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Edgar L. Feige [*]

Abstract

   Despite financial innovations that have created important new substitutes for cash usage, per capita holdings of U.S. currency amount to $2950. Yet American households and businesses admit to holding only 15 percent of the currency stock, leaving the whereabouts of 85 percent unknown. Some fraction of this unaccounted for currency is held abroad (the dollarization hypothesis) and some is held domestically undeclared, as a store of value and a medium of exchange for transactions involving the production and distribution of illegal goods and services, and for transactions earning income that is not reported to the IRS (the unreported economy hypothesis).

   We find that the percentage of U.S. currency currently held overseas is between 30-37 percent rather than the widely cited figure of 65 percent. This finding is based on the official Federal Reserve/Bureau of Economic Analysis data which is a proxy measure of the New York Federal Reserve's (NYB) "confidential" data on wholesale currency shipments abroad. We recommend that the NYB data be aggregated so as to circumvent confidentiality concerns, and be made readily available to all researchers in order to shed greater light on the questions of how much U.S. currency is abroad and on the particular location of overseas U.S. dollars.

   The newly revised official estimates of overseas currency holdings are employed to determine the Federal Reserve's seigniorage earnings from 1964-2010, which have provided a $287 billion windfall for U.S. taxpayers. Overseas currency stock data are also used to derive estimates of the *domestically* held stock of currency as well as narrow and broad measures of *domestic* monetary aggregates. These *domestic* monetary aggregates are believed to be better predictors of future economic activity than traditional monetary aggregates and are tested to determine their ability to predict fluctuations in real output and prices.

    Domestic cash holdings are finally used to estimate the size of the U.S. unreported economy as measured by the amount of income that is not properly reported to the IRS. By 2010, we estimate that legal and illegal source unreported income" is $1.9 - $2.4 trillion, implying a "tax gap" in the range of $400- $550 billion. Currently, we estimate that 18-23 percent of total reportable income is not properly reported to the IRS.

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New Estimates of U.S. Currency Abroad, the Domestic Money Supply and the Unreported Economy

Edgar L. Feige[1]

Introduction: The Currency Enigma Revisited

One of the most reliable economic statistics is the amount of U.S. currency in circulation held outside of depository intuitions by the public. By the end of 2010, U.S. currency in circulation with the public[2] had risen to $920 billion dollars, amounting to $2950 for every man, woman and child in the country. Over the past decades we have witnessed a host of cash-saving financial innovations, leading to widespread predictions of the advent of a "cashless society". But contrary to these expectations, the demand for U.S. dollars continues to rise and we remain awash in cash. Over the last twenty years, real *per capita* currency holdings increased by 79 percent and currency as a fraction of the M1 money supply rose from 30 percent to 49 percent.

To put these figures in perspective, they imply that the average American's bulging wallet holds 91 pieces of U.S. paper currency, consisting of: 31 one dollar bills; 7 fives; 5 tens; 21 twenties; 4 fifties and 23 one hundred dollar bills. Few of us will recognize ourselves as "average" citizens. Clearly, these amounts of currency are not normally necessary for those of us simply wishing to make payments when neither credit/debit cards nor checks are accepted or convenient to use.

Federal Reserve surveys (Avery et al. 1986, 1987) of household currency usage found that U.S. residents admitted to holding less than 10 percent of the nation's currency supply. Businesses (Anderson, 1977; Sumner, 1990) admitted to holding 5 percent. It seems that the whereabouts of roughly 85 percent of the nation's currency supply is unknown. This anomalous finding suggests that the "currency enigma" (Feige 1989, 1994) and the problem of "missing currency" (Sprenkel, 1993) is still very much with us.

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[2] The currency data used throughout the paper refers to the currency component of the M1 money supply defined as currency outside U.S. Treasury, Federal Reserve Banks and the vaults of depository institutions. (Not seasonally adjusted). (http://www.federalreserve.gov/releases/h6/hist/h6hist4.pdf) . The "currency outside banks" series from the Flow Of Funds Accounts of the United States Z.1 (Table L 204, line 6) (not seasonally adjusted) is typically somewhat larger than the currency component series.

The currency enigma has both a stock and a flow dimension. First we must determine who holds the outstanding stock of U.S. cash. Specifically, how much of this currency is abroad, (the dollarization hypothesis) and how much is held domestically (the underground economy hypothesis) by citizens reluctant to admit to their true cash holdings? The flow issue concerns the amount of cash payments sustained by that missing currency. If half of the missing currency is hoarded and the other half is used as a medium of exchange, turning over at an average velocity of between 30 and 50 transactions per year, (Feige, 1989a) the missing circulating currency stock would give rise to a flow of "missing payments" of an order of magnitude comparable to the entire GNP of the United States.

The location of America's currency stock and the frequency of its use (currency turnover or velocity) have important implications for a variety of economic issues. If a large fraction of U.S. currency is held abroad, U.S. citizens derive considerable benefit from seigniorage, since the U.S. government effectively obtains an interest free loan from foreign citizens holding U.S. dollars. U.S. dollars have historically been perceived to have many desirable properties that made them attractive to both domestic and foreign holders. As a relatively stable currency the dollar functioned as a safe and portable store of value, reducing user's risks of bank failures, devaluations and inflation. As an anonymous and widely accepted means of payment that left no paper trail, U.S. cash was a preferred medium of exchange for "underground" transactions. More recently, the growing popularity of the Euro and the rapid development of transition economies may have weakened overseas demand for U.S. dollars as a second currency, thereby reducing our overseas seigniorage earnings.

From the perspective of conducting domestic monetary policy, the relevant monetary aggregates to consider are the *domestic* money supply and the *domestic* monetary base (Feige, 1994). In order to determine the *domestic* monetary aggregates, the Federal Reserve needs to know what fraction of U.S. currency is held abroad and the annual net outflow of U.S. currency going abroad. Similarly, foreign monetary authorities need to know the extent to which their nations are "*de facto* dollarized" (Feige, 2003), and the magnitude of net inflows of foreign currencies into their economies. *De facto*

dollarization reduces the effectiveness of exchange rate stabilization policies and reduces seigniorage revenues.

The whereabouts of America's cash also has fiscal consequences. U.S. currency is a preferred medium of exchange for facilitating clandestine transactions, and for storing illicit and untaxed wealth. Knowledge of its location and usage is required to estimate the origins and volume of illicit transactions. These include the illegal trade in drugs, arms and sex as well as the amount of "unreported" income, that is, income not properly reported to the fiscal authorities due to noncompliance with the tax code. The fiscal revenue lost to the government creates a "tax gap" that measures the extent to which taxpayers do not file their tax returns and pay the correct tax in a timely manner. Tax evasion gains increasing importance at a time of severe fiscal deficits that could be reduced by improved tax compliance.

In short, our understanding of a number of key monetary and fiscal issues depends upon the answer to a single empirical question, namely, what fraction of the U.S. currency supply is held abroad? It is to this question and its implications that we now turn. Section 1 examines the evolution of the U.S. currency stock and changes in its denomination structure over time. Section 2 reviews the empirical controversy over the amount of U.S. currency held abroad, and presents new time series estimates of the fraction of U.S. currency held overseas. Section 3 reviews and evaluates the direct data sources bearing on the inflow and outflow of currency to and from the U.S. and reviews the methods used to obtain the official Federal Reserve's Flow of Funds statistics and the Bureau of Economic Analysis' data on currency flows abroad. Section 4 reviews the state of our knowledge concerning the specific location of U.S. dollars overseas. Section 5 examines the implications of overseas currency holdings for seigniorage earnings and Section 6 employs improved estimates of domestic monetary aggregates to examine their predictive power in explaining fluctuations in inflation and real output. Section 7 utilizes the latest estimates of the domestic currency supply to calculate the size and growth of the "unreported" economy in the U.S. and provides fiscal estimates of the "tax gap". The final section summarizes the implications of our findings.

1) The Evolution of Cash and its Denomination Structure

Financial innovation creates many substitutes for cash. Credit and debit cards, electronic payments, EZ pass transponders on toll roads, and pre-paid phone cards are common examples. Yet all predictions concerning the advent of a "cashless" society have proven false as evidenced by the evolution of U.S. currency held by the public between 1964 and 2010.

As shown in Figure 1, U.S. cash holdings of the public increased from $35 billion in 1964 to $920 billion by the end of 2010. Moreover, real per capita cash holdings which remained roughly stable over the first twenty year period more than doubled during the most recent twenty five years.

