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THE EVOLUTION OF PRODUCTIVITY GAPS AND SPECIALIZATION PATTERNS

Bart Los and Bart Verspagen* University of Groningen and Eindhoven University of Technology (March 2003; revised February 2005)

ABSTRACT

This paper presents an industry-level model of growth and trade, in which evolving specialization patterns are the endogenous result of innovation, international technology spillovers, learning-by-doing and balance of payments-restricted growth. Differences between industries with regard to their share in consumption are shown to reinforce or mitigate the effects of specialization on aggregate productivity convergence patterns, depending on other parameters. The implications of the model are studied by means of simulation analyses for a wide range of parameter configurations.

1. INTRODUCTION

The productivity growth performance of countries has always been of central interest to economists. Over time, many theories about the sources of growth have been proposed, tested and refined. In most theories, technological progress emerges as the engine of growth. But the nature of the technology–growth relationship remains a matter of debate. Given that technological change contains a considerable degree of uncertainty, one of the most debated issues at a fundamental level is about the predictability of growth patterns. In the words of Kaldor (1996, p. 22):

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In contrast to the neo-classical economists who believed that economics should be pursued [...] making use of the same type of tools as mechanics, the English classical economists saw human societies as being in a continuous process of evolution, [...] [having] more in common with the laws of biology (including the basic unpredictability of the lines of development) than with the methods of the sciences concerned with inanimate matter, such as physics.

In the contemporary literature, this fundamental difference of insight with regard to the nature and predictability of the growth process and the role of technology in it has been staged in the debate between 'evolutionary' economists (e.g. Nelson and Winter, 1982) and the neo-classical inspired new growth theory (e.g. Romer, 1990). New growth theory considers economic growth as a smooth steady-state phenomenon that may be tuned in a relatively straightforward way by technology and innovation policies. The evolutionary approach, on the other hand, argues that patterns of economic growth are much more unpredictable, and that innovation policy may often have unintended effects.¹

As the above quotation of Kaldor already points out, however, there are also other approaches in economic growth theory that would point to the 'historical' and unpredictable nature of the technology–economic growth relation. These are to be found in the (modern) classical approach to economics, as well as the post-Keynesian approach.

The main aim of this paper is to explore the consequences of a model in which a number of forces related to technological change are united. These forces are taken from various parts of the literature, and contain elements inducing smooth growth paths, as well as elements more in accordance with the evolutionary or classical view of unpredictability.

Building on the existing literature, three sources of technological progress are discerned: innovation, international knowledge spillovers (or imitation), and learning-by-doing. We feel that a model that presents a unified framework is asked for, because many complications blur the comparability of the major lessons to be learnt from more partial models. We therefore put these three forces together onto a skeleton model of international economic interaction, and explore the parameter space of the model by means of simulation analysis. The model describes the evolution of a system of two trading economies that consist of multiple industries. The productivity growth rates of industries, as well as the specialization patterns of countries, are the outcome of the interplay between innovation, spillovers and

¹ Verspagen (2004) summarizes this debate in more detail than is possible here.

learning-by-doing. In the systematic simulation experiments, we look for ranges of parameter space that yield stable, steady state-like patterns of convergence between countries, as well as for parameter ranges that yield more unstable patterns (including divergence between countries). This approach allows us to draw some broad conclusions about the characteristics (in terms of parameter values) of technological progress for which aggregate labor productivity levels of countries tend to be relatively equal and to describe the corresponding specialization patterns.

International trade plays an important role in our model. Especially the effects of learning-by-doing are highly dependent on the export performance of countries. Moreover, the international competitiveness of a country's products is affected by its technological standards *vis-à-vis* its rivals. Consequently, a process of virtuous or vicious circles emerges, which also affects the industry structure. Thus, the model sees as parts of an international interdependent system countries, and is thus likely to yield different outcomes than model that consider countries as autarkic entities.

The paper is organized as follows. In the next section, we will discuss the sources of productivity growth and their impact on the international growth process according to several growth theories. Special attention will be devoted to the interactions of these sources with changes in the industry structure and international trade. Sections 3 and 4 deal with the model equations. In section 5, we will analyze the behavior of the model, mainly by means of simulation analysis. Section 6 concludes.

2. GROWTH AND TECHNOLOGY: THEORETICAL PERSPECTIVES

Most economists will agree that in the long run, technological change is one of the main sources of economic growth. But technology has its impact on the economy in many different forms. Looking at the literature on growth and technology, one may distinguish three main sources of technological change.

The first, and perhaps most direct, way is through research and development activities, carried out by firms as well as (semi-)public research organizations. The role of R&D in economic growth is the topic of the endogenous growth literature that started with Romer (1986, 1990). The endogenous growth literature contains many different ways of representing the impact of technology and R&D on economic growth. Romer (1990) proposed a model of horizontal product differentiation, in which the main source of productivity growth is an expanding variety of consumption goods, or intermediate goods used to produce a homogenous consumption good. Aghion and Howitt (1992) suggest a model of vertical product differentiation, where

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economic growth is represented through the R&D-driven emergence of new product varieties with higher quality.

One crucial aspect of the models in this tradition is the existence of technological spillovers, which we consider as the second source of technological change. Technological knowledge has aspects of a public good. In technical terms, technology spillovers are the offsetting force for decreasing marginal returns to investment, and hence make growth possible in the long run. Empirical models of R&D spillovers between countries (e.g. Coe and Helpman, 1995; Verspagen, 1997) tend to find that for many countries, especially the small but developed ones, technology spillovers are an important source of growth. Grossman and Helpman (1991) present theoretical models of R&D spillovers between countries. Because they assume that spillovers are stronger within country borders, and spillovers stimulate own R&D efforts, country size is an important determinant of R&D. Moreover, they argue that spillovers (and endogenous R&D) are important drivers of the trade specialization pattern of countries. Hence, trade, specialization and economic growth become interwoven in a causal manner (in much the same way as in Dosi et al., 1990 and Krugman, 1990). Such a relationship between trade, specialization and economic growth is an important topic of the model we present below, and is also addressed by other theoretical streams, which we will survey shortly below.

Technology spillovers also play a role in other parts of the literature. For example, based on the work of Gerschenkron (1962), Abramovitz (1979) suggests that technological imitation by relatively backward countries is an important way of 'catching-up'. Literature in this tradition, which has been summarized in Fagerberg (1994), tries to identify empirically the factors that make technological imitation easier. Viewed in this way, technological spillovers become a potential source of convergence between countries.

The third source of technological change that we will discuss can be characterized as learning-by-doing or cumulative learning. This is an important topic in both the early literature (e.g. Young, 1928; Verdoorn, 1949; Arrow, 1962) and some of the new growth models (e.g. Young, 1991). Technological change is generated as a result of experience in production or use. Such a mechanism generates positive feedback, i.e. high rates of technological progress result from high activity levels, or high growth of activity levels. A variety of mechanisms can be used to explain this phenomenon at the microeconomic level. Most of these explanations argue that ideas and procedures for small (incremental) innovations related to implementation may emerge as a result of using a technology. Although every single incremental innovation may be small, their joint cumulative effect is often large, as is for example shown in the historical studies of Habakkuk (1962).

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Cumulative learning is often modeled as a source of divergence between countries. If using a technology enhances learning, the ones who are most successful at this will also learn most: success breeds success. This implies a tendency for divergence of technology levels between countries, rather than convergence. Kaldor (1966) and Dixon and Thirlwall (1975) use this argument to make a point about persistence of growth rate differentials between regions. Cimoli (1994), in extending Cimoli (1988), provides a model in this tradition in which trade, specialization and growth are jointly modeled. In a similar fashion, Lucas (1988) presents a model about persistence of growth rate differentials between countries.

