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Lo, W.C., Chan, C.C., Zhu, Z.Q. et al. (3 more authors) (2000) Acoustic noise radiated by PWM-controlled induction machine drives. *IEEE Transactions on Industrial Electronics*, 47 (4). pp. 880-889. ISSN 0278-0046

<https://doi.org/10.1109/41.857968>

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Acoustic Noise Radiated by PWM-Controlled Induction Machine Drives

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Abstract—This paper investigates the acoustic noise radiated from two nominally identical induction motors when fed from sinusoidal, and asymmetric regular sampling subharmonic and space-vector pulsewidth modulation (PWM) converters. The theory for analyzing the noise spectrum is developed further to account for the interaction between the motor and the drive. It is shown that manufacturing tolerances can result in significant differences in the noise level emitted from nominally identical motors, and that mechanical resonances can result in extremely high noise emissions. Such resonances can be induced by stator and rotor slot air-gap field harmonics due to the fundamental component of current, and by the interaction between the airgap field harmonics produced by the fundamental and the PWM harmonic currents. The significance of the effect of PWM strategy on the noise is closely related to the mechanical resonance with vibration mode order zero, while the PWM strategy will be critical only if the dominant cause of the emitted noise is the interaction of the fundamental air-gap field and PWM harmonics.

Index Terms—Acoustic noise measurement, induction motors, pulsewidth modulated inverters.

NOMENCLATURE

$b(\theta, t)$	Air-gap flux density harmonic components.
f_1	Operating frequency of the motor.
f_k	Frequency of k th current harmonics.
f_s	Switching frequency.
k, k th	Current harmonic order.
m	Mode order.
p	Number of pole pairs of the motor.
$F(\theta, t)$	Air-gap MMF.
F_1	Fundamental air-gap MMF wave produced by the fundamental current.
F_k	First-order MMF harmonics due to the k th current harmonics.
F_μ	Higher order MMF harmonics produced by the fundamental current of the rotor $\mu = q_2 Q_r + \nu, q_2 = 0, \pm 1 \pm 2, \dots$
F_ν	Higher order MMF harmonics produced by the fundamental current of the stator $\nu = (6q + 1)p, q =$

$F_{\mu k}$	Higher order MMF harmonics produced by the k th current harmonics of the rotor.
$F_{\nu k}$	Higher order MMF harmonics produced by the k th current harmonics of the stator.
Q_s	Slot number of stator.
Q_r	Slot number of rotor.
s_k	Slip of the k th time harmonic.
φ_{m0}	Phase angle of the vibration force density wave for mode order m .
$\lambda(\theta, t)$	Air-gap permeance.
μ, μ th	Rotor slot harmonics.
ν, ν th	Stator slot harmonics.
$\sigma_r(\theta, t)$	Vibration force density wave.
σ_m	Amplitude of the vibration force density wave for mode order m .
ω_1	Fundamental angular frequency of the supply.
ω_k	Angular frequency of the k th current harmonic.
ω_m	Angular frequency for mode order m .
ω_r	Mechanical angular frequency of the rotor.
$\omega_{\mu k}$	Harmonic angular frequency for $F_{\mu k}$.
ω_μ	Harmonic angular frequency for F_μ .
$\Lambda_0,$	Amplitudes of permeance related to the average air-gap length.
Λ_{k1}	Amplitudes of permeance related to the stator slotting.
Λ_{k2}	Amplitudes of permeance related to the rotor slotting.

I. INTRODUCTION

THE acoustic noise radiated by induction machines increases when they are operated from nonsinusoidal power supplies, such as quasi-square waveform and pulsewidth modulation (PWM) converters [1], [2]. This can be of considerable significance in certain applications, for example, when they are employed as traction machines in the drivetrain of electric vehicles. Since the total harmonic distortion is then increased, the emitted acoustic noise level can become unacceptable. However, although the effect of nonsinusoidal supplies on the acoustic noise has been addressed extensively [3]–[9], and various PWM strategies, such as natural sampling, asymmetrical regular sampling, harmonic elimination, optimal, space vector, and random PWM, have been developed primarily to reduce harmonic distortion and improve efficiency, their effect on noise emissions has been largely restricted to a consideration of the

Manuscript received June 23, 1999; revised January 22, 2000. Abstract published on the Internet April 21, 2000.

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Publisher Item Identifier S 0278-0046(00)06821-0.

switching noise of the drive, with relatively little consideration of their interaction with the machines.

In order to compare the relative merits of different PWM strategies, an equivalent A -weighted total harmonic distortion (THD) is introduced for noise estimation [3], viz., $\text{THD}_v = \sqrt{\sum (A_n V_n / V_1)^2} 100\%$ or $\text{THD}_i = \sqrt{\sum (A_n I_n / I_1)^2} 100\%$ where V_1 , I_1 , and V_n , I_n are the fundamental and harmonic components of the output voltage and current, and A_n is the A -weighted curve accounting for the nonlinear response of the human ear to the sound pressure level. For conventional THD $A_n = 1$, which is appropriate only in relation to a consideration of system losses, and is not appropriate when estimating the magnetic noise caused by harmonic components. Clearly, the equivalent A -weighted THD accounts for: 1) the harmonic voltage/current spectrum and 2) the acoustic behavior of the human ear. However, it still cannot account for mechanical resonances.

Both harmonic-eliminated and optimal PWMs with minimal harmonic content often result in reduced losses as well as a lower acoustic noise level [3]. However, as mentioned above, it is important to consider the A -weighted sound pressure level both for the switching harmonics and the natural frequencies. Bearing in mind that the current harmonics of a PWM-controlled drive are usually rich, while the relationship between the acoustic noise and current harmonics is nonlinear, both techniques may be very effective for a specific machine under constant speed operation, and they are not generally applicable and also difficult to realize for variable-speed drives.

Random PWM [4] disperses the tonal spectrum of a fixed-frequency switching PWM inverter drive into a wide-band atonal noise. Hence, it significantly reduces the subjective annoyance associated with the acoustic noise emitted from an inverter driven motor. The overall sound pressure level is largely unchanged with random switching, with any reduction arising from the nonexcitation of resonances which might previously be excited with fixed frequency switching [5]. In general, if a motor is operated from a random PWM converter: 1) the benefits will be insignificant if the motor noise is dominated by a resonance excited by the fundamental component of current; 2) the noise can be reduced significantly if the motor exhibits a resonance which is excited by the force due to the interaction of the fundamental component of current and PWM subharmonics; and 3) the noise may be increased, since random PWM may increase the probability of inducing mechanical resonances. Alternatively, by using music PWM techniques, otherwise arbitrary noise is converted into selected information, such as music, alarm, etc. Since the corresponding vibration and noise frequency will be centered around $2f_s$ and f_s , the switching frequency f_s should be equal to either the desired frequency or half of this frequency [6] in order to generate magnetic noise with the desired music frequency. However, since there are usually lots of noise components, in addition to those produced by the dominant current harmonics, the music effect is usually less than satisfactory.

