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**Novel optical imaging technique to determine the 3D orientation  
of collagen fibers in cartilage: variable-incidence-angle  
polarization-sensitive optical coherence tomography.**

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Running headline:

variable-incidence angle 3D PS-OCT

## SUMMARY

*Objective:* to investigate a novel optical method to determine the 3-D structure of articular cartilage collagen non-destructively.

*Methods:* Polarization-sensitive optical coherence tomography was used to determine the apparent optical birefringence of articular cartilage for a number of different illumination directions. A quantitative method based on the theory of light propagation in uniaxial crystalline materials was validated on equine flexor tendon. Qualitative maps of fiber polar and azimuthal orientation at sites on the posterior and anterior segments of the equine third metacarpophalangeal (fetlock) joint were produced, and the azimuthal orientations compared with data from a split-line experiment.

*Results:* Polar and azimuthal angles of cut flexor tendon broadly agreed with the nominal values but suggested that the accuracy was limited by our method of determining the apparent birefringence. On intact equine fetlock joints we found a non-zero polar tilt that changed in direction at various points along the apex, moving from the sagittal ridge outwards. The azimuthal orientation changes from being parallel to the sagittal ridge in the posterior region to being inclined to the ridge in the anterior region. This broadly agrees with split-line data for the anterior region but differs in the posterior region, possibly reflecting depth-dependent orientation changes.

*Conclusion:* General quantitative agreement was found between our method and histology in validation experiments. Qualitative results for cartilage suggest a complicated 3-D structure that warrants further study. There is potential to develop this approach into a tool that can provide depth-resolved information on collagen orientation in near-real-time, non-destructively and in-vivo.

**Keywords:** Polarization-sensitive OCT, collagen, birefringence, cartilage, osteoarthritis tissue engineering.

## INTRODUCTION

Osteoarthritis is generally recognized to involve a degradation of the extracellular matrix in articular cartilage. Treatments include osteochondral autograft, autologous chondrocyte implantation and tissue engineering of replacement cartilage tissue<sup>1</sup>. Unfortunately many tissue engineered cartilage constructs display poor adhesion to the surrounding native cartilage, leading to poor mechanical performance when exposed to in-vivo stresses<sup>2</sup>. Since the primary supplier of tensile strength is type-II collagen, it is likely that the organization of collagen fibers at a given location is strongly related to the mechanical demands existing at that site. Evidence exists that the superficial layer, containing fibers oriented parallel to the surface, is important for distributing applied compressive loads over a larger volume of tissue, for example<sup>3</sup>. Consequently it has been proposed that improved mechanical performance will result from ensuring that the collagen matrix regenerates to a morphologically similar state as existed in the original tissue and that, in tissue engineered constructs, this could be achieved by the application of a suitable mechanical stimulus<sup>4</sup>. To further this end, methods that could assess the 3-D organization of cartilage collagen *in situ* are potentially valuable.

A number of methods exist to determine collagen orientation. The simplest method is the “split-line” technique, in which the cartilage tissue is pricked with a needle and then splits along the direction of collagen alignment<sup>5</sup>. Obviously this technique is destructive and laborious. Small angle x-ray

scattering (SAXS) is powerful but cannot be used *in vivo* and lacks depth-penetration or intrinsic depth-sectioning<sup>6</sup>. Its use therefore is confined to histological sections. Recent advances in magnetic resonance imaging, especially diffusion-tensor imaging, now allow non-destructive determination of the 3-D orientation of collagen fibers in cartilage<sup>7</sup>. However, the method is too slow (hours per volume image) to apply *in vivo* and too expensive to be deployed routinely in, for example, a bioreactor. Also, the voxel size is typically around 100 microns, which is comparable to the length scale on which cartilage shows large variations in collagen organization (the superficial layer is typically about 100 microns thick).

Many biological tissues exhibit strong linear optical birefringence, particularly those whose main constituent is collagen. Hence polarized light microscopy, especially in conjunction with Sirius Red staining, has been used for decades to determine the collagen orientation from measurements of the birefringence fast-axis orientation<sup>8</sup>. However the method is destructive and gives definitive information only on fiber orientation within the plane of sectioning. More recently, polarized FTIR imaging has proven successful in determining collagen fiber orientations<sup>9</sup>. Again however FTIR imaging is limited to imaging the exposed surface of cut tissue, because of the low penetration of mid-IR light into biological tissue. It could not be used to remotely interrogate cultured tissues that were immersed in an aqueous environment. Hence there is a need for a tool that can yield high-resolution 3-D information cheaply, rapidly, non-destructively and remotely.

In recent years polarization-sensitive OCT (PS-OCT) has emerged as a powerful means to image tissue birefringence *in vivo*, with reported applications in studying burn depths in skin<sup>10</sup>, characterizing osteoarthritic changes in articular cartilage<sup>11</sup> and studying the variation of fiber

orientation with depth in muscle<sup>12</sup> and intervertebral disk. PS-OCT is derived from optical coherence tomography (OCT), which can be thought of as an optical analogue of ultrasound (US) imaging. Unlike US, OCT has lower tissue penetration ( $\leq 1$  mm depending on tissue type and optical wavelength used) but much higher spatial resolution ( $< 2$  microns axial resolution has been demonstrated and 10 microns lateral resolution is typical). Over the last decade, OCT has established itself as the method of choice for retinal imaging *in vivo*<sup>13</sup> and is attracting interest in many biomedical applications including tissue engineering<sup>14</sup>. OCT generates its image contrast in the same manner as US imaging *i.e.* it identifies tissue boundaries. It has shown promise as a tool for studying the in-situ development of cartilage allografts in a rabbit model of osteoarthritis<sup>15</sup>. PS-OCT extends the performance of OCT by adding a new contrast mechanism: tissue birefringence.

Previous reports on the use of PS-OCT have concentrated on situations in which the fibers are oriented so as always to lie parallel to the tissue surface. In this case it is only necessary to determine the ‘fast-axis’ orientation, which corresponds to the azimuthal orientation of the collagen fiber (since collagen is technically a ‘positive uniaxial’ material, the fast-axis lies at  $90^\circ$  to the long-axis of the fibers). However in cartilage it is well known from histology that this is not the case, with fibers showing a large variation in their polar angle with depth. The polar angle (measured relative to the surface normal), ranges from  $90^\circ$  in the superficial layer to around zero degrees in the radial layer, where the fibers then meet the tide-mark. In the intervening transitional layer the fibers have an intermediate and less ordered orientation.

In order to determine the fiber polar angle, we previously introduced a method of imaging the tissue using a series of angle-dependant measurements for a given location on the surface<sup>16</sup>. It is known

from the optics of uniaxial birefringent materials that if light propagates along the optic axis (*i.e.* the ‘*c*-axis’ in optical terminology), then the sample displays no birefringence whereas if the light beam travels orthogonal to the fiber long-axis then the observed birefringence reaches its maximum value<sup>17</sup>. It is generally assumed that this *c*-axis corresponds to the long-axis of the collagen fibers in birefringent biological tissues. We therefore crudely determined the 3-D collagen orientation by determining the illumination direction that apparently yielded zero birefringence. A further development was to make this method quantitative, by exploiting the known theoretical relationship between the “apparent” birefringence, the “true” birefringence (this latter quantity being an intrinsic optical property of the tissue, determined by the density and spatial ordering of collagen fibrils, the refractive index of the ground substance, etc<sup>18</sup>) and the angle between the *c*-axis and the light propagation direction<sup>19</sup>. This simplified method used illumination directions confined to a single-plane and assumed that the fibers were inclined only in this plane, *i.e.* it was effectively assumed that the azimuthal angle was zero. This simple quantitative approach was validated by determining the polar angle of fibers in a cut piece of equine flexor tendon.

In this report we extend the method to infer full 3-D information by relaxing this assumption and adding measurements for incident beams that are inclined in two orthogonal planes.

## METHODS

All measurements were conducted on *ex vivo* tissue samples taken from horses destined for the human food chain. Intact forelimbs were obtained from a local abattoir, operated in accordance with relevant legislation.

## ARTICULAR CARTILAGE SAMPLES

Tissue samples were taken from the equine fetlock joint, which permits rotation in the sagittal plane between the proximal phalanx and the third metacarpal bone. This joint often displays osteoarthritic lesions, probably because of the relatively small contact area available at this joint for the transmission of the ground reaction force during running on hard surfaces.

Intact equine forelimbs were dissected to separate the third metacarpal from the proximal phalanx. The condyle of the third metacarpal was then isolated by sawing away and discarding most of the shaft. Figure 1 shows a photograph of the tissue preparation, prior to imaging. The condyles, with intact cartilage attached, were then either imaged fresh or stored in a  $-80$  Celsius freezer for subsequent defrosting and imaging. During imaging, the samples were maintained moist by application of  $0.15\text{M}$  NaCl during measurements. In several experiments, the angle between the cartilage surface and the probe beam was varied in two orthogonal planes. This was achieved by mounting the specimen on a system of two graduated rotation stages, whose positions were adjusted as a function of inclination angle, in order to image a fixed site on the surface and whose axes of rotation allowed rotation of the joint surface in these planes.

