# Gender-based Indicators in Human Development: Correcting for 'Missing Women' 

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#### Abstract

Gender Development Index and Gender Empowerment Measure are two gender-based indicators provided by the United Nations Development Program. Population share of the genders enter the formulation of these indicators in such a way that it favours the better performing gender. This can lead to further additions to 'missing women'. A correction is proposed to capture this anomaly. This alternative satisfies an axiom of Monotonicity with its two corollaries, that is, given attainments the measure maximizes at ideal sex ratio and vanishes when one of the genders becomes extinct. An empirical illustration by taking life expectancy data of countries is given.


Keywords: Ideality, Extinction, Index, Inequality, Sex-ratio
JEL Codes: D63, J16, I31, O15

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# Gender-based Indicators in Human Development: Correcting for 'Missing Women' 

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## 1. Introduction

United Nations Development Program (UNDP) measures gender sensitive human development through two indicators, namely, Gender Development Index (GDI) and Gender Empowerment Measure (GEM). These indicators measure the overall achievement taking note of inequality between the two genders. GDI adjusts the average development, measured by Human Development Index (HDI), to reflect the gender inequalities in the three dimensions of health, education and ability to achieve a decent standard of living. GEM captures the inequalities in opportunities between men and women in the three dimensions of political participation, economic participation and power over economic resources. For each dimension of GDI and GEM, an equally distributed equivalent index, $X_{\text {ede }}$ is computed by combining female and male indices in a way that penalizes differences in achievement between the two genders. ${ }^{2}$ The population-proportion of female and male enter into the formulation of $X_{\text {ede }}$ as weights to female and male achievements respectively, like the case of weighted mean. This follows that for a given level of female and male achievements, a rise in the population proportion of the gender with a higher level of achievement will result in higher $X_{\text {ede }}$. It leads to rewarding of countries having imbalanced population-proportion biased towards the higher performing gender as shown in the following example.

The life expectancy indices of female and male for United Arab Emirates (UAE) are 0.892 and 0.905 respectively, and that of United Kingdom (UK) are 0.895 and $0.903 .{ }^{3}$ In terms of $X_{\text {ede }}$ of life expectancy, UAE and UK score 0.901 and 0.899 respectively and their ranks are 19 and 21 in the world. ${ }^{4}$ This indicates both the countries are close to each other in terms of health dimension of GDI. However, in terms of population-proportion, male/female for UAE is $0.68 / 0.32$ and that of UK is $0.49 / 0.51$. In fact UAE, with more than two males for

[^1]every female, has the most skewed sex ratio in the world. UK, on the contrary, has a balanced sex ratio. Also, the difference in life expectancy indices of female and male for UK is 0.008 which is less than that of UAE, which is 0.013 . Yet, UAE ends up fetching a better rank than UK. Instead of being penalized for imbalanced population-proportion, UAE gets rewarded as the imbalance favours male which has higher life expectancy.

The UAE story repeats for countries like Quatar, Kuwait, Bahrain, Oman, Saudi Arabia. Their imbalanced population-proportion acts to their advantage. This anomaly affects all equally distributed indices used in the measure different dimensions of GDI and GEM. These indices signal countries to favour the higher performing gender and neglect the gender which is lower in performance (typically female). This leads to further additions to 'missing women, ${ }^{5}$ For example, a country, where female literacy is lower than male can improve its education dimension of GDI, by improving the male/female ratio; through female infanticide, abandonment of newborn girls, and neglect of daughters. So, as gender sensitive development indicators, the signal of GDI and GEM is counter intuitive. Ideally, these indicators should signal countries to correct their gender imbalances in population-proportion, rather than to distort it further.

This paper revisits the gender-based indicators and proposes a correction so as to account for population-proportion of female and male in such a way that countries farther to the ideal sex ratio are penalized. An axiom of Monotonicity, with its two corollaries: Ideality and Extinction, is posited to characterize the measure. To demonstrate the advantage of the proposed measure, equally distributed life expectancy index has been used. ${ }^{6}$ The paper makes use of life expectancy data from the latest HDR (UNDP, 2007) and population data from United Nations (UN, 2008).

## 2. Conventional measure

For a pair of female and male achievements ( $X_{f}, X_{m}$ ), equally distributed equivalent index, $X_{\text {ede }}$ is given by general formula

$$
\begin{align*}
& X_{\text {ede }}=\left[\left(p_{f}\left(X_{f}\right)^{(1-\varepsilon)}+p_{m}\left(X_{m}\right)^{(1-\varepsilon \varepsilon}\right]^{1 /(1-\varepsilon)} \text { where } \varepsilon \geq 0 \& \varepsilon \neq 1 ;\right. \\
& X_{\text {ede }}=\left(X_{f}\right)^{P f}\left(X_{m}\right)^{P m} \text { for } \varepsilon=1 \tag{1}
\end{align*}
$$

[^2]where, $p_{f}$ and $p_{m}$ are proportion of female and male respectively such that $p_{m}+p_{f}=1$ and $\varepsilon$ is the aversion to inequality. For moderate penalty, the value 2 is used for $\varepsilon$ (UNDP, 2007). With $\varepsilon=2, X_{\text {ede }}$ is the harmonic mean of $X_{f}$ and $X_{m}$, given by
\[

$$
\begin{equation*}
X_{\text {ede }}=\left[\left(p_{f}\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right]^{(-1)}\right. \tag{2}
\end{equation*}
$$

\]

The properties of $X_{\text {ede }}$ are listed in Appendix 1. ${ }^{7}$ Given $\left(X_{f}, X_{m}\right), X_{\text {ede }}$ varies between $X_{f}$ to $X_{m}$ as $p_{f}, p_{m}$ vary. Fig. 1 plots this variation, with $X_{f}=0.3$ and $X_{m}=0.8$. A rise in the population proportion of the gender with higher level of achievement (here male, as $X_{m}>X_{f}$ ) results in higher $X_{\text {ede }}$. The boundary conditions are at $p_{m}=0, X_{\text {ede }}=X_{f}$ and at $p_{m}=1, X_{\text {ede }}=X_{m}$. All this is counter intuitive for a development indicator sensitive to gender. How can it boils down to the achievement of one gender when the other gets extinct! Does existence or extinction of genders or sex-ratio has nothing to do with gender-development or genderequity!


Fig. 1. Variation of $X_{\text {ede }}$ with population proportion $\left(p_{m}, p_{f}\right)$

Since rise in the population proportion of higher performing gender leads to higher $X_{\text {ede }}$, a country gets rewarded for deviation from the ideal sex ratio half of the time i.e. when

[^3]the deviation favours the advantaged gender. The irony is that instead of being penalized for not able to protect the gender, a country maximizes its $X_{\text {ede }}$ when the lower performing gender gets extinct. So, $X_{\text {ede }}$, and in turn the measures based on $X_{\text {ede }}$ do not signal countries to maintain population-proportion of female and male at a balanced state. The gulf countries, for instance, do not get any signal to have policies to balance their sex ratio. Rather they would prefer a more skewed sex ratio biased towards men, as it leads to higher value of $X_{\text {ede }}$. The signal of conventional measure of $X_{\text {ede }}$ is: 'more achievement, more proportion - the better'. The correct signal is: 'more achievement, ideal proportion - the better'. The following section briefs on ideal proportions of female $\left(p_{f i}\right)$ and male $\left(p_{m i}\right)$ in human population.

## 3. Ideal sex ratio for human population

The actual average sex ratio of entire world population is 1.01 (UN, 2008). ${ }^{8}$ However, the value of ideal sex ratio is under debate and may vary with regions and races. The sex ratio of a population depends on three factors: the sex ratio at birth, differential mortality rates between the sexes at different ages, and losses and gains through migration (Coale, 1991). In the absence of manipulation, the sex ratio at birth is remarkably consistent across human populations, at 1.05 to 1.07 (Coale, 1991, Campbell, 2001). Although sex ratio at birth favors males, differential gender mortality favors females (Teitelbaum, 1970; Sen, 1992, Waldron 1993). Higher life expectancy in females tends to even out the sex ratio in adult population, with male excess among the young and female excess among the old (Klasen and Wink, 2003). But, manipulation at birth manifested by sex-selective abortion, and neglect and abandonment of female children, and international migration characterized by shifting of male population affect sex-ratio. However, like other species, natural human sex ratio is approximately unity and deviation is a threat to the stability and security of the society (Zeng et al, 1993, Park and Cho, 2003, Hudson and Den Boer, 2004). For simplicity, unity sex ratio i.e. equal proportion of female and male ( $p_{f i}=p_{m i}=0.5$ ) is used in this paper for illustrations.

