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HAL Id: hal-00304237
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Submitted on 6 Jun 2008

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Quantitative performance metrics for stratospheric-resolving chemistry-climate models

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Received: 11 April 2008 – Accepted: 9 May 2008 – Published: 6 June 2008

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Published by Copernicus Publications on behalf of the European Geosciences Union.
Abstract

A set of performance metrics is applied to stratospheric-resolving chemistry-climate models (CCMs) to quantify their ability to reproduce key processes relevant for stratospheric ozone. The same metrics are used to assign a quantitative measure of performance (“grade”) to each model-observations comparison shown in Eyring et al. (2006). A wide range of grades is obtained, both for different diagnostics applied to a single model and for the same diagnostic applied to different models, highlighting the wide range in ability of the CCMs to simulate key processes in the stratosphere. No model scores high or low on all tests, but differences in the performance of models can be seen, especially for transport processes where several models get low grades on multiple tests. The grades are used to assign relative weights to the CCM projections of 21st century total ozone. However, only small differences are found between weighted and unweighted multi-model mean total ozone projections. This study raises several issues with the grading and weighting of CCMs that need further examination, but it does provide a framework that will enable quantification of model improvements and assignment of relative weights to the model projections.

1 Introduction

There is considerable interest in how stratospheric ozone will evolve through the 21st century, and in particular how ozone will recover as the atmospheric abundance of halogens continues to decrease. This ozone recovery is likely to be influenced by changes in climate, and to correctly simulate the evolution of stratospheric ozone it is necessary to use models that include coupling between chemistry and climate processes. Many such Chemistry-Climate Models (CCMs) have been developed, and simulations using these models played an important role in the latest international assessment of stratospheric ozone (WMO, 2007).

Given the importance of CCM simulations there is a need for process-oriented evalu-
A set of core validation processes relevant for stratospheric ozone, with each process associated with one or more model diagnostics and with relevant datasets that can be used for validation, has been defined by the Chemistry-Climate Model Validation Activity (CCMVal) for WCRP’s (World Climate Research Programme) SPARC (Stratospheric Processes and their Role in Climate) project (Eyring et al., 2005). Previous studies have performed observationally-based evaluation of CCMs (e.g., Austin et al., 2003; Eyring et al., 2006) using a subset of these key processes. However, although these studies compared simulated and observed fields they did not assign quantitative metrics of performance (“grades”) to these observationally-based diagnostic tests. Assigning grades to a range of diagnostics has several potential benefits. First, it will allow easy visualization of the model’s performance for multiple aspects of the simulations. Second, in the case of a systematic bias for all models, it will allow identification of missing or falsely modeled processes. Third, it will enable a quantitative assessment of model improvements, both for different versions of individual CCMs and for different generations of community-wide collections of models used in international assessments. Finally, it will make it possible to assign relative weights to the predictions by the different models and to form a best estimate plus variance that takes into account the differing abilities of models to reproduce key processes.

In this paper we perform a quantitative evaluation of the ability of CCMs to reproduce key processes for stratospheric ozone. Our starting point is the recent study by Eyring et al. (2006) (hereinafter “E06”) who evaluated processes important for stratospheric ozone in thirteen CCMs. We consider the same CCMs, diagnostics, and observational datasets shown in E06. This has the advantage that the model simulations, diagnostics, and graphical comparisons between models and observations have already been presented and don’t need to be repeated here. Also, E06 selected these diagnostics as they are important for determining the ozone distribution in the stratosphere. We further simplify our approach by using the same metric to quantify model-observations differences for all diagnostics. This quantification of each CCM’s ability to reproduce key observations and processes is then used to weight ozone projections for the 21st
century from the same CCMs, which were analyzed in Eyring et al. (2007) (hereinafter “E07”).

Several previous studies have performed similar quantitative evaluation of atmospheric models, although not stratospheric CCMs. For example, Douglass et al. (1999) and Strahan and Douglass (2004) performed a quantitative evaluation of stratospheric simulations from an off-line three-dimensional chemical transport model (CTM). In these two studies they assigned grades to multiple diagnostics to assess simulations driven by different meteorological fields. Brunner et al. (2003) compared model simulations of tropospheric trace gases with observations. In contrast to the comparison of climatological fields considered here, they focused on model-observations comparisons at the same time and location as the measurements. This is possible for CTMs driven by assimilated meteorological fields, but not for CCMs. More recently, several studies have performed quantitative evaluations of coupled ocean-atmosphere climate models, and formed a single performance index that combines the errors in simulating the climatological mean values of many different variables (e.g., Schmittner et al., 2005; Connolley and Bracegirdle, 2007; Reichler and Kim, 2008). Our approach draws on several features of the above studies. Several of the diagnostics considered here were considered in Douglass et al. (1999) and Strahan and Douglass (2004), and, in a similar manner to Schmittner et al. (2005), Connolley and Bracegirdle (2007), Reichler and Kim (2008) and Gleckler et al. (2008), we form a single performance index for each model.

The methods used to evaluate the models and weight their projections are described in the next section. The models and diagnostics considered are then described in Sect. 3. Results are presented in Sect. 4, and conclusions and future work discussed in the final section.
## 2 Method

### 2.1 General framework

The general framework used in this paper to evaluate the models and weight their predictions involves the following steps.

1. A suite of observationally-based diagnostic tests are applied to each model.

2. A quantitative metric of performance (grade) is assigned to the application of each observations-model comparison (diagnostic) to each model, i.e., \( g_{jk} \) is the grade of the \( j \)-th diagnostic applied to the \( k \)-th model.

