

COLD PROGRESSION AND ITS EFFECTS ON INCOME DISTRIBUTION

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Abstract

We present new empirical evidence for the US economy that inflation reduces the inequality of the earnings distribution. The main mechanism emphasized in this paper is the tax income bracket effect. Governments only adjust the nominal income tax brackets slowly to a rise in prices, typically less often than once every other year in the US post-war history. We also develop a theoretical general equilibrium monetary model with income heterogeneity. In this model, the effect of higher inflation on income distribution is shown to be rather small. However, we find that a longer duration between two successive adjustments of the income tax schedule reduces employment, savings, and output significantly.

JEL Code: D31, E31, E44, E52.

Keywords: cold progression, inflation, income distribution, tax income brackets.

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1 Introduction

The literature discusses several channels through which inflation may alter income, earnings, or wealth distributions. Among others, these channels include differential indexation of wages across income groups, disproportionately allocated subsidized loans, and the Tanzi-Olivera effect on taxes and governmental revenues. The “bracket creep effect,” i.e. the inflation-induced increase in marginal income taxes in case of less than fully or infrequently adjusted tax brackets, is also a major cited culprit for deteriorating effects on the income distribution.

There is a well-known early strand of literature representing a broad empirical research effort aimed to contribute information on the (re-)distributional effects of inflation on the US income and/or wealth distribution. It includes the works of Bach and Ando (1957), Budd and Seiders (1971), Bach and Stephenson (1974), and Wolff (1979). With some exceptions¹ this literature either (i) underlies a detailed disaggregate definition of wealth and discriminates a set of different income types (notably before taxes) and portfolios of different demographic groups of households, business and governmental sectors, etc. or (ii) investigates the effects of inflation determined by market forces and by public and private transfer policies, before any subsequent distribution through personal income tax. In contrast to this, we here explicitly focus on the latter and concentrate on individual income after taxes as our primary income type of interest. So far as we know, quantitative work on this topic is still rather thin if not to say a neglected issue hitherto.

The present paper contributes to the literature in quantitatively assessing bracket creep effects of inflation on the base of US data and providing novel insights. Our findings are based on techniques starting from different methodological premises: We begin our study investigating time series evidence of the relationship between the US inflation rate and income distributional measures. The applied techniques range from traditional Blinder-Esaki-Schultz (BES-) type single-equation regression models to the estimation of impulse

¹Bach and Ando (1957) and Bach and Stephenson (1974) see taxpayers as the main beneficiaries of inflation if it is assumed that debt will be paid off by collections from taxpayers and therefore the latter can be seen as “indirect debtors.” They argue that if debt in form of governmental interest charges is repaid by taxation, inflation redistributes real purchasing power in favor of the higher income groups since these were slightly heavier taxpayers than federal bondholders in the early and mid 1950s and early 1970s. See Bach and Ando (1957), p. 5-7, and Bach and Stephenson (1974), p. 2-7.

responses based on vector error correction models.

In addition, we develop a monetary general equilibrium model of progressive income taxation in order to study the effects of cold progression. While the individual agents face idiosyncratic risk with regard to their productivity, there is no aggregate uncertainty in the economy as the government adjusts its tax schedule in a deterministic way and the money grows at an exogenous and constant rate. In response to a higher inflation or a longer duration of the cold progression, individuals face higher income taxes, both on average and marginally as the US income tax is progressive. As a consequence, agents adjust their labor supply and savings decision. Surprisingly, agents do not change their behavior significantly between periods. However, if we consider a tax policy regime that adjusts the tax schedule for inflation more frequently, we find that agents increase both their labor supply and savings markedly compared to a system with less frequent adjustments. We, therefore, carefully conclude that the inflation rate is a less important phenomenon for the effects of cold progression compared to the duration of cold progression, i.e. the length of the time period between two successive income tax schedule adjustments for inflation.

The remainder of the paper is structured as follows. Section 2 presents empirical evidence for the US. Section 3 introduces the overlapping-generations model with two assets, money and equity. The model is calibrated with regard to the characteristics of the US economy in section 4. Our numerical results are presented in section 5. Section 6 concludes.

2 Empirical analysis

2.1 Data

For our empirical study of the present section, data on the US income distribution from 1951 to 1991 are taken from the popular Deininger and Squire (1996) data set (considering “accept” values only).² The contained time series are extensively documented in Deininger and Squire (1996) and are ultimately based on data provided by the US Census Bureau, published in its Current Population Reports. Apart from its frequent use in empirical

²Data are downloadable at: <http://www.worldbank.org/research/growth/dddeisqu.htm>. Note, we de-cumulated the quintile income shares, given as cumulative figures in the original data set.

studies (cf. Romer and Romer, 1998), this data set seems suitable for our aims, inasmuch it offers information on a relatively longer time period than, e.g., the series directly provided in the ‘Historical Income Tables’ by the US Census Bureau, ranging from 1966 to 1999. Time series on the US unemployment and inflation rate (the latter based on CPI data) are taken from the databases of the Bureau of Labor Statistics and the IMF (International Financial Statistics), respectively.

As documented, e.g., by Auerbach and Feenberg (2000), our observation period incorporates a number of major legislative changes in the individual income tax. These include: the Revenue Act of 1964, which reduced the top marginal income rate from 91 to 71%; the Tax Reform Act of 1969, which introduced a ceiling of 50% on the marginal tax rate on “earned” income; the Economic Recovery Tax Act of 1981, which reduced the top marginal rate on other income from 70 to 50%, and finally the Tax Reform Act of 1986, which reduced the marginal rate on the highest incomes to 28% and the top marginal rate to 33%. For the period 1951-86, the US tax system may be described as being based on nominal income and deductions, i.e., not indexed to the overall price level, as a system for which inflation raises the real value of taxes paid for any given level of real income, because the system is progressive with respect to nominal income. Therefore, during this period an individual with a given real income will appear “wealthier” and face a higher average tax burden. By the mid 1980s, the US tax system became effectively inflation-indexed when provisions that indexed rate brackets, personal exemptions and the so called “standard deduction” took effect;³ see Auerbach and Feenberg (2000), p. 4-6. Apart from these major legislative changes, several partial and substantial changes of tax bracket boundaries (*TBB*) and of regular tax rates for fixed tax bracket boundaries (*TRB*) took place. A comprehensive survey along with the detailed construction of our total tax brackets effect ($TTB = TBB + TRB$) variable based on publications of the Department of the Treasury, Internal Revenue Service (henceforth IRS), and the US Major Tax Guide is given in the appendix. Accordingly, for the period 1951-91 (1951-86) the US economy experienced changes of *TBB* on average every 2.93 (4.00) years, *TRB*-changes every 2.93 (3.60) years, and *TTB*-effects every 1.95 (2.25) years.

³These provisions were actually enacted already in 1981 as part of the Economic Recovery Act, but delayed in their implementation.

2.2 Evidence based on regressions of the BES-type

The traditional empirical model by Schultz (1969) characterizes the relationship between the Gini coefficient of the income distribution (G) and inflation (π) as follows

$$G_t = \beta_0 + \beta_1 \pi_t + \beta_2 u_t + \sum_{i=3}^n \beta_i f^i(t) + \varepsilon_t, \quad (1)$$

i.e. as a linear function of (i) a constant β_0 , referring to a component of the Gini coefficient that is autonomous with regard to the explanatories, (ii) the level of contemporaneous inflation π_t , (iii) the current overall unemployment rate u_t , and (iv) a trend function $\sum_{i=1}^n f^i(t)$, separating secular from cyclical influences on income distribution⁴ plus an i.i.d. normal error vector ε_t . Some ten years later, Blinder and Esaki (1978) extended this basic strategy by additionally considering relative income shares of different segments of the population as endogenous variables:

$$Q_{j,t} = \beta_0 + \beta_1 \pi_t + \beta_2 u_t + \sum_{i=3}^n \beta_i f^i(t) + \varepsilon_t, \quad (2)$$

where $Q_{j,t}$ denotes the share of the j th quintile ($j = 1, \dots, 5$) in the distribution of income among households in the t th year. This specification allows to estimate whether “side effects” of inflation change the relative income position of the different income groups of the society at stake. Contrary to the Schultz-specification, where inflation is expected to decrease income inequality in the presence of “cold progression” (i.e. a negative coefficient resultant for the inflation rate), the Blinder-Esaki-model does not predict a specific sign pattern. The signs of the coefficients are rather dependent on institutional characteristics, like the relative distribution of non-indexed financial assets and liabilities across income groups, particular groups’ ability to anticipate price shocks, etc. By considering u_t , specifications (1) and (2) implicitly test whether macroeconomic policies, including but not limited to financial policies, which impact on unemployment, will also have an impact on the distribution of income across households.

⁴Originally, this trend function was linearly specified ($n = 1$). However, we also employ more adequate polynomial trend functions ($n = 2$). To check the estimation results of the present subsection for robustness, we alternatively also consider smooth trend functions, as extracted from the original dependent series by means of the HP(100) and HP(6.25) highpass-filters; see Hodrick and Prescott (1997) and Ravn and Uhlig (2002).

Several variants of these specifications have been estimated since its establishment as the “standard model” in the area of single-country time series studies on the effects of inflation on income distribution in the 1980s.⁵ They became to be known as Blinder-Esaki-Schultz (BES-) type regressions. In the following, we will consider modified versions of specifications (1) and (2) that

- (a) allow for a non-monotone relationship between the income distributional measures (of inequality) and inflation, and
- (b) take major legislative changes, historical tax bracket adjustments, and changes in the relative tax rate for the US income tax into account.

