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The Incentive for Vertical Integration

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#### Abstract

This paper evaluates the incentive of firms to vertically integrate in a simple 2X2 Bertrand model of two substitutes that are each comprised of two complementary components. It confirms that all prices fall as a result of a vertical merger. Further, we find that, when the composite goods are poor substitutes, producers of complementary components are better off after integration. Thus, at equilibrium, each pair of complementary goods is produced by a single firm (parallel vertical integration). In contrast, when the composite goods are close substitutes, vertical integration reduces profits of the merging firms and is therefore undesirable. Thus, at equilibrium, all four products are produced by independent firms (independent ownership). The reason for the change in the direction of the incentive to merge is that, as the composite goods become closer substitutes, competition between them reduces prices (in comparison to full monopoly) thereby eliminating the usefulness of a vertical merger in accomplishing the same price effect. We also find that, for intermediate levels of substitution, firms producing complementary components prefer to merge only if the substitute good is produced by an integrated firm. Thus, for intermediate levels of substitution, both parallel vertical integration and independent ownership are equilibria. When the demand system is symmetric, total surplus is higher in parallel vertical integration, for all degrees of substitution among the products, even for the case when the goods are close substitutes and parallel vertical integration is not the equilibrium outcome. Thus, the market provides less vertical integration than is optimal from a social surplus maximizing point of view.

Key words: Mergers, vertical integration

JEL Classification: L1, D4

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### The Incentive for Vertical Integration

#### 1. Introduction

This paper evaluates the incentive of firms to vertically integrate in a simple setting. Cournot (1838) considered the case of two firms that produce complementary components, and each is a price-setting monopolist in its product line. He showed that each of them has an incentive to integrate vertically and become a single monopolist, earning higher profits. In the dual to his well-known quantity-setting game, Cournot showed and that the integrated monopolist has a lower price than the sum of the prices of two price-setting independent firms. His results were essentially based on the fact that, in a non-cooperative framework, each of two vertically related firms ignores the fact that the other one is also collecting a markup.<sup>1</sup> Thus, duopoly prices include two markups while a monopolist charges a single markup, higher than each of the markups of the duopolists, but lower than their sum.

How do these results fare in the presence of imperfect competition? The reduction of price resulting from vertical integration has been the subject of much discussion, especially in the context of the possibility or lack of substitution in the technology that combines the components.<sup>2</sup> The incentive for vertical integration has received relatively less attention. This paper will focus on the incentives for vertical mergers in a market where two composite goods are substitutes to each other.

The formulation of this paper is conceptually simple. I start with the model of Cournot where two complementary components are combined in fixed proportions to produce a composite good. I introduce a second composite good comprised of two new complementary components. I then vary the degree of substitution between the two composite goods and assess the incentive for vertical mergers. As long as the two composite goods are distant substitutes, by continuity, the result of Cournot must continue to hold: vertical integration of the components of one of the composite goods results in a lower price of that good and in higher profits.<sup>3</sup> As the composite goods become closer substitutes, I show that prices still fall as a result of a vertical merger. However, I also show that, when the composite goods are relatively close substitutes, a vertical merger results in a reduction of the total profits of the merged entities, and therefore it is undesirable to the merging firms.

Why does the incentive to merge vertically change as the degree of substitution changes, and in particular why are vertical mergers unprofitable in the presence of close substitutes? To give an intuitive answer to this question, we consider four ownership structures, *independent ownership*,

<sup>&</sup>lt;sup>1</sup> Economists typically use the term "double marginalization for the existence of two margins in complementary duopoly resulting in a higher price in duopoly than monopoly.

<sup>&</sup>lt;sup>2</sup> See, for example, Schmalensee (1973), Greenhut and Ohta (1979), and Salinger (1988, 1989), among others.

 $<sup>^{3}</sup>$  Of course this result has to be slightly qualified to make sure that the increase in price of composite good 1 is sustained in the presence of a substitute. Further, it is of interest to observe the effects of vertical integration on the price of the substitute composite good.

where each of the four components is produced by a separate firm; *partial vertical integration*, where a single firm produces the two components that comprise the first composite good, while the two components of the second composite good are each produced by separate firms; *parallel vertical integration*, where for each composite good, the pair of components comprising it are produced by the same firm; and *joint ownership*, where all components are produced by the same firm. A merger between one of the pairs of firms that produce complementary components changes the market structure from independent ownership to partial vertical integration. A further merger between the two firms that produce the other two complementary components changes the market structure from partial vertical integration to parallel vertical integration. From the point of view of the vertically integrated firm, Cournot's world of a single composite good is identical to our setting with zero substitution among the two composite goods, since, for zero substitution, the outcomes of partial vertical integration, parallel vertical integration, and joint ownership coincide.

The most important effect of a vertical merger is a reduction of all prices because of the elimination of double marginalization. When there is zero (or very weak) substitution between the composite goods, the reduction in price is desirable to the merged firms because it leads them away from the distortion of double marginalization and into full (or almost full) monopoly profits. However, when the composite goods are closer substitutes, the price reduction from the equilibrium prices of independent ownership is not necessarily desirable to the merging firms. This is because, when the composite goods are close substitutes, competition in the composite goods market drives prices under independent ownership below the prices of joint ownership. A merger that changes market structure from independent ownership to partial vertical integration reduces the prices even further, again *below* the prices of joint ownership. Thus, when the composite goods are close substitutes, the major effect of the merger in reducing the prices of the merging firms (because of the elimination of double marginalization) is detrimental to the merging firm, which instead would like to find a way to increase prices. It follows that when the composite goods are close enough substitutes, independent firms producing complements prefer not to merge. Thus, this argument shows that as the composite goods become closer substitutes, competition between them reduces prices (in comparison to joint ownership) thereby eliminating the usefulness of a vertical merger in accomplishing the same price effect.<sup>4</sup> A similar argument shows that the remaining independent firms under partial vertical integration would like to stay independent if the composite goods are sufficiently close substitutes.

The rest of the paper is organized as follows. Section 2 presents the basic model. Section 3 presents the equilibria in the various ownership structures. Section 4 discusses the individual incentive of firms to integrate. This section contains the essential comparisons of prices and profits across ownership structures. Section 5 defines the equilibrium ownership structures in the full game. Section 6 presents concluding remarks.

<sup>&</sup>lt;sup>4</sup> Our setting has firms choosing their prices simultaneously. Our general results also hold when prices are chosen sequentially, as for example when one of the firms chooses its price after the price for the complementary good has been disclosed.

#### 2. <u>The Model</u>

Let there be two types of goods, A and B, which are complementary to each other. Let there be two varieties of each type of good,  $A_1$ ,  $A_2$ ,  $B_1$  and  $B_2$ .  $A_i$  is combinable with  $B_i$  to form composite good  $A_iB_i$ . Thus, consumers demand composite goods  $A_1B_1$  and  $A_2B_2$  that are assumed to be substitutes.