## 4. Axiom of Monotonicity

This section presents Monotonicity property that a measure of equally distributed equivalent achievement should satisfy with respect to sex ratio.

[^4]Axiom of Monotonicity: ${ }^{9}$ Given the achievement level of two genders, the equally distributed equivalent achievement, increases as population approaches to its ideal sex ratio. Mathematically, given $X_{f}, X_{m}\left(0 \leq X_{f}, X_{m} \leq 1\right), X_{\text {ede }}$ increases as $\left(p_{m} / p_{f}\right) \rightarrow\left(p_{m i} / p_{f i}\right)$. Referring to Fig. 1, axiom of Monotonicity requires $X_{\text {ede }}$ to have a positive and negative slope for $p_{m}<p_{m i}$ and $p_{m}>p_{m i}$ respectively. Two corollaries of Monotonicity are axioms of Ideality and Extinction.

Axiom of Ideality: Given the achievement level of two genders, the equally distributed equivalent achievement maximizes at the ideal sex ratio. Mathematically, given $X_{f}, X_{m}\left(0 \leq X_{f}, X_{m} \leq 1\right), X_{\text {ede }}=\left(X_{\text {ede }}\right)_{\max }$ for $\left(p_{m} / p_{f}\right)=\left(p_{m i} / p_{f i}\right)$. Referring to Fig. 1, axiom of Ideality requires $X_{\text {ede }}$ to maximize at ideal proportion of female and male (say $p_{f i}=p_{m i}=0.5$ ). ${ }^{10}$

Axiom of Extinction: Irrespective of achievement levels of two genders, if any of the genders goes extinct, the equally distributed equivalent achievement reduces to minimum possible value i.e. 0 . Mathematically, for any $X_{f}, X_{m}\left(0 \leq X_{f}, X_{m} \leq 1\right) X_{\text {ede }}=0$ if $p_{f}=0$ or $p_{m}=0 .{ }^{11}$ Referring to Fig. 1, axiom of Ideality requires $X_{\text {ede }}$ to be 0 at points $p_{m}=0$ and $p_{m}=1$.

## 5. Proposed measure

The genesis of the weakness of the conventional measure lies with the absence of penalty for deviating from ideal sex ratio. The conventional measure does take note of inequality in the achievements of the two genders (i.e. between $X_{f}$ and $X_{m}$ ) in different dimensions like health, education; but inequality in proportion of population (i.e. between $p_{f}$ and $p_{m}$ ) is not accounted. ${ }^{12}$ Imposition of axiom of Monotonicity will make the measure sensitive to deviation from ideal sex ratio. Accordingly, a new measure of equally distributed equivalent achievement, ${ }^{n} X_{\text {ede }}$ is proposed.

$$
\left.\begin{array}{lc}
{ }^{n} X_{\text {ede }}=\left[p / p_{i}\right]^{\theta}\left[p_{f}\left(X_{f}\right)^{(1-\varepsilon)}+p_{m}\left(X_{m}\right)^{(1-\varepsilon)}\right]^{1 /(1-\varepsilon)} & \text { for } \varepsilon \geq 0, \theta \geq 0 \& \varepsilon \neq 1 \\
{ }^{n} X_{\text {ede }}=\left[p / p_{i}\right]^{\theta}\left(X_{f}\right)^{P f}\left(X_{m}\right)^{P m} & \text { for } \varepsilon=1, \theta \geq 0 \tag{3}
\end{array}\right\}
$$

where $p$ and $p_{i}$ are the actual and ideal proportion of that gender whose actual population is less than or equal to the ideal. The proposed measure is different from the conventional one in the first term, i.e. the penalty factor, which takes note of the deviation from ideal sex ratio.

[^5]The factor is powered by $\theta$, which controls the aversion to this deviation. Larger the $\theta$, smaller is the ${ }^{n} X_{\text {ede }} .{ }^{13}$ At $\theta=0,{ }^{n} X_{\text {ede }}$ reduces to $X_{\text {ede }}$ showing no concern for deviation from ideal sex ratio. For $\theta>0$, the penalty factor gets actuated. The axiom of Extinction gets satisfied for any $\theta>0$. This signifies, once ${ }^{n} X_{\text {ede }}$ is sensitive towards deviation from ideal sex ratio, howsoever small the sensitivity may be; it would reduce to zero if one of the genders goes extinct. This is rational, as any gender sensitive development indicator would penalize a society most severely where one of the genders could not survive in the first place, let alone develop.

For a moderate penalty on gender inequality in achievement i.e. $\varepsilon=2$, the axiom of Monotonicity is satisfied for $\theta \geq 1 .{ }^{14}$ So, for $\varepsilon=2,1$ is the minimum value of $\theta$ for which Monotonicity with both of its corollaries are satisfied; hence 1 is chosen for $\theta$. For $\varepsilon=2$ and $\theta=1$, equation (3) reduces to

$$
\begin{equation*}
{ }^{n} X_{e d e}=\left[p / p_{i}\right]\left[\left(p_{f}\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right]^{(-1)}\right. \tag{4}
\end{equation*}
$$

The propoerties of ${ }^{n} X_{e d e}$ are listed vis-à-vis $X_{e d e}$ in Appendix 1.


Fig. 2. Variation of ${ }^{n} X_{\text {ede }}$ with population proportion ( $p_{m}, p_{f}$ )

[^6]Fig. 2 plots ${ }^{n} X_{\text {ede }}$ against $p_{m}$ and $p_{f}$ for same values of $X_{f}$ and $X_{m}$ as in Fig. 1 i.e. $X_{f}=0.3$, and $X_{m}=0.8 .{ }^{n} X_{\text {ede }}$ is 0 at exitnction conditions ( $p_{m}=0$ or $p_{m}=1$ ) and maximizes at ideal sex ratio ( $p_{m} / p_{f}=p_{m i} / p_{f i}=0.5 / 0.5$ ). The maximum value, $\left({ }^{n} X_{\text {ede }}\right)_{\max }$ is the harmonic mean of $X_{f}=0.3$ and $X_{m}=0.8$, which coincides with the value of $X_{\text {ede }}$ at ideal sex ratio as the penalty factor reduces to 1 . For $p_{m}<p_{m i}$ the profile is represented by curve $I A^{C}$ and for $p_{m}>p_{m i}$, curve $I B^{C}$. The positive and negative slope of $I A^{C}$ and $I B^{C}$ respectively, validates the axiom of Monotonicity. The following propositions further characterize ${ }^{n} X_{\text {ede }}$.

