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MISALLOCATION, ECONOMIC GROWTH, AND INPUT-OUTPUT ECONOMICS

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ABSTRACT

One of the most important developments in the growth literature of the last decade is the enhanced appreciation of the role that the misallocation of resources plays in helping us understand income differences across countries. Misallocation at the micro level typically reduces total factor productivity at the macro level. Quantifying these effects is leading growth researchers in new directions, two examples being the extensive use of firm-level data and the exploration of input-output tables, and promises to yield new insights on why some countries are so much richer than others.

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1. Introduction

One of the most important developments in the growth literature of the last decade is the enhanced appreciation of the role that the misallocation of resources plays in helping us understand income differences across countries. Given an economy's stock of physical capital, labor, human capital, and knowledge, the way in which those aggregate quantities of inputs are allocated across firms and industries — and even potentially within firms — determines the economy's overall level of production. The best allocation will maximize welfare and, in a sense that can be made precise, output itself in the long run. Other allocations result in lower levels of output and therefore show up in the aggregate as a lower level of total factor productivity (TFP).

In some broad sense, this is an old idea with many antecedents. In the real business cycle literature, for example, it is commonly appreciated that tax distortions or regulations may show up as TFP shocks. Chari, Kehoe and McGrattan (2007) follows in this tradition.

In the literature on growth and development, Restuccia and Rogerson (2008) explicitly analyze a model of misallocation among heterogeneous plants to quantify the effect on aggregate TFP. Banerjee and Duflo (2005) argue that the marginal product of capital differs widely among firms in India, potentially reducing overall output. Hsieh and Klenow (2009) present empirical evidence that misallocation across plants within 4-digit industries may reduce TFP in manufacturing by a factor of two to three in China and India. A large literature surrounding these papers considers various mechanisms through which misallocation can lead to income differences.¹

This paper provides my own idiosyncratic perspective on misallocation and presents three basic points. First, I begin with an overview of misallocation. A simple toy model illustrates how misallocation can reduce TFP, and I outline several questions related to misallocation that might be considered in future research.

¹Examples include Parente and Prescott (1999), Caselli and Gennaioli (2005), Lagos (2006), Alfaro, Charlton and Kanczuk (2008), Buera and Shin (2008), Guner, Ventura and Xu (2008), La Porta and Shleifer (2008), Bartelsman, Haltiwanger and Scarpetta (2009), Vollrath (2009), Midrigan and Xu (2010), Moll (2010), and Syverson (2010).

Second, I suggest one way in which the effects of misallocation can be amplified: through the input-output structure of the economy. Because the outputs of many firms are used as the inputs of other firms, the effects of misallocation can be amplified. Finally, I provide an overview of the input-output structure of the United States and 34 other economies, albeit at a fairly high level of aggregation. In addition to supporting the basic point that the amplification associated with input-output economics can be quantitatively important, this overview suggests what I think is a remarkable similarity in the input-output structures of diverse economies. Understanding whether this really is the case, why it may be so, and what implications it entails is another useful area for future research.

2. Misallocation

This section provides an overview of the consequences of the misallocation of resources.

2.1. Misallocation and TFP

We begin by presenting a simple example that illustrates the basic point of the misallocation literature: misallocation reduces TFP.

Consider an economy in which the two key produced goods are steel and lattes:

$$\text{Production:} \quad X_{steel} = L_{steel}, \quad X_{latte} = L_{latte}$$

$$\text{Resource constraint:} \quad L_{steel} + L_{latte} = \bar{L}$$

$$\text{GDP (aggregation):} \quad Y = X_{steel}^{1/2} X_{latte}^{1/2}$$

One unit of labor can produce either a unit of steel or a cup of latte. The economy is endowed with \bar{L} units of labor. And we assume lattes and steel combine in a Cobb-Douglas fashion to generate a final good. This last equation could be replaced by a utility function, but then one would have to specify prices in order to aggregate the two goods; the approach here is simpler.

Obviously, the only allocative decision that has to be made is how much labor to employ producing steel versus lattes. Let $x \equiv L_{steel}/\bar{L}$ denote the allocation of labor. This could be determined by perfectly competitive markets, by a social planner, by markets distorted by taxes, or in any number of different ways.

Solving for GDP given the allocation yields

$$Y = A(x)\bar{L},$$

where TFP, $A(x)$, is given by

$$A(x) = \sqrt{x(1-x)}.$$

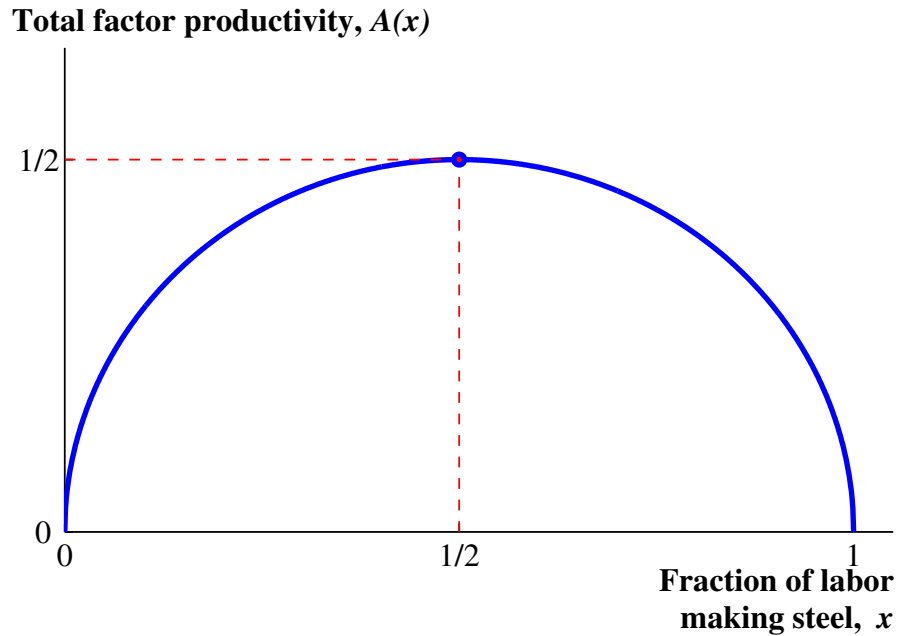
These two equations summarize in a simple way one of the key points of the recent literature on misallocation: the misallocation of resources reduces TFP. As is clear given the symmetry of the setup, the optimal allocation of labor in this simple economy features $x^* = 1/2$. Any departure from this allocation — putting either too little or too much labor into making steel — reduces TFP and therefore GDP. More generally, if the exponents in the production function were σ and $1 - \sigma$ instead of $1/2$, then TFP would simply be $A(x) = x^\sigma(1-x)^{1-\sigma}$; this expression will be useful later. The effects of misallocation are shown graphically in Figure 1.

This figure illustrates another key point: small departures from the optimal allocation of labor have tiny effects on TFP (an application of the envelope theorem), but significant misallocation can have very large effects. Given the large income differences that we see across countries, this possibility is appealing.

However, more careful consideration of Figure 1 indicates that this simple model has what may be an important limitation: in the presence of significant misallocation, a small improvement in the allocation of resources will have a large impact on TFP.

Contrast this with a hypothetical example like that in Figure 2. The dashed line in the figure repeats the effect of misallocation on TFP from Figure 1, while the new solid line depicts an alternative. It seems to me that the alternative better captures the world we live in. As before, small misallocation has small effects and large mis-

Figure 1: Misallocation Reduces TFP

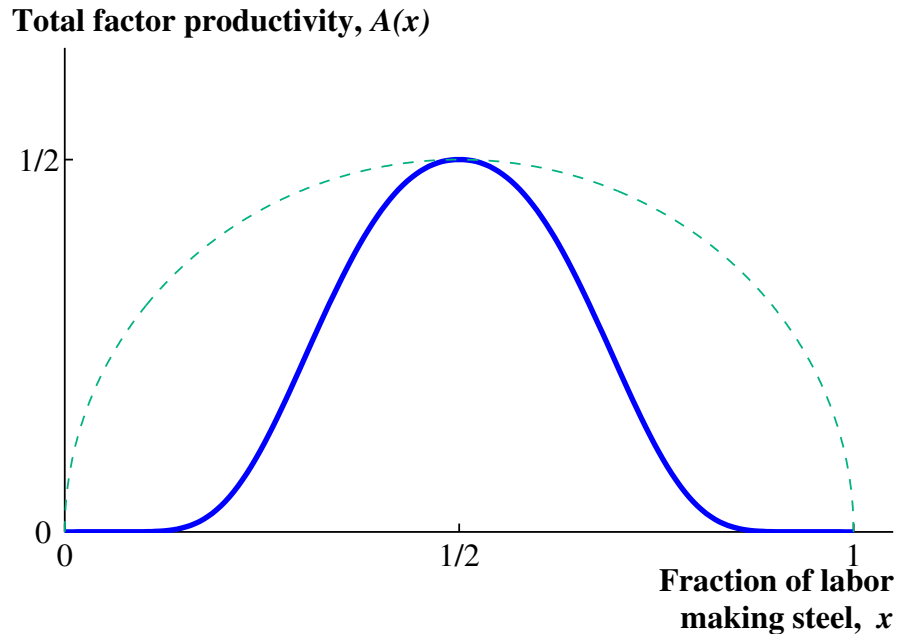


allocation has large effects. Now, however, an intermediate degree of misallocation can have large effects as well (e.g. if the allocation of labor has $x = 1/4$, TFP is *less* than $1/4$ rather than larger than $1/4$). Moreover, with a large degree of misallocation, the effect on TFP of an improved allocation of resources is small: reforms in many cases would have small effects. Growth miracles would be less common in the second world and would be more likely to occur among countries with an intermediate degree of distortions than a large degree of distortions. This kind of structure may even help explain the “twin peaks” structure of the world income distribution emphasized by Quah (1996).

One of the challenges going forward in models of misallocation is — perhaps — to ensure that they capture some of the features of Figure 2 rather than some of the limitations in Figure 1. Jones (2011) explores the possibility that the O-ring style complementarity of Kremer (1993) may help in this regard.

This simple example is useful in illustrating how misallocation reduces TFP, but it fails to capture one of the points emphasized in the recent literature on misalloca-

Figure 2: An Alternative Model of Misallocation?



tion. In the example, misallocation is *across* sectors: we may have too much or too little steel relative to what is optimal. The recent literature often emphasizes misallocation at a more microeconomic level: within the steel sector, there are some plants that are good at making steel and others that are less good. Misallocation may involve giving the less efficient plants too many resources. Clearly both kinds of misallocation (across and within sectors) can be important. One might even push this insight further: Why are some plants more productive than others? Maybe because of the misallocation of resources *within plants*. Organizing a plant and producing output involve an enormous number of decisions, and these decisions may be distorted or made incorrectly because of misallocation: maybe the plant manager is not the best person for the job (Caselli and Gennaioli, 2005), maybe the most talented workers within the plant are not promoted to the appropriate positions, maybe the incentives for the workers to produce efficiently are not present (Lazear, 2000), maybe unionization and job protection leads the firm to use too much labor inappropriately (Schmitz, 2005) and so on.

