Title:

An Underlay for Sensor Networks: Localized Protocols for Maintenance and Usage

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We propose localized and decentralized protocols to construct and maintain an *underlay* for sensor networks. An underlay lies in between overlay operations (e.g., data indexing, multicast, etc.) and the sensor network itself. Specifically, an underlay bridges the gap between (a) the unreliability of sensor nodes and communication and availability of only approximate location knowledge, and (b) the maintenance of a virtual geography-based naming structure that is required by several overlay operations. Our underlay creates a coarse naming scheme based on approximate location knowledge, and then maintains it in an efficient and scalable manner. The underlay naming can be used to specify arbitrary regions. The overlay operations that can be executed on the underlay include routing, aggregation, multicast, data indexing, etc. These overlay operations could be region-based. The proposed underlay maintenance protocols are robust, localized (hence scalable), energy and message efficient, have low convergence times, and provide tuning knobs to trade convergence time with overhead and with underlay uniformity. The maintenance protocols are mathematically analyzed by characterizing them as differential equation systems. We present microbenchmark results from a NesC implementation, and results from a largescale simulation of a Java implementation. The latter experiments also show how routing using the underlay would perform.

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1 Introduction

Wireless Sensor networking (henceforth simply *sensor networks*) applications in the future are likely to be supported by networking substrates. These substrates will provide services such as multicast, routing, data indexing (e.g., GHT [2], DIM [1]), aggregation [3]), etc. These protocols can be termed as *overlay* protocols, since they are all operations executed on the scale of the entire system (or parts of it) rather than at the level of individual sensor nodes [7] ¹. The main requirements from these overlay services are reliability, scalability, and energy-efficiency.

However, bridging the gap between the requirements of overlays on the one hand, and the inherent unreliability of sensor nodes and communication, as well availability of only approximate location knowledge (e.g., from GPS or localization algorithms) on the other hand, remains a challenge. For example, overlays for multidimensional range querying such as DIM and GHT [1, 2] require the network to be organized into a hierarchical structure (not necessarily just a spanning tree). Maintaining such a hierarchical structure that *underlies* the overlays has remained a difficult problem. Also, specifying arbitrary regions in the sensor network, and executing overlay operations on them (e.g., multicast, routing) requires a coarse naming scheme for the network that is only based on approximate location knowledge of sensor nodes.

¹This terminology is analogous to Internetwork-based overlays such as RON [4] and peer to peer systems.

In this paper, we propose protocols to maintain an **underlay** scheme that can be used to bridge the above-mentioned gap, while not compromising the reliability, scalability and energy-efficiency that the overlay operations seek to provide to the application. The underlay is called the Grid Box Hierarchy (GBH), and although the structure was proposed in [5], creation and maintenance of the underlay is an entirely different problem that was not addressed.

In the GBH hierarchy, sensor nodes are located only at the leaves, while the internal nodes of the hierarchy correspond to virtual aggregated grid boxes (and not to individual sensor nodes). The naming of these grid boxes and regions is based only on approximate location knowledge ². GBH allows us to (a) specify arbitrary regions, either geographically or as collections of sensor nodes, in terms of these virtual grid boxes, and (b) support a variety of overlay operations including (but not restricted to) aggregation, data indexing, multicast, and routing, either across the system or within regions.

In this paper, we focus on protocols for maintaining the GBH underlay, and evaluate their impact for a region-based routing protocol and a region-based multicast protocol. Aggregation using GBH was the focus of [5]. Supporting indexing schemes such as GHT and DIM over the GBH underlay is simple, and an evaluation is omitted due to space constraints.

The underlay maintenance protocols are localized and decentralized (i.e., do not rely on the election of leaders or cluster-heads). Our analysis and experimental results show that the protocol is robust, resilient, scalable and converges quickly to a stable state. In spite of events that may perturb the system (e.g., failures), the protocol continues to converge back to the stable state. Further, the protocol offers tuning parameters that can be adjusted so that metrics such as energy efficiency and speed of convergence can be traded off as per application requirements.

