

1 ***Monitoring the early stiffness development in epoxy adhesives for***  
2 ***structural strengthening***

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13 **ABSTRACT**

14 The present work aimed to assess the early-age evolution of E-modulus of epoxy adhesives  
15 used for Fibre-Reinforced Polymer (FRP) strengthening applications. The study involved  
16 adapting an existing technique devised for continuous monitoring of concrete stiffness since  
17 casting, called EMM-ARM (Elasticity Modulus Monitoring through Ambient Response Method)  
18 for evaluation of epoxy stiffness. Furthermore, monotonic tensile tests according to ISO  
19 standards and cyclic tensile tests were carried out at several ages. A comparison between the  
20 obtained results was performed in order to better understand the performance of the several  
21 techniques in the assessment of stiffness of epoxy resins. When compared to the other  
22 methodologies, the method for calculation of E-modulus recommended by ISO standard led to  
23 lower values, since in the considered strain interval, the adhesive had a non-linear stress-strain  
24 relationship. The EMM-ARM technique revealed its capability in clearly identifying the  
25 hardening kinetics of epoxy adhesives, measuring the material stiffness growth during the  
26 entire curing period. At very early ages the values of Young's modulus obtained with quasi-

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1 static tests were lower than the values collected by EMM-ARM, due to the fact that epoxy resin  
2 exhibited a significant visco-elastic behaviour.

3

4 **KEYWORDS**

5 A. Epoxy / epoxides

6 D. Elastic modulus

7 C. Non-destructive testing

8 D. Cure / hardening

9 Cyclic tensile test

## 1 1 INTRODUCTION

2 In recent years, the application of thermosetting resins in civil engineering applications has  
3 largely increased, mainly for their use in structural strengthening systems such as Fibre-  
4 Reinforced Polymer (FRP) reinforcements [1]. The most common resins employed as  
5 structural adhesive for bonding FRP to structural elements to be strengthened are two-  
6 component epoxy resins [2, 3].

7 In FRP installations, the mechanical behaviour of the strengthening system is strongly  
8 influenced by the epoxy adhesive, particularly at early ages, while the mechanical properties  
9 of the adhesive are still enduring significant evolution. Therefore, the final performance of the  
10 whole application strongly depends on adequate preparation, application and curing of the  
11 epoxy resin itself. During the curing period, the fluid resin transforms into a rubber (gelation)  
12 and then in a solid glass (vitrification), developing a progressively denser polymeric network  
13 [4].

14 It has been shown that the necessary curing time to reach the targeted bond strength of a  
15 given resin significantly depends on environmental conditions, such as temperature and  
16 moisture [5, 6]. Lapique et al. [7] and Moussa et al. [8] have investigated the effect of the curing  
17 temperature on the development of the mechanical properties of epoxy resins generally utilised  
18 for structural strengthening, reaching similar conclusions: as both time and temperature  
19 increase, the epoxy tensile strength increases. Additionally, adhesives used for FRP  
20 strengthening applications must cure in-situ at various environmental conditions.

21 From the above considerations, it is clear that the development and implementation of non-  
22 destructive methods that are able to provide continuous information correlated to the curing  
23 process of epoxy resins is of paramount importance for in-situ applications of strengthening  
24 systems. The determination of the time at which the material becomes actually capable of  
25 bearing structurally relevant stresses is fundamental (and especially important in the case of  
26 pre-stressed systems [9]), as well as the stiffness increase along time. In fact, the elasticity  
27 modulus (E-modulus) of a polymer material such as cured epoxy adhesive is one of the most  
28 significant material parameters in structural analysis. Usually E-modulus values are obtained

1 from tensile mechanical tests under a monotonic state of stress and there are already available  
2 several standards (e.g. ISO 527-1:2012 and ASTM D638M-93). It is nonetheless remarked  
3 that some of these standards are specifically directed to secant E-modulus, and do not take  
4 into account the strength of the material in the testing/calculation procedure. Additionally,  
5 tensile tests can solely provide measurements at discrete instants and they are complicated  
6 to perform on the construction site (most of the times due to economical unfeasibility).

7 For the aforementioned reasons, alternative vibration-based techniques are commonly utilized  
8 nowadays for the study of polymer-based plastic materials. The most widely used vibration-  
9 based techniques for E-modulus determination are the resonant frequency-based methods  
10 [10], as well as the dynamic mechanical analysis (DMA) [11]. Both these methods require the  
11 application of a mechanical force and therefore it is clear that these techniques are only  
12 suitable for specimens which have developed enough stiffness at the age of testing. Moreover,  
13 there are reports that the elastic modulus values obtained from DMA show large discrepancies  
14 between specimens and are in many cases different from those measured by quasi-static  
15 mechanical tests, as can be seen in the paper of Deng et al. [11]. Another promising dynamic  
16 test method is the novel torsion pendulum test developed by Yu et al. [12]. This technique  
17 allows measuring the dynamic shear modulus of adhesives since the early stages of the cure,  
18 monitoring the change of the resonant frequency with time.

19 Alternatively, techniques based on the propagation of ultrasonic waves through the sample  
20 can provide continuous measurement of the elasticity modulus of composite materials, ranging  
21 from the fluid-like stage up to the fully hardened state [13]. Even though these wave-based  
22 methods allow overcoming some of the drawbacks of the conventional techniques based on  
23 the resonance frequency, there are relatively frequent problems in the interpretation of the  
24 signals, and some of the basic assumptions for the interpretation of results (e.g. the tested  
25 material should be homogeneous and isotropic) are jeopardized when applied to a composite  
26 material as the case of epoxy resin [14].

27 Azenha et al. [15] proposed a novel method to measure E-modulus evolution in concrete,  
28 called Elasticity Modulus Measurement through Ambient Response Method (EMM-ARM). The

1 method is based on the direct measurement of the evolution of the natural frequency of  
2 vibration of a composite beam, filled with the material under testing. The evolving natural  
3 frequency of the composite beam can thus be directly converted into the E-modulus of the  
4 tested material, based on the dynamic equations of motion of the system. The method allows  
5 continuous concrete E-modulus measurements immediately after casting and was applied also  
6 to identify the elastic modulus evolution of cement pastes, mortars and stabilized soils [16].  
7 The present work aimed to study the early-age evolution of E-modulus of epoxy materials used  
8 for FRP applications, and better understand the relationship between distinct approaches for  
9 its assessment. For this purpose, a simultaneous study of E-modulus of the same adhesive  
10 mixture was carried out through EMM-ARM, together with tensile testing according to ISO  
11 standards (monotonic secant E-modulus) at several ages. Furthermore, since no publications  
12 were found in literature related to the inter-comparison of the epoxy E-modulus by means of  
13 monotonic tensile tests (such as the case of the ISO standard) and cyclic tensile tests, specific  
14 experiments were performed in such concern. Overall, this research work assists clarifications  
15 about the applicability of several approaches/techniques in predicting the stiffness of epoxy  
16 resins.

