## **Factors Influencing Marketing Margins in Cattle and Beef Markets**

Ardian Harri (662) 325-5179 Harri@agecon.msstate.edu

> John D. Anderson Johna@fb.org

John Michael Riley (662) 325-7986 Riley@agecon.msstate.edu

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### Introduction

Cattle and beef prices in the first quarter of 2010 have been, for the most part, an improvement from the prices experienced in much of 2009. First quarter Choice boxed beef values were approximately 5% above the first quarter in 2009. The five-area weighted average price for live steers was about 8% higher in the first quarter of 2010 compared to the first quarter of 2009. The price of 750 to 800 pound steers at Oklahoma City auction markets improved just over 7% in the same time frame. Despite the improvement, stocker operators and feeders are likely less enthusiastic about the high prices due to the environment in which they operate. Given the inherent nature of commodity markets these operators function on typically thin margins. More specifically, in times of high prices these operators purchase expensive cattle and must rely on the market to maintain its strength to remain at or above break-even when selling. Furthermore, the high prices increase the capital requirements of these operators.

Beef processors, feedlots, and stocker grazing/backgrounding enterprises all operate on a margin. Their gross margin is determined by the difference between the cost of the animals entering their production system and the value of the product sold at the end of the production system. This situation is common to any firm involved in adding form utility to a raw or intermediate product. In the beef industry, though, the estimation of these marketing margins is complicated by the long production lags. The long lags are primarily found in the backgrounding and feeding phases of the production system. For these operations in particular, the marketing margin is influenced not only by the differences in form between input and output but by the dynamic behavior of prices over the course of a three or four month long production

cycle. To a lesser extent, beef processors also rely on market stability when making purchasing decisions since pens of cattle are often bought anywhere from seven to 21 days in advance.

Of course, the cost of adding weight also factors into the equation for stockers and feeders and so the relative price of feed, hay and forage is important as well. As such, another aspect to consider regarding the marketing margin that stockers and feeders operate under is the relationship between prices of cattle in different weight classes. This relationship is well-known in the industry and is popularly referred to as the price/weight slide (or, more simply, the price slide). Generally, the price slide reflects an inverse relationship between cattle weight and price per pound. This relationship arises from the fact that it is generally possible to put weight on an animal for less than the value of that additional weight. Thus, lighter cattle are worth more per unit than heavier cattle because the potential profit from adding weight to the lighter animals is bid into their price. Analyses of the price slide are relatively common in the agricultural economics literature. Dhuyvetter, Schroeder, and Prevatt (2001) quantify the impact of key related prices (corn and fed cattle) on feeder cattle price slides. Brorsen et al. (2001) analyze formal price slides used in feeder cattle pricing arrangements, finding that such slides are generally not sufficient to ensure accurate estimates of feeder cattle sale weights by sellers.

While work on feeder cattle price slides is useful in the context of feeder cattle marketing and price discovery, it sheds very little light on the issue of marketing margins in the backgrounding and feeding phases of beef production. Price slides reflect differences in contemporaneous prices and do not take into account the very significant production lags inherent in the beef industry. Other authors have directly addressed the behavior of marketing margins but have generally not attempted to fully incorporate an accurate representation of the dynamic character of production. Research exploring marketing margins in the beef sector has largely been spurred by meat packer concentration concerns (Azzam and Anderson). The bulk of this literature focuses on the margin between feeders and processors and/or processors and retailers. Holt (1993) develops a three equation structural model of farm-retail beef price spreads. This work does not, however, extend farm level analysis any further upstream than the fed cattle level, thus avoiding the longer production lags in the backgrounding and feeding sectors. Similarly, Goodwin and Holt (1999), in evaluating price transmission in the beef industry define farm-level prices at the fed cattle level.

A recent study by Marsh and Brester states that from 1970 to 1998 the margin between beef wholesalers (processors) and retailers increased by 27%. Their model based on inverse demand and supply equations indicate that a multitude of factors impact wholesale-to-retail beef margins; however, again this analysis does not go any further back in the production system than the processor level. The United States Department of Agriculture (USDA) annually reports a farm-to-retail statistic; however, Brester, Marsh and Atwood (2009) determine that this margin is not a reliable indicator.

In summary, existing research examines contemporaneous price relationships in the feeder cattle market as well as marketing margins between the fed cattle and retail beef markets. Very little work has been done however, on intertemporal price relationships upstream from the fed cattle market. Price relationships across time and across stocker/feeder cattle classes represent marketing margins for backgrounding and feeding operations.

