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# The Effect of social security, demography and technology on retirement

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# The Effect of Social Security, Demography and Technology on Retirement\*

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## Abstract

This article investigates the causes in the reduction of labor force participation of the old. We argue that the changes in social security policy, in technology and in demography may account for most of the changes in retirement over the second part of the last century in the U.S. economy. We develop a dynamic general equilibrium model with endogenous retirement that embeds social security legislation. The model is able to match very closely the increase in the retirement rate of males aged 65 and older. It also quantifies the isolated impact on retirement and on the solvency of the social security system of the different factors. The model suggests that technological and demographic changes had a strong influence on retirement, so that it would have increased significantly even if the social security rules had not changed. However, as the latter became much more generous in the past, changes in social security policy can account not only for a sizeable part of the expansion of retirement, but also for the most of the observed increase in the social security expenses as a share of GDP.

**Key words:** social security; aging population; technology; retirement decision.

**JEL classification:** D11; B12

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# 1 The Effect of Social Security, Demography and Technology on Retirement

## 1.1 Introduction

One of the most important economic changes that took place in the last century, particularly in the second half, was the reduction of labor force participation by old people. In 1950, 42% of men older than 64 years in the United States were working in contrast to only 17.5% in 2000. Just four out of every ten 66 year old male were retired in 1950, but fifty years later almost seven out of ten were out of the labor force. This phenomenon is hardly exclusive of the United States. Blondal and Scarpetta (1998) and Gruber and Wise (1999) provide evidence that the workforce participation of the old population has declined in many countries of the OECD.

The importance of understanding the factors that may account for this sizeable increase in retirement is that they may be in the root of the fiscal crisis that the U.S. social security system is faced with today. In fact, according to the social security trustees 2002 report, in about 15 years the program will begin to experience permanent annual deficits. As a consequence, it is projected that in 2041 the program will not be able to pay legally scheduled benefits.

Because coverage under the law has expanded and benefits have increased throughout most of this time period, the social security retirement system is an obvious suspect for the reduction in labor supply among the elderly. For a long time, economists have investigated the importance of higher social security benefits as an explanation for the changes in retirement using a variety of estimation methods.<sup>1</sup> Nevertheless, the empirical evidence is inconclusive. Parsons (1982) and Gustman and Steinmeir (1986), for example, have found that social security have had strong negative effect on male labor supply, whereas Moffitt (1987), Burtless (1986) and Krueger and Pischke (1992) concluded that the large increase in real social security benefits over the past four decades had little effect. These results suggest

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<sup>1</sup>Surveys of the literature can be found in Diamond and Hausman (1984); Gustman and Steinmeier (1986); Sueyoshi (1989).

that either there are problems associated with the methods that have been used to investigate this relationship, or there are other explanations that must be taken in consideration.

At the same time there was a marked change in the demographic composition of the population in the U.S., namely, the aging of the population with the consequent expansion of the ratio of old to young people. In addition to obvious concerns on budgetary stability - as social security spending as a share of GDP tends to increase - the rise in longevity may play an important role in the decision to leave the labor force. Kalemli-Ozcan and Weil(2006), for instance, shows that exogenous decreases in the probability of death, which allows people to better plan saving for old age, generates longer retirement life.

Longevity may play an even stronger role in the decision to leave the labor force since the relative productivity of old workers have been declining in recent years at a faster pace than it used to. In fact, Heckman, Lochner and Todd (2003) provide evidence that old workers have become less productive relative to young workers over the second part of the last century. A technological explanation for this is most probable. Graebner(1980) argues that technical change leads to retirement because old people learn slower, making them obsolete in periods of faster innovation, such as the last twenty or thirty years. Moreover, because it reduces the opportunity cost of retirement and raises retirement benefits through increasing lifetime labor earnings, this change in the age-efficiency profile has an important effect on the decision of leaving the labor force, as shown by Ferreira and Pessôa (2007).

This article develops and calibrates a stochastic overlapping generations model of large scale in order to investigate the causes of the observed change in retirement behavior of the American population between 1950 and 2000. We focus on the role of social security, of demographic factors (associated with higher longevity) and of changes in the experience profile. In the model, individuals decide at each period whether to stay in the labor force or to retire, by comparing the expected return of each option. If they continue working, they also decide how to divide their time between leisure and labor. The usual consumption/saving decision over all periods of the life cycle also applies. Government plays a simple role in this economy: it taxes individuals to finance social security pensions.

The model is calibrated to the U.S. economy in 1950, our benchmark year, and it embeds the rules governing the contributions and payment of social security old age benefits. It is

then simulated taking into consideration the changes in social security, demography and age-efficiency profile between 1950 and 2000. The model simulations are able to reproduce very closely the retirement behavior in these two years. In particular, labor force participation of older males decreases to levels similar to those in the data. Moreover, the model is also consistent with the empirical evidence that older workers are working less hours.<sup>2</sup>

The present model is related to Rios-Rull (1996), Imrohoroglu, Imrohoroglu and Jones (1998), Huggett and Ventura (1999), Fuster *et. al.* (2006). These models provide a framework rich enough to deal with all the factors that potentially affect the retirement decision. Besides, this structure allows us to model more accurately the dynamic structure of social security. In these papers, however, retirement decision is exogenous.

In Kopechy (2006), in contrast, the decision to leave the labor force is endogenous, but hours worked are fixed in every period and there is no social security in the model, which plays an important role here. As a matter of fact, we show that the single most important reason for the rise in the rate of retirement of old males by age is the increasingly generosity of the social security system. Also, of particular importance are the changes in the individual productivity profile, with longevity coming in third.

By endogeneizing the retirement behavior, our framework is also very convenient to study the impact of the aging population on the budgetary stability. In the one hand, higher longevity tends to expand the proportion of retirees and so the amount of benefits paid. This effect of longevity arises through displacement of individuals toward states in which they are prone to retire. On the other hand, individuals, by living longer, give more weight to the future, which tends to raise capital accumulation, hours worked and, as a result, the output of economy.<sup>3</sup> Hence, it is not clear beforehand what would be the net effect. We show that the aging of the population tends to put only a little pressure on the equilibrium of social security system finances.

The paper also finds that even if social security rules had not changed, total retirement would be considerably higher today than in 1950, especially because of demographic changes. However, the increase in the benefits paid-output ratio would be significantly smaller than

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<sup>2</sup>See, for example, McGrattan and Rogerson (1998).

<sup>3</sup>Moreover, as argued by Spriggs and Price (2005), the latter effect tends to be amplified if we take in consideration the increase in the productivity of young workers.

that observed in the data. In contrast, other groups of simulations show that the changes in the social security affected much more the benefits paid-output ratio than total retirement, as benefits were now significantly higher than in the past.

The last result is at odds with others in the literature (Krueger and Pischke (1992), for instance) that argue that the reduction of the retirement benefits would not impact the solvency of the system as it has little effect on retirement. Hence, our analysis should serve as an useful point of reference for future proposals of social security reform: although the structure and the value of benefits are only one among many factors affecting retirement decision, its quantitative impact on the solvency of the system is substantial.

The article is organized as follows. The model is presented in Section 2 and the calibration procedures and data in Section 3. In Section 4 results are presented and discussed; Section 5 concludes.

## 2 The model

In what follows we describe the overlapping generation model that will be used to guide our quantitative analysis of retirement. In this economy, individuals start working as soon as they are born. After spending a part of their life working, agents optimally decide whether or not to leave the labor force toward retirement. There is a social security system and the amount of retirement benefits that individuals are entitled to depends on their historical earnings. In order to obtain a smooth retirement behavior, we assume that individuals are faced with idiosyncratic productivity shocks.<sup>4</sup> These shocks may also affect the retirement decision through the opportunity cost of leaving the labor force at a given age.

### 2.1 Demography

The economy is populated by a continuous of ex-ante identical agents who may live a maximum of  $T$  periods. There is uncertainty regarding the time of death in every period so that each individual faces a probability  $\psi_t$  of surviving to the age  $t$ . Thus, a fraction of the

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<sup>4</sup>Otherwise, if an agent decides to retire at a given age, all other agents will make the same decision. In this case, the aggregate retirement rate by age is zero or 100%.



population leaves accidental bequest, which is distributed equally among all surviving individuals. The age profile of the population  $\{\mu_t\}_{t=1}^T$  is modeled by assuming that the fraction of agents at the age  $t$  in the population is given by  $\mu_t = \frac{\psi_t}{(1+g_n)}\mu_{t-1}$  and  $\sum_{t=1}^T \mu_t = 1$ , where  $g_n$  denotes the population growth rate.