17

## 18 **2 EXPERIMENTAL PROGRAM**

19 The experimental program consisted in the execution of an epoxy resin mixture and the  
20 characterization of the corresponding stiffness evolution along the curing time by monotonic  
21 tensile tests (MTT), cyclic tensile tests (CTT) and EMM-ARM tests. The two-component epoxy  
22 resin-based adhesive used in the experimental work, produced by S&P® Clever  
23 Reinforcement, had the trademark 'S&P Resin 220 epoxy adhesive'. This adhesive is typically  
24 employed for bonding FRP laminates to concrete and steel, and therefore may be seen as  
25 representative. According to the manufacturer [17], the component A (resin) contains 20-25%  
26 (by weight) Bisphenol A-Epoxy Resin and 5-10% Neopentyl glycol diglycidyl ether and, the  
27 component B (hardener) includes 20-25% poly (oxypropylene) diamine, 1-2.5% piperazine and  
28 20-25% 3,6-diazaoctanethylenediamin; triethylenetetramine. All the specimens tested in the

1 scope of this research were originated from a single batch that involved a total volume of epoxy  
2 resin of ~1.2 litres. The individual components were separately stirred and then component B  
3 was added to component A at a ratio of 1:4 by weight of the respective constituents. To  
4 minimise air inclusions, the compound was thoroughly and slowly manually mixed until the  
5 colour was uniformly grey and free of any streaks. The whole mixing procedure lasted  
6 approximately 4 minutes.

7 All experimental procedures (mixing and testing) took place under controlled environmental  
8 conditions (in climatic chamber), with temperature of  $20\pm 1^\circ\text{C}$  and relative humidity of  $55\pm 5\%$ .  
9 The following sections detail the program of tests, methods and the procedures of test series,  
10 including sample geometries, test configurations and preparation of specimens.

11

## 12 **2.1 Tensile tests – MTT and CTT**

13 An extensive set of thirty tensile tests were performed in order to determine the epoxy E-  
14 modulus at several ages.

15 The specimens for testing were manufactured according to “type 1A” defined in EN ISO 527-  
16 2:2012. This specimen’s geometry is characterized by having a dog bone shape at both  
17 extremities, with a thickness of 4 mm and overall geometry defined as shown in Figure 1.  
18 Teflon moulds were devised for fabrication of the specimens. After mixing the two resin  
19 components, the homogenized compound was cast into the referred Teflon moulds.  
20 Afterwards an acetate sheet was placed on the top surface and pressed with a steel roller. The  
21 specimens were kept sealed in the curing environment and were removed from the moulds  
22 just before being tested. For all specimens, width and thickness were measured at the three  
23 sections (S1, S2 and S3) identified in Figure 1, using a digital calliper with a precision of  $\pm 0.01$   
24 mm, to check tolerances and for longitudinal stress calculation.

25 The experimental program comprised the testing ages of 12, 18, 36 and 84 hours. For each  
26 age of testing, three monotonic tests and three cyclic tests were carried out. It is however  
27 remarked that the mentioned cyclic tests were always performed on the same three  
28 specimens: i.e., after being tested at the age of 12 hours, the specimens were stored in the

1 curing environment and re-tested at 18h, 36h and 84h. This strategy was adopted because of  
2 the low levels of stress induced during the cyclic testing (1/3 of the tensile strength at the age  
3 of testing), which should not induce any kind of damage to the specimen and allow re-using it.  
4 Nonetheless, in order to confirm the feasibility of this re-utilization of specimens, three  
5 additional specimens were cast for cyclic testing solely at the age of 84h from a virgin state.  
6 The comparison of results of testing of the three virgin specimens and the three re-used  
7 specimens at the age of 84h can assist the assessment of the influence of the loading history  
8 on the elasticity modulus. A specific nomenclature was devised for the test specimens, each  
9 one being labelled as X\_Y\_Z, where X is the test type (MTT – Monotonic tensile test, CTT –  
10 Cyclic tensile test), Y is the testing time in hours (12, 18, 36 and 84) and Z is the specimen  
11 number within the series. The summary of all tensile tests performed is shown in Table 1. It is  
12 remarked that CTT\_84h\_1 to CTT\_84\_3 correspond to the specimens that were re-used  
13 among the several testing ages, whereas CTT\_84h\_4 to CTT\_84h\_6 correspond to the  
14 specimens that were solely tested at such age (here termed as virgin specimens).

15 Both types of tensile tests (MTT and CTT) were carried out in a universal testing machine (AG-  
16 X Shimadzu) with 50 kN capacity load cell and test force measurement precision of 1/1000  
17  $\pm 0.5\%$ . A TML strain gauge (type: BFLA-5-3-3L; measuring length: 5 mm; gauge factor: 2.08  
18  $\pm 1\%$ ) was installed on the top surface of each specimen (i.e. the surface that was bounded by  
19 the acetate sheet), at mid-length, to measure its longitudinal strain (see Figure 2). The  
20 monotonic tensile tests were conducted under displacement control, at a rate of 1 mm/min,  
21 according to EN ISO 527-1:2012. In regard to the load configuration of cyclic tests, the testing  
22 protocol was inspired and adapted from existing standards for determination of static modulus  
23 of elasticity in compression of cement-based materials (ISO 1920-10:2010). Each CTT  
24 experiment was composed of six load/unload cycles between 10 N and the force  
25 corresponding to 1/3 of the average tensile strength of the specimen at the age of testing. The  
26 schematic representation of the test cycles is shown in Figure 3. The cycles were generally  
27 performed under load control at the rate of 20 N/s, comprising 10 second long stretches of  
28 constant load upon reaching the maximum and minimum load values. The first loading was

1 slightly different in the sense that was made with a constant displacement rate of 1 mm/min  
2 until the maximum load of testing was reached. This initial stretch of testing was performed  
3 under displacement control by reason of the machine operation and as to ensure the respect  
4 of the targeted stress limits. It is further remarked that the choice of a load rate of 20 N/s for  
5 the all ages of testing was based on the fatigue tests carried out by Shen et al. [18] and was  
6 related to the intent of matching the strain rate of the standard tensile tests for an intermediate  
7 value of stiffness of 4 GPa (1/2 of the expected ultimate value in the studied mix).

