

# Flexible versus Designated Technologies and Inter-Fuel Substitution

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## Abstract

Zero demands for some types of energy are frequently observed in firm level data sets. To deal with this problem, two alternative solutions are retained in the literature: firstly, it can be assumed that the consumption of some kinds of energy is not allowed by the existing technology; secondly one can suppose that firms decide to use only some of the different kinds of energy allowed by the technology. In this paper we estimate the inter-fuel substitutions resulting from these two different situations. We take into account that increasing the price of an energy form possibly modifies the number of energy used by the firm. We show that even in this case an estimation of the elasticity of substitution can be obtained. The empirical results are based on a French manufacturing energy consumption survey.

**Key words :** Energy demand, Censored regression, Inter-fuel substitution

**JEL Classification :** 022, 212, 631, 723

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# 1 Introduction

Firm-level panel data sets reveal a salient feature of energy consumption: the great variability of energy uses. Examples of this variability include simultaneous adoption and abandon of some energy forms and large differences in the level of energy consumption over time and across firms. This heterogeneous behavior of firms with regards to energy consumption is observed even when relatively homogenous populations of firms are considered such as firms in the same industry.

Most of the published research on industrial energy demand makes use of aggregated data. Among them the most often cited are Fuss (1977), Griffin (1977), Halvorsen (1977), Pindyck (1979), Hall (1983) and Magnus and Woodland (1987).

Studies making use of individual data have most often focused on the residential sector (see Madlener (1996) for a survey). While demand theory commonly deals with situations where the demand is continuously variable, empirical works on residential energy demand are based on continuous-discrete choice models (Dubin and McFadden (1984)). In this framework, the discrete fuel choice involves comparisons of indirect utility attached to various fuel systems. Consistent with the theory of consumer behavior, continuous equation describing energy use are derived from the indirect utility function by using Roy's identity (Hanemann (1984)). For industrial energy demand the difficulty is similar but more severe because firms choose different fuel patterns (i.e. different combinations of different types of energy). As noted by Woodland (1993), the possibility of corner solutions leading to one or more zero values of some types of energy, can occur as a result of two alternative situations. First, different fuel patterns are determined by previous technology choice. In that case, for a given technology, some energy forms are required while other are not allowed. Firm behavior in the short run is restricted to the subset of energy forms allowed by firms' technology. Later in the paper we will call such a case "designated technology" where zero demand are the result of an exogenous rationing<sup>1</sup>. This is precisely the hypothesis assumed by Woodland (op.cit.) who estimates "conditional" production functions, that means as many production functions as significantly observed fuel patterns. Assuming that fuel patterns are the result of technological constraints, Bjorner and Jensen (2002) follow the same approach.

The second approach considers that zero consumptions may instead be the result of cost minimization behavior leading to a corner solution. In this framework all types of energy can potentially be used since the technology is flexible enough to allow substitutions between energy forms. This case

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<sup>1</sup> Given previous choice about the technology, ex-post the firm is like in a situation of exogenous rationing as some energy forms are not used whatever the level of energy prices.

will be called hereafter "flexible technology"; zero demand is the result of an endogenous rationing. Both multiple-reduced equipment and redundant or backup equipment can contribute to the switching capabilities between different kinds of energy. Then, if there is no switching costs, one or more energy forms cannot be used when their prices are sufficiently high relative to their marginal contribution to output. Lee and Pitt (1987) and more recently, Bousquet and al (1989) and (1998) develop such a model and apply it on individual firms' data.

The objective of this paper is to compare the differences in estimated inter-fuel substitution possibilities as measured under the two alternative assumptions about the energy technology leading to an energy demand system with ex-post exogenous or endogenous rationing.

In section 2 we present the data base used in the econometric analysis. The two possible assumptions about energy technology are discussed in light of some empirical evidence. Section 3 deals with the two theoretical models and shows how significant is the difference between the two modelling approaches. Section 4 and 5 are finally devoted to the empirical part of the analysis.

## 2 Heterogeneity in energy technology

Depending on energy market conditions and plant characteristics, energy technologies differ by their input requirement set. The energy technology is a varied collection of equipment, like boilers, ovens, heating apparatus, power engines, steam generators, ... designed to consume a single fuel or a combination of fuels. As a result, a given energy technology allows for a certain fuel substitution capability.

As noted by Doms(1993) the literature on energy technology for manufacturing plants is scant. Without knowledge about plant's energy technology characteristics and the link with energy use, it is nevertheless possible to consider two extreme assumption corresponding to either designated or flexible technology. It is then possible to explore one aspect of the manufacturing response to shocks in energy price and to highlight the importance of technology assumptions made in energy demand modelling.

### 2.1 Data description

The data set for this study is a cross-section of establishments built from the "Enquête Annuelle sur les Consommations d'Energies de l'Industrie". A general description of the energy survey and global statistics about energy consumption in the french industry are provided in the annual publication of the Ministère de l'Industrie (see SESSI (1997)). The data set includes approximately 13,000 observations. The survey reports energy consumptions for 11 kinds of energy (3 types of coal or coke, 3 types of gas, 2 types of oil,

electricity, heating, and others energies like wood, wastes,...). The quantity of energy consumed is measured in toe and in current Euro. Then, the energy prices are obtained by calculating the ratio of values over quantities. That means that prices in our data set are average prices over one year.<sup>2</sup> It should be recognized that average prices could be endogenous due to decreasing block pricing in relation with quantity consumed. But taking into account price endogeneity needs more information on ...rm's characteristics than we have. Moreover, prices does not depend on quantities consumed only, many other factors play an important role. Among them, peak-load pricing and transportation costs are certainly the most important. But, in a short term perspective, they can be considered as exogenous since ...rm's location is given, as well as wether or not the ...rms work in twenty four hours shifts. Finally, as pointed out by Pudney (1989), in large samples, average prices could be considered as approximately exogenous.