2.2. Misallocation and Ideas

Next, I wish to consider the interaction between two key themes of the literature on economic growth, the most recent theme of misallocation and the older theme of ideas. Much of the recent literature studies misallocation in neoclassical models in which all inputs are rival. Yet it is surely the case that efforts toward creating and using ideas are distorted as well. How can one think about this?

One useful starting place is the Romer (1990) variety model. The economy uses a range of capital goods — whose measure is A_t — to produce. Misallocation can take two forms: the capital goods could be used in the wrong amount or the range of goods that are available may be incorrect. Of course, this second form can be viewed as a special case of the first form, where the quantity used is set equal to zero. In fact, Romer (1994) explored this latter option and argued that it could have large effects.

A clear advantage of this approach is that the variety framework is straightforward to analyze, and misallocation in the presence of ideas turns out to be not that different from misallocation with rival inputs.

A puzzle is that when calibrated, the variety approach tends to yield relatively small effects. In particular, it is common to calibrate the elasticity of substitution among varieties to markups. With small markups, this elasticity is often large. And when varieties are good substitutes, it is just not that costly to be using the “wrong” variety. A recent example along these lines is Broda and Weinstein (2006). They use a variety model to study the welfare gains from imports of new varieties between 1972 and 2001. Over this thirty year period, they estimate that the number of imported product varieties increased by a factor of three, but the gain to U.S. consumers from having access to these varieties was just 2.6 percent of GDP. (Of course, given the relatively small import share in the United States, this number may not be so small after all.)

An open question for future research is the extent to which misallocation and ideas interact in important ways. It may be that a quality-ladder approach a la Aghion and Howitt (1992) and Grossman and Helpman (1991) can yield better re-

sults.

2.3. Key Questions

At some basic level, there are only two fundamental reasons for income differences across countries in the long run. Either economies have different production possibilities or they have different allocations. In the case of production possibilities, once we have endogenized ideas, the only remaining reason for differences is geographic. Maybe some pieces of land are more conducive to production than others. While there is probably something to this explanation, my current understanding is that these effects are small relative to the large income differences we see across countries. Probably the single most persuasive evidence on this point is the classic Mancur Olson (1996) argument: the large income difference that has emerged between North and South Korea over the last half century, for example, is surely not due to geography.²

This leaves differences in the allocation of resources to explain the bulk of income differences across countries. Given the production possibilities, allocations can then differ for two reasons: differences in preferences and misallocation. Again, there is probably something to the preference story (this seems like a plausible part of the explanation for the difference between the European and American allocation of resources). But at some basic level, people are people and any difference in preferences is probably itself an endogenous outcome.

This argument, then, suggests that all that is left, fundamentally, to explain differences in incomes across countries is misallocation, working both through traditional inputs like capital and labor and also through ideas. Income differences across countries result almost entirely from the misallocation of resources.

And yet to say misallocation is everything is perhaps not to say very much after all. In particular, three additional questions seem pertinent:

1. *What is the nature of the misallocation?* Are certain inputs misallocated more

²Obviously, there is a large literature debating this question; for example, see Gallup, Sachs and Mellinger (1999) and Acemoglu, Johnson and Robinson (2002).

than others? Is the misallocation related to ideas special in any way relative to the misallocation of traditional inputs? How significant is misallocation within sectors or between sectors or even within plants? How much misallocation is there in the richest countries?

2. *How precisely does the misallocation of resources lead to 50-fold income differences?* A simple version of this question is illustrated by the differences we saw back in Figures 1 and 2. In the first case, large income differences required extreme forms of misallocation, and small improvements in the allocation of resources would have large effects on income. In the second, neither of these points is necessarily true. Why does a given amount of misallocation lead to such large income differences? And why are income differences across countries generally rising over time?
3. *Why is there misallocation, and what can be done about it?* This last question takes us into the realm of political economy. The literature on political economy and growth/development has been extremely active in the last decade; see Acemoglu, Johnson and Robinson (2005) for an excellent overview. The state-of-the-art in that literature suggests that misallocation is the equilibrium outcome of a political process interacting with institutions and the distribution of resources (including physical capital, human capital, ideas, and natural resources). It is, evidently, not in the economic interests of the ruling elite to improve the allocation of resources, despite the potentially enormous increase in the size of the economic pie that is possible in the long run.

The distinction between Figures 1 and 2 is helpful in this respect and illustrates the important interaction that occurs between the production possibilities of the economy and the political process. In Figure 1 it is harder to understand why improvements in the allocation of resources would not take place in the most distorted countries because the immediate gains are so large. Such failures are easier to comprehend in an economy like Figure 2, where the immediate gains may be much smaller.

The remainder of this paper takes a much narrower focus and explores one di-

mension of these key questions about misallocation. In particular, it focuses on the production possibilities and seeks to understand why a given amount of misallocation can lead to large income differences rather than small income differences.

3. Input-Output Economics

Modern economies involve very sophisticated input-output structures. Goods like electricity, financial services, transportation, information technology and health-care are both inputs and outputs. A wide range of intermediate goods are used to produce most goods in the economy, and these goods in turn are often used as intermediates.

Despite our intuitive recognition of this point, standard models of macroeconomics and economic growth typically ignore intermediate goods.³ The conventional wisdom seems to be that as long as we are concerned about overall value-added (GDP) in the economy, we can specify the model entirely in terms of value-added and ignore intermediate goods. Hence the neoclassical growth model.

This conventional wisdom is incorrect, and the remainder of this paper explores some of the implications of the input-output structure of the economy for economic growth and development.

The first insight that emerges from thinking about intermediate goods is that they are very similar to capital. In fact, the only difference between intermediate goods and capital is one of short-run timing: intermediate goods can be installed more quickly than capital and “depreciate” fully during the course of production, while capital takes a bit longer to install and only partially depreciates during production. From the point of view of the long run — the perspective relevant in most of this paper — intermediate goods and capital are essentially the same. In particular, both are produced factors of production.

The key implications of intermediate goods for economic growth, development, and macroeconomics arise from seeing them as another form of capital. It has long been recognized that the share of capital in production is a fundamental determi-

³Of course, there is a significant literature of exceptions; these will be discussed below.

nant of the quantitative predictions of macro models. When the capital share is $1/3$, the intrinsic propagation mechanism of the neoclassical growth model is weak, convergence to the steady state is rapid, and the model generates a small multiplier on changes in productivity or the investment rate. In contrast, when the capital share is higher, like $2/3$, these deficiencies are largely remedied. A fairly large portion of the literature on economic growth can be viewed as an attempt to justify using a (broad) capital share of $2/3$ when the data for (narrow) capital loudly proclaim that the right number empirically is only $1/3$.⁴

As documented carefully below, the intermediate goods share of gross output is about $1/2$ across a large number of countries. The share of capital in value-added is about $1/3$, so its share in gross output is $1/6$. Combining these two kinds of capital, the share of capital-like goods in gross output is our magic number, $1/2 + 1/6 = 2/3$. Incorporating intermediate goods into macroeconomic models, then, has the potential to help us understand a range of economic phenomenon, including the propagation of business cycle shocks and the speed of transition dynamics. These applications will not be explored here. Instead, the main application in this paper will be to the puzzle of understanding why misallocation leads some countries to be 50 times richer than others, as opposed to only 10 times richer.

We begin by providing a simple example to illustrate how and why intermediate goods lead to large multipliers. In this example, a single final output good is used as the single intermediate good in the economy, so the input-output structure is very simple. Next, we build an N -sector model of economic activity, where each sector uses the outputs from the other sectors as intermediate goods. This model is very similar to the original multi-sector business cycle model of Long and Plosser (1983). The only technological difference is that we include international trade, allowing sectors to import intermediate goods from abroad. The substantive difference is in

⁴For examples of these points in various contexts, see Rebelo (1991), Mankiw, Romer and Weil (1992), Cogley and Nason (1995), and Chari, Kehoe and McGrattan (1997). Mankiw, Romer and Weil (1992) make many of these points, adding human capital to boost the capital share. Chari, Kehoe and McGrattan (1997) introduced “organizational capital” for the same reason. Howitt (2000) and Klenow and Rodriguez-Clare (2005) consider the accumulation of ideas, another produced factor. More recently, Manuelli and Seshadri (2005) and Erosa, Koreshkova and Restuccia (2010) have resurrected the human capital story in a more sophisticated fashion.

the application to economic growth and development.

Finally, we connect this model to the wealth of input-output data that exist. Data from 35 countries — including not only the currently rich countries but also Argentina, Brazil, China, and India — allows us to quantify the multiplier associated with the input-output structure of the economy.

Before continuing, it is worth noting that there is a very important branch of the economics literature that has studied the impact of intermediate goods. Historically, the input-output literature reigned in economics from the 1930s through the 1960s and is most commonly associated with Leontief (1936) and his followers. Hirschman (1958) emphasized the importance of sectoral linkages to economic development, which itself spawned a large literature. Hulten (1978) is also closely related, showing how intermediate goods should properly be included in growth accounting. More recently, the intermediate goods multiplier shows up most clearly in the economic fluctuations literature; see Long and Plosser (1983), Basu (1995), Horvath (1998), Dupor (1999), Conley and Dupor (2003), Gabaix (2005), and Basu, Fernald, Fisher and Kimball (2010). In the international trade context, Yi (2003) argues that tariffs can multiply up in much the same way when goods get traded multiple times during the stages of production. Ciccone (2002) is the first modern growth paper I know of to develop this insight, deriving a multiplier formula for a triangular input-output structure. Jones (2011) also emphasizes the importance of the intermediate goods multiplier, albeit for a relatively restrictive input-output structure.