8

## 9 **2.2 EMM-ARM tests**

10 The EMM-ARM is a variant of the traditional resonant frequency methods, based on the  
11 identification of the first flexural resonant frequency of a composite beam formed by a self-  
12 supporting mould filled with the material under testing. The natural frequency of the composite  
13 beam at each instant of testing can be analytically related to the E-modulus of the tested  
14 material, which allows determining the evolution of this elastic property since very early ages.  
15 In the original implementation of EMM-ARM for evaluating the stiffness evolution of concrete,  
16 the tested material was put inside an acrylic cylinder which was placed in simply supported  
17 condition [15]. Thereafter the methodology was adapted to study cement pastes by means of  
18 a smaller composite cantilever beam [16]. In order to adapt this ambient vibration technique to  
19 the study of epoxy adhesive used in FRP applications, some further alterations were  
20 necessary. Since the grain size of the filler of the epoxy (maximum grain size usually ranging  
21 between 0.2 and 0.5 mm [8]) is comparable to that of cement paste, it was decided to adopt a  
22 similar mould/strategy to the one used in EMM-ARM version applied to cement pastes, which  
23 is described in detail elsewhere [16]. Herein, focus will be addressed to essential aspects  
24 concerning the modified experimental setup, testing procedure and data acquisition.  
25 The EMM-ARM experimental setup adopted for testing epoxy resin is reproduced in Figure 4.  
26 For specific details on this implementation and the corresponding procedure, see the work of  
27 Benedetti [19]. The mould consists of a 330 mm long acrylic tube, with internal and external  
28 diameters equal to 16 and 20 mm, respectively. This cross-sectional size respects the principle



1 that the diameter of the beam should be at least 3 to 5 times larger than the nominal size of  
2 the particles of the tested material, in accordance to the criteria given by ASTM C192 / C192M.  
3 Taking into account the extensive experience of the authors with this testing technique and  
4 bearing in mind the trade-off that exists between the decrease in specimen size and the  
5 corresponding increase in resonant frequencies (thus less excitable structures), it was decided  
6 to limit the maximum acceptable resonant frequency values of 80 Hz for the composite beam  
7 upon full hardening of the tested material (~8 GPa). The limitation of 80Hz in the resonant  
8 frequency was associated to the intent of maintaining high excitability levels of the cantilever  
9 on behalf of ambient vibration, thus allowing this output-only modal identification technique to  
10 be applied with adequate robustness (i.e. clear identification of resonant frequencies without  
11 needing complex data processing algorithms). In order to fulfil this requirement, the free span  
12 of the cantilever beam was set to 250 mm. It is stressed that the adopted geometry  
13 simultaneously allows the test to endure a significant variation range of resonant frequency of  
14 50-80 Hz for a stiffening of the testing material from 0 to ~8 GPa. This wide range of frequency  
15 variation allows E-modulus evolution to be identified with a good resolution. A clamping device  
16 was used to assure complete fixation of the cantilever beam (see Figure 4). This clamping  
17 system, tested for the first time in the work performed by Granja et al. [20], consisted of two  
18 steel parts fastened together with four screws and thus forming a central hole with a diameter  
19 equal to the outer diameter of the acrylic tube. It is noted that the clamping device itself was  
20 screwed to a heavy steel profile as to allow the consideration of perfect fixing of the cantilever.  
21 In the EMM-ARM application for the study of cement pastes, the acrylic tube was already  
22 prepared with an extremity cap before the tube filling. In the present work, due to the higher  
23 viscosity of the epoxy adhesive after mixing, this was injected into the tube by using a 100 ml  
24 syringe, as shown in Figure 5. This method of injection had already been successfully verified  
25 in preliminary tests, checking the possible formation of air bubbles inside the tested material  
26 due to a potentially inefficient injection of epoxy inside the mould.  
27 When the tube was completely filled with the epoxy, two propylene lids were placed at both  
28 mould extremities. Finally, after putting the specimen in the final horizontal position, a ceramic

1 shear piezoelectric accelerometer (PCB® Piezotronics 352C34, with mass of 5.8 g, sensitivity  
2 100 mV/g; frequency range: 0.5 to 10000 Hz) was placed at the free end of the cantilever, in  
3 order to monitor the accelerations of the extremity of the beam in the vertical direction. The  
4 beam is solely acted by its self-weight and ambient excitations that correspond to the vibrations  
5 that naturally occur in proximity of the experiment (e.g., people walking nearby; room  
6 ventilation; vibrations produced by mechanical equipment). These vibrations can conceptually  
7 be considered as a white noise, i.e. with a uniform energy content throughout the range of  
8 frequencies of interest. In order to increase the ambient vibration level, a domestic fan was  
9 used for blowing air to the EMM-ARM specimens. The monitoring procedures started  
10 immediately after the correct placement of all components, which occurred within ~20 minutes  
11 after mixing the epoxy adhesive.

12 Figure 6 schematizes the necessary operations for obtaining the E-modulus evolution along  
13 time. The measured accelerations are acquired in a 24-bit data logger (NI-USB-9233) at a  
14 frequency ( $f_{acq}$ ) of 500 Hz, and divided in sets of 300 seconds (Figure 6a). Each recorded data  
15 set is converted to the frequency domain by applying Fast Fourier Transforms (FFT), using  
16 sub-sets of data with 4096 points ( $N_{FFT}$ ) and Hanning windows with 50% overlaps, according  
17 to the Welch procedure [21]. It is thus possible to obtain the frequency response spectrum of  
18 the beam (Figure 6b) for each 300 s period of testing with a frequency resolution ( $f_{res}$ ) of  
19 0.122 Hz (computed according to equation (1)), where the peak corresponds to the resonant  
20 frequency of the system in such a time interval.

$$f_{res} = \frac{1}{2} \cdot \frac{f_{acq}}{N_{FFT}} \quad (1)$$

21 By identifying the highest peak in each amplitude spectrum, it is possible to obtain the resonant  
22 frequency evolution of the cantilever along time (see Figure 6c).

23 The resonant frequency of the beam is finally related to the E-modulus of the tested material  
24 by application of the dynamic equations of the cantilevered structural system, together with the  
25 applied loads. The whole set of equations used for the characterization of E-modulus is  
26 explained in [16]. The final solution is the differential equation shown below:

$$a^3 [\cosh(a \cdot L) \cdot \cos(a \cdot L) + 1] + \frac{w^2 \cdot m_p}{EI} [\cos(a \cdot L) \cdot \sinh(a \cdot L) - \cosh(a \cdot L) \cdot \sin(a \cdot L)] = 0 \quad (2)$$

1 where  $a = \sqrt[4]{w^2 \times \bar{m}/EI}$ ,  $EI$  is the distributed flexural stiffness of the composite beam,  $\bar{m}$  is the  
2 uniformly distributed mass per unit length,  $m_p$  is the concentrated mass at the free extremity of  
3 the cantilever (owing to the accelerometer and lid),  $L$  is the span of the cantilever,  $f$  is the first  
4 flexural resonant frequency, and  $w = 2\pi f$  is the corresponding angular frequency.  
5 Therefore, for each measured frequency  $f$  it is possible to obtain the corresponding  $EI$  of the  
6 composite cantilever, and since the acrylic E-modulus  $E_a$  is known, the Young's modulus of  
7 the tested epoxy adhesive  $E_e$  can be estimated through the equation:

$$EI = E_a \frac{\pi(\varphi_e^4 - \varphi_i^4)}{64} + E_e \frac{\pi\varphi_i^4}{64} \quad (3)$$

8 where  $\varphi_e$  and  $\varphi_i$  are the outer and inner diameters, respectively. In this way, it is possible to  
9 relate the evolution of the first natural frequency with the elastic modulus development during  
10 the testing time and to obtain plots of E-modulus *versus* time for the epoxy (Figure 6d). This  
11 estimating methodology assumes that the fixed support of the cantilever is infinitely rigid and  
12 that the shear deformation and rotary inertia effects can be neglected. These assumptions  
13 were duly validated by parametric numerical analyses.

