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INTERNATIONAL FINANCE DISCUSSION PAPERS

A Two Country Model of Financial Capital Movements as Stock Adjustments with Emphasis on the Effects of Central Bank Policy

by

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A Two Country Model of Financial Capital Movements

as Stock Adjustments with Emphasis on the Effects

of Central Bank Policy*

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Lance Girton and Dale Henderson

I. Introduction

Over the past decade theoretical and empirical analyses of financial asset holding have relied increasingly upon the portfolio balance approach. According to this approach the desired holders depend upon the levels of the interest rates on the asset in question and on alternative assets, the size of the portfolio of the group of asset holders under consideration, and perhaps other variables. Changes in desired asset holdings depend upon changes in these variables.

In an open economy in which residents hold both domestic and foreign financial assets to result in capital flows. Previous authors who have applied the portfolio balance approach to the analysis of capital flows have divided $\frac{1}{2}/$ such changes in desired holdings into two components. The part of

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 $\frac{1}{(1970a)}$ See for example Bryant and Hendershott (1969), Miller and Whitman (1970a, and 1970b), Willett and Forte (1969), and Grubel (1968).

changes in desired asset holdings due to changes in one or more interest rates or other variables with the size of the portfolio held constant has been called the stock-shift component. The part of changes in desired asset holdings due to growth in the size of the portfolio with interest rates and other variables held constant has been called the $\frac{1}{2}/$ continuing-flow effect.

In this paper we focus upon the short run portfolio balancing behavior of wealth holders. We assume that the size of wealth holders' portfolios are fixed and examine in detail the stock-shift component of capital flows. This empirical evidence we have suggest that the stock-shift component of capital flows is very important quantitative stock-shift component of capital flows is very important quantitatively. Secondly, many observers have become increasingly convinced tively.

A slight modification of the formulation in Bryant and Hendershott (1970) allows us to write their expression for the desired holding of a financial asset designated as F^* , as follows:

$$F^* = g(R,0)S,$$

where R represents a vector of interest rates, 0 is a vector of other relevant variables, and S is a measure of portfolio size. The change in desired holdings when the right hand side variables change is,

$$AF* = Sdg(R,0) + g(R,0)dS.$$

The stock shift effect is Sdg(R,0), and the continuing flow effect is g(R,0)dS.

\(\frac{2}{\text{chr}}\) The size of wealth holders' portfolios is assumed to be fixed except in Chapter VI where the effects of a devaluation are considered. A devaluation directly affects the size of wealth holders' portfolios.

 $\frac{3}{2}$ See, for example, Miller and Whitman (1970a and 1970b).

that rapid movements of large amounts of financial capital across national boundaries, which are probably best viewed as being made up mainly of stock-shift changes in desired asset holdings, severely limit the freedom of policy makers to use the instruments at their command to achieve their policy objectives under a regime of fixed exchange rates.

Much useful effort has been expended in spelling out the

We believe that empirical work based on the theoretical model we consider interest rates and desired financial asset holdings. For this reason under the control of the policy authorities and both the level of able to specify in detail the relationship between variables directly Another important feature of our model is that we are . suonagoxa jointly determined with desired asset holdings instead of being taken as case from models of the small-country case is that interest rates are important feature which distinguishes our model of the large-country stitute the world economy. This model is outlined in Chapter II. One that deals explicitly with two countries which, taken together, conworld economy. In order to accomplish this objective we develop a model of the portfolio balance approach to economies which loom large in the Our objective is to trace out the implications small open economy. /ī implications of the portfolio balance formulation for the case of a

 $\frac{1}{2}$ See, for example, Mundell (1968, Chapter 18) and McKinnon and Oates (1966).

 $\frac{2}{\lambda}$ For examples of work on capital flows which takes interest rates as exogenously determined see inter alia Branson (1968), Branson and Hill (1971), Miller and Whitman (1970a and 1970b).

here would be of more use to policy makers in large countries than most of the existing empirical work on capital flows which is based $\frac{1}{2}/$ on the assumption that interest rates can be taken as exogenous.

In a static short-run portfolio balance model such as the

of which the gold standard is an example. In Chapter IV we turn to central banks. In Chapter III we investigate an outside reserve regime, regimes under various assumptions about the policy objectives of the We explore in detail the implications of two alternative fixed exchange of the game" under which the central banks pursue their policy objectives. pursuing some other objective. Also of primary concern are the "rules money supply or the interest rate on domestic liabilities or are central banks, that is, whether or not they are trying to stabilize the particularly important. We must know the policy objectives of the of the two central banks. Two aspects of central bank behavior are what this new equilibrium looks like depends crucially upon the behavior they hold their desired quantities of all financial assets. Exactly in both countries have attained a new equilibrium position in which reserves of central banks. These changes persist until wealth holders rates, flows of financial capital between countries, and changes in the disturbs an existing equilibrium and sets in motion changes in interest one we shall employ a change in some aspect of the economic environment

 $[\]underline{1}$ / Two recent empirical studies which attempt to take account of the fact that interest rates and desired asset holdings are simultaneously determined when the country being studied should be regarded as large are Miller and Whitman (1970c) and Kouri and Porter (1972).

what we call the key currency reserve regime which we believe captures some crucial aspects of more recent international monetary experience.

It has often been argued that exchange rate changes can be

expected to have little or no impact on desired holdings of financial assets and therefore on the flows of financial capital captured by the capital account of the balance of payments. This argument neglects the fact that an exchange rate change results in capital gains for some wealth holders and capital losses for others. These capital gains for gains and losses arise because of changes in the value of particular assets so that, in general, wealth holders are left with unbalanced portfolios. The implications of the wealth effects consequent upon a devaluation for interest rate levels and central bank reserve holdings are traced out in Chapter V.

For purposes of simplicity we assume throughout most of the paper that there is no commercial banking system, that is, that all money is in the form of currency or deposits at the central banks. In Chapter VI we relax this assumption in order to determine the sensitivity of our conclusions to the presence of a fractional reserve tivity of our conclusions to the presence of a fractional reserve

commercial banking system and in order to consider some of the impli-

cations of broadening the range of alternatives for the holding of international reserves available to central banks.

Armed with the results of previous Chapters, we attempt in Chapter VII to isolate some other factors which determine the effectiveness of a monetary policy action, such as an open market purchase, undertaken by the central bank in an open economy in attaining some

proximate objective, such as lowering the interest rate on liabilities of domestic residents. While, as we show in Chapters III through VI, the effectiveness of monetary policy depends in part on the behavior exchange rate two central banks and the prevailing type of fixed play extremely important roles. The effectiveness of monetary policy depends in an important and relatively straightforward way on the relative economic size of the country undertaking the policy action. In addition the degree of substitution between the liabilities of onestic residents and the liabilities of foreigners in the portfolios of the world's wealth holders has a significant if less obvious impact of the world's wealth holders has a significant if less obvious impact on the effectiveness of monetary policy.

In Chapter VIII we draw some general conclusions from our

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II. The Model

A. An Overview

In the world of our model there are two countries, the United States (U.S.) and the United Kingdom (U.K.). The U.S. analyze the dollar; the U.K. currency is the pound. We analyze the behavior of four groups: the United States Central Bank (UKCB), ultimate wealth holders in the U.S., and ultimate wealth holders in the U.K. We assume that there are only four types of assets: U.S. $\frac{1}{2}$ money, U.K. money, U.S. securities, and U.K. securities.

 $\underline{1}$ We assume initially that there are no private banking sectors in the two countries. A brief discussion of the effects of introducing a simple private fractional reserve banking system is included in Chapter VI.

The assumption that only a single type of security is issued in each country affords considerable simplicity in exposition and is not as restrictive as it might seem at first. It is well known that a bundle of securities can be treated as a simgle security if "enough" market participants view the securities in the bundle as perfect substitutes. Our results are applicable in situations in which this condition is fulfilled even if it is not literally true that only one security is issued in each country.

Our results would not be substantially affected by the introduction of non-bank financial intermediaries if these intermediaries did not hold cash and/or foreign assets (that is, if the intermediaries held only "primary" or "secondary" securities issued by domestic residents) and if "enough" market participants viewed the "secondary" securities (liabilities) issued by these intermediaries as perfect substitutes for the "primary" securities (liabilities) of the government, the non-financial corporate sector, and consumers.

Ultimate wealth holders in both countries regard the :wo securities in which the issuer resides and have variable interest rates. **/**\(\overline{z}\) Securities are fixed in nominal value in the currency of the country Money is held in the form of currency or deposits at the central bank. by the issuer's country of residence, are held in both countries. but both types of securities, which are identified wealth holders, Each country's money is held only by its own ultimate

in the model as imperfect substitutes.

Chapter VI. hold the money of the other country as part of its reserves. See The model can be adapted easily to allow each central bank to

ties had a coupon rate and a fixed maturity date or were a consol. results would be substantially unaffected if each of the two securiassumption makes the analysis much more straightforward, but the $\frac{1}{2}$ They are like call loans or savings and loan shares. This

are discussed in footnote 1, on the previous page. securities issued by the residents of a country as a "single" security The assumptions under which we could regard the bundle of by residents of the other country and denominated in that country's that country which is "different" from the "single" security issued given country as a "single" security denominated in the currency of advantageous to treat all the securities issued by the residents of a analysis. Given the issues we want to consider, we have found it most several alternative simple classification schemes for purposes of available in a two country world can obviously be arranged into 3/ The variety of financial assets which one can imagine being

"expected" to change? Perhaps most important is the fact that a flexible exchange rate system in which exchange rates are not as imperfect substitutes under a fixed exchange rate system or under What might cause wealth holders to view U.S. and U.K. securities

underlying sources of the value of the securities are subject to and home securities may not be treated as perfect substitutes if the denominated in domestic currency, at a small transaction cost, foreign nated in foreign currency can, in effect, be converted into a security if forward exchange markets are "perfect," so that a security denomibe viewed as having different degrees of "responsibility." Thus even affect investors views of "foreign" securities. Also governments may countries. In addition, actual or potential exchange restrictions may fluctuations in economic activity are not perfectly correlated across

different influences.

Everywhere in this study except in Chapter V it is assumed that the exchange rate is fixed and that ultimate wealth holders in both countries expect it to remain constant. Anticipated rates of inflation are assumed to be zero in both countries, so that there is no divergence between nominal and real interest rates. We analyze the behavior of central banks and ultimate wealth

holders in the "short run". Disturbances to financial asset equilibrium cause instantaneous adjustments in interest rates and in the financial asset holdings of both ultimate wealth holders and central banks, but in our short run prices, incomes, employment levels, and capital stocks remain fixed. We also assume that wealth holders do not take into account their current savings when deciding how to $\frac{2}{2}$ allocate their existing wealth among available assets.

B. The Portfolio Balancing Behavior of Ultimate Wealth Holders Ultimate wealth holders in the U S. base their nominal demands in terms of dollars for U.S. securities $(B^{\rm d})$, for U.K.

1/ We could carry out our analysis completely in terms of nominal rates of interest if wealth holders anticipated inflation in either or both countries so long as the disturbances we consider do not affect the anticipated inflation rates.

securities (F^d) , and for U.S. money (M^d) on their existing dollar denominated nominal wealth (W). We assume that the fraction of their nominal wealth which they wish to hold in each of these three assets depends only upon the interest rate on U.S. securities (r) and the interest rate on U.S. securities (r) and the interest rate on U.S. securities (r) and the

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Often asset demand innections are written so as to give demands for example of a quite general asset demand function is the following:

$$\left(\begin{array}{c} \frac{R}{Q} \end{array}\right)^{d} = h\left(x, x', \frac{PY + xBA + x'\Pi'FA - xBA'}{Q}\right),$$

where $\left(\frac{B}{Q}\right)$ is real asset value of U.S securities demanded, P is the where of the single U.S. good the output of which is given by Y, Q is price of the single U.S. good the relative weight in consumption of the single U.S. and the single U.K. good, BA represents U.S. holdings of U.K. u.S. securities, ThA is the dollar value of U.K. holdings of U.K. and PY + rBA + r'H FA - rB'A is the nominal income of U.S. residents and PY + rBA + r'H FA - rB'A is the nominal income of U.S. residents (assuming no taxes or transfers). The superscript (A) denotes actual holdings of an asset. If we ignore interest payments and assume that asset demand function is homogeneous of degree one in real wealth and that asset demand is unchanged so long as the ratio of real income to real wealth remains constant, we have,

$$\int_{0}^{M} \left(\frac{\underline{y}}{\mathbf{q}}, \mathbf{r}, \mathbf{r} \right) d = b \left(\frac{\underline{g}}{\mathbf{q}} \right)$$

Since prices, outputs, and existing nominal wealth levels are assumed to remain constant we can subsume $\frac{PY}{W}$ into the functional form and write,

$$\frac{W}{Q} (x, x) d = b \left(\frac{B}{Q} \right)$$

, TO

$$B_q = p(x,x')W.$$

We restrict our attention to this special form of asset demand function because of its simplicity and intuitive appeal.

$$B_{q} = p(x, x')W \tag{1}$$

$$\mathbf{F}^{\mathbf{d}} = \mathbf{f}(\mathbf{r}, \mathbf{r}) \mathbf{W} \tag{2}$$

$$M^{d} = m(r, r')W. \tag{3}$$

Similarly U.K. wealth holders base their pound denominated nominal demands for U.S. securities (\mathbf{F}^{d^i}) , for U.K. securities (\mathbf{F}^{d^i}) , and for U.K. money (\mathbf{N}^{d^i}) on their existing pound denominated nominal wealth (\mathbf{W}^i) . Their demand functions are assumed to have the same general

form as those of U.S. wealth holders,

$$\mathbf{B}_{\mathbf{q}_{i}} = \mathbf{p}_{i}(\mathbf{x}^{i}, \mathbf{x}_{i}) \, \mathbf{M}_{i} \tag{(4)}$$

$$\mathbb{E}^{d^i} = f^i(\mathbf{r}, \mathbf{r}^i) W^i \tag{5}$$

$$(9) \qquad \qquad M_{q_i} = u_i(x^i, x_i) M_i$$

The (') superscript denotes the value of a variable for the U.K. Since we assume that ultimate wealth holders do not take

existing wealth, disturbances to financial asset equilibrium result only in attempts by wealth holders to change the composition of the assets they hold. The behavior of each country's wealth holders in for ultimate wealth holders in, say the U.S., wealth is defined to be the sum of the nominal values of the securities and money they currently hold. This sum must be identically equal to the sum of the nominal values of the securities and money they currently hold. This sum must be identically equal to the sum of the nominal values of the securities and money they currently noid. This sum must be identically equal to the sum of the nominal values of the securities and money they currently hold. This sum must be identically equal to the sum of the nominal values of the securities and money they currently demands by U.S. wealth holders for all assets. They cannot, after all, tationally desire to allocate more wealth than they possess. Thus

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that if, as the result of an interest rate change, wealth holders want more of one asset they must want to reduce their holdings of one or both of the other two assets by the same amount. More technically, the sum of the partial effects on the three asset demands of a change in either of the two interest rates must be constraint in allocating their fixed wealth. All this means that under our assumption of fixed portfolio size in the short run only two of the three asset demand functions are independent in each country. We will use the implications of the balance sheet constraints for ultimate wealth holders in both countries repeatedly in what follows.

1/ From the U.S. balance sheet constraint we have,

$$\mathbf{W} \equiv \mathbf{B}^{\mathbf{A}} + \Pi \mathbf{F}^{\mathbf{A}} = \mathbf{M}^{\mathbf{A}} \equiv \mathbf{B}^{\mathbf{d}} + \mathbf{F}^{\mathbf{d}} + \mathbf{M}^{\mathbf{d}} \equiv \mathbf{W}$$

where W has a fixed dollar value by assumption. It is the dollar price of pounds. From the U.K. balance sheet constraint we have,

$$^{1}B_{M} + ^{1}A_{T} + ^{1}B_{G} = ^{1}A_{M} + ^{1}A_{T} + ^{1}B_{G} = ^{1}M$$

where W' has a fixed pound value. From the first of these two identities and equations (1) through (3) we have,

$$M^{d} \equiv m(r, r') W \equiv [1 - b(r, r') - f(r, r')] W.$$

A similar relationship holds for the U.K. Using the two identities and equations (1) through (6) we obtain,

$$p^{T} + E^{T} + w^{T} \equiv p^{T} + E^{T} + w^{T} \equiv p^{T} + E^{T} + w^{T} \equiv p^{T} + E^{T} + w^{T} \equiv 0$$

where $b_{\mathbf{r}}$ is the partial derivative of $b(\mathbf{r}, \mathbf{r}')$ with respect to \mathbf{r} , etc.

We assume that the two securities and home country money are strict gross substitutes in the portfolios of ultimate wealth holders in each of the two countries. This assumption means that if the interest rate on a given security rises, desired holdings of the other security increase while the desired holdings of the other security and money decline. Of course, we know from the balance sheet constraint that the sum of the declines in the desired holdings of the other security and money must equal the increase in desired holdings of the security the interest rate on which has risen. $\frac{1}{2}$

C. The Balance Sheets and Behavior of the Central Banks Consider first the U.S. Central Bank (USCB). Its only liability is the domestic money stock (currency and/or deposits at the USCB) denoted by M^3 ; its assets are its holdings of U.S. securities (B^C), the dollar value of its international reserve assets (σ R), and, if necessary, a dummy asset (S) which makes the balance sheet balance. The USCB balance sheet identity is given by,

 $\underline{1}$. More formally, the effects of a rise in the interest rate on U.S. wealth holders can be summarized as follows

$$b_{r} > 0$$
, $f_{r} < 0$, $m_{r} < 0$, $b_{r} + f_{r} + m_{r} \equiv 0$.

Similar relationships hold for the effect of an increase in r on J. K. portfolios and the effect of an increase in r on both J S. and J K. portfolios.

$$W_{g} \equiv B_{c} + \alpha B + C \qquad (1)$$

o is the dollar price of reserve assets. For the UKCB we have,

$$N_{S_i} \equiv F^{C_i} + \sigma^i R^i + S^i, \qquad (8)$$

where N^s is the U.K. money stock, $F^{c'}$ is the UKCB holdings of U.K. securities, σ' is the pound price of reserve assets so that $\sigma'R'$ is pound value of U.K. holdings of international reserves, and S' is a dummy asset which may be needed to balance the UKCB balance sheet. $\frac{1}{2}$ o and σ' are assumed to remain constant at a value of one throughout this study except in Chapter V where the effects of downlands are considered. Since $W = \frac{\sigma}{2}$, it remains constant at a downlanding are considered. Since $W = \frac{\sigma}{2}$, it remains constant at a

throughout this study except in Chapter V where the effects of devaluation are considered. Since $\Pi=\frac{\sigma}{\sigma}$, it remains constant at a value of one except in Chapter V. S and S' are assumed to remain constant throughout the study except in Chapter V when they are assumed to change so as to offset the initial effects of changes in σ and σ on the asset side of the USCB and UKCB balance sheets.

Although a full discussion of the behavior of the central banks must be deferred until we have finished laying out the model, some brief remarks here can provide a sense of direction. Central banks may respond "passively" to disturbances to asset equilibrium, or they may initiate such disturbances. How they choose to respond or what changes they choose to initiate will be reflected in which

1/ We assume that the USCB does not hold U.K. securities or U.K. money. In Chapter IV we examine the implications of a reserve currency system where the UKCB holds reserves in the form of U.S. securities and deposits at the USCB. In Chapter VI we make some comments on the implications of the UKCB holding reserves in the form of deposits at U.S. commercial banks.

items in their balance sheets they allow to or make change and which they keep constant. Our analysis of the effects of central bank behavior is based upon translating central bank responses and initiatives into changes in central bank balance sheets and spelling out the implications of these changes for the supplies of the various financial assets available to the public.

O. The Market Equilibrium Conditions

We are now prepared to consider the equilibrium conditions

for the markets in the four assets in the model. We turn first to the market for U.S. securities. The total supply of U.S. securities $\frac{1}{2}$ minus the holdings of the USCB must equal the demand for these

securities by ultimate wealth holders in the two countries,

$$\underline{B} - B_C = p(x, x')W + \Pi b'(x, x')W'$$
(9)

Similarly the total supply of foreign securities minus the holdings of the UKCB, both in dollar terms, must equal the dollar denominated

demand for these securities by ultimate wealth holders, 2/

$$\Pi (\overline{F} - F^{C_i}) = f(r, r')W + \Pi f'(r, r')W'.$$
(10)

I/ The total supply of U.S. securities (B) is equal to the sum of cumulated U.S. government deficits and the value of net claims to the income of the capital stock of the U.S. non-financial corporate sector. B might also include consumer debt, but we assume that obligations of ultimate wealth holders to one another are netted out. F has a similar interpretation.

countries it may be useful to restrict attention to some subset of sountries it may be useful to restrict attention to some subset of securities. A significant part of short-run financial capital movements seems to be made up of changes in holdings of short-term (liquid) assets. If people quickly balance money and short-term security holdings according to rates of return independently of their holdings of long-term (illiquid) securities, then for some purposes defining W and W' to include only short-term securities and money may be useful. Our treatment is theoretical, and we make no attempt to prejudge the question of what is the best tical, and we make no attempt to prejudge the question of what is the best empirical definition of allocatable wealth in any particular application.

money market equilibrium conditions for the two countries as follows Using the central bank balance sheet identifies we can write the

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 $B_c + Q E + S = M(L, L')W$ (II)

$$E_{ic} + c_i E_i + S_i = v_i (r, r') W'$$
 (12)

These four market equilibrium conditions are not

 Π σ'R' + S + Π S' is identically equal to W + Π W', so only three of l we obtain world wealth in dollar terms or W + Π W. \overline{B} + $\overline{\Pi}$ F + σR + If times l2 and taking account of the fact that b + f + m \equiv b' + f' + n' \equiv Π o'R' + S + Π S'. Adding the right hand sides of 9, 10, 11, and ultimate wealth holders, which can be expressed as $\overline{B} + \overline{\Pi} \, \overline{F} + \sigma R$ + ly we obtain the total dollar value for all assets available to independent. Adding the left hand sides of 9, 10, 11 and M times

to pay the interest on government securities when they calculate their that is, they do not take account of the fact that they will be taxed government securities they hold as part of their wealth or net worth; assumed that the residents of each of the two countries regard the levels of the residents of the U.S. and the U.K. respectively. It is In the text the symbols W and W' are used to refer to the wealth the four market equilibrium conditions are independent.

net worth. Under this assumption an open market operation which is

that in the short run the demand for money and securities (including as referring to the allocatable assets of the public. If we assume public but not its allocatable assets. Now let us reinterpret W and W' assumption open market operations would alter the net worth of the wealth holders which is net of discounted tax liabilities. Under this securities gross of discounted tax liabilities and the net worth of assets of wealth holders which include their holdings of government It is then useful to distinguish between the allocatable in their role as taxpayers treat government securities as their own an alternative treatment is adopted. Suppose private wealth holders reasonable assumptions our analysis is not substantially affected if This treatment affords considerable simplicity, but under some worth of the public. simply an exchange of securities for money does not affect the net

government securities) depends upon the level of allocatable wealth

spould be regarded as endogenous. clear from the situation being analyzed which three variables to be given exogenously. As the analysis proceeds it should be being endogenously determined and all the variables are considered and the stock of reserves held by the USCB (R) are regarded as one important case, for example, the two interest rates (r and r^{i}) the study depending upon the situation which is being analyzed. of three variables are taken to be endogenous at different stages in sufficient to determine three endogenous variables. Different sets Three independent market equilibrium conditions are

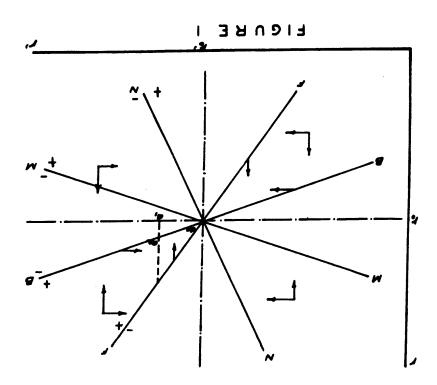
E. A Geometric Presentation of the Model

For most of what we do in the following chapters a geometric

which are compatible with equilibrium in each of the four financial Figure 1 we plot four schedules which show the pairs of r and r' under a fixed exchange rate system (II, o, and o' constant). presentation by using it to describe the equilibrium of the model to algebra in some of the later Chapters. We introduce the geometric presentation of the model will be sufficient though we will revert

1 Continued from previous page

which wealth holders regard their tax liabilities. materially affected by the assumptions made regarding the way in of models meant to refer to the medium or long run will be desires to accumulate on some net worth target then the results of a short run model. However, if wealth holders base their unaffected. This assumption seem quite reasonable in the context and is independent of the level of net worth then our analysis is



asset markets. The curve labeled BB gives the combinations of r and r' for which the private demand for securities issued in the U.S. is equal to the fixed supply of securities by the USCB. For a given supply of U.S. securities by the USCB. For a given supply of U.S. securities available for U.K. and U.S. residents to hold, an increase in the interest rate on U.S. securities must be accompanied by an increase in the interest rate on U.K. securities if private by an increase in the interest rate on U.K. securities if private wealth holders are to continue to be content to hold the available supply of U.S. securities. This is true because an increase in r causes an excess demand for U.S. securities so that r' must rise causes an excess demand for U.S. securities so that r' must rise

in order to cut demand back until it matches the fixed supply of U.S. securities to ultimate wealth holders. To the right of the BB curve there is an excess supply of U.S. securities, and to the left of BB there is excess demand for U.S. securities. A region which contains interest rate pairs that imply excess supply in a market is indicated by a minus sign near the schedule for that market in the relevant region of the diagram; a plus sign in a sector near in that sector imply excess demand. An excess supply of U.S. securities in that sector imply excess demand. An excess supply of U.S. securities in that sector imply excess demand for U.S. securities in the excess demand for U.S. securities in the excess demand for U.S. securities in the excess demand for U.S. securities tends to force down the U.S.

of r and r' which issue that the demand for securities issued in the U.K. is equal to the available supply given a fixed total supply and fixed holdings of U.K. securities by the UKCB. The FF curve is positively sloped; an increase in r is required to offset the excess

The curve labeled FF in Figure 1 represents the combinations

 $\underline{\underline{1}}$ Totally differentiating equation (9) with \overline{B} , B^c , Π , W, and W^i fixed and solving for the desired slope we have,

$$\frac{dx}{dx} \mid BB = -\frac{b_x}{b_x} \frac{W + \Pi b_x}{W + \Pi b_x} \frac{W}{W}.$$

pressure on r.

Given our assumption that the two securities are strict gross substitutes we have b_{r} , b_{r} < 0 and b_{r} , b_{r} > 0 so that $\frac{dr}{dr} > 0$.

demand caused by an increase in r' if private wealth holders are to continue to be satisfied holding the available supply of U.K. securities. The area to the right of the FF curve is an area of excess demand for U.K. securities; r' is too high given the level of r, and there is downward pressure on r'. For combinations of r and r' lying to the left of FF there is an excess supply of U.K. securities, and at any of these combinations upward pressure is exerted on r'. The horizontal arrows in Figure I represent the $\frac{2}{2}$ direction of pressure on the interest rate on U.K. securities.

holders in each of the two countries are strict gross substitutes insures that the slope of the FF curve must be greater than the slope of the BB curve. If r' is increased while r is held constant, there

The assumption that the three assets held by wealth

 $\overline{1}/$ Totally differentiating equation (10) with \overline{F} , F^c , Π , W, and W^i held fixed and solving for the desired slope we have,

$$\frac{d\mathbf{r}}{d\mathbf{r}'} = -\frac{\mathbf{f}_{\mathbf{r}} \mathbf{W} + \mathbf{\Pi} \mathbf{f}'_{\mathbf{r}} \mathbf{W}'}{\mathbf{f}_{\mathbf{r}} \mathbf{W}'_{\mathbf{r}} \mathbf{W}'}$$

The assumption that the two securities are strict gross substitutes insures that $\frac{1}{dr} |_{FF} > 0.$

 $\frac{2}{2}$ See the Appendix for a more detailed discussion of adjustment behavior.

of U.S. and U.K. money.

the excess demand for U.K. securities matches the excess supply than the BB curve as shown in Figure l. At point al in Figure 1, for U.K. securities is zero. Therefore the FF curve must be steeper of U.S. securities and both kinds of money when the excess demand reallocate their existing wealth. There cannot be an excess supply assets must sum to zero since, at a point in time, people can only sheet constraints for wealth holders. The excess supply for all not been crossed. However, this is inconsistent with the balance still be an excess supply of U.S. securities since the BB curve has the world excess demand for U.K. securities is zero, but there must is flatter than the BB curve. When the FF curve is encountered, Suppose that the FF curve is met first, that is, that the FF curve is raised both the FF and BB curves must be crossed eventually. substitute for U.S. and U.K. securities in both countries. As r the two kinds of money must increase since money is a strict gross supply of U.S. securities must decline. Also, the excess supply of level then the excess demand for U.K. securities and the excess and U.S. money. If now r is increased holding r' at its new higher U.K. securities and an excess supply of U S. securities, U.K. money, At the new, higher r' and constant r there is an excess demand for securities, the demand for money in each country must have fallen. assumed that money holdings are strict gross substitutes for of U.S. securities as at point al in Figure 1. Also, since it is Will be an excess demand for U.K. securities and an excess supply

Combinations of r and r' that equate the demand for and supply of U.S money, given a fixed U.S. money supply available for the public to hold, are plotted as the MM curve in Figure 1.