Proposition. The equally distributed equivalent achievement has a convex-decrease for fall in proportion of higher performing gender from ideal and a concave-decrease for lower performing gender. ${ }^{15}$

In Fig. 2, since $X_{m}>X_{f}, I A^{C}$ and $I B^{C}$ have convex and convex profiles respectively. The straight lines $I A^{L}, I B^{L}$ represent the profile of ${ }^{n} X_{\text {ede }}$ for fall in $p_{m}$ and $p_{f i}$ respectively under the condition of gender indistinguishability, i.e. both the genders are at same level of achievement, hence are not distinguishable from the achievement point of view. Substituting, $X_{f}=X_{m}=X$ in Eq. (4) we get the linear relationship between ${ }^{n} X_{\text {ede }}$ and population-proportion.

$$
\begin{equation*}
{ }^{n} X_{\text {ede }}=\left[p / p_{i}\right] X \tag{5}
\end{equation*}
$$

So, the common achievement $X$ coincides with $\left({ }^{n} X_{\text {ede }}\right)_{\text {max }}$. Under this condition of gender indistinguishability, for $p_{m i}=p_{f i}$, the profiles of ${ }^{n} X_{\text {ede }}$ at both sides of ideal are symmetric. $I A^{L}, I B^{L}$ are a pair of such symmetric lines corresponding to $X=(0.48 / 1.1)$ i.e. harmonic mean of $X_{f}=0.3$ and $X_{m}=0.8$.
$I A^{C}$ is below $I A^{L}$ and $I B^{C}$ is above $I B^{L}$. At a given population-proportion, a shift from $I A^{L}$ to $I A^{C}$ indicate a movement from gender indistinguishability, where all the population are at common achievement level, to a state where less than the ideal share population move to higher achievement level and rest move to a lower achievement level. Hence the overall achievement will fall. In case of movement from $I B^{L}$ to $I B^{C}$ more than the ideal share population move to higher achievement level leading to a improvement in overall achievement. This translates to the following lemma. ${ }^{16}$

Lemma 1. For any given population-proportion between ideality and extinction, when higher performing gender has more (less) share than ideal share, the equally distributed equivalent achievement is higher (lower) than the condition of gender indistinguishability.

On the basis of the above lemma, for $p_{f i}=p_{m i}$, it is straight forward to show that for a given population-proportion the equally distributed equivalent achievement is higher when

[^7]higher performing gender has more share than the case when the proportion is swapped between the two. Also, for $p_{f i}=p_{m i}$, magnitude wise the slope of $I A^{C}$ is higher than that of $I B^{C}$ at ideal. This is obvious from the fact that at equal population-proportion of two groups, fall of proportion of the higher quality group entails a greater loss to the society than the lower quality one. This leads to the following lemma.
Lemma 2. For equal population-proportion of genders at ideal the equally distributed equivalent achievement decreases at a faster rate at ideal when population proportion falls for the higher performing gender than for the lower one. For condition of gender indistinguishability, the rate of decrease lies in between.

The proof of the above is straight forward from the fact that $I A^{C}$ and $I B^{C}$ are convex and concave respectively lying below and above of $I A^{L}$ and $I B^{L}$ which are symmetric under unity ideal sex ratio.

## 6. Applying the new measure to equally distributed life expectancy index

Taking female and male life expectancy data for countries of the year 2005 from HDR 2007-2008 (UNDP 2007) and their population-proportion data from Population Division, Department of Economic and Social Affairs of United Nations (UN, 2008) ranks of the countries are obtained on the basis of $X_{\text {ede }}$ and ${ }^{n} X_{\text {ede }}$ (Appendix 5). A value of $p_{m i}=p_{f i}=0.5$ (i.e. sex ratio $1: 1$ ) is used for the purpose. The aversion parameters are taken as $\theta=1$ and $\varepsilon=2$. The difference in ranks indicates that a negative (positive) value implies a worse (better) performance of the country with the proposed measure when compared with the conventional one. The last column is population-proportion difference expressed as female share of population to male share, a negative value showing where male share is higher. The countries those have lost rank under new measure are referred to as losers. Similarly, those that moved up in the ranks are referred to as gainers. Following are some observations.

Table 1: Biggest Losers

| COUNTRY | Life Exp. <br> Index of <br> Female | Life Exp. <br> Index of <br> Male | Sex ratio <br> (males/ <br> females) | Conventi <br> onal <br> Rank | Sex ratio <br> adjusted <br> Rank | Rank <br> Diff. | Gender <br> Prop. <br> Diff. |
| :--- | ---: | :--- | :--- | :--- | :--- | ---: | ---: |
| United Arab <br> Emirates | 0.892 | 0.905 | 2.137 | 19 | 129 | -110 | -0.363 |
| Qatar | 0.805 | 0.868 | 2.064 | 41 | 134 | -93 | -0.347 |
| Kuwait | 0.868 | 0.887 | 1.500 | 33 | 101 | -68 | -0.200 |
| Bahrain | 0.825 | 0.857 | 1.323 | 43 | 93 | -50 | -0.139 |
| Oman | 0.820 | 0.852 | 1.284 | 47 | 87 | -40 | -0.124 |
| Saudi Arabia | 0.785 | 0.797 | 1.172 | 66 | 90 | -24 | -0.079 |

The six gulf countries, UAE, Qatar, Kuwait, Bahrain, Oman and Saudi Arabia; stand out as biggest looser as per the proposed measure of equally distributed life expectancy index. These six countries have the dubious distinction of world's top rankers in terms of unbalanced sex ratio biased towards male. Table 1 illustrates their case. In all these countries, male life expectancy index is more than female. Since men outnumber women by large margins, these countries get the undue advantage under the conventional measure. In the new measure they lost rank because of the penalty for deviation from ideal sex ratio.

Table 2: Some selected cases for comparison

| COUNTRY | Life Exp. <br> Index of <br> Female | Life Exp. <br> Index of <br> Male | Sex ratio <br> (males/ <br> females) | Conventi <br> onal <br> Rank | Sex ratio <br> adjusted <br> Rank | Rank <br> Diff. | Gender <br> Prop. <br> Diff. |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | ---: |
| Cuba | 0.872 | 0.888 | 1.000 | 32 | 22 | 10 | -0.001 |
| Kuwait | 0.868 | 0.887 | 1.500 | 33 | 101 | -68 | -0.200 |
| Nicaragua | 0.792 | 0.775 | 1.000 | 74 | 58 | 16 | 0.001 |
| Latvia | 0.830 | 0.733 | 0.842 | 75 | 97 | -22 | 0.085 |
| Iceland | 0.927 | 0.957 | 1.000 | 3 | 1 | 2 | 0.000 |
| Japan | 0.970 | 0.937 | 0.957 | 1 | 2 | -1 | 0.023 |

Table 2 gives a comparison between some selected gainers and losers. Cuba has less inequality in life expectancy for female and male than Kuwait. But Kuwait has managed to fetch a similar rank as Cuba because of its male biased sex ratio; so a higher weight of male performance contributing to the higher final value. However, under the new measure Cuba performed relatively better for its balanced sex ratio. Kuwait, on the contrary, having three males per two females lost its earlier rank by 68 positions.

It is not always true that men fared better than women. Male have a greater tendency to engage in risk behaviors and violence, thus increasing their risk of premature mortality (Waldron, 1993). Lativia is an example where not only females have more life expectancy, but also they are higher in population-proportion. This is the precise reason for which Lativia occupied a rank next to Nicaragua, which is much more equal in terms life expectancy across gender but also has a balanced sex ratio. Under the new measure, Lativia regresses to a lower rank on account of a biased sex ratio towards female, whereas Nicaragua improved its positions.

Japan tops the list under conventional measure, but when penalty for deviation from ideal sex ratio is introduced, Japan looses its rank to Iceland. As seen from the table Japan's sex ratio is biased towards females (only 957 males for 1000 females) and females have higher life expectancy index. In fact, Japanese women live the longest in the world. However,

Japan got penalized under the new measure whereas Iceland, with equal proportion of males and females (1:1), does not get affected by the penalty.

## 7. Conclusion

The present gender equity-sensitive development indicators suffer from the limitation that countries with unbalanced sex ratio get rewarded where sex ratio is biased towards the higher performing gender. This paper questions the rationality of such indicators which take note of, for instance, inequality in life expectancy without consideration of the 'life' itself! An axiom of Monotonicity is posited so that equally distributed equivalent achievement increases as the population closes to ideal sex ratio. Two corollaries; axiom of Ideality and axiom of Extinction make the measure respectively to maximize at ideal sex ratio and to reduce to zero when one of the genders gets extinct. A new measure has been proposed which brings in a penalty factor to capture the deviation from ideal sex ratio. The new measure has a convex-decrease for fall in proportion of higher performing gender from ideal and a concavedecrease for lower performing one. Under this proposed measure, gulf countries get penalized for their unnaturally unbalanced sex ratio biased towards male. Countries with higher level of achievement, lower disparity between male and female and population-proportion closer to ideal sex ratio get rewarded. Unlike the conventional measure, the new measure gives appropriate signal to countries to correct for the 'Missing Women'. The proposed measure is more flexible with different handles of aversion to proportion-inequality and achievementinequality. Though a uniform ideal sex ratio of $1: 1$ is used for the present analysis, the formulation is generic enough to consider different ideal sex ratios for different age group, countries, regions, and races. Moreover, the new measure can be used to find equally distributed equivalent achievement between two groups other than gender where a desired proportion of the two groups are postulated. For instance, the equally distributed equivalent index for education calculated for BPL (below poverty line) and APL (above poverty line) groups (note the desired population-proportion of BPL to APL is $0: 1$ ) using the proposed measure not only takes note of the inequality in achievement in education between the two gender, but also rewards a society who have higher proportion of people as APL However, the proposed measure is applicable to population of two groups. As a future scope, similar measures for more than two groups can be conceptualized.