In the current study we focus on the substitution between three different energy inputs:

- <sup>2</sup> gas, a composite good including natural gas and liquefied petroleum gas (LPG);
- <sup>2</sup> oil products, a composite good including heavy oil and domestic fuel oil;
- <sup>2</sup> electricity.

To measure electricity consumption by ...rms, we use electricity purchases; therefore, the own-production of electricity by ...rms is not taken into account in our study. Note that only 5% of plants produce electricity by their own.

We neglect ...rms that use coal, heating and other energy, since they are very few. The ...nal sample used for estimation includes 12745 observations.

From table 1 we can deduce the percentage of ...rms using a given form of energy. While all ...rms use electricity, only one half of the sample use oil and less than two third use gas.

One group of ...rms uses all the three types of energy. This group represents less than one third of plants in the industry. Note that, as a consequence, zero expenditure observations frequently occur in our sample. The major pattern is a mix between gas and electricity. The case where electricity is the only fuel or energy source used represents a significant proportion of the sample (see table 1).

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<sup>2</sup>Of course, prices are not observable when a zero demand occurs.

Table 1: Frequency of fuel patterns

Fuel pattern	Frequency
gas, oil and electricity	27%
gas and electricity	38%
oil and electricity	21%
electricity	14%

## 2.2 Fuel pattern and assumption about the energy technology

Bjorner and Jensen (2002) observe that companies over time do not change frequently from one fuel pattern to another, and use this finding to justify the Woodland approach, assuming that fuel patterns are given in the short term. The point of view is different in the empirical study of Doms (1993), who shows clearly that firms could change rapidly their energy technologies and that a significant part of the technologies are flexible. Moreover, the analysis based on the U. S. Manufacturing Energy Consumption Survey (henceforth MECS, see DOE/IEA (1994)), provides empirical evidence about the ability of firms to switch between different kinds of energy in the short run without changing the technology. In 1991, for instance, around 20% of manufacturing plants possess some capability to switch. The same year, the total capability to switch is estimated at 2.8 quadrillion Btu, that is 14% of the primary energy consumption in the manufacturing sector (which amounts to 20.3 quadrillion Btu). If necessary, 20% of Distillate Fuel Oil consumption could be replaced by other energy sources, this proportion is greater than 40% for LPG, coal and residual fuels. Natural gas appears to be an intermediate case with 35%.<sup>3</sup>

This empirical evidence shows that substitution possibilities among energy sources could be very high for a minor but significant part of the industry and energy consumption. Switching capability is an important dimension of heterogeneity in energy technologies. For energy demand modelling the consequence is that Woodland (1993) and Lee and Pitt (1987) are at the same time right and wrong, because a zero consumption for one kind of energy can be the result of an ex-post exogenous rationing as well as of an endogenous rationing, depending on the characteristics of the energy technology.

<sup>3</sup>For the MECS, manufacturers are said to have a fuel-switching capability if they are able to meet their requirements for heat, power and electricity generation by substituting one energy source for another within 30 days without modifying the equipment that consumes the fuel and resuming the same level of production following the switch.

### 3 Models for inter-fuel substitution

#### 3.1 Main assumptions

Following Hudson and Jorgenson (1974) and Grifin (1977), we assume that the different energy inputs make up a separable and homogeneous energy aggregate. For this study, we are obliged to make this hypothesis since data on other inputs than energy, and output of the firms are unavailable. Stated alternatively, we are making an analysis focusing on substitution possibilities between the different kinds of energy and we do not take into account others forces driving energy demand. The substitution elasticities inside the energy aggregate are independent of inputs prices outside the aggregate and also independent of the production level. These assumptions allow us to estimate separately the unit cost function of energy. Formally our model assumes that the cost function is weakly separable between energy and the others inputs.

The final step toward the specification of the econometric model is the choice of a functional form to represent the energy technology. Among the most popular flexible forms (the translog, generalized Leontief and symmetric generalized McFadden), the translog is clearly the most convenient in particular because it leads to a tractable econometric model in a context where the decision variables are censored<sup>4</sup>.

The three kinds of energy inputs included in our model are indexed  $i = 1; 2; 3$ .<sup>5</sup>  $p_i$  and  $x_i$  ( $i = 1; 2; 3$ ) are respectively the price and the quantity consumed of energy  $i$ . The total cost of energy is given by,

$$p_E E = \sum_{i=1;2;3} p_i x_i$$

where  $p_E$  and  $E$  denotes respectively the price index and the quantity index of the energy aggregate. Finally  $\epsilon_i$  ( $i = 1; 2; 3$ ) are disturbance terms assumed to be distributed  $N(0; \Sigma)$ .

