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Bipolarity in Flexible Querying of Information Systems Dedicated to Multimodal Transport Networks

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Abstract—Flexible querying of information systems dedicated to multimodal transport networks aims to help user organizing his/her trips by promoting public transport networks (bus, subway, train, boat, plane, etc.). In this context, it is necessary to provide an integrated environment in which it is possible for the user to express queries with complex preferences so as to meet his/her expectations. Complex preferences are modeled by fuzzy bipolar conditions which associate negative and positive conditions. Queries involving such conditions are called bipolar queries. In our case, such queries are addressed to multimodal transport information systems, which are often made of several distributed and heterogeneous databases. Therefore, semantic aspects have to be taken into consideration in the querying process so that only the most relevant data is targeted to evaluate queries. We introduce then in this paper a new approach for flexible querying of information systems that combines a reasoning mechanism (fuzzy bipolar DLR-Lite) with a relational language of a high expressiveness (bipolar SQLf language).

Index Terms—Flexible querying, complex preferences, fuzzy bipolar conditions, bipolar SQLf, fuzzy sets theory, fuzzy description logics, multimodal transportation.

I. INTRODUCTION AND MOTIVATION

Multimodal transport information system is intended to provide information called multimodal transport information (denoted MTI) which is about various modes and available transport networks and services to help travelers to plan and to organize their trips [17]. It covers information about transport modes, timetables, pricing, traffic analysis, etc.

User oriented services are developed to promote public transport networks for the planning of user’s daily journeys. To fulfill user requirements, multimodal transport information systems must be endowed with powerful and complex functionalities. The issues of the heterogeneity and distribution of data in the transport field have also to be taken into consideration. Ontologies could be used to manage these aspects because they not only unify the domain vocabulary but they also provide reasoning mechanisms capable to extract implicit data from explicit one. Several ontologies have been developed for the multimodal transport domain (see [7], [11], [15], [16], [18]). The more complete one is Ontology Transportation Network (OTN) [14], which allows the modeling of multimodal transport networks from different points of view such as spatial, temporal, services, etc.

Flexible querying systems allow users expressing preferences in their queries. These queries are addressed to regular relational databases and deliver a set of discriminated answers, which are ranked from the most to the least preferred element. Within the scope of flexible querying, the fuzzy set theory provides a general model for the interpretation of queries involving fuzzy predicates. It is also possible to consider fuzzy bipolar conditions to model preferences. Several interpretations are introduced for the evaluation of queries involving fuzzy bipolar conditions (see [10], [9], [21], [23], [24]), and in this paper, we rely on the interpretation introduced by Dubois and Prade [10], [9], in which a bipolar condition is made of two components: a constraint that is a mandatory condition and a wish that is an optional condition. More precisely, for the expression of user preferences, we rely on fuzzy bipolar conditions in which the constraint and the wish are defined by fuzzy sets. We define then a bipolar query as a query that involves bipolar conditions. A bipolar relational algebra is also proposed in [13], [3] and the algebraic operators (selection, projection, join, union, intersection) have been extended to fuzzy bipolar conditions.

We introduce in this paper a flexible querying approach of distributed and heterogeneous information systems, such as those developed for multimodal trip planning systems, which allows users to express complex preferences in their queries. In this context, the system has to deal with a large amount of data while taking into account efficiency in terms of quality of answers. Two aspects have been considered: (i) the expressivity in terms of complex preferences and query language and (ii) the efficiency of the data management. Our approach is then based on the combination of the Bipolar SQLf language (which is an extension of the SQLf language [2], [1] to fuzzy bipolar conditions, suitable to express complex preferences) with a reasoning system, built on a fuzzy bipolar DLR-Lite knowledge base (which is also an extension of the fuzzy DLR-Lite [8], [19] to fuzzy bipolar conditions, used to target the most relevant subset of data to answer user queries).
The remainder of the paper is organized as follows. Section II reminds both fuzzy sets theory (which is the main model for fuzzy conditions) and the SQLf language (which is an extension of the SQL language to fuzzy conditions). In section III, fuzzy bipolar conditions and Bipolar SQL language are respectively described. Section IV recalls the fuzzy DLR-Lite and introduces our contribution which consists in the extension of the fuzzy DLR-Lite to fuzzy bipolar conditions and Bipolar SQLf language. In section V, the fuzzy bipolar DLR-Lite is used to develop a sample application in the field of multimodal transportation, in order to show the improvement that could be gained from integrating fuzzy bipolar conditions into both fuzzy DLR-Lite and SQLf language. Section VI summarizes our contribution and draws some lines for future works.

II. FLEXIBLE QUERYING WITHIN THE SQLf LANGUAGE

In this section, we briefly introduce fuzzy sets theory, used to define fuzzy predicates such as fast, high, large, expensive, ..., and the SQLf language which is an extension of the SQL language to fuzzy conditions.

A. Fuzzy Sets Theory

The fuzzy sets theory is introduced by Zadeh [22] to express the gradual membership of an element to a set. Formally, a fuzzy set $F$ is defined on a referential $U$ by a membership function $\mu_F : U \rightarrow [0,1]$ such that $\mu_F(x)$ denotes the membership grade of $x$ in $F$.

In particular, $\mu_F(x) = 1$ denotes the full membership of $x$ in $F$, $\mu_F(x) = 0$ expresses the absolute non-membership and when $0 < \mu_F(x) < 1$, it reflects a partial membership (the closer to 1 $\mu_F(x)$, the more $x$ belongs to $F$).

A fuzzy set generalizes a crisp set in which membership grades are in $[0,1]$. If a fuzzy set is a discrete set then it is denoted $F = \{\mu_F(x_1)/x_1 + ... + \mu_F(x_n)/x_n\}$, else it is characterized by its membership function, generally a trapezoidal function.

