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INDIVIDUAL INCOME, INCOMPLETE INFORMATION, AND AGGREGATE CONSUMPTION

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Individual Income, Incomplete Information, and Aggregate Consumption

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Individual Income, Incomplete Information, and Aggregate Consumption

Abstract

Individual income is much more variable than aggregate per capita income. I argue that aggregate information is therefore not very important for individual consumption decisions and study models of life-cycle consumption in which individuals react optimally to their own income process but have incomplete or no information on economy wide variables. Since individual income is less persistent than aggregate income consumers will react too little to aggregate income variation. Aggregate consumption will be excessively smooth. Since aggregate information is slowly incorporated into consumption, aggregate consumption will be autocorrelated and correlated with lagged income. On the other hand, the model has the same prediction for micro data as the standard permanent income model. The second part of the paper provides empirical evidence on individual and aggregate income processes and calibrates the model using the estimated parameters. The model predictions do not match the empirical findings for aggregate consumption very closely.

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1. Introduction

Contrary to the predictions of the modern version of the permanent income hypothesis (Hall, 1978), aggregate consumption changes in the U.S. are correlated with lagged income changes (see Flavin, 1981). Moreover, Deaton (1987) and Campbell and Deaton (1989) demonstrated that consumption is smoother than predicted by the model if income follows a highly persistent process. In individual data, on the other hand, the orthogonality condition implied by the permanent income model is much harder to reject as a multitude of recent studies shows.² If it is true that the model holds for individual data but not for aggregate data³ then some type of aggregation bias should explain the differences.

A variety of possible biases have been explored. Finite lifetimes will introduce a dependence of consumption on cohort characteristics at the aggregate level and the martingale result found by Hall will not hold. Galí (1990) has developed this point in a recent paper and has shown that it is not important enough empirically to explain aggregate consumption data. Attanasio and Weber (1990) have stressed nonlinearities as a possible reason for excess sensitivity at the aggregate level. Finally, a recent paper by Goodfriend (1992) suggests that agents may lack contemporaneous information on aggregate variables which invalidates the martingale property of the model at the aggregte level. In this paper I explore the theoretical and empirical implications of this type of incomplete information.

It is not unlikely that aggregate information plays little role in household decisions since the economic environment in which individuals operate differs sharply from the economy as it is described by aggregate data. Most importantly, individual income is much more variable than aggregate income: Below, I estimate that the standard deviation of quarterly individual income changes is about thirty times larger than that for aggregate per capita income. While some of this variation will be attributable to measurement problems, a large part may reflect idiosyncratic

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² See Deaton (1992) for a recent survey of the literature.

³ The inability to reject the model in micro data may of course also stem from problems related to measurement error, inexact variable definitions, etc. that make these tests less powerful.

income shocks. Therefore, individuals may make little effort to gather information on the behavior of the economy, but rather watch only their own prospective fortunes. Furthermore, individual income processes are much less persistent than aggregate income. The optimal consumption response calculated on the basis of individual income processes differs substantially from the predictions of a representative agent model calibrated with aggregate data. Using these facts, I construct a simple model in which agents react optimally to their individual income innovations but do not incorporate information on economy wide variables. The model correctly predicts what we observe in aggregate data: the correlation of consumption changes with lagged income and excess smoothness.

A simple example makes clear how the model works. Suppose a worker gets laid off from his job; he does not know immediately whether this is due to specific conditions at his firm or because of the onset of a general recession. If the layoff is due to highly individual factors then it will be easy for the worker to find new employment and the income reduction associated with the unemployment spell does not call for a major revision in consumption expenditures. Should the unemployment be due to aggregate factors, employment will be depressed at other firms as well and lead to a much longer expected unemployment spell. The necessary revision in consumption will be much larger than in the former case. The worker adjusts consumption in a way that will be correct on average given his overall experience with unemployment.

Looking at aggregate data, an econometrician will find *ex post* that everybody revised consumption downward too little at the onset of a recession. Subsequently, there will be further revisions once workers learn about the true scope and persistence of the shock. Consumption will appear correlated with lagged income and will appear smoother than predicted by a model where agents know the cause and length of their unemployment spell immediately.

There are a number of well known expositions of the idea that individual agents may have incomplete aggregate information. Phelps (1969) and Lucas (1973) suggested a model in which workers/suppliers confuse aggregate and relative price movements. This yields an observable Phillips curve relationship in aggregate data which is not predicted by a full information representative agent model. Altonji and Ashenfelter (1980) use the same feature in a life-cycle model of labor supply to generate an intertemporal substitution effect. If the aggregate wage

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follows a random walk and agents have full information there is no room for intertemporal substitution. If workers only know the lagged aggregate wage and their own wage, consisting of an individual and an aggregate component, then the model yields aggregate employment fluctuations even if the aggregate wage is a random walk. Froot and Perold (1990) have recently suggested a model where securities market specialists observe only information on their own stock contemporaneously but not aggregate information. Their model yields correlated aggregate stock returns.

In all of these models agents observe the aggregate variable with a one period lag. An analogous model in which agents learn about aggregate income with a one quarter delay has been suggested for consumption behavior by Goodfriend (1992). His model yields an MA(1) process for consumption changes. Therefore, no variable lagged at least twice should be able to predict consumption changes. The hypothesis of lagged information on income has first been considered informally by Holden and Peel (1985). They reject this model on U.K. data by regressing consumption changes on income and consumption lagged twice. Campbell and Mankiw (1989) use information variables lagged at least two periods and find the same result for the U.S. and other countries.

This paper examines Goodfriend's model with lagged information on aggregate income as well as a version where agents know only their own income processes but never observe the aggregate component in their income. The latter feature has also been used by Deaton (1991) in a model of precautionary savings and liquidity constraints. To avoid convoluting information aggregation with other issues, I use Flavin's (1981) model with quadratic instantaneous utility as a tool for this analysis. This allows explicit solutions for the consumption process. Given the joint behavior of income and consumption it is then possible to calculate the regression coefficient of consumption changes on lagged income changes and the ratio of the variability in consumption to the variability in the income innovation. These predictions are easily compared to the sample statistics for aggregate data.

To calibrate the model it is necessary to have information on aggregate and individual income processes. While some estimates for individual earnings are available in the literature they are not well suited for the present purpose. In particular, no estimates are available that utilize

quarterly income information comparable to the sampling frequency of aggregate data. I use the 1984 Panel of the Survey of Income and Program Participation which contains monthly information on family income to construct the appropriate quarterly micro data. The estimates for the micro income process are adjusted for measurement error as far as it can be identified using the structure of the interviews.

Using these results, I find that the model yields predictions that are in the correct direction and deviate substantially from the full information case. Quantitatively, they do not match the results for U.S. aggregate data well. The model generally tends to predict too high a correlation of consumption with lagged income but not smooth enough consumption. Notice, however, that my procedure, using actual micro parameters to calibrate the model, subjects the model to a much more stringent test than is usually adopted in the macro consumption literature. I show that rational consumers would not concern themselves with acquiring aggregate information because the gain only amounts to a few cents every quarter.

The paper is organized as follows. In the next section, I review the basic full information model and the empirical failures it has generated. Using a simple income process as an example, section 3 analyzes the model with no observability of aggregate income and describes its implications. In section 4, I contrast this with the model of Goodfriend where aggregate information becomes available with a one period lag. The model implications of more general income processes are discussed in section 5. The next two sections are devoted to the estimation of individual and aggregate income processes; section 7 also summarizes the stylized facts on the consumption puzzles. Section 8 uses the estimates on the income processes to predict features of aggregate consumption and compares the results to the findings in the previous section. Section 9 concludes.

2. The Model with Complete Aggregate Information

In this section I will set up the model and review a simple example where agents have individual specific income processes that differ from the time series structure of aggregate income. However, each micro agent has full contemporaneous information on aggregate income. At the agggregate level, this model is equivalent to a representative agent model.

The consumer solves the life-cycle maximization problem:

$$\max_{\{c_i\}} E_t \sum_{s=t}^{\infty} \left(\frac{1}{1+\delta}\right)^{s-t} u(c_s)$$
(1)
s.t. $W_{t+1} = (1+r)[W_t + y_t - c_t]$
$$\lim_{t \to \infty} (1+r)^{-t} W_t = 0 \quad \text{a.s.}$$

 c_t is consumption, y_t is non-interest income, and W_t is non-human wealth at the beginning of period *t*. Income is paid and consumption takes place before interest accrues on wealth. *r* and δ are the interest rate and the time discount rate, respectively. Both are assumed to be constant.

Flavin (1981) has shown that a quadratic instantaneous utility function and $r = \delta$ yields the following relation for the change in consumption

$$\Delta c_{t} = r \sum_{s=0}^{\infty} \frac{(E_{t} - E_{t-1})y_{t+s}}{(1+r)^{s+1}}$$
(2)

i.e. consumption changes equal the present value of the news about future income.

If income follows a univariate time series process known to the consumer then (2) can be used to relate changes in consumption to the innovations in the income process directly. Let income be a process that is stationary in first differences so that it has a Wold representation $\Delta y_t = A(L)\varepsilon_t$. For this process the change in consumption is given by

$$\Delta c_t = A \left(\frac{1}{1+r} \right) \varepsilon_t \tag{3}$$

I will consider models where all individuals have identical income *processes* while each agent faces different realizations of this process. To fix ideas, consider a simple example where income consists of a random walk with innovations that are common to all individuals and a white noise component with shocks that are uncorrelated across individuals. In first differences this process takes the form

$$\Delta y_{it} = \varepsilon_t + u_{it} - u_{it-1} \tag{4}$$

Subscripts *i* denote individual variables while no subscripts refer to aggregate variables. ε_i is the aggregate income innovation, and u_{ii} is the individual income shock. The innovations are assumed to be uncorrelated.