We consider four possible market structures. In the first market structure (*independent* ownership, "I"), there are four independent firms, each producing one of the four components. In the second market structure (*partial vertical integration*, "PVI"), components  $A_i$  and  $B_i$  are produced by the same firm (i = 1 or 2), while components  $A_j$  and  $B_j$  (j = 1 or 2;  $j \neq i$ ) are each produced by an independent firm. In the third market structure (*parallel vertical integration*, "PLVI"), components  $A_1$  and  $B_1$  are produced by the same firm (firm 1), and components  $A_2$  and  $B_2$  are produced by the same firm (firm 2). In the fourth (reference) market structure (*joint ownership*, "J"), all components are produced by the same firm. Figure 1 shows all these market structures. Products contained in the same box are sold by the same firm. Since we want to focus on vertical mergers, we do not consider other ownership structures, where a single firm controls one component of each composite good.

We model competition as a two-stage game. Firms choose the degree of integration in stage 1 by deciding if they will merge, while prices are chosen in stage 2. We seek subgame-perfect equilibria.

#### 3. <u>Equilibria in the Price Games</u>

#### 3.1 Independent Ownership

We first find all non-cooperative equilibria in price subgames for every ownership structure. In the regime of *independent ownership* (I), each of the four components is provided by a different firm. Firm  $A_i$ , i = 1, 2, sells component  $A_i$  at price  $p_i$ , and firm  $B_j$ , j = 1, 2, sells component  $B_j$  at price  $q_j$ . Thus, composite good  $A_1B_1$  is sold at  $p_1 + q_1$ , and composite good  $A_2B_2$  is sold at  $p_2 + q_2$ . Let a single consumer have a quadratic utility function in  $A_1B_1$  and  $A_2B_2$  which is separable in the outside good  $D_0$ , *i.e.*,

$$U(D_0, D_1, D_2) = D_0 + \alpha_1 D_1 + \alpha_2 D_2 - (\beta_1 D_1^2 + \beta_2 D_2^2 + 2\gamma D_1 D_2)/2.$$
(1)

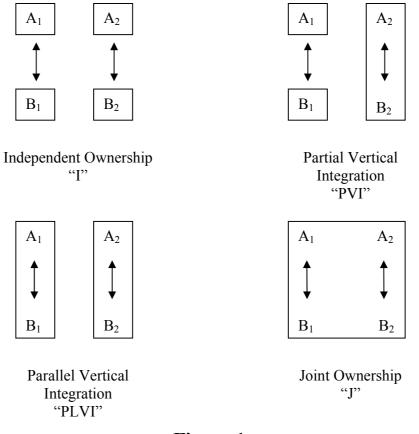
with  $\alpha_1, \alpha_2, \beta_1, \beta_2, \gamma > 0$ . Maximization of utility U(D<sub>0</sub>, D<sub>1</sub>, D<sub>2</sub>) subject to the budget constraint D<sub>0</sub> + (p<sub>1</sub> + q<sub>1</sub>)D<sub>1</sub> + (p<sub>2</sub> + q<sub>2</sub>)D<sub>2</sub> = I yields linear inverse demands

$$p_1 + q_1 = \alpha_1 - \beta_1 D_1 - \gamma D_2, \quad p_2 + q_2 = \alpha_2 - \gamma D_1 - \beta_2 D_2.$$
 (2)

As long as  $\beta_1\beta_2 \neq \gamma^2$ , this system can be inverted to give the demand equations for A<sub>1</sub>B<sub>1</sub> and A<sub>2</sub>B<sub>2</sub>

$$D_1 = a_1 - b_1(p_1 + q_1) + c(p_2 + q_2), D_2 = a_2 + c(p_1 + q_1) - b_2(p_2 + q_2).$$
 (3)

#### **Ownership Structures**





with  $a_1 = (\alpha_1\beta_2 - \alpha_2\gamma)/(\beta_1\beta_2 - \gamma^2)$ ,  $a_2 = (\alpha_2\beta_1 - \alpha_1\gamma)/(\beta_1\beta_2 - \gamma^2)$ ,  $b_1 = \beta_2/(\beta_1\beta_2 - \gamma^2)$ ,  $b_2 = \beta_1/(\beta_1\beta_2 - \gamma^2)$ ,  $c = \gamma/(\beta_1\beta_2 - \gamma^2)$ . The expression  $\sigma = c^2/(b_1b_2) = \gamma^2/(\beta_1\beta_2)$  measures *the degree of substitution* between the two composite goods. It can be shown that  $\sigma = \epsilon_{12}\epsilon_{21}/(\epsilon_{11}\epsilon_{22})$ , where  $\epsilon_{ii}$  is the own elasticity of demand of composite good i and  $\epsilon_{ij}$  is the cross elasticity of demand of good i with respect to changes in the price of good j.<sup>5</sup> Thus, the degree of substitution  $\sigma$  measures the relative size of cross elasticities in comparison with the own elasticity of demand. A zero value for  $\sigma$  means that the two composite goods  $A_1B_1$  and  $A_2B_2$  are independent. Restricting  $b_1$ ,  $b_2$ , and c to positive and finite values implies  $\sigma = \gamma^2/(\beta_1\beta_2) < 1.^6$  Thus, we restrict the degree of substitution  $\sigma$  to lie in the range [0, 1).

<sup>&</sup>lt;sup>5</sup> Since  $\varepsilon_{11} = (\partial D_1 / \partial p_1) / (D_1 / (p_1 + q_1)), \varepsilon_{12} = (\partial D_1 / \partial p_2) / (D_1 / (p_2 + q_2)), \text{ we have } -\varepsilon_{11} / \varepsilon_{12} = b_1 (p_1 + q_1)) / (c(p_2 + q_2)).$ Similarly,  $-\varepsilon_{22} / \varepsilon_{21} = b_2 (p_2 + q_2) / (c(p_1 + q_1)), \text{ so that } \varepsilon_{12} \varepsilon_{21} / (\varepsilon_{11} \varepsilon_{22}) = c^2 / (b_1 b_2) = \gamma^2 / (\beta_1 \beta_2) = \sigma.$ 

At the consumer's optimal choice  $(D_0^*, D_1^*, D_2^*)$ , the realized consumers' surplus is<sup>7</sup>

$$CS = U(D_0^*, D_1^*, D_2^*) = I + (\beta_1 D_1^{*2} + \beta_2 D_2^{*2} + 2\gamma D_1^* D_2^*)/2.$$
(4)

Under the assumption of zero costs, the profit functions are<sup>8</sup>

$$\Pi_{A_1} = p_1 D_1 = p_1 [a_1 - b_1(p_1 + q_1) + c(p_2 + q_2)], \quad \Pi_{B_1} = q_1 D_1 = q_1 [a_1 - b_1(p_1 + q_1) + c(p_2 + q_2)],$$
  
$$\Pi_{A_2} = p_2 D_2 = p_2 [a_2 + c(p_1 + q_1) - b_2(p_2 + q_2)], \quad \Pi_{B_2} = q_2 D_2 = q_2 [a_2 + c(p_1 + q_1) - b_2(p_2 + q_2)].$$
  
