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ABSTRACT

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We investigate the effects of inequality in wealth on the incentives to contribute to a public good when agents are inequity averse and may differ in ability. We show that equality may lead to a reduction of public good provision below levels generated by purely selfish agents. But introducing inequality motivates more productive agents to exert higher efforts and help the group to coordinate on equilibria with less free-riding. As a result, less able agents may benefit from initially disadvantageous inequality. Moreover, the more inequity averse the agents, the more inequality should be imposed even by an egalitarian social planner.

JEL Classification: H41, D31, D63, J31, M52

Keywords: public goods, inequality, inequity aversion, social welfare, voluntary provision, income distribution, heterogeneity

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1 Introduction

There is now a broad number of studies indicating that many people tend to dislike inequity. Formal models of inequity aversion such as those by Fehr and Schmidt (1999) or Bolton and Ockenfels (2000) have been quite successful in explaining patterns of behavior observed in laboratory experiments and in the field.¹ In this paper we analyze the effect of ex-ante inequality in wealth on the motivation of heterogeneous and inequity averse agents to contribute to a public good. While a straightforward conjecture would be that inequity aversion should lead to the optimality of a more egalitarian wealth distribution, we show that the optimal degree of wealth inequality may actually increase with the importance of inequity aversion in the agents' preferences.

We consider a simple setting in which two agents who are inequity averse simultaneously decide on their contributions to a public good. The joined output is increasing in each agent's contribution but both agents may have different abilities which determine the marginal effect of their contributions. When both agents benefit to the same extent from the public good, equality in initial wealth may then lead to inequity as the more able agent provides higher inputs and, in turn, has higher costs. We show that this inequity is endogenously offset to some degree as the agents adapt their contributions. Treating unequal agents equally may then have detrimental effects for the provision of the public good. But allocating a higher wealth to the more able agent may motivate the latter to increase her contribution. When the wealth differential is aligned to the difference in abilities, there will be multiple equilibria in which the agents attain the same utility even though their initial wealth differs. In these equilibria both agents have an incentive to match

¹For experimental evidence see for example Roth and Kagel (1995), Camerer (2003) and Engelmann and Strobel (2004). Using a more general notion of fairness, field evidence is given by e.g. Blinder and Choi (1990), Agell and Lundborg (1995), Campbell and Kamlani (1997), Bewley (1999) and Carpenter and Seki (2006). For a summary of the empirical evidence on social preferences see for instance Fehr and Schmidt (2002) and Sobel (2005).

their group-members' contribution and, in turn, the free-rider problem can be substantially reduced when the agents coordinate on the Pareto-dominant equilibrium. In particular, for intermediate levels of wealth inequality both agents exert higher efforts relative to the efforts maximizing their material payoffs.

We further analyze the optimal degree of inequality for two simple settings. In the first setting, we analyze the agents' individual preferences for redistribution of a given amount of total initial wealth. Here, we show that the less able agent may even benefit from ex-ante wealth inequality to her *disadvantage*. The reason is that the increased incentives of the more able agent to contribute to the public good can outweigh the loss in ex-ante wealth. In the second setting, we show that not only a utilitarian but also an egalitarian social planner will choose an unequal wealth distribution favoring the more productive agent. Most strikingly, the stronger the agents' inequity aversion, the *larger* should be the difference in initial wealth. Moreover, we show that an egalitarian wealth distribution can only be optimal when all agents have the same ability. On the contrary, in the case of heterogeneous agents such a policy always leads to a stronger underprovision of the public good causing welfare losses. Finally, we demonstrate that under the optimal distribution of wealth, total contributions are independent of the group composition, i.e. homogeneous and heterogeneous groups provide the same amount of the public good and identical levels of social welfare are attained.

In the existing public good literature, a well established result is that the private provision of a public good is unaffected by any reallocation of income amongst contributing agents. This result has first been shown by Warr (1983) and later been extended by Bergstrom et al. (1986). However, the latter also shows that an income redistribution which increases inequality by transferring wealth from non-contributing individuals to contributing individuals can have positive welfare effects (see also Itaya et al. (1997)). In a similar vein, Andreoni (1990) argues that public good provision can be en-

hanced by redistributing wealth from less altruistic to more altruistic people. We add to this literature by showing that redistribution can be beneficial even for the case of symmetric preferences and even if the set of contributors is left unchanged. While the reason for inequality in our model stems from the heterogeneity in the agents' characteristics, the agents' fairness concerns appear to be an important factor influencing the optimal degree of inequality.

In recent years, there also has been a couple of (predominantly experimental) studies investigating the effects of wealth heterogeneity on public good provision. However, empirical results from these studies are not clear-cut. While some papers find that inequality leads to lower contributions (e.g. Ostrom et al. (1994), Van Dijk et al. (2002), Cherry et al. (2005) and Anderson et al. (2008)), other studies report a neutral or even positive effect of wealth inequality (e.g. Chan et al. (1999), Buckley and Croson (2006)).² One reason for the non-conclusive evidence might be that these studies investigated inequality only in the income dimension. Yet, the claim of our study is that there is an interplay of inequality in the income dimension and heterogeneity in the agents' characteristics that affect "psychological" inequity costs which might hamper the cooperation in social dilemmas.

In this regard, our paper also contributes to the literature on the interplay of equity and equality in social exchanges (e.g. Homans (1958), Adams (1965), Konow (2000), Cappelen et al. (2007) or Konow et al. (2009)). Psychological equity theory (Adams (1965)) for instance argues that individuals do not strive to receive equal benefits or make equal contributions as long as the ratio between benefits and contributions is similar. Analogously, we show that if agents are sufficiently heterogeneous, i.e. if the difference in abilities (and hence their inputs) is large, equity between agents is only feasible when initial wealth levels are unequal suggesting that (in)equality does not necessarily imply (in)equity and vice versa.

²Chan et al. (1996) find evidence which is in line with the model of Bergstrom et al. (1986) on an aggregate level but not an individual level.