In the course of modification (a), we have a special interest in quantitatively assessing a non-linear (potentially convex) relationship between our distributional measures (G_t , $Q_{j,t}$) and the inflation rate (π_t). This stems from the fact that given there is a significant convex relationship, we will be able to determine a threshold value π^* that quantifies the critical inflation rate above which the progressive effect of inflation turns into a regressive one. Values of $\pi > \pi^*$ would then indicate an increasing inequality in the distribution of household incomes with every marginal increase in inflation. Formally, we consider the following basic specifications

$$G_t = \beta_0 + (\beta_1 + \beta_2 D_t) \pi_t + (\beta_3 + \beta_4 D_t) \pi_t^2 + \beta_5 u_t + \sum_{i=6}^n \beta_i f^i(t) + \varepsilon_t, \quad (3)$$

$$Q_{j,t} = \beta_0 + (\beta_1 + \beta_2 D_t) \pi_t + (\beta_3 + \beta_4 D_t) \pi_t^2 + \beta_5 u_t + \sum_{i=6}^n \beta_i f^i(t) + \varepsilon_t, \quad (4)$$

where $j = 1, \dots, 5$ and D_t denotes a dummy variable for $t = 1, \dots, T$. D_t takes on values of 1 for historical tax bracket boundaries adjustments and/or changes of the “regular” income tax rate for given boundaries – a value of 0 else. For detail on the construction of this binary variable and its different definitions for the post-World War (WW) II US economy, the reader is referred to the appendix. From (3), it can be easily seen that

$$\pi^* = -\beta_1 / (2\beta_3)$$

⁵A survey of these early studies is given, e.g., by Bulir and Gulde (1995).

in the case of abstracting from income tax adjustments⁶ and

$$\pi^* = -(\beta_1 + \beta_2) / [2(\beta_3 + \beta_4)]$$

in case of taking historical changes into account, give us the respective inflation threshold that minimizes income inequality as measured by G_t . In contrast to the related study by Galli and van der Hoeven (2001), our specification strategy allows for changes in the slope and shape of the convex relationship between Gini coefficient and inflation rate through D_t .

The results of our estimates of model (3) are displayed in Table 1 below. It reports our findings for 1951-86, i.e. the period up to tax year 1986, as well as for the full sample period, i.e. from 1951 to 1991. From 1986 on tax bracket boundaries were indexed for inflation, using the US Department of Labor Consumer Price Index for Urban Consumers (CPS-U); see IRS (2003), p. 327. According to our estimates, the threshold values of inflation, marking the start of a regressive regime for inflation rates higher than these critical values, are calculated as 10.08% (18.01%) for the 1951-86 subsample and 9.71% (29.71%) for our full sample period, where figures taking tax bracket changes into account are given in parantheses. These figures are remarkably concordant with the findings of Galli and van der Hoeven (2001). These authors suggest on the base of their estimates that ‘reducing inflation from moderate (around 12%) to low (around 6%) rates would decrease inequality in the US.’ As can be seen from Figure 1 and 2 below, our results are indicative for a U-shaped relationship and a predominating (though rather negligible in quantitative terms) cold progression-regime in a historically plausible range of values of the inflation rate.⁷ We find this predominance regardless of taking historical changes in income tax boundaries into account or not. However, although our findings remain qualitatively the same in case of employing the business cycle components as extracted by HP-filtering or log first differences of the series in our regressions,⁸ they are sensitive with regard to the following: (a) The chosen definition of our changes-in-tax-system dummy D_t and (b) the specification of the trend function $f(t)$ in case of estimating in levels. We obtain the reported significant results only by choosing for (a) TBB_t (for detail see appendix) and a polynomial trend

⁶I.e. for $D_t = 0$ for all $t = 1, \dots, T$.

⁷For our sample’s range, it is only the three-years period 1979-81, where the US inflation rate exceeds values of 10%.

⁸All time series and estimates are available on request from the authors.

function for (b). It should be noted that this sensitivity of results based on our BES-type estimates seems not to be due to a structural break in the relationship for the oil price shocks period or the post-1983 period, as suggested in Galli and van der Hoeven (2001). We find no significant evidence for such a structural break in our regressions.

BES-type estimates have often been criticized to exclusively capture cyclical elements of the impact of inflation on income distribution. However, in the limiting case where all variability of the income distribution could be ascribed to changes in inflation, unemployment, and some secular trend, one may sum the short-term effects to gauge the total long-run impact of inflation on income distribution *ceteris paribus*. This would correspond to the combined effect of the responsiveness of the economy (estimated coefficient) and the actual inflation outcomes; see Bulir and Gulde (1995). Thus, the long-term cumulative impact of inflation may simply be computed as

$$\beta_1 \sum_{t=1}^T \pi_t + \beta_3 \sum_{t=1}^T \pi_t^2$$

for an upper benchmark value of cold progression, resultant for the case without any income tax adjustments, and as

$$(\beta_1 + \beta_2) \sum_{t=1}^T \pi_t + (\beta_3 + \beta_4) \sum_{t=1}^T \pi_t^2$$

to assess the effects of cold progression in the presence of tax bracket adjustments with a frequency as witnessed by the post-WW II US economy. The resulting cumulative effects for specification (4) are reported in Table 2 below.

Table 1. Estimates of BES-type model; dependent variable: G_t

$$G_t = \beta_0 + (\beta_1 + \beta_2 D_t) \pi_t + (\beta_3 + \beta_4 D_t) \pi_t^2 + \beta_5 u_t + \beta_6 t + \beta_7 t^2 + \varepsilon_t,$$

Est. coeff.	Sub-sample: 1951–86	Full sample: 1951–91
β_0	35.356*** (0.318)	35.327*** (0.261)
β_1	-0.269*** (0.077)	-0.274*** (0.076)
β_2	0.110* (0.056)	0.143** (0.066)
β_3	0.013** (0.004)	0.014*** (0.004)
β_4	-0.008 (0.005)	-0.011* (0.006)
β_5	0.080 (0.064)	0.073 (0.048)
β_6	-0.141*** (0.031)	-0.130*** (0.031)
β_7	0.005*** (0.001)	0.005*** (0.001)
Adj. R^2	0.852	0.921
F-stat.	29.855	68.457
DW-stat.	1.396	1.383

Note: *, **, *** \equiv significance at 10, 5, 1% level of significance;
Newey-West HAC standard errors given in parentheses.

Figure 1: Convex relationship of inflation rate and Gini coefficient I

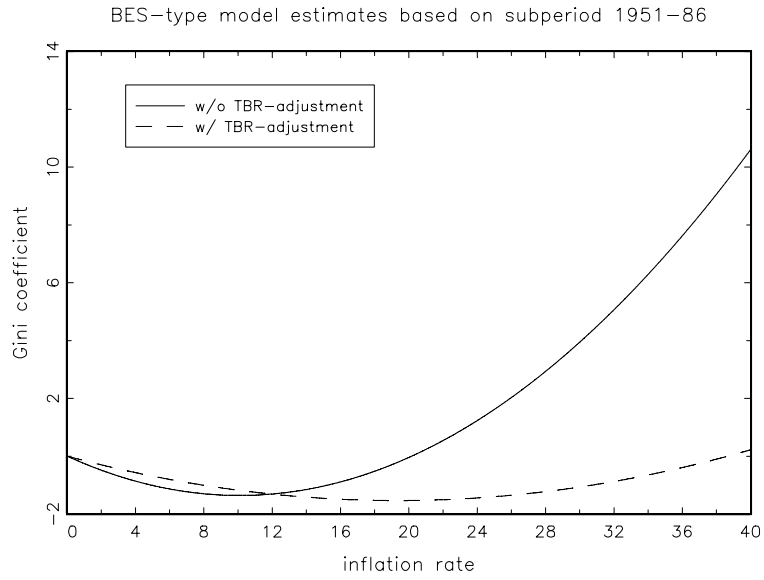


Figure 2: Convex relationship of inflation rate and Gini coefficient II

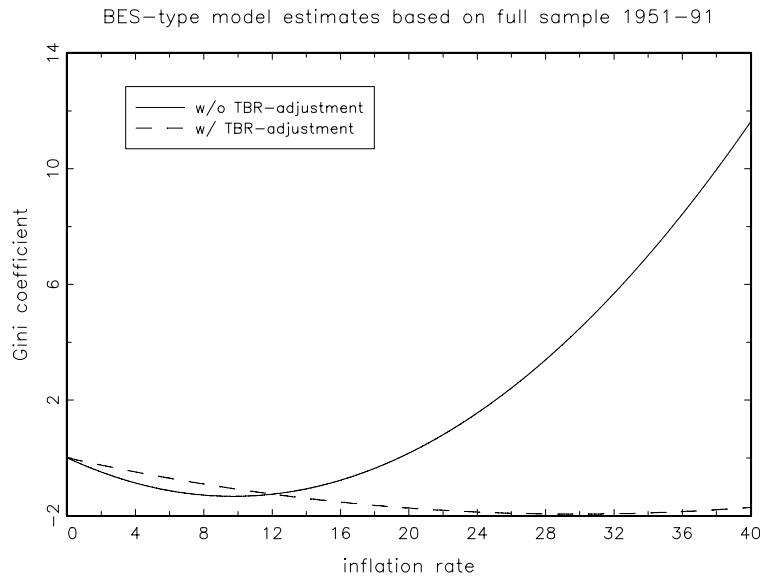


Table 2. Cumulative changes in percentage income shares (BES-type estimates)

period	dependent	inflation rate	inflation rate	unemployment rate
		w/o TBR-adj.	w/ TBR-adj.	
1951-86	Q_1	+0.124***	+0.092	-0.153**
	Q_2	+0.069***	+0.056	-0.104***
	Q_3	+0.022	+0.020	+0.022
	Q_4	-0.002	-0.032	+0.197**
	Q_5	-0.213	-0.136	-0.017
1951-91	Q_1	+0.146***	+0.102	-0.112**
	Q_2	+0.082***	+0.057	-0.118***
	Q_3	+0.023	+0.015	+0.029
	Q_4	-0.004	-0.043	+0.258***
	Q_5	-0.247	-0.132	-0.056

Note: *, **, *** based on coefficients estimates significant at 10, 5, 1% level.