#### **Research Objectives**

The general objective of this research is to define the factors that influence marketing margins in the beef industry. Specific objectives are twofold. First, this work will develop a conceptual

model of marketing margins for backgrounding operations, feeding operations, and beef processors that explicitly incorporates realistic production lags at the backgrounding and feeding stages. Second, an empirical model will be estimated that quantifies the impact of key variables on beef industry marketing margins.

#### **Conceptual Framework**

Following Gardner (1975) and Holt (1993), we assume that backgrounders and feeders operate in competitive markets. In addition, similar to Holt, we assume that both backgrounders and feeders form rational expectations of output price and price risk.

We assume, as in Brorsen et al. (1985), that a price-taking firm (a backgrounder or feeder) produces output y from a raw input x and a vector z of other inputs according to production function

(1) 
$$y = f(x,z)$$
.

We further assume that the production function is weakly separable and that y is produced in fixed proportions from the raw input x while other inputs z are used in variable proportions. Thus, each firm's technology can be represented by the Leontief production function

(2) 
$$y = min[x/k,g(z)]$$

where k is a positive constant. Let p denote the output price, r the price of the input x and q the vector of prices for other inputs z. The cost function associated with (2) is

(3) 
$$C(r,q,y) = min_{x,z}[rx+q'z] = rx^*(r,y) + q'z^*(q,y) = rky+q'z^*(q,y)$$

where  $x^*(r, y) = ky$  and  $z^*(q, y)$  are the cost-minimizing input demand functions, and *C* is a linear homogeneous function, increasing and concave in prices (r, q) and increasing and strictly convex in output *y*.

The firm profit function is then

(4) 
$$\pi = (p - kr)y - \widetilde{C}(q, y)$$

where  $\widetilde{C}(\boldsymbol{q}, y) = \boldsymbol{q}' \boldsymbol{z}^*(\boldsymbol{q}, y)$  is the cost for the variable inputs  $\boldsymbol{z}$ .

The random (inverse) demand schedule faced by the firms is given by

(5) 
$$p = \widetilde{p}(Y, s) + \sigma \varepsilon$$

where Y = my is industry output, *m* is the number of firms, *s* is a vector of exogenous demand shifters and  $\varepsilon$  is a random variable with  $E(\varepsilon) = 0$  and  $E(\varepsilon^2) = 1$ . The expected output price is then  $E(p) = \tilde{p}(Y, s)$  and the variance of the output price is  $\sigma^2$ .

Under the assumption that backgrounders and feeders goal is to maximize the expected utility of the firm's wealth, then they make the production decisions based on

(6) 
$$Max_y EU[w_0 + (p - kr)y - \hat{C}(q, y)]$$

where  $w_0$  is the initial wealth, U(w) is an increasing  $(\partial U/\partial w > 0)$  and concave  $(\partial^2 U/\partial w^2 < 0)$  function for a risk-averse firm, and *E* is the expectation operator. Taking the first-order condition of (6) we obtain

(7) 
$$\mathbb{E}[U'_{\{(p-kr)-\widetilde{c}(q,y)\}}] = \widetilde{p}(Y,s) - kw - \widetilde{c}(q,y) + cov(U',p)/\mathbb{E}U' = 0$$

where  $\tilde{c}(q, y) = \partial \tilde{C}(q, y) = q' z^*(q, y)$  and  $cov(U', p)/EU' = \rho \{\gamma^2 \cdot E[U' - EU']^2\}^{1/2}$  is the covariance between U' and p, with  $\rho$  being the correlation between marginal utility and output price. Under risk version, output price and marginal utility are negatively correlated (Baron,

1970). The solution to (7) is the firm's supply function. Given our focus on the marketing margin, one can obtain the function for the expected marketing margin (Brorsen et al., Holt) by inverting the firm's supply function

(8) 
$$\widetilde{p}(Y,s) - kw = \widetilde{c}(q, y) + \delta^* \gamma$$

where  $\delta^* = -(EU')^{-1} \rho \{ E[U' - EU']^2 \}^{1/2}$ . Given that  $\rho$  is negative,  $\delta^*$  will be positive.