The paper is organized as follows. Section 2 gives an overview of the GBH and the overview of our protocols. Section 3 presents two protocols to construct and maintain the grid box hierarchy. Section 4 presents two naming algorithms to name the grid boxes constructed. Section 5 analyzes the decentralized maintenance protocol. Section 6 describes an example overlay operation (routing) using the GBH. Section 7 presents our experimental results. Sections 8 and 10 discuss related work and our future work respectively. Section 9 concludes the paper.

2 Background

GBH Overview: The abstract structure of the Grid Box Hierarchy (GBH) is as follows [5]. The GBH for a sensor network of N sensor nodes consists of N/K grid boxes, each box containing an equal number of sensor nodes (K). K is a constant integer that is independent of N. Each grid box is assigned a unique $(log_K N - 1)$ digit address in base K (i.e., each digit is an integer between 0 and K - 1). All these grid boxes lie only at the leaves of the virtual hierarchy. For all $1 \le i \le log_K N$, subtrees of height i in the hierarchy contain the set of grid boxes (actually, the sensor nodes inside them) whose addresses match in the most significant $(log_K N - i)$ digits - this is used to name the internal node of the GBH with a series of wildcards at the end, as shown in Figure 1.



Figure 1: GBH with N = 8, K = 2

²Such approximate locations can be obtained using any localization algorithm or using GPS.

For sensor networks, we require that (1) sensor nodes within each given grid box are physically proximate, and (2) each pair of grid boxes with close-by names, are physically proximate. Indeed, these conditions are loosely stated because this turns out to be sufficient for the overlay operations we are interested in. Condition (2) implies that the smaller the integer difference between two grid boxes, the closer they are in physical space. Internal nodes in the GBH now correspond to physical regions, and condition (2) implies that physical proximity also extends to regions spanned by internal nodes of GBH.

Example of Using the GBH Underlay: Such a *GBH underlay* provides us a basis for building several important overlay operations. By virtue of the name-physical proximity relation (conditions (1) and (2)), if these overlay operations are designed in a manner that respects the hierarchy of the GBH, they will also be efficient in terms of actual message overhead within the wireless ad-hoc sensor network. For example, if an overlay operation minimizes message transfers between pairs of grid boxes that are far apart in the name space, the operation is also efficient in terms of actual message overhead. Thus, a designer of scalable and reliable protocols for overlay operations can design the protocol directly on top of the GBH underlay, and the GBH will ensure that the protocol will also be efficient in terms of actual overhead and energy usage.

Examples of overlay operations include:

- Any arbitrary *region* (specified either as a set of sensor nodes or a geographic region) can be mapped to a series of grid boxes and internal nodes in GBH.
- Anycast *routing* can then be done from any source node that is outside this region into the region itself.
- *Multicast* can be initiated within a given region by using either flooding or gossiping or a spanning tree.
- Aggregation can be done as follows [5]. A global aggregate function is calculated bottom up in this hierarchy, and in $log_K N$ phases. In the first phase, each sensor node M_j (or a representative) evaluates an estimate of the function when evaluated over the values of all sensor nodes in its grid box. In each subsequent i^{th} (i > 1) phase, each member M_j (or a representative) evaluates the value of the aggregate function over the set of votes by sensor node belonging to the same height i subtree as M_j . In each phase, the partial aggregates are spread by using the region multicast overlay operation.

We discuss regions, routing and multicast operations using GBH in Section 6.

Creating and Maintaining the GBH Underlay: We study protocols to crate and maintain the GBH underlay. Specifically, we wish to assign each sensor node to a grid box so that all grid boxes contain an equal number of nodes, and conditions (1) and (2) for the relation between name physical proximity is attempted to be maintained.

There are two components to our protocols: (a) *Balancing* protocols that ensure the balance of sensor nodes across grid boxes, and (b) *Naming algorithms* for maintaing conditions (1) and (2) above. The input to the creation algorithms

The GBH creation protocols take as input an approximate location for each node (obtained through a localization service) or GPS. These are used by the naming algorithm to assign names to grid boxes ³. The balancing algorithm then takes over, and ensures that the grid boxes balance out. The balancing algorithm continues to run throughout the lifetime of the network and in fact constitutes the maintenance protocol.

The creation and maintenance protocols are required to be localized, energy-efficient, self-reorganizing and robust against node failures and rebirths.