In summary, the above results based on BES-type regressions are indicative for the fact that inflation impacts on income distribution like a progressive income tax in a range of rates up to about 10% of inflation. In other words, they suggest a trade-off between the inflation rate and the Gini coefficient of households' incomes. However, this trade-off is close to negligible in quantitative terms. The computed cumulative effects of inflation on the US income distribution's quintile income shares is indicative for the following interpretation: The two lowest quintiles are significant relative long-term "winners" of inflation. Although, in the long run the second quintile is losing significantly more in share through higher unemployment rates than winning through inflation. As can be seen from Table 1 above, however, the contemporaneous unemployment rate shows no significant explanatory power in case of investigating the overall Gini coefficient as dependent variable. Tax bracket adjustments that took place during our observation period seem to predominantly lower the effects of inflation on the income shares of the highest quintile, to disadvantage primarily the first ("inflation-winners") and the fourth ("inflation-loosers"), and to impact only marginally on the other quintiles' income shares. However, it should be noted that the latter finding is speculative, insofar as it is not statistically significant.

2.3 Basic error correction model (ECM) estimates

At first glance, Figure 3 below is suggestive for a stationary deviation from long term equilibrium, i.e. a cointegrating relationship, between the US income distribution's Gini coefficient and the US inflation rate. Allowing for an integrated modelling of trend and autoregressive dynamics, we aim to test this hypothesis in the following with and without considering historical tax bracket boundaries adjustments (TBB_t) as introduced in the preceding paragraphs and documented in the appendix.

As is common practice in cointegration analysis, we estimate our ECM specifications in natural logs. Therefore, we need to scale our inflation rate variable to $\tilde{\pi}_t = 1 + \pi_t$ due to a negative value of the US inflation rate (deflation) in 1955, i.e. $\pi_{1955} = -0.49\%$.

In detail, we consider the following univariate ECM specifications

$$\Delta \ln G_t = \beta_0 + \beta_1 \Delta \ln \tilde{\pi}_t + \beta_2 \Delta \ln \tilde{\pi}_t^2 + \beta_3 \Delta \ln u_t + \sum_{i=4}^6 \beta_i (\ln G_{t-1} - \gamma_z \ln z_{t-1}) + \varepsilon_t, \quad (5)$$

$$\begin{aligned} \Delta \ln G_t = & \beta_0 + (\beta_1 + \beta_2 TBB_t) \Delta \ln \tilde{\pi}_t + (\beta_3 + \beta_4 TBB_t) \Delta \ln \tilde{\pi}_t^2 \\ & + \beta_5 \Delta \ln u_t + \sum_{i=6}^8 \beta_i (\ln G_{t-1} - \gamma_z \ln z_{t-1}) + \varepsilon_t, \end{aligned} \quad (6)$$

where ε_t is an i.i.d. normal error and the summation term represents the respective cointegrating or error correction equations. Δ denotes first differences and $z = \{\tilde{\pi}, \tilde{\pi}^2, u\}$. The γ_z -values are taken from the respective long term multiplier relationship estimated by general dynamic models of the form

$$\ln G_t = \alpha_0 + \alpha_1 \ln G_{t-1} + \rho_0 \ln z_t + \rho_1 \ln z_{t-1} + \varepsilon_t$$

for $z = \{\tilde{\pi}, \tilde{\pi}^2, u\}$. Thereof, γ_z is calculated as $\gamma_z = (\rho_0 + \rho_1) / (1 - \alpha_1)$. This procedure is well known as the Engle-Granger two-step estimator for models involving cointegrated variables; see Banerjee *et al.* (1993), p. 157-161.

As can be seen from Table 3 below, we find a significant stationary, or I(0), combination of G_t and $\tilde{\pi}_t$, i.e. a significant cointegrating equation, only in case of specification ECM1. All other specifications show no significant long-run relationship between G_t and $\tilde{\pi}_t$ or $\tilde{\pi}_t^2$.

Table 3. Basic ECM estimates; full sample: 1951-1991

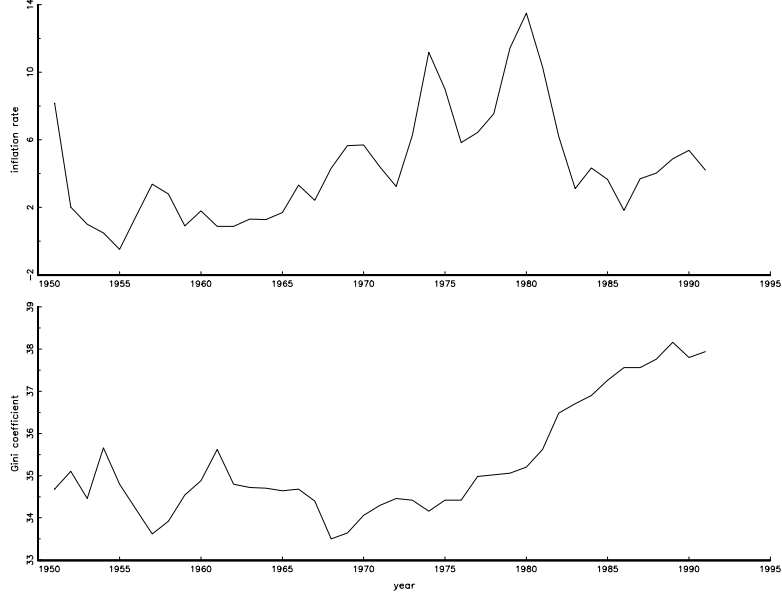
Specification:	ECM1	ECM2	ECM3
$\Delta \ln \tilde{\pi}_t$	-0.005	+0.026**	+0.020*
$\ln G_{t-1} - \gamma_{\tilde{\pi}} \ln \tilde{\pi}_{t-1}$	+0.023**	+0.114	+0.072
$\Delta \ln \tilde{\pi}_t^2$		-0.014***	-0.011**
$\ln G_{t-1} - \gamma_{\tilde{\pi}^2} \ln \tilde{\pi}_{t-1}^2$		-0.074	-0.052
$\Delta \ln u_t$			+0.028***
$\ln G_{t-1} - \gamma_u \ln u_{t-1}$			+0.017***
Adj. R ²	0.153	0.300	0.433
F-Stat.	4.540	5.184	5.977
$\Delta \ln \tilde{\pi}_t$	-0.005	+0.026**	+0.017*
$TBB_t \Delta \ln \tilde{\pi}_t$	-0.002	-0.088*	-0.032
$\ln G_{t-1} - \gamma_{\tilde{\pi}} \ln \tilde{\pi}_{t-1}$	+0.023**	+0.112	+0.051
$\Delta \ln \tilde{\pi}_t^2$		-0.014***	-0.011**
$TBB_t \Delta \ln \tilde{\pi}_t^2$		+0.035*	+0.017
$\ln G_{t-1} - \gamma_{\tilde{\pi}^2} \ln \tilde{\pi}_{t-1}^2$		-0.072	-0.036
$\Delta \ln u_t$			+0.030**
$\ln G_{t-1} - \gamma_u \ln u_{t-1}$			+0.019***
Adj. R ²	0.131	0.275	0.426
F-Stat.	2.972	3.471	4.619

Note: *, **, *** denotes significant at 10, 5, 1% level
(based on Newey-West HAC standard errors).

2.4 Vector error correction model (VECM) estimates

Although, we found no clear evidence of cointegration between the nonstationary G_{t-} and $\tilde{\pi}_t$ -series from our basic ECM estimates, we proceed to model them in a restricted VAR framework that has cointegrating restrictions built into the specification, i.e. in a VECM framework. This subsection therefore has two primary objectives: First, to give our empirical models a more vigorous dynamic structure and second, to investigate the empirical impulse responses calculated on the base of our VECM estimates.

Figure 3: US inflation rate and Gini coefficient: 1951-91



Consider a VAR of order p :

$$\mathbf{y}_t = \mathbf{A}_1 \mathbf{y}_{t-1} + \dots + \mathbf{A}_p \mathbf{y}_{t-p} + \mathbf{B} \mathbf{x}_t + \varepsilon_t,$$

where, in our case, \mathbf{y}_t is a 2×1 -vector of nonstationary I(1) variables, i.e. $(\ln G_t \ln \tilde{\pi}_t)'$, \mathbf{x}_t is a 4×1 -vector of deterministic variables, as given here by $(\ln \tilde{\pi}_t \ln \tilde{\pi}_t^2 \ln u_t \ln u_t^2)'$, and ε_t denotes a vector of innovations. We can rewrite this VAR as:

$$\Delta \mathbf{y}_t = \mathbf{\Pi} \mathbf{y}_t + \sum_{i=1}^{p-1} \mathbf{\Gamma}_i \Delta \mathbf{y}_{t-i} + \mathbf{B} \mathbf{x}_t + \varepsilon_t, \quad (7)$$

where

$$\mathbf{\Pi} = \sum_{i=1}^p \mathbf{A}_i - I, \mathbf{\Gamma}_i = - \sum_{j=i+1}^p \mathbf{A}_j.$$

For our particular variables of interest, the deterministic part of the corresponding unrestricted VAR of order 2 can be written as

$$\begin{pmatrix} \Delta \ln y_t \\ \Delta \ln \tilde{\pi}_t \end{pmatrix} = \begin{pmatrix} \alpha_0 \\ \alpha_1 \end{pmatrix} \begin{pmatrix} \beta_0 & \beta_1 & \beta_2 \end{pmatrix} \begin{pmatrix} 1 \\ \ln y_{t-1} \\ \ln \tilde{\pi}_{t-1} \end{pmatrix} + \begin{pmatrix} \beta_{1,3} & \dots & \beta_{1,7} \\ \beta_{2,3} & \dots & \beta_{2,7} \end{pmatrix} \begin{pmatrix} 1 & \Delta \ln y_{t-1} & \Delta \ln \tilde{\pi}_{t-1} & \ln z_t \end{pmatrix}', \quad (8)$$

for $y_t = \{G_t, Q_{1,t}, Q_{5,t}\}$, $y_{t-1} = \{G_{t-1}, Q_{1,t-1}, Q_{5,t-1}\}$, and $z_t = \{\tilde{\pi}_t, \tilde{\pi}_t^2, u_t, u_t^2\}$. Obviously, we concentrate on the lowest and highest income quintile and, by considering $u_t^2 \in z_t$, allow for a sort of Phillips Curve relationship in the second equation of the specified system.