14 In order to check the method's ability to obtain results with good repeatability, two tests were  
15 performed simultaneously, using the same epoxy adhesive mixture employed for tensile tests.  
16 Table 2 shows the geometric characteristics of the used moulds, as well as the density of  
17 acrylic and epoxy adhesive. The values of E-modulus and density of the acrylic were verified  
18 in the laboratory through modal identification and weighing (with a Kern PLS 4000-2 precision  
19 balance 0,01 g : 4000 g) of the empty moulds before each test.

20

## 1 3 RESULTS AND DISCUSSION

### 2 3.1 Tensile tests results

3 Figure 7 presents the stress-strain curves obtained at various ages by monotonic tensile tests.  
4 Stress was evaluated by dividing the applied load by the cross-sectional area of the specimen's  
5 mid-height section (where the strain gauge was placed). From this figure, it is possible to  
6 observe the increase on stiffness along the curing process of epoxy adhesive. At the age of  
7 12 hours, since the curing reactions had just begun, high values of strains were obtained. In  
8 fact, the monotonic tensile tests carried out at 12 hours were stopped at about 5% strain (limit  
9 of the used strain gauges). From 12 to 36 hours, the epoxy stiffness had a significant increase,  
10 shown by the strong slope difference of the curves obtained at 12, 18 and 36 hours. From 36  
11 to 84 hours, the stress-strain curves did not exhibit any significant variation: in that period the  
12 average maximum tensile strength increased only of 0.2 MPa (1%). On the contrary, a  
13 decrease of 18% (0.0006 m/m) in ultimate strain was observed, confirming that curing  
14 reactions were still in progress between 36 and 84 hours. The stress-strain curves obtained by  
15 cyclic tensile tests are depicted in Figure 8. From this figure the same considerations made for  
16 monotonic tests results can be drawn: from 12 to 36 hours after mixing of adhesive  
17 components, the material stiffness had an important increase, while, from 36 to 84 hours, it did  
18 not show any significant variation. In addition, Figure 8 clearly shows the viscoelastic effect  
19 that occurred during the consecutive loading/unloading cycles, especially at the early ages of  
20 testing. Furthermore, the strain-stress curves of the cyclic tensile tests concerning the  
21 additional three specimens tested just at the age of 84 hours (from the virgin state), and those  
22 of the repeatedly tested specimens, turned out to be very similar. This confirms that loading  
23 history did not influence the material stiffness for the maximum load levels applied.

24 The Young's modulus of epoxy adhesive was obtained by various methods. Concerning the  
25 monotonic tensile tests, two methods were contemplated: the first Young's modulus  $E_{\text{MTT-std}}$   
26 was calculated as the slope of the secant line between strain values of 0.05% and 0.25% on  
27 the stress-strain curve, in accordance to ISO standard 527-1; the second  $E_{\text{MTT-inslop}}$  represents  
28 the slope of the linear trend line of the experimental values gathered until 1/3 of the ultimate

1 strength, in accordance with the American Standard ASTM D638M-93. In order to avoid the  
2 error caused by the possible starting misalignment of the grips and the presence of microscopic  
3 structural flaws, the initial region of positive second derivative of each experimental curve was  
4 not considered for the calculation of  $E_{\text{MTT-inslop}}$ . The schematic representation of these two  
5 methods applied to the specimens MTT\_18h\_1 and MTT\_84h\_2 are shown in Figure 9. The  
6 two calculation methods tend to lead to different values of E-modulus. Young's modulus values  
7  $E_{\text{MTT-std}}$ , were always lower than  $E_{\text{MTT-inslop}}$  as shown in Figure 10, where the evolution of the  
8 average values of E-moduli calculated through these two methods are depicted. Moreover,  
9 this difference depended on the age of the epoxy specimen and slightly decreased over time  
10 (in relative terms). At the age of 12 hours, the average modulus calculated by the  $E_{\text{MTT-inslop}}$   
11 method resulted 49.3% larger than the secant modulus. At 84 hours, an average E-modulus  
12 ( $E_{\text{MTT-std}}$ ) of 7.16 GPa and an average  $E_{\text{MTT-inslop}}$  of 9.39 GPa (31.3% larger) were obtained. This  
13 large deviation is not negligible and deserves a careful consideration. The modulus calculation  
14 laid down by ISO standard takes into account stretches of the stress-strain relationship curve  
15 where the slope of the obtained curve was not constant, as visible in the examples of Figure 9  
16 (MTT\_18h\_1 and MTT\_84h\_2). Furthermore, it should be noted that failure of MTT specimens  
17 tested at the age of 84h occurred for a strain level of 0.27%, which is very close to 0.25%, thus  
18 probably inducing tensile damage to the specimen within this strain range. Conversely, the  
19 trend line method ( $E_{\text{MTT-inslop}}$ ) takes into account values in the range of low strains for all ages  
20 of testing, where the relationship between stress and strain can be properly considered linear.  
21 Consequently, the elasticity modulus determined by ISO 527-1 equation ( $E_{\text{MTT-std}}$ ) turned out  
22 to be systematically lower than that obtained through the trend line method ( $E_{\text{MTT-inslop}}$ ).  
23 Moreover, the average coefficient of determination for the curves obtained by the trend line  
24 method ( $R^2_{\text{inslop}}=0.9951$ ) resulted higher than that calculated for the ISO curves ( $R^2_{\text{std}}=0.9579$ ).  
25 Thus  $E_{\text{MTT-inslop}}$  approximates better the real data points, demonstrating that, in the considered  
26 range of values, the experimental curve is almost linear. This comparison confirms that  
27 standard recommendations may not estimate the actual stiffness of epoxy adhesive, since in

1 the strain interval of 0.05-0.25% the material may have an inelastic behaviour, especially at  
2 early ages.

3 The aforementioned E-modulus values computed with basis on the results of standard tensile  
4 test setups/procedures (with calculation methods  $E_{MTT-std}$  and  $E_{MTT-inslop}$ ) are now compared to  
5 those that can be obtained from the tensile cyclic tests results. Concerning the latter, the first  
6 cycle of loading was neglected and the slope of the trend line calculated for each following  
7 loading and unloading stage was taken into account for determining E-modulus values. Figure  
8 11 shows the strain-stress curves obtained in a cyclic test carried out at the age of 84 hours  
9 (CTT\_84h\_3). Based on this figure and Table 3, some considerations can be drawn: (i) the  
10 slopes corresponding to each loading and respective unloading stage resulted very similar; (ii)  
11 a relevant coherence between slopes pertaining to the five different subsequent cycles was  
12 obtained. Therefore it is feasible to average all these slopes within each test to obtain a  
13 representative E-modulus of the cyclic test ( $E_{CTT}$ ). It was also noticed that the dispersion of  
14 results among the five test cycles tends to decrease with increasing ages of testing.