(5a,b, c, d)

The solution of the individual firms' profit maximization conditions,<sup>9</sup>  $\partial \Pi_{A_1}/\partial p_1 = \partial \Pi_{B_1}/\partial q_1 = \partial \Pi_{A_2}/\partial p_2 = \partial \Pi_{B_2}/\partial q_2 = 0$ , defines the equilibrium prices and profits:<sup>10</sup>

$$p_{1}^{I} = q_{1}^{I} = (3a_{1}b_{2} + 2a_{2}c)/(9b_{1}b_{2} - 4c^{2}), \quad p_{2}^{I} = q_{2}^{I} = (3a_{2}b_{1} + 2a_{1}c)/(9b_{1}b_{2} - 4c^{2}). \quad (6a,b)$$

$$\Pi_{A_{1}}^{I} = \Pi_{B_{1}}^{I} = b_{1}(3a_{1}b_{2} + 2a_{2}c)^{2}/(9b_{1}b_{2} - 4c^{2})^{2}, \quad \Pi_{A_{2}}^{I} = \Pi_{B_{2}}^{I} = b_{2}(3a_{2}b_{1} + 2a_{1}c)^{2}/(9b_{1}b_{2} - 4c^{2})^{2}. \quad (7a,b)$$

#### 3.2 <u>Partial Vertical Integration</u>

In *partial vertical integration* ("PVI"), components  $A_1$  and  $B_1$  are sold by the same firm, while  $A_2$  and  $B_2$  are each provided independently. Let the price of good  $A_1B_1$  (provided by

<sup>7</sup> From the budget constraint,  $D_0 = I - (p_1 + q_1)D_1 - (p_2 + q_2)D_2 = I - \alpha_1D_1 - \alpha_2D_2 + \beta_1D_1^2 + \beta_2D_2^2 + 2\gamma D_1D_2$ . Substituting in the definition of  $U(D_0, D_1, D_2)$  yields  $CS = U(D_0^*, D_1^*, D_2^*) = I + (\beta_1D_1^{*2} + \beta_2D_2^{*2} + 2\gamma D_1D_2^*)/2$ .

<sup>8</sup> Clearly the same results hold for non-zero but constant marginal costs.

<sup>9</sup> Second order conditions also hold.

<sup>10</sup> In terms of the parameters of the utility function, the equilibrium prices, demand and profits are

$$\begin{split} p_{1}^{I} &= q_{1}^{I} = (3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})/(9\beta_{1}\beta_{2} - 4\gamma^{2}), \quad p_{2}^{I} = q_{2}^{I} = (3\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - 2\alpha_{2}\gamma^{2})/(9\beta_{1}\beta_{2} - 4\gamma^{2}), \\ D_{1}^{I} &= \beta_{2}(3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})/((\beta_{1}\beta_{2} - \gamma^{2})(9\beta_{1}\beta_{2} - 4\gamma^{2})), \quad D_{2}^{I} = \beta_{1}(3\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - 2\alpha_{2}\gamma^{2})/((\beta_{1}\beta_{2} - \gamma^{2})(9\beta_{1}\beta_{2} - 4\gamma^{2})), \\ \Pi_{A_{1}}^{I} &= \Pi_{B_{1}}^{I} = \beta_{2}(3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})^{2}/[(9\beta_{1}\beta_{2} - 4\gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})], \\ \Pi_{A_{2}}^{I} &= \Pi_{B_{2}}^{I} = \beta_{1}(3\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{1}\gamma - 2\alpha_{2}\gamma^{2})^{2}/[(9\beta_{1}\beta_{2} - 4\gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})]. \end{split}$$

<sup>&</sup>lt;sup>6</sup>  $b_1, b_2, c > 0$  requires  $\beta_1\beta_2 - \gamma^2 > 0$ , *i.e.*,  $\sigma = \gamma^2/(\beta_1\beta_2) < 1$ . A slightly stronger restriction,  $b_1 > c$ ,  $b_2 > c$ , (equivalent to  $\beta_1 > \gamma, \beta_2 > \gamma$ ) can be interpreted as "an increase in the price of all differentiated goods reduces the demand for each good." This restriction is commonly used in oligopoly models. To have  $a_1, a_2 > 0$ , we require  $\alpha_1\beta_2 > \alpha_2\gamma$  and  $\alpha_2\beta_1 > \alpha_1\gamma$ .

integrated firm 1) be  $s_1$ . The prices of the two components  $A_2$  and  $B_2$  of the second good are  $p_2$  and  $q_2$  as before. The demand and profit functions are now

 $D_1 = a_1 - b_1s_1 + c(p_2 + q_2), D_2 = a_2 + cs_1 - b_2(p_2 + q_2),$  (8a, b)

$$\Pi_1 = s_1 D_1 = s_1 (a_1 - b_1 s_1 + c(p_2 + q_2)), \tag{9a}$$

$$\Pi_{A_2} = p_2 D_2 = p_2 (a_2 + cs_1 - b_2 (p_2 + q_2)), \quad \Pi_{B_2} = q_2 D_2 = q_2 (a_2 + cs_1 - b_2 (p_2 + q_2)). \quad (9b, c)$$

The solution of the individual firms' profit maximization conditions,<sup>11</sup>  $\partial \Pi_1 / \partial s_1 = \partial \Pi_{A_2} / \partial p_2 =$  $\partial \Pi_{B_2} / \partial q_2 = 0$ , defines the equilibrium prices  $s_1^{PVI}$  for  $A_1B_1$ ,  $p_2^{PVI}$  for  $A_2$ , and  $q_2^{PVI}$  for  $B_2$  as

$$s_1^{PVI} = (3a_1b_2 + 2a_2c)/(6b_1b_2 - 2c^2),$$
 (10a)

$$p_2^{PVI} = q_2^{PVI} = (2a_2b_1 + a_1c)/(6b_1b_2 - 2c^2).$$
(10b)

Note that, if the demands for the two composite goods are equal at equal prices (*i.e.*, if  $a_1 = a_2$  and  $b_1 = b_2$ ), the composite good of the unintegrated firms is sold at a higher price,  $p_2^{PVI} + q_2^{PVI} > s_1^{PVI}$ . This is because the unintegrated firms faces double marginalization.

