

# Clustering and forecasting of dissolved oxygen concentration on a river basin

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## Abstract

The aim of this contribution is to combine statistical methodologies to classify geographically homogeneous groups of water quality monitoring sites based on similarities in the temporal dynamics of the dissolved oxygen concentration, to obtain accurate forecasts of this quality variable. Our methodology intends to classify the water quality monitoring sites into spatial homogeneous groups, based on the dissolved oxygen concentration, which has been selected and considered relevant to characterize the quality of the water. We apply clustering techniques based on Kullback Information measures which are obtained in the state space modeling process. For each homogeneous group of water quality monitoring sites, we model the dissolved oxygen concentration using linear and state space models which incorporate tendency and seasonality components in different ways. Both approaches are compared by the mean squared error of forecasts.

**Keywords:** *hydrological basin, water quality, clustering, state space model, linear model, Kalman filter.*

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