3. Next, the grades for each diagnostic are combined together to form a single performance index for each model, i.e., the single index of model \( k \) is

\[
\bar{g}_k = \frac{1}{W} \sum_{j=1}^{N} w_j g_{jk}
\]

(1)

where \( W = \sum_{j=1}^{N} w_j \), \( N \) is the number of diagnostics, and \( w_j \) is the weight (importance) assigned to each diagnostic. If all diagnostics have equal importance then \( w_j \) is the same for all \( j \).

4. Finally, the model scores are used to weight the predictions of a given quantity \( X \) from \( M \) models, i.e.

\[
\hat{\mu}_X = \frac{1}{\sum \bar{g}_k} \sum_{k=1}^{M} \bar{g}_k X_k
\]

(2)
If $\bar{g}_k$ are the same for all models then this reduces to the normal multi-model mean $\mu_X$. The model scores can also be used to form a weighted variance:

$$\hat{\sigma}_X^2 = \frac{\sum \bar{g}_k}{(\sum \bar{g}_k)^2} \sum_{k=1}^{M} \bar{g}_k (X_k - \hat{\mu}_X)^2. \quad (3)$$

Again, if $\bar{g}_k$ is the same for all models then this reduces to the normal multi-model variance $\sigma_X^2$.

The above framework is not fully objective as several subjective choices need to be made to apply it. For example, decisions need to be made on the diagnostics to apply, the observations to be used, the grading metric to be used, and the relative importance of the different diagnostics for predictions of quantity $X$. These issues are discussed below (see also discussion in Connolley and Bracegirdle, 2007).

2.2 Grading metric

To implement the above framework a grading metric needs to be chosen. Several different metrics have been used in previous model-observation comparisons. For example, Reichler and Kim (2008) used the squared difference between model and observed climatological mean values divided by the observed variance, whereas Gleckler et al. (2008) focus on the root mean squared difference between the model and observed climatological mean values. In this study we wish to use a grading metric that can be applied to all diagnostics, and can easily be interpreted and compared between tests. We choose the simple diagnostic used by Douglass et al. (1999)

$$g = 1 - \frac{1}{n_g} \frac{|\mu_{\text{model}} - \mu_{\text{obs}}|}{\sigma_{\text{obs}}} \quad (4)$$

where $\mu_{\text{model}}$ is the mean of a given field from the model, $\mu_{\text{obs}}$ is the corresponding quantity from observations, $\sigma_{\text{obs}}$ is a measure of the uncertainty (e.g. standard deviation) in the observations, and $n_g$ is a scaling factor. If $g=1$ the simulated field matches
the observations, and smaller $g$ corresponds to a larger difference between model and observations. If $g<0$ then the model-observations difference is greater than $n_g$ times $\sigma$. In our analysis we use, as in Douglass et al. (1999), $n_g=3$, for which $g=0$ if the model mean is $3\sigma$ from the observed climatological mean value. We reset negative values of $g$ to zero, so $g$ is always non-negative. As with the metrics used by Reichler and Kim (2008) and Gleckler et al. (2008), the metric $g$ provides a measure of the difference in model and observed climatological means.

There are several other possible metrics. One is the statistic $t$ used in the standard t-test (Wilks, 1995):

$$
t = \frac{\mu_{\text{model}} - \mu_{\text{obs}}}{\sigma_T \sqrt{\frac{1}{n_{\text{model}}} + \frac{1}{n_{\text{obs}}}}},
$$

where

$$
\sigma_T^2 = \frac{(n_{\text{model}} - 1)\sigma_{\text{model}}^2 + (n_{\text{obs}} - 1)\sigma_{\text{obs}}^2}{(n_{\text{model}} + n_{\text{obs}} - 2)}.
$$

Unlike the metric $g$, or the above metrics, the $t$-statistic involves the variance in both the observations and models. The $t$-statistic has the advantage over the metric (4) in that there is a standard procedure to determine the statistical significance of the differences between models and observations from it. However, the value of $t$ depends on the number of elements in the data sets, and it is not as easy to compare $t$ from different tests that use datasets with a different number of elements as for the metric $g$. Also, it cannot be applied to all our diagnostics as some lack long enough data records for calculation of variance in the observations.

Furthermore, there is in fact a close relationship between $g$ and $t$, and the statistical significance of the model-observations difference can be estimated from the value of $g$. To see this consider the case when the models and observations have the same number of data elements and also the same standard deviations. Then from (4) and
(5) we have
\[ t = \sqrt{\frac{n}{2} n_g (1 - g)}. \] (6)

where \( n = n_{\text{model}} = n_{\text{obs}} \). Given this relationship we can determine the value of \( t \), and hence the statistical significance of the model-observations difference, from the grade \( g \). For example, for \( n_g = 3 \) a grade \( g = 2/3 \) corresponds to \( t = \sqrt{n/2} \). For \( n = 10 \) this value of \( t \) indicates that the difference between the model and observations is significant at greater than 98% while for \( n = 20 \) the difference is significant at greater than 99%. This means that for comparisons of climatological values based on decadal or longer datasets a value of \( g < 2/3 \) is significant at greater than 98%. The above relationship holds only in the above special case, but as shown in Sect. 4.2 it is a good approximation for the more general cases considered here. Hence (6) can be used to estimate \( t \), and the statistical significance, from \( g \).

In the metric (4) the errors for different diagnostics are normalized by the uncertainty in the observations. This means that the mean grade over all models for each diagnostic will vary if the models are better/poorer at simulating a particular process or field. Also, some quantities may be more tightly constrained by observations than others, and this can be captured (by variations in \( \sigma_{\text{obs}} \)) by the metric (4). A different approach was used by Reichler and Kim (2008) and Gleckler et al. (2008), who normalized the error by the “typical” model error for each quantity. This approach means that the average grade over all models will be roughly the same for all diagnostics (around zero).