## Appendix 1

| Comparison of properties of conventional measure ( $\boldsymbol{X}_{\text {ede }}$ ) and proposed measure ( ${ }^{\boldsymbol{n}} \boldsymbol{X}_{\text {ede }}$ ) |  |
| :---: | :---: |
| (i) $\min \left(X_{f}, X_{m}\right) \leq X_{\text {ede }} \leq \max \left(X_{f}, X_{m}\right)$ | $0 \leq^{n} X_{\text {ede }} \leq \max \left({ }^{n} X_{\text {ede }}\right)$ <br> where $\max \left({ }^{n} X_{e d e}\right)=\left[\left(p_{f i}\left(X_{f}\right)^{(-1)}+p_{m i}\left(X_{m}\right)^{(-1)}\right]^{(-1)}\right.$ $=$ harmonic mean of $X_{f}$ and $X_{m}$ at $p_{m i}, p_{f i}$. This property qualifies the axiom of Ideality and Extinction. |
| (ii) at $\varepsilon=0, X_{\text {ede }}=X^{a}$ i.e. arithmetic mean of achievement of population; for $\varepsilon>0, X_{\text {ede }}<X^{a}$ | $\begin{aligned} & \text { at } \varepsilon=0,{ }^{n} X_{\text {ede }}=\left[p / p_{i}\right]^{\theta} X^{a} . \text { When } p=p_{i},{ }^{n} X_{\text {ede }}=X^{a} \\ & \text { For } \varepsilon>0,{ }^{n} X_{\text {ede }}<\left[p / p_{i}\right]^{\theta} X^{a} \leq X^{a} \end{aligned}$ |
| (iii) larger the $\varepsilon$, smaller is $X_{\text {ede }}$ | (iii) larger the $\varepsilon$, smaller is $X_{\text {ede }}$; larger $\theta$ smaller is $X_{\text {ede }}$. |
| (iv) $X_{\text {ede }} \rightarrow \min \left(X_{f}, X_{m}\right)$ as $\varepsilon \rightarrow \infty .{ }^{17}$ | (iv) ${ }^{n} X_{\text {ede }} \rightarrow\left[p / p_{i}\right]^{\theta}\left[\min \left(X_{f}, X_{m}\right)\right]$ as $\varepsilon \rightarrow \infty$. <br> When $\varepsilon \rightarrow \infty$ and $p \rightarrow p_{i}{ }^{\prime}{ }^{n} X_{\text {ede }} \rightarrow \min \left(X_{f}, X_{m}\right)$ |
| (v) $X_{\text {ede }}$ is monotonic increasing in both $X_{f}$ and $X_{m}$, the increase is at diminishing rate. ${ }^{18}$ | Property remains same for ${ }^{n} X_{\text {ede }}$. |
| (vi) a unit increase in performance for the gender with higher population but lower level of performance is more valuable socially (higher $X_{\text {ede }}$ ) than the unit increase in performance for the other gender. | Property remains same for ${ }^{n} X_{\text {ede }}$. |
| (vii) a rise in the population proportion of a sub group with higher level of achievement will result higher $X_{\text {ede }}$. | closer the proportion population to the ideal higher is ${ }^{n} X_{\text {ede }}$. This property validates axiom of Monotonicity. |
| (viii) more concave the underlining form of $X_{\text {ede }}$, smaller is $X_{\text {ede }}$. The present underlining form of $X_{\text {ede }}$ is $(1 /(1-\varepsilon)) X^{(1-\varepsilon)}$. | Property remains same for ${ }^{n} X_{\text {ede }}$ |
| (ix) the relative gender equality index, $E$ is maximum for $X_{f}=X_{m}$ and $\max (E)=1 .{ }^{19}$ | the relative gender equality index, $E$ is maximum for $X_{f}=X_{m}$ and $\max (E)=\left[p / p_{i}\right]^{\theta}$. When $p \rightarrow p_{i} ; \max (E) \rightarrow 1$. |
| (x) for equality of proportion, $\left(p_{f}=p_{m}\right) E$ is symmetric in $X_{f}$ and $X_{m}$. E $\rightarrow 0$, if $\left(X_{f} / X_{m}\right) \rightarrow 0$ or $\left(X_{f} / X_{m}\right) \rightarrow \infty$. | Property remains same for ${ }^{n} X_{\text {ede }}$ |

[^8]
## Appendix 2

Without loss of generality (wlog), Eq. (3) can be expressed in $p_{m}$, ( $p_{f}$ is substituted by (1- $p_{m}$ ))
${ }^{n} X_{\text {ede }}=\left[p_{m} / p_{m i}\right]^{\theta}\left[\left(1-p_{m}\right)\left(X_{f}\right)^{(1-\varepsilon)}+p_{m}\left(X_{m}\right)^{(1-\varepsilon)}\right]^{1 /(1-\varepsilon)} \quad$ for $\varepsilon \geq 0, \theta \geq 0 \& \varepsilon \neq 1$
Note the above equation is valid for $p_{m} \leq p_{m i}$. For $p_{m}>p_{m i}$ the penalty term changes to $\left[p_{f} / p_{f i}\right]^{\theta}=\left[\left(1-p_{m}\right) /\left(1-p_{m i}\right)\right]^{\theta}$. To satisfy the axiom of Monotonicity we need to prove $\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial p_{m}\right)>0$ for $p_{m} \leq p_{m i}$ and $\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial p_{m}\right)<0$ for $p_{m}>p_{m i}$. Differentiating Eq. (6),

$$
\begin{aligned}
& \frac{\partial\left(^{n} X_{e d e}\right)}{\partial p_{m}}=\left(\frac{p_{m}}{p_{m i}}\right)^{\theta} \frac{1}{(1-\varepsilon)}\left(\left(1-p_{m}\right) X_{f}^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right)^{\frac{\varepsilon}{(1-\varepsilon)}}\left(X_{m}^{(1-\varepsilon)}-X_{f}{ }^{(1-\varepsilon)}\right) \\
& +\theta\left(\frac{p_{m}}{p_{m i}}\right)^{\theta-1}\left(\frac{1}{p_{m i}}\right)\left(\left(1-p_{m}\right) X_{f}{ }^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right)^{\frac{1}{(1-\varepsilon)}} \\
& =\left(\left(1-p_{m}\right) X_{f}{ }^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right) \frac{\varepsilon}{(1-\varepsilon)} \frac{p_{m}{ }^{\theta-1}}{p_{m i}{ }^{\theta}}\left(\left(\frac{p_{m}}{(1-\varepsilon)}\left(X_{m}{ }^{(1-\varepsilon)}-X_{f}{ }^{(1-\varepsilon)}\right)\right)+\theta\left(\left(1-p_{m}\right) X_{f}{ }^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right)\right) \\
& =\left(\left(1-p_{m}\right) X_{f}{ }^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right)^{\frac{\varepsilon}{1(-\varepsilon)}} \frac{p_{m}{ }^{\theta-1}}{p_{m i}}\left(X_{m}{ }^{(1-\varepsilon)}\left(\theta p_{m}+\frac{p_{m}}{(1-\varepsilon)}\right)+X_{f}{ }^{(1-\varepsilon)}\left(\theta\left(1-p_{m}\right)-\frac{p_{m}}{(1-\varepsilon)}\right)\right) \\
& =\left(\left(1-p_{m}\right) X_{f}^{(1-\varepsilon)}+p_{m} X_{m}{ }^{(1-\varepsilon)}\right)^{\frac{\varepsilon}{(1-\varepsilon)}} \frac{p_{m}{ }^{\theta-1}}{p_{m i}{ }^{\theta}}\left(X_{m}^{(1-\varepsilon)} C_{m}+X_{f}{ }^{(1-\varepsilon)} C_{f}\right) \\
& \text { where } C_{m}=\left(\theta p_{m}+\frac{p_{m}}{(1-\varepsilon)}\right) \text { and } C_{f}=\left(\theta\left(1-p_{m}\right)-\frac{p_{m}}{(1-\varepsilon)}\right)
\end{aligned}
$$

