# **Testing for Volatility Changes in Grain Markets**

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## Selected Paper prepared for presentation at the Agricultural & Applied Economics Association's 2011 AAEA & NAREA Joint Annual Meeting, Pittsburgh, Pennsylvania, July 24-26, 2011

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### 1. Introduction

The dramatic rise in grain prices that occurred in 2007 began an unprecedented level of volatility in grain markets. For example, corn prices before 2007 fluctuated within a range of \$0.5 per bushel around an average price in the low \$2 range. However, they swung within a range of \$2 per bushel around \$5 per bushel in the 2007-2008 commodity boom. Increased price volatility results in greater costs for managing risks, such as more costly crop insurance premiums, higher option premiums, and higher hedging costs. In 2010 grain markets witnessed increases in volatility again. It adds to concern on price risk for stakeholders in grain markets so that regulators of the futures market are prompted to consider regulations on positions and trading limits. But, before appropriate policies are recommended to deal with consequences of the dramatic price swing, it is necessary to seek answers to many questions: Is the volatility change permanent or transitory? Is the change timing simultaneous across grain sectors? What are sources of the volatility change?

This study attempts to answer these questions. We investigate the nature of the change in the variability of grain prices by testing for the existence of structural changes in daily volatilities for two selected grain futures (corn and soybean) over the period 2001-2010. Traditionally volatility is treated as a latent variable as is the case in ARCH and stochastic volatility models. However, volatility becomes observable due to a flurry of recent research on the use of high frequency data for measuring volatility (e.g. Andersen, Bollerslev, Diebold, and Labys, 2001, among others). This measure, called realized volatility (RV), is constructed from the sum of intraday squared returns and provides an accurate estimate of the unobserved volatility. Therefore we investigate the evidence for structural changes in reduced form time series models of RV. We use the heterogeneous autoregressive (HAR) model proposed by Corsi (2004) to capture the strong serial dependence in RV series. We consider a logarithmic version of the HAR similar to that implemented by Liu and Maheu (2008). Three factors are postulated to affect volatility: daily log-volatility, weekly log-volatility, and monthly log-volatility.<sup>1</sup> We test for structural changes for individual commodity using the Bai and Perron (2006) method. This method uses an F test and is robust to serial correlation, heteroskedasticity, and differently distributed residuals across regimes (Bai and Perron, 2006). Importantly, the method treats the breaks as unknown, which means that break dates are estimated endogenously with other coefficients.

If the null hypothesis of no break is rejected in each grain, we further test for a common break in both commodities using Qu and Perron (2007) method. The common break is defined as at least one coefficient from each equation is significantly different across any two adjacent regimes resulted from the specified number of breaks. A likelihood ratio test is used to examine whether one statistically significant common break occurs. If the null hypothesis is rejected, Qu and Perron propose a sequential statistic to continue testing the exact number of breaks. The break dates are estimated by a quasi-maximum likelihood (QML) procedure. The distribution of break date estimates can be independent of the estimation and restrictions of other coefficients.

To investigate sources of structural changes, we decompose the realized volatility into the continuous sample path volatility and the variation arising from the total daily jumps. The continuous component is estimated by a bipower variation measure developed by Barndorff-Nielsen and Shephard (2006). We use the same framework for the realized volatility to model dynamic dependencies in the bipower variation and jumps. A similar test procedure is applied to

<sup>&</sup>lt;sup>1</sup> Liu and Maheu (2008) also took into account asymmetric effect in equity realized volatilities, but no such effect exits in commodity price dynamics.

determine whether there is a coincidence of the break date for both its components. This disaggregation will identify sources of the realized volatility change.

The rest of this paper is structured as follows. Section 2 presents the volatility relevant theory and measures. Section 3 discusses data descriptive statistics. Section 4 presents the models for realized volatility, bipower variation, and jump dynamics. Section 5 discusses the methodology of testing for breaks in individual and group commodities and estimating the number of breaks. Section 6 presents the test results and estimation. Section 7 contains some conclusions.