Every period agents observe their own income y_{it} as well as aggregate income y_i . Given that they also know the complete history of these variables they can infer the fundamental shocks ε_i and u_{it} . What is relevant to the consumer is how much each process contributes to permanent income. The optimal rule is to adjust consumption fully to the permanent (aggregate) shock and by the annuity value r/(1+r) to the transitory (individual) shock, i.e.

$$\Delta c_{ii} = \varepsilon_i + \frac{r}{1+r} u_{ii} \tag{5}$$

The change in average per capita consumption is found by summing over individuals. Because the individual shocks are mutually uncorrelated they will sum to zero in a large population so that we obtain

$$\Delta c_t = \frac{1}{n} \sum \Delta c_{it} = \varepsilon_t \tag{6}$$

Aggregate consumption is a random walk and the consumption change is just the aggregate income innovation. Hence this model yields the same predictions as a representative agent model where the representative agent faces the aggregate income process $\Delta y_r = \varepsilon_r$. In particular, consumption changes are uncorrelated with lagged aggregate variables, like lagged consumption or income changes. This martingale property has been tested by Hall (1978) by regressing consumption changes on lags of consumption, income, and stock prices. Hall found little

explanatory power for income but rejected nonpredictability for stock prices; Flavin (1981) also found correlations with lagged income. I will call this rejection of the full information model the *orthogonality failure*.

Hall's test only exploits the information contained in the Euler equation. Combined with the budget constraint the model has the additional implication that the variance of consumption changes should depend on the structure of the income process as pointed out by Deaton (1987). Taking variances in (3) and applying the formula to the representative agent model with random walk income yields

$$\frac{\sigma_{\Delta c}}{\sigma_{\varepsilon}} = A\left(\frac{1}{1+r}\right) = 1 \tag{7}$$

since A(z) = 1 for the random walk. The ratio of the standard deviation of consumption changes to the standard deviation of income innovations should equal the consumption response predicted by the model, one in this case. Deaton found that the empirical equivalent of this variance ratio is actually much too low based on an AR(1) for the first differences in aggregate income. Thus consumption exhibits *excess smoothness*.

Notice how Quah (1990) has used a representative agent model with an income process as in (4) to generate excess smoothness. Agents behave just as in (5) but both shocks ε_r and u_r are common across individuals. The econometrician only observes the compound income process and calculates the magnitude of the optimal consumption change based on this (misspecified) model. Quah demonstrates that the econometrician's model implies a more variable consumption series than the true series and therefore apparent excess smoothness. However, since consumption in (5) is uncorrelated with any lags of income this cannot account for the orthogonality failure also present in the data.

Using the simple example above, I will now address how incomplete information of agents on aggregate income can lead to both the orthogonality failure and excess smoothness at the aggregate level. A more general treatment will follow.

3. Unobservable Aggregate Shocks

Consider the income process in (4) again but now assume that individuals can only observe y_{it} . If the individual cannot distinguish the aggregate and the individual component then this process to her looks just like an MA(1) process for the first differences in income. The income process the individual observes can thus be written as

$$\Delta y_{it} = \eta_{it} - \theta \eta_{it-1} \tag{8}$$

The random variable η_{ii} will contain information on current and lagged aggregate and individual income innovations. Note that $\{\eta_{ii}\}$, though not a fundamental driving process of the model, is an innovation sequence with respect to the history of individual income changes. Muth (1960) has shown that $(1-\theta)\eta_{ii}$ is the optimal predictor of the innovation to the random walk component of income. The MA parameter θ in (8) depends on the relative variances of the aggregate and individual income shocks.⁴

Equation (3) still holds so that changes in individual consumption follow

$$\Delta c_{ii} = 1 - \frac{\theta}{1+r} \eta_{ii} = \frac{1+r-\theta}{1+r} \eta_{ii} \equiv A \eta_{ii} = A \frac{\Delta y_{ii}}{1-\theta L}$$
(9)

Individual consumption changes are a martingale with respect to the history of individual consumption and income. A researcher doing Hall's (1978) analysis on panel data for individuals should not reject the permanent income model.⁵ This type of testing procedure has been carried out, for example, by Altonji and Siow (1987) who do not reject the model. Estimating a structural model as in Hall and Mishkin (1982) would not be correct because their model assumes that

⁴ Define the first order autocorrelation coefficient in (4) $\rho = -\sigma_z^2/(\sigma_c^2 + 2\sigma_z^2)$. Then $\theta = -(1 - \sqrt{1 - 4\rho^2})/2\rho$. 5 The martingale property only holds with respect to variables that are in individuals' information sets. Many researchers using panel data control for macroeconomic shocks. Goodfiriend (1992) pointed out that such controls also invalidate the Hall procedure. I show below that the variance of individual income innovations is far larger than the variance of the aggregate component; this will therefore not be very important in practice.

consumers know the income components in (4).⁶ The correct structural model would use the income process in (8) instead. This has been pointed out by Speight (no date) who finds support for the model with incomplete information on Austrian panel data while the Hall and Mishkin model is rejected.

I want to focus here on the aggregate implications of the incomplete information case. To find the change in average per capita consumption use the last equality in (9) and equation (4) and sum over individuals.

$$\frac{1}{n}\sum\Delta c_{ii} = \frac{A}{n}\sum\frac{\Delta y_{ii}}{1-\Theta L} = \frac{A}{n}\sum\frac{\varepsilon_i + u_{ii} - u_{ii-1}}{1-\Theta L}$$
(10)

Individual shocks will sum to zero again so that we obtain

$$\frac{1}{n} \sum \Delta c_{ii} = \Delta c_i = A \frac{\varepsilon_i}{1 - \theta L}$$
$$\Delta c_i (1 - \theta L) = A \varepsilon_i \tag{11}$$

Equation (11) has a number of interesting implications. Unlike individual consumption, the per capita series of consumption is not a random walk as the representative agent model predicts. Consumption now follows an AR(1) in first differences. The intuition for this is rather simple. Suppose an aggregate shock hits the economy. All the individual consumers see their income changing but they assume that a part of the shock is idiosyncratic and therefore transitory. They will change their consumption but not by as much as the permanence of the shock calls for. Because the shock is persistent, in the following period they will be surprised again that their income is higher than expected, they will increase their consumption further and so on.

All this implies that an econometrician working with the representative agent model will find both the orthogonality failure and the smoothness result in aggregate data. Suppose the econometrician estimates the following model

⁶ This is not literally true. Hall and Mishkin (1982) only distinguish a permanent and a transitory income component. These are not identified with aggregate and individual income processes as in the example in the text. Furthermore, Hall and Mishkin find nonzero correlations between consumption changes and lagged income changes or lagged consumption changes in their data. Apart from the appropriateness of the structural income process it is these correlations that lead to a rejection of the model in their sample.

$$\Delta c_t = \alpha + \beta \Delta y_{t-1} + e_t \tag{12}$$

If the data are generated by (11) the expected value of β would be

$$\beta = \frac{cov(\Delta c_{t}, \Delta y_{t-1})}{var(\Delta y_{t-1})}$$
$$= \frac{E\left\{A\left(\frac{\epsilon_{t}}{1-\theta L}\right)\epsilon_{t-1}\right\}}{\sigma_{\epsilon}^{2}} = \frac{A\theta\sigma_{\epsilon}^{2}}{\sigma_{\epsilon}^{2}} = A\theta$$
(13)

Because individuals do not recognize an aggregate shock to be permanent they will not adjust their consumption by as much as they would if it were the only type of shock to occur. This will lead to more smoothness in aggregate data than predicted by the full information model where the variance of consumption changes equals the variance of aggregate income innovations. For the model with heterogeneous agents and incomplete information we get instead from (11)

$$\frac{\sigma_{\Delta c}}{\sigma_{\varepsilon}} = \frac{A}{\sqrt{1 - \theta^2}} \tag{14}$$

If idiosyncratic shocks are present and the interest rate is small enough the ratio of the standard deviations of the change in consumption and the aggregate income innovation will always be less than one. To see this more clearly, consider the case where $r \rightarrow 0$. In this case $A = 1 - \theta$ and (14) can be expressed as

$$\frac{\sigma_{\Delta c}}{\sigma_{\varepsilon}} = \sqrt{\frac{1-\theta}{1+\theta}}$$
(15)

This will be less than one if $\theta > 0$.

It is easy to see which features of the example drive the result. The representative agent model would hold for aggregate data if the aggregate and the individual income processes had the same persistence properties so that consumers would want to react in the same way to each type of shock. In this example, consumers do not want to increase consumption enough in response to an aggregate shock because they confuse it with the individual income innovation which is less persistent.

The results also hinge on the assumption that individuals cannot or do not find it profitable to distinguish aggregate and idiosyncratic shocks. Otherwise they would react differently according to the persistence properties of the specific shock observed. Goodfriend (1992) originally proposed such a model, where information on aggregate income becomes available with a one period lag. For comparison, I will analyze the implications of this model with lagged information on aggregate income in the following section.

4. Lagged Information about Aggregate Shocks

Suppose aggregate data are published with a one period lag. In period *t* individual *i* will observe y_{it} and the aggregate shock ε_{t-1} . Also assume again that the consumer has access to the infinite history of shocks and can therefore infer u_{it-1} as well once the aggregate shock is known. Write the income process (4) for the individual as

$$\Delta y_{ii} = v_{ii} - u_{ii-1} \quad \text{where} \quad v_{ii} = \varepsilon_i + u_{ii} \tag{16}$$

We can decompose the information the consumer gets every period into two parts. The first part is v_{ii} , the current period innovation which is contained in current individual income y_{ii} . The consumer does not know how the innovation in a particular period is composed of the permanent (aggregate) component and the transitory (individual) component. She will therefore attribute part of the current period innovation to each component given the relative variances. For every particular innovation there will be errors, of course. Secondly, the consumer gets information from the lagged aggregate shock. Once this information arrives she will be able to correct the error made last period in attributing the innovation to its components.