Figure 1
Currency and Real Per Capita Currency
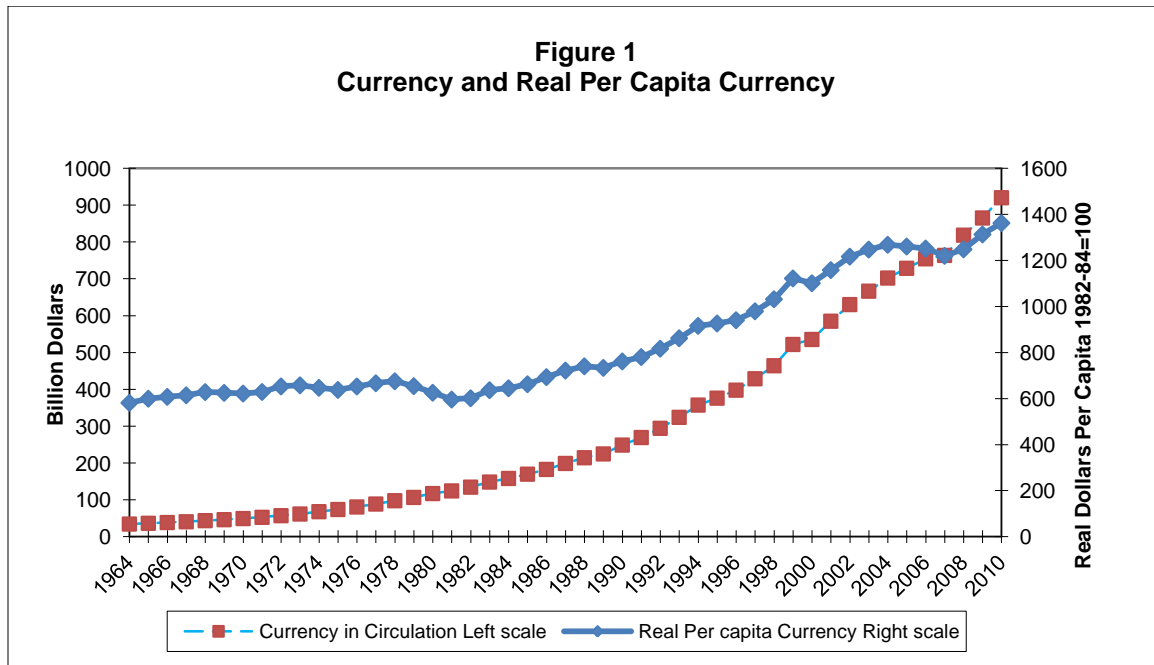
An examination of the evolution of the denomination structure of currency (Figure 2) reveals that fraction of the currency stock made up of the smallest denominations ($1-5) declined from 12.4 percent in 1964 to 2.6 percent in 2010 while the ($10-20) denominations dropped from 56.8 percent to 16.6 percent. The $50 denomination fluctuated around a 10 percent level whereas the $100 denomination showed the most dramatic increase, rising from 21.3 percent in 1964 to 73.3 percent in

2010. This radical change in the denomination structure might be expected to result from changes in the consumer price index which increased seven fold over the past 45 years.

Figure 2
Percent of Currency by Denomination

Figure 3
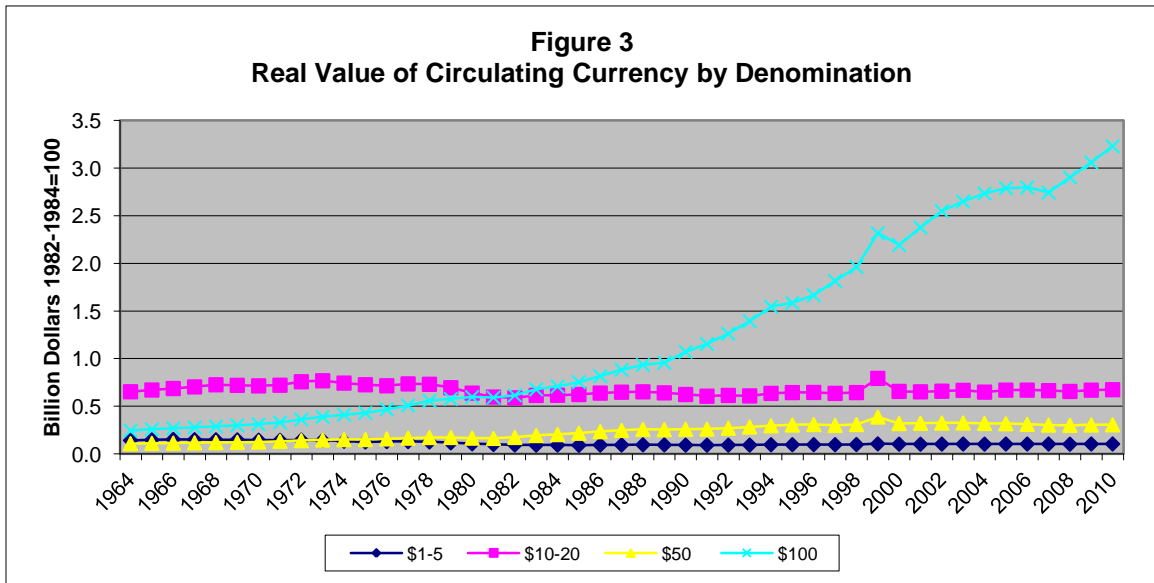**Real Value of Circulating Currency by Denomination**

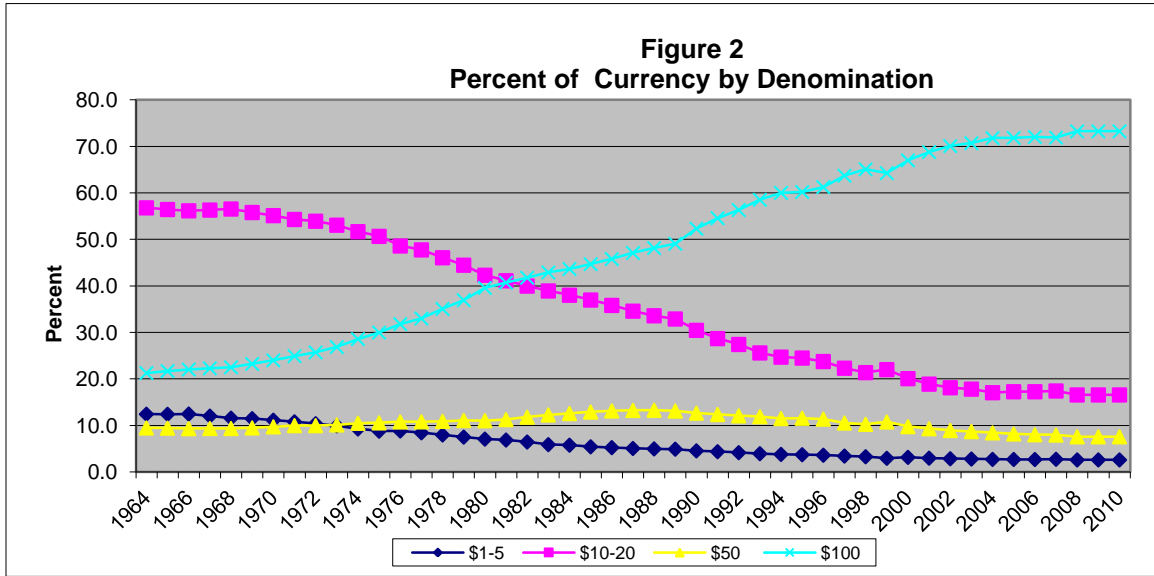Figure 3 depicts the real value of currency held by the public in different denominations. The real value of smaller denomination notes remained roughly constant with a slight rise in the holdings of the $50 notes. However, the real holdings of $100 bills increased fifteen fold during this period. The $100 bill is often used as a store of value although its efficacy as a store of value has declined due to inflation. Nevertheless,

the demand for $100 bills continued to rise in both nominal and real terms. One possible explanation is the "dollarization" hypothesis, (Feige, 2003; 2004) suggesting that U.S. currency, and particularly $100 bills are widely demanded as a second currency in foreign countries experiencing banking crises, political instability and/or hyperinflations.

An alternative source of cash demand arises from its use as a medium of exchange and store of value in the "underground" economy. Since cash usage is anonymous, without leaving a paper trail, it is the preferred medium for purchasing illegal goods and services and for hiding income that should be, but is not reported to the tax authority. The problem then is to determine what fraction of the U.S. currency supply is held abroad and what fraction is held domestically, albeit somewhat clandestinely.

2) The controversy over the location of U.S. currency.

Research in the early nineties witnessed a number of studies attempting to estimate the fraction of U.S. currency held abroad, resulting in an empirical controversy that persists to this day. Examining direct data sources [3] on net outflows of U.S. currency (Feige, 1994), and indirect methods, (variants of monetary demography models) Feige (1996) concluded *"that roughly 36 percent of U.S. currency is held abroad"*. Since alternative methods of estimating overseas currency holdings yielded a varied results, Feige (1997) suggested that the most plausible range of estimates was between 25-45 percent. Doyle (2000) subsequently estimated that in 1995, 30 percent of U.S. currency was held abroad.

Very different results were obtained by Porter and Judson (1996), whose indirect "seasonal" method estimated the share of currency held abroad, to be 70 percent. Taking account of alternative estimation methods, Porter and Judson reported a "median flow estimate" for 1995 of 55 percent abroad, similar to the estimate produced by Anderson and Rasche (1997) of 53.2 percent. Porter and Judson's key conclusion, which has often been cited in the literature, is "that between 55 percent and 70 percent of the U.S. currency stock is currently held outside the country".[4]

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[3] These included both Currency and Monetary Instrument Reports (CMIR) and the Federal Reserve Bank of New York's (NYB) confidential wholesale currency bulk transport data.
[4] Page 899.

