

Biofuels Subsidies and the Green Paradox

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Abstract

This paper develops sufficient conditions under which the Weak Green Paradox may (and may not) hold in terms of subsidies for biofuel production such that the supply-side responses by fossil fuel producers may more than offset the substitution to biofuels. Analytical results are derived and numerical simulations show that, under a wide range of parameter values, biofuel subsidies will increase the rate of extraction of fossil fuels in the short and medium term, and possibly bring climate-change damages closer to the present.

JEL-Code: Q54, Q42, Q30.

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1 Introduction

Biofuels are widely regarded as a means to reduce greenhouse gas (GHG) emissions because they have the potential, relative to the fossil fuels they replace, to reduce GHG emissions. Consequently, biofuel subsidies have been promoted because of their potential environmental benefits (Hill et al. 2006). In 2006, in selected OECD countries, the total level of government support for biofuels exceeded \$10 billion (Steenblik, 2007). This is despite the fact that, one, a first-best instrument to control GHG emissions would be to establish a carbon tax or an equivalent cap-and-trade scheme and, two, biofuels production is blamed for some of the recent increases in prices of a number of food staples (FAO 2008).

Until very recently the supply-side dynamics of biofuel subsidies and their effects on inter-temporal extraction of fossil fuels have been ignored. The presumption has been that by increasing the supply of a readily-available substitute this would lower the price of fossil fuels, thereby lowering the incentive to extract.¹ However, if fossil fuel resource owners optimally extract their reserves and expect on-going or increased subsidies for biofuel production then they may *increase* their current levels of extraction.² It is even possible that this supply-side effect may overwhelm the substitution effect from fossil fuels to biofuels and increase GHG emissions leading to a Green Paradox (Sinn, 2008b). However, this would depend, among other factors, on the direct reduction in GHG emissions that arises from biofuel-fossil fuel substitution.³

¹A secondary argument is that with increased production of biofuels, technological progress will lower costs of production due to learning by doing.

²This is similar to the insights of Long and Sinn (1985) who investigate how extractive firms respond to anticipation of future tax changes.

³The extent to which direct biofuel-fossil fuel substitution reduces GHG emissions is a matter of some debate. An authoritative study on this issue indicates that with direct substitution there would be a reduction in GHG emissions of 12% for ethanol and 41% for biodiesel (Hill et al. 2006).

The possibility that adverse supply side effects may arise has been identified by Sinn (2008a) in the case of carbon taxes. Sinn's view is supported by Hoel (2008) using a model of investment in a backstop technology, and extends earlier work on the optimal trend of fossil fuel taxation (Sinclair 1992, Ulph and Ulph 1994). We show that this line of argument is equally valid in the context of biofuels subsidies. In other words, policies designed to reduce GHG emissions by subsidizing biofuel production may increase fossil fuel production. We define such an outcome as a Weak Green Paradox. In turn, increased fossil fuel consumption may raise atmospheric GHG concentration levels that would depend on many factors such as future technological change that may affect extraction costs, the reductions in GHG emissions from biofuel-fossil fuel direct substitution, and the effects of GHG concentration levels on the rate of carbon decay in the atmosphere. We define this second outcome as a Strict Green Paradox.

In this paper we develop formal models to study the conditions under which the Weak Green Paradox would (or would not) hold in the context of the direct subsidization biofuels production (such as in the US) or quantitative regulations that ensure minimum levels of biofuel consumption (such as in the EU). The analysis focuses on the supply response of fossil fuel producers, and the resulting general equilibrium changes in price paths and quantity paths.

In the simplest case where the supply curve of biofuels is upward sloping, and where biofuels are a perfect substitute for fossil fuels, at any *given* price of energy a subsidy on biofuel production will shift the biofuel supply curve to the right, resulting in a lower demand for fossil fuels. However, the equilibrium price path of energy is *not given*, because suppliers of fossil fuels will react to the biofuel subsidies. Thus, as soon as a credible time path in terms of the subsidy rate is announced or deduced, fossil fuel producers should adjust their output paths. Depending on supply and demand elasticities, this

may induce increased fossil fuel production.

We first investigate the possible effects of biofuel subsidies on the time path of fossil fuel extraction.⁴ In this approach, consumption of fossil fuels is equal to extraction from an aggregate stock of fossil-fuel resource, \bar{R} . If biofuel subsidies have the effect of hastening the exhaustion of the stock \bar{R} (i.e., shifting extraction of fossil fuels to the present), this allows for the possibility of a Weak Green Paradox which arises when fossil fuel production more than offsets the direct substitution to biofuels. We examine separately the cases of linear and non-linear demand, and extraction costs that depend on the remaining reserves.

In addition to analytical results, we provide numerical simulations of the effects on fossil fuel production from biofuels subsidies under a range of parameter values. We also present a set of sufficient conditions for fossil fuel production to increase in the presence of biofuel subsidies, and sufficient conditions when it fails to hold. Overall, our findings indicate that biofuel subsidies could increase fossil fuel production in the foreseeable future and, thus, result in a Weak Green Paradox.

2 Weak Green Paradox: competitive extraction

This section presents a model of energy demand in a perfectly competitive world, and shows that increased fossil fuel production can more than offset substitution to biofuels due to subsidies for biofuel production.

In our model, there are two consumption goods: a numeraire good (leisure) and a manufactured good. The latter good uses fuels as an input. The demand for the manufactured good gives rise to the demand for fuels. Assume

⁴There are a number of studies of biofuel subsidies (e.g. Chakravorty et al., 2009, Bahel Marrouch, 2009) and but they do not focus on the effect of subsidies on the date of exhaustion of the fossil-fuel stock.

there are two types of fuels: fossil fuels and biofuels. For simplicity, we assume they are *perfect substitutes*.

Let P_t denote the market price of fuels at time t . The present moment is $t = 0$. Assume that the world economy's demand for fuels is

$$E_t^d = D(P_t)$$

where $D'(\cdot) < 0$.

Assume that biofuel producers receive a constant *ad valorem* subsidy rate $\theta \geq 0$, i.e. for each unit they sell, they receive $(1 + \theta)P_t$. Let $z \equiv 1 + \theta \geq 1$. We call z the “subsidy factor”, where $z = 1$ indicates that the subsidy rate is zero. Let B_t denote the quantity of biofuels supplied. The supply function of biofuels is

$$B_t = S_B(zP_t)$$

where we assume $S'_B > 0$ and $S_B(0) = g \geq 0$.

At time $t = 0$, there is a fixed aggregate stock of fossil fuels, \bar{R} . The suppliers of fossil fuels are far-sighted and perfectly competitive extractive firms. They perfectly forecast the equilibrium price path $P(t)$ which they take as given. We assume that the marginal cost of extraction is a constant $c \geq 0$. If extraction rates are strictly positive over some time interval $[0, T]$ then, by Hotelling's Rule,⁵ the “net price” (i.e. price minus extraction cost) $P_t - c$ must rise at a rate equal to the rate of interest, i.e.

$$\frac{\dot{P}_t}{P_t - c} = r \text{ for } t \in [0, T]. \quad (1)$$

The demand for fossil fuels is defined as the difference between the demand for fuels and the supply of biofuels:

$$D_f(P; z) \equiv D(P) - S_B(zP) \quad (2)$$

⁵See Gaudet (2007) for a survey of theoretical and empirical studies on Hotelling's Rule.