Assuming that the industry behaves like a representative firm, the aggregate expected margin equation for the backgrounding and feeding operations is

(9) 
$$M = \widetilde{p}(Y,s) - kw = \Pi(q,Y) + \delta_1 \gamma + e$$

where  $\widetilde{M}$  denotes expected margin and *e* is a stochastic error term. Brorsen et al. show that under decreasing absolute risk aversion (DARA)  $\partial \widetilde{M} / \partial Y > 0$ ,  $\partial \widetilde{M} / \partial q_i \ge 0$  ( $\le = 0$ ) as

$$\partial Y / \partial q_i \leq 0 \ (\geq = 0)$$
, and  $\partial M / \partial \gamma > 0$ .

#### **Data and Empirical Procedures**

The empirical model consists of six equations, three for the backgrounding operations and three for the feeding operations. For each of the two operations, the first and second equations represent respectively the demand for and the supply of cattle/beef at that operation. The third equation represents the marketing margin for the operation. Expected prices for feeder cattle are obtained from price of the futures contract for feeder cattle with a maturity date four months from the current date. Similarly, the expected price risk for feeder cattle is obtained from the implied volatility for the same feeder cattle contract. The marketing margin for the backgrounding operation is then defined as the difference between the expected price for feeder cattle and the current price for steers in the 500-600 pounds category. Expected prices for fed cattle are obtained from the price of the futures contract for live cattle with a maturity date five months from the current date. In addition, the expected price risk for fed cattle is obtained from the implied volatility for the same fed cattle contract. The marketing margin for the feeding operation is defined as the difference between the expected price for fed cattle and the current price for steers in the 700-800 pounds category. Appropriate weight conversions are also taken into account when calculating both margins. Specifically, an average weight of 500, 750, and 1,200 pounds is used respectively for stocker, feeder and fed cattle. Figure 1 displays the marketing margins for the feeding and backgrounding operations.

Data are monthly observations from January 1990 to September 2009. Cash prices for feeder cattle are from the *Weekly Weighted Average Summary* of cash prices reported by USDA's Agricultural Marketing Service (AMS) for Oklahoma City. Feeder cattle quantity is from the National Agricultural Statistics Service's (NASS) monthly *Cattle on Feed* report<sup>1</sup>. Cash fed cattle prices are from AMS's *Five Area Daily Weighted Average Direct Slaughter Cattle* report and wholesale beef prices are from AMS's *National Weekly Boxed Beef Cutout and Boxed Beef Cuts* report. The Chicago cash price for corn from AMS's *Weekly Feedstuff Wholesale Prices* report are used. Futures prices and implied volatilities for feeder and fed cattle are obtained from the *Commodity Research Bureau*. The consumer price index (CPI) (1982 = 100), and the wage rate for the feeding operations are obtained from the *Bureau of Labor Statistics*. The farm wage rate and the energy index are obtained from NASS. All prices are deflated by CPI.

The fed cattle demand is specified as

<sup>&</sup>lt;sup>1</sup> For this analysis the feeder cattle supply is the total number of cattle on feed less than 90 days. This is calculated by subtracting the cattle placed on feed greater than three months out from the current cattle on feed total.

$$\Delta P_{t}^{l} = \alpha_{0} + \alpha_{1} \Delta P_{t}^{BB} + \alpha_{2} \Delta P_{t-1}^{BB} + \alpha_{3} \Delta P_{t-2}^{BB} + \alpha_{4} \Delta P_{t-3}^{BB} + \alpha_{5} \Delta Q_{t}^{l} + \alpha_{6} \Delta Q_{t-2}^{l} + \alpha_{7} \Delta Q_{t-3}^{l}$$

$$(10) + \alpha_{8} Z P_{t-1}^{l} + \alpha_{9} SINl + \alpha_{10} COSl + \alpha_{11} SIN2 + \alpha_{12} COS2 + \sum_{i=1}^{11} \alpha_{12+i} \Delta P_{t-i}^{l} + \varepsilon_{It}$$

where  $\Delta$  is the first-difference operator,  $P^1$  is the five-area weighted average live weight price for fed steers in cents per pound,  $Q^1$  is commercial beef production in million pounds,  $P^{BB}$  following Marsh (2007) is the cut-out (wholesale) value of beef, *SIN*1, *SIN*2, *COS*1, and *COS*2 are harmonic variables used to capture the six- and twelve-month cycles<sup>2</sup>, and  $\alpha_0, ..., \alpha_{23}$  are parameters. Current and lagged values of the commercial beef production and the wholesale value of beef are included to capture the gradual response to quantity and wholesale price changes. Similarly, the lagged values of price changes capture short-run dynamics of fed cattle prices. Finally,  $ZP^1$  is an error correction term capturing the cointegrating relation between the  $P^1$  and  $P^{BB}$ . We test, using Dickey-Fuller (19179, 1981) and Phillips-Perron (1988) tests, whether  $P^1$  and  $P^{BB}$  are stationary. Both tests indicate that  $P^1$  and  $P^{BB}$  are I(1). Next, we use Johansen (1992) procedure to determine whether a linear combination (cointegrating vector) that is I(0) exists between  $P^1$  and  $P^{BB}$ . Results of cointegration testing and parameter estimates of the cointegrating vector used to construct  $ZP^1$  are reported in table 1.