Subsequently the U.S. Treasury Department (2006)[5] claimed "that nearly 60 percent of all U.S. banknotes in circulation, or about $450 billion of the $760 billion in circulation as of December 2005, is now held abroad". And most recently, Goldberg (2010) writing in a publication of the New York Federal Reserve asserts that, "about 65 percent of all banknotes are in circulation outside the country. Approximately $580 billion in physical U.S. currency outstanding was circulating overseas at the end of March 2009" [6]

Table 1
The Overseas Currency Controversy

Author	Year	Author's Estimated	Federal Reserve Flow of Funds	Author's Estimated	Federal Reserve Flow of Funds
		Percent abroad	Percent abroad	Amount Abroad (Bil.$)	Amount Abroad (Bil.$)
Feige (1994)	1992	43	30	127	88
Feige (1996)	1994	36	35	129	125
Feige(1997)	1996	25-45	37	100-179	148
Porter/Judson (1996)	1995	55-70	36	207-263	134
Anderson/Rasche (1997)	1995	53.2	36	200	134
Doyle (2000)	1996	30	37	119	148
U.S. Treasury Department (2006)	2005	60	39	450	280
Goldberg (2010)	2009	65	36	580	314

Table 1 summarizes the cited range of estimates of the percent and amount of U.S. currency held overseas for particular years and compares these to the most recent official Federal Reserve Flow of Funds (FOF) data pertaining to overseas currency holdings.[7] The table clearly reveals that whereas the literature has produced a disturbingly wide range of estimates (30-70 percent) of currency held abroad, the FOF statistics suggests that over the past two decades, the percentage of U.S. currency held overseas has remained in a relatively narrow range between 30-39 percent. Of particular

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[5] Page iv. These conclusions appear to based on the earlier work of Porter and Judson.
[6] Page 2. The source for these assertions appear to be the U.S. Treasury Department (2006)
[7] Federal Reserve Statistical Release Z.1 Flow of Funds Accounts of the United States March 10, 2011. Table L.204, (p.86). Line 23 records the stock of U.S. currency held abroad and line 6 records U.S. currency outside of banks. The ratio of line 23 to line 6 yields the faction of U.S. currency held abroad.

concern is the huge $264 billion discrepancy between Goldberg's (2010) estimate of currency abroad and the Board of Governors FOF estimate.

In light of these unsettlingly divergent estimates, we review the main data sources employed to determine the amount of U.S. currency held abroad. Our aim is to review earlier research results; explain the recent dramatic revisions adopted by both the Bureau of Economic Analysis[8] and the Federal Reserve[9] in their officially published estimates of currency held abroad; and to suggest how the long standing controversy over the true fraction of U.S. currency held abroad might be more readily resolved.

3) Direct data sources of currency inflows and outflows

The most direct method for estimating the faction of currency held abroad relies upon data systems designed to track currency outflows and inflows to and from abroad. Two such information systems are the U.S. Customs Service Currency and Monetary Instrument Reports (CMIR)[10] and the New York Federal Reserve Bank's (NYB) records of international wholesale currency shipments abroad.[11]

a) New York Federal Reserve Bank Wholesale Shipments Reports

At present, there is no information system that collects comprehensive data on the total amounts of currency flowing into and out of the U.S. Large overseas shipments of U.S. currency are typically handled by a number of commercial banks acting as bank-note brokers specializing in wholesale bulk currency transport to and from the U.S. Interviews with Federal Reserve officials suggest that the main source of currency provided to these bulk shippers comes from the New York Federal Reserve, with smaller portions originating in the San Francisco and Atlanta Federal Reserve districts.

Since 1988, bulk currency transporters informally reported their overseas shipments and receipts to the New York Reserve Bank Cash Office which maintains an internal confidential data base (NYB) on these currency inflows and outflows. The data are incomplete insofar as they do not reflect currency mailed or hand carried by travelers

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[8] BEA News release. June 17, 2008.
[9] The new figures appear in the 2008 Flow of Funds Z1 Tables F-204 and L-204, however no mention is made of the change in method employed to estimate the revised series of currency flows abroad.
[10] Currently known as the Report of International Transportation of Currency or Monetary Instruments (FinCEN Form 105).
[11] Both of these data systems are described, compared and evaluated in Feige (1996, 1997).

or guest workers. They may also exclude some currency shipments into or out of the country by non reporting shipping entities. Nevertheless, these data currently represent an informative (if at times imperfect) record[12] of currency inflows and outflows, and are invaluable for determining the geographic destination of cash shipments and the origins of cash receipts from overseas locations. Unfortunately, researchers have been denied access to the data for the last decade despite the fact that aggregation techniques (Feige and Watts, 1972) are readily available to overcome confidentiality concerns. Most recently, economists at the Federal Reserve Bank of New York (Hellerstein and Ryan, 2011, displayed graphs of aggregate monthly currency payments and receipts based on these NYB data for the period 1990-2007 but the underlying data were withheld on claims of confidentiality.

b) The FR-160 Proxy

In an effort to avoid the confidentiality restrictions that have prevented direct publication of the NYB data for the past two decades, Feige (1994) initially proposed using a proxy for these confidential data based on the Federal Reserve's FR-160 cash accounting system.[13] The FR-160 reports contain monthly data on denomination specific flows of currency paid into circulation (PIC) and received from circulation (RFC) for each of the 37 Federal Reserve cash offices. Net injections (PIC-RFC) of $100 denomination bills by the New York Federal Reserve cash office (NYNET) were found to be so highly correlated with the internal confidential New York Fed's series on aggregate bulk shipments that they were initially accepted as a serviceable proxy for the NYB series of net currency shipments abroad.[14] Subsequent investigation led Feige (1996) to warn that the NYNET proxy overstated true net outflows. [15]Recognizing that shipments and receipts of currency to and from Asian markets often originated at the Los Angeles cash office of the Federal Reserve, the Board of Governors of the Federal

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[12] In 2003, the Federal Reserve terminated its Extended Custodial Inventory (ECI) agreement with UBS and in 2004 followed with a $100 million civil penalty after discovering that UBS had falsified its reports of overseas shipments to the Federal Reserve over an eight year period. (Pasley, 2005)

[13] The historical background and evolution of the FR-160 reporting system is contained in the Board of Governors technical memorandum #91 entitled " Processing Procedures for the Cash Series", November, 1988.

[14] Feige, 1994.

[15] Feige, 1996, pp. 43-45.

Reserve and the Bureau of Economic Analysis[16] (BEA) adopted a refinement of the original proxy measure, [total net disbursements (PIC-RFC) of $100 notes from the New York City and Los Angeles cash offices (NYLA)] as the new official proxy measure of net currency flows abroad. This NYLA proxy was regularly reported as the net outflow of currency in the Flow of Funds Accounts Z.1 (Table F. 204, Line 23) and in the BEA's International Transactions Accounts (Table 1, Line 67). Corresponding estimates of the cumulative stock of U.S. currency abroad were published in the Flow of Funds (Table L.204) and in the BEA's annual estimates of the U.S. international investment position accounts. Based on the NYLA proxy, the BEA estimated that by the end of 2007, the amount of U.S. currency held abroad was $398 billion, or 52.1% of the currency in circulation. This original NYLA proxy measure of the percent of U.S. currency held abroad is displayed as the upper line in Figure 4 for the years 1974-2010.

Figure 4
Percent of Currency Abroad
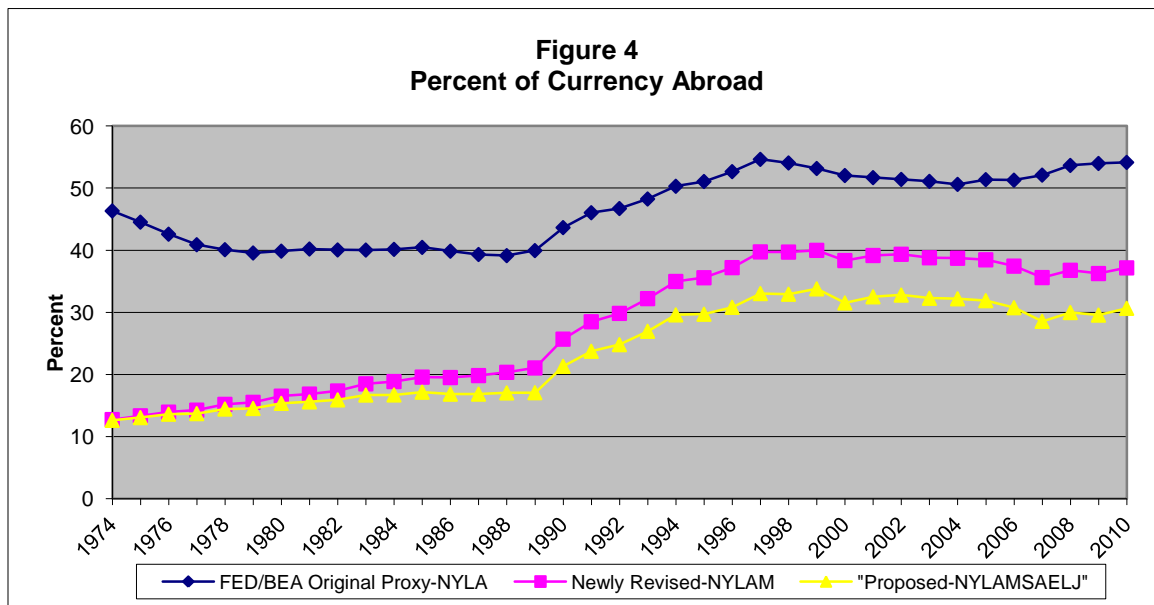
The official NYLA proxy was understood to have several shortcomings. It overstated net shipments abroad to the extent that some of the net injections of $100 bills represented domestic demand for those bills in the NY and LA districts. Moreover, the NYLA proxy took no account of net cash inflows from Latin America that were likely to appear in cash offices located in the southern U.S. border states. The proxy understated

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[16] Bach ,1997.

net shipments abroad to the extent that it excluded shipments of lower denomination notes and took no account of currency flows abroad resulting from tourism, immigrant remittances and U.S. military personnel stationed overseas.