3.1. A Simple Example

A simple example is helpful for understanding how intermediate goods generate a multiplier. Suppose gross output Q_t is produced using capital K_t , labor L_t , and intermediate goods X_t .

$$Q_t = \bar{A} (K_t^\alpha L_t^{1-\alpha})^{1-\sigma} X_t^\sigma. \quad (1)$$

Gross output can be used for consumption or investment or it can be carried over to the next period and used as an intermediate good. To keep things simple, assume a

constant fraction \bar{x} is used as an intermediate good:

$$X_{t+1} = \bar{x}Q_t. \quad (2)$$

GDP in this economy is gross output net of spending on intermediate goods: $Y_t \equiv (1 - \bar{x})Q_t$. In a steady state with no growth, it is easy to show that GDP will be given by

$$Y_t = \text{TFP} \cdot K_t^\alpha L_t^{1-\alpha}, \quad (3)$$

where

$$\text{TFP} \equiv (\bar{A}\bar{x}^\sigma(1 - \bar{x})^{1-\sigma})^{\frac{1}{1-\alpha}}. \quad (4)$$

TFP depends on the allocation of resources to intermediate goods. It will be maximized when $\bar{x} = \sigma$, which is the optimal spending share on intermediates. For any other spending share, however, TFP will be lower, and this effect will be amplified the higher is the intermediate goods share.

Going further, let's assume a constant fraction \bar{s} of GDP is invested:

$$\begin{aligned} K_{t+1} &= \bar{s}Y_t + (1 - \delta)K_t, \\ &= \bar{s}(1 - \bar{x})Q_t + (1 - \delta)K_t, \end{aligned} \quad (5)$$

Assume labor is exogenous and constant.

This model features a steady state, where the level of GDP per worker $y_t \equiv Y_t/L_t$ is

$$y^* \equiv \frac{Y}{L} = \left(\bar{A}\bar{x}^\sigma(1 - \bar{x})^{1-\sigma} \left(\frac{\bar{s}}{\delta} \right)^{\alpha(1-\sigma)} \right)^{\frac{1}{(1-\alpha)(1-\sigma)}}. \quad (6)$$

A key implication of this result is that the effects of misallocation or basic productivity differences get multiplied. In particular, consider the simple allocation term $\bar{x}^\sigma(1 - \bar{x})^{1-\sigma}$, familiar from our steel-and-latte economy. Now that the misallocation applies to a produced good, its effects are amplified: there is an exponent of $\frac{1}{(1-\alpha)(1-\sigma)} > 1$ that applies to misallocation.

To see this more simply, observe that a 1% increase in productivity \bar{A} increases output by more than 1% because of the multiplier $\frac{1}{(1-\alpha)(1-\sigma)}$. In the absence of in-

intermediate goods ($\sigma = 0$), this multiplier is just the familiar $\frac{1}{1-\alpha}$: an increase in productivity raises output, which leads to more capital, which leads to more output, and so on. The cumulation of this virtuous circle is $1 + \alpha + \alpha^2 = \frac{1}{1-\alpha}$.

In the presence of intermediate goods, there is an additional multiplier: higher output leads to more intermediate goods, which raises output (and capital), and so on. The overall multiplier is therefore $\frac{1}{(1-\alpha)(1-\sigma)}$. In fact, this multiplier can also be written as $\frac{1}{1-\beta}$, where $\beta \equiv \sigma + \alpha(1-\sigma)$ is the total factor share of produced goods in gross output, capital and intermediates here.

Quantitatively, the addition of intermediate goods has a large effect. For example, consider the multipliers using conventional parameter values, a capital exponent of $\alpha = 1/3$ and an intermediate goods share of gross output of $\sigma = 1/2$. In the absence of intermediate goods the multiplier is $\frac{1}{1-\alpha} = 3/2$, and a doubling of \bar{A} raises output by a factor of $2^{3/2} = 2.8$. But with intermediate goods, the multiplier is $\frac{1}{(1-\alpha)(1-\sigma)} = \frac{3}{2} \cdot 2 = 3$, and a doubling of \bar{A} raises output by a factor of $2^3 = 8$. As discussed in Jones (2011), if we think of the standard neoclassical factors (like \bar{s} in the example) as generating a 4-fold difference in incomes across rich and poor countries, then this 2-fold difference in TFP leads to an 11.3-fold difference in the model with no intermediate goods, but to a 32-fold difference once intermediate goods are taken into account, close to what we see in the data.⁵

The deeper question in this paper is whether this multiplier carries over into a model with a rich and realistic input-output structure. Perhaps the input-output structure in practice does not lead to these large feedback effects. Or perhaps importing intermediate goods dilutes the multiplier substantially in practice. In fact, the remainder of this paper shows that these concerns are not important in practice. The simple “one over one minus the intermediate goods share” formula suggested by this example turns out to be a very good approximation to the true input-output

⁵An implication of this reasoning that is worthy of further exploration is related to transition dynamics. A puzzle in the growth literature is why speeds of convergence are so slow, on the order of 2% per year; see Hauk and Wacziarg (2004) for a recent summary of the evidence. The standard neoclassical growth model with a capital share of 1/3 leads to a speed of convergence of about 7% per year. The presence of intermediate goods would slow this rate down, just as it raises the multiplier. (A difficulty in quantifying this effect is the question of how long it takes to produce and use intermediate goods: one week, one month, or one year? That is, how long is a period?)

multiplier in modern economies. Moreover, we introduce distortions explicitly and show how this same multiplier applies to misallocation.

4. Preliminary Exploration of a Full Input-Output Model

Assume the economy consists of N sectors. Each sector uses capital, labor, domestic intermediate goods, and imported intermediate goods to produce gross output. In turn, this output can be used for final consumption or as an intermediate good in production.

Given this general picture, we specialize to a particular structure with two goals in mind: analytic tractability and obtaining a model that can be closely connected to the rich input-output data. To these ends, the model augments the original Long and Plosser (1983) business cycle model, based on Cobb-Douglas production functions, by embedding it in a model with trade.

We begin by describing the economic environment and then allocate resources using a competitive equilibrium with distortions.

4.1. The Economic Environment

Each of the N sectors produces with the following Cobb-Douglas technology:

$$Q_i = A_i \left(K_i^{\alpha_i} H_i^{1-\alpha_i} \right)^{1-\sigma_i-\lambda_i} \underbrace{d_{i1}^{\sigma_{i1}} d_{i2}^{\sigma_{i2}} \cdots d_{iN}^{\sigma_{iN}}}_{\text{domestic IG}} \underbrace{m_{i1}^{\lambda_{i1}} m_{i2}^{\lambda_{i2}} \cdots m_{iN}^{\lambda_{iN}}}_{\text{imported IG}} \quad (7)$$

where i indexes the sector. A_i is an exogenous productivity term, which itself is the product of aggregate productivity A and sectoral productivity η_i : $A_i \equiv A\eta_i$. K_i and H_i are the quantities of physical and human capital used in sector i . Two kinds of intermediate goods are used in production: d_{ij} is the quantity of domestic good j used by sector i , and m_{ij} is the quantity of the imported intermediate good j used by sector i . (We assume imported intermediate goods are different, so that they are not perfect substitutes; this fits with the empirical fact that countries both import and produce intermediate goods in narrow 6-digit categories.) We abuse notation

by assuming there are N different intermediate goods that can be imported and by indexing these by j as well. The parameter values in this production function satisfy $\sigma_i \equiv \sum_{j=1}^N \sigma_{ij}$ and $\lambda_i \equiv \sum_{j=1}^N \lambda_{ij}$ and $0 < \alpha_i < 1$, so the production function features constant returns to scale.

Each domestically produced good can be used for final consumption, c_j , or can be used as an intermediate good:

$$c_j + \sum_{i=1}^N d_{ij} = Q_j, \quad j = 1, \dots, N. \quad (8)$$

Rather than specifying a utility function over the N different consumption goods and performing a formal national income accounting exercise, it is more convenient to aggregate these final consumption goods into a single final good through another log-linear production function:

$$Y = c_1^{\beta_1} \cdot \dots \cdot c_N^{\beta_N}, \quad (9)$$

where $\sum_{i=1}^N \beta_i = 1$.

This aggregate final good can itself be used in one of two ways, as consumption or exported to the rest of the world:

$$C + X = Y. \quad (10)$$

It is these exports that pay for the imported intermediate goods. We think of this (static) model as describing the long-run steady state of a model, so we impose balanced trade:

$$X = \sum_{i=1}^N \sum_{j=1}^N \bar{p}_j m_{ij}, \quad (11)$$

where \bar{p}_j is the exogenous world price of the imported intermediate goods.

Finally, we assume fixed, exogenous supplies of physical and human capital; the

effects of endogenizing physical capital in the usual way are well-understood.

$$\sum_{i=1}^N K_i = K, \quad (12)$$

$$\sum_{i=1}^N H_i = H. \quad (13)$$

4.2. A Competitive Equilibrium with Misallocation

To allocate resources in this economy, we will focus on a competitive equilibrium with distortions. As in Chari, Kehoe and McGrattan (2007), Hsieh and Klenow (2009), Lagos (2006), and Restuccia and Rogerson (2008), distortions at the micro (here sectoral) level can aggregate up to provide differences in TFP. For simplicity, we model these distortions as sector-specific reductions revenue, denoted τ_i . These distortions could literally be taxes, but they could also represent any kind of policy that favors one sector over another (regulations, special consideration for credit, and so on). The additional insight developed here is that the misallocation associated with these distortions gets amplified by the input-output structure of the economy.

Definition *A competitive equilibrium with misallocation* in this environment is a collection of quantities $C, Y, X, Q_i, K_i, H_i, c_i, d_{ij}, m_{ij}$ and prices $p_j, w,$ and r for $i = 1, \dots, N$ and $j = 1, \dots, N$ such that

1. $\{c_i\}$ solves the profit maximization problem of a representative firm in the perfectly competitive final goods market:

$$\max_{\{c_i\}} c_1^{\beta_1} \cdot \dots \cdot c_N^{\beta_N} - \sum_{i=1}^N p_i c_i$$

taking $\{p_i\}$ as given.

2. $\{d_{ij}, m_{ij}\}, K_i, H_i$ solve the profit maximization problem of a repre-

sentative firm in the perfectly competitive sector i for $i = 1, \dots, N$:

$$\max_{\{d_{ij}, m_{ij}\}, K_i, H_i} (1 - \tau_i) p_i A_i \left(K_i^{\alpha_i} H_i^{1-\alpha_i} \right)^{1-\sigma_i-\lambda_i} d_{i1}^{\sigma_{i1}} d_{i2}^{\sigma_{i2}} \cdot \dots \cdot d_{iN}^{\sigma_{iN}} m_{i1}^{\lambda_{i1}} m_{i2}^{\lambda_{i2}} \cdot \dots \cdot m_{iN}^{\lambda_{iN}} \\ - \sum_{j=1}^N p_j d_{ij} - \sum_{j=1}^N \bar{p}_j m_{ij} - r K_i - w H_i,$$

taking $\{p_i\}$ as given (τ_i , A_i , and \bar{p}_j are exogenous).

