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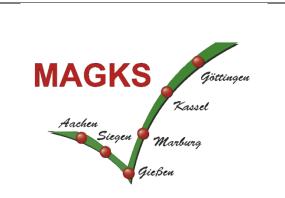Siegen
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A Historical Note on the Beauty Contest

A Historical Note on the Beauty Contest

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Abstract

Alain Ledoux, who was one of over 6,000 chess players taking part in Bühren and Frank´s (2012) online Beauty Contest experiment, turned out to be the forgotten inventor of that game. We reconstruct the birth of the Beauty Contest. In section 1 of our note, its first two authors outline the history of the game that metamorphosed into the famous guessing game experiment which was first run in the lab by Rosemarie Nagel. In section 2, Rosemarie Nagel adds further remarks and thoughts about the development of the experimental Beauty Contest.

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1. The History of the Beauty Contest Experiment

Rosemarie Nagel (1993, 1995) rightfully became known for the Beauty Contest experiment that she initially called guessing game. Ho, Camerer and Weigelt (1996, 1998) were the first to call this guessing game "p-Beauty Contest", inspired by Nagel´s reference in 1995 to Keynes' (1936, p. 156) famous comparison of stock market investments and newspaper beauty contests. The Beauty Contest is an import tool as it provides researchers with a clear and feasible concept of "depth of reasoning". It is Nagel's achievement to have discovered this potential of the game, she does not claim to be its inventor - in the initial footnote (Nagel, 1995, p. 1313) she writes: "I learned about the guessing game in a game-theory class given by Roger Guesnerie, who used the game as a demonstration experiment." Probably Guesnerie's source was Hervé Moulin (1986) who is the first who published this game in a social science context. In his textbook, the game was called "Guess the average", with each player picking an integer between 1 and 999. The game served as the introductory example to the chapter on successive elimination of dominated strategies. Moulin on his part was inspired by a source that had slipped his memory when later, in the nineties, consulted by Rosemarie Nagel. Our recent call for participation in an online Beauty Contest experiment (Bühren and Frank 2012) finally unearthed Moulin's source.

As a reminder: Participants in Nagel's first experiments (as in Guesnerie's class) were asked to guess a (real) number between 0 and 100, the winning number being the one that comes closest to a share p of the average. In Nagel (1995), p takes the values 1/2, 2/3 and 4/3, with p = 2/3 being most popular in later replications and variants of the experiment.

In 1981, the French magazine "Jeux & Stratégie", a popular magazine devoted mainly to strategic board games, but also covering card games and mathematical games, arranged a big readers' competition consisting of mathematical puzzles but also problems from games such as chess, bridge and go. Ledoux (1981) reports on almost 15,000 participants, 4,078 of them being *ex aequo*, hence the winner had to be decided in a playoff. All first round winners received a letter with new puzzles, and to avoid another round with multiple winners, chief editor Alain Ledoux invented in the last question of this letter what is today known as the Beauty Contest (the name given to it by Ledoux, according to an email to us from July 9th, 2009, was "psycho-statistique", although this does not appear to have appeared in print). Readers were asked to state an integer between 1 and 1,000,000,000, the wining number being the one closest to two third of the average! The average turned out to be

134,822,738.26, two third of this being 89,881,825.51. This is 8.99 percent of the maximum number, markedly less than what is typically found in first rounds of Beauty Contest experiments (Bosch-Domènech, Montalvo, Nagel and Satorra, 2002). However, as explained above, the participants had been pre-selected, having solved a series of puzzles in the first round of the contest, and they knew that everyone else was pre-selected. Both facts should have resulted in the pretty high depth of reasoning. The large interval (with 1,000,000,000 instead of 100 as the upper bound) could also have played a role - an untested hypothesis suggested to us by Rosemarie Nagel.

In 1983, Jeux & Stratégie held another readers' contest. There was a reference to the first experiment but not to its result. However, some readers might have remembered or looked up the result of the previous round. Again, the Beauty Contest was used as a tie break between equal players on the previous questions - 2898 participants if or reading of Ledoux (1983) is correct. The target number in 1983 (two third of the average guess) was 67,329,453, or 6.73 percent of the maximum number.

Our preliminary conclusion is that Alain Ledoux should be given some credit for starting this fascinating line of research, though no one is to blame for the fact that researchers have previously overlooked him. He did not even sign the articles in Jeux & Stratégie with his name, and not a single public or scientific library in Germany holds this journal. We would be glad to receive hints on similar cases already known; the best one that occurred to us so far is the balanced budget multiplier, typically credited to Haavelmo, but see Gelting (1941), written in a language alien to almost any economist.[1]

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[1] See also Al Roth in his blog on "**Nagel's guessing/beauty contest game: a famous experiment in game theory**" where he quotes from Roth and Sotomayor (1990, p.170): "What is important about Columbus' discovery of America is not that it was the first, but that it was the last. After Columbus, America was never lost again."

2. Some Further Remarks by Rosemarie Nagel[2]

1. In November 1990 in the LSE Tore Ellingsen presented a one shot guessing game in his master student IO class. I chose 22, according to 50*2/3*2/3. I did not further think about this game.