It can be shown that if the coefficient matrix $\mathbf{\Pi}$ has reduced rank $r < k = 2$, then there exist two $k \times r$ -matrices α and β each with rank r such that $\mathbf{\Pi} = \alpha\beta'$ and $\beta'y_t$ is stationary. The number of cointegrating relations, or cointegrating rank, is given by r , while β represents the cointegrating vector. The popular Johansen-Cointegration-test then consists in estimating matrix $\mathbf{\Pi}$ in its unrestricted form and proceedingly in testing whether the restrictions implied by the reduced rank of $\mathbf{\Pi}$ can be rejected.

In contrast to specification

$$\begin{aligned} \begin{pmatrix} \Delta \ln y_t \\ \Delta \ln \tilde{\pi}_t \end{pmatrix} &= \begin{pmatrix} \alpha_0 \\ \alpha_1 \end{pmatrix} \begin{pmatrix} \beta_0 & \beta_1 & \beta_2 \end{pmatrix} \begin{pmatrix} 1 \\ \ln y_{t-1} \\ \ln \tilde{\pi}_{t-1} \end{pmatrix} + \\ &\begin{pmatrix} \beta_{1,3} & \dots & \beta_{1,9} \\ \beta_{2,3} & \dots & \beta_{2,9} \end{pmatrix} \begin{pmatrix} 1 & \Delta \ln y_{t-1} & \Delta \ln \tilde{\pi}_{t-1} & \ln z_t \end{pmatrix}', \end{aligned} \quad (9)$$

for y_t and y_{t-1} as given above and $z_t = \{\tilde{\pi}_t, \tilde{\pi}_t^2, TBB_t\tilde{\pi}_t, TBB_t\tilde{\pi}_t^2, u_t, u_t^2\}$, i.e. the case of taking historical tax bracket boundaries adjustments into account, for specification (8) the L.R.-test as part of the Johansen-Test procedure rejects the hypothesis of no cointegration but not the hypothesis of at most one cointegrating relation. For (9) both hypotheses are rejected at the five percentage level of significance. Detailed results can be given in an extended appendix which is available and will be furnished on request.

Figures 4 and 5 below display the implied impulse responses (IRs) for the full sample (1951-91) and sub-sample (1951-86) period of estimations (8) and (9), respectively. Since none of our specifications generates statistically significant coefficient estimates for the inflation variables, we abstract from calculating bootstrapped or similar asymptotic confidence bands. Surprisingly, the qualitative result, i.e. the shape of the implied IR-functions is obviously not in line with our previous findings: After about three to four periods of adjustment a one percentage standard deviation shock on the inflation rate leads to a permanent increase (decrease) of the Gini coefficient and the highest quintile's income share (of the lowest quintile's income share). Apart from a somehow smoother adjustment of the Gini to the inflationary shock, taking historical tax bracket adjustments into account does not change the results qualitatively. Again, quantitatively it also implies negligible effects.

Figure 4: Impulse responses for VECM-specification: equation (8)

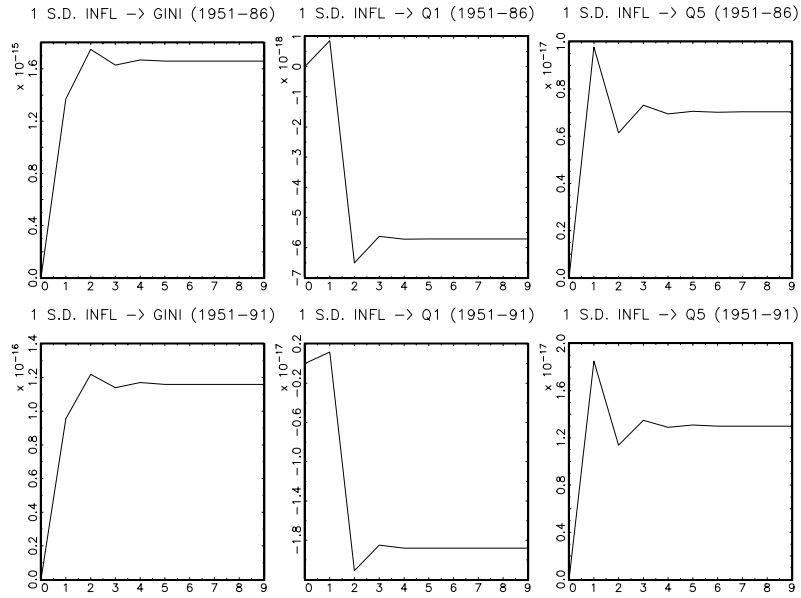
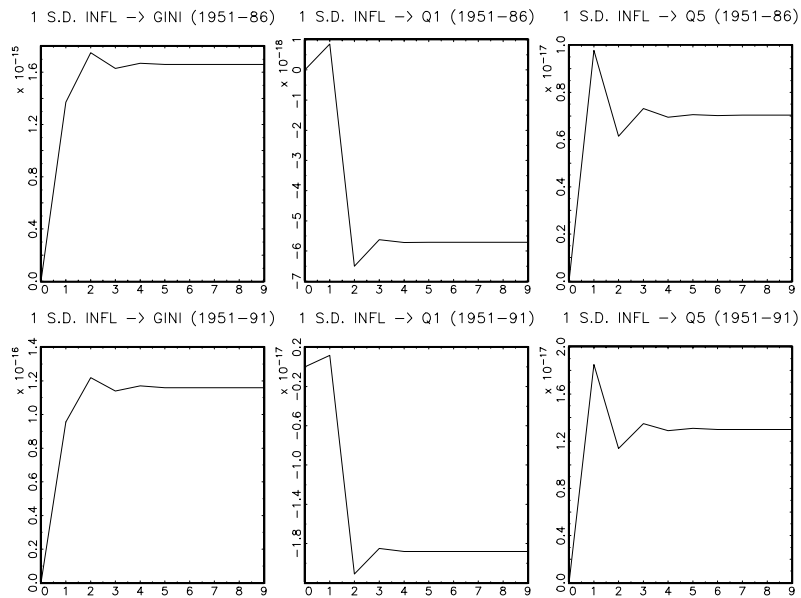


Figure 5: Impulse responses for VECM-specification: equation (9)



In summary, our empirical analysis lends support to the view that inflation reduces the inequality of the income distribution for the post-WW II US economy. Although, this trade-off is close to negligible in quantitative terms, it holds in case of considering historical tax bracket boundaries adjustments. Though not a statistically robust result, it seems that it was only the richest quintile profiting from these adjustments in terms of income share in the four decades at stake; cf. Table 2 above. Evidence on the long-run relationship between inflation and the considered measures of the US income distribution is notably mixed and mostly statistically insignificant. This, especially, holds for our (V)ECM estimates: Neither our ECM nor our VECM specifications produce statistically robust coefficient estimates for the inflation variables. Therefore, both reported results need to be interpreted with adequate caution.

3 A monetary general equilibrium model with progressive income taxation

In this section, we develop a general equilibrium overlapping generations model with endogenous equity and money distribution. Four sectors can be depicted: households, production, the government, and the central bank. Household maximize discounted life-time utility. Agents can save either with money or with capital. Individuals are heterogeneous with regard to their productivity and cannot insure against idiosyncratic income risk. Firms maximize profits. Output is produced with the help of labor and capital. The government provides unfunded public pensions which are financed by a progressive tax on wage and capital income. The money growth rate is set by the central bank and seignorage is redistributed lump-sum to the households.

3.1 Households

Every year, a generation of equal measure is born. A subscript j of a variable denotes the age of the generation. The total measure of all households is normalized to one.

Households live a maximum of $T + T^R$ years. Lifetime is stochastic and agents face a probability s_j of surviving up to age j conditional on surviving up to age $j - 1$. During

their first T years, agents supply labor l elastically. After T years, retirement is mandatory. Agent i maximizes her life-time utility:

$$E_0 \left[\sum_{j=1}^{T+T^R} \beta^{j-1} \left(\prod_{h=1}^j s_h \right) u(c_j^i, m_j^i, 1 - l_j^i), \right] \quad (10)$$

where β , c_j^i , and m_j^i denote the discount factor, consumption and real money balances of agent i at age j , respectively. Instantaneous utility $u(c, m, 1 - l)$ is given by:

$$u(c, m, 1 - l) = \ln c + (1 - \gamma) \ln m + B \ln(1 - l). \quad (11)$$

Workers are heterogeneous with regard to their labor earnings per working hour. The worker's labor productivity $e(z, j)$ is stochastic and depends on his age j and an idiosyncratic labor productivity shock z . We assume that the idiosyncratic part of productivity follows a first order finite state Markov chain with conditional transition probabilities given by:

$$\pi(z'|z) = Pr\{z_{t+1} = z' | z_t = z\}, \quad (12)$$

where $z, z' \in \mathcal{E}$. Although the dynamics of productivity may be modelled slightly better by a second order Markov chain (Shorrocks, 1976) the improvement in accuracy is rather small and does not justify the considerable increase in the model's complexity.

Furthermore, agents are born without wealth, $a_1 = 0$, and cannot borrow, $a_j \geq 0$ for all j . Wealth a is composed of real money m and capital k . Capital or, equally, equity k earns a real interest rate r . We further assume a short-sale constraint $k \geq 0$. Parents do not leave altruistic bequests to their children. All accidental bequests are confiscated by the state.

