

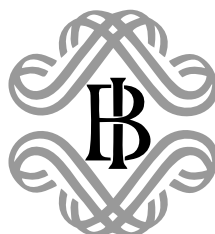
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**Canonical term-structure models with observable factors  
and the dynamics of bond risk premiums**

by M. Pericoli and M. Taboga



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# CANONICAL TERM-STRUCTURE MODELS WITH OBSERVABLE FACTORS AND THE DYNAMICS OF BOND RISK PREMIUMS

by Marcello Pericoli and Marco Taboga\*

## Abstract

We study the dynamics of risk premiums on the German bond market, employing no-arbitrage term-structure models with both observable and unobservable state variables, recently popularized by Ang and Piazzesi (2003). We conduct a specification analysis based on a new canonical representation for this class of models. We find that risk premiums display a considerable variability over time, are strongly counter-cyclical and bear no significant relation to inflation.

JEL classification: C5, G1.

Keywords: term structure models, yield curve, risk premium.

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## 1. Introduction<sup>1</sup>

We study the dynamics of risk premiums on the German bond market and their relation to macroeconomic variables. We employ no-arbitrage affine multifactor term-structure models following the approach, recently popularized by Ang and Piazzesi (2003), of including both observable and unobservable factors in the set of state variables. Conforming to the existing literature, the observable state variables we include are inflation and a measure of the output gap.

We derive a canonical representation for the class of affine models with both observable and unobservable variables including as special cases the models of Ang and Piazzesi (2003), Ang, Dong and Piazzesi (2004), Ang, Piazzesi and Wei (2005), Hördal, Tristani and Vestin (2005) and Rudebusch and Wu (2005). The new set of identifying restrictions implied by this representation is less restrictive than the set of restrictions first proposed by Ang and Piazzesi (2003). Ang and Piazzesi correctly acknowledge that identification schemes provided by Dai and Singleton (2000) for affine term-structure models cannot be applied to models with observable variables, since equivalent representations of the models can be obtained only by rotations and translations of the variables which leave the observable variables unchanged. Some of the over-identifying restrictions in Ang and Piazzesi (2003) are rejected by formal statistical tests in our sample. However, they have substantial consequences on estimated risk premiums only when their two-stage estimation procedure is employed instead of a joint estimation procedure. We use our canonical representation to perform a specification analysis and find that three unobservable state variables must be added to the two observables to obtain an accurate description of yield-curve dynamics. Hence, the classical finding that multifactor models with three unobservable factors provide the best balance between parsimony and statistical fit (e.g. Litterman and Scheinkman - 1991 and Knez, Litterman and Scheinkman -

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1994) is not altered by the inclusion of observable state variables. The inclusion of macroeconomic variables is nevertheless worthwhile: a variance decomposition analysis reveals that shocks to output and inflation explain a significant portion of the variability of risk premiums, hence they play a key role in determining the dynamics of bond yields. Estimating both the physical and the risk-neutral dynamics of the factors driving interest rates, we are able to separate risk premiums from the other components of bond yields, namely expectations and Jensen's inequality adjustments: this is achieved by deriving the no-arbitrage bond yields that would be observed if the market were populated by risk-neutral investors and then subtracting them from the yields implicit in actually observed market prices. We find that risk premiums display a considerable variability over time and that both the level and the variability of the premiums are increasing with the maturity of bonds. High negative correlation with the output gap provides evidence that the premiums are countercyclical, but there seems to be no systematic link between inflation and the premiums. When unobservable variables are included in the model, observable variables make only a minimal contribution to explaining the overall variability of yields. However, concentrating only on risk premiums we find that macroeconomic variables explain a significant portion of their variability. These pieces of evidence are only apparently conflicting: since the short-term interest rate is procyclical and risk premiums are countercyclical, long-term bond yields, being a sum of the two, do not react much to output shocks because the separate effects of these shocks on premiums and the short rate offset each other. This hypothesis is confirmed when we perform a variance decomposition on yields of different maturities: the proportion of variance explained by output shocks is higher for shorter maturities and lower for longer maturities; this result is due to the fact that risk premiums on shorter maturities are smaller and hence the compensating effect explained above is only partial.

Our study belongs to a recent strand of the literature which uses no-arbitrage pricing models to analyze the relation between the yield curve and macroeconomic fundamentals: some examples are Ang and Piazzesi (2003), Ang, Dong and Piazzesi (2004), Ang, Piazzesi and Wei (2005), Hördal, Tristani and Vestin (2005) and Rude-

busch and Wu (2005). For a survey, we refer the reader to Diebold, Piazzesi and Rudebusch (2005). Earlier studies investigating the relation between the yield curve and macroeconomic variables, such as Fama (1990), Mishkin (1990), Estrella and Mishkin (1995) and Evans and Marshall (1998) do not consider no-arbitrage relations among yields and do not model bond pricing. As a consequence, they are able to make predictions only about the yields explicitly analyzed (typically no more than three), they do not rule out theoretical inconsistencies due to the presence of arbitrage opportunities along the yield curve and they make no predictions about risk premiums and their evolution over time. For these reasons, the more recent studies we mentioned above have proposed to enrich macro-finance models with rigorous asset pricing relations, imposing no-arbitrage constraints on bond prices. All these studies employ Gaussian affine term-structure models where risk premiums are allowed to vary over time. Their primary focus, however, is on the relation among economic growth, inflation and interest rates, while they analyze the time-variation of risk premiums only incidentally. They implicitly characterize risk premiums and their dependence on macroeconomic variables, by specifying and estimating a pricing kernel, but they do not provide explicit measures of risk premiums across maturities and over time. The aim of our paper, instead, is to provide measures of risk premiums which have a straightforward economic interpretation; for each bond and at each point in time, we measure the extra-return per period required by bond market investors to bear interest rate risk. The bond pricing model we use allows for a rigorous separation of the risk premiums from the other components of the term spreads, namely expectations of future interest rates and Jensen's inequality adjustments. Furthermore, estimating a no-arbitrage pricing functional defined also on observable variables, we are able to assess separately the impact of changes in macroeconomic fundamentals on risk premiums and to understand to what extent the variability of risk premiums is generated by macroeconomic uncertainty or by other factors.

The paper is organized as follows: Section 2 presents the class of affine models we estimate and gives the minimal identifying conditions; Section 3 describes our

dataset; Section 4 discusses the empirical evidence, as well as some important details regarding the numerical procedures adopted to estimate the model; Section 5 concludes. The Appendix contains all the technical details.

## 2. The model

Our model of the term structure is a standard Gaussian affine model, set in discrete time, as in the majority of the recent literature about macro term structure models. The model consists of three equations. The first equation describes the dynamics of the vector of state variables  $X_t$  (a  $k$ -dimensional vector,  $k \in \mathbb{N}$ ):

$$X_t = \mu + \rho X_{t-1} + \Sigma \varepsilon_t \quad (1)$$

where  $\varepsilon_t \sim N(0, I_k)$ ,  $\mu$  is a  $k \times 1$  vector and  $\rho$  and  $\Sigma$  are  $k \times k$  matrices. Without loss of generality, it can be assumed that  $\Sigma$  is lower triangular. Furthermore, to ensure stationarity of the process, we assume that all the eigenvalues of  $\rho$  strictly lie inside the unit circle. The probability measure associated with the above specification of  $X_t$  will be denoted by  $P$ .

The second equation relates the one-period interest rate  $r_t$  to the state variables (positing that it be an affine function of the state variables):

$$r_t = a + b^\top X_t \quad (2)$$

where  $a$  is a scalar and  $b$  is a  $k \times 1$  vector.

The third equation is related to bond pricing in an arbitrage-free market. A sufficient condition for the absence of arbitrage on the bond market is that there exists a risk-neutral measure  $Q$ , equivalent to  $P$ , under which the process  $X_t$  follows the dynamics:

$$X_t = \bar{\mu} + \bar{\rho} X_{t-1} + \Sigma \eta_t \quad (3)$$

where  $\eta_t \sim N(0, I_k)$  under  $Q$  and such that the price at time  $t$  of a bond paying a unitary amount of cash at time  $t + n$  (denoted by  $p_t^n$ ) equals:

$$p_t^n = E_t^Q [\exp(-r_t) p_{t+1}^{n-1}] \quad (4)$$

where  $E_t^Q$  denotes expectation under the probability measure  $Q$ , conditional upon the information available at time  $t$ .