3. Markets clear

- (a) r clears the capital market: $\sum_{i=1}^N K_i = K$
- (b) w clears the labor market: $\sum_{i=1}^N H_i = H$
- (c) p_j clears the sector j market: $c_j + \sum_{i=1}^N d_{ij} = Q_j$

4. Balanced trade pins down X :

$$X = \sum_{i=1}^N \sum_{j=1}^N \bar{p}_j m_{ij}.$$

5. Production functions for Q_i and Y :

$$Q_i = A_i \left(K_i^{\alpha_i} H_i^{1-\alpha_i} \right)^{1-\sigma_i-\lambda_i} d_{i1}^{\sigma_{i1}} d_{i2}^{\sigma_{i2}} \cdot \dots \cdot d_{iN}^{\sigma_{iN}} m_{i1}^{\lambda_{i1}} m_{i2}^{\lambda_{i2}} \cdot \dots \cdot m_{iN}^{\lambda_{iN}} \\ Y = c_1^{\beta_1} \cdot \dots \cdot c_N^{\beta_N}.$$

6. Consumption is the residual:

$$C + X = Y.$$

Counting loosely, there are 12 equilibrium objects to be determined and 12 equations implicit in this equilibrium definition. Hiding behind the last equation is the fact that the revenues from distortions are assumed to be rebated lump sum to households. Because of balanced trade, however, there is no decision for households to make regarding final consumption C , and it is simply determined as the

residual of final output less exports.⁶

4.3. Solving

In solving for the equilibrium of the model, it is useful to define some notation involving linear algebra. This is summarized in Table 1. Then the following proposition characterizes the equilibrium (all proofs are given in the appendix):

Proposition 1 (Solution for Y and C) *In the competitive equilibrium with misallocation, the solution for total production of the aggregate final good is*

$$Y = A^{\tilde{\mu}} K^{\tilde{\alpha}} H^{1-\tilde{\alpha}} \epsilon, \quad (14)$$

where the following notation applies:

$$\mu' \equiv \frac{\beta'(I-B)^{-1}}{1-\beta'(I-B)^{-1}\lambda}, \quad (N \times 1 \text{ vector of multipliers})$$

$$\tilde{\mu} \equiv \mu' \mathbf{1}$$

$$\tilde{\alpha} \equiv \mu' \delta_K$$

$$\omega \equiv \frac{\beta' \omega_c + \beta'(I-B)^{-1} \omega_q}{1-\beta'(I-B)^{-1}\lambda}$$

$$\log \epsilon \equiv \omega + \mu' \bar{\eta}.$$

Moreover, because trade is balanced, GDP for this economy is given by C , which equals

$$C = Y \left(1 - \sum_{i=1}^N \sum_{j=1}^N (1 - \tau_i) \gamma_i \lambda_{ij} \right). \quad (15)$$

There are several points of this proposition that merit discussion. First, and not surprisingly, our N -sector Cobb-Douglas model aggregates up to yield a Cobb-Douglas aggregate production function. More interestingly, aggregate TFP depends on both sectoral TFPs and the underlying distortions. This latter point requires digging into the ϵ term, where distortions then enter in two places. Distortions enter

⁶Given Walras' Law, this equation could be replaced by $C = wH + rK + T$, where T is the lump sum rebate of the revenue obtained by the distortion; notice that all production is either consumed or exported.

Table 1: Notation for Solving the Model

Notation	Typical Element	Comment
<i>Matrices</i> ($N \times N$):		
B	σ_{ij}	The input-output matrix of intermediate good shares.
\bar{B}	$(1 - \tau_i)\sigma_{ij}$	The matrix of intermediate good exponents, adjusted for distortions.
I	—	Identity matrix.
<i>Vectors</i> ($N \times 1$):		
$\mathbf{1}$	$\mathbf{1}$	Vector of ones.
β	β_i	Vector of exponents in final goods production.
γ	γ_i	$\gamma \equiv (I - \bar{B}')^{-1}\beta$; “Domar” shares: $\frac{p_i Q_i}{Y} = \gamma_i$
λ	λ_i	Vector of import shares, $\lambda_i \equiv \sum_{j=1}^N \lambda_{ij}$.
δ_K	$\alpha_i(1 - \sigma_i - \lambda_i)$	Production elasticities for K_i
δ_H	$(1 - \alpha_i)(1 - \sigma_i - \lambda_i)$	Production elasticities for H_i
θ_K	$\frac{\delta_{K_i}\gamma_i}{\sum_{j=1}^N (1 - \tau_j)\delta_{K_j}\gamma_j}$	Solution: $K_i/K = (1 - \tau_i)\theta_{K_i}$
θ_H	$\frac{\delta_{H_i}\gamma_i}{\sum_{j=1}^N (1 - \tau_j)\delta_{H_j}\gamma_j}$	Solution: $H_i/H = (1 - \tau_i)\theta_{H_i}$
ω_K	$\delta_{K_i} \log \theta_{K_i}$	Sectoral allocation term for K_i
ω_H	$\delta_{H_i} \log \theta_{H_i}$	Sectoral allocation term for H_i
ω_d	$\sum_{j=1}^N \sigma_{ij} \log(\sigma_{ij}\gamma_i/\gamma_j)$	Sectoral allocation term for d_{ij}
ω_m	$\sum_{j=1}^N \lambda_{ij} \log(\lambda_{ij}\gamma_i/\bar{p}_j)$	Sectoral allocation term for m_{ij}
ω_q	$\omega_{K_i} + \omega_{H_i} + \omega_{d_i} + \omega_{m_i}$	Sum of allocation terms
ω_c	$\log(\beta_i/\gamma_i)$	Consumption allocation term
$\bar{\eta}$	$\log(\eta_i(1 - \tau_i))$	Sectoral productivity, adjusted for distortions

directly through $\bar{\eta}$, which is a vector of sectoral productivities, adjusted for distortion rates; this is the usual sense in which distortions “directly” affect productivity. Distortions also enter indirectly through the allocation terms, captured by ω . We will return later to the effect of distortions.

The second result to note is the presence of the input-output multiplier, reflected by μ . According to the proposition, this vector of multipliers is given by

$$\mu' \equiv \frac{\beta'(I - B)^{-1}}{1 - \beta'(I - B)^{-1}\lambda}. \quad (16)$$

Let’s break this down piece by piece, since it is one of the essential results of the paper.

The matrix $L \equiv (I - B)^{-1}$ is known as the Leontief inverse. The typical element l_{ij} of this matrix can be interpreted in the following way: (ignoring trade for the moment) a 1% increase in productivity in sector j raises output in sector i by l_{ij} %. This result takes into account all the indirect effects at work in the model. For example, raising productivity in the electricity sector makes banking more efficient and this in turn raises output in the construction industry. The Leontief inverse incorporates these indirect effects. (Notice that it is the matrix equivalent of $1/(1 - \sigma)$.)

Multiplying this matrix by the vector of value-added weights in β leads to $\beta'(I - B)^{-1} = \sum_{i=1}^N \beta_i l_{ij}$. That is, we add up the effects of sector j on all the other sectors in the economy, weighting by their shares of value-added. The typical element of this multiplier matrix then reveals how a change in productivity in sector j affects overall value-added in the economy.

This would be precisely correct if λ_{ij} were zero — that is, in the absence of trade. In the presence of trade, this multiplier gets adjusted by the factor $1/(1 - \beta'(I - B)^{-1}\lambda)$. We will discuss this factor in more detail below, but for now it is enough to note that this factor is larger than one: trade strengthens the multiplier rather than attenuating it.

The elasticity of final output with respect to aggregate TFP is $\tilde{\mu} \equiv \mu'1$. That is, we add up all the multipliers in μ since an increase in aggregate TFP affects not just sector j but all the sectors.

A final remark about Proposition 1 concerns the capital exponent in the aggregate production function, $\tilde{\alpha} \equiv \mu' \delta_K$. Recall that δ_K is the vector of capital exponents $\alpha_i(1 - \sigma_i - \lambda_i)$. The aggregate exponent is therefore a weighted average of the sectoral capital shares, where the weights depend on the intermediate good shares. This remark will make even more sense after the next proposition.

5. Special Cases, To Build Intuition

5.1. The Multiplier in a Special Case

The linear algebra formula is a useful theoretical result and will prove convenient when we apply the model to the rich input-output data that exists. However, analyzing a special case can be helpful in obtaining intuition for how the model works.

Consider the following special case. Suppose all sectors have the same cumulative elasticities of output with respect to domestic and imported intermediate goods, although the composition across sectors is allowed to vary. For example, one sector may use a lot of electricity and steel, while another sector uses a lot of financial services and information technology. The composition can vary across sectors, but suppose each sector spends 50 percent of its revenue on intermediate goods. What does the multiplier look like in a case like this?

The following proposition provides the answer. In fact, it allows for imported intermediate goods as well (where the overall share spent on these goods is the same in each sector):

Proposition 2 (Multiplier in a special case) *Assume $\sigma_i \equiv \sum_{j=1}^N \sigma_{ij} = \hat{\sigma}$ and $\lambda_i \equiv \sum_{j=1}^N \lambda_{ij} = \hat{\lambda}$ for all i , where $\hat{\sigma}$ and $\hat{\lambda}$ are positive scalars whose sum is less than one, and define $\bar{\sigma} \equiv \hat{\sigma} + \hat{\lambda}$ to be the total intermediate goods share. Then*

$$\frac{\partial \log Y}{\partial \log A} = \mu' \mathbf{1} = \frac{\beta'(I - B)^{-1} \mathbf{1}}{1 - \beta'(I - B)^{-1} \lambda} = \frac{1}{1 - \bar{\sigma}}.$$

This special case makes two general points about the model. First, the “sparseness” of the input-output matrix B is not especially important. For example, our

special case includes a “clock” structure, where every sector uses as an input only the good produced by the sector above it. It also includes the case where every sector uses only its own output. In both of these cases, the input-output matrix is very sparse, with zeros almost everywhere. Yet the overall multiplier remains equal to one over one minus the intermediate goods share. This special case suggests that if the overall intermediate goods share is about 1/2, we shouldn’t be surprised to find a multiplier of about 2. This intuition will be confirmed in the next section when we turn to quantitative results.

The second key point made in this proposition is that the intuition that imports would dilute the multiplier is a red herring. In fact, there is no dilution at all: in the proposition, it is the overall intermediate goods share $\bar{\sigma} \equiv \hat{\sigma} + \hat{\lambda}$ that matters for the multiplier, and the composition between domestic and imported goods is completely irrelevant.