Agent i receives income from capital k^i and labor l^i . The budget constraint of the working agent at age $j = 1, \dots, T$ in period t is given by

$$a_{j+1,t+1}^i = k_{j+1,t+1}^i + m_{j+1,t+1}^i = (1 + r_t)k_{jt}^i + \frac{m_{jt}^i}{1 + \pi_t} + w_t e(z, j) l_{jt}^i + t r_t - \frac{\tau_t (P_t y_{jt}^i)}{P_t} + c_{jt}^i, \quad (13)$$

where w_t and $\pi_t = \frac{P_t - P_{t-1}}{P_{t-1}}$ denote the wage rate per efficiency unit labor and the inflation rate in period t , respectively. P_t is the price level in period t . Individual nominal

income $P_t y_{jt}^i \equiv P_t w_t e(z, j) l_{jt}^i + P_t r_t k_{jt}^i$ is taxed at the progressive rate τ .⁹ In addition, the households receive transfers tr_t from the central bank.

During retirement, agents receive public pensions pen_t in period t irrespective of their employment history and the budget constraint of the retired agent at age $j = T+1, \dots, T+T^R$ is given by

$$a_{j+1,t+1}^i = k_{j+1,t+1}^i + m_{j+1,t+1}^i = (1 + r_t)k_{jt}^i + \frac{m_{jt}^i}{1 + \pi_t} + pen_t + tr_t - \frac{\tau_t(P_t y_{jt}^i)}{P_t} - c_{jt}^i. \quad (14)$$

The necessary conditions of the households with regard to consumption c_{jt}^i , capital $k_{j+1,t+1}^i$, real money $m_{j+1,t+1}^i$, and labor l_{jt}^i are as follows:

$$u_c(c_{jt}^i, m_{jt}^i, 1 - l_{jt}^i) = \lambda_{jt}^i \quad (15)$$

$$\lambda_{jt}^i = \beta E_t \left[\lambda_{j+1,t+1}^i \left(1 + r_{t+1} \left(1 - \frac{\partial \tau}{\partial P_{t+1} y_{j+1,t+1}^i} \right) \right) \right] \quad (16)$$

$$\lambda_{jt}^i = \beta E_t \left[\lambda_{j+1,t+1}^i \frac{1}{1 + \pi_{t+1}} + u_m(c_{j+1,t+1}^i, m_{j+1,t+1}^i, 1 - l_{j+1,t+1}^i) \right] \quad (17)$$

$$u_l(c_{jt}^i, m_{jt}^i, 1 - l_{jt}^i) = \lambda_{jt}^i w_t e(j, z) \left[1 - \frac{\partial \tau}{\partial P_t y_{jt}^i} \right], \quad (18)$$

where $u_x(\cdot)$ denotes the first partial derivative of the utility function with regard to the argument $x = c, 1 - l, m$.

3.2 Production

Firms are of measure one and produce output with effective labor N and capital K . Effective labor N_t is the product of working hours and individual productivity and is defined in more detail below.

Effective labor N_t is paid the wage w_t . Capital K_t is hired at rate r_t and depreciates at rate δ . Production Y_t is characterized by constant returns to scale and assumed to be Cobb-Douglas:

$$Y_t = F(K_t, N_t) = K_t^\alpha N_t^{1-\alpha}. \quad (19)$$

⁹In models similar to ours (but without a monetary sector), Ventura (1999) and Castañeda et al. (1999) study the effects of a flat rate tax reform on distribution and welfare. We follow Castañeda et al. who assume that both labor and interest income are taxed at the same rate.

In a factor market equilibrium, factors are rewarded with their marginal product:

$$w_t = (1 - \alpha)K_t^\alpha N_t^{-\alpha}, \quad (20)$$

$$r_t = \alpha K_t^{\alpha-1} N_t^{1-\alpha} - \delta. \quad (21)$$

3.3 Government

Government expenditures consists of government consumption G_t , government lump-sum transfers Tr_t to households, and social securities expenditures Pen_t . Government expenditures are financed by an income tax Tax_t and confiscated accidental bequests Beq_t :

$$G_t + Pen_t + Tr_t = Tax_t + Beq_t. \quad (22)$$

We follow Castañeda et al. (1999) and characterize the US income tax structure by a progressive tax function. In particular, we also adapt the following functional form for the income tax function that is based upon the estimates of Gouveira and Strauss (1994):

$$\tau(Py_t) = b_{0,t} \left(y - \left(y^{-b_{1,t}} + b_{2,t} \right)^{-\frac{1}{b_{1,t}}} \right) \quad (23)$$

We further assume that the government adjusts the nominal income tax brackets every TB year. Without the loss of generality, we assume that the income tax rate schedule is adjusted in periods (=years) $t \in \{0, TB, 2TB, 3TB, \dots\}$. With regard to our tax function (23), this is equivalent to assume that the tax parameters $\{b_{0,t}, b_{1,t}, b_{2,t}\}$ are adjusted every TB years so that the real tax burden is the same as in the benchmark year $t = 0$. As a consequence, agents average and marginal income tax rates increases in the years between two successive tax rate adjustments as inflation increases the nominal income Py_{jt}^i ceteris paribus.

3.4 Monetary authority

Nominal money grows at the exogenous rate θ :

$$\frac{M_t - M_{t-1}}{M_{t-1}} = \theta. \quad (24)$$

The seignorage is transferred lump-sum to the households:

$$tr_t = \frac{M_t - M_{t-1}}{P_t}. \quad (25)$$

3.5 Stationary equilibrium

The concept of equilibrium applied in this paper uses a recursive representation of the consumer's problem following Stokey et al. (1989). Let $V_{jt}^i(k_{jt}^i, m_{jt}^i, z)$ be the value of the objective function of the j -year old agent with equity k_{jt}^i , real money m_{jt}^i , and idiosyncratic productivity level z . $V_{jt}^i(k_{jt}^i, m_{jt}^i, z)$ is defined as the solution to the dynamic program:

$$V_{jt}^i(k_{jt}^i, m_{jt}^i, z) = \max_{k_{j+1,t+1}^i, m_{j+1,t+1}^i, c_{jt}^i, l_{jt}^i} \left\{ u(c_{jt}^i, m_{jt}^i, 1 - l_{jt}^i) + \beta s_{j+1} E_t [V_{j+1,t+1}^i(k_{j+1,t+1}^i, m_{j+1,t+1}^i, z')] \right\} \quad (26)$$

subject to (12), (13) or (14) and $k, m \geq 0$. Optimal decision rules of the agent i in period t at age j are a function of the individual state variables k_{jt}^i , m_{jt}^i , and z , the distribution of capital and money, μ , and the tax schedule. As the tax schedule is adjusted every TB periods, the period t is also an argument of the policy function. Let $c_t(k, m, z, j, \mu)$, $l_t(k, m, z, j, \mu)$, $k_t^l(k, m, z, j, \mu)$, and $m_t^l(k, m, j, \mu)$ denote the optimal consumption, labor supply, next-period capital stock, and next-period real money balances for a j -year aged individual with productivity z , capital stock k , and real money balances m , and distribution of capital k and money m in period t . Furthermore, let $\mu_t(k, m, z, j)$ denote the measure of j -year old agents with productivity z in period t that hold capital k and real money balances m .

We will consider a stationary equilibrium where the inflation rate is constant in every period t . Furthermore, government consumption is assumed to be constant, $G_t = G$, and pensions pen_t are assumed to be of equal magnitude every TB periods, respectively. As a consequence, the factor prices, aggregate capital and labor, and the distribution μ_t are also the same every TB periods, respectively.

Definition

A stationary equilibrium for a given government policy $\{b_{0,t}, b_{1,t}, b_{2,t}, G_t, pen_t\}$ and central

bank policy $\theta_t = \theta$ is a collection of value functions $V_{jt}^i(k, m, z)$, individual policy rules $c_t(k, m, z, j, \mu)$, $l_t(k, m, z, j, \mu)$, $k'_t(k, m, z, j, \mu)$, $m'_t(k, m, z, j, \mu)$, relative prices of labor and capital $\{w_t, r_t\}$, and a law of motion for the distribution $\mu_{t+1} = g(\mu_t)$ such that:

1. Money grows at the exogenous rate θ and the seignorage (25) is transferred lump-sum to the households.
2. The inflation rate π_t is constant and equal to the money growth rate θ .
3. The government adjusts the tax schedule in the years $\{0, TB, 2TB, \dots\}$. In the years $t \in \{p + TB, p + 2TB, p + 3TB, \dots\}$, $p = 0, \dots, TB - 1$, government consumption G_t and individual pensions pen_t are the same, respectively so that all exogenous variables in the economy are the same every TB periods.
4. The government budget (22) is balanced.
5. Individual and aggregate behavior are consistent:

$$K_t = \sum_{j=1}^{T+T^R} \int_k \int_m \int_z k \mu_t(k, m, z, j) dz dm dk, \quad (27)$$

$$N_t = \sum_{j=1}^T \int_k \int_m \int_z l_t(k, m, z, j, \mu) e(z, j) \mu_t(k, m, z, j) dz dm dk \quad (28)$$

$$C_t = \sum_{j=1}^{T+T^R} \int_k \int_m \int_z c_t(k, m, z, j, \mu) \mu_t(k, m, z, j) dz dm dk, \quad (29)$$

$$Pen_t = \sum_{j=T+1}^{T+T^R} \int_k \int_m \int_z pen_t \mu_t(k, m, z, j) dz dm dk, \quad (30)$$

$$Tax_t = \sum_{j=T+1}^{T+T^R} \int_k \int_m \int_z \frac{\tau(P_t y_t(k, m, z, j))}{P_t} \mu_t(k, m, z, j) dz dm dk, \quad (31)$$

$$Beq_t = \sum_{j=1}^{T+T^R} \int_k \int_m \int_z (1 - s_{j+1}) a'_{t-1}(k, m, z, j, \mu) \mu_{t-1}(k, m, z, j) dz dm dk \quad (32)$$

$$\frac{M}{P} = \sum_{j=1}^{T+T^R} \int_k \int_m \int_z m \mu_t(k, m, z, j) dz dm dk, \quad (33)$$

where $a'_t(\cdot) \equiv k'_t(\cdot) + m'_t(\cdot)$ are the optimal next-period assets and $y_t(k, m, z, j)$ denotes the real income of a j -year old agent with productivity z , capital k , and money m in period t . Furthermore, $tr_t = Tr_t$.