Applied to a team context within firms, our study provides insights on the question whether equal wages are always the best wage policy. While it has often been argued that unequal reward schemes provoke morale problems among co-workers leading to lower performances (e.g. Akerlof and Yellen (1990), Bewley (1999)), some other studies questioned whether equal payment, realized by wage compression, does eliminate all these problems.³ Winter (2004), for instance, shows that it might be even optimal to reward identical agents differently as coordination can be improved which has recently been confirmed in an experiment by Goerg et al. (2010). In another experiment, Abeler et al. (2010) find that paying equal wages after an unequal performance may lead to inequity and, in turn, to substantially lower efforts and a decline in efficiency over time. But while these papers argue for inequality in ex-post performance rewards, our paper shows that it may even be optimal to introduce ex-ante inequality in the non-performance contingent wage components. Furthermore, our paper also adds to the literature on behavioral contract theory studying the effects of inequity aversion on incentives.⁴ However, while in most of the studies inequity aversion leads to more equal payment structures, our model shows that inequity aversion may be a reason to introduce ex-ante inequality.

The remainder of this paper is structured as follows. The model is described in Section 2. Section 3 presents the equilibrium analysis. In Section 4 we compare the effort levels chosen by inequity averse and purely selfish agents. Section 5 analyzes preferences for redistribution and examines the effects of distribution policies and group composition on the public good provision and social welfare. Section 6 concludes.

³See e.g. Lazear (1989) who argues that “... it is far from obvious that pay equality has these effects”.

⁴For a theoretical investigation of this topic see for instance Itoh (2004), Grund and Sliwka (2005), Huck and Rey-Biel (2006), Demougin et al. (2006), Fehr et al. (2007), Rey-Biel (2008), Dur and Glazer (2008), Mohnen et al. (2008), Kragl and Schmid (2009), Neilson and Stowe (2010), Bartling and Von Siemens (2010) and Englmaier and Wambach (2010).

2 The Model

Two agents i and j can both contribute to a public good. An agent's contribution depends on her effort e_i and her ability a_i . Individual effort costs are linear in the exerted effort and equal to $c \cdot e_i$, $c \in \mathbb{R}^+$. The group output is determined by the sum of both agents' contribution:

$$a_i\sqrt{e_i} + a_j\sqrt{e_j}.$$

The agents directly benefit from a higher group output. Each agent receives a share η of the group output indicating her individual valuation of the public good (marginal per capital return). Furthermore, each agent i is provided with an initial endowment w_i .⁵ Let $\Delta w_i = w_i - w_j$ be the difference in initial endowments. Both agents are inequity averse with a Fehr and Schmidt (1999) type utility function. An agent's utility is⁶

$$U_i = w_i - c \cdot e_i + \eta \cdot (a_i\sqrt{e_i} + a_j\sqrt{e_j}) - v(w_i - c \cdot e_i - w_j + c \cdot e_j)$$

with

$$v(\Delta) = \begin{cases} -\alpha \cdot \Delta & \text{if } \Delta < 0 \\ \beta \cdot \Delta & \text{if } \Delta > 0 \end{cases}$$

where α measures the “psychological costs” of disadvantageous inequity and β that of advantageous inequity. Following Fehr and Schmidt (1999) we assume that $\alpha \geq \beta \geq 0$. Additionally, we assume that $\beta \leq \frac{1}{2}$.⁷

⁵In a team context, η represents e.g. the degree of team identification or the intrinsic benefit of the work output and w_i represents the wage.

⁶Hence, we allow that the disutility from inequity $v(\Delta)$ depends on the difference of the agents' net-wealth (rewards minus costs of effort).

⁷Note that $\beta > \frac{1}{2}$ connotes a very strong form of inequity aversion implying that ex-post, agents would be willing to donate parts of their wealth to less wealthy group members up to the point where wealth levels are completely equalized (compare Rey-Biel (2008)). We discuss implications of this assumption at the end of Section 3.

3 Equilibrium Analysis

Each agent i maximizes

$$\max_{e_i} w_i + \eta \cdot (a_i \sqrt{e_i} + a_j \sqrt{e_j}) - c \cdot e_i - v(w_i - c \cdot e_i - w_j + c \cdot e_j).$$

The function is continuous but not continuously differentiable as it has a kink at $e_i = \frac{\Delta w_i}{c} + e_j$ where i attains the same utility as j . Off the kink, the second derivative with respect to e_i is $-\frac{\eta a_i \sqrt{e_i}}{4e_i^2} < 0$. As the right-sided derivative at the kink is strictly smaller than the left-sided derivative, the function is strictly concave.

We have to consider two possible equilibrium types depending on whether there is inequity in equilibrium or whether both agents are equally well off. In an *inequitable equilibrium* one agent i is better off given the chosen effort levels, i.e. $w_i - ce_i > w_j - ce_j$. Suppose that such an equilibrium exists. When agent i is better off, the following two conditions must hold in equilibrium

$$\begin{aligned} \frac{\partial U_i}{\partial e_i} &= -c + \frac{\eta a_i}{2\sqrt{e_i}} + \beta c = 0, \\ \frac{\partial U_j}{\partial e_j} &= -c + \frac{\eta a_j}{2\sqrt{e_j}} - \alpha c = 0. \end{aligned}$$

The respective equilibrium efforts are therefore

$$e_i^* = \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} \text{ and } e_j^* = \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2}. \quad (1)$$

Such an equilibrium exists if at these effort levels we indeed have that $w_i - ce_i > w_j - ce_j$ or

$$w_i - c \cdot \left(\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} \right) > w_j - c \cdot \left(\frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} \right).$$

This directly leads to the following result:

Proposition 1 *If and only if the difference in initial wealth $\Delta w_i \equiv w_i - w_j$ is larger than $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right)$ an inequitable equilibrium exists in which agent i is strictly better off than agent j . Then, the equilibrium effort levels are*

$$e_i^* = \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} \text{ and } e_j^* = \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2}.$$

Note that both agents adapt their efforts as the contribution of the favored agent i increases in the degree of “compassion” β and that of her disadvantaged counterpart j decreases in the degree of “envy” α . Still, they here end up a situation which is inequitable ex-post. But as the result shows this is only the case when ex-ante inequality is sufficiently large.

