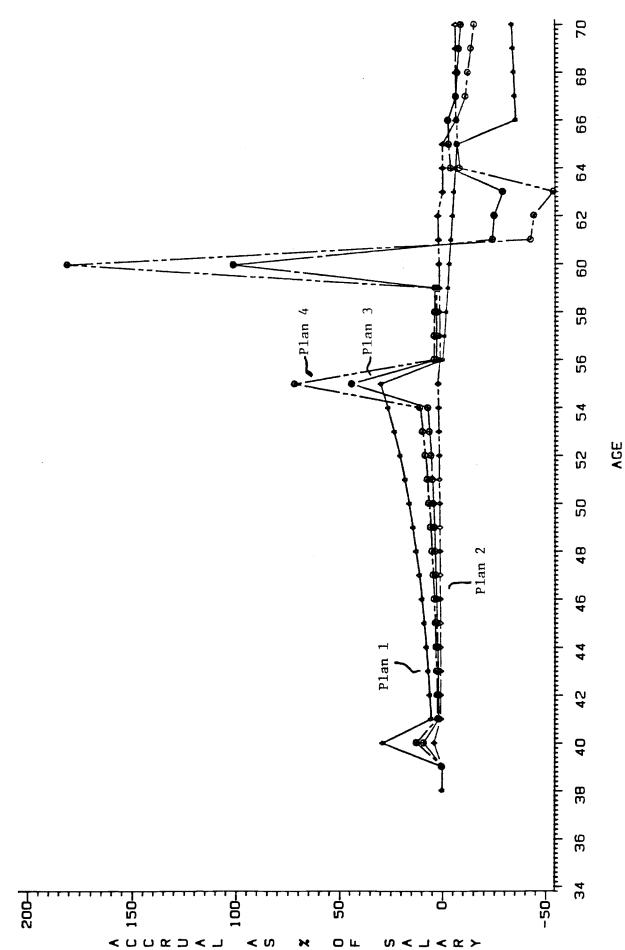
#### C. The Effect of Social Security Offsets

As described above, a substantial number of plans have social security offset provisions, under which pension benefits are reduced by an amount

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depending upon the recipients' social security benefits. The offset provisions vary widely among plans. In some instances the offset is enough to completely eliminate payment of pension benefits from the private pension plan. Private pension benefit payments are typically substantially lower with than without the offset provision. Accrual rates for percent of earning plans with 10-year cliff vesting and early retirement at 55 are shown in table 4 for selected normal retirement ages, with and without social security offset provisions. The average profiles for offset and non-offset plans with early retirement at 55 and normal retirement at 62 are graphed in figure 4. A noticeable difference between the two groups of plans is the relatively large spike at vesting for plans without the offset compared with the low rate of accrual at vesting for plans with the social security offset. In addition, the accrual ratio at 55 is larger for plans without the offset than for plans with it, and the drop in the rate of accrual is substantially larger for plans without than for plans with the offset. The accrual ratio for plans without an offset is .21 at 55 and drops by almost 60 percent to .09 at 56. In contrast, the accrual rate for plans with an offset is about 16 percent at 55 and drops by only about 26 percent to .12 at age 56. Both groups of plans show negative accrual rates after the age of normal retirement, 62, and both groups of plans show much larger negative accrual rates after 65. Table 4 indicates that the relative accrual rates of the two groups for plans with different normal retirement ages are similar to those shown in the figure.

The table also shows that pension accrual at the age of vesting is rather substantial for plans without a social security offset even among plans with normal retirement at 65. The average accrual rate at vesting for all plans

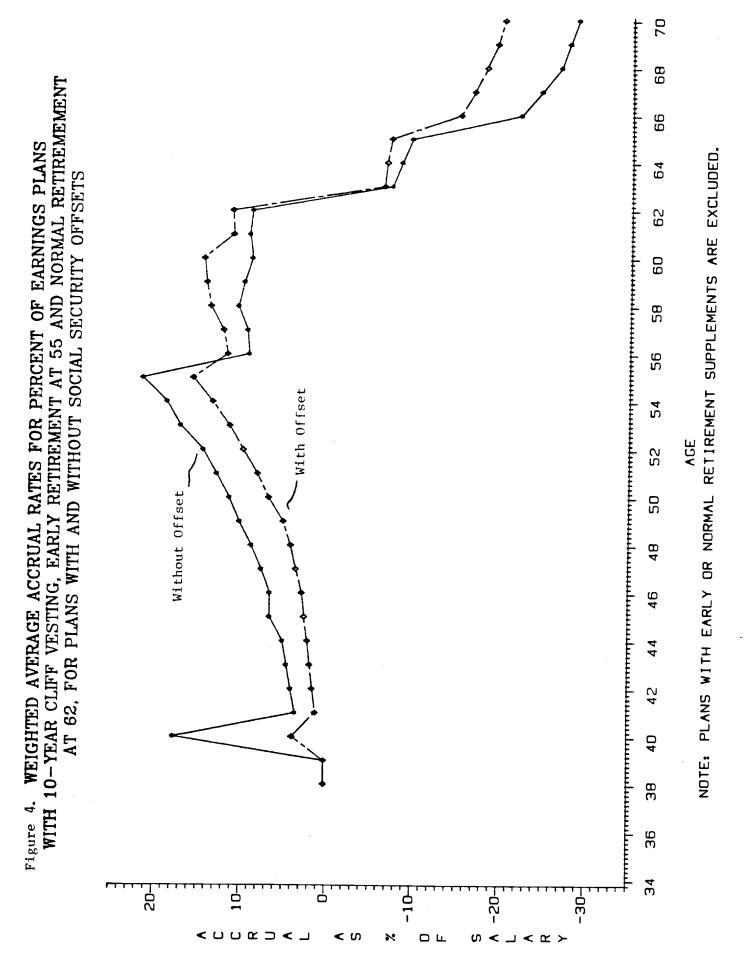
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Normal Ret. Offset				2 w offset	6 w/o offset	5 woffset
No. of Plans	135	17	103	84	254	259
Age						
40	<b>.</b> 260	.073	.175	.030	.121	•016
41	•049	.005	.034	.010	.022	.004
42	<b>.</b> 055	.008	.039	.014	<b>•0</b> 26	.005
43	<b>.</b> 062	.010	.044	.017	•029	<b>.</b> 006
44	•071	.013	.049	<b>.</b> 020	.033	.007
45	<b>.08</b> 0	.017	<b>₀</b> 064	.024	•037	.009
46	<b>.09</b> 0	<b>.03</b> 0	<b>.</b> 064	.027	.041	.011
47	.102	.039	•074	.034	•078	.013
48	.115	<b>.</b> 047	<b>.08</b> 6	<b>•0</b> 40	<b>.</b> 052	.016
49	.130	.061	.100	.049	<b>.</b> 058	.019
50	.147	.074	.112	.066	.065	.025
51	.166	.089	.127	.079	•072	.029
52	<b>.</b> 187	<b>.</b> 108	.143	.096	.081	.041
53	.211	<b>.</b> 127	.165	.112	•091	.051
54	.238	<b>.</b> 146	.185	.132	.102	.062
55	.269	.175	.213	.155	.116	•076
56	008	.042	.090	,115	.078	.058
57	016	<b>.</b> 036	<b>.</b> 092	<b>.</b> 120	<b>.</b> 077	.065
58	-,025	.040	.103	.135	<b>.</b> 076	<b>.</b> 076
59	034	<b>.</b> 034	<b>.</b> 096	.140	<b>.</b> 073	.082
60	043	.025	<b>.</b> 087	.143	.069	.091
61	052	004	<b>.09</b> 0	.109	<b>.</b> 071	<b>.06</b> 6
62	-,062	012	•087	.110	•061	.068
63	071	024	075	066	•047	<b>.06</b> 6
64	081	026	<b>-,08</b> 6	069	•040	.067
65	<b>09</b> 0	032	098	074	•025	.066
66	309	109	-,224	154	203	097
67	309	132	-,248	170	-,212	108
68	308	-,153	<b>-</b> •270	<b>-</b> •184	219	<b>-</b> •119
69	<b>3</b> 07	-,172	<b>-</b> •280	-,196	<b>2</b> 27	128
70	307	191	-,290	204	233	136

Table 4. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting and early retirement at age 55, by normal retirement age and social security offset.<sup>a</sup>

a. Plans with early or normal retirement supplements are excluded.

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with early retirement at 55 and normal retirement at 65 is .071, as shown in table 1 above. It can be seen in table 4 that that accrual is over 12 percent for plans without a social security offset while it is less than 2 percent for plans with a offset.

#### D. Accrual Ratios by Industry and Occupation

## 1. Industry

Accrual profiles for selected industries are shown in table 5. For purposes of comparison and for ease of exposition, profiles are presented only for plans with early retirement at 55 although profiles for three normal retirement ages, 55, 62, 65, are shown. The most apparent difference among industries is in the proportion of plans with particular early and normal retirement ages. For example, in retail trade and services almost all plans have normal retirement at 65, with only a few plans with early retirement at 55 or 62. On the other hand, almost 62 percent of plans in transportation have early and normal retirement at 55, with approximately 20 percent of plans showing normal retirement at 62 and 20 percent at 65. In manufacturing, 66 percent of plans have normal retirement at 65, 28 percent at 62, and about 6 percent at 55.

But among plans with the same early and normal retirement age, table 5 indicates little difference in average accrual profiles across industries. Table 6 isolates accrual ratios at critical ages, in particular before and after the age of early retirement and before and after the age of normal retirement. Averages are only presented for cells with more than 10 plans. Two dashes indicate that there were fewer than 10. The cell was left blank if the corresponding age did not represent a critical age for the plan in question.

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10-year cilff vesting
t of earnings plans with
I rates for percent of
accrua
Weighted average
Table 5.

and early retirement at 55, by industry and normal retirement age.<sup>3</sup>

	Man	Manu factur 1 ng	Ďu		Transportation	+1on	ě	Retail Trade	e		Flnance			Services	
Early Ret.	55	55	55	55	55	55	55	55	55	55	55	55	55	55	55
Normal Ret.	55	62	65	55	62	65	55	62	65	55	62	65	55	62	, j
No. of Plans	22	107	256	120	37	37	2	v	8	2	18	70	r.	~	
egA															
40	.227	•091 	•056	•	.168	.122	.021		•080	• 068	•086	.077	•251	.179	.068
41	•039	6	.011	.048	.035	.021	.020	• 000	.014	.027	• 020			 •033	-013
42	• 045	•024	•013	• 055	•040	.024	•019	•001	<b>.</b> 0126	.033	•023	•020	•053	.037	•015
43	• 051	•028	.015	• 062	<b>04</b> 5	<b>.</b> 027	.018	•001	•017	•039	•026	.023	•060	.042	.017
44	•058	•032	•017	•070	•050	•030	.017	•002	•019	• 048	•031	•026	•068	•048	•019
45	• 066	•037	•020	•029	<b>•</b> 075	•034	.015	*002	•021	•057	•035	•030	•076	•054	•023
46	• 078	.041	•023	060•	•067	•035	.016	•002	•023	• 068	•041	•033	•086	•061	<b>027</b>
47	•080	•050	•026	. 101	•075	•040	•016	•003	•026	• 080	•047	•038	<b>8</b> 60 <b>°</b>	•069	•030
48	. 101	•060	•030	.114	°085	•045	•016	•003	.028	• 095	•054	.044	.110	•078	•034
49	.115	•073	•035	.129	•060	•052	.087	•001	•031	• 109	•067	.050	.124	•087	•041
50	.129	•080	.041	. 146	.110	•060	.110	•015	•035	• 130	.117	•058	.140	660 <b>°</b>	•048
51	. 146	•092	•046	• 165	.127	.067	<b>.</b> 125	•020	•038	.152	<b>13</b> 5	•066	• 157	.111	•056
52	• 165	<b>103</b>	<b>.</b> 052	•187	.147	.081	.140	•022	.043	• 203	.172	•092	.178	.126	•064
_			-				_		_						

