

# ***METAGRAPHITI BY STATA***



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# ***METAGRAPHITI***

Statistical Graphics For  
Interpretation, Exploration  
And Presentation Of  
Meta-analysis Data

# ***METAGRAPHITI BY STATA***

## VISUOGRAPHIC FRAMEWORK FOR USING STATA FOR:

- ❑ Testing and correcting for publication bias
- ❑ Investigating heterogeneity
- ❑ Summary of Data and Sensitivity Analyses

# ***METAGRAPHITI***

- ❑ Avoid potential misrepresentation by faulty distributional and other statistical assumptions.
- ❑ Facilitates greater interaction between the researcher and the data by highlighting interesting and unusual aspects of the quantitative data.

# ***METAGRAPHITI***

- ❑ User-friendlier summaries of large, complicated quantitative data sets.
- ❑ Preliminary exploration before definite data synthesis.
- ❑ Effective emphasis of important features rather than details of data.

# CONTINGENCY TABLE FOR EXTRACTION OF DATA

		Target condition (reference test result)		Totals
		Present	Absent	
Index test result	Abnormal	a	b	a+b
	Normal	c	d	c+d
Totals		a+c	b+d	a+b+c+d

Sensitivity =  $a/(a+c)$

Specificity =  $d/(b+d)$

Positive Predictive value =  $a/(a+b)$

Negative predictive value =  $d/(c+d)$

Likelihood ratio abnormal test =  $\text{Sensitivity}/(1-\text{Specificity})$

Likelihood ratio normal test =  $(1-\text{Sensitivity})/\text{Specificity}$

Diagnostic Odds Ratio =  $(a \times d)/(c \times b)$

# DIAGNOSTIC VS. TREATMENT TRIAL

- ❑ **True Positives** = Experimental Group With the Monitored Outcome Present (a).
- ❑ **False Positives** = Control Group With the Outcome Present (b).
- ❑ **False Negatives** = Experimental Group With the Outcome Absent (c).
- ❑ **True Negatives** = Control Group With the Outcome Absent (d).

# DIAGNOSTIC VS. TREATMENT TRIAL

- ❑ The Expression for the Odds Ratio (OR)  $= (a \times d) / (b \times c)$ .
- ❑ Relative risk in experimental group  $\{ [a / (a + c)] / [b / (b + d)] \}$  = Likelihood Ratio for a Positive Test.
- ❑ Relative Risk in Control Group = Likelihood Ratio for a Negative Test.



# EXPLORING PUBLICATION BIAS

- ❑ Published studies do not represent all studies on a specific topic.
- ❑ Trend towards publishing statistically significant ( $p < 0.05$ ) or clinically relevant results.
- ❑ Publication bias assessed by examining asymmetry of funnel plots of estimates of odds ratios vs. precision.

# EXPLORING PUBLICATION BIAS

- Funnel plot
- Begg's rank correlation plot
- Egger's regression plot
- Harbord's modified radial plot

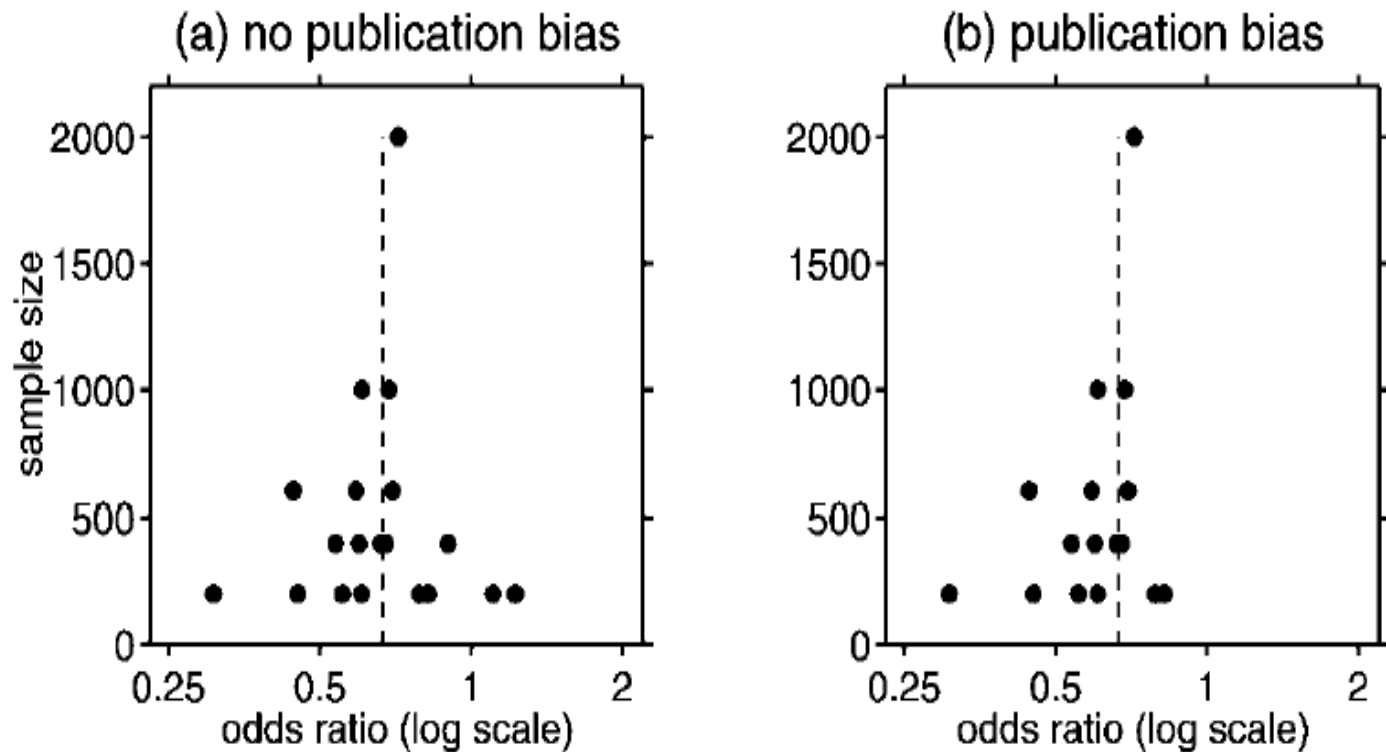
# FUNNEL PLOT

- ❑ A funnel diagram (a.k.a. funnel plot, funnel graph, bias plot):
- ❑ Special type of scatter plot with an estimate of sample size on one axis vs. effect-size estimate on the other axis

# FUNNEL PLOT

- ❑ Based on statistical principle that sampling error decreases as sample size increases
- ❑ Used to search for publication bias and to test whether all studies come from a single population

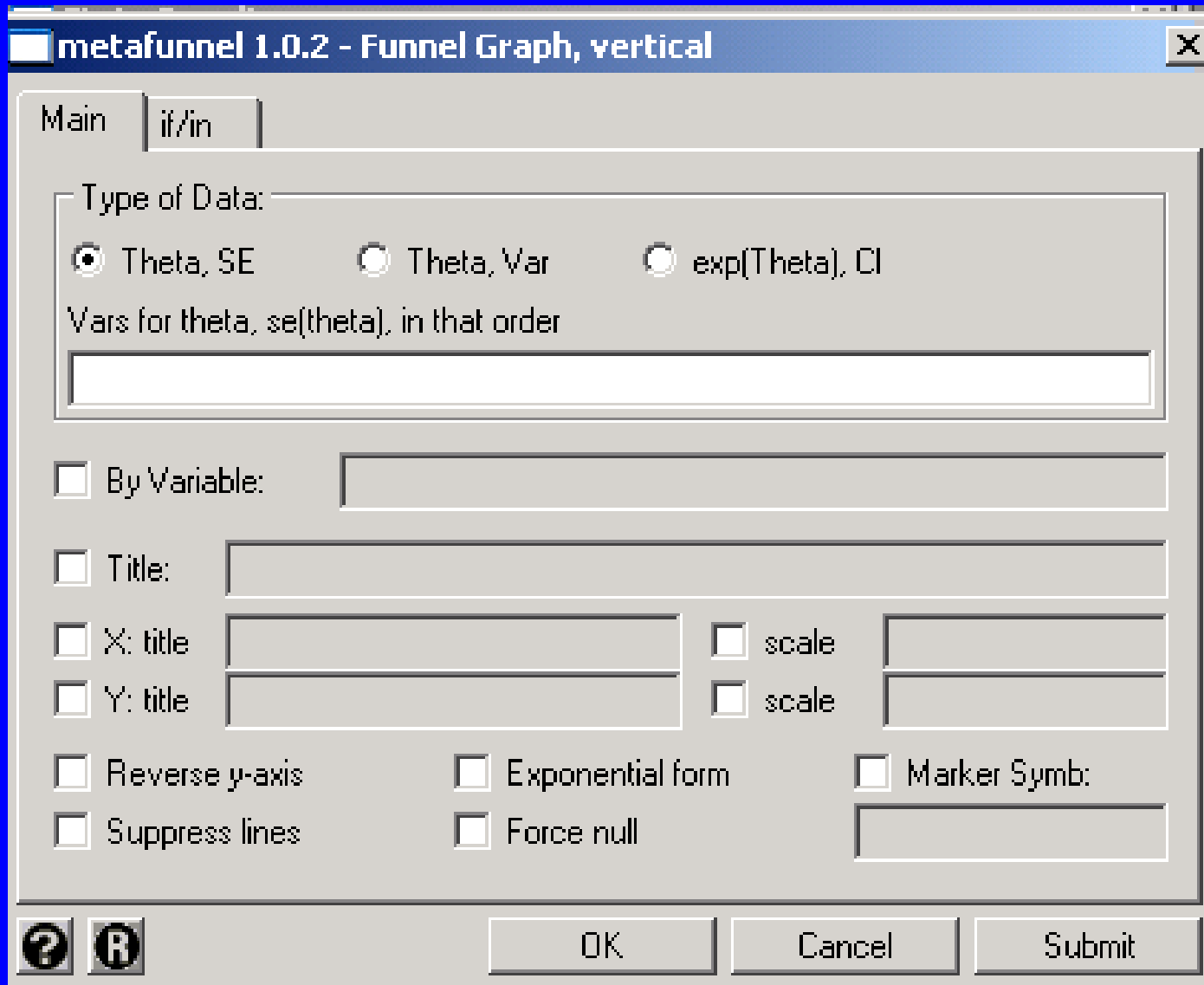
# FUNNEL PLOTS



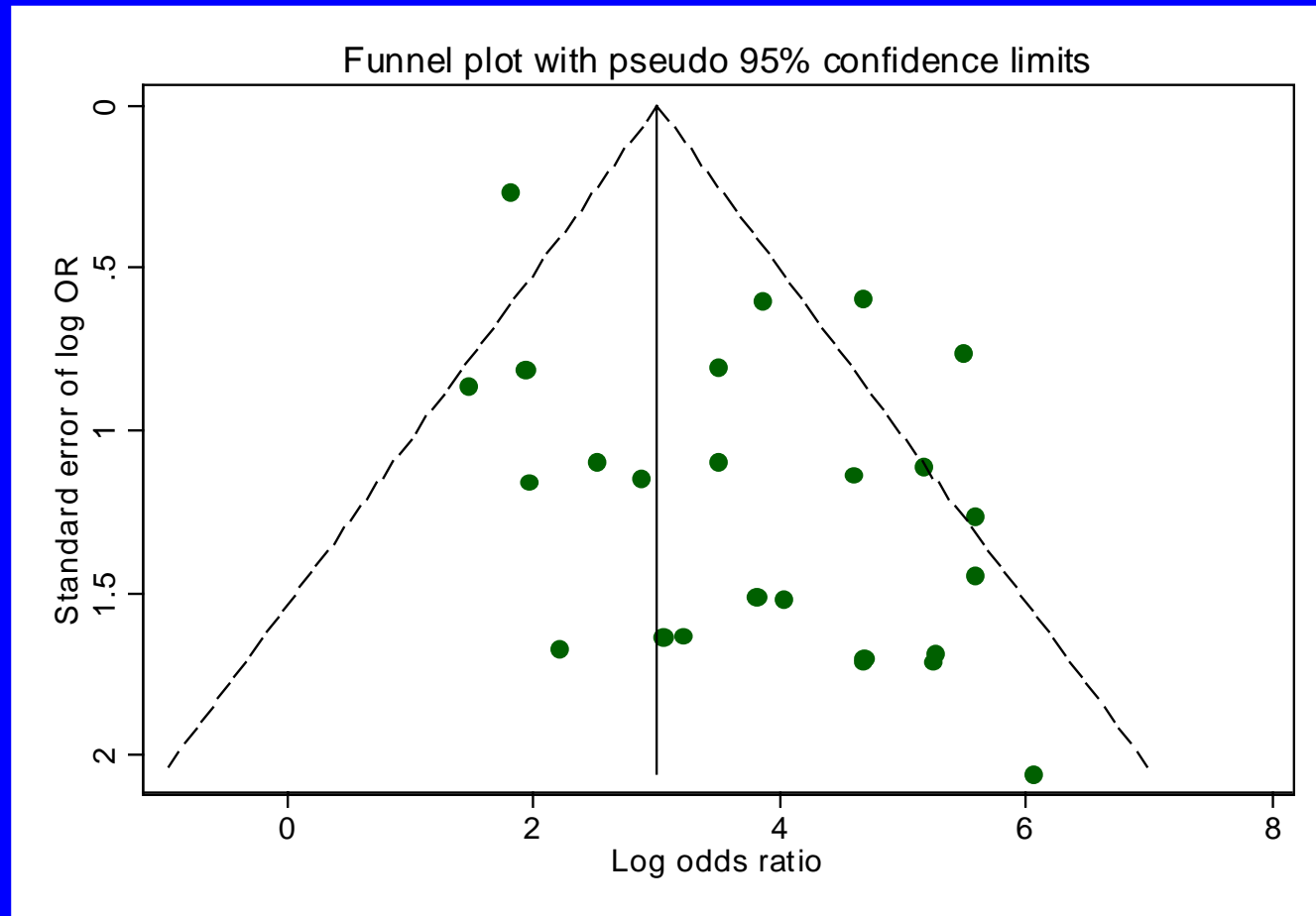
# FUNNEL PLOTS

## STATA SYNTAX/COMMAND

- `metafunnel lдор seldор, xlab(0(2)8) xtitle (Log odds ratio) ytitle(Standard error of log OR) saving(zfunnel, replace)`
- `metafunnel lдор seldор, xlab(0(2)8) xtitle(Log odds ratio) ytitle (Standard error of log OR) egger saving (eggerfunnel, replace)`