We now have to check whether there are also *equitable equilibria* in which both agents attain the same payoff. In that case $w_i - ce_i = w_j - ce_j$ and both agents choose their effort levels at the kink of the respective utility function. An effort tuple $(\bar{e}_i^*, \bar{e}_j^*)$ can be sustained in such an equitable Nash equilibrium if no agent has an incentive to deviate. As the function is strictly concave, necessary and sufficient conditions for the existence of the equilibrium are that for both agents the left hand side derivative of the utility function must be positive at $(\bar{e}_i^*, \bar{e}_j^*)$, the right hand side derivative negative and $w_i - c\bar{e}_i^* = w_j - c\bar{e}_j^*$. Hence, in an *equitable equilibrium*, the following five conditions must be met:

$$\left. \frac{\partial_- U_i}{\partial e_i} \right|_{e_i = \bar{e}_i^*} = -c + \frac{\eta a_i}{2\sqrt{e_i}} + \beta c \geq 0 \Leftrightarrow \bar{e}_i^* \leq \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} \quad (2)$$

$$\left. \frac{\partial_+ U_i}{\partial e_i} \right|_{e_i = \bar{e}_i^*} = -c + \frac{\eta a_i}{2\sqrt{e_i}} - \alpha c \leq 0 \Leftrightarrow \bar{e}_i^* \geq \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2} \quad (3)$$

$$\left. \frac{\partial_- U_j}{\partial e_j} \right|_{e_j = \bar{e}_j^*} = -c + \frac{\eta a_j}{2\sqrt{e_j}} + \beta c \geq 0 \Leftrightarrow \bar{e}_j^* \leq \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} \quad (4)$$

$$\left. \frac{\partial_+ U_j}{\partial e_j} \right|_{e_j = \bar{e}_j^*} = -c + \frac{\eta a_j}{2\sqrt{e_j}} - \alpha c \leq 0 \Leftrightarrow \bar{e}_j^* \geq \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} \quad (5)$$

$$\bar{e}_j^* = \bar{e}_i^* - \frac{\Delta w_i}{c} \quad (6)$$

From these conditions the following result can be derived:

Proposition 2 *If and only if $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right) \leq \Delta w_i \leq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right)$ there is a continuum of equitable equilibria with*

$$\max \left\{ \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}; \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} + \frac{\Delta w_i}{c} \right\} \leq \bar{e}_i^* \leq \min \left\{ \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}; \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} \right\} \quad (7)$$

and $\bar{e}_j^* = \bar{e}_i^* - \frac{\Delta w_i}{c}$.

Proof:

Inserting the equity condition (6) in conditions (4) and (5), we can conclude that an effort level \bar{e}_i^* can be sustained if and only if

$$\max \left\{ \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}; \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} + \frac{\Delta w_i}{c} \right\} \leq \bar{e}_i^* \leq \min \left\{ \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}; \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} \right\}.$$

Note that $\frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2} < \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}$ and $\frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} + \frac{\Delta w_i}{c} < \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}$. Hence, the set is non-empty for certain values of Δw_i if

$$\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} \geq \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} + \frac{\Delta w_i}{c}$$

and

$$\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} \geq \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}$$

which is the case when

$$\frac{\eta^2 a_i^2}{4(1+\alpha)^2 c} - \frac{\eta^2 a_j^2}{4(1-\beta)^2 c} \leq \Delta w_i \leq \frac{\eta^2 a_i^2}{4(1-\beta)^2 c} - \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c}. \quad (8)$$

■

This result has several interesting implications. First, note that there are always multiple equitable equilibria. The reason is that inequity averse agents have some interest to adapt their own effort according to the group member's effort in order to avoid the disutility from inequity. This leads to a coordination problem as the reaction functions are upward sloping.

Second, the set of equitable equilibria defined by (7) is the larger, the higher the agents' degree of inequity aversion: The more the agents care for equity, the larger is their willingness to adapt their efforts to reduce inequity which may either be triggered by inequality in initial wealth or the group member's effort level. The lower boundary of the equilibrium set is decreasing in α as more "envious" agents are willing to reduce their efforts to avoid being worse off than their group member. Analogously, the upper boundary is increasing in β as more "compassionate" agents are more willing to raise their efforts to reduce a group member's disadvantage. Likewise, the set defined by (8) is also increasing in the agents' inequity aversion implying that the stronger the agents' aversion against inequity, the larger may be the maximal initial wealth inequality the agents are willing to offset by adapting their contributions ending up in an equitable equilibrium.

Third, note that the lower boundary for Δw_i as defined by condition (8) exceeds zero (or the upper boundary is smaller than zero) when the abilities differ strongly and inequity aversion is not too strong. In these cases, equitable equilibria never exist when $\Delta w_i = 0$ and, hence, equity cannot be attained when wealth is distributed equally. The reason is that due to the

higher marginal productivity of effort, the more productive agent will have a higher incentive to exert more effort than her less productive fellow agent and, in turn, bears higher costs. But as both agents equally benefit from the public good the more able agent is worse off when both have the same initial wealth.⁸

Finally, the equilibrium effort levels are always bounded from below by $\frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}$ or $\frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2}$ respectively. Hence, an agent never chooses an effort level of 0. Figure 1 shows the sustainable equilibrium effort levels of both agents i and j as a correspondence of Δw_i .⁹ There are two cut-off values for Δw_i . For small values of Δw_i ($= -\Delta w_j$) below $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$ there is a unique inequitable equilibrium with $e_i^* = \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}$ and $e_j^* = \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2}$. For large values of Δw_i above $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right)$ there is a unique inequitable equilibrium with $e_i^* = \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}$ and $e_j^* = \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2}$. For intermediate values of Δw_i equitable equilibria exist.

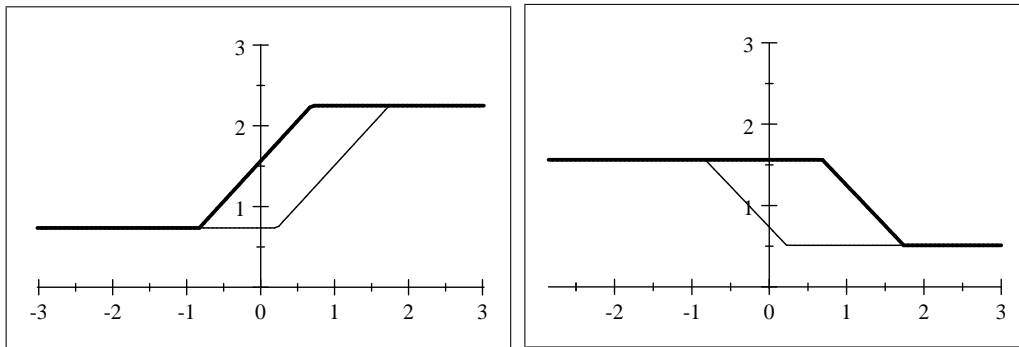


Figure 1: Effort Choice of agent i (left) and j (right) depending on Δw_i

Note that as both agents attain identical payoffs in an equitable equilibrium, they prefer the same one. Consequently, it is important to compare

⁸Note that this is always the case when the agents are purely selfish (i.e. $\alpha = \beta = 0$).