## 2.2 Technology

The technology in this economy is given by a Cobb-Douglas production function with constant returns to scale:  $Y_t = BK_t^\alpha (A_t N_t)^{1-\alpha}$  where  $\alpha \in (0, 1)$  is the output share of capital income, and  $Y$ ,  $K$  and  $N$  denote aggregate output, capital and labor respectively and  $B > 0$  is a constant scale parameter. The variable  $A$  denotes a labor augmenting productivity index that grows at the constant rate  $g_A$ . The problem of the firms is standard. They pick capital and labor optimally and the first order conditions are given by:

$$r = \alpha B \left( \frac{K}{AN} \right)^{\alpha-1} - \delta \quad (1)$$

$$w = (1 - \alpha) B \left( \frac{K}{AN} \right)^\alpha \quad (2)$$

where  $r$  denotes the net rate of return on capital,  $w$  the wage rate and  $\delta$  the depreciation rate of capital.

## 2.3 Preferences

Each individual maximizes the discounted expected utility from consumption and leisure throughout life:

$$E \left[ \sum_{t=1}^T \beta^{t-1} \left( \prod_{k=1}^t \psi_k \right) u(c_t, 1 - h_t) \right] \quad (3)$$

where  $c_t$  is consumption,  $h_t$  is labor supply (total hours is normalized to one),  $\beta$  is the discount factor and  $E$  the expectation operator. The utility function of each period is assumed to take the form:

$$u(c_t, 1 - h_t) = \frac{[c_t^{1-\rho}(1 - h_t)^\rho]^{1-\gamma}}{1 - \gamma} \quad (4)$$

where  $\gamma$  denotes the risk aversion parameter and  $\rho$  denotes share of leisure in the utility.

## 2.4 Budget constrains

In each period of their life, individuals make decisions about work supply and capital accumulation. When they reach the age of  $T_r$  and over they decide whether or not to leave the labor force. In our model, we set  $T_r$  to be the age in which the worker can apply for the social security system. While individuals are in the labor force, they earn a wage  $w$  and are submitted to idiosyncratic productivity shocks  $z$ . Let  $e(z, t)$  denote the efficiency index of an agent at age  $t$  with shock  $z$ , so that the labor earnings may be written as  $wh_t e(z, t)$ , where  $h_t$  denotes the labor supply.

All workers in this economy pay a tax  $\tau$  to the government, which is collected to finance the benefit payment to the retired agents. Given that there is a maximum benefit that a retired agent receives, we put a limit  $y_{\max}$  on the taxable income, following the Social Security legislation. Thus, we can write the earnings of a worker at age  $t$ , after tax, as:

$$y(z, t, \tau, y_{\max}) = wh_t e(z, t) - \tau \max \{wh_t e(z, t), y_{\max}\}$$

We assume that workers also pay a lump-sum contribution  $\phi$  which is used to balance the government budget at the equilibrium. Let  $a_t$  denotes the agent's asset holdings at age  $t$ ,  $c_t$  the consumption and  $\xi$  the lump-sum transfer of accidental bequests and. Given these assumptions, we can write the budget constraint facing an individual who is in the labor force as:

$$(1 + g_A)a_{t+1} = (1 + r)a_t + y(z, t, \tau, y_{\max}) + \xi + \phi - c_t \quad (5)$$

An agent aged  $T_r$  and over may apply for social security retirement benefits. Let  $b_t(t_r, x)$  denotes these benefits, where  $t_r$  is the age at which the retirement decision takes place and  $x$  the individual average lifetime earnings. We assume that if a worker decides to apply for

retirement benefits he has to leave the labor force and remains retired until the end of his life. Besides, the average of lifetime earnings is calculated by taking into account individual earnings up to age  $T_r$ . Thus, the law of motion for  $x$  can be written as:

$$x_t = \frac{x_{t-1} * (t - 2) + \max \{wh_{t-1}e(z, t - 1), y_{\max}\}}{t - 1}, \quad t = 2, \dots, T_r \quad (6)$$

Let  $T_r^n$  denotes the normal retirement age, that is, the age at which individuals can claim full retirement benefit. A worker that decides to retire at the age  $t_r = T_r^n$  will receive  $b_t^n(x, tr) = \frac{\tilde{b}(x)}{(1+g)^{t-t_r}}$  for the rest of his life. The specification of the function  $\tilde{b}(x)$  is based on the rules of the U.S. social security system:

$$\tilde{b}(x) = \begin{cases} \theta_1 x & \text{if } x \leq y_1 \\ \theta_1 y_1 + \theta_2(x - y_1) & \text{if } y_1 < x \leq y_2 \\ \theta_1 y_1 + \theta_2(y_2 - y_1) + \theta_3(x - y_2) & \text{if } y_2 < x \leq y_{\max} \end{cases} \quad (7)$$

where  $0 \leq \theta_3 < \theta_2 < \theta_1$ .

Hence, up to an average earnings level of  $y_1$  retirees are entitled to  $\theta_1 x$ , so that  $\theta_1$  corresponds to the replacement rate. If the past earnings are greater than  $y_1$  but less than  $y_2$ , retirees will earn  $\theta_1 y_1 + \theta_2(x - y_1)$ , and finally if the past earnings are greater than  $y_2$  but less than  $y_{\max}$ , retirees will be entitled to  $\theta_1 y_1 + \theta_2(y_2 - y_1) + \theta_3(x - y_2)$ .

In our model, however, the age  $t_r$  at which a worker decides to abandon the labor force and applies for social security retirement benefits may be less or greater than  $T_r^n$ . If individuals start their retirement benefits at the age  $t_r \in [T_r, T_r^n)$  then their benefits will be  $b_t(t_r, x) = \eta_{t_r} b_t^n(x, t_r)$ , where  $\eta_{t_r} \in [0, 1]$ . In contrast, social security benefits are increased by a rate  $g_d$  if individuals delay their retirement beyond full retirement age. In this case, the retirement benefit will be given by  $b_t(t_r, x) = b_t^n(x, t_r)(1 + g_d)^{t_r - T_r^n}$ . However, the benefit increase no longer applies when individuals reach age  $\bar{T}_r > T_r^n$ , even if they continue to delaying retirement.

Given these assumptions, the budget constraint of an individual who decides to leave the labor force at the age  $t_r$  is:

$$(1 + g_A)a_{t+1} = (1 + r)a_t + b_t(t_r, x) + \xi + \phi - c_t \quad (8)$$

Additionally, we assume that agents cannot have negative assets at any age, so that the amount of assets carried over from age  $t$  to  $t + 1$  is such that  $a_{t+1} \geq 0$ . Furthermore, given that there is no altruistic bequest motive and death is certain at the age  $T + 1$ , agents who survive until age  $T$  consume all their assets at this age, that is,  $a_{T+1} = 0$ .

Finally, we are going to focus on the state steady of the economy under study. As a consequence, we have divided consumption, asset holdings, lump sum transfers and wage rate by  $A$  in order to eliminate the effect of economic growth. This transformation accounts for the term  $(1 + g_A)a_{t+1}$  in the individual budget constraints above.

## 2.5 Government

In our economy, the government manages a social security system, wherein the pension benefits to pensioners are financed by collecting tax  $\tau$  from the current workers. This tax is assumed to be exogenous. The amount of benefit received by each retired agent depends on his or her individual average lifetime earning through a concave, piecewise linear function, which was presented in the last subsection. The government does lump-sum transfers to the individuals in order to balance the benefits payment and the amount of collected tax. Furthermore, we assume that the government collects the accidental bequests which are also transferred on lump-sum basis for all individuals in the economy.

