





# TEMPORAL AGGREGRATION IN A PERIODICALLY INTEGRATED AUTOREGRESSIVE PROCESS

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### **TEMPORAL AGGREGRATION IN A**

#### PERIODICALLY INTEGRATED AUTOREGRESSIVE PROCESS

by

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## ABSTRACT

A periodically integrated autoregressive process for a time series which is observed s times per year is a process for which there exist s-1 cointegration relations between the annual series containing the s seasonal observations. This means that there is a single unit root in the vector autoregression for these annual series. In this paper it is shown that temporally aggregating such a process does not effect the presence of this unit root, i.e. the aggregated series is also periodically integrated.

#### **AUTHORS' NOTES**

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### **1. INTRODUCTION**

Temporal aggregation in flow-type univariate time series processes is studied, e.g., in Amemiya and Wu (1972) and Weiss (1986) with respect to the order of the ARMA process for the aggregated time series. Recently, the focus is also on the effects of temporal aggregation on unit roots. For example, Hylleberg *et al.* (1992) investigate to what extent seasonal unit roots in monthly series are preserved in quarterly time series. In this paper we consider the effects of aggregating a periodic autoregression which contains a single unit root. Such a process is called a periodically integrated process.

Section 2 of the present paper is dedicated to a brief review of several concepts for periodically integrated autoregressions. Section 3 presents the main results.

### **1. PERIODIC INTEGRATION**

Consider a time series  $y_t$  which is observed s times a year during N years. The index t runs from 1 to n = sN. Assume that  $y_t$  can be described by a periodic autoregressive process of order p, [PAR(p)],

$$y_{t} = \mu_{s} + \phi_{1s}y_{t-1} + \dots + \phi_{ps}y_{t-p} + \varepsilon_{t}$$
(1)

where  $\varepsilon_t$  denotes a standard white noise process with variance  $\sigma^2$ . The index s indicates that the parameters are assumed to be time-varying, cf. Jones and Brelsford (1967) and Troutman (1979). Note that the mean of  $y_t$  may be  $\delta$ , i.e. nonperiodic, since (1) can originate from an PAR(p) process for  $y_t-\delta$ . The AR order p corresponds to the maximum order, i.e.  $p = \max(p_s)$ , where  $p_s$  is the AR order per season.

The process in (1) can be rewritten in vector notation by stacking the

observations  $y_t$  in the  $(s \times 1)$  vector of annual observations per season, to be denoted as  $Y_T$  with T = 1,..,N, and representing (1) by

$$A_{0} \begin{bmatrix} Y_{1T} \\ Y_{2T} \\ Y_{3T} \\ \vdots \\ Y_{sT} \end{bmatrix} = \mu + A_{1} \begin{bmatrix} Y_{1T-1} \\ Y_{2T-1} \\ Y_{3T-1} \\ \vdots \\ Y_{sT-1} \end{bmatrix} + A_{2} \begin{bmatrix} Y_{1T-2} \\ Y_{2T-2} \\ Y_{3T-2} \\ \vdots \\ Y_{sT-2} \end{bmatrix} + \dots + A_{f} \begin{bmatrix} Y_{1T-f} \\ Y_{2T-f} \\ Y_{3T-f} \\ \vdots \\ Y_{sT-f} \end{bmatrix} + \omega_{T}$$
(2)

where  $\mu$  and  $\omega_T$  are partitioned conformably with  $Y_T = (Y_{1T}, Y_{2T}, ..., Y_{sT})$ '. The  $\omega_T$  is a vector white noise process with covariance matrix  $\sigma^2 I_s$ . The matrices  $A_0, ..., A_f$  are  $(s \times s)$  parameter matrices, see also Osborn (1991).

This vector process of order f is stationary if the roots of the characteristic equation

$$|A_0 - A_1 z - \dots - A_f z^f| = 0$$
(3)

are outside the unit circle. In that case we say that the univariate series  $y_t$ is periodically stationary. If one  $z_i$  is equal to one, and for the remaining  $z_j$  it applies that  $|z_j|>1$ , there are s-1 cointegrating relationships between the s elements of  $Y_T$ , see Engle and Granger (1987) and Johansen (1991). The process  $y_t$  is then said to be periodically integrated. Boswijk and Franses (1992) and Franses (1991) propose tests for periodic integration. If there are s-1 cointegration relations between s variables, the  $Y_{iT}$  series are integrated of order 1, I(1), for i = 1,...,s, and the s-1 variables  $Y_{jT} - \delta_j Y_{j-1T}$  are integrated of order 0, I(0), for some  $\delta_j \neq 0$ , and j = 2,...,s.