⁹The figure shows a setting in which $a_i = 12$, $a_j = 10$, $\alpha = 0.4$, $\beta = 0.2$, $\eta = 0.2$, and $c = 1$.

the different feasible equitable equilibria with respect to the agents' utility which leads to the following result:

Corollary 1 *As long as $\beta \leq \frac{1}{2}$ the highest feasible equitable equilibrium is always Pareto optimal.*

Proof: See the appendix.

To understand this result note that there is a free-rider problem which is particularly strong when agents are selfish. Inequity aversion helps to overcome this free-rider problem as it allows agents to coordinate on higher effort levels which come closer to the first best. As long as β does not exceed $\frac{1}{2}$ the highest feasible equilibrium is still lower than the first-best and therefore is preferred by the agents. With a β larger than $\frac{1}{2}$, however, inequity aversion becomes so strong that an agent even would have an incentive to match an inefficiently high effort level chosen by her group member even though both would be better off with a lower effort.

Hence, both agents benefit from playing the equitable equilibrium with the highest sustainable effort level when they are not extremely "compassionate". This effort level is equal to $\min \left\{ \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}; \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} \right\}$ and, hence, strictly increasing in the degree of advantageous inequity aversion β .

4 Do Inequity Averse Agents Contribute More?

We now compare the attained effort levels with those chosen by purely selfish agents to study the effects of inequity aversion on the motivation to contribute to the public good. From Propositions 1 and 2 as well as Corollary 1 (assuming that the agents play the Pareto best equitable equilibrium)¹⁰ we

¹⁰Cooper et al. (1992), Blume and Ortmann (2007) for instance find experimentally that simple ex-ante cheap talk communication indeed very frequently leads to the choice of the Pareto efficient Nash equilibrium in coordination games. See Demichelis and Weibull (2008) for a theoretical argument based on lexicographic preferences for honesty.

know that the equilibrium effort levels of inequity averse agents (e_i^*, e_j^*) are given by

$$\left(\begin{array}{ll} \left(\frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}, \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} \right) & \text{if } \Delta w_i < \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right) \\ \left(\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}, \frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} \right) & \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right) \right] \\ \left(\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}, \frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} - \frac{\Delta w_i}{c} \right) & \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \right] \\ \left(\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}, \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2} \right) & \text{if } \Delta w_i > \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \end{array} \right) \quad (9)$$

as depicted by the solid upper boundary of the graphs in Figure 1. Note that both functions are continuous and weakly monotonic.

Suppose, w.l.o.g., that i is the more able agent i.e. $a_i \geq a_j$. Purely selfish agents' effort choices are not affected by initial wealth inequality as they consider only their marginal returns when choosing their efforts. Hence, efforts are given by¹¹

$$e_i^{selfish} = \frac{\eta^2 a_i^2}{4c^2} \text{ and } e_j^{selfish} = \frac{\eta^2 a_j^2}{4c^2}. \quad (10)$$

By comparing these effort levels of selfish agents with those of inequity averse agents as given by (9) we obtain the following result:

Proposition 3 *If $\Delta w_i \in \left(\frac{\eta^2 a_i^2}{4c} - \frac{\eta^2 a_j^2}{4(1-\beta)^2 c}, \frac{\eta^2 a_i^2}{4(1-\beta)^2 c} - \frac{\eta^2 a_j^2}{4c} \right)$ both agents contribute more when they are inequity averse (i.e. $e_i^* > e_i^{selfish}$ and $e_j^* > e_j^{selfish}$). If Δw_i is larger than the upper boundary of this set inequity aversion motivates agent i to exert higher efforts but de-motivates agent j (i.e. $e_i^* > e_i^{selfish}$ and $e_j^* < e_j^{selfish}$). The opposite holds when Δw_i is smaller than the lower boundary.*

Proof: By comparing (9) with (10) it is straightforward to see that $e_i^* > e_i^{selfish}$ if $\Delta w_i \geq \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ and $e_i^* < e_i^{selfish}$ if $\Delta w_i \leq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$.

¹¹To see that, just replace $\alpha = \beta = 0$ in the equilibrium efforts given by (2).

We only have to check the case in which $\Delta w_i \in \left(\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right) \right)$.

In this case $e_i^* > e_i^{selfish}$ if

$$\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} > \frac{\eta^2 a_i^2}{4c^2} \Leftrightarrow \Delta w_i > \frac{\eta^2 a_i^2}{4c} - \frac{\eta^2 a_j^2}{4(1-\beta)^2 c}.$$

Hence, we can conclude that $e_i^* > e_i^{selfish}$ if Δw_i exceeds this cutoff.¹² Analogously, $e_j^* > e_j^{selfish}$ if $\Delta w_j = -\Delta w_i > \frac{\eta^2 a_j^2}{4c} - \frac{\eta^2 a_i^2}{4(1-\beta)^2 c}$ which gives us the upper boundary. It is straightforward to check that the interval in which both $e_i^* > e_i^{selfish}$ and $e_j^* > e_j^{selfish}$ is non-empty \blacksquare

Hence, the initial wealth differential Δw_i is crucial to determine how inequity averse agents distort their effort choices relative to the efforts maximizing their material payoffs. For intermediate levels of initial wealth inequality, inequity aversion indeed helps to reduce the free-rider problem as both agents contribute more when coordinating on the Pareto-superior equilibrium.

But if initial wealth inequality becomes stronger, inequity aversion leads to an asymmetric reaction as the favored agent chooses a higher effort than the level maximizing her material payoff and the disadvantaged contributes less than would be optimal from a payoff maximizing perspective.

