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Simple Nonparametric Estimators for Unemployment Duration Analysis

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Abstract

We consider an extension of conventional univariate Kaplan-Meier type estimators for the hazard rate and the survivor function to multivariate censored data with a censored random regressor. It is an Akritas (1994) type estimator which adapts the nonparametric conditional hazard rate estimator of Beran (1981) to more typical data situations in applied analysis. We show with simulations that the estimator has nice finite sample properties and our implementation appears to be fast. As an application we estimate nonparametric conditional quantile functions with German administrative unemployment duration data.

Keywords: nonparametric estimation, censoring, unemployment duration

1 Motivation

More and more national governments make samples of administrative individual data available to the research community. As these data sets are large, applied researchers can use flexible statistical models for detailed data exploration. Existing estimators, however, are not always applicable because administrative data comes with important limitations as its data generating process can cause, among other things, various forms of censoring. The most common example in administrative data is an individual's wage, which is not observed below and above a certain limit. In this paper we suggest simple nonparametric estimators for conditional hazard rates and conditional quantile functions in the presence of censoring. We demonstrate that they can be directly applied to German administrative unemployment duration data.

Economic theory is often not fully conclusive for the specification of an econometric model as results are generally limited to partial effects. Being left without a full parametrization of the problem, empirical economists commonly apply classical models that are available in the main econometric software packages. In the case of unemployment duration these are, for example, the accelerated failure time or the proportional hazard model. These models impose restrictive conditions on the relationship between the regressors and the response that may not be met by the underlying empirical distribution (Koenker and Geling, 2001, Portnoy, 2004, Fitzenberger and Wilke, 2006). For this reason quantile regression is emerging as a popular alternative in applied economics, see Koenker and Biliias (2001), Machado and Portugal (2002), and others. In a (censored) quantile regression framework, however, the response may depend on the regressors in a variety of ways and it is difficult in an application to determine an appropriate functional form specification. For this reason this paper considers nonparametric estimators as they can provide beneficial information in this respect. In particular, we focus on conditional hazard rates and conditional quantile functions without imposing shape restrictions on the conditional density of the response. The resulting estimates provide insights into whether the shape of the functional is invariant across quantiles or they may detect important nonlinearities. We follow the nonparametric conditional hazard rate

estimator of Beran (1981) with the main difference that we use a nearest neighbour estimator (Yang, 1981) design. Akritas (1994) considers a similar estimation strategy and he derives asymptotic properties for this class of estimators.

We aim to convince applied researchers that our estimation strategy is an applicable solution to common empirical problems and take unemployment duration analysis as an example. A small application to German administrative data demonstrates the applicability of the estimator and it highlights the need for flexible functional form specifications. We perform simulations to study finite sample performance and computing time.

2 The Estimator

We consider a model for a pair of random variables (Y, X) with unknown joint distribution, where Y is a discrete response or duration and X is a continuous regressor. Let C denote a censoring variable. The duration Y and censoring C are assumed conditionally independent given x . Suppose there are $i = 1, \dots, n$ independent realisations Y_i, X_i and C_i . In our data, however, we have $i = 1, \dots, n$ observations (τ_i, ν_i, d_i) , where d_i is an indicator for censoring of Y_i with $d_i = 0$ if Y_i is censored and $\tau_i = \min(Y_i, C_i)$. The censoring of X can be from below and from above. If a realization of X falls below (or above) a threshold c_l (or c_u), it is set to any number $x_l < c_l$ (or $x_u > c_u$):

$$\nu_i = \begin{cases} x_l & \text{if } X_i < c_l \\ X_i & \text{if } c_l \leq X_i \leq c_u \\ x_u & \text{if } X_i > c_u. \end{cases}$$

Let $F(y|x)$ be the distribution function of Y given x and $S(y|x) = 1 - F(y|x)$ is the conditional survivor function. Let $h(y|x) = f(y|x)/S(y|x)$ be the conditional hazard rate with $f(y|x)$ as the conditional probability (mass) function. Our aim is to estimate the unknown conditional hazard rate and the conditional α quantile function $q_\alpha(x) = \inf\{y|S(y|x) \geq \alpha\}$.