The fed cattle supply is specified as

$$Q_{t}^{1} = \beta_{0} + \beta_{1}P_{t}^{2} + \beta_{2}P_{t}^{C} + \beta_{3}\sigma_{t}^{1} + \beta_{4}SINI + \beta_{5}COSI + \beta_{6}SIN2 + \beta_{7}COS2$$

$$(11) + \sum_{i=1}^{11}\beta_{7+i}Q_{t-i}^{1} + \varepsilon_{2t}$$

where  $P^2$  is the five-area weighted average live weight price for feeder steers in cents per pound,  $P^C$  is the price of corn, and  $\sigma_t^1$  is the implied volatility for fed cattle price.

<sup>&</sup>lt;sup>2</sup> The harmonic variables are  $SIN1 = sin(2\pi t/6)$ ,  $COS1 = cos(2\pi t/6)$ ,  $SIN2 = sin(2\pi t/12)$ , and  $COS2 = cos(2\pi t/12)$ , t = 1, ..., T.

The equation for the expected margin for the feeding operations is specified as

$$\Delta \widetilde{M}_{t}^{1} = \gamma_{0} + \gamma_{1} \Delta Q_{t}^{1} + \gamma_{2} \Delta P_{t}^{C} + \gamma_{3} \Delta W R_{t}^{P} + \gamma_{3} \Delta P E_{t} + \gamma_{4} \sigma_{t}^{1} + \gamma_{5} Z \widetilde{M}_{t}^{1} + \gamma_{6} SIN1 + \gamma_{7} COS1$$

$$(12) + \gamma_{8} SIN2 + \gamma_{9} COS2 + \sum_{i=1}^{11} \gamma_{9+i} \Delta \widetilde{M}_{t-i}^{1} + \varepsilon_{3t}$$

where  $\Delta \widetilde{M}_t^1 = w_1 \mathbb{E}[P_{t+5}^1] - w_2 P_t^2$  and  $\mathbb{E}[P_{t+5}^1]$  is the price of the futures contract for live cattle with a maturity date five months from the current date,  $w_1$  and  $w_2$  are respectively the average weights for fed and feeder cattle,  $WR^P$  is the wage rate for the feeding industry, *PE* is an energy index, and  $Z\widetilde{M}^1$  is an error correction term capturing the cointegrating relation between the  $\widetilde{M}^1$ ,  $P^C$ ,  $WR^P$ , and *PE*, based on the testing procedure for unit root and cointegration as mentioned above.

The feeder cattle demand and supply, and the expected margin for the feeding operations are, respectively, specified as

$$\begin{split} \Delta P_{t}^{2} &= \varphi_{0} + \varphi_{1} \Delta P_{t}^{1} + \varphi_{2} \Delta P_{t-1}^{1} + \varphi_{3} \Delta P_{t-2}^{1} + \varphi_{4} \Delta P_{t-3}^{1} + \varphi_{5} \Delta Q_{t}^{2} + \varphi_{6} \Delta Q_{t-2}^{2} + \varphi_{7} \Delta Q_{t-3}^{2} \\ (13) &+ \varphi_{8} Z P_{t-1}^{2} + \varphi_{9} SINI + \varphi_{10} COSI + \varphi_{11} SIN2 + \varphi_{12} COS2 + \sum_{i=1}^{11} \varphi_{12+i} \Delta P_{t-i}^{2} + \varepsilon_{4t} \\ Q_{t}^{2} &= \theta_{0} + \theta_{1} P_{t}^{3} + \theta_{2} P_{t}^{C} + \theta_{3} \sigma_{t}^{2} + \theta_{4} SINI + \theta_{5} COSI + \theta_{6} SIN2 + \theta_{7} COS2 \\ (14) &+ \sum_{i=1}^{11} \theta_{7+i} Q_{t-i}^{2} + \varepsilon_{5t} \\ \Delta \widetilde{M}_{t}^{2} &= \lambda_{0} + \lambda_{1} \Delta Q_{t}^{2} + \lambda_{2} \Delta P_{t}^{C} + \lambda_{3} \Delta W R_{t}^{F} + \lambda_{3} \sigma_{t}^{2} + \lambda_{4} Z \widetilde{M}_{t}^{2} + \lambda_{5} SINI + \lambda_{6} COSI \\ \end{split}$$