Equilibrium profits are<sup>12</sup>

$$\Pi_1^{\rm PVI} = b_1 (3a_1b_2 + 2a_2c)^2 / [4(3b_1b_2 - c^2)^2], \qquad (11a)$$

$$\Pi_{A_2}^{PVI} = \Pi_{B_2}^{PVI} = b_2 (2a_2b_1 + a_1c)^2 / [4(3b_1b_2 - c^2)^2].$$
(11b)

#### 3.3 <u>Parallel Vertical Integration</u>

We now consider *parallel vertical integration* ("PLVI"), where each substitute composite good is provided by an integrated firm. Let the price of composite good  $A_iB_i$  (sold by integrated firm i) be  $s_i$ , i = 1, 2. Demand and profit functions are now

$$^{11} \partial \Pi_1 / \partial s_1 = a_1 - 2b_1 s_1 + c(p_2 + q_2) = 0, \ \partial \Pi_{A_2} / \partial p_2 = a_2 + cs_1 - 2b_2 p_2 - b_2 q_2 = 0, \ \partial \Pi_{B_2} / \partial q_2 = a_2 + cs_1 - 2b_2 q_2 - b_2 p_2 = 0$$

<sup>12</sup> In terms of the parameters of the utility function, the equilibrium prices, demand, and profits are

$$\begin{split} s_{1}^{PVI} &= (3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})/[2(3\beta_{1}\beta_{2} - \gamma^{2})], \ p_{2}^{PVI} = q_{2}^{PVI} = (2\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - \alpha_{2}\gamma^{2})/[2(3\beta_{1}\beta_{2} - \gamma^{2})], \\ D_{1}^{PVI} &= \beta_{2}(3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})/(2(\beta_{1}\beta_{2} - \gamma^{2})(3\beta_{1}\beta_{2} - \gamma^{2})), \\ D_{2}^{PVI} &= \beta_{1}(2\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - \alpha_{2}\gamma^{2})/(2(\beta_{1}\beta_{2} - \gamma^{2})(3\beta_{1}\beta_{2} - \gamma^{2})), \\ \Pi_{1}^{PVI} &= \beta_{2}(3\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - 2\alpha_{1}\gamma^{2})^{2}/[4(\beta_{1}\beta_{2} - \gamma^{2})(3\beta_{1}\beta_{2} - \gamma^{2})^{2}], \\ \Pi_{A_{2}}^{PVI} &= \Pi_{B_{2}}^{PVI} = \beta_{1}(2\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - \alpha_{2}\gamma^{2})^{2}/[4(\beta_{1}\beta_{2} - \gamma^{2})(3\beta_{1}\beta_{2} - \gamma^{2})^{2}]. \end{split}$$

$$D_1 = a_1 - b_1 s_1 + c s_2, D_2 = a_2 + c s_1 - b_2 s_2, \Pi_1 = s_1 D_1, \Pi_2 = s_2 D_2.$$
 (12a, b, c, d)

The solution of the individual profit maximization conditions,<sup>13</sup>  $\partial \Pi_1 / \partial s_1 = \partial \Pi_2 / \partial s_2 = 0$ , defines the equilibrium prices and profits as<sup>14</sup>

$$s_1^{PLVI} = (2a_1b_2 + a_2c)/(4b_1b_2 - c^2), \ s_2^{PLVI} = (2a_2b_1 + a_1c)/(4b_1b_2 - c^2),$$
 (13a,b)

$$\Pi_1^{\text{PLVI}} = b_1 (2a_1b_2 + a_2c)^2 / (4b_1b_2 - c^2)^2, \quad \Pi_2^{\text{PLVI}} = b_2 (2a_2b_1 + a_1c)^2 / (4b_1b_2 - c^2)^2. \quad (13c,d)$$

#### 3.4 Joint Ownership

In *joint ownership* ("J"), all products are sold by the same firm. Its profit function is

$$\Pi = \Pi_1 + \Pi_2 = s_1 D_1 + s_2 D_2 = s_1 (a_1 - b_1 s_1 + c s_2) + s_2 (a_2 + c s_1 - b_2 s_2), \tag{14}$$

The solution of first order conditions,  $\partial \Pi / \partial s_1 = \partial \Pi / \partial s_2 = 0$ , defines the equilibrium prices

$$s_1^{J} = (a_1b_2 + a_2c)/[2(b_1b_2 - c^2)], \ s_2^{J} = (a_2b_1 + a_1c)/[2(b_1b_2 - c^2)].$$
 (15a, b)

Equilibrium profits from  $A_1B_1$  and  $A_2B_2$  are

$$\Pi_1^{J} = [a_1(a_1b_2 + a_2c)]/[4(b_1b_2 - c^2)], \ \Pi_2^{J} = [a_2(a_2b_1 + a_1c)]/[4(b_1b_2 - c^2)].$$
(16)

so that the total profits of the monopolist are<sup>15</sup>

$$\Pi^{J} = \Pi_{1}^{J} + \Pi_{2}^{J} = (a_{1}^{2}b_{2} + a_{2}^{2}b_{1} + 2a_{2}a_{1}c)]/[4(b_{1}b_{2} - c^{2})].$$
(17)

# 4. <u>The Choice to Integrate Vertically</u> 4.1 <u>Mergers that Lead from Independent Ownership to Partial Vertical Integration</u>

$$s_1^{PLVI} = (2\alpha_1\beta_1\beta_2 - \alpha_2\beta_1\gamma - \alpha_1\gamma^2)/(4\beta_1\beta_2 - \gamma^2), \\ s_2^{PLVI} = (2\alpha_2\beta_1\beta_2 - \alpha_1\beta_2\gamma - \alpha_2\gamma^2)/(4\beta_1\beta_2 - \gamma^2),$$

$$D_{1}^{PLVI} = \beta_{2}(2\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - \alpha_{1}\gamma^{2})/((\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})), \quad D_{2}^{PLVI} = \beta_{1}(2\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - \alpha_{2}\gamma^{2})/((\beta_{1}\beta_{2} - \gamma_{2})(4\beta_{1}\beta_{2} - \gamma^{2})),$$

$$\Pi_{1}^{PLV1} = \beta_{2}(2\alpha_{1}\beta_{1}\beta_{2} - \alpha_{2}\beta_{1}\gamma - \alpha_{1}\gamma^{2})^{2}/[(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})^{2}], \quad \Pi_{2}^{PLV1} = \beta_{1}(2\alpha_{2}\beta_{1}\beta_{2} - \alpha_{1}\beta_{2}\gamma - \alpha_{2}\gamma^{2})^{2}/[(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})^{2}].$$

<sup>15</sup> In terms of the parameters of the utility function, the equilibrium prices and profits are  $s_1^J = \alpha_1/2$ ,  $s_2^J = \alpha_2/2$ ,  $\Pi^J = (\alpha_2^2\beta_1 + \alpha_1^2\beta_2 - 2\alpha_1\alpha_2\gamma)/[4(\beta_1\beta_2 - \gamma^2)]$ .

<sup>&</sup>lt;sup>13</sup> They are  $\partial \Pi_1 / \partial s_1 = a_1 - 2b_1s_1 + cs_2 = 0$  (as in parallel vertical integration), and  $\partial \Pi_2 / \partial s_2 = a_2 + cs_1 - 2b_2s_2 = 0$ .