The well-known classical Kaplan-Meier type estimator for the unconditional haz-

ard rate of the distribution of Y , $h(y)$, is

$$h_n(y) = \frac{\sum_{i=1}^n \mathbf{1}_{\tau_i=y} \mathbf{1}_{d_i=1}}{\sum_{i=1}^n \mathbf{1}_{\tau_i \geq y}}, \quad (1)$$

where $\mathbf{1}_\theta$ is the indicator function for the event θ . The numerator divided by n estimates the conditional probability $P(Y = y|d = 1)$ and the denominator divided by n estimates the survivor function of the response $P(Y \geq y)$. If in an application Y is continuous, it may be useful for finite sample reasons to use an evaluation grid on the support of Y and uniform weights in the neighborhood of each grid point y_j . The ordered grid points y_j satisfy $y_j - y_{j-1} - 2\Delta = 0$ with $\Delta > 0$. The numerator in equation (1) is then $\sum_{i=1}^n \mathbf{1}_{\tau_i \in [y-\Delta, y+\Delta]} \mathbf{1}_{d_i=1}$ and the denominator is $\sum_{i=1}^n \mathbf{1}_{\tau_i \geq y-\Delta}$. This is in fact rounding of τ_i towards the closest grid point. Alternatively, one may use kernel smoothing in the dimension of Y as done by e.g., McKeague and Utikal (1990) and Van Keilegom and Veraverbeke (2001).

In order to study regression problems with censored data, Beran (1981) suggests the so-called conditional Kaplan-Meier estimator (see also Van Keilegom, 1998). Beran assumes for simplicity ordered design points x on $[0, 1]$. In case of no censoring his estimator is equivalent to Stone's (1977) estimator. In the case of uniform weights $1/n$ it is the univariate Kaplan-Meier estimator.

Our estimation strategy additionally accounts for possible censoring of the regressor. For this reason we adopt the nearest neighbour design of Yang's (1981) SNN estimator. The SNN estimator for the density of the marginal distribution of X , $g(x)$, is defined as:

$$g_n(x) = \frac{1}{nb_n} \sum_{i=1}^n K\left(\frac{G_n(x) - G_n(\nu_i)}{b_n}\right),$$

where $G_n(x) = (1/n) \sum_{i=1}^n \mathbf{1}_{\nu_i \leq x}$ is the empirical distribution function and b_n is a bandwidth. In our model $G_n(x)$ is a uniformly consistent estimator for the marginal distribution of x for $x \in [c_l, c_u]$. The estimator g_n has also nice properties for other censoring schemes of X than considered in this paper if there is a consistent estimator for the marginal distribution. For example in case of random censoring of X , one can use the univariate Kaplan-Meier estimator. Yang (1981) shows mean squared and uniform convergence of g_n under several conditions on K and the choice

of b_n . For this reason we assume that K is a continuous density function and the bandwidth goes to zero as the sample size tends to infinity. We suggest the following estimator for $h(y|x)$:

$$h_n(y|x) = \frac{\sum_{i=1}^n \mathbf{1}_{\tau_i=y} \mathbf{1}_{d_i=1} K\left(\frac{G_n(x)-G_n(\nu_i)}{b_n}\right)}{\sum_{i=1}^n \mathbf{1}_{\tau_i \geq y} K\left(\frac{G_n(x)-G_n(\nu_i)}{b_n}\right)} \quad (2)$$

for $x \in [c_l, c_u]$. The numerator and the denominator estimate the conditional probabilities $P(Y = y|d = 1, X = x)$ and $P(Y \geq y|X = x)$ which are smoothed in the dimension of x . While Beran's (1981) estimator and our estimator can be used for the same purpose, our implementation is very intuitive and it does not require distinct values τ_i . The advantages and disadvantages of Yang's estimator carry over to the estimation of conditional hazard rates: it is sufficient to have a consistent estimate of the rank of the X_i . The SNN smoothing works like a variable bandwidth which extenuates the boundary problems of the locally constant smoothing approach. We do not present a rule for the bandwidth choice here, since in exploratory data analysis an eye ball based bandwidth choice is justifiable. Note that in case of arbitrary uniform weights K the estimator becomes the conventional Kaplan-Meier estimator.