The translog form of the unit cost function of energy,  $p_E = C_E(p_1; p_2; p_3)$ , is then given by,

$$\ln(p_E) = \alpha_0 + \sum_{i=1}^3 \alpha_i \ln p_i + \frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \gamma_{ij} \ln p_i \ln p_j + \sum_{i=1}^3 \epsilon_i \ln p_i \quad (1)$$

where,

<sup>4</sup>Our analysis could be made with other quadratic flexible forms, but at a higher cost in term of estimation. The existing comparison between flexible functional forms concerns monotonicity and concavity restrictions (see Terrel (1996)), not the properties with respect to zero demands.

<sup>5</sup>Energy 1, 2 and 3 are respectively gas, oil and electricity.

$$\gamma_{ij} = \gamma_{ji} \quad \forall i, j = 1, 2, 3: \quad (2)$$

The linearly homogenous property in input prices of the unit cost function implies the following additional parameters restrictions,

$$\sum_{i=1}^3 \alpha_i = 1; \quad \sum_{j=1}^3 \gamma_{ij} = 0 \quad \forall i = 1, 2, 3: \quad (3)$$

From Shepard's lemma the value share of inputs are given by,

$$w_i = \alpha_i + \sum_{j=1}^3 \gamma_{ij} \ln p_j + \mu_i \quad i = 1, 2, 3: \quad (4)$$

Note that under (2) and (3), we necessarily have  $\sum_{i=1}^3 \mu_i = 0$  and  $\sum_{i=1}^3 w_i = 1$ .

### 3.2 The case of designated technologies

Following Woodland (1993), we assume here that observed fuel patterns are simply the consequence of a previous choice among a set of designated technologies. This previous choice restricts the set of energy forms that can be used. Then the problem of the firm is to determine the optimal allocation of its energy needs over a given subset of the different kinds of energy.

#### 3.2.1 The technology allows the firm to use all energy forms

The parameters of the translog unit cost function (1) are estimated using the Zellner iterative method applied to the system of cost share equations,

$$\begin{aligned} w_1 &= \alpha_1 + \gamma_{11} \ln \frac{p_1}{p_3} + \gamma_{12} \ln \frac{p_2}{p_3} + \mu_1; \\ w_2 &= \alpha_2 + \gamma_{21} \ln \frac{p_1}{p_3} + \gamma_{22} \ln \frac{p_2}{p_3} + \mu_2; \end{aligned}$$

Table 2 below gives the empirical results.

Table 2: Estimation when all energy forms are used

parameter	estimate	standard error
$\alpha_1$	0.24	0.0140
$\alpha_2$	0.11	0.0123
$\beta_{11}$	-0.23	0.0273
$\beta_{12}$	0.14	0.0191
$\beta_{22}$	-0.17	0.0247
$\alpha \frac{q_1^2}{E_1^{1/2}}$	0.17	0.0129
$\alpha \frac{q_2^2}{E_2^{1/2}}$	0.18	0.0111
$E_1^{1/2}$	-0.20	0.0122

### 3.2.2 The technology excludes one form of energy

The translog unit cost function of energy includes only 2 types of energy. Consequently, the system of value share equations is reduced to a single equation,

$$w_i = \alpha_i + \beta_{ii} \ln \frac{p_i}{p_3} + \mu_i;$$

where  $i = 1$  when gas is excluded and  $2$  when oil is excluded. The empirical results are given in table 3 and 4.

Table 3: Estimation when oil is excluded

parameter	estimate	standard error
$\alpha_1$	0.26	0.0124
$\beta_{11}$	-0.20	0.0325
$\alpha \frac{q_1^2}{E_1^{1/2}}$	0.14	0.0070

Table 4: Estimation when gas is excluded

parameter	estimate	standard error
$\alpha_2$	0.25	0.0199
$\beta_{22}$	-0.14	0.0382
$\alpha \frac{q_2^2}{E_2^{1/2}}$	0.16	0.0099

### 3.2.3 The technology excludes two forms of energy

In this case there is no need for an econometric estimation; the only energy used is electricity (energy 3) then,  $w_1 = w_2 = 0$  and  $w_3 = 1$ :



### 3.3 The case of a flexible technology

With a flexible technology, each firm is able to meet its requirements for heat, power etc. by substituting one energy form for another without modifying the equipment that consumes the fuel and obtaining the same level of production after the switch. The flexible technology assumption corresponds to the case where the energy technology allows the firm to change one kind of energy by another kind of energy at no cost<sup>6</sup> and for a constant production level. In this case a zero demand for one or more energies is the result of an endogenous rationing. Following Wales and Woodland (1983) and later on Lee and Pitt (1986) and (1987), the approach to the zero corner solution problem is based on the use of virtual prices. Virtual prices are those prices at which non-negativity constraints on input demands solve the analogous unconstrained cost minimization problem; in other words, they are prices at which the firm would be on the margin of consuming non used inputs. At that prices, the so called "notional" demand of input and the observed demand are the same whatever the observed demand is. If the market price is higher than the virtual price, the notional input demand is negative, which results in zero observed demand.<sup>7</sup> This approach characterizes a fuel pattern by a set of inequality and equality conditions where for each zero demand virtual prices are lower than market prices and respectively for each positive demands virtual prices and market prices are the same.

A complete treatment of the theory of virtual prices can be found in Neary and Roberts (1980) and in Pudney (1989). Their models provide directly the econometric specification which enters the generalized Tobit-type model. The main difference with a multiple censored regression is that virtual prices are endogenous thresholds explaining zero demands. These thresholds depend on the parameters of the model and are specific to each fuel pattern.