A final view on the role of technology in economic growth that we will survey briefly is the structural view. Contrary to the previous three streams, this does not represent a source of technology, but rather argues how the industrial composition of an economy interacts with technological change, and may produce different macro-growth patterns between countries. Differences between industries may be directly related to technology, through variables such as technological opportunity or age of the technology. But also more indirect variables, such as income elasticities, may play a role here, although only in combination with the more direct differences in technology between industries. If industries are characterized by different rates of productivity growth, or by different rates of demand growth (through, for example, income elasticities), economic structure becomes important for aggregate economic growth. This is a topic that is mostly explored in the post-Keynesian literature, such as Thirlwall (1979) and Pasinetti (1981). Whereas Pasinetti (1981) considers this topic mostly in the context of a closed economy, Thirlwall (1979) brings in foreign demand, and hence trade and specialization (similar to Krugman, 1990 and Grossman and Helpman, 1991). In Thirlwall's approach, the composition of exports and imports, and especially their respective income elasticities determine the growth potential of nations through balance-of-payments constraints.

The model developed in this paper aims to unite these different views on the technology–economic growth relationship. The model will be used to analyze how the mix of relative importance of the various mechanisms will affect the likelihood of convergence or divergence between countries in terms of their productivity levels. Thus, our model will take the form of a generic skeleton. On top of this skeleton, three different forms of technological change may be imposed: an (exogenous) steady-state exponential growth rate of productivity (we consider this as a simplified version of the endogenous R&D story), international technology spillovers between industries and productivity growth in the form of cumulative learning.

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3. MODEL DESCRIPTION: SHORT-RUN EQUATIONS

In order to keep the model relatively simple, we abstract from any other production factor than labor and further assume that commodities are produced for consumption purposes only.² The world economy consists of two countries, called North (N) and South (S). In this world, n commodities are produced. Both countries are assumed to be able to produce all commodities, but nothing precludes a situation in which some of the commodities are produced in just one country. The characteristics of a specific commodity are assumed to be independent of its country of origin. Consumption demand can be met by domestically produced and/or by imported commodities.

In each period, the output and employment levels for both countries are the result of the interplay of a number of state variables, presented in table 1.

The first set of state variables represents the technologies in use. The variables indicate the physical amounts of labor required to produce physical units of output, in each of the industries in North and South. Labor is supposed to be homogeneous, in the sense that workers can immediately and freely move from one industry to another. On the other hand, we assume that labor is immobile in a geographical sense, i.e. that workers do not migrate from North to South or vice versa. The second set of variables indicates the fractions of domestically produced outputs in consumption, for each of the commodities and for both countries. The third set reflects the preferences of consumers in both countries. These variables are defined as the shares of total consumption in a country devoted to a particular good, measured in constant prices. Finally, the fourth set of state variables indicates the prices of the goods, expressed in a common currency.

1.	$l_{Ni}^{c}, l_{Si}^{c} (i = 1,, n)$	Labor requirements per unit of output	
2.	$z_{\mathrm{N}i}, z_{\mathrm{S}i} \ (i=1 \ \ldots \ , n)$	Shares of domestically produced consumption	
		goods in consumption demand	
3.	$b_{Ni}, b_{Si} \ (i = 1, \ldots, n;$	Shares of commodities in aggregate	
	$\Sigma b_{\mathrm{N}i} = 1, \ \Sigma b_{\mathrm{S}i} = 1$	consumption	
4.	$P_{Ni}, P_{Si} (i = 1,, n)$	Commodity prices	

Table 1. State variables

Note: Indices N and S refer to North and South, respectively.

² See Los and Verspagen (2000) for a more elaborate model with intermediate input structures. In a qualitative sense, all conclusions are robust to the inclusion of input–output relations between industries.

The balance of payments plays an important role in our model. Arbitrary consumption vectors would only by chance yield a balance-of-payments (current account) equilibrium. As McCombie and Thirlwall (1994) argue, nothing prevents a country from being caught in a situation of current account deficits for a short time. In the long run, however, such a state of affairs is unsustainable unless capital inflows keep coming in infinitely and in steadily increasing amounts. Moreover, infinitely cumulating stocks of Southern (Northern) currency would not improve North's (South's) welfare.

Following Thirlwall (1979) and Verspagen (2001), we assume that total consumption levels in North and South must always correspond to balanceof-payments equilibrium. In reality, this does not necessarily happen immediately, but we consider this as a necessary simplification in the model. As we consider a closed system without exports and imports to and from third countries, we could write North's current account surplus (or deficit) as the difference between the value of the goods imported by South and the value of goods imported by North (see McCombie, 1993 for a similar approach). Hence, current account equilibrium prevails if and only if the following holds:

$$\sum_{i=1}^{n} p_{\mathrm{S}i}(1-z_{\mathrm{N}i}) b_{\mathrm{N}i} f_{\mathrm{N}} = \sum_{i=1}^{n} p_{\mathrm{N}i}(1-z_{\mathrm{S}i}) b_{\mathrm{S}i} f_{\mathrm{S}}$$
(1)

in which f_N and f_S denote the total consumption levels (in constant prices) in North and South, respectively. This equation can be rewritten in a way that expresses the current account-equilibrium consumption level in South in some of the state variables in table 1 and the level of consumption in North:

$$f_{\rm S} = \left[\frac{\sum_{i=1}^{n} p_{\rm Si}(1-z_{\rm Ni}) b_{\rm Ni}}{\sum_{i=1}^{n} p_{\rm Ni}(1-z_{\rm Si}) b_{\rm Si}}\right] f_{\rm N} \equiv \frac{r_{\rm N}}{r_{\rm S}} f_{\rm N}$$
(2)

Equation (2) shows that the solutions that represent current account equilibrium together constitute a line in the plane $f_N - f_S$. Since prices and consumption shares are always positive and trade shares cannot exceed 1, the slope of the line is positive. The interpretation of this result is rather straightforward. Increased consumption in North induces more imports from South, which enables South to import more from North. Given current account equilibrium, these imports increase South's consumption. The value of the slope depends on the relative prices (exporting a cheap good does not earn much money for South to import expensive goods from North), the trade

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shares (South does not gain much in terms of consumption from increased Northern consumption if North produces its own goods, or if South imports virtually everything) and the consumption shares (South does not gain much by exporting a good that is hardly demanded by North).

In order to determine a unique short-run solution for f_N and f_S , (i.e. to choose a specific point on the current account equilibrium line), we have to impose an additional equation. We assume that one of the countries is constrained by available labor resources. In each period, either employment in North equals its labor supply (l_N^{sup}) or employment in South equals its labor supply (l_S^{sup}) , depending on which country reaches its constraint first. Labor supply is exogenous and does not change over time. Since trade implies that employment levels in North do not only depend on North's own consumption but also on consumption in South (and vice versa), the full employment assumptions yield another two relations between the two total consumption levels f_S and f_N . Full employment prevails in North if and only if

$$l_{\rm N}^{\rm sup} = \sum_{i=1}^{n} l_{\rm Ni}^{c} \left[z_{\rm Ni} b_{\rm Ni} f_{\rm N} + (1 - z_{\rm Si}) b_{\rm Si} f_{\rm S} \right]$$
(3)

This expression can be rewritten as

$$f_{\rm S} = \frac{l_{\rm N}^{\rm sup}}{\sum_{i=1}^{n} l_{\rm Ni}^{c} (1-z_{\rm Si}) b_{\rm Si}} - \left[\frac{\sum_{i=1}^{n} l_{\rm Ni}^{c} z_{\rm Ni} b_{\rm Ni}}{\sum_{i=1}^{n} l_{\rm Ni}^{c} (1-z_{\rm Si}) b_{\rm Si}} \right] f_{\rm N} \equiv \frac{l_{\rm N}^{\rm sup}}{\lambda_{\rm S}} - \frac{\lambda_{\rm N}}{\lambda_{\rm S}} f_{\rm N}$$
(4)

