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**Published paper**

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# The Relationship between IR Effectiveness Measures and Users' Satisfaction

## ABSTRACT

This paper presents an experimental study of users assessing the quality of Google web search results. In particular we look at how users' satisfaction correlates with the effectiveness of Google as quantified by IR measures such as precision, Bpref and the suite of Cumulative Gain measures (CG, DCG, NDCG). Results indicate strong correlation between users' satisfaction, CG and precision, moderate correlation with DCG, with perhaps surprisingly negligible correlation with NDCG. The reasons for the low correlation with NDCG are examined.

## Categories and Subject Descriptors

B.8 [Performance and Reliability]: General

**General Terms:** Measurement, Performance

**Keywords:** User satisfaction, IR Effectiveness measures

## 1. INTRODUCTION

Search engines are among the most popular and useful services on the web. Since the effectiveness of a retrieval system should be evaluated on the basis of how much it helps users achieve their task effectively and efficiently [2], the rating of search engine results by the user should be taken into account to evaluate search engines as a whole. To our knowledge there is no previous work that directly addresses the relationship between *precision*, Cumulative Gain (*CG*), Discounted Cumulative Gain (*DCG*), Normalized Discounted Cumulative Gain (*NDCG*) and users' satisfaction. Therefore, this paper presents the relationship between these measures.

## 2. METHODOLOGY

The study asked 26 users to search on four queries from a pool of 104 queries. The tasks were designed to emulate a simple information finding task (i.e., find a document that contains material relevant to an information need). Users searched directly in Google<sup>1</sup>, which was chosen for its popularity and high effectiveness as identified by [1]. Time allotted for each task was twelve minutes and users were asked to judge the first ten documents resulting from the best query they issued. They rated the effectiveness of each document at three levels of relevancy: *highly-relevant*<sup>2</sup>; *reasonably relevant*<sup>3</sup>; *not relevant*<sup>4</sup>. They also

rated their satisfaction<sup>5</sup> with the "accuracy", "coverage" and "ranking" of the results.

<sup>1</sup> <http://www.google.co.uk/>

<sup>2</sup> The document directly addresses the core issue of the topic

<sup>3</sup> The document only points to the topic, but it does not discuss the themes of the topic thoroughly

<sup>4</sup> The document does not contain any information about the topic.

<sup>5</sup> very satisfied=1, partially satisfied=0.5, not satisfied=0

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## 3. FINDINGS

The effectiveness of Google' results were quantified based on Bpref, precision, CG, DCG, NDCG, users' satisfaction with the ranking of the results, as well as their satisfaction with accuracy and coverage, shown in Table 1.

**Table 1. Overall effectiveness of Google measured across users and queries (measures are computed at the first 10 documents)**

Bpref-10	0.88
NDCG	0.87
Precision	0.63
(U. S) <sup>6</sup> Accuracy	0.54
(U. S) Coverage	0.54
(U. S) ranking of results	0.50

Pearson's correlation was used to find the relationship between these measures, shown in Table 2. According to these figures, Cumulative Gain is the best measure to model users' perception of the results: it strongly correlates (0.79) with users' satisfaction with ranking of the results, and moderately correlates with their satisfaction of Accuracy (0.68) and Coverage (0.60). Precision is the second best measure to correlate with users' satisfaction; it strongly correlates with users' satisfaction with ranking (0.70), and moderately correlates with their satisfaction of Accuracy (0.59) and Coverage (0.53). DCG only correlates moderately with users' perception of the results; 0.69 with users' satisfaction of the ranking, (0.60) with their satisfaction of Accuracy and (0.50) with their satisfaction of Coverage. Perhaps surprisingly, NDCG did not correlate well with users' satisfaction of the results. We also note that users' assessments of the results (their satisfaction with accuracy, coverage and their satisfaction with the ranking) all correlate well with each other.

