

TEMPORAL AGGREGATION EFFECTS ON THE CONSTRUCTION OF PORTFOLIOS OF STOCKS OR MUTUAL FUNDS THROUGH OPTIMIZATION TECHNIQUES SOME EMPIRICAL AND MONTE CARLO RESULTS

George Xanthos & Dikaios Tserkezos

Greek Econometric Institute

Department of Economics

University of Crete

Gallos, GR-74100

Rethymno

GREECE

Abstract

In this paper we test the effects of temporal aggregation (disaggregation) on the efficiency of portfolio construction using the mean variance optimization approach. Using Monte Carlo techniques and empirical data from the Athens Stocks Exchange we confirm that the use of temporally aggregated data affects very seriously the efficiency of the constructed portfolio. Especially as the degree of temporal aggregation increases the application of optimization techniques could lead to different results regarding the percentage of stocks participation, the weights and finally the total portfolio performance.

Keywords: Portfolio Optimization, Stocks; Temporal Aggregation; Stochastic Simulation, The Banking Sector of the Athens Stocks Exchange;

JEL classification: C32, C43, C51, G14.

1. Introduction

Temporal aggregation poses many interesting questions which have been explored in time series analysis and which yet remain to be explored. An early example of research in this area is Quenouille (1957), where the temporal aggregation of $ARMA(p, d, q)$ processes is studied. Amemiya and Wu (1972), and Brewer (1973) review and generalize Quenouille's result by including exogenous variables. Zellner and Montmarquette (1971) discuss the effects of temporal aggregation on estimation and testing. Engle (1969) and Wei (1990) analyze the effects of temporal aggregation

on parameter estimation in a distributed lag model. Other contributions in this area include Tiao (1972), Stram and Wei (1986), Weiss (1984), Rossana R.J. and Seater, J.J.,(1995), Granger and Silkos (1995), Marcellino (1999), and finally Tommaso Di Fonzo(2003) to name but a few.

In this paper we investigate the effects of temporal aggregation on the application of the mean variance approach in portfolio management¹. More specifically we investigate the effects of temporal aggregation of the returns of the stocks of the portfolio. on the portfolio's performance, as this performance can be approximated from: (a) the percentage of the number o stock is participate in the portfolio, (b) the structure of the portfolio and finally (c) the future portfolio performance.

Using empirical data from the Athens Stocks Exchange and stochastic simulation techniques we end up with the general conclusion that the efficient portfolio management is closely related with the level of temporal aggregation (disaggregation) of the returns of the portfolio's stocks. In other words , the use of the returns of the stocks we want to participate to the portfolio, in daily, weekly, monthly etc basis, could lead us to different results about the number of the stocks to participate to the portfolio, the structure of the portfolio and finally the portfolio's future performance for different time horizons. This article is organized as follows. In section 2 we present very briefly the mean variance portfolio management and in section 3 we present the temporal aggregation effects on a portfolio management of stocks of the Banking sector of the Athens Stocks Exchange Market. Section 4 introduces the design of the simulation procedure and section 5 provides the simulation results. The last section concludes.

2.Mean Variance Frontier

Suppose there are $N > 1$ stocks and that $\mu \in R^N$ is a vector with the expected returns:

¹ Elton Edwin & Gruber Martin., (1977), Grinblatt M., Titman S., (1989) and Doumpou, M. and Zopounidis, C., (2002).

$$\mu = \begin{bmatrix} \mu_1 \\ \mu_2 \\ \vdots \\ \vdots \\ \vdots \\ \mu_N \end{bmatrix} \quad (1)$$

Where μ_j $j = 1, 2, \dots, N$ refers to the j expected returns. Suppose Σ is a $N \times N$ variance – covariance matrix with the variance-covariance matrix of the expected returns of the $j = 1, 2, \dots, N$ stocks.

$$\Sigma = \begin{bmatrix} \sigma_1^2 & \sigma_{12} & \dots & \sigma_{1N} \\ \sigma_{21} & \sigma_2^2 & \dots & \sigma_{2N} \\ \vdots & & & \\ \vdots & & & \\ \vdots & & & \\ \sigma_{N1} & \sigma_{N2} & \dots & \sigma_N^2 \end{bmatrix} = [\sigma_{ij}] \quad (2)$$

Where σ_{ij} corresponds to the covariance of the i and j stock (Mutual Fund). If the portfolio is a vector $w \in R^N$ with the constraint:

$$\sum_{j=1}^N w_j = 1 \quad (3)$$

Merton (1972) proved that a portfolio with weights w belongs to the mean variance frontier when: $w = g + hE$ for a level of expected returns E , when g and h are vectors of n dimensions and estimated as follows:

$$g = \frac{1}{D} [B(\Sigma^{-1} \iota) - A(\Sigma^{-1} \mu)] \quad (4)$$

$$h = \frac{1}{D} [C(\Sigma^{-1} \mu) - A(\Sigma^{-1} \iota)] \quad (5)$$

Where A, B, C and D are constants defined as :

$$A = i^T \Sigma^{-1} \mu \quad (6)$$

$$B = \mu^T \Sigma^{-1} \mu \quad (7)$$

$$C = i^T \Sigma^{-1} i \quad (8)$$

$$D = BC - A^2 \quad (9)$$

$$A, B, C, D \geq 0 \quad (10)$$

And with $\iota \in R^N$ a summation vector defined as :

$$i^T = \begin{bmatrix} 1 \\ 1 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ 1 \end{bmatrix} = [11 \dots 1] \quad (11)$$

with Σ^{-1} is the inverse of the matrix Σ .

3.Temporal Aggregation Effects on the Portfolio of Bank Stocks

In order to study the effects of temporal aggregation we used daily data from the Athens Stock Exchange. The data cover the period 1995/1/1 – 2005/3/28. The data set concerns the returns of seven Banks of the Athens Stocks Exchange², namely³:

National Bank, General Bank, Eurobank, Emporiki Bank, Alfa Bank, Bank of Attika and the Bank of Greece. A graphical presentation of the diachronic behavior of these stocks (with basis the 3/1/1995) is given in Figure 1.

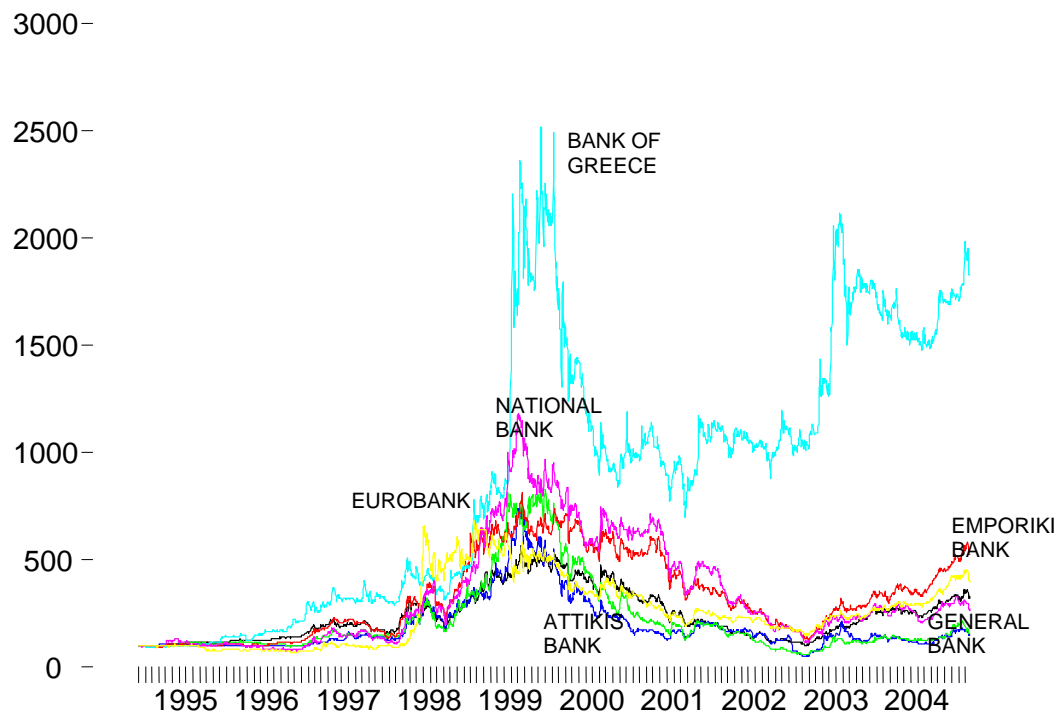


Figure 1: Competitive diachronic movement of the stock prices of the seven Banks of the Athens Stocks Exchange.