In response to some of the aforementioned criticisms, the BEA[17] recently released significantly revised estimates of the stocks and flows of U.S. currency abroad for the period 1974-2007. The new estimates are based on an adjusted flow proxy that measures total net disbursements (PIC-RFC) of $100 notes from the New York City, Los Angeles and Miami cash offices (NYLAM). These revised estimates decreased the presumed amount of currency held abroad at the end of 1973 from $30.5 billion to $7.7 billion. Since 2008, the revised series appears in both the official Federal Reserve Flow of Funds Accounts and the BEA International Transactions and International Positions Accounts.

According to the newly revised estimates displayed as (NYLAM) in Figure 4, the percent of U.S. currency held abroad at the end of 2010 was 37.2 percent, down from the former estimate of 51.6 percent. This substantial downward revision suggests that $133 billion, formerly thought to have been held overseas is now officially recognized as circulating domestically.

Further scrutiny of net cash disbursements of $100 bills from the Federal Reserve's cash offices in San Antonio (SA), El Paso (EL) and Jacksonville (J) reveals an unusual pattern of net cash inflows that cannot be readily explained by tourist inflows from other cash offices. These offices, located near our Southern border entry points, are likely recipients of funds flowing into the U.S. from Central and South America. I therefore propose to add the net cash disbursements from these additional border cash offices to the currency proxy in the hope of obtaining a more reliable estimate of net currency flows abroad. The resulting estimated percentage of currency held abroad as measured by the proposed (NYLAMSAELJ) proxy is displayed in Figure 4 and suggests that at the end of 2010, 30.7 percent of U.S. currency was held abroad, amounting to $282.2 billion.

To summarize, both Federal Reserve's Flow of Funds and the Bureau of Economic Analysis (FOF/BEA) base their official estimates of U.S. currency flows abroad on a proxy measure which is a surrogate for the New York Federal Reserve's

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[17] BEA (June 17, 2008) News Release

"confidential" data on wholesale bulk shipments of U.S. currency overseas (NYB). The accuracy of the official data therefore depends critically upon how closely it mimics the underlying NYB data. To our knowledge, the only official statement regarding the actual NYB flows appeared in Secretary of the Treasury (2006) which reported that "about $130 billion in U.S. banknotes, on net, moved abroad via wholesale banknote brokers in the eighteen years from 1988 through 2005.[18] By way of comparison, during the same eighteen year period, the official NYLAM proxy estimated that $241 billion had been shipped abroad whereas our proposed NYLAMSAELJ proxy estimated that $199 billion has been shipped abroad. Our tentative conclusion is that even the current "official" estimates of overseas currency are overstated and it is most likely that considerably less than 30 percent of U.S. currency is presently abroad.

c) Currency and Monetary Instrument Reports

As part of its regulatory responsibility under the Currency and Foreign Transactions Reporting Act, the U.S. Customs Service collects information on U.S. currency outflows and inflows. This act required persons or institutions exporting or importing currency or other monetary instruments in excess of $5000[19] to file a "Report of International Transportation of Currency or Monetary Instruments". Commonly known as "CMIRs", these reports have been collected by the U.S. Customs Service since 1977 and are now collected by the Financial Crimes Enforcement Network (FinCEN) of the Department of the Treasury. The CMIR records contain all reported cross border currency inflows and outflows including currency physically transported by currency retailers, non-financial businesses and individuals and currency shipped by financial institutions specializing in wholesale currency transactions. Exceptions as to who must file a CMIR form suggest that the CMIR's are likely to understate true net outflows of currency abroad.

The CMIR reports on currency inflows and outflows can be aggregated by origin and destination. With the cooperation of the U.S. Customs Service and the U.S. Treasury Department Financial Crimes Enforcement Network, the information contained in the

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[18] P.28.
[19] In 1980 the reporting threshold was raised to $10,000.

millions of accumulated confidential CMIR forms was combined by a specially designed algorithm that aggregated CMIR outflows (CTO) and inflows (CTI) so as to maintain the confidentiality of individual records in the CMIR data system. CMIR reports have their own limitations in so far as they exclude currency transactions that fall below the reporting requirement; shipments that circumvent the legal reporting requirements and direct shipments by Federal Reserve Banks and others who are not required to file a CMIR.[20] In the analysis that follows we have adjusted the CMIR data to include shipments and receipts of currency made directly by the New York Federal Reserve. We denote these adjusted aggregated CMIR outflows as CTO_{adj} and the adjusted aggregated CMIR inflows as CTI_{adj}.

Figures 5 and 6 respectively display alternative estimates of currency outflows and inflows for the period for which the CMIR data were available. Figure 5 reveals that


Figure 5
Estimated Currency Outflows
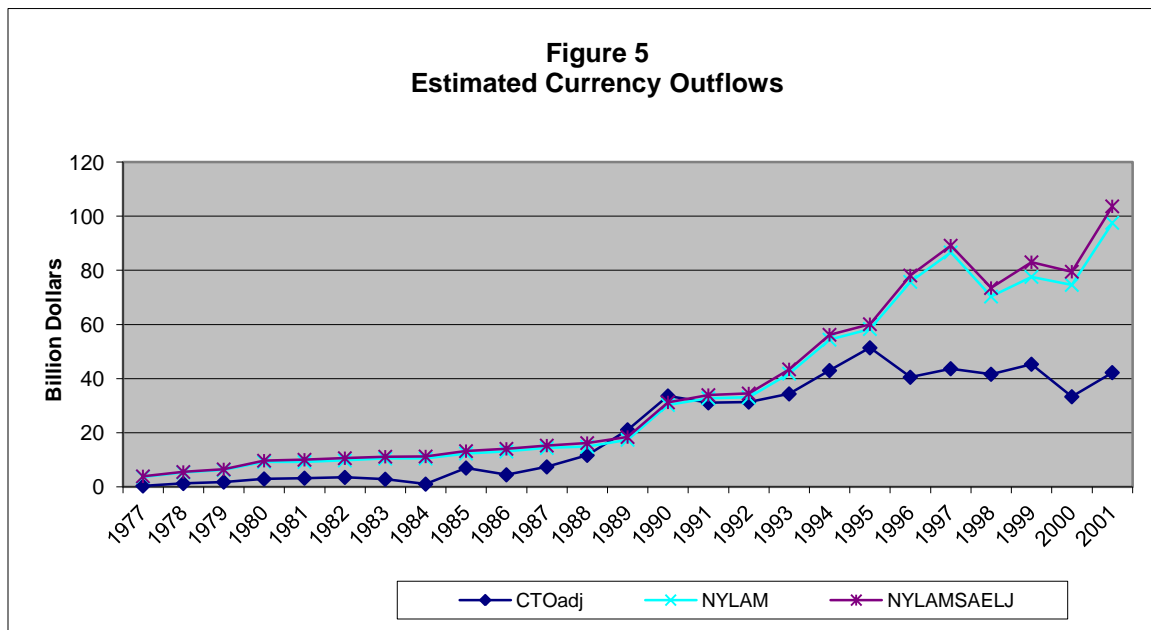
between 1977 and 1995, reported CMIR outflows were generally below the two alternative FR 160 proxy measures.[21] This shortfall results in part from the failure of CMIR's to capture currency outflows falling below the filing threshold and because there

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[20] Instructions concerning exceptions as to who must file are found on FinCEN form 105.
[21] The correlation coefficients between CMIR outflows and NYLAM and NYLAMSAELJ outflows for the period 1977-1995 are respectively .897 and .892. However the mean annual outflow for CMIR is almost $5 billion below the means of the two alternative outflow measures.

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is a general lack of awareness and enforcement of the requirement for individuals to file these reports when leaving the country. Individuals entering the country typically pass through customs and are specifically reminded to fill out the required CMIR form if they are carrying cash amounts above the threshold. The differential awareness and enforcement is reflected by the fact that roughly five times as many arriving travelers filed CMIR forms than did departing travelers and that recorded CMIR inflows for the period 1977-1995 are highly consistent with the two proxy flows as displayed in Figure

Figure 6
Estimated Currency Inflows
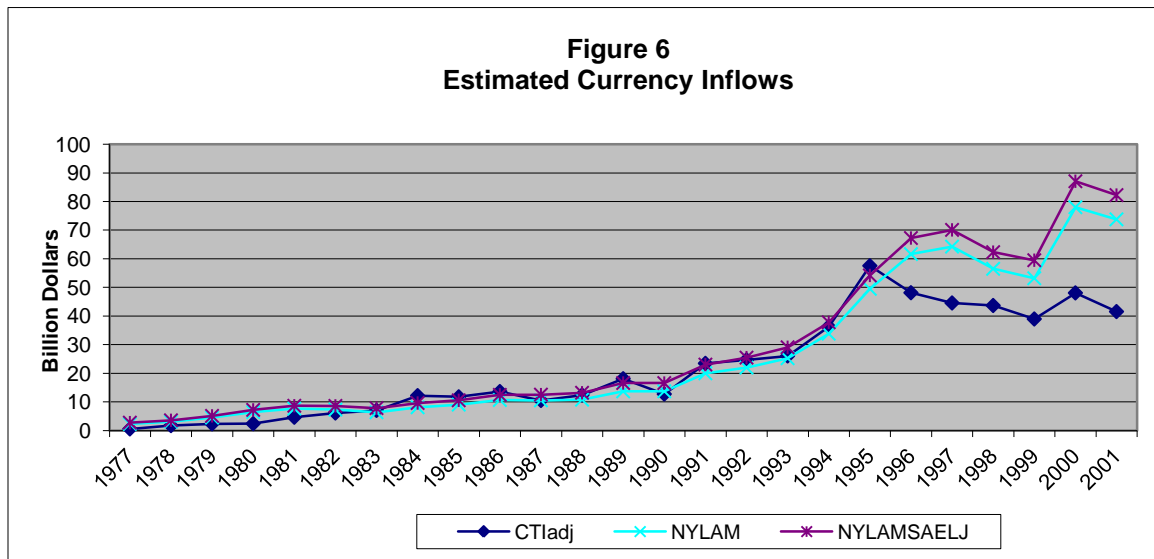
6.[22] We conclude that for the period 1977-1995 CMIR estimates of net currency flows abroad are understated, and should, at best, be considered as a lower bound estimate of the net currency sent abroad.

