

What is the best environmental policy? Taxes, permits and rules under economic and environmental uncertainty

by

Konstantinos Angelopoulos⁺, George Economides[#] and Apostolis Philippopoulos^{*±}

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Abstract: We welfare rank different types of second-best environmental policy. The focus is on the roles of uncertainty and public finance. The setup is the basic stochastic neoclassical growth model augmented with the assumptions that pollution occurs as a by-product of output produced and environmental quality is treated as a public good. To compare different policy regimes, we compute the welfare-maximizing value of the second-best policy instrument in each regime. In all cases studied, pollution permits are the worst recipe, even when their revenues are used to finance public abatement. When the main source of uncertainty is economic, the best recipe is to levy taxes (on pollution or output) and use the collected tax revenues to finance public abatement. However, when environmental uncertainty is the dominant source of extrinsic uncertainty, Kyoto-like rules for emissions, being combined with tax-financed public abatement, are better than taxes. Finally, comparing pollution and output taxes, the latter are better.

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⁺ University of Glasgow.

[#] Athens University of Economics and Business.

^{*} Athens University of Economics and Business; University of Glasgow; CESifo, Munich.

[±] **Corresponding author:** Apostolis Philippopoulos, Department of Economics, Athens University of Economics and Business, 76 Patission street, Athens 10434, Greece. Tel: 0030-210-8203357. Fax: 0030-210-8203301. Email: aphil@aueb.gr

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1. Introduction

Environmental degradation caused by human activities is a main concern worldwide. When economic agents do not internalize the effects of their actions on the environment, there is need for government intervention to enact appropriate policies that deal with the negative externalities of pollution emissions. Policy intervention can take many forms. It is thus useful to be able to rank alternative environmental policies according to certain criteria, so that the society can choose the best one (in dynamic models, see e.g. Stokey, 1988, and Jones and Manuelli, 2001).

Examples of environmental policy instruments include taxes, permits (also known as cap-and-trade policy) and numerical targets for cutting emissions (also known as command-and-control policy). All of them are distorting and thus second-best. In the case of taxes, for instance, taxes on pollution itself or on pollution-generating output, the government raises the price of economic activities. In the case of permits, the government creates a market for pollution, by issuing a number of permits, and firms pollute as much as they wish only to the extent that they pay the price. In the case of numerical targets, the government sets an emission standard directly so that firms have to restrict their production accordingly and/or make particular technology and fuel choices. Although this list is not exhaustive,¹ there has always been a lot of interest in the relative desirability of these three policy instruments, in terms of economic performance, environmental quality and social welfare (see e.g. Stokey, 1998, section 6).

Two issues are particularly important to the debate on the choice of the appropriate policy instrument. The first issue has to do with the size and source of uncertainty. In assessing the risks from climate change and the costs of averting it, there is a variety of uncertainties that contribute to big differences of opinion as to how, and how much, to limit emissions (on uncertainty and the environment, see e.g. the Congressional Budget Office paper prepared for the Congress of the US, 2005). The second issue refers to the public finance requirements of environmental protection. It is recognized that the more ambitious is the environmental policy, the

¹ For other policy instruments, see e.g. Goulder et al. (1999) and Bovenberg and Goulder (2002).

higher the finance requirements for adaptation and mitigation actions,² and public finance should play a key role in meeting these requirements (on finance and the environment, see e.g. the Communication from the European Commission, 2009).³

In this paper, we study the roles of uncertainty and public finance in the welfare ranking of different types of environmental policy in a micro-founded dynamic stochastic general equilibrium model. Motivated by the above, we focus on the following policy regimes: We first model the case in which the government levies taxes either on pollution itself or on output, and uses the collected tax revenues to finance public abatement activities. Second, we study the case in which public abatement activities are financed by the sale of auctioned pollution permits. Third, we study the case in which environmental policy takes the form of binding numerical rules à la Kyoto, which specify the speed to a long-term pollution target over time.⁴

Our setup is a basic stochastic neoclassical growth model augmented with the assumptions that pollution occurs as a by-product of output produced and environmental quality has a public good character. Within this setup, there is reason for policy intervention. There are two exogenous stochastic processes that create uncertainty about future outcomes and drive the stochastic dynamics of the model. The first is uncertainty about production technology (standard shocks to total factor productivity) and the second arises from uncertainty about the impact of economic activity on the environment.⁵ Loosely speaking, we call the former shock “economic” and the latter “environmental”.

We study the implications of the above policy regimes (taxes, permits and rules) for macroeconomic outcomes, environmental quality and, ultimately, social welfare. The latter is defined as the conditional expectation of the discounted sum of household’s lifetime utility. Since the equilibrium solution in each regime depends on

² According to the European Commission’s estimates, finance requirements could reach 100 billion euros per year by 2020 in developing countries only (see the Communication from the European Commission, 2009).

³ Governments undertake a lot of environmental protection activities (known as public abatement). Examples include policies that protect, conserve and generate (via innovation) the natural resources, as well as policies that provide the right environmental incentives. All these are costly activities that require public funds. Actually, the proportion of public expenditure in total expenditure on abatement is high in most countries (see e.g. Hatzipanayotou et al., 2003, and Haibara, 2009).

⁴ An example is the reduction of emissions by 25-40% compared to 1990 levels by 2020. Such rules were a key part of the Kyoto protocol designed in 1997 and continue to be a debated issue (see the Copenhagen UN Conference in December 2009).

⁵ Future trends in emissions are uncertain depending on the pace of economic growth, the demand for fossil fuel, the development of technologies, etc (see e.g. the Congressional Budget Office paper prepared for the Congress of the US, 2005).

the values of the second-best policy instruments employed, we welfare rank the alternative policy regimes when the policy instruments under each regime take their welfare-maximizing values. We focus on flat over time policy instruments (see also e.g. Stokey and Rebelo, 1995). To solve the model and compute the associated welfare under each policy regime, we approximate both the equilibrium solution and the welfare criterion to second-order around their non-stochastic long-run; in particular, we use the methodology of Schmitt-Grohé and Uribe (2004).

Our results are as follows. First, public abatement activities constitute an important part of environmental policy. Policies that yield no pollution revenues, and do not allow for public abatement, suffer a disadvantage relative to revenue-yielding policies like taxes and auctioned permits.⁶ In our setting, without being combined with public abatement policy, pure Kyoto-like rules cannot be comparable to taxes and permits and, at least for a wide range of parameter values, such rules are clearly inferior to taxes and permits. Hence, to make the comparison of alternative regimes meaningful when we move to a stochastic setup, instead of studying pure rules, we study mixed rules which combine (in the long run only) rules with public abatement policy financed by, say, output taxes. Now, when second-best policy instruments take their welfare-maximizing values, and we are in a deterministic setup, all policy regimes are equivalent and give the same welfare. This is as in Weitzman (1974).

Second, when we move to an uncertain world, permits are clearly the worst regime. They may help to fix environmental quality at a relatively high level, but only at the cost of exposing this quality to exogenous shocks/variability and damaging private consumption. Actually, the higher the extrinsic (economic or environmental) uncertainty, the worse is the disadvantage of permits relative to taxes and mixed rules. This holds for a wide range of parameters, shocks and relative variances of different categories of shocks. This happens because permits are a hybrid of price- and quantity-based regulations.⁷ As a price-based instrument, they are less closely connected to the heart of the market failure (pollution externality) than taxes. At the

⁶ This presupposes that any revenues from pollution taxes or auctioned permits are earmarked for the financing of public abatement. This is a conventional notion in the literature. See e.g. Haibara (2009). See also Auerbach (2010) who uses the term “dedicated taxes” to describe the case in which sources and uses of government funds are related.

⁷ As explained by Bovenberg and Goulder (2002, p. 1520), they are price-based because market forces determine the price of permits. On the other hand, they are quantity-based because the government sets the total amount of permits and emissions. See below for details.

same time, as a quantity-based instrument, they provide less controllability than numerical rules that command agents to produce or emit at a certain level.

Third, in an uncertain world, the verdict of (pollution and output) taxes versus mixed rules is open depending on the relative variances of different categories of shocks affecting the economy. The main advantage of mixed rules over taxes is that they reduce environmental volatility. But this is achieved at the cost of more volatile consumption. When extrinsic uncertainty arises from economic sources, the latter effect dominates and hence taxes are preferable to rules. However, when environmental uncertainty is the dominant source, the former effect dominates and so rules are preferable. To further analyze this finding, we examine the first and second moments of those endogenous variables that shape social welfare under each policy regime and each level of uncertainty. Rules to produce a certain level of output enjoy an efficiency advantage when environmental uncertainty is high and so the marginal benefits from nature protection are big. By contrast, when environmental uncertainty is relatively low, it is better to name a tax and let private agents find the optimal quantities themselves; in this case, policies like rules for emissions, which reduce the number of choices that private agents can make, hurt the economy. This intuition is consistent with Weitzman's (1974, pp. 485-6) interpretation when he compares price vs quantity controls in a static framework.⁸

Fourth, again in an uncertain world, when the comparison is between pollution taxes and output taxes, the latter are better. The attractiveness of output taxes gets bigger when environmental uncertainty is high. This result is due to the automatic stabilizing role of taxation. In particular, the tax base available to the government under output taxes is larger than under pollution taxes. Hence, under non-internalized market externalities, macroeconomic volatility is higher under pollution taxes and this hurts welfare.