² More about the characteristics of the Athens Stocks Exchange can be found in: Alexakis, P. and Petrakis, P., (1991), Apergis, N. and Eleftheriou, S., (2001), Barkoulas, J.T. and Travlos, N.G., (1998), Barkoulas, J.T., Baum, C.F. and Travlos, N.G., (2000), Bletsas, A. (1983), Coutts, J.A., Kaplanidis, C. and Roberts, J., 2000, Demos, A. and Parissi, S., 1998, Karathanassis, G. and Philippas, N., (1993), Karathanassis, G. and Philippas, N., (1993), Kirikos, D., (1996), Koutmos, G., Negakis, C. and Theodossiou, Laopodis, N. (1997), Mertzanis, H. and Siriopoulos, C., (1999), Milonias, A.E., Moschos, D., and Xanthakis, M., (1998), Milonas, N.T., (2000), Niarchos, N. and Alexakis, C., (1998), Papachristou, G., (1999), Papaioannou, G.J., Travlos, N.G. and Tsangarakis, N.V., (2000)

³ We choose these stocks due to data availability reasons.

TABLE 1 Average Total Returns of the Portfolio at Different Management Periods using the Mean Variance Approach at 15 Different Levels of Temporal Aggregation.

| Temporal Aggregation Level | 100 Days Management Average Return % | 100 Days Management Standard Deviation | 200 Days Management Average Return % | 200 Days Management Standard Deviation | 300 Days Management Average Return % | 300 Days Management Standard Deviation |
|----------------------------|--------------------------------------|--|--------------------------------------|--|--------------------------------------|--|
| 1 | -4,26989 | 0,248706 | -1,73558 | 0,353866 | -1,72507 | 0,441777 |
| 2 | -3,76852 | 0,123603 | -5,69069 | 0,180081 | -4,81034 | 0,222945 |
| 3 | -4,92971 | 0,03674 | -6,99234 | 0,075287 | -7,89973 | 0,110262 |
| 4 | -3,6876 | 0,030984 | -7,71721 | 0,033234 | -9,27713 | 0,054897 |
| 5 | -3,10115 | 0,023949 | -6,18948 | 0,026599 | -9,3336 | 0,028414 |
| 6 | -1,61094 | 0,028352 | -4,30539 | 0,028829 | -7,02999 | 0,024573 |
| 7 | -0,79912 | 0,032448 | -2,19834 | 0,044801 | -4,47001 | 0,043109 |
| 8 | 0,432031 | 0,030337 | -0,58951 | 0,051161 | -2,10361 | 0,05917 |
| 9 | 0,829176 | 0,027156 | 1,106782 | 0,045342 | 0,35224 | 0,062143 |
| 10 | 1,836383 | 0,031708 | 2,287912 | 0,044318 | 2,383864 | 0,062926 |
| 11 | 1,453018 | 0,025538 | 3,0804 | 0,03124 | 3,483179 | 0,044637 |
| 12 | 2,263866 | 0,021709 | 3,654791 | 0,025067 | 5,195121 | 0,036878 |
| 13 | 1,669787 | 0,017852 | 3,891006 | 0,019047 | 5,145972 | 0,023846 |
| 14 | 1,518146 | 0,018364 | 2,835893 | 0,016107 | 4,277454 | 0,017439 |
| 15 | 0,949198 | 0,017395 | 2,512184 | 0,017781 | 4,021305 | 0,02098 |

Source: *Our Estimates*

On the Table 1 we present the results of applying the Markowitz⁴ Mean Variance portfolio management on the seven stocks of the Banking Sector ,at 15 different levels of temporal aggregation, three portfolio management periods of 100, 200 and 300 days and for different dates of starting the portfolio management⁵. These average

⁴ Markowitz, H. M. (1959).

⁵ In order to make our results more representative the date of starting the portfolio management was selected randomly using 3000 experiments with random the starting day of the portfolio management. The mean returns refer to the 3000 experiments.

total returns are the means of the distributions of the 3000 iterations with random characteristic the date of starting the portfolio management. According to the results of Table 1 we observe a strong differentiation of our results regarding the average returns of the portfolio and the associated portfolio risk, at different levels of temporal aggregation (disaggregation). More specifically we observe an increase to the average total returns of the portfolio. Simultaneously we observe a decrease to the average risk of the portfolio as the risk is measured from its standard deviation. Figures 2,3 and 4 presents the analogous distributions of average total returns at 15 different levels of temporal aggregation of a portfolio management with 100,200 and 300 days, respectively.

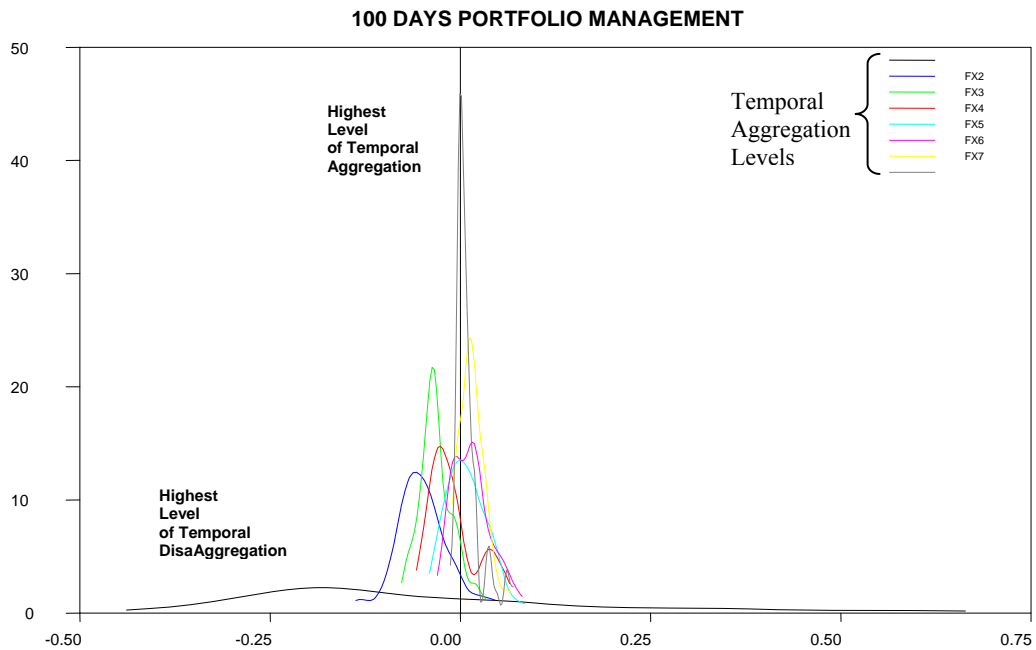


Figure 2. Average Returns Distributions at Different Levels of Temporal aggregation (100 Days Portfolio Management)

