

ALGORITHM FOR PAYOFF CALCULATION FOR OPTION TRADING STRATEGIES USING VECTOR TERMINOLOGY

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Abstract:

The aim of this paper is to develop an algorithm for calculating and plotting payoff of option strategies for a portfolio of path independent vanilla and exotic options. A general algorithm for calculating the vector matrix for any arbitrary combination strategy is also developed for some of the commonly option trading strategies.

Keywords: option trading strategy, payoff, vector, vanilla and exotic option.

JEL-Classification: C63, C88, C02, G00

1. Introduction

Hull (2009) discusses the payoffs for long and short positions in Call and Put options by using algebraic techniques. J.S. Chaput and L.H. Ederington (2003), Natenberg (1994) and Hull (2009) contain the bibliographies and survey of literature on the theoretical background of option strategies for the path independent vanilla and exotic options such as European, Bermuda, Forward Start, Digital/Binary and Quanto options. There are various open source option strategy calculators like "Option" [4] that only rely on algebraic, analytical and graph superposition techniques to plot graphs for overall profit/loss. We in this paper develop an algorithm using vector terminology to plot the final profit/loss graph of various option strategies.

2.1. Option strategies using vector notation

For a spot price S_T at time T and a strike price K, the payoff for a long position in call option is given by $Max(S_T-K,0)$ and the payoff is $Min(S_T-K,0)$ for the short position in the call option. Similarly the payoff for a long position in put is Max (K- S_T , 0) whereas it is Min (S_T -K, 0) for a short position in the put option. We can represent a vector payoff matrix for any option strategy as a 2xN matrix.

Vector	V_1	V_2	 V _n
Strike	K_1	K_2	 K _n
Price			

In the above matrix the strike prices K_1, K_2, \ldots, K_n for combination of options are in the ascending order, i.e., $K_1 \le K_2 \le \le K_n$. The vector V_i can be interpreted as slope of the payoff graph of option strategy. By default the smallest strike price is always taken to be zero i.e. K₁=0. The vector is always an integer in the interval $(-\infty, \infty)$. We can interpret the above matrix in terms of slope of the profit/loss curve obtained for option strategies.

$$slope = \begin{cases} V_{i}, \text{ for } K_{i} < K < K_{i+1} \text{ and } i < n \\ V_{i}, \text{ for } K > K_{i} \text{ and } i = n \end{cases}$$

Vector matrix for long and short position is given by

Long Position

V_1	V_2	 V _n
K_1	K_2	 K _n

Short Position

$-V_1$	-V ₂	 -V _n
K_1	K_2	 K _n

Using the above vector notation we can represent long and short position in call option as under:

Long call		
0	+1	
0	K_1	

Short Call		
0	-1	
0	K_1	

For long position in call, profit/loss curve has two slopes 0 and +1 whereas for a short position the slope of profit/loss curve has two slopes 0 and -1.

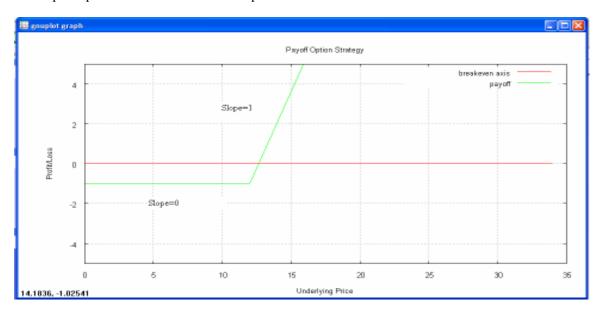


Figure 1. Long Position in Call Option

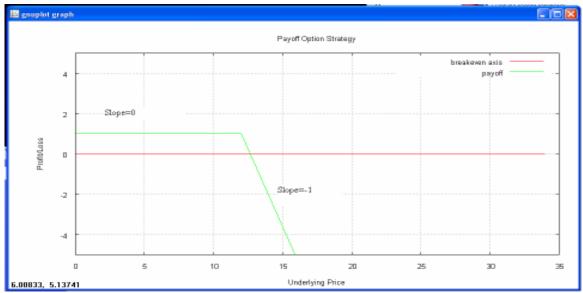


Figure 2. Short position in Call Option

Similarly, the vector matrix for long and short position in put options are:

Lon		
-1	0	
0	K_1	

Short Put			
+1	0		
0	\mathbf{K}_1		

For long position in stock, the slope of profit/loss curve is +1 and strike price is assumed to be zero whereas for short position in stock, the slope of profit/loss curve is -1 and strike price is assumed to be zero. The vector matrix notation is given as:



Short Stock				
	-1			
	0			

When we trade in n units of options using a particular option strategy, the entire vector row is multiplied by n.

n*V ₁	n*V ₂	 n*V _n
K_1	K_2	 K _n

The data set for a portfolio using n option strategies can be represented as

Strategy 1

V_{11}	V_{12}
K_{11}	K_{12}

Strategy 2

V_{21}	V_{22}
K_{21}	K ₂₂

. . .