6. Relative prices $\{w_t, r_t\}$ solve the firm's optimization problem by satisfying (20) and (21).
7. Given the government policy $\{b_{0,t}, b_{1,t}, b_{2,t}, G_t, pen_t\}$ and the distribution μ_t , the individual policy rules $c_t(\cdot)$, $k'_{t+1}(\cdot)$, $m'_{t+1}(\cdot)$, and $l_t(\cdot)$ solve the consumer's dynamic program (26).
8. The goods market clears in every period t :

$$K_t^\alpha N_t^{1-\alpha} = C_t + \delta K_t + K_{t+1} - K_t. \quad (34)$$

9. The dynamics of the distribution $\mu_{t+1} = g(\mu_t)$ are consistent with individual behavior:

$$\begin{aligned} \mu_{t+1}(k', m', z', j+1) = & \quad (35) \\ \int_k \int_m \int_z 1_{k'=k'_t(k,m,z,j,\mu)} \cdot 1_{m'=m'_t(k,m,z,j,\mu)} \cdot Pr(z'|z) \cdot \mu_t(k, m, z, j) dz dm dk, \end{aligned}$$

where $1_{k'=k'_t(\cdot)}$ is an indicator function that takes the value one if $k' = k'_t(\cdot)$ and zero otherwise. $1_{m'=m'_t(\cdot)}$ is defined in an analogous way. Furthermore, the new-born generation has zero wealth, $k = 0$ and $m = 0$.¹⁰ Notice further that, in particular, $\mu_t = \mu_{t+TB}$ in a stationary equilibrium.

In the Appendix, we describe the computational algorithm that we use in order to compute an approximation to this equilibrium.

4 Calibration

Periods correspond to years. We assume that agents are born at real lifetime age 20 which corresponds to $j = 1$. Agents work $T = 40$ years corresponding to a real lifetime age of 60. They live a maximum life of 60 years ($T^R = 20$) so that agents do not become older than real lifetime age 80. The sequence of conditional survival probabilities $\{s_j\}_{j=1}^{59}$ is set

¹⁰For computational purpose, agents of the first-year generation are endowed with small money balances so that the utility function does not take the value of infinity.

equal to the Social Security Administration's survival probabilities for men aged 20-78 for the year 1994.¹¹ The survival probabilities decrease with age, and s_{60} is set equal to zero.

The calibration of the parameters α , δ , pen , and θ and the Markov process $e(z, j)$ is chosen in accordance with existing general equilibrium studies. Following Prescott (1986), the capital income share α is set equal to 0.36. The annual rate of depreciation is set equal to $\delta = 0.08$. Pensions are distributed lump-sum to the retired agents. The replacement ratio of pensions to net average earnings amounts to 50% in every period t . Hence, pensions are a function of the distribution μ_t and, hence, K_t and N_t , and are the same every TB periods. The income tax rate is adjusted every $TB = 3$ years in accordance with the findings presented in section 2.¹² The model parameters are presented in Table 4.

The tax function (23) is calibrated with the help of the estimates from Gouveira/Strauss.¹³ In particular, we set the income tax parameters in period $t = 0$ (where we normalized the price level to one, $P_0 = 1$) equal to $b_0 = 0.258$, $b_1 = 0.768$, $b_2 = 0.031$. The income tax parameters b_0 and b_1 are taken from Gouveira/Strauss for the tax year 1989, while b_2 has been adjusted so that the tax rate of the average income in our model is equal to the tax rate of the average US income. Every TB years, these parameters are adjusted so that the average and marginal tax rates of the real income are unchanged between period TB and $p \cdot TB$, $p = 1, 2, \dots$

The labor endowment process is given by $e(z, j) = e^{z_j + \bar{y}_j}$, where \bar{y}_j is the mean lognormal income of the j -year old. The mean efficiency index \bar{y}_j of the j -year-old worker is taken from Hansen (1993), and interpolated to in-between years. As a consequence, the model is able to replicate the cross-section age distribution of earnings of the US economy. Following İmrohoroğlu et al. (1998), we normalize the average efficiency index to one. The age-productivity profile is hump-shaped and earnings peak at age 50.

The idiosyncratic productivity shock z_j follows a Markov process. The Markov process is given by:

$$z_j = \rho z_{j-1} + \epsilon_j, \tag{36}$$

where $\epsilon_j \sim N(0, \sigma_\epsilon)$. Huggett (1996) uses $\rho = 0.96$ and $\sigma_\epsilon = 0.045$. Furthermore, we

¹¹We thank Mark Huggett and Gustavo Ventura for providing us with the data.

¹²Our qualitative results are the same in the cases $TB = 2$ and $TB = 4$. The results for the case $TB = 4$ are also presented in section 5.

¹³These parameter values have also been applied by Castañeda et al (1999).

Table 4: Calibration of parameter values for the US economy

Description	Function	Parameter
utility function	$U = \gamma \ln c + (1 - \gamma) \ln m + B \ln(1 - l)$	$\gamma = 0.974, B = 1.72$
discount factor	β	$\beta = 0.969$
production function	$Y = K^\alpha N^{1-\alpha}$	$\alpha = 0.36$
depreciation	δ	$\delta = 0.08$
money growth rate	θ	$\theta = 0.05$
pension replacement rate		0.50
periods between tax schedule adjustments	TB	$TB = 3$
income tax function in $t = 0$ with $P_0 = 1$	$\tau(y) = b_0 \left(y - \left(y^{-b_1} + b_2 \right)^{-\frac{1}{b_1}} \right)$	$b_0 = 0.258, b_1 = 0.768,$ $b_2 = 0.031$
labor endowment process	$z_t = \rho z_{t-1} + \epsilon_t, \epsilon_t \sim N(0, \sigma_\epsilon)$ $\ln e(z, 1) \sim N(\bar{y}_1, \sigma_{y_1})$	$\rho = 0.96, \sigma_\epsilon = 0.045$ $\sigma_{y_1} = 0.38$

follow Huggett and choose a lognormal distribution of earnings for the 20-year old with $\sigma_{y_1} = 0.38$ and mean \bar{y}_1 . As the log endowment of the initial generation of agents is normally distributed, the log efficiency of subsequent agents will continue to be normally distributed. This is a useful property of the earnings process, which has often be described as log normally in the literature.

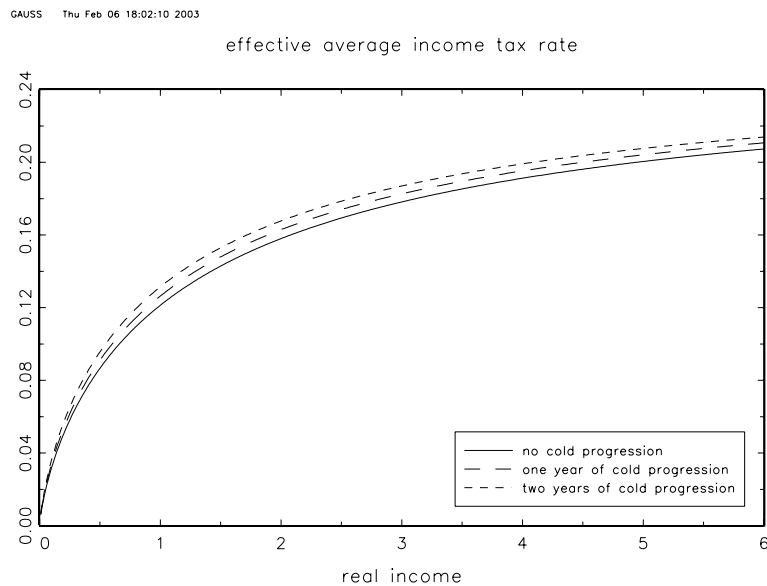
The remaining three parameters β , B , and γ from the utility function are chosen to match the following characteristics of the US economy as closely as possible: i) the capital-output ratio K/Y amounts to 3.0 as found by Auerbach and Kotlikoff (1995), ii) the average labor supply of the working households amounts to approximately one third of available time, and iii) the average velocity of money PY/M is equal to the annual velocity of M1 during 1960-2001, which is equal to 5.18. Our calibration $\beta = 0.969$, $B = 1.72$, and $\gamma = 0.974$ implies a capital-output ratio equal to 2.98, an average labor supply $\bar{l} = 0.326$, and an annual velocity of money equal to 5.12.

5 Results

In this section, we study the effects of a change of the money growth rate θ or, equally, the inflation rate π on the stationary distribution of income. Remember that, in our benchmark case, the inflation rate is equal to 5% and the tax schedule is adjusted every 3 years. The effect of the cold progression on the marginal and average tax rates is illustrated in Figures 6 and 7 (where the average real income of the economy is normalized to one). Obviously, the average income tax and the marginal tax rate hardly change after one or two years of cold progression. Hence, we would expect only small effects from the cold progression on the individual's savings and labor supply.