In summary, we use the metric (4) in our analysis because it can be applied to all the diagnostic tests, is easy to interpret, and can easily be compared between tests. Also, as shown above the statistical significance can be estimated from it.

One limitation with any metric, and in fact any comparison between models and observations, is uncertainties in the observations (and in particular, unknown biases in the observations). If the observations used are biased, then an unbiased model that reproduces the real atmosphere may get a low grade, while a model that is biased...
may get a high grade. The potential of a bias in the observational dataset used can be assessed for diagnostics where there are several sources of data, and we consider several such cases in Sect. 4.2 below. However, for most diagnostics considered here multiple data sets are not available.

3 Models and diagnostics

As discussed in the Introduction we consider the CCM simulations, diagnostics, and observations that were evaluated in E06. The thirteen models considered are listed in Table 1, and further details are given in E06 and the listed reference for each model.

The simulations considered in the E06 model evaluation, and used here to form model grades, are transient simulations of the last decades of the 20th century. The specifications of the simulations follow, or are similar to, the “reference simulation 1” (“REF1”) of CCMVal, and include observed natural and anthropogenic forcings based on changes in sea surface temperatures (SSTs), sea ice concentrations (SICs), surface concentrations of long-lived greenhouse gases (GHGs) and halogens, solar variability, and aerosols from major volcanic eruptions. The simulations considered in E07 are projections of the 21st century (“REF2” simulation), in which the Intergovernmental Panel on Climate Change (IPCC) Special Report on Emission Scenarios (SRES) A1B GHG scenario and the WMO (2003) Ab surface halogens scenario are prescribed. SSTs and SICs in REF2 are taken from coupled atmosphere-ocean model projections using the same GHG scenario.

The diagnostic tests applied to the past CCM simulations are listed in Table 2. Each diagnostic is based on a model-observations comparison shown in E06, and the figures in E06 showing the comparison are listed in Table 2. The exception is the middle latitude Cl\textsubscript{y} test where the comparison is shown in E07, and also Fig. 1 below. Note that E06 also compared the simulated ozone with observations. However, as ozone is the quantity of interest in our analysis, we focus solely on diagnostics of processes that are important for simulating ozone.
Many other diagnostic tests could be used in this analysis, such as those defined in Table 2 of Eyring et al. (2005). However, for this study we focus on a relatively small number of diagnostics that have already been applied. These diagnostics were chosen by E06 as they test processes that are key for simulating stratospheric ozone. In particular, the diagnostics were selected to assess how well models reproduce (a) polar dynamics, (b) stratospheric transport, and (c) water vapor distribution. Correctly simulating polar ozone depletion (and recovery) requires the dynamics of polar regions, and in particular polar temperatures, to be correctly simulated. Assessing the reality of these aspects of the CCMs is thus an important component of a model assessment. Another important aspect for simulating ozone is realistic stratospheric transport. Of particular importance is simulating the integrated transport time scales (e.g. mean age), which plays a key role in determining the distributions of Cl\textsubscript{y} and inorganic bromine (Br\textsubscript{y}). Changes in water vapor can have an impact on ozone through radiative changes, changes in HO\textsubscript{x}, or changes in formation of polar stratospheric clouds (PSCs), and it is therefore also important to assess how well models simulate the water vapor distribution.

Although the model-observations comparisons have already been presented further decisions still need to be made to quantify these comparisons. For example, choices need to be made on the region and season to be used in the grading metric (4). This choice will depend on the process to be examined as well as the availability of observations.

Another important issue in the calculation of the grade is the assignment of \(\sigma_{\text{obs}}\). For some quantities there are multi-year observations and an interannual standard deviation can be calculated, and in these cases we use this in metric (4). For other quantities these observations do not exist and an estimate of the uncertainty in the quantity is used as \(\sigma_{\text{obs}}\). This is not very satisfying, and it would be much better if in all cases \(\sigma_{\text{obs}}\) included both measurement uncertainty and variability. Note, however, that \(\sigma_{\text{obs}}\) does not impact the ranking of models for a particular test, it only impacts comparisons of the grades for different tests.
The regions, seasons, and observations used for each diagnostic are listed in Table 2 and are described in more detail below.

- For the polar temperature diagnostic we focus on the lower stratosphere during winter and spring, as these temperatures are particularly important for modeling polar ozone depletion. Specifically we consider polar average (60–90° N or S) temperatures averaged over 50 to 30 hPa and December to February (60–90° N) or September to November (for 60–90° S). These tests will be referred to as “Temp-NP” and “Temp-SP”, respectively. Climatological mean and interannual standard deviation of ERA-40 reanalyses (Uppala et al., 2005) for 1980-1999 are used for the observations in metric (4), and the same period is used to calculate the model climatology. The biases of the models relative to ERA-40 reanalyses are shown in Fig. 1 of E06.

- The transition to easterlies diagnostic (“U-SP”) measures the timing of the break down of the Antarctic polar vortices in the CCMs. It is based on Fig. 2 of E06, which shows the timing of the transition from westerlies to easterlies for zonal-mean zonal winds at 60° S. The grade is determined using the date for the transition at 20 hPa, and climatological ERA-40 reanalysis for the observations.

- The vertical propagation of planetary waves into the stratosphere plays a significant role in determining polar temperatures during winter and spring (Newman et al., 2001). This wave forcing can be diagnosed with the mid-latitude 100 hPa eddy heat flux for the regions and periods shown in Fig. 3 of E06: 40°–80° N for January-February (“HFlux-NH”), or 40°–80° S for July–August (“HFlux-SH”). This is only one aspect of the information shown in this figure, and grades could also be based, for example, on the slope of the heat flux – temperature relationship.