15 The evolution of the average elasticity moduli evaluated according to the cyclic tensile test  
16 methodology (CTT) is shown in Figure 10, together with the previous two methodologies. It is  
17 interesting to observe that the coherence between CTT tests results ( $E_{CTT}$ ) and those obtained  
18 through the trend line method on the MTT tests ( $E_{MTT-inslop}$ ) is quite satisfactory, particularly for  
19 the ages 18 and 84 hours. However, for all the tested ages the ISO calculation method ( $E_{MTT-}$   
20  $std$ ) identifies much lower values for the adhesive E-modulus when compared to the other  
21 methodologies, with differences that range from -70.4% to -22.1% during the several testing  
22 ages.

23

### 24 **3.2 EMM-ARM tests results**

25 The frequency spectra obtained for specimen EMM2 at several ages are shown in Figure 12.  
26 From this figure, it is possible to clearly identify the resonant frequency at the depicted ages,  
27 since the peaks are easily recognizable and no significant secondary peaks emerge in the  
28 frequency range of interest. If all computed power spectra are put side-by side according to

1 their time of occurrence, a meaningful 2D colour plot may be obtained, in which the intensity  
2 of the signal is revealed by colour scale, as shown in Figure 13. For each test, the curves of  
3 first natural frequencies *versus* time are identified, taking the peak of each power spectrum.  
4 The resonant frequencies evolution obtained for the two specimens are shown in Figure 14. It  
5 is remarked that the two frequency curves are very coherent, providing an indication of good  
6 repeatability of the experimental setup and procedures. Moreover, a wide range of frequencies  
7 was covered throughout the curing process of the epoxy adhesive, ranging from 51.3 Hz to  
8 79.6 Hz within the testing period; E-modulus evolution can thus be identified with a good  
9 resolution (0.034 GPa for 51.3 Hz and 0.052 GPa for 79.6 Hz). The frequency evolution curves  
10 appear to be plausible, showing an initial period of approximately 6.4 hours in which the  
11 frequency remains almost constant. After this threshold, the frequencies evolved significantly  
12 for both tested specimens until approximately 36 hours of curing. After such period, the slope  
13 of variation exhibits a significant decrease. The elasticity modulus of the tested epoxy adhesive  
14 mixture was estimated by applying equations (2) and (3). The stiffness evolution for both EMM-  
15 ARM specimens is shown in Figure 15. It is noted that based on the adopted test setup (sizes,  
16 stiffnesses and weights) and the frequency resolution mentioned above, the E-modulus  
17 minimum resolution is 0.05 GPa. The agreement between the results of the two specimens is  
18 very good, with absolute stiffness differences under 2.5% (0.22 GPa at the age of 168 hours),  
19 demonstrating adequate repeatability of EMM-ARM. In the initial period (during the first ~6.4  
20 hours) the epoxy adhesive stiffness was nearly null for both specimens, which is consistent  
21 with its fluid-like behaviour. The kinetics of evolution of E-modulus was consistent with the one  
22 already described and discussed for the frequency evolution, and the final reached value at  
23 the end of testing was 9.3 GPa/9.5 GPa for EMM1/EMM2.

24

### 25 **3.3 Comparison between EMM-ARM, MTT and CTT results**

26 Figure 15 also shows the comparison between the elastic modulus results obtained by EMM-  
27 ARM and by tensile test methods (monotonic and cyclic). At the age of 84 hours, there is a  
28 good agreement between the values obtained through the EMM-ARM (EMM1 and EMM2),

1 those collected in cyclic tests ( $E_{CTT}$ ) and those calculated from the initial slope of monotonic  
2 stress-strain curves ( $E_{MTT-inslop}$ ). However, the results show relevant differences at the earlier  
3 ages of 12, 18 and 36 hours. At such ages, all the E-modulus values obtained from tensile  
4 tests are significantly lower than the ones acquired from EMM-ARM, particularly at 12 and 18  
5 hours. This deviation may be explained by different time-scales and strain-rates of the  
6 experimental tests. However, the strain-rate of the different methods, ranging between 10 and  
7  $50 \mu\epsilon/s$  for EMM-ARM (computed through numerical integration of the accelerograms) and  
8 between 100 and  $110 \mu\epsilon/s$  for the monotonic tensile tests (computed directly from the strain  
9 measurements) are within the same order of magnitude and therefore are not different enough  
10 to justify the gap between the estimated E values. Nevertheless, the EMM-ARM has a much  
11 lower period of loading (within a range of 0.016 and 0.02 s) than the monotonic tensile tests  
12 (within a range of 10 and 20 s). This lower time-scale makes the method less sensitive to the  
13 viscoelasticity of the material.

14 Figure 16 presents the strain-time curves obtained in two exemplifying tests performed at the  
15 age of 18 and 84 hours. From this figure, it is possible to observe the increase of strain during  
16 the 10 seconds intervals in which the load remained constant. This increase was significantly  
17 evident at the earlier age, while it was much more attenuated at 84 hours. Moreover, a  
18 progressive accumulation of deformation while material was subjected to cyclic loading was  
19 verified. In fact, the peak strain increased with the increasing numbers of cycles. At the age of  
20 18 hours, an increase of 73.9% in maximum strain between the first and the last cycle was  
21 obtained (Figure 16a). At the age of 84 hours, the accumulated strain after six cycles turned  
22 out to be very lower (5.3% of the initial maximum strain), as shown in Figure 16b. This process  
23 of a continuous increase in strain is called cyclic creep (or ratcheting strain) [18] and it confirms  
24 that epoxy resin shows a typical visco-elastic behaviour. Therefore, the high visco-elasticity  
25 that epoxy exhibited at very early ages may have influenced the measurement of elastic  
26 modulus through tensile tests, leading to lower values. As the importance of creep strains  
27 decreased over curing time, the Young's modulus obtained by quasi-static tests got closer to  
28 the actual E-modulus.