To derive the likelihood function for this model, we need to distinguish the different fuel patterns. A fuel switching technology could lead to  $2^3 - 1 = 7$  possible fuel patterns. As all firms in the sample use electricity we may observe  $2^{3-1} = 4$  fuel patterns only. To characterize these 4 different cases, we introduce the following notations:

- <sup>2</sup>  $w_i$  and  $\bar{w}_i$  are respectively the observed and the notional value shares of input;
- <sup>2</sup>  $P_E^{XXX}$  is the unit cost of energy when all energy forms are used (XXX means gas, oil and electricity are used);

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<sup>6</sup>Excepted of course the difference between the cost of energy purchase after and before the switch.

<sup>7</sup>In this paper, since we use a translog specification of the unit cost function, we estimate value share of inputs. Thus, the different fuel patterns will be characterized through the concept of notional value share of input instead of notional demand of input.

$\lambda_2 P_E^{OXX}$ ,  $P_E^{XOX}$  and  $P_E^{OOX}$  are similarly defined ("O" means not used).

### 3.3.1 Fuel pattern XXX: No binding non negativity constraint

This case corresponds to an interior solution of the producer's optimization program. All types of energy are used, then notional demands coincide with observed demands, from (4) we have,

$$w_i(p_1; p_2; p_3) = w_i = \lambda_i + \sum_{j=1}^3 \tau_{ij} \ln p_j + \mu_i \quad \text{for } i = 1; 2; 3: \quad (5)$$

Similarly we have from (1),

$$\ln p_E^{XXX} = C_E(p_1; p_2; p_3) = \lambda_0 + \sum_{i=1}^3 \lambda_i \ln p_i + \frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \tau_{ij} \ln p_i \ln p_j + \sum_{i=1}^3 \mu_i \ln p_i: \quad (6)$$

### 3.3.2 Fuel patterns OXX or XOX: One binding non negativity constraint

There is now one corner solution only. The observed zero demand is the result of an endogenous rationing. When zero demand occurs for input 1,<sup>8</sup> the virtual price of input 1, denoted by  $\hat{p}_1$ , is solution to,

$$w_1(\hat{p}_1; p_2; p_3) = w_1 = 0:$$

This fuel pattern occurs when the price of energy 1 is too high, the condition is,  $p_1 > \hat{p}_1$ . Then in this case, provided that  $\tau_{11} < 0$ , it can be shown that we have  $w_1(p_1; p_2; p_3) < 0$ .

Substituting  $\hat{p}_1$  for  $p_1$  into the notional cost share for input 2 and 3 defined by (5) gives after straightforward computations the analytical expression of the cost shares of input 2 and 3,

$$w_2(\hat{p}_1; p_2; p_3) = w_2 = (\lambda_2 + \tau_{21} \ln \hat{p}_1 + \tau_{22} \ln p_2 + \tau_{23} \ln p_3) + \tau_{12} \ln \hat{p}_1 \ln p_2 + \tau_{13} \ln \hat{p}_1 \ln p_3 + \mu_2 \ln p_2;$$

$$w_3(\hat{p}_1; p_2; p_3) = w_3 = \lambda_3 + \tau_{31} \ln \hat{p}_1 + \tau_{32} \ln p_2 + \tau_{33} \ln p_3 + \tau_{13} \ln \hat{p}_1 \ln p_3 + \mu_3 \ln p_3;$$

Similar computations gives the expression of the unit cost function of energy for this fuel pattern<sup>9</sup>,

<sup>8</sup>The case where zero demand occurs for input 2 can be derived by symmetry.

<sup>9</sup>Virtual prices are used in the same way by Thomsen (2000) to determine the short run restricted cost function in a quasi-fixed capital model.

$$\ln p_E^{OOX} = C_E(\hat{r}_1; \hat{r}_2; p_3) = \alpha_0 + \frac{1}{2} \frac{(\alpha_1 + \alpha_2)^2}{\alpha_{11}} + (\alpha_2 + \alpha_2) + \frac{-\alpha_{12}(\alpha_1 + \alpha_2)}{\alpha_{11}} \ln \frac{p_2}{p_3} + \ln p_3 + \frac{1}{2} (\alpha_{22} + \alpha_{22}) + \frac{-\alpha_{12}^2}{\alpha_{11}} \ln \frac{p_2}{p_3} \quad (7)$$

Note that the constant term of this conditional cost function comprises the term  $\frac{1}{2} \frac{(\alpha_1 + \alpha_2)^2}{\alpha_{11}} > 0$  as  $\alpha_{11} < 0$ . This reflects the cost of the binding non-negativity constraint on input 1.

### 3.3.3 Fuel pattern OOX: Two binding non negativity constraints

We consider here the case with two corner solutions. The virtual prices of input 1 and input 2 are obtained by solving the simultaneous equations system,

$$\begin{aligned} w_1(\hat{r}_1; \hat{r}_2; p_3) &= w_1 = 0 \\ w_2(\hat{r}_1; \hat{r}_2; p_3) &= w_2 = 0; \end{aligned}$$

and this fuel pattern occurs when prices for energy 1 and 2 are such that  $p_1 < \hat{r}_1$  and  $p_2 < \hat{r}_2$ .