An illustrative example of the expressions in (1) through (3) is given by the periodic first order autoregressive model for a quarterly observed series  $y_t$  with zero mean, or

$$y_t = \phi_s y_{t-1} + \varepsilon_t, \tag{4}$$

where  $\phi_s$  is unequal to zero, with  $\phi_s \neq \phi$  for all s, and where some of the  $\phi_s$ can be larger than 1. Stacking the  $y_t$  into the vector  $Y_T = (Y_{1T}, Y_{2T}, Y_{3T}, Y_{4T})'$ ensures that (4) can be written as

$$A_0 Y_T = A_1 Y_{T-1} + \varepsilon_T, \tag{5}$$

with

The characteristic equation for (5) reads

$$|A_0 - A_1 z| = (1 - (\phi_1 \phi_2 \phi_3 \phi_4) z) = 0.$$
(6)

The process  $Y_T$  is periodically stationary if  $|\phi_1\phi_2\phi_3\phi_4| < 1$ , and periodically integrated if  $\phi_1\phi_2\phi_3\phi_4 = 1$ . To investigate the presence of cointegration relations between the  $Y_{sT}$  in (5), it is convenient to rewrite this process into

$$\Delta_1 Y_T = \Pi Y_{T-1} + \omega_T, \tag{7}$$

where  $\omega_T = A_0^{-1} \varepsilon_T$ . From Johansen (1991) it follows that the rank of  $\Pi$  determines the number of cointegrating relationships. In this case

$$\Pi = \begin{bmatrix} -1 & 0 & 0 & \phi_1 \\ 0 & -1 & 0 & \phi_1 \phi_2 \\ 0 & 0 & -1 & \phi_1 \phi_2 \phi_3 \\ 0 & 0 & 0 & \phi_1 \phi_2 \phi_3 \phi_4 - 1 \end{bmatrix}.$$
(8)

Under the restriction  $\phi_1\phi_2\phi_3\phi_4 = 1$ , this matrix has rank 3.

# 2. TEMPORAL AGGREGATION

Consider the temporal aggregation of an  $y_t$  series, which is observed s times per year and which can be described by a PAR process as in (1), to a series  $ya_t$ , that is  $s^*$  times observed, with  $ks^* = s$  and k usually is 6,4,3 or 2. In general, the  $ya_t$  series can be described by a periodic ARMA process [PARMA], see also Weiss (1984) for nonperiodic processes.

For example, consider the aggregation of the quarterly series  $y_i$ , which is generated from (4) into a bi-annual series  $z_{\tau}$ , where  $\tau$  runs from 1 through n/2. The observations  $z_{\tau}$  are generated as  $z_1 = y_1 + y_2$ ,  $z_2 = y_3 + y_4$ , and so on. Substituting the appropriate expressions for  $y_i$ , i = 1,...,n, one easily obtains that  $z_{\tau}$  follows a periodic ARMA process of order (1,1),

$$z_{\tau} = \alpha_s z_{\tau-1} + v_{\tau} + \beta_s v_{\tau-1} \tag{9}$$

with

$$\alpha_1 = ((\phi_2 + 1)\phi_1\phi_4)/(\phi_4 + 1) \tag{10}$$

$$\alpha_2 = ((\phi_4 + 1)\phi_2\phi_3)/(\phi_2 + 1), \tag{11}$$

where the  $v_{\tau} + \beta_s v_{\tau-1}$  is a moving average process of order 1 with parameter  $\beta_s$ which also varies with the season. Note that this assumes that  $\phi_2$  and  $\phi_4$  are not equal to -1. If this is the case,  $z_{\tau}$  becomes a white noise process. From (10) and (11) it is clear that  $\alpha_1 = \alpha_2$  only when a specific nonlinear parameter restriction holds. This suggests that temporal aggregation of a PAR generically yields a PARMA process.

Aggregating the  $y_t$  series in (4) to an annually observed time series  $x_T$  yields

$$x_T = \phi_1 \phi_2 \phi_3 \phi_4 x_{T-1} + \nu_T - \theta \nu_{T-1} \tag{12}$$

which is a nonperiodic ARMA(1,1) process.

**PROPOSITION:** Let  $\{Y_T\}$  be an  $(s \times 1)$  cointegrated process with cointegrating rank s-1 and  $s \times (s-1)$  matrix of cointegrating vectors  $\beta$ . Defined  $\beta_{\perp} \neq 0$  to be an s-vector that spans the null space of  $\beta$ , i.e.  $\beta'\beta_{\perp} = 0$ . Let A be an arbitrary  $(s \times s^*)$  matrix,  $s^* < s$ , and let  $\{X_T = A'Y_T\}$  be an  $s^*$ -vector process. Then  $X_T$  is a stationary process iff  $M(A) \subset M(B)$ , where M(.) denotes the column space, orequivalently iff  $A'\beta_{\perp} = 0$ ; Otherwise,  $\{X_T\}$  is a cointegrated process with cointegrating rank  $s^*-1$ .