#### 2. Volatility Measures

Let  $p_t$  denotes the logarithmic price of a grain futures. Assume that  $p_t$  follows a jump diffusion process (a semi-martingale process):

(1) 
$$dp_t = \mu(t)dt + \sigma(t)dW(t) + k(t)dq(t),$$

where the mean process  $\mu(t)$  denotes the drift term with a continuous and locally finite variation sample path;  $\sigma(t)$  denotes the instantaneous volatility; W(t) is a Brownian Motion; and k(t)dq(t) is the pure jump part with time-varying intensity  $\lambda(t)$  and jump size k(t). The quadratic variation  $(QV_t)$  measures the volatility over the trading day t:

(2) 
$$QV_t = plim \sum_{j=0}^{n-1} (p_{\tau_{j+1}} - p_{\tau_j})^2$$
,

where  $t - 1 = \tau_0 \le \tau_1 \le \cdots \le \tau_n = t$  denotes a sequence of partitions with  $\sup \{\tau_{j+1} - \tau_j\} \to 0$ for  $n \to \infty$ . Following the theory of quadratic variation, the total price variation at day *t* can be decomposed into its continuous component and a jump part:

(3) 
$$QV_t = \int_{t-1}^t \sigma(s)^2 ds + \sum_{j=1}^{N_t} k_{t,j}^2$$
,

where the first integrated volatility term represents the contribution from the continuous price path, while the second term accounts for the corresponding contribution to the QV from jumps; and  $N_t$  gives the number of jumps over day t.

The quadratic variation and its separate components are not observable. We make use of high-frequency data to construct their empirical volatility measures. Denotes the day t, j th within-day return by:

(4) 
$$r_{t,j} = p_{t-1+\frac{j}{M}} - p_{t-1+\frac{j-1}{M}}, \quad j = 1, \dots, M.$$

where M refers to the number of (equally spaced) return observations over the trading day t. A model-fee nonparametric measure, realized volatility, consistently estimates the quadratic variation:

(5) 
$$RV_t = \sum_{j=1}^M r_{t,j}^2$$
.

Following equation (2), the realized volatility will converge uniformly in probability to the quadratic variation as the sampling frequency goes to infinity (Andersen, and Bollerslev, 1998; Barndorff-Nielsen and Shephard, 2002, among others):

(6) 
$$RV_t(M) \xrightarrow{M \to \infty} QV_t$$
.

In order to distinguish the continuous variation from the jump component, Barndorff-Nielsen and Shepard (2004) propose an empirical estimator, bipower variation, defined by:

(7) 
$$BV_t = \frac{\pi}{2} \sum_{j=2}^{M} |r_{t,j}| |r_{t,j-1}|$$
.

Also, the bipower variation measure becomes immune to jumps and consistently estimates the integrated volatility with increasingly finely sample returns:

(8) 
$$BV_t(M) \xrightarrow{M \to \infty} \int_{t-1}^t \sigma(s)^2 ds.$$

Consequently, the difference between the realized volatility and the bipower variation consistently estimates the part of the quadratic variation due to jumps:

(9) 
$$RV_t(M) - BV_t(M) \xrightarrow{M \to \infty} \sum_{j=1}^{N_t} k_{t,j}^2$$
.

An empirically more robust measure proposed by Huang and Tauchen (2005) is the relative jump statistic:

$$(10) J_t = \log(RV_t) - \log(BV_t).$$

The  $J_t$  measure may be negative because of the finite values of M, although theoretically it is positive. Bolleslev et al. (2009) treated these "measurement errors" as part of the  $J_t$  process while Andersen et al. (2007) adopted a certain threshold to identify only the significant jumps by a jump detection test statistic. We will follow Bollesleve et al. (2009) method to measure jump in order to avoid the arbitrary choice of any pre-specified significant level.

#### 3. Data

Our data consist of five-minute price for corn and soybean futures contracts traded on the Chicago Board of Trade, ranging from Jan 2, 2001 to Apr 6, 2010. We calculate the realized volatility, bipower variation, and jump measures for most actively traded contracts in each period. We also exclude all overnight returns. The intraday five-minute prices span the time interval from 9:35 to 13:15, resulting in M=45 non-overlapping return observations per day. A five-minute sampling frequency is often used in finance literature, since on the one hand it is desirable as finely sampled observations, on the other hand it is robust to contaminating market microstructure noise (Andersen, Bollerslev, and Huang, 2010).