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#### 4 CONCLUSIONS

The present paper aimed to assess the early-age development of stiffness of an epoxy adhesive used in FRP strengthening applications, by means of three test methodologies: EMM-ARM, ISO standard monotonic tensile tests and cyclic tensile tests. The analysis of the obtained experimental results led to the following main conclusions:

- (1) During the entire tensile cycling process, the slope of the elastic loading and unloading did not decrease, i.e. the calculated E-modulus values were very similar for all the cycles. Moreover, coherence between the Young's moduli determined through cyclic tests and those obtained from monotonic tests by taking into account the initial slope of the stress-strain response was observed.
- (2) The method for calculation of E-modulus provided by ISO 527:1:2012 led to lower values of the elasticity modulus for the tested epoxy resin, due to the fact that, in the considered strain interval (0.05-0.25%), the stress-strain relationship of the adhesive was non-linear. Since the non-linear mechanical behaviour of epoxy adhesive is further marked at very early ages, it is clear that ISO method leads to even higher deviations (as compared to the other methods described here) for determining the epoxy resin E-modulus at the early stage of curing process. Therefore, a linear regression procedure applied on the part of the stress-strain curve corresponding to the values gathered until 1/3 of the ultimate strength is considered recommendable. In fact, at the indicated lower stress range, the stress-strain relationship can be considered linear.
- (3) The EMM-ARM technique revealed its capability in clearly identifying the hardening kinetics of epoxy adhesives, measuring the material setting time and the stiffness growth since very early ages. This method allows measurements since the tested material still has 'fluid-like' behaviour, overcoming the main drawback of the traditional resonance methods.
- (4) The results obtained by EMM-ARM were compared with the outcome of tensile tests. Quasi-static tests provided values of Young's modulus that were lower than the values

1 collected by EMM-ARM. This difference can be explained by the significant visco-  
2 elastic behaviour that epoxy resin exhibits especially at very early ages. In fact, this  
3 difference significantly decreased as the epoxy adhesive hardened, becoming  
4 negligible at the age of 84 hours.

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Table 1 – Experimental program of tensile tests.

<b>Age</b>	<b>Series</b>	<b>Number of specimens</b>	<b>Test type</b>	<b><math>\sigma_{max}^*</math> [MPa]</b>
12h	MTT_12h	3	Standard	-
	CTT_12h	3	Cyclic	2.4
18h	MTT_18h	3	Standard	-
	CTT_18h	3	Cyclic	4.7
36h	MTT_36h	3	Standard	-
	CTT_36h	3	Cyclic	7.0
84h	MTT_84h	6	Standard	-
	CTT_84h	6	Cyclic	7.0

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\*  $\sigma_{max}$ = 1/3 of ultimate strength

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Table 2 – Characteristics of EMM-ARM specimens.

Reference	$L$ [mm]	$\varphi_e$ [mm]	$\varphi_i$ [mm]	$m_p$ [g]	Acrylic density [kg/m <sup>3</sup> ]	Epoxy density [kg/m <sup>3</sup> ]
EMM1	250	20.15	15.99	12.11	1202.511	1742.935
EMM2	250	20.14	15.94	12.12	1198.909	1763.863

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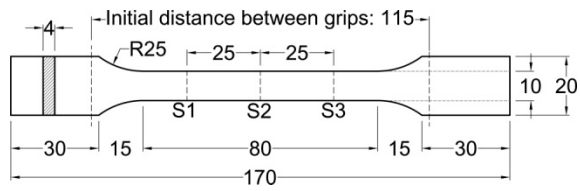
Table 3 – Summary of tests results.

Age	Reference	$E_{5cycles}$ [GPa]	CoV [%]	Reference	$E_{MTT-std}$ [GPa]	$E_{MTT-inslop}$ [GPa]	$EMM_{avg}$ [GPa]
12h	CTT_12h_1	2.32	8.96	MTT_12h_1	0.70	1.08	6.01
	CTT_12h_2	2.27	10.17	MTT_12h_2	0.66	0.93	
	CTT_12h_3	2.53	7.94	MTT_12h_3	0.74	1.14	
18h	CTT_18h_1	4.24	4.63	MTT_18h_1	2.55	3.57	8.23
	CTT_18h_2	3.75	6.29	MTT_18h_2	2.62	3.83	
	CTT_18h_3	3.71	5.83	MTT_18h_3	2.18	3.61	
36h	CTT_36h_1	8.20	0.66	MTT_36h_1	6.44	8.27	9.41
	CTT_36h_2	8.04	0.98	MTT_36h_2	6.84	8.81	
	CTT_36h_3	7.42	0.72	MTT_36h_3	6.50	8.21	
84h	CTT_84h_1	9.36	0.29	MTT_84h_1	7.36	9.59	9.69
	CTT_84h_2	9.17	0.20	MTT_84h_2	7.27	9.87	
	CTT_84h_3	8.71	0.41	MTT_84h_3	6.68	8.93	
	CTT_84h_4	8.85	0.30	MTT_84h_4	6.99	8.97	
	CTT_84h_5	9.44	0.21	MTT_84h_5	7.54	9.59	
	CTT_84h_6	9.19	0.29	MTT_84h_6	7.11	9.43	

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Notes:  $E_{5cycles}$  = average E-modulus of five loading cycles; CoV = coefficient of variation;  $EMM_{avg}$  = average of E-modulus values obtained by EMM-ARM.

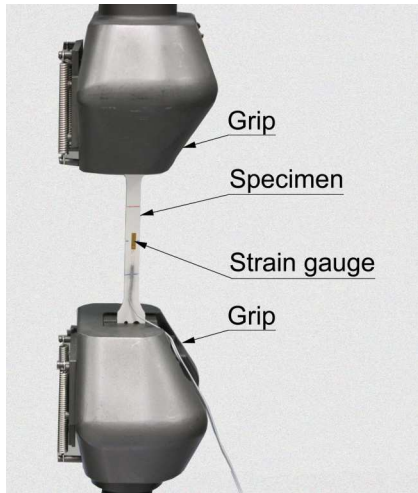




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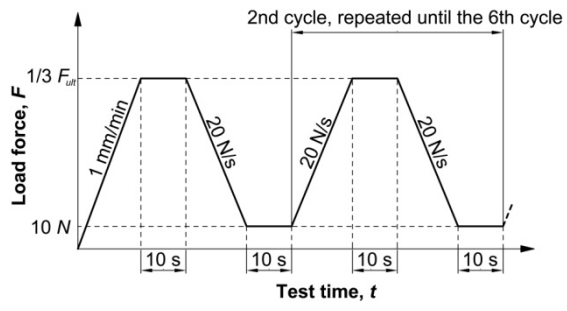
2 Figure 1 – Specimen dimensions according to ISO 527-2. Note: all dimensions are in

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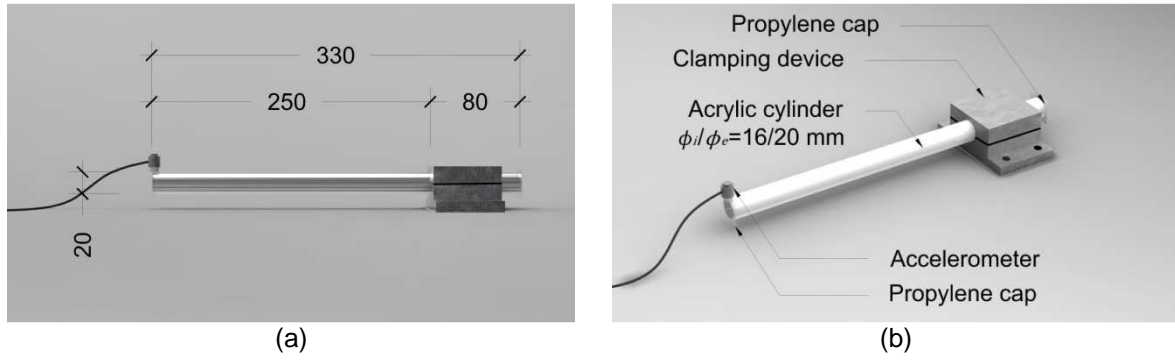
2 Figure 2 – Layout configuration of tensile tests.