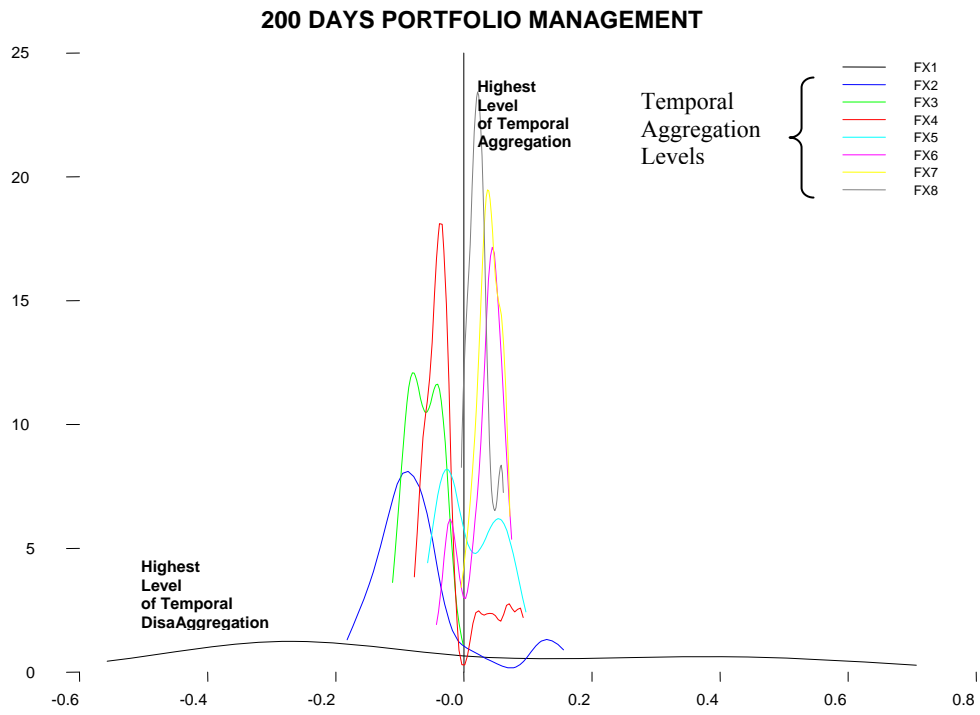


Figure 3. Average Returns Distributions at Different Levels of Temporal aggregation (200 Days Portfolio Management)

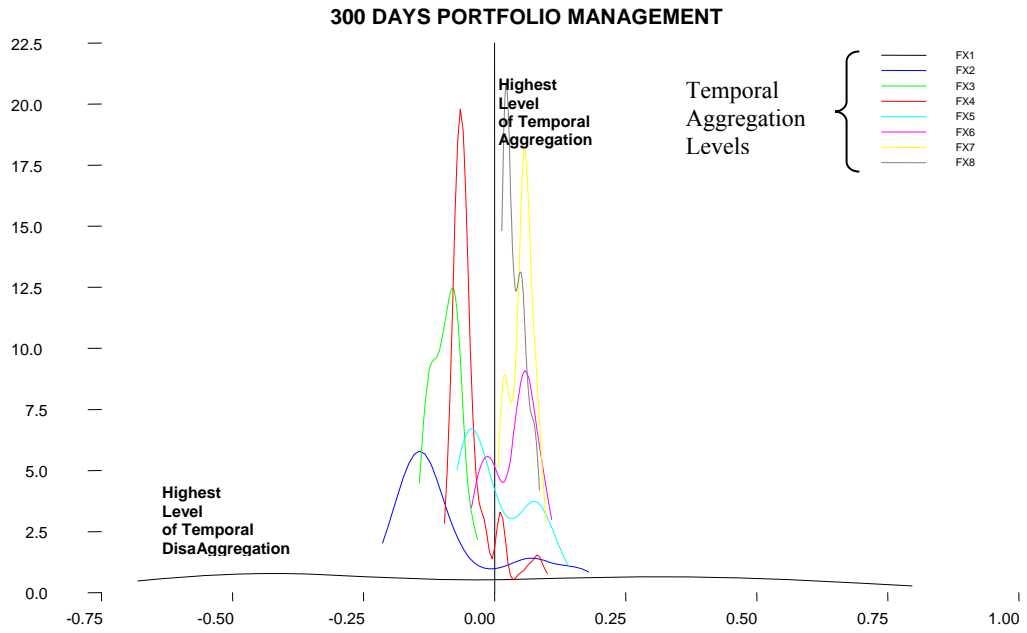


Figure 4. Average Returns Distributions at Different Levels of Temporal aggregation (300 Days Portfolio Management)

Finally in Figures 5 and 6 we present the average structure⁶ of the portfolio of the seven stocks at different levels of temporal aggregation. It is obvious the differentiation of the average structure of the portfolio due the temporal aggregation effects.

⁶ If the structure w of the portfolio of the $j = 1, 2, \dots, 7$ stocks at a level of temporal aggregation A , on the $i = 1, 2, \dots, 3000$ experiment is :

$$j = 1, 2, \dots, 7$$

$w_{j,i}^A$ with $A = 1, 2, 3, \dots, 15$ then the average structure of the portfolio is defined as:

$$i = 1, 2, \dots, 3000$$

$$mw_j^A = (\sum_{i=1}^{3000} w_{j,i}^A) / 3000$$

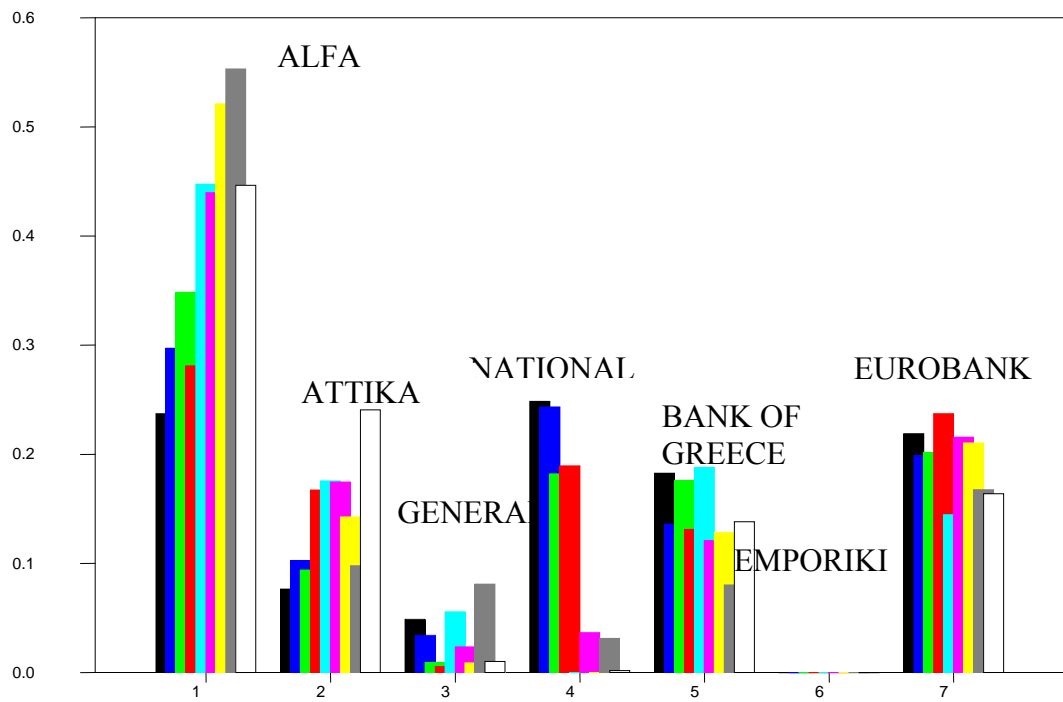


Figure 5. Average Structural of the Portfolio at Different Levels of Temporal Aggregation.