The optimal consumption response will have two parts corresponding to the two pieces of information: a response to the new innovation and a term that corrects for the error made in the previous period. The first part of the consumption response, the reaction to the current period innovation can be written as

$$\omega v_{it} + (1 - \omega) \frac{r}{1 + r} v_{it} = \frac{\omega + r}{1 + r} v_{it}$$
(17)

where $\omega = \sigma_r^2 / (\sigma_r^2 + \sigma_u^2)$ is the relative variance of the aggregate shock.⁷ The first term is the proportion of the new innovation expected to be permanent, the consumption response to that part is one. The second term is the part expected to be transitory, the response is r/(1+r).

Consider the correction for errors made last period. Define the negative of the error in the aggregate component as

$$\xi_{it-1} = \varepsilon_{t-1} - \omega v_{it-1} = \varepsilon_{t-1} - \omega (\varepsilon_{t-1} + u_{it-1}) = (1 - \omega) \varepsilon_{t-1} - \omega u_{it-1}$$
(18)

The errors in the individual component and in the aggregate component have to sum to zero since the signal extraction problem the individual solved in t-I yielded unbiased predictors of the two components. The response of consumption in period t to errors made in t-I is therefore

$$(1+r)\left[\xi_{it-1} + \frac{r}{1+r}(-\xi_{it-1})\right] = \xi_{it-1}$$
(19)

The first term in the square bracket is the correction of the error in the aggregate component, the second term the correction for the error in the individual component. Notice that interest accrued on the portions of the shocks that had not been consumed in the last period.

Putting together the two parts of the total consumption response from (17) and (19) we obtain

$$\Delta c_{it} = \frac{\omega + r}{1 + r} v_{it} + (1 - \omega) \varepsilon_{t-1} - \omega u_{it-1}$$
(20)

Like in the model of the previous section, individual consumption changes still follow a martingale with respect to the history of individual income and consumption.⁸ This can easily be seen by calculating the autocovariance $cov(\Delta c_u, \Delta c_{u-1})$. It will be proportional to $(1 - \omega)\sigma_e^2 - \omega \sigma_u^2$ which is zero. The lagged income innovations in (20) arise from the fact that errors are corrected after one period. However, optimal choice of the weight ω implies that these errors contain no information correlated with lagged income or consumption changes.

⁷ Note that $\omega = (1+2\rho)/(1+\rho) = (1-\theta)^2/(1-\theta+\theta^2)$. It is much more convenient to work with ω here.

⁸ I thank Steve Zeldes for pointing out an error in a previous draft.

Sum the individual consumption responses in (20) for a large population to get the per capita consumption response

$$\Delta c_{i} = \frac{1}{n} \sum \Delta c_{ii} = \frac{\omega + r}{1 + r} \varepsilon_{i} + (1 - \omega) \varepsilon_{r-1}$$
(21)

The change in aggregate consumption follows an MA(1) process. Notice that the impact response to an aggregate shock is smaller in the lagged information model than in the no information model because $(\omega + r)/(1 + r) < A = (1 - \theta + r)/(1 + r)^9$. This is because the relevant innovations that the consumer responds to differ in the two models. v_{ii} in the lagged information model only contains information on contemporaneous aggregate and individual shocks. η_{ii} in the no information model also contains new information on lagged shocks.

Both the orthogonality failure and the smoothness result will still arise in the lagged information model, but their quantitative importance will differ.¹⁰ Consider the regression of the change in consumption on the lagged income change in (13) again. The coefficient on lagged income will be

$$\beta = \frac{cov(\Delta c_t, \Delta y_{t-1})}{var(\Delta y_{t-1})}$$
$$= \frac{E\left\{\left[\frac{\omega+r}{1+r}\varepsilon_t + (1-\omega)\varepsilon_{t-1}\right]\varepsilon_{t-1}\right\}}{\sigma_{\varepsilon}^2} = 1-\omega$$
(22)

which is positive. Taking variances in (21) yields

$$\frac{\sigma_{\Delta c}}{\sigma_{\varepsilon}} = \sqrt{\left(\frac{\omega+r}{1+r}\right)^2 + (1-\omega)^2}$$
(23)

which is less than one for small values of r.

⁹ This follows from $\theta > 0$ and the relationship between θ and ω .

¹⁰ The test carried out by Campbell and Mankiw (1989) should not reject the model since their test only relies on instruments lagged at least two periods. Their rejection therefore is inconsistent with the model with lagged information.

Which of the two models presented above is more reasonable? Ideally, one would consider a hybrid where agents obtain some noisy aggregate information with a lag. The two models can be thought of as special cases of this hybrid model which generates an ARMA(1,1) process for consumption changes. The predictions for β and the ratio of the variability of consumption to the variability of the income innovation lie between the predictions for the two polar cases considered above. I do not elaborate on this here because I have not found tractable generalizations to other income processes for the model with noisy signals on aggregate income.

Among the two polar models the one with lagged information seems better suited to explain the behavior of rational decision makers who form expectations on the basis of all available information since basic aggregate statistics are provided virtually for free by the news media. However, a rational agent will not only consider the costs, which are admittedly small, but also the benefits. Cochrane (1989) has shown that it is possible to calculate the loss from nonmaximizing behavior and found that these losses are generally small for small deviations from the optimal path. The same should be true here. I will present results on the utility loss from ignoring aggregate information in section 8 after showing what reasonable estimates for the individual and the aggregate income processes are. First, turn to the formulation of the model with more general income processes.

5. More General Income Processes

It is straightforward to extend the examples in the sections 3 and 4 to more general processes for income. First return to the version of the model with no information. Let the first differences in individual income be stationary. This is a fairly general framework since it allows for stationarity in the levels as well, in this case the first differenced process has an MA unit root. Income consists of an aggregate and an individual component given by their respective Wold representations:

$$\Delta y_{it} = \phi(L)\varepsilon_t + \theta(L)u_{it}$$
(24)
where $\phi(z) = \sum_{i=0}^{\infty} \phi_i z^i$
 $\theta(z) = \sum_{i=0}^{\infty} \theta_i z^i$

Average per capita income is then given by

$$\Delta y_t = \phi(L)\varepsilon_t \tag{25}$$

Given stationarity, the process for individual income changes has a Wold representation

$$\Delta y_{ii} = A(L)\eta_{ii} \tag{26}$$

Individual consumption will follow

$$\Delta c_{ii} = A \left(\frac{1}{1+r} \right) \eta_{ii} \tag{27}$$

Define $\overline{\eta}_i$ as the population average of η_{ii} . Equating (24) and (26) and summing over individuals yields

$$A(L)\overline{\eta}_{t} = \phi(L)\varepsilon_{t} \tag{28}$$

If A(L) has no unit root (i.e. at least one of the two components is integrated of order one)¹¹ we can invert it to obtain

$$\Delta c_{\iota} = A \left(\frac{1}{1+r} \right) \overline{\eta}_{\iota} = A \left(\frac{1}{1+r} \right) A^{-1}(L) \phi(L) \varepsilon_{\iota}$$
(29)

Under what conditions does (29) imply excess smoothness in a representative agent model for aggregate consumption? For small interest rates, a necessary and sufficient condition for excess smoothness is given by

¹¹ The analysis proceeds analogously for stationary processes in levels after canceling the common unit root in $\phi(L)$ and A(L).

$$\frac{1}{2\pi} \frac{f_{A}(0)}{f_{\phi}(0)} \int_{-\pi}^{\pi} \frac{f_{\phi}(\omega)}{f_{A}(\omega)} d\omega < 1$$
(30)

where $f(\omega)$ is the normalized spectral density at frequency ω for the respective processes. A derivation is given in Appendix A. Condition (30) shows that relative persistence of the component processes is important: The higher is the spectral density at frequency zero of aggregate income compared to the compound process (and thus compared to individual income) the more likely is the model to yield excess smoothness. But a second component is present in (30) indicating that the entire spectral shape of the processes also matters. This is the case because individuals use current period income changes to extract not only information on current income innovations but on the entire history as well. The relative dynamics of aggregate and individual income determine how they evaluate an observed movement in income. Excess volatility of consumption can arise even if aggregate shocks are more permanent if certain spectral densities are not well represented in individual income. An example of such a case is an aggregate MA(1) in first differences with a coefficient of 0.3 combined with an individual MA(2) in first differences with coefficients 0.6 and -0.4 and an innovation variance ten times that of the aggregate income process. Aggregate income is more persistent, as measured by the spectral density at frequency zero. Nevertheless, aggregate consumption is more volatile than in the representative agent model.

The examples in the previous sections demonstrated the orthogonality failure through the correlation at the first lag. For specific processes, this correlation can be recovered from (29). However, there is no obvious way to parameterize the occurrence of the orthogonality failure in general. Since Galí (1991) has shown that either excess smoothness or excess volatility has to imply the orthogonality failure I will not pursue this issue separately here and refer the reader to Galí for details.

Now turn to the model with lagged information. Rewrite (24) as

$$\Delta y_{ii} = \varepsilon_i + u_{ii} + \overline{\phi}(L)\varepsilon_{i-1} + \overline{\theta}(L)u_{ii-1}$$
where $\overline{\phi}(z) = \sum_{i=1}^{\infty} \phi_i z^i$

$$\overline{\theta}(z) = \sum_{i=1}^{\infty} \theta_i z^i$$
(31)

Define v_{ii} again as the contemporaneous innovation. Since all the previous values of the aggregate shocks can be observed and all the previous values of the individual shocks can be inferred we can again think of information consisting of the innovation v_{ii} and the correction for the error made before. Equation (18) still defines the error made last period in attributing parts of the innovation to the aggregate and the individual processes. Analogously to equation (20) we obtain for the change in individual consumption

$$\Delta c_{ii} = \left\{ \phi \left(\frac{1}{1+r} \right) \omega + \theta \left(\frac{1}{1+r} \right) (1-\omega) \right\} v_{ii} + (1+r) \left\{ \phi \left(\frac{1}{1+r} \right) - \theta \left(\frac{1}{1+r} \right) \right\} \xi_{ii-1} \quad (32)$$

Aggregating yields¹²

$$\Delta c_{t} = \left\{ \phi \left(\frac{1}{1+r} \right) \omega + \theta \left(\frac{1}{1+r} \right) (1-\omega) \right\} \varepsilon_{t} + (1+r) \left\{ \phi \left(\frac{1}{1+r} \right) - \theta \left(\frac{1}{1+r} \right) \right\} (1-\omega) \varepsilon_{t-1}$$
(33)

The regression coefficient of consumption changes on lagged income changes is given by

$$\beta = \frac{(1+r)\left\{\phi\left(\frac{1}{1+r}\right) - \theta\left(\frac{1}{1+r}\right)\right\}(1-\omega)}{\sum_{i=0}^{\infty}\phi_i^2}$$
(34)

As in the previous section, the orthogonality condition holds at all further lags because agents incorporate all aggregate information after one period. It is obvious that for small interest rates the condition $\phi(1) > \theta(1)$ is necessary and sufficient for a positive regression coefficient in (34). It turns out that the same condition together with invertibility of $\theta(z)$ is also sufficient for excess smoothness. A demonstration of this fact is given in Appendix A.

