

Growth or equality ?

Losers and gainers from financial reform

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Abstract

We explore the consequences of liberalized credit markets for growth and inequality in a lifecycle economy with physical and human capital accumulation, populated by households of different abilities, and calibrated to match the long-run economic performance of a panel of emerging countries. Relatively modest improvements in extending credit to the ablest households appear to have large economic consequences: upfront costs (slower initial growth, higher income inequality) followed by delayed benefits (faster long-run growth). Reform also lowers lifecycle utility for a substantial majority of currently active households. Premature liberalization in the least developed countries (low TFP or capital intensity) may redirect economic growth towards a poverty trap.

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1 Introduction

Trends toward less public regulation of financial markets for household debt are emerging in different parts of the world. Liberalization of financial markets in OECD countries since the eighties is well documented.¹ In less developed countries, financial reform is more a question of creating lending institutions in order to promote investment in human and physical capital. Finally, in Eastern Europe, credit to households is now allowed in some segments of the market, but there is still some way to go.

Behind the slow implementation of reforms and/or the objections raised against liberalized financial markets, we find the idea that there are upfront costs that may be deterring. To understand the foundation of these criticisms, we study the medium and long-term impact of credit reform on the growth and distribution of income in a lifecycle economy populated by agents who differ in their ability to acquire human capital.

In this economy, deregulation amounts to an anticipated lifting of all borrowing constraints on households. We describe the qualitative and quantitative outcomes of this financial “big bang” on incomes, inequality, and on the welfare of particular social groups indexed by age and ability. Our starting point is that borrowing limits do not necessarily ration the poor, as it is assumed in much of the literature (see , e.g., Galor and Zeira (1993) and Piketty (1997)). They may ration instead the most efficient accumulators of human skills, that is, households with high potential income growth.

Important clues to the answer we are seeking are identified in papers by Jappelli and Pagano (1994), De Gregorio (1996), and De Gregorio and Kim (2000), which link market liberalization to economic growth and distribution.² We call these clues the *level effect*

¹Examples of this are higher loan-to-value ratios, increased competition between mortgage institutions and banks, and higher borrowing limits on consumers’ personal debt.

²See also Bencivenga and Smith (1991) and Ljungqvist (1993) who stress information and commitment issues in financial markets.

and the *growth effect* from credit market reforms.

The level effect of financial deregulation is strongest in the short-to-medium run. It reduces *net* household saving, slows down physical capital accumulation, and raises yields in societies without human capital. This mechanism was identified by Jappelli and Pagano (1994), who found some support for it in a panel of OECD countries. They conclude that financial deregulation in the eighties has contributed to the decline in national saving and growth rates in the OECD countries.³

Opposed to the level effect is the growth effect, identified in De Gregorio (1996). It refers to the rise in borrowing for investments in human skills, and the corresponding boost to long-run growth in small open societies which rely on human capital as their growth engine. Evidence for this channel appears to be mixed.

De Gregorio and Kim (2000) also find that financial reform is welfare improving but may raise the dispersion of earnings by permitting the more able to specialize in learning and the less able to specialize in working. As Becker (1964) had suggested, relaxing constraints on society's ablest households contributes to earnings inequality.

This paper is based on the assumption that physical and human capital need to be studied *jointly* both because they oppose each other and because they interact in subtle ways. For example, as the level effect raises yields and lowers wage rates, it will undermine the growth effect and itself by inducing less schooling by unconstrained people and greater labor supply. Without a complete general equilibrium model, it seems very hard to guess how financial reform now will affect output in the medium-run as well as the welfare of each currently living household.

Accordingly, section 2 sets up a simple economy with heterogeneous households, one

³A similar result for LDC's is obtained by Bandiera, Caprio, Honohan, and Schiantarelli (2000) who stress that liberalization - and in particular those elements that relax liquidity constraints - may be associated with a fall in saving. Norman, Schmidt-Hebbel, and Serven (2000) also find that the relaxation of credit constraints leads to a decrease in the private saving rate.

consumption good, and two reproducible inputs – physical capital and human capital. Assuming Cobb-Douglas technology and logarithmic utility, we characterize equilibria with a perfect loan market and with an extreme form of credit rationing, that is, a prohibition on all loans. We prove in section 3 that the return on capital is always higher in the economy with perfect markets. The transitional and long-term response of output and inequality to financial reform depends critically on how common credit rationing was before credit market liberalization.

The remainder of the paper conducts dynamic simulation experiments of financial deregulation in a model calibrated to fit the long-run economic performance of a panel of less developed countries in the 1960's. Specifically, we explore in section 4 the quantitative implications for per capita income growth and the Gini coefficients in these countries. We pay particular attention to the changes in welfare by cohort and ability group. We find that, even when credit constraints initially bind on relatively few people, the macroeconomic consequences of removing these constraints can be large, with upfront costs from a lower capital intensity and delayed benefits from long-term growth. Initial responses to financial deregulation are dictated by the adverse level effect: a decline in the growth of output, coupled with a rise in inequality and in real yields. The growth effect eventually takes over, boosting long-term growth by about one third of one percent per year. The impact of liberalization is adverse for all young households at the time of the reform and also for skilled older people.

The robustness of these results to changes in technology is investigated in section 5. In particular we show that, with CES technologies and low substitutability between capital and labor, financial reform shrinks the basin of attraction to the higher of the two balanced growth states. If the economy considered has a low initial capital/labor ratio, or if its total factor productivity is not high enough, then the lifting of borrowing constraints that comes from financial reform may redirect economic growth towards a

poverty trap. Section 6 sums up the costs and benefits from financial reform and discusses policies that would make liberalization more agreeable to a majority of households.

2 The model

The model is an overlapping generations model in the spirit of Azariadis and Drazen (1990), extending their approach to heterogeneous households and imperfect credit markets. Time is discrete and goes from 0 to $+\infty$. Each generation consists in a continuum of households, with mass expanding at a constant rate $n > -1$.

Each individual lives for two periods, youth and old age. The households of the same generation differ in their innate ability to work when young, ε^y , and when old, ε^o . Their utility function is defined over consumption when adult c_t and consumption when old d_{t+1} :

$$\ln c_t + \beta \ln d_{t+1}, \quad \beta \in \mathbb{R}_+.$$

A share of time λ_t is spent to build up human capital and $1 - \lambda_t$ to work. First-period income is allocated between consumption and savings s_t :

$$\varepsilon^y(1 - \lambda_t)w_t\bar{h}_t = c_t + s_t. \quad (1)$$

The individual variables c_t , s_t , λ_t and d_{t+1} will generally depend on ability. Economy-wide variables are w_t , the wage per unit of human capital, and \bar{h}_t which denotes the average human capital of the old generation at time t . The endowment of efficient labor when young is $\varepsilon^y\bar{h}_t$. Following Azariadis and Drazen (1990), each young person benefits from the average human capital of the previous generation. Old age human capital depends on the time spent on education when young, on the ability when old

ε^0 , and on the average value of the previous generation's human capital:

$$h_{t+1} = \varepsilon^0 \psi(\lambda_t) \bar{h}_t. \quad (2)$$

We think of \bar{h}_t as a measure of teacher quality. As we can see from equation (2), the individual characteristic ε^0 reflects both the ability to work when old and the ability to learn (i.e. to accumulate human capital). The function ψ is assumed increasing, concave and satisfies boundary conditions

$$\lim_{\lambda \rightarrow 0} \psi'(\lambda) = +\infty, \quad \lim_{\lambda \rightarrow 1} \psi'(\lambda) = 0, \quad (3)$$

which ensure that it is always optimal to spend a strictly positive time span building human capital.

The ability type $(\varepsilon^y, \varepsilon^0)$ is distributed over each generation according to a cumulative function G defined on \mathbb{R}_+^2 . The economy-wide average human capital is:

$$\bar{h}_t = \int_0^\infty \int_0^\infty h_t dG(\varepsilon^y, \varepsilon^0).$$

Old agents consume both labor earnings and capital income:

$$d_{t+1} = R_{t+1}s_t + w_{t+1}h_{t+1}. \quad (4)$$

R_{t+1} is the interest factor.