The resulting daily series for the logarithmic realized volatility and its two components are displayed in Figure 1, 2, and 3. The widely-documented volatility clustering effect is

exhibited in each series. Also, the level of the logarithmic realized volatility exceeds that of the logarithmic bipower variation series. In turn, the jump series depicted in the last panel exhibits mostly positive values. It follows from Table 1 that the unconditional distributions of both the logarithmic continuous volatility measures are approximately normal. However, the descriptive statistics for the relative jump measure clearly indicate a positively skewed and leptokurtic distribution. Turning to the lower panel in the table, all of the volatility measures exhibit highly significant own serial dependencies, as evidenced by the Ljung-box test statistics for up to 20<sup>th</sup> order autocorrelation. It is consistent with the widely-documented long memory feature in the literature. Meanwhile, the relative jump measure also exhibits similar long-memory characteristics. In contrast, much less autocorrelation exists in S&P500 index time series.

## 4. Model

For modeling the dynamic dependencies in realized volatilities, we consider the heterogeneous autoregressive model (HAR) proposed by Coris (2004). The model provides a good approximation to the dynamics of long memory and is easy to estimate. The specific HAR-RV model adopted here takes the form:

$$(11) (\log RV_i)_t = \beta_{i0} + \beta_{i1} (\log RV_i)_{t-1} + \beta_{i2} (\log RV_i)_{t-5,t-1} + \beta_{i3} (\log RV_i)_{t-22,t-1} + \varepsilon_{it},$$

where

$$(\log RV_i)_{t-5,t-1} = \frac{(\log RV_i)_{t-1} + (\log RV_i)_{t-2} + \dots + (\log RV_i)_{t-5}}{5},$$
$$(\log RV_i)_{t-22,t-1} = \frac{(\log RV_i)_{t-1} + (\log RV_i)_{t-2} + \dots + (\log RV_i)_{t-22}}{22},$$

and i = 1,2 for corn and soybean realized volatilities, respectively. This model postulates three factors that affect volatility: daily log-volatility, weekly log-volatility, and monthly log-volatility.

We rely on the similar model to describe the dynamic dependencies in the  $(logBV)_t$  series.

(12) 
$$(\log BV_i)_t = \alpha_{i0} + \alpha_{i1} (\log BV_i)_{t-1} + \alpha_{i2} (\log BV_i)_{t-5,t-1} + \alpha_{i3} (\log BV_i)_{t-22,t-1} + e_{it}$$

The descriptive statistics point toward fairly strong own serial autocorrelations in the relative jump series. To best accommodate the feature in the model, we specify a HAR-J model:

$$(13) J_{it} = \gamma_{i0} + \gamma_{i1} (J_i)_{t-5,t-1} + \gamma_{i2} (J_i)_{t-22,t-1} + v_{it},$$

where

$$(J_i)_{t-5,t-1} = \frac{(J_i)_{t-1} + (J_i)_{t-2} + \dots + (J_i)_{t-5}}{5},$$
$$(J_i)_{t-22,t-1} = \frac{(J_i)_{t-1} + (J_i)_{t-2} + \dots + (J_i)_{t-22}}{22}.$$

In the jump dynamics, the lagged jumps are generally insignificant. Other regressors, such as weekly and monthly log(BV), are also taken into account but omitted from the model due to the insignificance. Finally, the Ljung-box Q-statistics for all absolute residuals reveal no significant auto-correlations.<sup>2</sup>

### 5. Estimation and Test

We follow a setup in the Bai and Perron methodology to test for existence, number, and timing of the breaks in individual commodity realized volatility time series. The procedure is as follows. We estimate the linear equations for different sets of intercepts and slopes corresponding to different combinations of break points. The break date is pin down by obtaining global minimizers of the sum of squared residuals. An F-test is constructed to examine if there is a statistically significant break. If the null hypothesis of no break is rejected, we continue to determine the exact number and their location by the so-called sequential method. The method

<sup>&</sup>lt;sup>2</sup> But the Ljung-Box Q-statistics for the squared realized volatility and bipower variation residuals reveal clear evidence for significant conditional heteroskedasticity. We didn't augment the basic model with a GARCH error structure for the time-varying volatility of volatility, since on the one hand coefficient estimates are only limitedly improved, on the other hand in the break test, whether Bai and Perron test or Qu and Perron test, are robust to heteroskedasticity.