One simple method to reduce the effect of acoustic noise is to use ultrasonic switching [7] which effectively shifts the PWM harmonics out of the human audible frequency range (>20 kHz). It is, therefore, most desirable. However, current power

semiconductor switch technology limits this to low power levels using MOSFETs, since high switching frequency results in high switching losses in insulated gate bipolar transistors (IGBTs) and MOSFET-controlled thyristors (MCTs). A resonant converter facilitates ultrasonic frequency switching and thereby provides another potential for acoustic noise reduction [1]. Another method of reducing the noise from PWM controlled drives is to make sinusoidal output waveforms using filters which are connected to inverter output terminals [8]. However, although they are always beneficial, not all harmonics can be sufficiently eliminated since the magnetic noise is caused by the least residual harmonics, which cannot be absorbed by output filters.

It is interesting to note that by using two small inverters to drive a large induction machine equipped with two separate stator windings the noise and current ripple can be reduced by triggering two PWM inverters with inverse pulses so that the switching frequency harmonic voltages are in antiphase. In this way, the noise level can be reduced [9]. However, the method is really only practical for very high power induction machine drives.

This paper describes an investigation of the influence of PWM strategies on the acoustic noise emitted by two nominally identical, mass produced three-phase six-pole 50-Hz/60-Hz induction machines. Firstly, the noise variation from the machines is measured, and the noise and vibration spectra are analyzed for 50-Hz/60-Hz sinusoidal waveform operation. Asymmetric regular sampling and space-vector PWM (SVPWM) are then compared, and the effect of the operating speed and switching frequency is investigated.

II. NOISE SPECTRUM ANALYSIS

The electromagnetically generated acoustic noise spectrum can be determined from the radial vibration force waves, which are usually evaluated analytically by the Maxwell stress method by neglecting the circumferential component of the air-gap flux density. Although skewing affects the amplitudes of the resulting noise components it does not affect the corresponding frequencies, i.e., the frequency spectrum is the same for both skewed and unskewed machines. Therefore, assuming an unskewed machine, the general form of the vibration force density wave, $\sigma_r(\theta, t)$, is given by

$$\sigma_r(\theta, t) = b^2(\theta, t) / 2\mu_0 = \sum \sigma_m \cos(m\theta - \omega_m t - \varphi_{m0}) \quad (1)$$

where

$$\begin{aligned} \mu_0 &= 4\pi \times 10^{-7} \\ m &\text{ mode order;} \\ \omega_m &\text{ angular frequency;} \\ \sigma_m, \varphi_{m0} &\text{ amplitude and phase angle of the force wave,} \\ &\text{respectively.} \end{aligned}$$

The mode orders and angular frequencies can be computed from the orders and angular frequencies of the air-gap flux-density harmonic components, $b(\theta, t)$. In [2], the frequency spectra are calculated directly from (1). However, although it is entirely general, it gives little insight regarding the dominant components and the associated vibration modes. In this paper, these are derived analytically.

As an approximation, $b(\theta, t)$ may be deduced from the product of the airgap mmf, $F(\theta, t)$, and the air-gap permeance, $\lambda(\theta, t)$, i.e.,

$$b(\theta, t) = F(\theta, t)\lambda(\theta, t). \quad (2)$$

The MMF wave in a PWM-inverter-fed three-phase induction motor can be obtained in a similar way to the machines fed from sinusoidal power supply [10] and can be expressed as

$$\begin{aligned} F(\theta, t) &= F_1 \cos(p\theta - \omega_1 t - \varphi_1) + \sum_{k \neq 1} F_k \cos(p\theta - \omega_k t - \varphi_k) + \sum_{k \neq 1} \\ &\cdot F_{\nu} \cos(\nu\theta - \omega_1 t - \varphi_{\nu}) + \sum_{k \neq 1} F_{\mu} \cos(\mu\theta - \omega_{\mu} t - \varphi_{\mu}) + \sum_{k \neq 1} \\ &\cdot F_{\nu k} \cos(\nu\theta - \omega_k t - \varphi_{\nu k}) + \sum_{k \neq 1} F_{\mu k} \cos(\mu\theta - \omega_{\mu k} t - \varphi_{\mu k}) \end{aligned} \quad (3)$$

where

- p number of pole pairs;
- ω_1 fundamental angular frequency of the supply;
- $\omega_k = k\omega_1$ angular frequency of the k th current harmonic.

The first term is the fundamental air-gap MMF wave produced by the fundamental current, and the second term represents first-order MMF harmonics due to current harmonics. The third and fourth terms are higher order MMF harmonics produced by the fundamental current of the stator and the rotor, respectively, while the fifth and sixth terms are higher order MMF harmonics produced by the current harmonics of the stator and the rotor, respectively. For a three-phase induction motor, $\nu = (6q + 1)p$, $q = 0, \pm 1, \pm 2, \dots$ in which the slot MMF harmonics are $\nu = q_1 Q_s + p$, $q_1 = 0, \pm 1, \pm 2, \dots$ whilst $\mu = q_2 Q_r + \nu$, in which $\nu = p$ is usually the most important, and $q_2 = 0, \pm 1, \pm 2, \dots$ Q_s and Q_r being the stator and rotor slot numbers, respectively. The harmonic angular frequencies are [10]

$$\omega_{\mu k} = \omega_k \left[1 + q_2 \frac{Q_r}{p} (1 - s_k) \right] \quad (4a)$$

when $k = 1$,

$$\omega_{\mu} = \omega_1 \left[1 + q_2 \frac{Q_r}{p} (1 - s_1) \right] \quad (4b)$$

where s_k is the slip of the k th time harmonic.

$$s_k = (\omega_k - p\omega_r) / \omega_k \quad (5)$$

where ω_r is the mechanical angular frequency of the rotor. Clearly, $s_1 \approx 0$ at no load for the fundamental MMF, $k = 1$, while $s_k \approx 1$ for time harmonics and, hence, $\omega_{\mu k} \approx \omega_k$ for $k \neq 1$.

The air-gap permeance, accounting for stator and rotor slotting, can be expressed as [10]

$$\begin{aligned} \lambda &= \Lambda_0 \left(1 + \frac{\sum \lambda_1}{\Lambda_0} \right) \left(1 + \frac{\sum \lambda_2}{\Lambda_0} \right) \\ &\approx \Lambda_0 + \sum \lambda_1 + \sum \lambda_2 \end{aligned} \quad (6a)$$

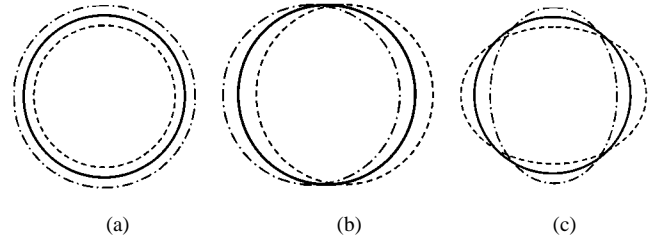


Fig. 1. Definition of vibration mode.