## 2.6 Equilibrium

Let  $s$  denote the individual states. It depends on the asset holdings  $a$  at the beginning of the period, on the lifetime average earnings  $x$  and on the idiosyncratic shock  $z$  so that  $s = (a, x, z)$ . Let  $V_t(s)$  denote the value function of an agent in the workforce at the age  $t$  and  $V_t^{t_r}(s)$  the value function of an agent at the age  $t$  whose the retirement age is  $t_r$ . The retirement decision is such that an individual at the state  $s$  retires at age  $t \geq T_r$  if  $V_t^{t_r}(s) > V_t(s)$ , while he or she remains in the labor market otherwise. The value functions  $V_t(s)$  and  $V_t^{t_r}(s)$  are

defined by the following dynamic programs:

*If retired* :

$$V_t^{tr}(s) = \max_{a'} \{u(c, 1) + \beta \psi_{t+1} V_{t+1}^{tr}(s')\} \quad (9)$$

*subject to* (8)

where  $s' = (a', x, z)$

*If worker* :

$$V_t(s) = \max_{h, a'} \{u(c, 1 - h) + \beta \psi_{t+1} E_{z'} [\max \{V_{t+1}^{tr}(s'), V_{t+1}(s')\}]\} \quad (10)$$

*subject to* (5), (6) and (7).

where  $s' = (a', x', z')$  for  $t \leq T_r$  and  $s' = (a', x, z)$  otherwise.

Suppose  $A, X \subset R_+$  and  $Z \subset R$ , are the sets of possible values that  $a$ ,  $x$  and  $z$  can take, so that we can define the state space as  $S = A \times X \times Z$ . Let  $g_t : S \rightarrow R_+$  and  $\varrho_t : S \rightarrow R_+$  be the policy functions associated with  $a'$  and consumption, respectively, in the dynamic programs (9) and (10), and  $n_t : S \rightarrow [0, 1]$  be the decision rule associated with  $h$  in (10). Finally, let  $\varphi_t : S \rightarrow \{0, 1\}$  be the decision rule of retirement, which is defined as following:

$$\varphi_t(s) = \begin{cases} 1 & \text{if } V_t^{tr}(s) > V_t(s) \\ 0 & \text{otherwise} \end{cases}$$

### 2.6.1 Recursive competitive equilibrium

At each point of time, agents are heterogeneous in regard to age  $t$  and to state  $s \in S$ . The agents' distribution at age  $t$  among the states  $s$  is represented by a measure of probability  $\lambda_t$  defined on subsets of the state space  $S$ . Let  $(S, \Omega(S), \lambda_t)$  be a space of probability, where  $\Omega(S)$  is the Borel  $\sigma$ -algebra on  $S$ . Thus, for each  $\omega \subset \Omega(S)$ , we have that  $\lambda_t(\omega)$  denotes the agents' fraction at age  $t$  that are in  $\omega$ . However, for  $t \geq T_r$  an individual can be in the

workforce or in retirement. Let  $\lambda_t^w(\omega)$  denote the agents' fraction at age  $t$  in the workforce and  $\lambda_t^r(\omega)$  the agents' fraction at age  $t$  in the retirement, so that  $\lambda_t(\omega) = \lambda_t^w(\omega) + \lambda_t^r(\omega)$ . The transition from age  $t$  to age  $t + 1$  for individuals that are in the workforce is governed by the transition function  $Q_t(s, \omega)$ , which depends on the decision rule  $g_t(s)$  of assets and on the realization of the idiosyncratic productivity shock  $z$ . The function  $Q_t(s, \omega)$  gives the probability of an agent at age  $t$  and state  $s$  to transit to the set  $\omega$  at age  $t + 1$ . On the other hand, the transition of retired individuals is not stochastic and is just governed by  $g_t(s)$ . A recursive competitive equilibrium for this economy is defined as following:

**Definition 1** *Given policy parameters  $\{\tau, \theta_1, \theta_2, \theta_3, y_1, y_2, y \max, T_r, T_r^n\}$ , a recursive competitive equilibrium for this economy is given by  $\{V_t^r(s), V_t(s), g_t(s), n_t(s), b(t_r, x), w, r, K, N, \xi, \phi, \lambda_t\}$  such that:*

- 1)  $g_t(s)$ ,  $n_t(s)$  and  $\varphi_t(s)$  solve the dynamic problems(9) and (10);
- 2) The individual and aggregate behaviors are consistent, that is:

$$\begin{aligned}\tilde{K} &= \sum_{t=1}^T \mu_t \int_S g_t(s) d\lambda_t \\ N &= \sum_{t=1}^T \mu_t \int_S n_t(s) e(z, t) d\lambda_t^w\end{aligned}$$

- 3)  $\{w, r\}$  are such that they satisfy the optimum conditions (1) and (2);
- 4) The final good market clears:

$$\sum_{t=1}^T \mu_t \int_S \{\varrho_t(s) + [(1 + g_A)g_t(s) - (1 - \delta)g_{t-1}(s)]\} = B\tilde{K}^\alpha N^{1-\alpha}$$

- 5) Given the decision rule  $g_t(s)$ ,  $\lambda_t^w(\omega)$  satisfies the following law of motion:

$$\begin{aligned}
\text{if } \varphi_{t+1}(\omega) &= 0 \\
\lambda_{t+1}^w(\omega) &= \int_S Q_t(s, \omega) d\lambda_t^w \quad \forall \omega \in \Omega(S) \\
\text{if } \varphi_{t+1}(\omega) &= 1 \\
\lambda_{t+1}^r(\omega) &= \int_S Q_t(s, \omega) d\lambda_t^r \quad \forall \omega \in \Omega(S)
\end{aligned}$$

6) *The distribution of accidental bequests is given by:*

$$\xi = \sum_{t=1}^T \mu_t \int_S (1 - \psi_{t+1}) g_t(s) d\lambda_t$$

7) *Given that  $x$  follows the law of motion (6),  $b_t(t_r, x)$  satisfies (7);*

8)  *$\phi$  is such that it balances the government's budget::*

$$\phi = \sum_{t=1}^T \mu_t \int_S \tau w n_t(s) e(z, t) d\lambda_t^w - \sum_{t=T_r}^T \mu_t \int_S b_t(t_r, x) d\lambda_t^r$$

### 3 Data and calibration

In this section, we describe the data used to calculate the model and the calibration procedures<sup>5</sup>. Initially, the model is calibrated taking into account 1950 data, which is set as a benchmark. After this, we introduce into the model the changes observed in the economic environment between 1950 and 2000 and investigate whether or not our model is able to replicate the main retirement facts. Finally, we isolate the effect of the social security, of aging population, and of the individual productivity profile and investigate the relative importance of each of these factors to the changes in retirement behavior in the period.

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<sup>5</sup>The standard calibration procedure of overlapping generations models can be found in Auerbach and Kotlikoff (1987) and in Rios-Rull (1996), which we follow here.

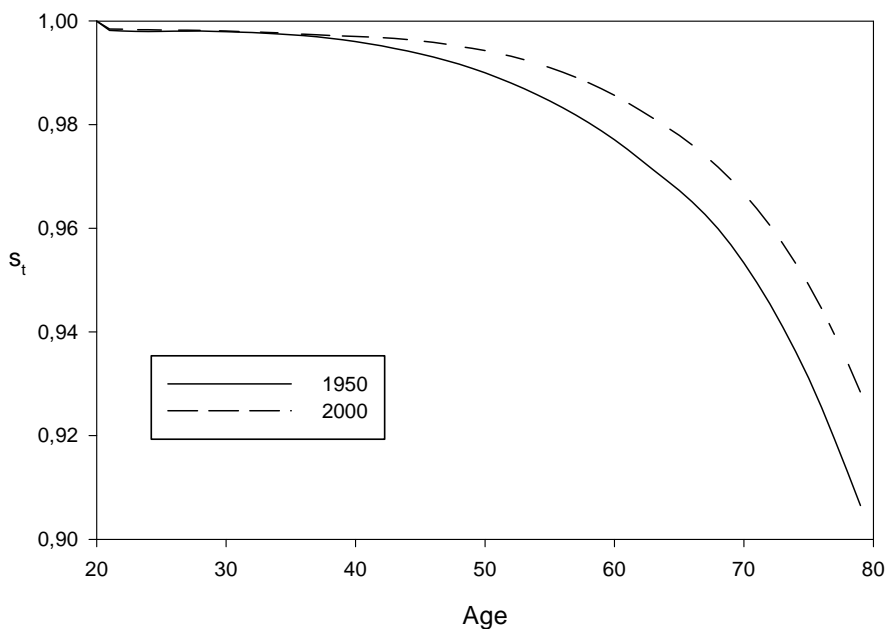
### 3.1 Demography

The population age profile  $\{\mu_t\}_{t=1}^T$  depends on the population growth rate  $g_n$ , on the survival probabilities  $s_t$  and on the maximum age  $T$  that an agent can live. In this economy, a period corresponds to one year and an agent can live 61 years, so that  $T = 61$ . Additionally, we assumed that an individual is born with 20 years old, so that the real maximum age is 80 years old.