The vector  $\bar{\mu}$  and the matrix  $\bar{\rho}$  are in general different from  $\mu$  and  $\rho$ , while equivalence of  $P$  and  $Q$  guarantees that  $\Sigma$  is left unchanged. The link between the risk-neutral distribution  $Q$  and the physical distribution  $P$  is given by the (time-varying) price of risk  $\lambda_t$ :

$$\lambda_t = \lambda_0 + \lambda_1 X_t \quad (5)$$

where  $\lambda_0 = \Sigma^{-1}(\mu - \bar{\mu})$  and  $\lambda_1 = \Sigma^{-1}(\rho - \bar{\rho})$ . According to Cameron, Martin and Girsanov's theorem (e.g. Kallenberg - 1997)

$$E_t^P \left[ \frac{dQ}{dP} \right] = \prod_{j=1}^{\infty} \exp \left[ -\frac{1}{2} \lambda_{t+j-1}^\top \lambda_{t+j-1} - \lambda_{t+j-1}^\top \varepsilon_{t+j} \right] \quad (6)$$

so that the pricing kernel

$$m_{t+1} = \exp \left( -r_t - \frac{1}{2} \lambda_t^\top \lambda_t - \lambda_t^\top \varepsilon_{t+1} \right) \quad (7)$$

can be used to recursively price bonds:

$$p_t^n = E_t^P [m_{t+1} p_{t+1}^{n-1}] \quad (8)$$

Multifactor affine models of the term structure, such as the one just described, are very popular in the finance literature and their properties have long been studied by many researchers. Thorough specification analyses of these models have been conducted (e.g. Dai and Singleton, 2000) and their properties are now well-known. A distinguishing feature of these models is that they are able to describe the dynamics of yields in terms of a small set of unobservable state variables: typically three variables are deemed a sufficient number to describe the whole yield curve and this is also supported by empirical studies, such as the seminal paper by Litterman and Scheinkman (1991). Although such models are capable of describing accurately and parsimoniously the evolution of interest rates over time, the factors they identify as the driving forces of interest rates often lack economic intuition and are difficult to



relate to relevant economic variables. This is one of the reasons why recent studies have proposed to augment the usual set of unobservable state variables with some observable variables. Typically, inflation and a measure of the output gap are the two observable variables, while a small number of unobservable factors, ranging from one to three, are included in the models: recent examples are Ang and Piazzesi (2003), Rudebusch and Wu (2005), Hördal, Tristani and Vestin (2005) and Ang, Piazzesi and Wei (2005). All these works impose some set of restrictions on the system of equations (1-3) and, after estimating the coefficients, derive bond prices using equation (4).

We take the same approach, adding inflation and output gap to the unobservable factors. However, rather than imposing ad hoc set of restrictions on the parameters of the model and arbitrarily defining the number of unobservable variables, we derive a set of minimal identifying restrictions and, placing only these restrictions on the model, we perform a specification analysis to select the number of unobservable factors.

Our minimal set of identifying restrictions is not the standard set of restrictions usually imposed for identification of affine term-structure models (e.g.: Dai and Singleton - 2000). Standard models of the term structure include only unobservable factors and equivalent representations of the factor dynamics can be obtained by performing any rotation and translation of the factors. On the contrary, our set of identifying restrictions takes into account the fact that in a model with both observable and unobservable factors equivalent representations can be obtained only with rotations and translations which leave the observable factors unchanged.

Suppose that the first  $k^o$  variables included in the model are observable and the remaining  $k^u = k - k^o$  are unobservable. Collect their values at time  $t$  into the  $k^o \times 1$  vector  $X_t^o$  and the  $k^u \times 1$  vector  $X_t^u$  respectively. Equations (1-3) can be written as follows:

$$\begin{aligned}
\text{Short-rate process} & \quad \left\{ \begin{array}{l} r_t = a + b^{o\top} X_t^o + b^{u\top} X_t^u \end{array} \right. \\
\text{Law of motion under } P & \quad \left\{ \begin{array}{l} X_t^o = \mu^o + \rho^{oo} X_{t-1}^o + \rho^{ou} X_{t-1}^u + \Sigma^{oo} \varepsilon_t^o \\ X_t^u = \mu^u + \rho^{uo} X_{t-1}^o + \rho^{uu} X_{t-1}^u + \Sigma^{uo} \varepsilon_t^o + \Sigma^{uu} \varepsilon_t^u \end{array} \right. \quad (9) \\
\text{Law of motion under } Q & \quad \left\{ \begin{array}{l} X_t^o = \bar{\mu}^o + \bar{\rho}^{oo} X_{t-1}^o + \bar{\rho}^{ou} X_{t-1}^u + \Sigma^{oo} \eta_t^o \\ X_t^u = \bar{\mu}^u + \bar{\rho}^{uo} X_{t-1}^o + \bar{\rho}^{uu} X_{t-1}^u + \Sigma^{uo} \eta_t^o + \Sigma^{uu} \eta_t^u \end{array} \right.
\end{aligned}$$

where all the matrices are obtained by separating into blocks the matrices in equations (1-3).

The following proposition, proved in the Appendix, gives the minimal set of restrictions to be imposed in order to identify the model:

**Proposition 1** *Let  $\bar{\rho}$  have distinct and real eigenvalues. Then model (9) always admits an equivalent representation (eventually after renaming the unobservable factors and the error terms) with the following restrictions:*

- $b^u = \bar{1}$  (a vector of 1s)
- $\bar{\mu}^u = 0$
- $\bar{\rho}^{uo} = 0$
- $\bar{\rho}^{uu}$  is diagonal
- $\Sigma^{oo}$  and  $\Sigma^{uu}$  are lower triangular

We impose the above set of minimal restrictions on the models we estimate. Proposition (1) allows us to understand restrictions imposed by models previously proposed in the literature. For example, Ang and Piazzesi's (2003) model, which can be re-parametrized as a special case of the general model in (9), imposes a set

of over-identifying restrictions equivalent to the following:  $\rho^{uo} = 0$ ,  $\rho^{ou} = 0$ ,  $\bar{\rho}^{ou} = 0$  and  $\Sigma^{uo} = 0$ . Hördahl, Tristani and Vestin (2005) also build a model which is a special case of (9): they impose on the  $P$ -dynamics a set of restrictions which are derived from a structural model of the economy using Söderlind's (1999) procedure and they specify the dynamics under  $Q$  with a restricted parametrization of the prices of risk  $\lambda_0$  and  $\lambda_1$ . Another structural model encompassed as a special case by (9) is derived in Rudebusch and Wu (2005).

Note that within this Gaussian framework bond yields are affine functions of the state variables:

$$y_t^n = -\frac{1}{n} \ln(p_t^n) = A_n + B_n^\top X_t \quad (10)$$

where  $y_t^n$  is the yield at time  $t$  of a bond maturing in  $n$  periods and  $A_n$  and  $B_n$  are coefficients obeying the following simple system of Riccati equations, derived from (4):<sup>2</sup>

$$A_1 = a \quad (11)$$

$$B_1 = b \quad (12)$$

$$\dots \quad (13)$$

$$A_n = \frac{1}{n} \left[ a + (n-1) \left( A_{n-1} + B_{n-1}^\top \bar{\mu} - \frac{n-1}{2} B_{n-1}^\top \Sigma \Sigma^\top B_{n-1} \right) \right] \quad (14)$$

$$B_n = \frac{1}{n} [b + (n-1) \bar{\rho}^\top B_{n-1}] \quad (15)$$

The yields  $\tilde{y}_t^n$  and the bond prices  $\tilde{p}_t^n$  that would obtain in an arbitrage-free market populated by risk neutral investors are instead obtained setting the prices of risk to zero ( $\lambda_t = 0$ ) in (7) and (8):

$$\tilde{p}_t^n = E_t^P [\exp(-r_t) \tilde{p}_{t+1}^{n-1}] \quad (16)$$

They obey the same system of recursive equations (11), where  $\bar{\mu}$  and  $\bar{\rho}$  are substituted by  $\mu$  and  $\rho$ . Subtracting the risk-neutral yields  $\tilde{y}_t^n$  thus calculated from the actual yields  $y_t^n$  one obtains the risk premiums  $\pi_t^n$ :

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<sup>2</sup>A proof by induction for a more general case can be found, for example, in Dai, Singleton and Yang (2003).

$$\pi_t^n = y_t^n - \tilde{y}_t^n \quad (17)$$

$\pi_t^n$  is the additional interest per unit of time required by investors to bear the risk associated with the fluctuations in the price of a bond expiring in  $n$  periods. Such premiums are in general time varying and they are constant only when  $\rho = \bar{\rho}$ .

### 3. The data

For our empirical analysis of the term structure we rely on a dataset of zero coupon rates extracted from German government bond yields and recorded at a monthly frequency, provided by the Deutsche Bundesbank : the yield curve consists of ten maturities, from 1 to 10 years. Since we estimate the model at a monthly frequency, we also include a one-month interest rate taken from the money market, as a control. The sample goes from January 1973 to September 2004 and the yields are registered on the last trading day of each month. We utilize all the eleven maturities to carry out estimation of the models. In this respect our paper differs from most existing studies, which select only small subsets of the available maturities and typically do not employ yields of maturities longer than five years. We prefer not to exclude a priori any maturity from our sample, because we are also interested in understanding the capability of the models to fit the entire yield curve.

We include two macroeconomic variables in our model: an inflation rate and a measure of the output gap. The inflation rate is the twelve-month growth rate of the German consumer price index. The output gap is derived from industrial production, applying band-pass filters with different frequency ranges (2-4, 3-5 and 2-8 years), as in Baxter and King (1995). We rely on industrial production to construct a measure of the output gap, because it is available at monthly frequency and it is widely considered a coincident indicator of the business cycle.

#### 4. Empirical evidence

The first step in our estimation strategy is to select the number of unobservable variables to include in the model. We estimate three models, all having inflation and the output gap as observable variables. The three models have one, two and three unobservable variables respectively and are estimated imposing only the minimal set of identifying restrictions given in Proposition 1.