**PROOF:** Johansen's version of the Granger representation theorem (Theorem. 4.1) states that

$$Y_T = \beta_{\perp} (\alpha_{\perp} \Psi \beta_{\perp})^{-1} \alpha_{\perp} S_T + U_T$$
(13)

where  $\alpha_{\perp}$  and  $\Psi$  are as defined in Johansen (1991), where  $S_T$  is an *s*-vector random walk, and where  $U_T$  is an (*s*×1) stationary process. Because  $\beta_{\perp}$  and  $\alpha_{\perp}$ are (*s*×1) vectors, there is one common trend in the system:  $\alpha_{\perp} S_T$  is a scalar random walk. The same single common trend appears in the system

$$X_T = A'\beta_{\perp}(\alpha_{\perp}'\Psi\beta_{\perp})^{-1}\alpha_{\perp}'S_T + A'U_T$$
<sup>(14)</sup>

unless  $A'\beta_{\perp} = 0$ , so that the linear combination  $A'Y_T$  annihilates the common trend and thus is stationary. Finally, Johansen's Theorem 4.1 implies that an  $s^*$ -vector process with a single common trend is cointegrated with cointegrating rank  $s^*-1$ .

For the periodic AR process  $y_t$  in (1) with a single unit root in the multivariate system (2), it applies that  $\beta$ ' is the  $(s-1)\times s$  matrix

$$\beta' = \begin{bmatrix} -\delta_2 & 1 & 0 & . & . & . & 0 \\ 0 & -\delta_3 & 1 & & & 0 \\ 0 & 0 & -\delta_4 & 1 & . & . & 0 \\ \vdots & \vdots & 0 & & \vdots & \vdots \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & & -\delta_s & 1 \end{bmatrix}$$
(15)

that  $\beta_{\perp}$  is given by

$$\beta_{\perp} = [1, \ \delta_2, \ \delta_2 \delta_3, \qquad , \ \delta_2 \delta_3 \dots \delta_{s-1}, \ \delta_2 \delta_3 \dots \delta_s]$$
(16)

For temporal aggregation of the process  $Y_T$  in (2), the matrix A' in the proposition is given by the  $(s^* \times s)$  matrix

$$A' = \begin{bmatrix} 1...1 & 0 & 0 & ... & 0\\ 0 & 0 & 1...1 & 0 & 0 & .\\ \vdots & \vdots & & & \vdots\\ 0 & 0 & & & 1...1 \end{bmatrix}$$
(17)

where the (1..1) parts are  $(1 \times k)$  vectors. The event that all s<sup>\*</sup> elements of  $A'\beta_{\perp}$  are equal to zero, where A and  $\beta_{\perp}$  are given by (16) and (17), has measure zero. Hence, if a periodically integrated process for an s times observed  $y_t$  series, i.e. a process with s-1 cointegration relations, is aggregated to an s<sup>\*</sup> times observed series  $ya_t$ , this  $ya_t$  series generically has  $s^*$ -1 cointegrating relations between its annually observed components.

An additional intuitive argument is that the only way to get rid of the unit root z = 1 is to use some differencing filter. Temporal aggregation of  $y_t$ does not involve such a filter, and hence the unit root is not removed.

For the periodically integrated AR(1) process in (4) the cointegration vectors are  $(-\phi_2,1,0,0)'$ ,  $(0,-\phi_3,1,0)'$  and  $(0,0,-\phi_4,1)'$ , and the (4×1) vector  $\beta_{\perp}$  is  $(\phi_1,\phi_1\phi_2,\phi_1\phi_2\phi_3,1)$ . Temporal aggregation to the  $z_{\tau}$  in (9) implies that

$$A' = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$
(18)

and hence  $z_{\tau}$  is periodically integrated unless  $A'\beta_{\perp} = 0$ , or  $\phi_2 = \phi_4 = -1$ , see below (10) and (11). The process in (9) can be represented in vector notation as  $B_0Z_T = B_1Z_{T-1} + \psi_T$ , with  $\psi_t$  is an moving average type error process. The characteristic equation is  $|B_0 - B_1z| = (1 - (\phi_1\phi_2\phi_3\phi_4)z) = 0$ , which is the same as that in (6). An expression for the cointegration vector can be found from

$$B_0^{-1}B_1 - I = \begin{bmatrix} -1 & ((\phi_2 + 1)\phi_1\phi_4)/(\phi_4 + 1) \\ 0 & \phi_1\phi_2\phi_3\phi_4 - 1 \end{bmatrix}$$
(19)

The rank of the matrix in (15) is at least one, and the cointegration relation between  $Z_{1T}$  and  $Z_{2T}$  is easily found.

To obtain the annual series  $X_T$  in (12), one uses A' = [1,1,1,1]. Hence, the  $X_T$  is an integrated series provided that  $\phi_1 + \phi_1\phi_2 + \phi_1\phi_2\phi_3 \neq -1$ .

In summary, in this paper it is shown that temporally aggregating a univariate periodically integrated autoregressive time series [PIAR], i.e. a process of the multivariate representation contains a single unit root, yields a PIAR again.

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