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penuj	
Cont	
5.	
Table	

•075	•086	<b>860</b> °	.082	.087	•096	•106	.112	•080	•075	•069	•063	•054	- 144	-, 152	-, 158	-, 164	169
.142	. 160	. 182	. 162	.161	,158	<b>,</b> 153	.1248	.277	.367	075	-,086	960*-	- 406	400	-, 395	-, 390	-, 384
•200	.226	•254	- 010	-,018	-,027	-,035	-045	053	- 062	-,072	-,081	060 -	316	-,311	807	-,302	-,297
.104	.122	.146		•060	.104	.108	.110	660 <b>*</b>	860*	•097	860.	•096	- 167	-, 175	-, 192	-,207	-,222
.193	•220	•250	•	.140	.143	.140	.134	•054	.044	- 003 - "093	-, 100	-, 108	- 187	-"214	-,238	-,245	-,251
.230	.267	• 306	092	083	083	074	064	-,052	-•065	-,078	088	660 <b>*-</b>	- 150	206	-,256	- 300	-,339
•046	•050	•056	•034	•032	•027	•018	<b>018</b>	.013	•002	017	027	-•059	- 156	-,158	-, 160	-, 161	-, 162
•025	•080	<b>860</b> •	. 087	•084	.114	.107	160°	•070	.045	- 040	-,054	-,068	- 160	<b>-</b> ,158	-,157	<b>-</b> ,158	-,159
, 163	.172	• 196	- 182	- 176	-,171	-, 167	-,164	161	-,159	-,158	-,159	-, 106	- 040	-044	- 048	-045	-•050
860*		.127	160	•094	•100	.103	•109	£60 <b>*</b>	•086	•063	•062	<b>,</b> 058	- 206	217	227	-,237	-,246
°178	.201	•228	• 078	°00°	.126	.126	.125	960 <b>°</b>	.087	- 077	-,085	- 094	-,242	<b>-,</b> 276	-,309	-,320	-,329
.211	•238	• 269	- 003	011	019	-,028	-,036	-,045	-054	-,062	-•071		. 300	-,301	-,302	-,302	-,302
•063	•074	•087	.067	•072	.079	.081	•084	•074	•074	.071	•070	•068	-,141	-,152	-,161	-,170	177
.119	.134	.158	.100	660 <b>°</b>	.103	.102	960°	•096	101.	- 080	-,087	<b>-</b> 002	- 158	-,174	-, 189	-,204	-,216
. 187	.211	.240	• 008	-,178	-025	-,035	046	057	-,068	<b>-</b> ,079	-,088	660*-	288	-,288	-,288	-, 288	-,288
53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70

a. Plans with early or normal retirement supplements are excluded.

•

Early and Normal		Indu	istry		
Retirement Ages, Age	Manufac- turing	Trans- portation	Retall Trade	Finance	Services
<b>55</b> 55					
40	<b>.</b> 227	<b>.</b> 257			***
55	<b>.</b> 240	<b>.</b> 269			case with resp
56	008	<b>-</b> .003		555 die au	đia me at
62					
63					
65	099	<b>08</b> 0			
<b>6</b> 6	288	300		9 <b>6</b> a	& <b>-</b> -
70	<b>28</b> 8	302	40 40 m		823 ATH 460
55-62		<u></u>			
40	.091	.168		<b>.</b> 086	800 600 cm
55	<b>.</b> 158	.228	***	<b>.25</b> 0	12-13-00
56	<b>.10</b> 0	.078	60 40 AV	.141	100 MBT 403
62	<b>.1</b> 01	<b>.</b> 087		.044	<b>69</b> 45 44
63	080	<del>-</del> •077	60 m er	093	40 GB 90-
65	-,095	097		108	\$## <b>=</b>
66	-, 158	242		187	
70	-,216	329		-,251	
55-65			···· ··· ·/_ */		
40	<b>.05</b> 6	.122	•080	•077	<b>_06</b> 8
55	.087	.127	<b>.05</b> 6	.146	<b>.</b> 098
56	<b>•0</b> 67	.091	.034	•092	•082
62					
63					
65	<b>•06</b> 8	<mark>05</mark> 8ء	059	.096	.054
<b>6</b> 6	141	<b>-</b> .206	156	167	144
70	177	246	162	-,222	169

Table 6. Weighted average accrual rates at selected ages for percent of earnings plans with 10-year cliff vesting early retirement at 55, early and normal retirement ages and industry. Only in manufacturing and transportation were there a substantial number of plans with early and normal retirement at 55. In these two industries, the accrual profiles look very similar. Three industries had a significant number of plans with early retirement at 55 and normal retirement at 62, and again there seems to be little noticeable difference among the plans by industry. All industries have plans with normal retirement at 65. But even in this case, the profiles seem quite similar. The only possible exception seems to be retail trade, where pension accrual relative to the wage rate is less generous than in the other industry groups.

Nonetheless, a typical worker apparently faces a much greater incentive to leave the labor force early in some industries than in others. For example, a large proportion of workers covered by pensions in transportation would experience a 27 percent reduction in effective compensation by continuing to work between 55 and 56. While at 55, pension accrual would be equivalent to about 27 percent of wage rates for many workers in this industry, if the worker continued in the labor force until age 66, his annual loss in pension wealth would be equivalent to 30 percent of wage earnings at 66. A large proportion of workers in manufacturing have plans with early retirement at 55 and normal retirement at 65. In this case, the accrual at 55 averages about 9 percent of the wage at 55 and declines only to about 7 percent of the wage by 65. But then the accrual rate becomes negative, and if the worker were to continued in the labor force between 65 and 66, the decline in pension accrual would amount to an effective reduction in compensation of about 21 percent.

## 2. Occupation

Among plans with the same early and normal retirement ages, the pension

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accrual ratios do not differ noticeably by occupation. Accrual ratios for professionals, clerical workers, and production workers are shown in table 7 for plans with early retirement at age 55 and 3 normal retirement ages--55, 62, and 65. Plans in the 55-65 group are graphed by occupation in figure 5. It seems clear from the table and the figure that given the age of normal retirement, there appears to be no substantial differences in accrual ratios by occupational group. Consider for example plans with normal retirement at age 55: at age 55, the accrual ratio is .29 for professionals, .25 for clerical workers, and .25 for production workers. At age 66, the accrual ratio has dropped to -.30 for professionals, -.30 for clerical workers, and -.29 for production workers. Similarly, close ratios are observed for the other two normal retirement ages. For example, at age 62 the accrual ratios for plans with normal retirement at 62 are .10 for professionals, .10 for clerical workers, and .10 for production workers. This is not to say that there are no differences in pension coverage by occupational groups. It simply says that conditional on having a plan with given early and normal retirement ages, the accrual ratios for the occupational groups are very similar. The data in table 7 may, however, be concealing intra industry variation in accrual profiles by occupation for given retirement ages.

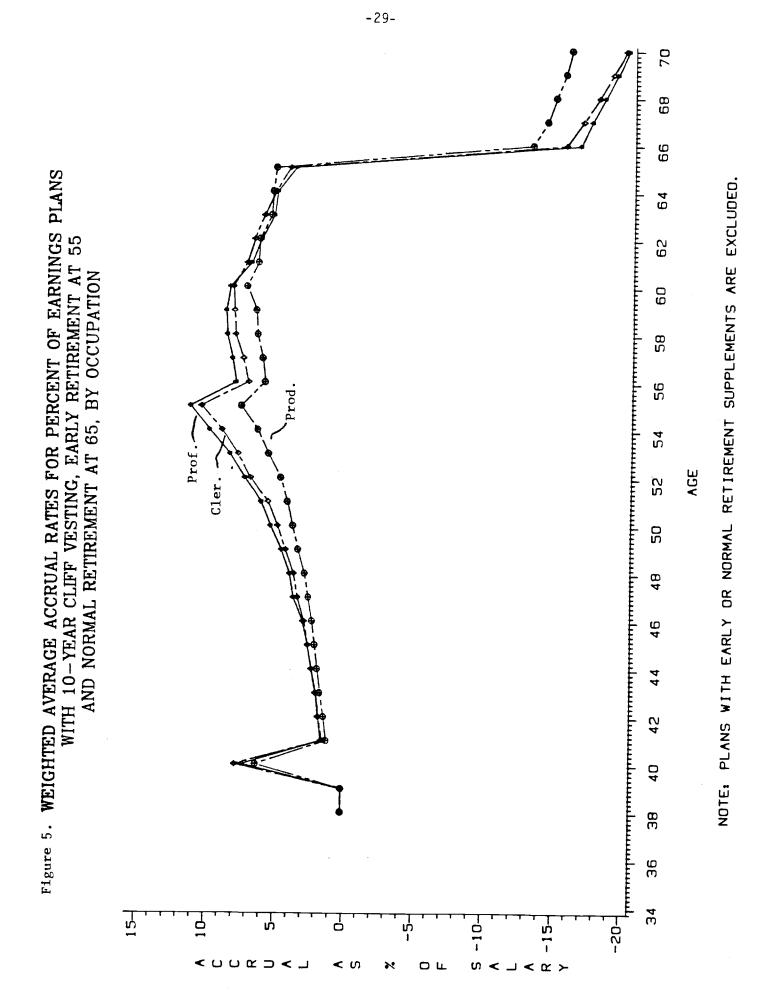
To address this potential ambiguity, accrual ratios for the same plans treated in table 7 are presented in table 8 but only for manufacturing. But here again there is very little difference in the accrual profiles by occupation. Consider, for example, the drop in accrual ratios between age 55 and 66. For plans with normal retirement at age 55, the decline is .58 (.287 minus -.295) for professionals, .51 for clerical workers, and .50 for production workers. Analogous declines are .29 for professionals, .30 for clerical

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	<u>.</u>					•			
Normal Ret.		55			62	·		65	
Occupation	Prof.	Cler.	, Prod.	Prof.	. Cler	Prod.	Prof.	Cler.	Prod.
No. of Plans	53	51	48	75	74	<b>3</b> 8	204	199	110
Age	<u> </u>			<u> </u>					<u></u>
40	.251	.240	.242	.091	.111	.115	.072	•077	.062
41	.047	.046	.044	.020	.023	.024	.015	.014	.011
42	.054	<b>.</b> 052	.050	.026	•027	.028	.017	•017	.013
43	.061	<b>.</b> 059	.056	.030	.031	.032	.019	.019	.016
44	.069	<b>。06</b> 6	.064	.035	.036	<b>03</b> 6	.022	.022	.018
45	.078	•075	<b>.</b> 073	.044	.044	.047	.025	.025	<b>.02</b> 0
<b>4</b> 6	.092	•084	<b>.0</b> 82	.045	,048	.047	.029	.028	.022
47	.105	<b>.</b> 095	.093	.054	.057	<b>.</b> 053	.036	.033	.025
48	.119	.107	.106	.062	<b>.</b> 067	.063	.039	<b>.</b> 036	.028
49	.135	.122	.120	071 ،	.078	<b>.</b> 078	.045	.042	.033
50	.154	.137	.135	.086	.095	.089	.053	.048	.037
51	.175	.154	<b>.</b> 153	.100	.108	.103	.060	.055	.041
52	. 199	.175	.173	.116	.128	.117	.072	.068	.046
53	,226	.196	.196	.132	.147	.141	.083	<b>.</b> 077	.055
54	.256	<b>.2</b> 20	.222	. 155	.166	.160	.098	.089	.063
55	.291	.248	,252	.177	. 191	.187	.112	.104	.075
56	.020	025	005	.102	.113	<b>0</b> 93	.079	.070	.058
57	.012	036	012	.106	.115	.096	.082	.074	.060
58	<b>.00</b> 6	046	020	.116	.127	.112	.086	<b>.080</b>	.064
59	001	-,058	027	.119	.126	.109	<b>.</b> 087	.081	.065
<b>6</b> 0	010	070	035	.118	.121	.104	.084	<b>.0</b> 82	<b>.</b> 072
61	019	087	044	. 103	.098	.097	•069	<b>。</b> 072	.064
62	027	101	052	.100	•098	.096	.062	<b>•0</b> 67	.063
63	036	114	<b>~.0</b> 60	069	077	068	.053	<b>.06</b> 0	•055
64	042	128	068	074	087	074	.051	.052	.054
65	049	140	075	080	098	083	<b>.03</b> 8	.042	.052
66	295	295	290	- 171	203	- 199	167	-, 157	133
67	298	~.298	289	185	223	224	175	169	-, 143
68	303	300	288	199	242	247	184		
69	306	-, 302	-,287	206	252	260			
70	310	304	1			272		-,199	
						1			

## Table 7. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting and early retirement at age 55, by normal retirement age and occupation.<sup>a</sup>

a. Plans with early or normal retirement supplements are excluded.