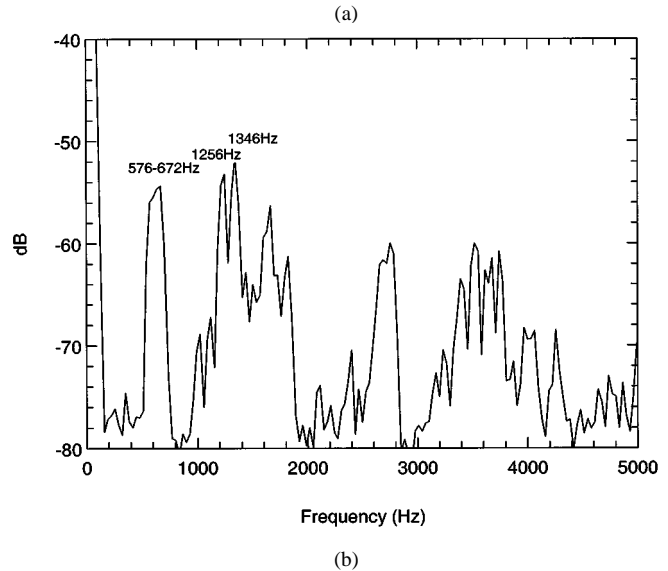
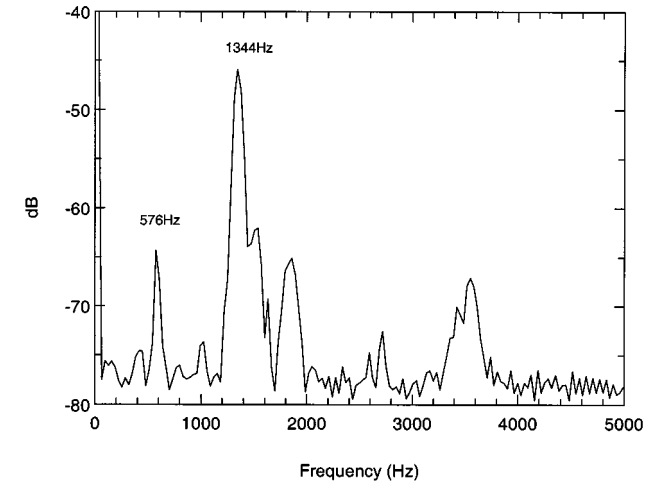


Fig. 2. Natural frequencies.

where

$$\sum \lambda_1 = \sum_{k_1=1,2,\dots} \Lambda_{k_1} \cos k_1 Q_s \theta \quad (6b)$$

$$\sum \lambda_2 = \sum_{k_2=1,2,\dots} \Lambda_{k_2} \cos k_2 Q_r \left[\theta - \frac{\omega_1}{p} (1 - s) t \right] \quad (6c)$$

where Λ_0 , Λ_{k_1} , and Λ_{k_2} are the amplitudes of permeance related to the average air-gap length, and the stator and rotor slotting, respectively.

The air-gap flux density and the radial vibration force waves can be deduced from (1) to (6). It is well known that the vibration

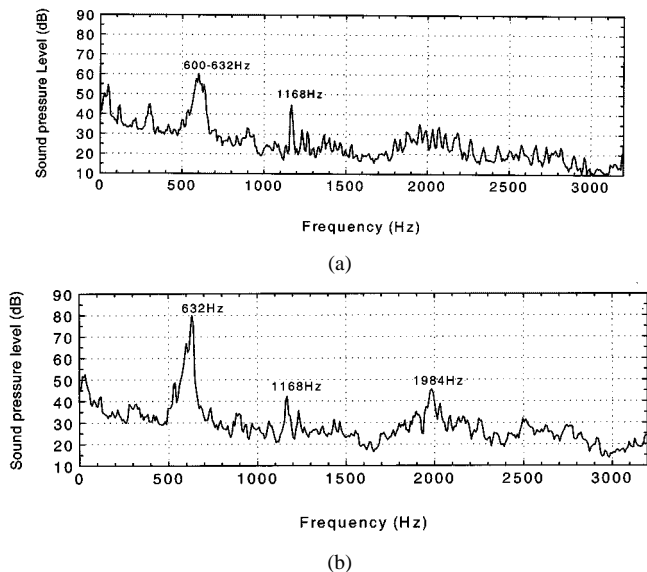


Fig. 3. Noise spectra when operated from 50-Hz/400-V sinusoidal supply

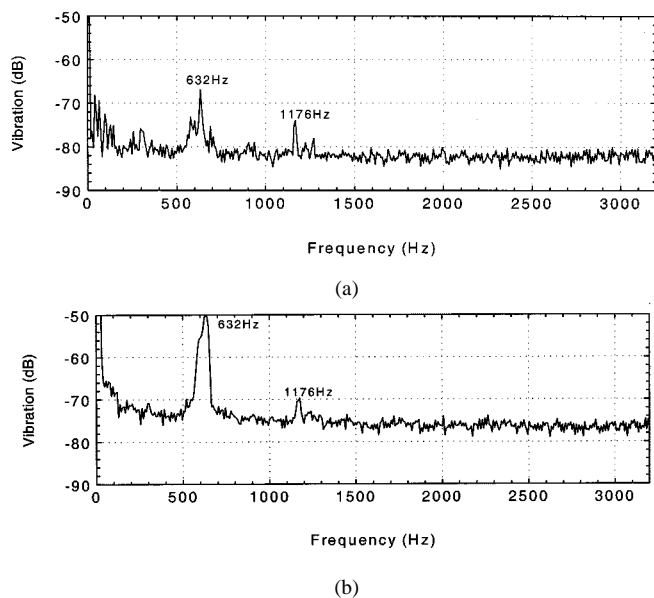


Fig. 4. Vibration spectra when operated from 50-Hz/400-V sinusoidal supply

force waves, the vibration response, and the radiated acoustic noise have identical frequency spectra. The important vibration forces are produced by the interactions between the following pairs of flux density waveforms (for simplicity, they are represented only by their amplitudes):