## POLARIZATION OCT SYSTEM.

Several excellent reviews of the PS-OCT technique can be found in the optics literature<sup>20</sup>. Our polarization-sensitive low-coherence interferometer design has been described in detail elsewhere<sup>21</sup>. Briefly, light from a  $0.9\text{ mW}$ ,  $1.3\mu\text{m}$  broad-band superluminescent diode (SLD) light-source is vertically polarized and launched into a bulk-optics PS-OCT interferometer. Visible light from a  $635$

nm laser diode is coupled into the SLD output fiber using a 90:10 2×1 coupler, thus aiding visualization of the near-infrared sample beam on the tissue surface. A non-polarizing beam splitter diverts 50% of the light into the sample arm, where it is passed through a quarter-wave plate, with fast-axis at 45° to the vertical, thus illuminating the sample with circularly polarized light. The sample light is focused onto the specimen using a 0.10 NA microscope objective, yielding a transverse resolution of approximately 20 μm FWHM. The reference arm light is passed through a quarter wave plate and variable neutral density filter<sup>22</sup> before entering a scanning optical delay. Movement of the mirror in this delay line allows us to acquire a single OCT A-scan, analogous to an US A-scan. A 2D cross-sectional images (*i.e.* an OCT ‘B-scan’) is built up by collecting multiple A-scans whilst laterally scanning the sample using a motor stage.

After interferometric recombination with the back-scattered sample beam, the light is split into horizontally and vertically polarized components using a polarizing beam splitter. Two OCT depth-resolved interferograms, one for the horizontal and one for the vertical polarized light components, are then detected by two identical photoreceivers, amplified and then digitized by an analog-to-digital converter card hosted by a PC. Standard OCT signal processing is then applied<sup>23</sup> which produces demodulated A-scans for the two orthogonal polarization states. Denoting the amplitudes of the demodulated signals for the vertical and horizontal polarization components as  $A_v(z)$  and  $A_h(z)$  respectively, where  $z$  is physical depth into the sample, then Hee *et al.* showed that the depth-resolved cumulative single-pass retardance  $\delta$  (*i.e.* the phase-difference between the horizontal and vertical electric field components that is accumulated by the light beam in propagating to a given depth in the medium) can be calculated using the following formula<sup>24</sup>:

$$\delta(z) = \tan^{-1}(A_v(z)/A_h(z)).$$

Equation 1

The retardance is related to a more fundamental quantity, which we will term the “apparent birefringence”  $\Delta n$  by the formula:

$$\delta(z) = z \frac{2\pi \Delta n}{\lambda_0},$$

Equation 2

where  $\lambda_0$  is the wavelength of the light in air (NB this formula is a simplified version which assumes that  $\Delta n$  does not vary with depth  $z$ ). Since both  $A_v(z)$  and  $A_h(z)$  are always positive, in this simple PS-OCT approach  $\delta$  will be determined modulo  $\pi/2$  radians. Hence for a tissue with uniform  $\Delta n$ , PS-OCT yields 2-D cross-sectional images of  $\delta$  (*i.e.* “retardance images”) that have a banded appearance with respect to depth  $z$ . The band-spacing  $d$  represents the distance  $z$  over which  $\delta$  increases from 0 to  $\pi$  and so can be used to infer  $\Delta n$  using the equation:

$$\Delta n = \frac{\lambda_0}{2d}$$

Equation 3

Hence the band-spacing in a PS-OCT retardance image gives a simple way to infer  $\Delta n$ .

However, there are situations in which this method may not be applicable, in particular in weakly birefringent media the retardation band may be so broad that its full extent cannot be discerned from the OCT image (the typical useable depth of which in cartilage is 0.7 to 1 mm). In this case one can try to determine the birefringence by measuring the slope of the retardance  $\delta$  with respect to  $z$  *i.e.* using the equation

$$\Delta n = \frac{\lambda_0}{2\pi} \frac{d\delta(z)}{dz}$$

Equation 4

This approach has the advantage that  $\Delta n$  can be estimated for weakly birefringent tissues such as cartilage, where a complete birefringence band may not be visible. It has the additional advantage that depth-dependent variations in  $\Delta n$  can be detected because  $\delta(z)$  versus  $z$  will not be a straight line. However in our experience it has the disadvantage that it tends to underestimate  $\Delta n$ . The reason for this is illustrated in Figure 2. The origin of Equation 1 is that one can show that the vertically and horizontally polarized interference amplitudes  $A_v$  and  $A_h$  oscillate with increasing depth according to the relation (in the ideal case)

$$A_v(z) = \sin\left(\frac{2\pi}{\lambda_0} \Delta n z\right) \quad A_h(z) = \cos\left(\frac{2\pi}{\lambda_0} \Delta n z\right).$$

Equation 5

In the absence of phase-resolved information only the magnitude of  $A_v$  and  $A_h$  are determined hence  $\delta(z)$  ideally starts at zero at  $z = 0$  (when  $A_v=0$ ), then increases uniformly to a peak value of  $\pi/2$  (at  $z = \lambda_0/4\Delta n$ , hence  $A_h=0$ ) until falling uniformly back to zero. This pattern then repeats indefinitely. In reality however a) the amplitudes of the back-scattered fields falls exponentially with depth with a decay constant  $\mu t$  and b) the measurements will always include background noise terms due to for example system measurement noise and also multiply backscattered and randomly polarized light. Hence  $A_v$  and  $A_h$  can never truly fall to zero and so  $\delta$  never fully achieves the values of zero and  $\pi/2$ . This effect becomes more pronounced with increasing depth. The “noise-affected” curve in Figure 2 is generated by modifying Equation 5 to the form:

$$A_v(z) = \sin\left(\frac{2\pi}{\lambda_0} \Delta n z\right) \cdot \exp(-2\mu_l z) + \sigma \quad A_h(z) = \cos\left(\frac{2\pi}{\lambda_0} \Delta n z\right) \cdot \exp(-2\mu_l z) + \sigma$$

Equation 6

where  $\sigma$  is a noise bias term.

For both methods of  $\Delta n$  determination, speckle noise was reduced by typically averaging 25 lateral A-scans are to produce the graph of retardance versus depth. Normal incidence of the OCT light beam onto the tissue surface was determined by maximizing the strength of the Fresnel reflection from the air/tissue interface. Rotation of the sample through a known angle was thus made relative to this known starting point.

#### DETERMINATION OF 3-D FIBER ORIENTATION: THEORY.

To describe the birefringence displayed by cartilage tissue with an arbitrary 3-D orientation of the collagen fibers, the tissue was modelled as a positive uniaxial birefringent crystal structure. As noted above, if light propagates along the  $c$ -axis of such a medium then the sample displays no birefringence whereas if the light beam travels orthogonal to the fiber long-axis then the observed birefringence reaches its maximum value. More quantitatively, it is well known that if an optical plane wave propagates through this material with angle  $\theta_c$  between the direction of propagation and the  $c$ -axis then two orthogonal polarization eigenmodes exist which experience refractive indices  $n_o$  and  $n$  respectively, where  $n$  is given by,

$$\frac{1}{n^2} = \frac{\sin^2 \theta_c}{n_e^2} + \frac{\cos^2 \theta_c}{n_o^2},$$

Equation 7

where  $n_o$  is the “ordinary” and  $n_e$  the “extraordinary” refractive index. This motivates us to define the apparent birefringence as  $\Delta n = n - n_o$  and the true birefringence as  $n_e - n_o$ . Clearly, the true birefringence of the tissue is the more fundamental quantity, whereas the apparent birefringence is determined by the true birefringence and geometric factors. The two quantities are related by:

$$\Delta n = n_o \left( \frac{n_e}{\sqrt{n_o^2 + \cos^2(\theta_c) \cdot (n_e^2 - n_o^2)}} - 1 \right).$$

Equation 8

Our method involves determining  $\Delta n$  using PS-OCT retardance images for a set of different illumination directions. In a previous paper we described a method to determine the polar angle of the optic axis of a uniaxial birefringent biological tissue quantitatively by making PS-OCT measurements with a number of incident illumination directions and hence different values of  $\theta_c$ <sup>19</sup>. By assuming a value for  $n_o$ , the simultaneous solution of a set of Equation 8 yields best-estimates for the unknown polar orientation and extraordinary refractive index  $n_e$ . The method was validated on equine flexor tendon, yielding a variability of 4% for the true birefringence and 3% for the polar angle. However this method assumed that the optic axis lay in a given plane and that the illumination directions lay in this same plane.