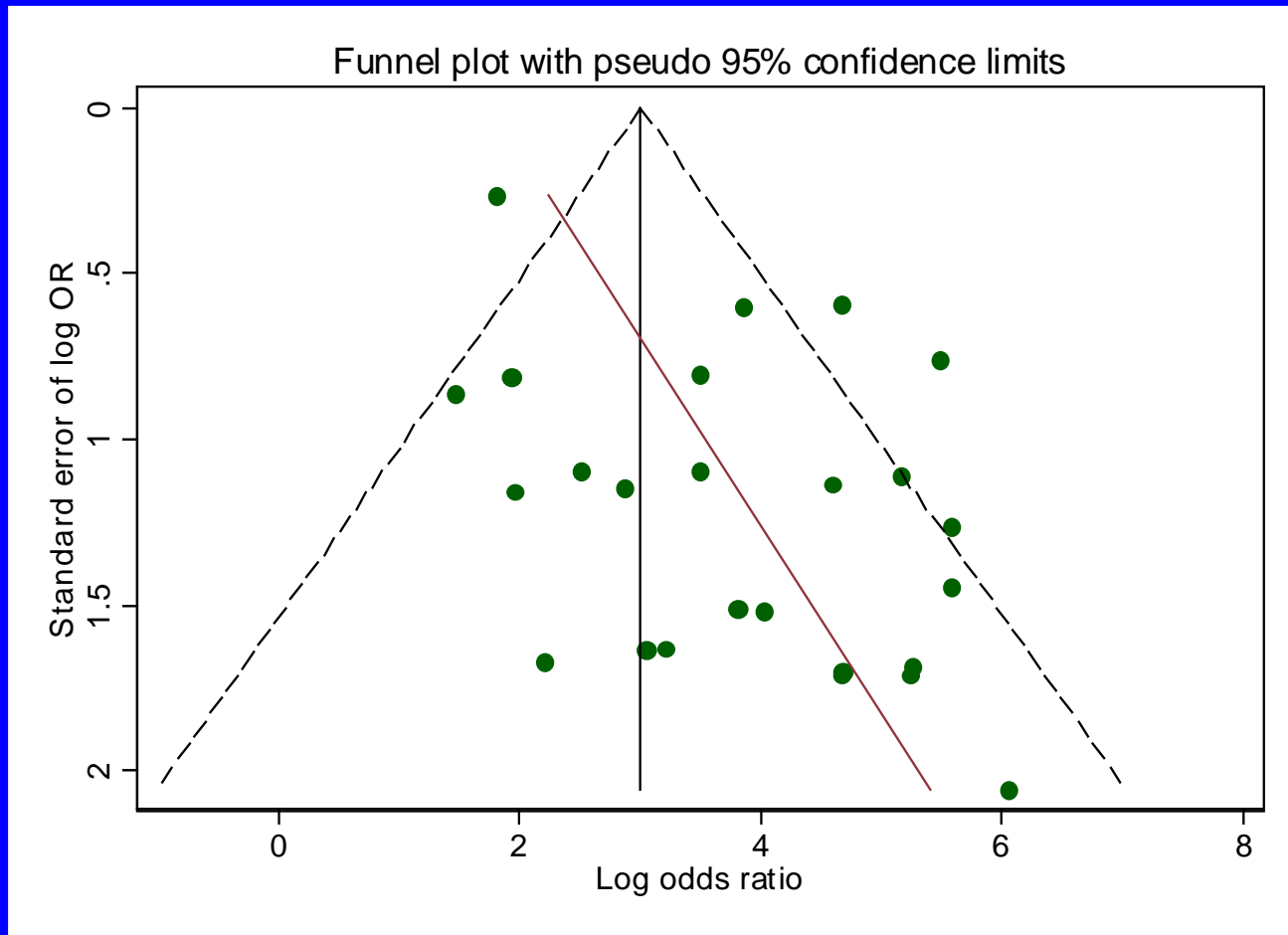


# FUNNEL PLOT





# FUNNEL PLOT



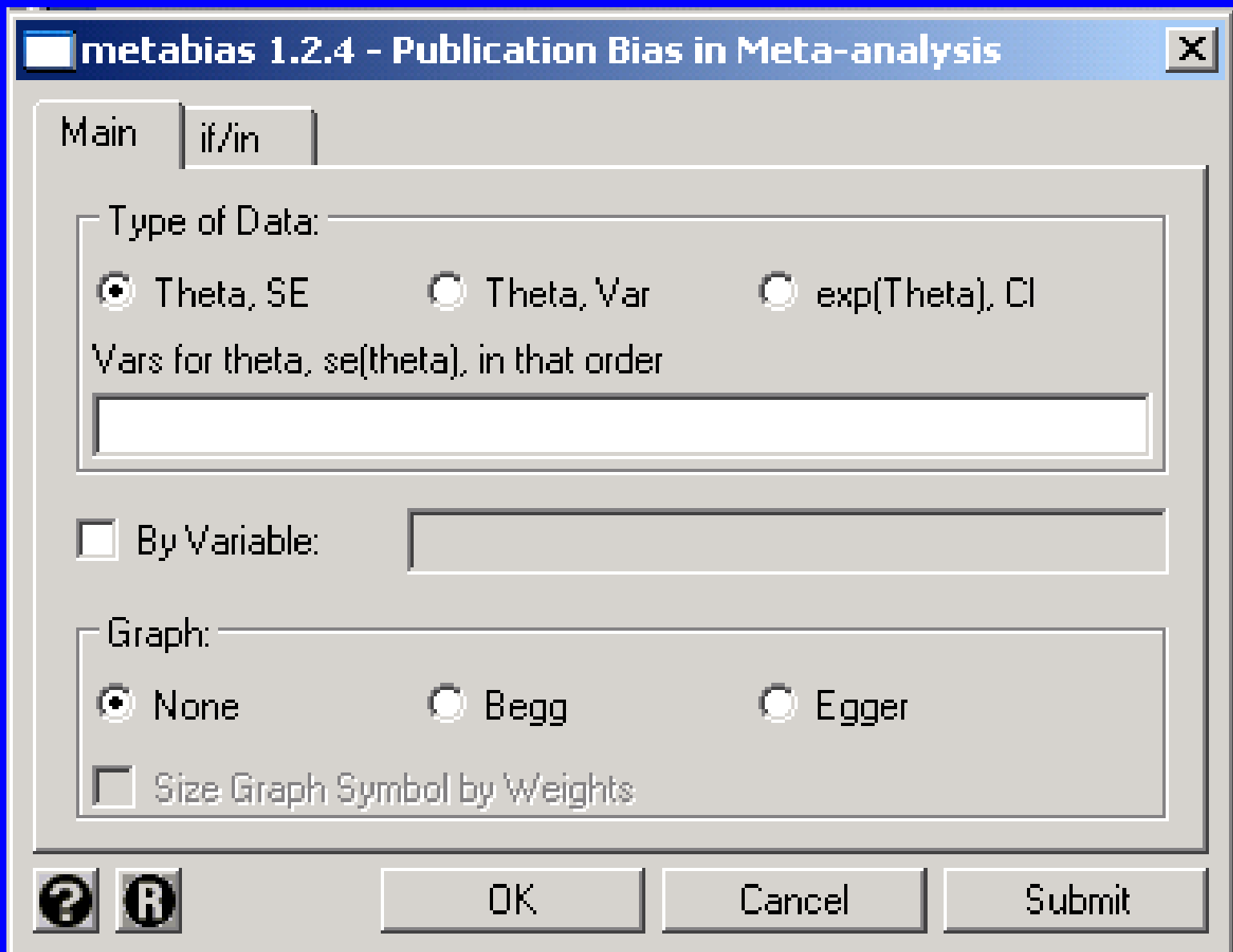
# BEGG'S BIAS TEST

- ❑ An adjusted rank correlation method to assess the correlation between effect estimates and their variances.
- ❑ Deviation of Spearman's rho from zero=estimate of funnel plot asymmetry.
- ❑ Positive values=a trend towards higher levels of effect sizes in studies with smaller sample sizes

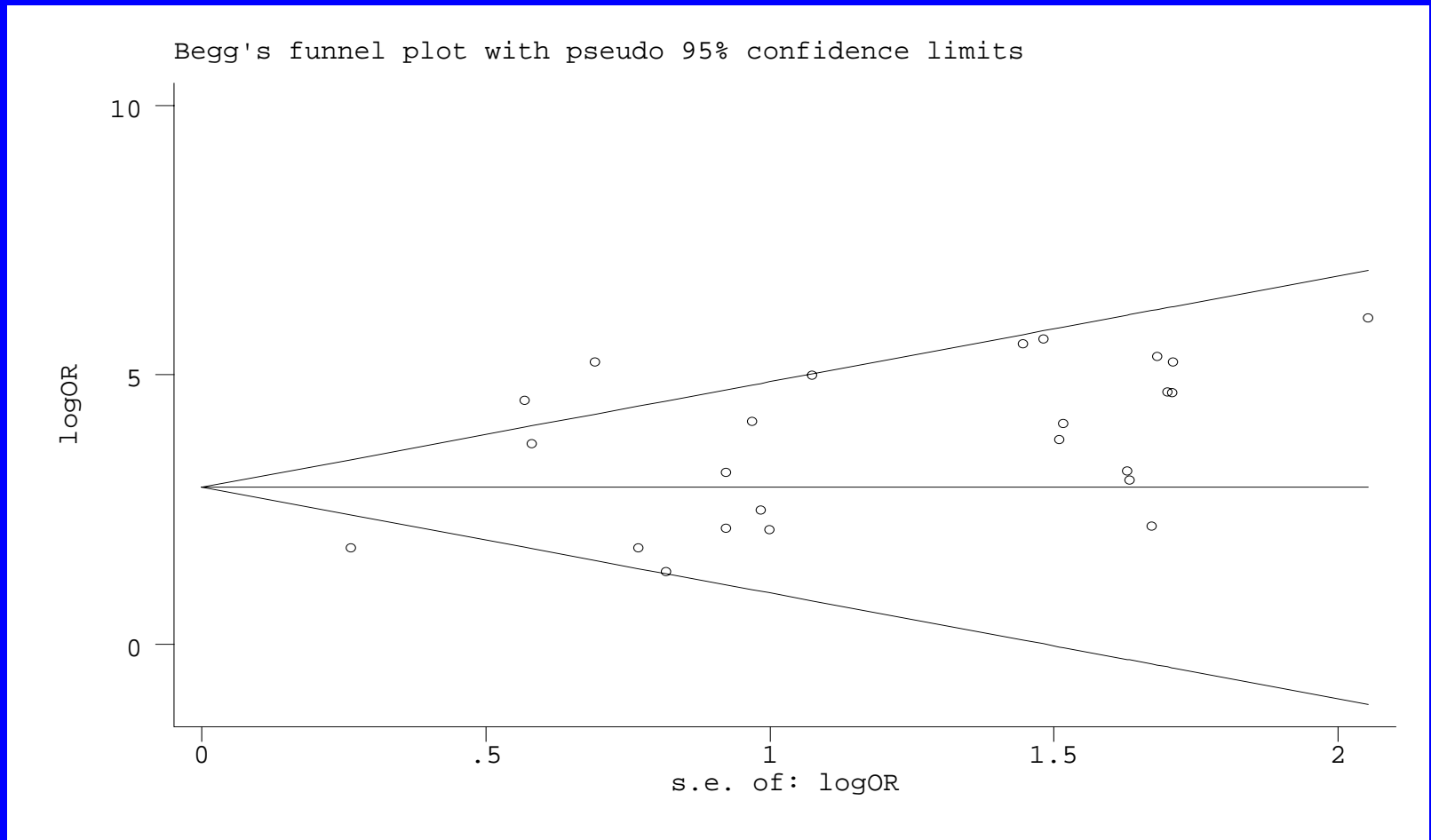
# BEGG'S BIAS TEST

STATA SYNTAX/COMMAND

`metabias LogOR seLogOR,  
graph(b) saving(beggplot,  
replace)`



# BEGG'S BIAS PLOT



# BEGG'S BIAS TEST

adj. Kendall's Score (P-Q) = 26

Std. Dev. of Score = 40.32

Number of Studies = 24

$z = 0.64$

$\text{Pr} > |z| = 0.519$

$z = 0.62$  (continuity corrected)

$\text{Pr} > |z| = 0.535$  (continuity corrected)

# EGGER'S REGRESSION METHOD

- ❑ Assesses potential association b/n effect size and precision.
- ❑ Regression equation:  $SND = A + B \times SE(d)^{-1}$ .  $SND$ =standard normal deviate (effect,  $d$  divided by its standard error  $SE(d)$ );  $A$  =intercept and  $B$ =slope. .

