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### Abstract

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JEL: E3, E32, F4, F41

Keywords: Dynamic conditional correlation, Business cycle synchronization, Recession

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# The Synchronization of GDP Growth in the G7 During U.S. Recessions. Is this Time Different?

Nikolaos Antonakakis\*      Johann Scharler†

## Abstract

Using the dynamic conditional correlation (DCC) model due to Engle (2002), we estimate time varying correlations of quarterly real GDP growth among the G7 countries. In general, we find that rather heterogeneous patterns of international synchronization exist during U.S. recessions. During the 2007 - 2009 recession, however, international co-movement increased substantially.

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# 1 Introduction

Conventional wisdom holds that during the slow down in economic activity such as that during 2007 to 2009 was highly synchronized across industrialized countries. However, so far only anecdotal evidence in favor of such statements is available. In this paper we present formal evidence indicating a strong increase in output growth correlations among the G7 countries during this period. According to our results, this increase was rather unusual in the sense that we find only little evidence suggesting that output growth rates became more synchronized during previous recessions.

We estimate time-varying correlations using the dynamic conditional correlation (DCC) model introduced by Engle (2002). To our knowledge, this is the first application of the DCC model to macroeconomic data.

Our analysis is closely related to the empirical literature on business cycle synchronization (see e.g. Imbs, 2004; Kose et al., 2003; Otto et al., 2001) and especially to Crucini et al. (2008), Ayhan Kose et al. (2008), Doyle and Faust (2005) and Stock and Watson (2005) who also study the correlation of business cycles in the G7 countries. In contrast to the existing literature, we focus explicitly on the synchronization of GDP growth during recessions. The only paper we are aware of that analyzes the synchronization of recessions is Claessens et al. (2009). They show that recession periods typically occur simultaneously across countries, whereas we investigate the cross-country correlation of output growth dynamics during recessions.

The remainder of the paper is organized as follows. Section 2 describes the data and methodology employed. Section 3 presents the empirical results and section 4 concludes this paper.

## 2 Data and methodology

Let  $y_t = (y_{1,t}, \dots, y_{7,t})'$  denote the vector of quarterly growth rates of per capita real GDP in the G7 countries (Canada, France, Germany, Italy, Japan, UK and US). We calculate  $y_{i,t}$  as the fourth difference of the log of quarterly real GDP per capita. The sample ranges from the first quarter of 1960 to the third quarter of 2009. Data are obtained from the

OECD Main Economic Indicators.

The estimation of the DCC model involves two steps: In the first step, we specify each conditional variance as a univariate Generalized Autoregressive Conditional Heteroskedasticity (GARCH) process and in the second step, we use the standardized residuals from the first step to construct the conditional correlation matrix. Specifically, the DCC model is defined as:

$$y_t = \mu_t + \epsilon_t, \quad \text{where } \epsilon_t | \Omega_{t-1} \sim N(0, H_t), \quad (1)$$

$$\epsilon_t = H_t^{1/2} u_t, \quad \text{where } u_t \sim N(0, I), \quad (2)$$

$$H_t = D_t R_t D_t, \quad (3)$$

where  $\mu_t = (\mu_{1,t}, \dots, \mu_{7,t})'$  is the conditional mean vector of  $y_t$ , which we specify to follow an autoregressive process of order four.  $\epsilon_t$  is the vector of residuals based on the information set available at time  $t-1$ ,  $\Omega_{t-1}$ . The residuals are normally distributed with zero mean and conditional covariance matrix  $H_t = (h_{i,j,t})$ .  $D_t = \text{diag}(h_{1,1,t}^{1/2}, \dots, h_{7,7,t}^{1/2})'$  is a diagonal matrix of square root conditional variances, where  $h_{i,i,t}$  follow univariate GARCH processes, and  $R_t$  is the matrix containing the time-varying conditional correlations defined as:

$$R_t = \text{diag}(q_{1,1,t}^{-1/2}, \dots, q_{7,7,t}^{-1/2}) Q_t \text{diag}(q_{1,1,t}^{-1/2}, \dots, q_{7,7,t}^{-1/2}), \quad (4)$$

where  $Q_t = (q_{i,j,t})$  is a symmetric, positive definite matrix:

$$Q_t = (1 - \alpha - \beta) \bar{Q} + \alpha u_{t-1} u_{t-1}' + \beta Q_{t-1}, \quad (5)$$

where  $u_t = (u_{1,t}, \dots, u_{7,t})'$  is the vector of standardized residuals,  $\bar{Q}$  is the unconditional covariance matrix of  $u_t$ , and  $\alpha$  and  $\beta$  are nonnegative scalars such that  $\alpha + \beta < 1$ .