The MM curve is negatively sloped since an increase in either r

or r' reduces the demand for U.S. money. If the U.S. money market

Footnote from previous derived in the two preceding footnotes $\underline{1}\backslash$ Using the expressions derived in the two preceding footnotes

$$\frac{dx}{dx} \left| FF - \frac{dx}{dx} \right|_{BB} = -\frac{f_x W + \Pi f'_x W'}{f_x W + \Pi f'_x W'} + \frac{b_x W + \Pi b'_x W'}{b_x W + \Pi b'_x W'}.$$

Using the results of footnote l, p. l2, this difference can be rewritten as,

$$\frac{dx}{dx} \left| \frac{FF}{x} - \frac{dx}{dx} \right| BB = -\frac{(m_x + b_x)W + \Pi (n_x + b_y)W}{(m_x + b_y)W + \Pi (n_x + b_y)W} = -\frac{\pi}{x}$$

$$\frac{\mathbf{W}_{\mathbf{L}} \mathbf{W} + \mathbf{\Pi} \mathbf{b}_{\mathbf{L}} \mathbf{W}}{\mathbf{W}_{\mathbf{L}} \mathbf{W} + \mathbf{\Pi} \mathbf{b}_{\mathbf{L}} \mathbf{W}} +$$

Collecting terms we have,

$$\frac{dx}{dx} = \frac{dx}{dx} = BB = 0$$

$$\frac{\sum_{m_{1}, m_{2}, m_{1}, m_{2}, m_{2}, m_{1}, m_{2}, m_{1}, m_{2}, m_$$

The numerator of this expression is positive given our assumption that the three assets held by wealth holders are strict gross substitutes. Using the results of footnote l, p, l2, the first term in the denominator can be rewritten as $-(f_TW + \Pi f'_TW')$. Using the strict gross substitute assumption again we can determine that the denominator is positive. Thus the FF curve has a larger positive slope than the BB curve.

is to remain in equilibrium when interest rates change then r and $\frac{1}{1}/$ r' must move in opposite directions. The area to the right of MM is a sector of excess supply of home country money, and the area to the left is a region of excess demand.

excess demand.

 $\frac{1}{2}$ Totally differentiating equation (II) with B°, oR, and S held constant and solving for the required slope we have,

$$\frac{dr}{dr} - = MM = \frac{rb}{r}$$

Our strict gross substitutes assumption implies that this expression is negative.

 $\frac{2}{10}$ Totally differentiating equation (12) with F^{c} , $\sigma^{i}R^{i}$, and S^{i} held constant and solving for the required slope we have,

$$\frac{1}{1} \frac{1}{1} \frac{1}{1} u = \frac{1}{1} \frac{1}{1}$$

The strict gross substitutes assumption implies that this expression is negative.

In Figure 1 the MM curve, The slope of the MM curve is more negative) slope than the MM curve. The slope of the MM curve if and only if the ratio of the response of U.K. money demand to the rate on U.S. securities to the response of U.K. money demand to the rate on U.S. securities is greater than the ratio of U.S. money demand responses to these same $\frac{1}{2}$ rates. We assume that this condition is fulfilled. This rates.

1 - 1 Sing the results of the preceding two footnotes we have,

$$\frac{1}{2} \frac{1}{n} + \frac{1}{2m} - = \frac{1}{NN} \left| \frac{1}{2b} - \frac{1}{NM} \right| \frac{1}{2b}$$

This expression is positive, that is, the MM curve is flatter (less negatively sloped) if $m_{\rm L}\,^{\rm i}\,^{\rm i}\,^{\rm i}$ $< m_{\rm L}\,^{\rm i}\,^{\rm i}\,^{\rm i}$

 $\frac{2}{8}$ The condition for the MM curve to be flatter than the NN curve given in the previous footnote is met if $|m_{\rm L}| > |m_{\rm L}|$ and $|n_{\rm L}| > |n_{\rm L}|$.

We have argued above that the four market equilibrium conditions are not independent because of the balance sheet contraints faced by ultimate wealth holders. If three of the four markets are three of the fourth market must also be cleared. In geometric terms if three of the fourt schedules intersect at a common point in Figure 1, the fourth schedules intersect at a common point in Figure 1, analysis proceeds it will become clear that it is useful to retain analysis proceeds it will become clear that it is useful to retain all four schedules even though in a given situation three schedules are sufficient to determine the equilibrium values of the endogenous variables.

It is worth pointing out that interest rate changes above are not sufficient to insure that three independent schedules will have a common intersection point. There must be a third variable not shown explicitly on the graph which can change if we are to be sure that a common intersection point exists. One possibility, which will be explored further in what follows, is that the stock of reserves held by the USCB changes so as to guarantee that the MM schedule, and by implication the NN schedule, will pass through the point of intersection of the BB and FF schedules on the interest

rate coordinates.

III. The Outside Reserve Regime

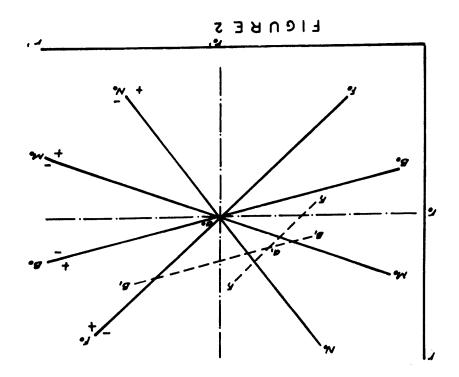
A. An Overview

In this Chapter we analyze the effects of disturbances to financial asset equilibrium in a regime under which all international reserves assets. Gold and reserves are held in the form of outside reserve assets. Under an outside reserve assets. Under an outside reserve assets. Under an outside reserve regime the total world supply of reserves (\overline{R}) is fixed in the short run so that, for example, if the U.S. gains reserves as the result of some disturbance, the U.K. must lose an equal amount of reserves $(\overline{R} = R + R')$. We turn first to consider the effect of a shift in the asset demands of ultimate wealth holders toward U.K. shift in the asset demands of ultimate wealth holders toward U.K.

B. The Effect of a Shift in Asset Preferences for Securities on

We can complete the first step in analyzing the effects of an exogenous shift in the asset preferences of wealth holders towards U.K. securities and away from U.S. securities on the basis of what we have learned so far. In Figure 2 the initial equilibrium pair of interest rates is given by the intersection of F_0F_0 , B_0B_0 , M_0M_0 , and interest rates is given by the intersection of F_0F_0 , B_0B_0 , M_0M_0 , and M_0M_0 . If there is a shift upward in the demand for U.K. securities while the supply of these securities to the public remains unchanged, the FF curve must shift to the left, say to F_1F_1 . A lower value of the FF curve must shift to the left, say to F_1F_1 . A lower value of

1/ In Chapter IV we study a key currency reserve regime under which the UKCB holds at least part of its reserves in the form of U.S. securities.



r' must be associated with each value of r after the shift in order to choke off the resulting excess demand. We assume that the upward shift in the demand for U.K. securities is matched by a downward shift of the same absolute magnitude in the demand for U.S. securities, the BB curve must shift of this decline in demand for U.S. securities, the BB curve must shift upward say to B_1B_1 . For each level of r' a higher level of r is required in order to raise demand for U.S. securities by enough to offset the original decline. The markets for both of the two

securities would be cleared at the intersection of the $\mathbf{F_1}^{\mathbf{F_1}}$ and $\mathbf{B_1}^{\mathbf{B_1}}$

scpedules.

region of excess demand for U.K. money and excess supply of U.S. We have drawn $\mathbf{F}_{\mathbf{I}}\mathbf{F}_{\mathbf{I}}$ and $\mathbf{B}_{\mathbf{I}}\mathbf{B}_{\mathbf{I}}$ so that they intersect in a

money. This must be the case. Since world excess demand for the

two kinds of securities is zero at the intersection of the FIFI and

 ${\mathtt B}^{\mathsf T}{\mathtt B}^{\mathsf J}$ curves, the excess demand for the two kinds of money must sum

to zero. If there is an excess supply of U.K.(U.S.) money, there

must be an excess demand for U.S.(U.K.) money. We have argued that

the assumed shift in asset demands will result in upward shifts in

both the FF and BB schedules. Given our assumption regarding the

relative slopes of the MM and MM schedules, FlF1 and BlB1 must

intersect at an interest rate pair at which there is an excess demand

for U.K. money and an excess supply of U.S. money.

If we allowed no change in any variables besides the two

interest rates, full equilibrium would be impossible since both

securities markets are cleared at the intersection of the $^{\mathrm{F}}_{1}^{\mathrm{F}}_{1}$ and

BlBl curves, and both money markets are cleared at the intersection

of the M_0M_0 and M_0M_0 curves, but these two intersection points do not

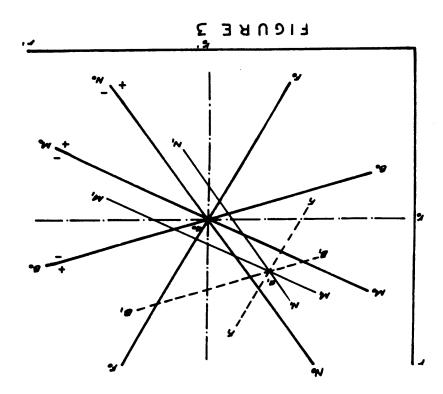
coincide. How this apparent dilemma is resolved depends crucially

consider in somewhat greater detail than we have up to this point. nbou the behavior of the two central banks which we must now

We consider first what we call the gold standard policy C. Policy Responses by the Central Banks response (GSPR). The shift in asset demands from U.S. to U.K. securities with the supplies of the two securities to the public unchanged leads to a selling off of U.S. securities which results in pounds place upward pressure on T. Sellers of U.S. securities attempting to buy pounds place upward pressure on T, the dollar price of pounds. To convert into outside reserve assets at the USCB. This operation extinguishes U.S. money and creates U.K. money in equal amounts in terms of dollars. Wealth holders bid for U.K. securities causing to fall. This process continues until the U.S. rate has risen rice of dollars. Wealth holders bid for U.K. securities causing with their altered asset preferences are willing to hold the still with their altered asset preferences are willing to hold the still with their altered asset preferences are willing to hold the still with their altered asset preferences are willing to hold the still

If both central banks employ a GSPR it is resolved by a decrease in the U.S. money stock and an increase in the U.K. money stock. In graphical terms MM and MN shift from M_0M_0 and M_0M_0 to M_1M_1 and M_1M_1 as in Figure 3. Decreases in the U.S. money stock result in upward shifts in the MM curve; for each r' there must be a higher r if demand for U.S. money is to shrink to match the reduced supply. Increases in the U.K. money stock necessitate leftward shifts in MN since for in the U.K. money stock necessitate leftward shifts in MN since for the U.S. money stock necessitate if demand for U.K. money is to rise each r there must be a lower r' if demand for U.K. money is to rise to equal the increased supply. We know that the U.S. money stock

What of the dilemma posed at the end of the last section?



decrease which is sufficient to insure that the U.S. money market clears at the intersection of $\mathbb{F}_1\mathbb{F}_1$ and $\mathbb{B}_1\mathbb{B}_1$ is exactly the same as the U.K. money supply increase which is sufficient to make the U.K. money market clear at the same intersection point from the fact that only three of the four market equilibrium conditions

are independent.

When both central banks employ a GSPR, the new equilibrium interest rate pair is the combination which clears the two securities markets given the shifts in asset demands. Some U.K. wealth holders

who held U.K. securities before the shift have willingly reduced their holdings to accomodate the new demand because r' is lower. They are induced to hold either U.S. securities sold off by dissatisfied holders because r is higher or U.K. money given the

dissatisfied holders because r is higher or U.K. money given the new configuration of r and r'. Some U.S. wealth holders hold more U.S. securities and fewer U.K. securities and less U.S. money at the new r, r' combination. Changes in the central banks' holdings of reserves match the adjustments in both countries' money supplies which are necessary for the reattainment of equilibrium when both central banks are pursuing a GSPR. It is important to notice that central banks are pursuing a GSPR. It is important to notice that

One of the central banks may, however, be unwilling to allow its money supply to change by as much as would be required under a GSPR. Suppose that the UKCB believes that its money supply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might pursuapply is "just right" for domestic purposes; then it might purposes is the purpose of the purpos

employing a GSPR.

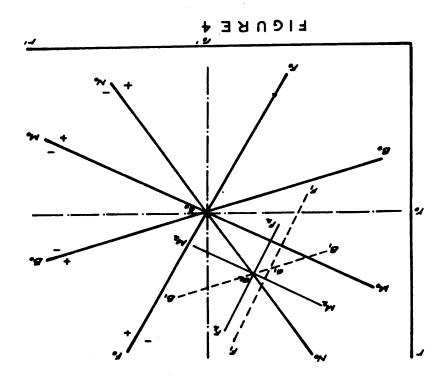
supply is "just right" for domestic purposes; then it might pursue a money supply constant policy response (MSCPR). We continue to assume that the USCB pursues a GSPR. Under these assumptions an of U.S. securities, an increase in r, upward pressure on II, and a decrease in the U.S. money supply with an accompanying outflow of international reserves. However, there is no increase in the U.K. money supply since the UKCB stands ready to sell as many U.K. secunities from its holdings as necessary to keep Ns' constant. In this rittes from its holdings as necessary to keep Ns' constant. In this

case the U.S. interest rate is higher, the U.K. interest rate is higher, the U.S. money supply is lower, and the U.K. money supply is lower when the new equilibrium is reached than was the case when both countries reacted according to the GSPR.

The dilemma posed at the end of the last section is resolved in a different way when the U.K. pursues a MSCPR. We know that following the demand shift FF and BB shift to $\mathbb{F}_1^{F_1}$ and \mathbb{B}_1^B and that MM and MM remain in their original positions, $\mathbb{M}_0\mathbb{M}_0$ and $\mathbb{M}_0\mathbb{M}_0$. We also know that given the policy response of the UKCB, $\mathbb{M}_0\mathbb{M}_0$ will not be shifted in the new equilibrium. In addition the supply of U.S. securities does not change so that once BB has shifted to finderest rate pair is given by the intersection of $\mathbb{M}_0\mathbb{M}_0$ and \mathbb{B}_1^B interest rate pair is given by the intersection of $\mathbb{M}_0\mathbb{M}_0$ and \mathbb{B}_1^B in a shift of MM to $\mathbb{M}_2\mathbb{M}_2$ while the sales of U.K. securities by the UKCB required to keep the U.K. money supply unchanged imply a shift of FF from \mathbb{F}_1^F to \mathbb{F}_2^F ?

The important difference between the current case and the case in which both central banks use a GSPR arises because the supply of U.K. securities available to the public is increased by the UKCB.

This increase in supply reduces to some extent the amount by which r' falls. However, the constant supply of U.S. securities must be held in equilibrium, so r must rise by more than before in order to assure that it will be held. The U.S. money stock must decline by



more and the U.K. money stock must rise by less than in the previous case since wealth holders as a group must be willing to hold more securities and less money in their portfolios than when the UKCB employed a gold standard policy response. The larger decline in the U.S. money stock implies a larger U.S. reserve loss than before. In contrast to the case in which both central banks pursued a GSPR in contrast to the case in which both central banks pursued a GSPR the UKCB holdings of U.K. securities are reduced.

Instead of trying to stabilize the outstanding stock of

constant policy response (IRCPR). We continue to assume that the

its monetary liabilities the UKCB might follow an interest rate

USCB employs a GSPR. Following the asset demand shift, all the same pressures arise as in the two previous cases, but now, instead of keeping its holdings of U.K. securities constant the UKCB sells securities to keep the U.K. money stock constant the UKCB sells enough securities to keep r' from falling at all. In this case the U.S. interest rate must rise even more than in the previous case and \frac{1}{\infty} \text{ interest rate must rise even more than in the previous case and \frac{1}{\infty} \text{ interest rate must rish.}

The graphical analysis in this case is slightly more difficult than it was in the two previous cases. Following the asset is $B_1 B_1$ in Figure 5. We know that the $B_1 B_1$ and the relevant $B_2 B_3$ curve must remain fixed since there is no change in the supply of U.S. securities to the public. We also know that the UKCB will increase the supply of U.K. securities to the public by whatever amount is necessary to insure that $E_1 B_2 B_3$ remains constant. The means that the new $E_2 B_3 B_3$ curve designated $E_3 E_3 B_4$ must intersect $E_3 E_3 B_4$ at the point as where $E_3 E_3 E_4$ curve designated $E_3 E_5 E_5$ line which passes through the original equilibrium point and which is parallel to the raxis. The MM and NN curves must therefore shift param $E_3 E_5 E_5$ should be a said $E_3 E_5 E_5$ and $E_3 E_5 E_5$ should be the raxis. The MM and NN curves must therefore shift param $E_5 E_5$ should $E_5 E_5$ should be said of E_5

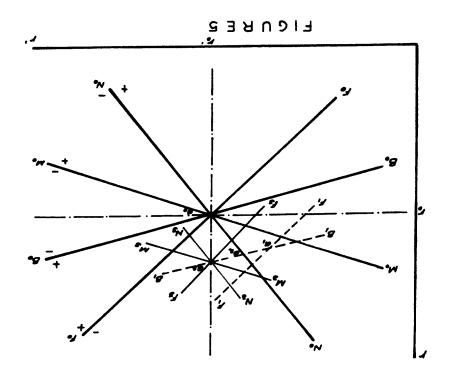
In this case we have the largest increase of any of the cases considered so far in the U.S. interest rate; it must rise by enough to remove the excess supply for U.S. securities since there is

 $\frac{1}{\lambda}$ Note that if the NN curve is vertical $(n)_{r} = 0$) then the results of a MSCPR and a IRCPR by the UKCB are the same.

The analysis up to this point highlights the fact that, although equilibrium is reattained in each of the three cases the impacts of the asset demand shift on the two countries' money supplies

D. Policy Responses and Target Variables

no movement in r' to help reduce the excess supply. The U.S. money stock must decline further than in any of the other cases, and the U.K. money stock must decline instead of rising because wealth holders as a group must hold an even larger amount of securities in their portfolios than they had to hold when the UKCB pursued a MSCPR.



rather than an IRCPR. the USCB, the UKCB might well choose to follow a MSCPR or even a GSPR target variable from its desired value to reduce the discomfiture of the UKCB is willing to experience some deviation of its proximate UKCB knows that the USCB is going to continue to pursue a GSPR and it the U.S. interest rate is driven away from its desired value. If the the U.K. interest rate while the USCB stubbornly sticks to a GSPR uses its single instrument to try to reattain the desired value of of discussion we are taking to be their desired levels. If UKCB countries are disturbed from their initial levels which for purposes holdings of domestic liabilities constant interest rates in both it holds. When both central banks pursue a GSPR, that is, keep their policy instrument, the amount of liabilities of domestic residents that rate of inflation. In our analysis each central bank has only one variables in its country such as the rate of unemployment and the from the point of view of the desired values of the ultimate target securities issued by residents of its country, to be exactly right target variable in its country, for example, the interest rate on shift the USCB and the UKCB each considered the level of the proximate and interest rates are quite different. Suppose that before the demand

However, there is a set of policy responses by the two central banks which affords an even happier resolution to the apparent conflict created by the assumed shift in asset demands. Suppose both central banks pursue an IRCPR, that is, that they both stand ready to

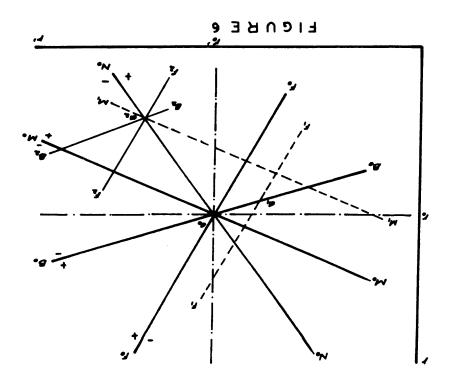
buy or sell enough securities issued in their own countries to stabilize the interest rate on those securities. In this case FF and BB lift from Γ_1^F and B_1B_1 back to Γ_0F_0 and B_0B_0 , and MM and MW sad stay fixed at M_0M_0 and M_0M_0 . Thus the two interest rate targets can both be attained if the central banks properly employ their two policy instruments. It is interesting to note that in this case keeping interest rates constant implies keeping money stocks constant. The same equilibrium point is reached if both central banks pursue an IRCPR or if they pursue a MSCPR.

E. Another Type of Shift in Asset Demands

Lt is not in general true that keeping both interest rates constant implies keeping both money stocks constant. To demonstrate this contention we consider a shift in the asset demands of U.S. wealth holders toward U.K. securities and away from U.S. money.

This shift in asset demand functions given fixed asset

supplies leads to shifts in MM and FF from M_0M_0 and F_0F_0 to M_1M_1 and F_1F_1 in Figure 6. If both central banks pursue an IRCPR all the schedules must intersect at the same point after adjustment is complete as they did before the disturbance. MM and FF must shift back from M_1M_1 and F_1F_1 to M_0M_0 and F_0F_0 . The USCB keeps its holdings of U.S. securities unchanged and allows the U.S. money supply to decline by the full amount of the original shift in asset demands. This is also the full amount of the original shift in order to prevent any decline in the UKCB must sell an amount of U.K. securities equal to the shift in asset demands. The UKCB must sell an amount of U.K. securities equal to the shift in asset demands. The U.K. money supply remains unchanged.



However, if both central banks pursue a MSCPR the new equilibrium interest rate pair is given by the intersection of M_1M_1 and M_0M_0 . BB and FF shift to B_2B_2 and F_2F_2 respectively. The USCB buys enough U.S. securities to offset the decline in the U.S. money supply which would otherwise result from the fact that the UKCB acquires and converts into reserve assets the dollars which U.S. citizens want to sell as a result of the shift in asset demands. The UKCB sells U.K. securities equal to the amount of pounds it sells to U.S. wealth holders. The increased supply of U.K. securities and diminished supply of U.S. securities resulting from the money stock

stabilization operations of the central banks will only be held by wealth holders if r falls and r' rises even when account is taken of the increased demand for U.K. securities. The U.S. loses reserves equal to the amount of U.S. securities the USCB must purchase in order to shift the BB curve from $^{6}0^{8}$ 0 to $^{8}2^{8}$ 2.

If both the MM and MM curves shift while the BB and FF curves stay fixed, an IRCPR by both central banks implies that both money stocks must change while a MSCPR by both central banks implies that both interest rates must change.

We can draw a general conclusion regarding cases in which

shifts in asset demands involve net shifts in only two schedules.

Under our assumptions so far whenever shifts in asset demands involve only shifts in demands for securities stabilizing interest rates implies stabilizing money supplies in the hands of the public and vice versa but whenever shifts in asset demands involve a shift in at least one money demand function stabilizing interest rates will involve a change in the supply held by the public of at least one of the two kinds of money in the model while stabilizing money of the two kinds of money in the public will involve a change in both

I) Both MM and MM could shift with no net shift in FF or BB if, for example, U.S. wealth holders asset demands shift in favor of U.K. securities at the expense of U.S. money and U.K. wealth holders experience a simultaneous shift in asset demand in favor of U.K. money at the expense of U.K. securities.

interest rates. This conclusion is consistent with the well known proposition from the theory of economic policy that if only two policy instruments are available, as in the present case, then all possible shocks to the system are considered. What our conclusion suggests is that for certain kinds of shocks more than two of only two policy instruments. If the initial levels by the use target variables can be returned to their initial levels by the use of only two policy instruments. If the initial levels by the use of only two policy instruments. If the initial levels by the use variables happen to be the desired levels, the cost to the two central banks of having fewer policy instruments than potential target

rities held by the public really are. emphasize the need for asking how important the supplies of secu-"equal" role in the analysis as our model attempts to do helps to to answer here. We only remark that giving "securities" a more is an interesting and unresolved question which we will not attempt to central banks' attention as "rates" and "monetary aggregates" hands of the public are variables which should have the same claim Whether or not the supplies of the two types of securities in the analysis to other available treatments of the same or similar issues. emphasize the importance of "monetary aggregates" to relate our emphasize the importance of "rates" and those who prefer to interest rates. This approach allows those readers who prefer to banks except in so far as those supplies affect money supplies and held by the public was a matter of indifference to the two central public and proceed as if the supplies of the two types of securities rates and on the supplies of the two types of money held by the We have focused our attention on the levels of the two interest

F. The Reserve Stock Constant Policy Response

For convenience in exposition we have been ignoring one type of possible policy response. Assume again that asset demands have shifted in favor of U.K. securities at the expense of U.S. securities and that the USCB is employing a CSPR. We know that as pressure on the U.S. rate and upward pressure on II as wealth holders try to sell off U.S. securities there is upward pressure on the U.S. rate and upward pressure on II as wealth holders convert the proceeds of their sales of U.S. securities into pounds. In each of the cases in Section C the U.S. money stock fell and the U.S. lost reserves of the same amount during the adjustment following asset demand shifts of the type being considered here. However, if the UKCB is satisfied with its holdings of international reserves, it might take steps to prevent any further accumulations of reserves; that is, it might pursue a reserve stock constant

In order to insure that its stock of reserves does not change the UKCB must add to the excess demand for U.K. securities. Although this result seems at first to be somewhat paradoxical, it can be easily explained. Since it is following a GSPR the USCB does nothing to directly affect the U.S. money stock. Thus if the U.S. money stock declines it is because the UKCB has had to buy dollars in the exchange market and, therefore, under our assumptions has added to its stock of outside reserves by converting the dollars at the USCB. All this means that in order to insure that

policy response (RSCPR).

its reserve stock does not change the UKCB must see to it that U.S. citizens are content to hold the money stock which they held before

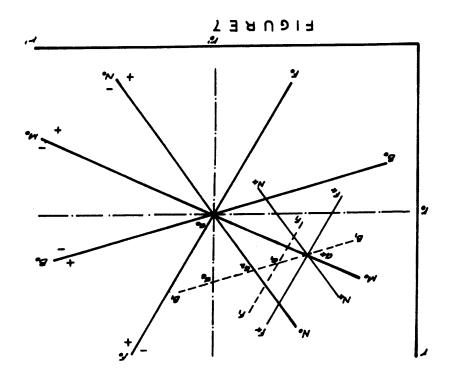
We know from our analysis in Section B of the case in which both countries pursue a GSPR after an asset demand shift of the kind considered here that if both countries do not change their holdings of domestic liabilities, the U.S. interest rate rises, the U.K. interest rate falls, and the U.S. money stock falls. Since the USCB is assumed to be pursuing a GSPR here, the UKCB must pursue an expansionary open market operation in order to drive r' down far enough so that U.S. citizens are persuaded to hold as much money as enough so that U.S. citizens are persuaded to hold as much money as they did before the shift in asset demands even though r rises somewhat.

 F_0F_0 and B_0B_0 to F_1F_1 and B_1B_1 as shown in Figure 7. In order to keep its stock of reserves constant the UKCB must purchase enough domestic liabilities to drive F_1 from F_1F_1 to F_4F_4 and F_1 from F_1F_1 to F_4F_4 and F_1 from F_1F_1 to F_4F_4 and F_1F_1 to F_4F_4 . Wealth holders as a group must hold fewer securities. U.S.

wealth holders take up part of the initial excess supply of U.S. securities and surrender some U.K. securities but hold the same amount of money as before the demand shift. U.K. wealth holders take up the rest of the initial excess supply of U.S. securities and increase their holdings of U.K. money while reducing their holdings

of U.K. securities.

the shift in asset demands.