The models are estimated by maximum likelihood using Chen and Scott's (1993) methodology: given a set of parameters, observed bond prices are used to infer the values of the unobservable factors (see the Appendix for details). In order to do so, one has to assume that a number of bonds equal to the number of unobservable factors are exactly priced and their prices are measured without error: we choose the 3-year bond for the model with one unobservable factor and we add first the 5-year and then the 10-year when we increase the number of unobservable variables to two and three. Different choices of the set of exactly priced bonds do not seem to change parameter estimates significantly, as long as shorter maturities (up to 2 years) are excluded from the set. The estimated standard deviations of the pricing errors on longer maturities are always very small (usually less than 5 basis points), indicating that the assumption of exact pricing is not overly restrictive for these maturities. On the contrary, when shorter maturities are not assumed to be exactly priced, the estimated standard deviations of their errors are quite high (in some cases more than 50 basis points), suggesting that one should exclude these maturities from the set of exactly priced bonds.

Due to the highly non-linear dependence of the likelihood function on the parameters of the risk-neutral distribution, numerical maximization is computationally quite burdensome. We find that a considerable increase in speed is achieved using the simulated annealing algorithm (this should also avoid local maxima) and using a Schur decomposition (see Meyer - 2001) to parametrize the matrix  $\rho$  and the block  $\bar{\rho}^{oo}$  of the matrix  $\bar{\rho}$ . We use the following Schur decomposition of an  $n$ -dimensional

square matrix  $A$  (Khuri - 2002):

$$A = UTU^\top \quad (18)$$

$$U = (I - Q)(I + Q)^{-1} \quad (19)$$

where  $Q$  is skew-symmetric ( $n(n - 1)/2$  parameters),  $T$  is upper triangular ( $n(n + 1)/2$  parameters) and  $U$  is orthogonal by construction. By constraining the elements on the principal diagonal of  $T$  (as well as the elements on the diagonal of  $\bar{\rho}^{uu}$ ) to be strictly less than 1 in absolute value, we ensure that  $\rho$  and  $\bar{\rho}$  have all their eigenvalues inside the unit circle, so that the process  $X_t$  is stationary both under the physical and the risk neutral measure. Although at an optimum we never find the latter constraints to be binding, the constraints considerably restrict the parameter space where numerical search is performed, hence increasing speed.<sup>3</sup>

Standard information criteria (SBC and AIC) suggest that the model with three unobservable variables is the most appropriate to describe the joint dynamics of interest rates and macro variables, hence we comment the results obtained with this model. Note that, although no lags of inflation and output gap are explicitly included in our model, the unobservable factors provide a flexible device to eventually capture lagged effects of the variables in the system (both linear and non-linear).

All the models were estimated three times, one for each of the three frequency ranges used to filter the output gap. The correlations between the measures of risk premiums obtained in each estimation were always higher than 0.995, indicating that the results are robust to different choices of the measure of output gap. We report the results obtained with the widest frequency range (2-8 years).

Table 5 displays the coefficients of the estimated model. The standard errors are obtained numerically, using two-sided approximated first and second order derivatives. Since the log-likelihood of the sample is the sum of non-independent conditional log-likelihoods, we account for serial correlation in the scores by using a

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<sup>3</sup>The constraints are implicitly imposed parametrizing each constrained parameter  $p$  as  $p = 0.9999 \cdot \cos(\theta)$ , so that an unconstrained maximization algorithm can still be used.

Newey-West estimator to compute the long-run covariance matrix. The bandwidth is set equal to 12 months, in view of the fact that annual inflation can artificially induce autocorrelations up to the eleventh lag. Further enlarging the bandwidth does not seem to produce relevant changes in estimated standard deviations. Standard deviations are generally quite small, making most parameters significantly different from zero. An exception are some off-diagonal elements of  $\rho$ , which are close to zero and have high standard deviations. The inferences to be drawn from the model are not altered when we apply the two-stage procedure adopted, for example, by Dai and Singleton (2000), which consists in re-estimating the model imposing zero constraints on the parameters not significantly different from zero. We find that the restrictions  $\bar{\rho}^{ou} = 0$  and  $\Sigma^{uo} = 0$  imposed by Ang and Piazzesi (2003) are rejected at all conventional confidence levels in our sample. However, their restrictions do not have substantial consequences on estimated risk premiums (Table 2 and Figure 7). Instead, we find a dramatic change when we adopt their two-stage consistent estimation strategy, which consists in estimating the parameters  $a$ ,  $b^o$ ,  $\mu^o$ ,  $\rho^{oo}$  and  $\Sigma^{oo}$  in a first step and the remaining parameters in a second step. With their two-stage procedure, estimated risk premiums are on average lower and more variable (Table 2 and Figure 7) and more than 25 per cent of the times estimated risk premiums are negative at all maturities.

Figure 1 displays the time series of risk premiums for the 3, 5 and 10-year bonds, calculated as the difference between the yield that the market required on those bonds at any point in time and the yield that a risk-neutral investor would have required to hold the same bonds. It is evident that bond risk premiums display a considerable variability across time: for example, the premium on the 10-year bond, which averages 186 basis points throughout our sample, has a standard deviation of 72 points and reaches a peak of 388 basis points in March 1975 and a trough of 15 in March 1992. Table 1 reports more details about the sample distribution of risk premiums for all the maturities.

The average risk premium in our sample is increasing with maturity (see Figure 2): it is quite small for shorter maturity bonds (3 and 35 basis points for the 1 and 2-

year bonds respectively), it averages about one hundred points for the intermediate maturities (4 to 6 years) and reaches a maximum of 186 points for the 10-year maturity. Dividing the sample into two sub-samples (before and after 1990), we find that risk premiums have been lower during the last fifteen years. Also the variability of risk premiums is increasing with the maturity: the standard deviation is about 27 points for the 1-year bond and increases to about 72 points for the 10-year bond.

The variation of risk premiums over time seems to be strongly related to macroeconomic variables. In particular, high negative (partial) correlation with the output gap at all maturities (see Table 5<sup>4</sup>) suggests that the risk premiums are counter-cyclical. If one assumes positive correlation between consumption and production, this is consistent with the hypothesis that the price of future consumption is low (interest rates are high) when current consumption is low (hence current marginal utility is high). Moreover, an impulse response analysis carried out on some yields (see Figure 5) suggests that an increase in output causes a decrease in risk premiums. The link of risk premiums to inflation seems to be less evident: there is a small negative partial correlation between inflation and risk premiums on shorter maturity bonds, while the correlation is positive, but not statistically significant, for longer maturities. Note that the pricing equation (4) is defined in nominal terms, but it is fully equivalent to one defined in real terms, once a proper change of numeraire has been performed: hence, a correlation of risk premiums with inflation cannot be attributed to the fact that we are estimating the model with nominal quantities. The impulse-response analysis (Figure 6) shows that risk premiums tend to decrease slightly when inflation increases, but they eventually revert and then remain above the equilibrium level for some time.

Tables 3 and 4 show the variance decomposition of risk premiums and interest

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<sup>4</sup>The estimates of the regressions reported in Table 5 are to be interpreted as estimates of the coefficients of an orthogonal projection of the risk premiums on the two-macroeconomic variables. The regressions have therefore no structural interpretation, also in view of the fact that the regressors are endogenous, but they provide a joint evaluation of the predictability of risk premiums, which takes into account the correlation between predictors.



rates. Within our sample, the proportion of the variance of interest rates explained by macroeconomic fundamentals is never greater than 20 per cent. As a general rule, the proportion of variance explained by macroeconomic variables increases with the forecasting horizon and with the maturity of the bonds. When we look only at risk premiums, the proportion of variance explained by macro-factors dramatically increases, up to almost 50 per cent: shocks to output play a prominent role in determining unexpected changes in the risk premiums; inflation plays a relevant role only for shorter maturities. The fact that the proportion of variance explained by macro-factors is much higher for risk premiums than for yields might seem puzzling at first. However this is explained by the fact that the short-term interest rate is pro-cyclical and risk premiums are counter-cyclical: long-term bond yields, being a sum of the two, do not react much to output shocks because the separate effects of these shocks on premiums and the short rate compensate each other.

## 6. Conclusions

We have analyzed the dynamics of risk premiums on the German bond market, employing no-arbitrage multifactor affine term-structure models. We have followed the approach, recently popularized by Ang and Piazzesi (2003), of including both unobservable and observable variables in the set of state variables, in order to assess the link between macroeconomic fundamentals and risk premiums. We carried out a specification analysis, based on a new set of identifying conditions, in order to select the best model. We found that, even after including inflation and output gap in the set of state variables, three unobservable variables are still needed to describe accurately yield curve dynamics, confirming what is already well-established for models with latent variables only. We have proposed a methodology to quantify risk premiums, which gives easily interpretable measures of the additional interest per unit of time required by investors for bearing the risk associated with bond price fluctuations. Our sample provides evidence that such premiums are strongly time-varying and a considerable portion of this variability is due to output and inflation shocks. There is a systematic relation between output and premiums, the latter being countercyclical, but we find no systematic relation between inflation and

premiums. Both findings are consistent with the predictions of economic theory.