Since both the numerator and the denominator of the slope coefficient are positive, the line described by equation (4) is downward sloping. If the consumption level in North would be reduced, the consumption level in South would have to increase in order to keep the Northern labor previously employed in the production of domestically demanded output at work. The slope itself is determined by productivity coefficients, trade coefficients and consumer preferences. Analogously, we can find a relation corresponding to full employment in South:

$$f_{\rm S} = \frac{l_{\rm S}^{\rm sup}}{\sum_{i=1}^{n} l_{\rm Si}^{c}(1-z_{\rm Ni}) b_{\rm Ni}} - \left[\frac{\sum_{i=1}^{n} l_{\rm Si}^{c} z_{\rm Si} b_{\rm Si}}{\sum_{i=1}^{n} l_{\rm Si}^{c}(1-z_{\rm Ni}) b_{\rm Ni}}\right] f_{\rm N} \equiv \frac{l_{\rm S}^{\rm sup}}{\mu_{\rm N}} - \frac{\mu_{\rm S}}{\mu_{\rm N}} f_{\rm N}$$
(5)

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Solving equations (2) and (4) yields the situation in which North's consumption is both balance of payments-constrained and resource-constrained, but South is only balance of payments-constrained:

$$f_{\rm N} = \frac{r_{\rm S}}{r_{\rm N}\lambda_{\rm S} + r_{\rm S}\lambda_{\rm N}} I_{\rm N}^{\rm sup} \quad \text{and} \quad f_{\rm S} = \left(\frac{r_{\rm N}}{r_{\rm N}\lambda_{\rm S} + r_{\rm S}\lambda_{\rm N}}\right) I_{\rm N}^{\rm sup}$$
(6)

Of course, we can also find the intersection of the upward sloping balanceof-payments line (2) and the downward sloping line (5), which corresponds to resources and balance-of-payments constraints on South's consumption and balance of payments-constrained consumption in North:

$$f_{\rm N} = \frac{r_{\rm S}}{r_{\rm S}\mu_{\rm S} + r_{\rm N}\mu_{\rm N}} l_{\rm S}^{\rm sup} \quad \text{and} \quad f_{\rm S} = \left(\frac{r_{\rm N}}{r_{\rm S}\mu_{\rm S} + r_{\rm N}\mu_{\rm N}}\right) l_{\rm S}^{\rm sup} \tag{7}$$

The short-run equilibrium point in the (f_N, f_S) plane is now defined as the minimum of the points given by equations (6) and (7), since one country would produce above its capacity in the other intersection point. In this short-run equilibrium one of the two countries will thus experience unemployment.³ Given these consumption levels and their composition with regard to industries and countries of origin, the output levels and its industry compositions in North and South can be determined for the period under consideration:

$$q_{Ni} = z_{Ni}b_{Ni}f_{N} + (1 - z_{Si})b_{Si}f_{S} \text{ and } q_{Si} = (1 - z_{Ni})b_{Ni}f_{N} + z_{Si}b_{Si}f_{S}$$

(*i* = 1,..., *n*) (8)

Finally, commodity-specific prices (expressed in a common currency, assuming an exchange rate which is known at the beginning of each period) are assumed to reflect labor costs:

$$p_{Ni} = w_N l_{Ni}^c$$
 and $p_{Si} = x w_S l_{Si}^c$ $(i = 1, ..., n)$ (9)

The symbols w_N and w_S denote the nominal wage rates (in North and South, expressed in the national currencies), which we assume to be given at the

³ Note that our notion of equilibrium does not imply equality of labor supply and demand at the world level.

beginning of each period. The exchange rate (also given at the beginning of each period) is denoted by x. This implies that we adopt the rule to express both Northern and Southern prices in Southern currency.

The short-run model we introduced in this section yields output and employment levels by industry and country, as well as consumption levels for each of the commodities produced in North and South. These levels are completely determined by the production technologies, trade relations, consumer preferences, labor supply, prices, the exchange rate and the nominal wage rates prevailing during a period. Since we are primarily interested in the long-run dynamics of the endogenous variables mentioned, we now turn to the specification of the equations that describe the intertemporal behavior of the variables that we have assumed so far to be fully exogenous.

4. MODEL DESCRIPTION: INTERTEMPORAL RELATIONS

In this section we present the intertemporal equations that allow us to study long-run issues such as output growth, convergence and structural change. Unlike the previous section, this section does not include the derivation of solutions. Due to the mathematical complexity caused by our explicit focus on economies consisting of multiple industries, analytical solutions are hard to derive. We will first deal with the equations describing technological progress and subsequently discuss the relations we specified with regard to trade share dynamics and exchange rate movements.

4.1 Technology dynamics

Following our earlier interindustry models of technological change (Los, 2001; Verspagen, 2001), we model innovation as changes of input coefficients. We define the (industry-specific) rates of technological progress as the proportional changes of the inverses of the l^e coefficients, i.e. the ratios between output and labor input. We write the dynamics of labor inputs per unit of output as

$$l_{Ni}^{c}(t+1) = \gamma_{Ni}(t+1)l_{Ni}^{c}(t) \quad \text{and} \quad l_{Si}^{c}(t+1) = \gamma_{Si}(t+1)l_{Si}^{c}(t)$$
(10)

We allow both for differences in productivity growth rates between industries and between countries. We model two regimes. In the first regime, the industry under consideration has lower labor requirements per unit of output than its foreign competitor. In this case, we call the industry in this country the

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leader industry, and the corresponding industry in the other country the lagging industry.

We assume that leader industries experience technological progress through two mechanisms. First, a constant exogenous productivity growth rate is assumed, which reflects the labor-saving effects of innovation.⁴ This reflects the (neo-classical) idea of steady-state growth at a fixed rate. Second, a mechanism that we label the Kaldor–Verdoorn mechanism represents cumulative learning: if the output of an industry grows, it is assumed that learning-by-doing and opportunities for specialization of workers lead to increased productivity.

In the lagging-behind regime, we assume that the Kaldor–Verdoorn mechanism is still functioning, but that the exogenous fixed rate of technological progress is absent. Instead, in the lagging country, the technology gap to the leader industry is assumed to cause spillovers through imitation of the competitor's production technology.

Summarizing, the reductions in labor coefficients under the two regimes can be represented by

Leader regime:
$$\gamma_{i}(t+1) = \frac{1}{1 + \kappa_{i} \left[\frac{q_{i}(t) - q_{i}(t-1)}{q_{i}(t-1)}\right]^{1/\sigma_{i}} + \rho_{i}}$$
 (11)

Lagging regime:
$$\gamma_i(t+1) = \frac{1}{1 + \kappa_i \left[\frac{q_i(t) - q_i(t-1)}{q_i(t-1)}\right]^{1/\sigma_i} + \alpha_i \ln\left[\frac{l_i^c(t)}{l_i^{c^*}(t)}\right]}$$
 (12)

in which κ (>0), σ (>1), ρ (>0) and α (0 < α < 1) are industry-specific parameters and l_i^{**} indicates the unit labor requirements in the corresponding leader industry. κ and σ relate to the Kaldor–Verdoorn mechanism taken from Verspagen (1993) and reflect the rate of dynamic learning. The mechanism brings a positive feedback into the dynamic model, since high output growth leads to high productivity growth (although at a decreasing marginal rate). ρ is the steady-state rate of technological progress in the leading industry; α reflects the spillover mechanism in the lagging country. The larger the productivity gap in terms of labor inputs per unit of output, the faster

⁴ For simplicity, we do not include stochastic arrivals of innovations, nor do we incorporate explicit search for innovations (R&D) in the model. See Los (2001) for an interindustry model with R&D and stochastic innovation in a single-country context.

productivity in the laggard industry will grow. The value of α is assumed to reflect social capability for assimilating spillovers (Abramovitz, 1979), which means this is taken as an exogenous factor. Note, however, that our multiindustry specification implicitly takes account of the fact that incompatibility of output structures plays an important role, i.e. technological congruence is endogenous. For example, if South would lag North in one industry but produces only a very small part of its output in this industry, aggregate labor productivity would not benefit much from this industry-specific technology gap.