³Some grid boxes may be nonexistent if the distribution of nodes is highly non-uniform - this simply results in an increase in the value of K in the distribution of nodes among the grid boxes.

3 Diffusion Based Balancing

In this section, we propose two new diffusion based balancing protocols for maintaining the GBH. These algorithms are similar to algorithms used for load balancing in multiprocessors. Sensor nodes transfer in between grid boxes (note that this is not physical movement) in order to restore balance.

3.1 Leader Based Diffusion

3.1.1 Direct Neighborhood (DN) Diffusion

This variant is based on leader-election. Figure 2 shows the psedudocode. The next section describes a decentralized variant. Each grid box G_i has a leader node L_i . L_i maintains a list of its grid box members, as well as a list of neighbor grid boxes, their leaders and their sizes. Every T_b time units, L_i checks its neighbor grid box sizes and picks a neighboring grid box G_j with maximum size difference and sends L_j a balancing request. If the request is accepted, then the leader of the larger box initiates a transfer of an appropriate number of nodes. The set of nodes transferred may include the leader L_i itself; however this node stays a leader for G_i ; leaders do not move very far from their grid boxes since grid boxes do not "move" large physical distances. Stale grid box size information in these messages does not cause inconsistency since each leader is participating in at most one transfer at a time. The communication between the leaders can be done through TTL-restricted flooding since they are likely to be close by. The nodes to be transferred may be chosen from among those that are close to the boundary of S_i and S_j , or those that are close to the centroid of G_j (this information is sent by L_j), or those that add maximum number of edges to G_i .

3.1.2 Average Neighborhood (AN) Diffusion

AN is an extension of DN whereby each grid box balances with more than one neighbor. Up to m neighbors may be used, where m varies from 1 to all neighbors. We expect that AN will take fewer messages and time than the DN algorithm. The AN algorithm uses the DN algorithm, where the m neighbors with highest differences are chosen, and are used for balancing. Implementation details are omitted since they are similar to DN in, and use $M_{req_balance}$, $M_{accept_req_balance}$, and $M_{reject_req_balance}$ messages.

Failure of the leaders in these schemes can hamper the convergence properties of the protocol. This motivates decentralized schemes that do not reply on leaders. We discuss these schemes in the next section.

3.2 Decentralized Probabilistic Diffusion

The pseudocode for the Decentralized Probabilistic Diffusion Balancing protocol is shown in Figure 3. We explain the protocol below.

Initialization: Each sensor node initially knows its approximate grid box address based on its approximate location and by using a *naming algorithm* (described in Section 4). It then starts to maintain the current membership GS_i of its grid box G_i . This is achieved by having a newly joining node TTL-flood an $M_{entering_gb}$ message, and receiving nodes in the grid box include this new node in their membership lists.

Balancing: After initialization is completed (specified by a timeout), each sensor node participates in the balancing protocol. Sensor nodes on the periphery of their grid boxes (those with neighbors in a different grid box) announce any changes in their grid box name and membership size to their neighbors through a $M_{my_grid_box}(G_i, GS_i)$ message, which are recorded at the recipients. Every T_b time units, sensor s_j selects a neighbor s_i such that $G_j \neq G_i$ and $|GS_j| > |GS_i| + 1$. Then, with probability P_T , s_j transfers itself from G_j to G_i . Nodes entering or leaving a grid box announce this by TTL-flooding $M_{entering_gb}$ and $M_{leaving_gb}$ messages respectively.

```
loop
  if time > time_T \land state = DOING\_NOTHING then
     choose neighboring grid box g' with maximum |size(g) - size(g')| greater than 1
    send M_{req\_balance}(g, L_g) to destination leader L_{g'}
     state \leftarrow SENT\_REQUEST
  end if
  receive msg
  if msg = M_{req\_balance}(g', L_{g'}) then
     if state = DOING_NOTHING then
       send M_{accept\_req\_balance}(g, L_g) to L'_g
       state \leftarrow BALANCING
       if size(g) > size(g') then
         choose S, a set of \lfloor \frac{size(g) - size(g')}{2} \rfloor nodes in grid box g
         inform S that their new grid box is g'
         inform L'_g to add S to grid box g'
         broadcast new size information to neighboring grid boxes
         state \leftarrow DOING\_NOTHING
       end if
     else
       send M_{reject\_req\_balance}(g, L_g) to L'_g
     end if
  end if
  if msg = M_{reject\_req\_balance} then
     state \leftarrow DOING\_NOTHING
     time_T \leftarrow time + T_b
  end if
  if msg = M_{accept\_req\_balance} then
     state \leftarrow BALANCING
```