	+			+			utacturi		
Normal Ret.		55			62			65	
Occupation	Prof.	Cler.	Prod.	Prof	. Cier.	, Prod.	Prof.	Cler.	Prod.
No. of Plans	9	7	6	44	45	18	101	99	56
Age	<u>↓</u>			†			1		
40	.247	.213	.219	.082	.081	.108	.064	•059	•050
4 1	.045	.037	.036	.018	.080	.022	.013	.009	<b>.</b> 010
42	.051	.043	.042	.026	.021	•025	.016	.011	•012
43	.057	•049	.048	.030	.024	.028	.018	•012	.014
44	.064	•056	.054	.035	.028	.032	.021	.015	•015
45	.072	<b>.</b> 065	.063	.040	.032	.036	.024	.017	.018
<b>4</b> 6	.091	•075	.071	.041	•039	.041	.029	<b>.02</b> 0	•020
47	.106	.085	.081	.053	•049	<b>.04</b> 6	.035	.023	.023
48	.120	.096	<b>.09</b> 1	.060	•061	<b>.</b> 059	.040	<b>.02</b> 8	<b>.</b> 026
49	.137	.109	.103	.068	•071	•078	.046	.034	<b>.</b> 030
50	.155	.123	.116	.078	•077	<b>.0</b> 86	.055	<b>.04</b> 0	.034
51	. 175	.139	•132	.089	<b>•08</b> 8	.099	.063	•047	•037
52	. 198	<b>.</b> 158	.148	.100	.100	.110	.072	.053	<b>.04</b> 0
53	.224	<b>.</b> 180	<b>.</b> 167	.114	.116	.126	.084	.064	•050
54	<b>.</b> 253	<b>.</b> 202	.188	.130	•131	.142	.102	•073	.058
55	.287	.231	.216	, 148	.155	.172	.117	•087	<b>.07</b> 0
56	.003	• <b>0</b> 02	018	.089	.113	.099	.085	.071	.055
57	008	006	027	•088	.120	.093	•087	.084	<b>.</b> 057
58	-,015	012	034	.093	.128	<b>.</b> 093	.093	.095	•062
59	<del>-</del> .027	020	044	.095	.127	<b>.</b> 087	.093	.102	.064
<b>6</b> 0	039	028	055	.094	.126	•077	.091	<b>.</b> 107	<b>.06</b> 8
61	051	036	066	<b>.</b> 092	.126	<b>•</b> 076	.080	•101	.059
62	062	045	077	.097	.139	.072	•077	•099	.061
63	076	<b>-</b> .053	089	084	047	104	•070	.101	•057
64	081	062	100	<b>08</b> 8	<b>-</b> .053	113	.064	<b>.09</b> 8	•059
65		070	4	094	061	124	.057	.095	.060
66	295	<b>2</b> 80	286	142	148	-,176	176	-,151	114
67	304	276	282	151	176	198	-, 182	166	127
68	314	<b></b> 272	278	-,161	193	217	194	179	-,133
69	323	270	273	171	211	235	<b>-</b> •203	189	-, 141
70	329	268	270	<b>-</b> .179	224	250	212	<b>19</b> 8	146

Table 8. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting and early retirement at age 55, by normal retirement age and occupation, for manufacturing.<sup>8</sup>

workers, and .35 for production workers, respectively, in plans with normal retirement at 62. Only among plans with normal retirement at age 65 is there a noticeable difference in the accrual ratios by occupation. In this case, the drop between age 55 and age 66 is .29 for professionals, .25 for clerical workers, but somewhat less than .18 for production workers. Thus we conclude that differences in pension accrual ratios by occupation are primarily due to different plan types or to differences in early and normal retirement, given the general type of plan. Production workers, for example, are more likely to have flat benefit plans than professionals.

# E. <u>The Effect of Alternative Post-Normal-Retirement Provisions on</u> <u>Pension Accrual</u>

Accrual ratios for percent of earnings plans with early retirement at 55 are shown in table 9 for selected normal retirement ages and for alternative post-normal retirement provisions. The post-normal retirement provisions have been grouped into five categories:

- Full Credit, Deferred: plans providing full credit according to the standard formula for years worked past the age of normal retirement, but with benefits beginning only after retirement.
- (2) No Credit, Deferred: plans with no credit given for work after the the age of normal retirement and with benefits beginning only after retirement.
- (3) No Credit, Immediate Payout or Actuarial Increase: plans with no credit given for additional work after the age of normal retirement, but with benefits beginnning immediately or increased actuarially until benefits are taken.

Table 9. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting

Normal Retire.		55				62					65		
Pro- vision	Full credit, Defer.	No credit, Defer.	Limited credit, Defer.	Full credit, Defer.	No credit, Defer.	No credit, Immed。 Payout or Actuarial Increase	Limited credit, Defer.	Limited credit immed. Payout or Actuariai	Full credit, Defer.	No credit, Defer.	No credit, Immed. Payout or Actuarial Increase	Limited credit, Defer.	Limited credit, immed. Payout or Actuarial
No. of Plans Age	18	5	129	76	7	2	66	35	212	207	63	22	6
40	. 186	•000	•252		.120	.243		.087	°.	•057	•082	.063	•023
41		1 05	•046	.022	.034		.021	.018	.016	110	.012		
42	• 040	600°	•053	•028	•039	•053	•024	•021	•018	<b>012</b>	•013	•015	•014
43	•045	<b>8</b> 00 <b>°</b>	•060	•032	<b>•</b> 044	•060	•028	•024	.021	.014	•015	.017	•016
44	•051	800°	•068	.036	•050	•068	•032	•028	•024	.016	.017	•020	•019
45	•058	•001	•077	•041	•057	•076	•050	•033	•028	.018	<b>610</b> *	•025	•022
46	•072	•001	•087	•045	•064	•086	<b>04</b> 5	•038	•031	•019	•022	•029	•028
47	• 085	•007	860*	•053	£70 <b>.</b>	<b>1</b> 60°	•054	•045	<b>,</b> 036	•025	•025	•034	•037
48	• 096	•001	.111	•063	• 082	.110	•062	.051	•040	•020	•028	•039	.045
49	.110	.026	.125	•076	£60°	.124	•072	• 060	•046	•029	•031	•045	•052
20	,125	•048	<b>,14</b> 2	• 091	.104	•139	<b>180</b>	•081	•053	•035	•035	•052	•058
51	. 143	•054	•160	• 106	.119	.156	•094	£60 <b>*</b>	•060	.040	•039	•054	•067
52	. 166	•060	.181	.123	.133	•176	•109	• 109	.072	•048	.044	•066	•076

and early retirement at 55, by normal retirement age and post-normal retirement provision. $^{\circ}$ 

Normal Retire.		55				62					65		
Pro- vision	Full credit, Defer.	No credit, Defer.	Limited credit, Defer.	Full credit, Defer.	No credit, Defer.	No credit, Immed. Payout or Actuarial Increase	Limited credit, Defer.	Limited credit immed. Payout or Actuariat increase	Full cred1t, Defer.	No credit, Defer.	No credit, Immed. Payout or Actuarial Increase	Limited credit, Defer.	Limited credit, immed. Payout or Actuarial
No. of Plans Ade	8	5	129	76	7	2	66	35	212	207	63	22	6
53	.188	•070	•204	<b>.</b> 145	.150	86I <b>°</b>	<b>1</b> 25	.124	,081	.057	.054	•082	.087
54	.214	•074	.231	<b>。</b> 164	.168	<b>.</b> 223	.147	.140	•092	•068	.063	•094	<b>960</b> •
55	4	•084	•261	191	٠,	•250	~	.161	<b>.</b> 105	•081	•077	.112	.116
56	.015	- 080 -		• 119	.137				.071		• • • • • •		.112
57	• 006	-•077	-,016	.116	. 145	•073	•070	•094	•074	•054	•067	•068	.116
58	• 008	-•075	-024	.120	.152	•064	<b>960</b> •	660 <b>°</b>	•076	•059	•068	.104	<b>128</b>
59	-•007	-,073	-033	.116	<b>.</b> 161	•053	£60*	<b>1</b> 05	•075	• 062	•071	.108	.127
60	-•017	071	-042	.110	.169	•042	£60°	.106	•074	•063	•082	•109	.122
61	-,039	070	-,051	•092	<b>1</b> 58	-•079	060°	<b>.</b> 073	•061	•057	060*	.071	•071
62	-,048	-• 069	- 060	.082	•		• 094	9	•053	•056	.088	•067	•063
63	-,058	-,068	- 069	• 064	- 37	0	033	- 051	•041	•052	•085	•052	•056
64	063	-•079	078	- 074	357	0	037	063	•038	•048	<b>.</b> 083	.048	•049
65	-•071	-,016	087	-,085	337	0	045	074		•041	<b>B</b> D	•041	in i
66	-,113	018	317	-,166	-,318	0	-•026	0	- 154		1 1 1 1		112
67	115	-•020	312	-,208	-,314	0	260	0	-,175	-,177	0	-, 175	- 148
68	-, 196	021	-,308	247	-,309	0	-,257	0	-,194	- 174	0	-, 185	-, 179
69	-,236	-•020	-,303	-,268	304	0	-,256	0	211	171	0	201	207
70	-,272	-,023	-,298	290	-299	0	-,251	0	226	-, 168	0	-,210	-,230

Table 9. Continued

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under the 55 normal retirement heading.

a. Men only. There were no plans with the provisions corresponding to the two deleted categories

- (4) Limited Credit, Deferred: plans with limited credit given for work after the age of normal retirement or with full credit for service post normal retirement up to a specified age or number of years; benefits are deferred in these plans until retirement.
- (5) Limited Credit, Immediate Payout or Actuarial Increase: plans with provisions analogous to the third category above but with limited credit rather than no credit.

With the exception of plans of type (3), these provisions typically lead to very negative accrual ratios after the age of normal retirement. Table 9 compares accrual ratios across these 5 types of plans with varying post normal retirement benefit porvisions. The table examines alternative normal retirement ages, with early retirement occurring at 55. The figures in table 9 are somewhat surprising, indicating quite negative accrual ratios for plans that fully credit post normal retirement service; indeed, in certain cases, these negative accrual ratios are larger in absolute value than negative accrual ratios of plans that provide no credit.

To isolate the impact of the choice of post retirement provisions, accrual ratios for percent of earnings plans with early retirement at 55 and selected normal retirement ages were calculated first assuming that all of the plans had a full credit provision and second, assuming that all the plans had a no credit provision. These results are shown in table 10. The table indicates that the effect of crediting service after normal retirement depends importantly on the age of normal retirement. For plans with a normal retirement age of 55 negative accrual ratios are larger in absolute value under no crediting prior to age 66 and smaller in absolute value thereafter.