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2 Figure 3 – Loading scheme of cyclic tests.

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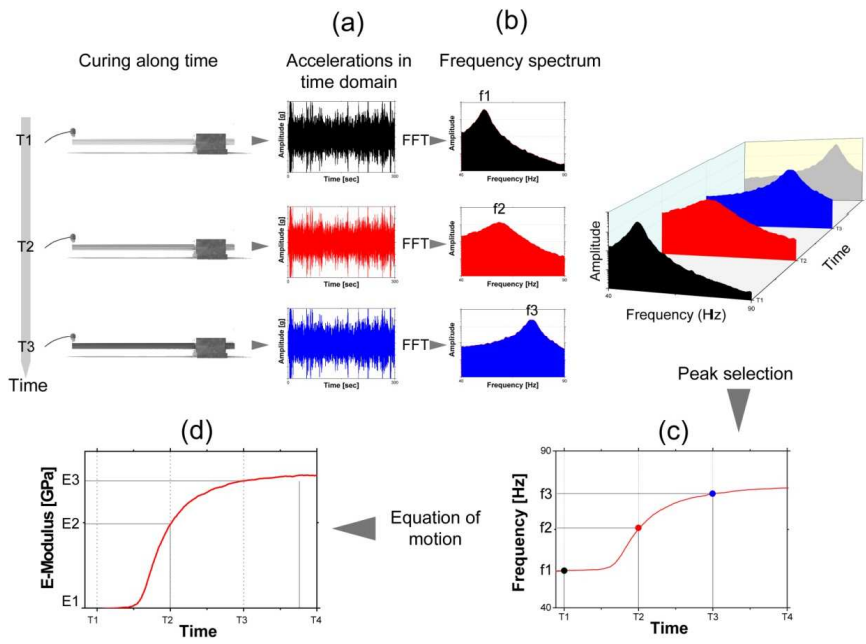


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3 (side view); (b) components of the experimental setup. Note: all dimensions are in  
4 millimeters.



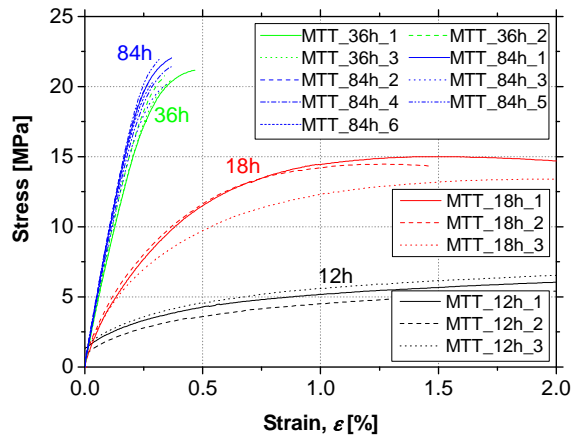
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2 Figure 5 – Photo of the epoxy injection into the acrylic tube.



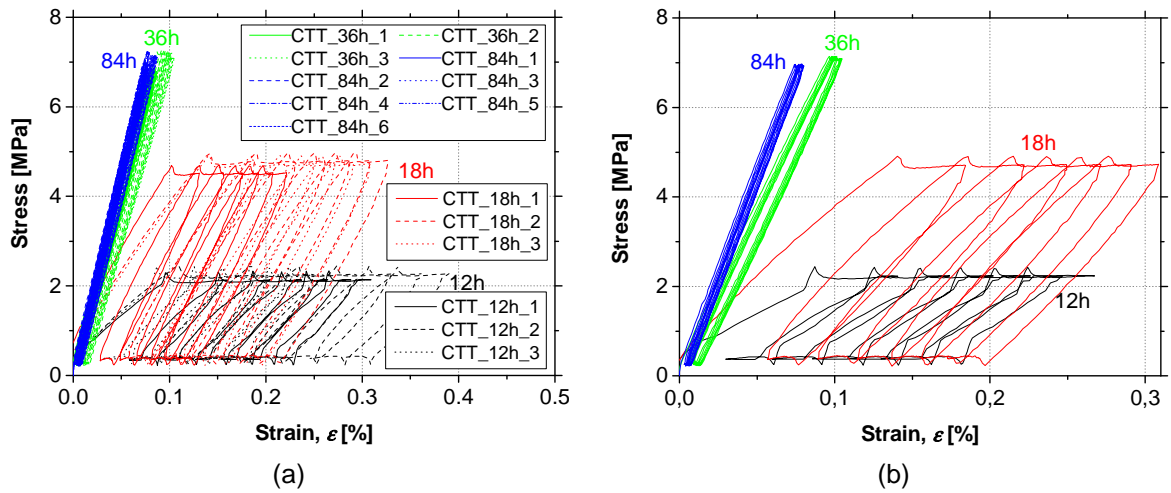
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2 Figure 6 – EMM-ARM data processing scheme.



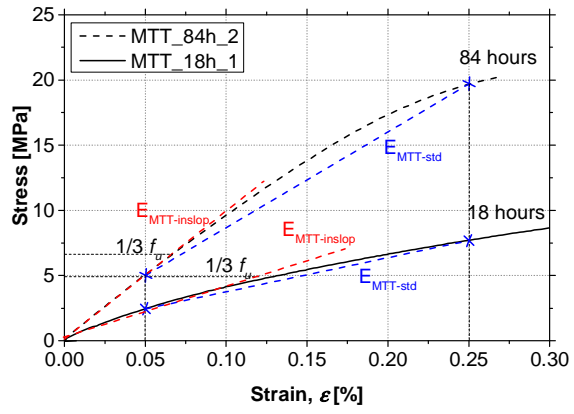
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2 Figure 7 – Stress-strain curves obtained from monotonic tensile tests.



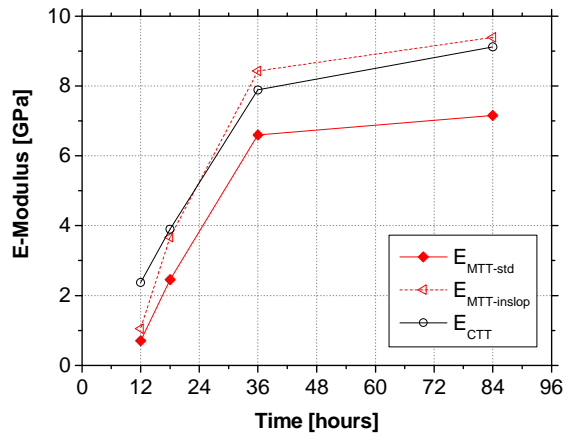
1 Figure 8 – Stress-strain curves obtained from cyclic tensile tests: (a) all specimens; (b) one  
 2 exemplifying specimen for each age.