adds one break each time the F-test is significant. The detailed theory on estimating and testing a single equation with multiple structural changes can be found in Bai and Perron (1998). Bai and Perron (2003) demonstrated the empirical application of the procedures. More statement will be placed on the Qu and Perron method, which proposed a general framework to test structural changes in multivariate regressions. Furthermore, it has not yet been applied too much. In fact, our study is one of the empirical applications of it.<sup>3</sup>

To test the common break in grouped realized volatilities, we cast the model (11) into an alternative form proposed by Qu and Perron (2007):

(14) 
$$y_t = (I \otimes z'_t) S \beta_j + u_t$$
,

where  $y_t = ((\log RV_1)_t (\log RV_2)_t)'$ ,  $z_t$  is the set that includes the regressors from two equations. A subscript j indexes a regime (j=1,2,...,m+1) when the total number of common structural breaks in the system is m. We denote the break dates by the m vector  $\mathcal{T} = (T_1, ..., T_m)$ and set that  $T_0 = 1$  and  $T_{m+1} = T$ . The matrix S is a selection matrix having dimension  $14 \times 8$ that involves elements with 0 or 1 to specify which regressors appear in each equation.  $u_t$  has mean 0 and covariance matrix  $\Sigma_j$  for  $T_{j-1} + 1 \le t \le T_j$  (j = 1, ..., m + 1). We define the 7 × 2 matrix  $x_t$  by  $x_t' = (I \otimes z_t')S$  so that (14) becomes

$$(15) y_t = x_t' \beta_i + u_t$$

Qu and Perron (2007) applied a quasi-maximum likelihood method based on normal errors to estimate multiple structural changes that occur at unknown dates in a system of equations. This is a fairly general method with the following flexibilities: a) allowing changes in the coefficients of the conditional mean; b) allowing changes in the coefficients of the covariance matrix of the residuals; and c) allowing arbitrary restrictions on these parameters so that we can analyze not

<sup>&</sup>lt;sup>3</sup> We are also gateful to Jushan Bai, Pierre Perron, and Zhongjun Qu for making their GAUSS programs available.

only common breaks that occur in all equations, but also breaks that occur in a subset of equations. Given the partition of the sample  $\mathcal{T} = (T_1, ..., T_m)$ , the system's quasi-likelihood function is

(16) 
$$L_T(\mathcal{T}, \boldsymbol{\beta}, \boldsymbol{\Sigma}) = \prod_{j=1}^{m+1} \prod_{t=T_j+1}^{T_j} f(\mathbf{y}_t | \mathbf{x}_t; \boldsymbol{\beta}_j, \boldsymbol{\Sigma}_j),$$

where  $f(\cdot | \cdot)$  is a multivariate normal distribution. Thus the quasi-likelihood ratio is

(17) 
$$LR_T = \frac{\prod_{j=1}^{m+1} \prod_{t=T_j+1}^{T_j} f(\mathbf{y}_t | \mathbf{x}_t; \beta_j, \Sigma_j)}{\prod_{j=1}^{m+1} \prod_{t=T_j^0+1}^{T_j^0} f(\mathbf{y}_t | \mathbf{x}_t; \beta_j^0, \Sigma_j^0)},$$

. . . ..

where a 0 subscript denotes the true value of the parameters. Then the parameter estimates are to maximize a log-likelihood ratio with parameter restrictions:

$$(18)\left(\widehat{\mathcal{T}},\widehat{\beta},\widehat{\Sigma}\right) = \arg\max_{(T_1,\dots,T_m;\beta,\Sigma)}(\log\left(LR_T\right) + \lambda'g(\beta,vec(\Sigma))),$$

where  $g(\beta, vec(\Sigma) = 0$  is a restriction on parameters.

Qu and Perron (2007) have corroborated that the log-likelihood ratio optimization problem can be split into two asymptotically independent components so that the estimates of the break dates  $\mathcal{T}$  and the coefficients ( $\beta$ ,  $\Sigma$ ) are unaffected each other. Furthermore, the restrictions on parameters do not also affect the distribution of the break dates. Under the theorem, the limiting distribution of the estimates of the break dates are easily derived (See theorem 2 and 3 in Qu and Perron (2007)).