Strategy i

V _{i1}	V_{i2}	 V _{ij}	
K _{i1}	K _{i2}	 K _{ij}	

.

Strategy n

V _{n1}	V_{n2}	 V_{nm}	
K _{n1}	K _{n2}	 K _{nm}	

Note that the number of columns in each option strategy can be different. We can use the above-derived vector matrices to form profit/loss function for any combination of option strategies using the following algorithm:

Algorithm

To plot the overall payoff strategy we need the initial Y intercept of the strategy apart from the resultant vector matrix. This Y intercept can be calculated using matrices of length greater than one using the formula

```
Yint = \sum ( -1*Vector(A[j])*Strike_price(A[j+1]) )
Yint = Yint + Net Premium Paid
```

```
Step 1
For I \leftarrow 1 to no of options
      For j ← 1 to length of option matrix
Insert A[j] in Result matrix in sorted increasing order on the basis of
Strike price(A[j]).
Step 2
For k \leftarrow 1 to length of Result matrix
      Vector(B[k])=0
      For I ← 1 to no of options
            For j ← 1 to length of option matrix
                   If Strike price(B[k]) = Strike price(A[i])
                         Vector(B[k]) = Vector(B[k]) + Vector(A[j])
                   ElseIf j < length of option matrix</pre>
If Strike price (A[j]) < Strike price (B[k]) < Strike price (A[j+1])
                         Vector(B[k]) = Vector(B[k]) + Vector(A[j])
                  Else
                         Vector(B[k]) = Vector(B[k]) + Vector(A[j])
Step 3
For I \leftarrow 1 to no of options
      i = 1
      If length of option matrix > 1
Yint = Yint + -1 * Vector(A[j]) * Strike price(A[j+1])
Yint = Yint + NetPremium
Step 4
For k \leftarrow 1 to length of Result matrix - 1
Plot line with slope Vector(B[k]) and Y Intercept Yint
between points Strike price(B[k]) and Strike price(B[k+1])
ypoint=Vector(B[k])*( Strike price(B[k+1]) - Strike price(B[k]) ) +
Yint
Yint = ypoint - Vector(B[k+1])* Strike price(B[k+1]
k = length of Result matrix
Plot line with slope Vector(B[k]) between points Strike price(B[k]) and
infinity
```

The source code for the above algorithm is written and implemented on VC++.Net 2005 using open source graph plotting utility Gnuplot.

Illustration 1: An investor buys \$3 put with strike price \$35 and sells for \$1 a put with a strike price of \$30. (Example 10.2, page 224 given in Hull [1])

The above data can be represented as

Buy Put		+	Sell Put		=	Payoff(Be	ear Spread)	
-1	0		+1	0		0	-1	0
0	35		0	30		0	30	35

Initial Y intercept is -1*(-1*35) + -1*(1*30) - 3 + 1 = 35 - 30 - 3 + 1 = 3

One can use the following form to input the data of his/her option strategy:

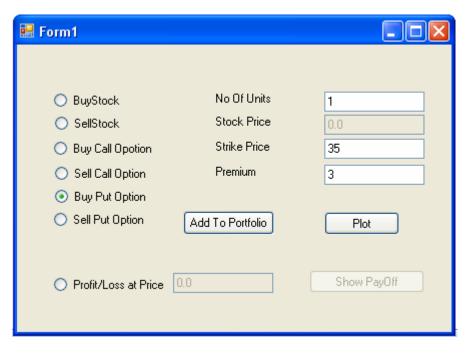


Figure 3. Input Screen

The following is the output of the final payoff of combination of option strategy in vector notation as discussed above.

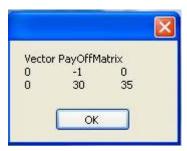


Figure 4. Vector Payoff Matrix

The algorithm gives the following resultant profit/loss graph of the above combination of option strategies in the form of a bear put spread.

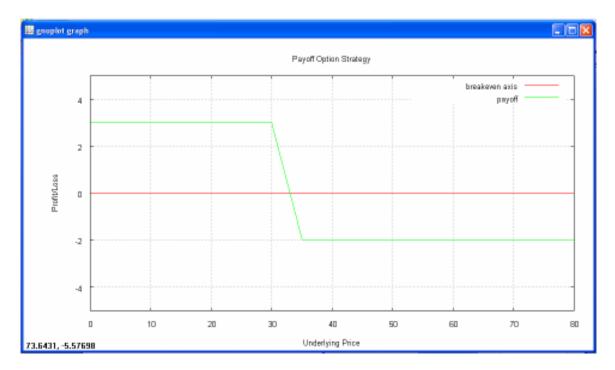
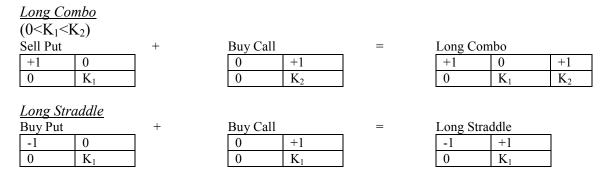


Figure 5. Payoff Graph

The loss is \$2 if stock price is above \$35 and the profit is \$3 if stock price below \$30.