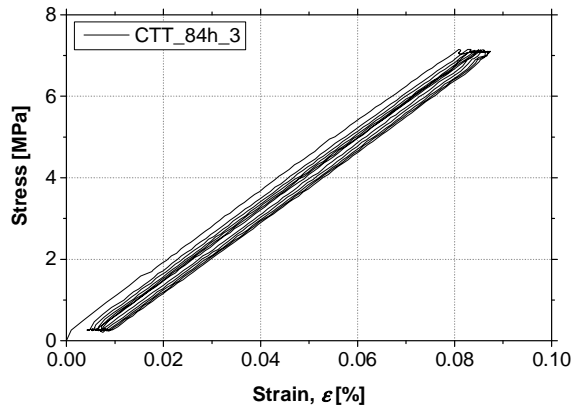
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2 Figure 9 – Example of different methods of E-modulus calculation.



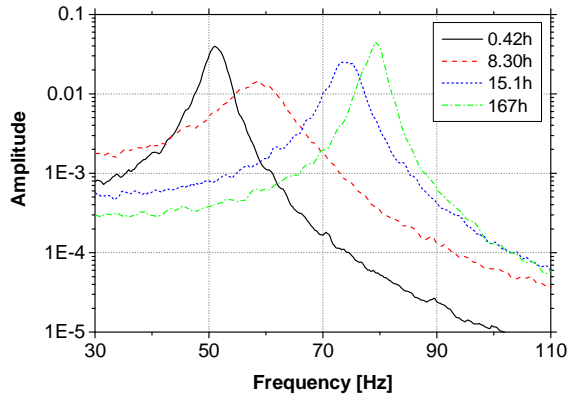
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2 Figure 10 – Epoxy E-moduli evolution obtained by tensile tests.



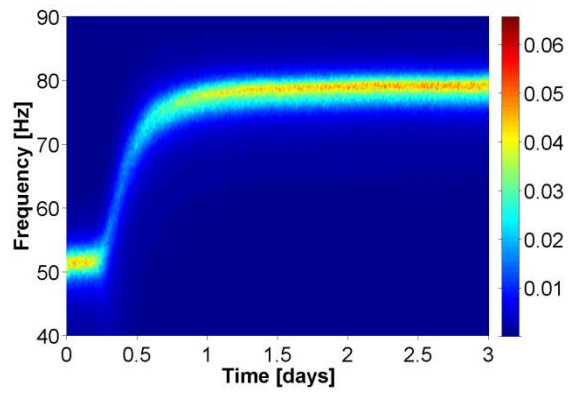
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2 Figure 11 – Example of stress-strain curve obtained from cyclic test at 84 hours.



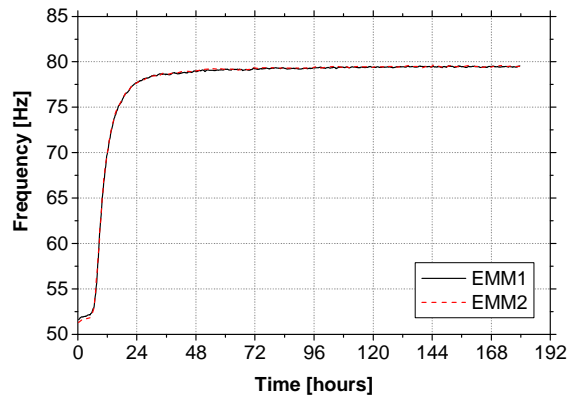
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2 Figure 12 – Frequency spectra for EMM-ARM beam EMM2 at different ages.



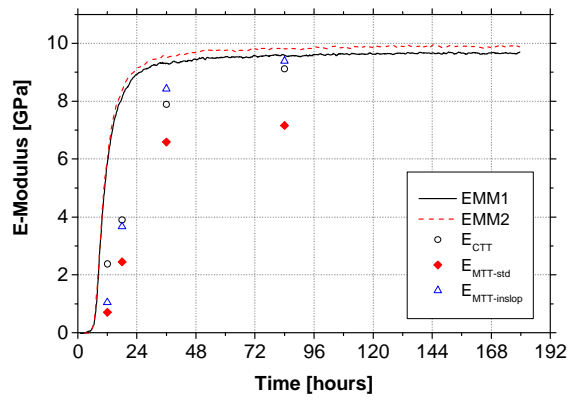
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2 Figure 13 – Colour map of measured frequency spectra along time for the specimen EMM2.



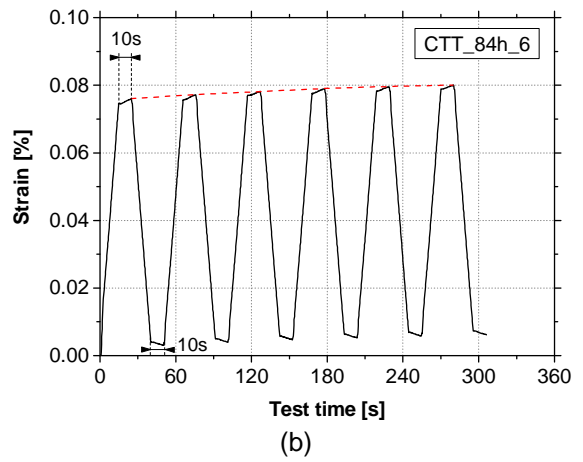
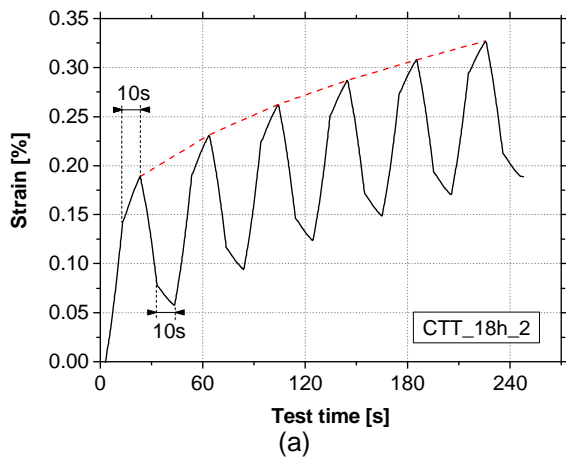
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2 Figure 14 – Resonant frequency evolution of the EMM-ARM beams.



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2 Figure 15 – E-modulus evolution obtained by EMM-ARM, MT and CT tests.



1 Figure 16 – Strain evolution along testing time at: (a) 18 hours; (b) 84 hours.