# EGGER'S REGRESSION METHOD

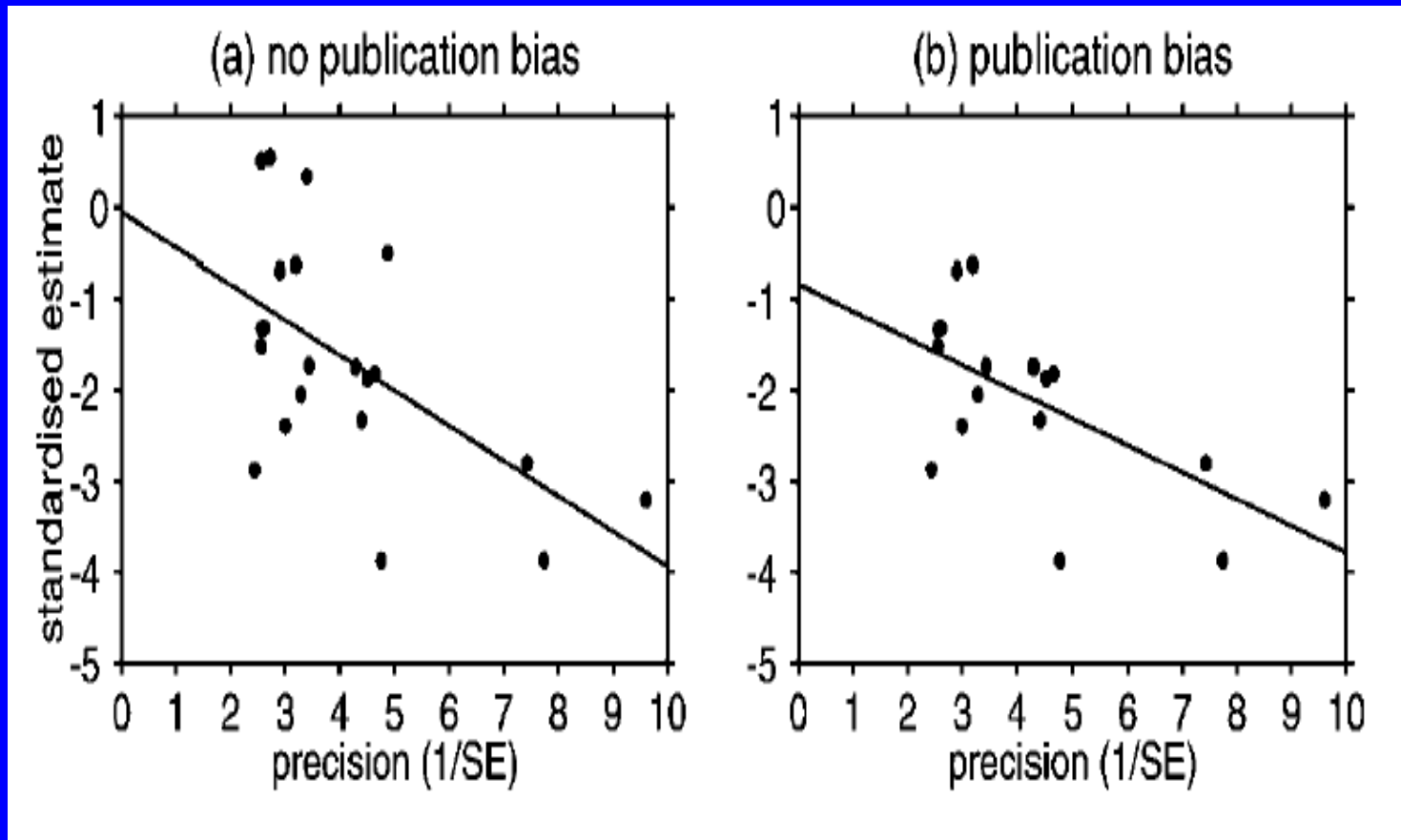
- The intercept value ( $A$ ) = estimate of asymmetry of funnel plot
- Positive values ( $A > 0$ ) indicate higher levels of effect size in studies with smaller sample sizes.



# EGGER'S REGRESSION METHOD

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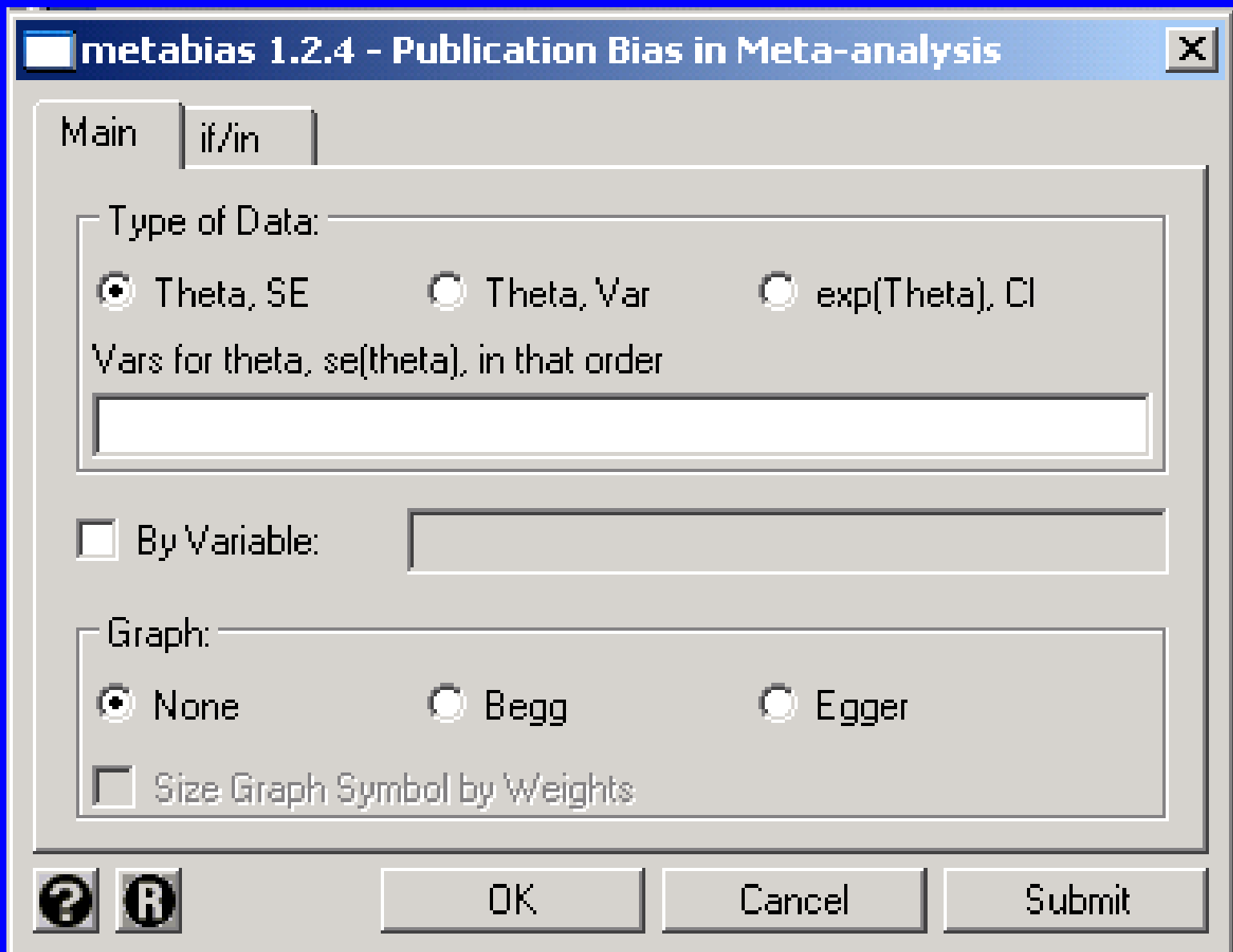
# EGGER'S PLOT



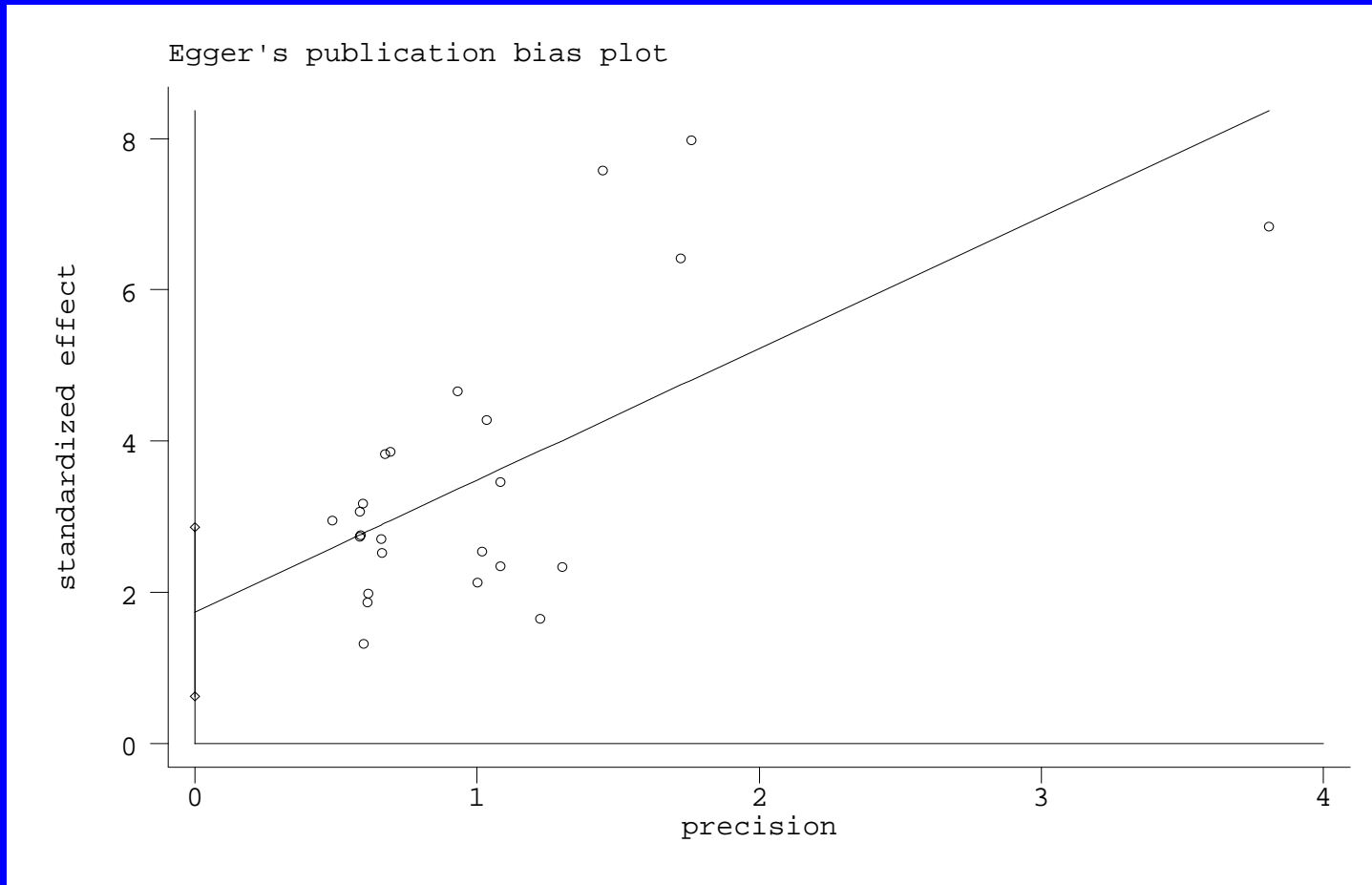
# EGGER'S METHOD

STATA SYNTAX/COMMAND

`metabias logOR selogOR,  
graph(e) saving(eggerplot,  
replace)`



# EGGER'S PLOT



# EGGER'S METHOD

```
-----  
Std_Eff |      Coef.      P>|t|      [95% CI]
```

```
-----+-----  
slope |      1.737492      0.001      .8528166      2.622168
```

```
bias |      1.796411      0.002      .7487423      2.84408
```

# HARBORD'S MODIFIED BIAS TEST

- Test for funnel-plot asymmetry Regresses  $Z/\sqrt{V}$  vs.  $\sqrt{V}$ , where  $Z$  is the efficient score and  $V$  is Fisher's information (the variance of  $Z$  under the null hypothesis).
- Modified Galbraith plot of  $Z/\sqrt{V}$  vs.  $\sqrt{V}$  with the fitted regression line and a confidence interval around the intercept.

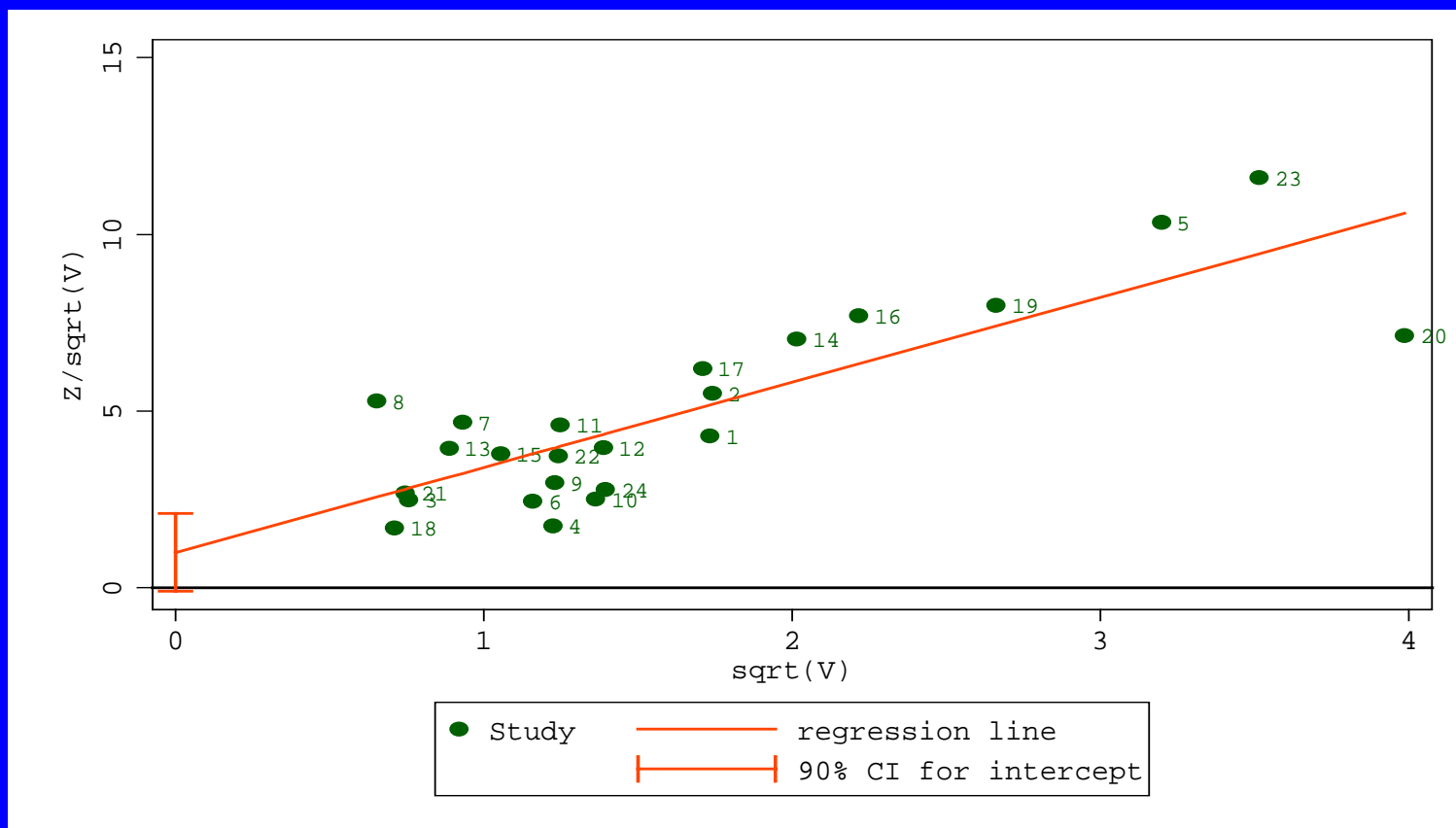
# HARBORD'S MODIFIED BIAS TEST

## STATA SYNTAX/COMMAND

metamodbias tp fn fp tn, graph  
z(Z) v(V) mlabel(index)  
saving(HarbordPlot, replace)