¹² Equations (32) and (33) correspond to equations (11) and (12) in Goodfriend (1992).

In contrast to the no information model income dynamics do not play a role here. Only the relative persistence of aggregate and individual shocks as measured by $\phi(1)$ and $\theta(1)$ matter. This is because households can separate new information v_{it} from lagged information which is not the case for the no information model.

6. Empirical Results on Micro Income Processes

The remainder of the paper explores whether the data bear out the implications of the models studied above. The strategy I pursue is to estimate simple models for the micro and macro income processes first. Using these estimates I calculate the implied values of the excess smoothness ratio and the regression coefficient for the orthogonality test at the aggregate level. The results are then easily compared to the aggregate sample values of these statistics.

I start in this section by presenting results on individual income processes. Previous studies in this area reveal that income innovations for individuals are less persistent than shocks to aggregate income and that individual income variation is far more important.

MaCurdy (1982) and Abowd and Card (1989) have analyzed the time series structure of earnings in micro data. They find that the log of earnings changes for male household heads in the U.S. is well described by an MA(2). Both MA coefficients are negative, with the first one between -0.25 and -0.4 and the second one closer to zero. The variance of log earnings changes is substantial. The standard deviations range from about 0.25 to a high of 0.45 for certain years. This means that a one standard deviation change in earnings is 25 percent to 45 percent of the previous level. Individual income risk is clearly the main source of income uncertainty individuals face.

MaCurdy only analyzes data from the Panel Study of Income Dynamics which is conducted annually. Abowd and Card also present results for data from the control groups of the Denver and Seattle Income Maintenance Experiments which correspond to semiannual income. They find generally first order autocorrelations that are even more negative for these data. However, this may not result from the different sampling frequency but from the fact that the experiment oversampled relatively poor households.

While these studies refer to earnings, results for the (annual) family income process are provided by Hall and Mishkin (1982). They estimate a restricted MA(3) for income changes with results very similar to the studies mentioned above. Family income apparently follows a process very similar to individual earnings.

None of these results are directly suited for the present purpose. The stylized facts on aggregate consumption have all been established on quarterly series. In order to have analogous results for individual income I estimated restricted covariance models with quarterly data that I constructed from the 1984 Survey of Income and Program Participation (SIPP). This panel survey was conducted three times a year from late 1983 to the beginning of 1986 in about 20,000 households and collected monthly income information. The interviews took place on a rolling basis, with one fourth of the sample being interviewed each month. In each interview, information was collection on the four past months. From these data I constructed a panel of quarterly income from the fourth quarter of 1983 to the first quarter of 1986, the longest span for which information on the entire sample is available.

Consumption decisions are most likely made at the family level. I therefore selected families that can be followed continuously throughout the sample period and did not change head or spouse. Most likely, events that change household composition in a major way will also lead to large income changes. The sample selection will therefore tend to understate the variance of income changes. Furthermore, I limited the sample to households whose head did not go to school in any part of the sample period. The latter group may have large movements in income which are anticipated by the individuals but would appear as random elements in the estimation. For example, an individual just finishing school will have a large increase in income. But this jump will have been foreseen and has therefore, according to the model, already been incorporated in previous consumption decisions. I also eliminated non-family households since

I cannot judge whether they make joint or individual consumption decisions. Finally, I limited the sample to families with heads between the ages of 16 and 70 during the survey period. Appendix B contains further details on the construction of the sample.

The correct income concept is net family income from all sources excluding capital income. Variables on total family income and income from capital are provided on the SIPP user tapes; these are aggregated from an array of detailed questions on various income categories for each family member. I use these variables although there are some problems associated with them. First, tax information is only collected infrequently and cannot be apportioned to single months. This is a severe shortcoming of the data because gross income will have a higher variance and (in a progressive tax system) exhibit more transitory fluctuations. Furthermore, the individual variables that make up family income can have imputations. Since the imputations occur at the disaggregated level it would be rather arbitrary to decide which observations to delete because of the imputations. I decided to use all the data. Imputations should lower the estimated variance of income changes, presumably largely at the cost of the transitory income component. Finally, all disaggregated income items are topcoded at \$8,333 per month. It is impossible to decide from the aggregated income items which variables have been topcoded. The topcoding only affects a small portion of the sample and will also reduce the income variance.¹³

¹³ About 2 percent of the households in each wave report total income of \$ 8,333 or more. This is an upper bound for the incidence of topcoding since it may result by summing various components that may each be below the cutoff. Deleting all the households that have income above this level in at least one month during the sample period eliminates 12 percent of the households. The variance of income changes is cut by 60 percent in this smaller sample while the estimated autocorrelations are very similar.

	Bas	Table 1 sic Sample Statistic	s		
	SIPP	Sample	CPS Sample		
	Mean	Std. Dev.	Mean	Std. Dev.	
Age	43.9	12.9	42.5	13.4	
Years of Schooling	12.6	3.25	12.5	3.22	
Non-White	0.12	0.32	0.13	0.34	
Male	0.77	0.42	0.73	0.44	
Never Married	0.09	0.29	0.14	0.35	
Family Size	3.03	1.50	2.82	1.56	
Family Income 1984 [quarterly]	6,663	4,933	6,666	5,060	
Sample Size	8,176		25,033		

I provide some basic characteristics of the sample in table 1 which also presents results from the March 1985 Current Population Survey. In most respects the SIPP sample matches the general population closely.

Measurement error. Before turning to the estimation of the quarterly income process I present a few features of the monthly income data for the sample just described based on the first eight waves¹⁴. As a referee pointed out, family income has the feature that it is constant over a period of time and only changes at infrequent intervals. This constancy of income in the SIPP is mainly a feature of the interview structure: 47 percent of the families in the sample report no change from one month to the next *within* interviews, while only 9 percent report constant income in two adjacent months *across* interviews. Remember that in each interview households are asked about income in the four preceeding months. A large fraction, 27 percent, reports constant income within the entire interview. These numbers, rather than telling us about the true dynamic

¹⁴ Only two of the four rotation groups in the 1984 SIPP had nine interviews.

structure of the income process, are indicative of substantial measurement error. Households seem to smooth income fluctuations within interviews in their reports while accetuating fluctuations across interviews.

The structure of the data collection process allows to recover part of the measurement error process. It is useful to characterize income and measurement error in the following way:

$$y_{ijt} = y_{ijt} + \mu_{ij} + \zeta_{ijt}$$
(35)

Subscripts *i* refer to families, *j* to interviews, and *t* to months. Measured income consists of true income (indicated by a star) and an additive measurement error. The measurement error is decomposed into two parts, the first ζ_{ijt} summing to zero within each interview while the second μ_{ij} is constant within interviews. Any additive measurement error can be decomposed in this way.

This decomposition has the feature that the two errors are uncorrelated and ζ_{ijt} is serially uncorrelated across interviews. Furthermore, to capture the feature that households report constant income within interviews, presumably ignoring some true fluctuations, ζ_{ijt} will have to be negatively correlated with true income. As is usual in this type of analysis, no features of this part of the error can be recovered from the data without outside information or strong identifying assumptions. I will therefore ignore it in the following analysis. Fortunately, there are good reasons to assume that this is not a major problem, since I work with aggregated quaterly data below so that some of this error will wash out in the aggregation process. Furthermore, the negative correlation with true income reduces the upward bias in estimating the variance of true income changes. Finally, since ζ_{ijt} is uncorrelated across interviews its influence on the measured dynamics of the income process will also be limited.

Given the way the SIPP data is collected it is possible to identify the variance and autocovariances of the second part of the measurement error μ_{ij} . Differencing (35) yields

$$\Delta y_{ijt} = \begin{cases} \Delta y_{ijt}^* + \Delta \zeta_{ijt} & \text{within interview} \\ \Delta y_{ijt}^* + \Delta \mu_{ij} + \Delta \zeta_{ijt} & \text{across interviews} \end{cases}$$
(36)

Table 2 presents these variances and the first eight autocovariances by interview month.

Table 2				
Variances and a	Autocovariances f	for Changes in I	Monthly Family	Income
	(Inco	ome / 1000)		
	(standard err	ors in parenthe	ses)	
	1. Month	2. Month	3. Month	4. Month
Variance	2.439	0.966	1.133	1.270
	(0.093)	(0.053)	(0.068)	(0.090)
Autocovariance 1	-0.680	-0.452	-0.481	-0.529
	(0.080)	(0.042)	(0.038)	(0.052)
Autocovariance 2	-0.059	-0.006	-0.020	0.017
	(0.022)	(0.020)	(0.021)	(0.013)
Autocovariance 3	-0.072	0.002	-0.013	-0.034
	(0.020)	(0.021)	(0.019)	(0.017)
Autocovariance 4	-0.501	-0.001	-0.022	0.005
	(0.030)	(0.019)	(0.024)	(0.017)
Autocovariance 5	-0.006	-0.029	0.023	0.009
	(0.022)	(0.023)	(0.020)	(0.022)
Autocovariance 6	0.020	0.004	0.018	-0.010
	(0.024)	(0.015)	(0.019)	(0.020)
Autocovariance 7	-0.026	-0.018	-0.012	-0.044
	(0.014)	(0.014)	(0.022)	(0.021)
Autocovariance 8	0.013	0.015	-0.011	0.018
	(0.027)	(0.013)	(0.025)	(0.019)

The most noticable feature in the data is the higher variance in month 1 and the negative autocovariance at lag 4 for the same month. The 1. month is the only one where the constant-within-interview measurement errors do not cancel by differencing. Therefore, these covariances are roughly consistent with a simple model for the measurement error where μ_{ij} is uncorrelated with true income and is serially uncorrelated across interviews.