- The tropical tropopause temperature diagnostic (“Temp-Trop”) is based on the tropical temperature at 100 hPa, shown in Fig. 7a of E06. For this diagnostic Eq. (4) is applied for each month separately, using ERA-40 climatological mean...
and interannual standard deviation for the observations, and then the average of these 12 values is used as the single grade for this diagnostic.

- The entry water vapor diagnostic ("H$_2$O-Trop") is based on the tropical water vapor at 100 hPa, see Fig. 7b of E06. As for the tropical tropopause temperature diagnostic Eq. (4) is applied for each month separately, this time using HALOE climatological mean and interannual standard deviation for the observations (Grooß and Russell, 2005), and the average of these 12 values is used as the single grade. The model climatology is for 1990–1999, whereas the HALOE observations are for 1991–2002.

- The three tracer gradient diagnostics are based on comparisons of the simulated and observed methane (CH$_4$) distributions, see Fig. 5 of E06. We focus on lower stratospheric gradients, and use these diagnostics to assess the lower stratospheric transport in the tropics and polar regions. As CH$_4$ at the tropical tropopause (100 hPa) is very similar in all models and observations we use the tropical (10° S–10° N) averaged values between 30 and 50 hPa to quantify differences in vertical tracer gradients in the tropical lower stratosphere ("CH$_4$-EQ"). Similarly, we use October CH$_4$ at 80° S averaged values between 30 and 50 hPa to quantify differences in vertical tracer gradients in the Antarctic lower stratosphere ("CH$_4$-SP"). We do not include a similar diagnostic at 80° N as HALOE rarely samples 80° N, even if equivalent latitude is used. For subtropical meridional gradients we use the difference in 50 hPa CH$_4$ between 0° N and 30° N, for March and between 0° N and 30° S for October ("CH$_4$-Subt"). A grade is determined for each month separately, and then averaged together to form a single grade for subtropical gradients.

- Diagnostics of the water vapor tape recorder (Mote et al., 1996) test the ability of models to reproduce the amplitude and phase propagation of the annual cycle in tropical water vapor, which in turn tests the model’s tropical transport. As in Hall et al. (1999), we use the phase speed $c$ ("Tape-c") and attenuation of the ampli-
tude $R$ (“Tape-R”) to quantify the ability of the models to reproduce the observed propagation of the $\text{H}_2\text{O}$ annual cycle. The attenuation $R=H/\lambda$, where $\lambda=c \times 1\text{yr}$ is the vertical wavelength and $H$ is the attenuation scale height of the amplitude, $A=\exp(-z/H)$. The values of $c (R)$ are determined from linear (exponential) fits to the simulated phase lag (relative amplitude) from the level of maximum amplitude to 10 km above this level, and compared with similar calculations using HALOE observations (see Fig. 9 of E06).

- The mean age diagnostics are based on comparisons of the simulated with observed mean age at 50 hPa and 10 hPa shown in Fig. 10 of E06. The mean age is an integrated measure of the transport in the stratosphere, and together with tape recorder diagnostics place a stringent test on models transport (e.g. Waugh and Hall, 2002). At each pressure level Eq. (4) is applied separately for the tropics ($10^\circ\text{S}–10^\circ\text{N}$) and northern mid-latitudes ($35^\circ\text{N}–55^\circ\text{N}$), and then the average of these 2 values is used as the single grade for each pressure level (“Age-10hPa” and “Age-50hPa”). Balloon observations are used for mean values and uncertainty at 10 hPa (see symbols in Fig. 10b of E06), whereas ER2 observations are used for 50 hPa (Fig. 10c of E06).

- The $\text{Cl}_y$ diagnostics are based on comparisons with the observed lower stratospheric (50 hPa) $\text{Cl}_y$ shown in Fig. 12 of E06 and Fig. 1 of E07, and repeated in Fig. 1. We calculate grades separately for spring in the southern polar region ($80^\circ\text{S}$, October; “Cly-SP”) and for annual-mean values in northern mid-latitudes ($30^\circ–60^\circ\text{N}$; “Cly-Mid”). The observed mean values and uncertainties used are the same as shown in Fig. 1. As the REF1 simulation in some models stops at the end of 1999, only observations in the 1990s are used in calculating the grade.
4 Results

4.1 Model grades

The diagnostic tests listed in Table 2 have been applied to the thirteen CCMs listed in Table 1 and grades $g$ determined using metric (4). We also calculate the grade for the “mean model”, i.e., the mean over all models is calculated for the various quantities listed in Table 2, and then a grade is calculated using this mean value in the metric (4).

We consider first, as an example, the grades of the Cl$_y$ tests. Figure 1 shows the time series of mid-latitude and polar Cl$_y$ at 50 hPa from the 13 models, together with observations and the mean of the models. As discussed in E06 there is a large spread in the modeled Cl$_y$, and some large model-observations differences. For polar Cl$_y$, models 1, 11, and 12 produce values close to the observations, and these models have grades around 0.9 for $n_g=3$ (see second to bottom row in Fig. 2). However, most of the models produce polar Cl$_y$ much lower than observed, and several models are more than 3$\sigma$ from the mean observations and have a grade of 0 (as noted above, values of $g$ less than zero are reset to zero). Models 4 and 9 are in fact more than 5$\sigma$ from the mean observations. For mid-latitude Cl$_y$ the model-observations differences are not as large as for polar Cl$_y$. Several models are within $\sigma$ of the mean value (and have $g>0.66$) and only one model (model 4) is 3 $\sigma$ away from the mean value. Note the model 8 has a high grade for mid-latitude Cl$_y$ because it agrees with observations before 2000, but Fig. 1 shows that the Cl$_y$ in this model continues to increase and deviates from observations after 2000. If these later measurements were used the grade for this model would be much lower.