Given the survival probabilities, the population growth rate in 1950 and in 2000 is chosen so that the age distribution in the model replicates the dependency ratio observed in the data. Thus, we set  $g_n = 0.0125$  for 1950 and  $g_n = 0.0105$  for 2000. These values generate dependency ratios of 12.13% and 17.27%, respectively.

Data on survival probability were extracted from Bell and Miller (2005). As Figure 1 suggests, life expectancy increased from 1950 to 2000, as the survival probability profile shifted up and to the right in the period. In 1950, for example, life expectancy for an individual at age 20 was roughly 49 years old, while in 2000 it rose to 54 years old and for an individual at age 50 the life expectancy rose from 72 to 77 years old in the same period.

Figura 1: Survival Probability





### 3.2 Preferences and technology

The values of the parameters related with the individual preferences  $(\beta, \gamma, \rho)$  are summarized in Table 1. The value of the relative risk aversion parameter  $\gamma$  follows the estimates of the microeconomic studies revised by Auerbach and Kotlikoff (1987). The values supported by the empirical evidence are within the range  $[1, 10]$ . In this study, we follow Auerbach and Kotlikoff (1987) and used  $\gamma = 4$ .

In representative agent models, given the capital income share and the depreciation rate, there is a one to one relationship between the parameter  $\rho$  and the fraction of time that individuals spend working in the stationary state. In overlapping generations models, however, such relation is more complicated because of heterogeneity among agents. In this case, the procedure used to choose  $\rho$  is such that the average fraction of time that individuals in our model spend working is consistent with the empirical evidence, which suggests a value near 33%.<sup>6</sup>

Table 1: Preferences and technological parameters

$\tilde{\beta}$	$\gamma$	$\rho$	$B$	$\alpha$	$\delta$	$g_A$
1.003	4.00	0.61	0.90	0.36	0.056	0.02

In our model, since there is technological progress, the discount factor is given by  $\beta = \tilde{\beta}(1+g_A)^{(1-\rho)(1-\gamma)}$ . Given  $g_A$ ,  $\rho$  and  $\gamma$  the parameter  $\tilde{\beta}$  is calibrated so that the capital-output ratio in the benchmark economy is equal to 3.

The values of technological parameters  $(B, \alpha, \delta)$  are also summarized in Table 1. We chose a value for  $\alpha$  based on U.S. time series data from the National Income and Product Accounts (NIPA).

The depreciation rate is given by:

$$\delta = \frac{I/Y}{K/Y} - g_A - n - ng_A$$

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<sup>6</sup>See, for instance, Juster and Stafford (1991).

We set the investment-product ratio  $I/Y$  equal to 0.26 and the capital-product ratio  $K/Y$  equal to 3.0. The productivity growth rate  $g_A$  is constant and consistent with the average growth rate of GDP per capita over the second half of the last century. Based on data from Penn-World Table, we set  $g_A$  equal to 2.00%. Thus, the equation above yields a  $\delta$  consistent with table 1.

Rios-Rull (1999) normalizes the value of parameter  $B$ , which measures the total factor productivity, in 1. In this paper, we follow Huggett (1996) so that we chose  $B$  to normalize the wage rate  $w$  in the benchmark economy. Thus, given a capital-product ratio of 3.0 and  $\alpha = 0.36$ , the value of  $B$  such that  $w = 1$  is 0.9.

### 3.3 Individual productivity

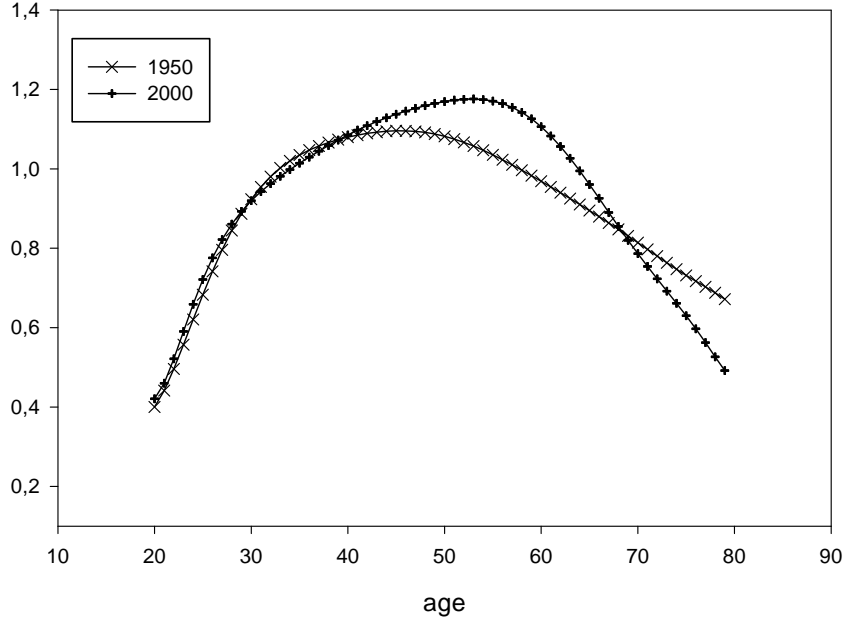
Each agent in this economy is endowed with an individual productivity level  $e(z_t, t) = \exp(z_t + \bar{y}_t)$ , where  $\bar{y}_t$  denotes the permanent component without risk that depends on age and  $z_t$  denotes a temporary component, which follows a first order auto-regressive process with parameters  $(\pi, \sigma_\varepsilon^2)$ . Several authors have estimated similar stochastic processes for labor productivity.<sup>7</sup> Controlling for the presence of measurement errors and/or effects of some observable characteristics as education and age, the literature provides a range of  $[0.88, 0.96]$  for  $\pi$  and of  $[0.12, 0.25]$  for  $\sigma_\varepsilon$ . In this article, we followed the estimates of Flodén and Lindé (2001) and set  $\pi$  and  $\sigma_\varepsilon^2$  to be equal to 0.91 and 0.0426, respectively.

The values for  $\bar{y}_t$  are constructed following Huggett (1996). We utilize data from Current Population Reports on median earnings of full-time workers for each cohort. We have divided these values by the total median earnings and, then, interpolated to get the individual productivity component by age  $\bar{y}_t$ . In Figure 3, we show the age-efficiency profile that is utilized in our calculation for 1950 and for 2000. The pattern of change between 1950 and 2000 shown in the figure is consistent with the empirical evidence provided by Heckman *et. al.* (2003) who show that the efficient indexes for old workers are smaller in 1990 than in 1950.

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<sup>7</sup>A revision of this literature can be found in Atkinson *et. al.* (1992).

Figure 2: Individual Productivity by age



For computational reasons, we have approximated the  $AR(1)$  process which describes the idiosyncratic productivity shock  $z$  by a finite Markov chain. First, we discretized the state space  $Z$  using a grid of 13 points equally spaced in the interval  $[-3\sigma_z, 3\sigma_z]$ , where  $\sigma_z$  denotes the unconditional standard deviation of  $z$ , that is,  $\sigma_\varepsilon/\sqrt{(1-\pi^2)}$ . The transition probabilities are computed using the algorithm described in Tauchen (1986). After calculating the matrix of stochastic transition among the states in  $Z$ , we calculated the invariant distribution associated with this matrix and, then, took this result to describe the agent initial distribution in the economy.

### 3.4 Social security

The social security system in our economy is modeled so that it takes into consideration some important characteristics of the U.S. Social Security System, such as the dependence on retirement benefits to lifetime earnings.