We call $D_f(P; z)$ the residual demand function. Given z , there is a unique price \bar{P} such that the supply of biofuels just matches the demand for fuels. The price \bar{P} is implicitly defined by

$$D(\bar{P}) - S_B(z\bar{P}) = 0 \quad (3)$$

Clearly, $P(t)$ cannot rise above \bar{P} . We call \bar{P} “the choke price for fossil fuels”. Notice that \bar{P} depends on the subsidy factor z . A higher z implies a lower \bar{P} . For ease of reference, we state this result as Fact 1:

Fact 1: $\bar{P} = \bar{P}(z)$ and its derivative is given by

$$\frac{d\bar{P}}{dz} = -\frac{\frac{\partial D_f(\bar{P}; z)}{\partial z}}{\frac{\partial D_f(\bar{P}; z)}{\partial P}} = \frac{\bar{P}S'_B(z\bar{P})}{D'(\bar{P}) - zS'_B(z\bar{P})} < 0 \quad (4)$$

Market equilibrium requires that the stock of fossil fuels be exhausted exactly at the (endogenously determined) time T when P reaches \bar{P} . We will show below how the exhaustion date T and the initial price P_0 depend on the subsidy factor z . In what follows, we assume that $\bar{P} > c$. By definition, the price of fuels at the exhaustion time T is equal to the the choke price for fossil fuels, \bar{P} :

$$P_T = \bar{P}$$

From Hotelling’s Rule, the present value of the net price is the same for all $t \in [0, T]$:

$$(P_t - c)e^{-rt} = (\bar{P} - c)e^{-rT} \text{ for all } t \leq T$$

i.e., for all $t \leq T$,

$$P_t = c + (\bar{P} - c)e^{r(t-T)} = c + [\bar{P}(z) - c] e^{r(t-T)} \equiv \phi(\bar{P}(z), t, T) \quad (5)$$

Note that the function $\phi(\bar{P}(z), t, T)$ has the following properties:

$$\frac{\partial \phi(\bar{P}(z), t, T)}{\partial T} = -r [\bar{P}(z) - c] e^{r(t-T)} = -r(P_t - c) < 0 \quad (6)$$

and

$$\frac{\partial \phi(\bar{P}, t, T)}{\partial \bar{P}} = e^{r(t-T)} > 0 \quad (7)$$

To determine T , we use the equilibrium condition that total demand for fossil fuels over the time interval $[0, T]$ is exactly equal to the initial stock \bar{R} :

$$\int_0^T D_f(P_t; z) dt = \bar{R} \quad (8)$$

where P_t is given by eq (5). In other words, the following equation uniquely determines the resource-exhaustion date T :

$$\int_0^T D_f(\phi(\bar{P}(z), t, T); z) dt = \bar{R} \quad (9)$$

We seek the answer to the following question: does an increase in the subsidy factor z bring the exhaustion time T closer to the present? If the answer is “yes”, then we say that the Weak Green Paradox is confirmed. As a first step, let us state a useful Lemma:

Lemma 1: *An increase in the subsidy factor z will bring the resource-exhaustion date T closer to the present if and only if*

$$\int_0^T \left[\frac{\partial D_f}{\partial P_t} \frac{\partial \phi}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial D_f}{\partial z} \right] dt > 0 \quad (10)$$

Proof: Let

$$G(T, z, \bar{R}) \equiv \int_0^T D_f(\phi(\bar{P}(z), t, T); z) dt - \bar{R} \quad (11)$$

The equilibrium condition that the stock of resources is exhausted at time T , i.e. $G(T, z, \bar{R}) = 0$, implicitly determines T as a function of z . The derivative dT/dz is given by

$$\frac{dT}{dz} = - \frac{\frac{\partial G(T, z, \bar{R})}{\partial z}}{\frac{\partial G(T, z, \bar{R})}{\partial T}} \quad (12)$$

where

$$\frac{\partial G(T, z, \bar{R})}{\partial T} = D_f(\phi(\bar{P}(z), T, T); z) + \int_0^T \frac{\partial D_f}{\partial \phi} \frac{\partial \phi}{\partial T} dt > 0 \quad (13)$$

and

$$\frac{\partial G(T, z; \bar{R})}{\partial z} = \int_0^T \left[\frac{\partial D_f}{\partial P_t} \frac{\partial \phi}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial D_f}{\partial z} \right] dt \quad (14)$$

■

In general, the sign of the right-hand side of equation (14) is uncertain. Let us consider a few special cases.

2.1 Weak Green Orthodox: linear demand

Let us consider the special case where the fuel demand function $D(\cdot)$ is linear,

$$D(p) = a - bP, \quad a > 0, b > 0$$

and the biofuel supply function is

$$S_B(zP) = g + \beta(zP)^\mu, \quad \beta > 0, \mu > 0$$

where g is a constant. Then the demand function for fossil fuels is

$$D_f(P; z) \equiv a - bP - g - \beta(zP)^\mu$$

The “fossil fuel choke price” $\bar{P}(z)$ is implicitly defined by

$$a - b\bar{P} - g - \beta(z\bar{P})^\mu = 0$$

Thus

$$\frac{d\bar{P}}{dz} = -\frac{\mu\beta z^{\mu-1}(\bar{P})^\mu}{b + \mu\beta z^\mu(\bar{P})^{\mu-1}} < 0$$

The integrand in equation (10) is

$$\frac{\partial D_f}{\partial p_t} \frac{\partial \phi}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial D_f}{\partial z} = [b + \mu\beta z^\mu (P_t)^{\mu-1}] e^{r(t-T)} \frac{\mu\beta z^{\mu-1}(\bar{P})^\mu}{b + \mu\beta z^\mu(\bar{P})^{\mu-1}} - \mu\beta z^{\mu-1} (P_t)^\mu \quad (15)$$

If $\mu = 1$, this integrand expression reduces to

$$\frac{\partial D_f}{\partial p_t} \frac{\partial \phi}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial D_f}{\partial z} = \beta [\bar{P}e^{r(t-T)} - P_t]$$

which is equal to

$$-\beta c [1 - e^{-r(T-t)}] \leq 0 \quad (16)$$

From Lemma 1 and equation (16), we can state a result that does not support the Weak Green Paradox:

Proposition 1: *Assume that the demand function for fuels and the supply function of biofuels are both linear. Then under perfectly competitive extraction,*

(i) *if extraction costs are zero ($c = 0$), an increase in the biofuel subsidy factor z will have no effect on the date of exhaustion of the resource stock \bar{R} ;*

(ii) *if extraction costs are positive ($c > 0$), an increase in the biofuel subsidy factor z will delay the date of exhaustion of the resource stock \bar{R} .*

2.2 Weak Green Paradox: non-linear demand

An unattractive feature of the linear demand specification is that the demand for fuels becomes zero at some finite price. Many people would argue that the demand for fuels is always positive at any finite price. Let us consider the case where the demand for fuels is of the form

$$E^d = (P + \delta)^{-\varepsilon} \equiv D(P) \quad (17)$$

where $\delta \geq 0$ and $\varepsilon > 0$.

The demand function (17) may be derived from the demand for the manufactured good. For example, suppose that to produce one unit of the manufactured good, one needs to use one unit of fuels and one unit of labor. Let P be the price of fuels and δ be the wage rate. Assume perfect competition and constant returns to scale in the manufactured good industry. Then the price of the manufactured good is equal to its unit cost, which is the sum of P and δ :

$$P_M = P + \delta$$

Assume the demand for the manufactured good is

$$Q^d = (P_M)^{-\varepsilon} \equiv D_M(P_M)$$

where $\varepsilon > 0$ is the elasticity of demand for the manufactured good:

$$\varepsilon = -\frac{P_M}{Q^d} \left(\frac{dQ^d}{dP_M} \right) > 0$$

By choice of units of measurement, $E^d = Q^d$. From this we obtain the fuel demand function (17). The elasticity of demand for fuels is denoted by η where

$$\eta \equiv -\frac{P}{E^d} \frac{dE^d}{dP} = -\frac{(P_M - \delta)}{Q^d} \left(\frac{dQ^d}{dP_M} \right) = \varepsilon + \frac{\delta}{Q^d} \frac{dQ^d}{dP_M} \quad (18)$$

Therefore η is smaller than or equal to ε , with equality holding only in the case where $\delta = 0$.