for $\varepsilon<1, C_{m}>0$. So, for $\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial p_{m}\right)>0$ for all values of $X_{f}, X_{m}, C_{f} \geq 0$, implies

$$
\theta\left(1-p_{m}\right) \geq \frac{p_{m}}{(1-\varepsilon)} \Rightarrow \theta \geq \frac{p_{m}}{\left(1-p_{m}\right)} \frac{1}{(1-\varepsilon)} \Rightarrow \theta \geq \frac{p_{m}}{p_{f}} \frac{1}{(1-\varepsilon)}
$$

for $\varepsilon=0.5, p_{m}=0.5, \theta \geq 2$; so $\theta$ should be at least 2 to satisfy the axiom of Monotonicity.
for $\varepsilon>1, C_{f}>0$. So, for $\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial p_{m}\right)>0$, for all values of $X_{f}, X_{m}, C_{m} \geq 0$, implies

$$
\theta p_{m} \geq \frac{p_{m}}{(\varepsilon-1)} \Rightarrow \theta \geq \frac{1}{(\varepsilon-1)}
$$

for $\varepsilon=2, \theta \geq 1$; so $\theta$ to be at least 1 to satisfy the axiom of Monotonicity for $p_{m} \leq p_{m i}$. Similarly, for $p_{m}>p_{m i}$, for $\varepsilon=2$ it can be shown $\theta$ to be at least 1 to satisfy $\left.\left(\partial{ }^{n} X_{\text {ede }}\right) / \partial p_{m}\right)<0$.

## Appendix 3

$W l o g$, for $p_{m} \leq p_{m i}$ Eq. (3) can be expressed in $p_{m}$ ( $p_{f}$ is substituted by $\left(1-p_{m}\right)$ ). For $\varepsilon=2$

$$
{ }^{n} X_{\text {ede }}=\left[p_{m} / p_{m i}\right]^{\theta}\left[\left(1-p_{m}\right)\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right]^{(-1)}
$$

Differentiating with respect to $p_{m}$

$$
\begin{aligned}
& \frac{\partial\left({ }^{n} X_{e d e}\right)}{\partial p_{m}}=\theta \frac{p_{m}^{\theta-1}}{p_{m i}^{\theta}}\left(\left(1-p_{m}\right) X_{f}^{-1}+p_{m} X_{m}^{-1}\right)^{-1}+\left(\frac{p_{m}}{p_{m i}}\right)^{\theta}(-1)\left(\left(1-p_{m}\right) X_{f}^{-1}+p_{m} X_{m}{ }^{-1}\right)^{-2}\left(X_{m}^{-1}-X_{f}^{-1}\right) \\
& \quad=\frac{p_{m}^{\theta-1}}{p_{m i}{ }^{\theta}}\left(\left(1-p_{m}\right) X_{f}{ }^{-1}+p_{m} X_{m}^{-1}\right)^{-1}\left(\theta-\frac{p_{m}\left(X_{f}-X_{m}\right)}{p_{m}\left(X_{f}-X_{m}\right)+X_{m}}\right)
\end{aligned}
$$

Differentiating again and simplifying,

$$
\begin{aligned}
& \frac{\partial^{2}\left({ }^{n} X_{e d e}\right)}{\partial p_{m}{ }^{2}}=\frac{p_{m}{ }^{\theta-2}}{p_{m i}{ }^{\theta}}\left(\left(1-p_{m}\right) X_{f}{ }^{-1}+p_{m} X_{m}{ }^{-1}\right)^{-1} \\
& \\
& \quad\left(\left(\theta-1-\frac{p_{m}\left(X_{f}-X_{m}\right)}{p_{m}\left(X_{f}-X_{m}\right)+X_{m}}\right)\left(\theta-\frac{p_{m}\left(X_{f}-X_{m}\right)}{p_{m}\left(X_{f}-X_{m}\right)+X_{m}}\right)-\frac{p_{m} x_{m}\left(X_{f}-X_{m}\right)}{\left(p_{m}\left(X_{f}-X_{m}\right)+X_{m}\right)^{2}}\right)
\end{aligned}
$$

For $\theta=1, \frac{\partial^{2}\left({ }^{n} X_{e d e}\right)}{\partial p_{m}{ }^{2}}=\frac{p_{m}{ }^{\theta-2}}{p_{m i}{ }^{\theta}}\left(\left(1-p_{m}\right) X_{f}{ }^{-1}+p_{m} X_{m}{ }^{-1}\right)^{-1}(-2) \frac{p_{m} X_{m}\left(X_{f}-X_{m}\right)}{\left(p_{m}\left(X_{f}-X_{m}\right)+X_{m}\right)^{2}}$
Hence, for $X_{f}>X_{m}, \frac{\partial^{2}\left({ }^{n} X_{\text {ede }}\right)}{\partial p_{m}{ }^{2}}<0$, the increase slope is diminishing i.e. the profile is concave.
For $X_{f}<X_{m}, \frac{\partial^{2}\left({ }^{n} X_{\text {ede }}\right)}{\partial p_{m}{ }^{2}}>0$, the slope is convex. Similar proofs can be obtained for $p_{m}>p_{m i}$.

## Appendix 4

$W l o g$, lets consider $X_{m}>X_{f}$. For $p_{m}<p_{m i}$ we need to prove

$$
\left[\left(p_{m} / p_{m i}\right)\left\{\left(1-p_{m}\right)\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]<\left[\left(p_{m} / p_{m i}\right) X\right]
$$

where $X=$ Harmonic Mean of $X_{f}$ and $X_{m}$ at condition of Ideality $p_{m}=p_{m i}, p_{f}=p_{f i}$. Replacing the value of $X$ in the above equation, the proof requires,

$$
\left[\left(p_{m} / p_{m i}\right)\left\{\left(1-p_{m}\right)\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]<\left[\left(p_{m} / p_{m i}\right)\left\{\left(1-p_{m i}\right)\left(X_{f}\right)^{(-1)}+p_{m i}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]
$$

Cancelling the common factor $\left(p_{m} / p_{m i}\right)$, the proof requires,

$$
\left[\left\{\left(1-p_{m}\right)\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]<\left[\left\{\left(1-p_{m i}\right)\left(X_{f}\right)^{(-1)}+p_{m i}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]
$$

The above inequality is true from property (vii) of $X_{\text {ede }}$ as mentioned in Appendix 1. Also this can be seen from Fig. 1 (in the text) where for $p_{m}<p_{m i}, X_{\text {ede }}$ increases with increase of $p_{m}$. Similarly, for $p_{m}>p_{m i}$, the inequality $\left[\left(p_{f} / p_{f i}\right)\left\{\left(1-p_{m}\right)\left(X_{f}\right)^{(-1)}+p_{m}\left(X_{m}\right)^{(-1)}\right\}^{(-1)}\right]>\left[\left(p_{f} / p_{f i}\right) X\right]$ can be proved.