# HARBORD'S MODIFIED BIAS TEST



# HARBORD'S MODIFIED BIAS TEST

```
-----  
ZoversqrtV |      Coef.   Std. Err.   P>|t|   [90% Conf. Interval]  
-----+-----  
      sqrtV|   2.406756   .3464027   0.000   1.811933   3.00158  
  
      bias|   .9965934   .6383554   0.133   -.0995549   2.092742  
-----
```

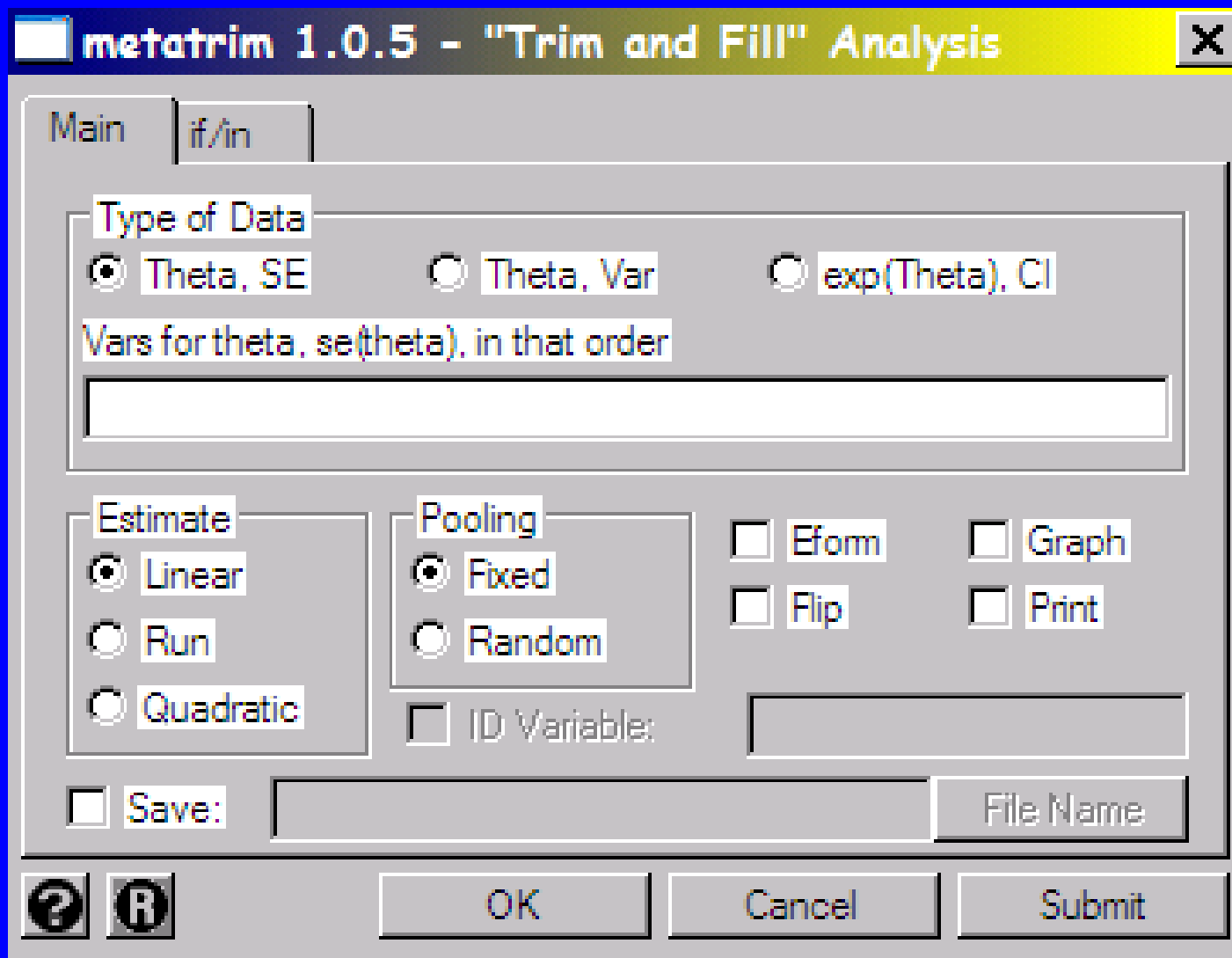
# TRIM AND FILL

- A rank-based data augmentation technique used to estimate the number of missing studies and to produce an adjusted estimate of test accuracy by imputing suspected missing studies. Both random and fixed effect models may be used to assess the impact of model choice on publication bias.

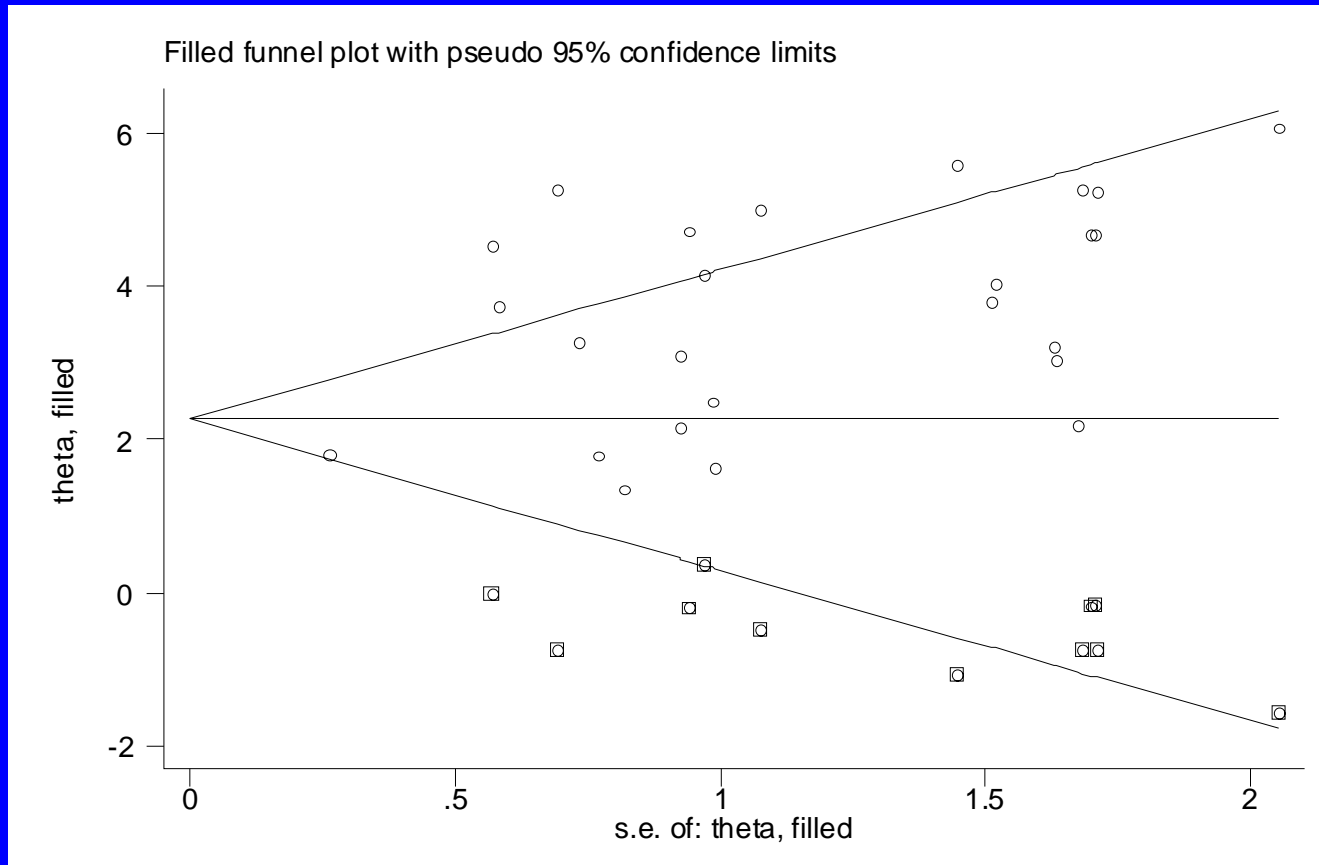
# TRIM AND FILL

## STATA SYNTAX/COMMAND

- `metatrim LogOR seLogOR, eform funnel print graph id(author)saving(tweedieplot, replace)`



# TRIM AND FILL



# INVESTIGATING HETEROGENEITY

- ❑ Heterogeneity means that there is between-study variation.
- ❑ Potential sources of heterogeneity:
  1. Study population
  2. Study design
  3. Statistical methods,
  4. Covariates adjusted for (if relevant).

# GALBRAITH PLOT

- Standardized effect vs. reciprocal of the standard error.
- Small studies/less precise results appear on the left side and the largest trials on the right end .



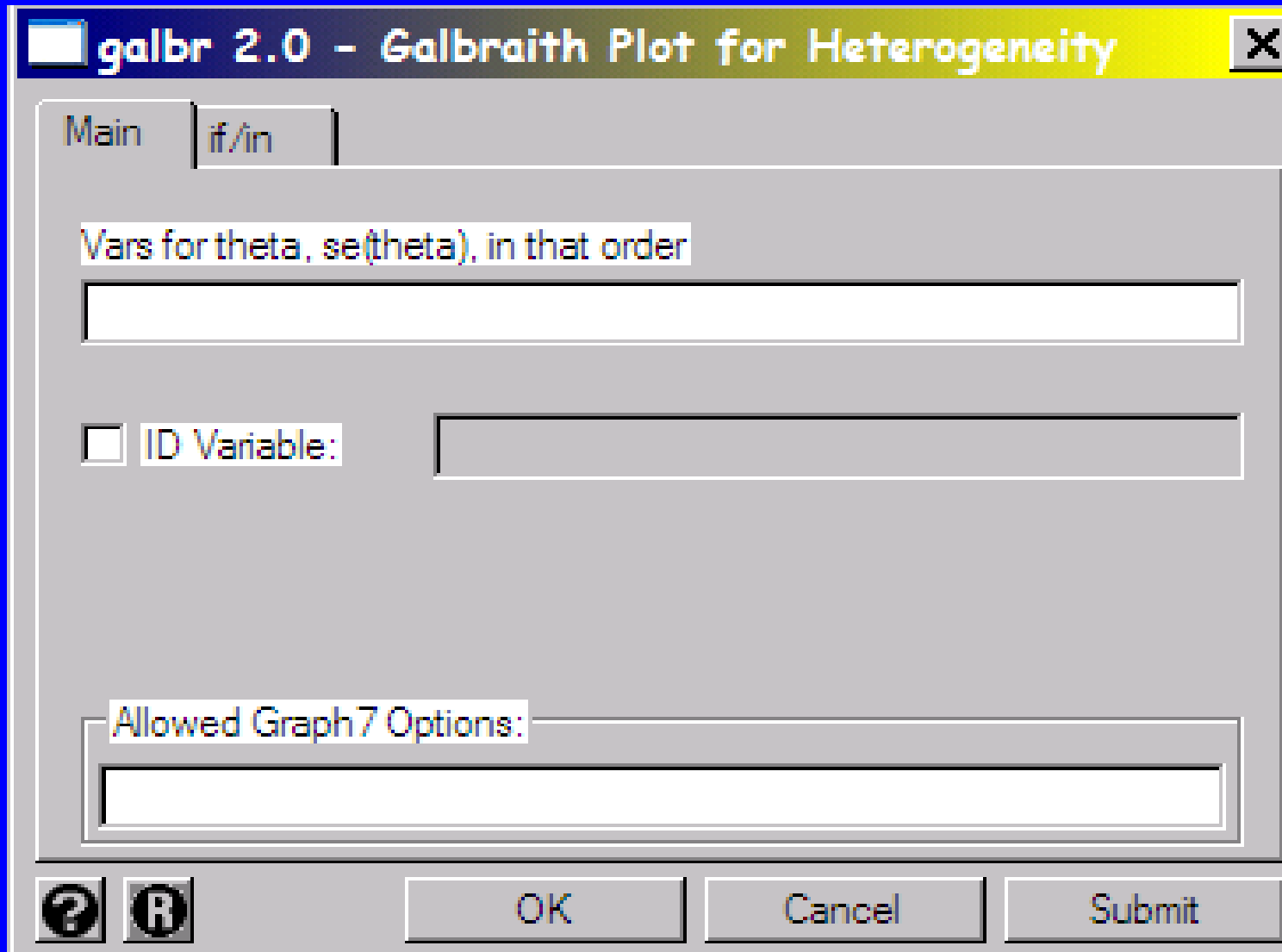
# GALBRAITH PLOT

- ❑ A regression line , through the origin, represents the overall log-odds ratio.
- ❑ Lines +/- 2 above regression line =95 per cent boundaries of the overall log-odds ratio.
- ❑ The majority of within area of +/- 2 in the absence of heterogeneity.