<sup>&</sup>lt;sup>14</sup> In terms of the parameters of the utility function, the equilibrium prices, demand, and profits are

We are interested in the comparison of prices and profits across regimes. We are most interested in the comparisons of profits or losses from mergers that lead to vertical integration. Starting with "independent ownership" where all components are produced by independent firms, we consider a merger of firms  $A_1$  and  $B_1$ . Such a merger will result in "partial vertical integration." We first compare prices. All prices fall as a result of the merger,<sup>16</sup>

$$s_1^{PVI} < p_1^I + q_1^I, \ p_2^{PVI} < p_2^I.$$
 (18)

The reduction in price is a direct effect of the elimination of double marginalization and is true under weak restrictions on general demand functions. Keeping for the moment the prices of firms  $A_2$  and  $B_2$  constant, we note that  $\partial \Pi_1^{PVI}/\partial s_1 = \partial \Pi_{A_1}^I/\partial p_1 + \partial \Pi_{B_1}^I/\partial p_1 = \partial \Pi_{B_1}^I/\partial p_1 < 0$ , when evaluated at the equilibrium prices of independent ownership, as long as  $A_1$  and  $B_1$  are complements. Given the concavity of  $\Pi_1^{PVI}$ , the integrated firm chooses a smaller price for  $A_1B_1$  (as a response to  $p_2 + q_2$ ) than the sum of the prices of its components chosen by independent firms in independent ownership. Since the composite goods are strategic complements, the competitors reduce prices in response.<sup>17,18</sup>

**Proposition 1:** Starting with independent ownership, a vertical merger of firms  $A_1$  and  $B_1$  (or  $A_2$  and  $B_2$ ), leading to partial vertical integration, reduces all prices.

We now compare the profits of the firms that merge as we move from independent ownership to partial vertical integration. The incentive for firms  $A_1$  and  $B_1$  to merge is measured by  $\Pi_1^{PVI} - (\Pi_{A_1}^I + \Pi_{B_1}^I)$ . We find that this is negative when the composite goods are close substitutes: for  $\sigma < 0.44$ ,<sup>19</sup> where  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2$  is the degree of substitution between the composite goods. Thus, when the composite goods are not close substitutes, it pays for firms  $A_1$  and  $B_1$  to merge (given that  $A_2$  and  $B_2$  are independent). The firms that did not participate in the merger are *always* made worse off as a result of the merger,  $\Pi_{A_2}^{PVI} < \Pi_{A_2}^i$ ,  $\Pi_{B_2}^{PVI} < \Pi_{B_2}^i$ .

<sup>&</sup>lt;sup>17</sup> The reduction in the prices of  $A_2$  and  $B_2$  has an additional dampening effect on  $s_1$ .

<sup>&</sup>lt;sup>18</sup> In this model, hybrid composite goods  $A_iB_j$ ,  $i \neq j$ , do not exist, and therefore the mergers considered have only vertical effects. This is in contrast with Economides and Salop (1992) where such "vertical" mergers have both horizontal and vertical effects.

<sup>&</sup>lt;sup>19</sup>  $(\Pi_{A_1}^{I} + \Pi_{B_1}^{I}) - \Pi_1^{PVI} = b_1(24b_1b_2c^2 - 8c^4 - 9b_1^{-2}b_2^{-2})(3a_1b_2 + 2a_2c)^2/[4(9b_1b_2 - 4c^2)^2(3b_1b_2 - c^2)^2]$ . In this expression, all terms are positive except for the term in the first set of parentheses. This term can be written as  $24b_1b_2c^2 - 8c^4 - 9b_1^{-2}b_2^{-2} = -(b_1b_2)^2(8\sigma^2 - 24\sigma + 9) = 8(b_1b_2)^2(2.56 - \sigma)(\sigma - 0.44)$ , where  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2$ . Since  $0 \le \sigma < 1$ , it follows that  $\Pi^i_{A_1} + \Pi_{B_1}^i < \Pi_{A_1}^{A_1}$  for relatively small  $\sigma, \sigma < 0.44$ .

<sup>&</sup>lt;sup>20</sup>  $\Pi_{A_2}^{I} - \Pi_{A_2}^{PVI} = \{b_1b_2c(3a_1b_2 + 2a_2c)[a_2b_1(36b_1b_2 - 14c^2) + a_1c(21b_1b_2 - 8c^2)]\}/[4(9b_1b_2 - 4c^2)^2(3b_1b_2 - c^2)^2] > 0$ , since  $b_1b_2 > c^2$ , and similarly for firm B<sub>2</sub>.

**<u>Proposition 2</u>**: Starting with independent ownership, firms  $A_1$  and  $B_1$  will find a merger with each other to be profitable if and only if the composite goods  $A_1B_1$  and  $A_2B_2$  are not close substitute, that is, iff  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2 < 0.44$ . Firms  $A_2$  and  $B_2$  are always made worse off as a result of the above merger.

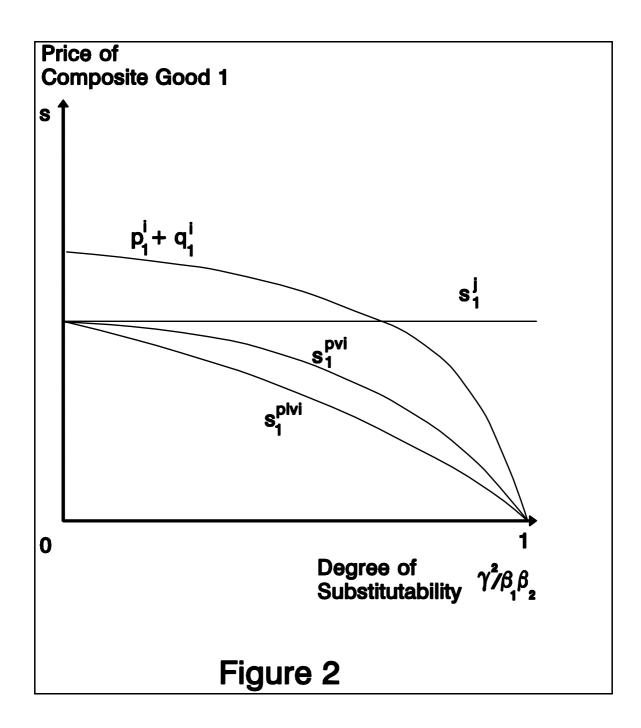
To understand these results, we need to elaborate on the effects of the merger on prices. Figure 2 shows the equilibrium price for composite good 1 as a function of the degree of substitution  $\sigma = \gamma^2 / \beta_1 \beta_2$  for independent ownership, partial vertical integration, parallel vertical integration, and joint ownership. The merger causes the composite price to jump from the "I" line to the "PVI" line. For independent composite goods, *i.e.*, for  $\sigma = 0$ ,  $s_1^J = s_1^{PVI} = s_1^{PLVI}$ . Therefore at  $\sigma = 0$  (and for small  $\sigma$ ),  $p_1^I + q_1^I > s_1^J$ . As the degree of substitution  $\sigma$  increases, competition depresses the composite price in independent ownership in comparison with joint ownership. Thus, for high enough  $\sigma$ ,  $p_1^I + q_1^I < s_1^J$ . Thus, the reduction in the composite price resulting from the merger, although beneficial for small  $\sigma$  because it brings the composite price in joint ownership. When the composite goods are close substitutes (large  $\sigma$ ), firms A<sub>2</sub> and B<sub>2</sub> are significantly disadvantaged as a result of the merger of their rivals A<sub>1</sub> and B<sub>1</sub>. Not only do their prices fall, but also the quantity they produce falls as seen below.