$$\Delta M_t^2 = \lambda_0 + \lambda_1 \Delta Q_t^2 + \lambda_2 \Delta P_t^2 + \lambda_3 \Delta W R_t^2 + \lambda_3 \sigma_t^2 + \lambda_4 Z M_t^2 + \lambda_5 SINI + \lambda_6 COSI$$

$$(15)$$

$$+ \lambda_7 SIN2 + \lambda_8 COS2 + \sum_{i=1}^{11} \lambda_{8+i} \Delta \widetilde{M}_{t-i}^2 + \varepsilon_{6t}$$

where  $P^3$  is the five-area weighted average live weight price for stocker steers in cents per pound,  $Q^2$  is quantity of feeder cattle in million heads, and  $ZP^2$  is an error correction term capturing the cointegrating relation between the  $P^2$  and  $P^1$ ,  $\sigma_t^2$  is the implied volatility for feeder cattle price,  $\Delta \widetilde{M}_t^2 = w_3 \mathbb{E}[P_{t+4}^2] - w_4 P_t^3$  and  $\mathbb{E}[P_{t+4}^2]$  is the price of the futures contract for feeder cattle with a maturity date four months from the current date,  $w_3$  and  $w_4$  are respectively the average weights for feeder and stocker cattle,  $WR^F$  is the wage rate for the backgrounding industry, and  $Z\widetilde{M}^2$  is an error correction term capturing the cointegrating relation between the  $\widetilde{M}^2$ ,  $P^C$ , and  $WR^F$ .

Based on preliminary analysis GARCH(1,1) processes were adequate for specifying the conditional variance dynamics for the different equations. The conditional variances were specified as

 $\neq j$ .

$$h_{iit} = \kappa_{i0} + \eta_{i1} \varepsilon_{it-1}^{2} + \psi_{i1} h_{it-1},$$
(16)  

$$h_{ijt} = \rho_{ij} (h_{iit} h_{jjt})^{1/2},$$

$$i, j = 1 (P^{1}), 2 (Q^{1}), 3 (\widetilde{M}^{1}), 4 (P^{2}), 5 (Q^{2}), 6 (\widetilde{M}^{2}), i$$

#### Results

Results of cointegration testing and parameter estimates of the cointegrating vectors for four equations, two demand and two margin equations, are reported in table 1. Table one reports the Johansen's trace tests for up to two cointegrating vectors. We find at most one cointegrating vector exist for each of the four cases. Table 1 also reports the normalized cointegrating vectors between the respective variables for each equation. The variables are  $P^1$  and  $P^{BB}$  for the fed cattle demand equation,  $\widetilde{M}^1$ ,  $P^C$ ,  $WR^P$  for the feeding margin equation,  $P^1$  and  $P^2$  for the feeder cattle demand equation, and  $\widetilde{M}^2$ ,  $P^C$ , and  $WR^F$  for the backgrounding margin equation.

Results shown in table 2 relate to the fed cattle equations and these retuned the expected signs for the demand and supply equations. Specifically, an increase in the wholesale price of beef (the boxed beef cutout value) results in an increase in demand for fed cattle. As beef production increases fed cattle price declines. Beef production is negatively influenced by the price of feeder cattle inputs. An increase in corn price has a positive impact on beef production while an increase in fed cattle price risk has a negative impact on beef production. However, both these effects, in our model, are not significant at conventional levels.

Referring to the elasticities in table 4, we find from the fed cattle demand equation that a one percent increase in the price of boxed beef and the total pounds of beef produced results in a 0.859 percent increase and a 0.063 percent decrease in the five area fed cattle price, respectively. For the supply equation for fed cattle, beef production declines by 0.044, 0.01 and 0.024 percent with respect to a one percent increase in the price of feeder cattle, the price of corn and the implied volatility of live cattle futures prices, respectively.