We continue to assume that the supply function of biofuels is of the form

$$S_B(zP) = g + \beta(zP)^\mu, \quad \beta > 0, \mu > 0, z > 0 \quad (19)$$

Then the (residual) demand for fossil fuels is

$$D_f(P; z) = (P + \delta)^{-\varepsilon} - g - \beta(zP)^\mu$$

and \bar{P} satisfies

$$(\bar{P} + \delta)^{-\varepsilon} - g - \beta(z\bar{P})^\mu = 0$$

From this, we get

$$\frac{d\bar{P}}{dz} = -\frac{\beta\mu z^{\mu-1}(\bar{P})^\mu}{\varepsilon(\bar{P} + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(\bar{P})^{\mu-1}} < 0$$

The integrand in equation (10) is

$$I(\phi(\bar{P}(z), t, T); z) \equiv \frac{\partial D_f}{\partial p_t} \frac{\partial \phi}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial D_f}{\partial z} =$$

$$e^{r(t-T)} \left[\frac{\beta\mu z^{\mu-1}(\bar{P})^\mu (\varepsilon(P_t + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(P_t)^{\mu-1})}{\varepsilon(\bar{P} + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(\bar{P})^{\mu-1}} \right] - \beta\mu z^{\mu-1}(P_t)^\mu$$

Let us formalize our result as follows:

Assumption A: *The fuel demand function has the form (17) and the biofuel supply function has the form (19).*

Proposition 2: *Under Assumption A, an increase in the subsidy factor z will bring the exhaustion date closer to the present if and only if*

$$\int_0^T \left\{ e^{r(t-T)} \left[\frac{\beta\mu z^{\mu-1}(\bar{P})^\mu (\varepsilon(P_t + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(P_t)^{\mu-1})}{\varepsilon(\bar{P} + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(\bar{P})^{\mu-1}} \right] - \beta\mu z^{\mu-1}(P_t)^\mu \right\} dt > 0$$

i.e.

$$\beta\mu z^{\mu-1}(\bar{P})^\mu \int_0^T \left\{ e^{r(t-T)} \left[\frac{\varepsilon(P_t + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(P_t)^{\mu-1}}{\varepsilon(\bar{P} + \delta)^{-\varepsilon-1} + \mu\beta z^\mu(\bar{P})^{\mu-1}} \right] - \left(\frac{P_t}{\bar{P}} \right)^\mu \right\} dt > 0 \quad (20)$$

This condition is satisfied under plausible specifications of parameter values.

Numerical examples

In our base-line scenario, the parameters are:

$$\varepsilon = \delta = \beta = \mu = 1, \quad r = 0.05, \quad c = g = 0 \quad (21)$$

Let the reserve size \bar{R} be large enough so that under this base-line scenario, the exhaustion time is $T = 100$ years.

Then we find that, starting at the initial subsidy factor $z = 1$, an increase in z leads to an earlier exhaustion time, that is,

$$\frac{dT}{dz} = -2.09$$

This shows that the Weak Green Paradox holds if the reserve size is such that $T = 100$. Is this result sensitive to the size of the reserve? Let us vary the reserve size so that T varies from 50 years to 200 years. We find that dT/dz remains negative, and not far different from -2.09 . Table 1 below reports the value dT/dz for various reserve sizes (and hence various T).

We also consider different initial subsidy levels, and keep $\varepsilon = \delta = \beta = \mu = 1$, $r = 0.05$, $c = g = 0$, $T = 100$. Table 2 reports the results and shows there is a Weak Green Paradox for this set of parameter values. Keeping $\beta = \delta = \mu = 1$, $r = 0.05$, $c = 0$, $T = 100$, we can also consider different values for demand elasticity ε of the manufactured good. These results are reported in Table 3. Finally, consider different values for supply elasticity of biofuels, μ . We find that the Weak Green Paradox holds for a wide range of μ , as reported in Table 4. As shown in this Table 4, with the exception of the first column where the supply elasticity of biofuels is small, an increase in the subsidy rate will hasten the exhaustion of fossil fuels.

3 Weak Green Paradox: cartel extraction

What happens if oil is supplied by a cartel that behaves like a monopolist?

We assume that the monopolist takes the subsidy factor z as a given constant. How does an increase in z affect the extraction path?

As in Section 2, the residual demand function facing the oil producer is

$$D_f(P; z) \equiv D(P) - S_B(zP)$$

The choke price for fossil fuels is \bar{P} , where $D(\bar{P}) - S_B(z\bar{P}) = 0$, and \bar{P} is decreasing in z , as we have stated in Fact 1, see equation (4). We continue to assume that \bar{P} is greater than the marginal cost of extraction, c .

Let R_t denote the monopolist's stock of reserves at time t , so that $R_0 = \bar{R}$ and $\dot{R}_t = -q_t$ where q_t is the extraction rate. We assume that the monopolist's extraction matches the demand for fossil fuels:

$$q_t = D_f(P_t; z)$$

The monopolist's optimization problem consists of choosing a time path of price $P_t \in [0, \bar{P}]$ and a terminal date T to maximize the present value of its

stream of discounted profit:

$$\max_{T, P_t} \int_0^T e^{-rt} [(P_t - c)D_f(P_t; z)] dt$$

subject to the constraint

$$\dot{R}_t = -D_f(P_t; z), \quad R_0 = \bar{R}$$

$$R_T \geq 0$$

Denote the elasticity of the demand for fossil fuels by $\theta_t(P_t; z)$

$$\theta_t(P_t; z) \equiv -\frac{P_t}{D_f} \left(\frac{\partial D_f}{\partial P_t} \right) > 0$$

Assumption B: *The elasticity of demand for fossil fuels is (i) greater than unity for sufficiently high P , and (ii) non-decreasing in P :*

$$\frac{\partial \theta_t(P_t; z)}{\partial P_t} \geq 0$$

Let ψ_t denote the current-value shadow price of the stock R_t and let H_t denote the current-value Hamiltonian. Then

$$H_t = (P_t - c)D_f(P_t; z) - \psi_t D_f(P_t; z)$$

The optimality conditions for the monopolist are⁶

$$P_t \left[1 - \frac{1}{\theta_t} \right] - c - \psi_t = 0 \Leftrightarrow \frac{\partial H_t}{\partial P_t} = 0$$

$$\dot{\psi}_t = r\psi_t$$

$$\psi_T \geq 0, \quad R_T \geq 0, \quad \psi_T R_T = 0$$

$$H_T = [P_T - c - \psi_T] D_f(P_T; z) = 0$$

⁶As is well known, the monopolist always restricts supply so that $\theta_t > 1$.

One can show that conditions imply that $\psi_T = P_T - c > 0$, $R_T = 0$, $P_T = \bar{P}$, $D_f(P_T; z) = 0$, and $\theta_T = \infty$. In particular, we obtain the Hotelling Rule for the monopolist: the present value of marginal profit is the same for all $t \in [0, T]$:

$$\left[\left(1 - \frac{1}{\theta_t(P_t; z)} \right) P_t - c \right] = (\bar{P} - c) e^{r(t-T)} \quad (22)$$

Equation (22) implicitly defines the monopolist's optimal price P_t as a function of \bar{P} , z , t and T :

$$P_t = \phi^m(\bar{P}(z), t, T; z) \quad (23)$$

Note that the function ϕ^m in (23) is of the same nature as the function ϕ in (5) but they do not have the same functional form. Furthermore, the function ϕ^m depends on z both via $\theta_t(P_t; z)$ and via \bar{P} .