To construct the QMLE, a general algorithm to the optimization problem (18) is a grid search, but it is no longer feasible in the computation of maximum likelihood estimate of order  $O(T^m)$ . Qu and Perron (2006) used a dynamic programming algorithm identical to Bai and Perron (2003). The main idea is to first calculate the overall value of the log-likelihood function for all possible segments, and then use this algorithm to assess which particular combination of m+1 segments leads to the highest likelihood value. After estimating the break dates by QMLE, a likelihood ratio statistic is constructed o test the null hypothesis with no change in any of the coefficients versus an alternative hypothesis with a pre-specified number of changes. The test statistic is

(19) 
$$Z_{\hat{T}} = 2 \left[ log \hat{L}_T (\hat{T}_1, \dots, \hat{T}_m) - log \tilde{L}_T \right],$$

where

$$\log \tilde{L}_T = -\left(\frac{Tn}{2}\right) (\log 2\pi + 1) - T/2\log |\tilde{\Sigma}|,$$

and

$$\log \hat{L}_T\left(\hat{T}_1,\ldots,\hat{T}_m\right) = -\left(\frac{Tn}{2}\right)\left(\log 2\pi + 1\right) - \sum_{j=1}^{m+1} \frac{T_j - T_{j-1}}{2} \log \left|\hat{\Sigma}_j\right|.$$

A tilde subscript denotes the parameter estimates under the null hypothesis (no change in structure), while a delta subscript denotes the parameter estimates under the alternative hypothesis (m structural changes in the system). If no change occurs, the QMLE is equivalent to the generalized least squares estimate, and thus other coefficients can be estimated as

$$\tilde{\beta} = \left(\sum_{t=1}^{T} x_t \tilde{\Sigma}^{-1} x_t'\right)^{-1} \sum_{t=1}^{T} x_t \tilde{\Sigma}^{-1} y_t,$$
$$\tilde{\Sigma} = \frac{1}{T} \sum_{t=1}^{T} (y_t - x_t' \tilde{\beta}) (y_t - x_t' \tilde{\beta})'.$$

The estimates can be obtained by beginning with the OLS of estimates of coefficients in the mean equation and iterate until convergence. Under the alternative hypothesis, the QMLE jointly solve the equations

$$\hat{\Sigma}_{j} = \frac{1}{T_{j} - T_{j-1}} \sum_{t=T_{j-1}+1}^{T_{j}} (y_{t} - x_{t}' \hat{\beta}_{j}) (y_{t} - x_{t}' \hat{\beta}_{j}),$$
$$\hat{\beta}_{j} = \left( \sum_{t=T_{j-1}+1}^{T_{j}} x_{t} \hat{\Sigma}_{j}^{-1} x_{t}' \right)^{-1} \sum_{t=T_{j-1}+1}^{T_{j}} x_{t} \hat{\Sigma}_{j}^{-1} y_{t}.$$

The estimates allow the structure change occurring in the conditional mean and the covariance matrix of the errors. The limiting distribution of the test statistic is derived by Qu and Perron (2007) and depends on the number of regressors whose coefficients are allowed to change, the

number of coefficients of the covariance matrix allowed to change, and the distribution the errors. If the test rejects the null hypothesis, we can use a sequential test statistic, as in Bai and Perron (2003), to examine how many structure changes occur. The test is also based on the estimates of the break dates from a global maximization of the likelihood function. It is to test the null hypothesis of l (l > 0) breaks versus the alternative hypothesis of l + 1 breaks. The procedure is to perform a one break test for each of the (l + 1) segments defined by the partition ( $T_1, ..., T_l$ ) and to assess whether the maximum of the tests is significant. It is defined by

(20) 
$$SEQ_T(l+1|l)$$

$$= \max_{1 < j < l} \sup \left[ \log \left( LR_T(\widehat{T}_1, \dots, \widehat{T}_{j-1}, \tau, \widehat{T}_j, \dots, \widehat{T}_l) \right) \right] - \log \left( LR_T(\widehat{T}_1, \dots, \widehat{T}_l) \right)$$

Also, the limiting distribution of this test can be derived straightforwardly based on the distribution function of  $Z_{\hat{T}}$ .