In this paper we again model biological tissue as a uniaxial crystal and solve for the orientation of the  $c$ -axis in three dimensional space. The simple analysis presented here assumes that the  $c$ -axis has a non-zero azimuthal angle  $\phi$ , in addition to a polar angle  $\theta$  different from  $90^\circ$  and that both of these parameters stay constant with depth.

Let the plane of incidence with azimuthal angle  $\phi = 0$  be the  $y$ - $z$  plane. Then  $k_{oz}$  and  $k_{ez}$  are the  $z$ -components of the ordinary and extraordinary wave-vector respectively. Hence the incident ordinary and extra-ordinary wave vectors can be written as:

$$\mathbf{k}_o = \beta \hat{y} + k_{oz} \hat{z} \quad \mathbf{k}_e = \beta \hat{y} + k_{ez} \hat{z}$$

Equation 9

A similar result applies when the plane of incidence is the  $x$ - $z$  plane i.e the azimuthal angle  $\phi = 90^\circ$ .

Here  $\beta$  is the tangential component of the incident wave-vector and is conserved during refraction across a plane interface.

On entering the tissue, Snell's law of refraction implies that the transmitted wave vector (denoted by primed symbols) becomes (Figure 3):

$$\hat{k}' = \sin \gamma' \cdot \hat{y} + \cos \gamma' \cdot \hat{z} = \frac{\sin \gamma}{n_0} \cdot \hat{y} + \left(1 - \frac{\sin^2 \gamma}{n_0^2}\right)^{1/2} \cdot \hat{z}$$

Equation 10

for the  $y$ - $z$  plane of incidence, where  $\gamma' (= \theta + \theta_c)$  is the polar angle of the transmitted wave vector.

Let the direction of the  $c$ -axis in 3-D space be defined by a unit vector  $\hat{c}$  in spherical polar coordinates  $(\theta, \phi)$ <sup>25</sup>:

$$\hat{c} = (\hat{x} \cdot \sin \phi + \hat{y} \cdot \cos \phi) \cdot \sin \theta + \hat{z} \cdot \cos \theta$$

Equation 11

From Figure 3 we see that  $\cos \theta_c = \hat{c} \cdot \hat{k}'$  and so when the plane-of-incidence is the  $y$ - $z$  plane then applying Equation 10 and Equation 11 we have:

$$\cos \theta_{c1} = \cos \phi \cdot \sin \theta \cdot \sin \gamma' + \cos \theta \cdot \cos \gamma'$$

Equation 12

A similar result holds for the  $x$ - $z$  plane-of-incidence.

If a value for  $n_o$  is assumed or measured then substituting Equation 12 and its equivalent into Equation 8 for measurements in two orthogonal planes respectively yields relationships between the apparent birefringence  $\Delta n$ , the angle of illumination  $\gamma$  and the three unknown parameters  $\phi$ ,  $\theta$  and  $n_e$ . Simultaneous solution of the resulting system of equations using measured values of  $\Delta n$  for different values of  $\gamma$  can then yield estimates for these unknowns. We obtain best-estimates for  $\phi$ ,  $\theta$  and  $n_e$  from an over-constrained problem by performing a 3-variable minimization of the error metric

$$\chi^2 = \sum_{i=1}^{10} \left( \Delta n_{i,\text{measured}} - \Delta n_{i,\text{predicted}} \right)^2,$$

Equation 13

where the 10 measurements correspond to 5 illumination directions for each of the two orthogonal planes of incidence.

## RESULTS

### VALIDATION EXPERIMENTS - I

To investigate the accuracy of our method to quantitatively characterize the three dimensional orientation of the optical  $c$ -axis in biological tissues a series of measurements on tendon tissue were made. A sample of equine flexor tendon was cut, whilst frozen, such that the  $c$ -axis was oriented at a polar angle of approximately  $20^\circ$ , as judged by a digital photograph. Then the sample was rotated in a holder to produce an azimuthal angle  $\phi \approx 30^\circ$ . The surface of the cut was illuminated at normal incidence and by clockwise and anticlockwise angle sequences  $\pm 20^\circ$ ,  $\pm 40^\circ$  in two orthogonal planes of incidence. Measurements of apparent birefringence were made in all cases by taking profiles through the resulting retardance images and measuring the physical spacing  $d$  of the retardance bands for each illumination direction (an ordinary tissue refractive index of  $n_o = 1.4$  was assumed in order to convert optical path into physical path). Sets of five measurements of  $\Delta n$  versus  $\gamma$  were then compiled and the error-metric  $\chi^2$  minimized w.r.t.  $n_e - n_o$ ,  $\theta$  and  $\phi$  using the Nelder-Mead simplex algorithm (Matlab® function `fminsearch`), using an initial guess for  $n_e - n_o$  equal to the largest  $\Delta n$  in the measurement set, the initial  $\theta$  equal to that  $\gamma'$  in the set which yields the smallest  $\Delta n$  and the initial  $\phi$  equal to  $0$  or  $90^\circ$  depending on whether the widest retardance band occurred for the  $y$ - $z$  or  $x$ - $z$  plane of incidence.

Table 1 lists the resulting estimates for  $n_e - n_o$ ,  $\theta$ ,  $\phi$  and also the minimum  $\chi^2$  achieved by the simplex algorithm for various samples. All samples had nominal polar fiber orientation approximately  $65$ - $75^\circ$  ( $\theta_{\text{nominal}}$ ) and  $30$ - $35^\circ$  nominal azimuthal angle ( $\phi_{\text{nominal}}$ ), as measured by a digital photograph. The incident light beam was oriented normal to the surface and at different incident angles  $\pm 20^\circ$ ,  $\pm 40^\circ$  for two orthogonal planes.

For the first sample the derived value of  $\theta$  ( $\theta_{\text{derived}}$ ) was within 4% of the nominal value and the derived value of  $\phi$  was within 5% of the nominal value. However the difference for the second and third samples was larger. The derived value of the polar angle fluctuates by 10 % and 5% and the value for azimuthal angle is within 3% and 5% of the nominal value respectively.

Our estimated experimental uncertainty in determining the retardance band spacing is about 10%. By manually adjusting the retardance bands spacing within this tolerance *i.e.* by about 10% we could derive polar and azimuthal angle for all samples within about 2% of their nominal values (columns  $\theta_{\text{adjusted}}$  and  $\phi_{\text{adjusted}}$  list the values). This suggests that our method is currently limited by our accuracy in determining the retardance band spacing. Often the bands were rather indistinct. We are currently working to improve the data collection procedure for retardance images and to improve the precision of the algorithm of birefringence calculations using Jones matrix methods.

## **VALIDATION EXPERIMENTS - II**

In some situations (for example when  $\theta$  or  $n_e - n_o$  are small) then  $\Delta n$  is too small for a complete birefringence band to be formed, for many of the illumination directions. To explore this case, we extended the method to make use of  $\Delta n$  derived using Equation 4. A sample of tendon was cut with a polar angle of  $20^\circ$  and adjusted so that  $\Phi = 0^\circ$ , then retardance images were collected in the usual way (see Figure 4). It is evident that it is not possible to infer the band-spacing from most of these images however  $\Delta n$  can be extracted using Equation 4. Table 2. Tendon experiments comparing results obtained by the method used in Table 1 with the method based on Equation 4. The last row reports results for the data shown in Figure 4 *i.e.* where the method used in Table 1 cannot be applied, due to the

absence of a complete retardance band. Table 2 summarizes the results of the tendon experiments comparing the method used in Table 1 with that based on Equation 4. The last row reports results for the data shown in Figure 4 i.e. where the method used in Table 1 cannot be applied, due to the absence of a complete retardance band. Note that where the two methods are compared, the fiber orientation information is in good agreement but the true birefringence is underestimated by the gradient-based method. This shows that careful calibration of noise-bias effects are needed if accurate birefringence measurements are to be obtained using PS-OCT deep in scattering tissues.

## ARTICULAR CARTILAGE COLLAGEN STRUCTURE

We expect that our method will help to clarify the situation regarding predominant fiber orientations in cartilage tissue where they are arranged in a complicated 3-D manner. Given the need to improve the precision of the quantitative 3-D method noted above, initially we have investigated the structure of cartilage in a semi-qualitative manner. Equation 8 shows that, for a given  $n_e$  and  $n_o$ , the smaller the  $\Delta n$  the smaller the angle between the light propagation direction and the  $c$ -axis. By observing whether the apparent birefringence is greater or smaller or roughly equal for incidence angles that are symmetrically placed about normal incidence, we have constructed a qualitative map of dominant  $c$ -axis orientation as follows.