## Appendix 5

| COUNTRY | Life <br> Exp. <br> Female <br> (in yrs) | Life <br> Exp. <br> Male <br> (in yrs) | Sex ratio <br> (males/ females) | Conve <br> ntional <br> Rank | Sex ratio <br> adjusted <br> Rank | Rank Diff. | Gender Prop. Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Iceland | 83.1 | 79.9 | 1.000 | 3 | 1 | 2 | 0.000 |
| Japan | 85.7 | 78.7 | 0.955 | 1 | 2 | -1 | 0.023 |
| Australia | 83.3 | 78.5 | 0.976 | 5 | 3 | 2 | 0.012 |
| Sweden | 82.7 | 78.3 | 0.985 | 7 | 4 | 3 | 0.008 |
| Canada | 82.6 | 77.9 | 0.983 | 8 | 5 | 3 | 0.009 |
| Israel | 82.3 | 78.1 | 0.979 | 10 | 6 | 4 | 0.011 |
| Spain | 83.8 | 77.2 | 0.965 | 6 | 7 | -1 | 0.018 |
| Norway | 82.2 | 77.3 | 0.987 | 12 | 8 | 4 | 0.007 |
| Switzerland | 83.7 | 78.5 | 0.939 | 4 | 9 | -5 | 0.031 |
| Singapore | 81.4 | 77.5 | 1.014 | 14 | 10 | 4 | -0.007 |
| New Zealand | 81.8 | 77.7 | 0.966 | 13 | 11 | 2 | 0.017 |
| Netherlands | 81.4 | 76.9 | 0.986 | 16 | 12 | 4 | 0.007 |
| France | 83.7 | 76.6 | 0.949 | 11 | 13 | -2 | 0.026 |
| Hong Kong, China (SAR) | 84.9 | 79.1 | 0.889 | 2 | 14 | -12 | 0.059 |
| Italy | 83.2 | 77.2 | 0.943 | 9 | 15 | -6 | 0.029 |
| Malta | 81.1 | 76.8 | 0.985 | 17 | 16 | 1 | 0.007 |
| Ireland | 80.9 | 76.0 | 0.989 | 26 | 17 | 9 | 0.005 |
| Greece | 80.9 | 76.7 | 0.977 | 24 | 18 | 6 | 0.012 |
| Austria | 82.2 | 76.5 | 0.956 | 15 | 19 | -4 | 0.022 |
| Belgium | 81.8 | 75.8 | 0.963 | 23 | 20 | 3 | 0.019 |
| Germany | 81.8 | 76.2 | 0.955 | 20 | 21 | -1 | 0.023 |
| Cuba | 79.8 | 75.8 | 1.002 | 32 | 22 | 10 | -0.001 |
| Chile | 81.3 | 75.3 | 0.979 | 28 | 23 | 5 | 0.011 |
| Korea (Republic of) | 81.5 | 74.3 | 1.005 | 29 | 24 | 5 | -0.003 |
| United Kingdom | 81.2 | 76.7 | 0.955 | 21 | 25 | -4 | 0.023 |
| Finland | 82.0 | 75.6 | 0.959 | 22 | 26 | -4 | 0.021 |
| Costa Rica | 80.9 | 76.2 | 1.034 | 25 | 27 | -2 | -0.017 |
| Luxembourg | 81.4 | 75.4 | 0.970 | 27 | 28 | -1 | 0.015 |
| Cyprus | 81.5 | 76.6 | 0.946 | 18 | 29 | -11 | 0.028 |
| Denmark | 80.1 | 75.5 | 0.980 | 31 | 30 | 1 | 0.010 |
| United States | 80.4 | 75.2 | 0.968 | 30 | 31 | -1 | 0.016 |
| Slovenia | 81.1 | 73.6 | 0.953 | 35 | 32 | 3 | 0.024 |
| Portugal | 80.9 | 74.5 | 0.935 | 34 | 33 | 1 | 0.033 |
| Albania | 79.5 | 73.1 | 0.984 | 38 | 34 | 4 | 0.008 |
| Belize | 79.1 | 73.1 | 1.015 | 39 | 35 | 4 | -0.007 |
| Brunei Darussalam | 79.3 | 74.6 | 1.078 | 36 | 36 | 0 | -0.037 |
| Panama | 77.8 | 72.7 | 1.018 | 46 | 37 | 9 | -0.009 |
| Barbados | 79.3 | 73.6 | 0.935 | 37 | 38 | -1 | 0.033 |
| Ecuador | 77.7 | 71.8 | 1.006 | 50 | 39 | 11 | -0.003 |
| Czech Republic | 79.1 | 72.7 | 0.949 | 40 | 40 | 0 | 0.026 |
| Mexico | 78.0 | 73.1 | 0.956 | 44 | 41 | 3 | 0.023 |
| Uruguay | 79.4 | 72.2 | 0.942 | 42 | 42 | 0 | 0.030 |
| Macedonia (TFYR) | 76.3 | 71.4 | 0.996 | 53 | 43 | 10 | 0.002 |
| Argentina | 78.6 | 71.1 | 0.957 | 49 | 44 | 5 | 0.022 |
| Viet Nam | 75.7 | 71.9 | 0.998 | 54 | 45 | 9 | 0.001 |
| Poland | 79.4 | 71.0 | 0.942 | 48 | 46 | 2 | 0.030 |
| Croatia | 78.8 | 71.8 | 0.928 | 45 | 47 | -2 | 0.037 |
| Syrian Arab Republic | 75.5 | 71.8 | 1.013 | 57 | 48 | 9 | -0.007 |
| Tunisia | 75.6 | 71.5 | 1.015 | 58 | 49 | 9 | -0.008 |
| Venezuela (Bolivarian Republic of) | 76.3 | 70.4 | 1.010 | 59 | 50 | 9 | -0.005 |
| Bosnia and Herzegovina | 77.1 | 71.8 | 0.945 | 51 | 51 | 0 | 0.028 |
| Malaysia | 76.1 | 71.4 | 1.031 | 55 | 52 | 3 | -0.015 |
| Slovakia | 78.2 | 70.3 | 0.942 | 52 | 53 | -1 | 0.030 |
| Saint Lucia | 75.0 | 71.3 | 0.963 | 60 | 54 | 6 | 0.019 |
| Libyan Arab Jamahiriya | 76.3 | 71.1 | 1.066 | 56 | 55 | 1 | -0.032 |
| Mauritius | 75.8 | 69.1 | 0.986 | 68 | 56 | 12 | 0.007 |
| Occupied Palestinian Territories | 74.4 | 71.3 | 1.035 | 62 | 57 | 5 | -0.017 |
| Nicaragua | 75.0 | 69.0 | 0.999 | 74 | 58 | 16 | 0.001 |
| Tonga | 73.8 | 71.8 | 1.040 | 64 | 59 | 5 | -0.020 |
| Colombia | 76.0 | 68.7 | 0.977 | 69 | 60 | 9 | 0.012 |
| Jamaica | 74.9 | 69.6 | 0.977 | 71 | 61 | 10 | 0.012 |