But it is important to note that the latter demotivating effect may arise for the more able agent even when she is richer than her less able colleague: The lower boundary for Δw_i in Proposition 3 is larger than zero if

$$\frac{\eta^2 a_i^2}{4c} - \frac{\eta^2 a_j^2}{4(1-\beta)^2 c} > 0 \Leftrightarrow a_i > \frac{a_j}{1-\beta}.$$

Hence, when a_i is much larger than a_j or when β is sufficiently small, the more able agent reduces her effort below $e_i^{selfish}$ unless Δw_i exceeds a *strictly positive* cut-off value. Or, in other words, she has to be paid sufficiently more than her colleague or otherwise will reduce her effort below the selfishly optimal level. To understand the reason for this effect, note again that the payoff

¹²Note that this cut-off is indeed always in the interior of the relevant interval.

maximizing effort is always larger for the more able agent as her marginal returns to effort are higher. As both equally benefit from the public good, she is worse off than her less able colleague when both have the same initial wealth. But when being inequity averse she suffers from this disadvantage which is the higher the larger a_i relative to a_j . If β is high, the more able agent will still choose an equilibrium effort level above $e_i^{selfish}$ as also her less able but “compassionate” counterpart puts in a sufficiently high effort and they can coordinate to a superior equilibrium. But when β is small, she can only reduce inequity by lowering her effort. Hence, not awarding the more able agent more money up front leads to an unfair distribution of payoffs and, in turn, to lower efforts.

5 Social Welfare, Redistribution, and Group Composition

We proceed by analyzing redistribution preferences of a) the agents and b) a social planner who can allocate a fixed budget. We further investigate the welfare consequences of a policy implementing an egalitarian wealth distribution irrespective of the distribution of the agents’ abilities. Finally, we examine the effect of group composition under the optimal distribution of the initial wealth.

5.1 Individual Preferences for Redistribution

We first study the agents’ ex-ante preferences on the initial wealth differential Δw_i when they take into account their equilibrium effort choices. These considerations will be a useful starting point for welfare analysis. To do that, it is instructive to consider a situation in which a certain budget $W = w_i + w_j$ can be distributed between the two agents. By inserting the equilibrium effort choices (9) into the agents’ utility functions we can describe their utility as

a function of the initial wealth differential Δw_i . Analyzing the shape of the indirect utility functions we obtain the following result:

Proposition 4 *The agents' utility function is continuous in Δw_i . If $\Delta w_i < \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ or $\Delta w_i > \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right)$ an agent i 's utility is strictly increasing in Δw_i . But between these two cut-off values it is strictly decreasing. Both agents' utility functions attain a local maximum at $\Delta w_i^* = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$.*

Proof: See the appendix.

This result is illustrated in Figure 2. The solid line shows agent i 's utility and the dashed line agent j 's utility both as a function of Δw_i .¹³ For extreme values of Δw_i each agent benefits from a redistribution in her favor and there is a straightforward conflict of interest between both agents. But in the interval between $\frac{\eta^2}{4c} \left(\frac{a_j^2}{(1-\beta)^2} - \frac{a_i^2}{(1+\alpha)^2} \right)$ and $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right)$ both agents' interests are fully aligned. The reason is that within this interval only equitable equilibria exist, and hence, any ex-ante inequality in wealth will be offset by adapted effort levels. Moreover, all values of Δw_i within this interval are Pareto-dominated by a initial wealth differential of $\Delta w_i^* = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ as at this point, agents can coordinate on an equilibrium leading to the highest contributions.

Proposition 4 has several interesting implications. Consider the situation of an individual agent who can (re-)distribute a given wealth allocation. Interestingly, an individual may benefit from ex-ante redistribution at her own expense as the following result shows:

Corollary 2 *If both agents receive the same initial wealth (i.e. $\Delta w_i = 0$) the less able agent j can be made better off by reducing her own initial wealth*

¹³The figure shows a setting in which $a_i = 12$, $a_j = 10$, $\alpha = 0.4$, $\beta = 0.2$, $\eta = 0.2$, and $c = 1$.

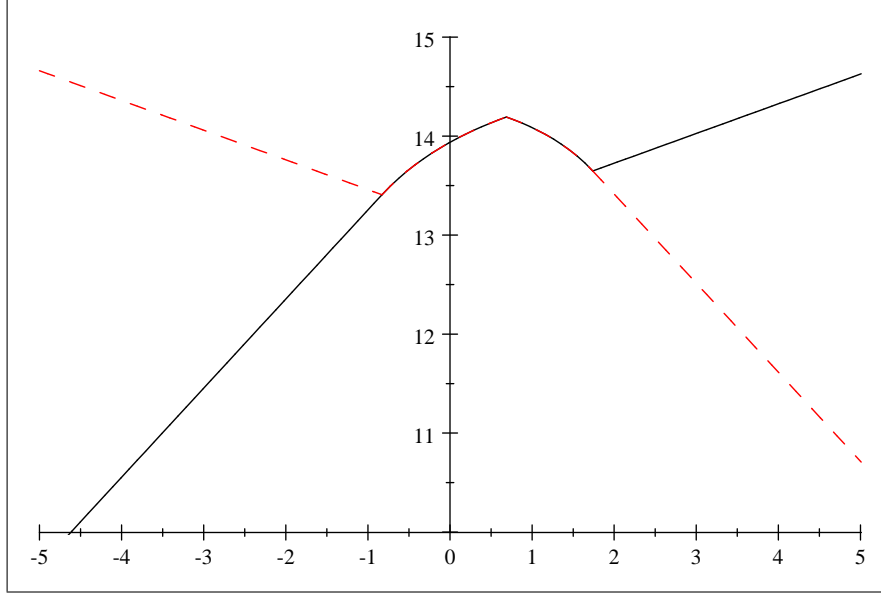


Figure 2: Agent i 's and agent j 's utilities in equilibrium depending on Δw_i

by $\frac{\eta^2}{8c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ and transferring this money to the more able colleague i if

$$\alpha > \frac{1-\beta}{3-4\beta} \sqrt{(2(6\beta^2 - 7\beta + 2))} + \frac{2(1-\beta)^2}{(3-4\beta)} - 1.$$

If α is smaller than this cut-off, such a transfer is still beneficial for agent j when her ability is not too small, i.e. if

$$\frac{a_j}{a_i} > \min \left\{ \frac{1-\beta}{1+\alpha}, \sqrt{\frac{1}{(1-2\beta)} \left(\frac{4(1-\beta)^2}{(1+\alpha)} + 1 - 4(1-\beta) - \frac{2\beta(1-\beta)^2}{(1+\alpha)^2} \right)} \right\}.$$

Proof: See the appendix.