We denote the relative wage by:

$$x_t \equiv \frac{w_{t+1}}{w_t R_{t+1}}.$$

From equations (1), (2) and (4), lifecycle income is proportional to the inherited human

capital \bar{h}_t :

$$\Omega_t = w_t [\varepsilon^Y (1 - \lambda_t) + \mathbf{x}_t \varepsilon^O \psi(\lambda_t)] \bar{h}_t.$$

2.1 Perfect markets equilibrium

Since the duration of schooling λ_t does not enter the utility function, we can solve the household planning problem in two separate steps. The optimal length of schooling maximizes lifecycle income, satisfying the condition:

$$\psi'(\lambda_t) = \frac{\varepsilon^Y}{\varepsilon^O \mathbf{x}_t}. \quad (5)$$

This equation represents the trade-off between studying and working put forward by Ben-Porath (1967). This relationship implies that the length of schooling depends positively on discounted future wage (the benefit from education) and negatively on current wage (the opportunity cost). It also depends positively on the ratio of innate abilities $\varepsilon^O/\varepsilon^Y$. Inverting equation (5) we obtain:

$$\lambda_t = \varphi(\varepsilon^O \mathbf{x}_t / \varepsilon^Y), \quad \varphi' > 0, \quad \varphi(0) = 0.$$

The average human capital of the next period grows at the rate $g_p(\mathbf{x}_t)$, where:

$$\frac{\bar{h}_{t+1}}{\bar{h}_t} = 1 + g_p(\mathbf{x}_t) = \int_0^\infty \int_0^\infty \varepsilon^O \psi(\varphi(\varepsilon^O \mathbf{x}_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^O). \quad (6)$$

Optimal savings are computed by maximizing utility subject to the budget constraints (1) and (4):

$$(1 + \beta) \mathbf{s}_t = \left(\beta \varepsilon^Y (1 - \lambda_t) w_t - \frac{w_{t+1}}{R_{t+1}} \varepsilon^O \psi(\lambda_t) \right) \bar{h}_t. \quad (7)$$

We define the increasing function:

$$\Phi(a) \equiv \varphi(a) + \frac{a}{\beta} \psi(\varphi(a)) \quad \Phi' > 0. \quad (8)$$

This allows us to rewrite savings as:

$$(1 + \beta)s_t = \beta w_t \varepsilon^y (1 - \Phi(\varepsilon^o x_t / \varepsilon^y)) \bar{h}_t. \quad (9)$$

Note that there is a threshold $\tilde{\mu}$ bearing on relative ability $\varepsilon^o / \varepsilon^y$ above which households borrow from financial markets. Indeed, we note from equations (5) and (7) that savings are positive if, and only if, $\beta \varepsilon^y (1 - \lambda_t) \psi'(\lambda_t) > \varepsilon^o \psi(\lambda_t)$. As $\psi(\cdot)$ is increasing in the interval $(0, 1)$ and $\psi'(\lambda_t)(1 - \lambda_t)$ is decreasing in λ_t , this inequality defines a critical value for schooling, $\tilde{\lambda}$, independent of time and such that:

$$\lambda_t < \tilde{\lambda} \Leftrightarrow s_t > 0.$$

Since λ_t is a monotone function $\varphi(\cdot)$ of ability, we can define the ability threshold as a function of the relative wage:

$$\tilde{\mu}_t = \frac{\varphi^{-1}(\tilde{\lambda})}{x_t} \equiv \frac{B}{x_t}. \quad (10)$$

This threshold again separates borrowers from lenders, that is,

$$\frac{\varepsilon^o}{\varepsilon^y} < \tilde{\mu}_t \Leftrightarrow s_t > 0.$$

Hence, households in cohort t with relative ability above $\tilde{\mu}_t$ (or, equivalently, with steeply rising wage profiles) will borrow while other households will lend.

To characterize the equilibrium we equate aggregate saving with the value of the cap-

ital stock. First we compute saving per young household from:

$$\bar{s}_t = \int_0^\infty \int_0^\infty s_t \, dG(\varepsilon^Y, \varepsilon^O) = \frac{\beta}{1+\beta} w_t \bar{h}_t \mathcal{S}_p(x_t). \quad (11)$$

where the function $\mathcal{S}_p(x_t)$ is defined as:

$$\mathcal{S}_p(x_t) = \int_0^\infty \int_0^\infty \varepsilon^Y (1 - \Phi(\varepsilon^O x_t / \varepsilon^Y)) \, dG(\varepsilon^Y, \varepsilon^O).$$

We assume that firms operate a constant return to scale technology $F(K_t, H_t)$ involving capital and labor inputs. Defining the capital – labor ratio as $k_t = K_t/H_t$, and an intensive production function $f(k_t)$, equilibrium factor prices are:

$$\begin{aligned} w_t &= f(k_t) - k_t f'(k_t) = \omega(k_t), \\ R_t &= f'(k_t) = R(k_t). \end{aligned}$$

This allows us to rewrite the relative wage x_t as a function of (k_t, k_{t+1}) :

$$x_t = \frac{\omega(k_{t+1})}{\omega(k_t) R(k_{t+1})}. \quad (12)$$

The total labor supply per young person H_t is obtained by averaging over young and old workers, that is,

$$H_t = \mathcal{H}_p(x_t) \bar{h}_t. \quad (13)$$

where the function $\mathcal{H}_p(x_t)$ is defined as:

$$\mathcal{H}_p(x_t) = \frac{1}{1+n} + \int_0^\infty \int_0^\infty \varepsilon^Y (1 - \varphi(\varepsilon^O x_t / \varepsilon^Y)) \, dG(\varepsilon^Y, \varepsilon^O).$$

Equilibrium in the financial market requires:

$$K_{t+1} = k_{t+1} H_{t+1} = \frac{\bar{s}_t}{1+n},$$

After using equations (6), (11) and (13), we find:

$$\frac{(1+\beta)k_{t+1}}{\beta\omega(k_t)} \mathcal{H}_p(x_{t+1}) = \frac{S_p(x_t)}{1+g_p(x_t)} \frac{1}{1+n} \quad (14)$$

Given initial conditions (k_0, \bar{h}_0) , a perfect foresight equilibrium can be characterized by a non-negative sequence $(x_t, k_{t+1}, \bar{h}_{t+1})_{t \geq 0}$ which solves equations (6), (12) and (14).

This dynamical system can be solved recursively when the production function is Cobb-Douglas, $f(k_t) = Ak_t^\alpha$, with complete depreciation of capital. Then we have:

$$\frac{k_{t+1}}{\omega(k_t)} = \frac{\alpha}{1-\alpha} \frac{\omega(k_{t+1})}{\omega(k_t)R(k_{t+1})} = \frac{\alpha}{1-\alpha} x_t,$$

and equation (14) reduces to a first-order difference equation in x_t :

$$\frac{(1+\beta)\alpha}{(1-\alpha)\beta} \mathcal{H}_p(x_{t+1}) = \frac{1}{x_t} \frac{S_p(x_t)}{1+g_p(x_t)} \frac{1}{1+n}.$$

This equation is analyzed further immediately below.

2.2 Equilibrium with credit rationing

We define an imperfect credit market as an environment in which young households cannot credibly commit their future labor income as a collateral against current loans. As in Kehoe and Levine (1993), we assume that individuals are allowed to borrow up to the point where they are indifferent between repaying loans and suffering market exclusion. Since everyone dies at the end of the second period, default involves no

penalty and is individually optimal. The borrowing constraint then takes a very simple form: $s_t \geq 0$.⁴

We saw in the previous subsection that the households with ability ratio $\varepsilon^o/\varepsilon^y$ above the threshold $\tilde{\mu}_t = B/x_t$ borrow from financial markets. Those households will now be rationed. They will not participate to the credit market, maximizing instead an autarkic utility function of the form:

$$\ln(1 - \lambda_t) + \beta \ln(\psi(\lambda_t)) + \text{constants.}$$

The first order condition is:

$$\psi(\lambda_t) = \beta \psi'(\lambda_t)(1 - \lambda_t).$$

Since $\psi(\cdot)$ is increasing in the interval $(0, 1)$ and $\psi'(\lambda_t)(1 - \lambda_t)$ is decreasing in λ_t , this equation defines a unique solution $\tilde{\lambda}$, which does not depend on prices, nor on ability type. It is the same as the threshold $\tilde{\lambda}$ defined in the previous section.