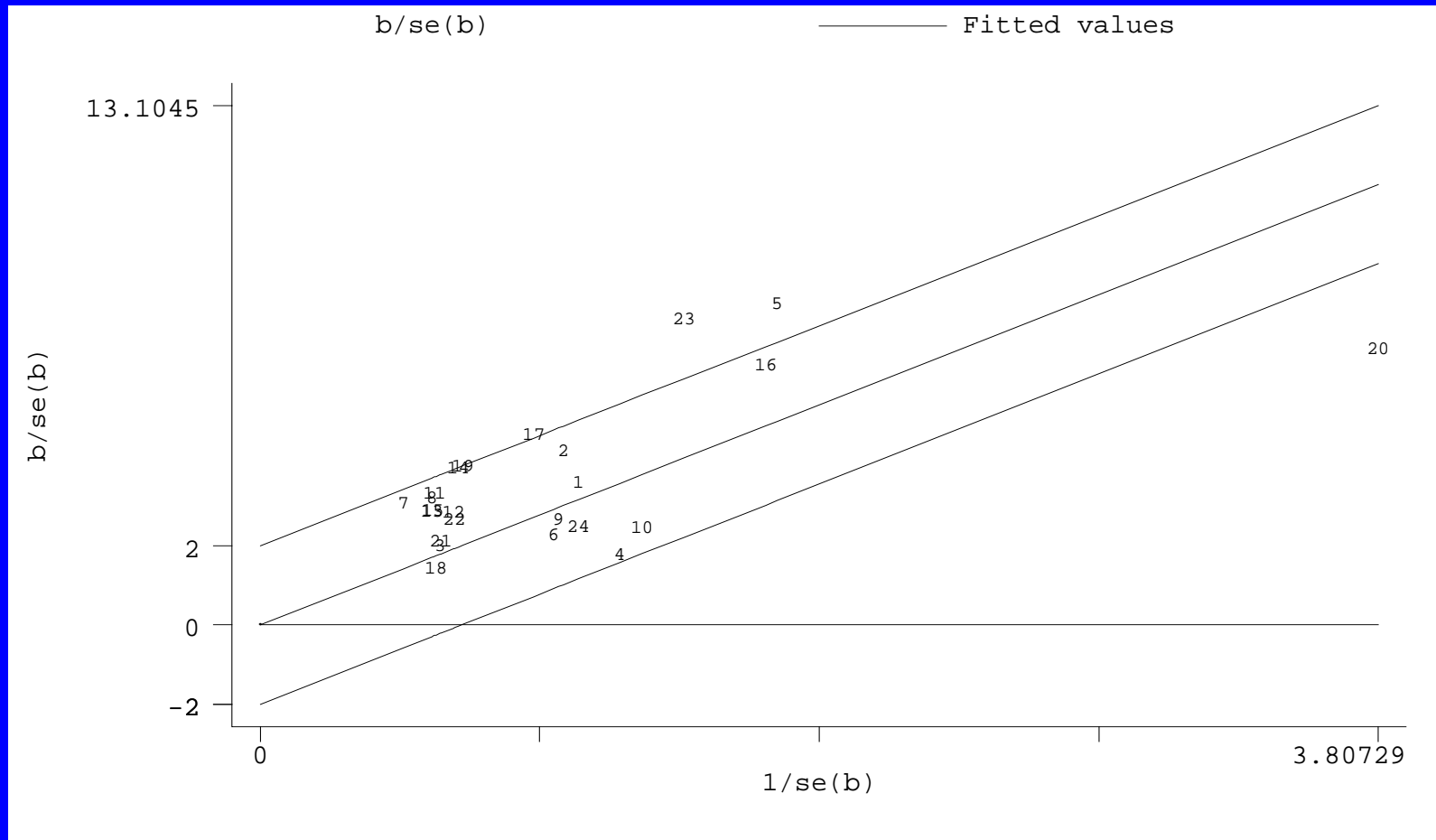
# GALBRAITH PLOT

## STATA SYNTAX/COMMAND

- `galbr LogOR seLogOR,  
id(index) yline(0)  
saving(gallplot, replace)`



# GALBRAITH PLOT



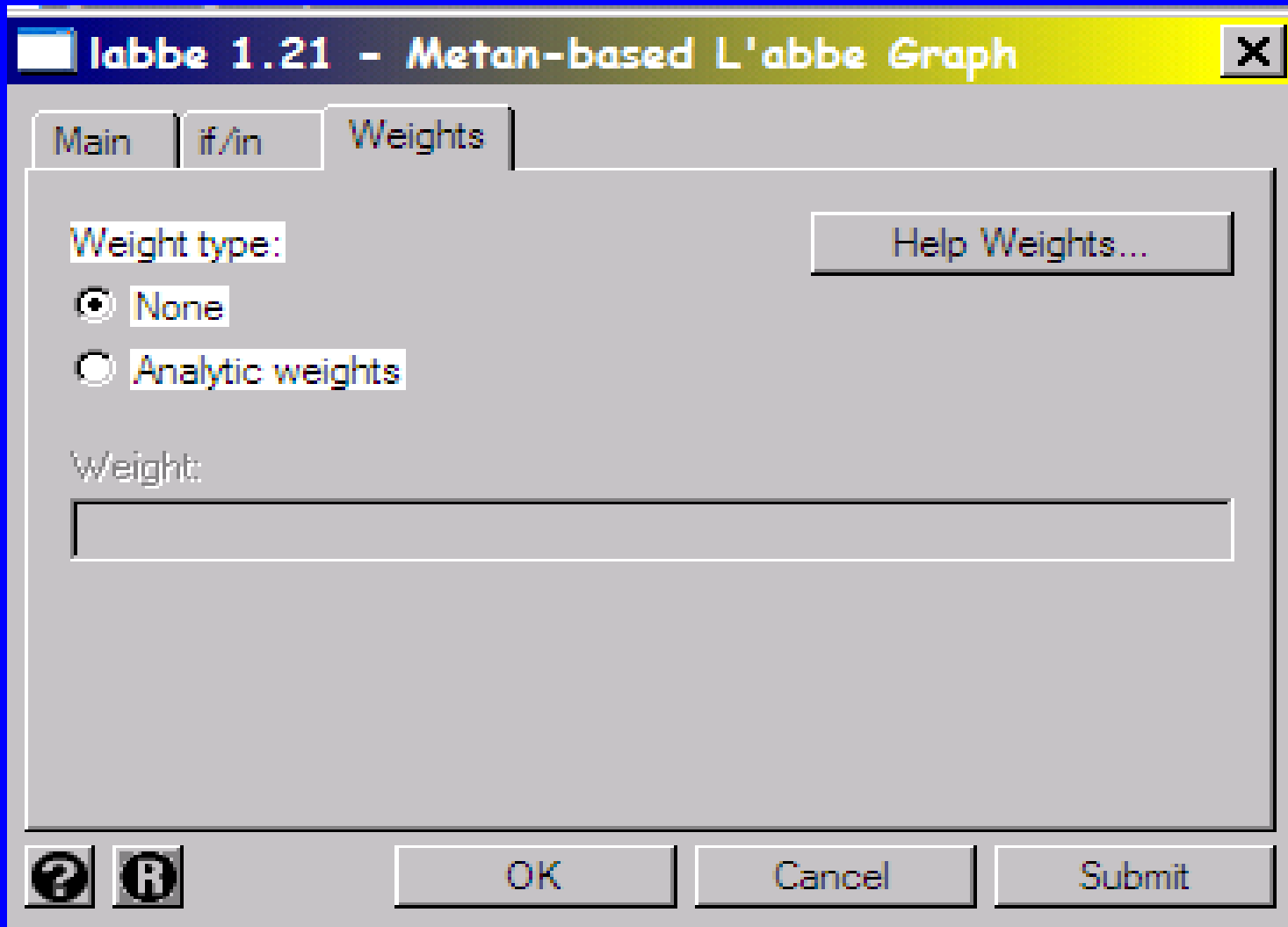
# L'ABBE PLOT

- This plots the event rate in the experimental (intervention) group against the event rate in the control group
- An aid to exploring the heterogeneity of effect estimates within a meta-analysis.

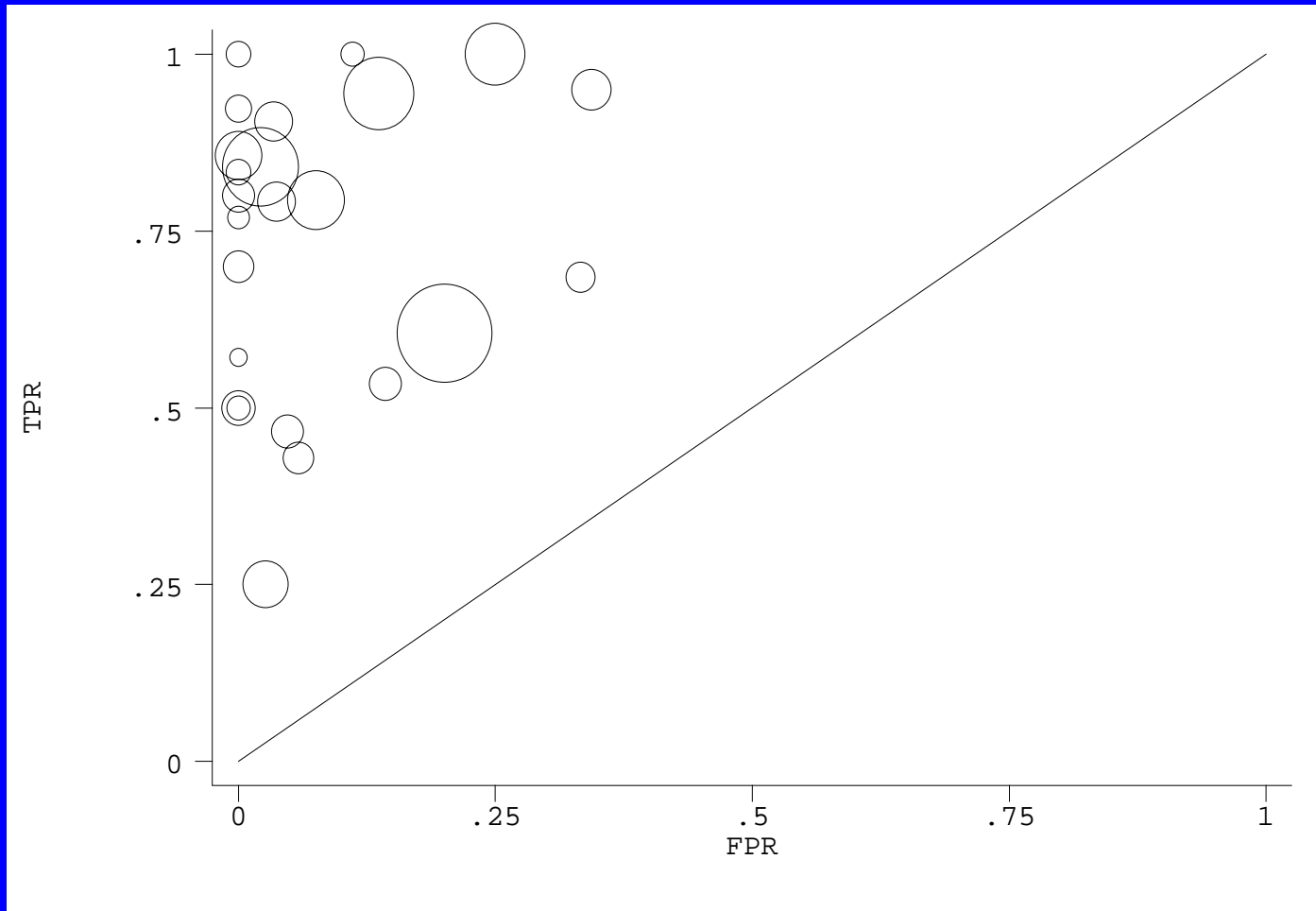
# L'ABBE PLOT

STATA SYNTAX/COMMAND

```
labbe tp fn fp tn, s(0)  
  xlab(0,0.25,0.50,0.75,1)  
  ylab(0,0.25,0.50,0.75,1) l1("TPR")  
  b2("FPR") saving(flabbepplot,  
  replace)
```