- 1) the stator and rotor mmf and permeance slot field harmonics, $\langle (F_\nu \Lambda_0) + (F_1 \Lambda_{k_1}), (F_\mu \Lambda_0) + (F_1 \Lambda_{k_2}) \rangle$, viz., the interaction between the resultant stator mmf and permeance slot harmonics and the resultant rotor MMF and permeance slot harmonics;
- 2) the first-order field harmonics produced by the fundamental current and its harmonics, $\langle (F_{k_1} \Lambda_0), (F_{k_2} \Lambda_0) \rangle$, in which $k_1 = 1$ or $k_2 = 1$ represents the fundamental component;

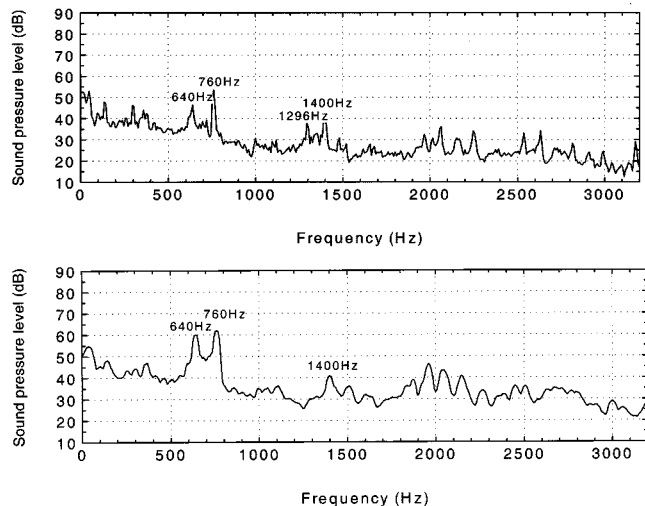


Fig. 5. Noise spectra when operated from 60-Hz/480-V sinusoidal supply

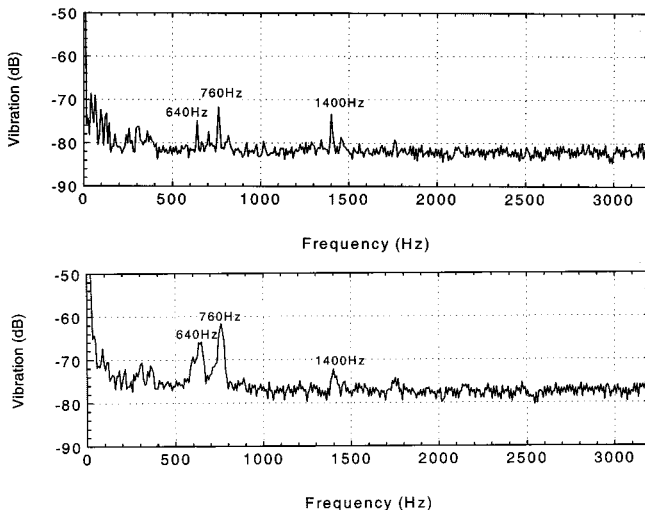


Fig. 6. Vibration spectra when operated from 60-Hz/480-V sinusoidal supply

- 3) the permeance field harmonics and the MMF field harmonics associated with the current harmonics, e.g.,

$$\begin{aligned}
 & \langle (F_1 \Lambda_{k_2}), (F_{\nu k} \Lambda_0) \rangle, \quad \langle (F_1 \Lambda_{k_1}), (F_{\mu k} \Lambda_0) \rangle, \\
 & \langle (F_1 \Lambda_{k_1}), (F_{\nu k} \Lambda_0) \rangle, \quad \langle (F_1 \Lambda_{k_2}), (F_{\mu k} \Lambda_0) \rangle; \\
 & \langle (F_k \Lambda_{k_2}), (F_\nu \Lambda_0) \rangle, \quad \langle (F_k \Lambda_{k_1}), (F_\mu \Lambda_0) \rangle, \\
 & \langle (F_k \Lambda_{k_1}), (F_\nu \Lambda_0) \rangle, \quad \langle (F_k \Lambda_{k_2}), (F_\mu \Lambda_0) \rangle; \\
 & \langle (F_\nu \Lambda_0), (F_{\mu k} \Lambda_0) \rangle, \quad \langle (F_\nu \Lambda_0), (F_{\nu k} \Lambda_0) \rangle, \\
 & \langle (F_\mu \Lambda_0), (F_{\mu k} \Lambda_0) \rangle, \quad \langle (F_\mu \Lambda_0), (F_{\nu k} \Lambda_0) \rangle; \\
 & \langle (F_1 \Lambda_{k_2}), (F_k \Lambda_{k_1}) \rangle, \quad \langle (F_1 \Lambda_{k_1}), (F_k \Lambda_{k_2}) \rangle.
 \end{aligned}$$

The vibration forces in 2) and 3) are associated only with nonsinusoidal current waveforms.

When rotor eccentricity and magnetic circuit saturation are neglected, the most important frequencies of the radial electromagnetic forces can be derived from (1)–(6) and are given by the following.

- a) Included are vibration forces produced by the interaction of the μ th stator and the ν th rotor slot harmonics, i.e., the