Finally, to test the source of structural change in realized volatilities, we decompose realized volatilities into a continuous component and a jump part. Qu and Perron (2006) methodology is again applied to partial structural change models where a subset of the equations does not change across regimes. We restrict all the coefficients in one equation unchanged to see if structural changes in the other are responsible for the break in realized volatilities. We don't test for structural change using a single component time series. Instead, we group them to apply the similar procedure since even if no change occurs in one equation, the precision of the estimates on break dates and other coefficients can be increased due to the correlation between error terms of equations. The improvement of efficiency is similar to an SUR (seemingly unrelated regression) model for linear regressions opposed to OLS. Based on existing results in the stochastic volatility literature, the disturbances in continuous volatility and jump are correlated. For example, Bollereslev, et al. (2009) found the sample correlation for the estimated

residuals from the Bipower variation and jump equations are -0.1847. Additionally, they also find there might exist nonlinear dependencies—a smirk-like relation between the innovations to the continuous volatility and jump components. Testing for a structural change in a system of equations because of interdependencies between disturbances would obviously improve estimation efficiency.

### 6. Results

First, we use the Bai and Perron (1998, 2003) method to estimate multiple breaks in individual grain commodity time series. At each step, according to the recommendation of Bai and Perron (2006), we test the null hypothesis of no breaks against an unknown number of breaks. If the null of no breaks is rejected, we use the sequential test to determine the number of and locations of breaks. Table 2 reports the test statistics and the 90% confidence interval for the break date estimates. Two interesting results are revealed from Table 2. Firstly, the SupF tests suggest that there is evidence of structural changes in the coefficients that govern the dynamics of realized volatilities for corn and soybean. We reject the null of no break in favor of the alternative of breaks. Secondly, the sequential tests suggest that only one structural change occurs in the soybean and corn volatilities. The break date for corn is estimated at Nov 18, 2006, while the date for soybean is estimated at one year later. Table 3 and 4 give other coefficient estimates for corn and soybean HAR models. The coefficient estimates show predictive ability of regressors has similar change for corn and soybean: in the second regime, weekly log-realized volatilities reduce its weight on the prediction while monthly log-realized volatilities increase its effect. This means in recent years long memory feature of these two commodities has become more prominent.

Next, we test whether there is a common structural break between the corn and soybean realized volatilities using the Qu and Perron test in a system of two equations. That is, we see whether the difference of break dates for corn and soybean is negligible in statistics. This approach restricts the breaks to occurring at the same time in both equations and therefore can detect breaks in the ratio when they occur in the component series simultaneously but with different magnitudes. Our test results indicate that there is little evidence of a common structural change in the corn and soybean realized volatilities. The *SupLR* test for 0 versus 1.000 break is 18.486, while the 10% and 5% significance levels are 20.78 and 23.21. In short, there are no common structural changes between corn and soybean realized volatilities.

To further investigate the source of realized volatilities in each commodity, we turn to the system of equations composed by the bipower variation and jump. We apply the same empirical methods as the case in the system of realized volatilities. Table 5 describes the test results. First we allow breaks in all the regression coefficients. The SupF test for the structural changes suggests one common structural change in corn bipower and jump time series. But the break date is prior to the date found in the single realized volatility series. The break date estimate is Feb 8, 2006, and the 90 percent confidence interval is Dec 7, 2005 to April 10, 2006. There is no evidence of a second structural break in the system. As for soybean, there is evidence of structural change. Furthermore, the break date estimate is almost exactly same as the case in the soybean realized volatilities. In order to check the timing of the structural break simultaneous across components, we restrict coefficients in one subset of equation unchanged. When coefficients in jump series is unchanged in the two regimes, we found the SupF test can not reject the null hypothesis, that is, there is no evidence of structural change in the bipower variation series regardless of corn or soybean. But if we keep coefficients in bipower variation

series unchanged, the test rejects the null hypothesis and there is a remarkable coincidence of the break date for the system of jump and bipower variation as a whole with and without restrictions. The statistical significance is very strong for soybean, say, 1% level, while it is about relatively weak for corn, say, 10% level. Apparently, the structural change in the realized volatilities for corn and soybean is due to roughly simultaneous breaks in the jump series.