The rest of the paper is organized as follows. The next section explains how we differ from the literature. Sections 3, 4 and 5 solve for taxes, permits and rules respectively. The first-best is in section 6. The key section is section 7 that compares welfare across regimes. Section 8 closes the paper. An appendix includes details.

⁸ Note that "prices" and "quantities" in Weitzman (1974) are closer to pollution taxes and pollution permits respectively in our setup. It is, thus, interesting that taxes are always found to be better than

2. How we differ from the literature

Our work is the first attempt to welfare-rank pollution taxes, output taxes, auctioned pollution permits and numerical rules for emissions in a unified micro-founded dynamic stochastic general equilibrium (DSGE) model, by paying particular attention to the source of uncertainty faced. Our work also differs because we allow the government to play a mix of roles (to correct for externalities, to raise funds to finance public abatement and to shield the economy from shocks) that are important in the policy debate. Finally, we look not only at the final welfare effects, but also at the various channels through which extrinsic uncertainty shapes welfare and, in particular, we look at the first and second moments of endogenous economic and environmental variables.

In his seminal work, Weitzman (1974) compared price- and quantity-based regulations showing that uncertainty causes otherwise equivalent policies to produce different results. Weitzman focused on the case in which the regulator is uncertain about the marginal cost and benefit of pollution and (as Bovenberg and Goulder, 2002, p. 1530, and Schöb, 1996, point out) worked in a first-best setting, in the sense that regulation did not distort private decisions. Since then there has been a rich and still expanding literature on the comparison of alternative policy instruments in the presence of uncertainty. However, in most of these papers, the approach has been static and/or partial equilibrium, and the comparison is between taxes and quotas only (see the survey by Bovenberg and Goulder, 2002, section 4.2). An exception is Pizer (1999) who used a DSGE model. However, here we use a second-order approximation to both the equilibrium solution and the welfare criterion (Pizer used a first-order approximation to the equilibrium solution). This is important because it allows us to take into account the uncertainty that the agents face when making decisions. Also, as shown by Rotemberg and Woodford (1997), Woodford (2003, chapter 6), Schmitt-Grohé and Uribe (2004, 2007) and many others, a second-order approximation to the model's equilibrium solution, as well as to the welfare function, helps us to avoid potential spurious welfare rankings of various regimes that may arise when the model's equilibrium solution is approximate to first-order only (see

permits (at least in the numerical specifications we have used), while the source and magnitude of extrinsic uncertainty becomes important to policy ranking only when we compare taxes to rules.

section 7 below for further details). Finally, Pizer (1999) compared “rate controls” with taxes only and did not allow for public abatement.

Finally, it is worth stressing that the previous environmental literature has not examined the importance of the source of extrinsic uncertainty for the choice of efficient policies; as we find, this is crucial. In addition, the literature has not considered public abatement together with pollution regulation.⁹ Finally, none of the previous studies has studied numerical rules for emissions.

3. A model with taxes

We augment the basic stochastic neoclassical growth model with natural resources and environmental policy. The economy is populated by a large number of identical infinitely-lived private agents that derive utility from private consumption and the stock of environmental quality. Private agents consume, save and produce a single good. Output produced generates pollution and this damages environmental quality. Since private agents take economy-wide environmental quality as a public good, i.e. they do not internalize the effects of their actions on the environment, the decentralized equilibrium is inefficient. Hence, there is room for government intervention.

In this section, government intervention takes the form of taxes. We focus on two types of taxes: first, taxes on output, where output is the polluting activity in our model; second, taxes on pollution itself. Whatever the type of taxation, any collected tax revenues are used to finance public abatement policy. Since output taxes are the most common policy instrument in the related growth literature (see e.g. Xepapadeas, 2004, and Economides and Philippopoulos, 2008), we start with them.

Private agents

For simplicity, the population size is constant and equal to one. The private agent’s expected utility is defined over stochastic sequences of private consumption, c_t , and the economy’s beginning-of-period environmental quality, Q_t :

⁹ Schöb (1996), Goulder et al. (1999) and Bovenberg and Goulder (2002, section 4.1), among many others, have also emphasized the public-finance aspect of environmental policies. But they focus on the so-called revenue recycling effect or the double-dividend effect, which means that funds so raised can

$$E_0 \sum_{t=0}^{\infty} \beta^t u(c_t, Q_t) \quad (1a)$$

where $0 < \beta < 1$ is a time preference rate and E_0 is an expectations operator based on the information available at time zero.

Without loss of generality, we use for instantaneous utility:

$$u(c_t, Q_t) = \frac{[(c_t)^\mu (Q_t)^{1-\mu}]^{1-\sigma}}{1-\sigma} \quad (1b)$$

where $0 < \mu, 1-\mu < 1$ are the weights given to consumption and environmental quality respectively and $\sigma \geq 1$ is a measure of risk aversion.

The private agent's within-period budget constraint is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = (1 - \tau_t)y_t = (1 - \tau_t)A_t k_t^\alpha \quad (2)$$

where $y_t = A_t k_t^\alpha$ is current output,¹⁰ k_{t+1} is the end-of-period capital stock, k_t is the beginning-of-period capital stock, A_t is a standard index of production technology (whose stochastic motion is defined below), $0 < \alpha < 1$ and $0 \leq \delta^k \leq 1$ are usual parameters, and $0 \leq \tau_t < 1$ is the tax rate on (polluting) output.

The agent chooses $\{c_t, k_{t+1}\}_{t=0}^{\infty}$ to maximize (1a-b) subject to (2) taking policy variables and environmental quality as given. The latter is justified by the open-access and public-good features of the environment.

Natural resources

The stock of environmental quality evolves over time according to:¹¹

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - p_t + v g_t \quad (3)$$

be used to reduce other taxes. Baldursson et al. (2008) focus on the time-consistency of various environmental policy instruments.

¹⁰ We abstract from labor-leisure choices to keep the model simpler. We report that this is not important qualitatively.

where $\bar{Q} \geq 0$ represents environmental quality without pollution, p_t is the current pollution flow, g_t is public spending on abatement activities, and $0 \leq \delta^q \leq 1$ and $\nu \geq 0$ are parameters measuring respectively the degree of environmental persistence and how public spending is translated into actual units of renewable natural resources.

The flow of pollution, p_t , is modeled as a by-product of output produced, y_t :

$$p_t = \phi_t y_t = \phi_t A_t k_t^\alpha \quad (4)$$

where ϕ_t is an index of pollution technology or a measure of emissions per unit of output.¹² We assume that ϕ_t is stochastic (its motion is defined below).

Government budget constraint

Assuming a balanced budget for the government, we have in each period:

$$g_t = \tau_t y_t = \tau_t A_t k_t^\alpha \quad (5)$$

where g_t is public spending on abatement policy.

Exogenous stochastic variables

We assume that the two technologies, A_t and ϕ_t , follow $AR(1)$ stochastic processes of the form:

$$A_{t+1} = A^{(1-\rho_a)} A_t^{\rho_a} e^{\varepsilon_{t+1}^a} \quad (6a)$$

$$\phi_{t+1} = \phi^{(1-\rho_\phi)} \phi_t^{\rho_\phi} e^{\varepsilon_{t+1}^\phi} \quad (6b)$$

where A and ϕ are constants, $0 < \rho_a, \rho_\phi < 1$ are auto-regressive parameters and $\varepsilon_t^a, \varepsilon_t^\phi$ are Gaussian i.i.d. shocks with zero means and known variances, σ_a^2 and σ_ϕ^2 .

¹¹ The motion of natural resources in (3) is as in Jouvét et al. (2005); see p. 1599 in their paper for further details. The inclusion of the parameter $\bar{Q} \geq 0$ is helpful when we solve the model numerically.

¹² One could assume that pollution technology has also an endogenous component depending on e.g. private and public investment in pollution-reducing technology.