2.2. Some More Complex Strategies

The following are the vector matrices for some of the commonly traded strategies:



Short Straddle

-1

+1

The vector matrix of short straddle is negative of that of long straddle

0	K_1				
<u>Strip</u> Buy call					
Buy call		+	Buy 2 puts	=	Strip
0	+1		-2 0		-2 +1
0	K_1		$0 K_1$		0 K_1

<u>Strap</u>

Buy 2 calls		
0	+2	
0	K_1	

	В
	_

Buy put	
-1	0
0	K_1

-1	+2
0	K_1

Long Strangle

$(0 < K_1 < K_2)$)
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Buy put	
-1	0
0	\mathbf{K}_1

Buy Can	
0	+1
0	K_2

Long Strangle

Long Strangic				
-1	0	+1		
0	K_1	K_2		

Short Strangle

The vector matrix of short strangle is negative of that of short strangle. $(0 \le K_1 \le K_2)$

+1	0	-1
0	K_1	K_2

Collar

$\overline{(0 \le K_1 \le K_2)}$

Long St	00
+1	
0	

ut

Duy rui	
-1	0
0	K_1

Sch can	
0	-1
0	K_2

Collar

0	+1	0
0	K_1	K_2

Box Spread

 $(0 < K_1 < K_2)$

Buy Call		
0	+1	
0	K_1	

Sell	call
Sen	can

Sell c	all
0	-1
0	\overline{K}_2

Sel	11 P	ut	
+	1	0	
0		K_1	

Buy	Put
-1	0
0	K_2

Box Spread

0	0	0
0	\mathbf{K}_1	K_2

Long Call Butterfly

$$(0 \le K_1 \le K_2 \le K_3)$$

Buy Call		
0	+1	
0	K_1	

Long Call Butterfly

Bong can battering			
0	+1	-1	0
0	K_1	K_2	K_3

Short Call Butterfly

The vector matrix of short call butterfly is negative of that of long call butterfly $(0 \le K_1 \le K_2 \le K_3)$

0	-1	+1	0
0	K_1	K_2	K_3

Long Call Condor

$$(0 < K_1 < K_2 < K_3 < K_4)$$

Buy Call +

 K_1

Sell call		
0	-1	
0	K_2	

Sell Call			+
0		-1	
0		K ₂	

Buy (Call	=
0	+1	
0	K_4	

Long Call Condor				
0	+1	0	-1	0
0	K_1	K_2	K_3	K_4

Short Call Condor

The vector matrix of short call condor is negative of that of long call condor $(0 \le K_1 \le K_2 \le K_3 \le K_4)$

0	-1	0	+1	0
0	K_1	K_2	K_3	K_4

Illustration 2: Let a certain stock be selling at \$77. An investor feels that significant change in price is un-likely in the next 3 months. He observes market price of 3 month calls as

Strike Price(\$)	Call Price(\$)
75	12
80	8
85	5

The investor decided to go long in two calls each with strike price \$75 and \$85 and writes two calls with strike price \$80. Payoff for different levels of stock prices is given as:

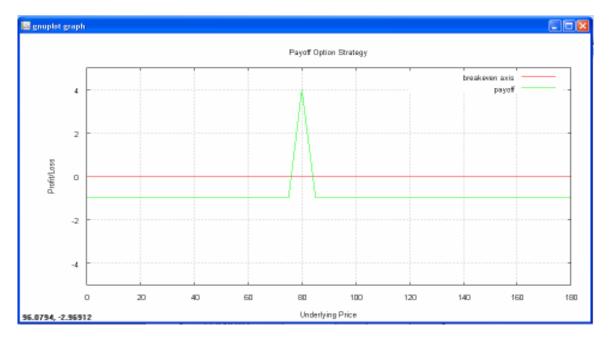


Figure 6. Payoff Graph

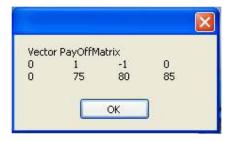


Figure 7. Vector Payoff Matrix

The profit /loss when stock price is at maturity is



3. References

- [1] Hull, J.C., (2009), Options, Futures, and Other Derivatives, Prentice Hall
- [2] Natenberg, S., (1994), Option Volatility and Pricing Strategies: Advanced Trading Techniques for Professionals McGraw-Hill Professional Publishing
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- [4] http://sourceforge.net/projects/option