Table 5 summarizes our results for the benchmark case. The first column gives the number of periods that have been elapsed since the last tax schedule adjustment. The remaining columns present the aggregate capital stock K_t , average labor supply l_t , aggregate effective labor N_t , aggregate production Y_t , average real money balances m_t , government transfers tr_t , and total income taxes Tax_t , and the Gini coefficients of the income distribution. Notice that the increase in the marginal and average income tax rates between two successive periods of the tax schedule adjustment results in an increase of total income taxes of

Figure 6: Average income tax rate



approximately 2.5% each year. Similarly, transfers to the households also increase in order to keep the government budget balanced. Surprisingly, aggregate savings, $K_t + \bar{m}_t$, and average labor supply \bar{l}_t even increase with higher marginal tax rates. However, quantitative effects are of negligible order. As a consequence, the pre-tax wage income remains almost unchanged during the course of cold progression and is characterized by a Gini coefficient equal to approximately 0.56. Notice that this value is close to values observed empirically. Díaz-Giménez et al. (1997) find a value of 0.51 for households aged 36-50. The Gini coefficient of the total net income is smaller and amounts to only 0.49 as income is taxed progressively and transfers are distributed lump-sum.

Our empirical analysis suggests that there exists an inflation rate in the range above 10% that minimizes the inequality in the income distribution. In order to consider the effects of a higher inflation rate, we recomputed the model for the money growth rate $\theta = \pi = 10\%$. The results for the high-inflation economy are summarized in Table 6.

Following an increase of inflation from 5% to 10%, agents reduce their stationary real money balances. The average real money balances \bar{m}_t drops from 0.142 to 0.090. Furthermore,

Figure 7: Marginal income tax rate

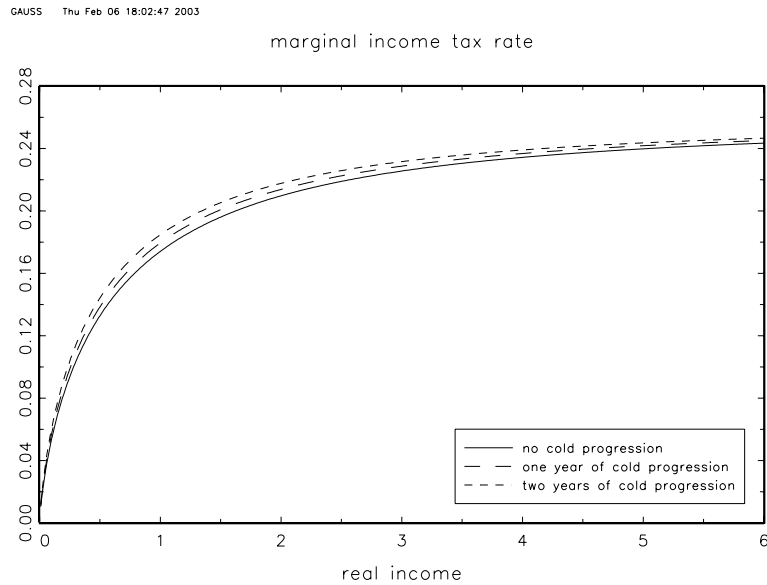


Table 5: Cold progression, aggregate values and distribution for $\pi = 5\%$

year t after tax code adjustment	K_t	\bar{l}_t	N_t	Y_t	\bar{m}_t	tr_t	Tax_t	Gini coefficient	
								Wage Income	Total Net Income
0	2.063	0.2963	0.3604	0.6754	0.1425	0.03532	0.06514	0.561	0.496
1	2.065	0.2992	0.3638	0.6797	0.1419	0.03676	0.06693	0.560	0.494
2	2.066	0.3027	0.3671	0.6838	0.1412	0.03820	0.06871	0.559	0.492

agents are subject to a more severe cold progression and governmental tax receipts increase by a higher percentage between period 0, 1, and 2. Again, our finding for an inflation rate $\pi = 5\%$ is confirmed that aggregate savings and average labor supply increase during the course of cold progression. In addition, higher inflation reduces both the average labor supply and the inequality of the after-tax income distribution in the presence of cold progression. However, quantitative effects are very small in the case of the income distribution and both the Gini coefficient of the pre-tax wage distribution and the total net income distribution are only affected to a negligible extent. In particular, the Gini coefficient of total net income two periods after the most recent tax schedule adjustment

Table 6: Cold progression, aggregate values and distribution for $\pi = 10\%$

year t after tax code adjustment	K_t	\bar{l}_t	N_t	Y_t	\bar{m}_t	tr_t	Tax_t	Gini coefficient	
								Wage Income	Total Net Income
0	2.065	0.2943	0.3583	0.6731	0.0900	0.0348	0.0647	0.561	0.495
1	2.068	0.2972	0.3616	0.8303	0.0898	0.6774	0.0676	0.560	0.492
2	2.069	0.3002	0.3649	0.8353	0.0895	0.6815	0.0705	0.559	0.489

Table 7: Cold progression, aggregate values and distribution for $\pi = 5\%$
Four-annual tax adjustments, $TB = 4$

year t after tax code adjustment	K_t	\bar{l}_t	N_t	Y_t	\bar{m}_t	tr_t	Tax_t	Gini coefficient	
								Wage Income	Total Net Income
0	1.983	0.2774	0.3333	0.6334	0.1451	0.03148	0.05909	0.560	0.495
1	1.986	0.2803	0.3370	0.6382	0.1445	0.03292	0.06089	0.560	0.494
2	1.988	0.2834	0.3407	0.6429	0.1436	0.03438	0.06271	0.559	0.492
3	1.989	0.2868	0.3446	0.6477	0.1426	0.03585	0.06453	0.557	0.490

only drops from 0.492 to 0.489.

As has been documented in section 2, the US government used to adjust its income tax schedule less frequently in the years prior to 1986 than in recent years. In order to analyze the effects of a less frequent income tax schedule adjustment and, hence, a longer duration of the cold progression, we extend the duration of the cold progression to $TB = 4$ years (keeping the inflation rate at $\pi = 5\%$). As can be seen by inspection of Table 7, agents decrease aggregate savings in this case by approximately 4.0%. The fall in the average labor supply \bar{l}_t is even more pronounced and amounts to approximately 6.3%. Accordingly, the duration of the cold progression seems to be more important for the individual's labor supply and savings decision than the yearly increase in the marginal and average income tax rates. Notice further, that, again, even a longer period of cold progression does not have an important effect on the equality of income distribution.

6 Conclusion

Cold progression has often been cited in the literature as one of the main reasons for an income-inequality reducing effect of (moderate) inflation. Both our empirical and our theoretical analysis support this hypothesis qualitatively. In our empirical analysis, furthermore, we find evidence that the inequality-minimizing inflation rate is in excess of 10%. However, the quantitative effects of higher inflation on (income) inequality are negligible and economically insignificant. We, therefore, carefully conclude that income redistribution due to cold progression should not have been a major policy concern during the US postwar period. One important reason, of course, is that the US income tax schedule has also been characterized by a lower progression than tax income schedules of other countries, e.g. many continental European countries like, among others, Germany. For this reason, an interesting extension of our analysis would be the study of these countries.

In addition, we find that, in our theoretical model, the duration of the cold progression, i.e. the time period between two successive income tax schedule adjustments, is more important for equilibrium values of aggregate savings and average labor supply than the annual change in the tax rates due to cold progression. A shorter duration of cold progression results in higher equilibrium labor supply and output. Our results give support to possible benefits from the change in the US tax policy in the year 1986 as, by the mid 1980s, the US tax system became effectively inflation-indexed.

7 Appendix

7.1 US income tax: Changes of tax brackets and rates 1951-91

The post-war changes of the US income tax schedule are summarized in Table 8 below. The main source of the entries in this table is IRS (2003) along with volumes of the US Major Tax Guide and the ‘Individual Tax Statistics: Complete Report Publications’ of the IRS, where these volumes were available.

In the first column of the table, the second date is the decisive one and gives the year of implementation of either a change of tax bracket boundaries (TBB_t) or of regular income tax rates for fixed boundaries (TRB_t) or of, at least, one of the former ($TTB_t = TBB_t + TRB_t$). Index t denotes the specific year of change. The strength of adjustment is classified ‘substantial’ (‘partial’) in case of at least two (at most one) changing brackets (bracket) and/or at least two (at most one) adjusted tax rates (rate) for fixed boundaries. In this context, it is noteworthy that the partial changes for tax years 1968, 1969, and 1970 refer to the highest bracket’s tax rate which was additionally burdened with a Vietnam War surcharge equal to 7.5% of tax for 1968, 10% of tax for 1969, and 2.5% of tax for 1970. This surcharge did not alter any other than the highest bracket’s rate.

For more detail on the major legislative changes enacted and realized during the period of observation the reader is referred to the brief outline in the text or to Auerbach and Feenberg (2000).

The changes of tax brackets reported in the following Table 8 are based on figures of boundaries for statutory taxable net income, i.e. income after subtracting deductions but before subtracting personal exemptions. Income in this definition still is the tax base for regular income tax, applicable to US citizens and residents. Deductions and provisions unique to nonresident aliens are not considered. The same holds for the tax rates underlying variable TRB_t . They also exclude the effect of tax liability reducing tax credits and refer to regular income tax, consisting in normal tax and surtax.¹⁴

¹⁴For tax years starting with 1954, normal tax and surtax rates were, in effect, combined into a single rate structure; see IRS (2003), p. 325.