According to Kaplan and Meier (1958), one can estimate the univariate survivor function with the product limit estimator:

$$S_n(y) = \prod_{y_j \leq y} (1 - h_n(y_j)),$$

with $h_n(y_j)$ as defined in equation (1), where y_j are the $j = 1, \dots, m$ points of support of Y . In our framework the $S(y|x)$ can then be estimated by

$$S_n(y|x) = \prod_{y_j \leq y} (1 - h_n(y_j|x)), \quad (3)$$

for $x \in [c_l, c_u]$ and $q_\alpha(x)$ can be estimated by

$$q_{n\alpha}(x) = \inf\{y | S_n(y|x) \geq \alpha\}. \quad (4)$$

Akritis (1994) derives asymptotic properties for the estimator of the conditional survivor function (3). Weak convergence can be established by an appropriate choice

of the bandwidth and under some technical assumptions. The numerator and the denominator of our estimator then converge to the conditional probabilities $P(Y = y|d = 1, X = x)$ and $P(Y \geq y|X = x)$, respectively. Akritas (1994) also derives an expression for the covariance function, but it is alternatively possible to use the bootstrap (Akritas, 1992). We follow the second approach because it appears to be more simple.

3 Simulation

We analyse the behaviour of estimator (4) for different functional relationships between X and Y and different distributions of error terms. We draw 500 random samples of size $n = 500$ or 5,000 for the models given in table 1. The specification of model 2 is adapted from Fan (1992) who investigates the behavior of kernel estimators in the mean regression model. In the following we focus mainly on the 0.3, 0.5 and 0.7 quantile function. As the kernel function we use the Epanechnikov kernel $K(x) = \max\{0.75(1 - x^2); 0\}$. As Y and C are continuous we round the τ_i 's to the first decimal point. We use three different bandwidths to analyze the sensitivity of the estimates with respect to the bandwidth choice. The mean runtime for one simulation is about 0.5 seconds for 500 observations and 2.5 seconds for 5,000 observations (AMD64 1.4 GHz, 64 Bit Linux, 64BIT Matlab v7.01) where we have $l = 1, \dots, 50$ grid points in the interval $[c_l, c_u]$ and 50 grid points on the support of y . This is evidently fast enough for real world applications.

In order to investigate the properties of our estimator in presence of a censored regressor, we censor the distribution of X on both sides. $\nu_i = 0$ if $X_i < 3$ and $\nu_i = 10$ if $X_i > 7$. Figure 1 illustrates the distribution of X and ν for one sample used in the simulation. 5% of the observations are on average affected by this data manipulation. Figure 2 presents the mean 0.3, 0.5 and 0.7 quantile functions as well as the 2.5%- and the 97.5%-quantile of the simulation distribution with $b_n = 0.1$ and the true quantile functions. The estimator generally recovers the true shape of the conditional quantile functions. The bias at both sides of the support of ν is due to two reasons: first, our estimator fits locally a constant. Therefore we have

| Model | Description |
|-------|--|
| 1 | $Y = X + \epsilon$, $X \sim N(5,1)$, $C \sim N(6.5,0.5)$ |
| a) | $\epsilon \sim N(0,0.5)$, 10% right censoring of Y_i |
| b) | $\epsilon \sim \exp(0.5)$, 20% right censoring of Y_i |
| c) | $\epsilon \sim N(0,0.2X)$, 10% right censoring of Y_i |
| 2) | $Y = \sin(0.75X) + 0.3 \cdot \epsilon$, $X \sim N(5,1)$, $C \sim N(6.5,0.5)$ |
| | $\epsilon \sim N(0,0.5)$, 10% right censoring of Y_i |

Table 1: Models for simulation study.

a boundary bias that starts at a distance of the bandwidth apart of the edge of observations. Second, G_n is inconsistent below c_l and above c_u . This aggravates the boundary bias but it does not affect interior estimates. Since we use the SNN smoothing we have a variable bandwidth given ν . The low density of ν at the boundaries implies a larger bandwidth given ν than in the interior of the support of ν .