The union $\cup$ and the intersection $\cap$ operators are defined with a couple of (t-norm, t-conorm) such as (min, max). Let $F, G$ be two fuzzy sets, $\mu_{F\cap G}(x) = \min(\mu_F(x), \mu_G(x))$, $\mu_{F\cup G}(x) = \max(\mu_F(x), \mu_G(x))$, and the complement of $F$, noted $F^c$, is defined by $\mu_{F^c}(x) = 1 - \mu_F(x)$.

The logical counterparts of $\cap$, $\cup$ and the complement are $\land$, $\lor$ and $\neg$. Other operators have also been defined such as fuzzy implications [4]. We consider particularly $R$-implications, which are based on the residual principle:

$$I_R(a, b) = \sup\{z \in [0,1] : T(a, z) \leq b\},$$

where $I_R(a, b)$ means $a \rightarrow_R b$ and $T$ is a triangular norm.

$R$-implications satisfy properties of monotonicity, neutrality, exchange, identity and of ordering [4]. For example, the Gödel fuzzy implication is an $R$-implication which is defined by the formula (2), in which the used t-norm is $\min$:

$$I_{G\delta}(a, b) = \sup\{z \in [0,1] : \min(a, z) \leq b\},$$

where $I_{G\delta}(a, b) = 1$ if $a \leq b$, $b$ otherwise.

B. The SQLf Language

The SQLf language [2], [1] is an extension of the SQL language to flexible querying by extending its statements to fuzzy conditions. When querying a regular relation $R$ with such conditions, a fuzzy relation $r$ (fuzzy set) is delivered. Each tuple $t$ from $r$ is attached with a degree of membership that expresses its level of satisfaction. The closer to 1 $\mu_r(t)$, the more $t$ is preferred.

Example 1: Let fast be a fuzzy predicate as defined in Fig. 1. A fuzzy relation fastJourney can be defined from the relation Journey (#journey, source, destination, cost, duration) s.t. for each tuple $t$: $\mu_{\text{fastJourney}}(t) = \mu_{\text{fast}}(t).duration$. Table I is an example of extension of fastJourney.

<table>
<thead>
<tr>
<th>#Journey</th>
<th>cost ($)</th>
<th>duration (h)</th>
<th>$\mu_{\text{fastJourney}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>80</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>13</td>
<td>75</td>
<td>3</td>
<td>0.66</td>
</tr>
<tr>
<td>10</td>
<td>65</td>
<td>4</td>
<td>0.33</td>
</tr>
</tbody>
</table>

Syntactic elements of the SQLf language:

The main form of an SQLf query (fuzzy restriction) is:

```
Select [distinct] [n]t[n, t] attributes From relations Where fuzzy_cond;
```

The above query returns a set of ranked tuples with their degree of satisfaction, where $n$ is a limitation of the size of the returned set and $t \in [0, 1]$ is a minimal threshold of satisfaction.

Example 2: We consider a sample database which is consistent with the Transmodel standard [6]. It contains the following relations: Network, Line, Station, Link and LinkLine. We define Journey relation as Journey (#journey, #link, de-
parture, arrival, source, destination, cost, duration, DepLink, ArrLink, modeLink, waitLink, durLink, costLink, compLink).

For example, the query "find the 2 fastest journeys from Lannion to Paris" could be expressed in SQLf by:

\[
\text{Select 2 \textit{from Journey Where source='Lannion' and destination='Paris' and fast (duration);} \]

The fuzzy condition fast(duration) delivers the fuzzy relation FastJourney (see table 1) and the query returns the 2 best answers: journeys #12 and #13, attached respectively with the satisfaction degrees 1 and 0.66.

The SQLf language allows more complex statements such as partitioning, nesting and division involving fuzzy relations.

III. FLEXIBLE QUERYING WITHIN BIPOLAR SQLf LANGUAGE

In this section, we briefly introduce fuzzy bipolar conditions and Bipolar SQLf language which is an extension of the SQLf language to fuzzy bipolar conditions.

A. Fuzzy Bipolar Conditions

A bipolar condition is an association of both negative condition (pole) and positive condition (pole). In this paper, a bipolar condition is made of two conditions defined on the same universe: i) a constraint \( c \), which describes the set of acceptable elements, and ii) a wish \( w \) which defines the set of desired or wished elements. The negation of \( c \) is the set of rejected elements (non-acceptable elements). Since it is not coherent to wish a rejected element, the following property of coherence holds: \( w \subseteq c \).

In addition, condition \( c \) is mandatory since an element which does not satisfy \( c \) is rejected (\( \neg c \) is the negative condition), whereas \( w \) is optional because its non-satisfaction by an element does not mean its rejection (\( w \) is the positive condition). In this paper, a bipolar condition is noted \((c, w)\) and means: "satisfy \( c \) and if possible satisfy \( w \)" [10], [9].

If \( c \) and \( w \) are boolean conditions, the satisfaction with respect to \((c, w)\) is a couple from \([0, 1]^2\). When querying a database with such a condition, tuples satisfying the constraint and the wish are returned in priority. If such answers do not exist, the tuples satisfying only the constraint are delivered.

If \( c \) and \( w \) are fuzzy conditions (defined on the universe \( U \)), the property of coherence becomes: \( \forall u \in U, \mu_c(u) \leq \mu_c(u) \) and the satisfaction with respect to \((c, w)\) is a couple of degrees from \([0, 1]^2\). Each element \( u \) from \( U \) is then attached with a couple of grades \((\mu_c(u), \mu_w(u))\) that expresses the degree of its satisfaction respectively to the constraint \( c \) and the wish \( w \).