Hence, a less able agent can be better off ex-post when sacrificing parts of her initial wealth which are then transferred to a more able individual. She then benefits from this colleague's higher willingness to contribute to the public good and this helps to reduce the free-rider problem. Interestingly, this

is always the case irrespective of the difference in abilities if α is sufficiently large. Moreover, note that the cut-off value for α is equal to $\frac{1}{3}$ when $\beta = 0$ and strictly decreasing in β . Hence, this condition holds for moderate values of α even when the agents only suffer from disadvantageous inequity. The reason is that a more able agent resents being worse off than her less able colleague when exerting a higher effort due to her higher productivity. But she is willing to exert higher efforts when she earns more. Therefore, a less able agent may benefit when her colleague's income is increased because, in turn, this colleague is willing to contribute more.

If α is rather small, the result still holds if the less able agent's productivity is not too small relative to her more able colleague's productivity. If, however, her ability is much smaller the transfer necessary to implement a performance maximizing equitable equilibrium is too large such that agent j prefers to stick with the case in which both receive the same initial wealth although this leads to a lower group output.

5.2 Social Welfare

We now study a situation in which an external authority can decide on the distribution of wealth. To do so, we consider, a social planner who has a social welfare function which is either egalitarian (i.e. who wants to maximize the utility of the least well-off) or utilitarian (i.e. wants to maximize the sum of both agents' utility). It directly follows from Proposition 4 that such a social planner always has a dominant choice:

Corollary 3 *A social planner who is either utilitarian or egalitarian will set $\Delta w_i^* = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$.*

Proof: It is straightforward to see that within the set of initial wealth differentials inducing equitable equilibria both egalitarian and utilitarian planners will always choose $\Delta w_i^* = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ as at this spread, both the sum and the

minimum of the agents' utilities are maximized. Moreover, for an egalitarian social planner any wealth differential which is not inducing an equitable equilibrium is always dominated by this choice as the utility of the least well off agent is always lower in an inequitable equilibrium. To see this formally note that when, w.l.o.g., j is favored $\frac{\partial u_i}{\partial \Delta w_i} = \frac{1}{2} + \alpha > 0$ for all Δw_i inducing an inequitable equilibrium (see (12) in the proof of Proposition 4) and as the utility function is continuous, i 's utility is always larger in an equitable equilibrium.

A utilitarian social planner will neither choose a wealth distribution inducing an inequitable equilibrium, as in an inequitable equilibrium which, w.l.o.g., favors agent j , the marginal gain from transferring money to agent i $\frac{\partial u_i}{\partial \Delta w_i} = \frac{1}{2} + \alpha$ is always larger than j 's marginal loss which is equal to $\frac{1}{2} - \beta$ (see again (12)). ■

Hence, even an egalitarian social planner who only considers the utility of the least well off individual should allow for inequality in ex-ante wealth. The reason is that it is precisely this ex-ante inequality induces an equilibrium in which equity is attained ex-post and in which the more able agent is willing to contribute more. This observation bears some resemblance to the result by Andreoni (1990) who argues that redistribution of income will increase the total contribution if it benefits the more altruistic individuals.¹⁴ It directly follows that the implementation of an egalitarian wealth distribution policy has detrimental effects if the group considered is not entirely homogenous in terms of abilities.

5.3 The Optimal Group Composition

So far, we only considered how wealth should be distributed treating the composition of agents within a group as exogenously given. However, it is

¹⁴Similarly, with respect to social welfare, Thurow (1971) argues that some redistribution of income is necessary in order to achieve a Pareto optimum.

also interesting to study the case in which the formation of groups can be determined as well. A straightforward conjecture is that group composition matters for the willingness to contribute if the agents are inequity averse towards their fellow group members. To investigate this, we consider a simple situation in which there are two agents of high and two of low ability that can be assigned into two groups of two. By comparing total contributions, we can derive the following result:

Proposition 5 *If all agents have the same initial wealth, total contributions are always higher with homogenous than with heterogenous groups. But when wealth can be adapted optimally, total contributions are independent of the group composition.*

Proof: Let $a_H > a_L$ be the ability of the high and low productive agent and let w_H and w_L denote the initial wealth levels of the two agents, respectively. Given the same initial wealth ($\Delta w = w_H - w_L = 0$) the total contribution with two homogenous groups is equal to

$$\frac{2\eta^2 a_H^2}{4(1-\beta)^2 c^2} + \frac{2\eta^2 a_L^2}{4(1-\beta)^2 c^2} = \frac{\eta^2 (a_H^2 + a_L^2)}{2(1-\beta)^2 c^2}. \quad (11)$$

With heterogenous groups it is given by

$$\begin{aligned} & \frac{\eta^2 a_H^2}{2(1+\alpha)^2 c^2} + \frac{\eta^2 a_L^2}{2(1-\beta)^2 c^2} & \text{if } \Delta w < \frac{\eta^2}{4c} \left(\frac{a_H^2}{(1+\alpha)^2} - \frac{a_L^2}{(1-\beta)^2} \right) \\ & \frac{\eta^2 (a_H^2 + a_L^2)}{2(1-\beta)^2 c^2} & \text{if } \Delta w \in \left[\frac{\eta^2}{4c} \left(\frac{a_H^2}{(1+\alpha)^2} - \frac{a_L^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_H^2 - a_L^2}{(1-\beta)^2} \right) \right]. \end{aligned}$$

In both cases, the expression is strictly smaller than (11).

If, however, the distribution of the initial wealth can be optimally adapted, i.e. $\Delta w^* = \frac{\eta^2}{4c} \left(\frac{a_H^2 - a_L^2}{(1-\beta)^2} \right)$, the total contribution of two heterogenous groups is

$$\begin{aligned} 2 \left(\frac{\eta^2 a_H^2}{4(1-\beta)^2 c^2} + \frac{\eta^2 a_L^2}{4(1-\beta)^2 c^2} - \frac{\Delta w^*}{c} \right) &= \frac{2\eta^2 a_H^2}{4(1-\beta)^2 c^2} + \frac{2\eta^2 a_L^2}{4(1-\beta)^2 c^2} - \frac{2\eta^2}{4c^2} \left(\frac{a_H^2 - a_L^2}{(1-\beta)^2} \right) \\ &= \frac{2\eta^2 (a_H^2 + a_L^2)}{4(1-\beta)^2 c^2}. \end{aligned}$$

But this is equal to the total contribution of the homogenous groups which is again given by (11) as $\Delta w^* = 0$ is optimal in this case. ■

Hence, when the wealth level is fixed and equally distributed it is beneficial to have homogenous groups. The reason is straightforward from the analysis above: Heterogeneity in abilities leads to a de-motivation of the more qualified agent when wealth is equally distributed. By matching agents into homogenous teams, this de-motivational effect can be avoided and group homogeneity helps the agents to coordinate on more favorable equilibria.