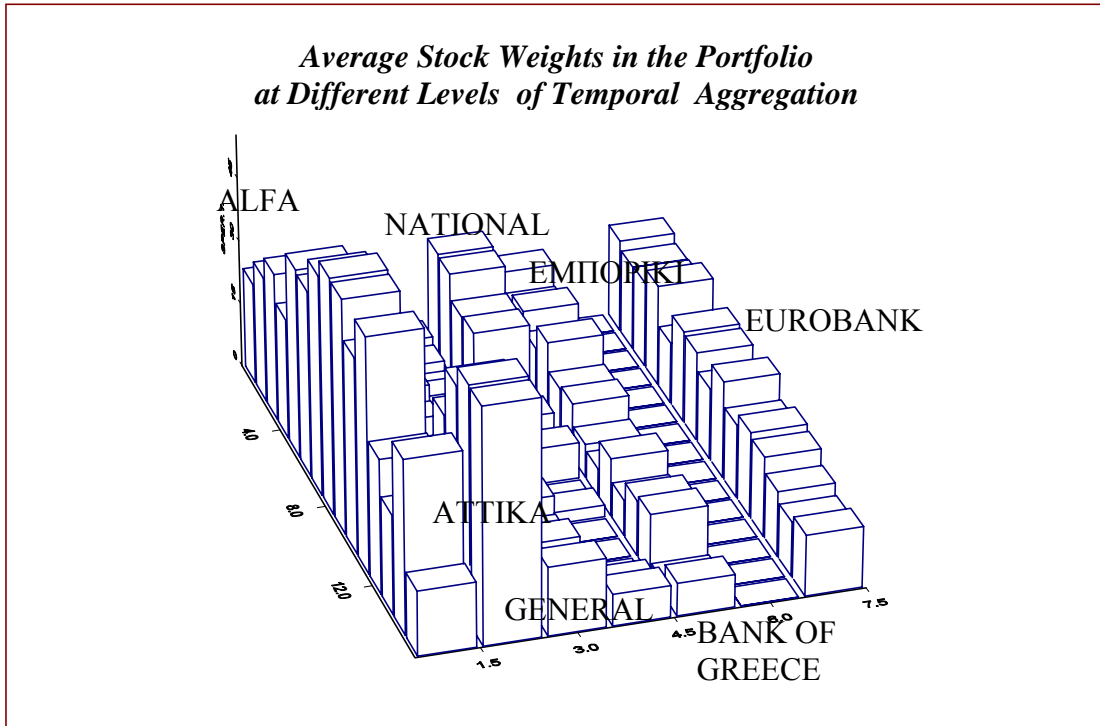


Figure 6. Average Structural of the Portfolio at Different Levels of Temporal Aggregation.

According to our empirical results the effects of temporal aggregation seems to be serious on the future returns of the portfolio, the structure and the number of the stocks to participate to the portfolio⁷.

In the next section we use Monte Carlo experiments in order to generalize our results.

4.The Monte Carlo Experiments

In our simulation experiments we used two Data Generating Process(DGP). In the first process (A) we assume ARCH characteristics⁸ and autoregressions⁹ of the simulated returns:

⁷ More information about the participation number of the stocks to the portfolio structure is available on request.

⁸ More sophisticated models were used in the simulation leading to similar results. More are available from the authors on request.

$$d_t = a_o + a_1 d_{t-1} + u_t \quad (12)$$

$$u_t = v_t \sqrt{(1 + 0.2u_{t-1}^2)} \quad (13)$$

$$v_t \approx NID(0,1) \quad (14)$$

In the second process (B) we assume that the returns follow a pure random behavior with ARCH characteristics:

$$d_t = 0.027656 + u_t \quad (15)$$

$$u_t = v_t \sqrt{(1 + 0.2u_{t-1}^2)} \quad (16)$$

$$v_t \approx NID(0,1) \quad (17)$$

where d_{jt} : the simulated returns of the j stock for $j = 1, 2, \dots, 12$

u_t : disturbances with ARCH characteristics.

v_t : disturbances.

In our experiments we used 20 different level of temporal aggregation. For each temporal aggregation level we estimate the aggregate returns using the relation:

$$d_T^A = C^{k=j} d_t \quad (18)$$

Where d_T^A is the time aggregated series, $j = 1, 2, 3, \dots, 20$ refers to the time aggregation level and C is a time aggregation matrix of the form:

⁹ In the simulations the parameters a_o and a_1 of (12) were specified as follows: $a_o = 0.06$ $a_1 = Uniform\ Distribution(.2, .8)$

$$C^j = (1/j) \begin{bmatrix} \overbrace{11\dots 1}^j & 00\dots 0 & \dots & 00\dots 0 & 00\dots 0 \\ 00\dots 0 & \overbrace{11\dots 1}^j & \dots & 00\dots 0 & 00\dots 0 \\ 00\dots 0 & 00\dots 0 & \dots & \overbrace{11\dots 1}^j & 00\dots 0 \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ 00\dots 0 & 00\dots 0 & \dots & 00\dots 0 & \overbrace{11\dots 1}^j \end{bmatrix} \quad (19)$$

The following steps used in the application of the Monte Carlo experiment: Using the relations (12)-(14) και (15)-(18) we simulate the returns of the seven stocks at the highest level of temporal disaggregation. ($j = 1$) . We aggregate with the temporal aggregation matrix C^j with $j = 1, 2, \dots, 20$ the returns $(d_{1t}, d_{2t}, \dots, d_{12t})$ at the different temporal aggregation levels and apply the Markowitz approach. We repeat this procedure (NITERS=4000) 4000 times.

The **Average total returns** for the three period of portfolio management and the 20 temporal aggregation levels were estimated using the following relations:

Weights based on the mean variance management approach.

$$w^A_{j,i} \quad (20)$$

With: $j = 1, 2, \dots, NEQ$ (Number of stocks) , $A = 1, 2, \dots, 20$ (Temporal aggregation Levels), $i = 1, 2, \dots, NITERS$ (Number of iterations)

Portfolio Returns.

$$r^A_{t,i=1,2,\dots,NITERS} = \sum_{j=1}^{NEQ} w^A_{j,i} d_{jt} \quad (21)$$

$d_{1t}, d_{2t}, \dots, d_{(NEQ)t}$: Simulated returns.

Total Returns

$${}^Q TR^A_{i=1,2,\dots,NITERS} = \sum_{t=1}^Q \sum_{j=1}^{NEQ} w^A_{j,i} d_{jt} \quad (22)$$

$Q = 100, 200, 300$ days, for the three periods of portfolio management.

Average Total Returns.

$$\text{Mean Total Returns} = \left(\sum_{t=1}^Q \sum_{j=1}^{NEQ} w_{j,i}^A d_{jt} \right) / \text{NITERS} \quad (23)$$

The number of participants of the $j = 1, 2, 3, \dots, NEQ$ stocks in the portfolio for the NITERS is defined as follows:

$$N_PARTICIP_j^A = N_PARTICIP_j^A + 1, \text{ if } w_j^A \neq 0 \quad (24)$$

$$N_PARTICIP_j^A = N_PARTICIP_j^A + 0, \text{ if } w_j^A = 0 \quad (24)$$

for $j = 1, 2, \dots, NEQ$ and $A = 1, 2, \dots, 20$ (Temporal Aggregation Levels)

The average portfolio structure is defined as follows:

$$mw_j^A = \left(\sum_{i=1}^{N_PARTICIP_j^A} w_{j,i}^A \right) / N_PARTICIP_j^A \quad (25)$$

$j = 1, 2, 3, \dots, NEQ$

15. The Monte Carlo results

In this part of the paper we present the Monte Carlo results of the temporal aggregation(disaggregation) effects on the mean variance portfolio management approach. 4000 simulated observations (NITERS=4000) , for each of the 12 stocks simulated returns (NEQ=12) were obtained using the data generating process (A) and (B). In the portfolio management only 1600 observations were used to apply the mean variance approach and the whole number of iterations approaches the number 4000. In each of these iterations we applied the mean variance approach to obtain the number of the stocks and their optimal weights of the stocks of the portfolio at 20 different temporal aggregation levels. These stocks with their weights were then used for portfolio management with horizon of 100,200 and 300 days.

In Table 2 and in figures 7-9, we present the Mean Total Returns of three different portfolio management periods of 100,200 and 300 days, using the mean variance approach at 20 different temporal aggregation(disaggregation) levels using the data generating process (12)-(14). These results are similar with the analogous results of

Table 1 with regard the mean portfolio risk¹⁰. As temporal aggregation increases we observe an analogous decrease on the mean portfolio risk using actual and simulated data. What is more interesting is the average number of participation and the average weight of each stock in the portfolio. In the three dimensions figures 10 and 11 we present the behavior of the number of participation and the average weigh of each stock at different level of temporal aggregation(20 levels of temporal aggregation). As the temporal aggregation increase we observe a decrease in the number of the participations of the stocks in the portfolio with a simultaneous increase on the weigh with which each stock participates in the portfolio. The results of Table 3 are completely different compared with the previous case , indicating no serious effects of temporal aggregation on the portfolio management using the mean variance approach, in the case the stocks of the portfolio exhibits random characteristics.