 $\mathbf{if} \ size(g) > size(g') \ \mathbf{then}$

end if

end if end loop

 $time_T \leftarrow time + T_b$

inform L'_q to add S to grid box g'

 $state \leftarrow DOING_NOTHING$

choose S, a set of $\lfloor \frac{size(g) - size(g')}{2} \rfloor$ nodes in grid box g inform S that their new grid box is g'

broadcast new size information to neighboring grid boxes

Require: L_g is node address, g is initial GB address, $time_T = T_b$ and $state = DOING_NOTHING$

Figure 2: Direct Neighborhood Diffusion (DN).

The probabilistic choice P_T prevents migrations of large numbers of sensor nodes. This scheme should be chosen so as to minimize oscillations and assure convergence and a stable solution. We discuss different ways of setting this probability in Section 3.3.

Maintenance: At regular intervals, every sensor floods (with a TTL enough to reach its grid box) a $M_{presence_update}$ heartbeat message. Each entry in GS_i at s_i has a time to live which is initialized to slightly higher than the heartbeat interval. Entries time out if heartbeats are not received, thus gracefully removing failed nodes from the grid box and the system itself. Any such change will result in a subsequent balancing movement.

When a new sensor node joins (or rejoins) the network, it requests its neighbors for their grid box numbers. It chooses one of them and joins that box. The distribution is balanced out then by the balancing protocol.

3.3 Probability of Transfer function P_T

We discuss different ways of setting the probability P_T that determines the rate at which nodes move across neighboring grid boxes.

Constant Probability p: P_T is set to a constant value of $\frac{p}{GS_i}$. Choosing the right value for p is crucial to the protocol's success. A high value for p could result in a large number of nodes in the periphery of a grid box transferring to a neighboring grid box. If this movement is large enough to alter the order of grid box sizes, this could cause node oscillations between grid boxes. On the other hand, a very low value for p will result in slow convergence.

Linear Probability: The probability P_T is set as $\frac{p\delta}{|GS_i|}$, where δ is the size of the imbalance (difference in number of nodes between grid box sizes). This ensures higher imbalances are balanced out faster (due to the higher probability of doing so).

3.4 Tree Based Update Dissemination

The TTL-flooding used to spread information within grid boxes and across neighboring grid boxes can be replaced by a tree-based dissemination protocol to spread these updates in a more message- and energy-efficient manner. The basic idea involves each grid box maintaining a spanning tree containing all its nodes, as well as a few nodes from neighboring grid boxes. We omit description of the tree building/maintenance protocol due to its simplicity.

4 Naming Algorithms

A naming algorithm assigns an initial grid box address to a sensor node based on its knowledge of its approximate geographic location. For simplicity, we assume that all sensor nodes know the layout of the entire area, and this area is rectangular.

Let X represent the length of the area and Y represent the width. Assume that n = N/K is a power of K. Consider two cases depending on whether n is an even or odd power of K.

- If $n = K^{2r}$, split the area into rectangular parts such that there are K^r boxes on each side. Each box is of length $\frac{X}{K^r}$ and width $\frac{Y}{K^r}$.
- If $n = K^{2r+1}$, split the area into rectangular parts such that there are K^r boxes on the smaller side and K^{r+1} on the larger side. If $X \ge Y$, each box is of length $\frac{X}{K^{r+1}}$ and width $\frac{Y}{K^r}$.