Consumers' surplus will rise as long as both quantities increase. Because the composite goods are substitutes, there is no guarantee that a reduction in the price of both goods will reduce the quantities sold of both. It can be shown that the equilibrium demand changes in opposite directions as the market structure changes from independent ownership to partial vertical integration. Despite the reduction in both prices as a result of the merger, the quantity of the firms that remain independent falls, while the quantity of the merging firms increases.<sup>21</sup> Therefore, we cannot use a general rule for surplus comparisons, and we have to rely on specific calculations. In the case of symmetric demand, defined by  $\alpha_1 = \alpha_2 = \alpha$ ,  $\beta_1 = \beta_2 = \beta$ , consumers' surplus rises as we switch from independent ownership to partial vertical integration.<sup>22</sup> Total welfare, TS = CS +  $\Sigma_i \Pi_i$ , also increases for a very wide range of values of the parameters.<sup>23</sup>

<sup>&</sup>lt;sup>21</sup> To see this, note that the demand differences are  $D_1^{PVI} - D_1^I = \Phi\beta_2(3\beta_1\beta_2 - 2\gamma^2)/[2(\beta_1\beta_2 - \gamma^2)(3\beta_1\beta_2 - \gamma^2)(9\beta_1\beta_2 - 4\gamma^2)]$ ,  $D_2^{PVI} - D_2^I = -\Phi\beta_1\beta_2\gamma/[2(\beta_1\beta_2 - \gamma^2)(3\beta_1\beta_2 - \gamma^2)(9\beta_1\beta_2 - 4\gamma^2)]$ , where  $\Phi = \beta_1(\alpha_1\beta_2 - \alpha_2\gamma) + 2\alpha_1(\beta_1\beta_2 - \gamma^2)$ . All terms in parenthesis are positive in the relevant range because  $\sigma = \gamma^2/\beta_1\beta_2 < 1$  and  $\alpha_1\beta_2 - \alpha_2\gamma = a_1(\beta_1\beta_2 - \gamma^2)$  where  $a_1 > 0$  is the intercept of the demand for firm 1. Therefore,  $\Phi > 0$ , and  $D_1^{PVI} > D_1^I$ ,  $D_2^{PVI} < D_2^I$ .

<sup>&</sup>lt;sup>22</sup>  $CS^{PVI} - CS^{I} = \alpha^{2}(1.59 - y)(1 - y)(1.23 + y)(2.86 + y)/[8(1 + y)(3 - 2y)^{2}(3 - y^{2})^{2}\beta]$ , where  $y = \sqrt{\sigma} = \gamma/\beta$ . Therefore  $CS^{PVI} > CS^{I}$  for all  $y \in [0, 1)$ .

 $<sup>^{23} \</sup> TS^{PVI} - TS^{I} = \alpha^{2}(1 - y)(1.62 - y)(0.98 - y)(2.47 + 3.1y + y^{2})/[8(1 + y)(3 - 2y)^{2}(3 - y^{2})^{2}\beta], \ \text{where} \ y = \sqrt{\sigma} = \gamma/\beta.$  Therefore  $TS^{PVI} > TS^{I}$  for  $0 < \sigma < 0.98$  and  $TS^{PVI} < TS^{I}$  for  $0.98 < \sigma < 1.$ 



#### 4.2 <u>Mergers that Lead from Partial Vertical Integration to Parallel Vertical Integration</u>

Starting from "partial vertical integration" (*i.e.*, integration of  $A_1$  and  $B_1$ ) consider a merger between  $A_2$  and  $B_2$  that leads to parallel vertical integration. All prices of composite goods decrease

as a result of the integration of firms A<sub>2</sub> and B<sub>2</sub>:  $s_1^{PVI} > s_1^{PLVI}$ ,  $p_2^{PVI} + q_2^{PVI} > s_2^{PLVI}$ .

**Proposition 3:** Starting with partial vertical integration of firms  $A_1$  and  $B_1$ , a vertical merger of firms  $A_2$  and  $B_2$  leading to parallel vertical integration reduces all prices.

Total profits of the firms that integrate are higher after integration when the composite goods are not close substitutes,  $\Pi_2^{PLVI} > \Pi_{A_2}^{PVI} + \Pi_{B_2}^{PVI}$  if and only if  $\sigma < 0.59$ , where  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2$  measures the degree of substitution between the composite goods.<sup>25</sup> Thus, when the composite goods are not close substitutes, it pays for firms  $A_2$  and  $B_2$  to merge (given that  $A_1$  and  $B_1$  are already merged). Profits of the firm that remains integrated fall as a result of the integration of the competitors,  $\Pi_1^{PLVI} < \Pi_1^{PVI \ 26}$ 

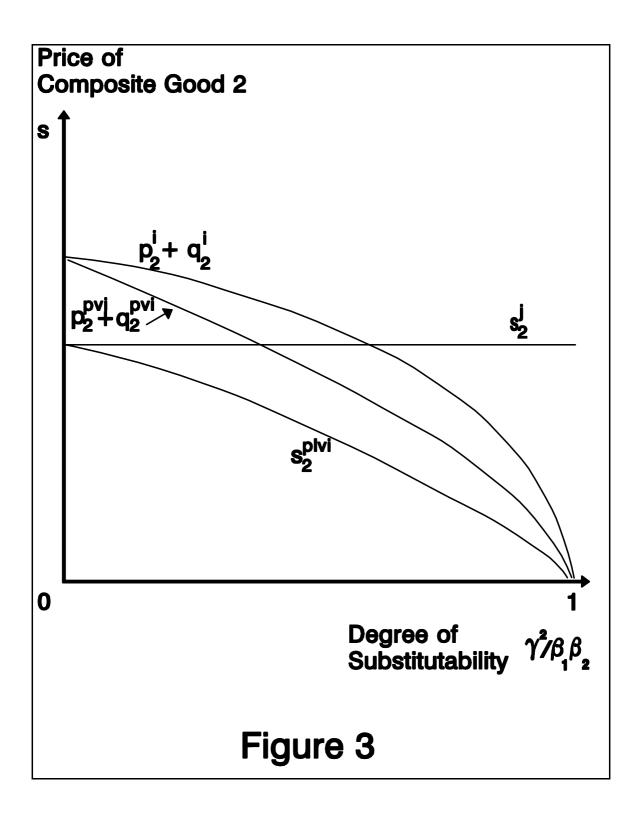
**Proposition 4:** Starting with partial vertical integration of firms  $A_1$  and  $B_1$ , firms  $A_2$  and  $B_2$  find a merger with each other profitable if and only if the composite goods  $A_1B_1$  and  $A_2B_2$  are not close substitutes, that is, iff  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2 < 0.59$ . The firm that is already integrated is made worse off as a result of the subsequent merger.