In 1950, the earliest age at which a person could receive Social Security retirement benefits

was 65 so we set  $T_r$  equal to 45 in the benchmark economy. After 1961, however, age 62 was adopted as an early retirement age, with reduced benefits. In our context, this implies that  $T_r = 42$  for 2000. The normal retirement age is the age at which a person may first become entitled to unreduced retirement benefits. This age was 65 in 1950 and in 2000, so we have that  $T_r^n = 45$  for both years.<sup>8</sup>

If individuals retire between 62 and 65 years old, their benefits are reduced by a formula that takes into account the remaining time to reach the normal retirement age. Thus, according to the Social Security Supplement (2001), if individuals retire at age 62, 63 or 64 they will receive 80%, 86.7% and 93.3% of the full retirement benefit, respectively. On the other hand, social security benefits are increased by a percentage if individuals delay their retirement beyond normal retirement age. This delayed retirement credit was instituted in 1972 to provide a bonus to compensate for each year past age 65 that a person delays receiving benefits, until age 70. Hence,  $g_d$  is equal to zero in our economy in 1950. For 2000, we set  $g_d$  equal to 0.05, which is the delayed retirement credit for those who reached age 65 in 1997-1998.

In the United States the old-age benefit payable to the worker upon retirement at full retirement age is called the primary insurance amount (PIA). The PIA is derived from the worker's annual taxable earnings, averaged over a period that encompasses most of the worker's adult years. Until the late 1970s, the average monthly wage (AMW) was the earnings measure generally used. For workers first eligible for benefits after 1978, average indexed monthly earnings (AIME) have replaced the AMW as the usually applicable earnings measure. In our context, both AMW and AIME are given by (6).

The function  $b_t(t_r, x)$  replicates the formula used to calculate the PIA. The complete parameterization of that function requires the specification of values for the parameters  $\{\theta_1, \theta_2, \theta_3, y_1, y_2, y_{\max}\}$ . The values used for each one of those parameters are presented in table 2. The parameters  $(y_1, y_2)$  correspond to the bend points applied in the formula of calculation of the PIA, while  $(\theta_1, \theta_2, \theta_3)$  determine the replacement rate applied in each one of the intervals defined by the bend points. For 1950 we used the bend points applied

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<sup>8</sup>The normal retirement age will increase gradually to 67 for persons reaching that age in 2027 or later, beginning with an increase to 65 years and 2 months for persons reaching age 65 in 2003.

to calculate the PIA from creditable earnings after 1936 according to the Social Security Bulletin (2001). In this case, the PIA corresponds to 40% of first \$50 of AMW plus 10% of next \$200 of AMW. We multiplied these values by 12, adapting to the annual base of the model and then we normalized the result by dividing by the average annual wage.

Table 2: Benefit function parameters

	1950	2000
$y_1$	0.23	0.19
$y_2$	-	1.17
$y_{\max}$	1.13	2.34
$\theta_1$	0.40	0.90
$\theta_2$	-	0.32
$\theta_3$	0.10	0.15

We followed similar procedure for 2000. The values in this case correspond to those applied in the calculation of the PIA for workers who were first eligible in 1979 or later according to Social Security Bulletin (2001). In 2000, the PIA equaled 90% of first \$531 of AIME, 32% of next \$2671 and 15% of AIME over 3202. We, again, divide these values by the average annual wage.<sup>9</sup>

Figures 3a and 3b plot the benefit function obtained for 1950 and for 2000, respectively. The horizontal axe corresponds to the average past earnings  $x$  and the vertical axe corresponds to the benefit. We have normalized both figures so that the average earnings in the economy,  $ym$ , is set equal to one. Thus, for example, if an individual has  $x$  exactly equal to  $ym$ , his benefit would be equal to 17% of the corresponding value in 1950. In contrast, his benefit would be 42% of  $ym$  in 2000. Hence, it is immediate to see from Figures 3a and 3b that benefits have become much more generous between 1950 and 2000.

Remember that  $y_{max}$  corresponds to the level of earnings above which earnings in So-

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<sup>9</sup>According to the Social Security Bulletin (2001), the average annual wage in 2000 was \$36564 and in 1950 was \$2654.

cial Security covered employment is neither taxable nor creditable for benefit computation purposes. In 1950, the maximum taxable annual earnings was \$3000, while in 2000 it was \$76200. We, then, divided these values by the average annual wage for both years in order to obtain  $y_{max} = \{1.13, 2.34\}$ , respectively.

Figura 3a: Benefit function in 1950

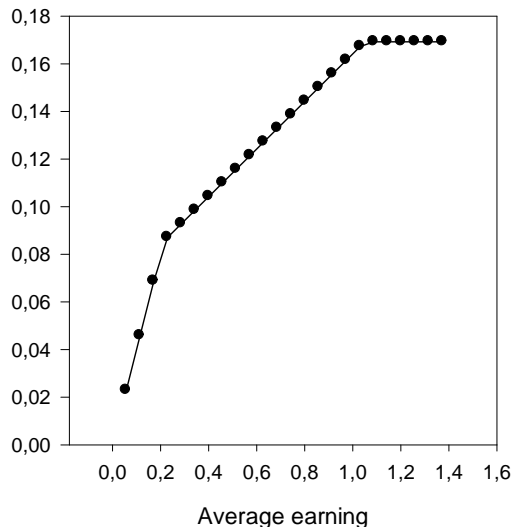
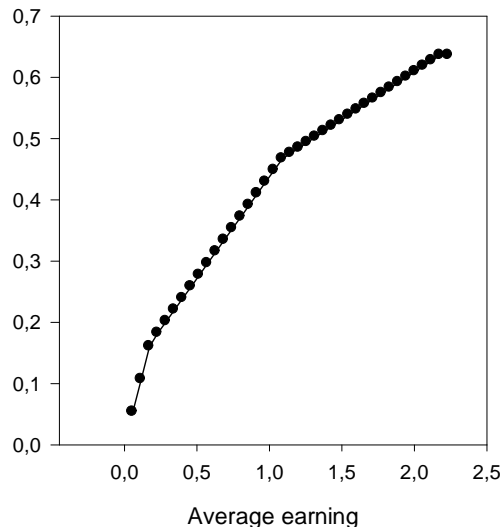


Figura 3b: Benefit function in 2000



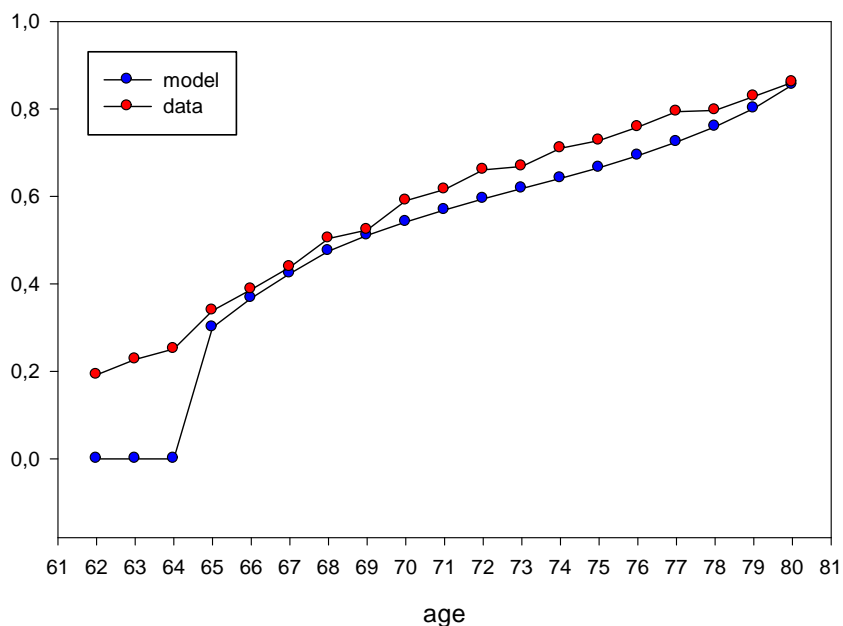
Finally, remember that the parameter  $\tau$  denotes the contribution from workers to the social security system. In 1950, American workers covered by the social security system contributed with 3.0% of their wages for Old-Age and Survivors Insurance (OASI), which pays monthly cash benefits to retired worker (old-age) beneficiaries, while in 2000 that contribution was 10.6%. Thus, we set  $\tau = 0.03$  for 1950 and  $\tau = 0.106$  for 2000.