We now consider the grades for all diagnostics. The results of the application of each test to each model are shown in Fig. 2. In this matrix (“portrait” diagram) the shading of each element indicates the grade for application of a particular diagnostic to a particular model (a cross indicates that this test could not be applied, because the required output was not available from that model). Each row corresponds to a different diagnostic test (e.g. bottom two rows show $g$ for the two Cl$_y$ tests), and each column
corresponds to a different model. The grades for the “mean model” are shown in the right-most column.

Figure 2 shows that there is a wide range of grades, with many cases with $g \approx 0$ and also many cases with $g > 0.8$. These large variations in $g$ can occur for different diagnostics applied to the same model (e.g., most columns in Fig. 2) or for the same diagnostic applied to different models (e.g., most rows in Fig. 2). The wide range in the ability of models to reproduce observations, with variations between models and between different diagnostics, can be seen in the figures in E06. This analysis quantifies these differences and enables presentation in a single figure.

The wide range of grades for all diagnostic tests shows that there are no tests where all models perform well or all models perform poorly. However, the majority of models perform well in simulating north polar temperatures and NH and SH heat fluxes (mean grades over all models are larger than 0.7), and, to a lesser degree, mid-latitude age (mean grade greater than 0.6), see Fig. 3. At the other extreme the majority of models perform poorly for the Tropical Tropopause Temperature, Entry Water Vapor, and Polar CH$_4$ tests (mean grades less than or around 0.2). Note that caution should be applied when comparing grades from different diagnostics as $g$ is sensitive to the choice of $\sigma$, e.g., use of a smaller $\sigma$ in a test results in lower grades, and some of the variations between diagnostics could be due to differences in the assigned $\sigma$.

Figure 2 also shows that there are no models that score high on all tests or score low on all tests. However, differences in the performance of models can be seen and quantified. For example, several models get low grades on multiple tests, i.e., models 4, 7, 8, and 9 have $g$ near zero for 4 or more transport tests. The poorer performance of these models for several of the transport diagnostics was highlighted in E06.

To further examine the difference in model performance we compare a single performance index calculated from the average grades ($\bar{g}_k$) for each model. This is shown in Fig. 4a, where the average grade is calculated assuming that all diagnostic tests are equally important (i.e., $w_j = 1$ in Eq. 1). If a grade is missing for a particular test and model (crosses in Fig. 2) then this test is not included in the average for that model.
There is a large range in the average performance of the models, with $\bar{g}$ varying from around 0.2 to around 0.7. The value of $\bar{g}$ changes with $n_g$ but there is a very similar variation between models and the ranking of models for different $n_g$. For example, using $n_g=5$ results in a grade around 0.1 larger, for all diagnostics.

The average grade for a model can also be calculated separately for diagnostics that are determined by transport or polar dynamics diagnostics, see Fig. 4b and c. The tropical tropopause temperature and H$_2$O diagnostics are not included in either the polar dynamics or transport averages. The range of model performance for the transport diagnostics is larger than the performance for dynamics diagnostics, with $\bar{g}$ varying from around 0.1 to around 0.8. Figure 4 also shows that some models simulate the polar dynamics much better than the transport (e.g., models 4, 8, and 9) while the reverse is true for others (e.g., models 6 and 13). Part of this could be because the dynamics tests focus on polar dynamics, whereas the majority of the transport diagnostics measure, or are dependent, on tropical lower stratospheric transport.

It is of interest to compare the model average grades shown in Fig. 4 with the segregation of models made by E07. In the plots in E06 and E07 solid curves were used for fields from around half the CCMs and dashed curves for the other CCMs, and E07 stated that CCMs shown with solid curves are those that are in general in good agreement with the observations in the diagnostics considered by Eyring et al. (2006). In making this separation E06 put more emphasis on the transport diagnostics than the temperature diagnostics, with most weight on Cl$_y$ comparisons. As a result the separation used in the E06 and E07 papers is not visible in the mean grades over all diagnostics but can be seen in the average of the transport grades is considered. The models shown as solid curves in E06 and E07 (models 2, 3, 5, 6, 12, and 13) all have high average transport grades, while nearly all those shown with dashed curves have low average transport grades. The exceptions are models 1 and 11 which were shown as dashed curves in E06 and E07 but whose average transport grades in Fig. 4 are high. The reasons for this difference is, as mentioned above, that E06 put high weight on the comparisons with Cl$_y$. Models 1 and 11 significantly overestimate the
mid-latitude $Cl_y$ and have a very low score for the mid-latitude $Cl_y$ test (Fig. 2).

Another interesting comparison is between the grades of individual models and that of the “mean model”. Analysis of coupled atmosphere-ocean climate models has shown that the “mean model” generally scores better than all other models (e.g. Gleckler et al., 2008). This is not however the case for the CCMs examined here (see right most column of Fig. 2). For some of the diagnostics the grade of the mean model is larger than or around the grade of the best individual model, e.g., the NH polar temperatures, heat flux, 10 hPa mean age, and mid-latitude $Cl_y$ diagnostics (see right most column in Fig. 2). However, for most diagnostics the grade for the mean model is smaller than that of some of the individual models, with a large difference for the transition to easterlies, south polar $CH_4$, tape recorder attenuation, and polar $Cl_y$ diagnostics. In these latter diagnostics there is significant bias in most, but not all, of the models, and this bias dominates the calculation of the mean of the models and the grade of the mean model is less than 0.3. But for each of these diagnostics there is at least one model that performs well (e.g., $g$ around or greater than 0.8), and has a higher grade than the mean model. The contrast between a diagnostic where the grade for the mean model is higher than or around the best individual models and a diagnostic where the grade for the mean model is lower than many individual models can be seen in Fig. 1. In panel (a) the $Cl_y$ for individual models is both above and below the observations, and the mean of the models is very close to the observations (and has a high grade). In contrast, in panel (b) most models underestimate the observed $Cl_y$ and the mean $Cl_y$ is much lower than the observations (and several models).