Since normality of the residuals is rejected, we estimate the DCC model using the Quasi-Maximum Likelihood estimator under the multivariate Student distribution.

### 3 Estimation Results

Table 1 shows the estimation results.<sup>1</sup> We see from Table 1 that 12 out of the 21 dynamic correlations are significant at 5% level of significance. Moreover, 16 correlations are sig-

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<sup>1</sup>For the sake of brevity, the GARCH estimation results for the first step are not presented here. Detailed results are available upon request.

nificant at the 10% level. In addition, the estimated correlations are large and significant for countries closely geographically related such as the European countries, and the U.S. and Canada. For instance, we obtain the highest and most significant correlations between Germany and France, Italy and France, and the U.S. and Canada. In contrast, the correlations between the U.S. and Italy, Canada and Italy, and Japan and Germany are quantitatively small and insignificant.

Note that the DCC model is well specified as the multivariate versions of the Portmanteau statistic of Hosking (1980) and Li and McLeod (1981) do not reject the null hypothesis of no serial correlation in the standardized and squared-standardized residuals, respectively, up to 10 lags.

Figure 1 shows the dynamic conditional correlations obtained from the DCC for each pair of countries along with U.S. recessions as defined by the National Bureau for Economic Research (NBER). Note that using U.S. recessions to define periods of economic downturns is not restrictive, since Claessens et al. (2009) show that the occurrence of recessions is quite synchronized across countries. The question remains: how synchronized output dynamics are during these periods of downturns? According to the figure, the highest degree of business cycle synchronization occurs during the 2007 to 2009 downturn as correlations reached a peak.

Although Figure 1 suggests that correlations increased during the 2007 to 2009 recession, we now present tests on the hypothesis that recessions, and in particular the 2007 to 2009 recession, are indeed associated with a stronger international synchronization of output growth.

To do so we estimate panel regressions of the form

$$dc_{i,j,t} = \alpha_{i,j} + \beta rec_t + \epsilon_{i,j,t}, \quad (6)$$

where  $dc_{i,j,t} = \log((1 + \rho_{i,j,t})/(1 - \rho_{i,j,t}))$  and  $\rho_{i,j,t}$  is the estimated dynamic correlation between countries  $i$  and  $j$ . Note that we transform the dynamic correlations to ensure that our dependent variable is not confined to the interval  $[-1, 1]$ . Our results are not sensitive to this transformation.  $\alpha_{i,j}$  are cross-section specific effects and  $rec_t$  denotes a dummy variables which is defined as  $rec_t = 1$  if the U.S. economy was in a recession in quarter  $t$  and  $rec_t = 0$  otherwise.

Table 2 shows the results. From Column (1) we see that U.S. recessions are associated with significantly higher international correlations. However, Column (2) shows that the correlations behave rather heterogeneously during individual recessions. Here, we estimate (6) with the dummies  $rec_{1980} = 1$  for the period 1980q1 to 1982q4 and zero otherwise.  $rec_{1990}$ ,  $rec_{2001}$  and  $rec_{2007}$  are defined analogously to capture the 1990, the 2001 and the 2007 to 2009 recessions.<sup>2</sup> According to our estimates, the recession during the early 1980s was associated with significant, albeit quantitatively small, increase in international synchronization. During the recessions in 1990 and 2001 we find no significant effect and in the former episode, the point estimate is even negative. However, during the 2007 - 2009 recession we obtain a highly significant and quantitatively large effect. According to the point estimate, the conditional correlations increased on average by slightly more than 0.2 points, which is not just statistically significant, but also economically substantial.