Why is this the case? The answer is that we have imposed balanced trade in our (long run) model. Therefore exports are used to “produce” imports. A higher productivity in the domestic computer chip sector raises overall exports, which in turn increases imports, so the virtuous circle is not broken by the presence of trade.⁷

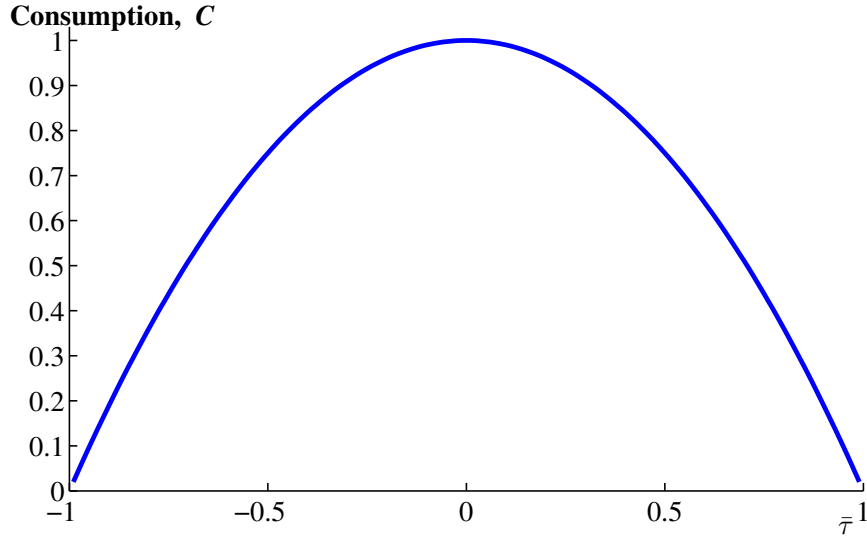
5.2. Symmetry and Distortions

Our second special case allows us to study the multiplier associated with distortions. First, we consider a world where the intermediate good shares of production are the same in every sector and there is a symmetric distortion at rate $\tau_i = \bar{\tau}$. In this case, GDP in the economy is given by the following proposition:

Proposition 3 (Symmetry and Distortions) *Suppose $\sigma_{ij} = \hat{\sigma}/N$, $\lambda_{ij} = \hat{\lambda}/N$, $\beta_i = 1/N$, $\alpha_i = \alpha$, and $\tau_i = \bar{\tau}$. Then*

$$\log C = \text{Constant} + \frac{\bar{\sigma}}{1 - \bar{\sigma}} \log(1 - \bar{\tau}) + \log(1 - \bar{\sigma}(1 - \bar{\tau})), \quad (17)$$

⁷This assumption of balanced trade is the key difference that makes the intuition from the Keynesian business cycle model inappropriate. In the business cycle context, an increase in exports leads to a trade surplus and does not increase imports.

Figure 3: Consumption versus the Average Distortion, $\bar{\tau}$ 

Note: This example is drawn for $\bar{\sigma} = 1/2$. Notice the similarity to Figure 1.

where $\bar{\sigma} \equiv (\hat{\sigma} + \hat{\lambda})$ denotes the total intermediate goods share, and Constant is a collection of terms that do not depend on $\bar{\tau}$. Moreover, consumption is an inverse-U shaped function of the distortion rate, with a peak that occurs at $\bar{\tau} = 0$.

An example of this proposition is shown in Figure 3. Notice that the effect of a change in the distortion rate on GDP depends essentially on $\bar{\sigma}$. If there are no intermediate goods in this economy, output distortions have no effect. This is because the distortions here represent a violation of the Diamond and Mirrlees (1971) dictum of “no taxation of intermediate goods.” In our (current) setup, K and H are non-produced factors, so a symmetric tax does not distort the allocation of capital.

The key distortion is between consumption and intermediate goods. A good that gets consumed suffers the distortion only once when the good is produced; a good that is used as an intermediate gets distorted when it is first produced then again when it is used as an intermediate. Since a constant fraction of output is consumed and the rest is used as an intermediate good, this process suffers from the vicious cycle of the multiplier.

Symmetric distortions affect GDP through the two terms in equation (17). The first term is the direct effect, where distortions enter the model very much like productivity: recall that both $1 - \tau_i$ and A_i are subject to the multiplier effect through the ϵ term in Proposition 1. The second term mitigates this effect somewhat and captures the indirect effect whereby higher distortions raise consumption (by reducing the purchase of intermediate goods).

5.3. Symmetry with Random Distortions

Our final special case allows us to consider variation in distortions across sectors. Suppose everything in the model other than distortions is symmetric, and allow distortions to be a log-normally distributed random variable:

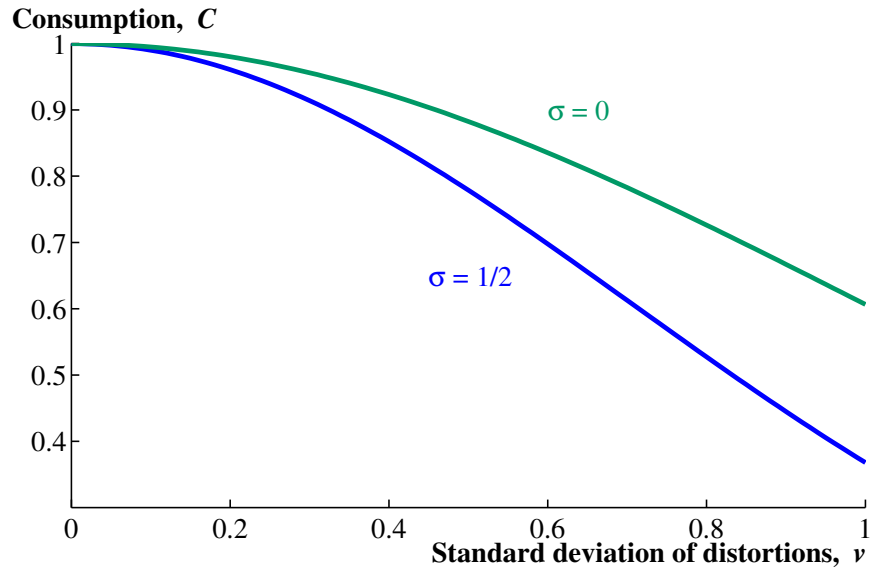
Proposition 4 (Symmetry with Random Distortions) *Suppose $\sigma_{ij} = \hat{\sigma}/N$, $\lambda_{ij} = \hat{\lambda}/N$, and $\beta_i = 1/N$, and let $\bar{\sigma} \equiv \hat{\sigma} + \hat{\lambda}$. Assume $\log(1 - \tau_i) \sim N(\theta, v^2)$ and let $1 - \bar{\tau} \equiv e^{\theta + \frac{1}{2}v^2}$ reflect the average distortion. Then*

$$\begin{aligned} \text{plim}_{N \rightarrow \infty} \log C = & \text{Constant} + \frac{\bar{\sigma}}{1 - \bar{\sigma}} \cdot (1 - \bar{\tau}) \\ & + \log(1 - \bar{\sigma}(1 - \bar{\tau})) - \frac{1}{1 - \bar{\sigma}} \cdot \frac{1}{2} \cdot v^2, \end{aligned}$$

where *Constant* is a collection of terms that do not depend on θ or v^2 . Moreover, consumption is maximized when there are no distortions.

In terms of the mean effect of distortions, this result is identical to the previous one. Now, however, we have an additional result related to the variance of distortions across sectors. In particular, a higher variance of distortions reduces GDP, even in the absence of intermediate goods, since random distortions will distort the allocation of capital and labor across sectors. However, the variance term itself is subject to the now-familiar multiplier effect associated with $1/1 - \bar{\sigma}$. A higher variance of distortions is more costly in an economy with intermediate goods. This makes sense: the first best in this economy is to have no distortions. Either a constant tax or a random tax distorts the allocation of resources and reduces GDP. The

Figure 4: Consumption versus the Standard Deviation of Distortions



Note: This example is drawn for $\bar{\tau} = 0$.

magnitude of the distortion depends on the Diamond-Mirrlees effect: how important intermediate goods are in production. An example is illustrated in Figure 4.

5.4. Random Distortions with a General I-O Structure

So far, I have lacked the right combination of time, talent, and insight to derive a more general result for the effect of log-normal distortions in the presence of the full input-output structure, though I suspect that good results are possible along these lines. The intuition from the previous propositions strongly suggests that something like the general multiplier $\tilde{\mu}$ will continue to play a crucial role. For the empirical applications that follow, I will therefore focus on this general multiplier.

6. Quantitative Analysis

We now turn to the rich input-output data that exists, both for the United States and for many other countries. This data allows us to calculate aggregate and sectoral multipliers and to study the effect of sectoral distortions on aggregate GDP. First, we use the six-digit level data available from the U.S. Bureau of Economic Analysis for the United States in 1997. Then we turn to the OECD Input-Output Database, which contains data for 48 industries and 35 countries.

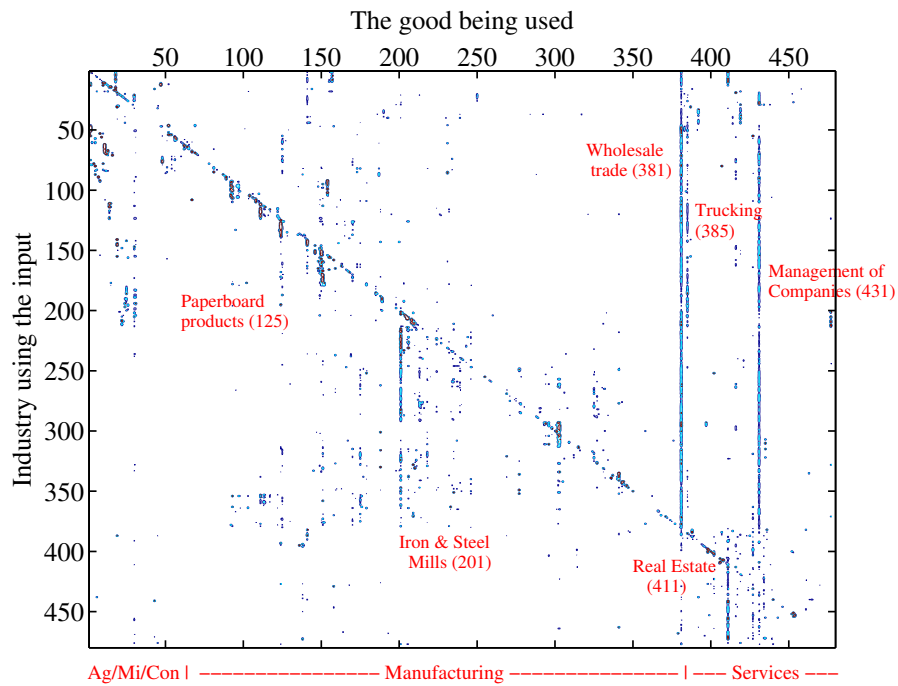
6.1. The U.S. Input-Output Data, 480 Industries

Figure 5 shows something very close to the B matrix for the United States, using the 480 commodities in the BEA's 1997 benchmark input-output data. Actually, we plot the matrix of $\sigma_{ij} + \lambda_{ij}$ instead, so that the entries show the overall exponents on intermediate goods used in producing each of the 480 goods. A contour plot method is used, showing only those shares greater than 2%, 4%, and 8%.