In 1996 the Treasury Department introduced a newly designed $100 denomination banknote with improved security features. In order to facilitate the rapid introduction of the new notes and to expedite the repatriation of older designed notes, the Federal Reserve established the Extended Custodial Inventory (ECI) program, creating overseas cash depots managed by the New York Federal Reserve. One of the unintended consequences of the establishment of the ECI program was to degrade the quality of CMIR reporting, which failed to appropriately capture currency outflows from the ECI's

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[22] The correlation coefficients between CMIR inflows and NYLAM and NYLAMSAELJ inflows for the period 1977-1995 are respectively .988 and .989 with comparable means.

to other countries as well as currency reflows from foreign countries back to the overseas ECIs. Figures 5 and 6 display the decline in measured CMIR outflows and inflows following the introduction of the ECI program. Taking the currency NYLAM proxy as a basis, it appears that the CMIR data reported lower net outflows during the period 1996-2001 by roughly $19 billion per year. How much of this discrepancy is due to the understatement of the CMIR data or to the overstatement of the NYLAM proxy is impossible to determine. However, the known decline in the reliability of the CMIR data further highlights the importance of obtaining the New York Federal Reserve's (NYB) wholesale currency shipments data in order to arrive at more reliable estimates of the true fraction of currency abroad as well as the country specific location of U.S. currency balances.

The most significant conclusion resulting from our review of direct measures of overseas currency is that far less currency appears to be circulating overseas than was previously thought to be the case. For 2008, the original "official" estimate of the percent of currency overseas was 51 percent whereas the new FED/BEA estimate now stands at 37 percent. If we include FR-160 data from the three additional southern border cash offices that are known to receive considerable amounts of currency from Latin America, the fraction of currency estimated to be overseas is reduced to 30 percent. These new estimates are well below the oft cited figures claiming that half to two thirds of the U.S. currency is held outside the United States.

The new official BEA/FED estimates (Figure 4) suggest that the percent of U.S. currency held abroad rose gradually from 11 percent in 1965 to 21 percent in 1989 and then rose steeply, reaching a peak in 1999 of 40.0 percent. During the past decade, the percentage of U.S. currency appears to have declined to 37 percent. The finding that overseas holdings of U.S. currency are considerably smaller than were previously thought to be the case implies that domestic holdings are even more puzzling.

Given the FOF/BEA estimates of overseas currency, Figure 7 displays the implied temporal growth in per capita *domestic* currency holdings which increased from $175 in 1966 to $1866 by the end of 2010. Real per capita domestic holdings increased by 53 percent during the period. As a percentage of GDP, domestic currency appears to have declined secularly from 1965 to 1998. The observed increase in the ratio between

1998 and 2003 may have been stimulated by concerns of a millennium interruption in the functioning of ATM machines and security concerns resulting from the aftermath of 9/11. Between 2003 and 2007 the ratio of domestic currency to GDP resumed its secular decline but has increased in the past three years. This finding flies in the face of the predictions of the emergence of a "cashless society". In an imaginative analysis, Jankowski et. al. (2007) studied the Chicago metropolitan area and concluded that Latin American immigrants demand "more $100 bills than both native-born residents and immigrants from regions other than Latin America."[23] Their evidence suggests that the dramatic increase in the number of immigrants has contributed to the increase in domestic demand for currency since the late 1990's.

Figure 7
Ratio of Domestic Currency to GDP and Per Capita Domestic Holdings
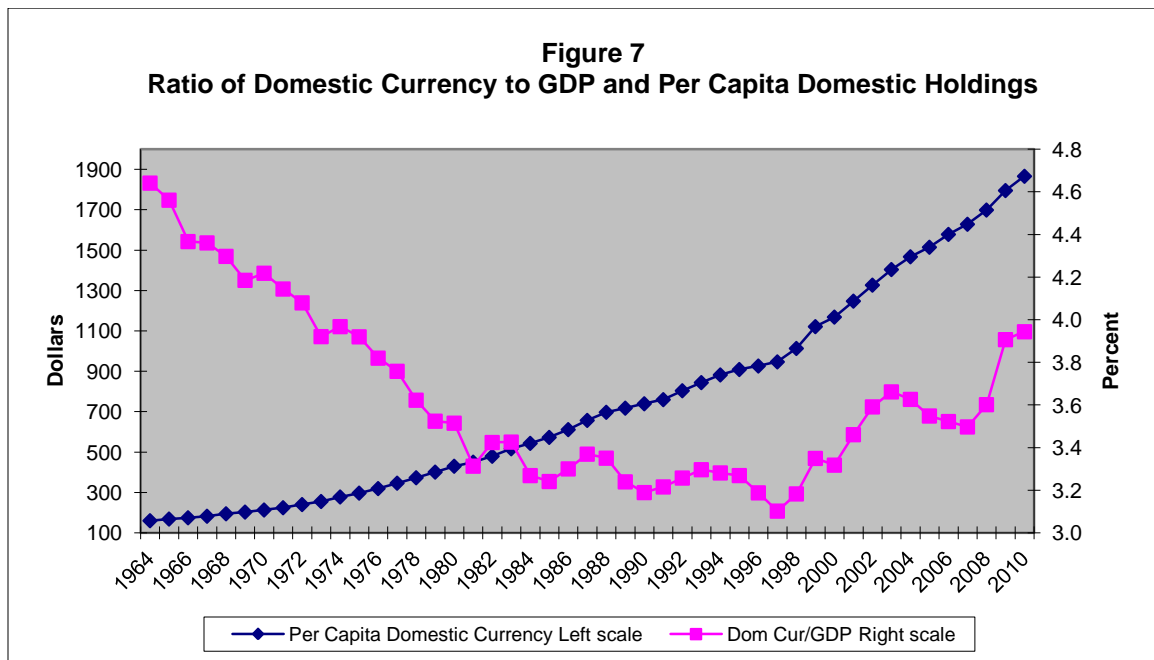
The recent study by Hellerstein and Ryan (2011) displays a graph of the "confidential" New York Federal Reserve (NYB) data on U.S. currency payments to and receipts from abroad. Their graph suggests that since 2002, receipts of currency from the rest of the world have exceeded payments in several years although the proxy employed by the BEA/FED shows positive net payments abroad for all years except 2007. The New

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[23] P. 15. This increased demand for currency is explained by the fact that this group encounters "obstacles to obtaining and using deposit accounts at financial institutions."(p.17.)

York Federal Reserve (NYB) data appear to imply that the percentage of currency currently held abroad is even lower than the NYLAM percentage displayed in Figure 4. Moreover, they suggest that the past decade has witnessed a significant decline in the rest of the world's demand for U.S. currency. If true, domestic currency holdings must have increased even more rapidly than implied by Figure 7.

4) The Location of U.S. Currency Held Abroad

Two sources of data are available for estimating the location of U.S. dollars overseas. Between 1994 and 2005 officials from the U.S. Treasury, the Board of Governors of the Federal Reserve, the New York Federal Reserve and the U.S. Secret Service visited forty-one countries to conduct informal surveys concerning the amount of U.S. currency in circulation. The amounts of U.S. currency believed to be held in each country are reported in the United States Treasury Department (2006) [Table 3.3] and are reproduced here in Table 2.

Unfortunately, the Treasury Report gives no indication of the method employed to obtain these "survey" estimates other than to obliquely state in a footnote: "For currency holdings, estimates were provided during the teams visit to each country and thus are estimates as of the most recent trip to each country".[24] Table 2 also includes estimates of currency held abroad in 12 additional countries not visited by the official teams. These additional country estimates are based on aggregated CMIR reports of currency inflows and outflows organized by country of origin and destination.

To examine the consistency of the "informal survey" results with the BEA/FED estimates of total currency abroad, we note that the amount of currency reportedly held in the 31 visited countries ($248.1 billion) during the period 1994-2005 exceeds the new official BEA/Fed estimate of the average amount of currency held abroad ($205.4 billion) during this period by $42.7 billion. The additional CMIR country estimates bring this discrepancy to $76.3 billion. We suspect that the anecdotal evidence presented as survey results grossly overstate U.S. currency holdings abroad.

[24] P. 25.