From (36) it can be seen that the difference of the across and within interview variances is equal to twice the variance of the measurement error. This yields an estimate of σ_{μ}^2 of 0.658. An alternative estimate is given by minus the fourth order autocovariance for month 1 which is 0.501. Optimally combining the sample information results in an estimate of 0.592 with a standard error of 0.024.¹⁵

Given this structure for the constant-within-interview measurement error it is straightforward to calculate the time series structure of the measurement error in the time aggregated quarterly data. The measurement error will follow an MA(2) at the quarterly level. It contributes 5.33 to the variance of measured quaterly income changes (divided by 1000), -1.78 to the first autocovariance, and -1.48 to the second autocovariance. Details are given in Appendix C.

The dynamics of measured income. Measured family income is aggregated into quarterly amounts. The estimation of the quarterly income process proceeds in three further stages. In a first step, I regressed changes in family income on a constant, changes in total family size, changes in the number of children, and age of the head to eliminate deterministic components of income dynamics; these regressors are similar to the ones used by Hall and Mishkin (1982). Separate regressions were run for each quarter. Thus the data will be purged of all common seasonal and aggregate components as well. None of the regressors explains income changes very well; as is usual in such regressions the R²s range from only 0.002 to 0.008!

The second step was to estimate the unrestricted covariance matrix of residual income changes. Table 3 displays this 9 x 9 matrix. The standard deviations of quarterly family income changes range from \$2,931 to \$3,353. The mean level of per capita family income is \$7,278. The standard deviations are between 40 and 46 percent of the income level, this is at the upper end of the range found by MaCurdy and Abowd and Card on annual data.

¹⁵ Formally, the restrictions implied by this simple model for the measurement error are rejected by the data. The covariances are estimated rather precisely due to the relatively large sample size. Obviously, there are other implications of the data that are neglected here. For example, table 2 shows that the variance of monthly income changes increases towards the end of the interview, maybe indicating better recall of changes in the income stream for the more recent months.

	Table 3								
	Covariance Matrix of Income Changes								
				(Incom	ne / 1000)				
			(stand	dard error	s in parer	theses)			
	84:1	84:2	84:3	84:4	85:1	85:2	85:3	85:4	86:1
84:1	10.321 (0.763)	-0.254	-0.126	-0.101	0.047	-0.039	-0.026	0.006	0.044
84:2	-2.390 (0.362)	8.592 (0.507)	-0.290	-0.168	-0.001	0.040	0.013	-0.039	-0.023
84:3	-1.207 (0.345)	-2.538 (0.406)	8.937 (0.625)	-0.236	-0.197	0.002	0.036	-0.064	-0.002
84:4	-1.023 (0.329)	-1.554 (0.331)	-2.233 (0.357)	9.978 (0.687)	-0.355	-0.142	-0.080	0.103	-0.026
85:1	0.510 (0.331)	-0.009 (0.304)	-1.971 (0.290)	-3.758 (0.554)	11.249 (0.720)	-0.306	-0.132	-0.036	0.058
85:2	-0.369 (0.228)	0.350 (0.237)	0.021 (0.216)	-1.332 (0.222)	-3.044 (0.354)	8.792 (0.461)	-0.245	-0.188	-0.013
85:3	-0.247 (0.213)	0.112 (0.201)	0.321 (0.233)	-0.755 (0.219)	-1.322 (0.249)	-2.175 (0.286)	8.954 (0.462)	-0.259	-0.171
85:4	0.068 (0.240)	-0.376 (0.200)	-0.621 (0.211)	1.066 (0.242)	-0.395 (0.289)	-1.815 (0.244)	-2.528 (0.295)	10.641 (0.631)	-0.326
86:1	0.472 (0.263)	-0.219 (0.214)	-0.024 (0.274)	-0.269 (0.246)	0.647 (0.283)	-0.124 (0.257)	-1.692 (0.241)	-3.511 (0.497)	10.884 (0.717)
Covarian	Covariances below the diagonal, correlations above the diagonal								

The first column in table 4 presents minimum distance estimates where the diagonals of the above covariance matrix are restricted to have constant elements.¹⁶ The first two autocorrelations are large in absolute value and comparable to the estimates for annual earnings. Since time aggregation of ARMA processes does not have this feature measurement error may be responsible for this finding. Beyond the second lag, the autocorrelations are closer to zero but some are still significant. The positive values at the 4th and 8th lag stick out. These may indicate that there are seasonal components at the individual level in these data. A look at table 3 shows

^{16 1} initially estimated covariances. The standard errors on the reported autocorrelations are obtained by the delta method.

that the 4th order autocorrelation is particularly large in the 4th quarter. Differing seasonal employment patterns in the last quarter, e.g. in construction versus retail trade, may be an explanation.

Stationary	Table 4 Processes for In	come Changes	
(star	dard errors in pa	rentheses)	
Coefficient	stationary process	MA(3)	MA(2)
Standard Deviation	2951 (45.5)	2900 (44.4)	2893 (23.6)
1st autocorrelation	-0.274 (0.009)	-0.271 (0.009)	-0.270 (0.009)
2nd autocorrelation	-0.169 (0.012)	-0.162 (0.012)	-0.182 (0.010)
3rd autocorrelation	-0.042 (0.012)	-0.025 (0.010)	
4th autocorrelation	0.058 (0.013)		
5th autocorrelation	-0.019 (0.012)		
6th autocorrelation	-0.029 (0.014)		
7th autocorrelation	-0.007 (0.017)		
8th autocorrelation	0.046 (0.026)		
Specification test χ ² -statistic [dof] p-value	60.2 [36] 0.007	82.8 [41] 0.000	89.4 [42] 0.000
Test for Stationarity χ^2 -statistic [dof] p-value		38.3 [26] 0.056	30.8 [21] 0.077

The specification test at the bottom of table 4 also reveals that the data is not very happy with the stationarity restrictions; there are significant differences in the variances and autocorrelations over the year. Income changes are less variable in summer as can be seen in table 3. These findings are indicative of possible deterministic components in household income changes, i.e.

changes that occur with some regularity but not in the same direction for every household. Compared to the short term dynamics in income changes as captured in the first two autocorrelations these regularities do not seem overly large. Lacking any identifying information on deterministic income changes and for reasons of tractability I will work with a stationary MA(2) model for income changes. The test in the last row of table 4 indicates that stationarity is not the major problem given higher order autocorrelations are restricted to zero.

The micro income process. Using the results in the last column of table 4 together with the results on constant-within-interview measurement error yields a standard deviation of "true" income changes of \$1,743. This implies a ratio of true variance to total variance of 0.36, a value substantial below the finding of about 0.65 reported by Bound et.al. (1989) from various validation studies for annual earnings. The standard deviation above has to be divided by average family size (3.03) to make it comparable to the per capita income results from aggregate data used below. Furthermore, I adjust it by the average of the CPI for urban consumers (base 1982-84) over the sample period (which is 105.3). This yields a standard deviation of \$546 which should be compared to a level of real per capita quaterly income of \$2,278 in these data. Making the appropriate adjustments for measurement error for the first and second autocorrelations yields values of -0.160 and -0.014, respectively. Practically all the second order autocorrelation is due to measurement error.

The parameters for an MA(2) process for the idiosyncratic component of income can be recovered easily from these autocorrelations. The estimate of the standard deviation of the income innovation is \$538 per family member per quarter. The MA coefficients are -0.167 and -0.014. According to these estimates income surprises are large and contain a substantial transitory component even after accounting for measurement error. As I have pointed out above, heterogeneity in the individual income process and income fluctuations known to the individual may bias these estimates. I present evidence below that this does not affect the conclusions very much as far as it leads to an overestimate of the individual income variance while the results are less robust to changes in the autocorrelations.

7. Aggregate Stylized Facts on Income and Consumption

In this section I report the stylized facts pertaining to income and consumption processes in aggregate data. This has two purposes. First, I will try to establish some simple time series model for the aggregate income process. Together with the results of the previous section this will allow me to calculate predictions from the model with heterogeneous agents for aggregate consumption. I will therefore also report results on consumption here to compare them to the predictions in the following section.

In order to replicate the results often cited in the literature I make the same adjustments to the NIPA data as Blinder and Deaton (1985) did.¹⁷ My sample ranges from the first quarter of 1954 to the fourth quarter of 1990, the data are taken from the 1991 Citibase tape. A detailed description of the adjustments I make is given in Appendix B.

Table 5 presents results on the income process. The income series refers to "labor" income, i.e. disposable income excluding capital income. There is a slight conceptual difference to the micro estimates since the aggregate income series excludes taxes. However, whether taxes are excluded or not makes little difference for the aggregate estimates. I therefore use the series commonly used in the literature. As for individual income I will use an MA(2) model for the first differences of aggregate income but I also present results for an AR(1). The MA coefficients are estimated by conditional least squares,¹⁸ the AR model is estimated by OLS. I report results for two different sample periods. 1954 to 1984 is the period of the Binder and Deaton (1985) dataset that has been used extensively by various researchers. Notice that extending the sample to 1990 reduces the autocorrelation in the income changes slightly. Both the AR(1) and the MA(2) fit the data well. The quarterly standard deviation for aggregate per capita income is only around \$15, compared to the \$500 I found for the individual income component above!