4.2 Trade share dynamics

Trade share dynamics are assumed to be ruled by changes in relative competitiveness. According to traditional theory, the competitiveness of countries is determined by costs per unit of output. In such a situation, the interplay of two developments would determine changes in a country's competitiveness: reductions in the amounts of labor required per unit of output and changes in the relative wage rates.⁵ These factors are summarized by prices (equation (9)), so that we assume that changes in a country's shares on the world markets are dependent on price differentials (only).

To determine the commodity-specific trade shares, we use the concept of an inverted logistic curve, as illustrated in figure 1. In mathematical terms, this relation between the price ratio and the 'equilibrium' market share of North's industry i on its domestic market for consumption goods is

$$z_{Ni}^{*} = \frac{1}{1 + e^{-\left(\ln\frac{p_{Ni}}{p_{Si}} - \varepsilon_{i}\right)/\varphi_{i}}} \quad \text{and} \quad z_{Si}^{*} = \frac{1}{1 + e^{-\left(\ln\frac{p_{Ni}}{p_{Si}} - \varepsilon_{i}\right)/\varphi_{i}}}$$
(13)
$$*\frac{z_{Ni}^{*}}{1 + e^{-\left(\ln\frac{p_{Ni}}{p_{Si}} - \varepsilon_{i}\right)/\varphi_{i}}} -5 \quad -3 \quad -1 \quad 1 \quad 3 \quad 5 \quad \ln(p_{Ni}/p_{Si})$$

Figure 1. Trade shares.

⁵ These unit labor costs are generally converted to a common currency. Hence, exchange rate changes may alter the competitiveness structure as well.

The parameter ε can be interpreted as the value of the logarithm of the price ratio for which the market shares are equally divided. For perfectly tradable goods this parameter will equal zero, but for most goods the price ratio corresponding to equal market shares will have a positive value. In this case, the market shares of domestically produced inputs will be larger than 50 per cent when prices are equal. The extent to which the market share at the unit price ratio differs from 50 per cent is also dependent on the parameter φ (>0), which represents the commodity-specific sensitivity of trade shares to changes in the price ratio. The lower φ , the more sensitive the trade shares are. The parameters φ may be affected by a number of things, such as costs of transportation, geographical distance and non-tariff trade barriers.

Trade shares are not assumed to adjust immediately to changes in prices. We model an adjustment process, in which the gap between the actual trade shares z and the equilibrium trade shares z^* vanish gradually in the absence of shocks:

$$z(t+1) = z(t) - \eta^{t} [z(t) - z^{*}(t+1)]$$
(14)

with η^t (0 < η^t < 1) denoting the speed of adjustment.

4.3 Wage rates, the exchange rate and remaining variables

The two country-specific nominal wage rates are assumed to be constant, at least if expressed in national currencies. When technological progress reduces the unit labor requirements, prices will consequently be reduced and the real wage rate will grow. One caveat applies, however. In a system of flexible exchange rates, the purchasing power of a given amount of Northern currency relative to an identical amount of Southern currency may change.

In the modeling of exchange rate dynamics we use a specification similar to that of trade shares. The exchange rate is a weighted average of the actual rate and an equilibrium rate based on purchasing power parity (PPP) of the two currencies.⁶

$$x(t+1) = x(t) - \eta^{x} [x(t) - x^{*}(t+1)]$$
(15)

⁶ In empirical studies, several ways to define PPP have been proposed. Our output-based specification in equation (16) should be considered as a convenient way to bring tendencies towards PPP into the model, not as an expression of a preference for any specific empirical methodology.

The smaller η^x ($0 \le \eta^x \le 1$), the more a system of fixed exchange rates is approximated. x^* is determined according to

$$x^{*}(t+1) = \frac{\sum_{i=1}^{n} p_{Ni}^{nat}(t)[q_{Ni}(t) + q_{Si}(t)]}{\sum_{i=1}^{n} p_{Si}^{nat}(t)[q_{Ni}(t) + q_{Si}(t)]}$$
(16)

The superindices nat indicate prices expressed in national currencies.

Finally, we assume that the consumption shares of the industries are fixed in each country. Moreover, we assume that these variables do not differ between countries. Thus, consumer preferences are assumed to be identical.⁷

5. MODEL ANALYSIS

5.1 Comparative statics of innovation

Before we turn to a discussion of some of the simulation results we obtained, we illustrate the basic effects of an innovation by a diagram that depicts some highly simplified comparative statics. In figure 2, the axes indicate the total consumption levels for North and South. The solid upward sloping line (I)

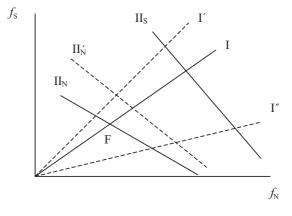


Figure 2. Consumption effects of innovation.

⁷ Los and Verspagen (2000) study the consequences of income-specific consumer preferences for productivity growth differentials, by means of a model that resembles the one introduced here.

reflects all pairs of consumption levels for which the balance of payments is in equilibrium in the initial situation (see equation (7)). The downward sloping solid lines (II_N and II_S) indicate all pairs of consumption levels for which full employment initially prevails in North and in South, respectively (see equations (10) and (11)). The slopes of these lines will generally differ, e.g. due to different compositions of consumption bundles with respect to countries of origin. In the situation depicted, consumption levels are given by the intersection point F, in which North experiences full employment and South faces excess labor supply.

Now, suppose that North generates a labor saving innovation. Consequently, the labor constraint will be less tight, and for given consumption levels in North higher consumption levels in South are attainable, since more 'effective' labor is available to produce exports. This is reflected by the upward shift of the Northern full employment line (dashed line II_N'). In general, the slope will change as well, but the sign of this change depends on the interplay of many parameter values. Nevertheless, the 'first-order' effect of technological progress in the labor-constrained country is an increase in both North's and South's consumption levels.

The supposed innovation in North also has some 'second-order' effects. The net effects of these are ambiguous, as will become clear after studying the dashed lines I' and I". The lines represent two important opposite effects. First, innovation yields a lower price per unit of output for North. This implies that for a given amount of exports, North can buy fewer imports and must reduce its consumption, while South can increase its import volume at constant costs (I'). This is a terms-of-trade effect. Second, North's reduced price enhances its competitiveness relative to South, which will cause higher market shares. Consequently, innovating North requires fewer imports per unit of output, which enables it to produce more consumption goods. For South the opposite holds and its attainable consumption level will fall. This effect is documented by curve I".

Which of the two second-order effects dominates depends on a number of parameters and variables, of which the sensitivity of market shares to price changes is an important one. The bottom line of this simple comparative statics analysis is that it is impossible to tell in advance which effect will dominate, and hence what the ultimate effect of an innovation on relative growth rates will be.⁸

 $^{^{8}}$ Alternatively, we could have studied the effects of a labor-saving innovation in South. This would lead to identical conclusions, except for the fact that it would not alleviate the scarcity of labor in North, which is the binding constraint for the world economy in the depicted case. Hence, the consumption levels would still remain on line II_N.

5.2 Spillover-cumulative-learning cycles'

The model often generates a particular cycle, which we dub the 'spillovercumulative-learning cycle'. This is caused by the interplay between the various forms of technological progress in the model, especially the combination of the Kaldor–Verdoorn learning and spillover effects. Since this cycle is rather crucial for the overall analysis of the model, we discuss it here in some detail. Under specific parameter values this cycle is a stable feature of the model, while it dampens out with different values. We will discuss in the next subsection how the behavior of the cycle changes under specific parameter values. Note that the 'spillover-cumulative-learning cycle' is in some respects similar to the properties of the model proposed by Landesmann and Stehrer (2000).