Let x represent the length of the system area in terms of boxes and y represent the width of the system area in terms of boxes. We model the naming scheme as a function f_{xy} that takes a grid box G_{ij} (where i and j represent the grid box's position along X and Y axes) and assigns it a number in base K. Two intuitive schemes are stated below,

Require: *i* is node address, *g* is initial GB address, *GS* is the initial member set of *g*, $time_T = T_b$ and *N* is set of known neighboring nodes and their grid box sizes

```
loop
  if time > time_T then
     choose (j, g', GS') from N with minimum |GS'|.
     if |GS| > |GS'| + 1 then
       if rand < p then
          GS \leftarrow GS' \cup i
          flood M_{entering\_gb}(g', i) and M_{leaving\_gb}(g, i)
          g \leftarrow g'
          broadcast M_{my\_gb}(i, g, GS)
       end if
     end if
     time_T \leftarrow time + T_b
  end if
  receive msq
  if msg = M_{my\_gb}(j, g', GS') then
     update N to contain neighbor j, its grid box address g' and its member set GS'
  end if
  if msg = M_{entering\_gb}(g, j) then
     GS \leftarrow GS \cup \{j\}
     broadcast M_{my-gb}(i, g, GS)
  end if
  if msg = M_{leaving\_gb}(g, j) then
     GS \leftarrow GS - \{j\}
     broadcast M_{my-gb}(i, g, GS)
  end if
end loop
```

Figure 3: Balancing through Decentralized Probabilistic Diffusion.

Linear: In this scheme $f_{xy}(G_{ij}) = j \times x + i$. In other words, the boxes are numbered row-wise. **Recursive:** Assume that we have to name K^n boxes. Split the area into $K \times K$ big boxes each of which has to house K^{n-2} grid boxes. Now number the big boxes in row-wise order from 0 to $K^2 - 1$. This needs 2 digits in base K and will act as prefix for the names of all boxes inside each big box. Now recursively split, name and add the prefixes.

A simple analysis below shows that the recursive scheme produces clusters that are more squarish than that produced by the linear scheme. This results in better proximity between nodes in the same cluster.

First consider the case when $n = N/K = K^{2r}$, an even power of K. Consider the subtree (in GBH) comprising of boxes that match in the t most significant digits. Let us compute the squareness of this level (we call this the t-level for simplicity) for both schemes. For the linear scheme, we need to consider two cases t < r and $t \ge r$. If $t \ge r$, then the t-level is a rectangle of size $K^{2r-t} \times 1$. If t < r, then the t-level is a rectangle of size $K^{2r-t} \times 1$. If t < r, then the t-level is a rectangle of size $K^r \times K^{r-t}$. Consider the recursive scheme. We need to consider two cases: t is even and t is odd. If t is even, then the t-level is going to be the same as the 0-level of a hierarchy with K^{2r-t} boxes. This is of size $K^{r-\frac{t}{2}} \times K^{r-\frac{t}{2}}$. If t is odd, then the t-level is going to be the same as the 0-level of a hierarchy with K^{2r-t} boxes. This is of size $K^{r-\frac{t}{2}} \times K^{r-\frac{t}{2}}$. If t is odd, then the t-level is going to be the same as a linear arrangement of the 0-levels of K hierarchies with $K^{2r-(t+1)}$ boxes. This is of size $K^{r-\frac{t-1}{2}} \times K^{r-\frac{t+1}{2}}$. Let us define squareness as the ratio of the smaller side to the larger side. The closer it is to 1, the better it is. Linear scheme has squareness $\frac{1}{K^{2r-t}}$ if $t \ge r$ and $\frac{1}{K^t}$ when t < r. Recursive scheme has squareness 1 if t is even and $\frac{1}{K}$ if t is odd. It is easy to see that recursive scheme achieves much better squareness. It can be similarly shown for the case when n is an odd power of K.

5 Analysis

In this section, we analyze the decentralized probabilistic balancing protocol with linear probabilities of transfer.

Let us consider a grid box system with $N \times N$ regular grid boxes. The analysis can be easily extended to a system where the sides are not equal. Let the grid boxes be numbered in a rowwise fashion and let s_i represent the size (in number of nodes) of grid box G_i . Assume G_i and G_j are boxes that share a common side. The two boxes can diffuse nodes between them if $s_i \neq s_j$. Assume w.l.o.g that $s_i > s_j$. Now the probability of transfer for a node on the boundary of the two boxes but on the G_i side is given by $\frac{p}{s_i}(s_i - s_j)$. If f is the fraction of s_i that form the boundary, then the overall rate of transfer of nodes from G_i to G_j is given by $f \times s_i \times \frac{p}{s_i}(s_i - s_j)$ which evaluates to $f \times p(s_i - s_j)$. Let us w.l.o.g assume f = 1 which results in a node transfer rate of $p(s_i - s_j)$ from G_i to G_j .