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Normal Ret. Assumed Post	<u> </u>	<b>5</b> 5		62		65
Normal Ret. Provision	Full Credit	No Credit	Ful) Credit	No Credit	Full Credit	No Credit
No. of Plans Age	152	152	187	187	513	513
40	.244	.244	100	404		
41	.045		.106	•106	.071	•071
42		.045	.023	.023	.013	.013
43	.051	.051	.027	•027	.016	.016
	.058	•058	.032	.031	.018	.018
44	<b>.06</b> 6	•066	.035	,035	.020	<b>°0</b> 50
45	.075	•075	•Q45	.045	.023	.023
<b>4</b> 6	.085	<b>08</b> 5	.046	.046	.026	<b>.02</b> 6
47	<b>.</b> 097	。097	.055	<mark>،</mark> 055	.031	<b>.</b> 031
48	.110	<b>.</b> 110	.064	<b>•0</b> 64	.035	.035
49	.124	.124	.076	.076	.040	<b>.04</b> 0
50	.141	.141	.090	<b>.09</b> 0	.046	<b>.04</b> 6
51	.159	.159	.104	.104	.052	<b>.</b> 052
52	.180	.180	.120	<b>.</b> 120	.062	<b>•0</b> 62
53	<b>.</b> 204	<b>.</b> 204	.140	<b>.14</b> 0	.072	.072
54	.231	.231	.160	<b>.</b> 160	.083	<b>.</b> 083
55	.261	.261	.185	.185	.097	.097
56	-,002	244	.102	.102	.068	.068
57	011	229	.105	.105	.072	.072
58	019	215	.118	.118	.076	.076
59	027	<b>2</b> 02	.117	.117	.077	.077
60	037	139	<b>.</b> 114	.114	.079	.079
61	-,049	-, 178	.099	.099	.068	•068
62	059	167	.098	.098	.064	.064
63	068	157	060		•056	•004 •056
64	077	148	069	267	.053	•058
65	086	139	<b>-</b> .079	252	.044	
66	133	130				.044
67	177		150	237	132	225
68		128	192	233	153	222
	219	127	231	232	172	219
69	261	124	<b>2</b> 60	227	190	216
70	-,301	123	285	223	205	212

Table 10. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting and early retirement at 55, by normal retirement age, <u>assuming</u> full credit and no credit post retirement provisions.

#### F. Early and Normal Retirement Supplements

Approximately 11.4 percent of plans have early and 7.5 have normal retirement supplements. The typical normal retirement supplement provides an addition to otherwise calculated benefits if the individual postpones retirement until the normal retirement age. The typical early retirement supplement provides an addition to benefits if retirement occurs after the age of early retirement. The average accrual rates for percent of earnings and flat plans with supplements and with 10-year cliff vesting and early and normal retirement at 55 and 65 respectively, are shown in table 11 by type of supplement. There are only two plans in the category with only normal retirement supplements, but nonetheless the effect of the supplements can be seen in the first column of the table. The accrual rate jumps from about 8 percent of the wage at age 64 to 60 percent of the wage at age 65. Thus the supplement apparently provides a relatively strong incentive to remain with the firm until age 65, but thereafter there is a sharp drop in the accrual rate to -18 percent. Accrual rates for plans with early retirement supplements are shown in the second column of the table. In this case there is a sharp increase in the accrual rate from .12 at age 54 to .44 at age 55, with a sharp drop thereafter. Again, the provision seems to provide a substantial incentive to remain with the firm to the age of early retirement, with a very substantial decline thereafter. Accrual rates for plans with both types of supplement are shown in the last column of the table. In this case there is a rather large spike at the age of early retirement, equal to 62 percent of the wage in that year, with a smaller but still noticeable spike at about the age of normal retirement.

Accrual rates for percent of earnings and flat plans with either type

-36-

	Normal	Type of Supplement	-+
		Early	Both
No. of Plans	2	10	10
Age	+ +		<u> </u>
40	.065	•111	•035
4 1	.012	.197	.009
42	.013	.023	.011
43	.015	.026	.013
44	.017	.031	.018
45	.019	.035	.023
46	.022	.040	.030
47	.025	.047	•037
48	.028	.053	.044
49	.032	<b>.0</b> 60	.052
50	<b>.03</b> 6	.069	.060
51	•040	.079	.070
52	.045	.094	•081
53	.051	.106	.095
54	<b>₀</b> 057	.121	.108
55	.065	.442	.621
56	•047	0007	051
57	•051	008	049
58	•054	014	<b>-</b> •043
59	<b>.</b> 058	022	046
60	.061	011	051
61	<b>•</b> 066	049	<b>-</b> .068
62	<b>.07</b> 0	058	<b>-</b> •072
63	•074	073	080
64	•078	022	.009
65	.601	<b>-</b> •031	•008
66	 - 181	247	 092
67	180	213	167
68	179	207	164
69	179	<b>-</b> •204	163
70	178	201	<b>-</b> .160
1			

Table 11. Weighted average accrual rates for percent of earnings and flat plans with 10-year cliff vesting, early and normal retirement at 55-65, and early or normal retirement supplement, by type of supplement.

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of supplement are shown in table 12 for selected early and normal retirement ages. The spikes in the accrual rates are highlighted with dashed lines. Consider for example plans with early retirement at age 55. The spike created by the early retirement supplement is from .22 to .39 for plans with normal retirement at 55, from .12 to .50 for plans with normal retirement at 60, and from .11 to .48 for plans with normal retirement at 65. Of the 56 plans with normal retirement at age 60, the pension accrual rate at that age is on average equivalent to 100 percent of the wage rate. Similar discontinuities in the accrual ratios are evident for plans with other early and normal retirement ages. For example, of plans with early and normal retirement at age 60, the accrual rate at that age is equivalent to 64 percent of the annual wage for persons aged 60. Thus these special supplements create very significant one-time additions pension wealth and therefore provide potentially very important incentives to remain with the firm until the age that the special supplement is awarded. The special supplements also further dramatize the wide variation in the incentive effects implicit in the provisions of private pension plans.

# III. Flat Benefit Plans

Accrual ratios for flat benefit plans with selected early and normal retirement are shown in table 13. This table can be compared to table 1 above which presents comparable numbers for percent of earnings plans. The accrual profiles for flat plans with early-normal retirement at ages 55-55, 55-60, 55-65 are shown graphically in figure 6. In general, the accrual profiles for the flat benefit plans look quite similar to those for percent of earnings plans.

-38-

	†			1		t
Early Ret. Normal Ret.	55 55	<b>55</b> <b>6</b> 0	55 65	60 60	60 65	62 62
No. of Plans	19	<b>5</b> 6	22	37	2	19
Age	<u> </u>			+		<u> </u>
40	.199	.136	.082	•078	<b>.</b> 068	.056
41	.039	.024	.015	.014	.012	.010
42	.045	.027	.018	.016	.013	.011
43	.052	٥ <b>3</b> 0	•021	.018	•015	.013
44	•059	۰0 <b>3</b> 4	.025	<b>.02</b> 0	<b>.</b> 017	.151
45	•068	.038	<b>°</b> 030	.022	•019	.180
<b>4</b> 6	•077	٥4 <u>3</u>	<b>03</b> 6	.023	•022	.020
47	•088	•049	.041	.027	•025	.023
48	.100	<b>.</b> 055	.048	.030	.028	.026
49	.114	۰06 <u>2</u>	<b>05</b> 6	.035	•032	.030
50	.129	<b>•07</b> 0	•064	.039	.036	.035
51	.148	<b>.08</b> 0	.074	.044	<b>•04</b> 0	.029
52	.167	<b>.09</b> 0	.087	.050	•046	.033
53	.191	.103	.099	.057	•053	.039
54	.220	.117	.113	.066	<b>.</b> 061	.044
<b>5</b> 5	.389	.498	.484	.075	•069	.060
<b>5</b> 6	019	•071	•016	.086	•080	.064
57	<del>-</del> .078	•071	.019	.099	•092	.161
58	048	.071	021	.114	<b>1</b> 07	.097
59	<del>-</del> .057	.069	<b>-</b> •026	.132	.123	.110
<b>6</b> 0	067	1.079	<b>0</b> 08	.643	.233	.127
61	<b>-</b> .085	-,292	049	208	.048	.146
62	093	-,301	<b>0</b> 56	212	<b>.</b> 045	.183
63	108	-,353	067	227	•039	078
64	079	079	006	102	•072	086
65	086	043	.018	099	<b>.</b> 194	094
<b>6</b> 6	-,124	088	<b>~</b> , 182	100	048	169
67	141	-,116	<b>-</b> .195	088	-,064	111
68	-,150	<b>-</b> .124	-, 191	092	<del>-</del> .072	-,112
69	-,151	<b>-.</b> 132	-, 188	097	112	113
70	<b>-</b> • <b>15</b> 1	141	186	102	<b>-</b> .120	114
				<u> </u>		

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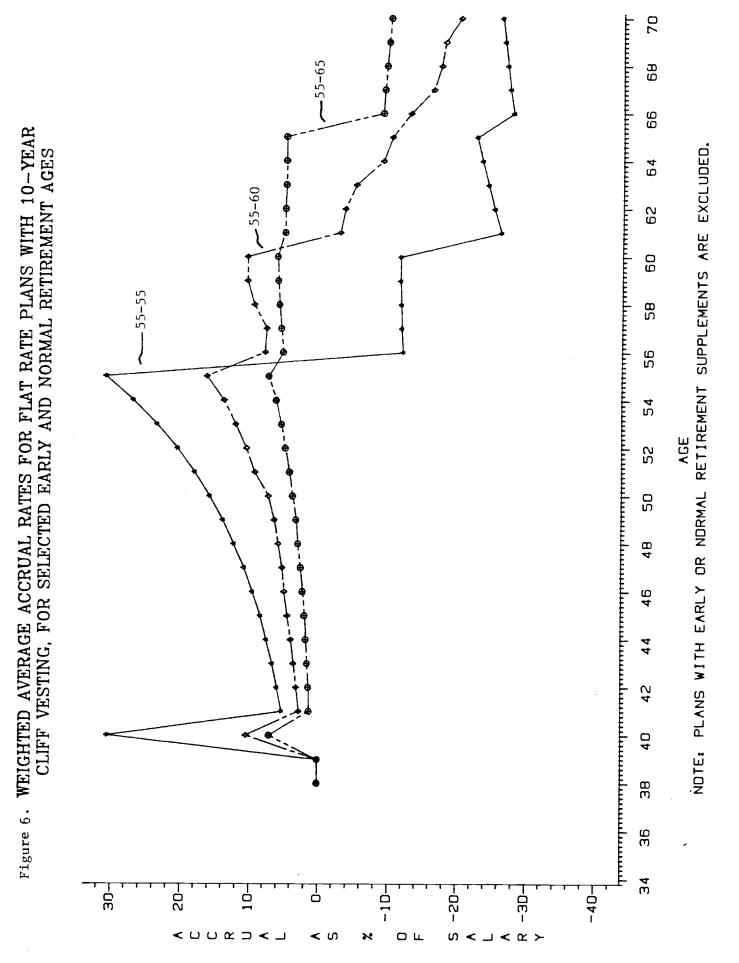
Table 12. Weighted average accrual rates for percent of earnings and flat plans with 10-year cliff vesting and early or normal retirement supplements, by early and normal retirement ages.<sup>a</sup>

a. There are no plans in the 62-65 or in the 65-65 early-normal retirement groups.

	u-year c		ting, by	exarty a	ing normal	i retire	ment age	•
Early Ret.	55	55	55	60	<b>6</b> 0	62	62	65
Normal Ret.	55	60	65	60	65	62	65	65
No. of Plans	3	<b>9</b> 0	106	10	48	3	17	14
Age	ŧ							
40	.304	.104	.070	.022	.046	.033	.025	.019
41	.052	.027	•012	.004	.008	.006	<b>,</b> 004	.006
42	.059	.031	.013	.004	<b>,0</b> 09	.007	.005	.006
43	.066	<b>.</b> 035	"015	.005	<b>.</b> 010	.007	<b>.0</b> 06	.006
44	.075	.039	.017	.006	•012	<b>.00</b> 8	.007	.007
45	.084	.044	.019	.006	.013	.009	<b>.</b> 007	.007
46	<b>.09</b> 6	.049	.022	.007	.015	<b>.</b> 010	•008	.007
47	.108	<b>.</b> 052	.025	.029	.017	•011	• <b>0</b> 09	.008
48	.123	<b>.</b> 058	.029	.053	.019	•013	•011	•009
49	.139	.064	•032	.063	.022	.015	•012	.009
50	.158	•073	•037	.067	<b>.</b> 025	•016	.013	.010
51	<b>. 18</b> 0	<b>.</b> 093	<b>.04</b> 2	.079	<b>.</b> 028	.018	<b>.</b> 015	.011
52	.205	.105	.048	.084	.032	.021	•017	.012
53	.235	.121	<b>.</b> 054	.098	.037	.024	<b>.02</b> 0	.014
54	,269	.138	<b>.</b> 062	.110	.042	.027	<b>.</b> 022	.015
55	• 308	.163	•073	.150	.048	.030	<b>.</b> 025	.017
56	-,121	.079	.052	.171	.055	<b>.</b> 035	.028	.018
57	119	•077	•055	.189	.063	.040	<b>.</b> 032	.020
58	-,118	•0 <del>9</del> 5	<b>.</b> 058	.228	<u>_</u> 073	.045	•037	<b>.03</b> 0
59	117	.105	<b>.06</b> 0	.258	.084	.052	.043	.036
60	117	.105	•061	<b>.</b> 285	.101	.059	<b>.05</b> 0	.042
61	263	029	<b>.05</b> 0	.005	.061	.068	<b>.</b> 058	.042
62	253	036	<b>.</b> 050	012	.062	<b>.</b> 078	.068	.049
63	244	-,052	.049	042	.063	014	.067	.058
64	-,235	091	.049	058	.034	015	•066	.069
65	227	104	.049	079	.069	<b>-</b> .017	•063	.083
66	280	131	091	174	074	085	037	074
67	275	164	093	267	076	083	040	074
68	271	175	096	255	078	082	042	074
69	-,267	181	099	246	<b>08</b> 0	081	046	074
70	263	<b>2</b> 03	<del>-</del> •102	244	083	<b>08</b> 0	049	074

Table 13. Weighted average accrual rates for flat rate plans with 10-year cliff vesting, by early and normal retirement age.<sup>a</sup>

a. Plans with early or normal retirement supplements are excluded.