# L'ABBE PLOT





# DATA SUMMARY

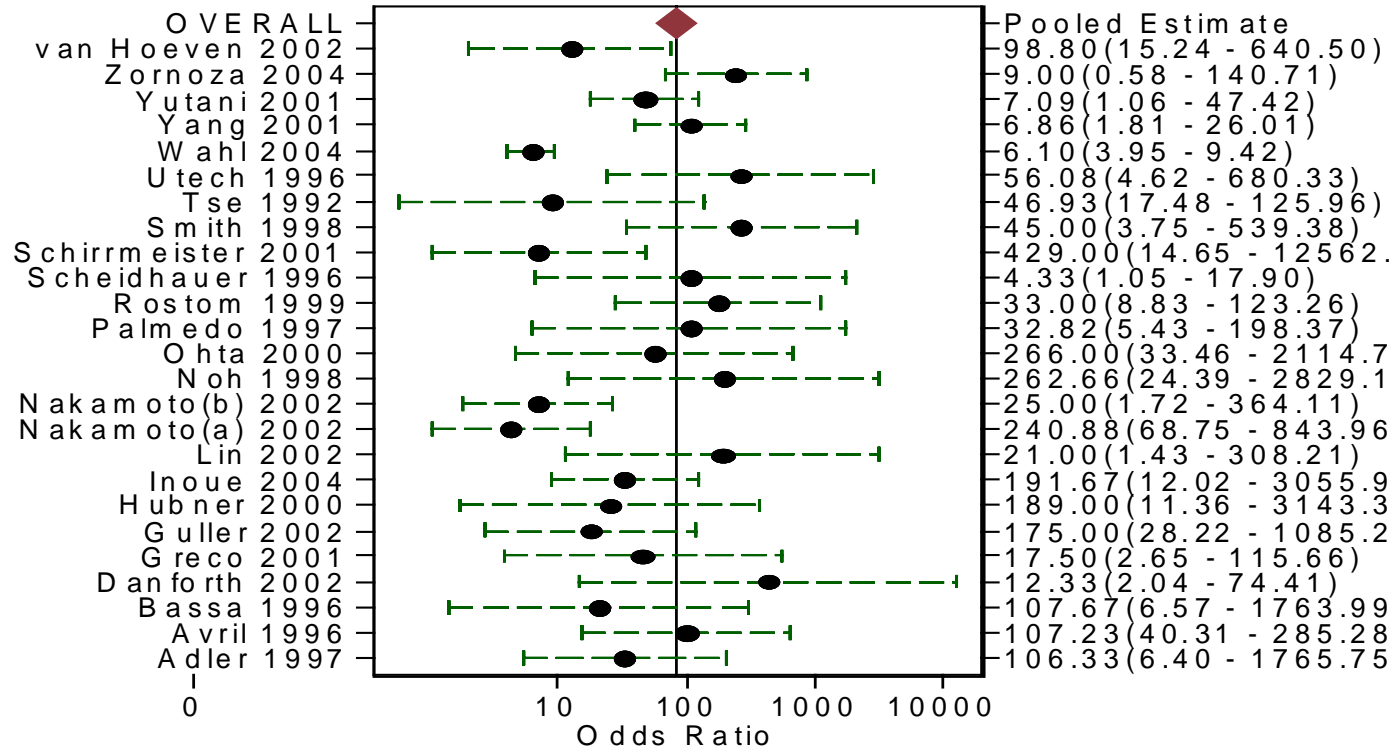
## STATA 8 SYNTAX

```
twoway (rcap dorlo dorhi Study, horizontal  
blpattern(dash))(scatter Study dor, ms(O)msize(medium)  
mcolor(black))(scatter DOR_with_CIs eb_dor, yaxis(2)  
msymbol(i) msize(large) mcolor(black))(scatteri 26 83,  
msymbol(diamond) msize(large)), ylabel(1(1)25 26  
"OVERALL", valuelabels angle(horizontal)) xlabel(0 10  
100 1000 10000) xscale(log) ylabel(1(1)25 26 "Pooled  
Estimate", valuelabels angle(horizontal) axis(2))  
legend(off) xtitle(Odds Ratio) xline(83,  
lstyle(foreground)) saving(OddsForest, replace)
```

# DATA SUMMARY

- `metan tp fn fp tn, or fixed nowt sortby(year)`  
`label(namevar=author, yearvar=year)`  
`t1(Summary DOR, Fixed Effects) b2(Diagnostic`  
`Odds Ratio) saving(SDORFE, replace) force`  
`xlabel(0,1,10,100,1000)`
- `metan tp fn fp tn, or random nowt sortby(year)`  
`label(namevar=author, yearvar=year)`  
`t1(Summary DOR, Random Effects)`  
`b2(Diagnostic Odds Ratio) saving(SDORRE,`  
`replace) force xlabel(0,1,10,100,1000)`

# STATA 8 FOREST PLOT

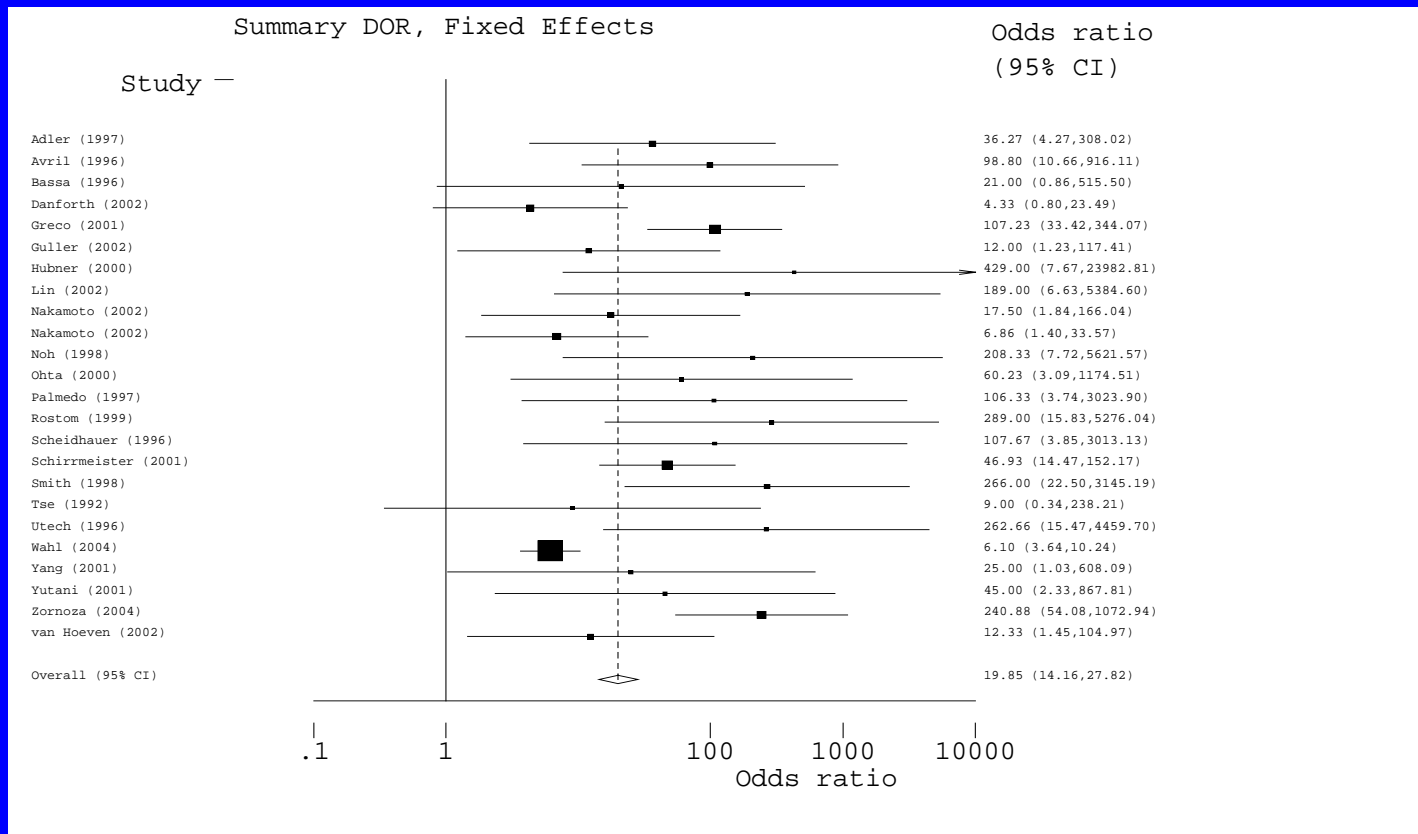


DOR\_with\_CIs

# FIXED EFFECTS META-ANALYSIS

- ❑ Assumes homogeneity of effects across the studies being combined the true effect size has a common true value for all studies.
- ❑ In the summary estimate only the variance of each study is taken into account.

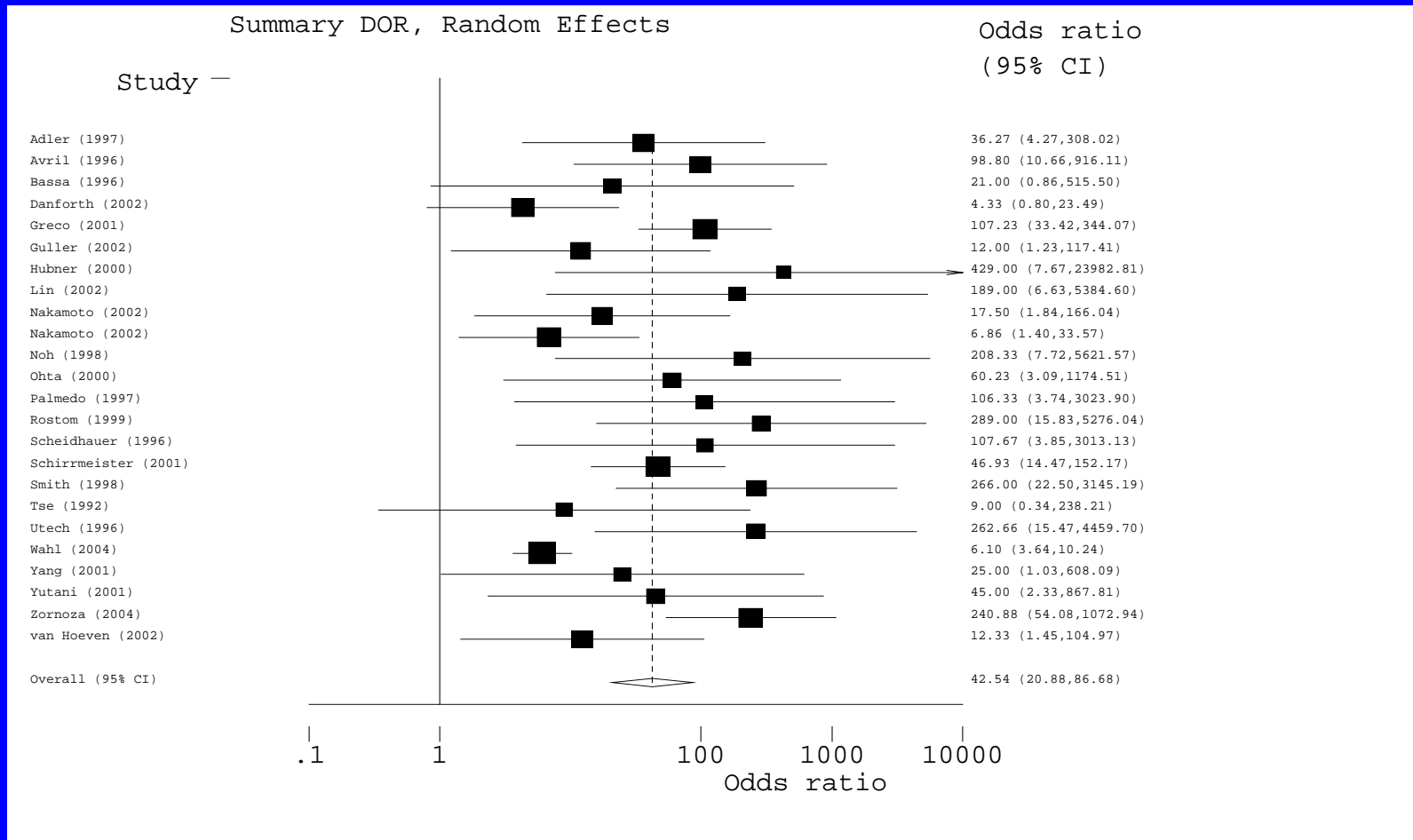
# FIXED EFFECTS FOREST PLOT



# RANDOM EFFECTS META-ANALYSIS

- ❑ Heterogeneity is incorporated into the pooled estimate by including a between study component of variance.
- ❑ Assumes sample of studies included in the analysis is drawn from a population of studies.
- ❑ Each sample of studies has a true effect size.

# RANDOM EFFECTS FOREST PLOT



# CUMULATIVE META-ANALYSIS

- studies are sequentially pooled by adding each time one new study according to an ordered variable. For instance, the year of publication; then, a pooling analysis will be done every time a new article appears.



# CUMULATIVE META-ANALYSIS

```
metacum LogOR seLogOR,  
eform id(author) effect(f) graph  
cline saving(year_fcummmplot,  
replace)
```

metacum 1.02 - Cumulative Meta-analysis

Main | Graph | if/in

Type of Data:

Theta, SE     
  Theta, Var     
  exp(Theta), CI

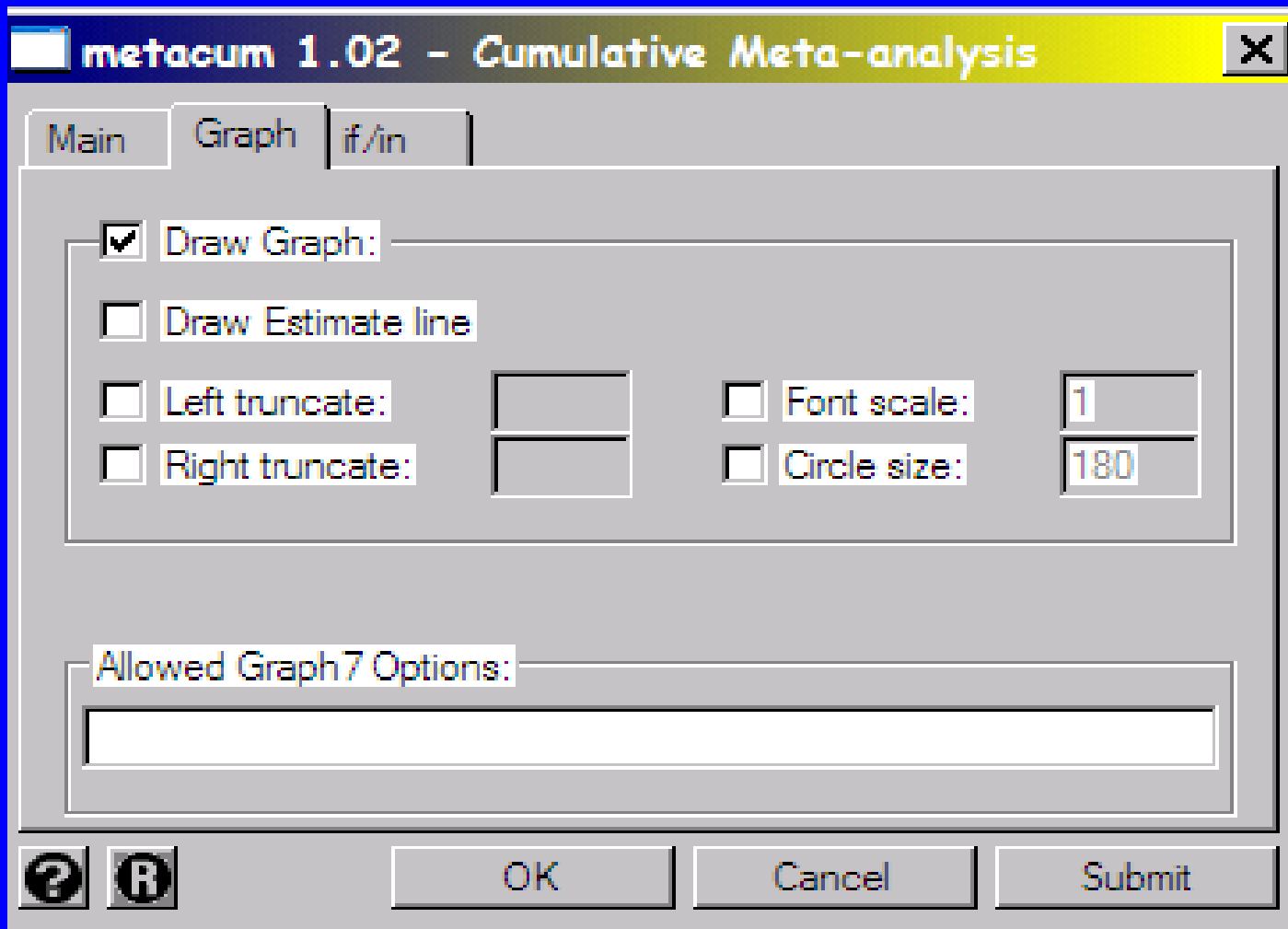
Vars for theta, se(theta), in that order