## Appendix

### 0.1 Proposition 1

**Proof.** The law of motion of the process under  $Q$  is:

$$X_t = \bar{\mu} + \bar{\rho}X_{t-1} + \Sigma\eta_t \quad (20)$$

Define a matrix  $C$  as follows:

$$C = \left[ e_1 \quad \dots \quad e_{k^o} \quad v_1^\top \quad \dots \quad v_{k^u}^\top \right]^\top \quad (21)$$

where:

$$e_1 = \left[ 1 \quad 0 \quad 0 \quad \dots \quad 0 \right]^\top \quad (22)$$

$$e_2 = \left[ 0 \quad 1 \quad 0 \quad \dots \quad 0 \right]^\top \quad (23)$$

$$\dots \quad (24)$$

are the first  $k^o$  vectors of the Euclidean basis of  $\mathbb{R}^{k^o+k^u}$  and  $v_1, \dots, v_{k^u}$  are  $k^u$  independent left eigenvectors of  $\bar{\rho}$ . Since  $\bar{\rho}$  has got distinct eigenvalues, it is always possible to choose  $v_1, \dots, v_{k^u}$  in such a way that  $C$  is invertible. Denote by  $\Lambda$  the diagonal matrix whose diagonal elements are the eigenvalues associated with  $v_1, \dots, v_{k^u}$  and define:

$$C^u = \left[ v_1^\top \quad \dots \quad v_{k^u}^\top \right]^\top \quad (25)$$

Pre-multiplying (20) by  $C$ , one obtains:

$$X_t^o = \bar{\mu}^o + \begin{bmatrix} \bar{\rho}^{oo} & \bar{\rho}^{ou} \end{bmatrix} X_{t-1} + \Sigma^{oo}\eta_t^o \quad (26)$$

$$C^u X_t = C^u \bar{\mu}^u + \Lambda C^u X_{t-1} + C^u \Sigma^{uo}\eta_t^o + C^u \Sigma^{uu}\eta_t^u \quad (27)$$

Transform the first equation in (26) as follows:

$$X_t^o = \bar{\mu}^o + \begin{bmatrix} \bar{\rho}^{oo} & \bar{\rho}^{ou} \end{bmatrix} X_{t-1} + \Sigma^{oo}\eta_t^o \quad (28)$$

$$= \bar{\mu}^o + \begin{bmatrix} \bar{\rho}^{oo} & \bar{\rho}^{ou} \end{bmatrix} C^{-1} C X_{t-1} + \Sigma^{oo}\eta_t^o \quad (29)$$

$$= \bar{\mu}^o + \begin{bmatrix} \bar{\rho}^{oo} & \bar{\rho}^{ou} \end{bmatrix} C^{-1} \left[ X_{t-1}^{o\top} \quad (C^u X_{t-1})^\top \right]^\top + \Sigma^{oo}\eta_t^o \quad (30)$$

Redefining  $X_t^u := C^u X_t$  and setting  $F = \begin{bmatrix} \bar{\rho}^{oo} & \bar{\rho}^{ou} \end{bmatrix} C^{-1}$  one gets:

$$X_t^o = \bar{\mu}^o + F X_{t-1} + \Sigma^{oo} \eta_t^o \quad (31)$$

$$X_t^u = C^u \bar{\mu}^u + \Lambda X_{t-1}^u + C^u \Sigma^{uo} \eta_t^o + C^u \Sigma^{uu} \eta_t^u \quad (32)$$

Since the eigenvectors of  $\bar{\rho}$  strictly lie inside the unit circle, it is possible to redefine  $X_t^u$  again as  $X_t^u := X_t^u - (I - \Lambda)^{-1} C^u \bar{\mu}^u$  so that it has zero mean. Multiplying each unobservable factor by its corresponding coefficient in  $b^u$ , one obtains the representation in Proposition 1 by appropriately matching the coefficients in Proposition 1 with those in (31) (note that redefining the unobservable factors also affects the law of  $X_t$  under  $P$ , so that in general no restriction can be imposed on the  $P$ -dynamics). ■

## 0.2 Inversion of yields

Suppose that at each time period bond yields of  $m$  (with  $m > k^u$ ) different maturities  $(n_1, n_2, \dots, n_m)$  are observable. Performing an "inversion" of  $k^u$  observable yields (in the spirit of Duffie and Kan - 1996 and Pang and Hodges - 1995), it is possible to express the unobservable factors as linear combinations of observable yields and observable factors. This procedure allows to recover a set of equations to be estimated where the unobservable factors do not appear:

$$\begin{cases} X_t^o = \alpha^o + \beta^{oo} X_{t-1}^o + \beta^{oe} y_{t-1}^e + T^{oo} \varepsilon_t^o \\ y_t^e = \alpha^e + \beta^{eo} X_{t-1}^o + \beta^{ee} y_{t-1}^e + T^{eo} \varepsilon_t^o + T^{eu} \varepsilon_t^u \\ y_t^f = \alpha^f + \beta^{fo} X_{t-1}^o + \beta^{fe} y_{t-1}^e + T^{fo} \varepsilon_t^o + T^{fu} \varepsilon_t^u \end{cases} \quad (33)$$

In the above system of equations  $y_t^e$  is the vector of  $k^u$  observable yields used to invert the unobservable factors,  $y_t^f$  is the vector containing the remaining  $m - k^u$  yields and the matrices  $\alpha^i$ ,  $\beta^{ik}$  and  $T^{ik}$  (of appropriate dimensions) are non-linear functions of the parameters of the model (the exact functional forms are reported below). Any choice of the  $k^u$  yields to be included in the vector  $y_t^e$  gives rise to

an equivalent representation of the system. (33) is a VAR, where the observable factors and  $k^u$  yields are regressed on their own lags, to which a system of regression equations explaining the remaining  $m - k^u$  yields has been adjoined. As it stands, the system can not be subjected to statistical estimation, because there are only  $k^u + k^o$  sources of error for a total of  $m + k^o > k^u + k^o$  equations to be estimated and the covariance matrix of the error terms is singular. The hypothesis usually made in order to estimate the system is that observed yields are subject to measurement or pricing errors, that is the econometrician does not observe  $y_t^e$  and  $y_t^f$ , but  $\tilde{y}_t^e$  and  $\tilde{y}_t^f$ , where:

$$\tilde{y}_t^e = y_t^e + D^e z_t^e \quad (34)$$

$$\tilde{y}_t^f = y_t^f + D^f z_t^f, \quad (35)$$

$z_t^e$  and  $z_t^f$  are  $k^u \times 1$  and  $(m - k^u) \times 1$  multivariate standard normal random vectors respectively and  $D^e$  and  $D^f$  are conformable matrices. It is often assumed (e.g. Chen and Scott - 1993 and Ang and Piazzesi - 2003) that the  $k^u$  yields in  $y_t^e$  are measured without error ( $\tilde{y}_t^e = y_t^e$ ): although theoretically restrictive, this assumption allows us to identify all the error terms, because it makes the number of errors equal to the number of equations; furthermore, both  $y_t^e$  and its lag  $y_{t-1}^e$  appear in the second equation of (33), hence if  $D^e \neq 0$  error terms are serially correlated and statistical estimation of (33) becomes much more involved.

Assuming exact pricing of  $y_t^e$ , the system of equations to be estimated is:

$$\begin{cases} X_t^o = \alpha^o + \beta^{oo} X_{t-1}^o + \beta^{oe} y_{t-1}^e + T^{oo} \varepsilon_t^o \\ y_t^e = \alpha^e + \beta^{eo} X_{t-1}^o + \beta^{ee} y_{t-1}^e + T^{eo} \varepsilon_t^o + T^{eu} \varepsilon_t^u \\ \tilde{y}_t^f = \alpha^f + \beta^{fo} X_{t-1}^o + \beta^{fe} y_{t-1}^e + T^{fo} \varepsilon_t^o + T^{fu} \varepsilon_t^u + D^f z_t^f \end{cases} \quad (36)$$

The above equations are simply regressions of the observable yields and the observable variables on one-period lags of the observable variables and the exactly priced yields. Although the same regressors appear on the right-hand side of all equations, OLS estimation is not feasible, because the regression coefficients and the covariance matrix are functions of the same parameters and cannot be estimated

independently. Following the majority of the literature on term-structure models, we propose maximum likelihood estimation of the system.