A typical situation is depicted in figure 3. The vertical axis of the upper diagram indicates the so-called technology gap, which is defined as the logarithm of the ratio between the labor requirements per unit of output in a

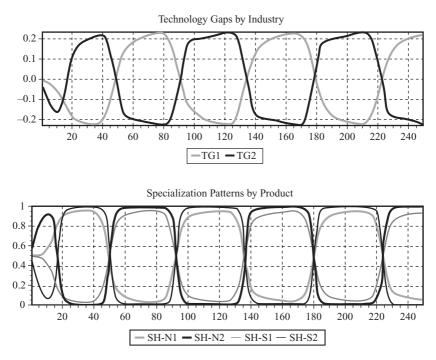


Figure 3. The 'spillover-cumulative-learning cycle'.

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Northern industry to such requirements in its Southern counterpart. Hence, a negative value points towards a technological advantage of a Northern industry. In the lower panel, the shares of North and South in the world production of the two goods are indicated on the vertical axis (e.g. SH-N1 stands for the share of North in the world production of good 1).

As can be concluded from the upper panel of figure 3, the initial parameter setting represents a situation in which North has a technological advantage in both industries. The most prominent phenomenon emerging is that so-called 'taking-over' occurs at the level of industries: not only does South take the technological lead in industry 2 after less than 20 periods, but after a subsequent interval of about 30 periods the leadership pattern is reversed. This taking-over happens almost simultaneously in both industries. Specialization patterns also evolve in a cyclical fashion. What drives these cycles?

The spillover part of the dynamics consists of technological imitation that drives the technology gap towards an equilibrium value. It is important to note that this equilibrium value can change endogenously over the simulation, and this is exactly what happens when the technology gaps alternate between positive and negative 'attractors'. Whether the equilibrium value is positive or negative depends on ρ and the Kaldor–Verdoorn effect. The first of these two factors (ρ) always gives the leading country an advantage, since $\rho = 0$ in the lagging country.

At the upper turning point of either one of the technology gaps in figure 3, the lagging country has been experiencing a fall of its market share, because the increasing gap has led to a competitive disadvantage of the lagging country. The technology gap approaches a short-run equilibrium value, because the spillover bonus increases, and thus offsets the effect due to ρ and Kaldor–Verdoorn. Because the technology gap now stops growing, the trend of a declining market share also stops. The laggard is now able to benefit from the generally expanding world market and realizes positive production growth. This sets in motion the Kaldor–Verdoorn learning effect. A slow-down of production growth in the leading country is induced because the lagging country captures more of the market. Through the Kaldor–Verdoorn effect, this induces a slowdown of the rate of productivity growth in the leading country. This changes the short-run equilibrium value of the technology gap, which becomes smaller. The result is that the gap now starts to decline.

When the gap becomes zero, the spillover bonus disappears, but now the country becomes the leading country, and the effect due to a positive ρ sets in. The other (formerly leading) country now loses the bonus due to ρ , but

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starts to experience a spillover bonus. In figure 3, the parameter values have been chosen such that the technology gap actually reverses sign, but with different parameter values, this does not need to happen. In particular, for higher values of ρ , the leader country has such a strong advantage that the gap does not change sign, and the lower turning point occurs on the same side of the horizontal zero level as the upper turning point. At the lower turning point, the same logic as for the upper turning point applies, but now with the roles (leader or laggard) of the two countries reversed. The dynamics are symmetric.

An important feature of figure 3 is that the Kaldor–Verdoorn mechanism (if strong enough) enables countries with an initial productivity lag in *both* industries to enter a symmetric situation in which both countries have a technological edge in one industry. In our more systematic study of relative performances under different parameter settings that follows in the next subsection, we will therefore assume such a symmetric situation in the initial periods already.

5.3 Behavior under various parameter value settings

In order to get insight into the behavior of the model beyond simple comparative statics, we resort to simulation analysis. We concentrate on the set of parameters related to technological progress, i.e. ρ , κ , σ and α . The number of industries is set to two in all simulations. To keep the analysis as tractable as possible, we choose our basic parameter configuration in a way that both goods and both countries are (initially) as similar as possible. Exact parameter values are documented in the Appendix, which shows that the production processes of both goods in North and South are initially the same, except for a very small difference in labor requirements to induce differences between the two countries in terms of the regimes of technological progress. Each country is assumed to be the technological leader in one industry. Initial trade shares are all equal. The only difference between industries lies in the consumption shares: good 1 is consumed four times as much as good 2. With respect to the other parameters that govern the dynamic processes, the two goods are perfectly identical.

The main variable that we are interested in is the aggregate level of inequality between countries, which we measure as the absolute value of the logarithm of the ratio between the macroeconomic labor productivity levels in North and South, averaged over the simulation period of a single run. All results are based on 250 periods, of which the first 100 were not used because they show

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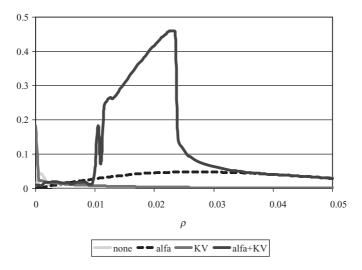


Figure 4. Effects of innovation rates on productivity gaps.

traces of the choice of initial conditions.⁹ An inequality indicator of, say, 0.4 thus means that the aggregate labor productivity levels differ on average by a factor $e^{0.4} \approx 1.5$. To illustrate some of the general tendencies of the model, we show in figure 4 the results for a range of values of ρ , while simultaneously switching on or off the other forms of technological progress. In the figure, the inequality indicator is depicted on the vertical axis (higher values indicate more inequality). Values on the horizontal axis denote the value of ρ . The values for σ and α are 6.0 and 0.2, respectively. We pick the value of κ such that the Kaldor–Verdoorn mechanism yields a 1 per cent growth rate of labor productivity for a growth rate of production equal to 1 per cent.

The figure contains four lines. The first one is denoted by 'none', which indicates that both the spillover parameters and the growth rate implied by the Kaldor–Verdoorn mechanism (cumulative learning) are set equal to zero. We see that this curve rises steeply in the segment of very low rates of technological

9 The expression used is

$$\frac{1}{T-t_0} \sum_{t=t_0}^{T} \left[\ln \frac{\sum_{i=1}^{n} q_{Ni}(t)}{\sum_{i=1}^{n} q_{Ni}(t) l_{Ni}^c(t)} - \ln \frac{\sum_{i=1}^{n} q_{Si}(t)}{\sum_{i=1}^{n} q_{Si}(t) l_{Si}^c(t)} \right]$$

with n = 2, t0 = 100 and T = 250. The term between brackets indicates that aggregate labor productivity is measured in quantities of outputs over labor requirements. This amounts to specifying units of goods in such a way that their unit prices equal 1 in the initial period.

progress in the leading industries, reaches a maximum average aggregate technology gap for $\rho = 0.001$ and approaches zero for larger values of ρ . This tendency towards zero is perhaps easiest to grasp. South is the leader in industry 1 and will thus also innovate in this industry. North is the leader and innovator in industry 2. Without any other ways of productivity increase, there is no way for the follower to converge to the leader, and the price gap between the two countries for each good will grow. Complete specialization is the result. Since both the rates of technological progress and the initial labor productivity levels are equal for both industries in this set of simulations, this will lead to equal macroeconomic levels of labor productivity.¹⁰

However, at low rates of innovation, we see the level of disparity between the countries rising with ρ . The reason for this is that specialization is less pronounced in this case, and both countries remain active forever in the industry in which they have a competitive disadvantage. This most heavily affects North, since it attracts the same share of the world production of good 1 as South attracts of the world production of good 2, but the market for good 1 is much larger. Consequently, more labor is allocated to low-productivity activities in North. This effect is obviously absent for $\rho = 0$, but increases for small positive values of ρ . This is reflected in the rising trend of disparity. When complete specialization starts to emerge for higher values of ρ , the curve peaks and starts to fall towards zero in the way already described.