It is, however, interesting to note that group composition is irrelevant for total contributions when the wealth level can be optimally adapted. In this case, the disadvantage of the more able agent can be entirely offset and, in turn, motivation to contribute is restored to the levels attainable in homogenous groups.

6 Conclusion

We analyzed the effects of wealth inequality on the incentives to contribute to a public good when agents are inequity averse. We have shown that it is optimal to introduce ex-ante inequality in wealth if agents differ in their abilities. The reason is that inequality in favor of a more able agent can motivate this agent to exert higher efforts. In particular, the stronger the agents' inequity aversion, the stronger is also this incentive effect of inequality and the larger should be the difference in initial wealth. Furthermore, we have shown that compared to the case when agents are purely self-interested, contributions are higher when agents are inequity averse as inequity aversion helps to reduce the free-rider problem and agents can coordinate on higher efforts.

Our results have several interesting implications. First of all, they cast doubt on simple statements sometimes heard in practice claiming that in-

equality among the members of a group is demotivating when people care for fairness. While this is indeed true for very large wealth differentials in our model, the opposite can also be the case, when wealth differentials are too small. Allocating agents of different abilities the same initial wealth can lead to highly inequitable situations. The reason is that in a public good setting, all agents equally benefit from the group output, but more able agents exert higher efforts as their marginal returns to effort are higher and, in turn, they incur higher costs. When agents are inequity averse this can demotivate the more able agents which is bad for the overall performance as their contributions are more valuable.

The results also may cast some light on the discussion about distributional politics (Alesina and Angeletos (2005), Durante and Putterman (2009)) and the effects on citizens' willingness to voluntarily donate to a common good. Some previous studies (e.g. Warr (1983) and Bergstrom et al. (1986)) have argued that the total provision of a public good is independent of the distribution of wealth. In contrast, our results indicate that equality in wealth may crowd-out the motivation to contribute. But introducing inequality may have positive effects on the citizens' willingness to work for the common good. However, our model also shows that this is the case only if the higher wealth is in the hands of those who can provide the most valuable contributions.

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7 Appendix

Proof of Corollary 1:

The value of e_i^{\max} directly follows from the upper boundary given by (7). Let

$$v_i^E(e_i) = w_i - ce_i + \eta \left(a_i \sqrt{e_i} + a_j \sqrt{e_i - \frac{\Delta w_i}{c}} \right)$$

be agent i 's utility which is equal to agent j 's utility in any equitable equilibrium. To compare the equilibria in the set defined by (7) we have to check which value of e_i maximizes this utility. Note that

$$\begin{aligned} \frac{\partial v_i^E(e_i)}{\partial e_i} &= -c + \eta \left(\frac{a_i}{2\sqrt{e_i}} + \frac{a_j}{2\sqrt{e_i - \frac{\Delta w_i}{c}}} \right) \text{ and} \\ \frac{\partial^2 v_i^E(e_i)}{\partial e_i^2} &= \eta \left(-\frac{a_i}{4} e_i^{-\frac{3}{2}} - \frac{a_j}{4} \left(e_i - \frac{\Delta w_i}{c} \right)^{-\frac{3}{2}} \right) < 0. \end{aligned}$$

As $v_i^E(e_i)$ is strictly concave, $\frac{\partial v_i^E(e_i)}{\partial e_i} \Big|_{e_i=e_i^{\max}} \geq 0$ is a necessary and sufficient condition for e_i^{\max} to be Pareto optimal. If $\Delta w_i < \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$, e_i^{\max} is equal to $\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}$ and the condition is equivalent to

$$\begin{aligned} -c + \eta \left(a_i \frac{1}{2\sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}}} + a_j \frac{1}{2\sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c} - \frac{\Delta w_i}{c}}} \right) \geq 0 \Leftrightarrow \\ \Delta w_i \leq \frac{\eta^2}{4c} \left(\frac{a_i^2}{\beta^2} - \frac{a_j^2}{(1-\beta)^2} \right). \end{aligned}$$

But $\frac{\eta^2}{4c} \left(\frac{a_i^2}{\beta^2} - \frac{a_j^2}{(1-\beta)^2} \right) \geq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$ as long as $\beta \leq \frac{1}{2}$. Hence, both agent's utility is maximal at e_i^{\max} in this case. If, however, $\Delta w_i \geq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$, e_i^{\max} is equal to $\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}$ and the condition is equivalent

to

$$-c + \eta \left(a_i \frac{1}{2\sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}}} + a_j \frac{1}{2\sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} - \frac{\Delta w_i}{c}}} \right) \geq 0 \Leftrightarrow$$

$$\Delta w_i \geq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{\beta^2} \right)$$

But $\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{\beta^2} \right) \leq \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1-\beta)^2} \right)$ is again equivalent to $\beta \leq \frac{1}{2}$. ■

Proof of Proposition 4:

By substituting the equilibrium efforts (9) into agent i 's utility function we obtain:

$$u_i = \begin{cases} \frac{W+\Delta w_i}{2} + \eta \left(a_i \sqrt{\frac{\eta^2 a_i^2}{4(1+\alpha)^2 c^2}} + a_j \sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2}} \right) - \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c} + \alpha \left(\Delta w_i - \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c} + \frac{\eta^2 a_j^2}{4(1-\beta)^2 c} \right) \\ \text{if } \Delta w_i < \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right) \\ \frac{W+\Delta w_i}{2} + \eta \left(a_i \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}} + a_j \sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2}} \right) - \left(\frac{\eta^2 a_j^2}{4(1-\beta)^2 c} + \Delta w_i \right) \\ \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right) \right] \\ \frac{W+\Delta w_i}{2} + \eta \left(a_i \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}} + a_j \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} - \frac{\Delta w_i}{c}} \right) - \frac{\eta^2 a_i^2}{4(1-\beta)^2 c} \\ \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \right] \\ \frac{W+\Delta w_i}{2} + \eta \left(a_i \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2}} + a_j \sqrt{\frac{\eta^2 a_j^2}{4(1+\alpha)^2 c^2}} \right) - \frac{\eta^2 a_i^2}{4(1-\beta)^2 c} - \beta \left(\Delta w_i - \frac{\eta^2 a_i^2}{4(1-\beta)^2 c} + \frac{\eta^2 a_j^2}{4(1+\alpha)^2 c} \right) \\ \text{if } \Delta w_i > \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \end{cases}$$