Again, to understand the incentives for the vertical merger we need to look carefully at the price relationships. Figure 3 shows the equilibrium prices for composite good 2 as functions of the degree of substitution  $\sigma$  for independent ownership, partial vertical integration, parallel vertical integration, and joint ownership. For  $\sigma = 0$ ,  $s_2^i$  coincides with  $s_2^{PLVI}$ , and  $p_2^i + q_2^i$  coincides with  $p_2^{PVI} + q_2^{PVI}$ . Under partial vertical integration (of firms A<sub>1</sub> and B<sub>1</sub>), the second composite good is sold at  $p_2^{PVI} + q_2^{PVI}$ , which lies always below  $p_2^I + q_2^I$  and above  $s_2^{PLVI}$ . For small  $\sigma$ ,  $p_2^{PVI} + q_2^{PVI}$  is above  $s_2^J$ . As substitution  $\sigma$  increases, competition drives prices down below partial vertical integration, and eventually  $p_2^{PVI} + q_2^{PVI}$  falls below  $s_2^J$ . Thus, the reduction in prices resulting from the merger of A<sub>2</sub> and B<sub>2</sub> to parallel vertical integration, although beneficial for small  $\sigma$  because it brings the composite price closer to the composite price of joint ownership, is detrimental for large  $\sigma$  because the composite price in partial vertical integration is already lower than in joint ownership.

 $<sup>\</sup>overline{[c^{24} \ s_1^{PVI} - s_1^{PLVI} = b_2 c (2a_2b_1 + a_1c) / [2(3b_1b_2 - c^2)(4b_1b_2 - c^2)]} > 0, \ p_2^{PVI} + q_2^{PVI} - s_2^{PLVI} = b_1 b_2 (2a_2b_1 + a_1c) / [(3b_1b_2 - c^2)(4b_1b_2 - c^2)] > 0.$ 

 $<sup>{}^{25} \ \</sup>Pi_{A_2}^{PVI} + \Pi_{B_2}^{PVI} - \Pi_2^{PLVI} = b_2(4b_1b_2c^2 - 2b_1^2b_2^2 - c^4)(2a_2b_1 + a_1c)^2/[2(3b_1b_2 - c^2)^2(4b_1b_2 - c^2)^2].$  In this expression, all terms are positive except for the term in the first set of parentheses. This term can be written as  $4b_1b_2c^2 - 2b_1^2b_2^2 - c^4 = -(b_1b_2)^2(\sigma^2 - 4\sigma + 2) = (b_1b_2)^2(3.41 - \sigma)(\sigma - 0.59),$  where  $\sigma = c^2/b_1b_2 = \gamma^2/\beta_1\beta_2$ . Since  $0 \le \sigma < 1$ , it follows that  $\Pi_{A_2}^{PVI} + \Pi_{B_2}^{PVI} < \Pi_2^{PVI} < \Pi_2^{PVI}$  for relatively small  $\sigma, \sigma < 0.59$ .

 $<sup>{}^{26} \</sup>Pi_1^{PVI} - \Pi_1^{PLVI} = b_1 b_2 c (2a_2b_1 + a_1c) (24a_1b_1b_2^2 + 14a_2b_1b_2c - 7a_1b_2c^2 - 4a_2c^3) / [4(3b_1b_2 - c^2)^2 (4b_1b_2 - c^2)^2] = b_1 b_2 c (2a_2b_1 + a_1c) [a_1b_2 (24b_1b_2 - 7c^2) + 2a_2c (7b_1b_2 - 2c^2)] / [4(3b_1b_2 - c^2)^2 (4b_1b_2 - c^2)^2] > 0.$ 



Seen from a different angle, the vertical integration of  $A_2$  and  $B_2$  puts them on equal footing with the integrated firm 1, and as a result, the quantity of composite good 2 sold increases.<sup>27</sup> However, this is done at the expense of the increased competition that accompanies vertical integration. When the market environment already allows only small margins because of high substitution  $\sigma$ , the decrease in the composite price (due to the increase in competition) is costly to the merging firms and is not sufficiently offset by the increase in its sales. Thus, a vertical merger of the second set of firms is undesirable to them when the composite goods are close substitutes. The already vertically integrated firm loses as a result of the merger, since both its price and its quantity fall.<sup>28</sup>

In terms of consumers' surplus, we are again unable to make general comparisons based solely on quantities, since the quantities of the different composite goods change in opposite directions. In the case of symmetric demand, we find that consumers' surplus increases as we switch from partial vertical integration to parallel vertical integration.<sup>29</sup> Total welfare, TS = CS +  $\Sigma_i$   $\Pi_i$ , also increases for all symmetric demands.<sup>30</sup>

#### 5. <u>Equilibrium Ownership Structures</u>

Suppose that firms  $A_1$ ,  $B_1$ ,  $A_2$ , and  $B_2$  play a merger game where two firms merge if their total post-merger profits are higher. Assume that firms move simultaneously, and each pair of merging firms assumes that the rest of the ownership structure of the rest of the industry does not change. Finally, assume that horizontal mergers are ruled out.

Clearly, different levels of substitution between the composite goods imply different equilibria. There are three relevant ranges of parameter values. First, for far substitutes,  $0 \le \sigma < 0.44$ , a pair of firms producing complementary components prefers to merge irrespective of the ownership structure. Therefore, for far substitutes, the only equilibrium will be parallel vertical integration. Second, for an intermediate range of closer substitutes,  $0.44 < \sigma < 0.59$ , a pair of independent firms producing complementary components prefers to merge if the substitute composite good is produced by an integrated firm but not otherwise. For every level of substitution that falls in this case, there are two equilibria: one at parallel vertical integration, and one at independent ownership. Finally, for very close substitutes,  $0.59 < \sigma < 1$ , independent firms

<sup>29</sup> CS<sup>PLVI</sup> - CS<sup>PVI</sup> = 
$$\alpha^2(1 - y)(20 + 12y - 5y^2 - 4y^3)/[8\beta(y - 2)^2(1 + y)(y^2 - 3)^2] > 0$$
, where  $y = \sqrt{\sigma} = \gamma/\beta$ .