¹⁷ Unlike Blinder and Deaton (1985) I did not adjust income and consumption for nontax payments to state and local governments since the series on Citibase is only available starting in 1958. For the post-1958 sample the difference is completely inconsequential.

¹⁸ This ignores the fact that initial values are assumed rather than derived from data when filtering the process for the MA innovations.

Table 5 Aggregate Stylized Facts on First Differences of Income (standard errors in parentheses)				
	AR (1)		MA(2)	
Sample Period		First coefficient	Second coefficient	Std. Dev. of Income Innovations
NIPA 1954-1984	0.368 (0.083)	0.392 (0.090)	0.022 (0.090)	16.1 (1.02)
NIPA 1954-1990	0.307 (0.079)	0.309 (0.083)	0.023 (0.083)	17.0 (0.99)

Table 6 reports some results on aggregate consumption for similar sample periods as the previous table. It has been customary in the macro literature to use consumer expenditure on nondurables and services as consumption measure. Like Blinder and Deaton I eliminated expenditures on clothing and shoes from the nondurable consumption series. To make units comparable to total income I multiplied these expenditures by the sample average of the ratio of total expenditures to expenditures on nondurables and services.

Aggre	gate Stylized Fac (standar	Table 6 ets on First Diffe et errors in parent	rences of Consu ntheses)	mption
Sample Period	Coef. of Consumption Changes on Income Lag	AR (1) coefficient	MA (1) coefficient	Excess Smoothness Ratio
1954-1984	0.138	0.225	0.220	0.583
	(0.047)	(0.087)	(0.088)	(0.060)
1954-1990	0.131	0.230	0.249	0.562
	(0.043)	(0.081)	(0.081)	(0.052)

The table reports the regression coefficient of consumption changes on lagged income changes which is in the order of 0.13 and clearly significant. Consumption changes are positively

autocorrelated as measured by an AR(1) or MA(1) parameter. The last column gives the excess smoothness ratio of about 0.6. All these estimates are in line with previous findings in the literature.

8. Predictions from the Model

I am now ready to present predictions from the models using the empirical estimates for the individual and aggregate parts of the income process. To check the robustness of the results I will present a number of cases.

I assume that both the individual income process and the aggregate income process are described by an MA(2) in first differences.

$$\Delta y_{it} = (1 + \phi_1 L + \phi_2 L^2)\varepsilon_t + (1 - \alpha_1 L - \alpha_2 L^2)u_{it}$$

= $(1 - \theta_1 L - \theta_2 L^2)\eta_{it}$ (37)

The consumption processes for the two models are given in (29) and (33) respectively. In the case of the no information model aggregate consumption follows an ARIMA(2,1,2) process. For the lagged information model, consumption changes are an MA(1). The formulas for β the coefficient for a regression of consumption changes on lagged income changes can be found in (34) and in Appendix A. The variance of consumption changes is easily obtained from (29) and (33).

Predictions for these parameters are shown in table 7 and compared to the aggregate stylized facts about consumption from table 6. The base case uses the estimates for the individual income process adjusted for measurement error as described in section 6 and the 1954 - 1990 results for aggregate income. Both the no information model and the lagged information model predict both parameters qualitatively correctly. Quantitatively, the results for the two models do not differ much in the base case; both overpredict β and $\sigma_{4c}/\sigma_{\epsilon}$ by about a factor of two.

Table 7 Comparison of Model Predictions and Aggregate Estimates							
	Aggregate Estimates No Information Model		Lagged Information Model		Utility Loss		
Case	β	$\sigma_{\Delta c}/\sigma_{\epsilon}$	β	$\sigma_{\Delta c}/\sigma_{\epsilon}$	β	$\sigma_{\Delta c}/\sigma_{\epsilon}$	[\$/quarter]
base	0.131	0.565	0.384	0.915	0.468	0.968	0.070
2	0.138	0.583	0.434	0.947	0.515	1.014	0.085
3	0.131	0.565	0.298	0.529	0.898	1.046	0.544
4	0,131	0.565	0.288	1.047	0.303	1.054	0.029
5	0.131	0.565	0.383	0.916	0.466	0.968	0.070
Base case: $\sigma_{u} = 538 , $\alpha_{1} = 0.167$, $\alpha_{2} = 0.014$, $\sigma_{e} = 16.99 , $\phi_{1} = 0.309$, $\phi_{2} = 0.023$, interest rate = 0.01, mean income = \$2,278, coef. of rel. risk aversion = 2 Case 2: As base case but $\sigma_{e} = 16.10 , $\phi_{1} = 0.392$, $\phi_{2} = 0.022$ Case 3: As base case but $\sigma_{u} = 814 , $\alpha_{1} = 0.431$, $\alpha_{2} = 0.225$ Case 4: As base case but $\sigma_{u} = 814 , $\alpha_{1} = 0.431$, $\alpha_{2} = 0.225$ Case 5: As base case but $\sigma_{u} = 269							

The last column presents the per capita utility loss for a household that uses no aggregate information compared to the full information case.¹⁹ The loss is expressed in Dollars per quarter and calculated for a coefficient of relative risk aversion of two. It amounts to 7 cents or 0.003 percent of total utility. This is similar to the findings by Cochrane (1989) who estimated the utility loss for a representative consumer exhibiting excess sensitivity. The loss for higher risk aversion is easily obtained by dividing by two and multiplying by the new coefficient. Even for a risk aversion coefficient of 10 the loss would still be minor. This provides some evidence that the assumptions of the no information model seem to be quite reasonable: it does not pay to collect aggregate information to improve consumption decisions.

The next rows present slight changes to the base case. Case 2 uses the aggregate estimates for the 1954 - 1984 period; the results are very similar. Case 3 presents calculations with the micro income process without adjustment for measurement error. The results in this case are much

¹⁹ Instead of comparing the model with no information to the Goodfriend model I use a model with full contemporaneous information on aggregate variables as benchmark. Utility for this model is calculated much more easily than for the lagged information model. The utility differences I present are therefore upper bounds for the differences between the two models in the paper. See Appendix D for details on the calculations.

more favorable to the no information model since the larger transitory component lowers the variability of consumption. Since the difference between the individual and aggregate income process is greater the utility loss from not having aggregate information is also larger.

Cases 4 and 5 investigate the possible implications for the model if the variance and transitory nature of the individual income process is overstated. Case 4 presents the results under the assumption that the mean reversion in individual income is spurious and the true process is a random walk. This lowers the predictions of β slightly and changes the excess smoothness ratio little. The last case uses only a half the standard deviation for individual income innovations compared to the base case. This change leaves the predictions of the models practically unaltered. Hence, this sensitivity analysis indicates that changing the variance of individual income changes affects the results very little while changes in the income dynamics can have a substantial impact. In the no information model the excess smoothness ratio is affected in particular, in the lagged information model the regression coefficient is more sensitive.

Since these results only pertain to the most simple minded version of a life-cycle consumption model it is not surprising that the results do not match the data more closely. But it becomes clear that incomplete information may play an important role in explaining excess sensitivity and excess smoothness at the aggregate level.

9. Concluding Comments

In this paper I have analyzed the implications of heterogeneity in income and incomplete information on the source of income shocks for the form of the aggregate consumption process and its relation to observed income. The failures of the full information life-cycle consumption model usually found in aggregate data clearly arise if individual consumers adjust their consumption correctly to individual income innovations but do not care to distinguish aggregate and idiosyncratic income variation. Using estimated parameter values for individual and aggregate income processes, the model gives predictions that deviate substantially from the full information benchmark. However, the results indicate too much correlation of consumption

changes with lagged income but not smooth enough consumption. Nevertheless, heterogeneity in income and incomplete information seem to account for a large portion of the deviations from the full information case.

Rational expectations models with incomplete aggregate information have mostly used the assumption that aggregate information arrives with a one period lag. In the present context, the no information model seems to yield somewhat better results than the lagged information model but does not clearly dominate it. Some combination of the two models will probably improve the predictions and certainly seems more reasonable as a description of reality. Consumers may not deliberately collect aggregate information. But their interaction with many other individuals will reveal a lot to them about the nature of their own income process. Formalizing models in which aggregate information arrives more slowly should be an area that deserves more attention.

The feature that drives the results in this paper is that the model yields an autocorrelated process for aggregate consumption changes. Galí (1991) has shown that excess smoothness of consumption can be characterized in the frequency domain with less restrictive assumptions than in Deaton (1987) or Campbell and Deaton (1989). Essentially, his results stem from the autocorrelation in consumption changes and are therefore consistent with the predictions from the no information model.

A number of other models have been suggested that lead to autocorrelated consumption. A simple model of habit formation (Deaton, 1987) or slow adjustment of consumers to income shocks (Attfield, Demery, and Duck, 1992) also leads to an AR(1) for consumption changes. Unlike for the models studied here, the micro parameters are generally not estimable in these cases so the models cannot be subjected to the same stringent test. Furthermore, these models imply that consumption should have the same autocorrelation structure in micro and in aggregate data. This seems to be at odds with the empirical findings.

Although in this paper I have focussed on implications of the no information model for aggregate data the model is roughly consistent with previous findings on micro data for consumption. It predicts correctly that the orthogonality conditions should not be rejected in panel data. The approach taken by Altonji and Siow (1987), Zeldes (1989) and Runkle (1991) is consistent with the model presented here. These studies find little evidence against the permanent income model

with food consumption data from the PSID. The exception is Zeldes (1989), who finds some evidence for such correlations for low wealth consumers in the PSID, interpreting them as liquidity constraints.

It seems quite reasonably a priori that part of the population is liquidity constraint. Interactions of liquidity constraints and precautionary savings motives with the incomplete information assumption are considered in Deaton (1991). In numerical simulations Deaton finds a regression coefficient of consumption growth on lagged income growth of 0.42 and a smoothness ratio just below one. His results are for logs of the variables and are therefore not directly comparable to mine. Nevertheless, it seems that incomplete information may be the major factor driving these results.