TABLE 2. Mean Total Returns at different portfolio management periods applying the Markowitz Mean Variance Approach at 20 different levels of Temporal Aggregation based on the DGP: $d_t = a_o + a_1 d_{t-1} + u_t$, $u_t = v_t \sqrt{(1 + 0.2u_{t-1}^2)}$ and $v_t \approx NID(0,1)$ Number of stochastic simulations 4000

| Temporal Aggregation Level | 100 Days Management Average Return % | 100 Days Management Standard Deviation | 200 Days Management Average Return % | 200 Days Management Standard Deviation | 300 Days Management Average Return % | 300 Days Management Standard Deviation |
|----------------------------|--------------------------------------|--|--------------------------------------|--|--------------------------------------|--|
| 1 | 9,877491 | 4,404032 | 19,95309 | 6,449186 | 30,2264 | 9,877491 |
| 2 | 4,859673 | 2,187426 | 9,809902 | 3,172157 | 14,86547 | 4,859673 |
| 3 | 3,182101 | 1,444495 | 6,412295 | 2,095391 | 9,820026 | 3,182101 |
| 4 | 2,39523 | 1,088696 | 4,822328 | 1,572933 | 7,305912 | 2,39523 |
| 5 | 1,900838 | 0,873127 | 3,83324 | 1,260072 | 5,81606 | 1,900838 |
| 6 | 1,521763 | 0,718703 | 3,154493 | 1,045153 | 4,828034 | 1,521763 |
| 7 | 1,319368 | 0,618039 | 2,662349 | 0,894258 | 4,030283 | 1,319368 |
| 8 | 1,132461 | 0,542542 | 2,369774 | 0,793258 | 3,540171 | 1,132461 |
| 9 | 1,033757 | 0,497729 | 2,084912 | 0,710868 | 3,155198 | 1,033757 |

¹⁰ The behavior of the mean total returns is not compatible as it depends on the characteristics of the actual stocks returns and the parameters of the simulated model.

TABLE 2 continues

| Temporal Aggregation Level | 100 Days Management Average Return % | 100 Days Management Standard Deviation | 200 Days Management Average Return % | 200 Days Management Standard Deviation | 300 Days Management Average Return % | 300 Days Management Standard Deviation |
|----------------------------|--------------------------------------|--|--------------------------------------|--|--------------------------------------|--|
| 10 | 0,938586 | 0,45213 | 1,891106 | 0,643665 | 2,863833 | 0,938586 |
| 11 | 0,845479 | 0,408212 | 1,696622 | 0,586485 | 2,564885 | 0,845479 |
| 12 | 0,747025 | 0,371393 | 1,508219 | 0,522958 | 2,373769 | 0,747025 |
| 13 | 0,654751 | 0,337094 | 1,407556 | 0,496214 | 2,178103 | 0,654751 |
| 14 | 0,657437 | 0,326758 | 1,318006 | 0,464761 | 1,986809 | 0,657437 |
| 15 | 0,55969 | 0,292005 | 1,218082 | 0,431829 | 1,885809 | 0,55969 |

Source: Our Estimates

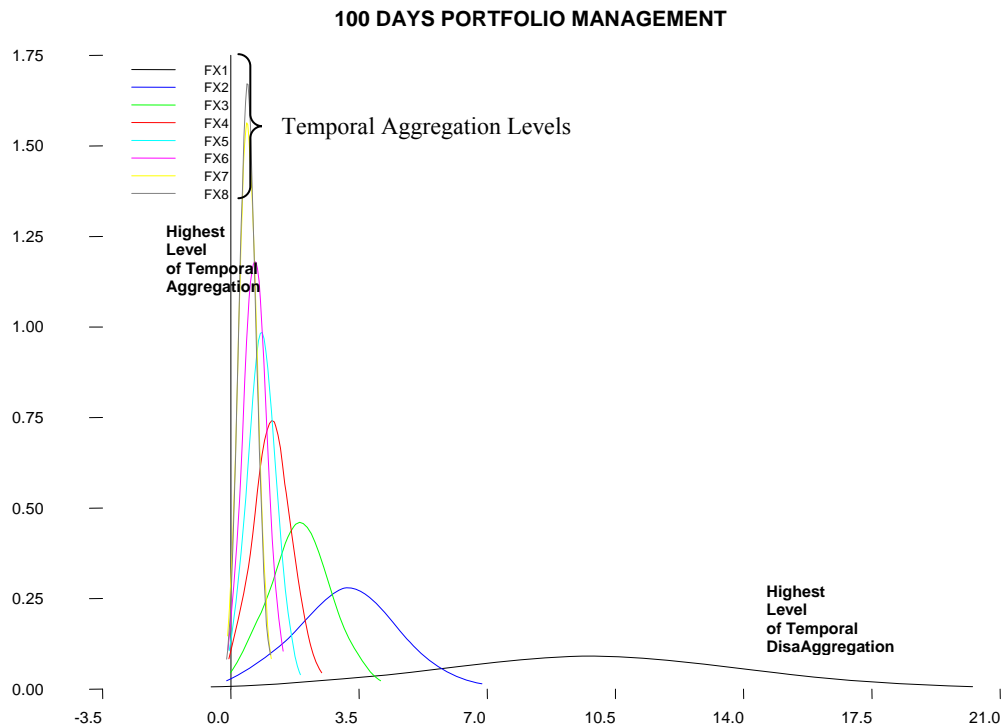


Figure7. Mean Returns Distributions at Different Levels of Temporal Aggregation (100 Days Portfolio Management)

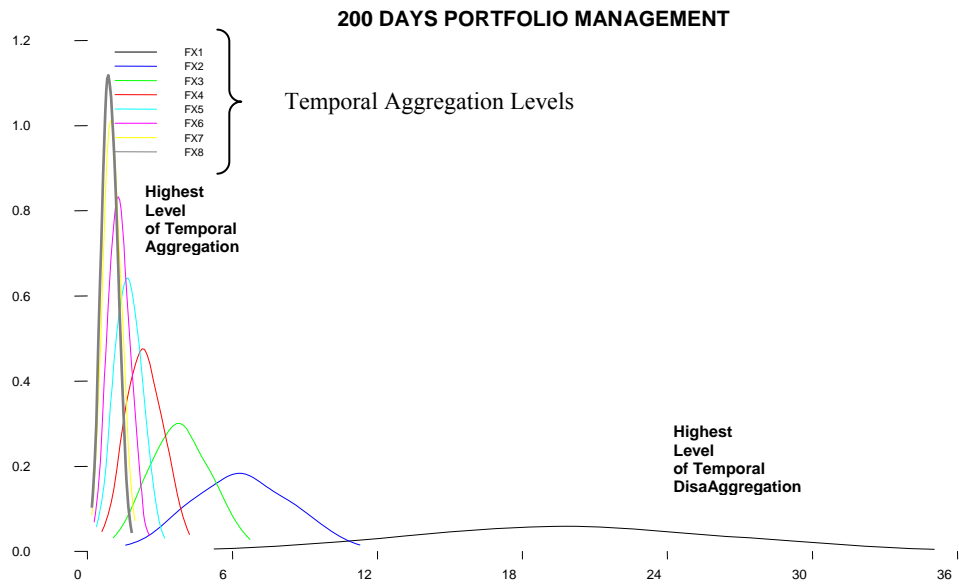


Figure 8. Mean Returns Distributions at Different Levels of Temporal Aggregation (200 Days Portfolio Management)