| COUNTRY | Life <br> Exp. <br> Female <br> (in yrs) | Life <br> Exp. <br> Male <br> (in yrs) | Sex ratio <br> (males/ females) | Conve ntional Rank | Sex ratio adjusted Rank | Rank Diff. | Gender <br> Prop. <br> Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| China | 74.3 | 71.0 | 1.056 | 65 | 62 | 3 | -0.027 |
| Bulgaria | 76.4 | 69.2 | 0.939 | 63 | 63 | 0 | 0.031 |
| Algeria | 73.0 | 70.4 | 1.018 | 79 | 64 | 15 | -0.009 |
| Dominican Republic | 74.8 | 68.6 | 1.019 | 78 | 65 | 13 | -0.010 |
| Brazil | 75.5 | 68.1 | 0.972 | 76 | 66 | 10 | 0.014 |
| Turkey | 73.9 | 69.0 | 1.016 | 82 | 67 | 15 | -0.008 |
| Bahamas | 75.0 | 69.6 | 0.946 | 70 | 68 | 2 | 0.028 |
| Paraguay | 73.4 | 69.2 | 1.015 | 83 | 69 | 14 | -0.007 |
| Sri Lanka | 75.6 | 67.9 | 1.033 | 77 | 70 | 7 | -0.016 |
| Romania | 75.6 | 68.4 | 0.951 | 73 | 71 | 2 | 0.025 |
| Philippines | 73.3 | 68.9 | 1.014 | 86 | 72 | 14 | -0.007 |
| Saint Vincent and the Grenadines | 73.2 | 69.0 | 0.983 | 87 | 73 | 14 | 0.008 |
| Hungary | 77.0 | 68.8 | 0.909 | 61 | 74 | -13 | 0.048 |
| Egypt | 73.0 | 68.5 | 1.006 | 90 | 75 | 15 | -0.003 |
| Lebanon | 73.7 | 69.4 | 0.961 | 81 | 76 | 5 | 0.020 |
| Peru | 73.3 | 68.2 | 1.011 | 89 | 77 | 12 | -0.005 |
| El Salvador | 74.3 | 68.2 | 0.967 | 84 | 78 | 6 | 0.017 |
| Morocco | 72.7 | 68.3 | 0.988 | 93 | 79 | 14 | 0.006 |
| Jordan | 73.8 | 70.3 | 1.082 | 72 | 80 | -8 | -0.039 |
| Indonesia | 71.6 | 67.8 | 0.997 | 96 | 81 | 15 | 0.001 |
| Iran (Islamic Republic of) | 71.8 | 68.7 | 1.029 | 94 | 82 | 12 | -0.014 |
| uriname | 73.0 | 66.4 | 0.996 | 97 | 83 | 14 | 0.002 |
| Lithuania | 78.0 | 66.9 | 0.874 | 67 | 84 | -17 | 0.067 |
| Samoa | 74.2 | 67.8 | 1.079 | 88 | 85 | 3 | -0.038 |
| Honduras | 73.1 | 65.8 | 1.016 | 99 | 86 | 13 | -0.008 |
| Oman | 76.7 | 73.6 | 1.284 | 47 | 87 | -40 | -0.124 |
| Thailand | 74.5 | 65.0 | 0.965 | 98 | 88 | 10 | 0.018 |
| Cape Verde | 73.8 | 67.5 | 0.920 | 91 | 89 | 2 | 0.041 |
| Saudi Arabia | 74.6 | 70.3 | 1.172 | 66 | 90 | -24 | -0.079 |
| Trinidad and Tobago | 71.2 | 67.2 | 0.973 | 101 | 91 | 10 | 0.014 |
| Guatemala | 73.2 | 66.2 | 0.950 | 95 | 92 | 3 | 0.025 |
| Bahrain | 77.0 | 73.9 | 1.323 | 43 | 93 | -50 | -0.139 |
| Armenia | 74.9 | 68.2 | 0.873 | 80 | 94 | -14 | 0.068 |
| Vanuatu | 71.3 | 67.5 | 1.038 | 100 | 95 | 5 | -0.019 |
| Georgia | 74.5 | 66.7 | 0.896 | 92 | 96 | -4 | 0.055 |
| Latvia | 77.3 | 66.5 | 0.843 | 75 | 97 | -22 | 0.085 |
| Grenada | 69.8 | 66.5 | 0.981 | 105 | 98 | 7 | 0.010 |
| Fiji | 70.6 | 66.1 | 1.034 | 104 | 99 | 5 | -0.017 |
| Estonia | 76.8 | 65.5 | 0.851 | 85 | 100 | -15 | 0.080 |
| Kuwait | 79.6 | 75.7 | 1.500 | 33 | 101 | -68 | -0.200 |
| Uzbekistan | 70.0 | 63.6 | 0.989 | 109 | 102 | 7 | 0.005 |
| Moldova | 72.0 | 64.7 | 0.916 | 103 | 103 | 0 | 0.044 |
| Tajikistan | 69.0 | 63.8 | 0.986 | 110 | 104 | 6 | 0.007 |
| Azerbaijan | 70.8 | 63.5 | 0.943 | 107 | 105 | 2 | 0.029 |
| Maldives | 67.6 | 66.6 | 1.056 | 108 | 106 | 2 | -0.027 |
| Belarus | 74.9 | 62.7 | 0.877 | 102 | 107 | -5 | 0.065 |
| Mongolia | 69.2 | 62.8 | 1.004 | 111 | 108 | 3 | -0.002 |
| Kyrgyzstan | 69.6 | 61.7 | 0.970 | 113 | 109 | 4 | 0.015 |
| Bolivia | 66.9 | 62.6 | 0.993 | 118 | 110 | 8 | 0.003 |
| Sao Tome and Principe | 66.7 | 63.0 | 0.987 | 116 | 111 | 5 | 0.006 |
| Ukraine | 73.6 | 62.0 | 0.847 | 106 | 112 | -6 | 0.083 |
| Bhutan | 66.5 | 63.1 | 1.027 | 117 | 113 | 4 | -0.013 |
| Kazakhstan | 71.5 | 60.5 | 0.920 | 112 | 114 | -2 | 0.042 |
| Comoros | 66.3 | 62.0 | 1.005 | 120 | 115 | 5 | -0.003 |
| Guyana | 68.1 | 62.4 | 0.941 | 114 | 116 | -2 | 0.031 |
| Pakistan | 64.8 | 64.3 | 1.060 | 119 | 117 | 2 | -0.029 |
| Lao People's Democratic Republic | 64.5 | 61.9 | 1.001 | 123 | 118 | 5 | -0.001 |
| Mauritania | 65.0 | 61.5 | 0.979 | 122 | 119 | 3 | 0.011 |
| India | 65.3 | 62.3 | 1.052 | 121 | 120 | 1 | -0.026 |
| Russian Federation | 72.1 | 58.6 | 0.866 | 115 | 121 | -6 | 0.072 |
| Bangladesh | 64.0 | 62.3 | 1.045 | 124 | 122 | 2 | -0.022 |
| Turkmenistan | 67.0 | 58.5 | 0.970 | 126 | 123 | 3 | 0.015 |
| Nepal | 62.9 | 62.1 | 0.982 | 128 | 124 | 4 | 0.009 |