ID Variable:

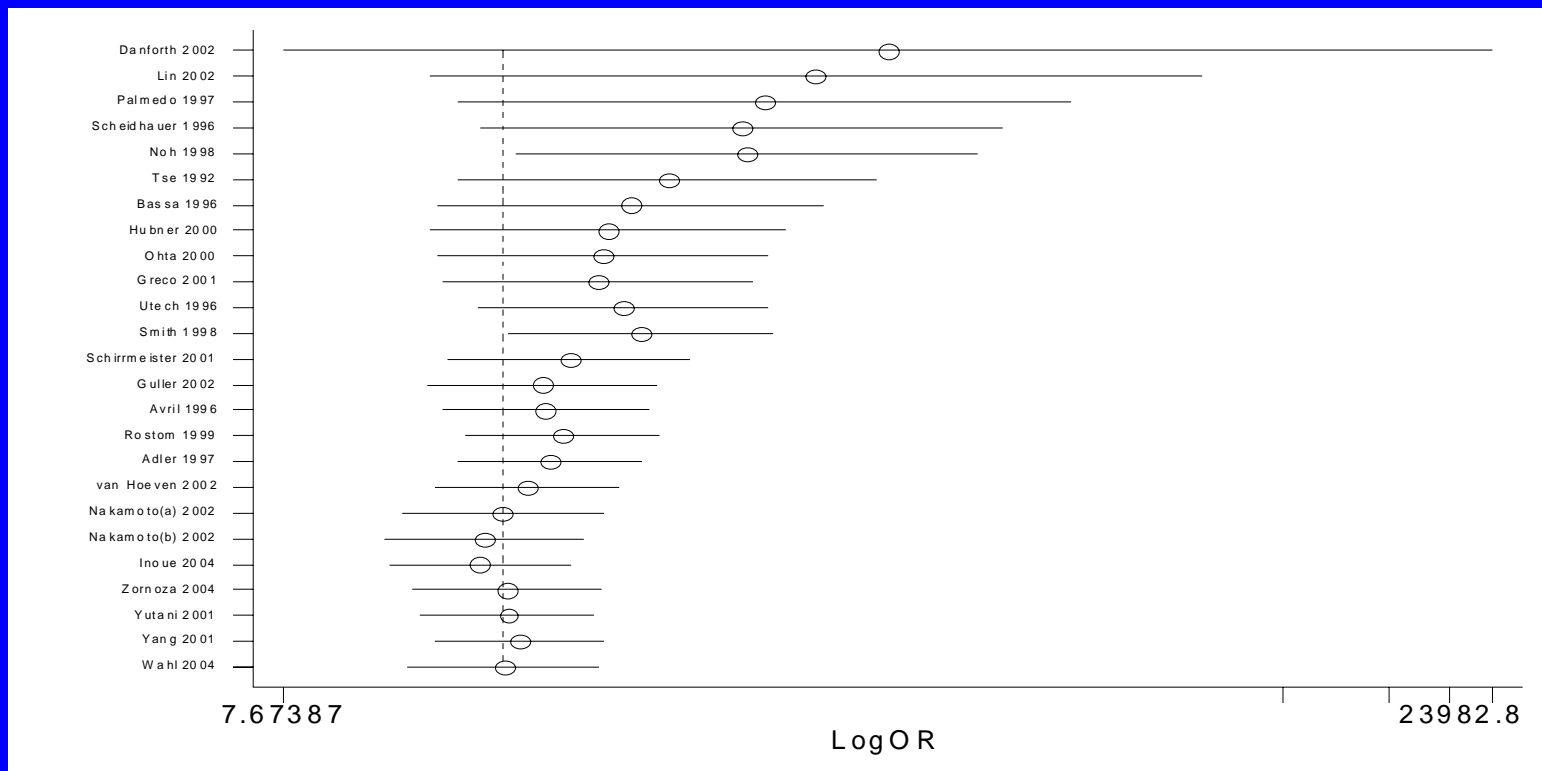
Pooling Model:

Fixed     
  CI Level: 95

Random     
  Use exp(theta)



# CUMMULATIVE META-ANALYSIS



# INFLUENCE ANALYSIS

- studies are pooled according to influence of a trial on overall effect defined as the difference between the effect estimated with and without the trial

# INFLUENCE ANALYSIS

```
□ metaninf tp fn fp tn, id(author)  
  saving(influplot, replace)  
  save(infcoeff, replace)
```

metainf 1.0.2 - Metan-based Influence Anal...

Main | Binary Opts | Contin. Opts | Effect Opts | if/in

Type of Data:

Binary Count     Continuous     Effect Size

Vars for Counts a, b, c, d, in that order

Labels for Data:

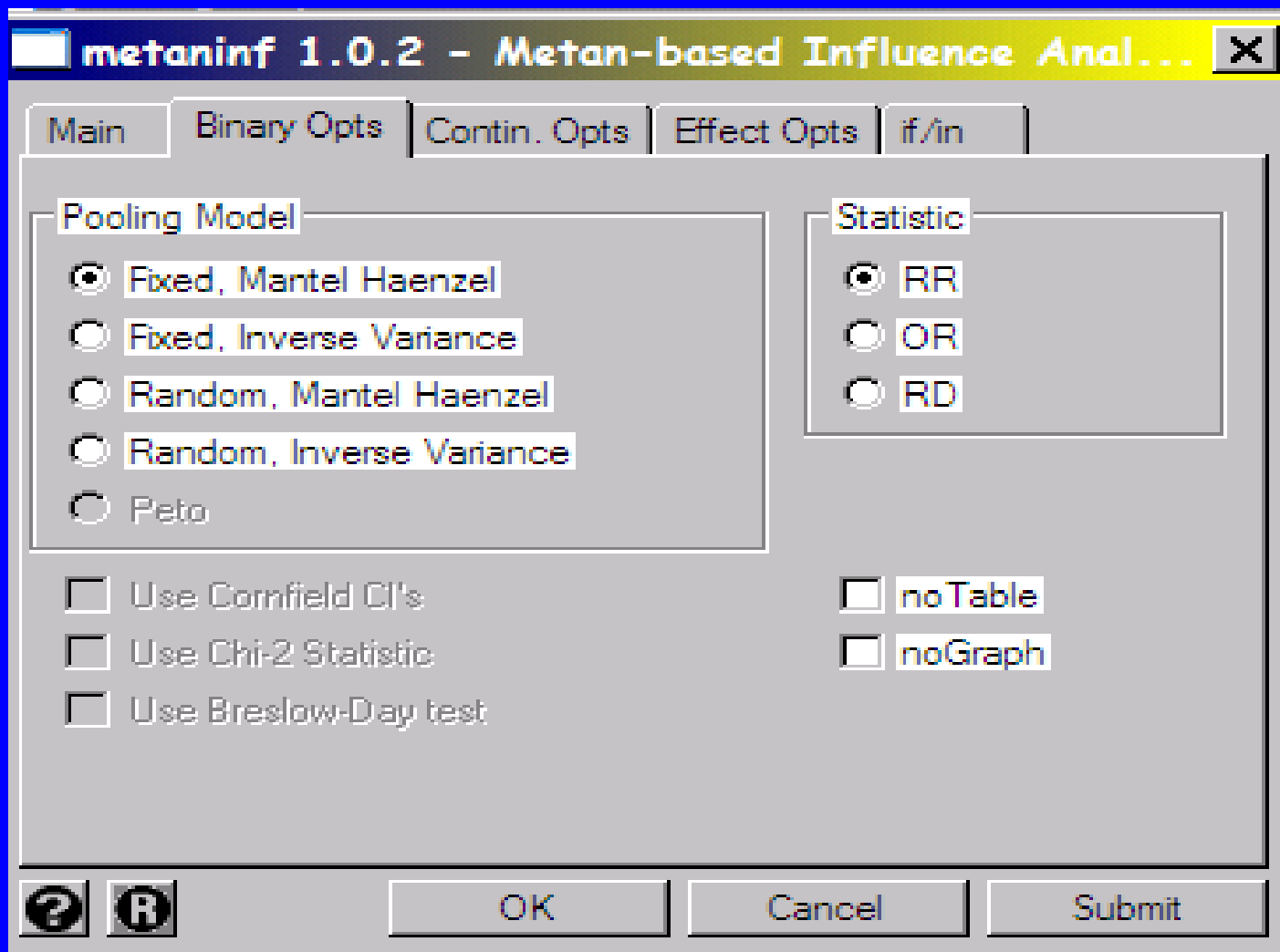
Name: \_\_\_\_\_

Year: \_\_\_\_\_

Save jack-knived estimates: vamame [, replace]