Example 1: Let $D(P) = a - bP$ and $S_B = g + zP$, where $a - g > 0$. Then

$$\theta = -\frac{P}{D_f} \left(\frac{\partial D_f}{\partial P} \right) = \frac{(b+z)P}{(a-g-(b+z)P)}$$

Equation (22) reduces to

$$P_t = \frac{1}{2} \left[(\bar{P} - c) e^{r(t-T)} + c + \frac{a-g}{b+z} \right] \equiv \phi^m(\bar{P}(z), t, T; z)$$

Returning to the general case, we make use of (23) to determine the monopolist's optimal exhaustion time T . It is the value of T such that total accumulated extraction equals the initial reserve level \bar{R} :

$$\int_0^T D_f(\phi^m(\bar{P}(z), t, T; z); z) dt = \bar{R} \quad (24)$$

Lemma 2: *An increase in the subsidy factor z will bring the monopolist's resource-exhaustion date T closer to the present if and only if the following integral is positive:*

$$\int_0^T \left[\frac{\partial D_f}{\partial P_t} \left(\frac{\partial \phi^m}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial \phi^m}{\partial z} \right) + \frac{\partial D_f}{\partial z} \right] dt \quad (25)$$

Proof: Let

$$G^m(T, z, \bar{R}) \equiv \int_0^T D_f(\phi^m(\bar{P}(z), t, T); z) dt - \bar{R}$$

The equilibrium condition that the stock of resources is exhausted at time T , i.e. $G(T, z, \bar{R}) = 0$, implicitly determines T as a function of z . The derivative dT/dz is given by

$$\frac{dT}{dz} = -\frac{\frac{\partial G^m(T, z, \bar{R})}{\partial z}}{\frac{\partial G^m(T, z, \bar{R})}{\partial T}}$$

where

$$\frac{\partial G^m(T, z; \bar{R})}{\partial T} = D_f(\phi^m(\bar{P}(z), T, T; z); z) + \int_0^T \frac{\partial D_f}{\partial \phi^m} \frac{\partial \phi^m}{\partial T} dt > 0$$

and

$$\frac{\partial G^m(T, z; \bar{R})}{\partial z} = \int_0^T \left[\frac{\partial D_f}{\partial P_t} \left(\frac{\partial \phi^m}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial \phi^m}{\partial z} \right) + \frac{\partial D_f}{\partial z} \right] dt \quad (26)$$

■

In general, the sign of the right-hand side of equation (26) is uncertain. Thus, we consider a few special cases.

3.1 Linear demand for fuels and linear supply of bio-fuels

Let $D(P) = a - bP$ and $S_B = g + zP$ where $a - g > 0$. Then

$$\phi^m(\bar{P}(z), t, T; z) = \frac{1}{2} \left[(\bar{P} - c) e^{r(t-T)} + c + \frac{a - g}{b + z} \right]$$

and

$$\begin{aligned} & \frac{\partial D_f}{\partial P_t} \left(\frac{\partial \phi^m}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial \phi^m}{\partial z} \right) + \frac{\partial D_f}{\partial z} \\ &= -\frac{c}{2} (1 - e^{-r(T-t)}) \leq 0 \end{aligned}$$

Proposition 3: *Assume that the demand function for fuel and the supply function of biofuel are both linear. Then, under monopoly extraction,*

(i) if extraction costs are zero ($c = 0$), an increase in the biofuel subsidy factor z will have no effect on the date of exhaustion of the resource stock \bar{R} ;

(ii) if extraction costs are positive ($c > 0$), an increase in the biofuel subsidy factor z will delay the date of exhaustion of the resource stock \bar{R} .

3.2 Non-linear demand

In this subsection, we consider the case where Assumption A is satisfied. In addition, assume $\mu = 1$ and $g = 0$. Then $D_f = (P + \delta)^{-\varepsilon} - \beta z P$, and the elasticity of demand for fossil fuels is

$$\theta_t = \frac{[\varepsilon(P_t + \delta)^{-\varepsilon-1} + \beta z] P_t}{(P_t + \delta)^{-\varepsilon} - \beta z P_t} > 0 \text{ for } P_t < \bar{P}$$

Note that if $\beta z > 0$ and $\varepsilon \geq 1$ then $\theta_t > 1$ because

$$\theta_t > \frac{\varepsilon P_t}{P_t + \delta} \geq \varepsilon$$

It can be verified that Assumption B is satisfied. Equation (22) becomes

$$\left\{ P_t - \frac{[\varepsilon(P_t + \delta)^{-\varepsilon-1} + \beta z] P_t}{\varepsilon(P_t + \delta)^{-\varepsilon-1} + \beta z} - c \right\} - (\bar{P} - c) e^{r(t-T)} = 0 \quad (27)$$

or

$$\left\{ P_t - \frac{1}{\theta_t} P_t - c \right\} - (\bar{P} - c) e^{r(t-T)} = 0$$

Denote the right-hand side of equation (27) by $F(P_t, \bar{P}, t, T, z)$. Equation (27) yields the implicit function $P_t = \phi^m(\bar{P}(z), t, T; z)$. Then

$$\frac{\partial \phi^m}{\partial \bar{P}} = - \frac{\partial F / \partial \bar{P}}{\partial F / \partial P_t} = \frac{e^{r(t-T)}}{\left(1 - \frac{1}{\theta_t}\right) + P_t \frac{d}{dP_t} \left(\frac{1}{\theta_t}\right)} \equiv \frac{e^{r(t-T)}}{\Omega_t} > 0$$

Furthermore,

$$\frac{\partial \phi^m}{\partial z} = - \frac{\partial F / \partial z}{\partial F / \partial P_t}$$

where

$$\partial F/\partial z = -\frac{P_t}{\theta_t^2} \left(\frac{\partial \theta_t}{\partial z} \right) < 0$$

because

$$\frac{\partial \theta_t}{\partial z} = \frac{\beta P_t}{(D_f)^2} [D_f + P_t \varepsilon (P + \delta)^{-\varepsilon-1} + z P_t] > 0$$

In other words, a higher biofuel subsidy increases the elasticity of demand for fossil fuels at any given price. Consequently,

$$\frac{\partial \phi^m}{\partial z} = -\frac{\frac{\beta P_t^2}{(\theta_t D_f)^2} [D_f + P_t \varepsilon (P + \delta)^{-\varepsilon-1} + z P_t]}{\Omega_t} < 0$$

We can now compute the crucial expression in Lemma 2, condition (25):

$$\begin{aligned} & \frac{\partial D_f}{\partial P_t} \left(\frac{\partial \phi^m}{\partial \bar{P}} \frac{d\bar{P}}{dz} + \frac{\partial \phi^m}{\partial z} \right) + \frac{\partial D_f}{\partial z} \\ &= \frac{\varepsilon (P_t + \delta)^{-\varepsilon-1} + \beta z}{\Omega_t} \left(\frac{\bar{P} \beta e^{r(t-T)}}{\varepsilon (\bar{P} + \delta)^{-\varepsilon-1} + \beta z} + \frac{\beta P_t^2}{(\theta_t D_f)^2} [D_f + P_t \varepsilon (P + \delta)^{-\varepsilon-1} + z P_t] \right) - \beta P_t \end{aligned}$$

It appears that using this expression, the integral (25) can be positive or negative, depending on parameter values.

Proposition 4: *Under Assumptions A and B, the Weak Green Paradox is a possibility when fossil fuels are supplied by a cartel.*

4 A Two-country Model

We now turn to the case where there are two countries with different energy policies. For simplicity we do not consider game theoretic or food policy issues (Bandyopadhyay et al. 2009). The “home country” is the U.S. The “foreign country” is China. There is no biofuel production in China. Assume that U.S. biofuels are not exported to China (e.g. because of high transport costs or other barriers to trade, or because the U.S. production subsidies are only given to domestically earmarked consumption).

Let P_t be the world price of fossil fuels. Assume that China's inverse demand function for fuels is

$$P_t = A - \frac{1}{M^c} E_t^c$$

where E_t^c is the quantity demanded in China. Similarly, the US inverse demand function for fuels is

$$P_t = A - \frac{1}{M^u} E_t^u$$

Then M^c/M^u is a measure of China's market size relative to the U.S.'s market size. By an appropriate choice of units, we can set $M^u = 1$.