We can now summarize our results in the following proposition:

Proposition 1 *Households whose ability profiles do not rise fast, i.e. $\varepsilon^o/\varepsilon^y < \tilde{\mu}_t$, save a positive amount given by equation (9); their investment in education λ_t equals $\varphi(\varepsilon^o x_t/\varepsilon^y)$ and depends positively on $\varepsilon^o/\varepsilon^y$. Households with fast rising ability profiles, i.e. $\varepsilon^o/\varepsilon^y > \tilde{\mu}_t$, are credit rationed, and invest the same amount in education, i.e. $\lambda_t = \tilde{\lambda} = \varphi(\tilde{\mu}_t x_t)$.*

Households with a steep potential earnings profile would like to borrow in order to study longer, but credit rationing prevents them from doing so. All others have positive saving and study as long as they wish. Note that the threshold $\tilde{\mu}_t$ depends on

⁴A related formulation, due to Jappelli and Pagano (1994), would be to permit borrowing up to a “natural” debt limit which amounts to a fixed, and typically small, fraction of the present value of future income.

prices through equation (10). For example, when yields are high, there will be fewer constrained households, other things being equal. Hence, although our borrowing constraint is very simple, *the proportion of rationed people depends on prices and hence varies over time.*

In the presence of rationing, the average human capital grows at a rate $g_c(\mathbf{x}_t) = \bar{h}_{t+1}/\bar{h}_t - 1$, that reflects the weight of constrained households, that is:

$$1 + g_c(\mathbf{x}_t) = \int_0^\infty \int_0^{\frac{\varepsilon^Y B}{x_t}} \varepsilon^0 \psi(\varphi(\varepsilon^0 \mathbf{x}_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0) + \psi(\tilde{\lambda}) \int_0^\infty \int_{\frac{\varepsilon^Y B}{x_t}}^\infty \varepsilon^0 dG(\varepsilon^Y, \varepsilon^0). \quad (15)$$

Average saving is:

$$\bar{s}_t = \frac{\beta}{1 + \beta} w_t \bar{h}_t \mathcal{S}_c(\mathbf{x}_t).$$

where the function $\mathcal{S}_c(\mathbf{x}_t)$ is defined as:

$$\mathcal{S}_c(\mathbf{x}_t) = \int_0^\infty \int_0^{\frac{\varepsilon^Y B}{x_t}} \varepsilon^Y (1 - \Phi(\varepsilon^0 \mathbf{x}_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0),$$

instead of the expression in equation (11). Similarly, average labor supply no longer satisfies equation (13); it is given instead by:

$$H_t = \mathcal{H}_c(\mathbf{x}_t) \bar{h}_t$$

where the function $\mathcal{H}_c(\mathbf{x}_t)$ is defined as:

$$\mathcal{H}_c(\mathbf{x}_t) = \frac{1}{1 + n} + \int_0^\infty \int_0^{\frac{\varepsilon^Y B}{x_t}} \varepsilon^Y (1 - \varphi(\varepsilon^0 \mathbf{x}_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0) + (1 - \tilde{\lambda}) \int_0^\infty \int_{\frac{\varepsilon^Y B}{x_t}}^\infty \varepsilon^Y dG(\varepsilon^Y, \varepsilon^0).$$

Labor supply is decreasing in x_t , that is, $\mathcal{H}'_c(\cdot) < 0$, since better earnings prospects

move households from work to school. Financial market equilibrium satisfies:

$$\frac{(1 + \beta)k_{t+1}}{\beta\omega(k_t)} \mathcal{H}_c(\mathbf{x}_{t+1}) = \frac{S_c(\mathbf{x}_t)}{1 + g_c(\mathbf{x}_t)} \frac{1}{1 + n}. \quad (16)$$

Given the initial conditions (k_0, \bar{h}_0) , a perfect foresight equilibrium with credit rationing is again a sequence $(\mathbf{x}_t, k_{t+1}, \bar{h}_{t+1})_{t \geq 0}$ which solves equations (15), (12) and (16).

With the Cobb-Douglas production function, equilibria are solutions to the dynamical system:

$$\frac{(1 + \beta)\alpha}{(1 - \alpha)\beta} \mathcal{H}_c(\mathbf{x}_{t+1}) = \frac{1}{x_t} \frac{S_c(\mathbf{x}_t)}{1 + g_c(\mathbf{x}_t)} \frac{1}{1 + n}, \quad (17)$$

$$k_{t+1} = A\alpha x_t k_t^\alpha. \quad (18)$$

This system is recursive. Equation (17) can first be solved for the path of x_t . Equation (18) is obtained from the definition of x_t in equation (12); it describes the evolution of the capital-labor ratio. The growth rate of human capital is obtained from (15). The solution to (15)-(17)-(18) is summed up in the following result.

Proposition 2 *The system (15)-(17)-(18) has a steady state (x_c, k_c, g_c) and equilibrium is unique in the neighborhood of that state.*

Proof: See appendix.

Q.E.D.

The same reasoning can be applied to the perfect market economy which also possesses a locally unique equilibrium in the neighborhood of the steady state (x_p, k_p, g_p) .

3 Interacting level and growth effects

As a general proposition, it is impossible to show that financial reform will spread inequality and promote long-term growth. For example, liberalization raises yields (see

proposition 3 below) and improves the income of retirees. Since this effect is stronger for less able retirees with relatively high saving, it tends to reduce inequality. What happens to long-term growth depends on how young households weigh the mixed incentives they receive in free financial markets: less credit rationing permits them to invest more in schooling while higher yields on physical capital shrink the present value of future earnings. We first state a key result according to which financial reform reduces aggregate saving and raises yields.

Proposition 3 *Assuming a unique steady state, the economy with perfect markets has a lower long-run capital-labor ratio than the one with imperfect markets.*

Proof: See appendix.

Q.E.D.

To assess the effect of financial reform on the long-run growth rate of per capita output (which equals the long-run growth rate of average human capital), we should compare the perfect market growth rate, $g_p(x_p)$, with the credit-rationed growth rate, $g_c(x_c)$. Two opposite effects interact: for the same long-run yield $1/x$, $g_p(x) > g_c(x)$. Indeed, some agents are constrained in the imperfect market economy, invest less than they want in education and growth is slower. However, as the yield is higher in the perfect market economy ($x_p < x_c$), agents are discouraged from investing in education, and this may or may not outweigh the direct positive effect. The first effect will dominate if there are enough constrained agents in the economy with imperfect markets.

What happens to the short-run growth rate of output depends on the interaction of several factors. First,

the forward-looking relative wage x drops when the reform is announced, and investment in physical capital starts to fall immediately which is bad for short-term growth (level effect). Second, the lifting of the borrowing constraints permits more investment

in education, which is good for growth (growth effect). Third, the supply of labor moves in opposite direction from investment in education, which depresses short-run growth. Last, there are additional dynamic effects when the reform is anticipated. To assess the relative importance of these mechanisms, we must rely on simulations.

4 Dynamic simulations

In the previous section we established that financial reforms which relax the borrowing constraints on households will lower the capital/labor ratio and improve growth in the long-run if the number of constrained households is sufficiently high. However, the transitional impact of these reforms is less clearcut and hard to characterize analytically. In order to study the interplay of long-run and medium-run forces along the transition path, we will rely on simulations of a calibrated version of the model. This will also allow us to assess the quantitative importance of liberalization for growth and inequality.

4.1 Calibration

We first choose functional forms for the production function of human capital and the distribution of abilities. The production of human capital has to satisfy the two limit conditions (3) to guarantee an interior solution for all agents. We use:

$$\psi(\lambda) = b \left(\frac{1}{\gamma} \lambda^\gamma - \lambda \right).$$

The abilities index $(\varepsilon^y, \varepsilon^o)$ is assumed to be distributed over the population according

to a bivariate lognormal distribution; the mean⁵ and variance-covariance matrix of the underlying normal distribution are respectively $(0, 0)$ and

$$\Sigma = \begin{pmatrix} \sigma_Y^2 & \rho \sigma_Y \sigma_O \\ \rho \sigma_Y \sigma_O & \sigma_O^2 \end{pmatrix}$$

Since we have no direct information to calibrate the variance-covariance matrix we carry out a sensitivity analysis of the correlation ρ between the two ability variables and of their relative variance σ_Y^2/σ_O^2 . The scope of the analysis will be restricted by assuming a positive correlation, $\rho > 0$. It also seems reasonable to assume that the ability to work when young is less widely dispersed than the ability to work when old. Indeed, ability in youth only reflects different endowments in efficient labor, while ability in old age also embodied the ability to accumulate human capital. We thus assume $\sigma_Y^2/\sigma_O^2 < 1$. Keeping this ratio constant, the absolute magnitude of the two variances will be chosen to match an income inequality coefficient (see below).

The productivity parameter of the Cobb-Douglas production function A plays no role given that the utility is logarithmic; it only scales the output and capital levels. The capital share parameter α is fixed to $1/3$ according to the consensus in the literature. The psychological discount factor of households is set to 1% per quarter. Assuming that one period of the model is 25 years, we have: $\beta = 0.99^{100} = 0.366$.

For fixed ρ and σ_Y^2/σ_O^2 there are four remaining parameters to calibrate: the growth rate of population n is directly observable; the productivity parameter b governs the long-term growth rate of output per capita; given b , the parameter γ determines the time spent on education in the first period of life; finally, the variance parameter σ_O^2 influences the distribution of income. We chose these parameters so that the steady state of the equilibrium with credit rationing matches some moments of a typical economy

⁵The mean can be normalized without loss of generality.

with imperfect credit markets. This representative economy is obtained from averaging eight economies considered by Bandiera, Caprio, Honohan, and Schiantarelli (2000) as having strongly imperfect credit markets in the sixties. These are Chile, Ghana, Indonesia, Korea, Malaysia, Mexico, Turkey and Zimbabwe.