When querying a relation \( R \) with a fuzzy bipolar condition, each tuple \( t \) from \( R \) is then attached with a couple of grades \((\mu_c(t), \mu_w(t))\) that expresses the degree of its satisfaction respectively to the constraint \( c \) and the wish \( w \); and a so-called fuzzy bipolar relation is obtained. A tuple \( t \) is then denoted \((\mu_c(t), \mu_w(t))/t\). We assume that any tuple \( u \) such that \( \mu_c(u) = 0 \) does not belong to the fuzzy bipolar relation. In such a context, tuples cannot be ranked using an aggregation of \( \mu_c \) and \( \mu_w \) because the constraint and the wish are not commensurable. However, they can be ranked using the lexicographical order:

\[ t_1 \text{ is preferred to } t_2, \text{ denoted } t_1 \succ t_2, \text{ if and only if } \mu_c(t_1) > \mu_c(t_2) \text{ or } (\mu_c(t_1) = \mu_c(t_2) \land \mu_w(t_1) > \mu_w(t_2)). \]

In this case, the satisfaction with respect to the constraint is firstly used to discriminate among answers (the constraint being mandatory). The satisfaction with respect to the wish being optional, it can only be used to discriminate among answers having the same evaluation with respect to the constraint. A total order is then obtained on \( \mu_c \) and \( \mu_w \) (with \((1, 1)\) as the greatest element and \((0, 0)\) as the least element).

Based on the lexicographical order, the \( lmin \) and \( lmax \) operators [12], [3] are introduced in order to define the conjunction (resp. intersection) and the disjunction (resp. union) of bipolar conditions (resp. relations). They are defined as follows:

\[
\begin{align*}
((0, 1] \times [0, 1])^2 & \rightarrow [0, 1] \times [0, 1], \\
((\mu, \eta), (\mu', \eta')) & \rightarrow lmin((\mu, \eta), (\mu', \eta')) = \\
& \begin{cases} 
(\mu, \eta) & \text{if } \mu < \mu' \lor (\mu = \mu' \land \eta < \eta'), \\
(\mu', \eta') & \text{else.}
\end{cases}
\end{align*}
\]

\[
\begin{align*}
((0, 1] \times [0, 1])^2 & \rightarrow [0, 1] \times [0, 1], \\
((\mu, \eta), (\mu', \eta')) & \rightarrow lmax((\mu, \eta), (\mu', \eta')) = \\
& \begin{cases} 
(\mu, \eta) & \text{if } \mu > \mu' \lor (\mu = \mu' \land \eta > \eta'), \\
(\mu', \eta') & \text{else.}
\end{cases}
\end{align*}
\]

The \( lmin \) (resp. \( lmax \)) operator is commutative, associative, idempotent and monotonic. The couple of grades \((1, 1)\) is the neutral (resp. absorbing) element of the operator \( lmin \) (resp. \( lmax \)) and the couple \((0, 0)\) is the absorbing (resp. neutral) element of the operator \( lmin \) (resp. \( lmax \)).

Remark 1: Fuzzy bipolar conditions generalize fuzzy conditions since a fuzzy condition \( c \) can be rewritten \((c, c)\) to express "satisfy \( c \) and if possible satisfy \( c \)". So, a fuzzy relation \( R \) is a particular case of a fuzzy bipolar relation such that \( \forall t \in R, \mu_R(t) = \mu_c(t) = \mu_w(t) \). It has been proven [12], [3] that the \( lmin \) (resp. \( lmax \)) extends the t-norm \( min \) (resp. the t-co-norm \( max \)) to bipolarity.

B. Basis of Bipolar SQLf Language

Bipolar SQLf language is an extension to fuzzy bipolar conditions of the SQLf language. We introduce in this subsection the fuzzy bipolar extension proposed in [12], [3] of the relational algebraic operators (the union, the intersection, the cartesian product, the projection, the selection and the join) of fuzzy bipolar relations. This extension is based on the couple of the extended t-norm and t-co-norm \((lmin, lmax)\).

Let \( r \) and \( s \) be two fuzzy bipolar relations defined respectively by fuzzy bipolar conditions \((c_1, w_1)\) and \((c_2, w_2)\).

1) The intersection operator: The intersection of \( r \) and \( s \) is a fuzzy bipolar relation, in which each tuple \( t \) is attached with a couple of degrees \((\mu_c(t), \mu_w(t))\). It is defined as follows:

\[
r \cap s = \{(\mu_c, \mu_w)/t | (\mu_c, \mu_w)/t \in r \land (\mu_c, \mu_w)/t \in s \land \\
(\mu_c, \mu_w) = lmin((\mu_c(t), \mu_w(t))),(\mu_c(t), \mu_w(t)))\}.
\]
2) The union operator: The union of \( r \) and \( s \) is a fuzzy bipolar relation, in which each tuple \( t \) is attached with a couple of degrees \((\mu_c(t), \mu_w(t))\). It is defined as follows:

\[
r \cup s = \{(\mu_c(t), \mu_w(t))/t \in r \land (\mu_c(s), \mu_w(s))/t \in s\}
\]

3) The cartesian product operator: The cartesian product of \( r \) and \( s \) is a fuzzy bipolar relation, in which each tuple \( t \) is attached with a couple \((\mu_c(t), \mu_w(t))\). It is defined as follows:

\[
r \otimes s = \{(\mu_c(t), \mu_w(t))/t \otimes t'/((\mu_c(t'), \mu_w(t')))/t \in r \land (\mu_c(s), \mu_w(s))/t' \in s\}
\]

where \( \otimes \) is the operator of concatenation of tuples.

4) The projection operator: The projection of distinct tuples on attributes \( a_1, \ldots, a_k \) from \( r \) is a fuzzy bipolar relation of elements \( (a_1, \ldots, a_k) \), defined as follows:

\[
\pi_{a_1, \ldots, a_k}(r) = \{(\mu'_c, \mu'_w)/((a_1, \ldots, a_k) \subseteq (\mu'_c(t), \mu'_w(t)))\}
\]

where \( t(a_1, \ldots, a_k) \) is the value of the tuple \( t \) on \( a_1, \ldots, a_k \).