Table 2
Foreign Holdings of U.S. Currency

Country	U.S. $ Billion	Country	U.S. $ Billion
Argentina*	50.0	Indonesia*	2.0
Armenia**	0.2	Korea*	15.0
Azerbaijan**	1.3	Latvia*	0.5
Belarus*	3.0	Lithuania*	0.5
Bolivia***	1.2	Mexico*	5.0
Brazil*	1.0	Nicaragua***	0.7
Bulgaria*	1.0	Panama*	2.0
Cambodia*	2.0	Peru*	5.0
Chile*	0.3	Paraguay*	0.1
China*	50.0	Philippines*	2.0
Colombia*	2.0	Poland*	1.0
Costa Rica***	0.8	Romania*	2.0
Dominican Republic*	1.5	Russia*	80.0
Ecuador*	1.0	Singapore*	1.0
Egypt*	1.0	South Africa*	2.0
El Salvador*	1.0	Taiwan*	1.0
Estonia**	0.6	Thailand*	0.3
Hong Kong*	2.0	Turkey*	10.0
Hungary**	0.3	Ukraine**	6.4
Kazakhstan**	17.1	Uruguay***	2.6
Kyrgyzstan**	0.1	Venezuela***	2.5
		Vietnam*	3.0
		Total	**281.7**

Sources: * Secretary of the Treasury Report (2006) P.25; ** Feige and Dean (2004) Table 14.1, p.309;
***Feige et al. (2003) Table 2.1. p. 53.

Table 2 does however provide a rough insight into the distribution of U.S currency by major region. Figure 8 displays the approximate regional composition of overseas holdings of U.S. currency. The greatest degree of dollarization appears to occur in the transition countries with Russia being the most dollarized country.

Figure 8
Distribution of U.S. Currency
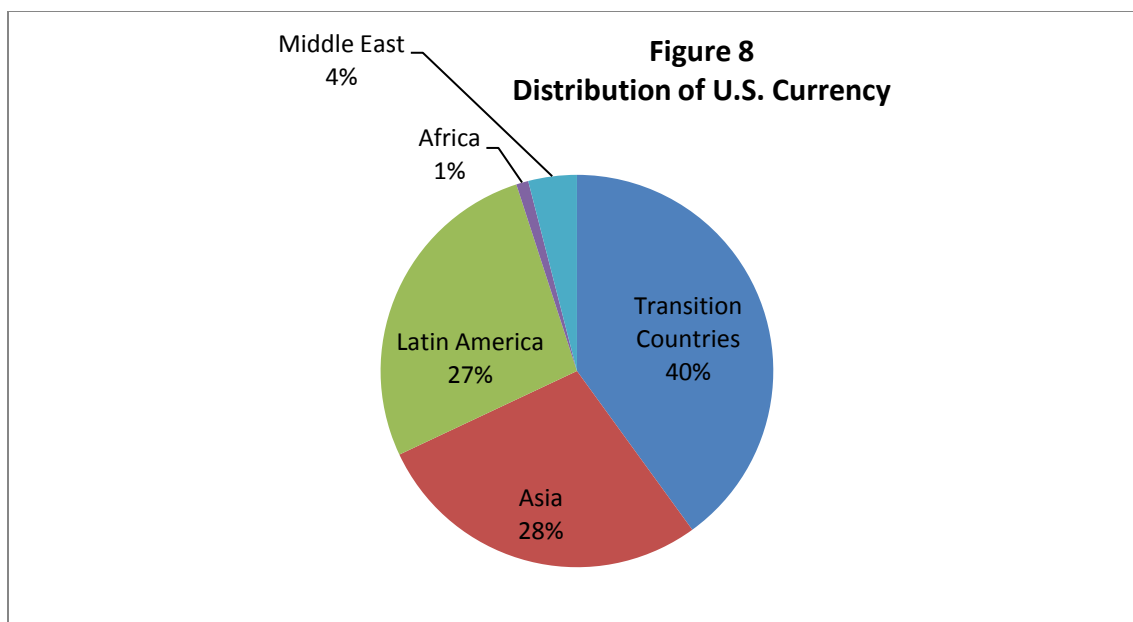
Latin America and Asia each hold over a quarter of the reported overseas holdings with Argentina and China being the major consumers. The regional graphs presented in the recent paper by Hellerstein and Ryan (2011) depict significant dollar net inflows from Latin America and Asia between 2003 and 2007, suggesting that the percentages displayed in Figure 8 for both regions are likely to be overstated.

5) Seigniorage

The Federal Reserve supplies currency on demand to both domestic and foreign customers willing to hold the non-interest bearing obligations of the U.S. central bank. The Federal Reserve earns seigniorage income when it uses these interest free proceeds to acquire interest bearing assets. After subtracting the costs of operating the currency system, the Federal Reserve remits the bulk of its annual interest earnings to the U.S. Treasury.

Figure 9 displays the annual seigniorage income of the Federal Reserve by its domestic and foreign (overseas) components. Domestic seigniorage earnings represent a redistribution of income from U.S. currency holders to U.S. taxpayers. On the other hand, seigniorage earnings on currency held abroad represent a net transfer of real resources from foreign currency holders to U.S. taxpayers. Since 1964 cumulative seigniorage earnings amounted to $916 billion of which $287 billion represents the windfall accruing to U.S. taxpayers resulting from the overseas holdings of foreigners.

Figure 9
Annual Seigniorage Earnings
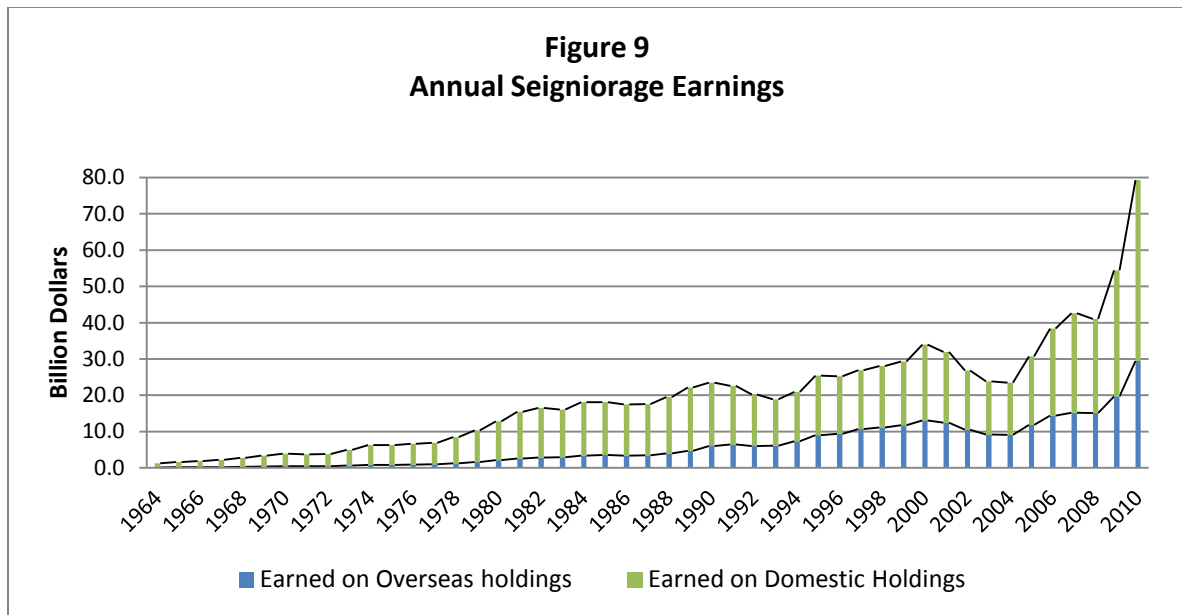
Income Source: Board of Governors of the Federal Reserve System Annual Report 2010: Table 11, Col 1.

The widespread circulation of U.S. banknotes abroad and their near universal acceptance as a medium of exchange makes America's currency an attractive target for counterfeiting. Judson and Porter (2010) estimate that the stock of counterfeits in the world as a whole is likely to be of the order of 1 per 10,000 of genuine notes ($20-$30 million in value terms) and no greater than 3 in 10,000 ($120-$220 million in value terms). These finding suggest that counterfeiting costs to the U.S. taxpayer are very small compared to the seigniorage earnings from abroad.

6) The Money, Output, Inflation Controversy

The stability and information content of the relationship between monetary aggregates and real output and inflation has been the subject of considerable controversy in macroeconomics since Sims (1972) discovered a unidirectional causality from money and income. Feige and Pearce (1979) showed that this empirical finding was highly sensitive to alternative specifications and concluded that "the relationship between money and income appears to be casual rather than causal."

As time series analysis became more sophisticated, Friedman and Kuttner (1992) reexamined the relationship between monetary aggregates and real income and prices in a

trivariate autoregressive framework and found that the "the U.S. experience does not indicate a close relationship between money and non-financial economic activity." Their key finding that "there is no evidence to show that fluctuations in money contain any information about subsequent movements in income or prices" is the hypothesis we wish to reexamine in light of our new information concerning the amounts of currency circulating abroad.

Feige (1994) suggested that "if a sizable and variable fraction of currency is held abroad, reliance on conventional monetary aggregates which include total currency in circulation would be misleading. The appropriate monetary aggregates to monitor would be the *domestic* monetary base and the *domestic* money supply rather than the total monetary base and the total money supply." Aksoy and Piskorski (2006) recently provided partial evidence to support this conjecture. They reexamined the Friedman Kuttner (1992) results employing earlier estimates of the domestic currency supply and found that 'currency corrected for foreign holdings has increased marginal predictive content for U.S. inflation and real output relative to standard unadjusted money series." Employing the same autoregressive specification for real output changes and inflation as used by Friedman and Kuttner (1992) and Aksoy and Piskorski (2006), we compare the results of Granger causality relationships between the newly revised *domestic* monetary aggregates and output and inflation and those based on conventional monetary aggregates.