Recall that we have assumed that the flat benefit increases with the rate of inflation, assumed to be 6 percent annually in our calculations. While it is not possible to make comparisons for plans with each of the early and normal retirement combinations because of the relatively small sample sizes in some of them for flat benefit plans, for several early-normal retirement age combinations, there are rather large numbers of plans of both types, e.g., the combinations 55-60, 55-65, and 60-65. The average decline in the accrual ratio between the age of early retirement to age 66 is .30 for percent of earnings plans versus .39 for flat benefits plans in the case of the 55-60 retirement age combination. It is .25 versus .16 for the 55-65 combination, and .26 versus .17 for the 60-65 combination.

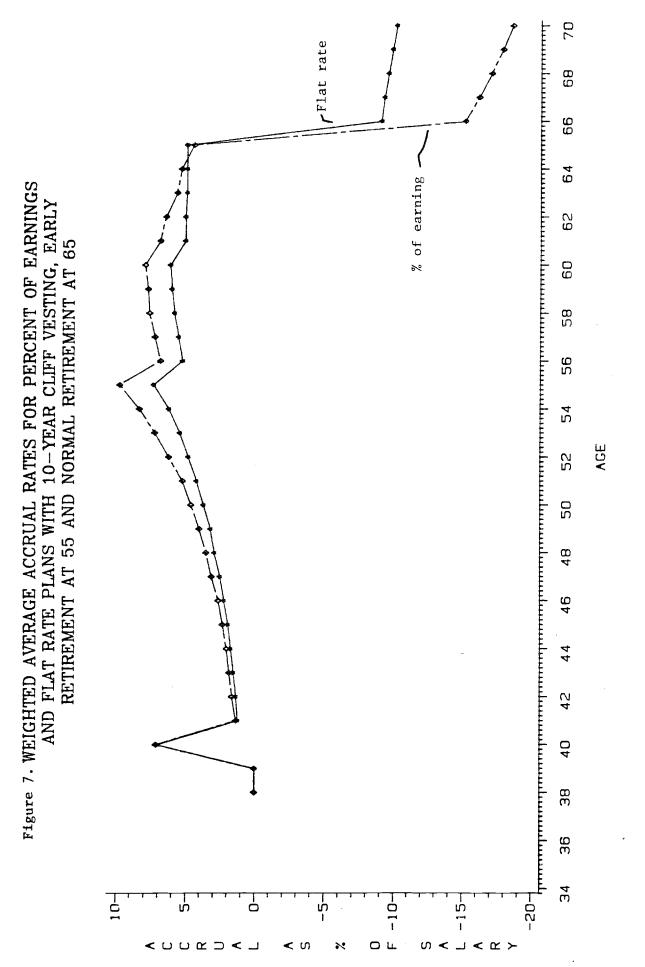
Accrual ratios at several critical ages for plans with early retirement at 55 and normal retirement at 65 are shown below for percent of earnings and flat benefit plans:

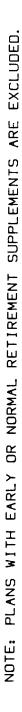
Age	Percent of Earnings Plans	<u>Flat Plans</u>
40	.071	.070
55 56	•097 •068	•073 •052
65 66	.044 152	.049 091
70	186	102

The accrual rates for these plans are graphed in figure 7. The evidence seems to indicate that the two types of plan provide rather similar incentive effects.

The provisions of flat rate plans, like those of percent of earnings plans, also yield widely differing ratios, even among plans with the same early and normal retirement ages. Indications of the dispersion of the accrual ratios

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among flat plans with early and normal retirement at 55 and 65 respectively are shown in table  $1^4$  and in figure 8. While the average accrual rate at age 55, for example, is 7 percent, the minimum value is 0 and the maximum  $2^4$  percent. Similarly at age 56, while the average is about 5 percent the maximum is 20 percent and the minimum about 0. At 65, the average is 5 percent, with a maximum of almost 33 percent and a minimum of about -20 percent. At 66 after the age of normal retirement, the average accrual rate is -9 percent, while the minimum is -56 percent and the maximum 0. Thus the incentive for retirement varies widely among flat, as well as percent of earnings plans.

#### IV. The Pension Cost of Job Change

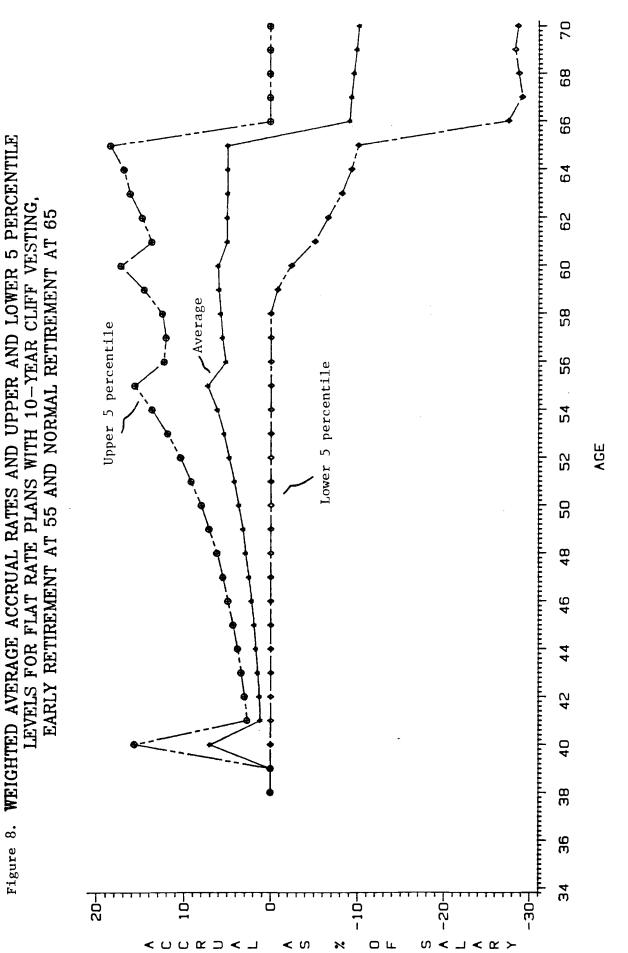
There are many ways to think about the effect of job change on pension accrual and the potential incentive effects of pension provisions on the job change decision. One approach is to consider the effect of job change on accrued pension wealth at the age of retirement, say the age of plan normal retirement. Another way is to consider the expected loss in future pension wealth from changing job as a proportion of expected future wages. We shall consider variants of both measures.

# A. If Change to a No-Pension Job

Consider a person who starts a job at some age, say 31. Suppose that at a given subsequent age the person could change to another job and obtain the same future wages as on the current job. His decision, assume, is either to stay on the current job until normal retirement, or to switch to the second job and stay on that one until the age of normal retirement. But suppose that the

	Weighted Average Accrual Ratios	Median Accrual Ratios	Minimum Accrual Ratios	MaxImum Accrual Ratios	Lowest 5th Percen- tile	Largest 5th Percen- tile
lo, of Plans	106	106	106	106	106	106
Age	100		100			100
40	•070	•073	0	<b>.</b> 260	0	<b>.</b> 157
41	.012	.013	0	.045	0	.027
42	<b>.</b> 013	•015	0	•050	0	•030
43	•015	•016	0	•057	0	•034
44	•017	•018	0	<b>.</b> 064	0	•038
45	.019	.021	0	<b>.</b> 072	0	•043
46	•022	•024	0	<b>.</b> 081	0	•049
47	<b>.</b> 025	•027	0	•091	0	•055
48	.029	•031	0	<b>.</b> 102	0	•062
49	•032	•035	0	<b>.</b> 115	0	<sub>•</sub> 071
50	<b>.</b> 037	•039	0	<b>.</b> 130	0	•080
51	.042	•045	0	<b>.</b> 147	0	٥92ء
52	•048	•041	0	<b>.</b> 166	0	<b>.</b> 104
53	•054	<b>•</b> 058	0	.187	0	.119
54	•062	<b>,</b> 067	0	<b>.</b> 212	0	.137
55	.073	.077	0	.240	.006	.157
56	.052	•053	<b>-</b> .006	<b>.</b> 195	0	,123
57	<b>.</b> 056	•055	<b>-</b> .007	<b>.</b> 192	0	.121
58	.058	•055	010	<b>.</b> 189	0	<b>.</b> 125
59	.060	<b>.</b> 055	<b>-</b> .013	<b>.</b> 183	008	<b>"</b> 146
60	<b>.</b> 061	<b>.</b> 056	031	<b>.</b> 184	024	<b>.</b> 173
61	.050	<b>.</b> 042	-,217	<b>.</b> 204	<b>-</b> •051	<b>.</b> 137
62	•050	•040	<b>-</b> ,213	<b>.</b> 226	<b>-</b> .066	<b>.</b> 148
63	•049	•035	209	<b>.</b> 400	082	<b>.</b> 162
64	.049	<b>.</b> 034	204	<b>.</b> 561	<b>~</b> _093	.169
65	.049	.029	198	.328	101	.184
66	091	067	560	0	<b>-</b> .275	0
67	093	073	<b></b> 552	•008	291	0
68	096	079	545	•055	<b>-</b> .287	0
69	099	096	<b>-</b> •536	•045	<b>-</b> .283	0
70	102	<b>-</b> .101	528	•035	286	0

Table 14. Dispersion of accrual rates for table 11 plans with age 55 early retirement and age 65 normal retirement.



NOTE: PLANS WITH EARLY OR NORMAL RETIREMENT SUPPLEMENTS ARE EXCLUDED.

new job has no pension. Then the loss in pension wealth is equal to the pension wealth that the worker would accrue if he were to stay with the current employer until the age of normal retirement. This loss relative to the present value of expected future wages is shown in tables 15, 16, and 17. Table 15 assumes that an individual begins employment with the first firm at age 31. Table 16 assumes a starting age of 41, and table 17 a starting age of 51. The tables present these loss ratios by plan normal retirement age, and loss ratios are calculated through the age of normal retirement. To obtain a more concise picture of the losses, they are shown for selected ages of job change in table 18. For plans with normal retirement at 65, the loss in pension wealth relative to expected wages is relatively small, between 4 and 6 percent for all ages of job change, with the exception of job change at age 59 when joining the firm at age 51. In the latter case, the remaining working life of the individual is short and he is not yet vested. Thus the loss in potential pension accrual is relatively large compared to future earnings. Among plans with earlier normal retirement--55, 60, or 62--the potential loss in future pension accrual is considerably larger, typically on the order of 8 to 20 percent of future earnings. The loss if one changes jobs just before normal retirement, however, is in some instances much larger than this, as high as 30 to 50 percent. For example, if at age 31 one enters a plan with normal retirement at age 60, the loss ratio if one changes job at 59 is 31 percent. If the individual enters at 51 and leaves at 59, the loss is almost 50 percent.