4.2 Sensitivity analysis

As discussed above several choices need to be made in this analysis. A detailed examination of the sensitivity to these choices is beyond the scope of this study. However, a limited sensitivity analysis has been performed for some tests.

We first consider the sensitivity of the grades to the source of the observations. We focus on diagnostics based on the temperature field, as data are available from dif-
different meteorological centers. Figure 5 shows the grades for the (a) Temp-NP, (b) Temp-SP, and (c) Temp-Trop tests when different meteorological analyses are used for the observations. The grades for Temp-NP (panel a) are not sensitive to whether the ERA40, NCEP stratospheric analyses (Gelman et al., 1996) or UK Met Office (UKMO) assimilated stratospheric analyses (Swinbank and O'Neill, 1994) are used as the observations. This is because the climatological values from the three analyses are very similar (within 0.2 K), and the differences between analyses is much smaller than model-observations differences (see Fig. 1 of E06). There is larger sensitivity for Temp-SP (panel b) as there are larger differences between the analyses. However, the general ranking of the models is similar which ever meteorological analyses are used in the grading, i.e., models 1, 5 and 9 have high grades and models 4, 6 and 7 have low grades for all 3 analyses.

The above insensitivity to data source does not, however, hold for the Temp-Trop diagnostic. Here there are significant differences between the meteorological analyses, and the model grades vary depending on which data source is used. The climatological mean UKMO values are around 1 to 2 K warmer than those of ERA40, depending on the month (see Fig. 7 of E06), and as a result very different grades are calculated for some models, see Fig. 5c. For models that are colder than ERA40 lower grades are calculated if UKMO temperatures are used in the metric (e.g., models 3, 5, 9, 12, and 13), whereas the reverse is true for models that are warmer than ERA40 (models 4, 6, 7, 8 and 10).

The above sensitivity to meteorological analyses highlights the dependence of the grading, and any model-data comparison, on the accuracy of the observations used. It is therefore important to use the most accurate observations in the model-data comparisons. With regard to the temperature datasets used above, intercomparisons and comparisons with other datasets have shown that some biases exist in these meteorological analyses. In particular, the UKMO analyses have a 1–2 K warm bias at the tropical tropopause, and the NCEP analyses have a 2–3 K warm bias at the tropical tropopause and a 1–3 K warm bias in Antarctic lower stratosphere during winter-spring
(Randel et al., 2004). Given these biases, it is more appropriate to use, as we have, the ERA40 analyses for the model grading.

Another choice made in the analysis is the metric used to form the grades. As discussed in Sect. 2.2, an alternate metric to the one used here is the $t$-statistic. It was shown in Sect. 2.2 that there is a simple linear relationship between $t$ and $g$ in cases with the same number of data points and same standard deviations for the models and observations (see Eq. 6). To test this in a more general case we compare $t$ and $g$ for tests using temperature and CH$_4$ fields. For these tests there are multi-year observational data sets, and the mean and variance from these observations and from the models can be used to calculate $t$ and $g$.

Figure 6 shows this comparison for the (a) Temp-NP and Temp-SP, and (b) CH$_4$-EQ and CH$_4$-SP diagnostic tests. For these comparisons we do not set negative values of $g$ to zero, so that we can test how well the relationship (6) holds. (If we set negative $g$ to zero then the points left of the vertical dashed lines move to the left to lie on this line.) As expected there is a very close relationship between the calculated values of $t$ and $g$, and an almost identical ranking of the models is obtained for both metrics. Furthermore, the values of $t$ are close to those predicted by (6), which are shown as the solid lines in Fig. 6. The deviations from this linear relationship are due to differences in $\sigma$ between models and observations. The above shows that a very similar ranking of the models will be obtained whether $t$ or $g$ are used, and the results presented here are not sensitive to our choice of $g$ as the metric.

4.3 Relationships among diagnostics

We now examine what, if any, correlations there are between grades for different diagnostics. If a strong correlation is found this could indicate that there is some redundancy in the suite of diagnostics considered, i.e., two or more diagnostics could be testing the same aspects of the models. Identifying and removing these duplications from the suite of diagnostics would make the model evaluation more concise. However, an alternative explanation for a connection between grades for different diagnostics could be that the
models that perform poorly for one process also perform poorly for another process. In this case the two diagnostics are not duplications, and the consideration of both might provide insights into the cause of poor performance.

Figure 7 shows the correlation between the grades for each of the different diagnostics. There are generally low correlations between the grades, which indicates that in most cases the tests are measuring different aspects of the model performance. There are however some exceptions, and several notable features in this correlation matrix.

As might be expected, several of these high correlations occur between grades for diagnostics based on the same field, e.g. between the two mean age diagnostics and the two tape recorder diagnostics. There might, therefore, be some redundancy in including two grades for each of these quantities, e.g., it might be possible to consider a single grade for mean age which considers just a single region or averages over all regions. However, this is not the case for all fields, and there are low correlations between the two Cl diagnostic, between the two polar temperature diagnostics, and between the CH diagnostic. Thus diagnostics using the same fields can measure different aspects of the simulations, and averaging into a single grade might result in loss of information.