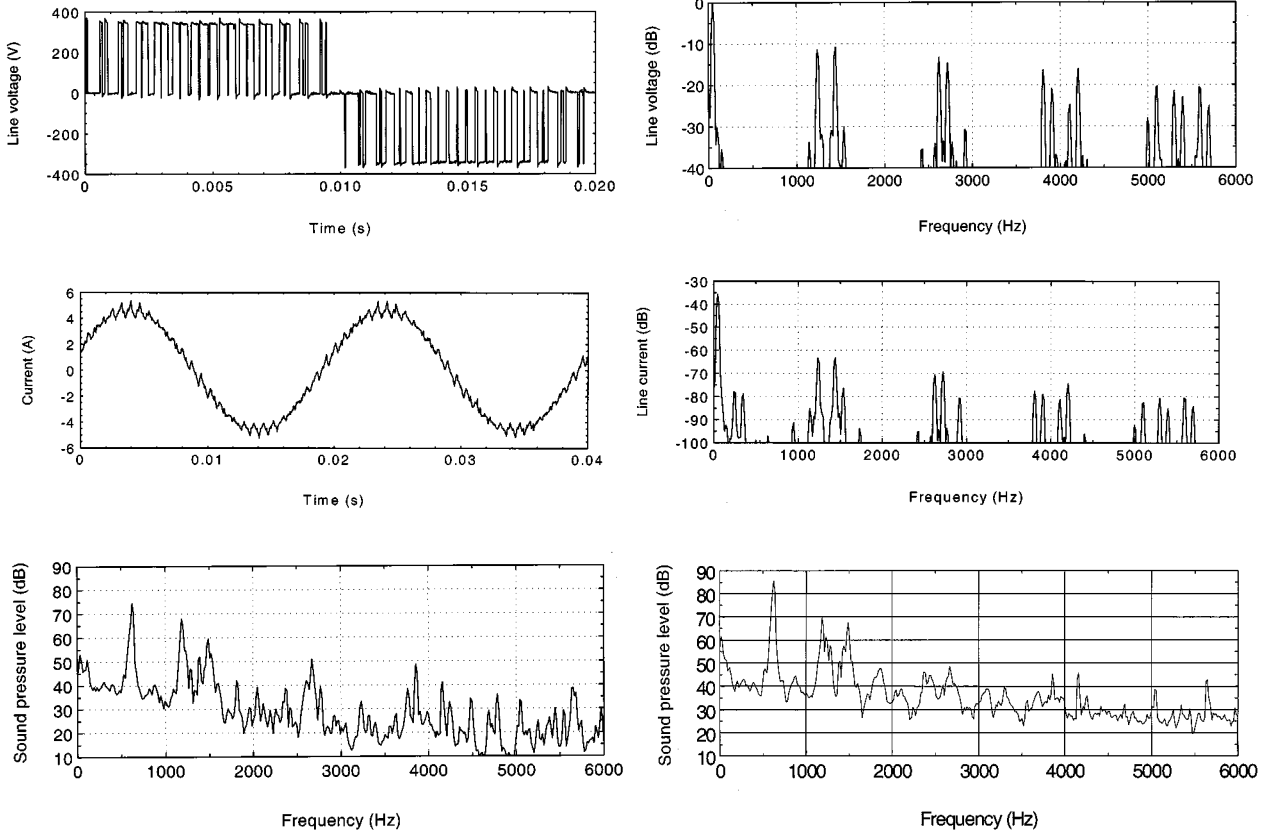


Fig. 7. Voltage, current, and noise for subharmonic PWM (SPWM), $f_1/f_s = 50/1350$ Hz, $M = 0.95$.

components in 1). In this case, the dominant force components are usually associated with the fundamental current and, hence, they are identical to those when operated from a sinusoidal supply. The frequencies and modes are given by

$$f = f_1 \left[q_2 \frac{Q_r}{p} (1 - s_1) + 2 \right],$$

for vibration mode order $m^+ = \mu + \nu$, (7a)

$$f = f_1 \left[q_2 \frac{Q_r}{p} (1 - s_1) \right],$$

for vibration mode order $m^- = \mu - \nu$, (7b)

where $q_2 = 0, \pm 1, \pm 2, \dots$, f_1 is the operating frequency of the motor. The higher the harmonic order μ and ν , the smaller the amplitudes of the magnetic field harmonics, while the lower the mode orders the more important the resulting vibration force. The important electromagnetic noise components under all load conditions are related to those force components having the lowest mode orders, i.e., $m = 0, 2, 3, 4$ (see Fig. 1). However, due to corresponding high field harmonic orders and higher natural frequencies, the noise components associated with $m = 0$, Fig. 1(a), are usually less important than those associated with $m = 2, 3, 4$ when operated from a sinusoidal supply.

b) Also included are vibration forces due to the interaction of the first-order field harmonics produced by the fundamental current and its harmonics, i.e., component 2). They are large in amplitude, and the frequencies are located around multiples of the switching frequency, while the vibration modes are zero, i.e.,

$$f = |(\pm f_{k_1}) - (\pm f_{k_2})| \text{ and } m = 0 \quad (8a)$$

where “+” and “-” correspond to forward and backward rotation of the field harmonics, respectively, and f_k is the frequency of k th current harmonics. For example, for natural PWM, the voltage and current harmonics are $f_k = n_1 f_s \pm n_2 f_1$ where if n_1 is an odd integer n_2 will be an even integer, while if n_1 is an even integer n_2 will be an odd integer, i.e., $f_k = f_s \pm 2f_1, f_s \pm 4f_1, \dots$ and $2f_s \pm f_1, 2f_s \pm 3f_1, \dots$ etc. where f_s is the switching frequency. However, in this case, normally the interaction between the fundamental air-gap field and the first-order field harmonics produced by the current harmonics is the most important, and the frequencies are given by

$$f = |(\pm f_k) - f_1| \text{ and } m = 0. \quad (8b)$$

c) Vibrations due 3) are also sometimes important, particularly on full load and when the vibration modes are low,

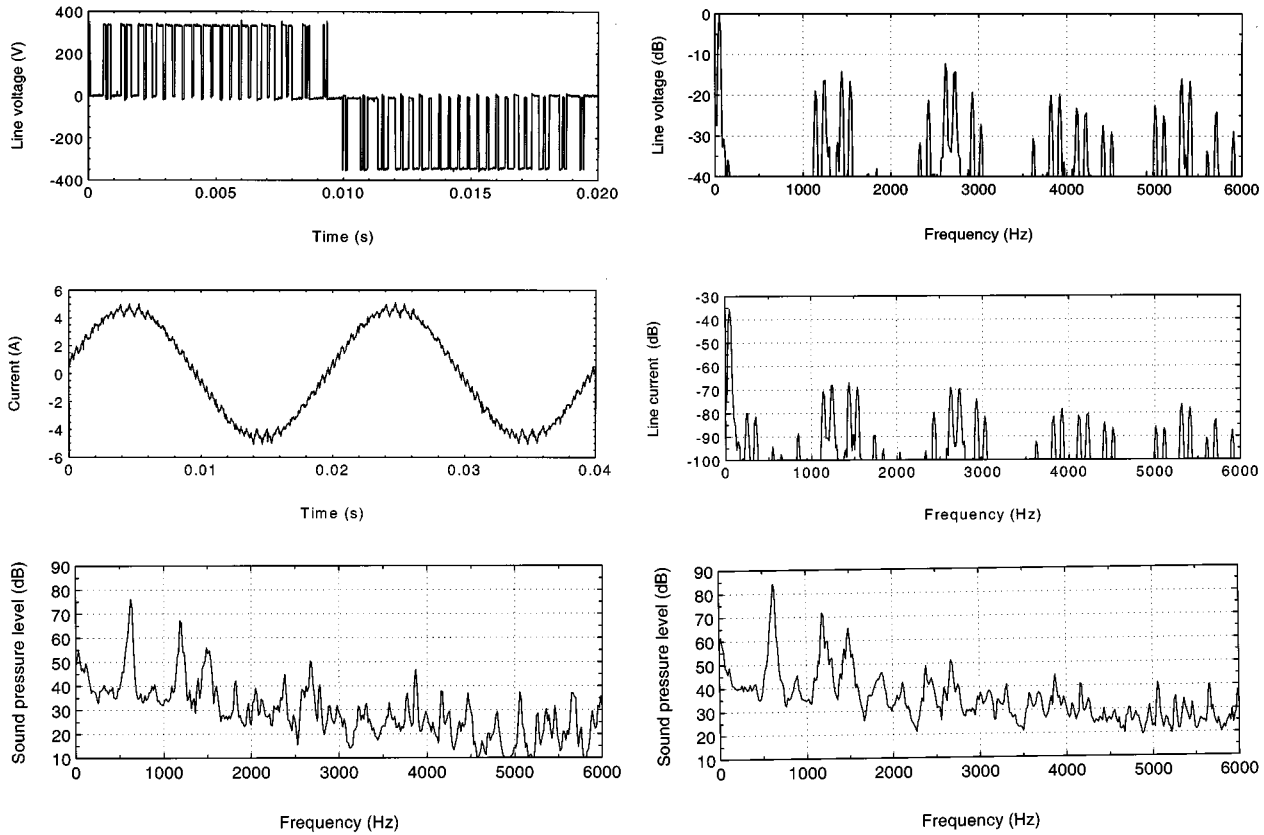


Fig. 8. Voltage, current, and noise for SVPWM, $f_1/f_s = 50/1350$ Hz, $M = 0.95$.