Table 2 presents the mean squared error (MSE), the squared bias and variance of the estimator for the different models. We only present the result for the median as the results for other quantiles ($\alpha = 0.3$ and $\alpha = 0.7$) do not differ remarkably. The MSE is calculated by using

$$MSE = \frac{1}{500 \cdot 50} \sum_{k=1}^{500} \sum_{l=1}^{50} (\hat{q}_k(x_l) - q(x_l))^2.$$

It is apparent from the table that the estimator has the typical behaviour with respect to the bandwidth choice. In particular, there is a bandwidth which minimises the MSE. In our small numerical exercise it takes on the smallest value for $b_n = 0.1$ in all models, but this would certainly not be the case for other simulation designs.

| Model | n | Bandwidth | MSE | Bias ² | Variance |
|-------|-------|-----------|--------|-------------------|----------|
| 1a) | 500 | 0.02 | 0.0307 | 0.0049 | 0.0258 |
| | | 0.1 | 0.0133 | 0.0038 | 0.0095 |
| | | 0.2 | 0.0436 | 0.0365 | 0.0071 |
| | 5,000 | 0.02 | 0.0056 | 0.0019 | 0.0038 |
| | | 0.1 | 0.0047 | 0.0028 | 0.0019 |
| | | 0.2 | 0.0404 | 0.0389 | 0.0014 |
| 1b) | 500 | 0.02 | 0.0485 | 0.0289 | 0.0197 |
| | | 0.1 | 0.0229 | 0.0169 | 0.0060 |
| | | 0.2 | 0.0541 | 0.0487 | 0.0054 |
| | 5,000 | 0.02 | 0.0204 | 0.0175 | 0.0029 |
| | | 0.1 | 0.0153 | 0.0143 | 0.0010 |
| | | 0.2 | 0.0484 | 0.0473 | 0.0011 |
| 1c) | 500 | 0.02 | 0.1248 | 0.0209 | 0.1041 |
| | | 0.1 | 0.0394 | 0.0087 | 0.0307 |
| | | 0.2 | 0.0395 | 0.0221 | 0.0174 |
| | 5,000 | 0.02 | 0.0339 | 0.0211 | 0.0129 |
| | | 0.1 | 0.0116 | 0.0076 | 0.0041 |
| | | 0.2 | 0.0218 | 0.0194 | 0.0024 |
| 2) | 500 | 0.02 | 0.0210 | 0.0011 | 0.0199 |
| | | 0.1 | 0.0039 | 0.0009 | 0.0030 |
| | | 0.2 | 0.0570 | 0.0034 | 0.0023 |
| | 5,000 | 0.02 | 0.0028 | 0.0010 | 0.0018 |
| | | 0.1 | 0.0020 | 0.0013 | 0.0008 |
| | | 0.2 | 0.0046 | 0.0040 | 0.0006 |

Table 2: Simulation results for $\alpha = 0.5$.

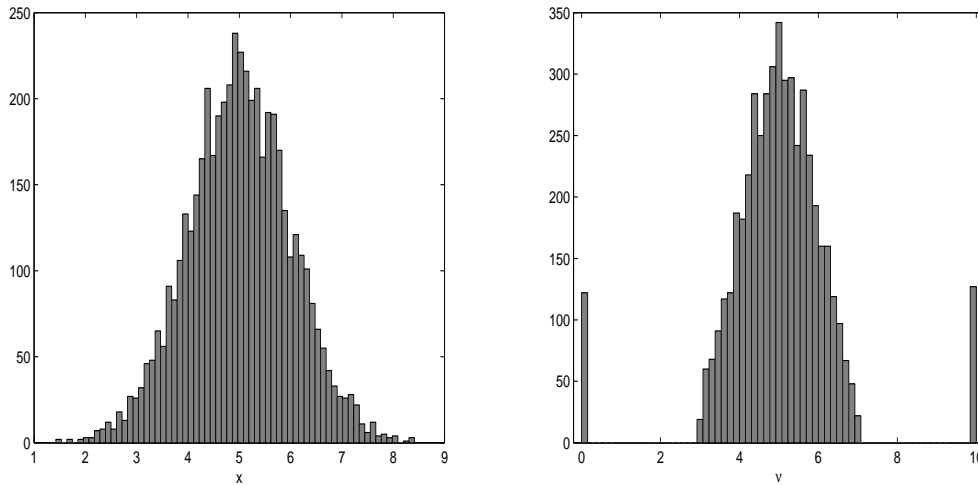


Figure 1: Distribution of X (left) and observed distribution of ν (right) used in the simulation study.