Introduction of the Kaldor–Verdoorn cumulative causation mechanism (line 'KV') leaves these dynamics essentially unchanged, but increases the intensity. Specialization in an industry causes output growth, which in turn leads to productivity growth and even more specialization. If the annual long-run growth rate implied by the Kaldor–Verdoorn mechanism is set at 0.01, very low levels of ρ (in the order of magnitude of 0.001) are already sufficient to reach almost full specialization before period 100. Hence the 'KV' line jumps up immediately after $\rho = 0$, but falls directly after that.

With only technological imitation of leaders by laggards being present, the nature of the dynamics is again similar (the 'alfa' line). A positive rate of innovation for leaders and a positive spillover rate for laggards imply convergence towards a constant technology gap, and therefore a constant degree of specialization. The higher ρ for the given value of α , the stronger is the long-run degree of specialization. Hence, for high values of ρ , specialization is almost complete and both countries perform equally well according to the macroeconomic labor productivity yardstick. For low ρ , we observe the same

¹⁰ It should be noted that this does not lead to equal GDP levels: the unequal consumption shares cause unemployment in the country that produces the good that is relatively unpopular with the consumers.

kind of dynamics as was seen for the 'none' line. Now, however, labor productivity levels of both industries in a country deviate much less, because of the tendency to converge to a fixed gap. Hence incomplete specialization is relatively harmless in terms of aggregate technology gaps. This is why the upward sloping part of the curve covers a wider span of ρ .

The by far most dramatic effects of changes in the rate of innovation in the leading industries are found if Kaldor–Verdoorn effects and spillovers are simultaneously taken into account (line 'alfa + KV'). In this case, the type of dynamics that was described in the discussion of figure 3 starts to play a role. In particular, the steep rise and decline of labor productivity differentials in the range of ρ s after the value $\rho = 0.009$ deserves special attention. It turns out that this sudden change of behavior of the aggregate productivity gap is due to a qualitative change in the 'spillover-cumulative-learning cycle'.

To the left of the point $\rho = 0.009$, the 'spillover-cumulative-learning cycle' unfolds as in figure 3, i.e. leadership periodically switches between the countries and the sign of the technology gaps reverses. The amplitude of the technology gap cycles is relatively small, i.e. the upper and lower turner points occur at relatively small (absolute) values of the gaps. Specialization patterns co-evolve with the technology gaps, and this yields inequality as described in the discussion of figure 3.

To the right of the 'bifurcation point' at $\rho = 0.009$, the technology gaps no longer change signs, and technological leadership always remains with one country. This is due to the fact that the bonus for the technological leader (ρ) is now so high that it prevents taking-over. As a result, trade specialization does not change sign over time, and this leads to a higher aggregate productivity gap because it is now always just one of the countries benefiting from the larger market for good 1. In fact, at values of ρ just slightly larger than 0.009, model behavior is characterized by the 'spillover-cumulative-learning cycle', until after a considerable number of periods the technology gaps start to converge to equilibrium values leading to a fixed, incomplete specialization pattern. We cannot give a clear explanation of what drives this regime change and its timing, but rather consider it as an example of non-steady-state aspects of the technology–growth relations stressed by our model.

The sharp drop in the 'alfa + KV' line at $\rho = 0.011$ corresponds to a situation in which South is the technological leader in both industries. The technology gap for North is equal in the two industries, and hence no specialization occurs: the share of North (South) in both industries is equal to each other. Specialization does not induce inequality in this case. To the right of the point $\rho = 0.011$, the behavior of the model does not change in a qualitative sense. Specialization becomes more pronounced, however, and hence inequality grows.

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Around the point $\rho = 0.022$, specialization becomes almost complete in both industries. The tendency for the equilibrium technology gaps to grow does not stop, due to the increasing ρ . Consequently, prices between the two countries keep diverging. Because of the complete specialization, the trade shares of both countries for the goods in which they are specialized cannot grow further, and the only effect of the price differentials is on the terms of trade. In terms of the discussion of figure 2 above, this means that one of the two second-order effects (associated to a shift of the balance-of-payments restriction line in figure 2) disappears. This causes more equality, which is reflected by the huge drop of the 'alfa + KV' curve in figure 4 for innovation rate values that exceed $\rho = 0.024$. For very high values of ρ , the 'alfa + KV' curve and the 'alfa' curve coincide, which reflects that the strong effects of exogenous innovations dominate the Kaldor–Verdoorn effect.

The point of the model is not so much to explain specific figures like figure 4. After all, by choosing different values of the parameters, or even by plotting values of a different parameter on the horizontal axis, it would be possible to generate quite different figures. Thus, figure 4 should only be considered as an illustration of the type of mechanisms that exist in the model, and the way they interact. In order to paint a broader picture of the range of possible outcomes, we proceed to vary the technological change parameters in a systematic way against each other.

In figure 5, we plot the macroeconomic productivity gap indicator that featured in figure 5 against two technology-related parameters, the innovation

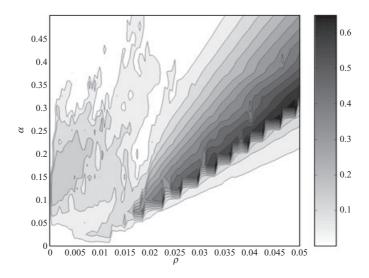


Figure 5. Joint effects of innovation and spillovers on productivity gaps.

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parameter ρ and the spillover parameter α . The Kaldor–Verdoorn parameter σ is held constant at 3.0. Dark (light) regions indicate parameter configurations for which the inequality indicator is high (low). The picture looks rather chaotic for some ranges of parameter values, but some tendencies emerge immediately. For very low values of ρ and very high values of α , the gaps are small. This is due to the well-known logic from technology gap theories of growth that equilibrium gaps are low for such parameter configurations. The technology gaps are thus small in both industries.

At first sight, the finding that the gaps are small for the opposite configuration, in which exogenous innovation is high and spillovers are virtually absent, may appear less straightforward. In this case, complete specialization prevails. Further, the terms-of-trade effect discussed with respect to the right-hand-side range of ρ values in figure 4 applies. The diagonally oriented combinations of ρ and α values that produce large productivity gaps correspond to the situation in which industry-level gaps are large but specialization is not yet complete. The steep decline 'to the southeast' also corresponds to the steep decline found in figure 4. Finally, no clear-cut pattern can be detected for the range characterized by low values of ρ and low to medium values of α . This is partly due to the presence of situations in which one country becomes the productivity leader in both industries and specialization hardly occurs (note in particular the 'narrow valley' for ρ s approximately equal to 0.02 and α s higher than about 0.15).

The relationship between the aggregate productivity gap on the one hand and the innovation rate ρ and cumulative learning mechanism σ on the other is depicted in figure 6. The value of the spillover parameter α is held constant at 0.2.

For very low values of σ , the aggregate productivity gap is huge (note the difference in the indicator values associated with a given level of darkness, relative to the figure 6). This is due to the fact that a modest growth of output leads to a substantial increase in productivity in this range of σ values. Consequently, the cycles from figure 3 have much higher amplitudes (industry-specific gaps will be large) and the frequency of the cycles is much higher. Specialization patterns change quickly, but full specialization occurs often. Hence, aggregate productivity gaps change sign quite often, but are large in the majority of time periods. This effect is reinforced if ρ takes on relatively high values, as is evidenced by the border between the lightest and lightest but one shade.