Three points stand out in the figure. First, there is a strong diagonal. Second, the matrix is relatively sparse. Finally, there are a few key exceptions to this sparseness: a few key goods are used by a large number of industries in a significant way. These include wholesale trade, trucking, management of companies, real estate, paper-board products, and iron and steel mills.

Table 2 reports some basic statistics of the U.S. input-output matrix that help put these visual conclusions in context. Even though the diagonal elements were important visually, the table makes the point that these elements are typically small: the mean of them is only 3.3% and the median is only 1.0%. This is true despite the fact that the typical industry pays a large share of its gross output to intermediate goods: 56.4% at the mean. The industry at the 75th percentile pays out about two-thirds of its revenue to intermediate goods, while even the industry at the 25th percentile pays nearly half. Along these lines, it is worth noting that even though just 0.13% of the elements of the input-output matrix exceed 10 percent, this is still 288 elements over all — on average about once for every two sectors. Similarly, 83 of the entries are greater than 20 percent. As the bottom of the table shows, the

Figure 5: The U.S. Input-Output Matrix, 1997 (480 Industries)



Note: The plot shows the matrix $[\sigma_{ij} + \lambda_{ij}]$, that is, the matrix of intermediate good shares for 480 industries. A contour plot method is used, showing only those shares greater than 2%, 4%, and 8%. Source: BEA 1997 Input-Output Benchmark data.

Table 2: Statistics of the U.S. Input-Output Matrix, 1997 (480 Industries)

Properties of the diagonal elements	
Mean:	0.033
75th percentile:	0.045
50th percentile:	0.010
25th percentile:	0.002
Fraction of all elements that are	
equal to zero:	0.510
below 0.1 percent:	0.882
below 0.5 percent:	0.958
below 1.0 percent:	0.979
below 5.0 percent:	0.996
above 10 percent:	0.0013
above 20 percent:	0.0004
above 50 percent:	0.0000
Mean of $\sigma_i + \lambda_i$:	
75th percentile:	0.666
50th percentile:	0.558
25th percentile:	0.477
Aggregate Multipliers	
Domestic, $\beta'(I - B)^{-1}\mathbf{1}$	1.61
Imports, $1/(1 - \beta'(I - B)^{-1}\lambda)$	1.03
Overall, $\tilde{\mu}$	1.65
Actual intermediate goods share:	0.434
“As if” intermediate goods share:	0.394

Note: Except where noted, statistics are reported for the overall input-output matrix of $\sigma_{ij} + \lambda_{ij}$.

overall intermediate goods share for the U.S. economy is about 43.4%: service industries are more important as a share of value-added, and these industries have lower intermediate goods shares.

The last part of the table computes the aggregate multiplier using the 6-digit input-output data. The overall multiplier is 1.65. This number is the product of a domestic multiplier of 1.61 (that would obtain if no intermediate goods were imported), and an import multiplier of 1.03. Imports are relatively unimportant in the multiplier.

To what extent is the simple $\frac{1}{1-\sigma}$ formula accurate? The multiplier of 1.65 would result from this formula if the intermediate goods share were 0.394. In fact, the intermediate goods share using this 6-digit data is 0.434. This simple aggregate formula appears to give a good approximation to the result found by computing the 480x480 Leontief inverse, although there is a small degree of dilution: applying the formula to the 0.434 share suggests a multiplier that overstates the truth by about ten percent.

6.2. The OECD Input-Output Data, 48 Industries

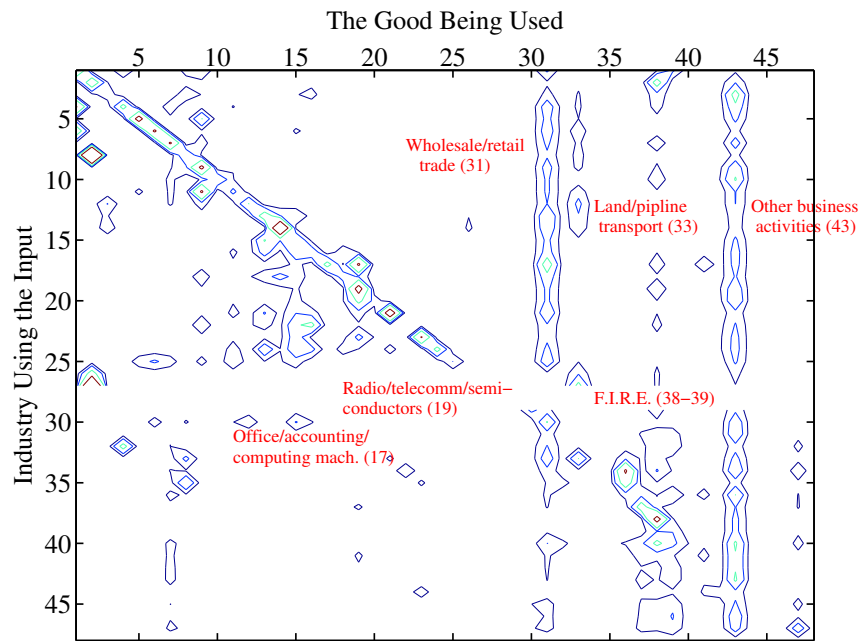
The 2006 edition of the OECD Input-Output Database contains input-output data for 35 countries and 48 industries, typically for the year 2000. In addition to covering OECD countries, the data also include some poor and middle-income countries, such as China, India, Argentina, Brazil, and Russia.

Figure 6 shows the input-output matrix for the United States at this higher level of aggregation. The pattern at the more detailed level of aggregation of a sparse matrix with a strong diagonal and just a few goods that are used widely is repeated at this higher level of aggregation.

One of the nice features of the OECD data is that we can consider the question of how much the input-output structure of an economy differs across countries. The general and perhaps surprising answer that one obtains is “not much.” Figure 7 shows the input-output matrix for two countries, Japan and China, as an example.

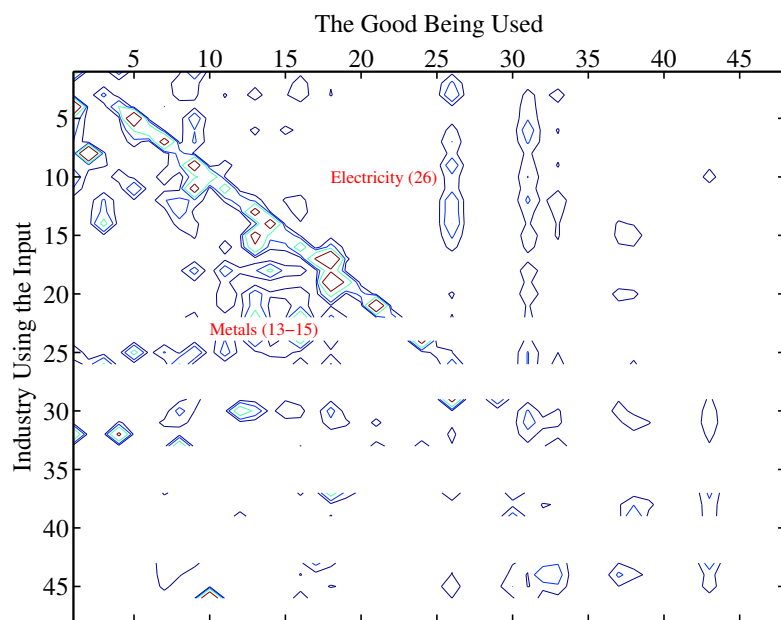
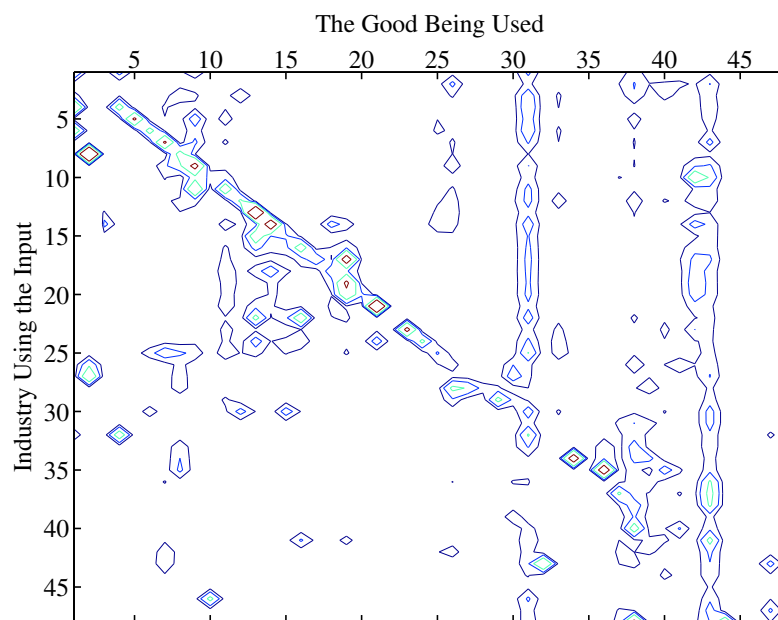
The matrix for Japan looks very much like the matrix for the United States. This

Figure 6: The U.S. Input-Output Matrix, 2000 (48 Industries)



Note: Note: The plot shows the matrix $[\sigma_{ij} + \lambda_{ij}]$, that is, the matrix of intermediate good shares for 48 industries. A contour plot method is used, showing only those shares greater than 2%, 5%, 10% and 20%. Source: OECD 2006 database.

Figure 7: Input-Output Matrix in Japan and China (48 Industries)



is true more generally, especially for the richer countries in the data set. But it is even true for the poorer countries. The input-output matrix for China is perhaps the most different from the United States, but the overall structure is still similar. Electricity shows up as being noticeably more important, and other business activities (which include advertising, accounting, and legal services) as somewhat less important. These are the main differences.

The first column of Table 3 makes these comparisons more systematically. It shows the fraction of elements in the input-output matrix that differ by more than 0.02 from the corresponding elements in the U.S. input-output matrix. Just over 16 percent of the elements exceed this difference in China's input-output matrix, while the corresponding number for Japan is about 9 percent. For this level of the cutoff, the average across the 35 countries is 11 percent. If we lower the cutoff to 0.01, the typical country has differences of this magnitude in just over 20 percent of the cells. If we raise the cutoff to 0.05, the average across countries is 3.9 percent of cells.