G. Policy Responses and Policy Initiatives $\label{eq:concerned} U_{p} \text{ to this point we have concerned ourselves with the}$

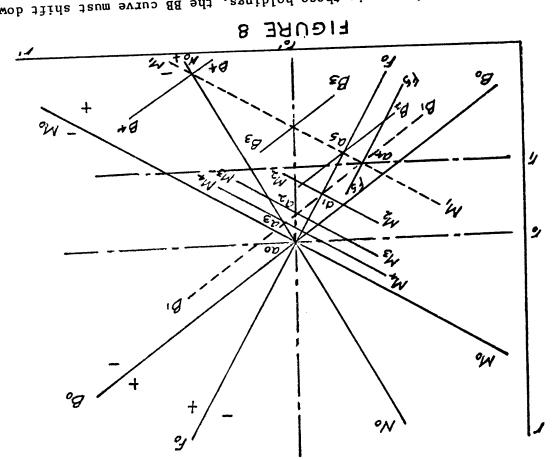
that we now turn,

implications of the way in which central banks respond to disturbances to asset equilibrium which take the form of shifts in asset demands. When we treated central bank objectives, we assumed that in the initial equilibrium at least two target variables had their desired values. If some target variables do not have their desired values in the existing equilibrium or if the desired values for some target variables change for any reason, central banks may wish to undertake variables in the contral banks may wish to undertake variables in the contral banks may wish to undertake

It is useful to consider the correspondence between policy

other central bank, taking it depending upon the policy response being pursued by the for the money stock and the interest rate of the country undergiven size. This policy initiative will have different implications which corresponds to the GSPR is an open market operation of a purchase of a given size by the central bank. The policy initiative call a gold standard policy initiative (GSPI), is just an open market assets at a new higher level. This policy initiative, which we will additional domestic assets and to stabilize its holdings of domestic have been too contractionary. It might decide to purchase some response but decides that the results of its behavior for the economy Suppose that a central bank has been following this kind of policy have called a GSPR a domestic assets constant policy response. as the result of disturbances to asset equilibrium. We could as well reserves, and the interest rate on domestic assets which occur accepts passively the changes in its money supply, international central bank keeps its holdings of domestic assets constant and response and policy initiatives. If it is following a GSPR, a

Using Figure 8 we can trace the implications of different U.K. policy responses to a GSPI undertaken by the U.S. As before, the initial equilibrium position is given by the intersection of the curves with the (0) subscript. If the U.S. authorities plan to increase their holdings of U.S. aecurities by a given amount and then to allow



equilibrium is at the intersection of M_0M_0 and B_1B_1 at point ag.

will be at point a2. If the UKCB decides to pursue a MSCPR, the new

at point a_1 . An IRCPR by the UKCB implies that the new equilibrium

follows a GSPR, that is, if they neither buy nor sell U.K. securities,

a GSPI, the new equilibrium must be on the new BB curve. If the UKCB

say from B_0B_0 to B_1B_1 since, for a given value of r', the public will

hold a reduced supply of U.S. securities only if r is lower. Following

the new equilibrium is given by the intersection of ${
m F}_0{
m F}_0$ and ${
m B}_1{
m B}_1$

no further changes in these holdings, the BB curve must shift down,

UKCB. residents is removed depends upon the policy response pursued by the rate combination. How this imbalance in the portfolios of U.S. satisfied with their holdings of money and securities at this interest original interest rate pair ro, ro whereas U.K. residents are excess supply of money and an excess demand for securities at the following the open market purchase U.S. wealth holders have an only if r is lower. Our assumption also implies that immediately wealth holders will voluntarily hold the increased supply of money BOBO to BIBI, MM must shift from MoMo to MiMI. For a given r', U.S. model. Our assumption means that, in addition to the shift of BB from folio as he likes. This fiction in no way affects the results of the securities for U.S. money but that he is then free to adjust his port-USCB tells each U.S. wealth holder that he must trade some of his U.S. it wants from U.S. wealth holders at unchanged interest rates. we adopt the convenient fiction that the USCB purchases the securities In order to facilitate further exposition of these results

First consider the case in which the UKCB follows a GSPR under which it passively accepts whatever changes occur in the U.K. money stock and the U.K. interest rate and keeps its holdings of domestic liabilities constant. As U.S. wealth holders reduce their excess money holdings by making net purchases of securities from U.K. residents downward pressure is exerted on both of the interest rates

 $\frac{1}{2}$. More specifically U.S. wealth holders have an excess demand for U.S. securities. They are satisfied with their holdings of U.K. securities at the original interest rate pair.

operations into reserve assets. UKCB converts the proceeds of its exchange rate stabilization loses reserves equal to the decline in the U.S. money supply as the through al the point of intersection of BlBl and FOFO. purchase is shown by the shift of MM from M1M1 to M2M2 which passes stock from the level it reaches immediately following the open market because of the lower interest rates. The decline in the U.S. money willing to surrender these securities and hold more U.K. money partly by net purchases of securities from U.K. residents who are interest rate declines which raise the U.S. demand for money and initial excess supply of money in the U.S. is removed partly by neither central bank pursues any offsetting measures. Thus the supply and raises the U.K. money supply by equal amounts since buy dollars for pounds, an action which reduces the U.S. money order to keep the dollar price of pounds from rising the UKCB must and upward pressure is exerted on the dollar price of pounds.

Suppose now that the UKCB reacts to an open market purchase by the USCB with an IRCPR. As before there is downward pressure on Doth interest rates and upward pressure on II, the dollar price of pounds, as U.S. wealth holders make net purchases of securities from U.K. residents. The UKCB sells pounds to relieve the upward pressure on II, and, in contrast to the previous case, supplies U.K. securities to private wealth holders in the amount required to keep r' from falling.

a part of that fraction of the U.S. money stock which it absorbs and supply declines more in this case. The UKCB, in effect, replaces because both interest rates are higher and since the U.S. money be the case since equilibrium U.K. money demand is less than before do not rise as much as U.S. money holdings have tallen. This must contrast to what we observed in the previous case, U.K. money holdings larger loss of reserves by the U.S. It is important to note that, in Corresponding to the larger decline in the U.S. money supply is a syilt of MM from M_1M_1 to M_3M_3 which passes through point a2. and the UKCB. The decline in the U.S. money stock is shown by the money is removed by net purchases of securities from U.K. residents the U.S. demand for money and more of the initial excess supply of money in the U.S. is removed by interest rate declines which raise this case as it did before, less of the initial excess supply of was pursuing a GSPR. Since neither interest rate falls as far in with a reduced supply of U.S. securities as it did when the UKCB r need not fall as far in order for wealth holders to be satisfied supply must be greater in this case. Since the UKCB is stabilizing r', the U.K. money supply rises, but the reduction in the U.S. money omitted the new FF curve. Here again the U.S. money supply falls and the original equilibrium point and parallel to the r axis. We have it passes through as where BlB1 intersects the dashed line drawn through This provision of securities by the UKCB shifts FF down from ${
m F}_0{
m F}_0$ until

extinguishes with U.K. securities and the rest with U.K. money instead

of simply taking in dollars and supplying pounds. The mix of assets available to the world's wealth holders contains more securities and less money than it did immediately following the policy initiative.

While the UKCB allows some increase to occur in the U.K.

the MM curve which passes through point ag. The corresponding reserve money stock in this case is shown by the shift of MM from M_1M_1 to M_4M_4 , pursued an IRCPR. The larger magnitude of the decline in the U.S. from U.K. residents and the UKCB than was the case when the UKCB money and even more must find its way into securities via net purchases excess supply of money in the U.S. is removed by increased demand for either of the two previous cases. Thus even less of the original hold the smaller supply of U.S. securities, but not as tar as in r must still fall in order for wealth holders to be content to undertaken implies that r' must be higher in the new equilibrium. in the previous cases. The fact that larger open market sales are involve even larger open market sales by the UKCB than were required woush stock, so preventing an increase in the money stock must we have seen, stabilizing r' involves some increase in the U.K. of BlBl and NoWo at point ag. The new FF curve is not shown. As operation shifts FF down until it passes through the intersection equal in pound value to the dollars it absorbs. This sterilization run down their excess money balances, the UKCB sells U.K. securities at all when it pursues a MSCPR. Forced to support II as U.S. citizens money stock when it pursues an IRCPR, it acts to prevent any increase

loss is, of course, larger here too. The actions of the UKCB when it follows a MSCPR represent the polar opposite of its actions in the GSPR case. Instead of being content to trade U.K. money for U.S. money the UKCB takes measures which are tantamount to replacing the fraction of the U.S. money stock which it receives through the exchange market with U.K. securities. The final mix of money and securities available to wealth holders is more like the original mix before the policy initiative than in the other two cases. The equilibrium world supply of securities contains a relatively higher equilibrium world supply of securities contains a relatively higher equilibrium of U.K. securities than it did in either of the other two cases or in the original position.

response, a RSCPR. In order to keep from gaining reserves the UKCB must see to it that interest rates move so as to make U.S. residents content with the money holdings they acquire as a result of the net purchases of securities from U.K. residents. When the UKCB net purchases of securities from U.K. residents will not make any detects downward pressure on r' and upward pressure on Π , it must add to the downward pressure on r' by buying U.K. securities so as to make to the downward pressure on r' by buying U.K. securities and U.S. U.K. securities less attractive relative to U.S. securities and U.S. securities of schieve its desired result the UKCB must buy enough securities to shift FF from F0F0 to F_5F_5 so that it passes through the intersection of B_1B_1 and M_1M_1 at point $a_{\bf t}$. Since the supplies of both securities are reduced both interest rates must end up lower than both securities are reduced both interest rates must end up lower than

We know that the UKCB can pursue a fourth kind of policy

in the original position. At these lower rates U.K. residents are content to increase their money holdings by an amount equal to the open market purchases of the USCB. They must do so since U.S. residents make no net purchases or sales of securities after the original sale called for by the GSPI.

There are policy initiatives which correspond to the other

types of policy responses besides the GSPR. For instance, if a scentral bank has been following a MSCPR, that is, if it has been sterilizing all gains and losses in international reserves, but concludes that, although this is the right rule for its behavior, it impacts of disturbances, it might pursue the necessary actions to involves the domestic money supply is stabilized at a new higher but what differentiates it from a GSPI is that a new value for the noney stock rather than a new value for the course, of domestic securities in the open market, but what differentiates it from a GSPI is that a new value for the of domestic assets is the objective. Achieving the new target of domestic sasets is the objective. Achieving the new target of domestic assets is the objective. Achieving the new target of domestic assets is the objective. Achieving the new target of domestic assets is the objective. Achieving the new target of domestic assets is the objective. Achieving the new target of domestic assets is the objective. Achieving the new target of the money stock will involve different sized open market.

the other central bank.

Since we explored the implications of different policy responses to a GSPI in some detail, we provide a somewhat briefer account of how different policy responses affect the results of a

A GSPR by the UKCB implies that it undertakes no open market same implications for all the variables in the model. pursuing a RSCPR, then a GSPI and a MSCPI of the same size have the original open market purchase by the USCB. Note that if the UKCB is hold the entire increase in U.S. money supply brought about by the interest rates down far enough that U.S. residents are content to residents because the UKCB purchases enough U.K. securities to drive residents end up making no net purchase of securities from U.K. purchase shifts BB from BOBO to BlBI and MM from MoMo to MiMi. U.S. of the increase in the money supply it desires. The open market represented by M_1M_1 by an open market purchase of exactly the amount the UKCB pursues a RSCPR, the USCB can achieve the money supply of a MSCPI possible new equilibria must be on the M₁M₁ curve. If case of a GSPI equilibrium points had to be on BlBl in the case decides to raise it to the level represented by M_1M_1 . While in the keeping the U.S. money stock at the level represented by M_0M_0 but MSCPI. We refer again to Figure 8. Suppose the USCB has been

A GSPR by the UKCB implies that it undertakes no open market operations. As we know from above, the ultimate increase in the U.S. money stock following an open purchase by the USCB is less than the size of open market purchase when the UKCB follows a GSPR. Thus in order to obtain an increase in the U.S. money stock from the level represented by M_0M_0 to the level represented by M_1M_1 the USCB must neepersented by M_0M_0 to the level represented by M_1M_1 the USCB must make an open market purchase larger than the desired increase in the money stock. The relative size of the required purchase is indicated

represented by the gap between $_{\rm B}{}_{\rm I}{}_{\rm B}{}_{\rm I}$ and $_{\rm B}{}_{\rm B}{}_{\rm S}$. exceeded the target increase in the money stock, it can also be just equal to the amount by which the original open market purchase Since the reduction in the U.S. money supply or the U.S. reserve loss is which are equal to U.S. reserve losses, cause MM to shift back to M_1M_1 . from U.K. residents. The net purchase of securities by U.S. residents, point as and partly by net purchases of securities by U.S. residents decline in interest rates from \mathbf{r}_0 , \mathbf{r}_1 to the levels represented by securities in the U.S. This excess supply is removed partly by a by the USCB there is an excess supply of money and an excess demand for bosition (not shown) below $\mathbf{W}^{\mathsf{I}}\mathbf{W}^{\mathsf{J}}$. Just after the open market purchase ober market purchase represented by B_2B_2 the MM curve is shifted to a corresponding to B_2B_2 must lie below MIMI. Immediately following the furersects $E_0 E_0$ and which lies below $B_1 B_1$. The MM curve which passes through the new equilibrium point at as where $M_1^{\rm I}M_1^{\rm I}$ ph the fact that the BB curve must be shifted from $^{0}\mathrm{B}^{0}$ to $^{0}\mathrm{B}^{5}$

A completely analogous method of argument can be used to show that the USCB must make even larger open market purchases to achieve the money supply represented by M_1M_1 if the UKCB pursues an IRCPR or a MSCPR. The successively larger U.S. reserve losses are represented by the gap between B_1B_1 and B_3B_3 and the gap between B_1B_1 and B_4B_4 in these two cases. These results arise because, as we have seen above, successively more of any initial increase in the U.S. money supply successively more of any initial increase in the U.S. money supply resulting from an open market purchase of a given size is extinguished

Schedules and points with the same labels represent the same assumptions about policy initiatives and policy responses in Figures 8 and 9.

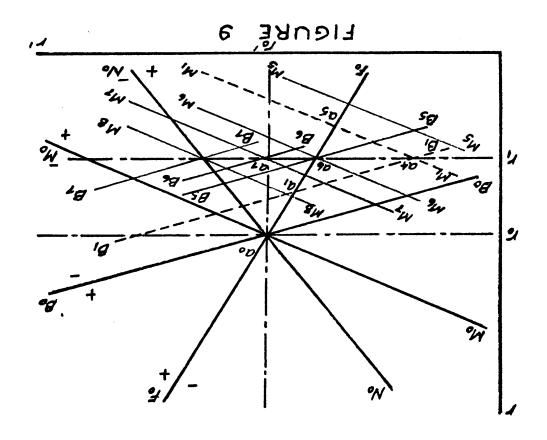
the UKCB pursues a RSCPR.

policy responses with the size of the open market purchase required when the USCB which are required to achieve rl when the UKCB pursues other It is interesting to compare the sizes of the open market purchases by to B₁B₁ or the MSP1 corresponding to M₁M₁ if the UKCB follows a RSCPR. is the interest rate which would emerge from the GSPI corresponding through point $a_{\underline{d}}$ parallel to the r' axis. We have chosen $r_{\underline{1}}$ because it different policy responses by the UKCB lie along the dashed line drawn ${}^{B_1}{}^{B_1}$, and for the MSCPI it was ${}^{M_1}{}^{M_1}$. In this case the equilibria for by the UKCB lay along a single line in Figure 8; for the GSPI it was were reached after the policy initiative and various policy responses policy initiatives by the USCB considered above the equilibria which USCB wants to lower r from r₀ to r₁ in Figure 9. Under both types of policy response being followed by the other central bank. Suppose the will involve different sized open market purchases depending upon the has been pursuing an IRCPR. An expansionary IRCPI by one central bank and maintaining of a new domestic interest rate by a central bank which interest rate constant policy initiative (IRCPI) involves the setting

by net purchases of securities by U.S. residents as we move from a GSPR by the UKCB to an IRCPR and then to a MSCPR. Larger and larger open market purchases, with the accompanying increases in reserve losses, are required to raise the money supply by a given amount as we consider this sequence of policy responses.

Following the logic employed so far we can see that an

Suppose the UKCB is following a GSPR. Our earlier analysis revealed that the GSPI by the USCB associated with B_1B_1 would lead to an equilibrium at point a_1 where r is higher than r_1 . The MSCPI corresponthan to M_1M_1 results in a new equilibrium at point a_5 where r is lower than r_1 . The open market purchase required to achieve r_1 is the one associated with B_5B_5 in Figure 9. This open market purchase is larger than the one associated with a_1 but smaller than the one associated with a_2 is drawn so that it passes through a_5 , the point of intersection of the dashed line drawn so that it passes point a_4 and so that it is of the dashed line drawn so that it passes point a_4 and so that it is



loss associated with the IRCPI when the UKCB pursues a GSPR is equal to securities by U.S. residents. The final MM curve is M_6M_6 . The reserve interest rates from (r_0, r_1) , and part is removed by net purchases of part of the excess supply for money is removed by the decline in and excess demand for securities in the U.S. Point a_6 is reached as operation we have the by now familiar pattern of excess supply of money following the open market purchase is M_{SM}_{S} . Following the open market

amount of the open market purchase represented by the movement from supply decline represented by the shift from M_1^{LM} to M_6^{LM} and the from $M_{S}M_{S}$ to $M_{6}M_{6}$ or, what is the same thing, the sum of the money the money supply decline associated with the movement in the MM curve

Using the same method of argument we can show that the BIBI to BSBS.

corresponding to the shifts from $^{\rm B}_{\rm I}^{\rm B}_{\rm I}$ to $^{\rm B}_{\rm I}^{\rm B}_{\rm I}$ and from $^{\rm M}_{\rm I}^{\rm M}_{\rm I}$ to $^{\rm M}_{\rm S}^{\rm M}_{\rm S}$ to B_6B_6 and from M₁M₁ to M₇M₇ under an IRCPR and by summing the amounts are given by summing the amounts represented by the shifts from $^{\mathrm{B}}\mathrm{I}^{\mathrm{B}}\mathrm{I}$ operation of a given size. The successively larger U.S. reserve losses which relieves the downward pressure on r generated by an open market the objectives of the UKCB lead it to sell U.K. securities, an action open market purchases are required in each of these two cases because reach r_l if the UKCB follows an IRCPR or a MSCPR. More substational USCB must undertake more substantial open market purchases in order to

under a MSCPR.

Corresponding to the RSCPR there is a reserve stock constant policy initiative (RSCPI). For example, a central bank which has been determined in the past to maintain a given stock of international reserves might decide that it now wants a smaller stock of international reserves.

There is an important difference between the RSCPI and other policy initiatives we have considered. If the USCB wants to undertake a GSPI, a MSCPI, or an IRCPI, it can accomplish its objective no matter which of the four types of policy response are pursued by the UKCB.

USCB depending upon the type of policy response being pursued by the the UKCB, but the objective can be achieved. The same cannot be said for an RSCPI. When the only reserves in the system are outside assets which are fixed in supply, one central bank can only increase its which are fixed in supply, one central bank is willing to reduce assets to an RSCPI. Thus a RSCPI is consistent with a GSPR, a MSCPR, or an its holdings. Thus a RSCPI is consistent with a GSPR, a MSCPR, or an its holdings. Thus a match and make the analysis of reserves if the other central bank is willing to reduce the match and make the match as a match and make the match and make the match and match and make the match and make the match and match and make the match and make the match and match and make the match and make the match and match and make the match and make the match and match and

central bank would undertake purchases of domestic liabilities in the open market. Exactly what the magnitude of these purchases would pursuing a GSPR a MSCPR, or an IRCPR. There is little need to show this in detail since a careful study of the cases already considered can reveal what is involved in a RSCPI. An example will suffice.

In order to achieve a decrease in reserves the "active"

Refer again to Figure 8. Suppose the U.S. wants to lose reserves in the amount corresponding to the shift from M_IM_I to M₂M₂ and it has reason to believe that the U.K. will react with a GSPR. The USCB should then pursue open market purchases large enough to shift BB to B_1B_1 and analysis above should convince the reader that smaller open market purchases would be required in order to achieve the same decline in reserves under an IRCPR or a MSCPR by the UKCB.

The Key Currency Reserve Regime

A. An Overview

Up to this point we have assumed that all reserves were held

in the form of outside reserve assets like gold or SDR's. However, a

notable feature of the international monetary system as it has evolved

in this century is that significant portions of the reserves of many

countries are held in the form of claims denominated in so called

"key currencies" and that a large proportion of international pay-

ments imbalances are financed by the use of these key currency assets.

We call the regime under which changes in reserves take the form of

changes in central bank holdings of key currency denominated assets

International economists have focused considerable attention the key currency reserve regime.

on some aspects of the key currency reserve regime. It has been

argued that the pressure to take corrective measures in the face of

persistent payments imbalances and the burden of adjustment when it

takes place are distributed assymetrically under such a regime. /ī

dollars in exchange rate support operations, the U.S. is not put liabilities instead of demanding gold or SDR's when they accumulate It is widely believed that if other countries will accept U.S.

Roper () has argued that if adjustment is actually to take to take corrective action. under pressure to adjust, but the other countries will feel pressure

Roper assumes that under an outside reserve regime each central currency reserve regime than under the outside reserve regime. level in other countries will have to rise by more under the key place the U.S. price level will have to fall by less and the price

international reserves falls (rises). bank allows its money supply to fall (rise) as its stock of

a natural framework within which to consider these relatively when they neither buy nor sell domestic assets. Our model provides outside reserve regime when central banks remain passive, that is, in reserves under the key currency reserve regime then under the determine whether or not given distrubances result in larger changes deficits for U.S. financial variables. It is also useful to find any discussion of the implications of security financing of U.S. the outside reserve regime. One must turn to the financial press to that they are operating under the key currency regime rather than and pursuing the same objectives must modify their behavior given It is important to know how central banks facing the same disturbances Other aspects of the key currency regime have received less attention.

specified the markets for securities. These markets have not been A central feature of our model is the way in which we have neglected problems.

adequately treated in many of the previous discussions of models which

had an adverse effect on the U.S. capital account. of the same analysts argued that these interest rate developments as much as they had been expected to rise for various reasons. Some securities helped to keep U.S. short term interest rates from rising that the conversions of dollar exchange to interest bearing Journal of Commerce, April 15, 1972, p. l. Some analysts believed widely discussed in the financial press. See, for example, official purchases of U S. securities on U.S. interest rates was $\frac{1}{2}$ In the spring and summer of 1972 the impact of large foreign

Modifications in the Model for U.S securities. regime to have a model when takes explicit account of the market passive. It is particularly useful when studying the key currency securities available for the public to hold when central banks are changes lead directly to a reduction in the amount of key currency changes are held in the form of key currency securities, reserve However, under the key currency reserve regime where reserve when central banks kept their holdings of domestic assets constant. reserve assets were associated with changes in national money supplies the outside reserve regime changes in central bank holdings of more important for studying the key currency reserve regime. Under A careful specification of the securities markets is, if anything, money stocks constant usually lead to a change in interest rates. since the changes in the supplies of securities required to keep insulate the economy from the effects of disturbances to equilibrium reserve changes on money supplies does not in general completely contrary to the view held by some, sterilizing the effects of economy. For example, in the last Chapter it was shown that, one of the avenues through which changes in reserves may affect an allow for capital movements. As a result these discussions have missed

In order to analyze the key currency regime some minor modifications in our model are required. The four market equilibrium conditions from the model presented in Chapter II with the necessary

alterations are summarized in the following equations:

$$B_S \equiv \overline{B} - B_C - B_{C_1} = p(x,x') W + \Pi b'(x,x')W'$$
 (93)

$$\Pi \ E^{S} \equiv \Pi \ (\overline{F} - F^{C}) = f(r,r')W + \Pi \ f'(r,r')W'$$
 (10a)

$$M_{\rm S} \equiv B_{\rm C} + O K + C = m(r,r')W + M^{\rm C}$$
 (IIa)

$$\Pi N^{S} \equiv \Pi (F^{C} + \sigma'R' + B^{C} + S') = \Pi n'(r,r')W'.$$
 (12a)

The holdings of U.S. securities and U.S. money by the UKCB are

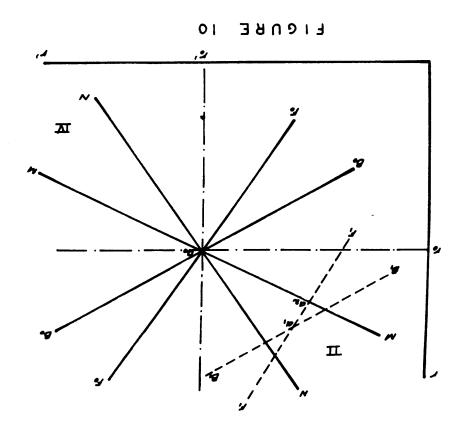
represented by Bc' and Mc' respectively. As before, only three of the four equations are independent, a fact which can be verified by noting modified equations can be represented using the same graphical framework that we have employed previously. As we shall see the set of possible new equilibrium positions following a given disturbance are the same under the key currency regime as they were under the outside operations to arrive at the same equilibrium position under the two operations to arrive at the same equilibrium position under the two alternative regime. However, the two central banks must undertake different operations to arrive at the same equilibrium position under the two alternative reserve regimes. To reasons the equilibrium position actually treached after a given disturbance may be different under alternative

C. A Speculative Shift

To illustrate how the key currency reserve regime operates we consider a type of shock to asset equilibrium which is especially pertinent given recent history, a shift in preferences away from U.S.

regimes even though all the same positions are attainable.

securities and toward U.K. securities due to a change in expectations regarding the exchange rate. As we saw in Chapter III above such a shift in preferences causes FF to move from $^{\rm F}_0{\rm F}_0$ to $^{\rm F}_1{\rm F}_1$ and BB to move from $^{\rm B}_0{\rm B}_0$ to $^{\rm B}_1{\rm B}_1$ as in Figure 10. We assume that the USCB move from $^{\rm B}_0{\rm B}_0$ to $^{\rm B}_1{\rm B}_1$ as in Figure 10.



follows a GSPR; that is, it keeps its holdings of U.S. securities constant. The UKCB follows a GSPR and accumulates reserves in the form of U.S. securities and an excess supply of U.S. securities at the original u.K. securities and an excess supply of U.S. securities at the original interest rate pair (r_0, r_0^{\dagger}) . As wealth holders seek to rebalance their

only be removed by a larger decline in r'. regime since with a lower r the excess demand for U.K. securities can purchases. r' falls but by more than it would under an outside reserve the initial excess supply of U.S. securities is removed by the UKCB the UKCB had accumulated reserves in outside assets because part of r rises but by less than if securities available to private holders. and the security purchases by the UKCB reduce the supply of U.S. they, in effect, sterilize the key currency country's money supply, country holds changes in reserves in the form of key currency securities, purchase U.S. securities in the open market. When the non key currency immediately uses the dollar proceeds of its support operations to supply, but the U S money supply remains unchanged because the UKCB operations. These operations result in a rise in the U.K. money and upward pressure on II. The UKCB buys dollars for pounds in support portfolios they exert downward pressure on r', upward pressure on r,

I/ Some of the recent increase in dollar-denominated, interest-bearing assets held by foreign official institutions has come in the form of special non-marketable securities. To study the effects of this form of reserve holding in the context of our model we can suppose that special non-marketable assets. This action, in itself, results in no reduction in the supply of U.S. securities available to the public. If the USCB wants to keep the U.S. money supply constant, it must no reduction in the supply of U.S. securities available to the public. If the USCB wants to keep the U.S. money supply constant, it must no reduction in the supply of U.S. securities available to the public. Our the USCB wants to keep the U.S. money supply constant, it must no reduction in the supply of U.S. securities available to the public. If the USCB wants to keep the U.S. money supply constant, it must no reduction in the supply of U.S. securities available to the public. If the USCB wants to keep the U.S. money supply constant, it must not in the secret conntries from the form of any kind of non-marketable instrument, the key currency country must actively pursue open market open matket in stations in order to sterilize its money stock.