Elasticities calculated from the feeding margin equation indicate that increases in corn price, wages and energy prices all cause the feeding margin to widen. Wages have the largest impact on the feeding margin. A one percent increase in wage rates result in a 0.844 percent increase in the feeding margin. With a one percent increase in the price of corn the feeding margin increases by 0.309 percent. A one percent increase in the energy price index increases the feeding margin by 0.494 percent. A one percent increase in current beef production leads to a 0.127 decrease in the feeding margin while a one percent increase in the volatility of futures prices result in a 0.016 percent increase in the feeding margin.

Table 3 provides the results for the backgrounding operations. Again, all the estimated coefficients have the expected signs. In regard to the elasticities for the feeder cattle demand and

supply equations we find that feeder cattle prices are most influenced by the cash price of fed cattle. A one percent increase in the five area cash price of fed cattle result in a 0.437 percent increase in feeder cattle prices. Feeder cattle supply is negatively impacted by the price of 500 pound incoming calves, corn price and increased feeder cattle price risk.

For the backgrounding margin equation, again, wages have the largest impact. A one percent increase in the wage rate results in a 1.334 percent increase in the backgrounding margin. With a corn price and quantity of feeder cattle supplies increase of one percent the backgrounding margin increases by 0.237 and 0.127 percent, respectively. The margin decreases by 0.054 percent as the implied volatility, a measure of price risk, increases by one percent.

#### Conclusions

Previous beef marketing margin research has focused on the wholesale to retail level. This analysis moves further upstream in the beef production system to determine the factors that impact the feeder calf to fed cattle and the fed cattle to wholesale marketing margins. We employ a six equation model that incorporates fed and feeder cattle supply and demand equations and the margins for each of these two industry segments.

The marketing margin equations are the focal point of this analysis. For the feeding and backgrounding margin wage rates have the largest overall impact. Corn prices, which have risen sharply since 2007, have a positive influence on both margins. Increasing corn prices cause the feeding margin to increase faster than the backgrounding margin while higher wages have a greater impact on backgrounding margin as opposed to feeding margin. The level of price risk, represented by the implied volatility of feeder and live cattle futures prices, have opposing impacts on each margin. Increasing fed cattle price risk causes the feeding margin to increase

while increasing feeder cattle price risk reduces the backgrounding margin. The first part of this is in line with Holt (1993). He explains that positive influence from price risk stems from the fact that fed cattle are also viewed as an investment. Backgrounders on the other hand are more likely to view their operation in a business framework.

|                |       |         | Johanser | 1 I               |           |          |                   |                  |                     |         |
|----------------|-------|---------|----------|-------------------|-----------|----------|-------------------|------------------|---------------------|---------|
|                |       | Coint   | egration | Test <sup>a</sup> |           | Normali  | zed Co            | ointegrating     | Vector <sup>b</sup> |         |
| Equation       | Test  | r = 0   | r = 1    | r = 2             |           |          |                   |                  |                     |         |
| Fed Cattle     | Trace | 55.38   | 12.35    |                   | Variables | Constant | $P^1$             | $P^{BB}$         |                     |         |
| Demand         |       | (29.38) | (15.34)  |                   |           | -        | 1.0               | 0.66             |                     |         |
|                |       |         |          |                   |           |          |                   | (<0.001)         |                     |         |
| Feeding Margin | Trace | 68.27   | 26.84    | 11.66             | Variables | Constant | $\widetilde{M}^1$ | $P^{\mathrm{C}}$ | $WR^{P}$            | PE      |
|                |       | (53.42) | (34.80)  | (19.99)           |           | 253.4    | 1.0               | 50.76            | -163.08             | 0.66    |
|                |       |         |          |                   |           |          |                   | (<0.001)         | (0.030)             | (0.001) |
| Feeder Cattle  | Trace | 24.48   | 6.65     | -                 | Variables | Constant | $P^1$             | $P^2$            |                     |         |
| Demand         |       | (19.99) | (9.13)   | -                 |           | -        | 1.0               | 0.63             |                     |         |
|                |       |         |          |                   |           |          |                   | (0.007)          |                     |         |
| Backgrounding  | Trace | 95.48   | 15.45    | 4.37              | Variables | Constant | $\widetilde{M}^2$ | $P^{\mathrm{C}}$ | $WR^{\rm F}$        |         |
| Margin         |       | (34.80) | (19.99)  | (9.13)            |           | -135.93  | 1.0               | 20.57            | 1.15                |         |
|                |       |         |          |                   |           |          |                   | (<0.001)         |                     |         |