The average growth rate of population and output is computed over the period 1960-70 using the GDP data of the Penn World Tables. For the share of time devoted to education we assume that the first period of the model covers ages 12-37 and the second one corresponds to ages 37-62. Doing so supposes that secondary and higher education are an alternative to working, but elementary education is not. The percentage of time devoted to schooling is therefore computed by adding the variables "average years of secondary schooling in the total population" and "average years of higher schooling in the total population" from Barro-Lee and dividing them by 25. Finally, we summarize the distribution of income by a Gini index from Deininger and Squire (1996).⁶

These computations lead to the following four moments: an annual growth rate of population of 2.73%, a long-term per capita growth rate of 2.903% per year, a Gini coefficient of 0.458 and a share of time devoted to education of 2.901%. The value of n matching the growth rate of population is $n = 0.962$. The value of the other three parameters depend on the assumptions on ρ and σ_Y^2/σ_0^2 .

Appendix A.4 gives the variance σ_0^2 which matches the Gini coefficient for different combinations of ρ and σ_Y^2/σ_0^2 . The parameters b and γ are picked to match output growth and schooling. Equilibrium outcomes are reported for the percentage of the young population rationed,

$$\int_0^\infty \int_{\frac{\varepsilon^Y B}{x_c}}^\infty \varepsilon^0 dG(\varepsilon^Y, \varepsilon^0),$$

⁶Where possible, the Gini coefficients are from 1970, otherwise we used the closest available year. The Gini in the model is computed over the incomes of both young and old people at steady state.

the saving rate,

$$\frac{1 - \alpha \mathcal{S}_c(\mathbf{x}_c)}{\mathcal{H}_c(\mathbf{x}_c)}$$

and the annual rate of return on capital,

$$\sqrt[25]{1/\mathbf{x}_c} - 1.$$

We draw three conclusions from this sensitivity analysis. First, the percentage of households subject to a borrowing constraint is never large, and reaches at maximum 19%. Second, when the correlation between the two random ability indexes is large, few people are constrained: in that case relative ability $\varepsilon^o/\varepsilon^y$ displays little variation across households and few people want to borrow. Third, the saving rate lies between 8.8% and 9.8%⁷ and the annual rate of return on capital is around 11.2%, whatever variance-covariance matrix we pick.

In order to choose a reasonable variance-covariance matrix Σ , we look at the characteristics of the distribution of income for different parameters values. Appendix A.5 reports income Gini indexes per cohort and the ratio of the mean to the median of the earnings distribution. We chose to use in the sequel $\rho = 0.2$ and $\sigma_y^2/\sigma_o^2 = 0.8$. A correlation of 0.2 seems reasonable given a span of 25 years between the two ability shocks, and the fact that ε^o incorporates the ability to learn while ε^y does not. A relative variance of 0.8 reproduces a ratio of Gini indexes of $0.42/0.53=0.79$ which is close to US data (see Diaz-Gimenez, Quadrini, and Rios Rull (1997)). Figure 1 plots the corresponding density function of abilities. The vertical plane represents the threshold above which people are rationed. Constrained households lie on the left side of the picture and represent 15.5 % of the population; they are those with a high income

⁷This lies below the average saving rate of 15.49% computed from the data of Bandiera, Caprio, Honohan, and Schiantarelli (2000) but seems still acceptable.

growth potential (either low ε^y or high ε^o).

[Figure 1 about here.]

4.2 Response to reform

We now simulate the transition from a steady state with credit rationing to the one in the perfect market economy. The relaxation of the borrowing constraints takes place at time $t = 3$ and is anticipated one period in advance. Time $t = 1$ represents the initial steady state with credit constraints. Figure 2 represents the dynamic path of the three key variables, $(x_t, k_t$ and $g_t^y)$, that is, relative wage, capital/labor ratio and growth rate in per capita income. When liberalization is announced, the relative wage x_t looks forward; it jumps close to the steady state level that will be reached at the time of the reform. This makes future wages less attractive, and discourages investment in human capital at $t = 2$.

Because x_t is also the investment rate, the capital-labor ratio k_t starts declining at $t = 3$. The saving rate drops by half a percent. This decline in the stock of capital is key in explaining the drop in the annual growth rate at $t = 3$ from 2.9% to 2.7% over 25 years.

[Figure 2 about here.]

At $t = 3$ the ablest households are now allowed to borrow, increasing their investment in education and lengthening average schooling from 2.9% to 3.6%. This is not very large but it is sufficient to drive growth above its initial level by about 0.15 percent. A sensitivity analysis of this magnitude to the chosen values of ρ and σ_V^2/σ_0^2 is presented in appendix A.6: the gain is between 0 and 0.30 percent, and depends on the percentage of constrained households in the initial balanced growth path.

What might have happened if we had calibrated on the same set of economies for a different time period, or on an altogether different set of emerging economies? To see how our outcomes are sensitive to parameters, we summarize in table 1 the response of constraints, saving rates, and growth rates as the parameter structure changes relative to the baseline calibration. We conclude that the increase in long-term growth is largest in economies with high schooling and slow population growth, and smallest in economies with high capital share and low initial inequality. Changes typically show weak sensitivity to any single parameter and are almost completely insensitive to the pre-reform growth rate.

[Table 1 about here.]

4.3 The cost of liberalization

[Figure 3 about here.]

To better grasp the cost of this financial reform, Figure 3 plots both the Gini coefficient and the difference between the GDP the economy would have enjoyed without reform and the one with the reform. Inequality peaks at $t = 3$ before stabilizing above its pre-reform level. The long-run effect is essentially explained by the fact that the ablest people can now fully exploit their advantage by going to school longer, implying that old able persons are much richer in the perfect market economy than in the credit constrained one.

The loss of output linked to the fall in physical capital also peaks at $t = 3$. It is around 5% at the time the reform. It takes three periods to catch-up and then overtake the level without reform.

Even though only 15.5% of the population was constrained in the initial state of the economy, financial reform leads to significant effects, both in the medium-run and in the long-run. We conclude that borrowing constraints may have a major impact on economic growth and inequality even if they affect a small fraction of households, provided that those include individuals with high income growth potential.

4.4 Losers and gainers

[Figure 4 about here.]

Gains from financial reform are displayed in Figure 4 which describes the increment in life-cycle utility for members of different cohorts as a function of their abilities. Recall that the reform reduces the wage per unit of human capital from $t = 3$ onwards and rises yields.

Looking first at the generations alive at the time of the liberalization, we can identify two two gainers:

1. The cohort born at $t = 2$ (old at $t = 3$) with low relative ability $\varepsilon^o/\varepsilon^y$ loses almost nothing in wages but do gain from the higher interest rate at $t = 3$; cf. the right side of panel (a).
2. The cohort born at $t = 3$ with high relative ability $\varepsilon^o/\varepsilon^y$ gains from the lifting of the borrowing constraints; cf. the left side of panel (b).

On the contrary, a huge majority of young households born at $t = 3$ (cf. right side of panel (b)) loses from liberalization, primarily because of lower wages per unit of human capital. Since in our model economy there is 1.962 young households for each old one, 32% of the total population living at $t = 3$ gains ($[1.962 \times 11 + 74]/2.962 = 32$).

Looking now at future generations, one out of two children of the generation born in $t = 4$ gain, essentially because they will benefit from the increase in GDP in their old days (see panel (c)). One hundred percent of the grand-children gain (see panel (d)).

5 Reforms and poverty traps

Forty years ago, Arrow, Chenery, Minhas, and Solow (1961) taught us that economic analysis based on a unitary elasticity of substitution between labor and capital often leads to unduly restrictive conclusions. For example, estimates for developed countries consistently find that the elasticity of substitution is not different from unity, but much lower values have been found for LDC's.⁸ This may reflect more limited technological options in emerging economies, i.e., entrepreneurs choosing from the set of technologies in current or local use rather than on the broader set of all potential technologies.

In our specific context, we have two reasons to believe that lower substitution between production factors might affect the adjustment to financial reforms. First, it makes factor prices more sensitive to changes in the capital-labor ratio. Liberalization is thus expected to increase yields in a stronger way and to diminish the growth effect from human capital accumulation.

Second, CES technologies are consistent with poverty traps in the basic overlapping generations model (Azariadis 1996). If the initial capital/labor ratio is low enough, the economy will converge to the trivial steady state with zero capital instead of the one with high capital/labor ratio. In our set-up, *financial reform tends to lower national saving and shrink the basin of attraction of the higher steady state*. As a result, more development

⁸For example, Sosin and Fairchild (1984) find an average elasticity of $1/2$ using a sample of 221 Latin American firms in the seventies.

paths will converge to the poverty trap. This is a powerful argument against reform: if the economy considered has an initial capital/labor ratio close to the region that leads to the poverty trap, the lifting of borrowing constraints that comes from financial reform may drive the economy *out* of the attraction basin of the high steady state.