## 4 Results

The retirement rate by age in the model,  $\lambda_t^r$ , is given by the measure of agents at age  $t$  that are out of the labor force  $\lambda_t^r$ . In Figure 4, we display the retirement rate generated by the model for the benchmark case and the retirement profile observed in the U.S. economy in 1950. In the last case, data on the status of labor force from IPUMS were used. For each age, we have divided the fraction of people who are out of the labor force by the fraction of those

who are in the labor force, leaving aside those who never participated of the labor force.<sup>10</sup> Especially for the individuals aged 65 and over the model is able to reproduce closely the retirement profile by age in 1950. In this year roughly 80% of workers older than 64 years had already left the labor force, hence the model gets a very good approximation of the overall retirement behavior of the American population in 1950.

Figure 4: Retirement rate by age for 1950



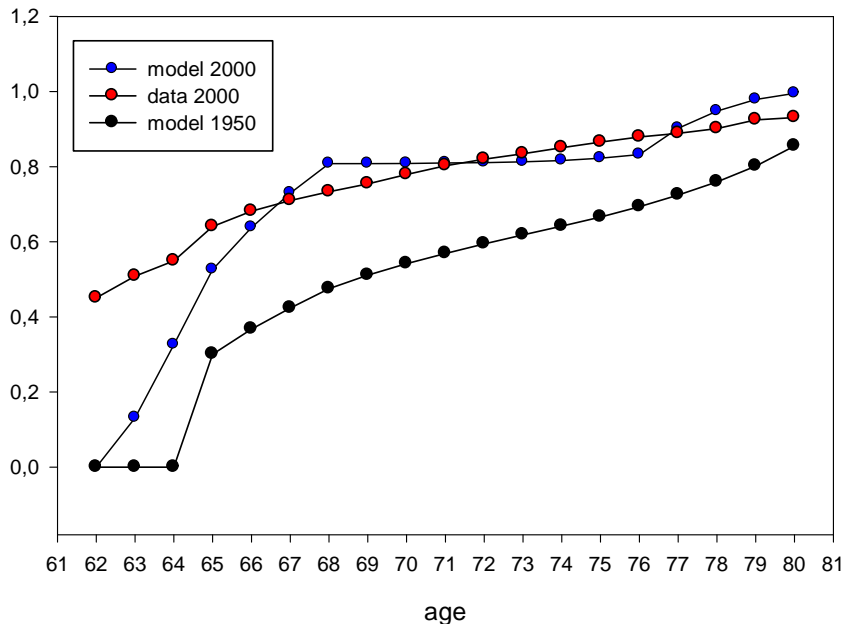
In order to investigate how well the model explains the changes in retirement between 1950 and 2000, we introduced into the model the data for 2000, as described in the last section. Figure 5 presents the retirement profile generated by the model and the retirement profile observed in the data, and we also display the simulated profile of 1950 for comparative purposes. The model is also able to match the retirement behavior for individuals aged 65 and over in 2000, and it is clear that the simulations capture the increase in retirement rate by age observed in the second half of the last century.

<sup>10</sup>This calculation is similar to that used in Kopecky (2006).

Note that the only differences between the 1950 and 2000 economies are the changes in the experience profile, changes in the demographic composition of population and the modifications in the parameters relative to the social security system. As there is very little left to be explained according to Figure 5, simulation results suggest that the changes in these variables account for almost all the observed change in retirement behavior over the period.

Nevertheless the model does not have a good performance in explaining the retirement behavior for ages 62-64. A possible reason is that we have not taken in consideration the heterogeneity of health conditions among individuals. Rust and Phelan (1997) show that individuals in bad health are roughly twice as likely to receive Social Security at 62 as 65.<sup>11</sup> These individuals have a higher disutility of work than those in good health. Thus, if there is market incompleteness, then the former will leave the labor force at the earliest age wherein they are entitled to receive retirement benefits. As we have homogeneity in regards to health condition at a given age, we are not able to capture this. Apart from this, the model is able to reproduce very closely retirement behavior in 1950 and 2000.

Figure 5: Retirement rate by age for 2000



<sup>11</sup>Those in good health are approximately twice as likely to receive benefits at 65 rather than 62



In Figure 6, we display the simulated labor profiles by age for the benchmark case and for 2000. The model is also able to reproduce another stylized fact regarding labor decision, which is the fact that older workers are working less. McGrattan and Rogerson (1998) shows that work hours of people aged 65-74 and 75-84 have fallen about 57% and 70%, respectively, over the second part of the last century. In our simulations, the fraction of time that workers aged 65-74 spend working is about 54% smaller in 2000 than in 1950, while for workers aged 75-80 that fraction decreased 73% in the same period.

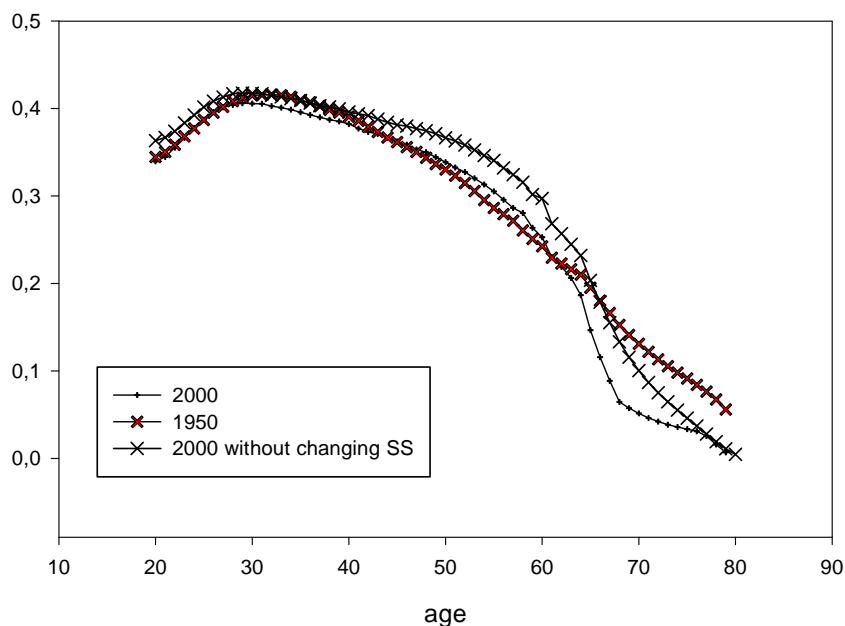
Feldstein (1974) argues that these drops in hours worked of older people could be explained by changes in social security benefits. To investigate the effect of social security on the labor supply, we also show in Figure 6 the result of a counterfactual exercise in which we maintain constant the parameters relative to the social security, but change everything else to their 2000 values. In this case, hours worked fall about 20% in the case of workers aged 65-74 and 68% for those aged 75-80. Thus, the model suggests that social security accounts for about 67% of the reduction in hours for workers aged 65-74 and about 10% for workers aged 75-80.

Moreover, the model suggests that the increase in social security benefits reduces the labor supply not only for the elderly, but over the whole working life. In fact, social security affects the labor supply decision through the payroll tax and the level of benefits at retirement. When the latter becomes less generous, workers need to work more intensively at young ages in order to provide consumption at old age.<sup>12</sup>

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<sup>12</sup>The econometric evidence on the effect of social security on labor supply is inconclusive. For example, Hurd and Boskin (1984), Burtless (1986) have found negative relationship, while Krueger and Pischke (1992) have found no effect of social security on labor supply.