In Column (3), we add the dummy  $rec_{<1980}$  which is equal to unity during recessions that occurred before 1980 and equal zero otherwise. We see that, although we obtain similar effects for the recessions that occurred after 1980,  $rec_{<1980}$  enters with a negative sign and significantly at the 10 percent level. Thus, it appears that before 1980, U.S. recessions were associated with a de-synchronization of GDP growth rates. To illustrate this point further we estimate a specification with  $rec_{<1980}$  and a dummy that captures recessions after 1980:  $rec_{>1980}$ . According to Column (4), a high degree of international synchronization during U.S. recessions occurs only since the early 1980s. And together with the results reported in Columns (2) and (3), this last result suggests that the overall higher synchronization during recessions we see in Column (1) is to some extent due to the early 1980s, but mostly to the 2007 to 2009 recession. This result illustrates further that the strong increase in international output co-movements is a rather unique feature of the latest downturn.

Stock and Watson (2005) find that business cycles have generally become less synchronized since 1985. To allow for such a structural break, we re-estimate (6) and include a dummy,  $D_t$ , which is equal to unity if  $t > 1984q4$  and equal to zero otherwise. Column (5)

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<sup>2</sup>Note that the recession during the early 80s was actually a sequence of two recessions. The first one occurring between 1980q1 to 1980q3 and the second one between 1981q3 to 1982q4. Since our results remain unchanged, we pool these two intervals and treat them as a single recession period.

of Table 2 shows the dummy enters negatively and significantly, whereas  $rec_{1980}$ ,  $rec_{1990}$  and  $rec_{2001}$  become insignificant. However, the dummy for the 2007 to 2009 recession remains highly significant.

As a robustness analysis we repeated the estimation with the correlation between contemporaneous GDP growth in the U.S. and lagged GDP growth in the remaining G7 countries. In addition, we augmented (6) with aggregate as well as cross-section specific time trends. Our results remain unchanged.

## 4 Conclusion

In this paper we show that the 2007 to 2009 recession in the U.S. is associated with unusually highly synchronized output growth dynamics in the G7 countries. We estimate that, on average, the conditional correlations of GDP growth rates increased by roughly 0.2 points during this period. A key question that arises is why output dynamics during this downturn were so synchronized across the G7 countries.

According to Mendoza and Quadrini (2009) financial integration and contagion may have been a source of the high synchronization. Buch et al. (2010) find that banks transmit shocks internationally. To the extent that banking sectors suffered from severe adverse shocks during the 2007 to 2009 downturn, this transmission channel may have contributed substantially and more than usually to the high synchronization of output growth rates. A detailed analysis of these issues remains an interesting direction for further research.