4 Empirical Results

We estimate conditional quantile functions with a sample of German administrative individual unemployment duration data. It is extracted from the IAB-Employment Sample 1975-2001 (IABS-R01) which contains employment trajectories of about 1.1 million individuals from West-Germany and about 200K individuals from East-Germany. It is a 2% random sample of the socially insured workforce. It contains daily information about periods of employment subject to social security taxation and periods of receipt of unemployment compensation. See Hamann et al. (2004) and Drews et al. (2006) for further details on this data such as the sampling design and the data structure. For estimation we use the same sample of unemployment spells that is used by Fitzenberger and Wilke (2007). However, we restrict the set of regressors to the age, gender and last daily wage before unemployment for all "nonemployment" spells starting in 1996 or 1997 in West-Germany. A nonemployment spell contains periods of unemployment compensation transfers and unobserved periods after an employment period. It requires at least one day of income transfers and it ends with a transition into employment. Otherwise it is right cen-

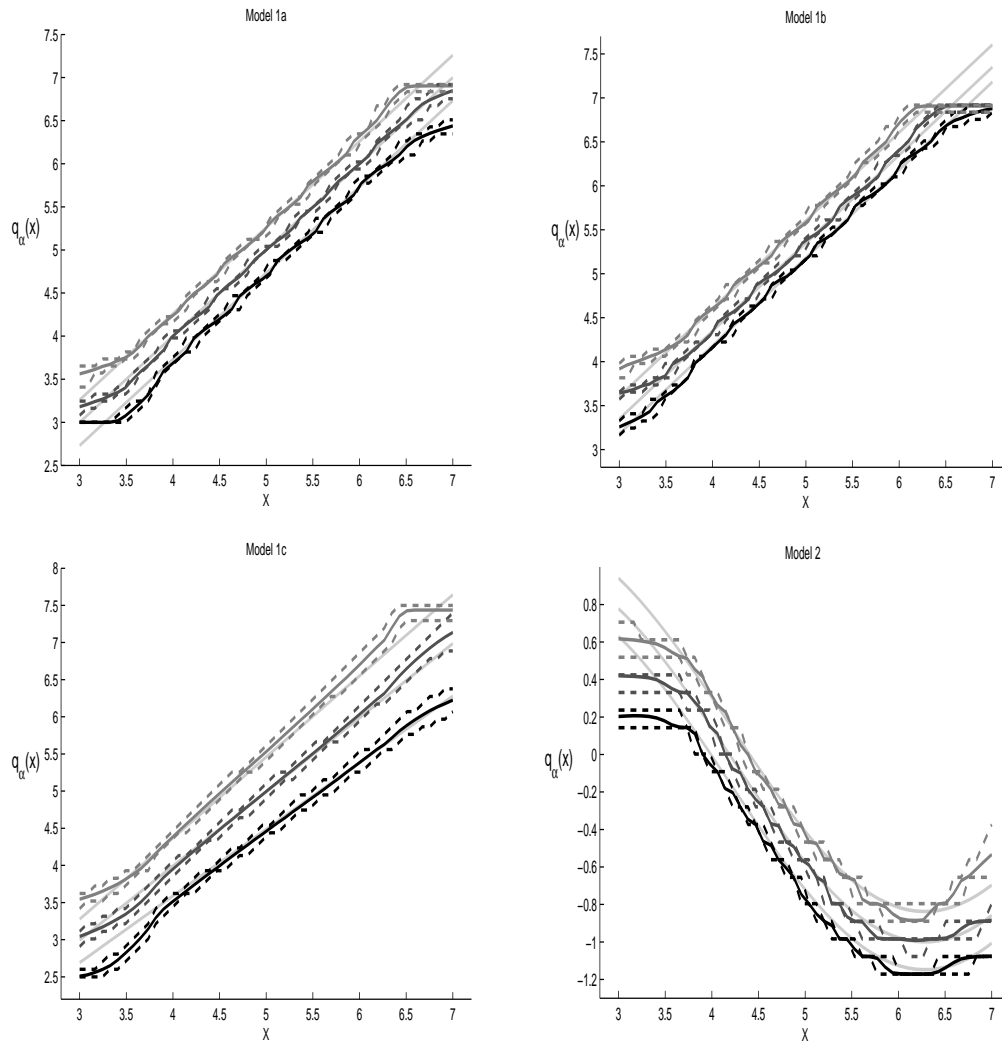


Figure 2: Mean of the simulation estimates of the **quantile functions** $q_\alpha(x)$ for $\alpha=0.3;0.5;0.7$ (from bottom to top), the 2.5%- and the 97.5%-bootstrap quantile for each estimate (dashed lines) and the true model (lighter lines) for 5,000 observations and a kernel bandwidth $b = 0.1$.

sored at the last observed day of income transfers. See Fitzenberger and Wilke (2004) for more details on the definition of unemployment periods in this data. Our sample comprises 21,685 observations with less than 150 individuals generating more than one spell.

We use the estimator defined in (4) to estimate smooth nonparametric conditional quantile functions of the distribution of unemployment duration conditional on age or previous wage level. According to our simulations, the bandwidth should not be too large or too small. After checking that the quality of our results does not change with small variations in the bandwidth, we decided to use $b_n = 0.1$. For the estimation of the standard errors we use the bootstrap method by drawing 500 resamples with replacement and plot the 5%- and the 95%- quantiles of the bootstrap distribution.

Figure 3 shows the estimation results conditional on age for the 0.3-, 0.5- and the 0.7-quantile for males (left) and females (right) with the 5- and 95%-bootstrap quantiles for each quantile. While age plays a less important role for the short-term unemployed men and women, there is a strongly positive influence of age in the group of the long-term unemployed men. The pattern for the longer unemployed women isn't as clear as it is for men, especially not for the 0.7-quantile. According to Lechner (1997), in Germany the probability of fertility has its maximum between the age of 26 and 30 in 1995. This fact could offer a possible explanation for the peak of the curve at the age of 32: At that age, mothers have passed their maternity leave and claim remaining entitlements for unemployment benefits. However, some of them may not actually look for a job. Note that both ends of the estimated curves can have some boundary bias.

For the estimations conditional on the previous daily wage we only use the males. This is because of some lack of information about part-time work which is rather frequent for females. The histogram in figure 4 (left) shows the distribution of the variable "previous wage". The value "0" means an income below and the value "200" means an income above the social security contribution ceiling ("Beitragsbemessungsgrenze"). For this reason we only plot results for the 10% – 90%-quantile of former income. The right panel of Figure 4 shows a weakly decreasing conditional

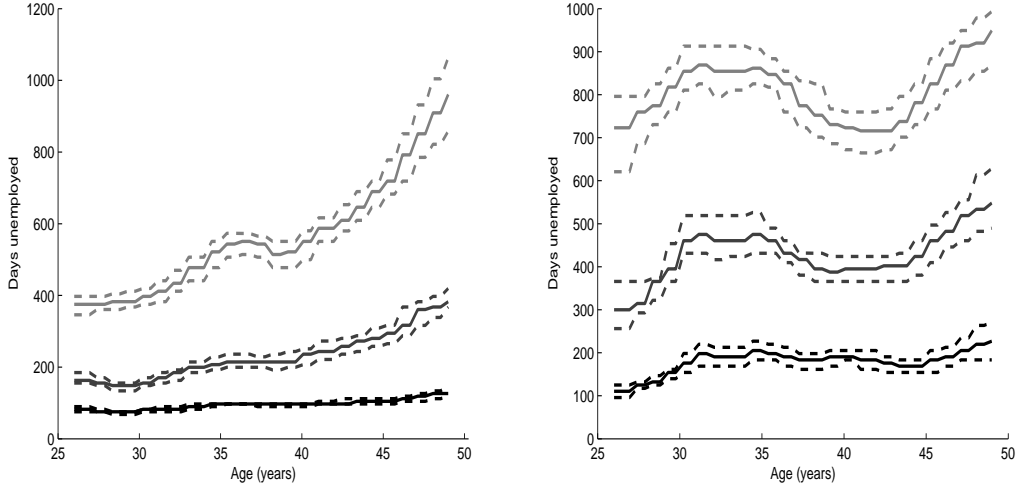


Figure 3: Estimated quantile functions conditional on age (for $\alpha = 0.3; 0.5; 0.7$ from bottom to top); **left:** males, **right:** females; dashed lines: 5%- and the 95%-bootstrap quantile for each estimate.