 ${}^{30} \text{ TS}^{\text{PLVI}} - \text{TS}^{\text{PVI}} = \alpha^2 (1 - y)(28 - 12y - 23y^2 + 4y^3 + 4y^4) / [8\beta(y - 2)^2(1 + y)(y^2 - 3)^2)] = \alpha^2 (1 - y)(y - 1.87)(y - 1.03) (1.53 + y)(2.37 + y)) / [2\beta(y - 2)^2(1 + y)(y^2 - 3)^2)] > 0, \text{ where } y = \sqrt{\sigma} = \gamma/\beta.$ 

<sup>&</sup>lt;sup>27</sup> The quantities sold of composite good 2 under partial vertical integration and under vertical integration are  $d_2^{PVI} = b_2(2a_2b_1 + a_1c)/(6b_1b_2 - 2c^2)$ ,  $d_2^{PLVI} = b_2(2a_2b_1 + a_1c)/(4b_1b_2 - c^2)$ . Their difference is  $d_2^{PLVI} - d_2^{PVI} = b_2(2a_2b_1 + a_1c)(2b_1b_2 - c^2)/((6b_1b_2 - 2c^2)(4b_1b_2 - c^2)) > 0$ .

<sup>&</sup>lt;sup>28</sup> Its sales under partial vertical integration and under vertical integration are  $d_1^{PVI} = b_1(3a_1b_2 + 2a_2c)/(6b_1b_2 - 2c^2)$ ,  $d_1^{PLVI} = b_1(2a_1b_2 + a_2c)/(4b_1b_2 - c^2)$ . Their difference is  $d_1^{PVI} - d_1^{PLVI} = b_1b_2c(2a_2b_1 + a_1c)/[(4b_1b_2 - c^2)(6b_1b_2 - 2c^2)] > 0$ .

producing complementary components will not merge no matter what is the ownership structure in the rest of the industry. Thus, in this case the outcome is independent ownership. These equilibrium results are summarized in the following table.

#### Table 1

Substitution Between the Composite Goods	$\frac{\text{Degree of Substitution}}{\sigma = \gamma^2 / \beta_1 \beta_2}$	<u>Equilibrium Outcome(s)</u>
Far	$0 \leq \sigma < 0.44$	Parallel Vertical Integration
Intermediate	$0.44 < \sigma < 0.59$	Independent Ownership and Parallel Vertical Integration
Close	$0.59 < \sigma < 1$	Independent Ownership

**Proposition 5:** The equilibrium ownership structure is parallel vertical integration when the composite goods are close substitutes; it is independent ownership when the composite goods are far substitutes; it may be parallel vertical integration or independent ownership for intermediate levels of substitution.

It is interesting to compare profits, consumers' and total surplus in the region of parameters where two equilibria (parallel vertical integration or independent ownership) exist. General comparisons across equilibria are inconclusive since they depend on the relative sizes of the demand. For symmetric demand, profits are lower under parallel vertical integration than under independent ownership for the whole ranges of intermediate and close substitution between the composite goods. Therefore in the intermediate range, where both parallel vertical integration and independent ownership can be equilibria, profits are higher under independent ownership.<sup>31</sup> For symmetric demand, the quantities of both goods increase as we switch from independent ownership to parallel vertical integration; therefore parallel vertical integration has higher consumers' surplus.<sup>32</sup> Moreover, for symmetric demand, total surplus is higher under parallel vertical integration than under integration than under independent ownership.<sup>33</sup> Thus, for symmetric demand, from a total surplus

<sup>33</sup> For symmetric demand,  $TS^{PLVI} - TS^{I} = \alpha^{2}(7 - 4y)(y - 1)^{2}/[\beta(y - 2)^{2}(1 + y)(2y - 3)^{2}] > 0$  where  $y = \sqrt{\sigma} = \gamma/\beta$ .

 $<sup>\</sup>frac{1}{3^{11}} \prod_{1}^{PLV1} - (\prod_{A_{1}}^{I} + \prod_{B_{1}}^{I}) = \beta_{2}(36\alpha_{1}^{2}\beta_{1}^{4}\beta_{2}^{4} - 132\alpha_{1}\alpha_{2}\beta_{1}^{4}\beta_{2}^{3}\gamma + 49\alpha_{2}^{2}\beta_{1}^{4}\beta_{2}^{2}\gamma^{2} - 84\alpha_{1}^{2}\beta_{1}^{3}\beta_{2}^{3}\gamma^{2} + 226\alpha_{1}\alpha_{2}\beta_{1}^{3}\beta_{2}^{2}\gamma^{3} - 56\alpha_{2}^{2}\beta_{1}^{3}\beta_{2}\gamma^{4} + 95\alpha_{1}^{2}\beta_{1}^{2}\beta_{2}^{2}\gamma^{4} - 132\alpha_{1}\alpha_{2}\beta_{1}^{2}\beta_{2}\gamma^{6} - 48\alpha_{1}^{2}\beta_{1}\beta_{2}\gamma^{6} + 24\alpha_{1}\alpha_{2}\beta_{1}\gamma^{7} + 8\alpha_{1}^{2}\gamma^{8})/[(9\beta_{1}\beta_{2} - 4\gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})^{2}(\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{2} - \gamma^{2})(4\beta_{1}\beta_{$ 

<sup>&</sup>lt;sup>32</sup> In general,  $D_1^{PLVI} - D_1^I = \beta_2(6\alpha_1\beta_1^{-2}\beta_2^{-2} - 5\alpha_2\beta_1^{-2}\beta_2\gamma - 6\alpha_1\beta_1\beta_2\gamma^2 + 3\alpha_2\beta_1\gamma^3 + 2\alpha_1\gamma^4)/[(\beta_1\beta_2 - \gamma^2)(4\beta_1\beta_2 - \gamma^2)(9\beta_1\beta_2 - 4\gamma^2)].$ For a symmetric demand system,  $\alpha_1 = \alpha_2 = \alpha$ ,  $\beta_1 = \beta_2 = \beta$ ,  $D_1^{PLVI} - D_1^I = \alpha(1 - y)/[\beta(y - 2)(1 + y)(2y - 3)] > 0$ , where  $y = \sqrt{\sigma} = \gamma/\beta$ .

maximization point of view, parallel vertical integration is desirable over independent ownership, for all degrees of substitution among the products, even for the case when the goods are close substitutes and parallel vertical integration is not the equilibrium outcome. Therefore the market tends to result in fewer vertical mergers than is socially desirable, at least when the demand is symmetric.

#### 6. <u>Concluding Remarks</u>

Extending the results of Cournot (1838), this paper shows that the producers of complementary components of a composite good that does not have a close substitute have an incentive to merge. This incentive is diminished and eventually it is reversed as the composite good faces competition from an increasingly close substitute. Thus, *vertically-related firms that face competition from a close substitute prefer to stay unintegrated*. In general, the welfare consequences of these vertical mergers are ambiguous. For the case of a symmetric demand system, consumers' and total surplus increase in both mergers from independent ownership to partial vertical integration and from partial vertical integration to parallel vertical integration. Thus, the market provides less vertical integration than is optimal from a social surplus maximizing point of view. The results of this model are expected to generalize to competition in the presence of more than one substitutes.

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