Since the specifications in this paper are very restrictive future research should incorporate incomplete information into more sophisticated models. Finite lifetimes and advance information of consumers about income changes are possible candidates that may play an important role in bringing the results presented here better in line with the data.

Appendix A Derivation of Conditions for Excess Smoothness

Let $\beta \equiv 1/(1+r)$ and use (3) and (25) so that excess smoothness in the aggregate is given by $\sigma_{A_r}^2 < \phi^2(\beta)\sigma_e^2$ or

$$\Psi \equiv \frac{\sigma_{\Lambda c}^2}{\phi^2(\beta)\sigma_c^2} < 1 \tag{A1}$$

Consider the no information case. Using (29) in the text the spectral density of aggregate consumption changes is

$$h_{\Delta c}(\omega) = \frac{A^2(\beta)}{2\pi} \frac{|\phi(e^{-i\omega})|^2}{|A(e^{-i\omega})|^2} \sigma_{\varepsilon}^2$$
(A2)

The variance of consumption changes can be found by integrating (A2)

$$\sigma_{\Delta c}^{2} = \int_{-\pi}^{\pi} h_{\Delta c}(\omega) \, d\omega = \int_{-\pi}^{\pi} \frac{A^{2}(\beta)}{2\pi} \frac{|\phi(e^{-i\omega})|^{2}}{|A(e^{-i\omega})|^{2}} \, \sigma_{\varepsilon}^{2} \, d\omega \tag{A3}$$

so that the quanity Ψ is given by

$$\Psi = \frac{1}{2\pi} \frac{A^{2}(\beta)}{\phi^{2}(\beta)} \int_{-\pi}^{\pi} \frac{|\phi(e^{-i\omega})|^{2}}{|A(e^{-i\omega})|^{2}} d\omega$$
$$= \frac{1}{2\pi} \frac{A^{2}(\beta)}{\phi^{2}(\beta)} \frac{\sigma_{\eta}^{2}}{\sigma_{\epsilon}^{2}} \int_{-\pi}^{\pi} \frac{h_{\phi}(\omega)}{h_{A}(\omega)} d\omega$$
$$= \frac{1}{2\pi} \frac{A^{2}(\beta)}{\phi^{2}(\beta)} \frac{\sigma_{\eta}^{2}}{\sigma_{\epsilon}^{2}} \frac{\sigma_{Ay}^{2}}{\sigma_{Ay}^{2}} \int_{-\pi}^{\pi} \frac{f_{\phi}(\omega)}{f_{A}(\omega)} d\omega$$
(A4)

where $f_x(\omega) = h_x(\omega)/\sigma_x^2$ is the normalized spectral density of process x. Taking limits as the interest rate approaches zero gives the following expression which appears as (30) in the text:

$$\lim_{r \to 0} \Psi = \frac{1}{2\pi} \frac{f_A(0)}{f_{\phi}(0)} \int_{-\pi}^{\pi} \frac{f_{\phi}(\omega)}{f_A(\omega)} d\omega$$
(A5)

Now turn to the lagged information model. From (33)

$$\frac{\sigma_{\Delta c}^2}{\sigma_{\epsilon}^2} = \left[\phi(\beta)\omega + \theta(\beta)(1-\omega)\right]^2 + (1+r)^2 \left[\phi(\beta) - \theta(\beta)\right]^2 (1-\omega)^2 \tag{A6}$$

Using condition (A1) and letting interest rates get small we obtain

$$\Rightarrow [\phi(1)\omega + \theta(1)(1-\omega)]^{2} + [\phi(1) - \theta(1)]^{2}(1-\omega)^{2} < \phi^{2}(1)$$
(A7)

Define $K(\omega) \equiv [\phi(1) - \theta(1)]\omega + \theta(1)$ which will be positive given $\phi(1) > \theta(1) > 0$. The latter inequality holds if $\theta(z)$ is invertible. Notice that (A7) can be rewritten as

 $\lim \Psi < 1$

$$K^{2}(\omega) + [\phi(1) - K(\omega)]^{2} < \phi^{2}(1)$$
(A8)

Thus we have to show that (A8) is satisfied. Use $\phi(1) > \theta(1)$, multiply both sides by $1 - \omega$ and rearrange to get

$$K(\omega) = [\phi(1) - \theta(1)]\omega + \theta(1) < \phi(1) \tag{A9}$$

Recall that $K(\omega)$ is positive, multiply both sides of (A9) by twice $K(\omega)$ and add $\phi(1)^2$ to complete the square. Rearranging yields (A8) which completes the proof.

Empirical Formulation. In the empirical model in section 8 both the aggregate and the individual income component are described by an MA(2). Then $A(L) = 1 + a_1L + a_2L^2$. The roots of this polynomial are defined by $\mu^2 + a_1\mu + a_2 = 0$. Writing consumption changes in its series representation.

$$\Delta c_{t} = \frac{A\left(\frac{1}{1+r}\right)}{\mu_{1}-\mu_{2}} \sum_{i=0}^{\infty} (\mu_{1}^{i+1}-\mu_{2}^{i+1}) (\varepsilon_{t-i}+\phi_{1}\varepsilon_{t-1-i}+\phi_{2}\varepsilon_{t-2-i})$$
(A10)

This can be used to derive the regression coefficient of consumption changes on lagged income changes

$$\begin{split} \beta &= \frac{A\left(\frac{1}{1+r}\right)}{(\mu_1 - \mu_2)\left(1 + \phi_1^2 + \phi_1^2\right)} \\ \times \{(\mu_1 - \mu_2 + \mu_1^3 - \mu_2^3)\left(\phi_1 + \phi_1\phi_2\right) + (\mu_1^2 - \mu_2^2)\left(1 + \phi_1^2 + \phi_2^2\right) + (\mu_1^4 - \mu_2^4)\phi_2\} \end{split} \tag{A11}$$

The variance of consumption changes can either be found by solving (A3) for the relevant processes or by solving the Yule-Walker equations corresponding to the ARMA(2,2) given by (A10). I have done the latter numerically.

Appendix B Sample Selection and Variable Definitions

Construction of the SIPP Sample. The 1984 Survey of Income and Program Participation was conducted in nine interview waves. Households were interviewed on a rolling basis, starting October 1983 for the first rotation group and ending July 1986 with the last rotation group. For wave 2, rotation group 2 was not interviewed, for wave 8 there is no interview for rotation group 3. In each interview, questions were asked about income for each of the previous four months. Thus monthly income data are available for all rotation groups from September 83 to March 86. Since I intend to construct quarterly observations I started with the October 83 variables.

I started by matching household heads from the nine interview waves. This resulted in 12,874 matches. I then restrict the matched sample as described in the text by selecting continuous heads for the period of analysis, that did not change marital status or their level of schooling in any month. Per capita family income is constructed by subtracting property income (F*-PROP) from total family income (F*TOTINC). Finally, I corrected reported age of the head so that age increments by one every four quarters. The final sample contains quarterly variables from the last quarter in 1983 to the first quarter in 1986. The sample only includes heads that were older than 16 years and younger than 70 years throughout the sample. The final sample has 8,176 observations.

Construction of the Aggregate Series. I created the consumption and income series from the National Income and Product Accounts largely following Blinder and Deaton (1985). The labor income series consists of labor and transfer income (the Citibase Series GW + GPOL + GPT) less social insurance contributions (GPSIN). To subtract the portion of taxes on labor income I created the ratio of wages, salaries and other labor income to income including interest, dividends and rents. Personal tax payments (GPTX) where multiplied by this ratio and the result subtracted from income. Proprietors' income (GPROP) was multiplied by the same ratio before adding it to the income series. Unlike Blinder and Deaton I did not add nontax payments to state and local governments to income and consumption because Citibase only reports this series starting from 1958. Income was adjusted in the second quarter of 1975 by subtracting the tax rebate and social security bonus. The numbers for this adjustment were taken from Blinder (1981), table 2.

The real consumption series is constructed by adding the constant dollar expenditures on nondurables and services and subtracting expenditures on clothing and shoes because these have

rather durable characteristics (GCN82+GCS82-GCNC82). The consumption deflator obtained by dividing the nominal consumption series by the real series is used to deflate income. Both income and consumption are divided by the total population (GPOP).

Finally, to make the scale of the consumption series comparable to the income series it is multiplied by the ratio of total expenditures (GC82) to expenditures on nondurables and services. Quarterly NIPA series are reported at annual rates. I divided all series by four to obtain quarterly amounts.

Appendix C Quaterly Measurement Error Process

The aggregated quaterly observations for income I construct from the SIPP will generally draw information from one or two interviews. Given that an interview covers four months, the three months making up a quarter will be sequences of pairs (0,3), (1,2), (2,1), (3,0), where the first digit indicates the number of months coming from the first interview and the second the months from the next interview. After this sequence the pattern repeats. Due to the rotation group design, each pair will be represented about equally each quarter. The following table indicates how the process for observed quarterly income changes looks when the monthly observations pertain to each of the four possible patterns.

Income	Table C1 Income Processes and Interview Structure			
Interview Overlap	Income Process			
(0,3)	$\Delta y_{ii} = \Delta y_{ii}^* + 3\mu_{ij} - 3\mu_{ij-1}$			
(1,2)	$\Delta y_{ii} = \Delta y_{ii}^* + 2\mu_{ij} - 2\mu_{ij-1}$			
(2,1)	$\Delta y_{ii} = \Delta y_{ii}^* + \mu_{ij} - \mu_{ij-2}$			
(3,0)	$\Delta y_{ii} = \Delta y_{ii}^* + 2\mu_{ii} - 2\mu_{ii-1}$			

Starred income variables in table C1 refer to true income plus variable-within-interview measurement error. The subscript *t* refers to quarters, *j* to interviews. Since the measurement error is uncorrelated across interviews and with true income, this yields the following variances and autocovariances. The calculations given in the rows labeled "average" are based on a value of 0.592 for σ_{μ}^2 . All autocovariances beyond the second are zero.