| COUNTRY | Life Exp. Female (in yrs) | Life <br> Exp. <br> Male <br> (in yrs) | Sex ratio <br> (males/ females) | Conve ntional Rank | Sex ratio adjusted Rank | Rank Diff. | Gender Prop. Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Senegal | 64.4 | 60.4 | 0.968 | 127 | 125 | 2 | 0.016 |
| Solomon Islands | 63.8 | 62.2 | 1.069 | 125 | 126 | -1 | -0.033 |
| Yemen | 63.1 | 60.0 | 1.029 | 129 | 127 | 2 | -0.014 |
| Myanmar | 64.2 | 57.6 | 0.986 | 130 | 128 | 2 | 0.007 |
| United Arab Emirates | 81.0 | 76.8 | 2.137 | 19 | 129 | -110 | -0.363 |
| Haiti | 61.3 | 57.7 | 0.971 | 132 | 130 | 2 | 0.015 |
| Ghana | 59.5 | 58.7 | 1.025 | 133 | 131 | 2 | -0.012 |
| Gambia | 59.9 | 57.7 | 0.983 | 134 | 132 | 2 | 0.009 |
| Timor-Leste | 60.5 | 58.9 | 1.081 | 131 | 133 | -2 | -0.039 |
| Qatar | 75.8 | 74.6 | 2.064 | 41 | 134 | -93 | -0.347 |
| Madagascar | 60.1 | 56.7 | 0.990 | 135 | 135 | 0 | 0.005 |
| Togo | 59.6 | 56.0 | 0.976 | 137 | 136 | 1 | 0.012 |
| Sudan | 58.9 | 56.0 | 1.013 | 138 | 137 | 1 | -0.007 |
| Cambodia | 60.6 | 55.2 | 0.935 | 136 | 138 | -2 | 0.033 |
| Papua New Guinea | 60.1 | 54.3 | 1.064 | 139 | 139 | 0 | -0.031 |
| Gabon | 56.9 | 55.6 | 0.991 | 141 | 140 | 1 | 0.004 |
| Eritrea | 59.0 | 54.0 | 0.964 | 140 | 141 | -1 | 0.018 |
| Benin | 56.5 | 54.1 | 1.016 | 143 | 142 | 1 | -0.008 |
| Niger | 54.9 | 56.7 | 1.046 | 142 | 143 | -1 | -0.023 |
| Guinea | 56.4 | 53.2 | 1.051 | 144 | 144 | 0 | -0.025 |
| Djibouti | 55.2 | 52.6 | 0.997 | 146 | 145 | 1 | 0.001 |
| Congo | 55.2 | 52.8 | 0.984 | 145 | 146 | -1 | 0.008 |
| Mali | 55.3 | 50.8 | 0.993 | 147 | 147 | 0 | 0.003 |
| Kenya | 53.1 | 51.1 | 1.003 | 148 | 148 | 0 | -0.001 |
| Ethiopia | 53.1 | 50.5 | 0.990 | 149 | 149 | 0 | 0.005 |
| Namibia | 52.2 | 50.9 | 0.983 | 150 | 150 | 0 | 0.008 |
| Burkina Faso | 52.9 | 49.8 | 1.011 | 151 | 151 | 0 | -0.005 |
| Tanzania (United Republic of) | 52.0 | 50.0 | 0.990 | 152 | 152 | 0 | 0.005 |
| South Africa | 52.0 | 49.5 | 0.965 | 153 | 153 | 0 | 0.018 |
| Chad | 51.8 | 49.0 | 0.979 | 154 | 154 | 0 | 0.010 |
| Equatorial Guinea | 51.6 | 49.1 | 0.980 | 155 | 155 | 0 | 0.010 |
| Cameroon | 50.2 | 49.4 | 0.990 | 156 | 156 | 0 | 0.005 |
| Uganda | 50.2 | 49.1 | 1.001 | 157 | 157 | 0 | -0.001 |
| Burundi | 49.8 | 47.1 | 0.954 | 158 | 158 | 0 | 0.024 |
| Botswana | 48.4 | 47.6 | 0.965 | 159 | 159 | 0 | 0.018 |
| Côte d'Ivoire | 48.3 | 46.5 | 1.034 | 160 | 160 | 0 | -0.017 |
| Nigeria | 47.1 | 46.0 | 1.024 | 161 | 161 | 0 | -0.012 |
| Malawi | 46.7 | 46.0 | 0.986 | 162 | 162 | 0 | 0.007 |
| Guinea-Bissau | 47.5 | 44.2 | 0.976 | 163 | 163 | 0 | 0.012 |
| Congo (Democratic Republic of the) | 47.1 | 44.4 | 0.984 | 164 | 164 | 0 | 0.008 |
| Rwanda | 46.7 | 43.6 | 0.940 | 165 | 165 | 0 | 0.031 |
| Central African Republic | 45.0 | 42.3 | 0.952 | 166 | 166 | 0 | 0.025 |
| Mozambique | 43.6 | 42.0 | 0.938 | 167 | 167 | 0 | 0.032 |
| Sierra Leone | 43.4 | 40.2 | 0.973 | 169 | 168 | 1 | 0.014 |
| Angola | 43.3 | 40.1 | 0.973 | 170 | 169 | 1 | 0.014 |
| Lesotho | 42.9 | 42.1 | 0.870 | 168 | 170 | -2 | 0.070 |
| Zambia | 40.6 | 40.3 | 1.003 | 173 | 171 | 2 | -0.001 |
| Zimbabwe | 40.2 | 41.4 | 0.984 | 172 | 172 | 0 | 0.008 |
| Swaziland | 41.4 | 40.4 | 0.931 | 171 | 173 | -2 | 0.036 |

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[^0]:    ${ }^{1}$ The author thanks an anonymous reviewer, who as one came to know later is Manoj Panda, and Srijit Mishra for their valuable comments and Amarendra Kumar for the useful discussions we had for some of the proofs. This also forms a part of the author's Ph.D. thesis.

[^1]:    ${ }^{2}$ For the expression of $X_{\text {ede }}$, see Section 2 of this paper. The formula for female and male indices is: Index=(actual-minimum)/(maximum-minimum).
    ${ }^{3}$ Life expectancy index is computed by positing a minimum and maximum. The minimum and maximum values for life expectancy at birth (in years) for female are 27.5 and 87.5 and for male, the corresponding figures are 82.5 and 22.5 respectively.
    ${ }^{4}$ The ranks for 173 countries, out of the total 177 countries listed in Human Development Report (HDR) 2007/2008 (UNDP, 2007), are computed on the basis of $X_{\text {ede }}$ of life expectancy. Life expectancy data for four countries Antigua and Barbuda, Dominica, Saint Kitts and Nevis, and Seychelles are not available.

[^2]:    5 'Missing women' is the term coined by Amartya Sen (Sen, 1992) to describe the terrible deficit of women in substantial part of Asia and North Africa due to sex bias in relative care. This term is used in the present paper as an analogy to describe disadvantaged gender which can be male as well. For instance, a country prone to war will have female life expectancy relatively higher due to decimation of men fighting war.
    ${ }^{6}$ The composite indices GDI and GEM are not recalculated here, as aggregated values will be inconclusive on the effect on individual dimensions.

[^3]:    ${ }^{7}$ These properties are noted in Anand and Sen (2003), some in the text, and some in Appendices. For details of the proof of the properties, see the same paper. Here, they are collated together in a tabular form for comparison of the present measure with the proposed one.

[^4]:    ${ }^{8}$ Sex ratio is expressed in this paper as (male population)/(female population)

[^5]:    ${ }^{9}$ Monotonicity, here means in a strong sense.
    ${ }^{10}$ It is not compulsory to assume $p_{f i}=p_{m i}=0.5$. The debate of 'what should be the ideal sex ratio' is out of the scope of the paper. However, axiom of Ideality simply says, $X_{e d e}$ must maximize at given ideal, $p_{f i}, p_{m i}$
    ${ }^{11}$ In general, axiom of Extinction is applicable only to the gender whose ideal proportion of population is non zero. Let us consider a hypothetical specie having ideal population proportion for female and male as 1:0. Here $p_{m}=0$ is the condition for Ideality, so $X_{\text {ede }}$ maximises. The axiom of Extinction is applicable only to female gender i.e. at $p_{f}=0$
    ${ }^{12}$ Under the assumption of unity ideal sex ratio, deviation from ideal can be captured as difference of population-proportion of female and male.

[^6]:    ${ }^{13}$ From Eq. (1) and Eq. (3) ${ }^{n} X_{\text {ede }}=\left[p / p_{i}\right]^{\theta}\left(X_{\text {ede }}\right),\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial \theta\right)=\left(X_{\text {ede }}\right)\left[p / p_{i}\right]^{\theta} \ln \left(p / p_{i}\right)$. Since $\left(p / p_{i}\right) \leq 1,\left(\partial\left({ }^{n} X_{\text {ede }}\right) / \partial \theta\right) \leq 0$
    ${ }^{14}$ Proof is in Appendix 2.

[^7]:    ${ }^{15}$ Proof for $\varepsilon=2, \theta=1$, is in Appendix 3
    ${ }^{16}$ Proof for $\varepsilon=2, \theta=1$, is in Appendix 4

[^8]:    ${ }^{17}$ This resembles to Rawlsian maximin situation where achievement is judged purely by the achievement of the worst off group.
    ${ }^{18}$ The diminishing rate of increase is not valid for all concave functions; but for standard cases like constant relative inequality aversion $\left(X_{\text {ede }}=(1 /(1-\varepsilon)) X^{(1-\varepsilon)}\right)$ and constant absolute inequality aversion $\left(X_{\text {ede }}=-e^{p x x}\right)$ (Anand and Sen, 2003)
    ${ }^{19} E=\left(X_{\text {ede }} / X^{a}\right)$ is the ratio of the $(1-\varepsilon)$ average to the arithmetic mean $(\mathrm{AM})$. The result is intuitive as $(1-\varepsilon)$ average of two numbers is same as AM only when the numbers are equal; in all other cases (1-غ) average $<$ AM.