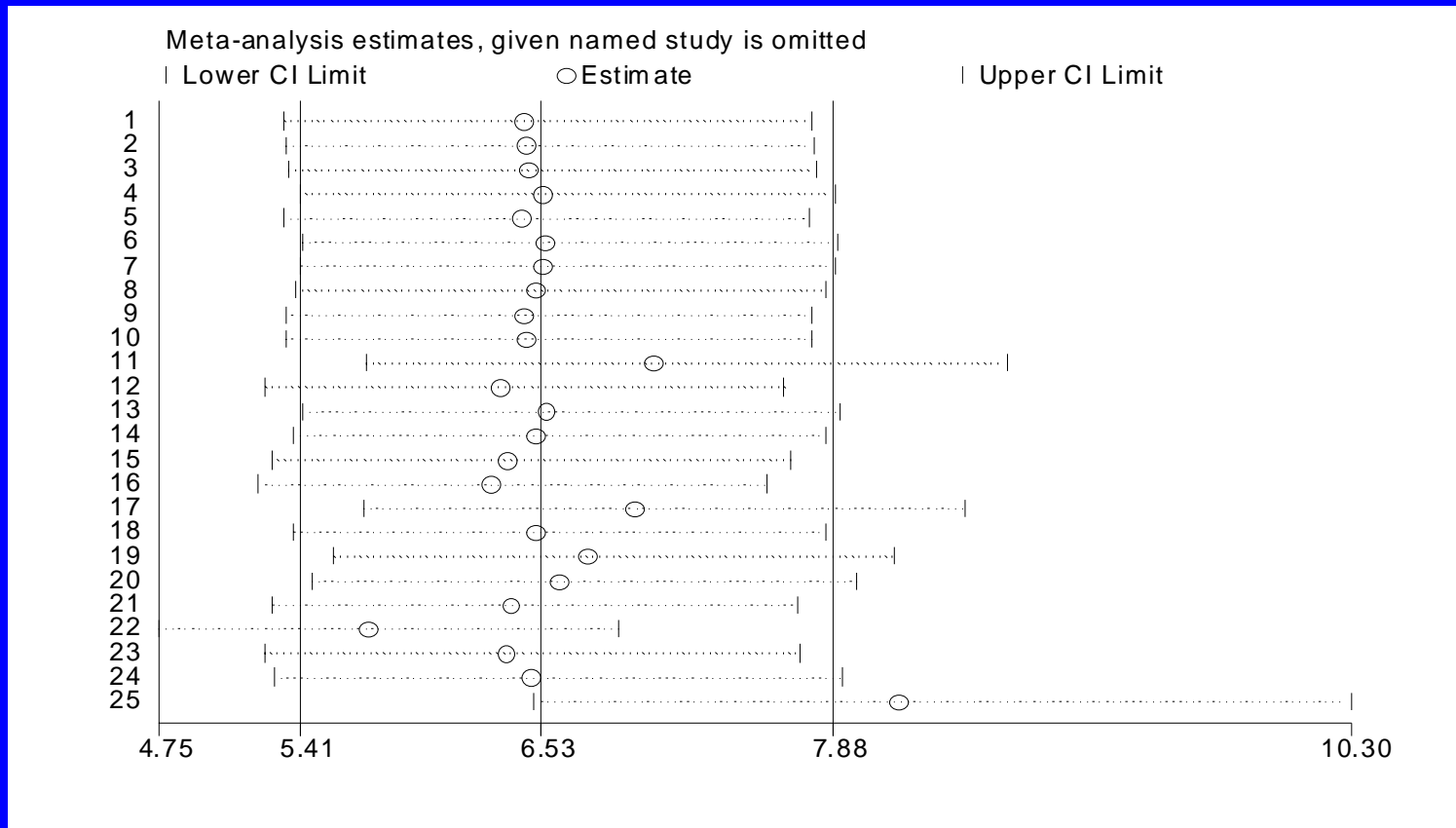
\_\_\_\_\_

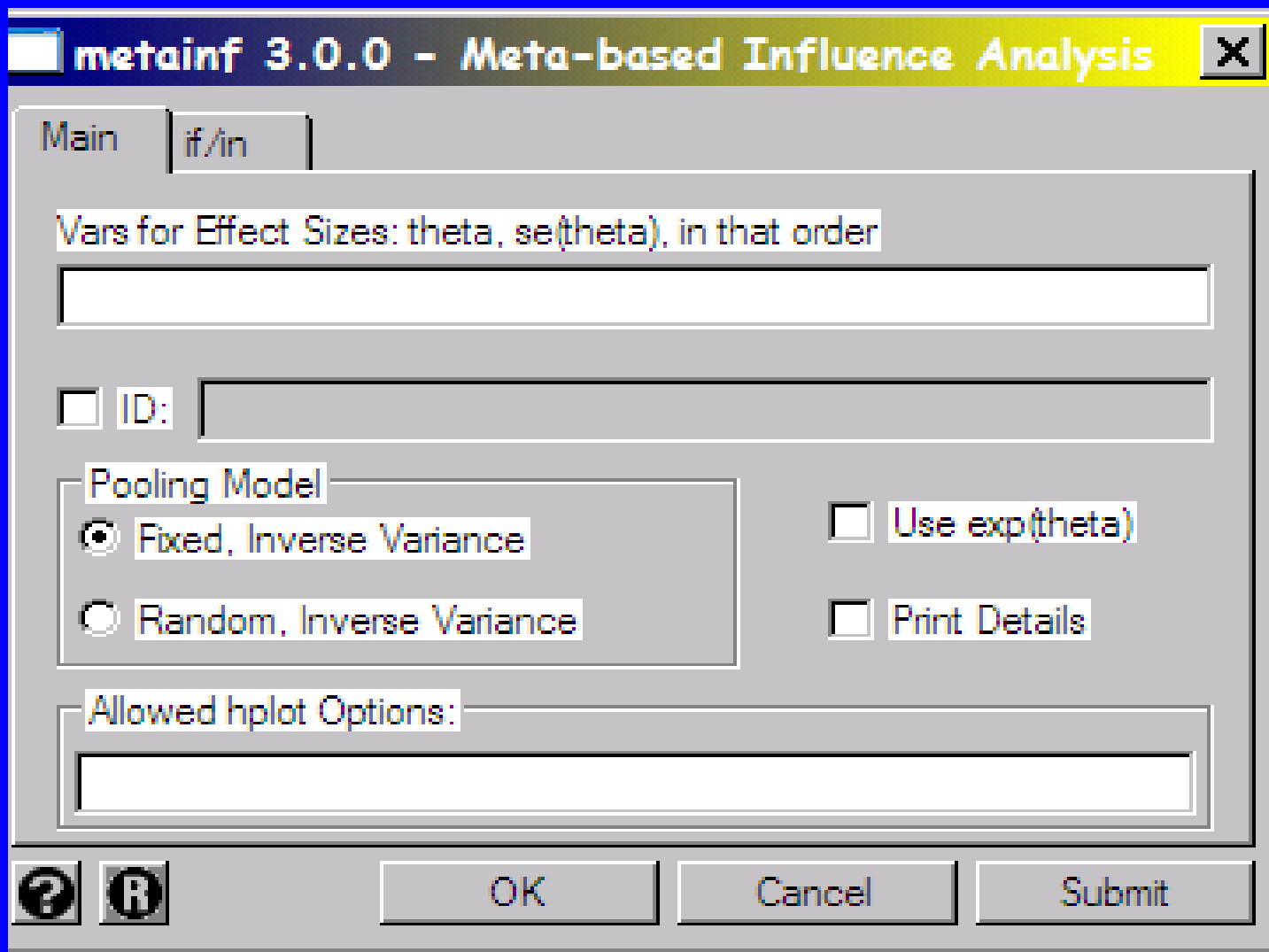
? R OK Cancel Submit





# INFLUENCE ANALYSIS





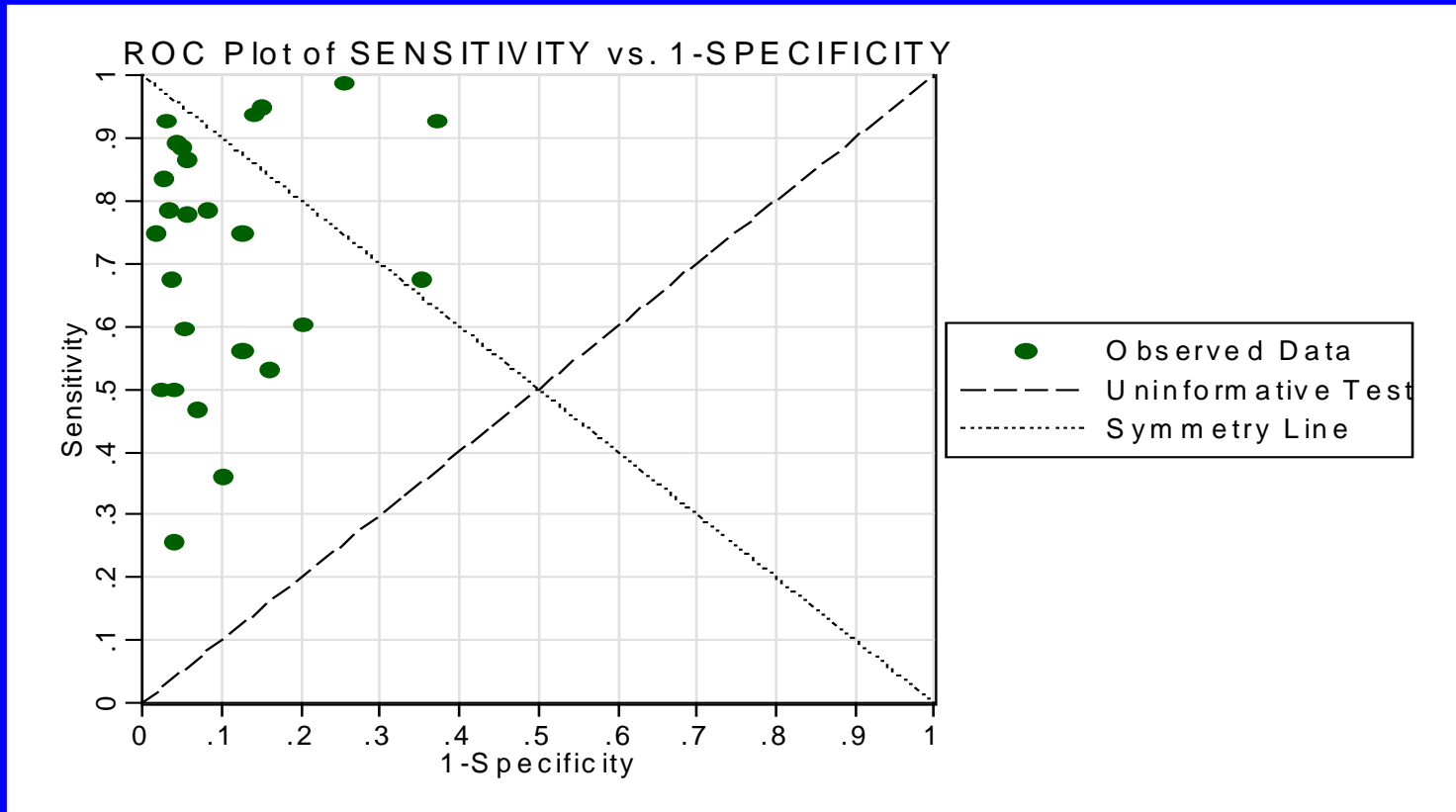
# ROC PLOT

- ❑ A scatter plot true positive fraction (sensitivity) vs. false positive fraction (1-specificity)
- ❑ aids in visualization of range of results from primary studies

# ROC PLOT

```
twoway (scatter TPF FPF, sort) (lfit uTPR FPF, sort
range(0 1) clcolor(black) clpat(dash) clwidth(vthin)
connect(direct)) (lfit sTPR FPF, sort range(0 1)
clcolor(black) clpat(dot) clwidth(vthin)
connect(direct)), ytitle(Sensitivity) ylabel(0(.1)1, grid)
xtitle(1-Specificity) xlabel(0(.1)1, grid) title(ROC Plot
of SENSITIVITY vs. 1-SPECIFICITY, size(medium))
legend(pos(3) col(1) lab(1 "Observed Data") lab(2
"Uninformative Test") lab(3 "Symmetry Line"))
saving(ROCplot, replace) plotregion(margin(zero))
```

# ROC PLOT



# LINEAR REGRESSION MODELS

ORDINARY LEAST SQUARES METHOD:

Studies are weighted equally

WEIGHTED LEAST SQUARES METHOD:

Weighted by the inverse variance weights of the odds ratio, or simply the sample size

ROBUST-RESISTANT METHOD:

Minimizes the influence of outliers

# REGRESSION ANALYSIS

- ❑ Logit transformations of the TP rate (sensitivity) and FP rate (1 - specificity).

$$D = \ln(\text{DOR}) = \text{logit}(\text{TPR}) - \text{logit}(\text{FPR})$$

- ❑ Differences in logit transformations, D, regressed on sums of logit transformations, S.

$$S = \text{logit}(\text{TPR}) + \text{logit}(\text{FPR})$$

- ❑  $\text{Logit}(\text{TPR})$  = natural log odds of a TP result and  $\text{logit}(\text{FPR})$  = natural log of the odds of a FP test result.

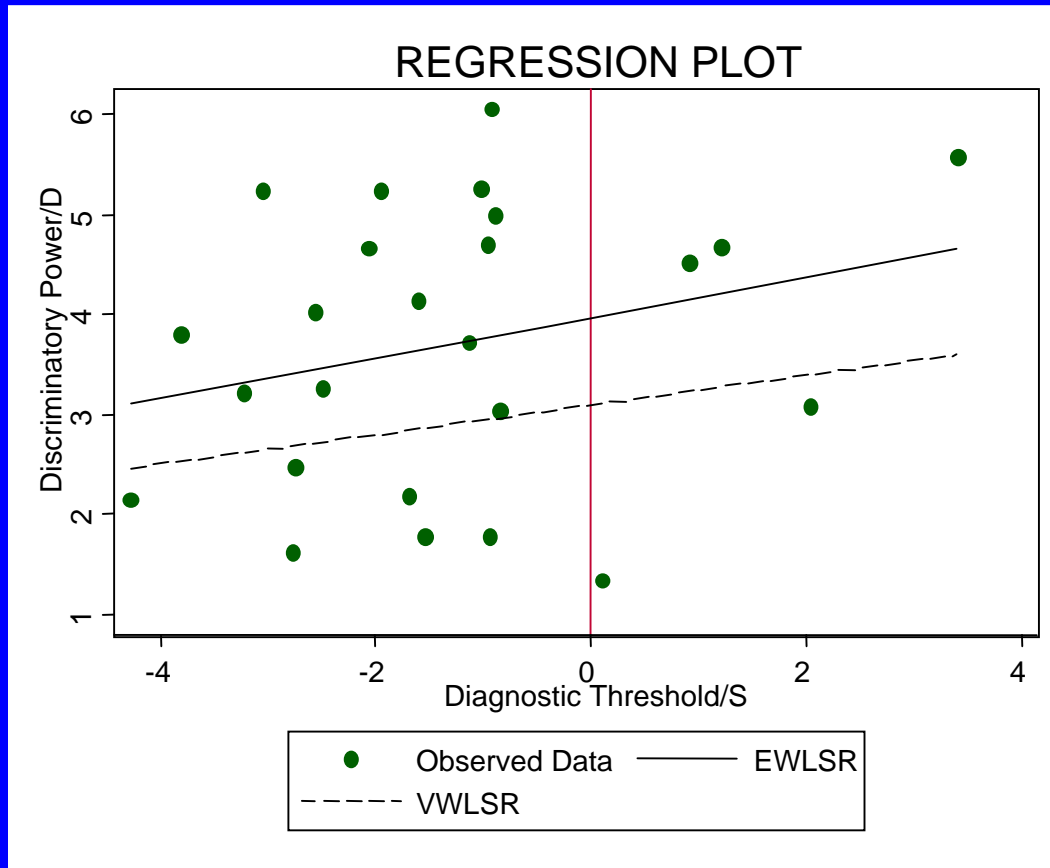
# ACCURACY-THRESHOLD

## STATA SYNTAX/COMMAND

- `twoway (scatter D S, sort msymbol(circle)) (lfit tfitted S, clcolor(black) clpat(solid) clwidth(thin) connect(direct))(lfit wfitted S, clcolor(black) clpat(dash) clwidth(thin) connect(direct)), ytitle(Discriminatory Power/D) xtitle(Diagnostic Threshold/S) title(REGRESSION PLOT) legend(lab(1 "Observed Data")lab(2 "EWLSR")lab(3 "VWLSR"))saving(regplot, replace) xline(0) yscale(noline)`



# ACCURACY-THRESHOLD



# SUMMARY ROC CURVE

- Back transformation of logistic regression to conventional axes of sensitivity [TPR] vs. (1 – specificity) [FPR] with the equation
- $TPR = 1 / \{1 + \exp[- a / (1 - b )]\} [(1 - FPR) / (FPR)]^{(1 + b) / (1 - b)}$ .
- Slope (b) and intercept (a) are obtained from the linear regression analyses

# SUMMARY ROC CURVES

- STATA SYNTAX/COMMAND
- `twoway (scatter TPF FPF, sort msymbol(circle) msize(medium) mcolor(black))(fpfit tTPR FPF, clpat(dash)clwidth(medium) connect(direct ))(fpfit wTPR FPF, clpat(solid)clwidth(medium) connect(direct ))(lfit uTPR FPF, sort range(0 1) clcolor(black) clpat(dash) clwidth(thin) connect(direct)) (lfit sTPR FPF, sort range(0 1) clcolor(black) clpat(dot) clwidth(medium) connect(direct)), ytitle(Sensitivity/TPF) yscale(range(0 1)) ylabel(0(.2)1,grid) xtitle(1-Specificity/FPF) xscale(range(0 1)) xlabel(0(.2)1, grid) legend(lab(1 "Observed Data")lab(2 "EWLSR")lab(3 "VWLSR")lab(4 "RRLSR")lab(5 "Uninformative Test") lab(6 "Symmetry Line") pos(3) col(1)) title(SUMMARY ROC CURVES) graphregion(margin(zero)) saving(aSROCplot, replace)`

# SUMMARY ROC CURVES