	Table C2 Quaterly Variances and Autocovariances and Interview Structure
Interview Overlap	Covariance
(0,3)	$var(\Delta y_{ii}) = var(\Delta y_{ii}^*) + 18\sigma_{\mu}^2$
(1,2)	$var(\Delta y_{ii}) = var(\Delta y_{ii}^*) + 8\sigma_{\mu}^2$
(2,1)	$var(\Delta y_{ii}) = var(\Delta y_{ii}^*) + 2\sigma_{\mu}^2$
(3,0)	$var(\Delta y_{ii}) = var(\Delta y_{ii}^*) + 8\sigma_{\mu}^2$
average	$var(\Delta y_{ii}) = var(\Delta y_{ii}^{*}) + 9\sigma_{\mu}^{2} = var(\Delta y_{ii}^{*}) + 5.33$
(0,3)	$cov(\Delta y_{it}, \Delta y_{it-1}) = var(\Delta y_{it}^*, \Delta y_{it-1}^*) - 6\sigma_{\mu}^2$
(1,2)	$cov(\Delta y_{it}, \Delta y_{it-1}) = var(\Delta y_{it}^*, \Delta y_{it-1}^*) - 6\sigma_{\mu}^2$
(2,1)	$cov(\Delta y_{it}, \Delta y_{it-1}) = var(\Delta y_{it}^*, \Delta y_{it-1}^*) + 2\sigma_{\mu}^2$
(3,0)	$cov(\Delta y_{it}, \Delta y_{it-1}) = var(\Delta y_{it}^*, \Delta y_{it-1}^*) - 2\sigma_{\mu}^2$
average	$cov(\Delta y_{it}, \Delta y_{it-1}) = var(\Delta y_{it}^*, \Delta y_{it-1}^*) - 3\sigma_{\mu}^2 = var(\Delta y_{it}^*, \Delta y_{it-1}^*) - 1.78$
(0,3)	$cov(\Delta y_{it}, \Delta y_{it-2}) = var(\Delta y_{it}^*, \Delta y_{it-2}^*) - 3\sigma_{\mu}^2$
(1,2)	$cov(\Delta y_{it}, \Delta y_{it-2}) = var(\Delta y_{it}^{\star}, \Delta y_{it-2}^{\star})$
(2,1)	$cov(\Delta y_{ii}, \Delta y_{ii-2}) = var(\Delta y_{ii}^{\star}, \Delta y_{ii-2}^{\star}) - 3\sigma_{\mu}^{2}$
(3,0)	$cov(\Delta y_{ii}, \Delta y_{ii-2}) = var(\Delta y_{ii}^{*}, \Delta y_{ii-2}^{*}) - 4\sigma_{\mu}^{2}$
average	$cov(\Delta y_{it}, \Delta y_{it-2}) = var(\Delta y_{it}^*, \Delta y_{it-2}^*) - 2.5\sigma_{\mu}^2 = var(\Delta y_{it}^*, \Delta y_{it-2}^*) - 1.48$

Appendix D Calculations of Utility Loss

In this appendix I discuss how to calculate the utility loss the household suffers by ignoring aggregate information in consumption decisions. The basic setup is taken from the appendix in Cochrane (1989, pp. 334-335). The second part gives the matrix representations of the full information model and the no information model used in the utility calculations.

Utility for the quadratic model can be written as

$$U(X_{t}) = E_{t} \sum_{j=0}^{\infty} \beta^{j} X_{t+j} R X_{t+j}$$
(D1)

where $\beta = 1/(1+r)$ and X_i represents the state vector of the system which evolves according to

$$X_{t} = AX_{t-1} + \Gamma\xi_{t}$$

$$E_{t}(\xi_{t+1}) = 0$$

$$E_{t}(\xi_{t}\xi_{t}') = \Sigma$$
(D2)

Equation (D1) can be rewritten as

$$U(X_i) = X_i' P X_i + \frac{1+r}{r} \operatorname{Trace}(P \Gamma \Sigma \Gamma')$$
 (D3)

where

$$P = R + \beta A' P A \tag{D4}$$

P will be a symmetric matrix; therefore (D4) cannot be solved directly for P. Cochrane shows, however, that

$$M\operatorname{vec}(P) = (I - \beta M(A' \otimes A')N)^{-1} M\operatorname{vec}(R)$$
(D5)

where M is a transformation matrix that deletes the redundant rows of a stacked symmetric matrix and N does the opposite operation, i.e.

$$\operatorname{vech}(P) = M\operatorname{vec}(P)$$

 $N\operatorname{vech}(P) = \operatorname{vec}(P)$

Cochrane uses (D3) and (D5) to solve analytically for $U(X_i)$. Instead, once the model is expressed in the form (D1) and (D2), these equations can easily be used to calculate utility numerically. I took this latter route.

The full information model. Instead of comparing the no information model to Goodfriend's model with lagged information I chose to use a model with full contemporaneous information on aggregate variables as the benchmark. This model will yield higher utility than Goodfriend's. The utility comparisons I present will therefore be upper bounds for the choice relevant to the consumer.

Since all the variables refer to a single household and the distinction between aggregate and individual variables is not important here I suppress i subscripts for notational convenience. Income in the full information model is given by the first line of (37) in the text.

$$\Delta y_t = (1 + \phi_1 L + \phi_2 L^2)\varepsilon_t + (1 - \alpha_1 L - \alpha_2 L^2)u_t \tag{D6}$$

Optimal consumption is given by

$$c_{t} = \frac{r}{1+r} \left[A_{t} + \sum_{i=0}^{\infty} \frac{E_{i} y_{t+i}}{(1+r)^{i}} \right]$$
$$= \frac{r}{1+r} A_{t} + y_{t} + \left[\frac{\phi_{1}}{1+r} + \frac{\phi_{2}}{(1+r)^{2}} \right] \varepsilon_{t} + \frac{\phi_{2}}{1+r} \varepsilon_{t-1} - \left[\frac{\alpha_{1}}{1+r} + \frac{\alpha_{2}}{(1+r)^{2}} \right] u_{t} - \frac{\alpha_{2}}{1+r} u_{t-1} \quad (D7)$$

and assets follow

$$A_{t} = (1+r)[A_{t-1} + y_{t} - c_{t}]$$

= $A_{t-1} - \left[\phi_{1} + \frac{\phi_{2}}{1+r}\right]\varepsilon_{t-1} - \phi_{2}\varepsilon_{t-2} + \left[\alpha_{1} + \frac{\alpha_{2}}{1+r}\right]u_{t-1} + \alpha_{2}u_{t-2}$ (D8)

Define the state vector as

$$X_{t} = [1 \ A_{t} \ y_{t} \ \varepsilon_{t} \ \varepsilon_{t-1} \ u_{t} \ u_{t-1}]'$$
(D9)

Using (D7) and (D9) we can write

$$c_t - \overline{c} = \left[-\overline{c} \quad \frac{r}{1+r} \quad 1 \quad \frac{\phi_1}{1+r} + \frac{\phi_2}{(1+r)^2} \quad \frac{\phi_2}{1+r} \quad -\left[\frac{\alpha_1}{1+r} + \frac{\alpha_2}{(1+r)^2} \right] \quad -\frac{\alpha_2}{1+r} \right] X_t \equiv F' X_t \quad (D10)$$

Then R in (D1) is given by

$$R = -\frac{1}{2}FF' \qquad (D11)$$

The transition equation for the system in (D2) becomes

The no information model. The income process to the household in the no information model looks like

$$\Delta y_{\mu} = (1 - \theta_1 L - \theta_2 L^2) \eta_t \tag{D13}$$

Consumption is given by

$$c_{t} = \frac{r}{1+r}A_{t} + y_{t} - \left[\frac{\theta_{1}}{1+r} + \frac{\theta_{2}}{(1+r)^{2}}\right]\eta_{t} - \frac{\theta_{2}}{1+r}\eta_{t-1}$$
(D14)

and assets follow

$$A_{t} = A_{t-1} + \left[\theta_{1} + \frac{\theta_{2}}{1+r}\right]\eta_{t-1} + \theta_{2}\eta_{t-2}$$
(D15)

Define the state vector as

$$X_{t} = [1 \ A_{t} \ y_{t} \ \eta_{t} \ \eta_{t-1}]' \tag{D16}$$

Using (D14) and (D16)

$$c_t - \overline{c} = \left[-\overline{c} \quad \frac{r}{1+r} \quad 1 \quad -\left[\frac{\theta_1}{1+r} + \frac{\theta_2}{(1+r)^2} \right] \quad -\frac{\theta_2}{1+r} \right] X_t \equiv F' X_t \tag{D17}$$

The transition equation becomes

$$\begin{bmatrix} 1\\A_{i}\\y_{i}\\\eta_{i}\\\eta_{i-1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0\\0 & 1 & 0 & \theta_{1} + \frac{\theta_{2}}{1+r} & \theta_{2}\\0 & 0 & 1 & -\theta_{1} & -\theta_{2}\\0 & 0 & 0 & 0 & 0\\0 & 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1\\A_{i-1}\\y_{i-1}\\\eta_{i-2} \end{bmatrix} + \begin{bmatrix} 0\\0\\1\\1\\0 \end{bmatrix}$$

$$(D18)$$

Once both models have been solved for the level of utility attained the utility difference is converted to quarterly rates by multiplying by r/(1+r). To convert the utility loss to dollar terms divide the utility loss by the expected value of marginal instantaneous utility

$$s \log / quarter = \frac{r}{1+r} \frac{\Delta U}{Eu'(c_i)} = \frac{r}{1+r} \frac{\Delta U}{(\overline{c}-\overline{y})} = \frac{r}{1+r} \frac{\gamma \Delta U}{\overline{y}}$$
(D19)

where γ is the coefficient of relative risk aversion. The calculations in the paper are for a coefficient of relative risk aversion of two and a mean income level of \$2,278.

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