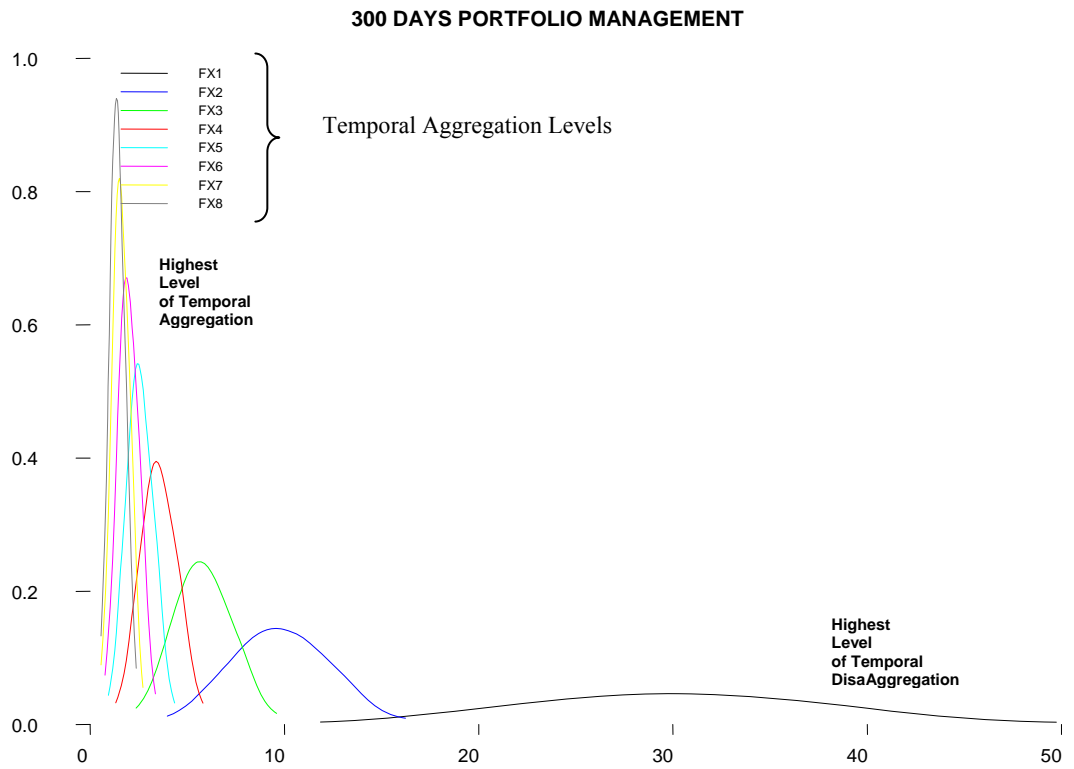


Figure 9. Mean Returns Distributions at Different Levels of Temporal Aggregation (300 Days Portfolio Management)

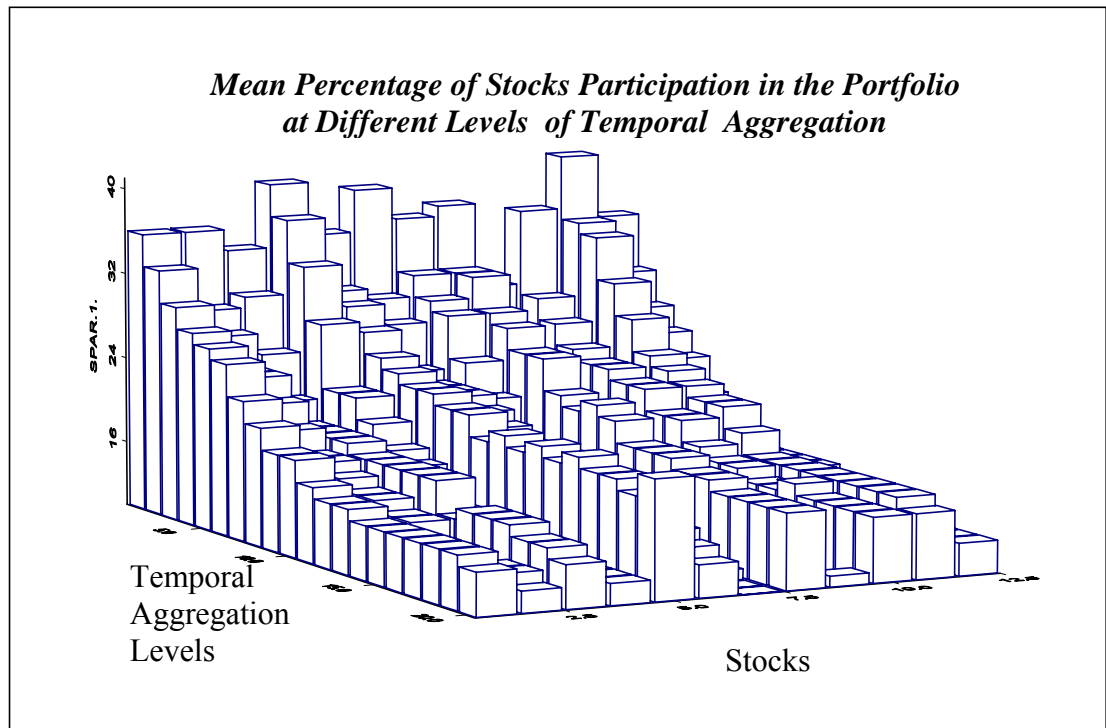


Figure 10.Percentage of participation of each stock in the portfolio at different level of temporal aggregation (Disaggregation).

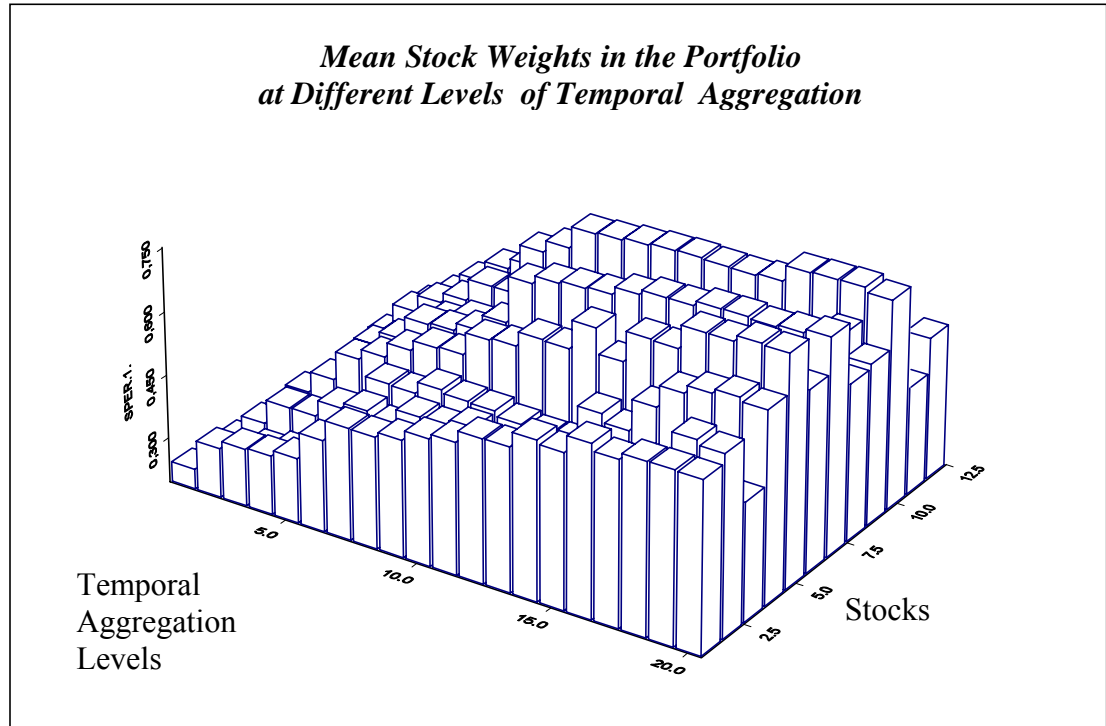


Figure 11. Mean Stock Weights at different level of temporal aggregation (Disaggregation).