### 0.2.1 Functional form of the regression coefficients

The yields are affine in the observable and unobservable factors:

$$\begin{cases} y_t^e = A^e + B^{eo}X_t^o + B^{eu}X_t^u \\ y_t^f = A^f + B^{fo}X_t^o + B^{fu}X_t^u \end{cases} \quad (37)$$

Note that the coefficients  $A^i$  and  $B^{ij}$  are functions of the parameters of the process  $X_t$  under the risk-neutral measure  $Q$ . Lag the first equation by one period and invert, to obtain:

$$X_{t-1}^u = (B^{eu})^{-1} (y_{t-1}^e - A^e - B^{eo}X_{t-1}^o) \quad (38)$$

The VAR (under  $P$ ) is:

$$\begin{cases} X_t^o = \mu^o + \rho^{oo}X_{t-1}^o + \rho^{ou}X_{t-1}^u + \Sigma^{oo}\varepsilon_t^o \\ X_t^u = \mu^u + \rho^{uo}X_{t-1}^o + \rho^{uu}X_{t-1}^u + \Sigma^{uo}\varepsilon_t^o + \Sigma^{uu}\varepsilon_t^u \end{cases} \quad (39)$$

Substituting (38) into (39), we get:

$$\begin{cases} X_t^o = \mu^o + \rho^{oo}X_{t-1}^o + \rho^{ou}(B^{eu})^{-1}(y_{t-1}^e - A^e - B^{eo}X_{t-1}^o) + \Sigma^{oo}\varepsilon_t^o \\ X_t^u = \mu^u + \rho^{uo}X_{t-1}^o + \rho^{uu}(B^{eu})^{-1}(y_{t-1}^e - A^e - B^{eo}X_{t-1}^o) + \Sigma^{uo}\varepsilon_t^o + \Sigma^{uu}\varepsilon_t^u \end{cases} \quad (40)$$

Now, use the two equations in (40) to eliminate  $X_t^o$  and  $X_t^u$  from the two equations in (37) and adjoin the first equation in (40) to obtain the following system of regression equations, involving only observable variables (factors and yields):

$$\begin{aligned} y_t^e &= \alpha^e + \beta^{eo}X_{t-1}^o + \beta^{ee}y_{t-1}^e + T^{eo}\varepsilon_t^o + T^{eu}\varepsilon_t^u \\ y_t^f &= \alpha^f + \beta^{fo}X_{t-1}^o + \beta^{fe}y_{t-1}^e + T^{fo}\varepsilon_t^o + T^{fu}\varepsilon_t^u \\ X_t^o &= \alpha^o + \beta^{oo}X_{t-1}^o + \beta^{oe}y_{t-1}^e + T^{oo}\varepsilon_t^o \end{aligned} \quad (41)$$

where:

$$\alpha^e = A^e + B^{eo} (\mu^o - \rho^{ou} (B^{eu})^{-1} A^e) + B^{eu} (\mu^u - \rho^{uu} (B^{eu})^{-1} A^e) \quad (42)$$

$$\beta^{eo} = B^{eo} (\rho^{oo} - \rho^{ou} (B^{eu})^{-1} B^{eo}) + B^{eu} (\rho^{uo} - \rho^{uu} (B^{eu})^{-1} B^{eo}) \quad (43)$$

$$\beta^{ee} = B^{eo} \rho^{ou} (B^{eu})^{-1} + B^{eu} \rho^{uu} (B^{eu})^{-1} \quad (44)$$

$$T^{eo} = B^{eo} \Sigma^{oo} + B^{eu} \Sigma^{uo} \quad (45)$$

$$T^{eu} = B^{eu} \Sigma^{uu} \quad (46)$$

$$\alpha^f = A^f + B^{fo} (\mu^o - \rho^{ou} (B^{eu})^{-1} A^e) + B^{fu} (\mu^u - \rho^{uu} (B^{eu})^{-1} A^e) \quad (47)$$

$$\beta^{fo} = B^{fo} (\rho^{oo} - \rho^{ou} (B^{eu})^{-1} B^{eo}) + B^{fu} (\rho^{uo} - \rho^{uu} (B^{eu})^{-1} B^{eo}) \quad (48)$$

$$\beta^{fe} = B^{fo} \rho^{ou} (B^{eu})^{-1} + B^{fu} \rho^{uu} (B^{eu})^{-1} \quad (49)$$

$$T^{fo} = B^{fo} \Sigma^{oo} + B^{fu} \Sigma^{uo} \quad (50)$$

$$T^{fu} = B^{fu} \Sigma^{uu} \quad (51)$$

$$\alpha^o = \mu^o - \rho^{ou} (B^{eu})^{-1} A^e \quad (52)$$

$$\beta^{oo} = \rho^{oo} - \rho^{ou} (B^{eu})^{-1} B^{eo} \quad (53)$$

$$\beta^{oe} = \rho^{ou} (B^{eu})^{-1} \quad (54)$$

$$T^{oo} = \Sigma^{oo} \quad (55)$$

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# 1 Tables

**Table 1** - The empirical distribution of risk premiums over time

Sample Period: Jan 1973 to Sept 2004										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	0.03	0.35	0.65	0.91	1.13	1.32	1.48	1.62	1.75	1.86
Std deviation	0.27	0.39	0.48	0.55	0.60	0.64	0.67	0.69	0.70	0.72
Min	-0.80	-0.83	-0.75	-0.64	-0.50	-0.36	-0.21	-0.07	0.05	0.15
First quartile	-0.16	0.12	0.35	0.55	0.73	0.90	1.04	1.16	1.28	1.37
Median	0.06	0.36	0.66	0.92	1.11	1.30	1.45	1.60	1.71	1.81
Third quartile	0.22	0.61	0.94	1.25	1.52	1.73	1.88	2.02	2.16	2.27
Max	0.57	1.25	1.88	2.37	2.75	3.07	3.32	3.54	3.72	3.88

Sample Period: Jan 1973 to Dec 1989										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	0.05	0.42	0.76	1.05	1.29	1.50	1.67	1.82	1.96	2.08
Std deviation	0.27	0.36	0.45	0.51	0.56	0.59	0.61	0.63	0.64	0.65
Min	-0.52	-0.39	-0.27	-0.11	0.06	0.23	0.39	0.42	0.44	0.46
First quartile	-0.16	0.19	0.47	0.70	0.92	1.11	1.30	1.46	1.59	1.72
Median	0.07	0.42	0.78	1.06	1.29	1.48	1.64	1.80	1.94	2.04
Third quartile	0.24	0.67	1.07	1.42	1.70	1.90	2.04	2.18	2.31	2.43
Max	0.57	1.25	1.88	2.37	2.75	3.07	3.32	3.54	3.72	3.88

Sample Period: Jan 1990 to Sept 2004										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	0.00	0.26	0.52	0.75	0.94	1.11	1.25	1.38	1.50	1.60
Std deviation	0.26	0.39	0.48	0.55	0.60	0.63	0.66	0.68	0.69	0.71
Min	-0.80	-0.83	-0.75	-0.64	-0.50	-0.36	-0.21	-0.07	0.05	0.15
First quartile	-0.17	0.01	0.23	0.45	0.64	0.76	0.89	0.99	1.10	1.19
Median	0.03	0.31	0.56	0.76	0.93	1.08	1.21	1.32	1.44	1.53
Third quartile	0.19	0.49	0.79	1.05	1.24	1.42	1.57	1.68	1.81	1.92
Max	0.43	0.98	1.49	1.90	2.23	2.49	2.71	2.90	3.06	3.20

Moments and quartiles of the time series of estimated risk premiums (in percentage points).

**Table 2** - The empirical distribution of risk premiums over time  
 Comparison with restricted models (sample period: Jan 1973 to Sept 2004)

Unrestricted model										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	0.03	0.35	0.65	0.91	1.13	1.32	1.48	1.62	1.75	1.86
Std deviation	0.27	0.39	0.48	0.55	0.60	0.64	0.67	0.69	0.70	0.72
Min	-0.80	-0.83	-0.75	-0.64	-0.50	-0.36	-0.21	-0.07	0.05	0.15
First quartile	-0.16	0.12	0.35	0.55	0.73	0.90	1.04	1.16	1.28	1.37
Median	0.06	0.36	0.66	0.92	1.11	1.30	1.45	1.60	1.71	1.81
Third quartile	0.22	0.61	0.94	1.25	1.52	1.73	1.88	2.02	2.16	2.27
Max	0.57	1.25	1.88	2.37	2.75	3.07	3.32	3.54	3.72	3.88

Ang and Piazzesi's (2003) restrictions - one-stage estimation										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	0.01	0.34	0.64	0.90	1.12	1.31	1.47	1.60	1.72	1.83
Std deviation	0.22	0.34	0.44	0.51	0.57	0.60	0.63	0.65	0.67	0.68
Min	-0.67	-0.54	-0.44	-0.31	-0.17	-0.02	0.13	0.27	0.41	0.52
First quartile	-0.15	0.09	0.32	0.53	0.71	0.87	1.01	1.12	1.23	1.31
Median	0.00	0.31	0.60	0.84	1.05	1.24	1.41	1.54	1.68	1.78
Third quartile	0.14	0.58	0.95	1.27	1.51	1.71	1.85	2.02	2.15	2.25
Max	0.53	1.00	1.62	2.16	2.54	2.78	3.05	3.28	3.48	3.66

Ang and Piazzesi's (2003) restrictions - two-stage estimation										
Maturity	1	2	3	4	5	6	7	8	9	10
Mean	-0.20	0.03	0.20	0.32	0.41	0.48	0.52	0.55	0.57	0.59
Std deviation	0.71	0.70	0.73	0.76	0.80	0.82	0.84	0.86	0.88	0.89
Min	-2.28	-2.08	-1.91	-1.75	-1.68	-1.66	-1.65	-1.63	-1.61	-1.59
First quartile	-0.64	-0.33	-0.23	-0.19	-0.15	-0.10	-0.05	-0.05	-0.08	-0.06
Median	-0.09	0.09	0.24	0.41	0.53	0.54	0.61	0.64	0.66	0.68
Third quartile	0.31	0.53	0.72	0.84	1.01	1.09	1.16	1.20	1.22	1.23
Max	1.16	1.42	1.80	2.11	2.35	2.53	2.67	2.78	2.87	2.93

Moments and quartiles of the time series of estimated risk premiums (in percentage points).