5.1 Liberalization and the effect on yields

Consider the class of CES production functions,

$$f(k) = A \left(\alpha k^{\frac{\nu-1}{\nu}} + 1 - \alpha \right)^{\frac{\nu}{\nu-1}}$$

with parameters ν , $A > 0$ and $\alpha \in (0, 1)$. We set the elasticity of substitution ν equal to $1/2$, which we regard as a lower bound on the actual elasticity. To better assess the role of the low elasticity of substitution, the parameters b , σ^2 , β and γ keep the same value as in the Cobb-Douglas case. We adjust the parameters A and α in order to obtain a high steady state as close as possible to the previous case both in terms of growth rate and capital share in production. With $A = 53.5$ and $\alpha = 0.425$, we obtain a steady state with imperfect market displaying the same growth and capital share as previously. All the other variables are very close to their level in the Cobb-Douglas case, and 15.8% of young households face borrowing constraints.

[Figure 5 about here.]

[Figure 6 about here.]

Figures 5 and 6 display the response to financial reform that follows the same timing as in the Cobb-Douglas case, i.e., the reform is announced at $t = 2$ and takes place at $t = 3$. Compared to Figures 2 and 3, we find three differences. First, as expected,

the effect on yields is stronger: the return on capital rises from 11% to 11.7% instead of going from 11% to 11.5% as it did in the Cobb-Douglas case. Second, the drop in output at $t = 3$ is almost of the same magnitude as previously, but the long-run gain is *lower*. Third, the gains from the reform take more time to materialize: GDP takes four periods instead of three to catch-up. As a consequence of the weaker growth effect, the long-term gains are much more modest; after 7 periods, GDP is 4% greater than it would be without reform, instead of 10% in the Cobb-Douglas case.

5.2 The perils of premature liberalization

[Figure 7 about here.]

To evaluate more fully how financial reform alters the course of an emerging economy, we need to understand the global dynamics of an economy with credit rationing. This economy is described by equations (12) and (16) which lead to the phase diagram shown in Figure 7. The phaselines $k_{t+1} = k_t$ and $x_{t+1} = x_t$ and the corresponding direction of motions are derived in appendix. Depending on parameter values, the two phaselines may or may not intersect. Figure 7 represents the typical case where there are three steady states; point S_1 is a source and points S_0 and S_2 are saddles. If initial capital is below k_1 , the equilibrium will converge to the trivial steady state S_0 in which there is no production. If it is above, the equilibrium converges to S_2 . Saddle-paths are indicated by bold lines.

Credit market reform does not modify the position of the phaseline $k_{t+1} = k_t$. Using the same arguments as in proposition 2, one can show that reforms moves the phaseline $x_{t+1} = x_t$ downward. Two situations may arise, depending on whether there is a positive steady state under a perfect credit market. This will depend crucially on values of the total factor productivity A and of the rate of time preference.

[Figure 8 about here.]

The bifurcation diagram in figure 8 shows how the existence of steady states and their stability characteristics are sensitive to the value of the total factor productivity A . The annualized capital yield $R(k)$ is on the vertical axis, and total factor productivity on the horizontal one. All other parameters are set at their calibrated values of the previous sub-section. Reading the chart from bottom to top, the solid line indicates the saddlepoint-stable steady state of the economy with rationing. The dashed line above gives the corresponding saddlepoint-stable steady state of the economy with perfect credit market. The vertical distance between the two lines measures the increase in the long-run return on capital caused by the financial reform at each value of total factor productivity.

Dotted lines represent the unstable steady state of the economy with rationing (top) and without rationing (bottom) respectively. These lines also define the attraction basin of the stable steady state: if the economy starts with an initial return $R(k_0)$ outside that basin, then equilibrium will converge to the poverty steady state, and $R(k_t)$ converges to the solid line $f'(0)$. The vertical distance between the two dotted lines measures how much the attraction basin shrinks after the liberalization.

This diagram sums up the economy's response to financial reform in four different regions:

Zone 1: For $A > 40$ (corresponding to a no-liberalization annual growth rate $g^y > 2.62$) liberalization affects the unstable steady state and the attraction basin very little. This is because yields are high at the unstable steady state, and very few agents (less than 1%) are credit rationed there.

Zone 2: For $40 > A > 35.718$ ($2.62 > g^y > 2.34$), liberalization shrinks the basin of attraction a bit more. If reform occurs when the economy is close to the low steady

state, then liberalization will drive the equilibrium into the poverty trap.

Zone 3: For $35.718 > A > 35.1579$ ($2.34 > g^y > 2.17$), there is *no* steady state for the economy with complete markets. In this case, liberalization will lead the economy into the poverty trap for *any* initial value of the capital-labor ratio.

Zone 4: For $A < 35.1579$, there is no positive steady state. The economy will converge to the poverty trap with or without reform.

The third zone describes a “premature” liberalization. An economy with a total factor productivity in this range should first build up its TFP by promoting structural microeconomic reforms before attempting financial reform. Note that this range does not correspond to totally unreasonable values of the endogenous variables. For example, with $A = 35.4$, the steady state with imperfect markets has a return rate on capital of 14.5%, a capital share in output of 60%, and a growth rate of 2.28%.

6 Conclusions and policy implications

Here is a review of our conclusions about the medium and long-run consequences of financial reform, followed by some thoughts on redistributive policies that spread the benefits of liberalization more evenly among different age and ability groups.

6.1 Costs and benefits

Financial reform in this paper amounts to abolishing credit constraints on the most efficient human capital accumulators of an emerging economy. Calibrating the model to match the long-run operating characteristics (schooling, growth rate, income distribution) of a panel of eight economies in the sixties, we find that reform:

1. Eases constraints on individuals with rising lifetime ability profiles (15% of the population), accelerating long-term growth by about 0.15 percent per year.
2. Reduces the household saving rate permanently, and lowers the GDP growth rate temporarily by 0.3% per year, relative to the no-reform path. Post-reform output does not recover fully until several periods later, when the impact of higher skills overcomes the weakness of aggregate savings.
3. Raises income inequality by a permanent margin.
4. Lowers the lifecycle utility of nine out of ten people aged 12-37 at the time of reform as well as the ablest 25% among the older group aged 37-62. Without some type of compensation scheme, the losers from reform represent about two-third of all economically active households.
5. Improves the welfare of half the generation born at the time of the reform and of all members in all cohorts born later.
6. May permanently change for the worse the growth path of least developed economies, if it occurs prematurely, that is, before total factor productivity becomes large enough. In particular, if the capital-labor elasticity of substitution is near $1/2$, and physical capital and factor productivity are both low enough to drive the annualized net yield on capital up to 15%-17%, then a financial reform of the type we consider here alters the course of economic growth permanently. Instead of converging to its pre-reform steady state yield of 14%-15%, the post-reform economy is diverted to a poverty trap with an annualized capital yield of nearly 19%.

Even if we ignore the increased potential for a poverty trap, most rational households in the economy we describe would object to financial reform as we defined it. It comes

as no surprise to us that opposition to less regulation and more competition in financial markets is so strong in actual economies; we are rather intrigued by the observation that majorities occasionally agree to reforms. Arguments in favor of reform are that altruism sways people to reckon the benefits that accrue to their descendants, and transfers from gainers persuade the losers to drop their objections.

6.2 Compensating the losers

The timing of gains and losses suggests that public debt is one device which may allow all generations to share the gains from reform. In particular suppose that the government pays subsidies to currently active households, by issuing public debt which will be repayed slowly by taxing future generations.

Public debt will typically crowd out capital, amplifying the adverse level effect of the reform in the medium-run and undermining the favorable long-run growth effect. How to strike the right balance between medium-term redistribution and long-term incentives is an open issue for economic policy.

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A Appendix

A.1 Proof of Proposition 2

Proof: To prove this result we show that there is a steady state in the dynamics of x_t given by equation (17), and that it is locally unstable. If this is true, the only possibility consistent with the existence of an equilibrium with perfect foresight is for the forward-looking variable x_t to be at steady state x for all $t \geq 0$. Given that $x_t = x_c \forall t$, the dynamics of k_t given by (18) converge monotonically to the steady state.