Empirical consideration of whether monetary aggregates can usefully play a role in monetary policy depends upon whether they help to predict future fluctuations in real income or prices that are not already predictable on the basis of fluctuations of income itself or price fluctuations. We therefore examine χ-square tests of the null hypothesis that all of the coefficients on the lagged growth of various monetary aggregates are zero in autoregressions of the form:

1) $\Delta y_t = \alpha + \sum_{i=1}^{4} \beta_i \Delta y_{t-i} + \sum_{i=1}^{4} \lambda_i \Delta p_{t-1} + \sum_{i=1}^{4} \delta_i \Delta m_{t-1} + v_t$

2) $\Delta p_t = \alpha + \sum_{i=1}^{4} \beta_i \Delta p_{t-1} + \sum_{i=1}^{4} \lambda_i \Delta y_{t-1} + \sum_{i=1}^{4} \delta_i \Delta m_{t-1} + v_t$

where Δy, Δp, and Δm are respectively, the quarterly growth rates of real output, inflation and alternative monetary aggregates.[25]

Table 3 presents the p-values of the Granger causality χ-square statistics computed with White (1980) heteroskedasticity consistent standard errors. The null hypothesis is that all coefficients on the lagged financial variables, considered individually in the autoregressive specifications, are zero. Table 3 is similar to the presentation in Aksoy and Piskorski (2006) who used the earlier estimates of domestic currency based on the NYLA proxy for foreign holdings described in Section 2 above.

Our estimates of domestic currency holdings are derived from the newly revised official BEA/FED estimates of foreign holdings based on the NYLAM proxy, and on our proposed NYLAMSAELJ proxy. Additionally, we examine estimates of the M1, M2, and MB aggregates corrected for alternative estimates of domestic currency holdings.

Table 3 reveals that in the real output equations, the only variables significant at the 5 percent level are the Fed Funds rate, the St. Louis monetary base and the proposed domestic currency component. At the 10 percent level we find that the conventional Board of Governors monetary base, the M2 monetary aggregate and the current estimate of domestic currency component are significant. We find no significant predictive content for either the conventional narrow monetary aggregates or the domestic monetary aggregates other than the currency component.

The conclusions are quite different for the inflation equations. At the 5 percent significance level we find that the domestic currency component and both the conventional and domestic narrow money supply aggregates are significant. However, none of the other conventional monetary aggregates, (M2 and monetary base) nor the domestic M2 and base aggregates have significant predictive content for inflation.

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[25] Real output is measured by real GDP; inflation by the GDP deflator and the monetary aggregates are respectively, C = Currency component of M1, M1= the M1 money supply; M2= M2 money supply; Mb_{SL} = the St. Louis Federal Reserve monetary base; Mb_{BoG} =Board of Governors Monetary base; C_{dom} = domestic currency; $M1_{dom}$ = domestic M1 money supply; $M2_{dom}$ = domestic M2 money supply; Mb_{dom} = domestic monetary base.

Table 3
p-Values:Granger Causality: X square-Statistic

Variable		Real Output 1974:2- 2008:4	Inflation 1974:2- 2008:4
Domestic Monetary Aggregates			
Domestic Currency component current	ln(Cdom)NYLAM	0.098	0.003
Domestic Currency Proposed	ln(Cdom)NYLAMSAELJ	0.039	0.001
Domestic M1adj Current	ln(M1dom)adjNYLAM	0.324	0.015
Domestic M1adj proposed	ln(M1dom)adjNYLAMSAELJ	0.321	0.016
Domestic M2 Current	ln(M2dom)NYLAM	0.119	0.783
Domestic M2 proposed	ln(M2dom)NYLAMSAELJ	0.115	0.786
MBBoG domestic Current	ln(Mbdom)BoG.NYLAM	0.267	0.317
MBBoG domestic Proposed	ln(Mbdom)BoG.NYLAMSAELJ	0.292	0.236
MBSL domestic current	ln(Mbdom)SL.NYLAM	0.115	0.456
MBSL domestic proposed	ln(Mbdom)SL.NYLAMSAELJ	0.114	0.382
Uncorrected Monetary Aggregates			
Currency Component of M1	ln(C)	0.150	0.736
M1	ln(M1)	0.464	0.010
M1adj for Sweeps	ln(M1)adj	0.303	0.013
M2	ln(M2)	0.099	0.748
MBBoG	ln(Mb)BoG	0.062	0.871
MBSL	ln(Mb)SL	0.021	0.982
FED Funds rate	ln(Funds)	0.000	0.229

Our findings, covering a longer time period, and revised estimates of the domestic currency component, confirm the Askoy and Piskorski (2006) results that domestic currency has significant predictive content for both real output and inflation. However, with the exception of the domestic M1 money supply in the inflation equation, none of the other domestic monetary aggregates appear to have significant predictive content for either real output or inflation.

7) Implications for the Unreported Economy and the Tax Gap

The foregoing estimates of the *domestic* currency supply are now employed to generate a time series estimates of the relative size of the unreported economy which reflects tax evasion activity in the U.S. We focus our discussion on the estimation of "unreported income" (Yu), namely the difference between the total amount of income that should be reported to the tax authority (Y_T) (under full compliance with the tax code) and the amount actually reported (Yo), namely, adjusted gross income (AGI). The most common method for estimating the relative size of the unreported economy relies on some variant of the general currency ratio (GCR) model described in Feige (1986; 1989).

The most restrictive specifications of the currency ratio model [Cagan (1958), Gutmann (1977)] assume that currency is the exclusive medium of exchange for unreported transactions, that the ratio of currency to checkable deposits remains constant except for changes induced by the growth of unreported income and that the amount of unreported income produced by a dollar of currency transacted in the unreported sector is the same as the amount of reported income produced by a dollar of currency transacted in the reported economy. In order to obtain a benchmark estimate of the size of the unreported sector, the restrictive model also assumes that in some benchmark year (1940), unreported income is zero.[26]

As described in greater detail in Cebula and Feige (2012), we refine the restrictive GCR model by relaxing some of its key assumptions. First we substitute our estimate of domestic currency in circulation (C_{dom}) for the total amount of currency in circulation (C) since currency held abroad does not reflect tax evasion activity in the U.S. Second we account for a major technological innovation in the financial industry (the introduction of sweep accounts) which reduced the volume of "checkable deposits" (D) in a manner totally unrelated to behavior in the unreported economy.

Figure 10 displays the effects of these two adjustments by comparing the conventional C/D ratio employed in many published estimates of the "underground"

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[26] As described in Feige (1989) and Cebula and Feige (2012) these restrictions imply that the ratio of unreported income (Yu) to reported income(Yo) can be estimated as follows:
Yu/Yo =(C-koD)/ (ko+1) D: where C = Currency, D= Checkable deposits and ko= (Co/Do), the currency deposit ratio in the official economy which is observed in the year (1940) when the underground economy is assumed to be zero.

economy with the new C/D ratio adjusted for both domestic currency holdings and the financial innovation of sweep accounts.

Figure 10
Conventional and Adjusted C/D Ratio
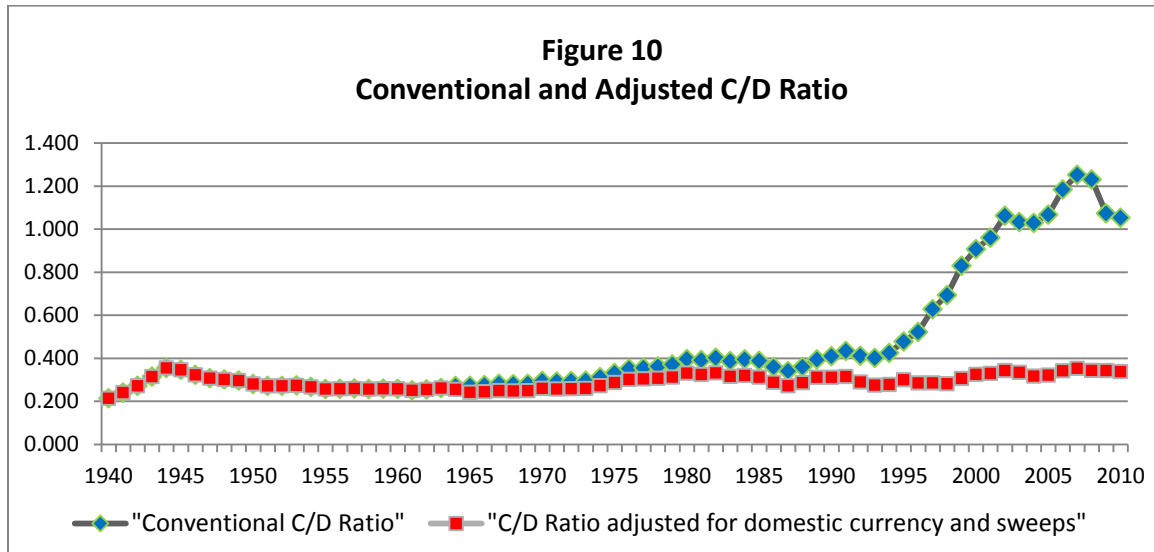
A further modification of the conventional currency ratio model is to drop the assumption that unreported income in 1940 was zero. A more reasonable alternative is to employ a benchmark estimate of total unreported income for a year in which an independent estimate of the ratio $Yu_t/Yo_t = \alpha_t$ is available.[27] We select 1988 as our benchmark year and employ the IRS estimate of legal source filer and non filer unreported income[28] derived from the Taxpayer Compliance Measurement Program (TCMP). These audit based estimates are regarded as "the most careful and comprehensive estimates of the extent and nature of tax noncompliance anywhere in the world."[29] The last published IRS estimate of unreported income from illegal sources was for the year 1981, at which time unreported illegal source income amounted to 15 percent of unreported legal source income.[30] Assuming that this percentage was constant between 1981 and 1988, we estimate total legal and illegal source unreported income for the year

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[27] Given α_t, the equation in footnote 26 can be solved for ko_t to derive a new benchmark estimate for generating the temporal development of Yu/Yo.