5) The selection operator: The selection of tuples from \( r \), based on the fuzzy bipolar condition \((\epsilon', w')\) is defined as:

\[
\sigma(r, (\epsilon', w')) = \{(\mu_c(t), \mu_w(t))/t \in r \land (\mu_c(t'), \mu_w(t'))=((\mu'_c(t), \mu'_w(t)))\}
\]

where \( \mu_c(t) \) (resp. \( \mu_w(t) \)) is the degree of satisfaction of \( t \) with respect to the constraint \( \epsilon' \) (resp. the wish \( w' \)).

6) The join operator: As in both boolean and fuzzy cases, the join operator is defined in the context of bipolarity by the combination of a cartesian product with a selection operator.

**Bipolar SQLf basic statements:**

A Bipolar SQLf basic statement is a fuzzy bipolar selection (restriction) of the following main format:

\[
\text{Select } [\text{distinct }] [n\{t_1, t_2]\} \text{[t_1, t_2]} \text{[attributes From relation as alias] Where fcond and if possible fcond}_2;
\]

The above statement is a simple selection of attributes from fuzzy bipolar relations based on the fuzzy bipolar condition \((\text{fcond}_2, \text{fcond}_2)_2\). It is also possible to express an \( n \)-top query by positioning the optional integer \( n \), which delivers the \( n \) best tuples. \((t_1, t_2) \subset [0, 1]^2\), such that \( t_2 \leq t_1 \), is a minimal threshold of satisfaction.

**Example 3:** We reuse the database defined in the example 2. The query "Find journeys which are fast and if possible not expensive", can be expressed in Bipolar SQLf as:

\[
\text{Select } \#\text{Journey From Journey as J Where fast(J.duration) and if possible notExpensive(J.cost)};
\]

Due to the coherence property of fuzzy bipolar conditions, the above bipolar query is interpreted as "Find journeys which are fast and if possible (fast and not expensive)".

We define, for example, the fuzzy predicate expensive as depicted in Fig. 2. Its negation is defined as follows:

\[
\forall x \in \mathbb{R}^+, \text{notExpensive}(x) = 1 - \text{Expensive}(x).
\]

![Fig. 2: The membership function of the fuzzy predicate expensive.](image)

**TABLE II: Fuzzy bipolar relation Journey(Fast, notExpensive)**

<table>
<thead>
<tr>
<th>#Journey</th>
<th>cost ($)</th>
<th>duration (h)</th>
<th>(\mu_{\text{Fast}})</th>
<th>(\mu_{\text{Fast} \text{Journey} \land \mu_{\text{notExpensive}}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>80</td>
<td>2</td>
<td>1</td>
<td>0.40</td>
</tr>
<tr>
<td>13</td>
<td>75</td>
<td>3</td>
<td>0.66</td>
<td>0.50</td>
</tr>
<tr>
<td>10</td>
<td>65</td>
<td>4</td>
<td>0.33</td>
<td>0.33</td>
</tr>
</tbody>
</table>

Based on the definition of fuzzy predicates fast and not expensive, the query is evaluated over the relational table Journey and delivers the fuzzy bipolar relation Journey(Fast, notExpensive).

Table II is an example of extension of Journey(Fast, notExpensive) and the delivered tuples are ranked, using the lexicographical order, from the best journey to the worst one, depending on their satisfactions to both the constraint fast and the wish not expensive: \((1, 0.40)/12, (0.66, 0.50)/13, (0.33, 0.33)/10\).

**IV. FUZZY BIPOLAR DLR-LITE**

In this section, we introduce the fuzzy DLR-Lite and our contribution which consists in its extension to bipolarity called fuzzy bipolar DLR-Lite.

**A. The Fuzzy DLR-Lite**

The flexible querying system developed in [8], [19] is based on a Description Logic extended to \( m \)-ary Relations, noted DLR-lite [5]. The knowledge base \( K \) of the fuzzy DLR-Lite consists of three components \((\mathcal{O}, \mathcal{F}, \mathcal{A})\) defined as follows:

1) The facts component \( \mathcal{F} \): It contains extensions of relations of the form \( R(c_1, \ldots, c_m)[s] \), where \( R \) is an \( m \)-ary relation, \( c_i=1, \ldots, m \) are constants and \( s \in [0, 1] \) is a degree of membership of tuple \( (c_1, \ldots, c_m) \) in the relation \( R \).

2) The ontology component \( \mathcal{O} \): The ontology defines the relevant abstract concepts of the application domain by means of projection and inclusion axioms:

a) The inclusion axiom: The inclusion axiom has the form \((R_i \sqcap R_j \sqcap \ldots \sqcap R_l) \subseteq R_s[s] \), where \( l \geq 1 \), \( R_{i, i=1, \ldots, l} \) are relations of the same arity and \( s \in [0, 1] \) is the truth value of the axiom. This axiom states that if \( c \) is an instance of \( R_{i, i=1, \ldots, l} \) to degree \( s_{i, i=1, \ldots, l} \) then \( c \) is an instance of \( R_s \) to degree at least \( s \otimes s_1 \otimes \ldots \otimes s_l \), where \( \otimes \) is a t-norm.

b) The projection axioms: They allow defining new concepts by extracting columns from other relations. Two kinds of projection axioms are defined: the simple projection and the restricted projection. The former is of the form \( \exists[i_1, \ldots, i_k] R \) that expresses the projection of the relation \( R \) on the columns \( i_1, \ldots, i_k \) and the latter is of the form \( \exists[i_1, \ldots, i_k] R. (\text{Cond}_1 \sqcap \ldots \sqcap \text{Cond}_k) \) which restricts the projection of \( \exists[i_1, \ldots, i_k] R \).
according to conditions $\text{Cond}_{i,t=1...h}$ of the form $([i] \theta v)$, where $\theta \in \{<,\leq,\neq,>,\geq\}$ and $v$ is a value.