Figure 8 shows the aggregate multipliers, $\tilde{\mu}$ for the 35 countries in our sample. The average value for the multiplier in this sample is about 1.9. It ranges from a high of 2.53 in China to lows of 1.51 in Greece and 1.59 in India. Interestingly, China and India are two of the poorest countries in the sample, and they have widely different multipliers. The multiplier for the United States using this data works out to be 1.77, slightly higher than what we found in the 6-digit data.

Table 3 shows these multipliers in more detail, including the contribution from imported intermediate goods as well as the aggregate intermediate goods share and the “as if” share that corresponds to the multiplier computed using the Leontief inverse. The simple approximation of “one over one minus the intermediate goods share” does a very good job of approximating the true multiplier.

6.3. Take-away from the IO Data

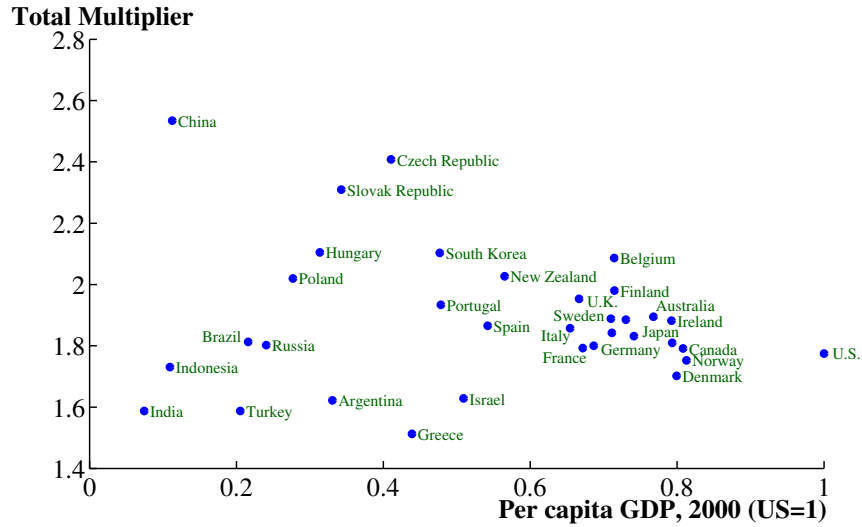
What do we learn from the input-output data? Three things, I think. First, the common $1/1 - \bar{\sigma}$ formula that emerges from simple models of intermediate goods is remarkably robust: more careful analysis with full input-output structures across

Table 3: The Multiplier across a Range of Countries (48 Industries)

Country	Fraction	— Multipliers —			Overall	“As If”
	> .02 Different	Domestic	Import	Total	Interm. Share	Interm. Share
China	0.161	2.21	1.14	2.53	0.63	0.61
Czech Republic	0.115	1.75	1.38	2.41	0.62	0.58
Slovak Republic	0.114	1.68	1.38	2.31	0.61	0.57
Hungary	0.107	1.53	1.38	2.10	0.60	0.52
Korea	0.109	1.72	1.22	2.10	0.58	0.52
Belgium	0.104	1.60	1.30	2.09	0.57	0.52
New Zealand	0.114	1.77	1.15	2.03	0.54	0.51
Poland	0.120	1.73	1.17	2.02	0.53	0.50
Finland	0.101	1.63	1.21	1.98	0.53	0.50
United Kingdom	0.096	1.72	1.14	1.95	0.51	0.49
Portugal	0.112	1.63	1.18	1.93	0.52	0.48
Australia	0.104	1.71	1.11	1.89	0.49	0.47
Sweden	0.096	1.57	1.21	1.89	0.51	0.47
Netherlands	0.096	1.54	1.22	1.89	0.51	0.47
Ireland	0.135	1.35	1.39	1.88	0.53	0.47
Spain	0.099	1.59	1.17	1.87	0.50	0.46
Italy	0.094	1.62	1.15	1.86	0.50	0.46
Austria	0.085	1.51	1.22	1.84	0.48	0.46
Taiwan	0.104	1.53	1.20	1.83	0.52	0.45
Japan	0.092	1.75	1.05	1.83	0.48	0.45
Brazil	0.109	1.69	1.07	1.81	0.48	0.45
Switzerland	0.151	1.54	1.17	1.81	0.49	0.45
Russia	0.242	1.63	1.11	1.80	0.47	0.45
Germany	0.104	1.58	1.14	1.80	0.49	0.44
France	0.104	1.63	1.10	1.79	0.48	0.44
Canada	0.087	1.52	1.18	1.79	0.48	0.44
United States	0.000	1.68	1.05	1.77	0.46	0.44
Norway	0.098	1.53	1.15	1.75	0.46	0.43
Indonesia	0.133	1.52	1.14	1.73	0.49	0.42
Denmark	0.098	1.48	1.15	1.70	0.43	0.41
Israel	0.106	1.49	1.10	1.63	0.41	0.39
Argentina	0.096	1.53	1.06	1.62	0.42	0.38
Turkey	0.114	1.43	1.11	1.59	0.41	0.37
India	0.153	1.49	1.07	1.59	0.44	0.37
Greece	0.114	1.37	1.10	1.51	0.38	0.34
Average	0.110	1.61	1.17	1.88	0.50	0.46

Note: The first column reports the fraction of entries in a country's input-output matrix that differ from those in the U.S. matrix by more than 0.02.

Figure 8: The Multiplier across a Range of Countries (48 Industries)



The figure plots the value of $\tilde{\mu}$ computed for each country against 2000 per capita GDP from the Penn World Tables.

a range of economies suggest that the basic multiplier from simple models carries over quite well. Working with simpler models, then, may be appropriate.

Second, there is a surprising degree of similarity in these matrices across countries. This is surprising in that one might have expected significant differences both for technological reasons and for reasons related to misallocation. On the technological front, countries at different levels of development presumably produce with different technologies, and one might have expected to see this more strongly in the input-output structure of these economies. This is particularly true given the specialization arguments associated with international trade.

On the misallocation front, it should be appreciated that many distortions that might be present would show up by changing observed factor shares, even if the underlying technologies were the same. One way to see that is to recall the first-order condition in a simple neoclassical growth model with Cobb-Douglas production: $(1 - \tau)\alpha\frac{Y}{K} = r$. Firms rent capital until the post-distortion marginal product falls

to equal the rental rate. But in this case, $rK/Y = \alpha(1 - \tau)$, so the observed capital share will differ from the technological parameter by the distortion rate.

This in turn has important implications. There is a fundamental identification problem: we see data on observed intermediate goods shares, and we do not know how to decompose that data into distortions and differences in technologies. This identification problem is not solved in anything I have done. Instead, I've simply shown that the observed spending shares are remarkably similar across countries.

My tentative conclusion given this fact is that the misallocation across 4-digit sectors is not particularly large in this sample of countries. Without solving the basic identification problem, however, this conclusion must remain tentative. One useful way to check this would be to assume the U.S. input-output structure measures the true technology for all countries, and to use observed spending shares on intermediate goods to measure the distortions that apply on average *across* the 4-digit sectors. This would be a valuable exercise. Of course, one could certainly question the assumption that the underlying technologies in all countries are the U.S. factor shares. Moreover, this approach would not measure the distortions that apply *within* each sector, which may be quite important in practice. Redoing the Hsieh and Klenow (2009) analysis using gross output and intermediate goods within sectors for China and India (and other countries) would also be valuable.

7. Conclusion

One of the most exciting directions in the growth literature in recent years has been the recognition that the misallocation of resources at the micro level can aggregate up to look like differences in total factor productivity. Quantifying these effects in novel ways, two examples being the extensive use of firm-level data and the exploration of input-output tables, is yielding new insights on why some countries are so much richer than others and likely has a promising future.

A Appendix: Proofs of the Propositions

Proof of Proposition 1. Solving for Y and C

We begin by considering the profit maximization problems for the final goods and intermediate goods firms. For the final goods firms, recall that the problem is

$$\max_{\{c_i\}} c_1^{\beta_1} \cdot \dots \cdot c_N^{\beta_N} - \sum_{i=1}^N p_i c_i$$

This yields a FOC where the spending shares are the exponents:

$$\frac{p_i c_i}{Y} = \beta_i. \quad (18)$$

Next, consider the intermediate firms:

$$\begin{aligned} \max_{\{d_{ij}, m_{ij}\}, K_i, H_i} (1 - \tau_i) p_i A_i \left(K_i^{\alpha_i} H_i^{1-\alpha_i} \right)^{1-\sigma_i-\lambda_i} d_{i1}^{\sigma_{i1}} d_{i2}^{\sigma_{i2}} \cdot \dots \cdot d_{iN}^{\sigma_{iN}} m_{i1}^{\lambda_{i1}} m_{i2}^{\lambda_{i2}} \cdot \dots \cdot m_{iN}^{\lambda_{iN}} \\ - \sum_{j=1}^N p_j d_{ij} - \sum_{j=1}^N \bar{p}_j m_{ij} - r K_i - w H_i, \end{aligned}$$

The first order conditions for this problem are

$$(1 - \tau_i) \alpha_i (1 - \sigma_i - \lambda_i) \frac{p_i Q_i}{K_i} = r \quad (19)$$

$$(1 - \tau_i) (1 - \alpha_i) (1 - \sigma_i - \lambda_i) \frac{p_i Q_i}{H_i} = w \quad (20)$$

$$(1 - \tau_i) \sigma_{ij} \frac{p_i Q_i}{d_{ij}} = p_j \quad (21)$$

$$(1 - \tau_i) \lambda_{ij} \frac{p_i Q_i}{m_{ij}} = \bar{p}_j. \quad (22)$$

Now we are ready to use these FOCs to solve for some allocations. Begin with the resource constraint for sector j :

$$c_j + \sum_{i=1}^N d_{ij} = Q_j.$$

Now use equation (21) to get rid of d_{ij} and rearrange slightly to get:

$$p_j c_j + \sum_{i=1}^N (1 - \tau_i) \sigma_{ij} p_i Q_i = p_j Q_j.$$

Finally, from the first-order condition for the final goods firm that $p_j = \beta_j Y / c_j$. Using this expression for p_j and canceling Y from both sides of the equation gives

$$\beta_j + \sum_{i=1}^N (1 - \tau_i) \sigma_{ij} \frac{\beta_i Q_i}{c_i} = \frac{\beta_j Q_j}{c_j}. \quad (23)$$

Now, define $v_j \equiv \frac{\beta_j Q_j}{c_j}$ and let v denote the $N \times 1$ vector of v_j . Then we can stack the N equations in (23) to get an equation involving vectors and a matrix:

$$\beta + \bar{B}' v = v \quad (24)$$

where β is the $N \times 1$ vector of final goods exponents and \bar{B} is the $N \times N$ matrix of intermediate goods shares adjusted for taxes: a typical element is $(1 - \tau_i) \sigma_{ij}$. This equation solves easily to give

$$v^* = (I - \bar{B}')^{-1} \beta \equiv \gamma. \quad (25)$$

Notice that this defines the solution for $\beta_j Q_j / c_j$ as γ_j . It is easy to show in fact that these elements are also the solution for $p_j Q_j / Y = \gamma_j$, so that the γ_j terms are the “Domar” weights — the ratio of total spending on intermediate good j to Y .