0.3 quantile function. At the 0.5 and 0.7-quantiles, the decrease is much stronger until a previous wage level of 65 Euro per day. As discussed in detail by Fitzenberger and Wilke (2007), the much longer long-term unemployment periods for low wage individuals are probably related with high and almost time invariant wage replacement rates. The income transfers for this group generally do not decrease after expiration of unemployment benefits as they often do not exceed the level of social benefits. It is unlikely that presented estimates have a boundary bias as we only report them in the range 20-120 EUR.

Biewen and Wilke (2005) and Fitzenberger and Wilke (2007) estimated the semi-parametric hazard rate model, the accelerated failure time model and Box-Cox quantile regression to similar or the same data. While there is no evident contradiction between their and our results, we claim that the estimated conditional quantile functions of this paper give more detailed insights on the conditional distribution of unemployment duration.

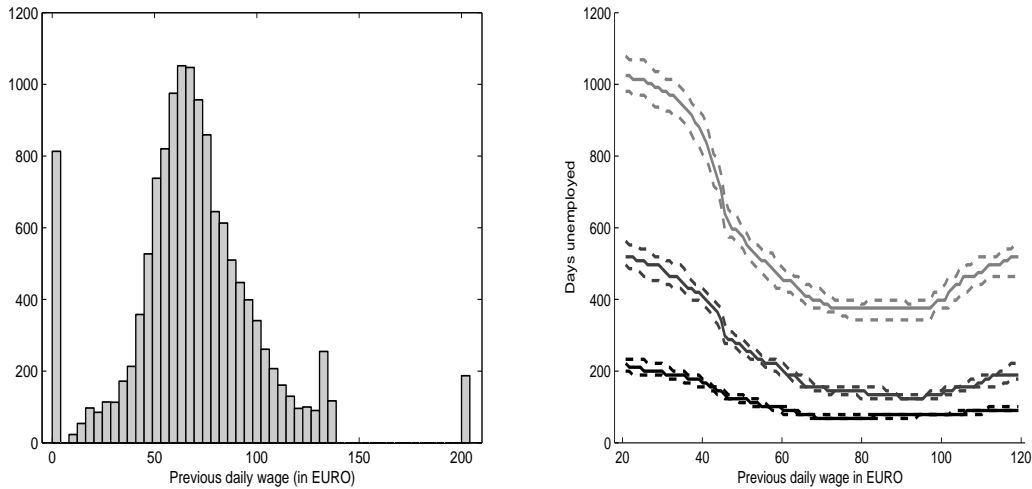


Figure 4: **left:** Histogram of the previous wage for males; **right:** Estimated quantile functions conditional on the previous wage (for $\alpha = 0.3; 0.5; 0.7$ from bottom to top) for males; dashed lines: 5%- and the 95%-bootstrap quantile for each estimate.

5 Conclusion and Outlook

This paper proposes simple nonparametric estimators for the conditional hazard rate and the conditional quantile function when the distribution of the response and of the regressor are both censored. Our simulations and our application show that these estimators are a meaningful and fast tool for data exploration that works without strong assumptions. Resulting estimates can be used for the specification of a statistical model of more structure.

There are several interesting topics for future research that may be beneficial for applied analysis: one could introduce a partially linear approach or one may establish a link to the approach of Portnoy (2004). One could allow for discrete regressors or an additive nonparametric structure. In our application we found some evidence that the conditional quantile functions possess different shapes across quantiles. Therefore one may also develop a test for shape invariance of those functions. Such a test would then provide elaborate information whether a more structural model, such as censored quantile regression, would require different model specifications

across the quantiles. It would also be straightforward to extend the estimator given in (2) to multivariate X of dimension $k = 1, \dots, D$ by applying the idea of product kernels. The estimator for the conditional hazards rates is then

$$h_n(y|x) = \frac{\sum_{i=1}^n \mathbf{1}_{\tau_i=y} \mathbf{1}_{d_i=1} \prod_k K\left(\frac{G_n(x_k) - G_n(\nu_{ik})}{b_{nk}}\right)}{\sum_{i=1}^n \mathbf{1}_{\tau_i \geq y} \prod_k K\left(\frac{G_n(x_k) - G_n(\nu_{ik})}{b_{nk}}\right)}.$$

Note that this estimation strategy, however, suffers from the curse of dimensionality. For multivariate regressors see also Dabrowska (1995).

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