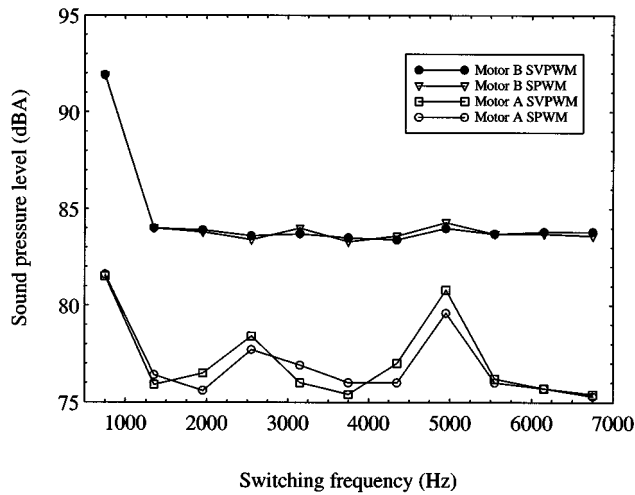


Fig. 9. Variation of noise with SVPWM and SPWM ($f_1 = 50$ Hz, $M = 0.95$).

e.g., 0 or 2. It can be shown that the corresponding frequencies are given by

$$f = \begin{cases} |(\pm f_k) - f_1| \\ |f_k \pm (f_1 + q_2 \frac{Q_r}{p} (1-s)f_1)| \end{cases}, \text{ when } m = 0, 2 \quad (9)$$

It will be shown that the noise sources a) and b) are the most important components on no load. However, as the load

TABLE I
ANALYSIS OF NOISE SPECTRA (RESOLUTION FOR FREQUENCY READING IS 16 Hz; “+” = FORWARD ROTATING; “-” = BACKWARD ROTATING)

Noise (Hz)	Vibration Mode	SVPWM (Hz)	SPWM (Hz)
1	2	50, stator/rotor slotting	50, stator/rotor slotting
2	0	(50, 1136 ⁻) (50, 1232 ⁺)	(50, 1232 ⁺)
3	0	(50, 1440) (50, 1536 ⁻)	(50, 1440)
4	0	(50, 2624) (50, 2736 ⁻)	(50, 2624) (50, 2736 ⁻)
5	0	(50, 3824) (50, 3920 ⁻)	(50, 3824) (50, 3920 ⁻)
6	0	(50, 4112) (50, 4224 ⁻)	(50, 4112) (50, 4224 ⁻)

increases, the noise source c) also becomes important. If the frequencies and modes of the important vibration forces coincide with mechanical natural frequencies and modes, the machine will emit a high acoustic noise. Clearly, the acoustic noise radiated from PWM-controlled variable-speed induction machine drives depends on various electromagnetic, mechanical, acoustic, and control parameters, e.g., 1) the pole number, the stator and rotor slot number combination; 2) the motor operating frequency; 3) the PWM switching frequency; and 4) mechanical natural frequencies and vibration modes of the system.

It is worth emphasizing that, although natural frequencies and vibration forces in a PWM-controlled induction machine are both very rich, (8) shows that the vibration mode of the most important excitation forces associated with PWM harmonics is zero, which is a pulsating mode [see Fig. 1(a)]. Hence, it is possible to select appropriate PWM strategies to avoid mechanical resonances.

III. ANALYSIS OF NOISE WHEN MACHINES FED FROM SINUSOIDAL POWER SUPPLY

In the following analysis, the motors had six poles and a 36 stator slot/32 rotor slot combination. A dynamic signal analyzer, HP35660A, and a precision sound level meter, B&K 2221, were used to measure the natural frequencies and acoustic noise spectra on no load. The influence of the load condition will be reported in due course. The noise measurements were made in an anechoic chamber, all the measurements being made with the microphone placed 200 mm from the outer surface of the motors. The noise problem was identified as electromagnetic, rather than aerodynamic or mechanical, as will be evidenced from the subsequent analysis.

The natural frequencies of both Motors A and B were obtained by applying an impulse force radially using a force hammer onto the stator of the whole machine assembly and measuring the vibration response using an accelerometer; the details of the test method can be found in [11]. The results are shown in Fig. 2. It will be seen that they exhibit a number of natural frequencies, which are associated with different vibration modes. However, as a result of normal manufacturing tolerances, the lowest natural frequency for Motor B is around 576–672 Hz (wide peak), while that for Motor A is 576 Hz (narrow peak). The mode order is 1 [see Fig. 1(b)], which is essentially an oscillating vibration of the stator with reference to the rotor. It was shown [11] that when the frequency of the excitation force is close to the natural frequency of such a vibration mode a mechanical resonance will occur even when the mode order of the excitation force is different. In addition, there is another natural frequency around 9–10 kHz associated with vibration mode zero, which, as will be shown later, is the most important regarding the noise due to the vibration forces produced by the interaction of the fundamental air-gap field and the first-order field harmonics resulting from the current harmonics.