As input 3 is the only input used we necessarily have<sup>10</sup>

$$w_3(\hat{r}_1; \hat{r}_2; p_3) = w_3 = 1.$$

The energy unit cost function under OOX regime is given by the price of energy 3 up to a constant term,

$$\ln p_E^{OOX} = C_E(\hat{r}_1; \hat{r}_2; p_3) = \alpha_0 + \frac{1}{2} \frac{(\alpha_1 + \alpha_2)^2 - \alpha_{12} \frac{2(\alpha_1 + \alpha_2)(\alpha_2 + \alpha_2) - \alpha_{12} + (\alpha_2 + \alpha_2)^2}{\alpha_{11} - \alpha_{22} + \frac{-\alpha_{12}^2}{\alpha_{11}}}}{\alpha_{11} - \alpha_{22} + \frac{-\alpha_{12}^2}{\alpha_{11}}} + \ln p_3 \quad (8)$$

To understand why there is a constant term in (8), we must remember that when the only input used is input 3, the optimal demands for input 1 and 2 are negative. Then, zero demands for input 1 and 2 are not necessarily optimal in our model. The constant in (8) reflects the cost resulting from the fact that the non negativity constraints on input 1 and 2 are binding.

### 3.3.4 Estimation

The estimation is based on the method of maximum likelihood. Our model is a discrete/continuous choice model but, contrary to most of the models of this type, the discrete choice (the choice of the fuel pattern) and the

<sup>10</sup>Of course, substituting the expressions giving virtual prices for input 1 and 2 into the notional cost share for input 3 gives  $w_3 = 1$ .

continuous choice (the level of demand) are here derived from the same cost minimization problem. Consequently, the decision rules for the discrete and continuous choices depend on the same set of parameters and errors terms.

Following Van Soest and Kooreman (1990), it is well known that this econometric model is correctly specified only if certain coherency conditions are satisfied. In generalized Tobit models, a model is defined to be coherent if, for each possible values of the regressors and the errors terms, there exists a unique value for the endogenous variables. Coherency is clearly a minimal requirement for model specification. For binding non-negativity constraint, Van Soest and Kooreman show that coherency conditions are necessarily satisfied when the cost function is globally concave. In our case, the cost shares and fuel pattern are unambiguously defined and the likelihood function is well defined over the disjoint regimes of demand.

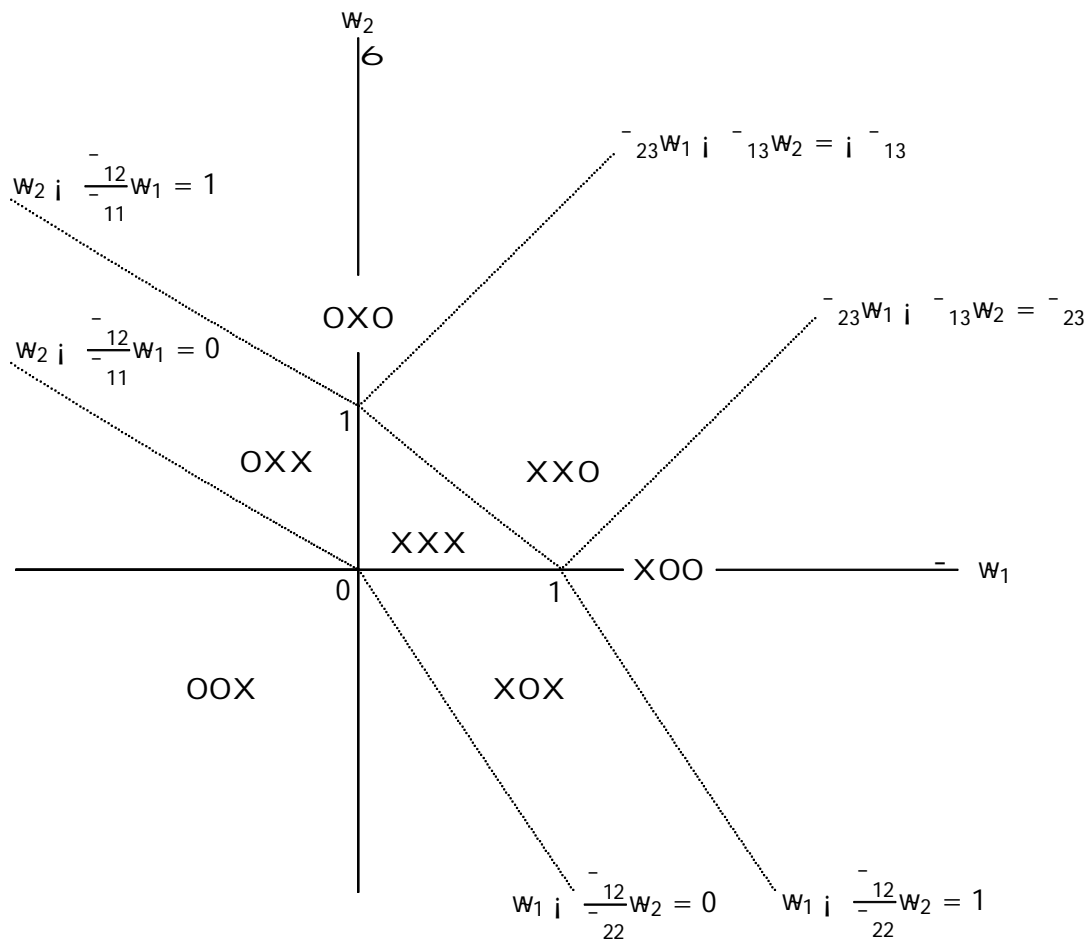


Figure 1 Coherency conditions.