For higher values of σ (exceeding 2.5), another interesting phenomenon emerges from the figure. Both low and high values of ρ yield small gaps on average, whereas intermediate values yield larger gaps. Again, this resembles the hump shape observed in figure 4. For low values, gaps and specialization

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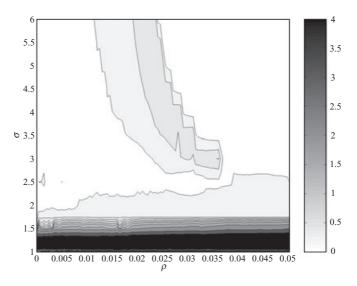


Figure 6. Joint effects of innovation and learning-by-doing on productivity gaps.

patterns behave cyclically and for high values specialization is complete. Due to negative terms of trade effects, inequality declines for higher ρ values. The inverse relation between ρ and σ that characterizes this 'ridge of divergence' is due to the strong Kaldor–Verdoorn effect, which promotes cyclical behavior. Thus, for a low value of σ , which indicates strong cumulative learning effects, a high exogenous innovation parameter value ρ is required to offset this tendency and obtain full specialization.

Finally, figure 7 gives an impression of the model's behavior for combinations of varying spillover parameter α and the learning-by-doing parameter σ . The exogenous innovation rate is held constant at 0.025. As in figure 6, the productivity inequality is huge for low values of σ . Again, this is due to large productivity gaps at the industry level and fast reversals of specialization patterns. It should be noted, however, that a relatively modest strength of the cumulative learning mechanism suffices to generate such patterns for low values of α . This is due to the fact that weak spillovers yield large short-run equilibrium gaps for a given innovation rate. Consequently, leader industries can benefit to a significant extent from learning-by-doing.

Another noticeable feature is the 'ridge of divergence' that emerges for configurations with high values of α and σ . On the left of this ridge, the aggregate gaps are small, due to the terms-of-trade effects that also cause the drop in figure 4. For low values of α , industry-level technology gaps are

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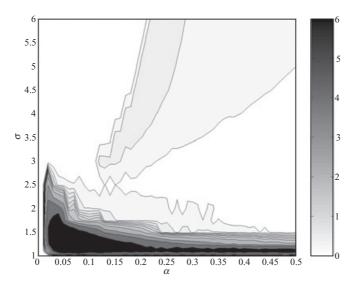


Figure 7. Joint effects of spillovers and learning-by-doing on productivity gaps.

large. In this sense, this phenomenon also resembles the northeast region of figure 6. High values of ρ and low values of α both yield large equilibrium technology gaps at the industry level. On the right-hand side of the ridge, spillovers are so strong that technology gaps at the industry level remain very small. Thus, specialization is far from complete, but because labor productivity levels between industries do not deviate much, this does not have strong effects on macroeconomic productivity gaps.

6. CONCLUDING REMARKS

The two-country-two-industry model that was developed in this paper integrates a number of well-known partial determinants of economic growth. First, demand-side and supply-side mechanisms were merged. The post-Keynesian notion that the rate of export expansion limits the attainable output growth rate was combined with the more mainstream argument that output growth is determined by the increasing availability of production factors or the growth of their productivity. In the model, the latter determines the size of the world markets, whereas the former play an important role in the division of the world markets between the two countries.

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A second important integration of well-recognized explanations concerns the sources of technological progress. The model distinguishes between two regimes, one in which the industry is on the technological frontier, and one in which the industry lags its foreign competitor in terms of labor productivity. Both regimes have one source of productivity growth in common: the benefits from learning-by-doing, specified as a causal relationship from output growth to productivity growth. Further, exogenous productivity growth is present in the leader regime. In the laggard regime, the industry can benefit from knowledge that cannot be appropriated by the competing industry at the productivity frontier.

The model is set up in a very general way, so that it can be helpful in analyzing a wide range of issues regarding relations between technological change, trade and growth. The generality of the model comes at the cost of complexity, and we resort to simulation experiments for analysis of the model. The focus of these experiments was on the effects of the three sources of technological progress on relative performance in aggregate labor productivity levels and trade specialization. The chosen parameter configurations were such that the two industries we distinguish were as identical as possible between countries, with the exception of their share in consumption demand. The latter then induces specialization between the countries.

Under these circumstances, the simulations showed that small changes in parameter values might have substantial effects on the relative performance of the two countries. In particular, in cases in which the three sources of technological change were assumed to be in operation simultaneously, we found several 'bifurcation values' that demarcate ranges of parameter values for which industry-level productivity growth, structural change and international specialization interact in quite different ways.

Our results thus show that the dynamics of innovation, spillovers and learning are far from simple. The parameter space of our model has large subspaces in which productivity convergence between the countries is far from automatic, and divergence rules. Cases of 'automatic convergence' (often assumed in empirical work on growth) seem to be only islands in a sea with (big) waves of divergence. From this result, we draw two sets of conclusions, one with regard to the literature on convergence and divergence of productivity levels, and one with regard to policy.

With regard to the existing literature, our model is in line with the conclusion (e.g. Abramovitz, 1979; Fagerberg, 1994) that convergence is by no means an automatic process that will unfold itself as a natural traverse towards a steady state. However, while the existing literature mostly reaches this conclusion on the basis of arguments on the complexity of technological change as a process (e.g. difficulties associated to imitating

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foreign technology), our model adds to this the complexity of economic structure. The (bi-causal) interaction between economic structure and technological change adds complexity to the story, but it may also increase the level of empirical reality of the theory, especially if applied to countries that are relatively close to each other in terms of the general level of technological knowledge. We hope to be able to put (parts of) our model to the empirical test in a future paper.

With regard to policy, we draw two conclusions. The first one refers to the issue of trade policy in general. The model shows that free trade may in many cases lead to a situation in which the productivity gaps between countries are significant. This suggests that there are winners and losers from trade, where losers (winners) are those countries for which the (endogenous) specialization pattern implies low (high) growth. This finding is not an argument against free trade, since no static welfare analysis, or a 'counterfactual' of growth patterns under autarky, has been undertaken. But the results do show that under free trade, a loss of growth potential and/or an increase of technology gaps may result in some specific cases. This can be interpreted as a warning against a too simple representation of the free trade argument, sometimes found in the popular debate, suggesting that knowledge spillovers associated with free trade will erase all technology gaps in the long run. It can also be interpreted as a plea for thinking further about the circumstances under which industrial and technology policies can be admitted as useful instruments for development and breaking out of 'bad' specialization patterns.

The second policy conclusion refers to the interplay between specific policies, and the expected results of these. The model suggests that convergence of productivity levels is not achieved by single issue-oriented approaches. Convergence is a more complex process than just (for example) enhancing social capability or technological congruence (Abramovitz, 1979). As an example, our results indicated that the results of increasing social capability (similar to the α parameter in our model) greatly depend on other parameters, e.g. the rate of learning-by-doing (the σ parameter in our model). Low values of the rate of learning-by-doing prohibit convergence even if social capability is high (figure 7).

But picking the right policy mix is far from straightforward. Because specialization emerges and changes endogenously, the results of specific policies aimed at productivity increases may have unexpected results. This is largely the result of the fact that the model shows bifurcations, i.e. the possibility that qualitative outcomes of the model (such as whether or not industry-level productivity leadership switches periodically, or whether or not specialization is complete) change at some threshold value of one or several parameters. From the point of view of policy, this implies that the

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'rules of the game' may change as a result of policy itself. For example, a policy aimed at increasing learning-by-doing at the firm level may shift the whole economy into a different regime, in which the result of the increased learning rate is adverse. In the real world, as opposed to our model, these regime changes (bifurcations) may be subtle and reveal themselves only after some time. They are probably also much less easy to detect in terms of causal relations than in our simple model. Although we cannot stretch the results from the model too far, we suggest that, at least at a metaphorical level, the complexity of these dynamics may be seen as one of the reasons why countries that started with roughly similar initial conditions experienced so widely different growth patterns. For example, countries in South-East Asia have been able to converge to the world productivity frontier during the second half of the 20th century, while Latin American countries have mostly been left behind.