# Table 1. Cointegration Test Results and Cointegrating Vectors

Note: <sup>a</sup> Numbers in parentheses are 5-percent critical values. <sup>b</sup> Numbers in parentheses are p-values.

| Equation    | Parameter      | Variable                              | Coefficient | Standard Error |
|-------------|----------------|---------------------------------------|-------------|----------------|
| Fed Cattle  | $lpha_0$       | Constant                              | 0.020       | 0.004          |
| Demand      | $\alpha_1$     | $\Delta P^{BB}t$                      | 0.451       | 0.020          |
|             | $\alpha_2$     | $\Delta P^{BB}t-1$                    | 0.076       | 0.037          |
|             | $\alpha_3$     | $\Delta Q^{l}t$                       | -0.261      | 0.084          |
|             | $lpha_4$       | $ZP^{l}t$                             | -0.209      | 0.045          |
|             | $\alpha_5$     | SIN1                                  | 0.004       | 0.002          |
|             | $\alpha_6$     | SIN2                                  | -0.003      | 0.002          |
|             | $\alpha_7$     | COS1                                  | -0.011      | 0.002          |
|             | $\alpha_8$     | COS2                                  | 0.006       | 0.002          |
|             | <i>α</i> 9-19  | $\Sigma \Delta P^{l} t$ -i            | -0.123      |                |
| Fed Cattle  | <b>K</b> 10    | Constant                              | 0 099       | 0.070          |
| Variance    | $n_{10}$       | E                                     | 0.056       | 0.055          |
| variance    | 711<br>)/(11   | <b>b</b> ,                            | 0.050       | 0.000          |
|             | $\varphi_{11}$ | <i>nu</i> <sub>1<i>t</i>-1</sub>      | 0.075       | 0.212          |
| Fed Cattle  | $\beta_0$      | Constant                              | 8.403       | 2.064          |
| Supply      | $\beta_1$      | $P^2t$                                | -0.929      | 0.511          |
|             | $\beta_2$      | $P^{C}t$                              | -0.067      | 0.065          |
|             | $\beta_3$      | $\sigma^{l}{}_{t}$                    | -0.041      | 0.028          |
|             | $\beta_4$      | SIN2                                  | -0.697      | 0.188          |
|             | $\beta_5$      | COS1                                  | 0.232       | 0.099          |
|             | $\beta_6$      | COS2                                  | -1.072      | 0.221          |
|             | $\beta_{7-17}$ | $\Sigma Q^{l}t$ -i                    | 0.748       |                |
| Feeding     | 20             | Constant                              | 1 705       | 2 962          |
| Margin      | 70<br>V1       | $\Delta P^{C}t$                       | 25 383      | 5 096          |
| maight      | 71<br>V2       | $\Delta WR^{P}t$                      | 1 638       | 1 050          |
|             | 72<br>V2       | $\Delta PE$                           | 1.608       | 0.630          |
|             | 73<br>V4       | $AO^{l}t$                             | -1 523      | 0.750          |
|             | γ4<br>γ5       | $\sigma_{t}^{l}$                      | 2.491       | 1.624          |
|             | 76<br>76       | $Z\widetilde{M}_{t}^{1}$              | -0.278      | 0.053          |
|             | י גע<br>אר     | SIN1                                  | -5.136      | 1.671          |
|             | 28<br>28       | SIN2                                  | -8.560      | 1.724          |
|             | 29-19          | $\Sigma \Delta \widetilde{M}_{t-i}^1$ | -0.424      |                |
|             | ,,             |                                       |             |                |
| Feeding     | $\kappa_{20}$  | Constant                              | 0.034       | 0.029          |
| Margin      | $\eta_{21}$    | $\mathcal{E}_{lt-l}$                  | 0.112       | 0.037          |
| Variance    | $\psi_{21}$    | $h_{1t-1}$                            | 0.908       | 0.030          |
| Log Likelih | ood            |                                       | -1706       |                |