The greater relative loss with earlier normal retirement is shown in figure 9, which presents loss ratios versus age for normal retirement at 55 and at 65, starting at age 31. The effect of starting age is shown graphically in

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Table 15. Loss in expected pension wealth if change to no-pension job, as percent of expected wages, by age of job change and by normal retirement age, starting initial job at age 31.

Normal Ret.	55	60	62	65
No. of Plans Age	184	446	442	858
31	.072	•055	.048	<b>.</b> 026
32	<b>.07</b> 6	<b>.</b> 058	.050	•027
33	.080	•061	.053	•028
34	•084	•064	•055	<b>.</b> 029
35	<b>.</b> 089	<b>.</b> 067	<b>.</b> 058	.030
36	<b>.</b> 095	•071	.060	<b>.</b> 032
37	.101	•075	.064	•033
38	.108	.079	•067	.035
39	.116	.084	.071	•037
40	.106	.083	,069	•035
41	.111	.087	<b>.</b> 072	•037
42	.116	•092	•075	.038
43	.122	.097	•078	•040
44	<b>.</b> 128	.103	.081	<b>"</b> 041
45	<b>.</b> 134	<b>"</b> 108	<b>.</b> 083	.043
46	.140	.115	<b>.</b> 086	<b>.</b> 044
47	<b>.</b> 145	.121	.089	<b>.</b> 046
48	.151	.128	<b>.</b> 092	<b>.</b> 047
49	<b>.</b> 156	.135	.094	<b>.</b> 048
50	.161	. 143	.095	۰049 •
51	<b>.</b> 163	.152	.097	•050
52	<b>.</b> 163	<b>.</b> 161	۰097»	<b>.</b> 050
53	<b>.</b> 154	.171	•096	<b>.</b> 050
54	<b>.</b> 124	.182	,093	•048
55		.182	.082	<b>.</b> 044
56		.174	<b>080</b>	•043
57		. 199	•077	•042
58		•237	o71°،	•040
59		.310	.062	.037
60			.031	<b>.03</b> 2
61			•022	<b>.03</b> 0
62				<b>.</b> 026
63				•02 <b>3</b>
64				•016
65				

Normal Ret.	55	60	62	65
No. of Plans	57	349	546	1009
Age				
41	.079	.064	<b>.</b> 062	.034
42	.086	<b>.</b> 068	•066	.036
43	.093	.073	.071	<b>03</b> 8
44	<b>.</b> 103	.079	<b>.</b> 076	.040
45	.114	<b>.</b> 085	•082	.043
46	.127	.092	<b>• 08</b> 8	<b>.</b> 046
47	<b>.</b> 143	.101	• <b>09</b> 6	<b>.</b> 050
48	.164	•111	.104	•054
49	<b>.</b> 191	<b>.</b> 122	<b>.</b> 114	<b>.</b> 058
50	.117	.096	.097	•048
51	<b>.</b> 121	.100	.102	•049
52	•122	.103	<b>.</b> 106	.051
53	.119	.106	.110	•052
54	.103	<b>1</b> 08	<b>.</b> 115	•053
55		• 104	<b>.</b> 111	.052
56		.105	<b>.</b> 106	<b>.</b> 053
57		.105	<b>.</b> 111	•053
58		.100	<b>.</b> 119	<b>.</b> 052
59		•085	.130	•051
60			.132	.047
61			<b>.</b> 168	•046
62				.044
63				•040
64				.031
65				

Table 16. Loss in expected pension wealth if change to no-pension job, as percent of expected wages, by age of job change and by normal retirement age, starting initial job at age 41.

Normal Ret.	55	60	62	65
No. of Plans	32	178	451	1287
Age				
51	<b>.00</b> 0	.080	<b>.</b> 094	<b>.04</b> 6
52	•000	.091	.105	.051
53	.000	.104	.118	.056
54	•000	.122	.134	•062
55		.146	.150	.069
56		.178	.169	.079
57		.229	<b>.</b> 203	.090
58		.313	<b>.</b> 251	.104
59		<b>.</b> 482	.325	.122
60			. 183	•059
61			.246	•060
62				•059
63				.055
64				•044
65				

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Table 17. Loss in expected pension wealth if change to no-pension job, as percent of expected wages, by age of job change and by normal retirement age, starting initial job at age 51.

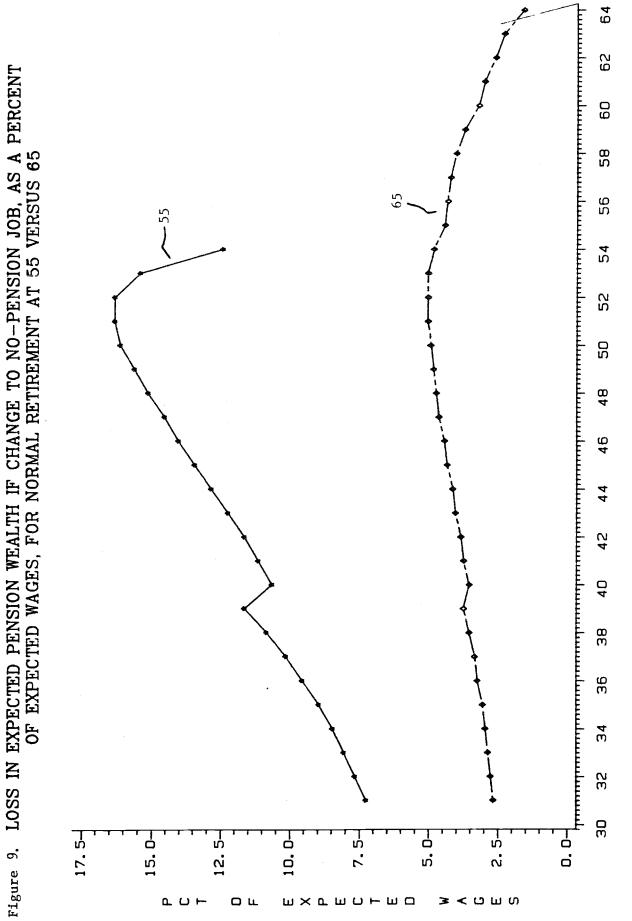
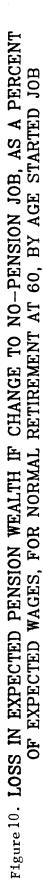


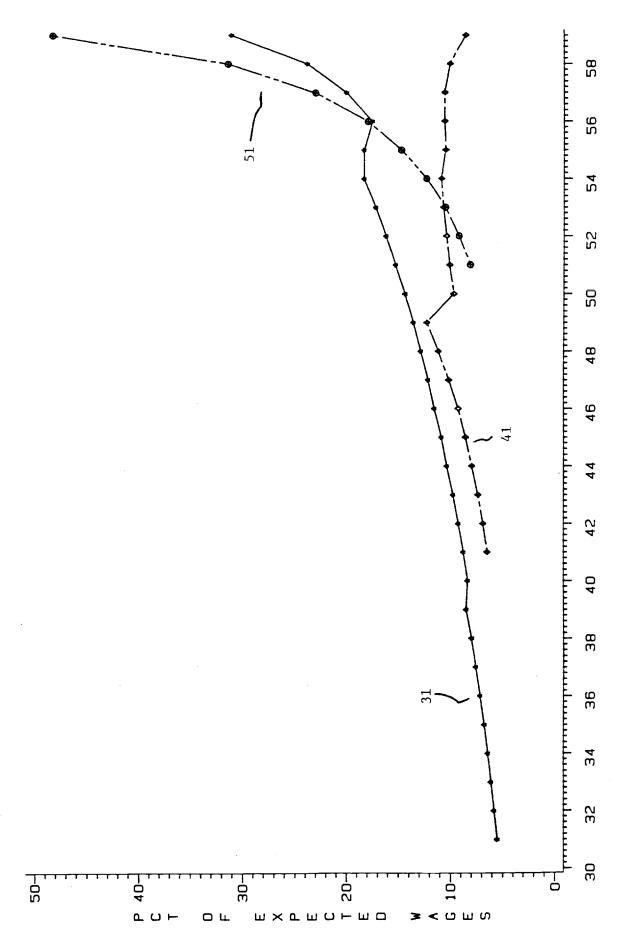
figure 10 for plans with normal retirement at 60.

A limiting case of numbers like those presented in table 18 is the present discounted value of expected pension benefits at the age of hire as a proportion of expected wages at that time. These numbers of course indicate the cost to the employer of pension benefits versus wages if a person stays with the employer from the time of hire to the age of early or normal retirement. Such ratios are presented in table 19 by age of initial employment and plan normal retirement age. The ratios are presented first assuming that the individual remains with the firm until the age of early retirement and then assuming that the person remains until the age of normal retirement. It can be seen from the table that the present discounted value of pension versus wage compensation is small on average, ranging from about 2 percent to about 10 percent. The average proportion of compensation in pension benefits is typically larger the later the age of initial employment. For example, the ratio of pension benefits to wages for plans with normal retirement at 62 is .049 if one enters the firm at 31 and stays to the age of normal retirement. The ratio is .062 if one enters at 41, and .094 if one enters at 51. It is important to understand that while these ratios may appear relatively small, the pattern of pension accrual may still have a very substantial effect on worker labor force participation, as demonstrated above.

And, possibly the most striking feature of these loss ratios, is the wide variation among plans. To demonstrate the dispersion, the mean loss ratio together with the minimum and maximum at each age, are shown in table 20 for plans with normal retirement at 65 and for persons who enter the firm at age 31. Up to age 55--which is the age of early retirement for a substantial proportion

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AGE

Starting Age and	Plan Normal Retirement				
Age	55	60	62	65	
31:					
44	.13	.10	.08	.04	
49	<b>.</b> 16	.14	•09	.05	
54	<b>.</b> 12	<b>.</b> 18	.09	.05	
59	-	.31	.06	•04	
41:					
44	<b>.</b> 10	.08	.08	•04	
49	<b>.</b> 19	.12	•11	<b>0</b> 6	
54	<b>.</b> 10	•11	.15	.05	
59		•09	.13	.05	
51:					
44			**	· • • •	
49	<b>67</b> - 64				
54		.12	<b>.</b> 13	.06	
59		<b>.</b> 48	.33	<b>. .</b> 12	

Table 18. Loss in expected pension wealth if change to no-pension job, as percent of expected wages by age of job change, age of starting job, and age of normal retirement.<sup>a</sup>

a. With expectations evaluated to plan normal retirement age.

Age of Hire and Plan Normal Retirement Age	if Retire at Early Retirement Age	lf Retire at Normal Retirement Age	
31:	······································		
ALL -	.038	.044	
55	•072	.072	
60	.044	<b>.</b> 055	
62	.043	.049	
65	<b>.</b> 022	<b>.</b> 026	
41:			
ALI	<b>。</b> 042	.049	
55	•078	.079	
60	•060	.064	
62	<b>.</b> 051	<b>.</b> 062	
65	•027	.034	
51:			
ATI	<b>.</b> 045	.060	
55			
60	<b>。</b> 069	•080	
62	•054	•094	
65	•039	.046	

Table 19. Present discounted value of expected pension benefits as a proportion of expected wages, at age of hire, by age of hire and plan normal retirement age.

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Age	Mean	table 15 with normal r Minimum	MaxImum
31	<b>.02</b> 6	0	•098
32	•027	0	•101
33	•028	0	<b>.</b> 105
34	.029	0	.110
35	.030	0	<b>.</b> 115
36	.032	0	<b>.</b> 120
37	.033	0	<b>.</b> 125
38	•035	0	.131
39	•037	Ũ	.137
40	.035	+.010	.139
41	•037	<b>-</b> •009	.145
42	<b>.</b> 038	008	<b>•</b> 152
43	<b>.</b> 040	007	<b>.</b> 158
44	.041	005	<b>.</b> 166
45	.043	003	<b>.</b> 173
46	.044	004	<b>.</b> 182
47	.046	<b>0</b> 05	.190
48	.047	005	.199
49	•048	<b>-</b> .007	.209
50	.049	012	<b>.</b> 219
51	<b>°05</b> 0	022	•229
52	<b>.05</b> 0	<b>-</b> .034	.240
53	<b>.05</b> 0	049	.252
54	.048	<b>-</b> .068	•264
55	044	182	.276
56	.043	181	.289
57	.042	<b>-</b> .178	•301
58	.040	175	<b>.</b> 313
59	•037	187	<b>.</b> 325
<b>6</b> 0	.032	229	.335
61	.030	221	.341
62	•026	233	•339
63	•023	248	•321
64	•016	220	•367
65			
1			

Table 20. Dispersion of loss in expected pension wealth if change to no-pension job, for plans in table 15 with normal retirement at age 65.