Figure 1 is like a map of the different fuel pattern, given possible values of notional cost shares. Another look at coherency conditions could be

provided by the comparison of conditional unit cost functions across the different fuel patterns. It is easy to show that coherency conditions ensure that firms are able to minimize cost over the different fuel patterns. As a consequence, the firm can choose a (unique) fuel pattern corresponding to the lower cost among the set of alternatives. This means that we need a globally concave cost function to be sure that the discrete choice model gives us the optimal cost (see Blundell and Smith 1994).

We do not illustrate here the way to build the likelihood function of this model, a complete description is given by Bousquet and Ivaldi (1998). As in generalized Tobit models, the likelihood function involves for each fuel pattern the product of a probability and a conditional density function corresponding to the discrete and continuous choice among the three energies we consider. Assuming a bivariate normal distribution for the additive error terms in the relative costs shares  $(\varepsilon_1, \varepsilon_2)$ , the likelihood function could be written in a closed form.

As the prices associated to zero demands are not observable, we need an additional hypothesis. We consider that non-observed prices are equal to the maximum price from the observed distribution of energy prices.<sup>11</sup>

Table 5 : Estimation results for a flexible technology

parameter	estimate	standard error
$\alpha_1$	0.22	0.0028
$\alpha_2$	0.01	0.0033
$\beta_{11}$	-0.47	0.0073
$\beta_{12}$	0.26	0.0077
$\beta_{22}$	-0.51	0.0076
$\frac{q_1}{E_1} \varepsilon_1^2$	0.21	0.0036
$\frac{q_2}{E_2} \varepsilon_2^2$	0.23	0.0046
$E(\varepsilon_1 \varepsilon_2)$	-0.50	0.0228

As in the previous estimations, all the parameters are here highly significant. Another way to check the quality of the estimates is to compare the observed fuel patterns with the one predicted by the model. Table 6 below shows that the prediction is globally acceptable; 98% of firms using a mix of gas and electricity and 94% of firms using a mix of oil and electricity are correctly predicted.

The prediction is less good for firms using all the three energy inputs, since only 39% of these firms are predicted in this fuel pattern. For these

<sup>11</sup>A similar solution is taken in labor supply models where the wage for an unemployed is taken as the minimum value found in the observed wage distribution. Here, we have replicated the estimation when, instead of the maximum price, we use the upper centile of the price distribution; we have found very little differences in the estimation results.

...rms, the model often predicts that the optimal fuel pattern is a mix between gas and electricity. When electricity is the unique energy source the prediction is only correct for 56%; 44% of ...rms using electricity alone are predicted to use also oil.

Table 6: Predicted fuel patterns vs observed one

observed patterns	predicted patterns				
	Gas+Oil+Elec.	Gas+Elec.	Oil+Elec.	Elec.	Total
Gas+Oil+Elec.	1342	1675	429	25	3471
Gas+Elec.	34	4769	3	62	4868
Oil+Elec.	0	0	2526	168	2694
Elec.	9	0	747	956	1712
Total	1385	6444	3705	1211	12745

## 4 Price Elasticities

Price elasticities are defined by,

$$e_{ij} = \frac{\partial \ln x_i}{\partial \ln p_j} \Big|_{dE=0; dp_k=0 \quad k \neq j} \quad (9)$$

Using Shephard's lemma, it can be easily shown that (9) is equivalent to,

$$e_{ij} = \frac{p_j C_{ij}}{C_i} \quad i, j = 1, 2, 3 \quad (10)$$

where  $C_i$  and  $C_{ij}$  are respectively given by,

$$C_i = \frac{\partial \ln p_E}{\partial \ln p_i}; \quad i = 1, 2, 3$$

$$C_{ij} = \frac{\partial^2 \ln p_E}{\partial \ln p_i \partial \ln p_j}; \quad i, j = 1, 2, 3$$

Using (10), straightforward computations show that in the translog case we have,

$$e_{ij} = \frac{-\alpha_{ij} + \omega_i \omega_j}{\omega_i}; \quad i \neq j; \quad (11)$$

$$e_{ii} = \frac{-\alpha_{ii} + \omega_i^2}{\omega_i}; \quad (12)$$

where  $\hat{w}_i$  is the expected value of the relative share of energy  $i$ .

We can easily use (11) and (12) to determine price elasticities in the case of a designated technology.

In the case of a flexible technology a marginal change of an input price can move consumption smoothly within a single fuel pattern, or yields to a drastic change in consumption when the firm changes its fuel pattern. This discontinuity of the demand behavior complicates significantly the analytical expression of the price elasticities. Nevertheless, we can get an approximation of these elasticities. Our method is the following:

- <sup>2</sup> the observed price of a given energy form is increased at the margin;
- <sup>2</sup> this implies new values of the relative prices from which we can determine the optimal fuel pattern chosen by each firm<sup>12</sup>
- <sup>2</sup> the partial derivatives appearing in (10) are evaluated by using the GRADP and HESSP routines of the GAUSS software applied to the unit cost function given by (6), (7) or (8) depending on the fuel pattern the firm has chosen.