**Table 3** - Risk premiums - variance decomposition

10 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	23.2	13.2	7.9	5.3	3.8	3.0	2.5	2.2	2.1	2.1
Output	22.4	28.9	28.4	26.3	23.9	21.7	19.6	17.6	15.7	14.1
Other factors	54.4	58.0	63.7	68.5	72.3	75.4	78.0	80.2	82.2	83.9

3 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	24.4	14.1	8.4	5.4	3.6	2.6	1.9	1.4	1.2	1.0
Output	21.3	27.9	27.6	25.4	23.1	20.8	18.7	16.7	14.9	13.2
Other factors	54.3	58.0	64.1	69.2	73.3	76.6	79.5	81.9	84.0	85.8

1 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	25.4	18.6	12.4	8.4	5.8	4.1	3.0	2.1	1.5	1.1
Output	18.8	25.0	24.2	21.4	18.5	15.9	13.7	11.7	10.0	8.6
Other factors	55.8	56.4	63.4	70.2	75.7	80.0	83.4	86.2	88.4	90.3

Variance decomposition of the errors in forecasting risk premiums. Contribution (in percentage points) of the orthogonalized disturbances relative to each factor to the mean-squared forecast error, for different forecasting horizons (1, 3 and 10 years).

**Table 4 - Yields - variance decomposition**

10 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	6.1	6.4	6.9	7.4	7.9	8.4	8.8	9.2	9.5	9.8
Output	13.8	11.6	9.7	8.3	7.3	6.5	6.0	5.6	5.3	5.0
Other factors	80.1	82.1	83.4	84.3	84.8	85.1	85.2	85.2	85.2	85.2

3 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	4.8	4.6	4.9	5.2	5.7	6.1	6.6	7.0	7.4	7.7
Output	13.3	10.7	8.4	6.6	5.3	4.4	3.7	3.2	2.9	2.6
Other factors	81.9	84.7	86.7	88.2	89.0	89.5	89.7	89.7	89.7	89.6

1 year forecasting horizon										
Maturity	1	2	3	4	5	6	7	8	9	10
Inflation	3.9	3.1	2.9	2.9	3.0	3.2	3.4	3.7	3.9	4.0
Output	9.6	8.4	7.0	5.9	4.9	4.2	3.7	3.3	3.0	2.7
Other factors	86.5	88.6	90.1	91.3	92.1	92.6	92.9	93.1	93.2	93.3

Variance decomposition of the errors in forecasting yields. Contribution (in percentage points) of the orthogonalized disturbances relative to each factor to the mean-squared forecast error, for different forecasting horizons (1, 3 and 10 years).

**Table 5** - Regressions of risk premiums on inflation and output gap

Maturity	1	2	3	4	5	6	7	8	9	10
Constant	0.19 (0.02)	0.51 (0.02)	0.79 (0.03)	1.03 (0.04)	1.22 (0.05)	1.38 (0.05)	1.52 (0.05)	1.64 (0.06)	1.74 (0.06)	1.82 (0.06)
Inflation	-0.05 (0.00)	-0.05 (0.01)	-0.05 (0.01)	-0.04 (0.01)	-0.03 (0.01)	-0.02 (0.01)	-0.01 (0.02)	0.00 (0.02)	0.01 (0.02)	0.01 (0.02)
Output Gap	-0.28 (0.02)	-0.44 (0.02)	-0.52 (0.03)	-0.56 (0.04)	-0.58 (0.05)	-0.58 (0.05)	-0.58 (0.05)	-0.57 (0.06)	-0.55 (0.06)	-0.54 (0.06)

**Table 6 - Parameter estimates**  
(continued on the next page)

$a_0$					
4.5923					
(0.1748)					
$a_1$		$a_2$		$a_3$	
1.4876		0.22231		1	
(0.0114)		(0.0035)		-	
$a_4$		$a_5$			
1		1		1	
-		-		-	
$\mu_1$		$\mu_2$		$\mu_3$	
0.10721		-0.04044		0.30042	
(0.0354)		(0.0902)		(0.1589)	
$\mu_4$		$\mu_5$			
-0.3377		-0.2132			
(0.3524)		(0.2703)			
$\bar{\mu}_1$		$\bar{\mu}_2$		$\bar{\mu}_3$	
-0.38181		2.5069		0	
(0.0227)		(0.2247)		-	
$\bar{\mu}_4$		$\bar{\mu}_5$			
0		0		0	
-		-		-	
$\rho_{i1}$		$\rho_{i2}$		$\rho_{i3}$	
$\rho_{1j}$	1.0014	-0.0141	0.0424	0.0429	0.0373
	(0.0614)	(0.0539)	(0.1393)	(0.1720)	(0.0478)
$\rho_{2j}$	0.0081	0.9837	-0.0662	-0.0816	-0.0016
	(0.0122)	(0.0207)	(0.0443)	(0.0504)	(0.0147)
$\rho_{3j}$	-0.0413	-0.3142	1.5011	0.6488	0.0000
	(0.1866)	(0.2221)	(0.0881)	(0.0721)	(0.0450)
$\rho_{4j}$	0.0579	0.3276	-0.5879	0.2527	0.0000
	(0.2230)	(0.1698)	(0.2295)	(0.1171)	(0.0510)
$\rho_{5j}$	-0.0212	0.1052	-0.1168	-0.1381	0.9287
	(0.1801)	(0.0637)	(0.2841)	(0.3254)	(0.0664)

The subscripts refer to: 1) Inflation 2) Output gap 3-5) Unobservable factors. Standard errors in parentheses.

	$\bar{\rho}_{i1}$	$\bar{\rho}_{i2}$	$\bar{\rho}_{i3}$	$\bar{\rho}_{i4}$	$\bar{\rho}_{i5}$
$\bar{\rho}_{1j}$	1.0261 (0.0063)	0.0062 (0.0017)	-0.5014 (0.0086)	-0.7066 (0.0155)	0.9965 (0.0167)
$\bar{\rho}_{2j}$	-0.2956 (0.0147)	0.9419 (0.0053)	3.2777 (0.0253)	4.5729 (0.0336)	-5.4499 (0.0200)
$\bar{\rho}_{3j}$	0 -	0 -	0.9928 (0.0020)	0 -	0 -
$\bar{\rho}_{4j}$	0 -	0 -	0 -	0.9905 (0.0024)	0 -
$\bar{\rho}_{5j}$	0 -	0 -	0 -	0 -	0.7421 (0.0175)

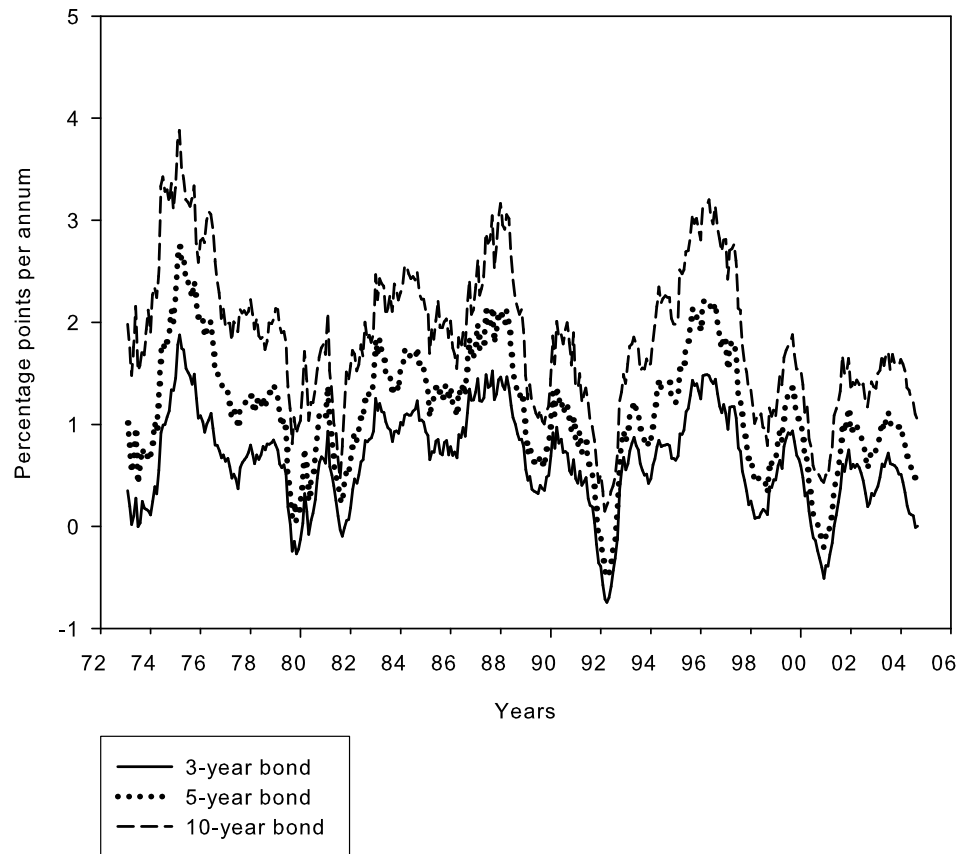
	$\Sigma_{i1}$	$\Sigma_{i2}$	$\Sigma_{i3}$	$\Sigma_{i4}$	$\Sigma_{i5}$
$\Sigma_{1j}$	0.3030 (0.0230)	0 -	0 -	0 -	0 -
$\Sigma_{2j}$	0.0076 (0.0073)	0.1270 (0.0100)	0 -	0 -	0 -
$\Sigma_{3j}$	-0.2212 (0.0120)	0.0812 (0.0234)	1.0621 0.0108	0 -	0 -
$\Sigma_{4j}$	0.2041 (0.0246)	-0.0756 (0.0144)	-1.0442 (0.0159)	0.1742 (0.0195)	0 -
$\Sigma_{5j}$	-0.3294 (0.0195)	0.0397 (0.0296)	-0.2054 (0.0253)	0.0000 (0.0234)	0.3317 (0.0314)