Now, we figure out the total rate of transfer out of G_i by considering all 4 neighboring boxes (which may be 3 or 2 depending on edge/corner cases). This can be represented as $-\frac{ds_i}{dt} = p(s_i - s_{i-1}) + p(s_i - s_{i+1}) + p(s_i - s_{i-N}) + p(s_i - s_{i+N})$. More concisely, $\frac{ds_i}{dt} = p(s_{i-1} + s_{i+1} + s_{i-N} + s_{i+N} - 4s_i)$. Let NG_i represent the set of neighboring grid boxes of grid box G_i . Then the equation for rate of change of s_i can be given as,

$$\frac{ds_i}{dt} = p\{\left(\sum_{G_j \in NG_i} s_j\right) - |NG_i| \times s_i\}\tag{1}$$

We prove convergence properties of a simple system at first and then extend it to any general system. All theory behind the proofs can be found in [27].

5.1 A Simple System

For an example 2×2 system, the rate of change equations can be given by,

$$\frac{ds_0}{dt} = p(s_1 + s_2 - 2s_0) \tag{2}$$

$$\frac{ds_1}{dt} = p(s_0 + s_3 - 2s_1) \tag{3}$$

$$\frac{ds_2}{dt} = p(s_0 + s_3 - 2s_2) \tag{4}$$

$$\frac{ds_3}{dt} = p(s_1 + s_2 - 2s_3) \tag{5}$$

Let s represent the column vector containing the sizes of grid boxes in row wise order. Then, the above set of equations can be given as $\dot{s} = As$, where A is the coefficients matrix,

$$\mathbf{A} = p \times \left(\begin{array}{rrrr} -2 & 1 & 1 & 0 \\ 1 & -2 & 0 & 1 \\ 1 & 0 & -2 & 1 \\ 0 & 1 & 1 & -2 \end{array} \right)$$

A linear differential equation system as above can be solved for by computing the eigenvalues and eigenvectors of **A**. The eigenvalues of **A** can be computed as the roots of the characteristic equation $|\mathbf{A} - \mathbf{I}\lambda| = 0$. The roots are $\lambda = 0, -2p, -2p, -4p$ where -2p is a repeating root. The corresponding eigenvector for each eigenvalue λ_i can be computed as a solution \mathbf{v}_i to $\mathbf{A}\mathbf{v}_i = \lambda_i \mathbf{v}_i$. We then have,

$$\lambda_{0} = 0 \quad \mathbf{v}_{0} = \begin{pmatrix} 1 & 1 & 1 & 1 \\ \lambda_{1} = -2p & \mathbf{v}_{1} = \begin{pmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & -1 \end{pmatrix}$$

$$\lambda_{2} = -2p \quad \mathbf{v}_{2} = \begin{pmatrix} 1 & -1 & 1 & -1 \\ \lambda_{3} = -4p & \mathbf{v}_{3} = \begin{pmatrix} 1 & -1 & -1 & 1 \\ 1 & -1 & -1 & 1 \end{pmatrix}$$

Then the general solution to $\dot{\mathbf{s}} = \mathbf{As}$ is given by, $\mathbf{s} = \sum_{0 \le i \le 3} c_i \mathbf{v}_i e^{\lambda_i t}$. For the eigenvalues and eigenvectors computed above, this can be written out as,

$$s_0 = c_0 + (c_1 + c_2)e^{-2pt} + c_3e^{-4pt}$$
(6)

- $s_1 = c_0 + (c_1 c_2)e^{-2pt} c_3 e^{-4pt}$ (7)
- $s_2 = c_0 (c_1 c_2)e^{-2pt} c_3 e^{-4pt}$ (8)

$$s_3 = c_0 - (c_1 + c_2)e^{-2pt} + c_3 e^{-4pt}$$
(9)