Equation (17) can be written

$$J(x_{t+1}) = H(x_t).$$

Computing the limits of these functions on their interval of definition we find

$$J(0) = \frac{(1+\beta)\alpha}{(1-\alpha)\beta} \frac{2+n}{1+n} > J(\infty) = \frac{(1+\beta)\alpha}{(1-\alpha)\beta} \left(\frac{2+n}{1+n} - \tilde{\lambda} \right)$$

$$H(0) = +\infty > H(\infty) = 0$$

Given that $H(0) > J(0)$ and $H(\infty) < J(\infty)$, there is a steady state x such that $J(x) = H(x)$. The local instability of x is guaranteed by $-H'/J' > 1$. Q.E.D.

A.2 Proof of Proposition 3

Proof: To compare the steady states in the two economies we define the functions

$$T(x, i) = (1+n) \frac{(1+\beta)\alpha}{(1-\alpha)\beta} \left(\int_0^\infty \int_0^{i\varepsilon^Y} \varepsilon^0 \psi(\varphi(\varepsilon^0 x_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0) + \psi(\tilde{\lambda}) \int_0^\infty \int_{i\varepsilon^Y}^\infty \varepsilon^0 dG(\varepsilon^Y, \varepsilon^0) \right) x$$

$$W(x, i) = \frac{\int_0^\infty \int_0^{i\varepsilon^Y} \varepsilon^Y (1 - \Phi(\varepsilon^0 x_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0)}{\frac{1}{1+n} + \int_0^\infty \int_0^{i\varepsilon^Y} \varepsilon^Y (1 - \varphi(\varepsilon^0 x_t / \varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^0) + (1 - \tilde{\lambda}) \int_0^\infty \int_{i\varepsilon^Y}^\infty \varepsilon^Y dG(\varepsilon^Y, \varepsilon^0)}$$

The steady state x_p of the perfect market economy is characterized by $T(x_p, \infty) = W(x_p, \infty)$. The one of the economy with credit rationing x_c is given by $T(x_c, B/x_c) = W(x_c, B/x_c)$.

The function T is increasing in both of its arguments. To evaluate the sign of the derivatives of $W(\cdot)$, we replace the function Φ by its value from (8), and we obtain after some manipulations:

$$1 - W(x, i) = \frac{1 + \int_0^\infty \int_0^{i\varepsilon^Y} \frac{\varepsilon^O x}{\beta} \psi(\varphi(\varepsilon^O x/\varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^O) + \frac{B}{\beta} \psi(\tilde{\lambda}) \int_0^\infty \int_{i\varepsilon^Y}^\infty dG(\varepsilon^Y, \varepsilon^O)}{\frac{1}{1+n} + \int_0^\infty \int_0^{i\varepsilon^Y} \varepsilon^Y (1 - \varphi(\varepsilon^O x/\varepsilon^Y)) dG(\varepsilon^Y, \varepsilon^O) + (1 - \tilde{\lambda}) \int_0^\infty \int_{i\varepsilon^Y}^\infty \varepsilon^Y dG(\varepsilon^Y, \varepsilon^O)},$$

which is increasing in x for fixed i and increasing in i for fixed x . We deduce that the function W is decreasing in both of its arguments.

Hence the condition $T(x, i) - W(x, i) = 0$ defines an implicit function

$$x = Q(i) \quad \text{with } Q' < 0.$$

Since i is infinite in the perfect market case and finite in the imperfect case, we obtain that $x_p < x_c$. Using (18) which holds for both economies, we obtain that the capital/labor ratio is lower in the perfect market economy. Q.E.D.

A.3 Phase diagram

The first relationship, equation (12),

$$x_t = \frac{\omega(k_{t+1})}{\omega(k_t) R(k_{t+1})},$$

describes an implicit function

$$k_{t+1} = \Gamma(k_t, x_t), \quad \Gamma_k > 0, \quad \Gamma_x > 0,$$

which is increasing in each argument. Note also that $\Gamma(0, x) > 0$ for any $x > 0$, because, for any CES production function with $\nu < 1$, $R(k)$ is bounded from above.

The locus of points where $k_{t+1} = k_t$ is defined by $x_t = 1/R(k_t)$, which is increasing and has a positive intercept $1/f'(0)$ for an elasticity of substitution $\nu < 1$. Above this line $k_{t+1} > k_t$ because Γ is increasing in x_t .

The second relationship $x_{t+1} = \Psi(k_t, x_t)$ is derived from equation (16) where k_{t+1} has been replaced by $\Gamma(k_t, x_t)$:

$$\frac{1 + \beta}{\beta} \mathcal{H}_c(x_{t+1}) = \frac{\mathcal{S}_c(x_t)}{1 + g_c(x_t)} \frac{\omega(k_t)}{(1 + n)\Gamma(k_t, x_t)}. \quad (19)$$

The LHS of this relation is decreasing in x_{t+1} while the RHS is decreasing in x_t . Furthermore, for any elasticity of substitution $\nu < 1$, one can show that $\omega(k)/\Gamma(k, x)$ is increasing in k for each fixed x . It follows that the function $\Psi(k, x)$ is decreasing in k and increasing in x :

$$x_{t+1} = \Psi(k_t, x_t), \quad \Psi_k < 0, \quad \Psi_x > 0.$$

The locus of points where $x_{t+1} = x_t$ defined by $x_t = \Psi(k_t, x_t)$ has a zero intercept: for any $x > 0$, the fact that $\Gamma(0, x) > 0$ implies that $x = 0$ is the only solution to the equation $x = \Psi(0, x)$. Furthermore, repeating the arguments in the proof of Proposition 2, we can show that $\Psi_x(k, x) > 1$ for each fixed k . In addition, the equation $x = \lim_{k \rightarrow \infty} \Psi(k, x)$ has a bounded solution in x . Therefore, the phaseline $x_{t+1} = x_t$ is upward sloped, starting below the phaseline $k_{t+1} = k_t$ at $k_t = 0$, and ending below it as $k_t \rightarrow \infty$.

A.4 Sensitivity analysis with respect to Σ

Calibrated value of σ_o^2

ϱ	σ_Y^2/σ_o^2				
	0.2	0.4	0.6	0.8	1.0
0.0	1.45	1.07	0.88	0.74	0.64
0.2	1.44	1.09	0.89	0.74	0.65
0.4	1.44	1.09	0.90	0.76	0.65
0.6	1.44	1.11	0.90	0.77	0.68
0.8	1.42	1.11	0.92	0.78	0.69

Rationed households (% of population)

ϱ	σ_Y^2/σ_o^2				
	0.2	0.4	0.6	0.8	1.0
0.0	14.2	15.8	17.2	18.1	18.8
0.2	12.4	13.6	14.6	15.6	16.3
0.4	10.3	10.8	11.6	12.4	13.1
0.6	8.0	7.6	7.7	8.3	8.9
0.8	5.4	3.7	3.1	3.0	3.4

Saving rate

ρ	σ_Y^2/σ_O^2				
	0.2	0.4	0.6	0.8	1.0
0.0	9.4	9.6	9.7	9.8	9.8
0.2	9.3	9.4	9.5	9.6	9.7
0.4	9.1	9.3	9.4	9.5	9.6
0.6	9.0	9.1	9.2	9.4	9.5
0.8	8.8	8.9	9.1	9.2	9.4

Annual return on capital

ρ	σ_Y^2/σ_O^2				
	0.2	0.4	0.6	0.8	1.0
0.0	11.2	11.1	11.1	11.0	11.0
0.2	11.3	11.2	11.1	11.1	11.0
0.4	11.3	11.3	11.2	11.2	11.1
0.6	11.4	11.3	11.3	11.2	11.2
0.8	11.5	11.4	11.4	11.3	11.2

A.5 Income distribution as a function of Σ

Mean to median ratio for all earnings

ϱ	σ_Y^2/σ_O^2				
	0.2	0.4	0.6	0.8	1.0
0.0	1.29	1.37	1.40	1.41	1.42
0.2	1.30	1.35	1.39	1.43	1.42
0.4	1.30	1.36	1.40	1.40	1.44
0.6	1.29	1.37	1.41	1.43	1.42
0.8	1.28	1.36	1.40	1.43	1.44

Earnings Gini – young generation

ϱ	σ_Y^2/σ_O^2				
	0.2	0.4	0.6	0.8	1.0
0.0	0.30	0.36	0.40	0.42	0.43
0.2	0.30	0.36	0.40	0.42	0.44
0.4	0.30	0.36	0.40	0.42	0.44
0.6	0.29	0.36	0.40	0.43	0.43
0.8	0.29	0.36	0.40	0.42	0.45

Earnings Gini – old generation

ϱ	σ_Y^2/σ_o^2				
	0.2	0.4	0.6	0.8	1.0
0.0	0.70	0.62	0.57	0.52	0.49
0.2	0.69	0.62	0.56	0.53	0.49
0.4	0.70	0.62	0.56	0.53	0.49
0.6	0.71	0.62	0.57	0.52	0.48
0.8	0.71	0.62	0.56	0.52	0.47