TABLE 3. Average Total Returns at different Management periods applying the Markowitz Mean Variance at 20 different levels of Temporal Aggregation based on the DGP: $d_t = 0.027656 + u_t, u_t = v_t \sqrt{(1 + 0.2u_{t-1}^2)}$ and $v_t \approx NID(0,1)$ Number of stochastic simulations 4000

| Temporal Aggregation Level | 100 Days Management Average Return % | 100 Days Management Standard Deviation | 200 Days Management Average Return % | 200 Days Management Standard Deviation | 300 Days Management Average Return % | 300 Days Management Standard Deviation |
|----------------------------|--------------------------------------|--|--------------------------------------|--|--------------------------------------|--|
| 1 | 29,96946 | 1,411991 | 60,01385 | 1,963478 | 99,96048 | 2,538399 |
| 2 | 29,95714 | 1,55704 | 60,00749 | 2,173367 | 99,95497 | 2,769195 |
| 3 | 29,94403 | 1,725282 | 60,00138 | 2,400607 | 99,93769 | 3,034335 |
| 4 | 29,9456 | 1,878832 | 60,01538 | 2,616035 | 99,94721 | 3,283664 |
| 5 | 29,95962 | 2,031148 | 60,03782 | 2,837422 | 99,96961 | 3,544813 |
| 6 | 29,95003 | 2,177938 | 60,04175 | 3,041662 | 99,97051 | 3,808691 |
| 7 | 29,97418 | 2,29858 | 60,05984 | 3,216882 | 99,97872 | 4,029769 |
| 8 | 29,95898 | 2,419763 | 60,05824 | 3,375905 | 99,97938 | 4,228155 |
| 9 | 29,97588 | 2,533694 | 60,08823 | 3,582397 | 100,0244 | 4,477729 |
| 10 | 29,97907 | 2,646102 | 60,08217 | 3,714452 | 100,0341 | 4,651665 |
| 11 | 29,98784 | 2,734067 | 60,08085 | 3,848902 | 100,0187 | 4,819371 |
| 12 | 29,97169 | 2,831648 | 60,08964 | 3,999841 | 100,0228 | 4,958048 |
| 13 | 29,97793 | 2,908079 | 60,09445 | 4,113783 | 100,0389 | 5,124506 |
| 14 | 29,99946 | 2,9943 | 60,10229 | 4,240489 | 100,0362 | 5,320245 |
| 15 | 29,99261 | 3,08865 | 60,09851 | 4,369803 | 100,0487 | 5,487046 |
| 16 | 29,99401 | 3,148463 | 60,08641 | 4,466462 | 100,0515 | 5,605604 |
| 17 | 30,00599 | 3,228907 | 60,11446 | 4,600073 | 100,0555 | 5,74897 |
| 18 | 30,01007 | 3,318959 | 60,12062 | 4,727127 | 100,0468 | 5,948275 |
| 19 | 29,99432 | 3,394803 | 60,11317 | 4,798886 | 100,0434 | 6,017908 |
| 20 | 30,00813 | 3,466233 | 60,12032 | 4,925773 | 100,0412 | 6,22934 |

Source: *Our Estimates*

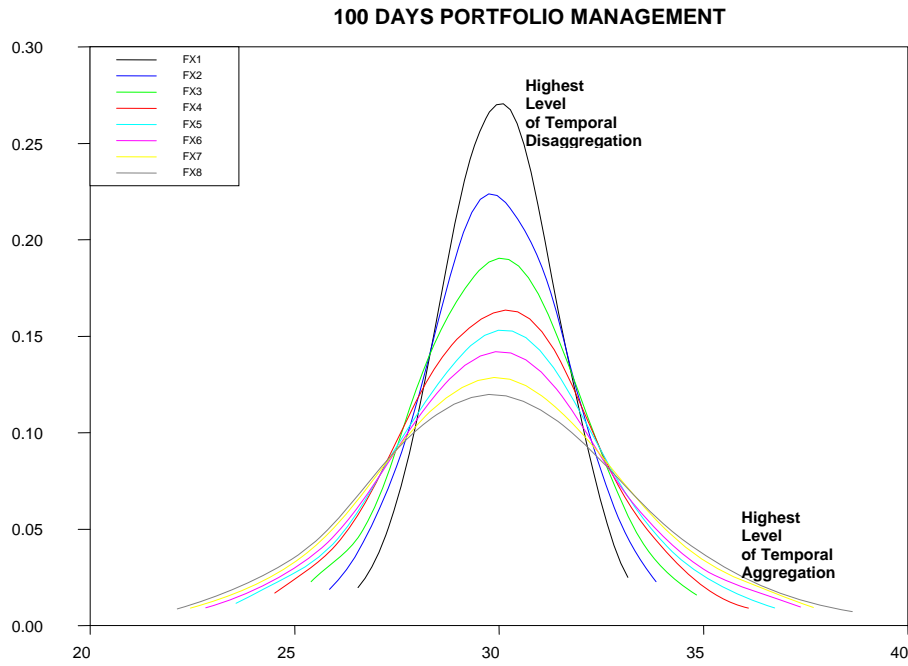


Figure 12. Average Returns Distributions at Different Levels of Temporal Aggregation (100 Days Portfolio Management)

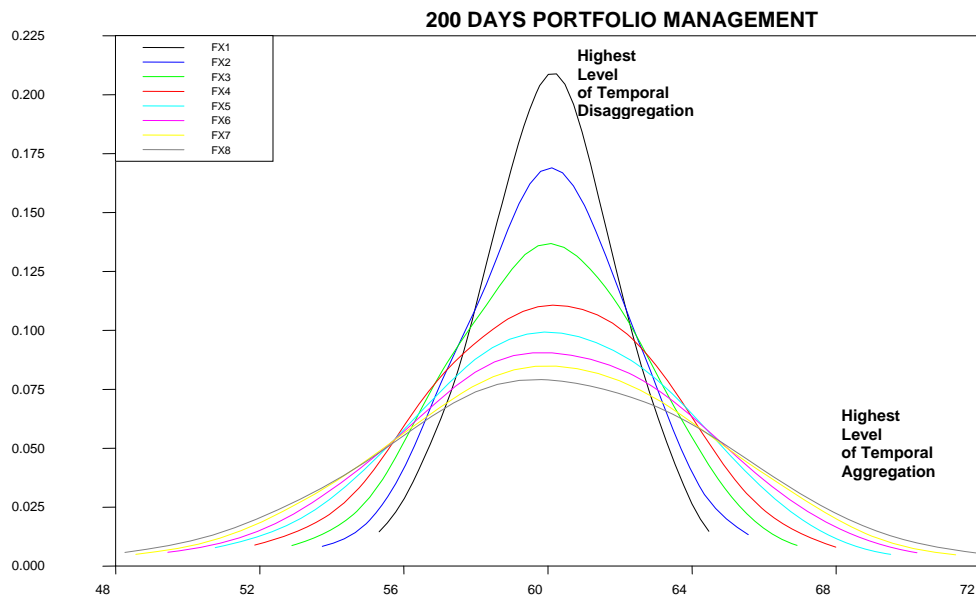


Figure13. Average Returns Distributions at Different Levels of Temporal Aggregation (200 Days Portfolio Management)

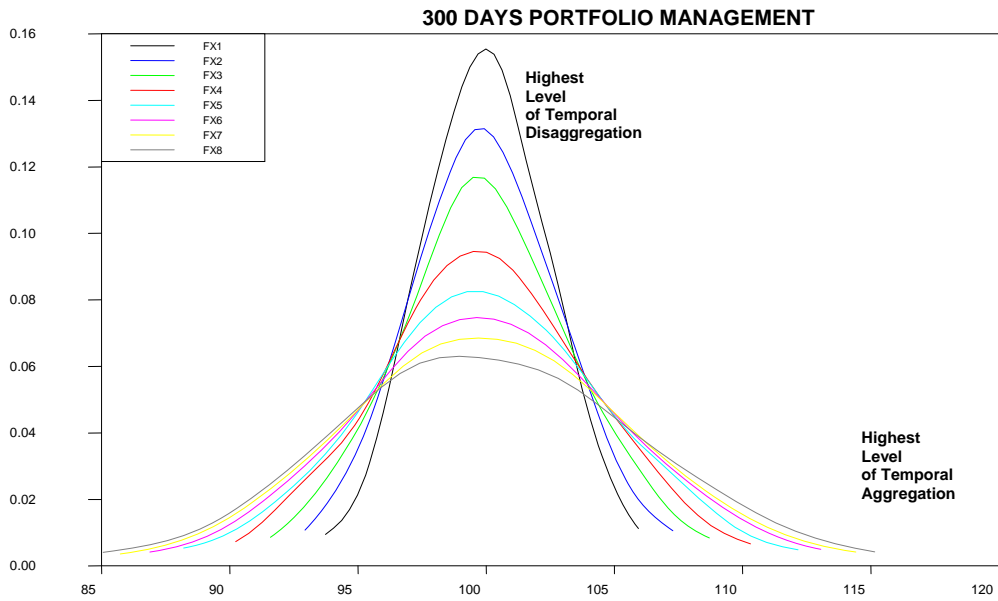


Figure14. Average Returns Distributions at Different Levels of Temporal Aggregation (300 Days Portfolio Management)