3) The abstraction component A: It forms the set of statements which connect concepts and relations, defined in the ontology component, to physical relational tables from a database. Simple and complex abstraction statements are defined as follows:

a) Simple abstraction statement: It has the form $R_1 \longrightarrow R_2(c_1[t_1],...,c_k[t_k])|c_s|$ which states that the $k$-ary relation $R_1$ of the ontology component is mapped into the projection on columns $c_1$ of type $t_1$, $c_2$ of type $t_2$, and on $c_k$ of type $t_k$ of the $m$-ary table $R_2$. The score of these tuples is provided by the column $c_s$.

b) Complex abstraction statement: It has the form $R_1 \longrightarrow (t_1,...,t_k)|c_s|$.sgl, where $R_1$ is a $k$-ary relation of the ontology component and $sgl$ is an SQL query which returns the $k$-ary tuples $(t_1,...,t_k)$ ranked in decreasing order of scores provided by column $c_s$.

4) The query language: A query in a fuzzy DLR-Lite knowledge base querying system consists of a conjunctive query with a scoring function to rank between answers. The query has the following form:

$$g(x)[s] \leftarrow \exists y R_1(z_1)[s_1],...,R_l(z_l)[s_l], \text{OrderBy}(s = f(s_1,...,s_l)), (3)$$

where $q$ is an $m$-ary relation, every $R_i$ is either an $m_i$-ary relation or a concrete predicate of the form of $(\theta v)$, where $\theta \in \{<,\leq,\neq,>,\geq\}$ and $v$ is a value of a datatype, $x$ (resp. $y$) is a vector of distinguished (resp. non distinguished) variables, $z_i$ is a tuple of constants or variables in $x$ or $y$, $f$ is a scoring function which combines scores $s_1,...,s_l$ and $s$ is a degree of satisfaction of a tuple $x$ to the query $q$.

B. Extension of the Fuzzy DLR-Lite to Bipolarity

The bipolarity is integrated into the fuzzy DLR-Lite knowledge base in order to provide means to define and to handle fuzzy bipolar concepts and relations. For that purpose, we propose the extension of the fuzzy DLR-Lite to fuzzy bipolar concepts as described in what follows.

1) Extension of the facts component $\mathcal{F}$: Facts in our case are delivered from fuzzy bipolar relations. A fact has the following form: $R(c_1,...,c_n)|s,c,s_w|$, where $c_i=1,...,n$ are constants which form the tuple $u = (c_1,...,c_n)$, $R$ is a fuzzy bipolar relation defined by the fuzzy bipolar condition $(c,w)$ and $s_w$ is the grade of satisfaction of the tuple $u = (c_1,...,c_n)$ with respect to the constraint $c$ (resp. to the wish $w$). The consistency condition holds for each element $u$ ($s_w \leq s_c$) and every tuple $u$ s.t. $s_c(u) = 0$ is discarded.

2) Extension of the abstraction component A: Simple and complex abstraction rules are both extended to fuzzy bipolar conditions as follows:

a) The simple abstraction rule: It has the form $R_1 \longrightarrow R_2(c_1,...,c_n)|s,c,s_w|$, where $R_1$ is a relation or concept (in the sense of the fuzzy DLR-Lite); $R_2$ is an $m$-ary fuzzy bipolar relation from a database, $c_1,...,c_n$, with $n \leq m$, are columns from $R_2$ and $(s_c,s_w)$ is the couple of grades of satisfaction attached to the tuple $(c_1,...,c_n)$ with respect to the fuzzy bipolar condition $(c,w)$ which is used to define $R_2$.

b) The complex abstraction rule: It has the form $R_1 \longrightarrow (c_1,...,c_n)|s,c,s_w|$.sglfb, where sglfb is a Bipolar SQL query which delivers $n$-ary tuples $(c_1,...,c_n)$ with their corresponding couples of grades $(s_c,s_w)$.

3) Extension of the ontology component $\mathcal{O}$: The ontology component defines intersection axioms ($\cap$), simple and conditional projection axioms and subsumption (inclusion) axioms ($\subseteq$). They are extended to bipolarity as follows:

a) The intersection axiom: It is denoted $R_1 \cap R_2$, where $R_1$ and $R_2$ are fuzzy bipolar relations defined resp. by fuzzy bipolar conditions $(c_1,w_1)$ and $(c_2,w_2)$. It is interpreted as a fuzzy bipolar relation $R$ in which each tuple $u$ is attached with a couple of degrees $(s_c(u),s_w(u))$, defined as follows:

$$\forall u, (s_c(u),s_w(u)) = \min((\mu_c(u),\mu_{w_1}(u)),(\mu_{c_2}(u),\mu_{w_2}(u))) \quad (4)$$

b) The simple projection axiom: It is denoted $\exists [i_1,...,i_k]R$. It corresponds to the projection of columns $i_1,...,i_k$ from the fuzzy bipolar relation $R$ of arity $n$ such that $n \geq k$. This projection extracts new facts from a database or from facts already defined in $\mathcal{F}$.

This rule is interpreted as a bipolar projection of distinct elements of fields $i_1,...,i_k$ from the fuzzy bipolar relation $R$ defined by the fuzzy bipolar condition $(c,w)$. This axiom delivers a fuzzy bipolar relation made of the projected columns and its interpretation attaches a couple of grades for each retrieved tuples $u = (i_1,...,i_k)$ as follows:

$$\forall u, (\exists [i_1,...,i_k]R)(u)^2 = (s_c(u),s_w(u)) = \max_{i \in R \cap [i_1,...,i_k]} ((\mu_c(t),\mu_{w_1}(t))) \quad (5)$$

c) The restricted projection axiom: It is denoted $\exists [i_1,...,i_k]R.(\text{Cond}_1 \cap ... \cap \text{Cond}_k)$, where $\text{Cond}_{i=1...h} = ([i] \theta v)$ are conditions of selection of fields with $\theta \in \{<,\leq,\neq,>,\geq\}$, $[i]$ is a column number corresponding to a field from the fuzzy bipolar relation $R$, defined by the fuzzy bipolar condition $(c,w)$.