In subsequent sections we will refer to two orthogonal planes in the tissue. The plane containing the sagittal ridge is the “sagittal plane” while the “coronal plane” is orthogonal to this but also contains the long-axis of the bone shaft. Referring to Figure 6 we see that these two planes divide the half-space lying above the joint surface into four octants. Labelling directions lying in these planes as A, P, M and L (meaning directions in the

anterior, posterior, medial or lateral direction), then we can label these octants as AM, AL, PM and PL (for anterior-medial etc). For PS-OCT scanning we arrange the joint surface such that the sagittal plane is aligned with the laboratory vertical. We then illuminate a fixed point on the sample with five illumination directions as follows: direction '0' is normal to the surface, 'v1' and 'v2' are directions confined to the lab vertical plane and symmetrically oriented about the surface normal with incident angles  $+35^\circ$  and  $-35^\circ$  whilst 'h1' and 'h2' are the equivalent directions lying in the lab horizontal plane. Then for each of these five illumination directions we obtain PS-OCT retardance images and qualitatively score the birefringence on a five-point scale of increasing birefringence, denoted by the symbols (-, \*, \*\*, \*\*\*, \*\*\*\*) where for example '-' denotes the absence of observable birefringence. Then we can ascribe a qualitative 3-D c-axis orientation to the c-axis as follows. Imagine projecting the c-axis out of the tissue and up into the positive half-space. If the location of the distal end of this vector lies in the octant 'AM' then we denote this orientation as AM, indicating a polar tilt and also an azimuthal orientation into octant AM. If the c-axis lies parallel to the surface and also in the sagittal plane then we denote this as A $\rightarrow$ P. If the c-axis has a polar tilt and is confined to the sagittal plane, such that the distal end of the vector is directed towards the anterior, then we denote this as SA. If the vector points parallel to the surface normal then we denote this as N. In total there are 13 such directions. Table Y tabulates a subset of these and shows how the qualitative birefringence score for the five illumination directions has a unique pattern for each 3-D orientation, in terms of the symmetry/asymmetry and absolute values of the  $\Delta n$  values obtained for each direction. In this way we obtain a qualitative 3-D mapping of cartilage. The only serious restriction of this approach occurs when the fibers lie in the plane of the surface (i.e.  $\theta = 90^\circ$ ). In this case it is not

possible to determine the position of the  $c$ -axis uniquely as its position can be mirrored in the sagittal or coronal plane and still produce the same apparent birefringence. However this situation is readily handled by determining the fast-axis orientation using phase-resolved methods<sup>26</sup> (although we have not done that in this report).

We first collected PS-OCT images taken at anterior and posterior sites with illumination directions lying in the coronal plane. At each point, a sequence of measurements was made in the two orthogonal planes, with equal but opposite illumination angles. For all locations and angles 4 mm wide by 1 mm deep retardance images were acquired. Figure 7 shows the results. PS-OCT images from the posterior region (upper row) showed similar retardance images for equal and opposite polar angles of illumination (left and right columns), with no distinct retardance bands visible. On the other hand, results for anterior part (lower row) show a clear asymmetry, with a distinctive retardance band visible for illumination direction  $-35^\circ$ , but not for  $+35^\circ$ . This means that in the posterior region the apparent birefringence is low for both illumination directions but in the anterior region is markedly higher for the negative illumination direction. In earlier studies, we collected PS-OCT images taken at these same sites with illumination directions lying in the sagittal plane. From these previous studies we inferred that at these sites the dominant  $c$ -axis has a polar angle oriented as shown in Figure 8. Combining this information with that obtained from the coronal plane, we infer that the fibre long axis lies approximately in the plane parallel to sagittal ridge in the posterior region. In the anterior region the data suggest that the fibres long axis is inclined towards the internal part of the joint, *i.e.* in the direction of sagittal ridge, as shown schematically in Figure 9. These results suggest a complicated 3-D structure for the collagen fibre orientation in the radial layers of the cartilage.

To gain confidence that such variations in fiber orientations genuinely exist and are not spurious artefacts, independent assessments were made using the established techniques of split-line analysis and polarised-light micrographs. Firstly, an intact metacarpophalangeal joint was pricked with a needle dipped in India Ink. Figure 10 shows the anterior surface of the joint, with the ridge to the left and the apex towards the top. Note the similarity between the azimuthal orientation of the fibers in the superficial layer and that suggested by PS-OCT for the deeper regions (Figure 9). Figure 11 shows a pair of polarized-light micrographs, obtained from the metacarpophalangeal joint. Samples of bone with cartilage attached were cut while frozen into 20 micron thick coronal sections. Images collected from sites at each end of the slice, separated by about 1 cm, are shown in the figure. These images clearly demonstrate that the preferred orientation of chondrocyte cells, and by implication the collagen matrix, is highly changeable on centimetre length scales.

To study collagen fiber orientation further, we collected a series of OCT images along a line to the anterior side of the apex, extending from close to the sagittal ridge to the margin (Figure 12). This area is of interest as it is subjected to high loading yet rarely demonstrates osteochondral lesions<sup>27</sup>. Sequences of angle-resolved measurements were made for three spots along that line (Figure 13). Rows 1 to 3 correspond to points 1-3 respectively. For all locations and angles, 4 mm long images were acquired. Images for equal and opposite polar angles show inverse appearance of retardation bands. At site 1 there are retardation bands for positive polar angles of illumination but at the third site a banded retardation image arises for negative polar illumination angle. This implies that the polar angle of the fibers changes as one moves from the ridge towards the margin, as shown schematically in Figure 14. This “twist effect” of collagen fiber polar orientation at points along the

apex in articular cartilage may be related to *in-vivo* load distributions. A detailed investigation of the 3-D collagen fiber orientation through the whole area of articular cartilage therefore appears to be justified.

## DISCUSSION

We have described a novel optical technique to determine 3-D structural information concerning collagen alignment in intact articular cartilage. The method is rapid, non-destructive and offers good penetration (1-2 mm) into intact tissue. It could potentially be applied *in-vivo* during arthroscopy or as a monitoring tool in a bioreactor. This report introduces the basic concept and produces qualitative maps of the dominant fiber orientation in cartilage based on measurements of apparent optical birefringence using multiple illumination directions in two orthogonal planes. This work further suggests that this structure is non trivial, with site-to-site variations in polar and azimuthal angles for the collagen in the radial zone. The work is however merely a starting point and the method has, we believe, significant potential for improvement.

Firstly the quantitative application of our method to tendon uses the simplest method of determining the apparent birefringence  $\Delta n$ , which is to measure the band-spacing in the retardance images. However this method of estimating  $\Delta n$  restricts quantitative application to tissues with high  $\Delta n$ . Since tissues such as cartilage and meniscus have lower  $\Delta n$ <sup>28</sup> our reported results for cartilage are qualitative. However more sophisticated methods exist for calculating  $\Delta n$  e.g. calculating the slope of retardance versus distance or using Jones-matrix/Stokes-vector approaches. These methods do not require the presence of a complete

birefringence band and so an interesting area for further development is to apply these approaches to the quantitative mapping of cartilage structure.

Secondly, measurement of apparent birefringence in two orthogonal planes is experimentally cumbersome and likely to be difficult to perform *in-vivo* during an arthroscopy. More fundamentally, the two planes of imaging obviously do not overlap in 3-D space, which means the tissue must have broadly uniform collagen organization over an area of a few square millimeters, so that the data from the two planes can meaningfully be combined. However, in this report we have only used part of the information available from PS-OCT, namely the apparent birefringence. PS-OCT can also provide information on the apparent fast-axis orientation<sup>26,29</sup>. A formalism exists, the Extended Jones Matrix calculus, to relate both quantities to the absolute 3-D c-axis orientation, so that it should be possible to extract the desired information using illumination directions confined to a single plane<sup>30</sup>.

Thirdly, PS-OCT intrinsically yields depth-resolved information so that the rather qualitative picture of collagen orientation in the radial zone presented here could be refined considerably. There have been several reports in which the fast-axis orientation of birefringent tissues has been inferred as a function of depth for muscle and intervertebral disk. This approach typically use a more sophisticated PS-OCT system than that used in our study, in which the incident polarization state is modulated and the back-scattered polarization state analyzed in order to infer the depth-resolved Jones matrix of the sample. By combining these approaches with multiple illumination directions it should be possible to determine the 3-D structure of the superficial and radial zones independently and also infer the extent of the transitional zone, as the random orientation of fibers in this region

should manifest itself as a region with very low apparent birefringence for all illumination directions. The development of such an algorithm is an ongoing project in our laboratory. Further results will be reported in due course.

The ability to determine the 3-D structure of cartilage collagen non-destructively and rapidly has a number of potential applications. Firstly it would allow a complete characterization of normal joints and allow one to relate fiber morphology to *in-vivo* load distributions. Secondly, the production of a tissue-engineered construct to replace damaged cartilage at a particular site could then include site-specific information when determining the appropriate scaffold geometry needed to promote correctly oriented collagen *in-situ*. Thirdly, the implanted construct could be monitored arthroscopically and the degree to which collagen had correctly regenerated could be quantitatively studied. Finally, basic biomechanical data concerning the properties of cartilage could be obtained by exploiting the near real-time data acquisition speed of PS-OCT. Since PS-OCT is non-contact, one could envisage an experiment in which cartilage is dynamically loaded over physiologically relevant timescales (*e.g.* to match load-bearing exercise) and the dynamic reorientation of the fibers in 3-D space monitored.