5. Conclusions

In this paper we analyze the effects of temporal aggregation on the efficient management of a portfolio of stocks using the Markowitz Mean Variance approach. Using real data of the Athens Stocks Exchange and simulation techniques we end up with the conclusions that efficient portfolio management is closely related with the appropriate level of temporal aggregation the returns are selected. The effects of temporal aggregation on the portfolio performance are very serious usually leading in different results related with the temporal aggregation level the data are used. The different results of temporal aggregation effects are related with the number each stock is participating in the portfolio, its weights in the portfolio and finally the future performance of the portfolio.

Reference

- Alexakis, P. and Petrakis, P., (1991), Analysing Stock Market Behaviour in a Small Capital Market, *Journal of Banking and Finance*, Vol.15, pp.471-83.
- Amemiya, T. and R.Y. Wu (1972), The Effect of Aggregation on Prediction in the Autoregressive Model, *Journal of the American Statistical Association*, No. 339, 628-632.
- Apergis, N. and Eleptheriou, S., (2001), Stock Returns and Volatility: Evidence from the Athens Stock Market Index, *Journal of Economics and Finance*, Vol. 25, pp. 50-61.
- Barkoulas, J.T. and Travlos, N.G., (1998), Chaos in an Emerging Capital Market? The Case of the Athens Stock Exchange, *Applied Financial Economics*, Vol. 8, pp. 231-243.
- Barkoulas, J.T., Baum, C.F. and Travlos, N.G., (2000), Long Memory in the Greek Stock Market?, *Applied Financial Economics*, Vol. 10, pp. 177-184.
- Bletsas, A. (1983), Rates of Return on Investments in the Athens Stock Exchange: 1955-1975, *Greek Economic Review*, Vol. 4, pp. 242-254.
- Brewer K.R.W., (1973), 'Some consequences of temporal aggregation and systematic sampling for ARIMA and ARIMAX models', *Journal of Econometrics*, 1, pp.133-154
- Coutts, J.A., Kaplanidis, C. and Roberts, J., (2000), Security Price Anomalies in an Emerging Market: The Case of the Athens Stock Exchange, *Applied Financial Economics*, Vol. 10, pp 561-571.
- Demos, A. and Parissi, S., (1998), Testing Asset Pricing Models: The Case of the Athens Stock Exchange, *Multinational Finance Journal*, Vol. 2, pp. 189-223.
- Di Fonzo Tommaso (2003)., Temporal disaggregation of economic time series: towards a dynamic extension., Luxembourg: Office for Official Publications of the European Communities, 2003
- Doumpos, M. and Zopounidis, C.,(2002). *Multicriteria Decision Aid Classification Methods.* , Kluwer Academic Publishers, Dordrecht.
- Elton Edwin & Gruber Martin.,(1977)., Modern portfolio theory ,1950 to date., *Journal of Banking and Finance.*,1977.,pp.1743-1759.
- Engle, R.F. (1969), Biases from Time-Aggregation of Distributed Lag Models, Ph.D. Dissertation, Cornell University.
- Granger, C.W.J., and T.-H. Lee (1999), The Effect of Aggregation on Nonlinearity, *Econometric Reviews*, 18, 259-269.

- Granger C.W.J. and Siklos, P.L.,(1995). 'Systematic sampling, temporal aggregation, seasonal adjustment, and cointegration: Theory and evidence', *Journal of Econometrics*, 66, pp.357-369
- Grinblatt M., Titman S., (1989), Portfolio Performance Evaluation: Old Issues and New Insights, *The review of Financial Studies*, Vol 2, No 3 (1989), pp 393-421, <http://rfs.oupjournals.org/cgi/reprint/2/3/393>
- Karathanassis, G. and Philippas, N.,(1993), The Use of Error Components Models in Business Finance: A Review Article and an Application, *Spoudai*, Vol. 43, pp. 95-110.
- Kirikos, D., (1996), Risk Aversion and the Efficient Markets Model for Stock Prices: Evidence from the Athens Stock Exchange, in Doukas, J. and Lang, L., eds., *Research in International Business and Finance*, Supplement 1, pp. 279-295, London, JAI Press.
- Koutmos, G., Negakis, C. and Theodossiou, P., (1993), Stochastic Behaviour of the Athens Stock Exchange, *Applied Financial Economics*, Vol. 3, pp. 119-126.
- Laopodis, N. (1997), Distributional Properties and Weekly Return Patterns of the Athens Stock Exchange, *Applied Economics Letters*, Vol. 4, pp. 769-774.
- Marcellino, M. (1999), Some Consequences of Temporal Aggregation in Empirical Analysis, *Journal of Economic and Business Statistics*, 17, 129{136.
- Markowitz, H. M. (1959)., *Portfolio Selection: Efficient Diversification of Investments*, New York: JohnWiley and Sons.
- Mertzanis, H. and Siriopoulos, C., (1999), Financial Regulation and Stock Market Volatility in the Athens Stock Exchange, *Economia Internazionale*, Vol. 52, pp. 191-213.
- Milionis, A.E., Moschos, D., and Xanthakis, M., (1998), The Influence of Foreign Markets on the Athens Stock Exchange, *Spoudai*, Vol. 48, pp 140-156.
- Milonas, N.T., (2000), Similarly Traded Securities: Greek Common vs. Preferred Stock, *European Financial Management*, Vol. 6, pp. 343-366.
- Niarchos, N. and Alexakis, C., (1998), Stock Market Prices, 'Causality' and Efficiency: Evidence from the Athens Stock Exchange, *Applied Financial Economics*, Vol. 8, pp. 167-174.
- Papachristou, G., (1999), Stochastic Behaviour of the Athens Stock Exchange: A Case of Institutional Nonsynchronous Trading, *Applied Financial Economics*, Vol. 9, pp. 239-250.

Papaioannou, G.J., Travlos, N.G. and Tsangarakis, N.V., (2000), Valuation Effects of Greek Stock Dividend Distributions, *European Financial Management*, Vol. 6, pp. 515-531.

Quenouille, M.H. (1957), *The Analysis of Multiple Time Series*, London: Griffin.

Rossana R.J. and Seater, J.J.,(1995). 'Temporal aggregation and economic time series', *Journal of Business and Economic Statistics*, 13, pp.441-451

Stram, D.O. and W.W.S. Wei (1986), Temporal Aggregation in the ARIMA Process, *Journal of Time Series Analysis*, 7, 279-292

Tiao, G.C. (1972), Asymptotic Behaviour of Temporal Aggregates of Time Series, *Biometrika*, 59, 525-531.

Tserkezos D. ,Georgutsos D and Kouretas G,(1998).,'Temporal Aggregation in Structure VAR Models.' *Applied Stochastic Models and Data Analysis*, 14,pp. 19-34

Wei, W.W.S. (1990) *Time Series Analysis: Univariate and Multivariate Methods*.Addison-Wesley, California.

Weiss, A.A. (1984) Systematic sampling and temporal aggregation in time series models, *Journal of Econometrics*, 26, 271-281.

Zellner,A. and Montmarquette,C (1971) A study of some aspects of temporal aggregation problems in econometric analyses, *Review of Economics and Statistics*, 63, 335-342.