This rule corresponds to a combination of a bipolar projection and a bipolar selection of distinct tuples from $R$. It delivers a fuzzy bipolar relation formed by the retrieved tuples $u = (i_1,...,i_k)$. The attached couples of grades are defined by the formula (5) applied on the retrieved tuples limited to those satisfying the boolean condition $\text{Cond} = (\text{Cond}_1 \cap ... \cap \text{Cond}_k)$.

$$\forall u, (\exists [i_1,...,i_k]R.(\text{Cond}_1 \cap ... \cap \text{Cond}_k))(u)^2 = (s_c(u),s_w(u)) = \max_{j \in R \cap [i_1,...,i_k]} ((\mu_c(t),\mu_{w_j}(t))) \quad (6)$$
d) The subsumption (inclusion) axiom: This axiom is denoted \((R_l \subseteq R_r)[n_1, n_2]\), where \(R_l\) and \(R_r\) are fuzzy bipolar concepts (relations) of the same arity defined respectively by fuzzy bipolar conditions \((c_l, w_l)\) and \((c_r, w_r)\).

The interpretation of this axiom is based on the strengthened membership-based interpretation of fuzzy bipolar conditions. Let \(R\) be a fuzzy bipolar relation defined by a fuzzy bipolar condition \((c, w)\). \(R\) is seen as a particular fuzzy set of desired elements such that each element \(u\) holds two grades:

- \(\mu_u(c)\) is a basic grade of membership to the fuzzy set,
- \(\mu_u(w)\) is a strengthening grade of membership that make distinguishable tuples having the same basic grade. In other terms, for tuples having the same basic grade, more a tuple satisfies the wish more it belongs to the fuzzy set.

In this context, it becomes possible to extend the interpretation of the inclusion axiom to bipolarity as follows:

\[
((R_l \subseteq R_r)[n_1, n_2])^T \iff \forall x \in R_l, lmin((\mu_{c_l}(x), \mu_{w_l}(x)), (n_1, n_2)) \leq_{lex} (\mu_{c_r}(x), \mu_{w_r}(x))
\]  

(7)

where \(\leq_{lex}\) is the operator s.t. \((a, b) \leq_{lex} (a', b') \iff lmin((a, b), (a', b')) = (a, b)\). The couple of degrees \((n_1, n_2)\) is interpreted as the minimal threshold of inclusion of \(R_l\) in \(R_r\), and it processed by the following formula:

\[
((R_l \subseteq R_r)[n_1, n_2])^T \iff lmin_{x \in R_l}(((x \in R_l) \land (x \in R_r))^T) = (n_1, n_2)
\]  

(8)

The formula (8) is the extension to fuzzy bipolar conditions of the formula (9), which is introduced in [20] to compute the truth value of inclusion axioms in the case of fuzzy DLR-Lite.

\[
((R_l \subseteq R_r)[n])^T \iff min_x(R_l(x) \land_{Göd} R_r(x)) = n,
\]  

(9)

where \(\land_{Göd}\) is the Gödel fuzzy implication.

The formula \((if \ x \in R_l \then x \in R_r)^T\) defines a kind of implication for bipolar elements. We propose the extension of the formula (2) to bipolarity to define an extended bipolar \(R\)-implication operator. The formula (10) is, then, proposed:

\[
Ir((a_c, a_w), (b_c', b_w')) = lmax\{((z, z') : z' \leq z \land lmin((a_c, a_w), (z, z')) \leq_{lex} (b_c', b_w'))\}
\]  

(10)

Finally, we obtain the following interpretation for \((if \ (x \in R_l) \then (x \in R_r))^T\) in the bipolar context:

\[
(if \ (x \in R_l) \then (x \in R_r))^T = \begin{cases} 
(1, 1) & if (\mu_{c_r}(x), \mu_{w_r}(x)) \leq_{lex} (\mu_{c_l}(x), \mu_{w_l}(x)), \\
(\mu_{c_r}(x), \mu_{w_r}(x)), & else.
\end{cases}
\]  

(11)

It is easy to prove that formula (11) verifies properties of \(R\)-implications extended to bipolarity (monotonicity, neutrality, exchange, identity and ordering).

It is also easy to show that formula (11) is compatible with formula (10) and it defines an extension of the Gödel fuzzy implication to fuzzy bipolar conditions. Indeed, in the formula (10), when \((a_c, a_w) = (b_c, b_w)\), any valid couple of degrees \((z, z')\) from \([0, 1]^2\) satisfies \(lmin((a_c, a_w), (z, z')) = lmax((a_c, a_w), (z, z'))\) and the greatest couple of degrees is \((1, 1)\).

When \((a_c, a_w) > (b_c, b_w)\), couples of degrees which satisfy \(lmax((a_c, a_w), (z, z')) = (b_c, b_w)\) are \((z, z')\) such that \((z, z') \leq (b_c, b_w)\); then, the greatest couple of degrees \((z, z')\) corresponds to \((b_c, b_w)\).

4) Extension of the query language to bipolarity: A query addressed to a fuzzy bipolar DLR-Lite knowledge base consists in a conjunctive query which is extended to bipolarity. The main form of such queries is:

\[
q(x)[s_c, s_w] \leftarrow \exists y(R_1(z_1)[s_{c1}, s_{w1}], ..., R_l(z_l)[s_{cl}, s_{wl}]).
\]

(11)

\[
\text{OrderBy}((s_c, s_w) = f((s_{c1}, s_{w1}), ..., (s_{cl}, s_{wl}))).
\]

(12)

Syntactically, couples of the form \([1, 1]\) could be omitted.