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of plans--the loss is close to zero for some plans and indeed is even negative for some. For other plans, however, the loss is very high, ranging up to 26 percent of future earnings at age 54. After 55, the maximum loss is typically over 30 percent, while the minimum is close to -20 percent at each age. Pension accrual after the age of early retirement is negative in many instances. For a member of such a plan, it would pay to leave this firm, taking early retirement benefits, and join another firm, assuming that one could join the second firm and obtain the same expected future wages.

#### B. Job Change and Pension Wealth at Age of Normal Retirement

Pension wealth at the age of normal retirement may be reduced very substantially by job change, as shown in Table 21. A person who began work at 31 and changed to another job at 41 would have accrued, on average, only 72 percent of the pension wealth of a person who began at 31 and remained in the same firm. If he changed jobs at 41 and again at 51, he would accrue only 43 percent of the pension wealth of a person with no job change. This percent ranges from a low of 30 on average in transportation to 60 percent in construction. Thus the loss in pension wealth with job change seems to provide a potentially large incentive against job mobility.

Because some plans place a limit on years of service that are credited in calculating benefits, it may in some instances pay to change jobs and begin to accrue benefits in a new plan. This leads to ratios that are greater than one in a few instances. The minimum and maximum values, over all industries arise in anomalous plans, and these should not be given much weight; but they do suggest that there is substantial variation among plans in this respect, as well as in other respects discussed above.

# Table 21: Weighted average pension wealth (or ratio) at normal retirement, by age of initial employment, and by job change,

# and by Industry, all plans.

Industry	Ag	ge of init emptoymen		Pension wealth at normal retirement relative to wealth without job change if:			
and No. of plans	31	41	51	Change at 41	Change at 51	Change at 41 and 51	
All industries 2342	32491	21410	10924	.72	.85	.43	
Minimum	0	0	0	0	0	0	
MaxImum	197070	175899	117291	4.97	8,18	5.09	
Mining 39	44856	27237	13147	•62	.81	•38	
Construction 9	35778	<b>286</b> 80	16837	.87	1.02	•60	
Manufacturing 1297	31448	20393	10633	.73	<b>.</b> 85	.44	
Transportation 328	38680	<b>2235</b> 0	8598	•57	.81	•30	
Wholesale trade 100	30836	21989	13135	.74	<b>.</b> 87	•50	
Retail trade 260	19453	13002	6024	•67	<b>.</b> 80	<b>.</b> 41	
Finance 7	<b>38</b> 864	<b>3</b> 0766	17309	.91	1.01	<b>•</b> 58	
Services 8	2 <del>9</del> 993	22551	12520	.77	.87	<b>.</b> 47	

# C. Pension Accrual Ratios and Age of Initial Employment

Pension accrual rates for percent of earnings plans with 10-year cliff vesting are shown in tables 22 and 23 for persons beginning employment at ages 41 and 51 respectively. The tables are analogous to table 1 above, presenting information by plan early and normal retirement ages. To provide an easier comparison of the accrual rates by starting age, accrual rates for selected ages are shown in table 24. The numbers are taken from table 1, table 22, and table 23. Accrual ratios for plans with early and normal retirement at 55 and 65 respectively are graphed in figure 11. The accrual rate at vesting is the most important difference across initial employment ages. For example, as shown in table 24, the accrual rate at vesting is .24 for persons beginning employment at 31, it is .62 for those beginning at age 41, and .92 for those beginning at age 51. The difference is simply due to the fact that the later the age of initial employment, the nearer is the time of benefit receipt at the age of vesting. The accrual rate at vesting increases with age of initial employment for each early-normal retirement age category. Otherwise, the pattern of accrual rates does not vary by starting age, except that the absolute value of the rates, both positive and negative, is smaller as the age of initial employment increases. Again, this is simply because potential benefits are lower with later starting ages and, thus, potential losses after the age of early or normal retirement are smaller. Notice that the accrual rate after the age of 65 is negative in each case. Plan provisions typically make the age of early and normal retirement dependent upon age and years of service. Thus in practice, the ages of early and normal retirement are typically somewhat higher for persons beginning employment at age 51. But in no case is the age of normal retirement greater

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	+			÷		+		t
Early Ret.	55	55	55	<b>6</b> 0.	60	62	62	65
Normal Ret.	55	60	65	60	65	62	65	65
No. of Plans	38	63	5 <b>7</b> 6	169	<b>8</b> 6	27	10	56
Age								
50	.618	.347	<b>.</b> 209	.349	.127	.017	<b>.</b> 135	.126
51	.106	<b>.06</b> 6	<b>.</b> 040	.065	.026	.051	.021	.029
52	. 123	.082	.046	.075	•029	.059	.024	.033
53	. 14 1	<b>_09</b> 5	<b>.</b> 052	.085	.035	.068	•02 <b>7</b>	.038
54	.160	.109	<b>.06</b> 0	.098	.041	.083	•030	.044
55	<b>.</b> 184	.125	<b>.07</b> 0	.112	.047	.095	<b>。</b> 034	.052
56	.006	.094	.069	. 128	<b>.</b> 055	.101	•037	.061
57	<b>.0</b> 02	.099	<b>.</b> 065	.146	<b>.</b> 064	.118	.042	<b>.0</b> 70
58	.0003	.107	.068	.167	<b>.</b> 077	.137	•047	.085
59	004	.116	.071	. 185	<b>.</b> 088	. 155	<b>.</b> 053	.099
60	010	<b>.</b> 120	.073	.209	<b>.</b> 103	.179	<b>.</b> 056	.116
61	016	<b>00</b> 1	.075	007	.080	.198	•061	.123
62	022	004	<b>.</b> 074	015	.081	.223	•067	. 138
63	029	006	.075	023	<b>.0</b> 80	016	<b>.</b> 035	.161
64	036	012	.075	031	<b>.</b> 083	027	•034	. 181
65	043	019	•073	040	.084	038	•032	. 204
<b>6</b> 6	116	115	107	192	060	- 193	<b>-</b> .077	117
67	128	137	-,117	-, 195	074	191	<b>-</b> •077	126
68	141	159	125	197	089	190	<b>-</b> .076	134
69	154	167	134	197	102	- 189	075	141
70	166	174	142	198	114	188	074	148

Table 22. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting, by early and normal retirement age, starting job at age 41.ª

a. Plans with early or normal retirement supplements are excluded.

			+		+		+	
Early Ret.	55	55	55	60	60	62	62	65
Normal Ret.	55	60	65	60	65	62	65	65
No. of Plans	23	23	143	60	419	52	11	425
Age	-							
55	.000	0	.001	.0002	.000	.004	0	.000
56	.000	0	.001	.0002	.000	.004	0	.000
57	.000	0	.001	.0002	.000	.004	0	.000
58	.000	0	<b>.0</b> 01	.0002	.000	.003	0	.000
59	.000	0	.001	.0002	.000	.003	0	•000
60	.923	.774	<b>.</b> 613	1.040	<b>.</b> 451	•644	.541	.449
61	.041	.033	.081	.034	.056	.132	.091	.084
62	.036	•029	.081	.028	.059	. 169	.103	.098
63	.028	.023	.082	.021	<b>.</b> 063	.047	.077	.112
64	.022	.018	.084	.015	,065	.039	.079	.126
65	.013	.012	<b>.</b> 081	.007	.067	.030	.083	.145
66	104	045	- <u>.</u> 076	039	036	057	075	070
67	- 108	059	083	052	043	061	074	077
68	- 113	073	091	066	050	066	079	085
69	- 118	<b>-</b> ,077	099	074	051	068	083	092
70	124	080	106	081	056	076	088	099

# Table 23. Weighted average accrual rates for percent of earnings plans with 10-year cliff vesting, by early and normal retirement age, starting job at age 51.<sup>8</sup>

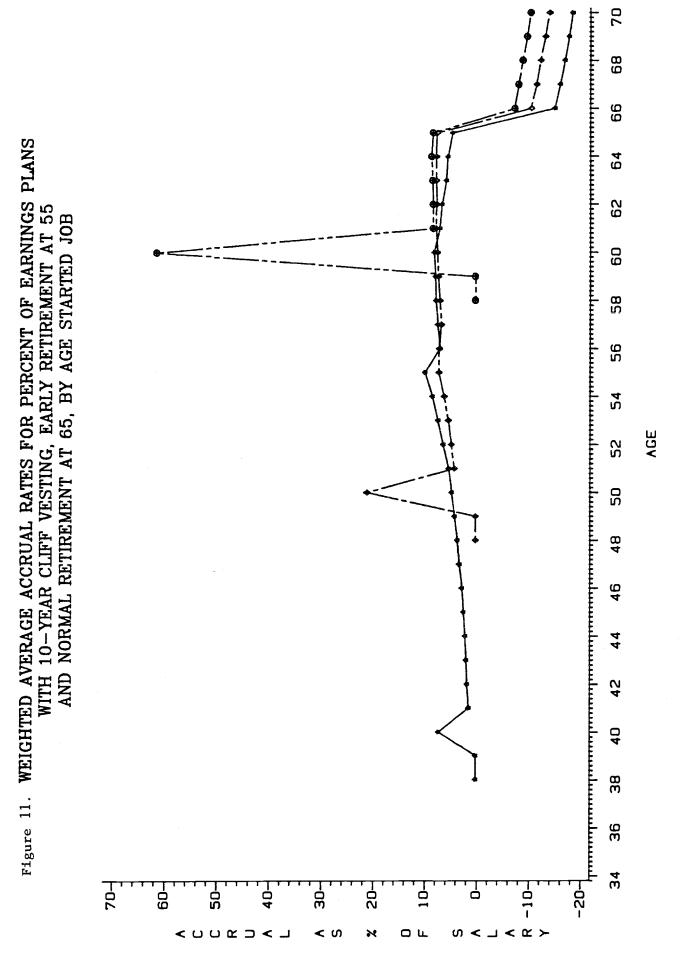
a. Plans with early or normal retirement supplements are excluded.

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			Early	-No	rmal Ref	tiremen	+		
Starting Age	55	55		55	60	60	62	62	65
and Age	55	60		65	60	65	62	65	65
31: 40	.24	.11		•07	.03	•05	.04	.05	.04
50	.14	.08		.05	.07	.03	.07	.02	.03
55	<b>.2</b> 6	.13		<b>"</b> 10	.15	•08	.13	.04	.07
60	04	.14		.08	.27	<b>.</b> 17	.24	.05	. 12
62	06	09		•06	09	.12	.25	.07	.15
65	09	09		.04	12	.11	14	.01	.21
66	29	-,17	-	. 15	14	09	27	08	19
41: 40	0	0		0	0	0	0	0	0
50	.62	.35		.21	•35	.13	.02	. 14	.13
55	.18	• •13		•07	.11	•05	.10	•03	.05
60	01	.12		.07	.21.	.10	. 18	.06	.12
62	02	00		.07	02	.08	•22	.07	. 14
65	04	02		.07	04	•08	04	.03	.20
66	12	-,12		.11	19	06	-,19	08	12
51: 40	0	0		0	0	o	0	0	0
50	0	0		0	0	0	0	0	0
55	0	0		0	0	0	0	0	0
60	.92	<b>.7</b> 7		.61	1.04	.45	.64	.54	<b>•</b> 45
62	.04	.03	•	.08	•03	.06	.17	.10	.10
65	•02	•01	•	.08	.01	.07	.03	.08	.15
66	<del>-</del> <sub>+</sub> 10	05		.08	04	04	06	08	07

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Table 24. Pension accrual rates for percent of earnings plans with 10-year cliff vesting, by early and normal retirement age and by age of initial employment, for selected ages



NOTE: PLANS WITH EARLY OR NORMAL RETIREMENT SUPPLEMENTS ARE EXCLUDED.

than 65.