A.6 Growth effect as a function of Σ

Output growth in the perfect market economy

ϱ	σ_Y^2/σ_o^2				
	0.2	0.4	0.6	0.8	1.0
0.0	3.30	3.19	3.15	3.11	3.09
0.2	3.25	3.12	3.09	3.05	3.02
0.4	3.19	3.08	3.04	3.02	3.00
0.6	3.13	3.01	2.98	2.96	2.95
0.8	3.06	2.94	2.92	2.91	2.91

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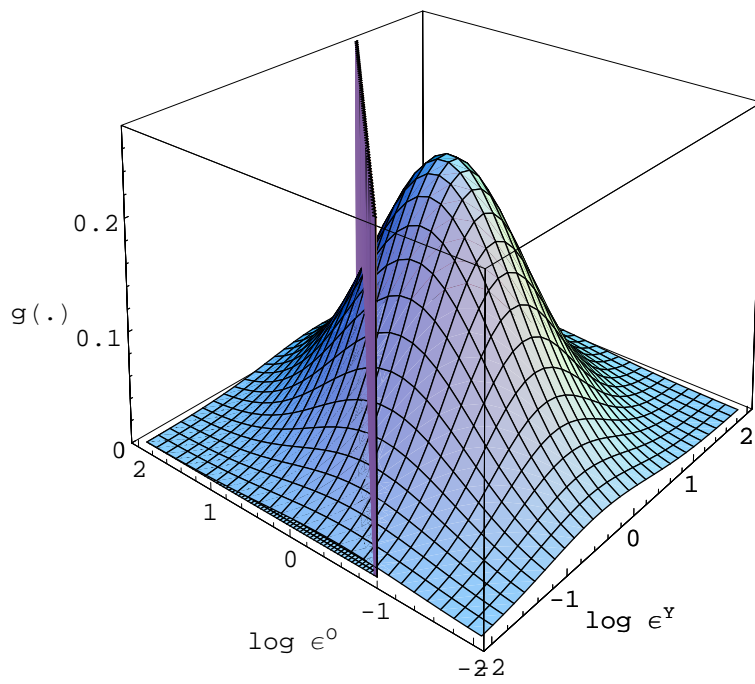


Figure 1: The distribution of abilities and rationed households

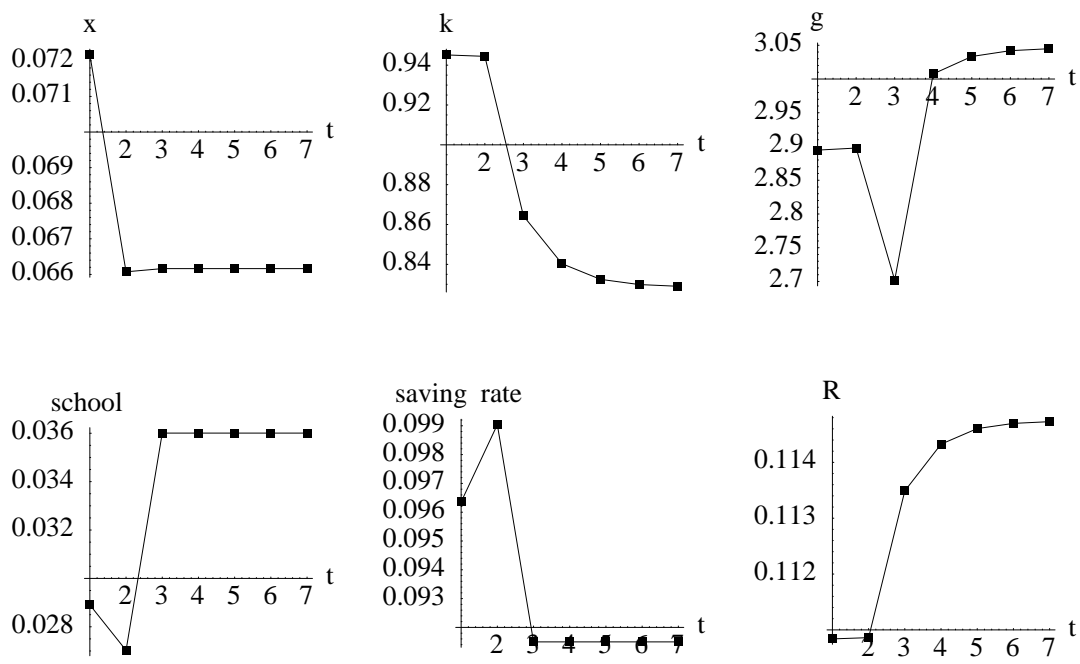


Figure 2: Dynamic responses to reform

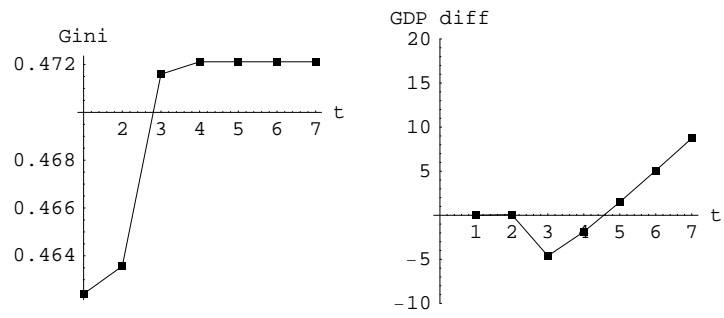
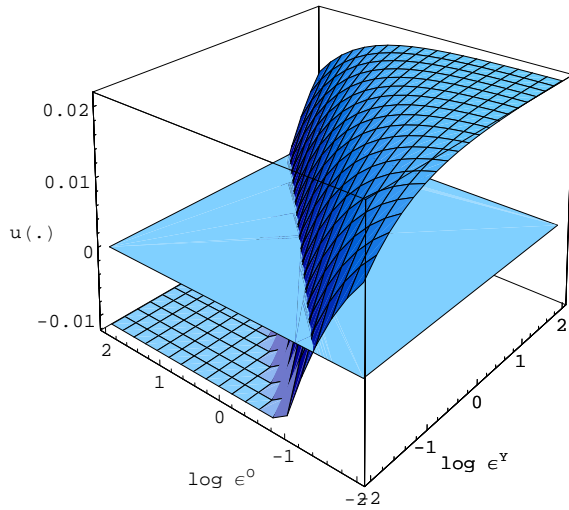
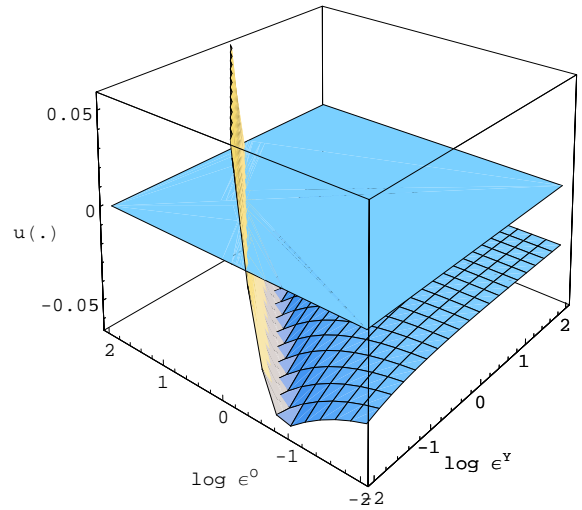


Figure 3: Costs of liberalization

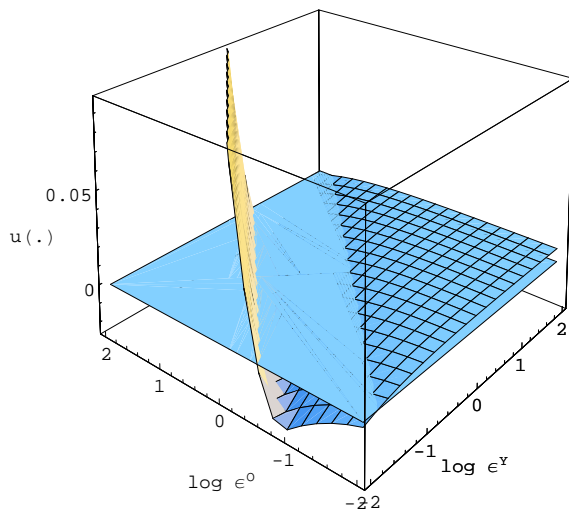
Panel (a)
Cohort born at $t = 2$ (74% of gainers)



Panel (b)
Cohort born at $t = 3$ (11% of gainers)



Panel (c)
Cohort born at $t = 4$ (52% of gainers)



Panel (d)
Cohort born at $t = 5$ (100% of gainers)