V. FUSY BIPOLAR DLR-LITE APPROACH FOR FLEXIBLE QUERYING: A SAMPLE APPLICATION

We show the relevance of the fuzzy bipolar DLR-Lite based approach through the design and the querying of a sample application in the field of multimodal transportation networks.

The relational database previously introduced in the example 2 is reused. For each table from the database, a relation is defined in the ontology component and an abstraction statement is associated to it in the abstraction component. In addition, we define the following relations in the ontology:

\[
\text{Step} \equiv \exists[2, 3, 4, 5, 6] \text{Journey} \ \text{is a simple projection of Journey relation on columns \#link, source, destination, departure and arrival.}
\]

\[
\text{AreaStation} \equiv \exists[1, 2, 3, 4] \text{Station} \ \text{defines stations such as railway station and airport. It is a simple projection of Station relation on columns \#station, designation, city and type.}
\]

Let RailwayStation, noted RailStation, and Airport be two concepts, extracted from the AreaStation by the following restricted projection axioms:

- \(\text{RailStation} \equiv \exists[1] \text{AreaStation}(([3] = "\text{Railway}"))\)
- \(\text{Airport} \equiv \exists[1] \text{AreaStation}(([3] = "\text{Airport}"))\)

Let PreferredRailStation be a fuzzy bipolar concept defined by the fuzzy bipolar condition \((\text{Large}, \text{NearCenter})\) that corresponds to railway stations which are large and if possible (large \(\land\) located near to the town center). This concept could be expressed by the following abstraction rule:

\[
\text{PreferredRailStation} \rightarrow (\text{#station}).\text{Select} \ #station \ \text{From RailStation Where LargeRail(#station) and if possible NearCenter(#station)};
\]

where LargeRail (resp. NearCenter) is the membership function of the fuzzy predicate LargeStation (resp. near
TABLE III: Examples of relations from the facts component.

(a) PreferredRailStation relation.

<table>
<thead>
<tr>
<th>#station</th>
<th>designation</th>
<th>μ_Large</th>
<th>μ_Large ∧ μ_NearCenter</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>RailStation1</td>
<td>0.5</td>
<td>0.4</td>
</tr>
<tr>
<td>2</td>
<td>RailStation2</td>
<td>1</td>
<td>0.7</td>
</tr>
<tr>
<td>3</td>
<td>RailStation3</td>
<td>0.6</td>
<td>0.5</td>
</tr>
</tbody>
</table>

(b) PreferredAirport relation.

<table>
<thead>
<tr>
<th>#airport</th>
<th>designation</th>
<th>μ_Large</th>
<th>μ_Large ∧ μ_NearCenter</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>Airport1</td>
<td>1</td>
<td>0.8</td>
</tr>
<tr>
<td>11</td>
<td>Airport2</td>
<td>0.5</td>
<td>0.3</td>
</tr>
<tr>
<td>12</td>
<td>Airport3</td>
<td>0.4</td>
<td>0.4</td>
</tr>
</tbody>
</table>

TABLE IV: hasPreferredRestaurant relation.

<table>
<thead>
<tr>
<th>#place</th>
<th>designation</th>
<th>μ_Good</th>
<th>μ_Good ∧ μ_Cheap</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>RailStation1</td>
<td>0.6</td>
<td>0.6</td>
</tr>
<tr>
<td>102</td>
<td>RailStation2</td>
<td>0.8</td>
<td>0.7</td>
</tr>
<tr>
<td>103</td>
<td>RailStation3</td>
<td>0.8</td>
<td>0.3</td>
</tr>
<tr>
<td>104</td>
<td>Airport1</td>
<td>0.7</td>
<td>0.6</td>
</tr>
<tr>
<td>105</td>
<td>Airport2</td>
<td>0.5</td>
<td>0.4</td>
</tr>
<tr>
<td>106</td>
<td>Airport3</td>
<td>0.5</td>
<td>0.3</td>
</tr>
<tr>
<td>107</td>
<td>ShoppingCentre1</td>
<td>0.6</td>
<td>0.25</td>
</tr>
<tr>
<td>108</td>
<td>Hotel1</td>
<td>0.4</td>
<td>0.3</td>
</tr>
</tbody>
</table>

to the town center). Similarly, let PreferredAirport be a fuzzy bipolar concept defined by the fuzzy bipolar condition (Large, NearCenter) that corresponds to airports which are large and if possible (large ∧ not located far from the town center). Tables IIIa and IIIb displays examples of facts attached respectively to these concepts.

We can enrich the system with data from web services or other information systems. For example, we query a web service about restaurants, from which we define the fuzzy bipolar relation hasPreferredRestaurant, which corresponds to places which have good and if possible cheap restaurants as railway stations, hotels, airports, shopping centers (see table IV). Instead of saving the table IV on the facts component, we focus only on data related to our transport system. For efficiency reason, we represent them as data summary using the two following bipolar inclusion axioms:

\[(\text{PreferredRailStation} ⊆ \exists [1]\text{hasPreferredRestaurant})[n_1, n_2] \]
\[(\text{PreferredAirport} ⊆ \exists [1]\text{hasPreferredRestaurant})[n_3, n_4] \]

where \((n_1, n_2)\) (resp. \((n_3, n_4)\)) is the minimal couple of degrees of inclusion of PreferredRailStation (resp. PreferredAirport) in the set of hasPreferredRestaurant. These couples of degrees are processed based on formulas (7), (8) and (11):

\[(n_1, n_2) = \operatorname{lmin}(0.5, 0.4) \rightarrow (0.6, 0.6), \]
\[(1.0, 0.7) \rightarrow (0.8, 0.7), (0.6, 0.5) \rightarrow (0.8, 0.3)) \]
\[= \operatorname{lmin}(1.1), (0.8, 0.7), (1.1)) = (0.8, 0.7).
\[(n_3, n_4) = \operatorname{lmin}(1.0, 0.8) \rightarrow (0.7, 0.6), \]
\[(0.5, 0.3) \rightarrow (0.5, 0.4), (0.4, 0.4) \rightarrow (0.5, 0.3)) \]
\[= \operatorname{lmin}(0.7, 0.6), (1.1), (1.1)) = (0.7, 0.6).