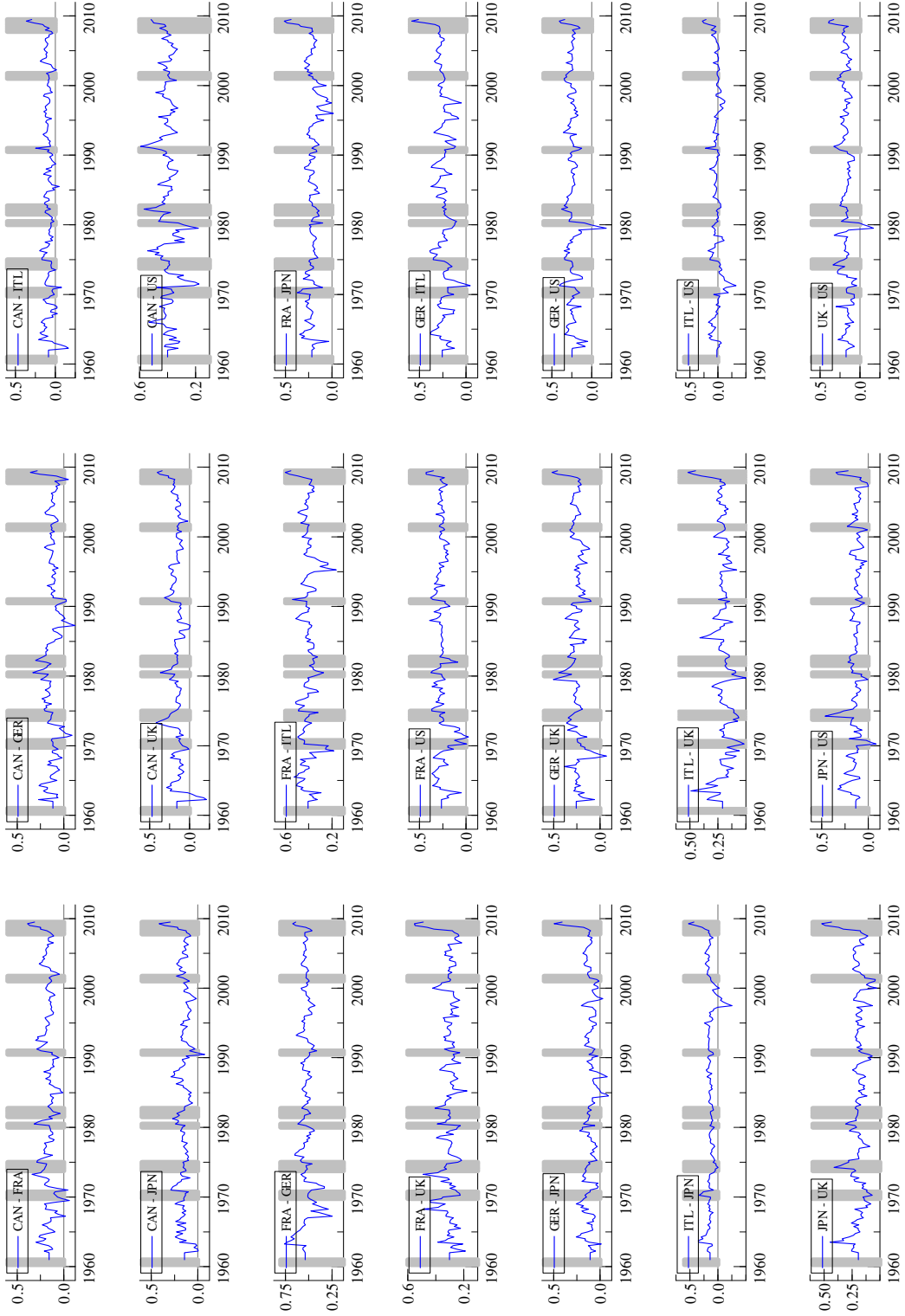
## References

- Ayhan Kose, M., Otrok, C., Whiteman, C. H., 2008. Understanding the evolution of world business cycles. *Journal of International Economics* 75 (1), 110–130.
- Buch, C. M., Carstensen, K., Schertler, A., 2010. Macroeconomic shocks and banks' foreign assets. *Journal of Money, Credit and Banking* 42 (1), 171–188.
- Claessens, S., Kose, M. A., Terrones, M. E., 2009. What happens during recessions, crunches and busts? *Economic Policy* 24, 653–700.



- Crucini, M. J., Kose, M. A., Otrok, C., 2008. What are the driving forces of international business cycles? NBER Working Papers 14380, National Bureau of Economic Research, Inc.
- Doyle, B. M., Faust, J., 09 2005. Breaks in the variability and comovement of G-7 economic growth. *The Review of Economics and Statistics* 87 (4), 721–740.
- Engle, R., 2002. Dynamic Conditional Correlation: A Simple Class of Multivariate Generalized Autoregressive Conditional Heteroskedasticity Models. *Journal of Business & Economic Statistics* 20 (3), 339–50.
- Hosking, J., 1980. The Multivariate Portmanteau Statistic. *Journal of American Statistical Association* 75 (75), 602–608.
- Imbs, J., 2004. Trade, finance, specialization, and synchronization. *The Review of Economics and Statistics* 86 (3), 723–734.
- Kose, M. A., Prasad, E. S., Terrones, M. E., 2003. How does globalization affect the synchronization of business cycles? *American Economic Review* 93 (2), 57–62.
- Li, W., McLeod, A., 1981. Distribution of the Residual Autocorrelation in Multivariate ARMA Time Series Models. *Journal of the Royal Statistical Society* 43, 231–239.
- Mendoza, E. G., Quadrini, V., Oct. 2009. Financial globalization, financial crises and contagion. NBER Working Papers 15432, National Bureau of Economic Research, Inc.
- Otto, G., Voss, G., Willard, L., 2001. Understanding OECD output correlations. RBA Research Discussion Papers rdp2001-05, Reserve Bank of Australia.
- Stock, J. H., Watson, M. W., 09 2005. Understanding Changes in International Business Cycle Dynamics. *Journal of the European Economic Association* 3 (5), 968–1006.