Decentralized competitive equilibrium (given output taxes)

The Decentralized Competitive Equilibrium (DCE) of the above economy is summarized by the following equations at $t \geq 0$ (see Appendix A.1 for details):

$$k_{t+1} - (1 - \delta^k)k_t + c_t = (1 - \tau_t)A_t k_t^\alpha \quad (7a)$$

$$\frac{\partial u_t}{\partial c_t} = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} [1 - \delta^k + (1 - \tau_{t+1})\alpha A_{t+1} k_{t+1}^{\alpha-1}] \right] \quad (7b)$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - (\phi_t - v\tau_t)A_t k_t^\alpha \quad (7c)$$

where $\frac{\partial u_t}{\partial c_t} = \mu(c_t)^{\mu(1-\sigma)-1} (Q_t)^{(1-\mu)(1-\sigma)}$. This is a three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$. This DCE is for given policy (where the latter is summarized by output tax rates $\{\tau_t\}_{t=0}^\infty$ levied by the government), initial conditions for the stock variables, k_0 and Q_0 , and stochastic processes for the exogenous variables, A_t and ϕ_t . Section 7 will choose the output tax rate.

Decentralized competitive equilibrium (given pollution taxes)

When there are taxes on pollution itself rather than on polluting activities like output, the DCE is summarized by the following equations at $t \geq 0$ (see Appendix A.3 for details):

$$k_{t+1} - (1 - \delta^k)k_t + c_t = (1 - \phi_t \theta_t)A_t k_t^\alpha \quad (8a)$$

$$\frac{\partial u_t}{\partial c_t} = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} [1 - \delta^k + (1 - \phi_{t+1} \theta_{t+1})\alpha A_{t+1} k_{t+1}^{\alpha-1}] \right] \quad (8b)$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - (\phi_t - v\phi_t \theta_t)A_t k_t^\alpha \quad (8c)$$

We thus have a new three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$. This DCE is for given policy (where the latter is summarized by pollution tax rates $\{\theta_t\}_{t=0}^\infty$ levied by the

government), initial conditions, k_0 and Q_0 , and stochastic processes, A_t and ϕ_t . Section 7 will choose the pollution tax rate.¹³

4. The same model with permits

Now the government creates a market for pollution by issuing a number of permits that matches its maximum target amount of pollution. In order to pollute legally, a private agent has to hold a number of permits equal to its own quantity of pollution. In turn, the government uses the collected revenues to finance public abatement policy. The model in this section is similar to that used by Jouvét et al. (2005).¹⁴

In particular, we assume that, at each time t , the government issues a quantity of pollution permits, \bar{P}_t , and auctions them at a price, q_t . These permits are bought in the current period but can be used by the polluting private agent/firm in the next time period, $t+1$.¹⁵ Thus, the private agent's budget constraint changes from (2) to:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + q_t p_{t+1} = y_t = A_t k_t^\alpha \quad (9)$$

where $p_{t+1} = \phi_{t+1} y_{t+1} = \phi_{t+1} A_{t+1} k_{t+1}^\alpha$.

The government budget constraint changes from equation (5) to:

$$g_t = q_t \bar{P}_t \quad (10)$$

¹³ The special case in which the government uses taxes to internalize externalities only (Pigouvian case) is in Appendix A.2.

¹⁴ Jouvét et al. (2005) focus on whether permits should be given away rather than sold by the government.

¹⁵ In this model specification, we cannot assume that permits are bought and used in the same current period. This is because current-period pollution is given (see Appendix B.4, where the right-hand side of equation (B.5d) consists of exogenous and predetermined variables only, implying that \bar{P}_t cannot be a policy control variable). This applies to the transition path; by contrast, it is not a problem in the long run (see Appendix B.4 for details). Allowing, for instance, for endogenous labor could allow permits to be bought and used within the same period but it would complicate the model unnecessarily. As we report below when we study the long run, even quantitative results are affected very little by this timing assumption. In any case, it is worth noting that our assumed timing (namely, that permits are bought today but are used in the next period) is close to the recent Obama climate-change bill, where the

Decentralized competitive equilibrium (given the quantity of pollution permits)

The DCE of the above economy is summarized by the following equations at $t \geq 0$ (see Appendix B.1 for details):¹⁶

$$k_{t+1} - (1 - \delta^k)k_t + c_t + q_t \bar{P}_t = \frac{\bar{P}_{t-1}}{\phi_t} \quad (11a)$$

$$\frac{\partial u_t}{\partial c_t} (1 + \alpha q_t E_t[\phi_{t+1} A_{t+1} k_{t+1}^{\alpha-1}]) = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + \alpha A_{t+1} k_{t+1}^{\alpha-1}) \right] \quad (11b)$$

$$Q_{t+1} = (1 - \delta^q) \bar{Q} + \delta^q Q_t - \bar{P}_{t-1} + \nu q_t \bar{P}_t \quad (11c)$$

$$\bar{P}_t = E_t p_{t+1} = E_t [\phi_{t+1} A_{t+1} k_{t+1}^\alpha] \quad (11d)$$

We thus have a four-equation system in $\{c_t, k_{t+1}, Q_{t+1}, q_t\}_{t=0}^\infty$. This new DCE is for given policy - where the latter is summarized by the quantity of pollution permits $\{\bar{P}_t\}_{t=0}^\infty$ issued by the government - initial conditions, k_0 and Q_0 , and stochastic processes, A_t and ϕ_t . Section 7 will choose the quantity of pollution permits.¹⁷

5. The same model with numerical rules for emissions

We next study the case in which the government specifies the speed to a long-term pollution target. By speed, we mean that pollution tomorrow will be a fraction of pollution today, where this fraction is part of environmental policy. This approach can be captured by a policy rule like:

$$p_{t+1} = (1 - \gamma_t) p + \gamma_t p_t \quad (12)$$

where p is long-run pollution and $0 < \gamma_t \leq 1$ is an autoregressive “parameter”.

government issues a fixed number of permits to emit carbon dioxide each year, which firms must buy before releasing their stuff into the atmosphere (see e.g. *The Economist*, July 4, 2009, p. 37).

¹⁶ Equation (11d) is a market-clearing condition which states that, in equilibrium, agents’ demand for pollution equals supply with the latter determined by the government. See also Jouvét et al. (2005).

¹⁷ The special case in which the government uses permits to internalize externalities only is in Appendix B.2. Appendix B.3 shows the case in which the government sets the price of permits allowing their quantity to be market determined.

Assuming that emission rules are binding all the time, and since $p_t = \phi_t y_t = \phi_t A_t k_t^\alpha$, the motion of pollution in (12) also determines the motion of capital, $\{k_{t+1}\}_{t=0}^\infty$; in turn, private consumption follows residually from the private agent's budget constraint.¹⁸ Note that now, under pure rules, there are neither public revenues nor public cleanup, $g_t = \tau_t = q_t = 0$ (see below for further details).

Decentralized competitive equilibrium (given pollution rules)

The DCE of the above economy can be summarized by the following equations at any $t \geq 0$ (see Appendix C.1 for details):

$$k_{t+1} - (1 - \delta^k)k_t + c_t = A_t k_t^\alpha \quad (13a)$$

$$k_{t+1} = \left(\frac{(1 - \gamma_t)p}{A_{t+1}\phi_{t+1}} + \frac{\gamma_t \phi_t A_t k_t^\alpha}{A_{t+1}\phi_{t+1}} \right)^{1/\alpha} \quad (13b)$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha \quad (13c)$$

We thus have a three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$. This new DCE is for given policy - where the latter is summarized by the long-run pollution target, p , and the autoregressive “parameter” $\{\gamma_t\}_{t=0}^\infty$ in (12) - initial conditions, k_0 and Q_0 , and stochastic processes, A_t and ϕ_t . Section 7 will choose the values of policy instruments. Note that the value of γ_t is irrelevant in the long run when variables do not change.

6. Social planner solution (benchmark case)

We finally present the social planner's solution. This is the first-best serving as a benchmark. The planner chooses allocations $\{c_t, g_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$ directly to maximize (1a-b) subject to resource constraints only. The solution is (see Appendix D for details):

¹⁸ See also the discussion in Stokey (1998, p. 18). The property that, in this policy regime, the private agent is left with nothing to choose is a special case of the more general property that all command-

$$k_{t+1} - (1 - \delta^k)k_t + c_t + g_t = A_t k_t^\alpha \quad (14a)$$

$$\frac{\partial u_t}{\partial c_t} = \beta \frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + \alpha A_{t+1} k_{t+1}^{\alpha-1}) - \beta \xi_{t+1} \phi_{t+1} \alpha A_{t+1} k_{t+1}^{\alpha-1} \quad (14b)$$

$$Q_{t+1} = (1 - \delta^q) \bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha + v g_t \quad (14c)$$

$$\xi_t = \beta \frac{\partial u_{t+1}}{\partial Q_{t+1}} + \beta \delta^q \xi_{t+1} \quad (14d)$$

$$\frac{\partial u_t}{\partial c_t} = v \xi_t \quad (14e)$$

where $\frac{\partial u_t}{\partial c_t} = \mu (c_t)^{\mu(1-\sigma)-1} (Q_t)^{(1-\mu)(1-\sigma)}$, $\frac{\partial u_{t+1}}{\partial Q_{t+1}} = (1-\mu)(c_{t+1})^{\mu(1-\sigma)} (Q_{t+1})^{(1-\mu)(1-\sigma)-1}$ and

$\xi_t > 0$ is a dynamic multiplier associated with (14c). We thus have a five-equation system in $\{c_t, g_t, k_{t+1}, Q_{t+1}, \xi_t\}_{t=0}^\infty$. This is given initial conditions for the stock variables, k_0 and Q_0 , and stochastic processes for the exogenous variables, A_t and ϕ_t . We report that, in all numerical solutions below, this first-best solution will always be welfare superior to the second-best regimes studied in sections 3-5 (this will hold for any feasible values of the distorting policy instruments).

7. Evaluation of second-best policies

This section evaluates the alternative second-best policy regimes developed in sections 3-5 above. In our context, when choosing its distorting policy instruments in the least damaging way, the government aims at the following:¹⁹ First, to correct for pollution externalities (Pigouvian policy). Second, to create revenues to finance public abatement (and, in richer contexts, to reduce other taxes). Third, since there is also uncertainty, the risk-averse government aims to reduce volatility. Optimal policy will reflect all these tasks.

We start by explaining how we work and by presenting parameter values used in the numerical solutions.

and-control policies reduce the number of choices that private agents can make.

How we work

Since the DCE solution and the resulting welfare, under each policy regime, depend on the values of the second-best policy instruments employed, we will compare the maximum welfare across regimes, namely, the welfare resulting from the welfare-maximizing values of the policy instruments in each regime. Welfare is defined as the conditional expectation of the discounted sum of household's lifetime utility. We focus on flat policy instruments, namely, policy instruments that remain constant over time (see also e.g. Stokey and Rebelo, 1995, and Ortigueira, 1998). In all cases reported, there is a tradeoff in policy and hence a well-defined welfare-maximizing value of policy instruments.

To solve the system of non-linear expected difference equations that form the DCE in each regime, we approximate both the DCE solution and the welfare criterion to second-order around the associated non-stochastic steady state solution. We then compute welfare for a wide range of values of the flat policy instrument in each regime and thus find the welfare maximizing-value of the policy instrument and the associated maximum welfare under that regime.²⁰

In particular, the second-order approximation to welfare follows from equations (1a-b) and is given by:

$$E_0 \sum_{t=0}^{\infty} \beta^t u(c_t, Q_t) \cong \frac{u(c, Q)}{1 - \beta} + E_0 \sum_{t=0}^{\infty} \beta^t \{a_1 \hat{c}_t + a_2 \hat{Q}_t + a_3 (\hat{c}_t)^2 + a_4 (\hat{Q}_t)^2 + a_5 (\hat{c}_t \hat{Q}_t)\} \quad (15)$$

where, for any variable x_t , $\hat{x}_t \equiv \ln(x_t/x) \cong (x_t - x)/x$ and x is the long-run value of

x_t . Also, $a_1 \equiv \mu(1 - \sigma)u(c, Q)$, $a_2 \equiv (1 - \mu)(1 - \sigma)u(c, Q)$, $a_3 \equiv \frac{\mu^2(1 - \sigma)^2 u(c, Q)}{2}$,

$a_4 \equiv \frac{(1 - \mu)^2(1 - \sigma)^2 u(c, Q)}{2}$, $a_5 \equiv \mu(1 - \mu)(1 - \sigma)^2 u(c, Q)$. The values of \hat{c}_t and \hat{Q}_t

follow from the second-order approximation of the DCE solution as said above.

¹⁹ See also Bovenberg and Goulder (2002, p. 1514).

²⁰ To solve and simulate the second-order approximation of the DCE solution under each regime, we use the Matlab functions made available by Schmitt-Grohé and Uribe (2004). Note that in the cases of output taxes, pollution taxes and pollution permits, there is obviously a single policy instrument as defined in (7a-c), (8a-c) and (11a-d) respectively. In the case of rules in (13a-c), the long-run pollution target, p , will be set so as to reproduce the long-run welfare under the other regimes so that only γ is chosen optimally in the dynamic, stochastic system (see below for further details). See Schmitt-Grohé

Finally, we need a measure of comparison of welfare gains/losses associated with alternative regimes. This measure, denoted as ζ_{ij} in what follows, is obtained by computing the percentage compensation in private consumption that the private agent would require in each time-period under regime j so as to be equally well off between regimes i and $j \neq i$ (see the notes in Table 3 for the value of ζ_{ij}). This is a popular measure in dynamic general equilibrium models (see e.g. Lucas, 1990).

Parameter values

We keep all parameter values the same across different regimes, so that the evaluation of different policies is not blurred by parameter differences. Whenever parameter values are important for the results obtained, we will explicitly discuss their effects and robustness. As said above, the policy instrument in each regime is chosen to maximize welfare. The parameter values used are reported in Table 1.

Table 1 around here

The values of the economic parameters are rather standard. In particular, the baseline values used for the rate of time preference (β), the depreciation rate of capital (δ^k), the capital share in output (α), the intertemporal elasticity of substitution ($1/\sigma$), the constant term (A) and the persistence parameter (ρ_a) of the TFP process, are as in most dynamic stochastic general equilibrium calibration and estimation studies. As discussed earlier, we will experiment with different values of the standard deviation of the TFP process (σ_a).

There is, of course, much less empirical evidence and consensus on the value of environmental parameters. For our baseline results, we set μ (i.e. the weight given to private consumption vis-à-vis environmental quality in the utility function) at a relatively low level, 0.6, and discuss other results later on. Regarding the parameters characterizing the exogenous process for environmental technology, we choose a high persistence parameter, $\rho_\phi = \rho_\alpha = 0.933$, and normalize its constant term, ϕ , at 0.5. Finally, we set ν (i.e. how public abatement spending is translated into actual units of

and Uribe (2005) and Kollmann (2008) on how this type of optimally computed policy differs from optimal policy in the Ramsey sense.

environmental quality) at 5; this parameter value helps us to match the units in the environmental quality equation (3) and hence obtain a well-defined trade-off in second-best policy. Since ν is the same across regimes with public abatement spending (taxes and permits), its value does not matter for the comparison of these two regimes. Nevertheless, it can matter when we compare these two regimes to the command-and-control regime which does not allow for public abatement spending (we discuss this issue below).

We are now ready to present numerical results. Before investigating the relatively general case in which exogenous shocks cause fluctuations around steady state, we study the deterministic steady state. This will help us to understand the working of the model and how results change when uncertainty is introduced. We will report results for some key variables as well as for the associated welfare.

Evaluation of regimes at steady state (certainty)

We first present results when the economy remains at its non-stochastic steady state. Steady-state results for consumption, c , environmental quality, Q , output, y , as well as the resulting welfare, defined as $u^*(c, Q)$, under each regime, are reported in Table 2 (policy instruments are set at their welfare-maximizing values).

Table 2 around here

The second column in Table 2 presents long-run results for the model in equations (7a-c), where the government sets output taxes and uses the collected tax revenues to finance its abatement policy. In the third column, the policy instrument is pollution taxes (see the model in equations (8a-c)). The fourth column presents results for the model in equations (11a-d), where the government sets the quantity of pollution permits and finances its abatement policy from the sale of those permits. In the fifth column, we present results for the model in equations (13a-c), where the government uses numerical rules; in contrast to previous regimes, now there are no revenues and hence no abatement policy on the side of the government. The very last column reports the social planner solution in equations (14a-e); this gives the best outcome as expected (from now on, we do not study this first-best case).

Output taxes, pollution taxes and pollution permits (see second, third and fourth column in Table 2) are equivalent.²¹ On the other hand, rules (see fifth column) clearly differ from taxes and permits. In particular, using our baseline parameter values, Kyoto-like rules appear to be much worse than both taxes and permits. In general, however, this welfare comparison is ambiguous depending on parameter values.²² This finding arises simply because pure rules are not really comparable to the other two regimes: in our setting, by assumption, such rules do not generate public revenues and hence do not allow for public abatement policy (or, more generally, given tax bases, they allow for less public abatement policy than revenue-raising regimes like taxes and permits). Thus, to get a meaningful comparison of different regimes when we introduce uncertainty below, we have to make them equivalent in a deterministic setup. We therefore add public abatement policy financed by, say, an output tax into the regime of pure Kyoto-like rules (see Appendix C.3 for details). Specifically, we choose the long-run pollution target and the long-run output tax rate so as to reproduce the same long-run solutions for consumption and environmental quality, and thus the same long-run welfare, as in the other second-best regimes. Results are reported in the sixth, second from the end, column in Table 2. In what follows, instead of pure rules, we will work with this mixed regime – Kyoto-like rules combined (in the long run only) with public abatement financed by taxes – and compare this regime to taxes and permits. All policy regimes are now equivalent in a deterministic setup (see also Table 3 below); this respects Weitzman (1974).

To summarize, there are two policy messages. First, public abatement activities constitute an important part of environmental policy. Policies that yield no revenues, and hence do not allow for public abatement, suffer a disadvantage relative

²¹ In the results for the deterministic steady state in Table 2, any second, or higher, decimal point differences are due to numerical solution approximations of the welfare-maximizing value of policy instruments. In addition, in the case of permits, any differences from the other regimes are due to the assumed timing, namely, permits are bought in the current period but are used in the next period (see also footnote 15 and Appendix B.4). In any case, these differences are quantitatively very small and do not affect our conclusions.

²² Specifically, our comparative static exercises imply that rules are welfare inferior to taxes and permits in the long run, when $\nu \geq 0$ (which measures how public spending on cleanup is translated into actual units of nature) is relatively high and/or $0 < \mu < 1$ (which is the weight given to private consumption vis-à-vis environmental quality) is relatively low. Intuitively, when public abatement policy, being financed by tax or permit revenues, is effective in preserving the environment (i.e. when ν is high) and/or we value little the distorting effects of taxes and permits on private consumption (i.e. when μ is low), numerical rules are inferior to taxes and permits. As ν gets smaller and/or μ gets larger, this inferiority diminishes. For very low values of ν and/or very high values of μ , numerical rules can turn out to be welfare superior to taxes and permits.

to revenue-yielding policies. This of course presupposes that any revenues from pollution taxes or permits are earmarked for the financing of public abatement. In this literature, the key role of public finance has already been pointed out, although the emphasis has been on the revenue recycling effect (see e.g. Bovenberg and Goulder, 2002, section 4.1). In our model, without being combined with public abatement policy, pure Kyoto-like rules are not really comparable to taxes and permits and, at least for a wide range of parameter values used, such rules are inferior to taxes and permits, especially in terms of environmental quality. Second, to the extent that policy instruments are chosen optimally, and there is no uncertainty, the choice of the second-best policy instrument is irrelevant to social welfare. Of course, this can apply to regimes that are comparable (in our case, all of them allow for abatement policy).

Evaluation of regimes under uncertainty

We now allow for uncertainty coming from the exogenous stochastic autoregressive processes for production and pollution technologies in equations (6a-b). We suppose that the economy is initially at its steady state studied above and, starting from $t = 0$, there are shocks to A_t and ϕ_t .

Working as explained above and using the same baseline parameter values, we compute discounted expected lifetime utility under each regime for a varying degree of uncertainty as summarized by the standard deviations of production and pollution technologies, σ_a and σ_ϕ . Results are reported in Table 3. For expositional reasons, we study: (i) the deterministic case ($\sigma_a = \sigma_\phi = 0$); (ii) when there is only one source of uncertainty ($\sigma_a = 0.01$ and $\sigma_\phi = 0$; $\sigma_a = 0$ and $\sigma_\phi = 0.01$); (iii) a case of relatively low uncertainty in both stochastic variables ($\sigma_a = \sigma_\phi = 0.01$); (iv) two scenarios representing high levels of uncertainty in one of the two stochastic variables ($\sigma_a = 0.01$ and $\sigma_\phi = 0.05$; and $\sigma_a = 0.05$, $\sigma_\phi = 0.01$); (v) a scenario with relatively high uncertainty in both stochastic variables ($\sigma_a = \sigma_\phi = 0.05$).

Table 3 around here

Table 3 confirms that, in a deterministic environment ($\sigma_a = \sigma_\phi = 0$), all regimes imply the same welfare. By contrast, in a stochastic setup where $\sigma_a, \sigma_\phi > 0$, the choice of the policy instrument does matter. Table 3 also reports the welfare gain/loss (i.e. the value of ζ_{ij}) when we choose regime i instead of regime $j \neq i$. A positive value of ζ_{ij} means that i is superior to j . For instance, if $\zeta_{ij} = x > 0$, an agent, who happens to be in j , will require a permanent consumption subsidy of $x\%$ to become indifferent between j and i .

Welfare differences between output taxes and pollution taxes are summarized by the values of ζ_{12} in Table 3. Output taxes are more attractive and this attractiveness gets bigger when environmental uncertainty is relatively high. For instance, when $\sigma_\phi = 0.05$ and $\sigma_\alpha = 0.01$, a welfare gain of 2.16%, in terms of private consumption, can be obtained if we use output, instead of pollution, taxes. As we will see in the next subsection, this has to do with the automatic stabilizing role of taxation. The tax base available to the government under output taxes is larger than under pollution taxes. Hence macroeconomic volatility is higher under pollution taxes and this is bad for welfare. It is not surprising that the case for output taxes becomes stronger when environmental uncertainty is high. The reason is that, only under some market imperfection, larger governments can moderate the effects of external shocks. In our model, economic shocks are internalized by private agents themselves. By contrast, environmental shocks are not internalized since environmental quality is treated as a public good. This is why a large government size can play its automatic stabilizing role when environmental uncertainty is high. This result is consistent with the macroeconomic literature, where a mix of rigidities is needed to produce the negative correlation between government size and output volatility (see e.g. Andrés et al., 2008).

Welfare differences between output taxes and permits are summarized by the values of ζ_{13} , while welfare differences between pollution taxes and permits are summarized by the values of ζ_{23} , in Table 3. Both types of taxes are always superior to permits. For instance, when $\sigma_\alpha = \sigma_\phi = 0.01$, a welfare gain of 3.04% is obtained if we use output taxes instead of permits. The superiority of taxes further increases with the degree of uncertainty. For instance, when $\sigma_\alpha = \sigma_\phi = 0.05$, the gain, from using

output taxes instead of permits, rises to 7.38%. Notice that taxes are superior even when environmental uncertainty is higher than economic uncertainty. Also notice that these are substantial welfare gains relatively to those found, for instance, in the literature on the welfare implications of tax reforms (see e.g. Lucas, 1990, who compares Ramsey to suboptimal tax structures).

We next compare taxes to mixed rules. Welfare differences between output taxes and mixed rules, and between pollution taxes and mixed rules, are summarized respectively by the values of ζ_{14} and ζ_{24} in the last two columns of Table 3. When economic uncertainty (σ_a) is higher than, or equal to, environmental uncertainty (σ_ϕ), taxes are better than mixed rules. For low levels of uncertainty, such welfare differences are small, but the higher σ_a and σ_ϕ become, the higher the superiority of taxes over rules, as long as $\sigma_a \geq \sigma_\phi$. For instance, when $\sigma_a = 0.05$ and $\sigma_\phi = 0.01$, the gain from using output (resp. pollution) taxes is 4.69% (resp. 4.61%), while when $\sigma_a = \sigma_\phi = 0.05$, the gain is 3.23% (resp. 1.48%). On the other hand, when environmental uncertainty is higher than economic uncertainty ($\sigma_a < \sigma_\phi$), rules are better than taxes, especially than pollution taxes. For instance, when $\sigma_a = 0.01$ and $\sigma_\phi = 0.05$, the welfare gain from switching from output taxes to mixed rules is 2.10%, while the gain from switching from pollution taxes to mixed rules is 4.26%. Pollution taxes perform worse than output taxes because their automatic stabilizing effect is smaller, as discussed above.

To summarize, as shown by Weitzman (1974), ex ante uncertainty affects the choice of the policy instrument. Taxes and mixed rules are substantially better than permits; this holds over the whole range of parameter values, the sources of uncertainty, and the size of variances of shocks, that we have experimented with. Welfare benefits from the use of taxes, instead of permits, can be high for high levels of uncertainty irrespectively of where this uncertainty comes from. Comparing output to pollution taxes, the former are better. However, differences between output and pollution taxes are small relatively to differences between taxes and permits and between taxes and rules. On the other hand, the comparison between taxes and mixed rules depends on the relative variances of different categories of shocks. Taxes are better than rules when economic uncertainty is no smaller than environmental

uncertainty. But, when environmental uncertainty is the dominant source of uncertainty, mixed rules are superior to taxes, especially to pollution taxes that allow for a relatively small automatic stabilizing effect.

The intuition behind these welfare results will be discussed in the next subsection that presents means, variances and covariances of the arguments in the welfare criterion.