When they were run on no load from a 50-Hz/400-V power supply, the noise spectra of both Motors A and B were dominated by the 640-Hz frequency component (note that the frequency may exhibit a small error due to the discretized nature of the spectrum). See Fig. 3. According to the theory which was presented earlier, this is due to the radial vibration force produced by the interaction between the first stator and rotor slot harmonics (see Fig. 4) for which the corresponding vibration mode order is 2 [see Fig. 1(c)]. There is another component at 1176 Hz with mode order 2, which is due to the interaction between the second stator and rotor slot harmonics, although it is not as prominent as the 640-Hz frequency component. Since the frequency of the main radial excitation force when operated from the 50-Hz power supply is 640 Hz, it is clear from

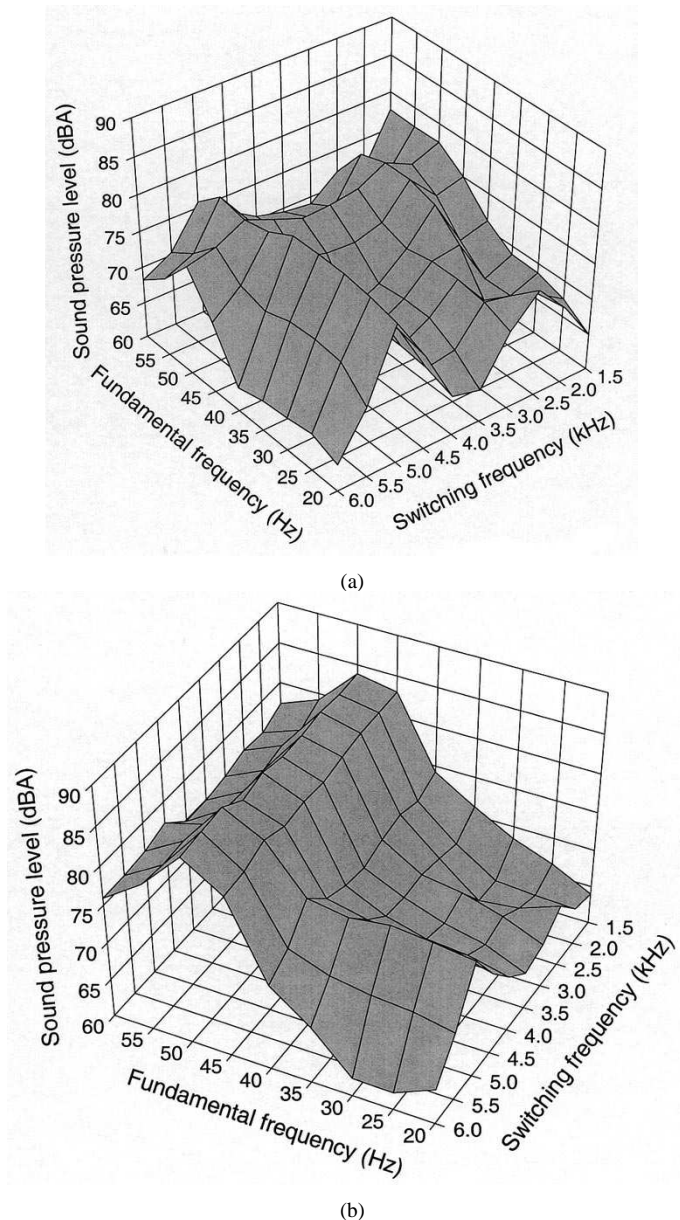


Fig. 10. Variation of noise with fundamental operating frequency and switching frequency when supplied from an SVPWM converter under constant V/f_1 .

Figs. 2(b), 3(b), and 4(b) that it coincides with a mechanical resonance for Motor B. Although the vibration mode order corresponding to the excitation force at this frequency is 2, while the vibration mode order corresponding to the lowest natural frequency is 1 [see Fig. 1(b)] (i.e. they are different), it can still cause resonance as long as the natural vibration mode order is 1 as mentioned earlier. In contrast, Motor A does not exhibit a mechanical resonance since its lowest natural frequency is below 600 Hz. It should be noted that the above-mentioned mode orders are referred to as vibration mode orders, not force mode orders. Vibration response can be measured easily by using accelerometers, as compared with forces.

When the motors were supplied from a 60-Hz/480-V power supply, the dominant frequency components in the noise spectra for both Motors A and B shift to 760 and 1400 Hz, although their vibration modes remain the same (see Figs. 5 and 6). Since

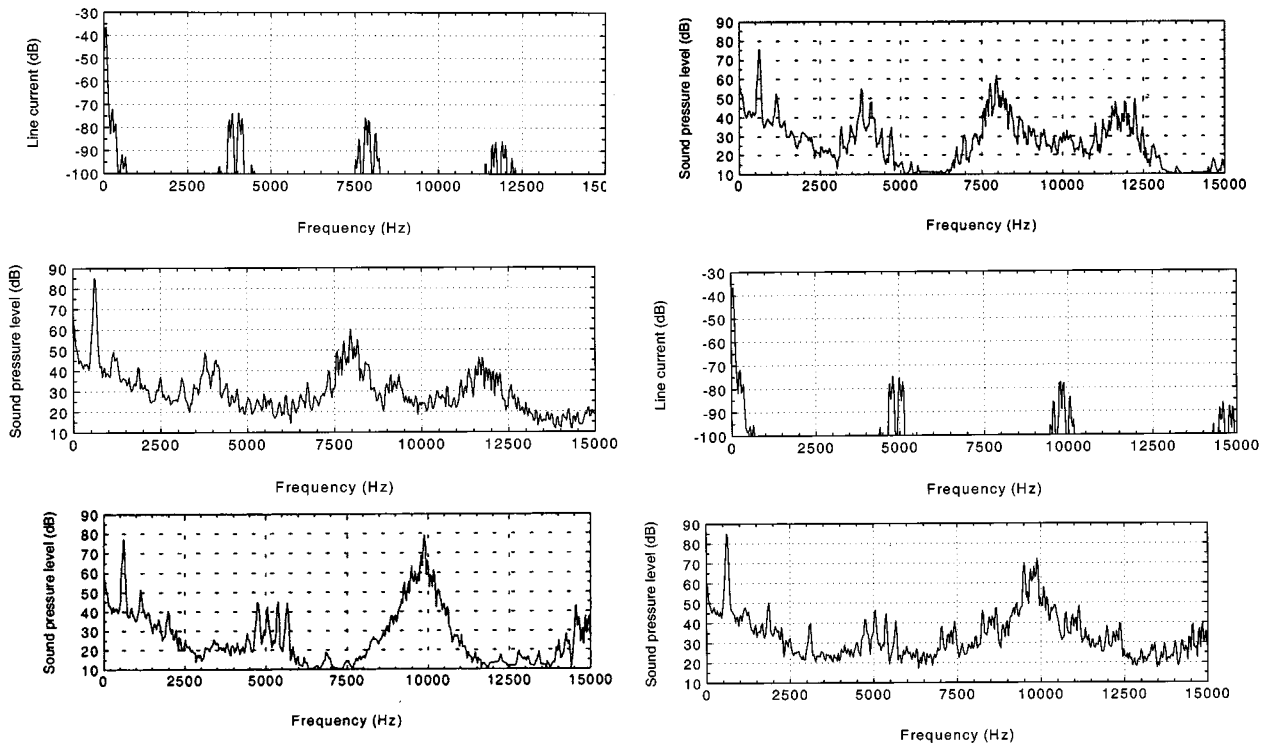


Fig. 11. Current and noise spectra.

the frequency of the main radial excitation force is now 760 Hz, there is no resonance and, hence, the total noise level is lower. However, there is another excitation frequency of 640–660 Hz with vibration mode order 4, which is also produced by the interaction between the first stator and rotor slot harmonics, and which is now coincident with the lowest natural frequency (see Figs. 5 and 6). However, since the mode order of the excitation force is high, the resonance is not so severe, and the associated noise level is much lower. Therefore, the motors were much quieter when they were run from a 60-Hz supply rather than 50 Hz.