When the price is P_t , U.S. biofuel producers earn zP_t for each unit they sell domestically, where z is the subsidy factor. The biofuel supply function is $S_B = \beta(zP)^\mu$ and the U.S.'s residual demand for fossil fuels is $D_f^u = A - P - \beta(zP)^\mu$. Let \bar{P}_u be the solution of

$$A - \bar{P}_u - \beta(z\bar{P}_u)^\mu = 0 \tag{28}$$

Note that

$$\frac{d\bar{P}_u}{dz} = -\frac{z^{\mu-1}(\bar{P}_u)^\mu}{\frac{1}{\beta\mu} + z^\mu(\bar{P}_u)^{\mu-1}} < 0 \tag{29}$$

Given a positive constant subsidy factor $z > 0$, the world equilibrium consists of two phases. In the first phase, fossil fuels are consumed in both the U.S. and China. This phase ends at an endogenously determined time T^u , when P_t reaches the value \bar{P}_u . In the second phase, fossil fuels are only used in China, and U.S. energy demand is completely satisfied by biofuel production. The second phase ends at time T^w , when the world price of fossil fuels reaches the choke price A and China's demand for fossil fuels becomes zero.

Our task is to find out how the subsidy rate z influences the two critical times T^u and T^w , and how it influences the equilibrium price path of fossil fuels, and hence the rate of emissions of CO_2 at each point of time.

Let $D^w(t)$ be the world (US and China) demand for fossil fuels during phase I, and $D^c(t)$ be China's demand for fossil fuels in phase II. Let \bar{R} be the initial stock of fossil fuels. Equilibrium requires that the total use of fossil fuels equals its stock:

$$\int_0^{T^u} D^w(t)dt + \int_{T^u}^{T^w} D^c(t)dt = \bar{R} \quad (30)$$

We begin by evaluating the second integral on the left-hand side of (30). Assume zero extraction cost and perfect competition. Hotelling's Rule gives us,

$$P_t e^{-rt} = P(T_u) e^{-rT^u} = P(T^w) e^{-rT^w}$$

Given that $P(T^w) = A$ and $P(T_u) = \bar{P}_u$,

$$T^w - T^u = \frac{1}{r} (\ln A - \ln \bar{P}_u(z)) \equiv J(z)$$

This indicates that the length of Phase II is an increasing function of the subsidy factor z .

$$\frac{dJ}{dz} = -\frac{1}{r\bar{P}_u} \left(\frac{d\bar{P}_u}{dz} \right) > 0$$

China's oil consumption during Phase II is

$$\begin{aligned} \int_{T^u}^{T^w} D^c(P_t)dt &= M^c \int_{T^u}^{T^w} (A - P_t)dt = M^c \int_{T^u}^{T^w} (A - A^{-r(T^w-t)})dt \\ &= AM^c \left\{ T^w - T^u - \frac{1}{r} [1 - e^{-r(T^w-T^u)}] \right\} \\ &= AM^c \left\{ J(z) - \frac{1}{r} [1 - e^{-rJ(z)}] \right\} \equiv K(z) \end{aligned}$$

It is easy to verify that $K(z)$ is an increasing function: the higher is the biofuel subsidy factor in the U.S., the greater is China's total consumption in Phase II.

$$\frac{dK}{dz} = AM^c (1 - e^{-rJ(z)}) \frac{dJ}{dz} > 0$$

Let us turn to Phase I, in which fossil demands are positive in both countries. The total accumulated consumption of fossil fuels in Phase I must equal $\bar{R} - K(z)$:

$$\int_0^{T^u} [D_f^u(P_t) + D^c(P_t)] dt = \bar{R} - K(z)$$

where

$$P_t = \bar{P}_u e^{-r(T^u-t)} \equiv \phi(\bar{P}_u(z), t, T^u)$$

Define

$$G(T^u, z, \bar{R}) \equiv \int_0^{T^u} [D_f^u(\phi, z) + D^c(\phi)] dt - \bar{R} + K(z)$$

The effect of an increase in the subsidy factor z on T^u is given by

$$\frac{dT^u}{dz} = -\frac{\partial G/\partial z}{\partial G/\partial T^u}$$

where

$$\partial G/\partial T^u = D^c(\bar{P}_u) + \int_0^{T^u} \left[\frac{\partial D_f^u}{\partial P_t} + \frac{\partial D^c}{\partial P_t} \right] \frac{\partial \phi}{\partial T^u} dt > 0$$

and

$$\partial G/\partial z = \int_0^{T^u} \left[\left(\frac{\partial D_f^u}{\partial P_t} + \frac{\partial D^c}{\partial P_t} \right) \frac{\partial \phi}{\partial \bar{P}_u} \frac{d\bar{P}_u}{dz} + \frac{\partial D_f^u}{\partial z} \right] dt + \frac{dK}{dz}$$

where, using Hotelling's Rule, the integrand can be simplified to

$$z^{\mu-1} \mu \beta e^{r(t-T)} \left[\frac{1 + M_c + \mu \beta z^\mu (P_t)^{\mu-1}}{1 + \mu \beta z^\mu (\bar{P}_u)^{\mu-1}} - 1 \right]$$

which is positive if $\mu \simeq 1$.

What about the effect of an increase in z on T^w ?

$$\frac{dT^w}{dz} = \frac{dT^u}{dz} + \frac{dJ}{dz}$$

This expression is negative if and only if

$$-\int_0^{T^u} \left[\left(\frac{\partial D_f^u}{\partial P_t} + \frac{\partial D^c}{\partial P_t} \right) \frac{\partial \phi}{\partial \bar{P}_u} \frac{d\bar{P}_u}{dz} + \frac{\partial D_f^u}{\partial z} \right] dt - \frac{dK}{dz} + (\partial G/\partial T^u) \frac{dT^u}{dz} < 0$$

i.e. iff

$$- \int_0^{T^u} \left[\left(\frac{\partial D_f^u}{\partial P_t} + \frac{\partial D^c}{\partial P_t} \right) \frac{\partial \phi}{\partial \bar{P}_u} \frac{d\bar{P}_u}{dz} + \frac{\partial D_f^u}{\partial z} \right] dt - \left[\frac{dJ}{dz} \right] [AM^c(1 - e^{-rJ(z)}) - (\partial G/\partial T^u)] < 0$$

So, if $\frac{d\bar{P}_u}{dz}$ is sufficiently large in absolute value, an increase in biofuel subsidy will bring the resource exhaustion date closer to the present.

Proposition 5: *An increase in the subsidy factor z will lengthen Phase II and may shorten Phase I. The exhaustion date will be brought closer to the present if $\frac{d\bar{P}_u}{dz}$ is sufficiently large in absolute value.*

Remark: From equation (29), higher values of $\beta\mu$ will be favourable to the Green Paradox.

5 Weak Green Paradox with stock-dependent extraction costs

We now turn to an investigation of the possibility of a Weak Green Paradox result in the case where extraction costs are stock-dependent. In what follows, we consider a model where extraction cost rises as the remaining stock falls. There are two possible scenarios. In the first scenario, the marginal cost of extracting the ‘last drop of oil’, although high, is still below the choke price for fossil fuels, and therefore all the fossil fuel stock will eventually be exhausted. In the second scenario, the last drop of oil is prohibitively expensive to extract, and therefore firms will abandon their deposits without exhausting them.⁷ We investigate the possibility of the Weak Green Paradox in both cases.

⁷Some authors have therefore modeled the “resource exhaustion” in the sense of an “economic abandonment” of the deposit after the profitable part has been exploited (see for example Karp, 1984, Rubio and Escriche 2001, Salo and Tahvonen, 2001, Chou and Long, 2009, Fujiwara and Long, 2009).

5.1 A model of stock-dependent extraction costs

We assume that oil firms are perfectly competitive. They take the price path as given. Let $R_0 = \bar{R}$ denote the initial stock of the representative firm, and q_t denote its output at t . Let R_t be the stock that remains at time t . Then $\dot{R}_t = -q_t$. We postulate that the total cost of extracting q_t is linear in q_t for given R_t :

$$[c_0 + c_1 (\bar{R} - R_t)] q_t, \quad c_0 \geq 0, c_1 \geq 0, R_t \in [0, \bar{R}], R_0 = \bar{R}.$$

Then $c_0 + (\bar{R} - R_t)c_1$ is the marginal cost of extraction at time t . As the remaining stock R_t falls, the marginal extraction cost rises. If $R_t = 0$, the marginal extraction cost is $c_0 + c_1\bar{R}$. Thus $c_0 + c_1\bar{R}$ is the marginal cost of extracting the last drop of oil, and c_1 is the sensitivity of marginal cost to the remaining stock.