# V. Pension Accrual Rates and Pension Cost by Sex

Because women on average live longer than men, women would typically receive pension benefits longer than otherwise equivalent men. The effect of this difference in life expectancy on pension accrual and the value of pension benefits is considered in this section. The weighted average of the accrued benefits of women versus the accrued benefits of men by age are shown in table 25 for all plans in the sample. At the most common vesting age, 10 years, the ratio is about 1.08, so that women's vested benefits are approximately 8 percent higher than men's. The ratio increases gradually to about 1.10 at age 60 and about 1.13 at 65. If otherwise identical men and women were to work until age 70, the average ratio would be 1.17. The ratios do not vary significantly by early and normal retirement age, and thus a breakdown by plan type is not presented.

## VI. Summary

The ratios of pension benefit accrual to wage earnings are presented for a wide range of pension plans. Typical plan provisions provide a strong incentive for retirement after the age of plan normal retirement, and several plan types provide a strong incentive for retirement after the age of early retirement. A striking feature of the incentive effects of pension plans is their wide variation among plans. For example, while the average plan may provide reduced but still positive accrual after the age of early retirement, for a large proportion of plans the accrual rate after this age is very negative. Thus it would not be unusual for the reduction in pension benefit

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Age	Ratio	Age	Ratio
31	1	51	1.109
32	1	52	1,106
33	1	53	1.103
34	1	54	1.099
35	1.032	55	1.094
<b>3</b> 6	1,030	56	1.096
37	1.032	57	1.098
38	1.037	58	1.101
39	1.036	59	1.103
40	1.082	60	1.102
41	1.083	61	1,108
42	1.085	62	1,113
43	1.087	63	1.120
44	1.089	64	1.126
45	1.091	65	1,131
46	1.094	66	1.138
47	1.096	67	1.145
48	1.099	68	1.153
49	1.102	69	1.161
50	1,105	70	1.170

Table 25. The ratio of accrued pension benefits of women vs. men, by age, all plans<sup>a</sup>

a. There are 2342 plans. Starting age is 31.

accrual after the age of early retirement to be equivalent to a 30 percent reduction in wage earnings. The accrual rate at the age of vesting can range from as low as 2 percent of wage earnings in that year to as high as 100 percent of wage earnings, depending upon the plan type and on the age of initial employment. Thus for some employees, vesting could be a very important determinant of labor force participation decisions. Special early and normal retirement provisions may also add very substantially to accrued pension wealth at particular ages and may thus encourage workers to remain with a firm until these benefits are received. The accrual profiles under flat benefit plans seem very similar to the accruals under percent of earnings plans, if one assumes that the flat benefit is increased to keep pace with the rate of inflation. Given early and normal retirement ages, there is little difference in plan accrual profiles by industry or by occupation. Differences in pension benefits by industry depend more on the type of plan than on variations among plans with the same basic provisions. While the expected loss in pension benefits due to job change is apparently relatively small in many instances, it is rather large in others, and there is very wide variation among plans with the loss very high in some cases and, indeed, in other cases a gain may be had by changing job. In addition, accrued benefits at the age of retirement are typically very much lower with job change than if a person remains on the same job. Because women typically live longer than men, accrued pension benefits at any age are higher for women than for men, about 13 percent on average at age 65, for example. In short, the evidence suggests that the rapid increase in pension plan coverage over the past two or three decades may well have contributed very substantially to the reduction in the labor force participation of older workers during this period. The plans may also have an important effect on labor mobility.

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## FOOTNOTES

1. Gary Heaton accomplished the very substantial programming task that the paper required and served as a continuous source of information, explanation, and expertise. We thank Tom Gustafson for his very helpful comments.

2. Only plans with incomplete or inconsistent information were classified by the BLS as unusable.

3. Our calculations ignore service requirements for early retirement, since this inclusion could have considerably complicated our accrual computations. Excluding early retirement service requirements from the analysis is not likely to significantly alter the results. Virtually all workers covered by such requirements are enrolled in plans with early retirement service requirements of 15 years or less. (Kotlikoff and Smith, 1983).

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## APPENDIX

The source of discontinuities in age accrual profiles is clarified by considering a simple earnings-related defined benefit plan with "cliff vesting" at 10 years of service. Vested accrued benefits are clearly zero prior to the age at which the worker has ten years of credited service in the plan. Let R(a,t) denote the ratio of I(a) to W(a) for a worker age a with t years of tenure, where I(a) is defined in (1) in the text. Then R(a,t) is zero for t < 9. If a person age a with 9 years of service works an additional year, the ratio of the increment to the wage, W(a), is

(A1) 
$$R(a,9) = \frac{B(a,t)A(55)(1+d)^{10}(1+r)^{(55-(a+1))}}{W(a)}$$

In (A1), B(a,t) is the retirement benefit available to the worker who terminates employment with the plan sponsor at age a after t years of service, but who delays receipt of pension benefits until the plan's normal retirement age. The normal and early retirement ages assumed for this stylized plan are 65 and 55 respectively. Terminating workers in this example are eligible for early retirement benefits. Our hypothetical plan reduces benefits by d percent for each year that early retirement preceeds normal retirement. The benefit reduction rate, d is assumed to be less than the actuarial fair rate.

The function A(55) is the actuarial discount factor that transforms benefit flows initiating at age 55 into expected stocks of pension wealth at age 55. Expectations here are taken with respect to longevity. Thus A(55) is the annuity value of a dollar's worth of pension benefits to be received each year until death, beginning at age 55. For simplicity asume that the probability of dying prior to age 55 is zero. Hence the present value at age a of A(55) is  $A(a) = A(55) (1 + r)^{-(55 - a)}$  for a < 55. If pension benefits are determined as a constant  $\lambda$  times the product of final year's earnings and service, and there is no offset for receipt of social security benefits, B(a,t) is simply:

(A2)  $B(a,t) = \lambda W(a)t$ , and

(A3) 
$$R(a,9) = \lambda(1+d)^{-10} (1+r)^{-(55-(a+1))} A(55)10 \frac{W(a+1)}{W(a)}$$

R(a,t), for t increasing pari-passus with age, is zero prior to t equals 9 and jumps at t equals 9 to the value given in (A3). Cliff vesting thus produces spikes in the accrual profile such as that in Figure 1 at 10 years of service. Between the age at cliff vesting and age 55 pension wealth, Pw(a), is given by:

(A4)  $Pw(a) = \lambda W(a)(1 + d)^{-10}(1 + r)^{-(55 - a)}A(55)t$ , and the increment to pension wealth I(a) divided by the wage W(a) is given by (A5)  $R(a,t) = \lambda(1 + d)^{-10}(1 + r)^{-(55 - (a + 1))}A(55)t\left[\frac{W(a + 1)}{W(a)}\frac{t + 1}{t} - 1\right]$ Equations (A3) and (A5) suggest a drop in R(a,t) as a increases to a + 1 concurrent with an increase in t from 9 to 10. Equation (A5) will be positive if the bracketed term exceeds zero. This will be the case if the percentage increase in the wage plus the percentage increase in years employed (1/t) is greater than zero. Assuming the term in brackets is positive and is roughly constant, R(a,t) will increase exponentially due to the exponential decline in the discount factor,  $(1 + r)^{-(55 - (a + 1))}$ , as a approaches 55.

If the value of d is considerably less than actuarially fair, a discontinuity in R(a,t) occurs at the early retirement age, 55. At ages 55 and 56 we have:

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(A6) 
$$Pw(55) = \lambda W(55)(1 + d)^{-10} A(55)t$$
, and

(A7) 
$$P_w(56) = \lambda W(56)(1 + d)^{-9} A(56)(t + 1).$$

Hence,

(A8) 
$$R(55,t) = \lambda(1+d) (1+r)A(55)t \begin{bmatrix} W(56) & t+1 & A(56) & (1+d) \\ \hline W(55) & t & A(55) & (1+r) & -1 \end{bmatrix}$$

Assuming wage growth at 54 is close to that at 55 and A(56) approximately equals A(55), then R(55,t) primarily differs from R(54,t - 1) because the first terms in the bracket in (7) is now multiplied by (1 + d) while the second term, -1, is multiplied by (1 + r). Since r exceeds d by assumption, R(55,t) can easily be less than R(54,t -1). Indeed, this change in the functional form of R(a,t) can produce sharp drops in accrual rates at the early retirement age for a host of pension plans and a range of realistic economic assumptions.

It is important to realize that the early retirement reduction, lower wages, and one less year of tenure yield lower benefits at 55 than at 56. The early retirement reduction reduces benefits at the rate d. But if benefits were taken at 55 they could accrue interest at the rate r. Thus by foregoing the early retirement option of receiving benefits at 55, a cost is incurred that depends on the difference r - d. If this loss is not offset by the increase due to wage growth and 1 year of additional tenure, there will be a drop in the benefit accrual rate between 55 and 56.

The same considerations pertain to benefit increments between 56 and 65. Recall that we have assumed a less than fair early retirement reduction

so that benefits accrued before 55 are valued based on the assumption that benefits are received starting at the age that yields maximum pension wealth. The optimum time to receive benefits accrued between 55 and 56 is 56, between 56 and 57 is 57, and so forth. But to gain benefits from working another year, it is necessary to forego the option of immediately taking acrued benefits at an advantageous reduction rate.

Between ages 56 and 65, R(a,t) equals:

(A9)  $R(a,t) + \lambda(1+d)^{-(65-a)}(1+r) A(a)t \left[\frac{W(a+1)}{W(a)} \frac{(t+1)}{t} \frac{A(a+1)}{A(a)} \frac{(1+d)}{(1+r)} - In contrast to the R(a,t) formula in (A5) that applies to the period between cliff vesting and early retirement, (A9) indicates that the actuarial reduction factor d, rather than the interest rate r, imparts an upward tilt in the R(a,t) profile between early and normal retirement, as long as the term in brackets is positive. In (A9) as in (A5) and (A8) the accrual rate, R(a,t), is an increasing function of the rate of nominal wage growth. Larger nominal interest rates reduce acrual rates at all ages, with a negative interaction with age prior to early retirement.$ 

While the expression (A5) is unlikely to be negative, large differences between wage growth and the interest rate r can yield negative increments in pension wealth after the early retirement age. To a first approximation, the bracketed term in equation (A9) will be positive if  $\Delta W/W + 1/t > r - d$ , where  $\Delta W/W$  is the percentage increase in wages, and 1/t is the percentage increase in tenure. It is easy to see, however, that low wage growth and high interest rates will yield negative increments.

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Pension accrual after normal retirement can be significantly negative. Assume that our hypothetical plan neither credits service after normal retirement nor provides an actuarial increase in benefits for postponing benefit receipt beyond the normal retirement age. In this case R(a,t) after normal retirement is given by:

(A10) 
$$R(a,t) = \lambda t^* A(a) \left[ \frac{A(a + 1)}{A(a)} - (1 + r) \right],$$

Where t\* equals the worker's service prior to age 65. Note that for the following reasonable parameter values:

 $\lambda$  = .02, t\* = 30, A(a) = 15, r = .04, and A(a + 1) = 14, R(a,t) = -.96, a quite substantial negative accrual ratio.

While the preceeding formulae are suggestive of the general shape of accrual rate profiles, there are few earnings-based plans with features as simple as the one considered here. In addition to more complicated rules for plan participation and vesting that often involve age as well as service requirements, there are a variety of methods of computing earnings bases, including career averages, and averages of earnings, possibly highest earnings, over a specified period or number of years. Reduction rates for early retirement are often a specified function of age, if not length of service. Some plans allow no further accrual after a given number of years of service. Roughly thirty percent of defined benefit participants belong to plans that are integrated with social security, and the form of "integration" can have an important effect on the pattern of benefit accrual. Other plans, in particular, those with social security offset formulae, provide supplemental benefits for early retirees prior to their receipt of social security benefits. In addition to these earnings-related plans, a significant number of plans

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covering over forty percent of defined benefit participants calculate benefits independent of the participant's earnings. Finally, there are plans that specify minimum and maximum benefit levels.