Tates to reduce their holdings of U.K. securities and to hold the increased U K. money stock. The increase in the U.K. money stock which is identical to the increase in U.K. reserves is represented by the shift of MM from M0M0 to M_1M_1 which passes through the intersection of F_1F_1 and the original MM curve at a.. We know from above that if the position would have been at a.. Position a. implies a larger increase in reserves for the U.K. since MM must shift down further from M_0M_0 to reach a.. This conclusion demonstrates the contention that the same shock may lead to a greater accumulation of contention that the same shock may lead to a greater accumulation of the reach a.. This conclusion demonstrates the reserves by the non key currency country under a key currency reserve regime than would occur under an outside reserve regime.

passive, U.K. reserve holdings will fluctuate more for given shocks to asset equilibrium if the UKCB holds reserve changes in U.S. securities than if it holds these changes in outside assets. No matter what the form of the disturbance the BB and FF curves resulting directly

securities than if it holds these changes in outside assets. No matter what the form of the disturbance the BB and FF curves resulting directly from the shock in regions of excess demand for one type of money and excess supply of the other. These regions are designated as money and excess supply of the other. These regions are designated as

always shift further to reach the intersection of the new FF and MM curves than to reach the intersection of the new FF and BB $\frac{1}{2}$

The analysis above suggests that the European countries might have had to accumulate fewer reserves preceding the formal suspension of dollar convertibility in August 1972 if they had taken reserve increases in the form of outside assets. Although this course of action was impossible, since the dollar was de facto inconvertible, our model can be used to show that the size of European reserve accumulations could have been limited in exactly the same way if Europeans had held reserve increases in the form of U.S. money instead of in the form of U.S. securities. They would still have had to

In terms of our model the demonstration of this contention is quite straightforward. If we continue to assume that both central banks are passive the new equilibrium following the speculative shift is the same when reserve changes are held as key currency money as the equilibrium reached under the outside reserve regime. The UKCB sccumulates dollars and supplies pounds in support operations but

been smaller. There would, of course, have been a loss of interest

income on securities.

curves.

 $\underline{1}$ It is not possible to make a general statement about the relative movements of the two interest rates between equilibria under the two different reserve holding regimes. Depending upon the type of disturbance to equilibrium the initial equilibrium pair of interest rates (r0, r0') may be anywhere inside the four sided figure bounded by the new MM, NN, FF, and BB curves or even outside this figure.

does not convert the dollars into either outside assets or U.S.

securities. Thus the U.S. money supply falls and the U.K. money supply rises until equilibrium is reestablished at point a_1 , but this is exactly what happened under the outside reserve regime. The $\frac{\sin 2}{\sin 2}$ of U.K. reserve gains are exactly the same when reserve changes are held as money as when reserve changes are held as outside assets. We should not be too quick to conclude, however, that if non

key currency countries want to minimize reserve fluctuations they should hold reserve changes in outside assets during periods of effective convertibility and in key currency money during periods of the central bank of the key currency country would remain passive as we have been assuming up until now. Turning again to the model vegardless of how the UKCB holds its reserve changes, then if the UKCB holds its reserve changes, then if the disturbances to asset equilibrium by holding reserve changes in the form of U.S. securities the effects on the U.S. money supply of disturbances to asset equilibrium by holding reserve changes in the form of U.S. securities the effects on the U.S. money supply of disturbances to asset equilibrium by holding reserve changes in the form of U.S. securities the effects on the U.S. money supply of disturbances to asset equilibrium is at all all the only purchases. In either case the new equilibrium is at all all the only purchases. In either the UKCB is whether to hold assets paying interest or non interest bearing assets.

Of course if the USCB only offsets

if the U.S. monetary authorities were pursuing a money supply target in the summer of 1972, it would have made no difference for the behavior of interest rates if foreign official institutions had chosen to hold the proceeds from their support operations in the form of U.S. money rather than using them to purchase U.S. securities from the public. The USCB would have bought enough securities from the public to keep the money supply on target if foreign official institutions had not done so.

part of any decline in the U S. money stock the UKCB can reduce its reserve accumulation to some extent, at some cost in terms of interest foregone, by holding reserve increases in non interest

bearing assets.

1/ Of course, if a devaluation is anticipated asset demands shift away from the securities of the country which is expected to devalue. After the devaluation has occurred assets demands prosider here the less realistic case of an unanticipated devaluation in order to highlight what we believe to be a necessary modification of conventional arguments. Later we consider the case in which a shift in asset demands occurs at the same time as a devaluation.

U.S. and U.K. securities have the same relative attractiveness after the exchange rate change as before it. Thus, the argument proceeds, there should be no incentive for wealth holders to alter their

portfolios.
This argument is correct as far as it goes. What it ignores

is the fact that some wealth holders experience capital gains and others experience capital losses as a result of the devaluation and that these changes in wealth are realized completely in the first instance as changes in the home currency value of foreign assets.

Both the losers and the gainers from the devaluation find themselves with the wrong mix of assets at the prevailing interest rate given their changed wealth and the form in which the change has accrued. Thus when the wealth effects of the devaluation are taken into account there is an incentive for wealth holders to alter their portfolios.

Consider a devaluation of the dollar in the framework of

our model. U.S. citizens experience a capital gain of $\mathbf{F}^{A}d\Pi$ dollars

I/ There may be other avenues in addition to those we consider below in the text through which an exchange rate change can affect the relative attractiveness of U.S. and U.K. securities. For example, if a country devalues in order to free itself from an underemployment-economic activity resulting from the direct impact of the devaluation and a relaxation of constraints on expansionary policies would lead to a higher return on the securities of the devaluing country. Our model is not well suited for an investigation of these effects, so we abstract from them here.

 $\frac{2}{2}$ The devaluation may be reflected in a change in σ , the dollar price of outside reserve assets; in σ , the pound price of outside reserve

(Footnote continued on next page)

while U.K. residents suffer a capital loss of -B^{A'}dM pounds where M is the dollar price of pounds, taken to be unity initially, and F^A and b^{A'} are the initial holdings of U.S. securities by U.K. residents and the initial holdings of U.S. securities by U.K. residents first instance as an increase in wealth in the U.S. comes in the of U.S. securities, and the decrease in wealth in the U.K. comes in initially in the form of a decrease in the pound value of U.K. comes initially in the form of a decrease in the pound value of U.K. residents have an excess demand for U.S. securities and U.S. money residents have an excess demand for U.S. securities and U.S. money and an excess supply of U.K. securities and U.K. residents have an and an excess demand for U.S. recurities and U.S. money and an excess supply of U.K. securities and U.K. residents have an

\overline{I} \ continued from previous page

reserve assets; or in both. Of course, at least one currency price of reserve assets must change. The relationship between dil, do, and do' is given by,

$$d\Pi = \frac{1}{\sqrt{10}} = d\sigma - \frac{\sigma}{\sqrt{10}} = \Pi b$$

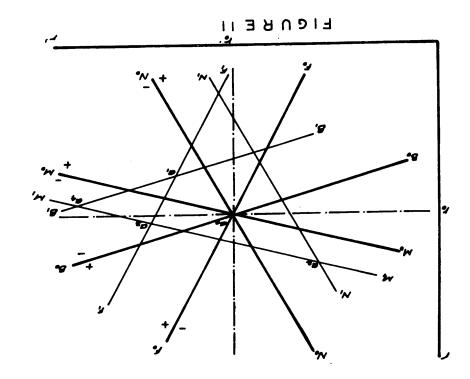
Changes in σ and σ ' alter the domestic currency value of the initial reserve holdings of both central banks. The size of these effects, the impact effects of a devaluation on the value of reserve holdings, depends upon how much of the devaluation is reflected in σ and how much in σ . We want to assume that these impact effects themselves cause no changes in the money supply of either country, so we assume that the two central banks simply change S and S' so as to offset the impact effects of changes in σ and σ on the domestic currency value of their assets,

$$dS = R d\sigma$$

$$dS' = (\overline{R} - R) d\sigma'.$$

 $\underline{1}$ / We continue to assume that asset demands are homogeneous of degree one in nominal wealth and that output prices are constant.

excess demand for U.S. securities and an excess supply of U.K. securities and U.K. money at the original interest rate pair. Thus, there is a world excess demand for U.S. securities and a world excess supply of U.K. securities. In Figure II the pre-devaluation equilibrium



is at the intersection of the schedules with the (0) subscript. The impact effect of the devaluation is shown by the schedules labeled $\frac{1}{2}/$ with the (1) subscript.

 $\overline{1}/$ For reasons discussed in detail above the new FF and BB curves must intersect between the new MM and MM curves.

curves back to their original positions so that they intersect at the actions by central banks described above is to shift all the by U.K. residents or [(1-f)F^A + (1-b')B^{A'}]dM. Of course, the effect of of U.K. securities by U.S. citizens plus the purchases of U.S. securities unwanted U.K. securities. U.K. reserve losses are equal to the sales must meet the demand for U.S. securities and the UKCB must absorb the U.S. securities. If interest rates are to remain unchanged the USCB F'B dI additional pounds into dollars in order to buy (1-b'AI) money and bEAdII in U.S. securities. U.K. residents want to sell (1-f)FA'dM in U K, securities and hold mFAdM of the proceeds in U.S. remains constant. U.S. residents want to divest themselves of proportion of wealth held in each asset by residents of both countries money. If interest rates are held constant by central bank action the and the UKCB holds changes in its reserves as outside assets or U.S. to begin with the case in which both central banks pursue an IRCPR upon the policy responses of the USCB and the UKCB. It is instructive of interest rates and the required changes in reserve holdings depend As we have come to expect by now the ultimate configuration

If the UKCB uses U.S. securities instead of outside assets or U.S. money to finance imbalances it will increase the supply of

·nisgs os

 $\overline{\underline{1}}$ For reasons discussed in detail above the new FF and BB curves must intersect between the new MM and NN curves.

U.S. securities by the full amount of the sales of U.K. securities by U.S. citizens plus the amount of the purchase of U.S. securities by U.S. citizens plus the amount of the purchase of U.S. securities by the initial excess demand for U.S. securities at the original interest in order to increase their money balances. In this case the USCB must buy U.S. securities in an amount equal to the initial excess demand for money in the U.S. at the original interest rate pair in demand for money in the U.S. at the original interest rate pair in order to keep U.S. interest rates from rising.

Returning again to the assumption that outside reserves are used to finance payments imbalances we find that if both central banks follow GSPR's, the new equilibrium is at the intersection of B_1B_1 and P_1F_1 at a_1 . I must fall, and I' must rise in order to remove the initial excess demand for U.S. securities and excess supply of U.K. securities. MM and MM must shift down until they pass through a_1 . The U.S. money supply increases and the U.K. money supply declines by equal amounts. The shift of reserves from the U.K. to the U.S. can be represented by either the shift in MM or the shift in MM.

when they follow MSCPR's implies that equilibrium must be at point algories M_1M_1 and M_1M_1 intersect. The USCB sells enough U.S. securities and the UKCB buys enough U.K. securities to cause the U.S. interest rate to rise and the U.K interest rate to decline by the amount

Complete monetary sterilization by the two central banks

necessary to remove the initial excess demand for money in the U.S. and the excess supply of money in the U.K. The loss of reserves by the UKCB is equal to the purchases of securities by the UKCB which are equal in amount to the sales of securities by the USCB and can thus be represented by the shift in either FF or BB from $\mathbb{F}_1\mathbb{F}_1$ or $\mathbb{B}_1\mathbb{B}_1$ to the position they would have to have if they were to pass through \mathbb{A}_2 .

Point a₃ is the equilibrium point if the U.S. money supply and the supply of U.K. securities reamin unchanged. This point would be reached if imbalances are financed by changes in outside reserves and the U K. pursues a GSPR while the USCB employs a MSCPR. Saset equilibrium would also be at point a₃ if the UKCB sells U.S. In this case the U.K. interest rate must rise in order to induce residents of both countries to hold the unchanged supply of U.K. securities. The U.S. rate may rise (as in Figure II) or fall since either the USCB or the UKCB sells off enough U.S. securities to keep either the USCB or the UKCB sells off enough U.S. securities to keep either U.S. money stock constant, and these sales may exceed or fall since the U.S. money stock constant, and these sales may exceed or fall short of the excess demand for U.S. securities at an unchanged U.S.

In graphical terms the question is whether or not the distance between M_0M_0 and M_1M_1 measured along a line through (r0, r0) and parallel to the r¹ axis is greater than the distance between F_0F_0

interest rate given the U.K. interest rate on FlF1 corresponding to

the unchanged U.S. rate.

(footnote continued on following page)

losses due to portfolio shifts if it pursues a RSCPR to the U.S.

devaluation while the U.S. follows either a GSPR, a MSCPR, or an IRCPR.

Ly

the UKCB pursues a large enough contractionary open market operation it can assure that the new equilibrium is at point at where BlBl and MlMl intersect. Since neither the U.S. money stock nor USCB holdings of U.S. securities is changed at at, U.S. reserves must be unchanged.

Of course, this policy response by the UKCB implies an increase in the U.K. interest rate and a decline in the U.K. money supply. Point at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB at would also be attained if the USCB employed a MSCPR while the UKCB attained if the USCB employed a MSCPR while the UKCB attained if the USCB employed a MSCPR while the UKCB attained if the USCB employed a MSCPR while the UKCB attained in UKCBB attained in UKCBBB a

$\frac{1}{2}$ footnote continued from previous page

and $^{\rm F}{\rm l}^{\rm F}{\rm l}$ measured in the same way. An algebraic analysis reveals that the answer to this question is indeterminante. The shift in MM is given by,

$$\frac{dx^{1}}{d\Pi} = -\frac{mK}{m^{2}M},$$

and the shift in FF is given by,

$$\frac{\mathrm{d} r^{1}}{\mathrm{d} \Pi} \mid_{\mathbf{F} = \mathbf{F}_{\mathbf{Q}}} = \frac{\mathbf{f} \mathbf{r}^{1} \mathbf{w} + \mathbf{f}^{1} \mathbf{r}^{2} \mathbf{w}^{1}}{\mathbf{f} \mathbf{F}^{1} \mathbf{w} + \mathbf{f}^{1} \mathbf{B}^{1} \mathbf{w}^{1}}.$$

The expressions for both shifts are positive and the difference between them may be positive or negative.

 $\underline{\underline{1}}$ The two central banks cannot, of course, attain inconsistent reserve targets.

\frac{2}{\text{impact}} It was explained in footnote I on page 70 that a devaluation has impact effects on the values of initial reserve holdings. In describing the reserve changes consequent upon a devaluation we ignore the impact effects and concentrate insteady on reserve changes which reflect changes in the two money supplies and changes in central bank holdings of securities.

pursued a RSCPR. The analysis is somewhat more difficult if the USCB employs an IRCPR, and we will not consider this case.

the following: $a_4 < a_1 < a_3 < a_2$. The techniques for ranking each ranking points from least to greatest U.K. reserve loss we obtain as since the BB curve must shift even further to reach az. Thus to the conclusion that az involves a larger U.K. reserve loss than stock is the same at all and at a_3 . The same line of argument leads position it would have if it passed through a3 since the U S. money a3 can also be represented by the shift in BB from $\mathtt{B_IB_I}$ to the constant. The U.K. reserve loss (U.S. reserve gain) implied by point declines further while UKCB holdings of U.K. securities are still U.K. reserve loss is implied by point a3 since the U.K. money supply the UKCB holdings of U.K. securities remain fixed. An even greater reserve loss by the UKCB since the U.K. money supply declines while U.S. must not have gained any reserves. Point al involves some money stock nor the USCB holdings of U.S. securities has changed the looking at the balance sheet of the USCB. Since neither the U.S. was an equilibrium which involved no reserve loss for the UKCB by either the USCB or the UKCB balance sheet. We showed that point $\mathbf{a}_{oldsymbol{\psi}}$ assessing the implication of each of the equilibrium positions for relative magnitude of UKCB reserve losses depends crucially upon positions we have considered. The technique for assessing the magnitude of UKCB reserve losses implied by some of the equilibrium The graphical analysis can be used to determine the relative

pair of points is to find an item on the balance sheet of one central bank or the other which remains unchanged between the two points and then compare the changes in another item between the two points; this $\frac{1}{1}$, comparison allows us to determine how the third item must have changed.

The magnitude of U.S. reserve gains from the portfolio adjustments due to the wealth effects of a devaluation depends upon the policy responses of the two central bank which in turn depend upon what policies the central banks deem appropriate from a domestic point of view and how convinced the UKCB is that the U.S. should be allowed to accumulate reserves.

If a devaluation by the U.S. has been expected, asset demands may have been shifted away from U.S. securities and in favor of U.K.

·Se pue 'Ze 'Ee 'Ie in the four-sided figure in Figure II the corners of which are call mixed money-security adjustment which lead to points which lie any combination of the two pure adjustment mechanisms and what we more efficient and pure security adjustment alone is less efficient than shown in Part II of the Appendix that pure money adjustment alone is while pure security adjustment alone leads to point az. It is also adjustment. Pure money adjustment alone leads to point al in Figure II adjust, that is, to rely completely upon what we call pure security money supplies constant and allow their holdings of securities to what we call pure money adjustment, than for central banks to keep and allow money supplies to change, that is, to rely completely upon brium for central banks to keep their holdings of securities constant in terms of the reserve shift required for the reattainment of equilibrium, of which devaluation is only one example, it is more efficient is shown in Part II of the Appendix that for any shock to asset equililoss for point ao is ranked between the losses for point al and al. in this case. However, it can be proved algebraically that the reserve We have not ranked a Decause the graphical technique is insufficient

securities at some point before the devaluation. After the devaluation, asset demands might well shift back to their original configuration; that is, the demand for U.S. securities would rise at the expense of the demand for U.K. securities. If this shift in asset demands occurred BB and FlF1 at the time of the devaluation. This increased shown by BlB1 and FlF1 at the time of the devaluation. This increased shift means that the size of the adjustments in the quantity variables in the model required in order for equilibrium to be reattained are larger. For any given combination of policy responses by the USCB and UKCB, changes in stocks of money and securities by the USCB and UKCB, changes in stocks of money and securities $\frac{1}{2}$ have been without the additional shift in asset demands. $\frac{1}{2}$ have been without the additional shift in asset demands.

 $\frac{1}{2}$ Examples can be constructed to show that the same statement cannot be made for the required changes in interest rates.

VI. Fractional Reserve Commercial Banking

A. An Overview

on demand deposits.

In this Chapter some of the implications of introducing a fractional reserve commercial banking system into the model are explored. We show how our model can be modified to incorporate a relatively simple description of fractional reserve commercial banking. In order to suggest what difference fractional reserve asset preferences in the modified model with the effects of a shift in banking under some alternative assumptions about central bank behavior. In the modified model we are able to allow for the possibility that the UKCB might hold some of its international reserve teserves at the USCB or as deposits at U.S. commercial banks. At reserves at the USCB or as deposits at U.S. commercial banks. At the end of the Chapter we discuss briefly the analytical equivalance

B. Assumptions and Modifications in the Model
In order to facilitate the analysis we make several

we call "fractional reserve central banking."

convenient simplifying assumptions. We assume that U.S. (U.K.) commercial banks must hold bank reserves equal to a constant fraction, $\frac{1}{2} \frac{1}{2}$ α (α), of their deposit liabilities; Commercial bank reserves in α (α), of their deposit liabilities; Commercial bank reserves in α (α), of their deposit liabilities;

between our description of fractional reserve commercial banking and what

 $\frac{2}{2}$ α and α' could be interpreted as customary reserve ratios or as sums of required and customary reserve ratios.

the U.S. (H^b) and in the U.K. (J^b) are deposits at the USCB and the UKCB respectively. In order to avoid confusion between international reserves and bank reserves we call the latter "high powered money." There is no currency in the model. Commercial banks in both countries hold only domestically issued securities. As is customary at this level of abstraction we assume that banks in both countries are "fully loaned up," that is, that they expand their deposit liabilities as much as possible in order to be able to hold deposit liabilities as much as possible in order to be able to hold as many interest bearing securities as possible. Thus for any given supplies of high powered money in the U.S. and the U.K., H^b and J^b , supplies of high powered money in the U.S. and the U.K., H^b and J^b ,

respectively, are given by,

$$W_{g} = \frac{\alpha}{I} H_{p}$$

$$N_{\rm g} = \frac{1}{1}$$
 $n_{\rm p}$

and commercial bank demand for securities in the U.S. and U.K. $(B^b \text{ and } F^{b^{-1}} \text{ respectively}) \text{ are given by,}$

$$E_{p_i} = \frac{\alpha_i}{1 - \alpha_i} P_{p_i}$$

$$E_{p_i} = \frac{\alpha_i}{1 - \alpha_i} P_{p_i}$$

The supplies of high powered money to the commercial banks in the U.S.

and the U.K. are given by,

$$1_{p} \equiv B_{c} + \alpha(\underline{R} - R) + \frac{1}{1} (B_{c} + M_{c} + H_{c}) + Z,$$

$$H_{p} \equiv B_{c} + \alpha R - H_{c} + Z$$

^{1/} This assumption does little violence to reality in the case of U.S. Danks to the extent that the Voluntary Foreign Credit Restraint (VFCR) ceilings are binding.

interpreted in the same way as they were in previous Chapters. UKCB deposits at U.S. commercial banks. All other symbols should be where H^{C} represents UKCB deposits at the USCB and M^{C} represents

Given the assumptions above we can rewrite the equilibrium

conditions of the model in the following way,

$$B_{S} \equiv \underline{B} - B_{C} - B_{C} - \left(\frac{\alpha}{I - \alpha}\right) \left(B_{C} + \alpha B - H_{C} + C\right) =$$

(96)

$$\pi_{\overline{F}} s \equiv \pi \left[\overline{F} - F^{c'} - \left(\frac{1 - \alpha'}{\alpha'} \right) \left\{ F^{c'} + \alpha' (\overline{R} - R) + \frac{1}{\alpha'} (T_{c'} F') W' \right\} \right]$$
(10b)

$$\frac{1}{L}(B^{C'} + M^{C'} + H^{C'}) + S' \bigg\} = f(r,r')W + \pi f'(r,r')W'$$
 (10b)

$$M_{S} = \frac{1}{\alpha} (B^{c} + \sigma R - H^{c'} + S) - M^{c'} = m(r, r')W$$
 (IIc)

$$M(I_{1})M = M - (S + 3H - R_0 + 3H) \stackrel{\triangle}{=} R_M$$

$$(12c) \qquad \qquad u'(r,r')W'$$

four assets available for the public to hold. Since adding the four where, as before, B^S , F^S , M^S , and N^S represent the quantities of the

are independent. In analytical terms the important modification which equations together yields an identity, only three of the four equations

snbbj λ of high powered money to commercial banks given by $H_{D}\equiv B_{C}$ arises from the introduction of commercial banking systems is that the

 $+\alpha R$ - R - R^{c} + S for the U.S. [Jb' \equiv Bc' + α (\overline{R} - R) + $\frac{1}{\pi}$ (Bc' + Mc'

+ $\mathrm{H}^{\mathrm{C}^{\,\prime}}$) + S' for the U.K.] enters as an argument in the U.S. (U.K.)

security market equilibrium condition so that changes in $\mathrm{H}^b(\mathrm{J}^b{}^i)$ shift

both the MM and BB schedules (NN and FF schedules).

Now we make an assumption which allows us to highlight the essential features of fractional reserve commercial banking in the context of a somewhat simplified framework. We assume that the UKCB always manipulates $F^{C'}$ so as to keep the supply of money in the hands of the U.K. commercial banks and, therefore, the supply of money in the hands of the U.K. public constant; that is, the UKCB pursues a MSCPR. In terms of our graphical analysis, the UN schedule will always remain fixed. This assumption allows us to analyze the effects of introducing fixed. This assumption allows us to analyze the effects of introducing commercial banking system since the size of the U.S.

Assuming that α' , π , σ' , \overline{R} , and S' are constant, we have $dF^{C'} = \sigma' dR - \frac{1}{\pi} (dB^{C'} + dM^{C'} + dH^{C'})$.

.səsoqzuq commercial banking, we consider two polar possibilities for illustrative equity. Since it is not our purpose to develop a comprehensive treatment set of logically compelling assumptions regarding the valuation of bank the banking system on the variables in the model. We have discovered no profits is a factor in determining the impact of changes in the scale of securities. The way in which bank shareholders react to changes in bank so bank equities are a part of \overline{B} , the total supply of U.S. issued bank profits. Presumably, the commercial banks are owned by shareholders, tions the expansion of the banking system will lead to an increase in range of changes in bank scale under consideration. Given these assumpall costs of running the banking system are constant, at least over the from paying explicit or implicit interest on demand deposits and that which contains only two interest rates (r and r') that banks are prohibited bearing assets. We assume in accordance with the spirit of our model banks to expand their deposit liabilities and to purchase more interest requirement on deposit liabilities. This action enables U.S. commercial we will deal with it in this study. Suppose the USCB lowers the reserve $\frac{1}{2}$ In this footnote we discuss a rather complicated problem and how

Footnote continued on following page

C. A Shift in Asset Preferences

To illustrate how the system operates with fractional reserve commercial banking we take the case of a preference shift by the public away from U.S. securities and toward U.K. securities. As before, this in Pigure 12. First consider some combinations of responses by the USCB and forms of UKCB reserve holding that make the analysis essentially the are assuming that the UKCB always acts so as to keep the U.K. money are assuming that the UKCB always remains at $\rm M_0M_0$. If the UKCB holds its supply constant so that MM always remains at $\rm M_0M_0$. If the UKCB holds its increases in reserves in the form of outside reserve assets and the USCB pursues a MSCPR, then the UKCB will sell U.K. securities and the USCB increases in reserves in the form of outside reserve assets and the USCB discretes a MSCPR, then the UKCB will sell U.K. securities and the USCB increases in reserves in the UKCB will sell U.K. securities and the USCB discrete a MSCPR, then the UKCB will sell U.K. securities and the USCB discrete a MSCPR, then the UKCB will sell U.K. securities and the USCB discrete a MSCPR, then the UKCB will sell U.K. securities and the USCB

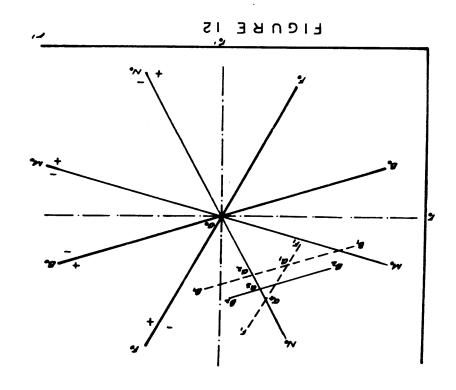
$\overline{\mathbf{I}}$ tootnote continued from previous page

If, on the one hand, we assume that bank shareholders anticipate that any increase in bank profits is transitory, then the value of bank equities, and therefore \overline{B} , will not change by any significant amount. A lowering of the reserve requirement under this assumption leads to an excess supply of money and an excess demand for U.S. securities. This disequilibrium is resolved in the usual way.

will purchase U.S. securities in order to sterilize their respective

If, on the other hand, we assume that bank shareholders anticipate that any increase in bank profits is permanent, then the value of bank equity, and therefore \overline{B} , rises by the amount of bank purchases of interest, bearing assets. Assuming that all bank shareholders are U.S. residents, W also rises by the same amount since the amount of money available to the public increases while the amount of securities available to the asset demands there will be an excess supply of money, an excess demand for U.S. securities, and an excess demand for U.S. securities, and the excess demand for U.S. securities will be smeared for U.S. securities will be smaller than in the previous case.

We assume throughout this Chapter except in footnote 1 on page 87 that bank shareholders assume that all changes in bank profits are transitory. This assumption implies that changes in the scale of the banking system do not affect $\overline{\mathbf{B}}$ and \mathbf{W} .



money supplies. In this situation the BB and FF curves will shift back to their original positions, and the new equilibrium will be at a0.

The same result will hold if the UKCB holds its reserves as U.S. securities and the USCB is passive. The size of the U.S. commercial banking system has not been changed in either of these cases, so fractional reserve banking does not affect the conclusions.

form of outside assets and the USCB does not sterilize, then the supply of high powered money to the U.S. commercial banking system will, of course, necessitate a multiple contraction in deposits at U.S. commercial banks. Less obviously, the contraction of the U.S. commercial banks. Less obviously, the contraction of the U.S. commercial banks it to sell of U.S. securities. The decline in the banking system causes it to sell of U.S. securities. The decline in the of securities by the commercial banks shifts the BB curve up and to the left from Blb1. In addition the increase in the sales

FF to shift down and to the left from F_1F_1 . The MM, BB, and FF curves shift until they meet at a point, say point a3 where B_2B_2 and F_2F_2 intersect, which must lie above a2 and below a4 on N_0N_0 . Point a3 must lie below point a_4 , the point at which there would be no change in UKCB reserves, because reserves flow toward not away from the U.K. Since it is assumed that the UKCB always pursues a MSCPR, the relative magnitude of the reserve flow can be measured by the shift in FF from

securities due to the sterilization operations of the UKCB causes

 $\mathbf{F}_1\mathbf{F}_1$ required to reach the new equilibrium position. It was shown in Chapter II that if the USCB pursues a GSPR and the UKCB pursues a MSCPR and there is no fractional reserve commercial banking system point a2, where $\mathbf{B}_1\mathbf{B}_1$ and $\mathbf{M}_0\mathbf{M}_0$ intersect, is reached. We can conclude that although the reserve flow is in the same direction it is smaller with a fractional reserve flow is in the same direction it is smaller with a fractional reserve flow is in the same direction it is smaller with a fractional reserve flow is in the same direction it is smaller with a fractional reserve flow is in the same direction it is smaller with a fractional reserve flow is in the case described in the

previous paragraph is that the absorbtion of securities by the U.S.

banking from other sectors of the world economy is positively related to the change in U.S. high powered money which, in the absence of sterilization operations by the USCB, is positively related to changes in the international reserves held by the USCB. The multiple contraction process can be conceptually separated into two parts. As reserves flow out the supply of high powered money, and therefore the money supply out the public, drops by an equal amount. Also, the reserve in the hands of the public, drops by an equal amount. Also, the reserve

effect, like a contractionary open market operation but which emanates from the commercial banks rather than the USCB. The additional contractionary process reduces the need for reserves to flow.