It is convenient to define a new state variable, Y_t , which represents accumulated extraction from date 0 to date t :

$$Y_t \equiv \bar{R} - R_t, \quad Y_0 = 0, \quad \dot{Y}_t = q_t$$

Then the marginal extraction cost function may be written as $C(q_t, Y_t) = c_0 + c_1 Y_t$.

As in the earlier sections, let the demand function for fuels be $E_t^d = D(P_t)$, $D' < 0$, where E^d is the quantity of fuels demanded. Let the supply function for biofuels be $B_t = S_B(zP_t)$, $S'_B > 0$. Then the demand for fossil fuels falls to zero at the “fossil fuel choke price” \bar{P} defined by

$$D(\bar{P}) - S_B(z\bar{P}) = 0$$

Since the representative oil firm’s marginal cost is $c_0 + c_1 Y_t$, and $Y_t \leq \bar{R}$, we conclude that:

(i) if $c_0 + c_1\bar{R} < \bar{P}(z)$ then the representative firm will eventually exhaust all its stock,

(ii) if $c_0 + c_1\bar{R} > \bar{P}(z)$, the representative firm will abandon its deposit when the reserve level falls to some positive level R_L defined by

$$\bar{c} - c_1(\bar{R} - R_L) = \bar{P}(z), R_L > 0 \quad (31)$$

We will consider these two cases separately. Before doing so, let us make some clarification about the Hotelling Rule which we will use to explore the Weak Green Paradox.

5.2 Hotelling Rule when extraction costs are stock-dependent

What is the correct Hotelling Rule if the marginal extraction cost depends on the stock? The answer depends on the assumption one makes about the behavior of the firms. If firms do not “internalize” the added future cost caused by its current extraction, the present value of net price (price minus marginal extraction cost) must be the same at any pair of dates (t, t')

$$[P_t - (c_0 + c_1Y_t)] e^{-rt} = [P_{t'} - (c_0 + c_1Y_{t'})] e^{-rt'} \quad (32)$$

or

$$P_t - (c_0 + c_1Y_t) = [P_{t'} - (c_0 + c_1Y_{t'})] e^{-r(t'-t)}$$

Differentiating with respect to t we get

$$\dot{P}_t - c_1\dot{Y}_t = r [P_{t'} - (c_0 + c_1Y_{t'})] e^{-r(t'-t)}$$

Taking the limit as $t' \rightarrow t$, we get the “*non-internalized*” Hotelling Rule⁸

$$\dot{P}_t - c_1\dot{Y}_t = r [P_t - (c_0 + c_1Y_t)] \quad (33)$$

⁸Solow and Wan (1976) considered a macro-model of resource extraction with a continuum of heterogeneous firms, and assumed each firm produces only at a point of time. By construction, these firms do not internalize the added cost, since each firm’s operating life is infinitesimally small. The authors obtained a kind of “non-internalized” evolution of price. For a discussion of Solow and Wan (1976), see Kemp and Long (2009).

On the other hands, if firms internalize the added future cost caused by its current extraction, then the correct Hotelling Rule is the following “*internalized Hotelling Rule*”⁹

$$\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)] \quad (34)$$

To prove that the rule (34) follows from optimizing behavior of far-sighted firms in the absence of externalities, consider the firm’s optimization problem

$$\max_{q_t, T} \int_0^T e^{-rt} [P_t - (c_0 + c_1 Y_t)] q_t dt$$

subject to $\dot{Y}_t = q_t$, $Y_0 = 0$ and $Y_T \leq \bar{R}$. Let λ_t be the co-state variable. The current-value Hamiltonian is

$$H = P_t q_t - (c_0 + c_1 Y_t) q_t + \lambda_t q_t$$

The necessary conditions include

$$\begin{aligned} P_t - (c_0 + c_1 Y_t) + \lambda_t &= 0 \\ \dot{\lambda}_t = r\lambda_t - \frac{\partial H_t}{\partial Y_t} &= r\lambda_t + c_1 q_t \end{aligned}$$

From these two equations, we obtain the “*internalized Hotelling Rule*”, $\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)]$.

In what follows, we will use the internalized Hotelling Rule.

5.3 Weak Green Paradox with stock-dependent extraction costs and finite exhaustion date

As we have stated above, if the marginal cost of extracting the last drop of oil, $c_0 + c_1 \bar{R}$, is lower than the fossil fuel choke price, $\bar{P}(z)$, then the entire stock \bar{R} will be exhausted at some time T . In this case, the Weak Green Paradox is said to hold if a marginal increase in z leads to an earlier exhaustion date.

⁹See Gaudet (2007) for a literature review of internalized Hotelling Rule.

To determine the exhaustion date T , we must solve the following system of differential equations

$$\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)]$$

$$\dot{Y}_t = D_f(P_t; z)$$

subject to three boundary conditions: $Y_0 = 0$, $Y_T = \bar{R}$, $P_T = \bar{P}(z)$. Once we have found T , we can investigate how T responds to an increase in the biofuel subsidy.

5.3.1 The linear demand case

Suppose the demand function $D_f(P; z)$ is linear. Let

$$D_f(P; z) = a - (b + \beta z)P, \quad a > 0, b > 0, \beta > 0, z > 0$$

Then

$$\bar{P}(z) = \frac{a}{b + \beta z}$$

Assume $\frac{a}{b + \beta z} > c_0 + c_1 \bar{R}$ so that the whole stock \bar{R} will be exhausted in finite time.

We must analyze the system

$$\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)]$$

$$\dot{Y}_t = a - (b + \beta z)P$$

subject to three boundary conditions: $Y_0 = 0$, $Y_T = \bar{R}$, $P_T = \bar{P}(z)$. The Appendix gives the solution.

In this case, we can show that the Weak Green Paradox does not hold. This is stated as Proposition 6 below.

Proposition 6: *If the demand function $D_f(P; z)$ is linear in P , and the entire stock \bar{R} is exhausted at some time T , then*

- (i) *an increase in the subsidy factor z will delay the exhaustion date,*
- (ii) *higher sensitivity of extraction cost with respect to the remaining stock results in a later exhaustion date.*

Proof:

From the assumption that $\frac{a}{b+\beta z} > c_0 + c_1\bar{R}$, let us define

$$\tilde{Y}(z) \equiv \frac{a}{c_1(b + \beta z)} - \frac{c_0}{c_1} > \bar{R}$$

In the Appendix, we show that the exhaustion date T is the unique positive solution of the following equation

$$\frac{(\rho_2 - \rho_1)}{\rho_2 e^{-\rho_1 T} - \rho_1 e^{-\rho_2 T}} = \left(\frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)} \right)$$

where ρ_1 and ρ_2 are functions of z :

$$\rho_2 = \frac{1}{2} \left(r + \sqrt{r^2 + 4rc_1(b + \beta z)} \right) > 0$$

$$\rho_1 = \frac{1}{2} \left(r - \sqrt{r^2 + 4rc_1(b + \beta z)} \right) < 0$$

Define

$$F(T, z) = \frac{(\rho_2 - \rho_1)}{\rho_2 e^{-\rho_1 T} - \rho_1 e^{-\rho_2 T}}$$

and

$$G(T, z) \equiv F(T, z) - \left(\frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)} \right)$$

To prove part (i), note that the effect on T of an increase in the subsidy z is

$$\frac{dT}{dz} = -\frac{\frac{\partial G}{\partial z}}{\frac{\partial G}{\partial T}}$$

We can show that

$$\frac{\partial G}{\partial T} = -\frac{\rho_1 \rho_2 (\rho_2 - \rho_1)^2 e^{\rho_2 T}}{\{\rho_2 e^{(\rho_2 - \rho_1)T} - \rho_1\}^2} [e^{\rho_2 T} - e^{(2\rho_2 - \rho_1)T}] < 0$$

and

$$\frac{\partial G}{\partial z} = \frac{\partial F}{\partial z} - \bar{R} [\tilde{Y}(z)]^{-2} \frac{d\tilde{Y}}{dz} > 0$$

since $\frac{\partial F}{\partial z} > 0$.