High correlations between grades might also be expected for some pairs of diagnostics that are based on different fields but are dependent on the same processes. One example are the Temp-Trop and H2O-Trop diagnostics. As the water vapor entering the stratosphere is dependent on the tropical tropopause temperature a high correlation is expected between these two diagnostics. There is indeed a positive correlation, but the value of 0.48 may not be as high as expected. The fact that the correlation is not higher is mainly because of two models, whose performance differs greatly for these two diagnostics. The 100 hPa temperature in model 2 is much colder than observed (with a zero grade for this diagnostic) but the 100 hPa water vapor is just outside 1σ of the observed value (g=0.61). The reverse is true for model 9, which has a low water vapor grade but reasonable temperature grade. For the remaining models, models with low grades for the tropical temperature tend to have low grades for the water vapor
There are high positive correlations between many of the transport diagnostics, i.e., there are generally high correlations between the tape recorder, mean age, and equatorial CH$_4$ diagnostics. This is likely because these diagnostics measure, or are dependent, on tropical lower stratospheric transport, and a model with good (poor) transport in the tropical lower stratosphere will have good (poor) grades for all these diagnostics.

Another area where strong correlations might be expected is between the heat flux, polar temperatures, and transition to easterlies diagnostics. However, in general, the correlations between these fields is not high. The exception is the high correlation (0.75) between the eddy heat flux and transition to easterlies in the southern hemisphere. A high correlation between these diagnostics might be expected as weak heat fluxes might lead to a late transition. However, this is not likely the cause of the high correlation. First, the heat flux diagnostic is for mid-winter (July–August) and the late-winter/spring heat fluxes are likely more important for the transition to easterlies. More importantly, several of the models with late transitions, and very low grades for this diagnostic, actually have larger than observed heat fluxes (models 1, 5 and 13), which is opposite than expected from the above arguments. Again, this anomalous behavior suggests possible problems with these models and the need for further analysis.

Figure 7 also shows some correlation between the transport and dynamics diagnostics. In fact there are several cases where there is moderate to high negative correlations between a dynamics diagnostic and a transport diagnostic, suggesting that there are models that perform poorly for (tropical) transport diagnostics but perform well for (polar) dynamical diagnostics. As discussed above this is indeed the case for several
models (most notably models 8 and 9) see Fig. 4).

4.4 Weighted ozone projections

The assignment of grades to the diagnostic tests enables relative weights to be assigned to the ozone projections from different models, and for a weighted mean to be formed that takes into account differing abilities of models to reproduce key processes. We explore this issue using ozone projections for the 21st century made by the same CCMs, and shown in E07. Note, models 6 and 11 did not perform simulations into the future, and the analysis below is only for the other 11 models listed in Table 1.

E07 examined the model projections of total column ozone for several different regions and for different diagnostics of polar ozone. We focus here on two ozone diagnostics: (a) annual mean northern mid-latitude total ozone (Fig. 5 of E07) and (b) minimum Antarctic total column ozone for September to October (Fig. 8b of E07). Similar results are found for all total ozone quantities shown in E07.

To form a weighted mean it is necessary to form a single performance index for each model (e.g. \( \bar{g}_k \) in Eq. 1). If all diagnostics considered here are given equal weight then the weighted mean using these indices is very similar to the unweighted mean (not shown). If however, the performance index is based only on the transport diagnostics there is a larger variation between models (see Fig. 4), and some differences between weighted and unweighted may be expected.

To examine these differences we compare the unweighted and weighted mean using model indices based on the average transport grade. We are using this index for the weighting only for illustrative purposes, and not to imply this is the best index to use. In Fig. 8 the ozone for individual models is shown as black curves, the unweighted mean in red, and the weighted mean in blue. The jumps in the mean curves, e.g. at 2050, occur because not all model simulations cover the whole time period, and there is a change in the number of model simulations at the location of the jumps, e.g. eight models performed simulations to 2050, but only three models simulate past 2050.

For both the northern mid-latitude ozone and Antarctic minimum ozone there are
only small differences between the weighted and unweighted mean values, even when only transport diagnostics are used for the weighting. This is because there is a wide range in the ozone projections, and for most time periods models that simulate ozone at opposite extremes have similar grades. For example, there are large differences (≈100 DU) in minimum Antarctic ozone after 2050 between one of the three models and the other two, but the three models have similar average grades (\(\bar{g} \approx 0.6–0.7\)) and the unweighted and weighted means are very similar. The largest difference between unweighted and weighted means occurs between 2030 and 2050. This difference is primarily because of the ozone and index for model 8. During this period model 8 predicts much lower ozone than the other models (the black curve with lowest ozone between 2020 and 2050 is model 8), but this model has a low index (≈0.2) which means that less weight is put on the ozone from this model in the weighted mean. As a result the weighted mean is larger than the unweighted mean.

The conclusion from the above analysis is that, at least for these CCM simulations, weighting the model results does not significantly influence the multimodel mean projection of total ozone. A similar conclusion was reached by Stevenson et al. (2006) in their analysis of model simulations of tropospheric ozone, and by Schmittner et al. (2005) in their analysis of the thermohaline circulation in coupled atmosphere-ocean models.

5 Conclusions

The aim of this study was to perform a quantitative evaluation of stratospheric-resolving chemistry-climate models (CCMs). To this end, we assigned a quantitative metric of performance (grade) to each of the observationally-based diagnostics applied in Eyring et al. (2006). The same metric was applied to each diagnostic, and the ability of the thirteen CCMs to simulate a range of processes important for stratospheric ozone quantified.

This analysis quantified several features noted in Eyring et al. (2006). A wide range
of grades were obtained, showing that there is a large variation in the ability of the CCMs to simulate different key processes. This large variation in grades occurs both for different diagnostics applied to a single model and for the same diagnostic applied to different models. No model scores high or low on all tests, but differences in the performance of models can be seen. This is especially true for transport processes where several models get low grades on multiple transport tests, as noted in Eyring et al. (2006).