In summary, variable-incidence-angle PS-OCT has the potential to become a tool with unique capabilities for studying the collagen structure of intact articular cartilage. The prospects of improved tissue-engineered constructs and the quantitative assessment of ECM production *in-situ* should act as a powerful stimulus to fully develop the method.

## ACKNOWLEDGMENTS

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## FIGURE CAPTIONS

Figure 1. Photograph illustrating the equine third metacarpophalangeal joint. The sagittal ridge is clearly seen in the middle of the condyle (end of left-most bone).

Figure 2. A comparison between the ideal and actual (i.e. "noise-affected") depth-resolved retardance curve for a uniformly birefringent material such as tendon. Note how the gradient of the actual retardance profile systematically underestimates the gradient of the "ideal" curve and hence produces an estimate of  $\Delta n$  that is lower than that inferred from the band-spacing.

Figure 3. Refraction of light between an isotropic (top) and uniaxially anisotropic (bottom) medium.

Figure 4. Retardance images obtained from a tendon sample cut such  $\theta = 20^\circ$  and  $\phi = 0^\circ$  (i.e. collagen fibers oriented so as to run vertically in the lab frame).  $\Delta n$  is consequently low and hence a full birefringence band is not evident for many angle of illumination. Left column: illumination directions lying in the laboratory horizontal plane with polar angles of  $-40^\circ$ ,  $0^\circ$  and  $+40^\circ$  respectively. Right column: ditto for the vertical plane. As can be seen, it is impossible to infer  $\Delta n$  from the band-spacing for most of these images, however it can be inferred from the curve of retardance versus depth.

Figure 5. Illustrative curve of retardance versus physical depth extracted from the bottom-left image in Figure 4.

Figure 6. Illustrating the sagittal and coronal planes in relation to the tissue surface normal and also the anterior, posterior, lateral and medial directions (A, P, L, M respectively). These planes divide up the tissue into four octants AM, PM, AL, PL respectively, each of which represents a unique 3-D *c*-axis orientation that can be inferred using the semi-qualitative method described in the text.

Figure 7. Retardance images obtained at a point on the posterior surface of the condyle (top row) and anterior (bottom row), using angles of incidence in air of  $-35^\circ$  (left) and  $+35^\circ$  (right), where a negative angle signifies that the beam propagates from the margin towards the sagittal ridge. The tissue surface is at the top of the image, but the air above the surface appears as grey noise rather than a dark region, because  $A_v$  and  $A_h$  are zero in this region and so the retardance is then calculated as the ratio of two noisy quantities. Note the approximately symmetric appearance of the retardance images in the posterior region but the marked asymmetry for the anterior region, with a clear retardance band visible using an angle of incidence in air of  $-35^\circ$ .

Figure 8. Reproduced from 16 shows the dominant *c*-axis polar orientation inferred by comparing  $\Delta n$  values for different illumination directions that are confined to the sagittal plane (retardance images not shown).

Figure 9. Schematic diagram of the apparent variation in azimuthal orientation of type-II collagen fibers of the equine fetlock joint on the posterior and anterior surfaces. Coronal view: the joint apex is at the top of each diagram.

Figure 10. The anterior surface of a condyle after performing a split-line experiment. The apex is at the top of the photograph. The general fiber alignment suggested by destructive testing of the superficial layer is in qualitative agreement with the alignment suggested by non-destructive PS-OCT of the deeper layers.

Figure 11. Polarized-light micrographs obtained from each end of a 1.5 cm coronal cartilage section. Clear differences in the directional alignment are evident over cm length scales, lending support to the indications from PS-OCT.

Figure 12. Schematic of the condyle (sagittal ridge in gray), with the three measurement sites on the anterior side of the apex labeled 1 to 3.

Figure 13. Retardance images obtained at the points 1-3 are shown in rows 1-3 respectively (the tissue surface is towards the bottom of the images). The left column is a 4×1 mm sagittal section image taken with the illumination beam inclined in the sagittal plane by an angle of 40° towards the posterior side of the joint (i.e. the beam travels from the posterior towards the anterior: defined as -40°) while the right column shows the corresponding image obtained with an equal and opposite positive angle of illumination i.e. inclination towards the anterior side.

Figure 14. The dominant polar orientation of collagen fibers at the measurement sites 1-3, as suggested by the asymmetric retardance images shown in Figure 9. At point 1, nearest the sagittal ridge, the fibers are directed towards the anterior. This orientation changes to being directed towards the posterior at the point nearest the margin.

## TABLE CAPTIONS.

Table 1. Best-estimates of the true birefringence  $n_e-n_o$ , fiber polar angle  $\theta$  and azimuthal angle  $\phi$  of a sample of tendon cut to possess nominal parameters  $\theta_{\text{nominal}}$  and  $\phi_{\text{nominal}}$ . Each row reports results obtained using incidence angles of  $[-20^\circ, +20^\circ, 0^\circ, -40^\circ, +40^\circ]$  for the light beam in both orthogonal planes.

Table 2. Tendon experiments comparing results obtained by the method used in Table 1 with the method based on Equation 4. The last row reports results for the data shown in Figure 4 i.e. where the method used in **Table 1** cannot be applied, due to the absence of a complete retardance band.

Table 3. Illustrating how the qualitative 5-point scoring of apparent birefringence, obtained using 5 illumination directions, can be used to infer the approximate orientation of the fiber c-axis in 3-D space. This semi-qualitative method is used to analyze the cartilage data.

## TABLES

<i>sample number</i>	$n_e - n_o$	$\theta_{\text{derived}}$	$\theta_{\text{nominal}}$	$\theta_{\text{adjusted}}$	$\phi_{\text{derived}}$	$\phi_{\text{nominal}}$	$\phi_{\text{adjusted}}$	$\chi^2$ (min)
1	$5.3 \times 10^{-3}$	$76.6^\circ$	$73^\circ$	$75.7^\circ$	$34^\circ$	$33^\circ$	$35^\circ$	$2.6 \times 10^{-6}$
2	$5.4 \times 10^{-3}$	$78.6^\circ$	$69^\circ$	$72.2^\circ$	$38^\circ$	$31^\circ$	$32.1^\circ$	$5.3 \times 10^{-7}$
3	$4.7 \times 10^{-3}$	$79.3^\circ$	$63.5^\circ$	$66.7^\circ$	$31^\circ$	$33^\circ$	$31^\circ$	$1.4 \times 10^{-6}$

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$\theta_{\text{nominal}}$	$\phi_{\text{nominal}}$	$\theta_{\text{derived}}$	$\phi_{\text{derived}}$	$n_e - n_o$	$\theta_{\text{derived}}$	$\phi_{\text{derived}}$	$n_e - n_o$
		<i><math>\Delta n</math> from band-spacing</i>			<i><math>\Delta n</math> from retardance gradient</i>		
90°	0°	85°	0°	$5.1 \times 10^{-3}$	96°	-9°	$2.2 \times 10^{-3}$
20°	0°	n/a	n/a	n/a	23°	0°	$3 \times 10^{-3}$

Table 2. Tendon experiments comparing results obtained by the method used in Table 1 with the method based on Equation 4. The last row reports results for the data shown in Figure 4 i.e. where the method used in Table 1 cannot be applied, due to the absence of a complete retardance band.

	0	h1	h2	v1	v2
N	-	**	**	**	**
A→P	****	****	****	**	**
AM	**	*	***	*	***
SA	**	**	**	*	***

Table 3. Illustrating how the qualitative 5-point scoring of apparent birefringence, obtained using 5 illumination directions, can be used to infer the approximate orientation of the fiber c-axis in 3-D space. This semi-qualitative method is used to analyze the cartilage data.

## FIGURES



Figure 1. Photograph illustrating the equine third metacarpophalangeal joint. The sagittal ridge is clearly seen in the middle of the condyle (end of left-most bone).

Ideal vs noise-affected retardance profiles.