What happens if the UKCB holds its increased reserves as deposits at the USCB then the amount of high powered money available to U.S. commercial banks will decline unless the USCB sterilizes by purchasing

securities. If the USCB is passive then the U.S. banking system will release contract. The contraction in the U.S. banking system will release securities increasing the supply of securities to the public, and point a₃ will be reached. If the USCB instead sterilizes then the U.S. commercial banking system will not be affected by the reserve flow and position a₀ will be reattained.

at U.S. commercial banks, the supply of deposits available to the public will decline unless the USCB pursues sterilizing expansionary open market operations. If the USCB sterilizes it will purchase securities and supply high powered money so that total deposits at without reducing the amount of deposits held by the public. The securities purchased by the U.S. commercial banks will be at a₀. If the equal the reserve flow, and the equilibrium will be at a₀. If the equal the reserve flow, and the equilibrium will be at a₀. If the equal the reserve flow, and the equilibrium will be at a₀. If the ontract but the supply of deposits available to the public will decline contract but the supply of deposits available to the public will decline will have at a₀. If the contract but the supply of deposits available to the public will decline the manual public at a₁.

1\ We have indicated how the model would behave with the introduction of fractional reserve commercial banking if bank shareholders anticipate that any increases in profits in the banking system is transitory. As we have seen in footnote 2 on page 83 we could alternatively the banking system is permanent. This case is more difficult to handle graphically than the case dealt with in the text because the size of private wealth holders' portfolios change when the size of the commercial

(footnote continued on following page)

D. A Note on "Fractional Reserve Central Banking"

It is interesting to note that we could have captured the

essence of fractional reserve banking without ever introducing commercial banks. Suppose that we revert to the model of Chapter II with no commercial banking and postulate that the USCB always acts as at o maintain a constant ratio of international reserves to its monetary liabilities. We call such behavior "fractional reserve central banking". Under this assumption a loss of international reserve market operations if it wishes to undertake contractionary open international reserves to monetary liabilities which is less than one. Now consider the model of the current Chapter. When the

banking system changes. A decrease in the size of the commercial banking system reduces private wealth since the amount of money available for the public to hold decreases, but the amount of securities (including claims on banks) available for the private non-

footnote continued from previous page.

securities (including claims on banks) available for the private non-banking sector to hold remains unchanged.

curve between at and az.

leftward. The equilibrium position will be at some point on the ${
m M_0M_0}$ the value of U.S. allocatable assets decline, shifting the BB curve a decline in the demand for U.S. securities (and U.K. securities) as Now, instead of an increase in the supply of U.S. securities, there is the public to hold resulting from the sales by the commercial banks. the BB curve because of the increase in U.S. securities available for off earning assets. Before, this process involved a leftward shift in commercial banking system reduces its deposit liabilities and sells money supply will contract as high powered money decreases and the The U.S. keeps the U.K. money supply constant and that the USCB is passive. curves before adjustment takes place. Assume as before that the UKCB In Figure 12 the Blb1 and F1F1 curves are the shifted security marker U.S. bank stock is held by U.S. residents then the following will occur. and away from U.S. securities dealt with previously and assume that all If we take the case of a preference shift toward U.K. securities

features of the problem under consideration. as an intra sector item without losing sight of any of the essential and the commercial banking system and cancel out high powered money under appropriate assumptions we can consolidate the central bank in Part IV of the Appendix. It is important because it implies that which they are explicitly included. We state and prove this proposition commercial banks is exactly the same as the behavior of a model in the behavior of a model which does not take explicit account of assumptions we can specify central bank behavior in such a way that one example of the more general proposition that under certain deposit liabilities in the model of the current Chapter. This is but Chapter II is the same as the required ratio of high powered money to ratio of international reserves to monetary liabilities in the model of of the two models is exactly equivalent if the central bank's desired securities. Under the circumstances specified above the behavior powered money which causes the commercial banks to sell off

VIII. The Dependence of the Effects of Monetary Policy Upon the Degree of Substitutability Between Securities and Upon Relative Economic Size

A. Introduction

Up to this point we have assumed that U.S. and U.K. securities tutes but not perfect substitutes for one another in the

context of our model. A second purpose is to explore the way in yield familiar results for the effects of monetary policy in the purpose of this Chapter is to show that familiar polar assumptions in economic size when compared to the rest of the world. One their attention to the case of a single open economy which is small Often these analysts have restricted securities issued abroad. either completely non-substitutable or perfectly substitutable for a given country regard securities issued in that country as being the effects of monetary policy in models in which wealth holders in domestic and foreign securities. Other analysts have considered capital market integration is increased substitutability between upon the effectiveness of monetary policy. One aspect of increased been focused upon the impact of increased capital market integration the U.K. are of roughly equal economic size. Recently attention has portfolios of the two countries' wealth holders and that the U.S. and are substitutes but not perfect substitutes for one another in the

¹ For models in which it is assumed that wealth holders regard securities issued at home and abroad as perfect substitutes see Mundell (1968, Chapter 18) and McKinnon and Oates (1966). For a model in which it is assumed that wealth holders regard securities issued abroad as completely non-substitutable for both securities issued at home and domestic money see McKinnon (1969).

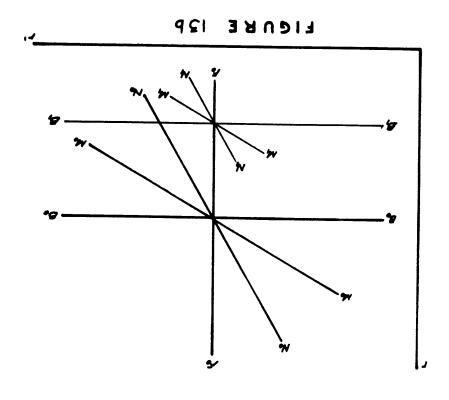
which increases in the degree of substitutability between assets affect the effectiveness of monetary policy in the intermediate range in which U.S. and U.K. securities are substitutes but not perfect substitutes for one another. A third purpose is to spell out the special limitations on the effectiveness of monetary policy faced by a country which is small in economic size relative to the rest of the world even if the securities issued in the small country are not perfect substitutes for those is substitutes for those

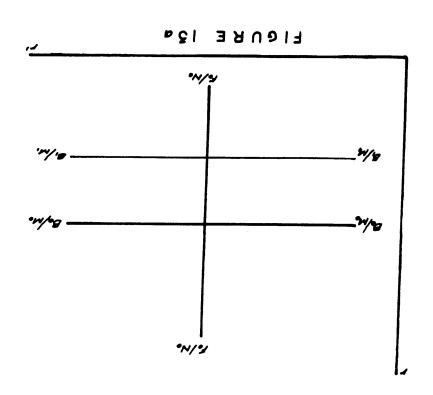
For the most part when we refer to monetary policy in this Chapter we mean an open market purchase of U.S. securities by the USCB. In our terminology the policy action we are investigating is a GSPI by the USCB. Attention is focused upon the effects of this policy initiative upon the differential between the rate on U.S. securities and the rate on U.K. securities and upon the level of the rate on U.S. securities. We usually assume that there is no attempt in either country to sterilize the effects on money supplies associated with reserve changes; that is, the GSPI by the USCB is met with a GSPR by the UKCB. We restrict our analysis in this way only to avoid an unwieldy proliferation of cases. We do not intend to take a position here, either explicitly or implicitly, as to whether the proximate target of monetary policy should be a "rate" or an "aggregate". We sketch the implications of the "rate" or an "aggregate". We sketch the implications of the "rate" or an "aggregate". We sketch the implications of the "rate" or an "aggregate". We sketch the implications of the "saumptions explored for the ability of the USCB to control the U.S.

money supply. As we shall see, the choice of the rate on U.S. securities as an illustrative proximate target for U.S. monetary policy is of little consequence since when the USCB can control this rate, it can also control the U.S. money stock, and when it cannot control this rate, it cannot control the control the cannot control this rate, it cannot control the money stock either.

B. The Effects of Monetary Policy in Some Polar Cases First we explore the implications of some polar assumptions

the money market and the market for securities issued at home. In of the interest rate on securities issued at home must clear both only assets considered suitable for wealth holding, the same value Since in each country money and securities issued at home are the The MM and BB schedules coincide as do the NN and FF schedules. holding is concerned these two economies are "closed" economies. either U.K. securities or U.K. money. So far as financial asset citizens do not consider U.S. securities to be substitutes for to be substitutes for either U.S. securities or U.S. money and U.K. a situation in which U.S. citizens do not consider U.K. securities subcases which are shown in Figures 13a and 13b. Figure 13a shows securities as completely non-substitutable. There are two important case in which wealth holders in both countries regard the two of roughly equal economic size. We begin our discussion with the securities retaining the assumption that the U.S. and the U.K. are regarding the degree of substitutability between U.S. and U.K.





this case an open market purchase by the USCB causes the rate on U.S. securities to fall by enough to make U.S. residents willing to reduce their holdings of U.S. securities and increase their holdings of money by the amount of the open market purchase. Of course, the differential between the U.S. and U.K. rate is reduced by the full amount of the decline in the U.S. rate.

Figure 13b portrays a situation in which U.S. and U.K.

declines by the amount of the decline in the U.S. rate. and the USCB loses reserves. Once again the interest differential same reason the rise in the U.S. money stock is less than before, residents surrender some U.S. securities to the USCB. For the smaller decline in the U.S. interest rate in this case because U.K. previous case, an open market purchase of equal size causes a of U.S. money demand to the U.S. rate is the same here as in the the amount of the open market purchase. Of course, if the response holdings of U.S. securities and increase their holdings of money by enough to make both U.S. and U.K. residents willing to reduce their purchase by the USCB causes the rate on U.S. securities to fall by no longer coincides with the BB (FF) schedule. Here an open market completely non-substitutable for one another. The MM (NN) schedule money even though the two types of securities are regarded as being residents view both types of securities as substitutes for domestic residents hold both types of securities and in which both groups of

There are good arguments in favor of using each of the two cases just discussed as a base case against which to measure the

effects of increases in the degree of substitutability between the two types of securities. It seems that the base case one chooses should depend upon the question under consideration. If, on the one hand, we are interested in contrasting the effect of monetary policy in a large open economy in which wealth holders view assets effects of the same policy in a large closed economy, the first ease is a preferable base case. If, on the other hand, our concern is focused more narrowly on the implications of increased substitutability between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors as possible billity between securities with as many other factors.

We turn now to the other polar case, the case in which U.S. and U.K. securities are virtually perfect substitutes. First we treat this case graphically. Some of our assertions about the effect on the four curves of allowing the two securities to become virtually perfect substitutes are supported by a mathematical argument later. As the degree of asset substitutability increases without limit, the slopes of the BB and FF curves approach positive one. As the two securities become virtually identical, any increase in r' must be offset by an almost identical, increase in r in order for either of the two securities markets to remain in equilibrium. The slopes of the two securities markets to remain in equilibrium. The slopes of the two securities approach negative one as the two securities

become indistinguishable. Since wealth holders in, say, the U.S. view the two securities as being almost completely alike, the responses of their money demand to the two interest rates should become very the money demand responses of U.S. wealth holders. The limiting the money demand responses of U.S. wealth holders. The limiting positions of the four curves are shown by the BOBO/FOFO and MOMO/NOMO schedules in Figure 14.

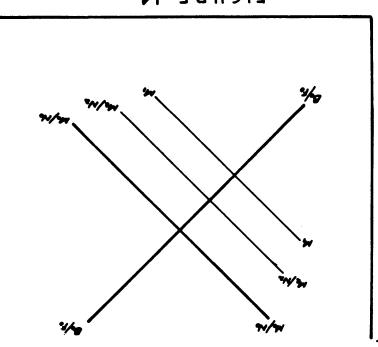


FIGURE I4

Interpose of the MM and MM curves never actually take on the value of negative one for if the two securities were exactly identical in every respect a decline in r would lead residents in both countries to try to move completely out of U.S. securities into U.K. securities, but there seems to be no reason why wealth holders should want to change their money holdings. When the two securities are exactly alike the their money holdings. When the two securities are exactly alike the their mand MM schedules reduce to single points which must lie on the line with a slope of positive one which represents the BB and FF schedules.

Now consider an open market purchase by the USCB. One of

what is effectively one rate the larger the reduction in this rate the sensitivity of the demands for money in the two countries to must change in order for equilibrium to be reestablished. The lower and the two types of money in the world so the world interest rate market purchase alters perceptibly the relative supplies of securities The USCB can effect this change because a plausible sized open result might be that the USCB can lower the world interest rate. effectively only one world rate, so a better way of stating the perfect substitutes. Of course, in the limiting case there is making an open market purchase even when securities are virtually at M2M2/N2M2. The USCB can still lower the U.S. interest rate by the MM curve shifts up and the NN curve shifts down until they meet than its initial value, and the U.K. money supply rises. Graphically, immediately following the open market purchase but remains higher residents. The U.S. money supply declines from the value it assumed market purchase, so they make net purchases of securities from U.K. residents hold too much money and too few securities after the open U.S. securities. However, the MM schedule is shifted to M_IM_I. takes virtually no change in r to remove a given excess demand for leaves the BB/FF schedule unaffected in the limiting case since it causes a massive change in security demands. An open market purchase securities is that a small change in either of the two interest rates the implications of very high degree of substitutability between

consequent upon the open market purchase. This result accords with the one obtained by other analysts.

As we would expect the differential between the U.S. and U.K. rates is unaffected by an open market purchase in the limiting case. Any change in the differential would lead wealth holders to want to make an indefinitely large shift between U.S. and U.K. securities, so no such change can occur. In graphical terms we move along a line with a slope of positive one, so that any change in r must be matched by an equal change in r' in the same direction in order for equilibrium to be maintained in the markets for securities.

C. The Impact of Increases in the Degree of Substitutability on the Effects of Monetary Policy in the General Gase

Analyzing the impact of increases in the degree of substitutability between securities on the effects of money policy when securities are neither completely non-substitutable nor virtually perfect substitutes is a somewhat more difficult task than the one we have just completed. Up to this point we have assumed that U.S. securities, U.K. securities, and domestic money are strict gross substitutes in the portfolios of wealth holders in each of the two countries and that the ratio of the response of U.S. money demand to the rate on U.K. securities to the response of U.S. money demand

1 See, for example, the Appendix in Mundell (1968, Chapter 18).

to the rate on U S. securities is less than the ratio of U.K. money

In order to make the problem

2/ See page 24 above.

demand responses to these same rates.

like that shown in Figure 15b which could occur under our earlier The schedules must have the position shown in Figure 15a; cases NN schedule has a negative slope which is more negative than negative negative slope which is less negative than negative one, and that the positive slope which is greater than one, that the MM curve has a positive slope which is less than one, that the FF curve has a strict gross substitutes assumption assure that the BB curve has a These two assumptions in conjunction with the issued at home. demand to a one percentage point increase in the rate on securities issued abroad is less than the absolute value of the response of money money demand to a one per cent increase in the rate on securities assume that in each country the absolute value of the response of changes on other security demands are analagous. Secondly, we U.S. residents. The implications for the effects of interest rate in the U.K. rate (cross rate) on the demand for U.S. securities by than the absolute value of the effect of a one percentage point rise (own rate) on the demand for U.S. securities by U.S. residents is greater lute value of the effect of a one percentage point rise in the U.S. rate wealth holders. This assumption implies, for example, that the absorate effects" on the demand for securities by both U.S. and U.K. First, we assume that "own rate effects" are greater than "cross at hand more tractable, we resort to somewhat stronger assumptions.

- 66 -

weaker assumptions are ruled out.

 $[\]frac{1}{p}$ More explicitly we assume the following: $\mathbf{b_r} > | \mathbf{b_r}$, $| \mathbf{f_r} | \cdot | \mathbf{f_r} |$, $| \mathbf{f_r} | \cdot | \mathbf{f_r} |$.

^{2/} See page 24 above.

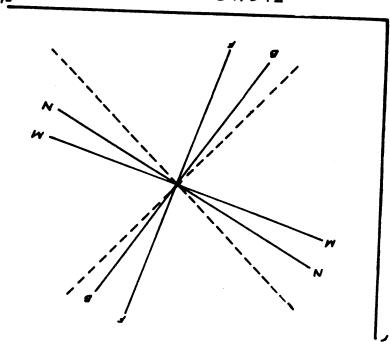
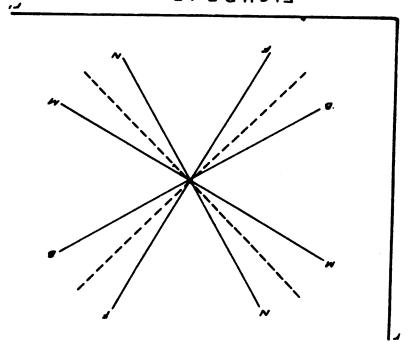
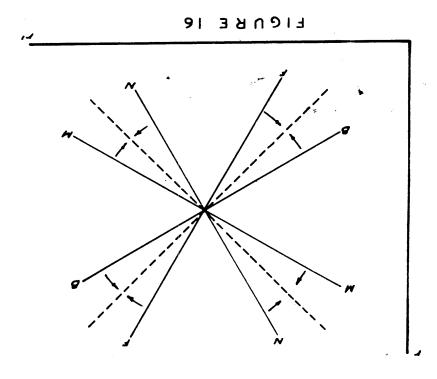


FIGURE 15a



in the manner we have outlined. The reader who is satisfied with the explore below some assumptions which assure that the schedules behave the schedules may not behave in the way we have suggested. changes in the schedules which we have described seem reasonable, movements we have described are shown in Figure 16. While the changes in the money demand responses of U.K. wealth holders. The should become more similar. We can make an analogous case regarding slike, the responses of their money demand to the two interest rates say, the U.S. come to view the two securities as being more and more two securities become better substitutes. Since wealth holders in schedule should fall (rise) continuously toward negative one as the It also seems reasonable to suppose that the slope of the MM (NN) toward one as the degree of substitutability between assets increases. suggests that the slope of the FF schedule should fall continuously two securities become virtually identical. A similar argument in r should be approaching equality with the rise in r' as the appear to wealth holders in both countries and that the required rise supply arising from an increase in r' the more alike the two securities plausible that r should have to rise tarther to remove the excess schedule to increase continuously toward positive one. It seems substitutability between assets should cause the slope of the BB analysis. Intuition suggests that increases in the degree of substitutability between U.S. and U.K. securities for our graphical Now we must investigate the implications of increases in



suggestive but incomplete reasoning regarding the movement of the

surrounding Figure 17. scyedules which we have given up to this point can skip to the text

without limit as substitutability increases. We regard all of the are completely nonsubstitutable and which rises continuously and Let s be a variable which takes on the value zero when the two assets increases in substitutability between U.S. and U.K. securities. and what we believe to be an intuitively appealing way to represent increased substitutability between securities we choose a convenient which the schedules are affected in the way we have described by In order to specify more exactly some conditions under

as functions of s and write them as, for example, $b_{\rm I}(s)$. We define demand responses to interest rate changes by U.S. and U.K. residents

three vectors $\alpha(s)$, $\beta(s)$, and $\gamma(s)$,

$$(s)_{1}^{T} u$$

$$(s)_{2}^{T} u$$

$$(s)_{3}^{T} u$$

$$(s)_{4}^{T} u$$

$$(s)_{5}^{T} u$$

$$(s)_{7}^{T} u$$

$$(s)_{7}^{T}$$

continuously without limit and the values of the cross rate effects substitutability increases the values of the our rate effects rise $\alpha(0) = -\gamma(0)$ and $\beta(0) = 0$. We assume that as the degree of securities are perfectly non-substitutable for one another we have earlier analysis we know that $\alpha(s) + \beta(s) + \gamma(s) \equiv 0$. When the two effects; Y(s) is a vector of money demand responses. From our $\alpha(s)$ is a vector of own rate effects; $\beta(s)$ is a vector of cross rate

countries we have, completely non-substitutable for domestic money by residents of both table for one another and securities issued abroad are considered to be In the case in which the two securities are completely non-substitu-

$$\begin{bmatrix} (0)^{1}u^{-} \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = (0)\lambda - = \begin{bmatrix} (0)^{1}q \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \equiv (0)^{N}$$

decrease continuously without limit,

$$\alpha_{s} > \frac{\alpha}{0} < \frac{\omega}{s}$$

$$\beta_{s} < \frac{\omega}{s}$$

$$\alpha_{s} + \frac{\omega}{s}$$

$$\beta_{s} + \frac{\omega}{s}$$

$$\beta_{s} + \frac{\omega}{s}$$

$$\beta_{s} + \frac{\omega}{s}$$

between them approaches zero as s increases, demands in each country become more alike, and that the difference Also we assume that the two cross rate effects on the security

$$0 = (_{\mathbf{I}}^{\mathbf{I}} - _{\mathbf{I}}^{\mathbf{I}}^{\mathbf{J}}) \text{ mil}$$

$$\infty \leftarrow \mathbf{z}$$

$$0 = (_{\mathbf{I}}^{\mathbf{I}} + _{\mathbf{I}}^{\mathbf{I}}^{\mathbf{J}}) \text{ mil}$$

$$0 = (x' 1 - x' d) \min_{\infty \in S}$$

for the interest rate responses of U.K. money demand, so we have, value which lies between them as a limit. We make analogous assumptions one another continuously and that these effects tend toward a common the values of the interest rate responses of U.S. money demand approach Finally we assume that as the two securities become better substitutes

$$m_{\text{TS}} > 0$$
, $m_{\text{T}} > 0$, $s < 0$, $n_{\text{TS}} > 0$

where $m_{\mathbf{r}} \leq k_{\mathbf{l}} < m_{\mathbf{r}}$ and $\mathbf{n'_{\mathbf{r'}}} \leq k_{\mathbf{2}} < \mathbf{n'_{\mathbf{r'}}}$ It could be argued that $m_{\mathbf{r}}$ and $\mathbf{n'_{\mathbf{r'}}}$ should remain constant and that $m_{\mathbf{r'}}$ and $\mathbf{n'_{\mathbf{r'}}}$ should decline to equal them if we characterize increases in substitutability as arising from changes which make wealth holders consider foreign securities to be more like domestic securities in both countries. We leave this issue open for the present.

The assumptions we have made so far regarding money demand

responses are sufficient to insure that the slope of the MM curve becomes continuously more negative and approaches negative one as a limit and that the slope of the MM curve becomes continuously less negative and approaches negative one as a limit as the degree of

The analysis of what happens to the BB and FF curves as

substitutability increases is somewhat more complicated. As we shall see, what happens to the BB and FF curves as the interest rate responses of the security demands increase and decrease without limit depends crucially upon what happens to four ratios:

 $-\frac{b_{\mathbf{r}^{\,\prime}}}{b_{\mathbf{r}}} \,, \, -\frac{b_{\mathbf{r}^{\,\prime}}}{b_{\mathbf{r}^{\,\prime}}} \,, \, \mathrm{and} \, -\frac{f_{\mathbf{r}^{\,\prime}}}{f_{\mathbf{r}}} \,. \quad \text{Each of the ratios is the quotient of a cross effect divided by an own effect or <math display="inline">\underline{\text{vice}}$ $\underline{\text{versa}}$ for a particular security and for a single identifiable behavior group. The assumptions we have made up to this point insure that all four ratios approach positive one as a approaches infinity. Using the implications of the two balance sheet constraints and a little manipulation we can write the four sums of own effects and

cross effects as follows:

We have assumed that the terms in brackets approach zero as a approaches infinity, so, given our assumptions regarding money demand responses, all of these sums approach constants as a approches infinity. Since the numerators and denominators of each of the four ratios are either increasing or decreasing without limit and since the sum of the numerator and denominator of each ratio approaches a constant, all numerator and denominator of each ratio approaches a constant, all

We also need to know what happens to these four ratios as

s is increased in intermediate ranges, but our assumptions up to this point have no decisive implications for this situation. In our view a plausible characterization of increases in substitutability could well include the added assumption that $\frac{b_{r'}}{f_{r}} \quad \text{and} \quad \frac{b_{r'}}{b_{r}} \quad \text{tise continuously toward positive one and that } \frac{f_{r'}}{f_{r}} \quad \text{and} \quad \frac{f_{r'}}{f_{r}} \quad \text{fall}$ continuously toward positive one. This assumption states simply that own effects and cross effects become continuously more alike except for sign as substitutability between securities increases. We presume that this assumption holds in what follows. It will be apparent that little progress can be made in the analysis of increased substitutability in intermediate ranges without it.

We are now prepared to investigate the behavior of the BB and FF schedules as the degree of substitutability is increased.

The slope of the BB curve is given by,

$$\frac{\mathrm{d}\mathbf{r}}{\mathrm{d}\mathbf{r}} \mid_{\mathrm{BB}} = -\frac{\mathrm{b}_{\mathbf{r}} \cdot \mathsf{W}}{\mathrm{b}_{\mathbf{r}} \mathsf{W}} + \mathrm{b}_{\mathbf{r}} \mathsf{W}' \cdot \mathsf{W}'}.$$

This expression can be rewritten as,

$$\left(\frac{\mathbf{r}^{\mathbf{r}}}{\mathbf{d}} - \right) \left(\mathbf{l}^{\mathbf{m}-1}\right) + \left(\frac{\mathbf{r}^{\mathbf{d}}}{\mathbf{d}} - \right) \mathbf{l}^{\mathbf{m}} = \frac{\mathbf{l}^{\mathbf{m}}}{\mathbf{d}}$$

мреке

$$\frac{1}{1} \frac{\mathbf{M_T} \mathbf{M_T} + \mathbf{M_T} \mathbf{d}}{\mathbf{d}} = \mathbf{I}^{\omega}$$

s. the slope of the BB schedule is a weighted average of

that is, the slope of the BB schedule is a weighted average of the change in r required to offset a change in r' in order to keep demand for U.S. securities constant in the U.S. and the change in r required to accomplish the same effect in the U.K. Each weight is the ratio of the demand response of the country in question to a change in r divided by the total world demand response to a change in r. Since $\frac{b_{r'}}{b_{r}}$ and $\frac{b'_{r'}}{b'_{r}}$ approach one as a approaches infinity we have, $\frac{b_{r'}}{b_{r}}$

$$I = \begin{bmatrix} dx & \frac{dx}{dx} \end{bmatrix} \quad \begin{array}{c} miI \\ \infty \leftarrow z \end{array}$$

This result justifies the assertion that the slope of the BB curve approaches positive one as a approaches infinity which we made in our discussion of the polar case of perfect substitutability.

Differentiating the expression for the slope of the

BB curve we have,

$$\omega_{\mathrm{IS}} = \frac{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}}{\mathbf{b}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}} = \frac{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}}{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}} = \frac{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}}{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}} + (\mathbf{I} - \omega_{\mathrm{I}}) + \frac{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}}{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}} + (\mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}) + \frac{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}}{\mathbf{a}_{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}} + (\mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}) + (\mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}) + (\mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}}) + (\mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I}} - \mathbf{b}_{\mathrm{I}}^{\mathrm{I$$

Thus the possibility of a "perverse" movement in the slope of the BB is zero if the two countries are exactly alike in either or both respects. own effects or in terms of per cent changes in own effects and that are the two countries either in terms of the ratios of cross effects to whatever its sign, it is smaller in absolute value the more alike third term in the expression. What we can say, however, is that, We have found no convincing argument to determine the sign of the on the larger of the two terms $\frac{b'r'}{b'r}$ and $\frac{br'}{br}$ tends to rise (fall). in b'r. The weighted average tends to rise (fall) if the weight the per cent increase in $b_{\mathbf{r}}$ is greater (less) than the per cent increase weights do not, in general, remain constant. Wl rises (falls) if held constant the weighted average definitely rises. However, the the right hand side are positive; that is, with the weights both countries is sufficient to insure that the first two terms on rate effects on the demand for U.S. securities become more alike in be the case. Our earlier assumption that own rate effects and cross s increases should be positive. However, this need not necessarily the expression for the change in the slope of the BB schedules as We have suggested above that intuition would lead us to believe that

a condition which we assume to be fulfilled in what follows, continuously as s increases if the two countries are "similar enough" approaches infinity and that the slope of the FF curve decreases assure that the slope of the FF curve approaches positive one as s argument we can establish that our assumptions are sufficient to weighed by the other two for all s. Using a similar line of increases, that is, that if the third term is negative it is outenough" that the slope of the BB curve rises continuously as s proceed under the assumption that the two countries are "similar curve arises because of differences in the two countries. /Ī

somewhat less natural to assume that such distribution effects are "distribution effects" which are usually assumed away. It seems economy macro economics problems like this are said to be due to demand schedules for two types of securities and money. In closedeconomy with two well defined groups of wealth holders with different $\frac{1}{2}$ A similar problem would arise if we were analyzing a closed

unimportant in a two country world.

 $\frac{dx}{dx} = -\frac{f_x W + f'_x W'}{f_x W + f'_x W'}$ $\frac{2}{2}$ The slope of the FF curve is,

which can be rewritten as,
$$\frac{dr}{dr} = \omega_2 \left(-\frac{f_r!}{r^{\frac{1}{2}}} \right) + (1-\omega_2) \left(-\frac{f_!r!}{r^{\frac{1}{2}}} \right),$$

$$\frac{dr}{dr} \left| FF \right|^{2} \left(\frac{r}{r} \right)^{2} \left(\frac{r}{r} \right)^{2}$$

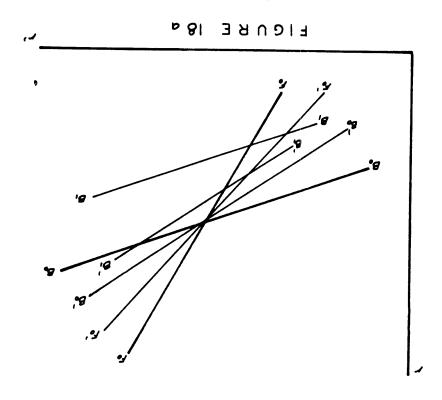
 $\cdot \frac{\mathbf{w}_{\mathbf{1}}}{\mathbf{w}_{\mathbf{1}}} = \mathbf{z}^{\omega}$ MUGLE

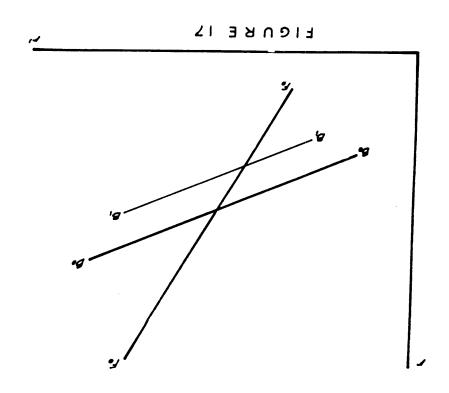
The derivative of the slope of the FF curve with respect to s is,

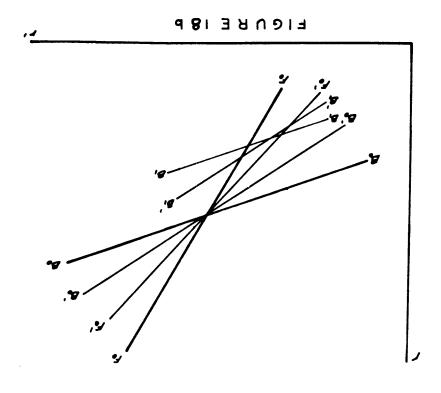
$$\text{Abere} \qquad \text{Apere} \qquad \frac{\left[\begin{array}{ccc} \frac{1}{4} & \frac{1}{4} &$$

if the two countries are similar enough. third term may be of either sign, but the whole expression is positive The first two terms are positive under our earlier assumptions.

tain equilibrium in the market for U.K. securities r' must fall if r ouce the USCB has made the open market purchase, but in order to mainflatter than $\mathbf{F}_0\mathbf{F}_0$. We know that \mathbf{r} must fall to reestablish equilibrium and U.K. rates. This result follows simply from the fact that F_0F_0 is size causes less of a reduction in the differential between the U.S. substitutability implies that an open market purchase of a given securities. It is clear from both diagrams that an increase in takes a smaller change in r to remove a given excess demand for U.S. Bobo and BlBI in both diagrams; as substitutability increases it the distance between $\mathbf{B}_0^1\mathbf{B}_0^1$ and $\mathbf{B}_1^1\mathbf{B}_1^1$ is less than the distance between the B_0B_0 , B_1B_1 , and F_0F_0 schedules. Note that for a given value of r higher degree of substitutability between the two securities than Figures 18a and 18b. The $B_0^{'}B_0^{'}$, $B_1^{'}B_1^{'}$, and $F_0^{'}F_0^{'}$ schedules represent a an open market purchase of a given size by the USCB can be seen in implications of an increase in substitutability for the effects of U.S. rate must be greater than the decline in the U.K. rate. The FF curve has a slope which is greater than one, the decline in the rates. The BB schedule is shifted down from ${\rm B_0B_0}$ to ${\rm B_1B_1}$. Since the case an open market purchase reduces both the U.S. and U.K. interest complete. By reference to Figure 17 we can see that in the general U.K. interest rate and on the level of the U.S. rate is finally market purchase by the USCB on the differential between the U.S. and increases in the degree of substitutability for the effects of an open The groundwork for our consideration of the implications of







falls. As substitutability is increased each decrease in r must be

Determining the implications of increased substitutability in the market for U.K. securities. matched by a larger decrease in r' if equilibrium is to be maintained

caused an open market purchase to lead to a smaller reduction in r and 18b we see that in the first case increased substitutability has been unable to arrive at a determinate result. Comparing Figures 18a the countervailing tendencies which lead to the ambiguity, we have purchase by the USCB is more difficult. Although we can spell out for the effect on the level of the U.S. rate of an open market

and that in the second case increased substitutability has caused an open market purchase to lead to a larger reduction in r. Increased substitutability has two kinds of effects on the schedules which are important here. It causes both BB and FF to rotate toward a line with a slope of positive one, and for a given r' it causes the downward shift in the BB schedule resulting from an open market purchase by

We have drawn Figures 18a and 18b so that they are completely identical except that in Figure 18b the distance between $B_0^{\,}B_0^{\,}$ and $B_1^{\,}B_1^{\,}$ is greater than in Figure 18a. Clearly for a given amount of rotation of the BB and FF schedules the more likely it is that an increase in substitutability leads to a reduction in the amount by which r falls after an open market purchase. Experimentation with the graph, which schedule the smaller the amount of rotation of either the BB or FF schedules the more likely it is that an increase in substitutability which is a given downward shift in the BB schedules the more likely it is that an increase in substitutability schedules the more likely it is that an increase in substitutability is a reduction in the amount by which r falls after an open schedules the more likely it is that an increase in substitutability schedules the more likely it is that an increase in substitutability is a reduction in the amount by which r falls after an open schedules the more likely it is that an increase in substitutability is a reduction in the amount by which r falls after an open schedules.

The economic interpretation of the fact that the downward shift in the BB schedules is reduced is that smaller reductions in rare required to remove a given amount of excess demand in the market for U.S. securities for a given value of r'. The fact that both FF and BB are rotating means that a larger decrease in r' is required

market purchase.

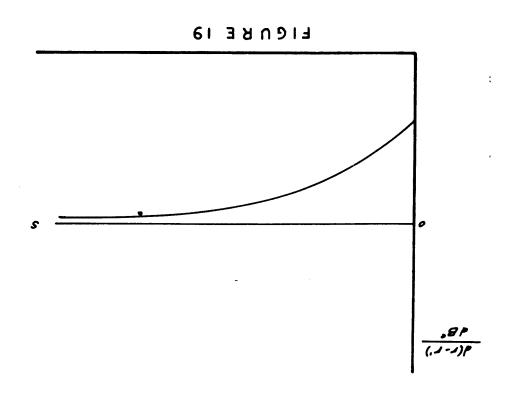
the USCB to be reduced.

to offset the effect of a given decline in r on the market for U.K. securities and that a larger drop in r is required to offset the effect of any decline in r' on the market for U.S. securities. The increased direct effect (reduced downward shift in BB) of a decline in r on the demand for U.S. securities tends to reduce the required decrease in r following the open market purchase while the increased in r following the open market purchase while the increased the required decrease in r following the open market purchase. We have not been able to determine whether or not one of these tendencies dominates the other except in one very special case.

Lower not been able to determine whether or not an increase in subsective open the question as to whether or not an increase in substitutability between securities causes a decline in the reduction in the U.S. interest rate caused by a given sized open market purchase by the USCB when the two securities are neither completely non-substitutable nor nearly perfectly substitutable.

I/ When the two countries are exactly identical in terms of the responses of asset demands to interest rate changes, a rise in a causes demands of asset demands to interest rate changes, a rise in a causes of asset demands to interest rate changes are identical in the two countries is not compatible with our earlier assumption regarding the responses of money demands in the two countries to interest rate changes. Two restrictions required by our interpretation of what it means for countries to be identical are that $\mathbf{m_T} = \mathbf{n_T}$ and $\mathbf{m_T}^{-} = \mathbf{n_{T^{-}}}$ We have assumed above that $|\mathbf{m_T}| > |\mathbf{m_T}| > |\mathbf{n_{T^{-}}}|$, and this assumption in conjunction with our new restrictions implies $|\mathbf{n_T}| > |\mathbf{n_{T^{-}}}|$ which violates our earlier assumptions. If we are to assume that countries are identical in the sense described here and to retain as much of the spirit of our earlier assumptions. The sample we must also assume $\mathbf{m_T} = \mathbf{m_{T^{-}}}|$, and functions as possible we must also assume $\mathbf{m_T} = \mathbf{m_{T^{-}}}|$.

Our conclusions regarding the impacts of increases in substitutability upon the effect of an open market purchase on the differential between U.S. and the U.K. rate are summarized in Figure 19. No matter which base case we begin from there is a continuous decrease in the reduction in the interest differential continuous decrease in the reduction as increases.



The same kind of simple summary is, of course, not possible in the case of the impact of increases in substitutability upon the effect of an open market purchase of the level of the U.S. rate, but we can say something. First, we must ask whether or not a given

open market purchase is less effective in lowering the U.S. interest rate when the two securities are virtually perfect substitutes than when the two securities are perfectly non-substitutable for one another but are both somewhat substitutable for money. When the securities are completely nonsubstitutable for one another the effect of an open market purchase on the U.S. rate is given by,

$$\frac{dr}{1 \pm m} = \frac{dr}{dB^{C}} - \frac{1}{b_{r}(0)W + b_{r}(0)W} = \frac{m_{r}(0)W + n_{r}(0)W^{T}}{m_{r}(0)W^{T}} - \frac{dr}{m_{r}(0)W^{T}}$$

As we have seen above the U.S. rate must fall by enough to induce U.S. and U.K. residents to surrender U.S. securities to the USCB and replace them in their portfolios with money. When the two securities are virtually perfect substitutes for one another the ... effect of an open market purchase on the U.S. rate is given by,

$$\lim_{\substack{l \text{im} \\ k_1 \text{m}}} \frac{dr}{dB^2} = \frac{1}{2} \frac{k_1 w + k_2 w}{l}$$

\(\frac{1}{2}\)\ We handle the comparison of the case in which the securities are ron-substitutable and in which wealth holders in each country regard foreign securities as being completely non-substitutable for money in footengn

2/ When wealth holders in each country regard foreign securities as being completely nonsubstitutable for money initially this

$$\frac{dx}{dB}c = -\frac{1}{b_T(0)W} = \frac{1}{m_T(0)W}.$$

$$|5(k^{I}M + k^{S}M_{i})| > |m^{L}(0)M|$$

 $\frac{1}{1}$ In the case treated in the previous two footnotes the condition is,

Condition may or may not be met. We can certainly find plausible assumptions under which the condition is met. For example, if k_1 is the simple average of $m_T(0)$ and $m_{T'}(0)$ and k_2 is such a simple average of $m_T(0)$, the condition is met. $k_1(k_2)$ would be such simple average if $m_T(n_{1})$ became continuously less negative as uch a way that the sum $m_T + m_{T'}(n_{1}) + m_{T'}(n_{1})$ remained constant, that is one percentage point rise in both rates always caused to the same movement out of money into bonds taken together in both countries. It is plausible but by no means necessary that wealth holders money let is plausible but by no means necessary that wealth holders money demand sensitivities would change in this way as they came to regard

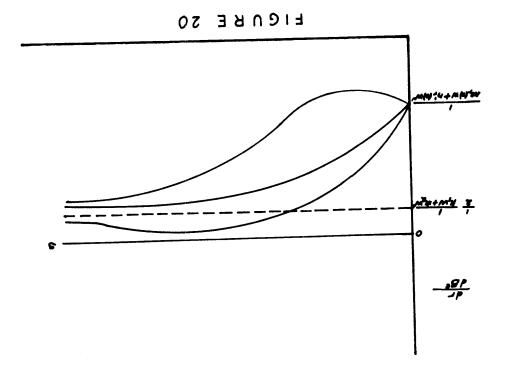
substitutes if and only if,
$$\left|2(k_1W+k_2W')\right|>\left|m_T(0)W+n'_T(0)W'\right|.$$

where as above $m_T(0) \le k_I < m_{T^1}(0)$ and $n_{T^1}(0) \le k_2 < n_{T}(0)$ and k_I is the limiting value of both m_T and m_{T^1} and k_2 is the limiting value of both n_{T^1} as a approaches infinity. In this case decreases in both the U.S. and U.K. rates induce wealth holders to surrender U.S. securities and replace them with money in their portfolios. The reduction in the U.S. interest rate following an open market purchase is less when the two securities are virtually perfect

the two securities as better substitutes. There are, of course, less restrictive assumptions which would lead to the fulfillment of the conditions given above, but we do not explore them here.

Even if we are prepared to presume that a given sized

open market purchase is less effective in reducing r when the two securities are perfect substitutes than when they are completely non-substitutable we are still left with the fundamental ambiguity purchase becomes continusously less effective as the degree of substitutability is increased in the range where securities are neither virtually perfect substitutes nor completely non-substitutable. This information is summarized in Figure 20 in which three possible versions of what happens to $\frac{\mathrm{d} \mathbf{r}}{\mathrm{d} \mathbf{r}}$ as a is increased are shown.

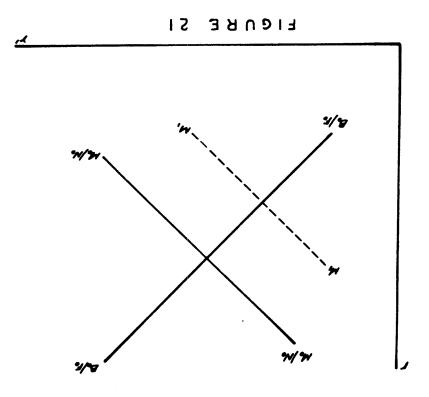


D. Relative Economic Size and the Effects of Monetary Policy

purchase in this more general case. or the size of its own money supply by a plausible sized open market may well be unable to affect either of the two world interest rates are perfect substitutes in order to demonstrate that a small country in the section we relax the assumption that U.S. and U.K. securities a plausible sized open market purchase in the limiting case. the single world interest rate nor the size of its own money supply by yields the familiar result that a small country can affect neither securities are perfect substitutes in order to show that our model section with a consideration of the case in which U.S. and U.K.substitutes for those issued in the rest of the world. We begin this tion that the securities issued in the small country are perfect analysts have combined the "small country" assumption with the assumpwith the economic size of the U.K. measured in the same way. Many as measured by nominal wealth in dollar terms is negligible when compared that the U.S. is a "small country" in the sense that its economic size In this section we explore the implications of the assumption

Consider first the perfect substitutes case shown in Figure 21. As we argued in the last section an open market purchase by the USCB leaves the $^{\rm B}0^{\rm B}0^{\rm /F}0^{\rm F}0$ schedule unaffected and shifts the MM schedule from $^{\rm M}0^{\rm M}0^{\rm /M}0^{\rm M}0^{\rm M}0^{$

 $\frac{1}{N}$ For another demonstration of this result see the Appendix to Mundell (1968, Chapter 18).



hold more money and fewer securities than they want to hold, so they make net purchases of securities from U.K. residents. The MM curve shifts up, but when the U. S. is small relative to the U.K. the UM the point at which M_0M_0/M_0M_0 , so the final equilibrium point is rate and the U.S. money stock are unchanged; U.S. reserves decrease and the U.K. money stock are unchanged; U.S. reserves decrease and the U.K. money supply increases by the amount of the open market purchase. To understand this conclusion we must realize that since the U.K. is large relative to the U.S. a very small decline and in the limit no decline in the world interest rate will induce U.K. residents limit no decline in the world interest rate will induce U.K. residents to reduce their holdings of securities and increase their holdings of to reduce their holdings of securities and increase their holdings of

money by the relatively small amount necessary to satisfy the desires of U.S. residents to rebalance their portfolios following a plausible sized open market purchase by the USCB.

Our conclusion can be demonstrated formally by an analysis of the U.K. money market. The equilibrium condition for this market in the limiting case under consideration can be written as,

$$N_{S_{\downarrow}} \equiv E_{C} + \overline{E} - E + S_{\downarrow} = \sum_{n=1}^{\infty} (\overline{E}) (\overline{M} - M)$$

 N^s , F^c , \overline{R} , R, S^r , and W have the same interpretation as in our earlier discussions. $\ddot{n}^r(\ddot{r})$ gives the proportion of their wealth which U. K. citizens wish to hold in the form of money as a function of the single world interest rate \ddot{r} . \overline{W} is the nominal value of world wealth which is assumed to remain constant, so \overline{W} - W is equal to W^r , the nominal value of U. K. Wealth. The U. S. money stock is,

$$W_{\rm S} \equiv B_{\rm C} + E + S$$
.

Since we want to consider variations in W and W' with as many other factors as possible held constant we assume that in both countries the ratio of central bank held securities to wealth is independent of wealth

so we have,

$$B_C = \epsilon M$$

$$E_C = \varepsilon_i M_i$$
.

An open market purchase by the USCB is represented by an increase in ε . Substituting for B^c in the balance sheet identity for the USCB we

 $\underline{\mathbf{I}}$ It is assumed here that the UKCB holds all its reserves in the form of outside reserves.

see that if the U.S. money stock is to remain constant following an open market purchase we must have,

$$aB = - Md_{\varepsilon}$$

The change in \dot{r} consistent with equilibrium in the U.K. money market given that the U.S. money stock remains constant after an open market purchase is found by totally differentiating the U.K. money market equilibrium condition. Substituting in the expression above for dR and rearranging we obtain, $\frac{1}{2}$

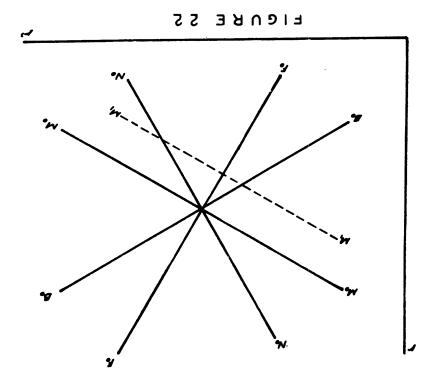
$$\cdot \frac{\underline{W} - \underline{W}}{\underline{w}} = s_{\underline{M}} = s_{\underline{M}} = s_{\underline{M}} = s_{\underline{M}}$$

This expression approaches zero continuously as W approaches zero. Thus a plausible-sized market purchase by the USCB results in no change in the world interest rate when the U.S. is small and U.S. and U.K. securities are perfect substitutes.

Now we turn to the case in which the U.S. is small but in

which U.S. and U.K. securities are neither completely non-substitutable nor perfectly substitutable for one another in the portfolios of wealth holders. This case is shown in Figure 22. The initial effect of an open market purchase is to shift the MM schedule from M_0M_0 to M_1M_1 . The open market purchase increases the U.S. money supply, and, if U.S. citizens are to be induced to hold this increase at a fixed r', there must be a decline in r. In contrast to the case in which the two countries are of roughly equal size, an open market purchase leaves the

 $\underline{1}/$ c', W, W', \overline{R} , S, and S' are held constant when the equilibrium condition is differentiated.



BB schedule unaffected when the U.S. is a small country. The equilibrium conditions in the market for U.S. securities is,

 $(W - \overline{W}) ('x, ')' d + W('x, ') d = W(3-1)$

where W has the same interpretation as in our previous discussion and e is ratio of U.S. securities held by the USCB to U.S. wealth. As before we assume that e is independent of the level of U.S. wealth and that open market purchases by the USCB are represented by increases in e. Totally differentiating the equilibrium condition for U.S. securities and rearranging we arrive at the expression for the change in r required to offset a rise in e given a fixed r',

$$\frac{dz}{d\varepsilon} \begin{vmatrix} z' = \overline{z}' \\ BB \end{vmatrix} = - \frac{b_x W + b'_x (\overline{W} - W)}{W}.$$

This expression approaches zero as W approaches zero unless b'r also approaches zero. Thus the BB schedule does not shift following an open market purchase by the USCB when the U.S. is relatively small unless the interest sensitivity of U.K. demand for U.S. securities approaches zero.

The decrease in the supply of U.S. securities available to private wealth holders resulting from an open market purchase is -Wde. The absolute value of this decrease approaches zero as the U.S. becomes of negligible size. The decrease in demand for U.S. securities by U.K. residents caused by a decline in r is -b'r(W-W). The absolute value of this decrease remains finite so long as b'r remains finite as to induce the fall in U.K. demand for securities necessary to offset to induce the fall in U.K. demand for securities necessary to offset to induce the fall in U.K. demand for securities necessary to offset from an open market purchase so long as b'r remains finite.

Would approach zero as W approaches zero only if U.S. securities were an indispensible asset in the portfolios of U.K. wealth holders, that an indispensible asset in the portfolios of U.K. wealth holders, that is, only if there were no finite r and r' pairs at which U.K. wealth holders would approach to prepared to hold no U.S. securities in their portfolios.

 $\frac{1}{L}$ Whether or not the absolute value of $\frac{dr}{d\varepsilon} \Big|_{r=r}^{BB}$, declines continuously as W declines is difficult to determine in general, and we leave this question open.

Returning to Figure 22 we see that if the BB schedule is

If U.S. securities were indispensable assets, further analysis would be required, but we will not treat this case here.

unaffected by the open market purchase the equilibrium values of the two interest rates are unchanged. The MM curve shifts back to M_0M_0 as U.S. citizens rebalance their portfolios by making net purchases of securities from U.K. residents. The U.S. loses reserves equal to the tull amount of the open market purchase. Thus the central bank in a small country is able to affect neither the interest rate on securities issued in its country nor its country's money supply by an open market purchase even if its securities are not perfect substitutes for those issued in the rest of the world provided that substitutes for those issued in the rest of the world provided that world's wealth holders.

VIII. Conclusions

A. An Overview

more general areas of concern.

constructive insights can be gained from it regarding all three of these capital account of the balance of payments in the short run, but deals exclusively with the determinants of the balance on the portfolio money as determinants of the overall balance of payments. Our model which emphasizes the role of changes in the supply of and demand for the "monetarist" approach to balance of payments analysis, an approach Third, we compare and contrast our portfolio balance analysis with librium is reattained after a disturbance except in extreme cases. disequilibrium system," However, in our model capital account equicurrent world payments arrangements may constitute an "international times may leave the world economy without an adjustment mechanism -argued that the mode of operation of monetary authorities in recent regarding the international adjustment mechanism. Robert Mundell has policy actions. Secondly, we draw some implications from our it provides a useful framework for highlighting the similarities among of alternative policy actions under different institutional arrangements, emphasize the fact that while our model can be used to study a variety approach for three separate areas of concern are stressed. First, we specific results obtained in earlier Chapters. The lessons of the general properties of our approach rather than to a summary of the This final Chapter is devoted to a discussion of some of the

B. The Economic Impact of Policy Actions

change rate change of a given amount.

One of the primary purposes of analytical economics is to cut through the institutional details surrounding a particular set of policy actions and to focus attention upon the economic impact of the

policies. One outcome of this type of activity is that policy actions which on the face of things seem quite different either because the sequence of actions taken is different can be shown to have equivalent economic impacts, that is, to be, in effect, the same policy action.

A familiar example of such an application of analytical economics is the demonstration that there exists a certain pattern of trade taxes and subsidies which has the same economic effect on trade flows as an example of such an example of such an action of analytical economics is the demonstration that there exists a certain pattern of trade taxes and subsidies which has the same economic effect on trade flows as an example of such and subsidies which has the same economic effect on trade flows as an example of such and subsidies which has the same economic effect on trade flows as an example of such and subsidies which has the same economic effect on trade flows as an example of such and subsidies which has the same economic effect.

A similar kind of result emerges from our model. There are four magnitudes under the direct control of the two central banks which influence the desired holdings of assets by private wealth holders, the available for the public to hold. Of course, central banks are limited in affecting these magnitudes by their balance sheet constraints. Since we assume that markets in all four financial assets are perfect, it we assume that markets in all four financial assets are perfect, it $\frac{1}{2}$ as a single for the public of assets available for the public to hold. So there is a single for the supplier of assets available for the public to hold.

 $\frac{1}{2}$ To simplify the discussion we assume that all money is either currency or a deposit at a central bank.

long as the policy responses of the central banks are specified, a given initial shift in asset supplies, no matter how it is accomplished, results in the same change in equilibrium interest rates and asset holdings. It is also important to recognize that a given initial shift may be the result of a chain of actions containing several intermediate steps. All that is important for tracing the economic impact of the actions is the net effect of the actions on supplies of the two kinds of money and two kinds of securities to the public.

Suppose we are informed that some central bank has purchased U.S. securities with U.S. money in a transaction with the private sector. This action will shift both the MM and the BB curve down so that the continuate section of the original FF and the new BB schedules lies above and equilibrium position will be uniquely determined by the pattern of policy responses of the two central banks. The identity of the central bank which caused the original shift is of no consequence. If the USCB initiates such an action we call it an open market purchase while if the initiates such an action we call it as shift in the composition of U.K. reserves. No matter what we call it, the economic impact is the of U.K. reserves. No matter what we call it, the economic impact is the same given the policy responses of the two central banks.

The same kind of argument can be used to demonstrate that two policy responses to a given initial disequilibrium which are superficially different are really the same from the point of view of economic impact. Consider an initial disequilibrium caused by a shift in wealth holders

preferences in favor of U.K. securities and away from U.S. securities resolved by central bank sales of pounds for dollars coupled with central bank use of these dollars to purchase U.S. securities. This knowledge is sufficient to determine the new equilibrium position. It makes no difference whether the UKCB performs both operations accumulating reserves in the form of U.S. securities and making no attempt to sterilize the U.K. money supply or both central banks perform the operations with the UKCB accumulating reserves in the form of outside assets and the USCB pursuing open market operations to sterilize the U.S. money supply.

1 Mundell (1968, ch. 15).

librium system from a balance of payments point of view. no matter what is happening to the balance of payments is a disequiset the value of the money supply in accordance with domestic objectives can persist indefinitely. Thus a system in which monetary authorities effects of payments imbalances on the money supply, these imbalances

money supplies matter. deficit (surplus). For Mundell security supplies do not matter; only without setting in motion any forces leading to the removal of the could take place without any change in interest rates and therefore available for the public to hold. In Mundell's model this process (sales) which reduce (increase) the quantity of domestic securities (surplus) a country must continually undertake open market purchases that in order to sterilize its money supply in the face of a deficit What Mundell failed to account for adequately is the fact

Although our short run portfolio balance model is not

ideally suited for a complete analysis of the questions posed at the

the standard IS-LM framework. affects some analysis of the financing of government budget deficits in results described in the text. A similar type of inconsistency also holders' behavior that allows Mundell to arrive at the misleading the interest rate is lowered. It is this assumed inconsistency in wealth Wealth holders will accept more real balances at a given income only if function is consistent with more usual portfolio balancing behavior. effect to the familiar liquidity trap. However, Mundell's money demand are in what might be called a "security trap" which is analogous in constant interest rates without altering their behavior. Wealth holders to experience increases or decreases in their security holdings at implication of this assumption is that wealth holders must be prepared will be a constant and finite net capital flow per unit time. account. He assumes that at any given level of interest rates there disequilibrium system Mundell employs a flow specification of the capital In his discussion (Mundell 1968, Ch. 15) of the international

a short run equitibrium in which there are no flows of financial capital.

If we change one or more parameters in the model a new short run equilibrium is attained in which there are no flows of financial capital. It we change one or more parameters in the model a new short run equilibrium to another. This movement from one equilibrium on portolio capital account to another occurs whatever the behavior of the monetary authorities does affect the behavior of the nonetary authorities does affect the size of the net capital flow which must occur between the two equilibrium positions. The large variety of cases considered in earlier chapters of this paper are proof enough that there are many alternative ways for equilibrium to be recertablished in our model, but here we limit our consideration to two important cases. Suppose some parameter change causes the MM to two important cases. Suppose some parameter change causes the MM to two important cases. Suppose some parameter change causes the MM and NN curve to intersect at a different interest rate pair than the

in the preferences of U.S. wealth holders in two cases Consider s shift in the preferences of U.S. wealth holders in favor of U.S. money and in the preferences of U.S. wealth holders in favor of U.S. money and sway from U.S. securities. If the two types of securities are perfect substitutes so that changes in relative supplies of securities with the new equilibrium cannot be reached when both countries sterilize their money supplies since the total supply of securities outstanding remains unchanged. If the MM and NN curves have the same slope, sterilization of money supplies in both countries alope, sterilization of money supplies in both countries alope, sterilization brought about by the change in the relative supplies of the two kinds brought about by the change in the relative supplies of the two kinds of securities cannot by the change in the relative supplies of the two kinds of securities cannot by themselves equilibrate both money markets.

inhibit the adjustment process. mechanism, it is not in general possible for monetary authorities to security adjustment mechanism are also possible. Whatever the exact two pure adjustment mechanisms as well as what we call a mixed moneywe call a pure security adjustment mechanism. Combinations of these given by this intersection. Adjustment is accomplished through what banks so that they satisfy security demands at the interest rate pair supplies are changed through open market operations by the two central given by the intersection of the MM and NN schedules and security if they pursue what we have called a MSCPR, the new equilibrium is other hand, both central banks sterilize their money supplies, that is, through what we call a pure money adjustment mechanism, rate pair given by this intersection. Adjustment is accomplished and money supplies adjust so as to satisfy money demands at the interest equilibrium is given by the intersection of the BB and FF schedules supplies, that is, if they pursue what we have called a GSPR, the new central banks accept passively whatever changes occur in their money one at which the BB and FF curves intersect. If on the one hand

We have shown rigorously that there is an automatic mechanism which shuts off any flow deficit or surplus on portfolio capital account. In order to obtain results which are strictly comparable to Mundell's we would have to imbed our two country portfolio balance model in a larger two country model in which outputs, price levels, trade flows, and perhaps other relevant variables are determined. Several other features of the model such as whether or not the labor supply is allowed to grow of the model such as whether or not the labor supply is allowed to grow

of the model such as whether or not the labor supply is allowed to grow and whether or not technical progress is incorporated would also be

Ver rigorous definitions of pure money adjustment, pure security adjustment, and mixed money-security adjustment and a discussion of some of the implications of relying on each of the different adjustment mechanisms or combinations of them see Part II of the Appendix, ment mechanisms or combinations of them see Part II of the Appendix.

approach.

important. In a portfolio balance model of an open economy in which the interest rate, output, and the capital stock are endogenous variables but in which there is no growth in the labor force and no continuing balance of payments deficit (surplus) even when the monetary authorities sterilize the money supply unless the country and for experiencing a budget deficit (surplus) of the same amount.

A crucial feature of McKinnon's model is that it refers to a period long enough that one of the requirements for equilibrium is that consumption expenditure equal disposable income; that is, wealth holders have their desired wealth levels. Certainly there is need for further research into the nature of the international adjustment mechanism, but it is clear that it is important to account for the mechanism, but it is clear that it is important to account for the mechanism, but it is clear that it is important to account for the mechanism, but it is clear that it is important to account for the portfolio balance considerations which have formed the basis of our portfolio balance considerations which have formed the basis of our

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The Relationship Between Changes in the Demand for and Supply of Money and Net International Movements of Financial Capital

of Money and Net International Movements of Financial Capital

money supply of an open economy is balance of payments surpluses (deficits). Some theorists have used this insight to develop a new approach to balance of payments analysis which focuses upon changes in the demand for and supply of money. This approach has been called the monetarist approach. This approach is founded on the assumption that the money market is always in equilibrium. In terms of our model the condition for equilibrium in, for example, the U.S. money market is,

equilibrium condition to be transformed into a theory of the balance

In order for the monetarists' rewriting of the money market money market equilibrium.

securities taken together by U.S. residents required to reestablish the same thing is that dR represents the net change in holdings of all which the securities were originally issued. Another way of saying sold by U.S. residents to U.K residents regardless of the country in securities purchased from U.S. residents by U.K. residents over those our model dR represents net capital inflow, that is, the excess of over the increase in the supply of money from domestic sources. of reserves must match the excess of the increases in money demanded money from foreign sources associated with an increase in the stock and would interpret it as stating that the increase in the supply of

 $qB = -qB_C + w^{\mathsf{T}} M q x + w^{\mathsf{T}} M q x_1 + w^{\mathsf{T}} M q h^{\mathsf{T}}$ rewrite this equation as, by changes in demand. A monetarist would find it more instructive to This equation simply states that changes in supply must be matched

 $dR + dB^{C} - m_{I} W dr + m_{I} W dr' + m_{I} W d\mu = 0.$ policy action we must have, market is to return to equilibrium after a change in tastes or some holders toward money and away from other assets. If the U.S. money where increases in µ represent shifts in the tastes of U.S. wealth

 $W_{g} \equiv B_{c} + E + Z = w(x, x, \mu)W$

of payments or, more accurately in the context of our model, a theory of reserve changes the monetarist must explain how dr and dr' are determined. $\frac{1}{2}$ determined. $\frac{1}{2}$ determined. $\frac{1}{2}$ design is amall, dr and dr' are given exogenously. Let under consideration is small, dr and dr' are given exogenously. Let assume for simplicity that they are both equal to zero. Suppose in addition, we assume, as monetarists often do, that there are no shifts in the demand for money so that dµ is equal to zero. In this case reserve thanges are equal to the negative of open market purchases by the central bank and we have a complete theory of the portfolio capital account for a small country.

However, as we have seen once we abandon the small country assumption dr and dr' can no longer be taken as exogenous. dR, dr, and dr' are jointly determined and their values depend upon the type

1/ We find it useful to describe what we believe to be the essence of the monetarist approach in terms of our model which refers only to the stock shift component of financial capital flows and ignores the continuing flow component of financial capital flows as well as trade flows and some direct investment flows. We have also restricted ourselves to consideration of changes that occur between one equilibrium and another.
The monetarist approach [Johnson (1962)] is usually presented in The monetarist approach [Johnson (1962)] is usually presented in

The monetarist approach [Johnson (1962)] is usually presented in terms of the growth rates of the variables considered. To obtain the equilibrium relationship between these growth rates the condition for respect to time; then various other algebraic manipulations are performed. The demand for real balances is assumed to depend upon real income as well as upon interest rates. In these more complete monetarist models the time rate of change of the stock of reserves monetarist models the time rate of change of the stock of reserves managed.

of disturbance or policy action undertaken and upon the policy responses of the central banks. When attempting to analyze the determinants of reserve changes due to net flows of financial capital for a large country it seems to us that it is necessary to look beyond the equation of equilibrium changes for the money market to a more the equation of equilibrium changes for the money market to a more fully specified model of the type we have investigated in this paper.

Appendix

The Comparative Statics Model

The equilibrium conditions for the four markets studied

in this essay when there is no commercial banking system in either

conutry can be written as follows:

$$p(x,x',h_{11a})W + \pi b'(x,x',h_{21a})W' - (B-B^c - B^c') = 0$$
 (A1)

$$f(r,r',h_{12})W + \pi f'(r,r',h_{22})W' - \pi(\overline{F}-F^{c'}) = 0$$
 (A2)

$$m(r,r,h_{13})W - (B^{c} + OR + S) = 0$$
 (A3)

$$\Pi n'(r,r',h_{23})W' - \left\{ \Pi[F^{C'} + \sigma'(\overline{R}-R) + S'] + B^{C'} \right\} = 0$$
 (A4)

The h_{ij}a's are shift parameters which cause changes in asset demands All of the symbols except the h_{ij}a's are defined in the text.

 $\epsilon_m = \epsilon_1 = \epsilon_q$ (**ZA**) subject to the following restrictions:

$$(9\forall) \qquad \qquad ```` u = ``` j = ``` q$$

$$(7A) (2,1=i 0 = ii 3$$

can be analyzed by setting the $h_{\underline{i},\underline{j}}$'s appropriately. equal to zero and then letting a increase. Other preference shifts setting hil equal to one, hiz equal to minus one, and all other hij's U.K. securities and against U.S. securities can be represented by example, a shift in the preferences of U.S. citizens in favor of values appropriate to the problem under consideration so that, for functions with respect to their third arguments. The hijs are given where b3, f3, etc., are the partial derivatives of the asset demand

whatever values are appropriate for the problem under consideration; If it is assumed that the hij's are held constant at

that $\overline{B},\overline{F}$, and \overline{R} are fixed; that $B^{c'}$ is held constant at Zero^{-1} ; and that W are fixed unless π changes, we can rewrite the

system in the following form,

$$(8A) (0 = (\underline{x})A$$

$$(A) \qquad (A) \qquad (A) \qquad (A) \qquad (A) \qquad (A) \qquad (A) \qquad (B) \qquad (B)$$

(01A)
$$(0 = (S \cdot \overline{x})M$$

(IIA)
$$0 = ('s', 'v', x)N$$

where \underline{x} is defined as follows:

$$\underline{x} \equiv (r,r',R,B^c,F^{c'},\pi,a),$$
 (A12)

As we have argued on page 16 of the text only three of the four market equilibrium conditions are independent, so we have,

$$B_{x_1} + F_{x_1} + M_{x_1} = 0$$
, (A13)

where $x_{\underline{i}}$ is any element of the vector $\underline{x}_{\boldsymbol{\cdot}}$ It is important to note

that when π changes, W and W' change so, for example,

$$B_{\Pi} = b'W' + bF^{A} - \frac{1}{\Pi}f B^{A'}, \qquad (A14)$$

where \mathbb{P}^A represents the holdings of U.K. securities by U.S. citizens in the equilibrium position which prevailed before the exchange rate change and $\mathbb{P}^{A'}$ represents holdings of U.S. securities by U.K. citizens in the same equilibrium position. $\frac{2}{2}$ It should also be observed that

 $[\]underline{\underline{l}}$ The exposition which follows could be smended to allow for a non-zero B^{c} , and for changes in B^{c} , but the benefits from added generality do not exceed the costs of increased complexity given the objectives of this Appendix.

 $[\]frac{2}{2}$ If this result does not seem clear, refer to the definitions of W and W' in the text.

the effect of a change in a on the excess demand for a given asset depends upon the values of the relevant h_{ij}'s so that, for example,

$$B^{3} = p^{3}y^{II}M + p^{3}y^{5}IM$$

In order to analyze the comparative statics properties of the model we find the total differentials of equation (A8) through (A11). We make use of two definitions and impose two restrictions when obtaining the total differentials. The changes in ${
m B}^{
m C}$ and ${
m F}^{
m C}$

are defined as follows: are defined as follows: (A16)

$$dFc' \equiv \lambda' dR + dFc'$$
 (A17)

by the USCB in order to sterilize the impact of reserve inflows on the U.S. money stock while dB^C represents open market purchases unrelated to sterilization activities. Similarly, $\lambda^i dR$, where $0 \le \lambda^i \le 1$, represents open market purchases undertaken by the U.K. money stock while dB^C represents open purchases undertaken by the sterilization activities the impact of reserve outflows on the sterilization activities. We call λ and λ^i the coefficients of sterilization activities. We call λ and λ^i the coefficients of sterilization activities in λ^i and λ^i the balancing items on the sterilization. Changes in λ^i and λ^i the balancing items on the central bank balance sheet, are restricted to be equal in size but opposite in sign to changes in the home currency value of outside opposite in sign to changes in the country due to a change in λ^i .

(81A)
$$, DA = Bb$$

$$dS' = -(R-R)d_{\sigma}', \quad d_{\sigma}(R-R)$$

where the relationship among $d\pi$, $d\sigma$, and $d\sigma$ is given by,

(02A)
$$\cdot \left[{}^{1} \nabla b \, \frac{\nabla}{^{1} \nabla} - \nabla b \right] \, \frac{1}{^{1} \nabla} = \pi b$$

Given the definitions and restrictions of the last paragraph we can write the total differentials of (A8) through (A11) in matrix form as shown in Table I. This is a system of tour <u>interdependent</u> equations in seven unknowns. Omitting any one of the four equations yields a system of three independent equations in seven unknowns. All of the comparative statics results in the text can be derived by selecting the appropriate set of three variables to regard as endogenous and treating the remaining variables to regard as endogenous and treating the remaining and the h_{ij}'s which appear in the partial derivatives of the excess demand functions with respect to a. L

 $\frac{1}{2}$ See footnote 1 on page of Appendix. If we allowed for a non-zero BC and for changes in BC we could derive all the results in Chapter III plus some additional ones.

ᅜ - (1- χ) (1-λ') a× а В dR dr' dr dπ Ю

Table I

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II. The Effect of Central Bank Sterilization Behavior on the Changes in International Reserve Holdings Required for Adjustment.

In the text we argued that in our model wealth holders can

successfully adjust their portfolios following a disturbance to portfolio equilibrium whether or not central banks act to sterilize international reserves except in some extreme limiting cases. In this section we demonstrate that the larger the proportion of changes in international reserves which are sterilized by either to changes in international reserves which absolute size of the change in international reserve which absolute size of the change in international reserve holdings which must occur when wealth holders adjust their portfolios following absolute size of the change in international reserve holdings which must occur when wealth holders adjust their portfolios following adjustment and what we call pure soney etcrilization behavior of the two central banks and show that the sterilization behavior of the two central banks and show that

money adjustment without increasing reliance on pure security
adjustment increases the efficiency of the adjustment mechanism in
the sense that smaller absolute changes in international reserve
holdings are required for the reattainment of equilibrium no matter
what the initial disturbance.

Dropping the fourth equation from the system shown in Table I and taking dr, dr', and dR as the endogenous variables leads to the

following system:

$$B_{\mathbf{r}} \qquad B_{\mathbf{r}} \qquad -\lambda \qquad d_{\mathbf{r}} \qquad = \qquad \frac{B_{\mathbf{r}}}{B_{\mathbf{r}}} \qquad \frac{d\mathbf{r}}{d\mathbf{r}} \qquad (A21)$$

 \overline{dy} is a 4x1 column vector and \overline{dy} is given by

$$\frac{d\mathbf{y}'}{d\mathbf{y}'} \equiv [\overset{\sim}{d\mathbf{E}}^{\mathbf{c}} \overset{\sim}{d\mathbf{\pi}} d\mathbf{\pi} \quad d\mathbf{a}]. \tag{A22}$$

derivatives of B, F, and M with respect to the variables the differentials $\overline{P_X}$, $\overline{Y_Y}$ and $\overline{M_X}$ are lxt row vectors of the negatives of the partial

of which are the elements of \underline{dy} so, for example,

$$\mathbf{B}_{\underline{Y}} \equiv [-1 \quad 0 \quad -\mathbf{B}_{\overline{\Pi}} \quad -\mathbf{B}_{\overline{\alpha}}]. \tag{A23}$$

Let C be the matrix of the coefficients of dr, dr', and dR.

$$qef C = - (I-Y)(B^{L}E^{L_1}-E^{L}B^{L_1}) + Y_1(B^{L_1}M^{L_1}-B^{L}M^{L_1})$$

$$+ \lambda(F_{\mathbf{r}}^{\dagger}M_{\mathbf{r}}^{\dagger}-F_{\mathbf{r}}M_{\mathbf{r}}^{\dagger}) \qquad (A24)$$

Now define:

Then we have;

$$\nabla^{BE} \equiv B^{T}E^{T_{\parallel}} - E^{T}B^{T} > 0 \tag{452}$$

$$\Delta_{BM} \equiv B_{L}^{\dagger}M_{L} - B_{L}M_{L}^{\dagger} > 0 \tag{A26}$$

$$\nabla^{LM} \equiv \mathbf{E}^{L_1} \mathbf{W}^{L_2} - \mathbf{E}^{L} \mathbf{W}^{L_1} < 0 \tag{A27}$$

$$\nabla^{L} = \mathbf{k}^{L} \cdot \mathbf{k}^{L} = \mathbf{k}^{L} \mathbf{k}^{L} = 0$$
 (Y7V)

$$\Lambda_{\text{T}} \equiv \mathbf{F}_{\text{A}} \mathbf{V} - \mathbf{F}_{\text{A}} \mathbf{V} < 0 \tag{A28}$$

$$\Delta_{\mathbf{F}N} \equiv \mathbf{F}_{\mathbf{r}} \mathbf{i} \mathbf{u}_{\mathbf{r}} - \mathbf{F}_{\mathbf{r}} \mathbf{u}_{\mathbf{r}} \mathbf{i} < 0 \tag{A28}$$

$$\triangle_{MN} \equiv M_{L}N_{L} - M_{L}N_{L} > 0$$
 (A29)

is less negatively sloped than the MM schedule implies $\triangle_{MN} > 0$. for \triangle_{BF} , \triangle_{FM} , \triangle_{FM} , and \triangle_{FW} . Our assumption that the MM schedule Our assumption of gross substitutes implies the signs shown above

 $\frac{2}{2}$ See footnote 1.

1/ This identity can be established by using (Al3).

changes due to changes in international reserves which are sterilized

Thus we have proved that the larger the proportion of money supply

that raising either A or A' makes det C a smaller negative number,

determine that D does not depend upon A or A'. We know from (A32)

inspecting all the terms that are involved in calculating D we can

where D is a scalar which can be either positive or negative.

 $dR = (det C)^{-1}(-\Delta_{FM} BY + \Delta_{BM} FY + \Delta_{BF} MY) dY \equiv (det C)^{-1}D \quad (A35)$

Solving for dR we find,

. I \geq ' λ ', $\lambda \geq 0$ Tolegative for C λ ', λ ' of the simple of the simple specifical contents of the s

 $M_{\text{A}} = M_{\text{A}} - M_{\text{A}}$ (4£A)

and we can establish that, $\frac{2}{2}$

det C = \triangle_{BM} + \triangle_{FM}

(EEA)

 $\lambda = \lambda' = 1$. However, from (A30) we can see that if $\lambda = \lambda' = 1$ then,

see that det C is at its least negative (most positive) when

 \triangle_{BF} is positive, but \triangle_{FM} and $-\triangle_{\mathrm{FM}}$ are positive, so from (A32) we can

We can establish that det C is negative for all $0 \le \lambda$, $\lambda' \le 1$.

(SEA)

we can also write,

· NT - T8 - ≡ MT (IEA)

If is helpful to note that since, $\frac{1}{L}$

(0£A)

Given these definitions we can rewrite det C as,

international reserves required for adjustment. ph either central bank the larger the absolute change in holdings of

The economics behind this result can be more easily

understood if we multiply and divide (A34) by \triangle_{BF} to obtain,

$$q_{R} = E^{-L}G$$
 (A36)

MyGLG'

$$E = \left[-(1-\lambda) + \lambda' \frac{\Delta_{BM}}{\Delta_{BF}} + \lambda \frac{\Delta_{FM}}{\Delta_{BF}} \right], \tag{A37}$$

$$G = D\left(\Delta_{BF}\right)^{-1}, \tag{A38}$$

(0)A) (1)
$$[0]$$
 agis = $[0]$ mgis

required to reequilibrate the two securities markets following a in R taking into account the fact that the interest rate changes the net reduction in the excess demand for money caused by a rise adjusted to clear both securities markets and E can be viewed as created by the disturbance $\underline{d}\underline{Y}$ given that interest rates are in this form, G can be viewed as the net excess demand for money since \triangle_{BF} is positive. When the expression for dR is written

$$E = \left[- (1-\lambda) + M_{x} \left(\frac{B_{x'}\lambda' + F_{x'}\lambda}{\Delta_{BF}} \right) + M_{x'} \left(- \frac{B_{x}\lambda' + F_{x}\lambda}{\Delta_{BF}} \right) \right]. \quad (A41)$$

change in r, and - $(\triangle_{BF})^{-1}(B_r\lambda^i + F_r\lambda)$ is the change in r' which are resulting from an increase in R. $(\triangle_{\mathrm{BF}})^{-1}(B_{\mathbf{r}},\lambda'+F_{\mathbf{r}},\lambda)$ is the - $(1-\lambda)$ is the direct reduction in the excess demand for money

This interpretation of E is easier to explain if we rewrite it as,

rise in R have repercussion effects on the excess demand for money.

(A42)
$$\log \left[\frac{\partial E}{\partial \delta}\right] = \operatorname{sgn}\left[\frac{\partial E}{\partial \delta}\right] > 0 , \qquad (A42)$$

$$\operatorname{sgn}\left[\frac{\partial E}{\partial \delta}\right] = \operatorname{sgn}\left[\frac{\partial E}{\partial \delta}\right] = \operatorname{sgn}\left[\frac{\partial$$

$$sgn \left[\frac{\partial E}{\partial \lambda^{1}}\right] = sgn \left[\frac{\partial \det C}{\partial \lambda^{1}}\right] > 0 .$$
 (A43)

the amount by which a rise in R indirectly reduces (increases) (offsetting) indirect effect. An increase in A' lowers (raises) must more than offset the increase (decrease) in the reinforcing money. From (A42) we know that the reduction in the direct effect a rise in R indirectly reduces (increases) the excess demand for The same increase in A also raises (lowers) the amount by which which a rise in R directly reduces the excess demand for money. We can see from (A41) that an increase in A lowers the amount by

It is instructive to investigate how central bank the excess demand for money.

public. From the two central bank balance sheets we have, $\frac{1}{2}$ in money supplies and supplies of securities in the hands of the for adjustment, but here we focus attention on the required changes Of course, changes in both interest rates are usually necessary portfolio adjustment following an initial disturbance proceeds. sterilization behavior affects the channels through which the

the adjustment process following an initial disturbance. equilibria they do not affect the changes in these supplies during and supplies of securities in the hands of the public between while these variables affect the total changes in money supplies Here we view dBc and dFc' as initial disturbances so that

an increase in R is always a reduction in the excess demand for We know that the net impact of the direct and indirect effects of decreases in either r or r' partially offset the direct effect. of an increase R in lowering the excess demand for money while Of course, increases in either r or r' reinforce the direct effect general case the interest rates may both move in either direction. that a rise in R leads to a fall in r and a rise in r'. In the If λ is equal to λ ,, our assumption of gross substitutes implies A is positive), then a rise in R leads to rise (fall) in r and r'. limiting cases. If A is zero and A' is positive (A' is zero and tends to drive both rates down. It is helpful to consider some interest rates up, but the decrease in supply of U.K. securities increase in the supply of U.S. securities tends to drive both supply of U.K. securities available for the public to hold. increase in the supply of U.S. securities and a reduction in the Sterilization operations following an increase in R lead to an operations in the two countries following an increase in R. changes in security supplies which result from sterilization required to reequilibrate the two securities markets given the

money since E is always negative.

We also know that an increase in either how hi lowers

demand for money since,

(∠ \ ∀)	$qE_{g} = \gamma_{i}qB^{2}$
(9 7 ¥)	$qB_{g} = -yqB$
(S4 Y)	$qN_{S} = -(1-\lambda^{\dagger})dR,$
(₱₱♥)	$dM^{S} = (1-\lambda)dR,$

respective assets in the hands of the public and dR is the change where, as before, $M^{\rm s}$, $M^{\rm s}$, $B^{\rm s}$ and $F^{\rm s}$ refer to the supplies of the

by an equal but opposite change in the other country's money supply. may be accomplished by a change in one country's money supply matched some useful distinctions. Part of the adjustment in asset supplies process involves changes in all four asset supplies, but we can make in USCB reserves required for adjustment. In general the adjustment

Another part of the We call this form of adjustment pure money adjustment. If involves

a redenomination of the world's money supply.

country's securities matched by an equal but opposite change in the adjustment may be accomplished by a change in the supply of one

adjustment pure security adustment. It involves a redenomination of supply of the other country's securities. We call this form of

passive $(\lambda = \lambda' = 0)$ the necessary adjustment in asset supplies is the world's supply of securities. When both central banks remain

"composition of the world monetary base" whenever there is a "creation In the terminology of Roper (1972) there is a change in the

distribution" of the world monetary base if it is assumed "that resiposition of the world monetary base "implies a change in the liabilities by the other central bank, " and a change in the comof new liabilities by one central bank and the destruction of

in the currency of their respective countries." dents of each country hold only cash balances which are denominated

The case in which $0 \le \lambda$, $\lambda' \le 1$ but $\lambda \ne \lambda'$ is a little more on pure money adjustment implies equal decreases in λ and λ' . in reserve holdings are required for adjustment since greater reliance efficient the adjustment mechanism in the sense that smaller changes so far the greater the reliance on pure money adjustment the more redenominated. We can conclude that in the cases we have considered securities remains constant but some part of both supplies is $(1-\lambda) = (1-\lambda^{\dagger})$. The world money supply and the world supply of adjustment, |dk|, accomplished by pure money adjustment is given by adjustment and pure security adjustment. The proportion of the total adjustment is accomplished through a combination of pure money is redenominated. If $0 \le \lambda$, $\lambda' \le 1$ and $\lambda = \lambda'$, then we say that change in money supplies. Part of the fixed world supply of securities accomplished completely though pure security adjustment with no changes in their money supplies $(\lambda = \lambda' = 1)$, adjustment is money supply is redenominated. When both central banks sterilize all in the supply of either type of security. Part of the fixed world accomplished completely through pure money adjustment with no change

difficult. In this case part of the adjustment is pure money adjustment, and part is pure security adjustment, but a part of the adjustment is accomplished by increases (decreases) in the world money supply matched by decreases (increases) in the world supply of bonds, a process which we call mixed money-security adjustment. The proportion of the total adjustment, |dR|, accomplished by pure money adjustment is {min [(l-\lambda)), adjustment of adjustment accomplished by pure security (l-\lambda)),

adjustment is $\{\min [\lambda, \lambda']\}$; the proportion of adjustment accomplished by mixed money-security adjustment is $\{\max [\lambda, \lambda'] - \min [\lambda, \lambda']\}$. We can now state the general conclusion that if reliance on pure money adjustment is increased with no increase in the reliance on pure security adjustment then the adjustment mechanism is made more efficient, since an increase in the reliance on pure money adjustment requires a decrease in the larger of λ and λ ' while no increase in reliance on pure security adjustment $\frac{1}{\lambda}$ and λ ' does not increase.

2 tramtsuibe vogen cano es es it

\(\frac{1}{2}\)\ When an increase in reliance on pure money adjustment is accompanied by an increase in reliance on pure security adjustment the implications for the efficiency of the adjustment mechanism can only be obtained by analyzing the effects of changes of \(\hat{A}\) in (A35).
The problem encountered here is analogous to the problem of the problem of a consumer is better off when we observe determining whether or not a consumer is better off when we observe the standard of the consumer is a consumer in the problem of the

him consuming a new consumption bundle. If he consumes more (fewer) of all goods, he is unambiguously better (worse) off, but if he consumes more of some goods and fewer of others, we must know his utility function before we can determine whether or not his lot has improved.

In the present case if both λ and λ' fall (rise), adjustment is more (less) efficient, but if they move in opposite directions, we must know the values of the parameters in (det C)-1 before we can

determine whether adjustment is more or less efficient.

III. Some Implications of the Application of Stability Analysis

In this section we investigate the implications of applying stability analysis of the conventional kind to the important variant of our model in which r, r', and R are the endogenous variables.

We have two major points to make. First, we show that the restrictions on the slopes of the BB, FF, MM, and NN schedules employed in the text are consistent with stability under a plausible set of assumptions about how the endogenous variables change in response to disequilibria. Second, we show that certain restrictions must be placed upon the relative speeds of adjustment in the different markets if stability is to be guaranteed under our assumptions and suggest why these restrictions are required.

Let us assume that the way in which the endogenous variables change in response to disequilibria can be described by the following set of equations:

$$\frac{\dot{\mathbf{r}}}{\mathbf{r}} = -\alpha_1 \frac{\mathbf{B}(\underline{\mathbf{x}})}{\mathbf{B} - \mathbf{B}^c} , \alpha_1 > 0, \tag{A47}$$

$$\frac{\dot{\mathbf{r}'}}{\mathbf{r'}} = \alpha_2 \frac{\mathbf{F}(\mathbf{x})}{\pi(\overline{\mathbf{F}} - \mathbf{F}^{\mathbf{c'}})}, \quad \alpha_2 > 0, \quad (A48)$$

$$\frac{R}{R} = \alpha_3 \frac{M(\underline{x}, \sigma, S)}{B^C + \sigma R + S}, \quad \alpha_3 > 0.$$
 (A49)

r rises in response to excess supply of U.S. securities; r' rises in response to excess supply of U.K. securities; R rises in response

as a percent of supply in that market. Under this assumption al, to the excess supply or demand in the market to which it responds in each endogenous variable as a percent of its level is proportional $\frac{1}{1}$ to excess demand for money in the U.S. We assume that the change

 α_2 , and α_3 are dimensionless.

the system about the equilibrium values $(\mathbf{r}_0,\ \mathbf{r}_0',\ \mathbf{R}_0)$ using the in the neighborhood of an equilibrium. The results of linearizing system by investigating the behavior of the associated linear system We can study the local stability properties of our dynamic

 $\frac{2\sqrt{3}}{4r}$, and dR represent deviations of the definitions and restrictions of Part I of the Appendix are displayed

respective variables from $(\mathbf{r}_0, \mathbf{r}_0^1, R_0)$.

to excess demand for money in the U.K. so that, <u>I</u>/ It would be just as plausible to assume that R falls in response

(A50)
$$\frac{R}{R-R} = -\alpha_{\varphi} \frac{N(\underline{x}, \sigma', S')}{\pi[Fc' + \sigma'(\overline{R}-R) + S']}, \alpha_{\varphi} > 0.$$

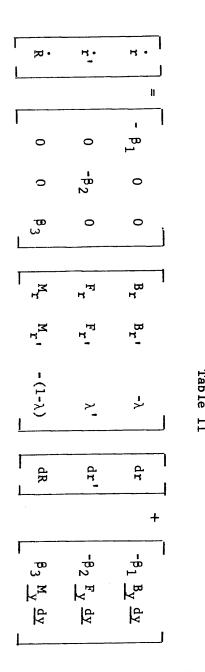
footnotes the similarities and minor differences in results implied both money markets. Here we restrict ourselves to reporting in carefully what would happen to R when there is excess demand in specified. It would take us too far afield to try to specify more arises in other, more familiar models if all markets are fully demand in both money markets. A similar potential inconsistency (A49) and (A50) can be inconsistent since for some \underline{x} there is excess

.(949) lo bestead (02A) gaisu yd

$$\frac{2}{3}$$
 Note that $\dot{t}_0 = \dot{t}_0' = 0$

$$B_{\rm c} - B_{\rm c}^0 = -y(g - g^0) + \tilde{g}_{\rm c} - \tilde{g}_{\rm c}^0,$$
 (Y21)

$$E_{c_1} - E_{c_2}^0 = Y_1(B - B_0^0) + E_{c_1} - E_{c_2}^0$$
 (A27)



 $\frac{R}{\Delta}$, $\frac{Y}{\Delta}$, and $\frac{dY}{dX}$ are defined as in Part II of the Appendix. /T

 β^{1} , β^{5} , and β^{3} are given by,

$$b_{\perp} = \alpha_{\perp} \frac{\overline{B} - B_{C}^{0}}{\overline{x}_{0}} > 0,$$

$$\beta_2 = \alpha_2 \frac{r_0^2}{m_0(\bar{r} - r_0^2)} > 0$$

$$\beta_3 = \alpha_3 \frac{R_0^2 + \sigma_0 R_0 + S_0}{R_0^2 + \sigma_0 R_0 + S_0} > 0.$$

The stability analysis proceeds according to the usual pra-

The characteristic polynominal of the system of Table II

is given by,

$$(-1) \begin{vmatrix} -\beta_1 B_r - \delta & -\beta_1 B_r \\ -\beta_2 F_r & -\delta & -\beta_2 V_r \\ -\beta_3 M_r & -\beta_3 (1-\lambda) - \delta \end{vmatrix} = 0, \quad (A52)$$

which can be written in the form,

$$(62A) 0 = \epsilon_B + \delta_{\Delta^B} + \epsilon_{\delta}$$

$$\overline{\underline{1}}$$
/ That is, $\overline{dB}^c = \overline{B}^c - B G$, $\overline{dF}^c = \overline{F}^c$, $-\overline{F}^c$, $\overline{d\pi} = \pi - \pi_0$, and $\overline{da} = a - a_0$.

.954-924, for example, Samuelson (1965), pp. 429-439.

where,

$$a_{1} = \beta_{1}B_{r} + \beta_{2}F_{r} + \beta_{3}(1-\lambda),$$
(A57)

$$a_{2} = \beta_{1}\beta_{2} \Delta_{BF} + \beta_{1}\beta_{3} [(1-\lambda)B_{r}-\lambda M_{r}]$$

$$A_{2} = \beta_{1}\beta_{2} \Delta_{BF} + \beta_{1}\beta_{3} [(1-\lambda)B_{r}-\lambda M_{r}]$$

$$+ b^{5}b^{3} [(I-Y)E^{r_{1}} + Y,W^{r_{1}}],$$
 (A58)

$$s^3 = b^T b^S b^3 [(I-y)Q^B E - yQ^E M - y,Q^B M]$$

$$= - b^{I} b^{S} b^{3} q^{GF} C ag{429}$$

If our comparative statics results are to be meaningful,

the system which describes the responses of the endogenous variables

1/ Agr, Arm, Agm and det C are defined as in Part II of the Appendix.

each bluow ew (94A) to be tread of (04A) be would have $\frac{2}{2}$

$$a_{1} = \beta_{1}B_{r} + \beta_{2}F_{r} + \beta_{4}(1-\lambda^{\dagger}), \tag{A54}$$

$$a^{2}_{2} = \beta_{1}\beta_{2} \Delta_{BF} + \beta_{1}\beta_{4} [B_{r}(1-\lambda^{2}) - \lambda^{2}N_{r}]$$

$$+ \beta_{2}\beta_{4} [F_{r}(1-\lambda^{2}) - \lambda^{2}N_{r}]$$
(A55)

$$a^{3} = \beta_{1}\beta_{2}\beta_{4} [(1-\lambda^{1}) \Delta_{BF} + \lambda\Delta_{FN} + \lambda^{1}\Delta_{BN}]$$

$$= \beta_1 \beta_2 \beta_{\varphi} \text{ det } K.$$

where those symbols defined in Part II of the Appendix have the same

meaning here and,

$$\beta_{4} = \alpha_{4} \frac{\bar{R} - \bar{R}_{0}}{[\bar{R} - \bar{R}_{0}]^{1} + \sigma_{0}^{1}(\bar{R} - \bar{R}_{0}) + \sigma_{0}^{1}]}$$

$$\nabla^{BN} = B^{L_1} N^{L_2} - B^{L} N^{L_1} > 0$$

.besizearized. coefficients dr, dr', and dR when the system made up of (A47), (A48), and det K is the determinant of the matrix K, the matrix of the

conditions for the stability of the system of Table II are given by, to excess supplies and demands must be stable. Necessary and sufficient

$$(08A)$$
 $0 < I^{B}$

(19A)
6

$$(20A) \qquad \qquad 0 < \epsilon^{B} - \epsilon^{B}$$

responses and the restrictions on A and A' just stated, al is always $\frac{2}{\sqrt{2}}$ if ≥ 1 , $\lambda \geq 0$ IIs Given our assumptions about interest rate behavior by the two central banks, the conditions above must hold for To assure that the system is stable for all plausible sterilization

From our analysis of det C in Part II of the Appendix

 $\Delta_{
m BF}$ and $\Delta_{
m MN}$ are positive. Thus, if the system of Table II is to we know that a_3 is positive for all $0 \le \lambda$, $\lambda' \le 1$ if and only if

1 See, for example, Samuelson, op. cit.

consider cases in which λ , λ < 0. $\frac{1}{2}$ As we shall see in Part IV of the Appendix it is also useful to

 $\frac{3}{1}$ a is also positive if $\lambda < 0$.

assumptions and restrictions. $\frac{4}{4}$ in footnote 2 page 155 is always positive under these same

Am is defined as in Part II of the Appendix.

be stable for all $0 \le \lambda$, $\lambda' \le 1$, the relative slopes of the BB and FF and of the MM and MM curves must be as we have described them in the text.

So far it has not been necessary to consider the relative magnitudes of the adjustment coefficients α_1 , α_2 , and α_3 . However, if $a_1a_2-a_3$ is to be positive for all $0 \le \lambda$, $\lambda' \le 1$, we must place restrictions on these coefficients. The easiest way to see this is to note that (A60), (A61), and (A62) together imply $a_2 > 0$, but from (A55) we can see that a_2 need not be positive for all values of a_1 , a_2 , a_3 , that is, for all values of a_1 , a_2 , and a_3 , if λ and λ' are allowed to take on all values between zero and one. To see this

rewrite a₂ as,

 $1/a_3$ is positive for all λ , $\lambda'<0$ if and only if $\Delta_{\rm BF}>0$. The same conditions are necessary and sufficient to insure that

 $\frac{2}{\ln}$ The same conditions are necessary and sufficient to insure that ay in footnote 2 on page 155 is positive. a_3 is at its most negative when $\lambda = \lambda' = 1$ as can be seen from the fact that a_3 can be written as

 $a_{3}^{1} = B_{1}B_{2}B_{4}$ ($\Delta_{BF} + \lambda\Delta_{FW} - \lambda^{1}\Delta_{BM}$),

'apurs

 $\Delta_{BM} = \Delta_{BF} - \Delta_{BW}$

Furthermore we have that,

 $\mathbf{a}_{3} = \begin{cases} \mathbf{a}_{1} \mathbf{b}_{2} \mathbf{a}_{3} & \Delta_{\mathbf{M}}, & \text{if } \lambda = \lambda' = 1, \\ \mathbf{a}_{1} \mathbf{a}_{2} \mathbf{a}_{3} & \Delta_{\mathbf{M}}, & \text{if } \lambda = \lambda' = 1, \end{cases}$

since, $\Delta_{MN} = \Delta_{FN} + \Delta_{BN}.$

.0 < EB - $\Delta^{\rm B}I^{\rm B}$ VI is not true that all > 0, all and a3 > 0 imply all $\Delta^{\rm B}$.

(footnote continued on following page)

$$G_{2} = \beta_{2}^{2}\beta_{3}F_{\mathbf{r}}^{\dagger}M_{\mathbf{r}} < 0. \tag{A65}$$

$$c_{1} = \beta_{2}^{2} F_{r_{1}}^{\Delta_{BF}} + \beta_{2} \beta_{3} (B_{r_{1}}^{M_{r_{1}}} - F_{r_{M_{r_{1}}}}) \ge 0, \tag{A64}$$

$$g_{1} = \beta_{2}^{2} F_{r_{1}}^{\Delta} B_{F} + \beta_{2} \beta_{3} (B_{r_{1}}^{\Delta} M_{r_{2}} - F_{r} M_{r_{1}}) \geq 0, \tag{A64}$$

$$G^{0} = \beta^{5} B^{L} \nabla^{BE} - \beta^{3} B^{L} W^{L} > 0,$$
(Ye3)

$$a_{1}a_{2} - a_{3} = c_{0}\beta_{1}^{2} + c_{1}\beta_{1} + c_{2},$$
 (A62)

 $0 \le y$, $\lambda' \le 1$. Now when $\lambda = \lambda' = 1$ we have,

Thus if $a_1a_2 - a_3$ is positive for $\lambda = \lambda' = 1$, it is positive for increases in λ and λ ' and reach their minimum values for $\lambda = \lambda$ ' = 1. when $\lambda = \lambda' = 1$. It can also be shown that all and all decline with larger the larger are A and A' and that it reaches its maximum value β_3 and therefore, α_1 , α_2 , and α_3 , we have that $\alpha_3 = -\beta_1\beta_2\beta_3$ det C is from the analysis of Part II of the Appendix that, given bl., B2, and tion for ala2 - a3 to be positive for all $0 \le \lambda$, $\lambda' \le 1$. We know $\frac{1}{2}$ In this footnote we sketch the derivation of a sufficient condi-

system is unstable. enough to one, at is negative, so ala? - al is negative, and the For values of \$2 near enough to zero and values of \$ and \$7 near

An analogous rewriting of a2 yields,
$$a_{2}^{\perp} = \beta_{1}\beta_{4} \left\{ \frac{\beta_{2}}{\beta_{4}} \Delta_{BF} + [(1-\lambda')B_{T} + \lambda N_{T}] + \frac{\beta_{2}}{\beta_{1}} [(1-\lambda')F_{T}] \right\}$$
(A61)

 $\frac{1}{2}$ An analogous rewriting of aly yields,

can be described less formally. Suppose that Figure 23 represents but the destabilizing pressures the effects of which must be limited $^{6}1^{8}2^{-3}$ is positive for all $0 \le \lambda$, $\lambda' \le 1$ are not very instructive,

The exact conditions on α_1 , α_2 , and α_3 which insure that

alastanu si mesetive, and the system is unstable. to zero and values of λ and λ near enough to one, as is negative, so $\underline{1}/$ λ and λ ' approach one. It is clear that for values of α_1 near enough

and let β_1 approach zero, that is, let α_1 approach zero, and let

$$a_{2} = \beta_{2}\beta_{3} \left\{ \frac{\beta_{1}}{\beta_{3}} \Delta_{BF} + \frac{\beta_{1}}{\beta_{2}} \left[(1-\lambda)B_{r} - \lambda M_{r} \right] + \left[(1-\lambda)F_{r} \right] + \lambda^{2}M_{r} \right\}$$
(A60)

A similar line of argument can be used to sketch a derivation of a sufficient condition for $a_1^{1a}a_2^{1}-a_3^{1}$ to be positive for all $0 \le \lambda,\lambda' \le 1$, but we do not pursue this line of argument here.

a way that α_1 is always greater than $\left(\frac{\overline{B} - B\overline{0}}{10}\right)^*\beta_1$.

 $a_1a_2 - a_3$ to be positive for $\lambda = \lambda' = 1$ and is a sufficient condition for $a_1a_2 - a_3$ to be positive for all $0 \le \lambda$, $\lambda' \le 1$. If the speed of adjustment in the market for 0.5, securities is "large enough" relative to afunction of the speeds of adjustment in the other two markets which increases in value with an increase in either of the other two speeds of adjustment, then $a_1a_2 - a_3$ is positive. Since we are assuming that all the asset markets adjust instantaneously, what we really require is that α_1 , α_2 , and α_3 increase without limit in such really require is that α_1 , α_2 , and α_3 increase without limit in such

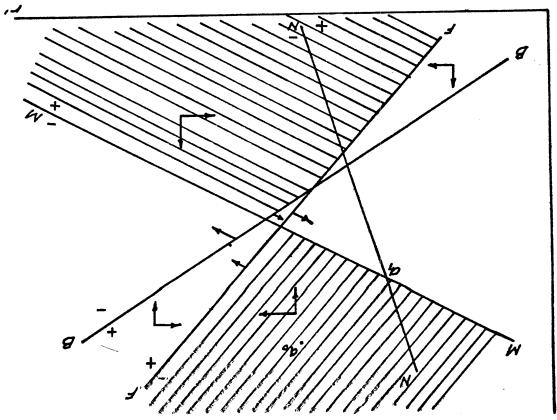
 α_1 greater than $\left(\frac{\overline{B}-B_0^C}{\overline{L}_0}\right)^*$ is a necessary and sufficient condition for

(866)
$$\frac{c_0}{69} - \frac{c_0}{4} \left(\frac{c_0}{69}\right) \frac{1}{4} \sqrt{c_0} + \frac{c_0}{69} \frac{1}{4} - c_0$$

Given all the other parameters, we can solve for the positive value of \$1 which makes ala2 - a3 equal to zero,

(footnote continued from previous page)

FIGURE 23



pair can become "trapped" in this region, and the process can tions are placed on α_1 , α_2 , and α_3 , the prevailing interest rate falls, and the U.S. continues to lose reserves. Unless some restricrate pair remains in the shaded region above MM and FF, r' rises, r BB anf FF move to the southeast. As long as the prevailing interest U.S. money, and the sterilization of U.S. reserve losses implies that At a₀, for example, there is an excess supply of two central banks. in the supply of U.K. securities due to sterilization operations of the (increase) in the supply of U.S. securities and an increase) lates) reserves. These losses (accumulations) lead to a decrease excess supply of (demand for) U.S. money, and the U.S. loses (accumu-For all interest rate pairs above (below) the MM schedule there is an the effects of sterilization operations on the BB and FF schedules. on r. Diagonal arrows pointing southeast and northwest represent U.S. securities, so there is upward pressure on r' and downward pressure there is an excess supply of U.K. securities and an excess demand for the pressure on \mathbf{r} in each of the same four regions. At \mathbf{a}_0 , for example BB and FF schedules. Vertical arrows pointing up and down represent the pressure on r' in each of the four regions marked off by the point is at al. Horizontal arrows pointing left or right represent the shock was at a_0 and that $\lambda = \lambda' = 1$ so that the new equilibrium initial disturbance. Let us assume that the equilibrium point before the configuration of the BB, FF, MM, and NN schedules after an

^{1/} If we replace (A49) by (A50), BB and FF move northwest if the prevailing interest rate pair lies above NN and southeast if the prevailing interest rate pair lies below NN.

This same line of argument with minor modifications can be tains the prevailing interest rate pair, and the system is unstable. region above MM and FF expands rapidly enough so that it always con-BB and FF. If $\alpha_{\rm L}$ is "too small" relative to $\alpha_{\rm Z}$ and $\alpha_{\rm 3}$ the shaded excess supply of money accentuate the southeastward movement of Decreases in R due to U.S. citizens attempts to get rid of their U.K. securities accentuate the southeastward movement of BB and FF. FF, but increases in r' while tending to equilibrate the market for U.S. securities and retard the southeastward movement of BB and central banks. Increases in r tend to equilibrate the market for size of U.S. reserve losses and sterilization operations by the two citizens to their excess supply of money, a3, which determines the r' to excess supply for U K. securities, all the response of U.S. demand for U.S. securities, α_{1} , is small relative to the response of the shaded region above MM and FF if the response of r to excess can conclude that the prevailing interest rate pair will remain in continue without limit. Without attempting to be precise

used to suggest how a value of α_1 which is "too small" can result in the prevailing interest rate pair becoming "trapped" in the shaded region below MM, BB, and FF. In this case r' falls, r rises, and the U.S. accumulates reserves without limit.

We have seen above that for $\lambda = \lambda' = 1$ and a value of which is "small enough" we can have ala? - a3 negative in which

 $\frac{1}{2}$ See footnote $\frac{1}{2}$ on page 158.

 $\frac{2}{2}$ See footnote l on page 158.

case the characteristic equation of the system must have one positive root or a pair of complex roots with a positive real part, and the system is unstable. In terms of Figure 23 the prevailing interest rate pair eventually becomes "trapped" in one of the two shaded

When $0 \le \lambda, \lambda' < 1$, similar destabilizing forces are at work. The discussion above could be modified to take account of this more complicated case. As above, the size of α_1 relative to the size of α_2 and α_3 would be important in determining whether or not instability could arise.

regions.

However, this essay is concerned with the comparative statics analysis is only meaningful when the system attains a new equilibrium after an initial disturbance, we assume that α_l is "large enough" relative $\frac{1}{2}$ to α_l and α_l to assure that the system is stable for $0 \le \lambda, \lambda' \le l$.

IV. The Comparative Statics Model With Fractional Reserve Commercial Banking

The purpose of this part of the Appendix is to show that, under certain assumptions, conclusions based on the model of Part I of the Appendix, when properly interpreted, are identical to conclusions based on a model which takes explicit account of fractional reserve commercial banking. The equilibrium conditions

 $\frac{1}{1}$ See footnote 1 on page 158 for a condition sufficient to insure stability.

for the four markets studied in this essay when fractional reserve

 $p(\mathbf{r}, \mathbf{r}', \mathbf{h}_{11a})W + \pi b'(\mathbf{r}, \mathbf{r}', \mathbf{h}_{21a})W' - [\overline{B} - R^{c} + S)] = 0$ (A67)

$$f(\mathbf{r}, \mathbf{r}', h_{12}) + \pi f'(\mathbf{r}, \mathbf{r}', h_{22}) W' - \pi \left[\overline{F} - F^{C'} + G' + G' + G' + G' \right] = 0 \quad (A68)$$

$$m(\mathbf{r}, \mathbf{r}', h_{13^a}) W - \left[\frac{1}{\alpha} (B^c + \sigma R - H^c' + S) - M^{c'} \right] = 0 \quad (A69)$$

$$\pi n'(\mathbf{r}, \mathbf{r}', h_{23}a)W' - \pi \left[\frac{1}{\alpha'} \left\{ F^{C'} + \alpha'(\overline{R} - R) + H^{C'} + A^{C'} + H^{C'} + S' \right\} \right] = 0 \quad (A70)$$

These equations are the same as those on page 82 of the text except for the $h_{i,j}a$'s which are shift parameters which have the same interpretation as in Part I of the Appendix. If it is assumed that the $h_{i,j}$'s are held constant at whatever values are appropriate for the problem under consideration; that \overline{B} , \overline{F} , \overline{R} , α , and α ' are fixed; that $h_{i,j}$'s are held constant at zero; and that W and W' are fixed; that \overline{B} is an interpretation of \overline{B} is a same of \overline{B} in the following are fixed unless \overline{B} changes we can rewrite the system in the following are fixed unless \overline{B} changes we can rewrite the system in the following

$$(17A) 0 = (\underline{x})\hat{\mathbf{d}}$$

$$(\Delta \Lambda A) \qquad (\Delta \Lambda A) = 0,$$

$$(\varepsilon \nabla A) \qquad \qquad , 0 = (z, \overline{x})^{M}$$

$$(\lambda \Lambda A) \qquad \qquad 0 = (\Omega_{1} \Omega_{1} \Sigma_{2}) \tilde{M}$$

Although \underline{x} is defined as above, we repeat the definition here for

convenience,

: wro;

$$\underline{x} \equiv (x, x', R, B^{c}, \overline{x}^{c}, \pi, a). \tag{A75}$$

As we have argued on page 82 of the text only three of the four

market equilibrium conditions are independent, so we have,

 $\hat{A}_{xi} = \hat{A}_{xi} + \hat{A}_{xi} + \hat{A}_{xi} = 0$ (9ZA)

where x_1 is any element of the vector \underline{x} . As in Part I of the

Appendix, W and W' change when π changes so, for example,

 $A_{\Pi} = b'W' + bF^A - \frac{1}{\pi}fB^{A'}$ (77A)

on the excess demand for a given asset depends upon the value of the where \mathbf{F}^{A} and $\mathbf{B}^{\mathsf{A}'}$ are defined as above. The effect of a change in a

We now obtain the total differentials of (A71) through relevant h_i's.

The changes in B^{c} and $F^{c'}$ are defined as follows: (A74) making use of two definitions and imposing two restrictions.

 $qB_c \equiv -V qB + qB_c$

$$(A79) \qquad \text{(A79)}$$

(87A)

 $qE_{c} \equiv Y$, $qE + qF_{c}$.

the USCB to sterilize the impact of reserve inflows on U.S. high - $^{\wedge}_{\lambda}dR$, where $0 < ^{\wedge}_{\lambda} < 1$ represents the open market sales undertaken by

of reserve flows on the U.K. money stock, and dpc' represents open open market purchases undertaken by the UKCB to sterilize the impact sterilization activities. Similarly, λ 'dR, where $0 \le \lambda$ ' ≤ 1 , represents powered money while dB^c represents open market purchases unrelated to

market purchases unrelated to sterilization activities. λ and λ are

the coefficients of sterilization for high powered money.

As before changes in S and S', the balancing items on the central bank balance sheet, are restricted to be equal in size but opposite in sign to changes in the currency value of outside reserve assets in the relevant country due to a change in T,

$$OBA - = Zb$$

(18A)
$$(1 - \overline{A}) - 1 - 1 = 1$$

where the relationship among dm, do, and do' is given by,

$$d\pi = \frac{1}{\sigma} \left[d\sigma - \frac{\sigma}{\sigma^{\dagger}} d\sigma^{\dagger} \right]. \tag{A82}$$

Given the definitions and restrictions of the last para-

graph we can write the total differentials of (A71) through (A74) in matrix form as shown in Table III. The system of Table III is identical to the system of Table I except for the third column of the coefficient matrix and the two entries $\frac{1}{\alpha} d^{\Lambda}c$ and $\frac{1}{\alpha} d^{\Lambda}c$ in the vector of differentials. Another way of saying the same thing is that the partial derivatives of \hat{B} , \hat{h} , \hat{M} , and \hat{M} with respect to

r, r', π, and a are equal to the partial derivatives of B, F, M, and

N from Part I with respect to the same variables.

The term $[\frac{\lambda}{\lambda}-(1-\frac{\lambda}{\lambda})]$ represents the change in the supply

of U.S. securities available for the public to hold as a proportion of the increase in international reserves held by the USCB. The supply of securities available to the public rises by λ dR because of open market sales by the USCB undertaken in order to sterilize part of the effect of dR on high powered money. The supply of securities available to the public falls by $(1-\lambda)$ $\frac{1-\alpha}{\alpha}$ dR because the stock of

	Γ	r ^N	r K	r r	B _r	
		Nr,	",	Fr'	B _r '	
		$(1-\hat{\chi}^{\dagger})\frac{1}{\alpha}$	- $(1-\mathring{\chi})\frac{1}{\alpha}$	$\hat{\lambda}' - (1 - \hat{\lambda}') \frac{1 - \alpha'}{\alpha'}$	$- \left[\frac{\lambda}{\alpha} - (1 - \frac{\lambda}{\alpha}) \frac{1 - \alpha}{\alpha} \right]$	Table III
		0	Ļ	0	H	·
		Ļ	0	H	0	
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 $[\Lambda - (1 - \Lambda)]$ has an analogous interpretation. It should be supply of U.S. securities available to the public. The term U.S. commercial banking system may be either a rise or fall in the The net effect of the open market sales and the expansion of the tions on the supply of U.S. securities available to the public. banking system works to offset the effect of sterilization operasecurities by $(1-\lambda)$ $\frac{1-\alpha}{\alpha}$ dR. The expansion of the U.S. commercial commercial banking system is able to increase its holdings of high powered money expands by $(1-\lambda)dR$, and, as a result, the U.S.

 $Ab \left[\frac{1-\alpha}{\omega}(\lambda-1) - \lambda\right] - 1 = Ab\frac{1}{\omega}(\lambda-1)$

due to an increase in international reserves held by the USCB and is the increase in the U.S. money supply in the hands of the public

Now if we let, that $(1-\lambda')\frac{1}{\alpha}$, has an analogous interpretation.

 $y = \begin{bmatrix} \lambda & -1 & \lambda \\ \lambda & -1 & \lambda \end{bmatrix} = \lambda$

$$\lambda^{i} = \left[\lambda^{i} - (1 - \lambda^{i}) \frac{1 - \alpha^{i}}{\alpha^{i}} \right],$$

negative values. that the permissible values of A and A' have been expanded to include is completely identical to the coefficient matrix of Part I except where - $\infty < \lambda$, λ ' $\leq \lambda$ the coefficient matrix of the current model

associated with sterilization operations of $d\tilde{B}^{\text{C}}$ makes possible an In the current model an open market by the USCB not

expansion of the money supply by $\frac{1}{\alpha}dB^{Ac}$ and leads to a total reduction in the supply of securities available to the public by $\frac{1}{\alpha}dB^{C}$. $\frac{1}{\alpha}dF^{C}$ has an analogous interpretation. If we let,

$$q_{\mathbf{E}_{\mathbf{C}}} = \frac{\alpha}{1} q_{\mathbf{E}_{\mathbf{C}}}^{\mathbf{V}}$$

the vector of differentials for the current model is completely identical to the vector of differentials in the model of Part I.

(A71) through (A74) which are stated fully in Chapter VI and under the additional restrictions outlined at the beginning of Part IV of the Appendix conclusions based on the model of Part I are not affected by the presence of fractional reserve commercial banking except for the relatively minor consideration that negative

values of λ and λ must be considered.

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