Before we move on, we report that we get well-defined values for the welfare-maximizing policy instrument in each regime (although we realize that numerical solutions should be treated with caution, these values are within the expected range). Results are in Table 3. For instance, when $\sigma_\alpha = \sigma_\phi = 0.01$, the optimal output tax rate is found to be 0.33, the optimal pollution tax rate is 0.66, the optimal quantity of permits is 0.62 and the optimal degree of pollution persistence under mixed rules is 0.94. Notice that, in general, the values of the policy instruments are not monotonically increasing in the degree of uncertainty. The reason is that policy intervention comes at a cost, and also, as explained above, stabilization is only one of the goals of policy.

Looking behind welfare under uncertainty

To understand what is driving the above welfare differences under uncertainty, we study the first and second moments of the two arguments in the utility function, namely, private consumption, c_t , and the stock of environmental quality, Q_t . Note from the second-order approximation to the welfare function (15) that, in addition to the steady state values of c_t and Q_t and their deviations from these steady state values, what also matters for welfare is the squared deviations and cross-products of c_t and Q_t from their steady state values. Given that the steady state solution values are the same across policy regimes, any welfare differences in the stochastic setup are driven by differences in expected means, variances and covariances of the series for c_t and Q_t (see Appendix E for details).

Tables 4a-d present the expected means, standard deviations and correlations of c_t and Q_t for all four regimes under various levels of uncertainty. Welfare increases when the means of c_t and Q_t increase, their variances decrease and their correlation decreases.

Tables 4a-d around here

As can be seen in Tables 4a-d, different policy regimes imply different trade-offs in outcomes whose net, total effect on welfare was summarized in Table 3 above. Some regimes are good for consumption, while others are good for environmental quality.

In particular, output and emission taxes (see Tables 4a-b) and mixed rules (see Table 4d) imply higher expected consumption than permits (see Table 4c), while permits are superior in terms of expected environmental quality, especially when uncertainty is high. On the other hand, the variance of environmental quality is higher under permits than under taxes and rules. The higher volatility in environmental quality, in combination with lower expected consumption, makes permits the worst regime in all experiments studied. On the other hand, a weak point of taxes is the high correlation between consumption and environmental quality (by contrast, correlation is negative in all cases under permits and in most cases under rules, and this is good for welfare).

The comparison of the two better regimes, taxes and mixed rules in Tables 4a-b and 4c respectively, implies that the main advantages of mixed rules are that they reduce environmental variation and also allow consumption deviations to move counter-cyclically with deviations in environmental quality. For this to be achieved, however, all the adjustment from an exogenously caused stochasticity has to be absorbed by consumption. In particular, consumption volatility is higher under rules than under taxes. When economic uncertainty is no smaller than environmental uncertainty, as was summarized in Table 3, it is the adverse consumption volatility effects that dominate so that welfare is higher under taxes.²³ But when environmental uncertainty is the dominant source of uncertainty, the benefits from lower variation in environmental quality and the inverse correlation between environment and consumption become important enough to make rules superior to taxes (this happens, for instance, when $\sigma_a = 0.01$ and $\sigma_\phi = 0.05$ in Tables 3 and 4).

To summarize, in an uncertain world, permits are the worst regime. They can fix expected environmental quality at a relatively high level, but only at the cost of

²³ This is despite a relatively low value for the weight given to consumption versus environmental quality in the utility function in our calibration (see Table 1). Hence, if anything, our calibration does not do any favours to the tax regime.

exposing this expected quality to high volatility and damaging expected private consumption. The higher the extrinsic uncertainty, the higher is the disadvantage of permits relative to taxes and mixed rules. This holds for a wide range of parameters, shocks and relative variances of different categories of shocks. Auctioned permits are inferior because (as pointed out by Bovenberg and Goulder, 2002, p. 1520) they are a hybrid of price- and quantity-based regulations. They are price-based because market forces determine the price of permits. They are quantity-based because the government sets the total amount of permits and hence emissions. The problem is that, as a price-based instrument, they are less closely connected to the heart of the problem (pollution externality) than taxes. At the same time, as a quantity-based instrument, they provide less controllability than numerical emission rules that command agents to produce or emit a certain level. This argument is also supported by the result that when the government uses the price of permits, instead of their quantity, as a policy instrument (see Appendix B.3), permits and taxes become very similar on and off steady state (results are available upon request).

The comparison between taxes and mixed rules is open depending on the relative variances of different categories of shocks affecting the economy. When uncertainty arises from economic factors, taxes are preferable. But when environmental uncertainty becomes the dominant source, mixed rules are preferable. We believe this is consistent with Weitzman's (1974, pp. 485-6) intuition. As Weitzman has shown in a first-best setting, quantities are better than prices, as planning instruments, when the benefit function is more curved and/or the cost function is more linear. In our model, this seems to be the case under Kyoto-like rules in the presence of high uncertainty over the environment. In such a situation, better environmental quality gives a direct welfare benefit to private agents; hence, when environmental uncertainty is relatively high, the marginal benefits of an extra unit of natural resources change rapidly and thus the curvature of the benefit function is high. By contrast, when environmental uncertainty is relatively low, the benefit function is closer to being linear. In such a situation, prices are a better instrument; the marginal benefit is almost linear in some range so that it is better to name a price and let private agents find the optimal quantities themselves. In this case, policies like rules, that reduce the number of choices that private agents can make, hurt the macro economy.

8. Concluding remarks and possible extensions

We evaluated output taxes, pollution taxes, auctioned pollution permits and Kyoto-like emission rules, in a unified micro-founded dynamic stochastic general equilibrium model. We focused on the role of uncertainty and showed the importance of public finance and abatement. The latter is an important ingredient of any environmental policy. Permits, despite their popularity among politicians, are the worst regime. When we compare taxes and rules, taxes are better when economic volatility is the main source of uncertainty. On the other hand, when environmental shocks are the dominant source of extrinsic uncertainty, rules perform better. Between taxes, output taxes are better than pollution taxes as a consequence of the small tax base available to governments taxing only pollution.

We are aware that many issues have not been studied. For instance, it would be interesting to search for the best international agreement in our setup and, in particular, the design of international carbon market and international public funding. It is also important to evaluate environmental policies under structural uncertainty resulting from model misspecification of the environmental/pollution process. We leave such issues for future research.

Table 1: Baseline parameter values

Parameter	Description	Value
α	Capital share in production	0.33
δ^k	capital depreciation rate	0.1
σ	curvature parameter in utility function	2
β	Time discount factor	0.97
μ	Consumption weight in utility function	0.6
\bar{Q}	environmental quality without pollution	1
δ^q	persistence of environmental quality	0.9
A	long-run total factor productivity	1
ρ_a	persistence of total factor productivity	0.933
ϕ	long-run pollution technology	0.5
ρ_ϕ	Persistence of pollution technology	0.933
ν	transformation of spending into units of nature	5

Table 2: Different regimes at deterministic steady state

Variable	Output taxes financing abatement	Pollution taxes financing abatement	Permits financing abatement	Pure rules	Mixed rules	Social planner
c	0.65	0.65	0.65	0.12	0.65	0.68
Q	15.99	15.99	15.76	0.40	15.98	17.34
y	1.29	1.29	1.29	0.12	1.29	1.50
$u^*(c, Q)$	-14.30	-14.30	-14.36	-171.75	-14.30	-13.41

Notes: (i) Mixed rules: pure rules plus (in the long run only) abatement financed by an output tax. (ii)

$u^*(c, Q) \equiv \frac{(1-\beta^t)}{(1-\beta)} u(c, Q)$, where $t = 300$ and $\beta^{300} = 0$. We work with discounted welfare to make it

comparable to the results in Tables 3-4 below, where simulations are run for 300 years. This is also consistent with equation (15).