Even if we have no restaurant relation in the facts component and without querying any external database, the system can answer queries about journeys which involve preferred restaurants, such as “go from Lannion to Paris in 2 steps with a preferred restaurant at the midway”, which is expressed by:

\[q(x_1, x_2)[s_c, s_w] \leftarrow \exists a, b, c, d, e, f, g, h, i.
\]
\[\text{AreaStation}(a, e, ”Lannion”), \text{Step}(x_1, a, c, d, g), \]
\[\text{Step}(x_2, c, b, d, h), \text{AreaStation}(b, f, ”Paris”), \]
\[\text{hasPreferredRestaurant}(c, i)[s_c, s_w], \]
\[\text{OrderBy}((s_c, s_w) = (s_{c_1}, s_{w_1})), \]

To evaluate this query, the atom hasPreferredRestaurant is substituted by the left-hand side of each inclusion axiom in which it appears in its right-hand side. Each substitution generates a new query. Two subqueries are, then, obtained:

\[q_1(x_1, x_2)[s_c, s_w] \leftarrow \exists a, b, c, d, e, f, g, h.
\]
\[\text{AreaStation}(a, e, ”Lannion”), \text{Step}(x_1, a, c, d, g), \]
\[\text{Step}(x_2, c, b, d, h), \text{AreaStation}(b, f, ”Paris”), \]
\[\text{PreferredRailStation}(c)[s_c, s_w], \]
\[\text{OrderBy}((s_c, s_w) = \operatorname{lmin}(s_1, s_2), (0.8, 0.7))).
\]
\[q_2(x_1, x_2)[s_c, s_w] \leftarrow \exists a, b, c, d, e, f, g, h.
\]
\[\text{AreaStation}(a, e, ”Lannion”), \text{Step}(x_1, a, c, d, g), \]
\[\text{Step}(x_2, c, b, d, h), \text{AreaStation}(b, f, ”Paris”), \]
\[\text{PreferredAirport}(c)[s_c, s_w], \]
\[\text{OrderBy}((s_c, s_w) = \operatorname{lmin}(s_3, s_4), (0.7, 0.6))).
\]

The scoring function in both \(q_1\) and \(q_2\) takes into consideration the inclusion axiom used in the substitution process. Both \(q_1\) and \(q_2\) are to be translated into Bipolar SQLf queries, in order to be evaluated over the facts component.

For example, query \(q_1(x_1, x_2)\) is expressed as follows:

Select R1.#step, R2.#step From Step as R1, Step as R2 Where R1.destination = R2.source and R1.source in (Select #station From Station Where city = 'Lannion') and R2.destination in (Select #station From Station Where city = 'Paris') and R2.Source in (Select #station From PreferredRailStation);

The answers are ranked depending on couples of degrees delivered by \(\operatorname{lmin}((s_1, s_2), (0.8, 0.7)), where (s_1, s_2)\) is the couple of degrees attached to each R2.Station corresponding to a preferred rail station. The query \(q_2(x_1, x_2)\) is similarly processed and the obtained sets of answers are merged, while respecting the lexicographical order.

The Main Architecture of the System:

For implementation purpose, we propose a software architecture which consists of a combination of a reasoning system (based on the fuzzy bipolar DLR-Lite) and a flexible information system (based on Bipolar SQLf).

As depicted in Fig. 3, the system is of two parts. The left side consists of the following modules:

\(a\) Query interpreter: It provides the user with interface that receives queries and returns answers.
b) Bipolar SQLf generator: It performs user queries transformation (relevant substitutions based on the inclusion axioms) using the fuzzy bipolar DLR-Lite knowledge base and generates equivalents bipolar SQLf queries to be evaluated by the right side of the system.

c) Fuzzy bipolar DLR-Lite knowledge base: it defines the knowledge base of the system (relations, facts, axioms).

The right side deals with the mediation issues for the combination of data fetched from remote databases, and processes bipolar SQLf queries received from the bipolar SQLf generator. It is composed by the following modules:

d) Mediation: It evaluates the received bipolar SQLf queries by retrieving the needed data from relevant remote databases, and by translating queries using the right vocabulary in compliance with a domain ontology (taxonomy).

e) Taxonomy: It is based on the Ontology Transportation Networks (OTN). Depending on the remote information system to query, this module provides the Mediation module with the right vocabulary to use in the query translation process.

VI. CONCLUSION AND FUTURE WORKS

To be able to express complex preferences in user queries, addressed to distributed and heterogeneous information systems, we have proposed a new flexible querying approach in which the fuzzy DLR-Lite is extended to both fuzzy bipolar conditions and Bipolar SQLf language.

We showed through an application the relevance of this approach in the field of the multimodal transportation networks. The bipolar fuzzy DLR-Lite can go beyond relational tables by inferring implicit knowledge and by summarizing data, while improving widely the expressiveness of the system. So, it becomes possible to express complex preferences of the form "c and if possible w" and to handle them within a reasoning system to answer user queries.

A software architecture for such a querying system has also been proposed. The common formal framework (fuzzy sets theory) of both Bipolar SQLf language and fuzzy bipolar DLR-Lite allows their combination in a consistent way.

An implementation of the system is in progress. It is based on algorithms for query evaluation which are introduced in [19]. As future works, we plan the study of performances of our approach in terms of response time and quality of answers, i.e. in which extent answers meet user expectations.

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