Tables 7 and 8 give the estimated price elasticities averaged over firms having the same fuel pattern under the hypothesis of designated and flexible technologies respectively. Tables 9 and 10 give these elasticities averaged over the whole sample.<sup>13</sup>

Two main conclusions arise from tables 7 and 8. Firstly, it appears that inter-fuel substitution possibilities are higher for firms using the three energy forms compared to firms using two kinds of energy only, whatever the technology is supposed to be: designated or flexible. In table 7, oil-price elasticity is  $-6.83$  when firms use all kinds of energy while it is  $-1.36$  when firms use oil and electricity only. The same elasticities in table 9 are respectively  $-11.50$  and  $-5.30$ .

Secondly, the two alternative models we use give very different results about the substitution possibilities between energy forms. For instance, own-price-elasticities for gas, oil and electricity are respectively  $-1.81$ ,  $-6.83$  and  $-0.68$  when firms have a designated technology while they are respectively  $-5.23$ ,  $-11.50$  and  $-1.07$  when firms have a flexible technology (this when all kinds of energy are used).

A last comment applies to both tables, oil is clearly much more sensitive to its own price than gas and electricity.

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<sup>12</sup>As few firms are located at the frontier between two fuel patterns, in practice a marginal increase in the energy price is not sufficient to induce a change in the fuel pattern. But, as we will see in the next section, this effect could be highlighted for significant changes in energy prices.

<sup>13</sup>Of course, when the fuel pattern is given, the price elasticity of an energy form not used by the firm is zero.

Comparing tables 9 and 10 shows that in the model where the technology is considered as flexible, the elasticities are, of course, bigger in absolute value, than in the model where the technology is considered as designated. The empirical 95 % confidence intervals of the elasticities appearing in tables 9 and 10 call for several remarks. First they are smaller in the designated case than in the flexible one. This of course is the result of the less constrained model we use in the flexible case. Something strange, a priori, is the very high absolute value of the elasticities in some cases. This is a feature of the Translog model that the elasticities explode when factor share approaches zero (see equations (12) (11)).

We can check on our sample that, for a given energy form, the larger is the elasticity (in absolute value) the smaller is the share of this kind of energy in the total energy consumption of the firm. It means that the elasticities do not allow to conclude from the point of view of how the industrial sector reacts, as a whole, to a variation of the relative energy prices. But aggregated firm's behaviour in response to relative energy price variations can be simulated as proposed in section 5.

These simulations are also useful for another reason. We know that elasticities, by definition, give the input demand response to a marginal price increase. In the flexible model, when a given price is increased only at the margin, the firms changing their fuel pattern are very few. Then, the estimation of price elasticities does not allow us to measure the consequences on energy demand of a drastic change in the relative prices of energy forms. Such a change is however possible, for instance to implement an energy policy aiming at reducing CO<sub>2</sub> emissions.

Table 7: Price elasticities in the case of designated technologies within a given fuel pattern

	fuel pattern								
	Gas+Oil+Electricity			Gas+Electricity			Oil+Electricity		
	gas	oil	elec.	gas	oil	elec.	gas	oil	elec.
Gas	1:81	0:59	1:22	1:45	-	1:45	-	-	-
Oil	4:01	6:83	2:82	-	-	-	-	1:36	1:36
Elec.	0:47	0:21	0:68	0:62	-	0:62	-	0:45	0:45

Table 8: Price elasticities in the case of flexible technologies within a given fuel pattern

	fuel pattern								
	Gas + Oil + Electricity			Gas + Electricity			Oil + Electricity		
	gas	oil	elec.	gas	oil	elec.	gas	oil	elec.
Gas	5:23	2:64	2:58	2:10	-	2:10	-	-	-
Oil	5:81	11:50	5:69	-	-	-	-	5:30	5:30
Elec.	0:55	0:51	1:07	0:80	-	0:80	-	0:64	0:64



Table 9: Price elasticities in the case of designated technologies

	Gas	Oil	Elec.
Gas	$\epsilon_i$ 1:10 $]\epsilon_i$ 3:16; 0[	0:18 $]\epsilon_i$ 1:10[	0:92 $]\epsilon_i$ 2:30[
Oil	0:37 $]\epsilon_i$ 2:64[	$\epsilon_i$ 1:01 $]\epsilon_i$ 4:59; 0[	0:63 $]\epsilon_i$ 1:98[
Electricity	0:36 $]\epsilon_i$ 0:76[	0:15 $]\epsilon_i$ 0:53[	$\epsilon_i$ 0:52 $]\epsilon_i$ 0:82; 0[

Table 10: Price elasticities in the case of flexible technologies

	Gas	Oil	Elec.
Gas	$\epsilon_i$ 1:62 $]\epsilon_i$ 6:11; 0[	0:27 $]\epsilon_i$ 2:22[	1:34 $]\epsilon_i$ 4:19[
Oil	0:61 $]\epsilon_i$ 6:53[	$\epsilon_i$ 2:79 $]\epsilon_i$ 20:93; 0[	2:18 $]\epsilon_i$ 15:18[
Electricity	0:46 $]\epsilon_i$ 1:08[	0:24 $]\epsilon_i$ 0:97[	$\epsilon_i$ 0:71 $]\epsilon_i$ 1:31; 0[

## 5 The consequences of a carbon tax

Following Bousquet and al. (2004), we use a tax of 30 Euro per ton of carbon. Using the carbon content of the different kinds of energy, we can translate the carbon tax in price increase for each form of energy as shown in table 11.