Table 3: Expected lifetime utility (ELU) under different regimes for various levels of uncertainty

σ_a	σ_ϕ	ELU maximizing output tax rate (τ)	(1) ELU under output taxes	ELU maximizing pollution tax rate (θ)	(2) ELU under pollution taxes	ELU maximizing permit (\bar{P})	(3) ELU under permits	ELU maximizing pollution persistence (γ)	(4) ELU under mixed rules	ζ_{12} (%)	ζ_{13} (%)	ζ_{23} (%)	ζ_{14} (%)	ζ_{24} (%)
0	0	0.3319	- 14.30	0.6638	- 14.30	0.6425	- 14.36	-	- 14.30	0	0.31	0.31	0	0
0	0.01	0.3321	- 14.30	0.6617	- 14.32	0.6361	- 14.53	0.931	-14.29	0.10	1.14	1.04	- 0.07	- 0.17
0.01	0	0.3318	- 14.44	0.6637	- 14.44	0.6224	- 14.95	0.941	-14.49	0	2.48	2.48	0.26	0.26
0.01	0.01	0.3320	- 14.45	0.6639	- 14.47	0.6196	- 15.06	0.937	-14.48	0.10	3.04	2.94	0.18	0.08
0.01	0.05	0.3318	- 14.38	0.6530	- 14.82	0.5808	- 16.28	0.920	-13.97	2.16	8.96	6.80	- 2.10	- 4.26
0.05	0.01	0.3290	- 18.07	0.6558	- 18.09	0.5311	- 19.82	0.941	- 19.28	0.08	6.69	6.61	4.69	4.61
0.05	0.05	0.3289	- 18.00	0.6491	- 18.44	0.5241	- 19.94	0.932	- 18.82	1.75	7.38	5.63	3.23	1.48

Notes: (i) The fourth regime (mixed rules) includes tax-financed abatement policy at steady state so that it is equivalent to the other regimes in a deterministic setup. (ii) The value of ζ_{ij} is given by $\zeta_{ij} \cong \frac{1}{\mu(1-\sigma)} \log(V_i^i / V_i^j)$, where V_i^i and V_i^j denote the discounted sums of second-order approximations to welfare in equation (14) and averaged over 1000 simulations. (iii) To evaluate the expectation in the welfare calculations, we use numerical integration with 1000 simulations. As said, we use 300 years in our evaluation of life-time welfare since, because of discounting, there is practically a zero weight attached to later outcomes.

Table 4a: First and second moments for c_t and Q_t under output taxes

σ_a	σ_ϕ	$E(c_t)$	$E(Q_t)$	$\sigma(c_t)$	$\sigma(Q_t)$	$\rho(c_t, Q_t)$
0	0.01	0.64565	15.998	0.0003	0.11943	- 0.41974
0.01	0	0.64594	15.984	0.020051	0.43533	0.84781
0.01	0.01	0.64565	15.994	0.020043	0.45187	0.81163
0.01	0.05	0.64594	16.023	0.020106	0.74281	0.45248
0.05	0.01	0.64588	15.838	0.10051	2.1731	0.84464
0.05	0.05	0.64602	15.874	0.10054	2.2602	0.80892

Table 4b: First and second moments for c_t and Q_t under pollution taxes

σ_a	σ_ϕ	$E(c_t)$	$E(Q_t)$	$\sigma(c_t)$	$\sigma(Q_t)$	$\rho(c_t, Q_t)$
0	0.01	0.64744	15.93	0.010019	0.20947	- 0.96973
0.01	0	0.64587	15.986	0.020048	0.4354	0.84781
0.01	0.01	0.64571	15.99	0.022422	0.48289	0.47867
0.01	0.05	0.65737	15.581	0.053613	1.1086	-0.69282
0.05	0.01	0.64745	15.778	0.10127	2.1701	0.82753
0.05	0.05	0.65605	15.481	0.11351	2.3535	0.4847

Table 4c: First and second moments for c_t and Q_t under permits

σ_a	σ_ϕ	$E(c_t)$	$E(Q_t)$	$\sigma(c_t)$	$\sigma(Q_t)$	$\rho(c_t, Q_t)$
0	0.01	0.6361	16.381	0.028102	0.60575	- 0.97038
0.01	0	0.59204	17.661	0.025287	1.5217	- 0.92889
0.01	0.01	0.58519	17.89	0.035702	1.576	- 0.82458
0.01	0.05	0.50656	20.602	0.11027	2.19	- 0.71098
0.05	0.01	0.39463	22.477	0.07966	3.9753	- 0.88201
0.05	0.05	0.39337	22.833	0.11334	4.2228	- 0.61149

Table 4d: First and second moments for c_t and Q_t under mixed rules

σ_a	σ_ϕ	$E(c_t)$	$E(Q_t)$	$\sigma(c_t)$	$\sigma(Q_t)$	$\rho(c_t, Q_t)$
0	0.01	0.6460	15.978	0.0004568	0.11790	0.57035
0.01	0	0.6456	15.980	0.03343	0.13156	- 0.71178
0.01	0.01	0.64588	15.977	0.03342	0.17706	- 0.50837
0.01	0.05	0.65125	15.97095	0.03641	0.54824	0.08256
0.05	0.01	0.64063	15.97728	0.16064	0.66842	- 0.70381
0.05	0.05	0.64475	15.97011	0.16111	0.84335	- 0.49271

APPENDICES

Appendix A: DCE with taxes

1. The first-order conditions of the individual's problem include the budget constraint in (2) and the Euler equation (7b). Then, using (4)-(5) into (3), we get (7c). All this gives (7a-c) which is a three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^{\infty}$ in terms of $\{\tau_t\}_{t=0}^{\infty}$. The long-run DCE follows if we simply drop time subscripts.

2. A policy of Pigouvian taxes can follow as a special case. Suppose that any revenues from pollution taxes are returned to the individual in the form of lump-sum transfers, S_t . The budget constraint of the individual is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = (1 - \tau_t)A_t k_t^\alpha + S_t \quad (\text{A.1})$$

while the budget constraint of the government is:

$$S_t = \tau_t A_t k_t^\alpha \quad (\text{A.2})$$

and therefore the DCE is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = A_t k_t^\alpha \quad (\text{A.3a})$$

$$\frac{\partial u_t}{\partial c_t} = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} [1 - \delta^k + (1 - \tau_{t+1})\alpha A_{t+1} k_{t+1}^{\alpha-1}] \right] \quad (\text{A.3b})$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha \quad (\text{A.3c})$$

Equations (A.3a)-(A.3c) are a new three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^{\infty}$ given $\{\tau_t\}_{t=0}^{\infty}$. The long-run DCE follows if we simply drop time subscripts.

3. In the case of pollution taxes, θ_t , and since pollution is $p_t = \phi_t y_t = \phi_t A_t k_t^\alpha$, the budget constraint of the individual changes from (2) to:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = (1 - \phi_t \theta_t)A_t k_t^\alpha \quad (\text{A.4})$$

so that the Euler condition in (8b) follows.

The government budget constraint in (5) becomes:

$$g_t = \theta_t \phi_t y_t = \theta_t \phi_t A_t k_t^\alpha \quad (\text{A.5})$$

so that (8c) follows.

Appendix B: DCE with permits

1. The first-order conditions of the individual's problem include the budget constraint in (9) and the Euler equation (11b). Then, using (10) for g_t and $p_t = \phi_t A_t k_t^\alpha = \bar{P}_{t-1}$ into (3), we get (11c), while (11d) was explained in the text. All this gives (11a-d) which is a four-equation system in $\{c_t, k_{t+1}, Q_{t+1}, q_t\}_{t=0}^\infty$ in terms of $\{\bar{P}_t\}_{t=0}^\infty$. The long-run follows if we simply drop time subscripts.

2. A policy of "Pigouvian permits" can follow as a special case. Suppose that any revenues from the same of pollution permits are returned to the individual in the form of lump-sum transfers, S_t . That is, the budget constraint of the agent is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + q_t p_{t+1} = A_t k_t^\alpha + S_t \quad (\text{B.1})$$

while the budget constraint of the government is:

$$S_t = q_t p_{t+1} = q_t \bar{P}_t \quad (\text{B.2})$$

and therefore the DCE is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = \frac{\bar{P}_{t-1}}{\phi_t} \quad (\text{B.3a})$$

$$\frac{\partial u_t}{\partial c_t} (1 + \alpha q_t E_t[\phi_{t+1} A_{t+1} k_{t+1}^{\alpha-1}]) = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + \alpha A_{t+1} k_{t+1}^{\alpha-1}) \right] \quad (\text{B.3b})$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - \bar{P}_{t-1} \quad (\text{B.3c})$$

$$\bar{P}_t = E_t p_{t+1} = E_t [\phi_{t+1} A_{t+1} k_{t+1}^\alpha] \quad (\text{B.3d})$$

Equations (B.3a)-(B.3d) are a four-equation system in $\{c_t, k_{t+1}, Q_{t+1}, q_t\}_{t=0}^\infty$ given $\{\bar{P}_t\}_{t=0}^\infty$. The long-run DCE follows if we drop time subscripts.

3. When the instrument is the price of permits, rather than their quantity, the DCE is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + q_t \phi_{t+1} A_{t+1} k_{t+1}^\alpha = A_t k_t^\alpha \quad (\text{B.4a})$$

$$\frac{\partial u_t}{\partial c_t} (1 + \alpha q_t E_t[\phi_{t+1} A_{t+1} k_{t+1}^{\alpha-1}]) = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + \alpha A_{t+1} k_{t+1}^{\alpha-1}) \right] \quad (\text{B.4b})$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha + v q_t \phi_{t+1} A_{t+1} k_{t+1}^\alpha \quad (\text{B.4c})$$

Equations (B.4a)-(B.4c) are a three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$ given $\{q_t\}_{t=0}^\infty$.