To prove part (ii), we use $\frac{dT}{dc_1} = -\left(\frac{\partial G}{\partial c_1}\right) / \left(\frac{\partial G}{\partial T}\right)$ and show that $\left(\frac{\partial G}{\partial c_1}\right) > 0$. ■

As a numerical example, let $a = 3, b = \beta = z = 1$ and $\bar{R} = 80$. We find the stock \bar{R} will be exhausted in 370 years. If the subsidy factor is $z = 1.1$, we find that T increases to 410 years. In this special case, the Weak Green Paradox does not hold, at least in the long run.

5.3.2 The non-linear demand case

We conclude our results with the more general case of a non-linear demand and suppose that

$$D_f(P, z) = (P + \delta)^{-\varepsilon} - \beta(zP)^\mu$$

Thus $\bar{P}(z)$ is the solution of

$$(P + \delta)^{-\varepsilon} - \beta(zP)^\mu = 0$$

The system to be analyzed is as follows:

$$\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)]$$

$$\dot{Y}_t = (P + \delta)^{-\varepsilon} - \beta(zP)^\mu$$

subject to three boundary conditions: $Y_0 = 0, Y_T = \bar{R}, P_T = \bar{P}(z)$. Unlike linear demand case, we cannot obtain an analytical solution.

Consider an example. Let $\varepsilon = \mu = \beta = \delta = 1$. Then \bar{P} is the solution of

$$\frac{1}{(P + 1)} - zP = 0$$

At $z = 1$, the fossil fuel choke price is 0.618. Assuming that $c_0 = 0.005$, $c_1 = 0.0001$ and $\bar{R} = 80$, we can solve for the current oil price $P(0) = 0.017$, and the exhaustion date $T \simeq 106.9$ years. These cost and oil reserve parameters imply that the current extraction cost/price ratio is 29%. Until the exhaustion date, costs in this case increases slightly from 0.005 to 0.013, but the fuel price increases faster from 0.017 to 0.618, and thus the relevant cost/price ratio at the exhaustion date is just 2%.

For fossil fuel producers to abandon extraction before reserves are exhausted, the subsidy must satisfy:

$$c_0 + c_1 \bar{R} = 0.013 > \bar{P}(z) \text{ or } z > 153.8$$

Does a small increase in z lead to an increase or a decrease in T ? The answer depends on various parameters, particularly cost sensitivity or c_1 . Our numerical simulations show that if extraction costs increase faster as the reserve depletes (a large value of c_1), then, starting from $z = 1$, a small increase in the subsidy will make oil reserves last longer (a larger T). On the other hand, if c_1 is small enough, then an increase in the subsidy may lead to earlier exhaustion. We illustrate this in Table 5 where the subsidy z is increased from 1 to 1.2 ($\Delta z = 0.2$). Table 5 illustrates it is possible to find a large range of cases where fossil fuel reserves are exhausted faster, and the Weak Green Paradox holds.

The findings in Table 5 do not imply the Weak Green Paradox is a general result. Indeed, if condition (31) holds, we can show that with linear demand and a marginal extraction costs that increases linearly with accumulated extraction, and without technological change, fossil fuel deposits are abandoned before exhaustion and a subsidy for biofuels production results in a smaller overall consumption of fossil fuels. In that case, we say that the Weak Green Paradox does not hold in the long run. However, the long run is very long (abandonment takes place at time infinity). Thus, even when

the Weak Green Paradox does not hold in the long run, our results indicate that it can plausibly hold in the short or medium term.

The time period over which the Weak Green Paradox holds is critically important. In terms of climate change and avoiding the severe impacts of climate change, what happens to cumulative emissions over the next 30 years interval is critical. It is this period of time that is likely to be the important period in terms of biofuels subsidies as we might reasonably assume that new, carbon neutral energy technologies will become more widespread beyond 30 years. Thus, in the time periods that matter we have real cause for concern that biofuel subsidies may actually encourage larger GHG emissions from fossil fuel combustion and increase the likelihood of the more severe impacts of climate change.

Another relevant issue is technological change that affects extraction costs and the net price path on non-renewables. Technological change would seem to be especially important in terms of stock-dependent extraction costs. Positive technological change should offset the effect of stock-dependent extraction, and may do so for a long time. The overall impact of technological change would depend on the relative changes of z over time, on the extent to which technological changes affect the extraction costs and the cost of biofuel production, and the nature of stock dependent costs.

6 Concluding Remarks

We examine some possible cases under which there may be a Weak Green Paradox lurking behind policies of biofuel subsidies whereby the supply-side response by fossil fuel producers more than offset any gains from substitution to biofuels. Whether the Weak Green Paradox holds or not depends on demand and supply elasticities, expected changes in subsidies, technological change in fossil fuel extraction and how extraction costs respond to changes

in remaining reserves.

Our results suggest that a Weak Green Paradox from biofuel subsidies is a real possibility: policies designed to reduce GHG emissions may, perversely, hasten climate change. Further development of our models is necessary to take into account game-theoretic issues, the effects of technological change on extraction costs, the impacts of GHG atmospheric concentrations and the rates of decay, and the GHG reductions from direct biofuel-fossil fuel substitution. Nevertheless, our findings are sufficiently well developed to require, at the very least, that policy makers carefully evaluate the supply-side effects of biofuel subsidies on the extraction rate of fossil fuels by resource owners.

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APPENDIX

Exhaustion with stock-dependent cost and linear demand

With the linear demand $D_f(P_t; z) = a - (b + \beta z)P_t$, the fossil fuel choke price is $\bar{P}(z) = \frac{a}{b + \beta z}$. Assume that the marginal cost of extracting the last drop of oil is lower than the fossil fuel choke price:

$$\bar{R} < \frac{a}{c_1(b + \beta z)} - \frac{c_0}{c_1} \equiv \tilde{Y}(z)$$

Consider the system

$$\dot{P}_t = r [P_t - (c_0 + c_1 Y_t)], \quad r > 0, c_0 > 0, c_1 > 0$$

$$\dot{Y}_t = D_f(P_t; z) = a - (b + \beta z)P_t, \quad a > 0, b > 0, \beta > 0, z > 0$$

subject to three boundary conditions: $Y_0 = 0$, $Y_T = \bar{R}$, $P_T = \bar{P}(z)$.