Table 11: Carbon content of the different energy forms<sup>14</sup>

	tC/toe	Price increase
Gas	0:65	+19%
Oil	0:89	+26%
Electricity	0:00	0%

Table 12 gives the changes in energy consumption and in CO<sub>2</sub> emissions in the industrial sector resulting from the carbon tax.

<sup>14</sup>The 0 carbon content of electricity is explained by both the high level of nuclear share in the electricity production in France and because industrial demand is mainly base load demand.

Table 12: CO<sub>2</sub> Emissions

	Designated technology	Flexible technology
Gas	↓ 17%	↓ 25%
Oil	↓ 24%	↓ 45%
Electricity	+8%	+11%
CO <sub>2</sub> emissions	↓ 20%	↓ 33%

This table shows that CO<sub>2</sub> emissions reductions can be misestimated by one third if the hypothesis on the technology, flexible or designated, is wrong. For oil demand, the most pollutant energy, the misestimation is close to 50%.

When the technology is considered as flexible of course, the way the firms are distributed among the different energy patterns plays an important role. As shown in table 13, there is a very important change in the fuel pattern frequencies when a carbon tax is imposed. The number of firms changing their fuel pattern is particularly high for those using all energy form before the energy prices changes. There are 2 times less firms using all forms of energy after the tax than before. Clearly, firms substitutes oil to gas and electricity.

Table 13: Number of firms following the different energy patterns

energy pattern	estimated before tax	estimated after tax
Gas+ Oil + Elec.	1385	783
Oil + Elec.	3705	3021
Gas + Elec.	6444	6907
Elec.	1211	2034

From these results, the model choice appears as having an important consequence on the measurement of substitution possibilities between energy forms. Certainly more important than it is generally considered in the literature. As we know the level of flexibility of the technology is certainly between the two extremes assumptions we have studied in this paper. This calls for future research aiming at finding a new way for building model of producer behavior, and at including data on technology characteristics in energy demand modelling.

## 6 Conclusion

The present study is to our knowledge the first attempt to evaluate the consequences on individual data of the usual assumptions made on energy

technology. Using a unique data set, the French manufacturing energy consumption survey, we estimate energy technology under two extreme assumptions depending on the assumed flexibility of the technology. In the literature about energy demand modeling it is well known that firms do not use in general all kinds of energy. Zero demands could be interpreted as zero corner solution derived from a flexible technology (Lee and Pitt 1987) or could be simply determined by the technology (Woodland 1993).

Under these two possible assumptions about the energy technology, this paper shows by how much the estimated inter-fuel substitution differs. The differences between the inter-fuel substitution elasticities in the two models induce large differences in the predicted energy mix as a response to a change in the relative price between electricity, natural gas and oil products. This research outlines the importance of a proper estimation of inter-fuel elasticities and the consequences for greenhouse gas abatement policies.

In the real world energy technology is probably in between the two extreme assumption made in this paper. It is difficult to keep the same framework to test a mix of these two assumptions. The reason for that is quite simple and could be shown through an example. Consider a particular firm with positive demands on electricity and gas. Since oil is not consumed we could consider that oil is not used because its price is too high if the technology is flexible, or we could consider alternatively that the technology do not allows the use of oil. Clearly, we have not considered all the possible cases of the underlying technology. A zero demand for oil, could occur when the firm have a dual fixed equipment using oil or gas and a specific equipment using electricity only. This example corresponds to an intermediate case of a flexible technology between oil and gas and a designated technology for electricity.

We know that with three inputs we may have seven fuel patterns. If we consider that the technology are designated, perfectly flexible with respect to all inputs, or partially flexible (with respect to two inputs in our case), then it is easy to see that all the observed fuel patterns could come from 14 different technologies.

A problem with the Lee and Pitt's approach is that it is difficult to extend these kinds of models when the number of inputs is larger than three. This dimension problem could be solved through simulation techniques, at the frontier of recent development in econometrics methods. But it seems to us that the main problem is that price at the individual level is not observable when the demand is zero. One way to alleviate this problem consists to extend the model and to include price estimates as function of individual characteristics.

The Woodland's approach is more simple but correct only for the estimation of short term price elasticities for firms owning energy technology with limited flexibility. Moreover, results depend on the observed fuel patterns. Since estimations are realized over each empirically relevant fuel patterns,

results may be particularly sensitive to the level of aggregation between different kinds of energy. Finally, if fuel patterns are fixed given the energy technology, the question about the optimal choice between some energy technologies remains. In fact, separated estimations by fuel patterns do not ensure that energy cost is optimal. Clearly in the Woodland approach's, the observed fuel pattern does not necessarily correspond to the optimal designated technology. A qualitative choice model must also be considered in order to understand how firms choose energy technologies in a first step, and energy use in a second one.

Theoretical development in energy demand modelling will try to solve this kind of problems in the future. Moreover, a particular attention must be paid on technology characteristics in energy consumption surveys. In the same time, we need to pursue our analysis by industry sector subdivision and firm size, to see more precisely where the differences between existing alternative approaches to measure inter-fuel substitutions matter.

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