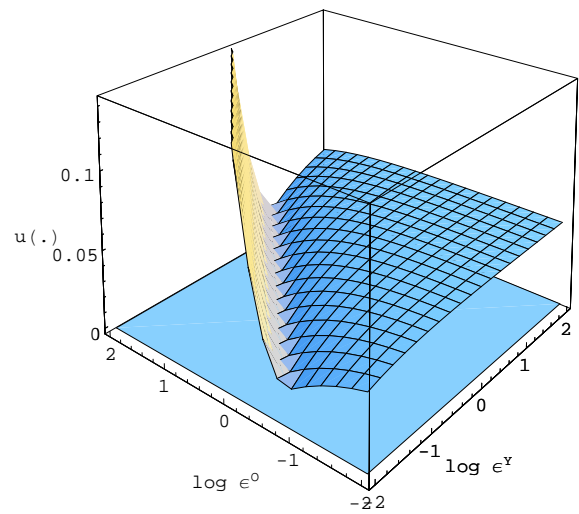


Figure 4: Gains in lifecycle utility by cohorts

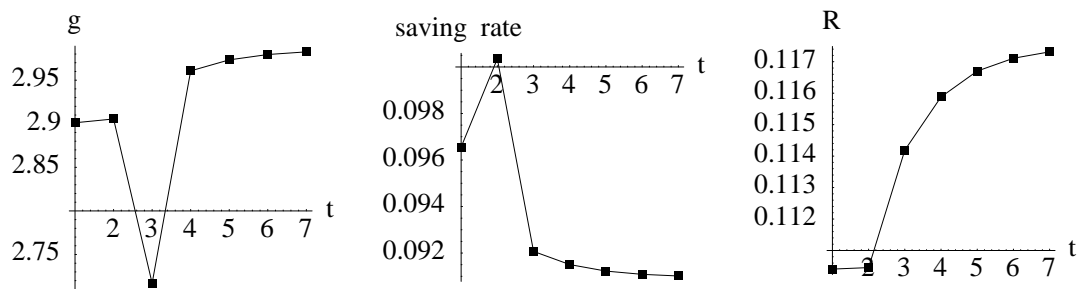


Figure 5: Dynamic responses to reform - CES case

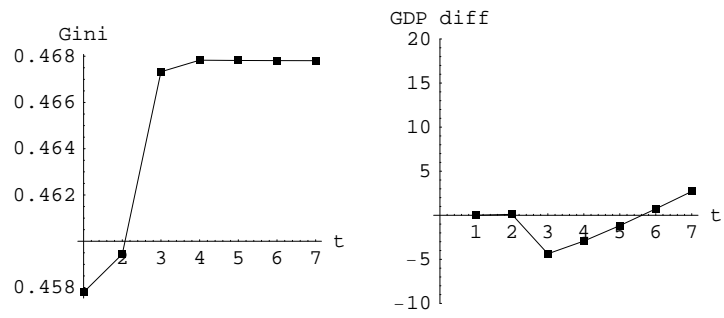


Figure 6: Costs of liberalization - CES case

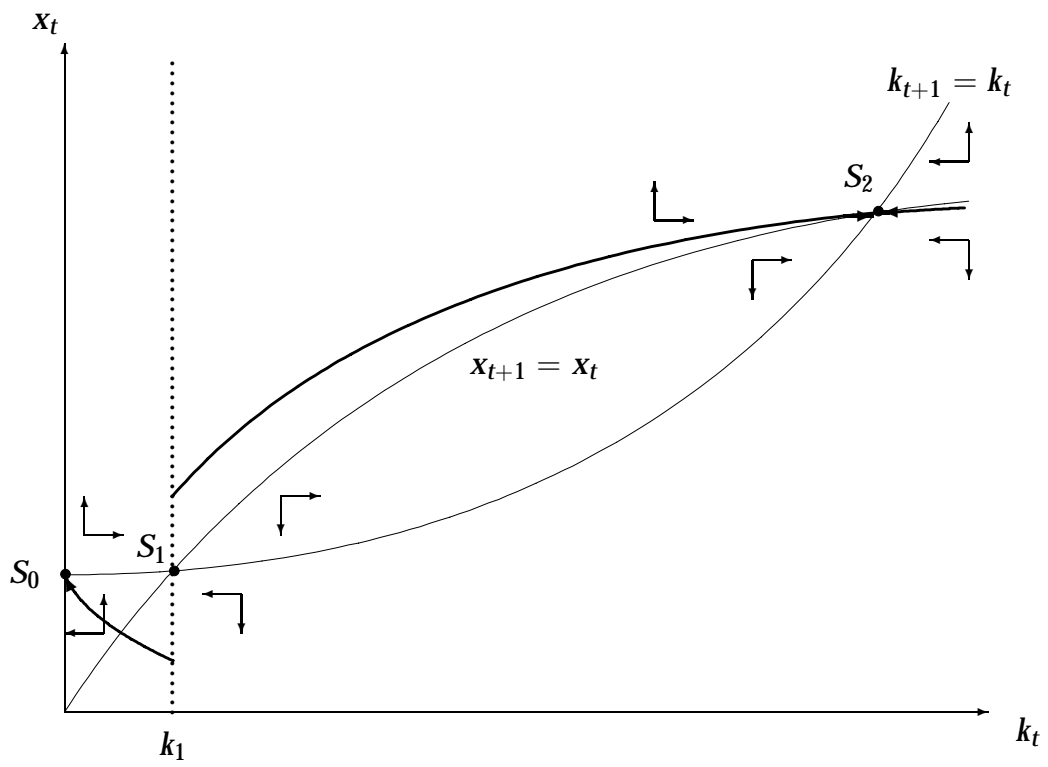


Figure 7: Phase diagram – CES case

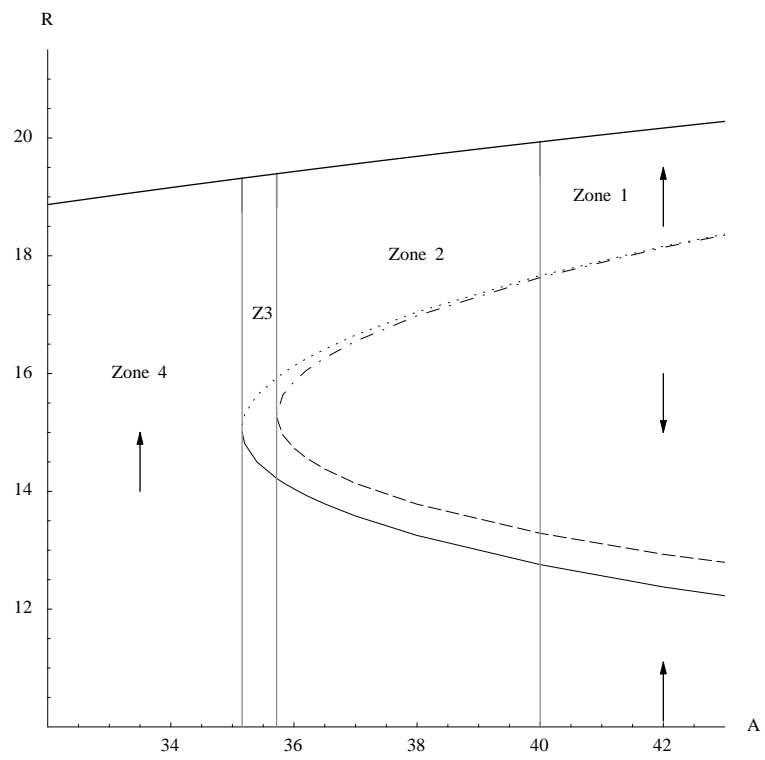


Figure 8: Bifurcation diagram for financial reforms

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1 Sensitivity analysis 48

	γ	B	σ_O^2	% constr.	saving rate	drop in saving r.	gain in growth
Baseline case	0.234	0.739	0.74	15.5	9.6	-0.5	+ 0.15
More schooling (5% instead of 2.9%)	0.456	2.694	0.67	18.8	9.5	-0.6	+0.27
Slower popul. growth (1.6% instead of 2.9%)	0.210	0.619	0.74	18.0	8.5	-0.5	+0.17
Higher capital share ($\alpha = 1/2$)	0.370	1.982	0.67	8.2	8.1	-0.2	+0.08
Less inequality (Gini=0.35)	0.232	0.877	0.41	10.5	8.8	-0.3	+ 0.07
Less output growth (1.5% instead of 2.9%)	0.234	0.523	0.75	15.6	9.6	-0.5	+0.15
More patience ($\beta = .995^{100}$)	0.152	0.359	0.77	12.1	14.0	-0.5	+0.08

Table 1: Sensitivity analysis