**Table 2. Correlation between measures**

Measures	Pearson's Correlation
CG vs. DCG	0.90
CG vs. NDCG	0.37
CG vs. Precision	0.88
CG vs. Bpref-10	0.55
CG vs. U. S. ranking of results	0.79
CG vs. U.S. Accuracy	0.68
CG vs. U.S. Coverage	0.60
DCG vs. NDCG	0.46

<sup>6</sup> U.S.= Users' Satisfaction

DCG vs. Precision	0.75
DCG vs. Bpref-10	0.48
DCG vs. U. S. ranking of results	0.69
DCG vs. U.S. Accuracy	0.60
DCG vs. U.S. Coverage	0.50
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NDCG vs. Precision	0.14
NDCG vs. Bpref-10	0.29
NDCG vs. U. S. ranking of results	0.26
NDCG vs. U.S. Accuracy	0.10
NDCG vs. U.S. Coverage	0.10
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Precision vs. Bpref-10	0.54
Precision vs. U. S. ranking of results	0.70
Precision vs. U.S. Accuracy	0.59
Precision vs. U.S. Coverage	0.53
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Bpref-10 vs. U. S. ranking of results	0.35
Bpref-10 vs. U.S. Accuracy	0.28
Bpref-10 vs. U.S. Coverage	0.20
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U. S. ranking of results vs. U.S. Accuracy	0.79
U. S. ranking of results vs. U.S. Coverage	0.67
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U.S. Accuracy vs. U.S. Coverage	0.72

\*The highlighted measures indicate strong and significant correlation ( $p < 0.05$ )

## 4. DISCUSSION

NDCG was initially tested and proven to work well in test collection evaluations with the existence of a wide range of relevance judgments [3] [4]. However, the work discussed here has a very limited set of judgments which effected NDCG during the normalizing step, especially in cases where the ranking was identical to the ideal which led  $NDCG=1.0$  (this situation was unlikely to occur in the past work [3] [4]). Hence NDCG does not correlate strongly with other measures (such as precision, users' satisfaction with coverage, accuracy and ranking of the results) when working with a limited number of relevance judgments.

Figure 3 shows some example systems: showing in the first column the rank position, (r), followed by the gain:  $g(r)$ , ( $g(2)$  = highly relevant,  $g(1)$  = reasonably relevant,  $g(0)$  =not relevant). The next columns are the cumulative gain,  $cg(r)$ , discounted cumulative gain,  $dcg(r)$ , normalized discounted cumulative gain,  $ndcg(r)$ , and precision, (p). Systems A, B, C, D, E, and F all show the advantages of NDCG by incorporating all levels of relevance judgment, while giving precedence to more relevant items. However, NDCG has some drawbacks in disregarding the degree of relevancy if a system returns only documents with one level of relevancy (e.g. G & H), in these systems  $NDCG=1$ , because they are considered to have a perfect order (ideal ranking) and cannot be normalized (i.e., rearranging the documents in descending order of relevancy). This problem also occurs if a system has only one relevant item and at the top of the rank (I & J); NDCG doesn't distinguish between the degrees of relevancy in these cases. Moreover, in the last two systems (K, L), NDCG is equal to 0.67; though these systems differ in relevancy but both have one relevant item located at the same rank. Therefore, for the last six systems, precision is a more appropriate measure than NDCG. Precision also has its limitation as shown in the first six systems (A, B, C, D, E, F) in disregarding the location of relevant items as

well as in not considering multiple relevance judgments. Therefore, examining a combination of measures appears to be better because some measures work well in some conditions while others work better in others.

System A	System B																																																												
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Figure 3. Imaginary systems that reflect NDCG vs. Precision

## 5. CONCLUSION

We have quantified the quality of Google based on a range of common IR measures with over 104 user queries. We have concluded that CG and precision correlate better than NDCG with users' satisfaction of the results, though NDCG has been proven to work well in search engine evaluation. We have also shown that both NDCG and precision have their own shortcomings, therefore, a combination of measures is better to complement each other when evaluating the effectiveness of IR systems.

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