2. Shortly thereafter I saw the game again in Gueneries' Phd game theory class, like some other students who were also in Tore's class. I chose a number a bit lower than in the other class and won. Then Guenerie asked us to play again. And again I won. I also saw the choices and saw some numbers near and at 33 and 22. I asked Guenerie for the data set and analyzed it, and I also did a pilot in LSE. …. I find this important to add because it shows that sometimes you need to have been your own subject to see the beauty of some idea. Remember, the game was around for some years, but nobody thought it was interesting to do an experiment. First of all at that time grade students were not interested/educated in doing experimental economics. And the theorists only saw that behaviour is not in equilibrium, which is of course trivial. I needed two inputs of classes to see its beauty. At the time I was already a researcher-phd student in experimental economics and searching for a topic far away from ultimatum games which I had done in my first paper. Guenerie used this game as a demonstration experiment to show that rationalizability doesn't work in this game while I used this game to test the $50*p^n$ model, which I had actually used in Tore Ellingsen's class. However, I needed this second class by Guenerie to appreciate the game.

3. One Phd student, Klaus Kultti, like me in LSE in 1991, now Helsinki University, pointed out that the game (maybe also my reasoning process) is due to Keynes beauty contest.

4. Reinhard Selten, my supervisor, was against the name beauty contest as Keynes´ contest has multiple equilibria and so we named it guessing game. (John Duffy insisted to call it Keynes beauty contest in Duffy and Nagel (EJ 1997)), which indeed is also correct since it is just a special case with the parameter equal 1 (1*average).

5. In Pittsburgh in 1995 Oliver Schulte a graduate student in Computer science and philosophy in Carnegie Mellon (now computer science prof.) found the guess the average game in Moulin's book which Oliver used for teaching purposes.

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[2] See also Coricelli and Nagel (2010) for a personal account on the guessing game history.

6. I saw in 1995 in a public choice conference (I think) Herve Moulin and told him that I had done experiments in his game. He then referred me to *Pour la Science* (French version of Scientific American) as his original source, which now actually turned out to be Jeux & Stratégie.

Now finally the game has found his founding father, who, however, saw no special interest in it besides providing a tie breaker.

References

Bosch-Domènech, Antoni, José G. Montalvo, Rosemarie Nagel and Albert Satorra (2002), One, Two, (Three), Infinity, ... : Newspaper and Lab Beauty-Contest Experiments, American Economic Review 92, 1687-1701

Bühren, C. and B. Frank (2012), Chess Players' Performance Beyond 64 Squares: A Case Study on the Limitations of Cognitive Abilities Transfer, Talent Development and Excellence, forthcoming.

Coricelli, Giorgio and Rosemarie Nagel (2010), Walking with Reinhard Selten and the Guessing Game: From the Origin to the Brain of the Guessing Game, in The Selten School of Behavioral Economics A Collection of Essays in Honor of Reinhard Selten Ockenfels, Axel; Sadrieh, Abdolkarim (Eds.) 1st Edition, 2010, XV, Springer Verlag

Duffy, John and Rosemarie Nagel (1997), On the Robustness of Behaviour in Experimental 'Beauty Contest' Games, Economic Journal 107, 1684-1700

Gelting, Jørgen (1941), Nogle Bemaerkninger om Finansieringen af offentlig Virksomhed, Nationaløkonomisk Tidsskrift 79, No. 5, 293-299

Ho, Teck-Hua, Colin Camerer and Keith Weigelt (1996), Iterated Dominance and Iterated Best-Response in Experimental p-Beauty Contests, Social Science Working Paper 974, California Institute of Technology

Ho, Teck-Hua, Colin Camerer and Keith Weigelt (1998), Iterated Dominance and Iterated Best-Response in Experimental p-Beauty Contests, American Economic Review 88, No. 4, 947-969

Keynes, John M. (1936), The General Theory of Interest, Employment and Money, London: Macmillan

[Ledoux, Alain] (1981), Concours résultats complets. Les victimes se sont plu à jouer le 14 d'atout, Jeux & Stratégie 2, No. 10, 10-11

[Ledoux, Alain] (1983), Concours J&S 83. On a retrouvé la stanta barbara!, Jeux & Stratégie 4, No. 22, 12-14

Moulin, Hervé (1986), Game Theory for Social Sciences, New York University Press

Nagel, Rosemarie (1993), Experimental Results on Interactive Competitive Guessing, Discussion Paper No. B-236, University of Bonn, April 1993

Nagel, Rosemarie (1995), Unraveling in Guessing Games: An Experimental Study, American Economic Review 85, 1313-1326

Roth, Alvin E. and Marilda A. Oliveira Sotomayor (1990), Two-Sided Matching. A Study in Game-Theoretic Modeling and Analysis, Cambridge University Press

Roth, Alvin E. (2009), Nagel's Guessing/Beauty Contest Game: a Famous Experiment in Game Theory, http://marketdesigner.blogspot.com/2009/09/nagels-guessingbeauty-contest-game.html, retrieved February 20th, 2012