### 7. Conclusion

We use newly nonparametric volatility measures and break techniques to estimate common breaks across grain futures over the recent ten years. Our results show one structural change in realized volatilities occurred in 2006 for corn and in 2007 for soybean. But the date difference between them cannot be negligible. We disaggregate the realized volatilities into a continuous component and a jump part and found the source of structural beak in realized volatilities is from jumps.

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	Corn			Soybean			
	log (RV)	log (BV)	Jump	log (RV)	log (BV)	Jump	
Mean	-9.142	-9.467	0.325	-8.978	-9.142	0.164	
Median	-9.199	-9.459	0.252	-9.037	-9.208	0.126	
Std. dev.	0.879	1.000	0.324	0.725	0.746	0.226	
Skewness	0.239	-0.166	2.418	0.392	0.318	2.235	
Kurtosis	3.104	3.114	18.73	3.172	3.166	16.27	
Ljung-Box(5)	3214	3642	219.1	3291	3084	125.4	
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
Ljung-Box(10)	5769	6657	493.6	5896	5386	171.9	
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
Ljung-Box(15)	8021	9931	682.9	8107	7311	227.5	
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	
Ljung-Box(20)	10030	11716	840.8	10031	9001	269.3	
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	

Table 1 Descriptive statistics for Corn and Soybean volatility measures

	SupF Test		SEQ Test		Break Date	90%	
	0vs.1 break	<i>CV</i> <sub>5%</sub>	1 vs. 2 breaks	<i>CV</i> <sub>5%</sub>		Confidence Interval	
Corn	21.20	16.19	7.26	18.11	11/18/2006	[7/5/2006 5/10/2007]	
Soybean	17.12	16.19	17.51	18.11	11/27/2007	[11/1/2007 6/5/2008]	

Table 2. Bai and Perron Test for Structural change in Individual Grain

Note: we did not give the test statistics for the no-break versus one more breaks because all of them reject the null hypothesis.

Coe.	Estimate	St. Er.	p-value
$eta_{10}$	-1.60	0.35	0.00
$eta_{11}$	0.11	0.03	0.00
$eta_{12}$	0.47	0.06	0.00
$eta_{13}$	0.27	0.06	0.00
$eta_{20}$	-1.39	0.44	0.00
$eta_{11}$	0.16	0.04	0.00
$eta_{12}$	0.23	0.08	0.00
$\beta_{13}$	0.44	0.08	0.00

Table 3. Estimates for the Corn HAR Model

Coe.	Estimate	St. Er.	p-value
$\beta_{10}$	-0.78	0.29	0.01
$eta_{11}$	0.12	0.04	0.00
$eta_{12}$	0.51	0.07	0.00
$eta_{13}$	0.27	0.06	0.00
$eta_{20}$	-0.91	0.44	0.04
$eta_{11}$	0.26	0.05	0.00
$eta_{12}$	0.22	0.09	0.02
$eta_{13}$	0.41	0.09	0.00

Table 4. Estimates for the Soybean HAR Model

	SupF Test		SEQ Test		Break Date	90%	
	0vs.1 break	<i>CV</i> <sub>5%</sub>	1 vs. 2 breaks	<i>CV</i> <sub>5%</sub>		Confidence Interval	
All coefficients in regressions are allowed changed							
Corn	48.3	21.5	15.68	21.70	2/8/2006	[12/7/2005	4/10/2006]
Soybean	17.12	16.19	17.51	18.11	11/26/2007	[8/30/2007	2/22/2008]
Only coefficients in jump regressions are allowed changed							
Corn	18.89	21.37	15.33	24.50	1/5/2006	[8/19/2005	5/19/2006]
Soybean	36.99	21.37	17.33	24.50	11/26/2007	[7/30/2007	4/3/2008]
Only coefficients in Bipower variation regressions are allowed changed							
Corn	13.48	25.09					
Soybean	17.06	25.09					

Table 5. Qu and Perron Test for Structural change in a system of equations



Figure 1. Time series of logarithmic realized volatility, logarithmic bipower variation, and jumps for corn futures from 2001 to 2010





Figure 2. Time series of logarithmic realized volatility, logarithmic bipower variation, and jumps for soybean futures from 2001 to 2010