Standard deviations of pricing errors

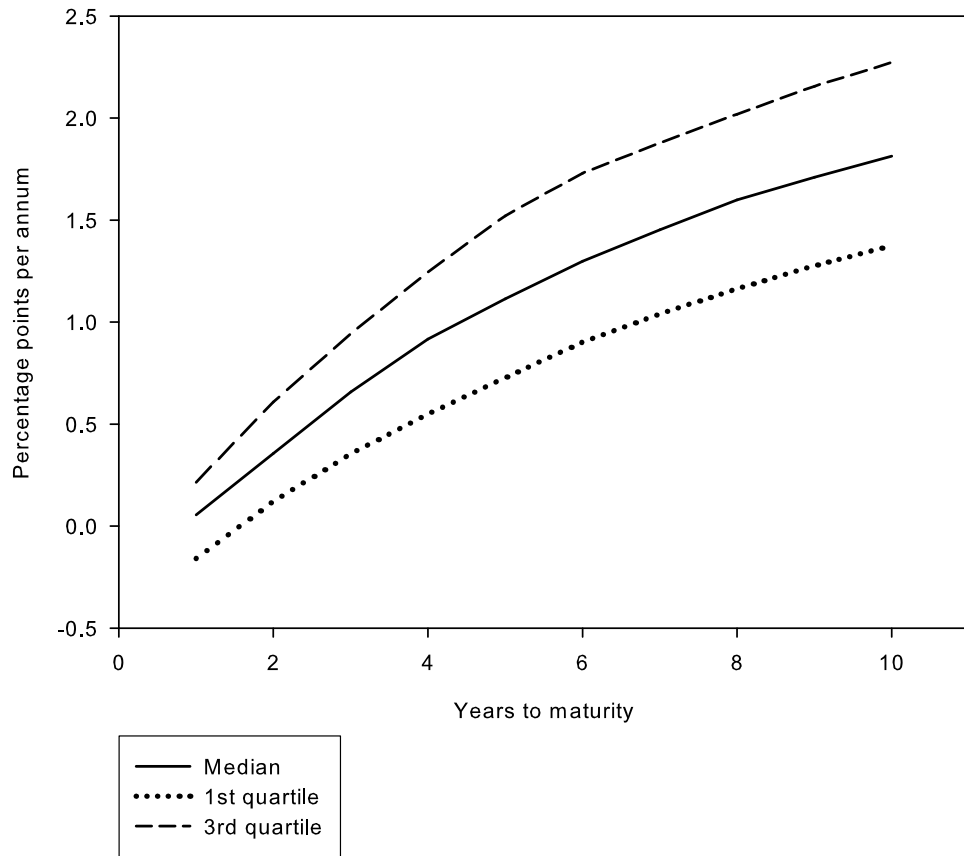
	1m	1y	2y	4y	6y
	0.7668 (0.0827)	0.3381 (0.0340)	0.0778 (0.0081)	0.0101 (0.0010)	0.0116 (0.0012)
	7y	8y	9y		
	0.0180 (0.0019)	0.0180 (0.0019)	0.0116 (0.0012)		



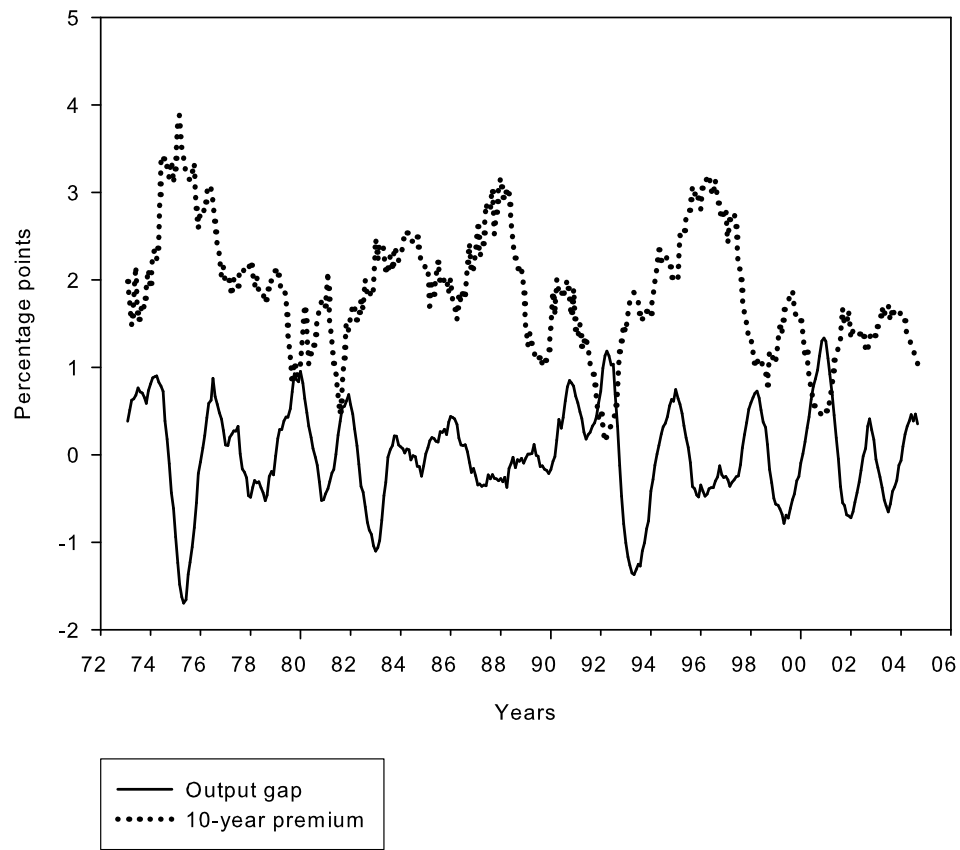
## 2 Figures



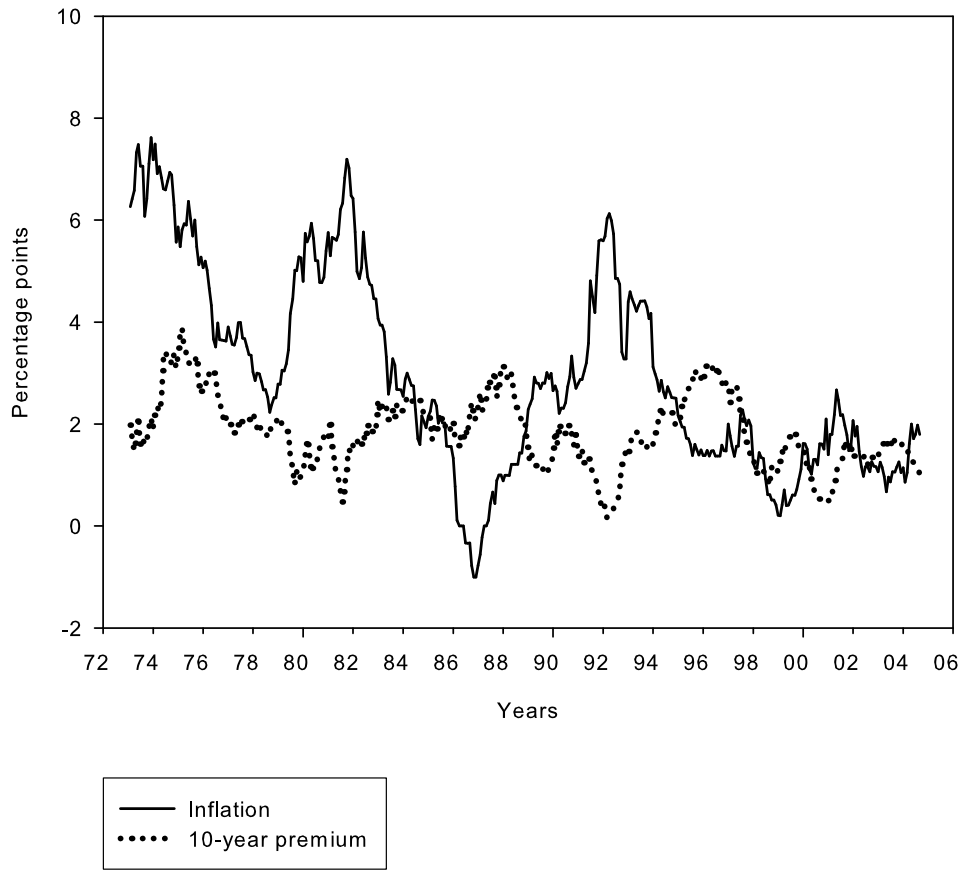
**Figure 1** - Risk premiums (in percentage points per annum) on bonds of different maturities.