Figure 6: Labor profile generated by the model

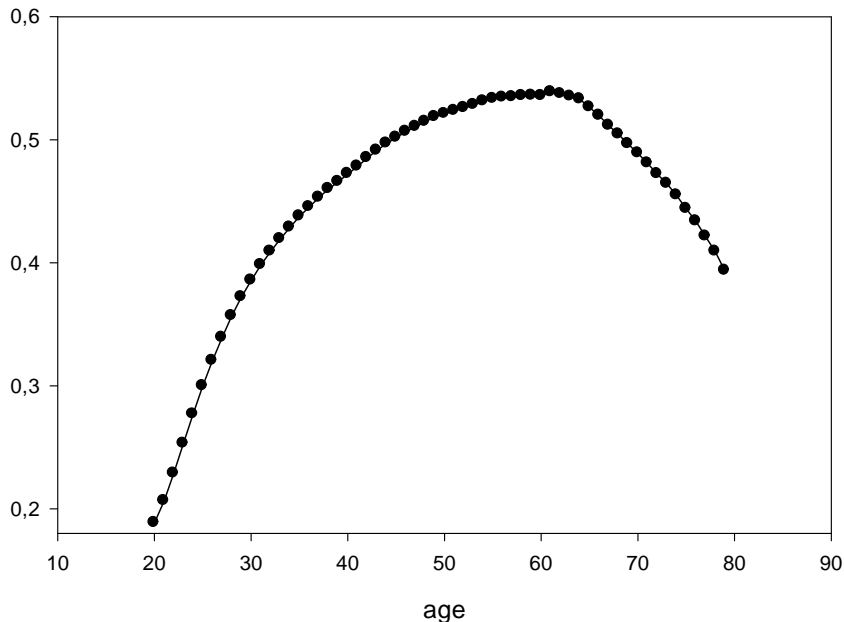


Although the aggregate labor profile in Figure 6 is continuous, the individual labor profile generated by the model presents a discontinuity when individuals leave the labor force. In fact, one important feature of retirement is that workers make discontinuous transitions from full time work to not working at all. In order to reproduce this feature some authors have assumed that the agents in the economy supply labor indivisibly to the market while working.<sup>13</sup> We have instead treated hours of work as a continuous choice variable. Even so, we were able to reproduce the discontinuous transitions from full time work to not working through the discontinuous decision rule for retirement, which was described in subsection 2.6. In this case, agents decide whether or not to leave the labor force at age  $t$  based on which choice generates more utility for them. Hence, if the decision to retire at age  $t$  yields more utility than the decision to stay in the labor force, given the state  $s$ , workers will leave the labor force and offer zero hours of work.

<sup>13</sup>See, for example, Rust and Phelan (1997) and Kopecky (2006).

In Figure 7, we show the average consumption profile generated by the model in the benchmark case. According to evidence from Hurd (1980), among many, there is a drop in consumption at the time of retirement. Nevertheless, basic life-cycle models are not able to replicate this pattern since consumption in these models is smooth or even growing over lifetime.<sup>14</sup> In order to reconcile the empirical evidence with the theory, some authors have argued that it is necessary to introduce into the basic life-cycle model the death risk (e.g., Davies (1981)) or/and an intratemporally non-separable utility (Attanasio and Weber (1993)). Our model includes these two hypotheses and, as a consequence, it is able to replicate the reduction in consumption at the time of retirement.

Figure 7: Average consumption profile - benchmark



#### 4.1 Unraveling the channels to the changes in retirement

In this sub-section we investigate the role and measure the relative importance of the changes in the social security system, in demography and in the individual productivity profile to the changes in the retirement pattern.

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<sup>14</sup>The problem appears when the discount factor is larger than 1 which is possible in models with finite horizon. In this case, the euler equation implies that the substitution rate between consumption tomorrow and consumption today is also larger than 1. As a consequence, consumption is growing throughout the life-cycle.

In Figure 8 we show simulation results for changing one factor each time, keeping everything else constant. In order to analyze the effect of each change, we also show in that figure the retirement profile generated by the model in the benchmark case.

One can see that the changes in the social security system and in the experience profile over the time period under study shift up the retirement rate by age. On the other hand, the changes in demography shift down the retirement rate except for the oldest individuals. For instance, the retirement rate for 70 year old individuals in the benchmark case is 61%. As we change only the parameters of social security, the retirement rate of this group increases to 75%, while in the full simulation it goes to 81%. For the case in which everything is kept constant but the individual productivity profile is changed to its 2000 values, the increase in the retirement rate for this group is a little smaller, 75%. In contrast, retirement rate at age 70 falls to 60% for changes exclusively in demography.

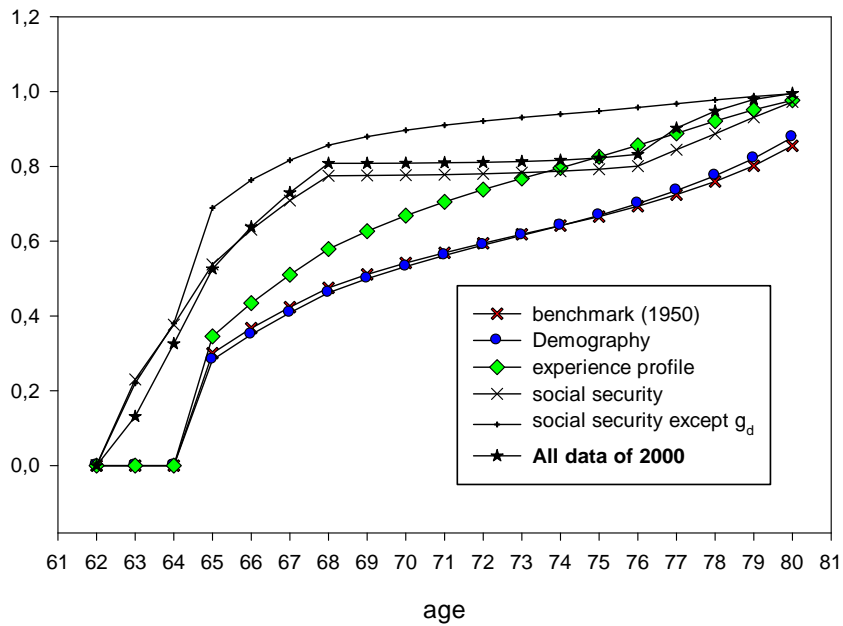
Thus, the model suggests that the changes in government policy with respect to social security and in technology ( that changed experience profiles) over the second part of the last century account for most of the changes in the retirement profile by age.

Kalemlı-Ozcan and Weil (2006) have shown that the fall in mortality increases retirement. The idea is that the decision about labor supply over lifetime is affected by uncertainty in regard to the date of death. If mortality is high, individuals who saved up for retirement would face a high risk of dying before he could enjoy their planned leisure and, as a result, they would plan optimally to work up to the end of their life. As the death risk falls, nevertheless, individuals would plan and save for retirement. According to Figure 8, our model suggests this “uncertainty effect” is small and, in fact, appears only for individuals aged 75 and over. This result is due to the presence of the social security system, which provides insurance against the death risk.

In order to investigate further the effect of the new social security rules on retirement behavior, we also show in Figure 8 the result of a simulation in which only the parameters of social security are changed but the delayed retirement credit on the retirement,  $g_d$ , remained as in 1950 (this is the curve "social security except  $g_d$ " in Figure 8). The model suggests that if the delayed retirement credit had not been raised, the increase in retirement would be significantly larger than it was indeed, as the curve corresponding to this simulation is

everywhere above the full 2000 simulation. In other words, the delayed retirement credit is a powerful policy tool to induce workers to postpone their retirement.

Figure 8: Retirement rate for changing one factor each time



It is well documented that there is a peak in retirement at age 65. Rust and Phelan (1997) suggest that the main reason for this are the rules of social security. In particular, the retirement behavior at age 65 would be strongly influenced by the disincentive to continue in the labor force due to the retirement earning test - the rule that reduces social security benefits of those who have labor earnings above a certain threshold - and by the small incentive to continue working associated with the negligible delayed retirement credit.<sup>15</sup> However, the retirement earning test was abolished in 2000 for those between the full retirement age and 70 years of age and the delayed retirement credit has increased significantly. Our model can be used to investigate the impact of these policy changes in the retirement behavior. Figure 9 shows the distribution by age of applications for social security produced by the model in two cases: the full simulation using 2000 parameters and another using 2000 parameters but leaving the delayed retirement credit unchanged, that is,  $g_d = 0$ .<sup>16</sup> It can be seen that the

<sup>15</sup>Rust and Phelan (1997) have set the delayed retirement credit equal to 1%.