IV. INVESTIGATION OF ACOUSTIC NOISE IN PWM-CONTROLLED INDUCTION MACHINE DRIVES

In this section, the acoustic noise when the motors are supplied from asymmetric regular sampling SPWM [12] and SVPWM [13] converters is compared, and the effect of the operating speed and the switching frequency are investigated.

In order to investigate the effect of PWM current harmonics on the radiated acoustic noise, the motor was supplied from a TMS320C50 digital-signal-processor-controlled MOSFET inverter for various operating frequencies f_1 , the modulation index being varied to maintain a constant V/f ratio. Figs. 7 and 8 show the line–line voltage and current waveforms and their corresponding spectra for a specific ratio of the fundamental to switching frequency f_1/f_s . It can be seen that, for SVPWM, both the voltage and current harmonics exhibit a slightly wider harmonic bandwidth than those for regular sampling asymmetrical SPWM, but the amplitudes are lower. However, measurements show that SVPWM results in almost the same noise spectra and noise level as SPWM (see Figs. 7 and 8). This is not surprising, since, although the difference between

the vibration forces, which are due to the interaction of the fundamental air-gap field and the first-order field harmonics produced by the current harmonics, is noticeable on a linear scale, the corresponding difference in the radiated acoustic noise level (in decibels) is insignificant. It is pertinent to note that, since SVPWM has a wider harmonic bandwidth than SPWM, it is more likely to induce a mechanical resonance and, indeed, a slightly higher acoustic noise can be observed in Fig. 9 around switching frequencies of 2.5 and 5 kHz, respectively, which cause mechanical resonances at the natural frequency around 10 kHz. However, it will be noted that for the resultant A-weighted sound pressure level these are only noticeable on Motor A, for which the frequencies of the vibration force produced by the stator and rotor slot harmonics do not coincide with a mechanical resonance. Fig. 9 also shows that, when supplied from both SPWM and SVPWM converters, Motor B still radiates much higher acoustic noise than Motor A, due to the resonance of Motor B at the 50-Hz fundamental frequency. However, when the switching frequency is very low, the current harmonics and the acoustic noise increase very significantly for both motors, which were found to be almost as noisy as when they were operated from a quasi-square converter.

Applying the theory for the noise spectrum analysis, the dominant noise components can be identified. The results are summarized in Table I, where it can be seen that the dominant noise components for both SVPWM and SPWM are identical.

From (7), it can be shown that component 1 in Table I, i.e., 640 Hz, is due to the radial vibration force produced by the interaction of the first order stator and rotor slot field harmonics associated with the 50-Hz fundamental current, and that the corresponding vibration mode is 2. As when the machines are fed from a sinusoidal power supply, this vibration force

induces a mechanical resonance at the lowest natural frequency of 576–672 Hz for Motor B.

From (8), it can be shown that noise components (2 and 3), 4, (5 and 6) in Table I are due to vibration forces produced by the interaction of the fundamental air-gap field and the first-order field harmonics produced by current harmonics around the switching frequency f_s and its multiples, $2f_s$ and $3f_s$, as indicated by (50, 1136), etc. where 50 and 1136 Hz are the frequencies of the fundamental and harmonic current components. The corresponding vibration modes are all zero. In Table I, the symbols “+” and “-” indicate that the first-order field harmonic produced by this current harmonic is either forward and backward rotating. As shown in Table I, one noise component is usually produced by a pair of vibration forces.

In order to further illustrate the influence of the operating and switching frequencies, Fig. 10(a) and (b) shows the effect of varying both the motor speed (20–60 Hz) and the switching frequency (1.5–6 kHz) of the SVPWM for Motors A and B. It is seen that Motor B still exhibits a mechanical resonance when operated at 50-Hz fundamental frequency, when the effect of the PWM switching frequency becomes minimal. However, below this frequency the switching frequency has a significant effect on the emitted acoustic noise. Both Motors A and B also exhibit resonances around 10 kHz, induced by the excitation force produced by the fundamental air-gap field and the harmonics located around multiples of the switching frequency. As a result, the noise level is a maximum at 2.5- and 5-kHz switching frequencies over the motor operating speed range, as mentioned earlier. However, this is only critical when there is no resonance solely due to the fundamental phase current.

Fig. 11 clearly illustrates the two types of mechanical resonances discussed above, namely: 1) the resonance of Motor B at 640 Hz when operated at 50 Hz fundamental frequency and 2) the resonance at 10 kHz induced by PWM current harmonics at 2.5- and 5-kHz switching frequencies. Since Motors A and B have nominally identical electromagnetic characteristics, only the current spectra for Motor A are included in Fig. 11.

V. CONCLUSIONS

The acoustic noise radiated from two nominally identical induction motors, fed from sinusoidal, asymmetric regular sampling SPWM and SVPWM converters, has been investigated theoretically and experimentally at different operating speeds and PWM switching frequencies. The following points have been shown.

- 1) Manufacturing tolerances can result in significant differences in the noise emitted from nominally identical motors.
- 2) Mechanical resonances can result in extremely high noise emissions, such resonances being induced by the fundamental current and PWM harmonics, both independently and in combination.
- 3) Analysis of the acoustic noise should consider the stator and rotor slot air-gap field harmonics due to the fundamental current, and the interaction between the air-gap

field harmonics produced by the fundamental and PWM harmonic currents.

- 4) The vibration modes associated with the radial force produced by the interaction between the stator and rotor slot harmonics depend on the stator and rotor slot numbers and pole number, while the vibration modes are zero associated with the radial force produced by the interaction between the fundamental air-gap field and the first-order field harmonics produced by the current harmonics.
- 5) The significance of the effect of PWM switching frequency is closely related to the mechanical resonance whose vibration mode is zero.
- 6) The difference between the acoustic noise produced by the induction machine fed from SPWMs and SVPWMs is generally insignificant.
- 7) A motor which is noisy when fed from a sinusoidal supply will be still noisy when supplied from a PWM converter. However, the reverse may not be the case.
- 8) The PWM strategy is critical only when the emitted noise is dominated by the electromagnetic force resulting from the interaction of the fundamental air-gap field and PWM harmonics. Thus, the influence of the PWM strategy is likely to be minimal if a machine exhibits a resonance due to the fundamental current.

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