The assignment of grades to diagnostic tests enables a single performance index to be determined for each CCM, and for relative weights to be assigned to model projections. Such a procedure was applied to the CCMs’ projections of 21st century ozone (Eyring et al., 2007). However, only small differences are found between weighted and unweighted multi-model mean ozone projections, and weighting these model projections based on the diagnostic tests applied here does not significantly influence the results.

Although the calculation of the grades and weighting of the ozone projections is relatively easy, there are many subjective decisions that need to be made in this process. For example, decisions need to be made on the grading metric to be used, the source and measure of uncertainty of the observations, the set of diagnostics to be used, and the relative importance of different processes/diagnostics. We have performed some limited analysis of the sensitivity to these choices, and Gleckler et al. (2008) have discussed these issues in the context of atmosphere-ocean climate models. However, further studies are required to address this in more detail. In particular, determining the relative importance of each diagnostic is not straightforward, and more research is needed to determine the key diagnostics and the relative importance of each of these diagnostics in the weighting.

This study provides only an initial step towards a quantitative grading and weighting of CCM projections. We have evaluated only a subset of key processes important for stratospheric ozone, in particular we have focused on diagnostics to evaluate transport and dynamics in the CCMs and to a lesser extent the representation of chemistry
and radiation. Also we have only evaluated the climatological mean state and not the ability of the models to represent trends and interannual variability. However, this study does provide a framework, and benchmarks, for the evaluation of new CCM simulations, such as those being performed for the upcoming SPARC CCMVal Report (http://www.pa.op.dlr.de/CCMVal/).

Acknowledgements. We acknowledge the CCM groups of AMTRAC (GFDL, USA), CCSRNIES (NIES, Tsukuba, Japan), CMAM (MSC, University of Toronto and York University, Canada), E39C (DLR Oberpfaffenhofen, Germany), GEOSCCM (NASA/GSFC, USA), LMDZrepro (IPSL, France), MAECHAM4CHEM (MPI Mainz, Hamburg, Germany), MRI (MRI, Tsukuba, Japan), SOCOL (PMOB/WRC and ETHZ, Switzerland), ULAQ (University of LAquila, Italy), UMETRAC (UK Met Office, UK, NIWA, NZ), UMSLIMCAT (University of Leeds, UK), and WACCM (NCAR, USA) for providing their model data for the CCMVal Archive. Co-ordination of this study was supported by the Chemistry-Climate Model Validation Activity (CCMVal) for WCRP’s (World Climate Research Programme) SPARC (Stratospheric Processes and their Role in Climate) project. We thank the British Atmospheric Data Center for assistance with the CCMVal Archive. This work was supported by grants from NASA and NSF.

References


Austin, J., Wilson, R. J., Li, F., and Vomel, H.: Evolution of water vapor concentrations and


### Table 1. CCMs used in this study.

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<th>Reference</th>
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<td>CCSRNIES</td>
<td>Akiyoshi et al. (2004)</td>
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<td>CMAM</td>
<td>Fomichev et al. (2007)</td>
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<td>LMDZrepro</td>
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<td>MAECHAM4CHEM</td>
<td>Steil et al. (2003)</td>
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<td>MRI</td>
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<td>ULAQ</td>
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<td>UMETRAC</td>
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<td>UMSLIMCAT</td>
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### Table 2. Diagnostic tests used in this study.

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<th>Fig. E06</th>
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<td>Temp-SP</td>
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<td>U-SP</td>
<td>Transition to Easterlies</td>
<td>U, 20hPa, 60° S</td>
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<td>JF, 40°–80° N, 100 hPa</td>
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<td>HFlux-SH</td>
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<td>H2O-Trop</td>
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<td>ER2 CO2</td>
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<td>30°–60° N, 50 hPa, Annual mean</td>
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Fig. 1. Time series of (a) annual-mean, 35°–60° N, and (b) October-mean, 80° S Cl$_2$ at 50 hPa from CCM simulations (curves) and observations (symbols plus vertical bars).
Fig. 2. Matrix displaying the grades (see color bar) for application of each diagnostic test to each CCM. Each row shows a different test, and each column a CCM. The right most column is the “mean model”. A cross indicates that this test could not be applied, because the required output was not available from that model.
Fig. 3. Average grade over all models for each diagnostic test.
Fig. 4. Average grade for each model for (a) average over all diagnostic tests used in this study (see Table 2), (b) average only over transport diagnostics, and (c) average only over polar dynamics diagnostics. Note, we have evaluated only a subset of key processes important for stratospheric ozone.
Fig. 5. Comparison of model grades for the (a) Temp-NP, (b) Temp-SP, and (c) Temp-Trop tests when ERA40 (black), UKMO (red), or NCEP (blue) meteorological analyses are used for the observations in the metric (4).
Fig. 6. Comparison of $t$-statistic with grading metric $g$ for (a) Temp-NP and Temp-SP tests or (b) CH$_4$-EQ and CH$_4$-SP diagnostic tests. The solid lines show the theoretical relationship given by Eq. (6) for (a) $n=20$ and (b) $n=11$. 
Fig. 7. Matrix displaying the correlation between the grades for different diagnostics.
Fig. 8. Temporal variation of (a) annual mean anomalies for total ozone averaged over northern mid-latitudes (35° N to 60° N) and (b) minimum Antarctic ozone for individual models (black curves), unweighted mean (red) and weighted mean (blue) of all models. The thick black curve and shaded region in (a) shows the mean and range of observed ozone anomalies, while the black dots in (b) show the observed minimum total ozone, see E06 for details.