<sup>16</sup>Notice that we have not taken into account the retirement earning test. Gustman and Steinmeier (2004) have shown that the abolition of that test for ages between 65-70 has increased the full time work.

increase in the delayed retirement credit reduces significantly the peak in retirement at age 65. The model estimates that almost 40% of the applications would occur at age 65 with  $g_d = 0$  as opposed to less than 20% with the new rules.<sup>17</sup>

Figure 9: Distribution of ages of application

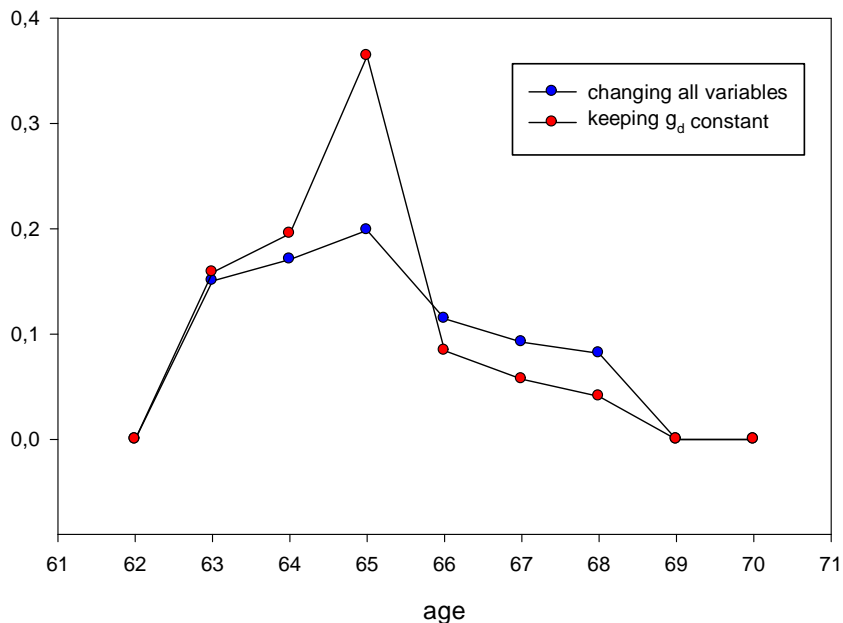


Table 3 displays further results on the effects of the changes in social security legislation, demography and age-efficiency profile upon the aggregate retirement behavior and on the benefits paid-output ratio. The first column shows which factor was modified in the simulation. The second shows the aggregate retirement rate - the ratio between retired population and total population - and the third column the total benefits paid-output ratio - social security spending as a share of GDP. Finally, the fourth column presents the sensibility of the total benefits paid-output ratio to the variations in the retirement rate.

Results in the table show that the changes in social security are the most important source of changes in aggregate retirement rate, following by changes in demography and in the age-efficiency profile, respectively. In fact, when only the parameters of the social security are modified, aggregate retirement rate expands to 8.84%, accounting for 45% of the increase in the full simulation, 12.26%. The aggregate retirement rate goes to 8.23%

<sup>17</sup>The former result is close to that observed in a sample of individuals in good health conditions used by Rust and Phelan (1997).

in the case in which only demographic parameters are changed and 7.21% when only the age-efficiency profile is modified (36% and 20% of all increase, respectively).

Thus, despite results suggesting that demographic changes have little effect on the retirement decision at a given age, they have a strong impact on the aggregate retirement rate. This is so because aging population increases the concentration of individuals in states in which they are prone to retire.

Note also that the increases in retirement caused by changes in the social security have larger effects on the benefits paid-output ratio than those caused by the other factors. In fact, one percentage point increase in retirement is associated with an expansion of 0.56 percentage point in the benefits paid-output ratio. This variation rate is significantly smaller for changes in demography 0.09 and the age-efficiency profile 0.08.

In the last line, the simulation in which we changed demographic factors and experienced profile, but kept social security at the benchmark calibration, produced an aggregate retirement rate and a benefits paid-output ratio that are, roughly, 18% and 72% smaller, respectively, than in the full simulation. The previous findings allow one to conclude that if social security had not been changed, retirement would still be much higher in 2000 than 1950 (9.95% of the population, as opposed to 5.93%), but social security expenses as a share of output would be much smaller than otherwise (0.87% as opposed to 3.11%).

Variables changed in each Simulation	Retirement rate = $\lambda$ %	Benefit total/output = $b$ %	$\Delta b / \Delta \lambda$
Benchmark (1950)	5.93	0.52	-
All	12.26	3.11	0.41
Parameters of Social Security	8.84	2.16	0.56
Parameters of social security except $g_d$	10.34	2.44	0.43
Experience profile	7.21	0.63	0.08
Demography	8.23	0.72	0.09
Experience profile and demography	9.95	0.87	0.09

Finally, we also show in the table results of a simulation in which all the parameters of social security were changed, except the delayed retirement credit, kept at its benchmark calibration. In this case the retirement rate jumps to 10.34%, and the benefits paid-output ratio to 2.44%. These values are above those of the simulation where all parameters of social security are changed, including  $g_d$ .

Note, however, that the sensibility of the benefits paid-output ratio to changes in retirement is lower in the former (0.43) than in the latter case (0.56). When  $g_d$  remains unchanged, social security spending as a share of output varies less proportionally than the retirement rate.

## 5 Conclusions

In this paper we have studied an stochastic life-cycle economy in which individuals pick optimally the time to leave the labor force. The model mimics relevant features of the American economy and takes special care in the calibration of the social security system. Simulations were able to match very closely the changes in retirement of American men aged 65 and over from 1950 to 2000.

The model suggests that the changes in demography, in technology and in social security may account for the most part of the variation in retirement over the time period under study. Furthermore, even if social security policy had not changed over time, retirement would still be higher, but the benefits paid-output ratio would be significantly smaller. Although the aging population accounts for an important part of the increase in aggregate retirement rate, about 36% in our simulations, it is able to explain only a small part of the increase in the benefits paid-output ratio. In fact, the most important factor behind the sizeable increase in the social security expenses as share of output is the increase in retirement benefits.

## 6 Appendix: Computational details

We first compute the steady state for 1950, our benchmark year. We use backward induction to compute an agent's value functions and policy functions. The process is iterated until



convergence on the transfers of accidental bequest and capital. The algorithm for computing equilibria is as following:

1. Guess values for  $K_0$ ,  $\xi_0$ ,  $N$ ,  $\phi$ .
2. Use the first-order conditions of the profit maximization program of the firm to obtain factor prices. The average income in the economy is then calculated and used to estimate retirement benefits.
3. Solve the dynamic programs of individuals in order to obtain the decision rules for assets, labor supply and retirement.
4. Use these decision rules to iterate on equilibrium condition 4 in order to obtain the age-wealth distribution.
5. Calculate  $K_1$ ,  $\xi_1$ ,  $N$  and  $\phi$ . If  $K_1$  and  $\xi_1$  is approximately equal to  $K_0$  and  $\xi_0$ , respectively, stop. Otherwise, update  $K$  and  $\xi$  and go to step 2.

We set a grid on the asset holdings  $a$ , on the past average earnings  $x$  and on the idiosyncratic shocks  $z$ . The number of grid points is 300, 40 and 13, respectively. The maximum value on the asset holding gridpoint is chosen such that the solution of the individuals' dynamic problem is never biding. Also, the spacing between points on this grid increases with asset level.<sup>18</sup> The points on the past average earnings grid are equally spaced and the maximum taxable income for social security is taken to be the upper limit on this gridpoints.

To calculate the individuals' decision rules, we first use golden section search to solve labor supply as a function of initial and final asset level and, then, given the initial asset level, we iterate the value functions on asset gridpoints in order to find the optimal asset choice. Associated with this optimal asset choice, there is an interval at which the average earnings in next period belongs to. We interpolate the value function on this interval to obtain the final value function.

Finally, given individuals' asset choices and the stochastic transition matrix on  $Z$ , the age wealth distribution is calculated through interaction on equilibrium condition 4.

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<sup>18</sup>The points on the asset holdings grid are given by  $a_i = \frac{a_{\max}}{301^{2.35}} i^{2.35}$ , where  $a_{\max}$  detones the upper limit.

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