Table 8. US individual income tax: Changes of tax brackets and rates 1951-91

Consecutive tax years	Adjustment strength	Major legislative change	Variables		
			TBB_t	TRB_t	TTB_t
50 - 51	substantial	—	0	1	1
51 - 52	substantial	—	0	1	1
53 - 54	substantial	—	0	1	1
63 - 64	substantial	Revenue Act	1	1	1
64 - 65	substantial	—	1	1	1
67 - 68	partial	—	0	1	1
68 - 69	partial	Reform Act	0	1	1
69 - 70	partial	—	0	1	1
76 - 77	substantial	—	1	0	1
78 - 79	substantial	—	1	0	1
80 - 81	substantial	Recovery Act	0	1	1
81 - 82	substantial	—	1	1	1
82 - 83	substantial	—	1	1	1
83 - 84	partial	—	1	0	1
84 - 85	substantial	—	1	0	1
85 - 86	substantial	Reform Act	1	0	1
86 - 87	substantial	—	1	1	1
87 - 88	substantial	—	1	1	1
88 - 89	substantial	—	1	0	1
89 - 90	substantial	—	1	0	1
90 - 91	substantial	—	1	1	1
sum (pre-86):			9	10	16
mean frequency (pre-86):			4.00	3.60	2.25
sum (51-91):			14	14	21
mean frequency (51-91):			2.93	2.93	1.95

In general, there are four different (historical) sets of rates and brackets depending on the respective tax paying person(s): First, “income splitters,” i.e. married taxpayers who “use the joint return filling status” and split their income for tax purposes in an effort

to effectively double the width of their taxable (or net income) size brackets. Figures underlying the chronological categorization of Table 8 above are based on this set. Second, starting with 1952, a set of rates was introduced for “heads of households,” i.e., for unmarried individuals who paid over half of the cost of maintaining a home for a qualifying person (e.g., a child or parent), or for certain married individuals who had lived apart from their spouses for the last six months of the tax year. This filling status was liberalized in 1970 and provides approximately half the advantages of the income-splitting. Third, the so-called “surviving spouse”-set of rates and brackets for which both, rates and taxable income brackets, are designed analogously to the ones of income-splitters. Finally, the remaining taxpayer-set is given for single persons. Since the late 1960s there is an effort of convergence of this set with the one of married couples filing jointly.

It is noteworthy that the 1986 Reform Act implemented during the Reagan-era hallmarks the start of a new period of lower rates and a reduced number of tax brackets. The latter along with the fact that by 1985 the US income tax system became effectively inflation-indexed, led us to discriminate, in our empirical analysis, between the full sample period (1951-91) and the 1951-86 subsample.

7.2 Computation

The model of section 3 cannot be solved analytically, but only numerically. The solution algorithm is described by the following steps:

1. Parameterize the model. Let TB denote the number of years between two adjustments of the nominal income tax schedule.
2. Make initial guesses of the law of motion for the aggregate capital stock $\{K_0, K_1, K_2, \dots, K_{TB-1}\}$, aggregate effective labor $\{N_0, N_1, N_2, \dots, N_{TB-1}\}$, aggregate real money $\{M/P_0, M/P_1, M/P_2, \dots, M/P_{TB-1}\}$ and aggregate (=individual) transfers $\{tr_0, tr_1, \dots, tr_{TB-1}\}$.
3. Compute the values of w_t and r_t for $t = 0, 1, \dots, TB - 1$ that solve the firm’s Euler equations. Compute the pension pen_t so that the replacement rate of pensions with regard to net average labor income is equal to the empirical value.

4. Compute the household's decision functions by solving the Euler equations.
5. Compute the distribution μ_t of the individual state variable $\{k, m, j\}$ by forward induction over age $j = 1, \dots, T + T^R$ for $t = 0, 1, \dots, TB - 1$.
6. Compute the aggregate capital stock $\{K_0, K_1, \dots, K_{TB-1}\}$, aggregate effective labor $\{N_0, N_1, N_2, \dots, N_{TB-1}\}$, aggregate real money $\{M/P_0, M/P_1, M/P_2, \dots, M/P_{TB-1}\}$ and aggregate transfers $\{tr_0, tr_1, \dots, tr_{TB-1}\}$. Update $\{K_0, K_1, \dots, K_{TB-1}\}$, $\{N_0, N_1, N_2, \dots, N_{TB-1}\}$, $\{M/P_0, M/P_1, M/P_2, \dots, M/P_{TB-1}\}$ and $\{tr_0, tr_1, \dots, tr_{TB-1}\}$ and return to step 2 until convergence.

We discretize the state space (k, m, z) using an equispaced grid over the capital stock k , the money balances m , and the individual productivity z . The upper grid points $k_{max} = 20.0$ and $m_{max} = 0.4$ are found to be non-binding. For the productivity z , the (five-point) grid ranges from $-2\sigma_{y_1}$ to $2\sigma_{y_1}$. The probability of having productivity shock z_1 in the first period of life is computed by integrating the area under the normal distribution. The transition probabilities are computed using the method of Tauchen (1986). As a consequence, the efficiency index $e(z, j)$ follows a finite Markov chain.

In step 4, a finite-time dynamic programming problem is to be solved. We use piecewise linear functions in order to approximate the policy functions $c_t(k, m, z, j)$, $k'_t(k, m, z, j)$, $m'_t(k, m, z, j)$, and $l_t(k, m, z, j)$ between grid points. In particular, we solve the Euler functions (15)-(18) for given sequence of the aggregate capital stock K_t , aggregate effective employment N_t , and transfers tr_t .

As the household is born without any assets, his first-period wealth and his real money balances are zero. As a consequence, the value function would take the value $-\infty$ as $m_{1t} = 0$. For computational purposes, therefore, we slightly change the utility function and introduce a small constant ψ into (11), $\tilde{u} = u(c, m + \psi, 1 - l)$.

References

- Auerbach, A.J. and D. Feenberg, 2000, The Significance of Federal Taxes as Automatic Stabilizers, *NBER Working Paper Series*, Working Paper 7662.
- Auerbach, A.J. and L. Kotlikoff, 1995, *Macroeconomics: An Integrated Approach*, South-Western College Publishing, Cincinnati, OH.
- Bach, G.L. and A. Ando, 1957, The Redistributive Effects of Inflation, *Review of Economics and Statistics*, vol. 39, 1-13.
- Bach, G.L. and J.B. Stephenson, 1974, Inflation and the Redistribution of Wealth, *Review of Economics and Statistics*, vol. 56, 1-13.
- Banerjee, A., J. Dolado, J. Galbraith, and D. Hendry, 1993, *Cointegration, Error-Correction and the Econometric Analysis of Non-Stationary Data*, Oxford University Press, Oxford.
- Blinder, A.S. and H.Y. Esaki, 1978, Macroeconomic Activity and Income Distribution in the Postwar United States, *Review of Economics and Statistics*, vol. 60, 143-162.
- Budd, E.C. and D.F. Seiders, 1971, The Impact of Inflation on the Distribution of Income and Wealth, *American Economic Review Papers and Proceedings*, vol. 61, 128-138.
- Bulir, A. and A.-M. Gulde, 1995, Inflation and Income Distribution: Further Evidence on Empirical Links, *International Monetary Fund Working Paper* 95/86.
- Castañeda, A., J. Díaz-Giménez, and J.-V. Ríos-Rull, 1999, Earnings and Wealth Inequality and Income Taxation: Quantifying the Trade-Offs of Switching to a Proportional Income Tax in the US, mimeo.
- Deininger, K. and L. Squire, 1996, A New Data Set Measuring Income Inequality, *World Bank Economic Review*, No. 10, 565-591.
- Díaz-Giménez, J., V. Quadrini, and J.V. Ríos-Rull, 1997, Dimensions of Inequality: Facts on the U.S. Distributions of Earnings, Income, and Wealth, *Federal Reserve Bank of Minneapolis Quarterly Review* 21, 3-21.
- Galli, R. and R. van der Hoeven, 2001, Is Inflation Bad for Income Inequality: The Importance of the Initial Rate of Inflation, *International Labor Organization Employment Paper* 2001/29.
- Gouveia, M. and R.O. Strauss, 1994, Effective Federal Individual Income Tax Functions: An Exploratory Empirical Analysis, *National Tax Journal*, vol. 47(2), 317-39.
- Hansen, G., 1993, The cyclical and secular behavior of the labor input: comparing efficiency units and hours worked, *Journal of Applied Econometrics* 8, 71-80.

- Hodrick, R. and E. Prescott, 1997, Postwar U.S. Business Cycles: An Empirical Investigation, *Journal of Money, Credit and Banking*, vol. 29, 1-16.
- Huggett, M., 1996, Wealth distribution in Life-Cycle Economies, *Journal of Monetary Economics*, vol. 17, 953-69.
- İmrohoroğlu, A, İmrohoroğlu, S., and D.H. Joines, 1998, The Effect of Tax-favored Retirement Accounts on Capital Accumulation, *American Economic Review*, vol. 88, 749-68.
- IRS, Internal Revenue Service, 2003, Selected Historical and Other Data Tables, Department of the Treasury, Washington.
- Prescott, E., 1986, Theory Ahead of Business Cycle Measurement, *Federal Reserve Bank of Minneapolis Quarterly Review*, vol. 10, 9-22.
- Ravn, M.O. and H. Uhlig, 2002, On Adjusting the Hodrick-Prescott Filter for the Frequency of Observations, *Review of Economics and Statistics*, vol. 84, 371-376.
- Romer, C.D. and D.H. Romer , 1998, Monetary Policy and the Well-Being of the Poor, *NBER Working Paper Series*, Working Paper 6793.
- Schultz, P.T., 1969, Secular Trends and Cyclical Behavior of Income Distribution in the United States, *NBER Studies in Income and Wealth*, vol. 33, 663-681.
- Shorrocks, A.F., 1976, Income Mobility and the Markov Assumption, *Economic Journal*, vol. 86, 566-578.
- Stokey, N., J.R. Lucas, and E.C. Prescott, 1989, *Recursive methods in economic dynamics*, Harvard University Press, Cambridge, Ma.
- Tauchen, G., 1986, Finite State Markov-Chain Approximations To Univariate and Vector Autoregressions, *Economics Letters*, vol. 20, 177-81
- Ventura, G., 1999, Flat tax reform: A quantitative exploration, *Journal of Economic Dynamics and Control*, vol. 23, 1425-1458.
- Wolff, E.N., 1979, The Distributional Effects of the 1969-75 Inflation on Holdings of Household Wealth in the United States, *Review of Income and Wealth*, vol. 25, 195-207.

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