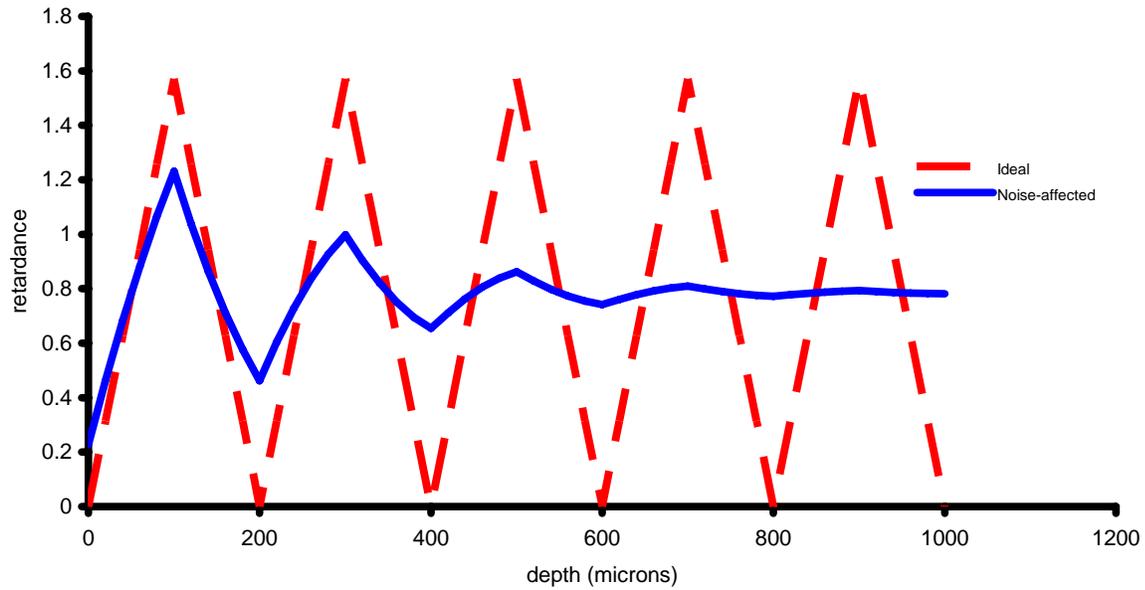


Figure 2. A comparison between the ideal and actual (i.e. "noise-affected") depth-resolved retardance curve for a uniformly birefringent material such as tendon. Note how the gradient of the actual retardance profile systematically underestimates the gradient of the "ideal" curve and hence produces an estimate of  $\Delta n$  that is lower than that inferred from the band-spacing.

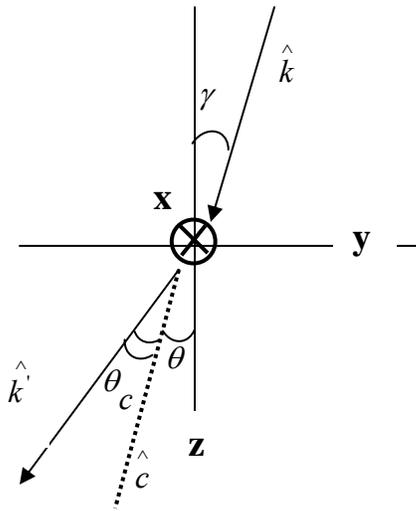


Figure 3. Refraction of light between an isotropic (top) and uniaxially anisotropic (bottom) medium.

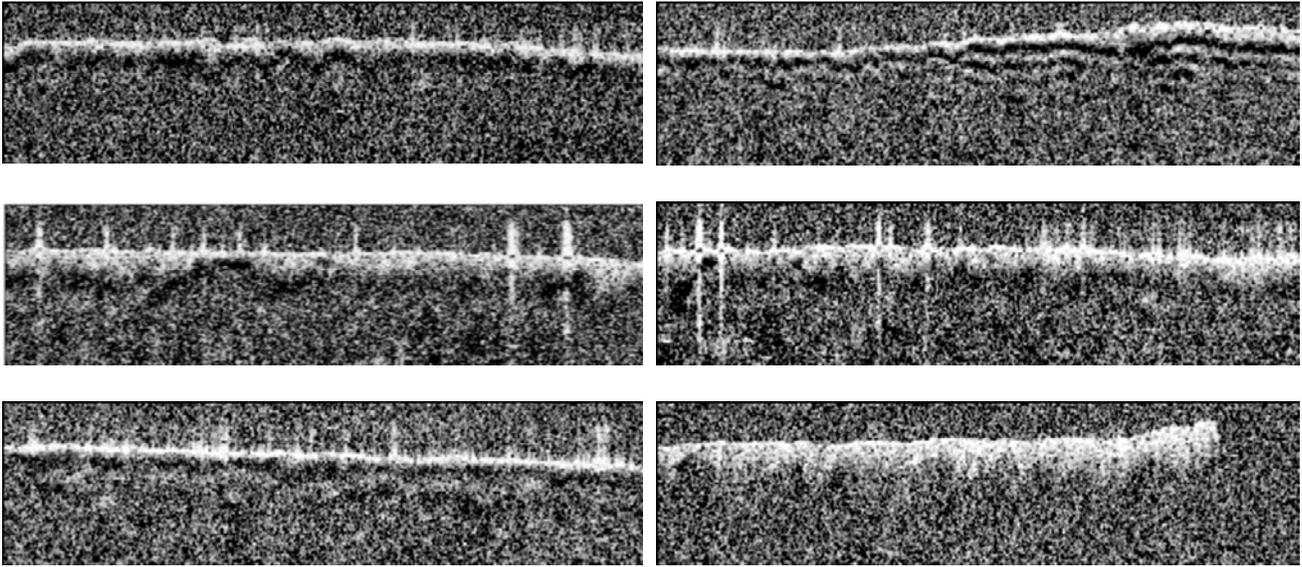


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### Retardance versus depth

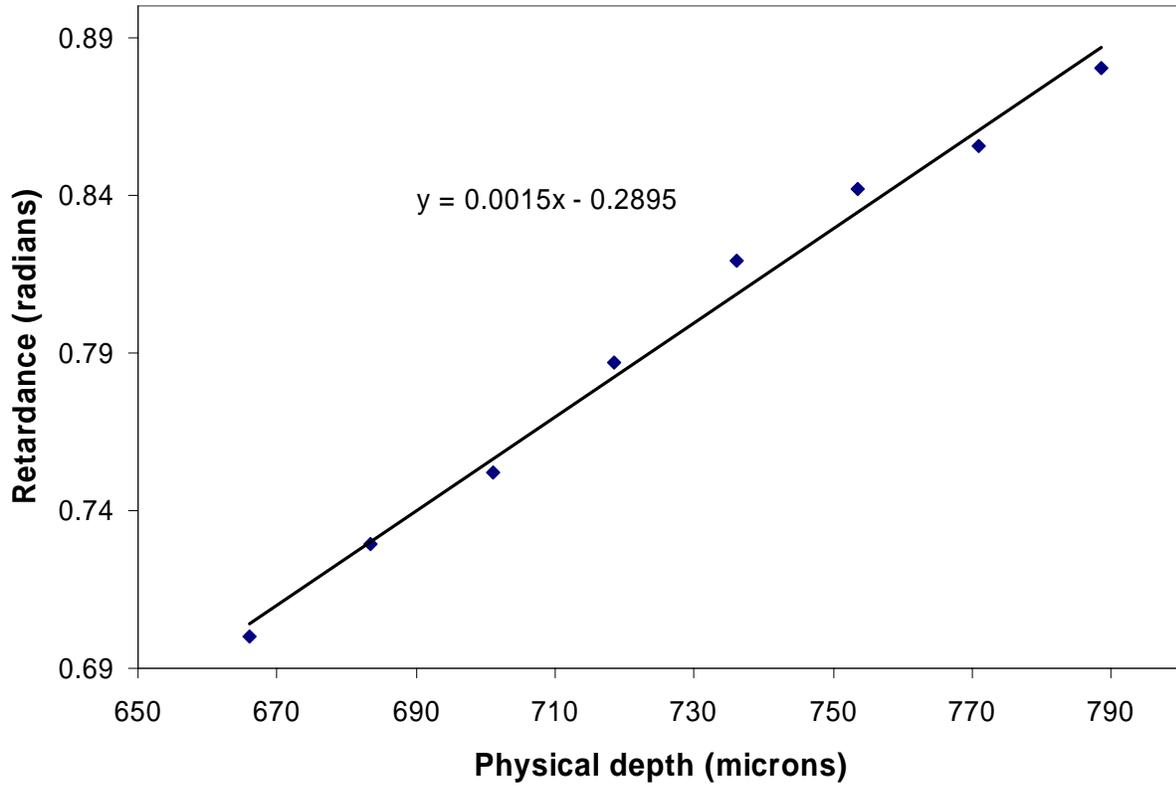


Figure 5. Illustrative curve of retardance versus physical depth extracted from the bottom-left image in Figure 4.

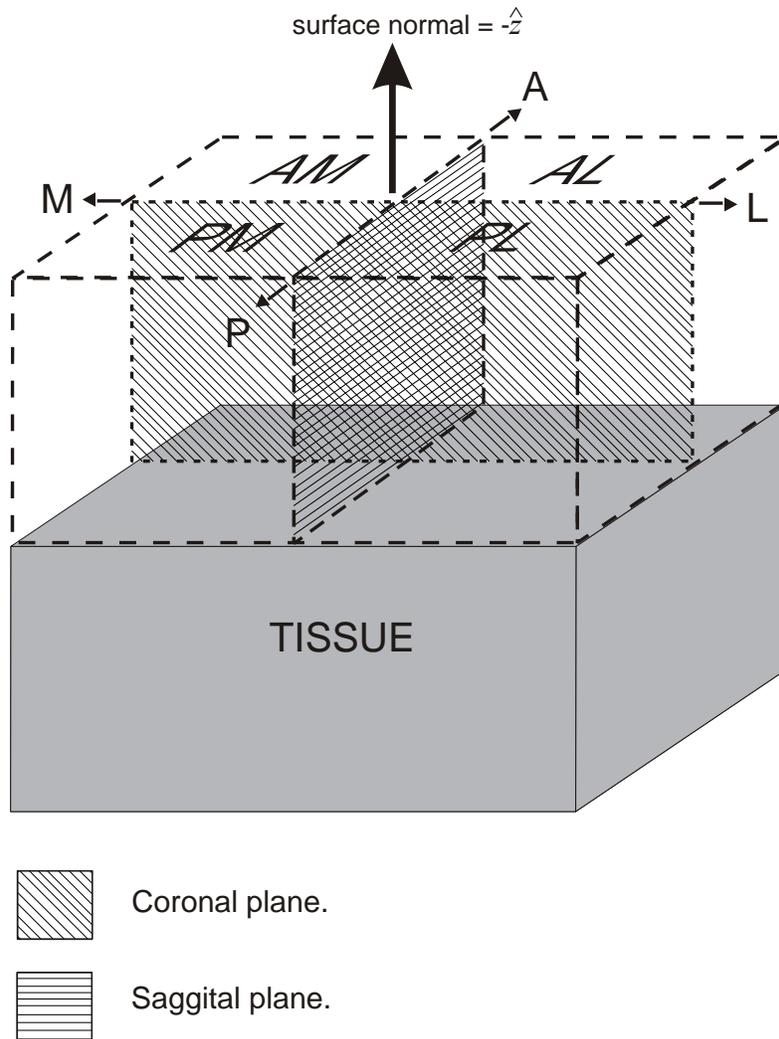


Figure 6. Illustrating the sagittal and coronal planes in relation to the tissue surface normal and also the anterior, posterior, lateral and medial directions (A, P, L, M respectively). These planes divide up the tissue into four octants AM, PM, AL, PL respectively, each of which represents a unique 3-D  $c$ -axis

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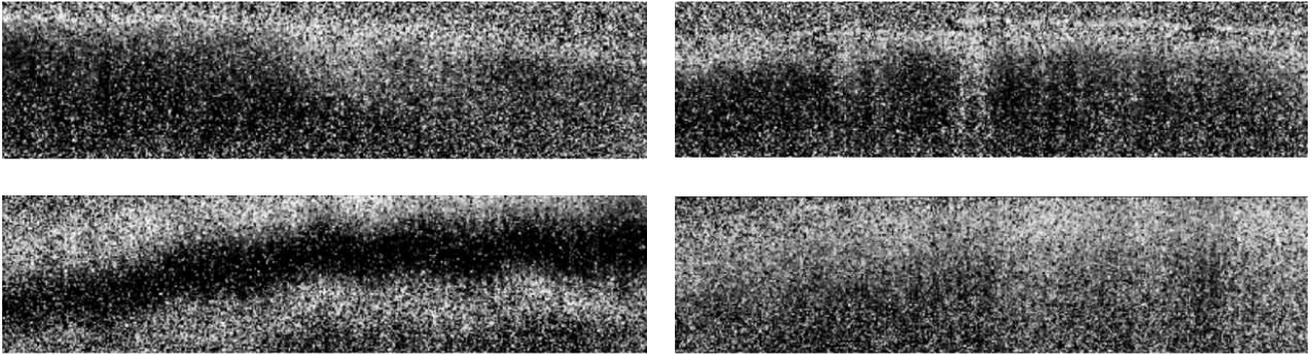


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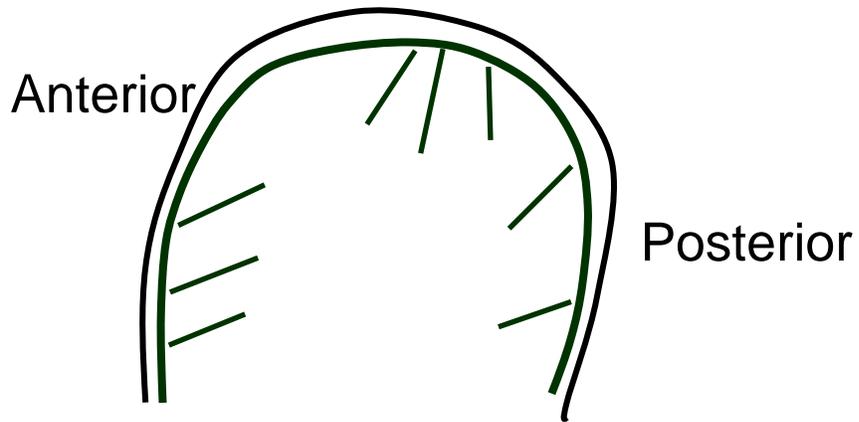


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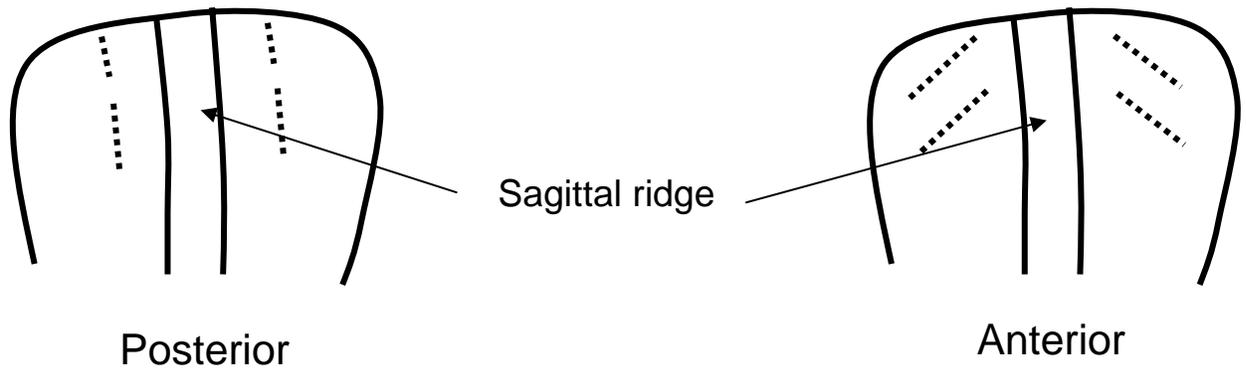


Figure 9. Schematic diagram of the apparent variation in azimuthal orientation of type-II collagen fibers of the equine fetlock joint on the posterior and anterior surfaces. Coronal view: the joint apex is at the top of each diagram.

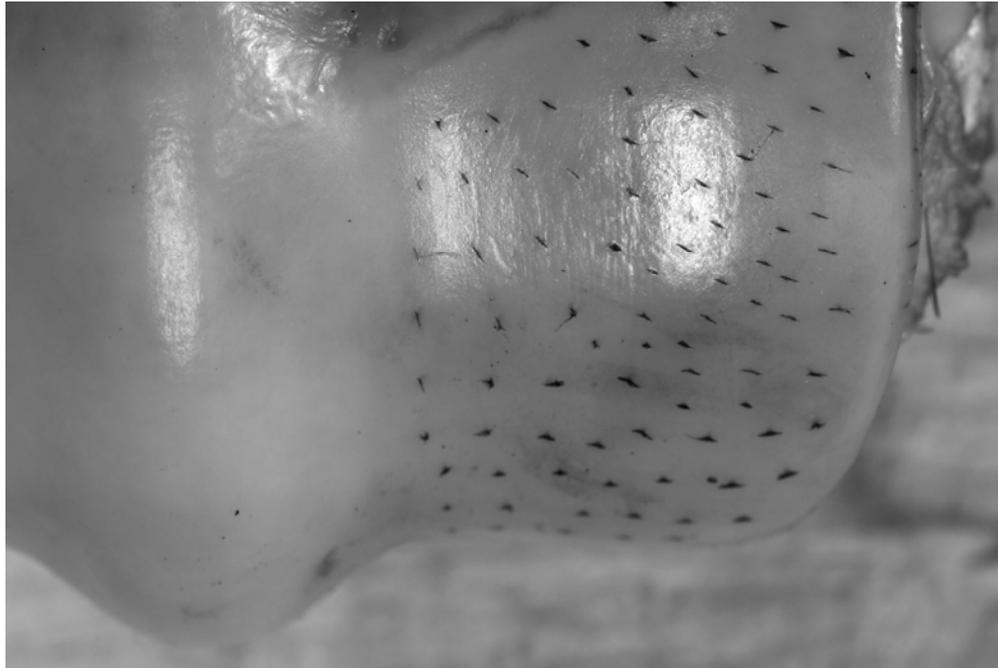


Figure 10. The anterior surface of a condyle after performing a split-line experiment. The apex is at the top of the photograph. The general fiber alignment suggested by destructive testing of the superficial layer is in qualitative agreement with the alignment suggested by non-destructive PS-OCT of the deeper layers.

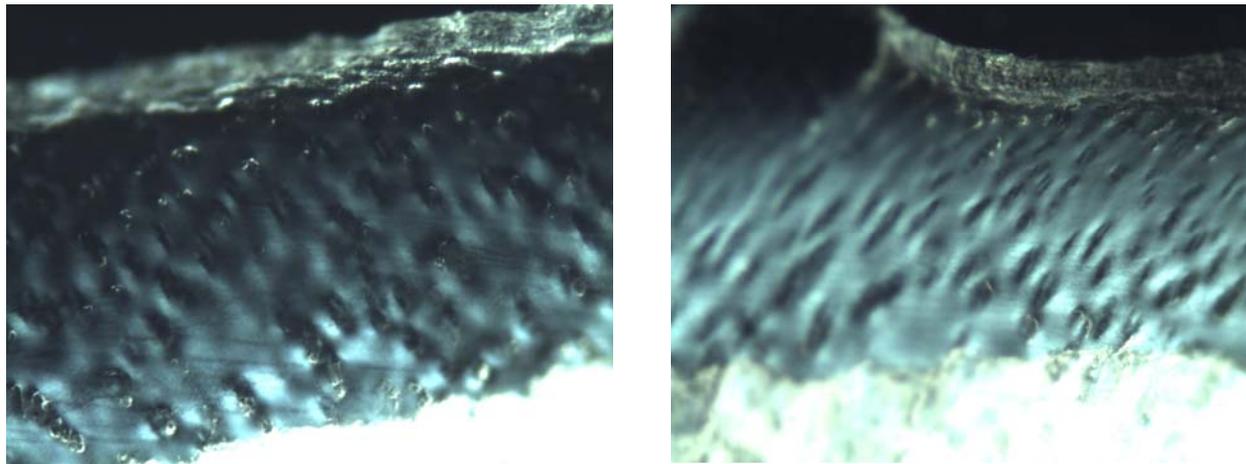


Figure 11. Polarized-light micrographs obtained from each end of a 1.5 cm coronal cartilage section. Clear differences in the directional alignment are evident over cm length scales, lending support to the indications from PS-OCT.

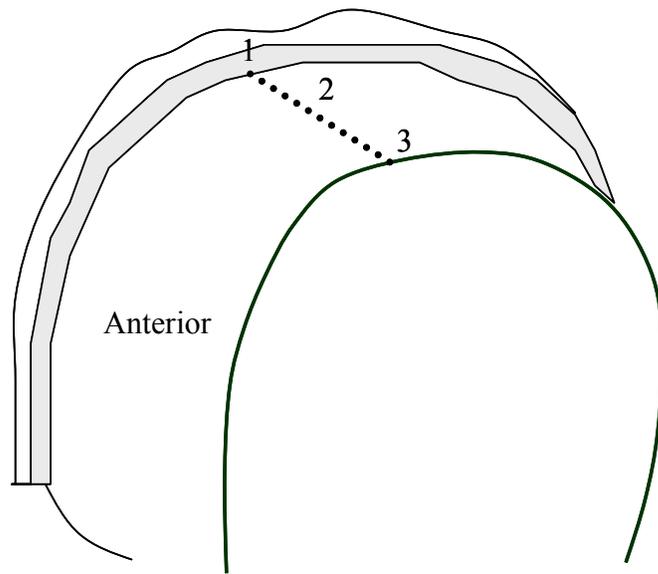


Figure 12. Schematic of the condyle (sagittal ridge in gray), with the three measurement sites on the anterior side of the apex labeled 1 to 3.

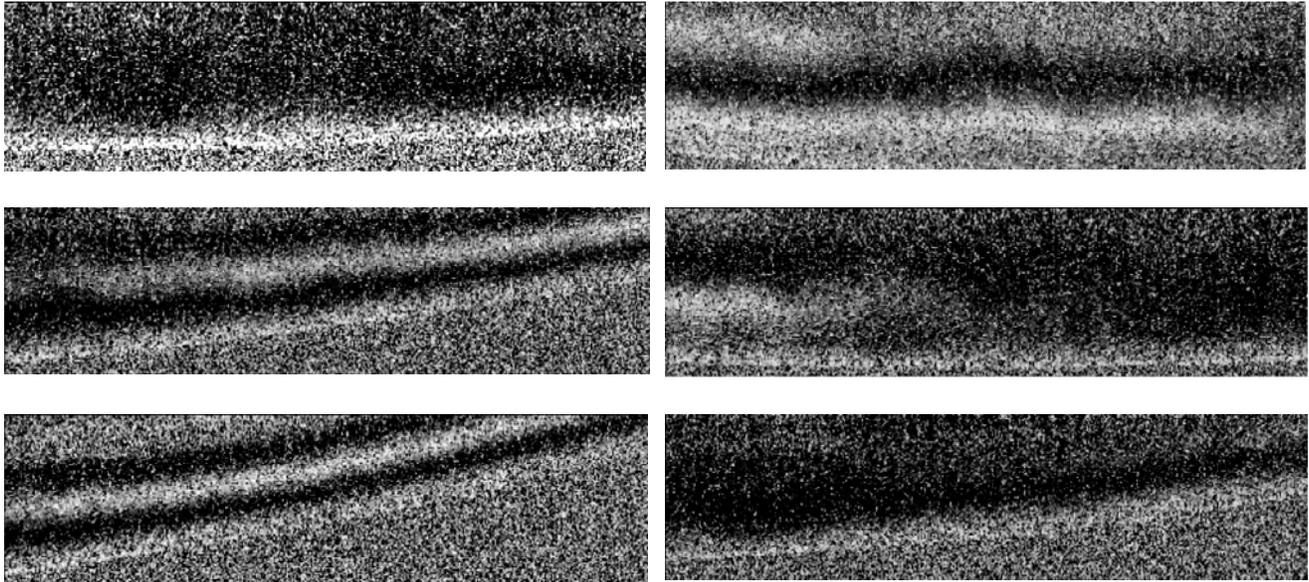


Figure 13. Retardance images obtained at the points 1-3 are shown in rows 1-3 respectively (the tissue surface is towards the bottom of the images). The left column is a 4×1 mm sagittal section image taken with the illumination beam inclined in the sagittal plane by an angle of 40° towards the posterior side of the joint (*i.e.* the beam travels from the posterior towards the anterior: defined as -40°) while the right column shows the corresponding image obtained with an equal and opposite positive angle of illumination *i.e.* inclination towards the anterior side.

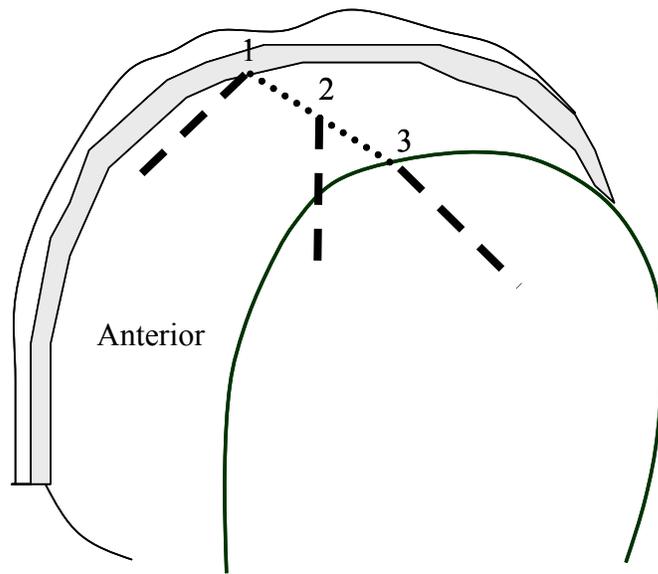


Figure 14. The dominant polar orientation of collagen fibers at the measurement sites 1-3, as suggested by the asymmetric retardance images shown in Figure 9. At point 1, nearest the sagittal ridge, the fibers are directed towards the anterior. This orientation changes to being directed towards the posterior at the point nearest the margin.

## **CONFLICT OF INTEREST STATEMENT**

The authors declare that there are no conflicts of interest affecting the publication of this manuscript.