The first derivative of this function is

$$\frac{\partial u_i}{\partial \Delta w_i} = \begin{cases} \frac{1}{2} + \alpha & \text{if } \Delta w_i < \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right) \\ -\frac{1}{2} + \frac{\eta \cdot a_i}{2c \sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}}} & \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right) \right] \\ \frac{1}{2} - \frac{\eta \cdot a_j}{2c \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} - \frac{\Delta w_i}{c}}} & \text{if } \Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \right] \\ \frac{1}{2} - \beta & \text{if } \Delta w_i > \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \end{cases} \quad (12)$$

Note that the slope in the second interval is *strictly* positive if

$$\begin{aligned} -\frac{1}{2} + \frac{\eta \cdot a_i}{2c \sqrt{\frac{\eta^2 a_j^2}{4(1-\beta)^2 c^2} + \frac{\Delta w_i}{c}}} &> 0 \Leftrightarrow \\ \frac{\eta^2}{4c} \left(4a_i^2 - \frac{a_j^2}{(1-\beta)^2} \right) &> \Delta w_i \end{aligned}$$

which is always true for any $\Delta w_i \in \left[\frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right) \right]$ and $\beta \leq \frac{1}{2}$. Furthermore, it is always positive at $\Delta w_i = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ for any $\beta \leq \frac{1}{2}$ and equal to zero if and only if $\beta = \frac{1}{2}$.

Similarly, the slope in third interval is *strictly* negative if

$$\begin{aligned} \frac{1}{2} + \eta \cdot a_j \frac{-\frac{1}{c}}{2 \sqrt{\frac{\eta^2 a_i^2}{4(1-\beta)^2 c^2} - \frac{\Delta w_i}{c}}} &< 0 \Leftrightarrow \\ \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - 4a_j^2 \right) &< \Delta w_i \end{aligned}$$

which is always true as well for any $\Delta w_i \in \left] \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right), \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1-\beta)^2} - \frac{a_j^2}{(1+\alpha)^2} \right) \right]$ and $\beta \leq \frac{1}{2}$. Furthermore, it is always negative at $\Delta w_i = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ for any $\beta \leq \frac{1}{2}$ and equal to zero if and only if $\beta = \frac{1}{2}$. ■

Proof of Corollary 2:

The utility of agent j at $\Delta w_i = 0$ is always smaller as compared to $\Delta w_i = \frac{\eta^2}{4c} \left(\frac{a_i^2 - a_j^2}{(1-\beta)^2} \right)$ if agent j 's utility function is increasing at $\Delta w_i = 0$ which is the case when

$$0 > \frac{\eta^2}{4c} \left(\frac{a_i^2}{(1+\alpha)^2} - \frac{a_j^2}{(1-\beta)^2} \right) \Leftrightarrow \frac{a_j}{a_i} > \frac{1-\beta}{1+\alpha}.$$

If this is not the case we have to compare the utility of the less able agent j at the local maximum of both agents' utility function

$$\frac{W}{2} - \frac{\eta^2 (a_i^2 + a_j^2)}{8(1-\beta)^2 c} + \frac{\eta^2 (a_i^2 + a_j^2)}{2(1-\beta) c}$$

with her utility at $\Delta w_i = 0$, which for $\frac{a_j}{a_i} < \frac{1-\beta}{1+\alpha}$ is given by

$$\frac{W}{2} + \frac{\eta^2 a_j^2}{2(1-\beta) c} + \frac{\eta^2 a_i^2}{2(1+\alpha) c} - \frac{\eta^2 a_j^2}{4(1-\beta)^2 c} + \beta \left(\frac{\eta^2 a_j^2}{4(1-\beta)^2 c} - \frac{\eta^2 a_i^2}{4(1+\alpha)^2 c} \right).$$

Hence, agent j is better off with an unequal income when

$$\frac{a_j^2}{a_i^2} > \frac{1}{(1-2\beta)} \left(\frac{4(1-\beta)^2}{(1+\alpha)} + 1 - 4(1-\beta) - \frac{2\beta(1-\beta)^2}{(1+\alpha)^2} \right)$$

Note that if $\left(\frac{4(1-\beta)^2}{(1+\alpha)} + 1 - 4(1-\beta) - \frac{2\beta(1-\beta)^2}{(1+\alpha)^2} \right) < 0$ this holds for all values of a_j . As $4\beta - 3 < 0$ this condition is equivalent to

$$\left((1+\alpha) - \frac{2(1-\beta)^2}{(3-4\beta)} \right)^2 > \frac{2(1-\beta)^2}{(3-4\beta)^2} (6\beta^2 - 7\beta + 2)$$

Note that $6\beta^2 - 7\beta + 2 > 0$ as this function is = 0 at $\beta = \frac{1}{2}$ and decreasing

for $0 < \beta < \frac{1}{2}$. Rearranging the equation gives

$$\alpha > \frac{1 - \beta}{3 - 4\beta} \sqrt{2(6\beta^2 - 7\beta + 2)} + \frac{2(1 - \beta)^2}{(3 - 4\beta)} - 1$$

which proves the first claim. If, however, $\left(\frac{4(1-\beta)^2}{(1+\alpha)} + 1 - 4(1 - \beta) - \frac{2\beta(1-\beta)^2}{(1+\alpha)^2}\right) > 0$, the condition is equivalent to

$$\frac{a_j}{a_i} > \sqrt{\frac{1}{(1 - 2\beta)} \left(\frac{4(1 - \beta)^2}{(1 + \alpha)} + 1 - 4(1 - \beta) - \frac{2\beta(1 - \beta)^2}{(1 + \alpha)^2} \right)}.$$

which establishes the second claim. ■