Figure 1: Estimated Conditional Correlations



Notes: The figure shows the estimated correlations of real GDP growth rates in the G7 countries. Shaded grey areas denote U.S. recessions as defined by NBER.

Table 1: Estimation Results of AR(4)-DCC models, Period: 1960q1 - 2009q3

$\rho$	CAN	FRA	GER	ITL	JPN	UK
FRA	0.1590 (1.966)					
GER	0.1158 (1.332)	0.5370 (8.743)**				
ITL	0.0875 (1.079)	0.4049 (5.291)**	0.2554 (2.830)**			
JPN	0.1439 (1.807)	0.2164 (2.522)*	0.1072 (1.265)	0.1399 (1.703)		
UK	0.1589 (1.884)	0.3020 (3.825)**	0.2552 (2.764)**	0.2086 (2.484)*	0.1939 (2.489)*	
US	0.3992 (5.532)**	0.2645 (3.158)**	0.2485 (2.944)**	0.0171 (0.200)	0.1356 (1.613)	0.1734 (2.171)*
$\alpha$			0.0534 (3.22)**			
$\beta$			0.6580 (9.10)**			
df			9.5963 (4.24)**			
Log-Lik			4460.44			
AIC			-44.9276			
SBC			-43.5848			
HQC			-44.3839			
Shibata			-45.1490			
$H(10)$			358.399 [0.13]			
$H^2(10)$			374.152 [0.09]			
$Li - McL(10)$			349.188 [0.15]			
$Li - McL^2(10)$			372.186 [0.10]			

Notes:  $H(10)$ ,  $H^2(10)$  and  $Li - McL(10)$ ,  $Li - McL^2(10)$  are the multivariate Portmanteau statistics of Hosking (1980) and Li and McLeod (1981), respectively, up to 10 lags.  $t$ -values in parenthesis and  $p$ -values in square brackets. \*\*  $p < 0.05$ , \*  $p < 0.01$ .

Table 2: International Correlations and U.S. Recessions

	(1)	(2)	(3)	(4)	(5)
<i>rec</i>	0.0408*** (0.00795)				
<i>rec</i> <sub>1980</sub>		0.0211** (0.00963)	0.0197** (0.00964)		0.0148 (0.0101)
<i>rec</i> <sub>1990</sub>		-0.0332 (0.0215)	-0.0345 (0.0216)		-0.0270 (0.0216)
<i>rec</i> <sub>2001</sub>		0.00414 (0.0111)	0.00282 (0.0111)		0.0104 (0.0112)
<i>rec</i> <sub>07</sub>		0.212*** (0.0201)	0.211*** (0.0201)		0.219*** (0.0201)
<i>rec</i> <sub><i>t</i>&lt;1980</sub>			-0.0203* (0.0111)	-0.0203* (0.0111)	
<i>rec</i> <sub><i>t</i>&gt;1980</sub>				0.0679*** (0.00905)	
<i>D</i> <sub>1985</sub>					-0.0125*** (0.00473)
<i>Obs</i>	4095	4095	4095	4095	4095
<i>R</i> <sup>2</sup>	0.740	0.757	0.758	0.744	0.758

Notes: In each specification, the dependent variable is the transformed conditional correlation  $dc_{i,j,t} = \log((1 + \rho_{i,j,t}) / (1 - \rho_{i,j,t}))$ , where  $\rho_{i,j,t}$  is the estimated dynamic correlation between countries  $i$  and  $j$ . All specifications include cross-section specific effects. Robust standard errors in parentheses, \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .