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BugsXLA: Bayes for the Common Man

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Abstract

The absence of user-friendly software has long been a major obstacle to the routine application of Bayesian methods in business and industry. It will only be through widespread application of the Bayesian approach to real problems that issues, such as the use of prior distributions, can be practically resolved in the same way that the choice of significance levels has been in the classical approach; although most Bayesians would hope for a much more satisfactory resolution. It is only relatively recently that any general purpose Bayesian software has been available; by far the most widely used such package is **WinBUGS**. Although this software has been designed to enable an extremely wide variety of models to be coded relatively easily, it is unlikely that many will bother to learn the language and its nuances unless they are already highly motivated to try Bayesian methods. This paper describes a graphical user interface, programmed by the author, which facilitates the specification of a wide class of generalised linear mixed models for analysis using WinBUGS. The program, BugsXLA (v2.1), is an Excel Add-In that not only allows the user to specify a model as one would in a package such as SAS or S-PLUS, but also aids the specification of priors and control of the MCMC run itself. Inevitably, developing a program such as this forces one to think again about such issues as choice of default priors, parameterisation and assessing convergence. I have tried to adopt currently perceived good practices, but mainly share my approach so that others can apply it and, through constructive criticism, play a small part in the ultimate development of the first Bayesian software package truly useable by the average data analyst.

Keywords: Bayesian analysis, GLMM, Microsoft Excel, graphical user interface, WinBUGS.

1. Introduction

The use of Bayesian methods in academia appears to have increased at an exponential rate over the last ten to twenty years. There can be little doubt that this is due to the availability of Markov chain Monte Carlo (MCMC) algorithms to implement such methods that simply did not exist previously: see Gelfand and Smith (1990), Smith and Roberts (1993) or Tierney (1994) for details of this approach. The philosophical debate will never go away, but even amongst academics it is the practicality of being able to solve real problems that has greater influence. Although Bayesian methods are used more today in business and industry than they were twenty years ago, the increase is nowhere near as marked. I suggest that one of the barriers to greater use is the unavailability of Bayesian software with a good user interface. The **WinBUGS** package of Spiegelhalter, Thomas, Best, and Lunn (2003b) is the most widely used Bayesian data analysis program. It provides an easy to learn language that allows a wide variety of models to be specified. Its popularity is probably due to the user not needing to know very much about the MCMC methods that underpin it, and the fact that it is free! However, there is inevitably a learning curve barrier associated with any new software that requires sufficient motivation to overcome. If it were possible to specify a model in a similar manner to that in SAS, S-PLUS or Genstat, then I believe a much larger number of people used to working with such programs would try a Bayesian approach.

This paper describes a graphical user interface for **WinBUGS** that allows a wide class of generalised linear mixed models (GLMMs) to be specified in a manner familiar to users of more conventional statistical software. This interface, **BugsXLA** (v2.1), is a Microsoft Excel Add-In that is also freely available via the **BUGS** website: http://www.mrc-bsu.cam.ac. uk/bugs or direct from http://www.pipshome.freeserve.co.uk/stats; see Appendix B for instructions on how to download and install the software. Section 2 provides a brief overview of WinBUGS. Section 3 describes the types of model that can be fitted, and how the model statement is converted into **WinBUGS** code. Section 4 explains how priors are specified, including a graphical tool to help in the elicitation process. Section 5 briefly discusses the options available for controlling the MCMC run itself. An example is provided in Section 6 to illustrate how the user interacts with the interface. The remaining functionality not illustrated by the example is given in Section 7. A few concluding remarks are made in Section 8. Since segments of WinBUGS code are shown throughout the paper, Appendix A gives a very brief explanation of the key elements of the language. However, readers not familiar with **WinBUGS** may simply wish to skip those parts that discuss the generated code, as it is not necessary to understand this in order to use BugsXLA.

2. Brief overview of WinBUGS

WinBUGS was developed by Spiegelhalter *et al.* (2003b) and is an interactive Windows program for Bayesian analysis of complex statistical models using Markov chain Monte Carlo (MCMC) techniques. In the Bayesian approach all quantities in the model are treated as random variables, and inferences are made by conditioning on the data to obtain a posterior distribution for the parameters in the model; see Lee (2004) for an introduction to Bayesian statistics. The MCMC approach is used to marginalise over the posterior distribution in order to obtain inferences on the main quantities of interest.

WinBUGS contains a programming language that allows an arbitrarily complex statistical model to be defined. This code is then compiled into a form suitable for efficient computation, and a sampler operates on this structure to generate appropriate values of the unknown quantities in order to feed the MCMC algorithms. Instead of calculating exact or approximate estimates of the necessary numerical integrals, MCMC generates a stream of simulated values for each quantity of interest. **WinBUGS** also has tools to monitor the stream for convergence, and summarise the accumulated samples.

3. Specifying the model using BugsXLA

All the major statistical packages used to facilitate classical methods of data analysis allow the user to specify the model to be fitted by means of a relatively concise model statement. It is likely that in order to persuade many users of packages such as SAS, S-PLUS and Genstat to try a Bayesian analysis of their problems, amongst other things, they will need software that allows models to be specified in a familiar way. **BugsXLA** uses a very similar set of design statement symbols as that used in Genstat:

- + : addition of a term
- . : interaction between two terms, or a nested term
- *: crossing of two terms, i.e., both main effects and the interaction
- / : nesting of second term inside the first
- () : grouping; used to determine the order of evaluation for complex models
- : subtraction of a term
- @: only expand terms to order specified, e.g., A*B*C@2 = A*B*C A.B.C
- [^]: power term (covariates only), e.g., temp² is the quadratic term for temp

These enable quite complex models to be specified very concisely. For example, (A + B)*C is shorthand for a model with the terms A + B + C + A.C + B.C, while (A + B)/C is a model with main effects of both A and B, plus a factor C nested within the combination of these factors. This would be expanded to A + B + A.B.C. Note that although A.B.C is written exactly the same here, when defining a nested term, as it would be written when defining a three way interaction term, it may need to be interpreted differently when constructing the appropriate code to fit the model.

As well as being able to include both independent ("fixed" in classical terminology) and exchangeable ("random") effect terms in the model, it is possible to specify covariates. When specifying the covariate part of the model, the . symbol is used to denote the product of two covariates. Polynomials can be easily specified by using the @ and $^$ operators, e.g., $(X1*X2*X3*X4)@2 + (X1+X2+X3+X4)^2$ would fit all terms up to the second order.

Clearly there is nothing new in developing software that is able to interpret the algebra of a design statement (see Heiberger 1989, for a thorough explanation of how this can be done). What is novel is to derive code that fits the specified model using a Bayesian analysis. This has been achieved by generating the appropriate code that can be run by the **WinBUGS** Version 1.4 software package. By utilising the script facility added to this version of the software, it is then possible to call the program from within Excel, using VBA code, and retrieve the results after the analysis is complete. All this is possible without the end user having to know how to use the **WinBUGS** package at all. There are some dangers in this approach, which I will briefly discuss in the concluding remarks.

The majority of generalised linear models used in practice are Normal/identity, Poisson/log or Binomial/logit. These can all be routinely fitted using **BugsXLA**, the generated **WinBUGS** code being of the form:

mu[i] <- Beta0 + ... Y[i] ~ dnorm(mu[i], tau) or

```
log(mu[i]) <- Beta0 + ...
Y[i] ~ dpois(mu[i])
or
```

```
logit(mu[i]) <- Beta0 + ...
Y[i] ~ dbin(mu[i], N[i])</pre>
```

where log() and logit() are functions, and dnorm(), dpois() and dbin() are distributions intrinsic to WinBUGS corresponding to Normal, Poisson and Binomial distributions respectively. Note that the BugsXLA user does not need to know how to code in, or run, WinBUGS at all. BugsXLA creates this code automatically after interpreting a much simpler model statement as explained above.

By only using link functions that allow the parameters to vary over the whole real line, it is possible to generalise the code for defining the priors and likelihood contributions of the parameters.

Software written to use classical methods of statistical analysis converts the list of model terms to be fitted into an appropriate design matrix. This matrix provides the substrate on which the numerical algorithms developed to give the parameter estimates are applied. Categorical factors are converted into dummy variables with constraints to ensure estimable functions are defined. For example, by default SAS constrains the last level of each main effect to be zero, while Genstat's default is to constrain the first level. A different approach has been taken when generating the data files and code for WinBUGS. Each categorical factor term, be it main effect or interaction, is stored as a single vector consisting of integers indexing the level set for each observation. This allows the linear predictor to be specified in WinBUGS code using the generic statements:

```
for (j in 1: N.obs) {
  for (i in 1: N.X) {
     X.row[i, j] <- X.Eff[i, X[j, i]]
  }
  for (i in 1: N.Z) {
     Z.row[i, j] <- Z.Eff[i, Z[j, i]]
  }
  mu[j] <- Beta0 + sum(X.row[, j]) + sum(Z.row[, j])
}</pre>
```

where N.obs is the number of observations, N.X and N.Z are the number of independent and exchangeable effects terms respectively, X[,] and Z[,] are matrices made up of the independent and exchangeable level indexing vectors respectively, X.Eff[,] and Z.eff[,] are the parameters defining the independent and exchangeable effects respectively, BetaO is the constant parameter, and mu[] is the linear predictor in the generalised linear mixed model. The intrinsic WinBUGS function sum() sums over the missing index of its vector argument. One of the main tasks underpinning BugsXLA is to convert a model statement of the form (A + B)*C into the appropriate X[,] ("fixed effects"), or Z[,] ("random effects"), design matrix. Note that each row of these matrices represents a different observation, and each column represents a different term in the model, with the entries representing the associated factor level set. X.Eff[,], Z.Eff[,] and BetaO are what WinBUGS coders refer to as "stochastic nodes", representing the statistical parameters of the model, and will need to have priors specified (see Section 4).

It is equally as simple to write generic code for including covariates. The only additional issue to consider is the need to centre and scale the covariates, which greatly improves the performance of the MCMC algorithm as discussed in Gilks and Roberts (1995). The code required to achieve this in **WinBUGS** is:

```
for (i in 1: N.V) {
    mean.V[i] <- mean(V[ , i]) ; sd.V[i] <- sd(V[ , i])
    Cov.Coeff[i] <- V.Beta[i] / sd.V[i]
    for (j in 1: N.obs) {
        std.V[j, i] <- (V[j, i] - mean.V[i]) / sd.V[i]
    }
    mean.Beta[i] <- Cov.Coeff[i]*mean.V[i]
}
alpha <- Beta0 - sum(mean.Beta[])
for (j in 1: N.obs) {
    V.row[j] <- inprod(std.V[j, ], V.Beta[] )
    mu[j] <- Beta0 + V.row[j]
}</pre>
```

where N.V is the number of covariates, V[,] is a matrix made up of the covariates, std.V[,] is a matrix of centred and scaled covariates, Cov.Coeff[] and V.Beta[] are the vectors of regression parameters for the original and scaled covariates respectively, and alpha and BetaO are the intercept parameters for the original and scaled covariates respectively. The terms mean(), sd() and inprod() are intrinsic WinBUGS functions with obvious results. Note that the semicolon separator ; allows more than one statement on the same line.

It should be clear that it is straightforward to combine the different code segments such that linear models of arbitrary complexity can be defined using **BugsXLA**. Of course, it does not follow that any model that can be defined will always lead to a successful **WinBUGS** analysis. Also, since the files created by **BugsXLA** are all in text form, users knowledgeable in the **WinBUGS** language can edit these generated code and data files and rerun the script to obtain extensions of the standard models offered by **BugsXLA**.

4. Specifying and eliciting priors

The most conspicuous difference between any software that facilitates a Bayesian, as opposed to a classical, statistical analysis is the need to include prior distributions in the model specification. Currently **BugsXLA** has only a limited choice of priors from which to choose. These

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Constant term	$Normal(\mu_Y, 10000\sigma_Y^2)$
Independent effect contrasts	$Normal(0, 10000\sigma_Y^2)$
Exchangeable effect st.dev.	$Half-Normal(9\sigma_Y^2)$
Covariate regression coefficient	$Normal\left(0, 10000 rac{\sigma_Y^2}{\sigma_X^2} ight)$
Normal residual variance	Inv-Gamma(0.001, 0.001)

Table 1: Default priors.

consist of a Normal distribution for the independent effects and covariate regression coefficients. More choice is provided for the exchangeable effects: the default is a Half-Normal for their standard deviation (as suggested by Spiegelhalter, Abrams, and Myles 2003a), but this can be changed to the Uniform, Half-Cauchy (as suggested by Gelman 2004), or Root-Inverse-Gamma. A Half-Normal distribution is also offered as a prior for any covariate regression coefficient whose sign is known with certainty. For Normal linear models the prior for the lowest level variance parameter is an inverse-gamma distribution.

Initially default priors are set that should, under most circumstances, allow the likelihood to dominate when forming the posterior distribution. These defaults are given in Table 1 where μ_Y is the sample mean of the response and σ_Y^2 and σ_X^2 are the sample variances of the response and covariate respectively. When a link function other than the identity is used, the response is appropriately transformed before calculating the mean and variance.

Currently, one of the most controversial topics amongst Bayesians fitting these types of models is the choice of prior for the exchangeable effects, or more specifically for the standard deviation of the Normal distribution used as the prior. The problem mainly arises when there is little information in the likelihood with which to estimate this term. The default chosen here – a Half-Normal with scale parameter equal to $3\sigma_Y^2$ – is an attempt to keep this prior weak, while not giving much support to extremely large values.

Although the parameters defining these priors are calculated from the data, their variances are a sufficiently large multiple of the range of the response that there is little danger that the likelihood is being used twice. The priors are specified this way simply to ensure that, irrespective of the location and spread of the response, the default prior is essentially flat over the range of the likelihood.

In principle it is not necessary to impose any constraints on the independent factor effects; although they will not converge, any estimable function of them will and could therefore be successfully monitored during the MCMC run. In practice leaving these effects free often severely hampers the performance of the MCMC algorithm. Hence, **BugsXLA** imposes corner constraints on these effects similar to those adopted by SAS or Genstat. Instead of literally fixing some of the effects to zero, in order to make it easier to write a generic code segment, these constrained effects are given a prior distribution centred on zero with an extremely small variance. The priors for independent and exchangeable factor effects (Half-Normal prior) is coded:

```
for (i in 1: N.X) {
  for (j in 1: levs.X[i]) {
    tau.X[i, j] <- 1/Var.X[j, i]</pre>
```

```
X.Eff[i, j] ~ dnorm(0, tau.X[i, j])
}
for (i in 1: N.Z) {
  for (j in 1: levs.Z[i]) {
    Z.Eff[i, j] ~ dnorm(0, tau.Z[i])
    }
    tau.Z[i] <- 1/sigma2.Z[i] ; sigma2.Z[i] <- pow(sigma.Z[i], 2)
    sigma.Z[i] <- abs(hyper.Z[i])
    hyper.Z[i] ~ dnorm(0, tau.hyperZ[i]) ; tau.hyperZ[i] <- 1/Var.Z[i]
}</pre>
```

where levs.X[] and levs.Z[] are the number of levels for each independent and exchangeable effects term respectively, and Var.X[,] and Var.Z[] are the variances and Half-Normal parameters of the priors for independent effects and exchangeable effects standard deviations respectively. The prior for the covariate coefficients is coded in a very similar way to that for the independent factor effects.

Currently, the priors for the independent factor effects and covariate coefficients are obtained by the user entering values for the parameters that define them. Although this can also be done for the exchangeable factor effects, a graphical feedback interface (GFI) is also provided to facilitate this process. The GFI is shown in Figure 1. This figure shows the elicitation option for an exchangeable factor's prior in a Normal linear model. It is possible to consider the effects' standard deviation τ directly or, as shown, think in terms of the difference between the effects of two randomly chosen levels of the factor. The user is asked to enter the maximum credible size of this difference, this being interpreted as the approximate 95th percentile of its prior distribution. Simulation work, not discussed here, has shown that if

$$\tau \sim Half-Normal(\sigma^2)$$

 $\delta \sim Half-Normal(2\tau^2)$

then

```
\sigma \approx \delta_{.95}/3
```

where $\delta_{.95}$ is the 95th percentile of the distribution of δ .

In **BugsXLA** the elicited maximum credible difference defined above is interpreted as 3σ .

The GFI is designed such that the graph of the prior distribution, as well as some of its percentiles, is updated in real time as the user changes the credible difference using the spinner control. It is possible to plot the exponential of the X-axis, this being useful when log or logit link is used. When this transformation is applied the axis can then be interpreted as the ratio (log) or odds-ratio (logit) of two randomly chosen effects.



Figure 1: Prior elicitation process via the graphical feedback interface.

5. Controlling the MCMC run

Probably the most difficult aspect to automate is the settings used to control the MCMC run. **BugsXLA** allows direct control of the parameters in Table 2 (the default settings are in parentheses).

It is not suggested that the default settings for these are adequate even for the majority of GLMM's that are likely to be fit in practice. Their use is primarily for the case when it is unsure if **WinBUGS** will run the model at all, providing a quick and dirty run. They may also be adequate for models with no exchangeable effects terms ("fixed" effects models). For this reason the program offers three alternative pre-defined settings with some advice on when to use them.

Burn In	Number of initial MCMC samples to be discarded.
(1000)	Convergence assumed past this point.
Samples	Number of MCMC samples to be generated from Posterior Distribution.
(1000)	
Thin	If set to K then only every Kth sample is saved. Use when high
(1)	autocorrelation is present to reduce the number of samples required to give
	good coverage of the posterior distribution.
Chains	Number of separate chains to be generated.
(1)	
Auto Quit	Determines whether WinBUGS is automatically closed after the MCMC run.
(Yes)	

Table 2: Default MCMC control settings.

Simple model

(Burn In: 5,000 Samples: 10,000 Thin: 1 Chains: 1 Auto Quit: Yes)

Orthogonal design, may include one exchangeable effects term with variance estimate having 3 or more effective degrees of freedom

Regular model

(Burn In: 25,000 Samples: 10,000 Thin: 10 Chains: 1 Auto Quit: Yes)

Nearly orthogonal design, may include covariate(s), but with each variance estimate having 3 or more effective degrees of freedom. Although not part of the default settings, I would recommend that 'Auto Quit' be turned off and at least 2 chains run so that MCMC convergence can be checked before using the results.

Complex model

(Burn In: 100,000 Samples: 20,000 Thin: 50 Chains: 1 Auto Quit: No)

Messy design, may include covariate(s), or some variance estimates having less than 3 effective degrees of freedom. Note that 'Auto Quit' is turned off as it is strongly recommended that MCMC convergence be checked before using the results. Although not part of the default settings, I would recommend that at least 2 chains be run. Mixing can often be greatly improved if informative priors are provided for poorly estimated variance components. These need not be strong priors, just sufficiently precise to effectively rule out incredibly large values.

Initial values are automatically generated using the following procedure:

- The lowest level precision parameter (Normal models) is initialised to 10 times the precision of the response. This equates to an expected R^2 of about 90%.
- Any independent factor effects are initialised to 0.3 times the minimum of the standard deviation of the response and the prior standard deviation of the effect itself. The reason for the 0.3 multiplier will be explained when multiple chains are discussed later.
- The standard deviation for exchangeable factor effects is initialised to 0.3 times the minimum of the standard deviation of the response and the prior Half-Normal sigma parameter for this term.
- The covariate regression coefficient is initialised to 0.3 times the minimum of the ratio of standard deviations of the response and covariate, and the prior standard deviation of this coefficient itself.

For both the independent factor effects and the covariate regression coefficients, the signs of the initial values are alternated between successive terms fitted in the model. A maximum of 5 chains can be run using **BugsXLA** with the following multipliers for the default values defined above used to obtain a range of initial values: 1, 0.1, 10, 0.3, and 3. These multipliers were chosen so that initial values differing by one or two orders of magnitude would be obtained, without getting values too far into the tails of the prior distribution.

Currently, I have only limited experience on which to comment on the adequacy of this advice. I certainly would not unreservedly recommend this advice, and include it in the program mainly as a placeholder for better guidance as experience with the program develops. I do believe that providing such guidance is an essential feature of any software that is aimed at the average data analyst. If nothing else, I would hope that this attempt would raise discussion on the general guidance that can be given.

6. Worked example

To illustrate how the user interacts with **BugsXLA**, the 'Seeds' example, originally from Table 3 of Crowder (1978) but also used by Spiegelhalter, Thomas, Best, and Gilks (1996b), is reanalysed. Figure 2 shows the completed model specification form, in this case defining a binomial error model with logistic link. The variables R and N contain the number germinated and total number of seeds, respectively, in a study undertaken to assess the effects of seed and root extract types. As well as fitting independent ("fixed") main and interaction effects for the "treatment structure", over-dispersion is accommodated by including an exchangeable ("random") effects term for the 21 plates used in the experiment.

By clicking on the button labelled 'MCMC & Output Options' another form is shown that allows the user to alter the default settings as given in Figure 3.

Importing 'Stats' or 'Samples' will result in the **WinBUGS** summary statistics or generated samples from the posterior distribution being imported into Excel respectively. Selecting 'Predicted Averages' gives the predicted mean response for every possible combination of the factors specified to have independent effects, averaged over the levels of any exchangeable effects, and with any covariates set to their mean value. The scaled residuals are the raw residuals divided by:

Normal error: σ Poisson error: $\sqrt{\mu}$ Binomial error: $\sqrt{N\mu(1-\mu)}$

After setting these options and confirming that the model is specified correctly, the prior distributions for each of the terms can be altered. Figure 4 shows the default settings for the exchangeable effects of the plate term.

The button labelled 'GFI' would bring up the graphical feedback interface as illustrated in Figure 1. In the 'Seeds' example, since a logit link has been specified, the user would be prompted to think about his or her prior beliefs in terms of the odds-ratio of the effects of two randomly chosen plates.

Once the user is satisfied with the priors, by clicking 'OK' the program generates all the files needed by **WinBUGS** to complete the analysis: data files (including the constants needed to define the model), initial value files, the code itself as well as the script file that controls the **WinBUGS** analysis. Provided that a successful exit from **WinBUGS** is achieved, the user is then prompted to import the results, which in the case of the summary statistics will be formatted as in Figure 5.

The column with the header 'WinBUGS Name' shows the generic node names used in **Win-BUGS** and is of little use unless an experienced user wished to edit the code directly later. Informative names for the parameters are given in the column with the header 'Label'. Inspection of the summary statistics shows that the first level of each independent main effects

	A	В	С	D	Е	F G H I J K L M N			
1	R	N	Seed	Root	Plate	Hierarchical Ceneralized Linear Model (Ravesian Analysis)			
2	10	39	O. aeg 75	Bean	1				
3	23	62	O. aeg 75	Bean	2	- Data (single column variables, all same length)			
4	23	81	O. aeg 75	Bean	3	Data (single column variables, all same length)			
5	26	51	O. aeg 75	Bean	4	Data Rappe testivitetaa			
6	17	39	O. aeg 75	Bean	5				
7	5	6	O. aeg 75	Cucumber	6	Data is —			
8	53	74	O. aeg 75	Cucumber	7				
9	55	72	O. aeg 75	Cucumber	8	Set valiable types			
10	32	51	O. aeg 75	Cucumber	9	Unin rows ☐ Blank cells = MVs (Response only)			
11	46	79	O. aeg 75	Cucumber	10				
12	10	13	O. aeg 75	Cucumber	11	Model			
13	8	16	O. aeg 73	Bean	12	Fliciting Drives Only			
14	10	30	O. aeg 73	Bean	13	Distribution Binomial			
15	8	28	O. aeg 73	Bean	14				
16	23	45	O. aeg 73	Bean	15	usu Looit 🔻			
17	0	4	O. aeg 73	Bean	16				
18	3	12	O. aeg 73	Cucumber	17				
19	22	41	O. aeg 73	Cucumber	18	Decreases			
20	15	30	O. aeg 73	Cucumber	19	Response R/N			
21	32	51	O. aeg 73	Cucumber	20				
22	3	7	O. aeg 73	Cucumber	21	Censored			
23									
24						- Factors			
25						Fixed Root*Seed			
26									
27						Pandom			
28						Plate			
29									
30						Covariates			
31						Independent			
32									
33						Bardan -			
34						Random Careffe			
35						Coerrs			
36									
37						MCMC 8			
38						Help!? Output Options Clear Form Exit OK			
39									

Figure 2: Data in an Excel sheet, with the completed model specification form.

WinBUGS MCMC & HGLM Output Options						
MCMC Options	─ Import Stats for ── ✓ Fixed Terms	Import Samples for Fixed Terms				
Samples 10000 • Thin 1 • Over Relax • Chains 1 •	 Covariate Coeffs Intercept Exch. Coeffs Variance Compts 	Covariate Coeffs Intercept Exch. Coeffs Variance Compts Var O SD Random Terms Deviance Predicted Averages				
Auto Quit Yes	C Var SD Random Terms Deviance DIC Predicted Averages					
C Regular Model C Complex Model	C Scaled Residuals	C Scaled Residuals				
Help!?	Restore Defaults Exit (n	o save) Save Changes				

Figure 3: MCMC and output options form showing default settings.

Ind, Covariates	E	ixch. Covariates
Ind. Factors	Errors	Exch. Factors
- Prior for Random	Factors -	
Exchang Effe tau	jeable effects ct ~ N(0, ta u ~ Dist'n(Pai	; of levels u^2) rm)
Term	Dist'ı	n Parm
Plate	Half-	N 5
Alter Prior Distribu	tion	 •
Alter Prior Distribu	tion ———	Half-N 💌
Alter Prior Distribu Plate Elicit prior beliefs C directly	tion s for tau Via level eff	Half-N 💌
Alter Prior Distribu Plate Elicit prior beliefs C directly Specify maxim difference betw of lev	tion 5 for tau 0 via level eff um credible veen effects els	Half-N V
Alter Prior Distribut Plate Elicit prior belief: C directly Specify maxim difference betw of lev Load Default	tion for tau via level eff um credible veen effects els GFI	Half-N V fects

Figure 4: Form used to specify prior distributions.

	Label	Mean	St.Dev.	2.5%	Median	97.5%	WinBUGS Name		
	CONSTANT	-0.5520	0.2217	-1.0120	-0.5520	-0.1035	Beta0		
Root	Bean	0.0000	0.0000	0.0000	0.0000	0.0000	X.Eff[1,1]		
Root	Cucumber	1.3590	0.3104	0.7541	1.3500	2.0250	X.Eff[1,2]		
Seed	O. aeg 75	0.0000	0.0000	0.0000	0.0000	0.0000	X.Eff[2,1]		
Seed	O. aeg 73	0.0670	0.3478	-0.6635	0.0748	0.7320	X.Eff[2,2]		
Root x Seed	Bean, O. aeg 75	0.0000	0.0000	0.0000	0.0000	0.0000	X.Eff[3,1]		
Root x Seed	Cucumber, O. aeg 75	0.0000	0.0000	0.0000	0.0000	0.0000	X.Eff[3,2]		
Root x Seed	Bean, O. aeg 73	0.0000	0.0000	0.0000	0.0000	0.0000	X.Eff[3,3]		
Root x Seed	Cucumber, O. aeg 73	-0.8379	0.4787	-1.8200	-0.8230	0.0934	X.Eff[3,4]		
	SD(Plate)	0.3535	0.1520	0.0928	0.3383	0.6793	sigma.Z[1]		
Model	[\$A\$1:\$E\$22]								
Distribution	Binomial								
Link	Logit								
Response	R/N								
Fixed	Root*Seed								
Random	Plate								
Priors									
CONSTANT	N() mu:0 sigma:100								
Root	N() mu:0 sigma:100								
Seed	N() mu:0 sigma:100								
Root x Seed	N() mu:0 sigma:100								
Plate	N(0,tau^2); tau ~ Half-N() sigma:{	5						
WinBUGS M	ICMC Settings								
Burn-In: 5000	Samples: 10000 (Thin:	1; Chain	s:1)						
Run took 23	seconds								
BugsXLA (2.1									
BugsXLA is p	provided without any warr	anty of a	ny kind, e	either exp	pressed o	r implied.			
The user is responsible for any consequences arising from use of this program.									
See also the disclaimer provided with the WinBUGS package.									

Figure 5: Summary statistics as imported into Excel.

term has been constrained to zero, with appropriate constraints on the interaction effects also. The output also provides a summary of the model fitted, plus the prior distributions specified. It also records the settings for the MCMC run with the time taken to run. Due to the inherent uncertainties currently associated with using MCMC sampling methods to tackle generic problems, a final warning message is displayed to ensure the user remains cautious when interpreting the results.

One of the distinct advantages of using **WinBUGS** is that it is possible to characterise the whole posterior distribution by viewing and summarising the generated samples for any of the parameters, or arbitrarily complex functions of them. This is particularly useful for distributions that are distinctly non-Normal, such as the variance component for the plate effect in this example. The imported samples can be subsequently pasted into your favourite statistics package, and a histogram, or other summaries, created. Alternatively the 'Post v Prior' icon on the **BugsXLA** toolbar can be selected, which runs a utility program that can do this within Excel. Figure 6 shows the form that appears when this option is chosen.

After identifying the column of data to be graphed and clicking on 'Update Parameter Information' the name and prior specified for this parameter are shown. Clicking on update graph will produce a plot of the posterior distribution (histogram) and prior overlaid. Figure 7 shows such a plot after adjusting the bins for the histogram using the options on the form.

7. Other functionality in BugsXLA

- Additional distributions and links: Weibull, t and log-Normal; probit and complementary log-log links for binomial data.
- Multinomial and ordered categorical data; the data can be either grouped into counts or recorded as individual responses.
- Censored data: lower bound, upper bound, interval or any mixture of these. The button labelled 'Set Variable Types' in Figure 2 launches a form that facilitates the classification of variables as one of Factor, Variate or Censor.
- Factor by covariate interactions: easy fitting of group regression coefficients.
- Covariates with exchangeable coefficients, i.e., 'random coefficients'.
- Allow over-relaxed samples to be generated as discussed in Neal (1998).
- Calculation and importing of the DIC statistic as defined in Spiegelhalter, Best, Carlin, and van der Linde (2002).
- Able to create a 'Bugfolio' using the 'Create Bugfolio' feature shown in Figure 3. By creating a Bugfolio all the files created by **BugsXLA** are stored in the folder specified. This is useful for experienced **WinBUGS** programmers who wish to use **BugsXLA** to generate some basic code and then modify the code, script or data files to run a more complex model not possible using **BugsXLA** directly.
- Help is provided on-line by clicking on the 'Help?!' box found at the bottom left of most of the forms (see Figure 2 for example). Features that have help text provided are highlighted, and the help is obtained by moving the mouse over the highlighted area.



Figure 6: Form shown after the 'Post v Prior' icon is selected from **BugsXLA** toolbar. The specified prior is shown, in this case a Half-Normal, constrained to be positive, with a scale parameter of 5.



Figure 7: Histogram of 10,000 samples generated during the MCMC run. This graph should closely approximate the posterior distribution for the between plates standard deviation parameter. The specified prior distribution has been overlaid (solid black line) suggesting that the likelihood has dominated in the estimation of this parameter.

8. Concluding remarks

The purpose of **BugsXLA** is to provide a tool that makes it easier for the average data analyst to try Bayesian methods. By allowing models to be specified in a manner that is familiar to users of such packages as SAS, S-PLUS and Genstat, it removes one of the major barriers to those people who are curious but uncommitted to the Bayesian approach. An initial attempt has been made to provide guidance on appropriate settings for the MCMC run when GLMMs are being fitted. It is also shown how a prior elicitation interface could be integrated into a Bayesian analysis program.

By removing the need to know how to code the models, import the data and export the results, it allows the user to focus on the more important issues:

- Is the model appropriate?
- What priors can I justify?
- What inferences am I trying to make?

As well as providing a tool for tackling real problems, this could also provide a useful aid for those teaching Bayesian methods.

As Spiegelhalter *et al.* (2003b) state in the **BUGS** manuals, "MCMC sampling can be dangerous!". It could be argued that **BugsXLA** increases the risks due to the possibility of the **WinBUGS** output being accepted without checking for convergence or satisfactory mixing. These risks can be mitigated by education in how to use such software, as well as the software providing appropriate guidance both during the specification of the model and MCMC run, as well as during the analysis stage. **BugsXLA** offers some such guidance, but future packages aimed at a broad audience need to offer much more. Ultimately, the most effective way to grow the knowledge needed to feed this advice is to engage a much broader group of people who regularly use GLMMs in business and industry. My hope is that **BugsXLA** can help to encourage even more people to try Bayesian methods and, through its constructive criticism, play a small part in the ultimate development of the first Bayesian software package truly useable by the average data analyst.

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A. Key elements of the WinBUGS language

I explain only enough here to enable anyone familiar with statistical modelling to follow the code segments in the main paper. Most of this is directly copied from the **BUGS** 0.5 Manual written by Spiegelhalter, Thomas, Best, and Gilks (1996a).

The code provides a declarative description of the probability model, which is compiled before running. There are two types of relations:

~ which means "is distributed as"

<- which means "is to be replaced by"

These relations are used to define stochastic and deterministic nodes respectively. For example,

alpha dnorm(mu, tau)

defines a Normally distributed variable, alpha, with mean mu and precision (1/variance) tau. While,

mu <- beta*time

defines mu to be equal to the product of the two nodes beta and time; these latter nodes could themselves either be variables or predefined constants.

Vectors and arrays are represented using square brackets, e.g., x[i, j]. The indexing convention broadly follows those of S-PLUS, so that, for example, x[, 3] indicates all the values of the third column of the two dimensional array x.

Repetitive structures can be succinctly described using for loops. Note that these constitute a declarative description of the model and should not be interpreted in a procedural way. The syntax follows that of S-PLUS;

For (name in expression1:expression2) { ... }

B. Downloading and installing BugsXLA

BugsXLA (v2.1) is a Microsoft Excel Add-In that is freely available via the **BUGS** website: http://www.mrc-bsu.cam.ac.uk/bugs or direct from http://www.pipshome.freeserve. co.uk/stats. After clicking on "Download BugsXLA (v2.1)" and saving the self-extracting zip file to a convenient location on your PC, follow these instructions to install **BugsXLA** as an Excel add-in. It is necessary to have Windows 98 or higher (tested on 98, 2000 and 2002), MS Excel (tested on 2000 and 2002; will not work on 97), MS Notepad and **WinBUGS** v1.4 already loaded on your PC.

It is important that Excel be closed before starting.

1. Run the self-extracting zip file; by default this puts the files in

C:\Program Files\WinBugsXLA

- 2. Open MS Excel
- 3. Select Tools: Add-Ins and Browse in the directory to which the zipped files have been extracted (see step 1), ensuring that Files of Type: All Files has been selected.
- 4. Select the file BugsXLA.sta and make sure that 'BugsXLA' has been checked in the Add-Ins dialog box before clicking 'OK'.
- 5. If you are warned that either **WinBUGS** or Notepad is not in 'specified location', click 'Yes' and alter the directory entries so that these programs can be found.
- 6. A toolbar titled 'BugsXLA' should appear that could be moved to your favoured location on the Excel frame.

You can find an Excel Workbook with a few example data-sets in the 'unzipped to' directory specified in step 1:

BugsXLA Egs.xls $\,$

Help is available on some of the **BugsXLA** forms. Click on the 'Help?!' checkbox and hover the mouse over any areas that are highlighted.

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