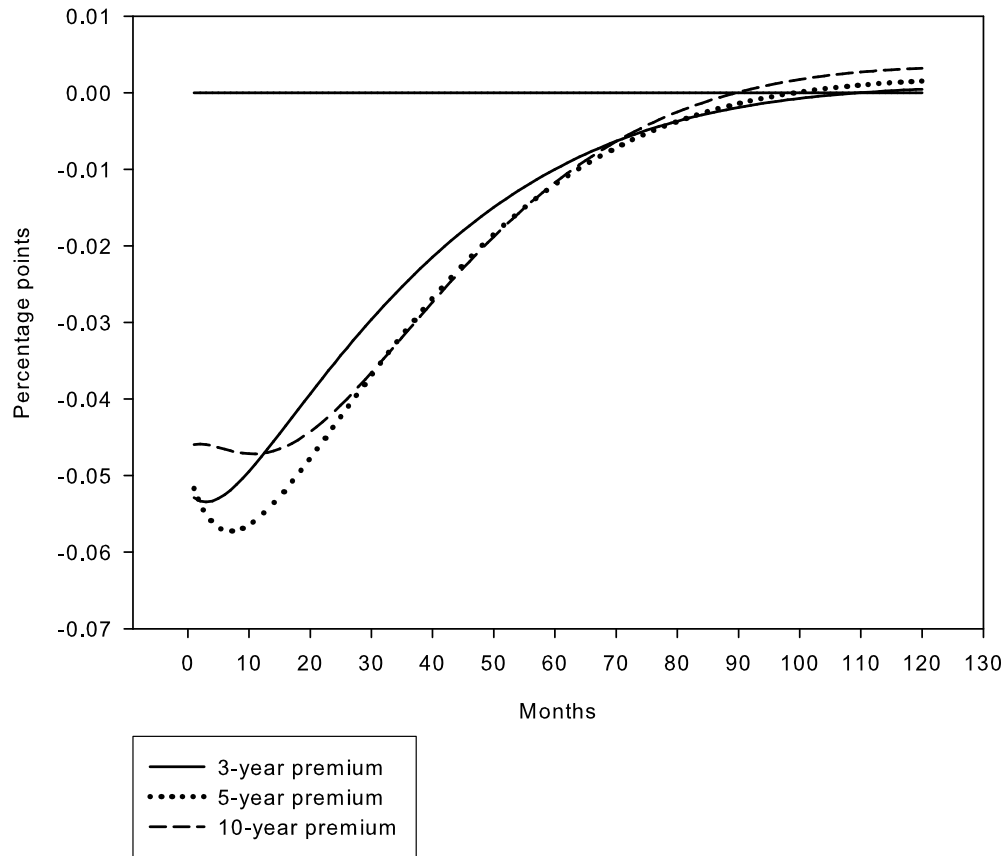
**Figure 2** - The term structure of risk premiums. The quartiles of the empirical distribution of estimated risk premiums are plotted against bond maturities.



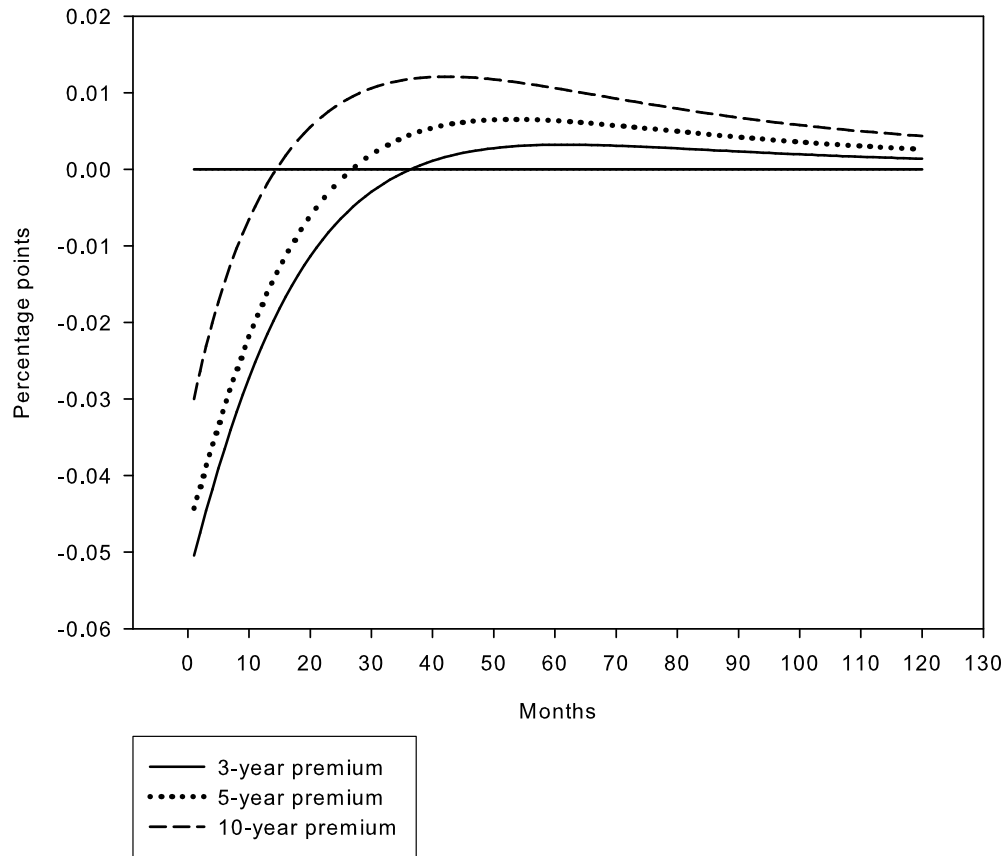
**Figure 3** - The output gap and the risk premium on the 10-year bond.



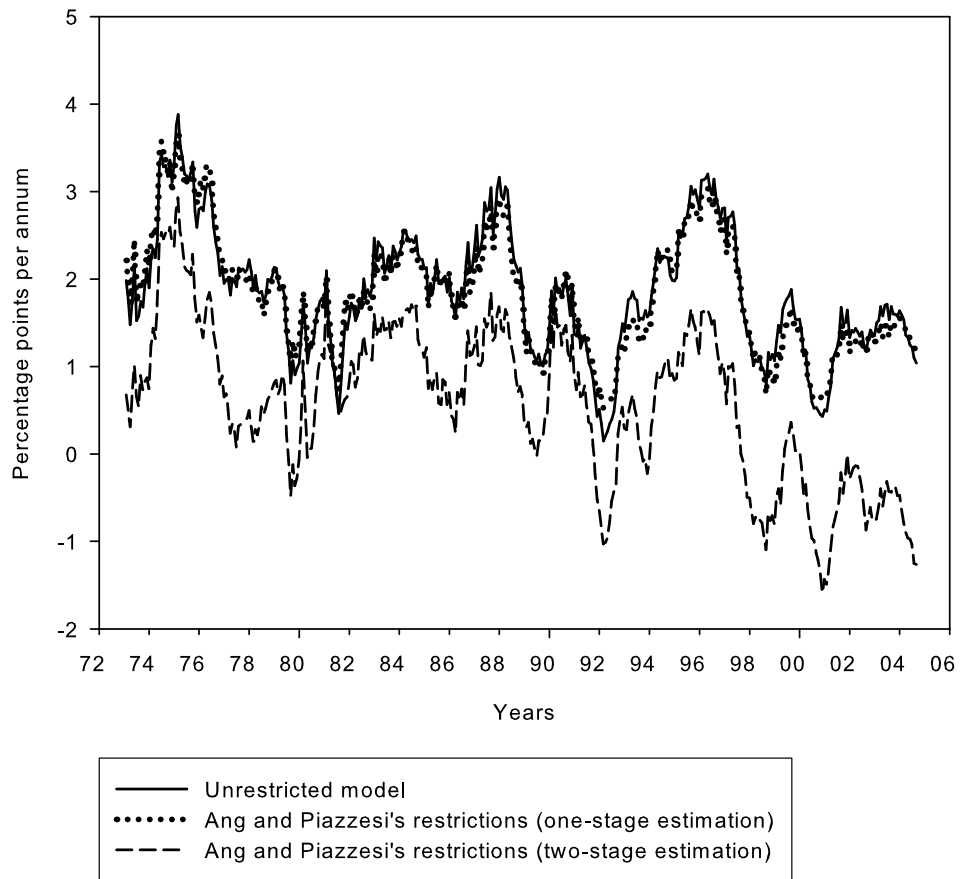
**Figure 4** - Inflation and the risk premium on the 10-year bond.



**Figure 5** - Impulse-response analysis. Response of risk premiums to a one standard deviation positive shock to output.



**Figure 6** - Impulse-response analysis. Response of risk premiums to a one standard deviation positive shock to inflation.



**Figure 7** - Risk premium on the 10-year bond. Comparison with restricted models.

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