 Table 2. Maximum Likelihood Estimates of a Multivariate GARCH Model of the Beef

 Feeding Operations

| Equation       | Parameter              | Variable                              | Coefficient | Standard Error |
|----------------|------------------------|---------------------------------------|-------------|----------------|
| Feeder Cattle  | $arphi_0$              | Constant                              | -0.014      | 0.017          |
| Demand         | $arphi_1$              | $\Delta P^{l}t$                       | 0.647       | 0.047          |
|                | $\varphi_2$            | $\Delta P^{l}t-2$                     | -0.140      | 0.051          |
|                | $\varphi_3$            | $\Delta Q^2 t$                        | -0.026      | 0.012          |
|                | $arphi_4$              | $\Delta Q^2 t$ -1                     | -0.010      | 0.005          |
|                | $arphi_5$              | $ZP^{l}t$                             | 0.059       | 0.026          |
|                | $arphi_6$              | COS1                                  | 0.012       | 0.003          |
|                | $arphi_7$              | COS2                                  | -0.023      | 0.003          |
|                | $arphi_{8-18}$         | $\Sigma \Delta P^2 t - i$             | 0.344       |                |
| Feeder Cattle  | <i>K</i> <sub>30</sub> | Constant                              | 0.004       | 0.002          |
| Variance       | $\eta_{31}$            | $\mathcal{E}_{lt-l}$                  | 0.415       | 0.169          |
|                | $\psi_{31}$            | $h_{1t-1}$                            | 0.195       | 0.260          |
| Feeder Cattle  | $	heta_0$              | Constant                              | 5.497       | 1.152          |
| Supply         | $\hat{\theta_1}$       | $P^{3}t$                              | -0.894      | 0.680          |
| 11.5           | $\theta_2$             | $P^{C}t$                              | -0.136      | 0.093          |
|                | $\theta_3$             | $\sigma_t^2$                          | -0.051      | 0.020          |
|                | $\theta_4$             | SIN1                                  | -1.370      | 0.238          |
|                | $\theta_5$             | SIN2                                  | -1.402      | 0.267          |
|                | $	heta_6$              | COS2                                  | -1.572      | 0.272          |
|                | $	heta_{	extsf{7-17}}$ | $\Sigma Q^2_{t-i}$                    | 0.966       |                |
| Backgrounding  | $\lambda_0$            | Constant                              | 6.448       | 2.785          |
| Margin         | $\lambda_1$            | $\Delta P^{C}t$                       | 8.110       | 3.943          |
| -              | $\lambda_2$            | $\Delta W R^F t$                      | 0.899       | 0.492          |
|                | $\lambda_3$            | $\Delta Q^2 t$                        | 0.071       | 0.033          |
|                | $\lambda_4$            | $\sigma_{t}^{2}$                      | -3.637      | 1.686          |
|                | $\lambda_5$            | $Z \widetilde{M}_t^2$                 | -0.240      | 0.073          |
|                | $\lambda_6$            | SIN2                                  | -2.615      | 0.269          |
|                | $\lambda_{7-17}$       | $\Sigma \Delta \widetilde{M}_{t-i}^2$ | -1.659      |                |
| Backgrounding  | $\kappa_{40}$          | Constant                              | 7.381       | 3.754          |
| Margin         | $\eta_{41}$            | $\mathcal{E}_{It-I}$                  | 0.045       | 0.027          |
| Variance       | $\psi_{41}$            | $h_{1t-1}$                            | 0.941       | 0.033          |
| Log Likelihood |                        |                                       | -1706       |                |

 Table 3. Maximum Likelihood Estimates of a Multivariate GARCH Model of the Beef

 Backgrounding Operations

| Equation      | Variable           | Elasticity |
|---------------|--------------------|------------|
| Fed Cattle    | $P^{BB}t$          | 0.859      |
| Demand        | $Q^{l}t$           | -0.063     |
| Fed Cattle    | $P^2t$             | -0.044     |
| Supply        | $P^{C}t$           | -0.010     |
|               | $\sigma^{l}{}_{t}$ | -0.024     |
| Feeding       | $P^{C}t$           | 0.309      |
| Margin        | $WR^{P}t$          | 0.844      |
|               | $PE_t$             | 0.494      |
|               | $Q^{l}t$           | -0.127     |
|               | $\sigma^{l}{}_{t}$ | 0.016      |
| Feeder Cattle | $P^{I}t$           | 0.437      |
| Demand        | $Q^2 t$            | -0.073     |
| Feeder Cattle | $P^{3}t$           | -0.017     |
| Supply        | $P^{C}t$           | -0.008     |
|               | $\sigma_{t}^{2}$   | -0.012     |
| Backgrounding | $P^{C}t$           | 0.237      |
| Margin        | $WR^F t$           | 1.334      |
|               | $Q^2 t$            | 0.127      |
|               | $\sigma_{t}^{2}$   | -0.054     |

Table 4. Estimates of Short-Run Elasticities



Figure 1. Feeding and Backgrounding Margins (cents/lb)

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