The long-run DCE follows if we drop time subscripts.

4. We model the case in which the firm buys and uses permits within the same period.

The DCE changes from (11a-d) to:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + q_t \bar{P}_t = \frac{\bar{P}_t}{\phi_t} \quad (\text{B.5a})$$

$$\frac{\partial u_t}{\partial c_t} = \beta E_t \left[\frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + (1 - q_{t+1} \phi_{t+1}) \alpha A_{t+1} k_{t+1}^{\alpha-1}) \right] \quad (\text{B.5b})$$

$$Q_{t+1} = (1 - \delta^q) \bar{Q} + \delta^q Q_t - \bar{P}_t + v q_t \bar{P}_t \quad (\text{B.5c})$$

$$\bar{P}_t = p_t = \phi_t A_t k_t^\alpha \quad (\text{B.5d})$$

Notice that in (B.5d), given exogenous shocks and the predetermined value of capital, \bar{P}_t has to follow residually. This is different from (11d) with the other timing assumed. Also, notice that, in contrast to the transition path, (B.5a-d) can give a long-run solution. Namely, given policy, (B.5d) gives k , and then (B.5a-c) give c, Q, q .

Appendix C: DCE with rules

1. Using (4) into (12), we get (13b) which gives the motion of private capital. All this gives (13-c) which constitute a three-equation system in $\{c_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$ in terms of p and $\{\gamma_t\}_{t=0}^\infty$. In the long run, equations (13a-c) are reduced to two equations:

$$\delta^k \left(\frac{p}{\phi A} \right)^{1/\alpha} + c = \frac{p}{\phi} \quad (\text{C.1a})$$

$$Q = \bar{Q} - \frac{p}{(1 - \delta^q)} \quad (\text{C.1b})$$

which can be solved for c and Q in terms of p (recall that, in the long-run, p is a policy instrument and that, in all periods, $p_t = \phi_t A_t k_t^\alpha$).

2. We now add public abatement financed by lump-sum taxes, S_t . That is, the budget constraint of the individual is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t = A_t k_t^\alpha - S_t \quad (\text{C.2})$$

while the budget constraint of the government is:

$$G_t = S_t \quad (\text{C.3})$$

and therefore the DCE is:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + G_t = A_t k_t^\alpha \quad (\text{C.4a})$$

$$k_{t+1} = \left(\frac{(1-\gamma_t)p}{A_{t+1}\phi_{t+1}} + \frac{\gamma_t\phi_t A_t k_t^\alpha}{A_{t+1}\phi_{t+1}} \right)^{1/\alpha} \quad (\text{C.4b})$$

$$Q_{t+1} = (1-\delta^q)\bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha + \nu G_t \quad (\text{C.4c})$$

In the long run, equations (C.4a)-(C.4c) are reduced to two equations:

$$\delta^k \left(\frac{p}{\phi A} \right)^{1/\alpha} + c + G = \frac{p}{\phi} \quad (\text{C.5a})$$

$$Q = \bar{Q} - \frac{p - \nu G}{(1-\delta^q)} \quad (\text{C.5b})$$

which can be solved for c and Q in terms of p and G .

3. We now add public abatement financed by output taxes, τ_t . The budget constraint of the individual is:

$$k_{t+1} - (1-\delta^k)k_t + c_t = (1-\tau_t)A_t k_t^\alpha \quad (\text{C.6})$$

while the budget constraint of the government is:

$$G_t = \tau_t A_t k_t^\alpha \quad (\text{C.7})$$

and therefore the DCE is:

$$k_{t+1} - (1-\delta^k)k_t + c_t = (1-\tau_t)A_t k_t^\alpha \quad (\text{C.8a})$$

$$k_{t+1} = \left(\frac{(1-\gamma_t)p}{A_{t+1}\phi_{t+1}} + \frac{\gamma_t\phi_t A_t k_t^\alpha}{A_{t+1}\phi_{t+1}} \right)^{1/\alpha} \quad (\text{C.8b})$$

$$Q_{t+1} = (1-\delta^q)\bar{Q} + \delta^q Q_t - (\phi_t - \nu\tau_t)A_t k_t^\alpha \quad (\text{C.8c})$$

In the long run, equations (C.8a)-(C.8c) are reduced to two equations:

$$\delta^k \left(\frac{p}{\phi A} \right)^{1/\alpha} + c = (1-\tau) \frac{p}{\phi} \quad (\text{C.9a})$$

$$Q = \bar{Q} - \frac{\left(1 - \frac{\nu\tau}{\phi}\right)p}{(1-\delta^q)} \quad (\text{C.9b})$$

which can be solved for c and Q in terms of p and τ . We choose the values of p and τ so as to hit the long-run solution of the previous regimes.

Appendix D: Social planner's solution

The planner chooses $\{c_t, g_t, k_{t+1}, Q_{t+1}\}_{t=0}^\infty$ to maximize (1a-b) subject to the resource constraints:

$$k_{t+1} - (1 - \delta^k)k_t + c_t + g_t = A_t k_t^\alpha \quad (\text{D.1a})$$

$$Q_{t+1} = (1 - \delta^q)\bar{Q} + \delta^q Q_t - \phi_t A_t k_t^\alpha + \nu g_t \quad (\text{D.1b})$$

The optimality conditions include (D.1a), (D.1b) and:

$$\frac{\partial u_t}{\partial c_t} = \beta \frac{\partial u_{t+1}}{\partial c_{t+1}} (1 - \delta^k + \alpha A_{t+1} k_{t+1}^{\alpha-1}) - \beta \xi_{t+1} \phi_{t+1} \alpha A_{t+1} k_{t+1}^{\alpha-1} \quad (\text{D.2a})$$

$$\xi_t = \beta \frac{\partial u_{t+1}}{\partial Q_{t+1}} + \beta \delta^q \xi_{t+1} \quad (\text{D.2b})$$

$$\frac{\partial u_t}{\partial c_t} = \nu \xi_t \quad (\text{D.2c})$$

where $\xi > 0$ is a dynamic multiplier associated with (D.1b),

$$\frac{\partial u_t}{\partial c_t} = \mu (c_t)^{\mu(1-\sigma)-1} (Q_t)^{(1-\mu)(1-\sigma)}, \quad \text{and} \quad \frac{\partial u_{t+1}}{\partial Q_{t+1}} = (1 - \mu) (c_{t+1})^{\mu(1-\sigma)} (Q_{t+1})^{(1-\mu)(1-\sigma)-1}. \quad (\text{D.1a})-$$

(D.1b) and (D.2a)-(D.2c) constitute a five-equation system in $\{c_t, k_{t+1}, Q_{t+1}, g_t, \xi_t\}_{t=0}^\infty$.

The long-run follows if we drop time subscripts.

Appendix E: Statistical moments

To see that examining the means, variances and covariances of the variables in levels is equivalent to examining the same moments for the variables defined as deviations from their (common) steady state, note the following. For the random variables x and y , define $\hat{x} = x - \bar{x}$ and $\hat{y} = y - \bar{y}$, where \bar{x} (resp. \bar{y}) is the average value of x (resp. y). The relationship between the mean of x and the mean of \hat{x} is given by:

$$E(\hat{x}) = E(x) - \bar{x} \quad (\text{E.1})$$

(E.1) implies that, when \bar{x} is the same across regimes, any differences in the mean of x are due to differences in the mean of \hat{x} . The relationship between \hat{x}^2 and the variance of \hat{x} is given by:

$$\text{var}(\hat{x}) = E[\hat{x} - E(\hat{x})]^2 = E(\hat{x})^2 - [E(\hat{x})]^2 \quad (\text{E.2})$$

Hence, given the mean of \hat{x} , any differences in the average value of \hat{x}^2 are captured by differences in the variance of \hat{x} . Further, the variances of x and \hat{x} are the same, i.e. $\text{var}(\hat{x}) = E[\hat{x} - E(\hat{x})]^2 = E[(x - \bar{x}) - (E(x) - \bar{x})]^2 = \text{var}(x)$. Finally, given their means, any differences in the cross-products of \hat{x} and \hat{y} are captured by their covariance, i.e. $\text{cov}(\hat{x}, \hat{y}) = E[\hat{x}\hat{y}] - E(\hat{x})E(\hat{y})$, where:

$$\text{cov}(\hat{x}, \hat{y}) = E\{[\hat{x} - E(\hat{x})][\hat{y} - E(\hat{y})]\} = E\{[(x - \bar{x}) - (E(x) - \bar{x})][(y - \bar{y}) - (E(y) - \bar{y})]\} = \text{cov}(x, y) \quad (\text{E.3})$$

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