Write the system of differential equations in matrix form:

$$\begin{bmatrix} \dot{P} \\ \dot{R} \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} P \\ R \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \end{bmatrix}$$

where $a_{11} = r$, $a_{12} = -rc_1$, $a_{21} = -(b + \beta z)$, $a_{22} = 0$, $b_1 = -rc_0$ and $b_2 = a$. In simpler notation,

$$\dot{\mathbf{w}} = \mathbf{A}\mathbf{w} + \mathbf{b}$$

where $\det \mathbf{A} = a_{11}a_{22} - a_{12}a_{21} = -rc_1(b + \beta z) < 0$

$$\mathbf{A}^{-1} = \frac{1}{-rc_1(b + \beta z)} \begin{bmatrix} 0 & rc_1 \\ b + \beta z & r \end{bmatrix}$$

Define $\tilde{\mathbf{w}}$ by

$$\tilde{\mathbf{w}} = -\mathbf{A}^{-1}\mathbf{b}$$

Then

$$\tilde{\mathbf{w}} = \begin{bmatrix} \frac{a}{b + \beta z} \\ \frac{a}{(b + \beta z)c_1} - \frac{c_0}{c_1} \end{bmatrix} \equiv \begin{bmatrix} \tilde{w}_1 \\ \tilde{w}_2 \end{bmatrix}$$

Now let us define \mathbf{x} by

$$\mathbf{x} \equiv \mathbf{w} - \tilde{\mathbf{w}}$$

Let $\rho_1 < 0$ and $\rho_2 > 0$ be the characteristic roots,

$$\begin{aligned}\rho_{1,2} &= \frac{a_{11} + a_{22} \pm \sqrt{(a_{11} + a_{22})^2 - 4(a_{11}a_{22} - a_{12}a_{21})}}{2} \\ &= \frac{1}{2} \left(r \pm \sqrt{\Delta} \right) \text{ where } \Delta \equiv r^2 + 4rc_1(b + \beta z)\end{aligned}$$

Then the general solution is

$$\begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} = \begin{bmatrix} h_1 \\ -(a_{12})^{-1}(a_{11} - \rho_1)h_1 \end{bmatrix} \exp(\rho_1 t) + \begin{bmatrix} h_2 \\ -(a_{12})^{-1}(a_{11} - \rho_2)h_2 \end{bmatrix} \exp(\rho_2 t) \quad (35)$$

where h_1 and h_2 are constants (to be determined using boundary conditions).

Define

$$v_1 \equiv -(a_{12})^{-1}(a_{11} - \rho_1) = \frac{\rho_1 - r}{-rc_1} \quad (36)$$

$$v_2 \equiv -(a_{12})^{-1}(a_{11} - \rho_2) = \frac{\rho_2 - r}{-rc_1} \quad (37)$$

Setting $t = T$ in the matrix equation (35), and noting that have $x_1(T) = P_T - \tilde{w}_1 = 0$ and $x_2(T) = Y_T - \tilde{w}_2 = \bar{R} - \tilde{w}_2 \equiv \bar{R} - \tilde{Y}(z)$, we get two equations:

$$0 = h_1 \exp(\rho_1 T) + h_2 \exp(\rho_2 T) \quad (38)$$

$$\bar{R} - \tilde{Y}(z) = v_1 h_1 \exp(\rho_1 T) + v_2 h_2 \exp(\rho_2 T) \quad (39)$$

Equation (38) gives

$$h_1 = -h_2 \exp[(\rho_2 - \rho_1) T] \quad (40)$$

Substituting into equation (39) to get

$$\bar{R} - \tilde{Y}(z) = -v_1 h_2 \exp(\rho_2 T) + v_2 h_2 \exp(\rho_2 T)$$

Therefore

$$h_2 = \frac{\bar{R} - \tilde{Y}(z)}{(v_2 - v_1) \exp(\rho_2 T)} \quad (41)$$

Setting $t = 0$ in the matrix equation (35), we get two equations

$$P_0 - \bar{P}(z) = h_1 + h_2 \quad (42)$$

$$Y_0 - \tilde{Y}(z) = v_1 h_1 + v_2 h_2 \quad (43)$$

Since $Y_0 = 0$, substituting (40) and (41) into (43) we get

$$-\tilde{Y}(z) = \frac{\bar{R} - \tilde{Y}(z)}{(v_2 - v_1) \exp(\rho_2 T)} [v_2 - v_1 \exp[(\rho_2 - \rho_1) T]]$$

or

$$\frac{(v_2 - v_1) \exp(\rho_2 T)}{v_2 - v_1 \exp[(\rho_2 - \rho_1) T]} = \frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)} \quad (44)$$

Now, using (36), (37) and (44)

$$\frac{(\rho_2 - \rho_1) \exp(\rho_2 T)}{-\rho_1 + \rho_2 \exp[(\rho_2 - \rho_1) T]} = \frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)}$$

Let

$$\phi(T, z) \equiv \frac{(\rho_2 - \rho_1)}{-\rho_1 \exp[-\rho_2 T] + \rho_2 \exp[-\rho_1 T]}$$

The function $\phi(T, z)$ has the following properties: $\phi(0, z) = 1$, $\partial\phi(T, z)/\partial T < 0$ for all $T > 0$, and

$$\lim_{T \rightarrow \infty} \phi(T, z) = 0$$

It follows that the equation

$$\phi(T, z) = \frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)}$$

has a unique solution $T > 0$ (which depends on z).

Numerical examples

Suppose $\bar{R} = 80$, $r = 0.05$, $a = 3$, $b = \beta = z = 1$, $c_0 = 1$. Let $c_1 = 0.001$. Then

$$\tilde{Y}(z) = \frac{a}{(b + \beta z) c_1} - \frac{c_0}{c_1} = \frac{1}{c_1} \left(\frac{a}{b + \beta z} - c_0 \right) = \frac{0.5}{c_1} = 500$$

$$\rho_1 = -4.950975 \times 10^{-4}$$

$$\rho_2 = 5.0495098 \times 10^{-2}$$

The equation

$$\frac{(\rho_2 - \rho_1)}{-\rho_1 \exp(-\rho_2 T) + \rho_2 \exp(-\rho_1 T)} = \frac{\tilde{Y}(z) - \bar{R}}{\tilde{Y}(z)} = 0.84$$

yields the unique solution $T = 370$.

Now let z increase to 1.1. Then T increases from 370 years to 410 years.

If c_1 is higher, $c_1 = 0.002$, while $z = 1$ and $\bar{R} = 80$. It will take 394 years to exhaust \bar{R} .

Now let z increase to 1.1. Then T increases from 394 years to 475 years.

| | | | | | |
|-----------------|-------|-------|--------------|--------|--------|
| T | 50 | 75 | 100 | 150 | 200 |
| $\frac{dT}{dz}$ | -1.75 | -2.04 | -2.09 | -2.110 | -2.113 |

Table 1: Effect of a Biofuel Subsidy on Exhaustion Date for Different Fossil Fuel Reserve Sizes

| | | | | | |
|-----------------|------|-------|--------------|-------|-------|
| z | 0.5 | 0.75 | 1 | 1.5 | 2 |
| $\frac{dT}{dz}$ | -6.6 | -3.43 | -2.09 | -0.99 | -0.56 |

Table 2: Effect of a Biofuel Subsidy on Exhaustion Date for Different Initial Subsidy Levels

| | | | | | |
|-----------------|-------|-------|--------------|-------|-------|
| ε | 0.1 | 0.5 | 1 | 2 | 3 |
| $\frac{dT}{dz}$ | -0.35 | -1.34 | -2.09 | -2.89 | -3.32 |

Table 3: Effect of a Biofuel Subsidy on Exhaustion Date for Different Demand Elasticities of the Manufactured Good

| | | | | | |
|-----------------|-------------|-------|--------------|-------|-------|
| μ | 0.5 | 0.75 | 1 | 1.5 | 2 |
| $\frac{dT}{dz}$ | 1.45 | -2.07 | -2.09 | -3.88 | -3.75 |

Table 4: Effect of a Biofuel Subsidy on Exhaustion Date for Different Supply Elasticities of Biofuel

| Cost sensitivity parameter | Marginal extraction cost of the 'last drop' | Choke price of fuel when $z=1.2/z=1$ | ΔT | $\Delta T/\Delta z$ | Paradox/ No Paradox |
|----------------------------|---|--------------------------------------|------------|---------------------|---------------------|
| 0 | 0.005 | 0.54/0.618 | -0.270 | -1.35 | Paradox |
| 0.0001 | 0.013 | 0.54/0.618 | -0.176 | -0.88 | Paradox |
| 0.0002 | 0.021 | 0.54/0.618 | -0.077 | -0.39 | Paradox |
| 0.0003 | 0.029 | 0.54/0.618 | 0.025 | +0.13 | No Paradox |
| 0.0005 | 0.045 | 0.54/0.618 | 0.244 | +1.22 | No Paradox |

Table 5: Parameter Values for the Weak Green Paradox

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