The controlled simulation experiments in this paper have only explored a small subset of the possible dynamics in this respect. A more complete analysis of the policy implications would require searching a larger part of parameter space of the model. For example, our assumption (implemented for analytical transparency) that parameter values do not differ between countries (or industries) is clearly at odds with the idea of policy differences between countries. We expect that different dynamics may emerge if we would allow the parameters to vary between industries and/or countries. But what we expect to be a robust conclusion is that finding the right mix of policies may be more a matter of trial-and-error than of implementing a grand design on the basis of the insights of economic theories.

APPENDIX

Parameter and initial variable configuration

The values below were used as the benchmark values for figures 5–7. It was also used to generate the 'alfa + KV' line in figure 4 for various values of $\rho_1 = \rho_2$.¹¹ Unless stated otherwise, the documented values refer to both North and South, and to both industry 1 and industry 2.

¹¹ Note that figure 4 was generated with $\sigma = 6.0$ and $\kappa = 0.021544$. The implied long-run growth rate of the Kaldor–Verdoorn parameters was thus maintained at 0.01 per period.

100.0	l ^{sup}	(labor supply levels)
0.8	η^x	(exchange rate adjustment parameter)
0.8; 0.2	$b_1; b_2$	(consumption shares)
0.2	α	(spillover parameters)
3.0	σ	(Kaldor-Verdoorn parameters)
0.046416	к	(Kaldor-Verdoorn parameters)
0.05	arphi	(trade share adjustment parameters)
0.0	ε	(trade share adjustment parameters)
0.5	$\eta^{\scriptscriptstyle t}$	(trade share adjustment parameter)
160.0; 40.0	$q_1; q_2$	(initial output levels)
200.0	f(-1)	(total consumption levels in period -1)
0.5	t	(initial trade shares)
0.500000; 0.4999999	$l_{ m N1}^{c}; l_{ m N2}^{c}$	(initial labor requirements in North)
0.499999; 0.500000	$l_{S1}^c; l_{S2}^c$	(initial labor requirements in South)

REFERENCES

- Abramovitz, M. A. (1979): 'Rapid growth potential and its realisation: the experience of capitalist economies in the postwar period', in Malinvaud, E. (ed.): *Economic Growth and Resources*, vol. 1, *The Major Issues*, Macmillan, London.
- Aghion, P., Howitt, P. (1992): 'A model of growth through creative destruction', *Econometrica*, 60, pp. 323–51.
- Arrow, K. J. (1962): 'The economic implications of learning-by-doing', *Review of Economic Studies*, 29, pp. 155–73.
- Cimoli, M. (1988): 'Technological gaps and institutional asymmetries in a North-South model with a continuum of goods', *Metroeconomica*, 39, pp. 245–74.
- Cimoli, M. (1994): 'Lock-in and specialization (dis)advantages in a structuralist growth model', in Fagerberg, J., Verspagen, B. and Von Tunzelmann, N. (eds): *The Dynamics of Technol*ogy, *Trade and Growth*, Edward Elgar Publishing, Aldershot.
- Coe, D. T., Helpman, E. (1995): 'International R&D spillovers', *European Economic Review*, 39, pp. 859–87.
- Dixon, R. J., Thirlwall, A. P. (1975): 'A model of regional growth-rate differences on Kaldorian lines', Oxford Economic Papers, 11, pp. 201–14.
- Dosi, G., Pavitt, K., Soete, L. (1990): *The Economics of Technological Change and International Trade*, Wheatsheaf, Brighton.
- Fagerberg, J. (1994): 'Technology and international differences in growth rates', Journal of Economic Literature, 32, pp. 1147–75.
- Gerschenkron, A. (1962): *Economic Backwardness in Historical Perspective*, Harvard University Press, Cambridge, MA.
- Grossman, G. M., Helpman, E. (1991): Innovation and Growth in the Global Economy, MIT Press, Cambridge, MA.
- Habakkuk, H. J. (1962): American and British Technology in the 19th Century, Cambridge University Press, Cambridge, UK.
- Kaldor, N. (1966): Causes of the Slow Rate of Economic Growth in the United Kingdom; an Inaugural Lecture, Cambridge University Press, Cambridge, UK.
- Kaldor, N. (1996): Causes of Growth and Stagnation in the World Economy (Raffaele Mattioli Lectures), Cambridge University Press, Cambridge, UK.

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Krugman, P. (1990): Rethinking International Trade, MIT Press, Cambridge, MA.

- Landesmann, M., Stehrer, R. (2000): 'Industrial specialization, catching-up and labour market dynamics', *Metroeconomica*, 51, pp. 67–101
- Los, B. (2001): 'Endogenous growth and structural change in a dynamic input-output model', *Economic Systems Research*, 13, pp. 3-34.
- Los, B., Verspagen, B. (2000): 'Shifting consumption patterns: a neglected determinant of growth performance?', Paper presented at the 13th International Conference on Input– Output Techniques, 21–25 August, Macerata, Italy.
- Lucas, R. E. (1988): 'On the mechanisms of economic development', *Journal of Monetary Economics*, 22, pp. 3–42.
- McCombie, J. S. L. (1993): 'Economic growth, trade interlinkages, and the balance-of-payments constraint', *Journal of Post Keynesian Economics*, 15, pp. 471–505.
- McCombie, J. S. L., Thirlwall, A. P. (1994): *Economic Growth and the Balance-of-payments Constraint*, Macmillan, London.
- Nelson, R. R., Winter, S. G. (1982): An Evolutionary Theory of Economic Change, Harvard University Press, Cambridge, MA.
- Pasinetti, L. L. (1981): Structural Change and Economic Growth, Cambridge University Press, Cambridge, UK.
- Romer, P. M. (1986): 'Increasing returns and long-run growth', *Journal of Political Economy*, 4, pp. 1002–37.
- Romer, P. M. (1990): 'Endogenous technological change', *Journal of Political Economy*, 98, pp. S71–102.
- Thirlwall, A. P. (1979): 'The balance of payments constraint as an explanation of international growth rate differences', *Banca Nazionale del Lavoro Quarterly Review*, 32, pp. 45–53.
- Verdoorn, P. J. (1949): 'Fattori che Regolano lo Sviluppo della Produttivita del Lavoro', L'Industria, 1, pp. 3–10.
- Verspagen, B. (1993): Uneven Growth between Interdependent Economies, Avebury, Aldershot.
- Verspagen, B. (1997): 'Estimating international technology spillovers using technology flow matrices', Weltwirtschaftliches Archiv, 133, pp. 226–48.
- Verspagen, B. (2001): 'Evolutionary macroeconomics: a synthesis between neo-Schumpeterian and post-Keynesian lines of thought', *The Electronic Journal of Evolutionary Modeling and Economic Dynamics*, no. 1007. Available at: http://www.e-jemed.org/1007/index.php
- Verspagen, B. (2004): 'Innovation and economic growth', in Fagerberg, J., Mowery, D. C. and Nelson, R. R. (eds): *Oxford Handbook of Innovation*, Oxford University Press, Oxford.
- Young, A. A. (1928): 'Increasing returns and economic progress', *Economic Journal*, 38, pp. 527–42.
- Young, A. (1991): 'Learning by doing and the dynamic effects of trade', *Quarterly Journal of Economics*, 106, pp. 369–405.

Bart Los University of Groningen Department of Economics PO Box 800 NL-9700 AV Groningen The Netherlands Email: b.los@eco.rug.nl Bart Verspagen Eindhoven University of Technology ECIS PO Box 513 NL-5600 MB Eindhoven The Netherlands Email: b.verspagen@tm.tue.nl

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