At this point, we can use this solution to get useful expressions for d_{ij} and m_{ij} as well. Equation (18) implies that $\frac{p_i}{p_j} = \frac{\beta_i}{\beta_j} \cdot \frac{c_j}{c_i}$. Substituting this into the FOC for d_{ij} in (21) leads to

$$d_{ij} = (1 - \tau_i) \sigma_{ij} \frac{\gamma_i}{\gamma_j} \cdot Q_j. \quad (26)$$

Similarly, m_{ij} satisfies

$$m_{ij} = (1 - \tau_i) \lambda_{ij} \gamma_i Y / \bar{p}_j. \quad (27)$$

The FOCs for K_i and H_i similarly yield

$$\frac{K_i}{K} = \frac{(1 - \tau_i)(1 - \sigma_i - \lambda_i)\alpha_i\gamma_i}{\sum_i(1 - \tau_i)(1 - \sigma_i - \lambda_i)\alpha_i\gamma_i} \equiv \bar{\theta}_{K_i} \quad (28)$$

and

$$\frac{K_i}{K} = \frac{(1 - \tau_i)(1 - \sigma_i - \lambda_i)(1 - \alpha_i)\gamma_i}{\sum_i(1 - \tau_i)(1 - \sigma_i - \lambda_i)(1 - \alpha_i)\gamma_i} \equiv \bar{\theta}_{H_i}. \quad (29)$$

In this expression, the “bars” over the θ s denote that these expressions include the $(1 - \tau_i)$ terms in the numerator; this is useful below.

Now we can substitute the expressions in (26) through (29) back into the main production function for intermediate goods. Factoring out the $1 - \tau_i$ terms (and letting the $\theta_{K_i} \equiv \bar{\theta}_{K_i}/(1 - \tau_i)$) gives

$$Q_i = A_i(1 - \tau_i) \left((\theta_{K_i}K)_i^\alpha (\theta_{H_i}H)^{1-\alpha_i} \right)^{1-\sigma_i-\alpha_i} \cdot \prod_{j=1}^N (\sigma_{ij}Q_j\gamma_i/\gamma_j)^{\sigma_{ij}} \cdot \prod_{j=1}^N (\lambda_{ij}\gamma_i Y/\bar{p}_j)^{\lambda_{ij}}. \quad (30)$$

Taking logs of this expression, stacking into a vector, and using much of the notation in Table 1 gives

$$q = \bar{a} + \omega_q + \delta_K \log K + \delta_H \log H + Bq + \lambda \log Y, \quad (31)$$

where q is the vector with typical element $\log Q_i$, \bar{a} is a vector with typical element $\log A_i(1 - \tau_i)$, and B is the matrix of σ_{ij} (see the table for the rest of the notation).

This equation can be solved to yield

$$q = (I - B)^{-1}(\bar{a} + \omega_q + \delta_K \log K + \delta_H \log H + \lambda \log Y) \quad (32)$$

We will use this expression shortly. First, though, we go back to the final goods production function. Recall that $c_i = \beta_i Q_i/\gamma_i$. Taking logs and stacking into a vector, this gives

$$c = \omega_c + q \quad (33)$$

where ω_c is a vector with typical element $\log \beta_i/\gamma_i$ and c denotes the vector of $\log c_i$.

Then, from the final goods production function and using the vector notation,

$$\log Y = \beta'c = \beta'\omega_c + \beta'q.$$

We are now at the last step. Substitute (32) into this last expression to get

$$\log Y = \beta'\omega_c + \beta'(I - B)^{-1}(\bar{a} + \omega_q + \delta_K \log K + \delta_H \log H + \lambda \log Y) \quad (34)$$

Let $A_i \equiv A\eta_i$. This last equation can then be solved for $\log Y$ to yield

$$\log Y = \tilde{\mu} \log A + \tilde{\alpha} \log K + (1 - \tilde{\alpha}) \log H + \log \epsilon \quad (35)$$

where the notation used is that in Table 1.

The expression for consumption comes from using balanced trade and the expression for m_{ij} given in (22).

Proof of Proposition 2. The Multiplier in a Special Case

In matrix notation, the assumption that all sectors have a cumulative domestic intermediate goods share of $\hat{\sigma}$ is simply $B\mathbf{1} = \hat{\sigma}\mathbf{1}$. This implies the following:

$$\begin{aligned} (I - B)\mathbf{1} &= (1 - \hat{\sigma})\mathbf{1} \\ \mathbf{1} &= (I - B)^{-1}\mathbf{1} \cdot (1 - \hat{\sigma}) \\ \mathbf{1} = \beta'\mathbf{1} &= \beta'(I - B)^{-1}\mathbf{1} \cdot (1 - \hat{\sigma}) \\ \Rightarrow \quad \beta'(I - B)^{-1}\mathbf{1} &= \frac{1}{1 - \hat{\sigma}}. \end{aligned}$$

Similarly, $\beta'(I - B)^{-1}\lambda = \frac{\hat{\lambda}}{1 - \hat{\sigma}}$. Therefore

$$\mu'\mathbf{1} = \frac{\beta'(I - B)^{-1}\mathbf{1}}{1 - \beta'(I - B)^{-1}\lambda} = \frac{1}{1 - (\hat{\sigma} + \hat{\lambda})} = \frac{1}{1 - \bar{\sigma}}.$$

Proof of Proposition 3. Symmetry and Distortions

The key step in solving the model is to use the same general result as in the previous proposition: if a matrix X has rows that sum to the same value, \bar{x} , then $(I - X)^{-1}\mathbf{1} = \mathbf{1} \cdot \frac{1}{1 - \bar{x}}$. In this case, this result is used in computing $\gamma = (I - \bar{B}')^{-1}\beta$,

where $\beta_i = 1/N$. Because of the symmetry, one obtains

$$\gamma_j = \hat{\gamma} \equiv \frac{1/N}{1 - \sigma(1 - \bar{\tau})}.$$

Substituting this result into the FOCs, one gets

$$d_{ij} = (1 - \bar{\tau})\hat{\sigma}Q_j/N$$

$$m_{ij} = (1 - \bar{\tau})\hat{\lambda}/N\hat{\gamma}Y/\bar{p}_j$$

as well as $K_i/K = H_i/H = 1/N$.

Using these condition to compute the allocation terms, one obtains

$$\omega_{qi} = -(1 - \hat{\sigma} - \hat{\lambda})\log(1 - \bar{\tau}) - \hat{\lambda}\log(1 - \hat{\sigma}(1 - \bar{\tau})) + \text{Constant}$$

where the constant does not depend on $\bar{\tau}$ or on the sector i . In addition, $\beta'\omega_c = \log(1 - \hat{\sigma}(1 - \bar{\tau}))$.

Following the definitions in Table 1, these expressions can be combined to yield the allocation term:

$$\omega = \log(1 - \hat{\sigma}(1 - \bar{\tau})) - \log(1 - \bar{\tau}) + \text{Constant}$$

for some other constant that does not depend on $\bar{\tau}$.

Substituting this into the definition of ϵ gives

$$\log \epsilon = \log(1 - \hat{\sigma}(1 - \bar{\tau})) + \frac{\hat{\sigma} + \hat{\lambda}}{1 - (\hat{\sigma} + \hat{\lambda})}\log(1 - \bar{\tau}) + \text{Constant}.$$

Furthermore, $\log Y$ will have the same form.

Finally, we need to get the expression for GDP, C . Recall that because of balanced trade,

$$C = Y \left(1 - \sum_{i=1}^N \sum_{j=1}^N (1 - \tau_i)\gamma_i\lambda_{ij} \right).$$

Similar arguments to those above give

$$C = Y \left(\frac{1 - (\hat{\sigma} + \hat{\lambda})(1 - \bar{\tau})}{1 - \hat{\sigma}(1 - \bar{\tau})} \right).$$

Substituting this into the expression for Y (or rather $\log \epsilon$) above completes the proof.

Proof of Proposition 4. Symmetry with Random Distortions

This proof follows that for Proposition 3 fairly closely. The main exception turns out to be in getting the solution for $\mu' \ell$, where ℓ denotes the $N \times 1$ vector with typical element $\log(1 - \tau_i)$. This proceeds as follows. Using the fact that $\beta_i = 1/N$

$$\mu' \ell = \frac{1 - \hat{\sigma}}{1 - (\hat{\sigma} + \hat{\lambda})} \cdot \frac{1}{N} \cdot \mathbf{1}'(I - B)^{-1} \ell \quad (36)$$

The key step is then to show that $\mathbf{1}'(I - B)^{-1} = \frac{1}{1 - \hat{\sigma}} \cdot \mathbf{1}'$. This can be shown as follows. Let σ denote an $N \times 1$ vector where each element is $\hat{\sigma}$. Then, since B is an entire matrix of $\hat{\sigma}$, it follows that

$$\mathbf{1}'B = \sigma'.$$

Then

$$\mathbf{1}' - \mathbf{1}'B = \mathbf{1}' - \sigma'$$

and therefore

$$\mathbf{1}'(I - B) = (1 - \hat{\sigma})\mathbf{1}'.$$

Post-multiplying by $(I - B)^{-1}$ and rearranging gives the result we wanted: $\mathbf{1}'(I - B)^{-1} = \frac{1}{1 - \hat{\sigma}} \cdot \mathbf{1}'$. Once this is substituted into equation (36), one gets the expected result that

$$\mu' \ell = \frac{1}{1 - (\hat{\sigma} + \hat{\lambda})} \cdot \frac{1}{N} \sum_i \log(1 - \tau_i).$$

Following the same arguments used in proving Proposition 3, one gets

$$\log C = \log(1 - (\hat{\sigma} + \hat{\lambda})(1 - \bar{\tau})) - \log(1 - \bar{\tau}) + \frac{1}{1 - (\hat{\sigma} + \hat{\lambda})} \cdot \frac{1}{N} \sum_i \log(1 - \tau_i) + \text{Constant}.$$

The rest of the proposition follows naturally from the log normal assumptions on $1 - \tau_i$.

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