[28] IRS (1988) Table D-17

[29] Slemrod (2007, p.26)

[30] IRS (1983) Table VI-2

1988 and use the ratio of total unreported income to reported AGI as our new benchmark measure of the relative magnitude of tax evasion in 1988.

A final refinement of the GCR model is to relax the assumption that currency is the exclusive medium of exchange for transactions involving tax evasion. Income from interest and dividend payments, state tax refunds, capital gains, taxable unemployment benefits, pensions and annuities, estates and trusts and social security payments is typically paid by check. According to the 1988 TCMP audits, the sum of unreported filer income from all of these sources amounted to eighteen percent of total unreported filer income. [31] If twenty percent of unreported income is paid by check and the remaining eighty percent paid by cash, the ratio of currency to deposits the unreported economy (ku) = 4.

Figure 11 displays estimated total unreported income as derived from the refined GCR model which accounts for overseas currency holdings, financial innovations resulting from the introduction of sweep accounts and is benchmarked to the 1988 IRS audit based estimate of legal plus illegal unreported income. The series labeled GCR(1988) assumes that currency is the exclusive medium of exchange in the unreported economy, whereas the series labeled GCR (1988, $k_u = 4$) represents the scenario where twenty percent of unreported income is paid by check. The third series represents the IRS

Figure11
Estimated Total Unreported Income

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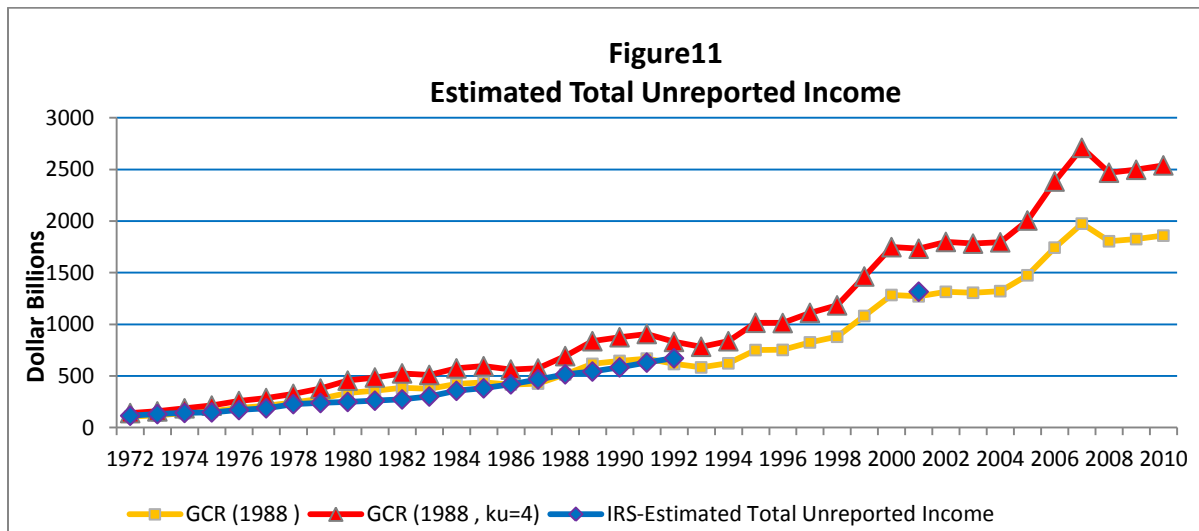
[31] Internal Revenue Service (1988), Table A-50.

estimate of total unreported income for those years for which projections of earlier audit based estimates are published.[32] Unreported income appears to have risen steadily over the past four decades, peaking in 2007. The GCR models suggest that by 2010, total unreported income amounted to $1.9 -2.4 trillion, giving rise to a tax gap of roughly $400-$550 billion. While these estimates relax several of the key assumptions usually associated with the currency demand approach, they remain quite sensitive to alternative specifying assumptions.

8) Summary and Conclusions

Financial innovations have created major substitutes for currency, yet per capita holdings of U.S. currency in circulation outside of the banking system amount to $2950. American households and businesses admit to holding less than 15 percent of this huge stock of U.S. currency, giving rise to what has been called the "currency enigma". Two complementary hypotheses have been advanced to explain the whereabouts of the remaining 85 percent of the currency supply.

Some fraction of the currency is believed to be held abroad in nations whose citizens and businesses feel it prudent to employ U.S. currency as a substitute for their own national currencies as both a medium of exchange and as a store of value. Evidence has been brought to bear (Table 2) that extensive "dollarization" occurred, primarily in Russia, Argentina and China, but the percentage of the U.S. currency supply believed to be held abroad remains in dispute. Porter and Judson (1996) suggested that at its peak in 1995 as much as 70 percent of the nation's stock of $100 bills were held abroad and concluded that the percentage of currency overseas was between 55 and 70 percent. The notion that between half and two thirds of U.S. currency is held abroad is widely reiterated in the press, by the U.S. Treasury and in Federal Reserve publications despite the fact that since 2008, the official Federal Reserve Flow of Funds (FOF) statistics and the U.S Bureau of Economic Analysis (BEA) places the percentage abroad between 36-37 percent. We have proposed an alternative proxy measure which includes net currency

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[32] The1972-92 estimates are derived from IRS (1988) Appendix D adjusted for illegal income IRS (1983) assumed to be a constant proportion of legal source income. The data point for 2001 is based on the IRS estimated tax gap due to underreporting (adjusted for illegal underreporting), divided by the 2001 NBER estimated marginal tax rate.

outflows from several additional U.S. southern border Federal Reserve branch banks. This alternative estimate suggests that only 30 percent of U.S. currency is presently held abroad.

The official Federal Reserve/ BEA measures of overseas currency are proxy based surrogates for the "confidential" New York Federal Reserve Bank data (NYB) pertaining to wholesale bulk currency shipments abroad. Indeed, the yet to be fully disclosed, (NYB) data[33] suggests that the percent of currency abroad may be substantially lower than the current (FOF/BEA) estimate and implies that the demand for U.S. dollars has declined quite precipitously during the past decade. Hopefully, the New York Federal Reserve will make these important data concerning overseas currency flows readily available, so that researchers can more accurately determine both the amount of currency abroad and its likely location. Aggregation procedures are available that can satisfy confidentiality requirements without compromising the information content of this important data source.

Taking the current official FOF/BEA data at face value implies that seigniorage earnings from abroad are considerably smaller than is usually presumed and that the demand for dollars from abroad has declined relative to the domestic demand for U.S. currency. Domestic per capita holdings of U.S. currency are now roughly $1900 and the overwhelming portion of these holdings are in the form of $100 bills that are used both as a store of value and as a medium of exchange. The dramatic growth in real per capita domestic currency holdings flies in the face of widespread predictions of the emergence of a "cashless" society. One partial explanation (Jankowski et. al., 2007) for the increase in domestic currency demand is the rapid growth in the number of Latin American immigrants who encounter barriers to participation in the mainstream financial system.

Domestic currency is also known to be the preferred medium of exchange for transactions that individuals and businesses wish to conceal. Such transactions include: the production and distribution of illegal goods (drugs) and services (prostitution); and incomes earned that are not reported to the fiscal authority in order to evade taxes. In order to examine this "underground" economy hypothesis, we employ a modified

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[33] The data in question are displayed in Figure 1 of Hellerstein and Ryan (2011) but to date; researchers have been denied access to the underlying data, despite the fact that these highly aggregated data eliminate any concerns of confidentiality.

currency ratio model to estimate both the volume of "unreported income" and the "tax gap" resulting from this underreporting. Our findings suggest that by 2010, unreported income amounted to $1.9-$2.4 trillion resulting in a "tax gap" ranging from $400 to $550 billion per year. Currently, we estimate that 18-24 percent of total reportable income is not properly reported to the IRS. Despite several key refinements of the traditional currency ratio models, these estimates remain highly sensitive to alternative specifications[34] and estimates of overseas cash holdings.

Given the revised estimates of overseas currency holdings, we reexamine the relationship between monetary aggregates and output and inflation. Particular interest centers on the question of whether new estimates of domestic currency holdings and of domestic monetary aggregates have better predictive power in explaining output and price fluctuations than do conventional monetary aggregates that take no account of overseas currency holdings. Following the specifications of Friedman and Kuttner (1992) we confirm the limited findings of Aksoy and Piskorsky (2006) that the revised domestic currency component has significant predictive power for real output and inflation. However, with the exception of the domestic M1 money supply in the inflation equation, none of the other domestic monetary aggregates appear to have significant predictive content for either real output or inflation. Thus, with the surprising exception of the domestic currency component, it appears that adjusting the conventional monetary aggregates to reflect only the domestic money supply does not significantly improve the predictive power of these aggregates in forecasting future real output or price fluctuations.

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[34] Cebula and Feige (2012) show that estimates of unreported income will increase if allowance is made for the likelihood that the income velocity of unreported income exceeds that of reported income, and if the secular rise of plastic payment mechanisms which substitute for cash usage are taken into account.

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