We can make a number of observations from the solution above for the relatively simple system,

- Given s_0^{in} , s_1^{in} , s_2^{in} , s_3^{in} as the initial grid box sizes, we can solve for the constants c_i . In particular, c_0 turns out to be equal to $\frac{\sum_i s_i^{in}}{4}$ which is the average grid box size.
- All non-constant terms are negative exponential terms which converge to 0 as $t \to \infty$. This implies each s_i converges to c_0 as $t \to \infty$. But c_0 is the average grid box size and hence all grid boxes converge to an equal number of nodes.

Thus we have proven that the system converges to a state where every grid box size is equal. In the next section, we briefly prove without explicitly solving that this extends to any general grid box system.

5.2 A General System

Consider a general grid box system with $N \times N$ grid boxes whose sizes vary as given by the equations,

$$\frac{ds_i}{dt} = p\{\left(\sum_{G_j \in NG_i} s_j\right) - |NG_i| \times s_i\}$$
(10)

As mentioned in the previous section, this system of differential equations can be concisely represented by $\dot{\mathbf{s}} = \mathbf{As}$, where \mathbf{A} is the coefficients matrix of equations 10.

Lemma 5.1. A has real eigenvalues.

Proof: It is known that a symmetric real matrix has real eigenvalues. We are done if we show that \mathbf{A} is symmetric.

Recall that **A** is the coefficients matrix corresponding to the N^2 equations in N^2 variables. Hence, A_{ij} is the coefficient of s_j in the equation for $\frac{ds_i}{dt}$. Looking at Equation 10 it is obvious that all coefficients outside of the main diagonal are either -1 or 0. More precisely when $i \neq j$, A_{ij} is 1 *iff* G_j is a neighbor of G_i and 0 otherwise. Thus $A_{ij} = A_{ji}$ which concludes the proof.

Lemma 5.2. 0 is an eigenvalue of A.

Proof: ¿From Equation 10, we can see the sum of coefficients in each equation is 0. This means the each row of \mathbf{A} sums to 0. This further implies that,

$$\mathbf{A}. \begin{pmatrix} 1\\1\\...\\1 \end{pmatrix} = 0 = 0. \begin{pmatrix} 1\\1\\...\\1 \end{pmatrix}$$

Therefore 0 is an eigenvalue of \mathbf{A} with eigenvector $\begin{pmatrix} 1 & 1 & \dots & 1 \end{pmatrix}$. Hence proved.

Defn: A symmetric real square matrix \mathbf{A} is negative semidefinite if for any nonzero vector \mathbf{x} , we have $\mathbf{x}^T \mathbf{A} \mathbf{x} \leq 0$.

Lemma 5.3. A is a negative semidefinite matrix.

Proof: We will first see how this is proved for the 2×2 system given in the previous section. This is in spite of actually solving the system to illustrate a proof technique.

$$\mathbf{x}^{T} \mathbf{A} \mathbf{x}$$

$$= \mathbf{x}^{T} p \begin{pmatrix} -2 & 1 & 1 & 0 \\ 1 & -2 & 0 & 1 \\ 1 & 0 & -2 & 1 \\ 0 & 1 & 1 & -2 \end{pmatrix} \mathbf{x}$$

$$= 2p(x_{0}x_{1} + x_{0}x_{2} + x_{1}x_{3} + x_{2}x_{3} - \sum_{i} x_{i}^{2})$$

$$= -p[(x_0 - x_1)^2 + (x_0 - x_2)^2 + (x_2 - x_3)^2 + (x_1 - x_3)^2]$$

$$\leq 0$$

So intuitively, the proof will proceed by proving $\mathbf{x}^T \mathbf{A} \mathbf{x}$ can always be written as the negation of a sum of squares.

Let $a = \mathbf{x}^T \mathbf{A} \mathbf{x}$ for a general \mathbf{A} . Notice that $\mathbf{A} \mathbf{x}$ is a column vector with the i^{th} row being $\frac{dx_i}{dt}$. Therefore the coefficient of x_i^2 in a is $-|NG_i|$ from Equation 10. Similarly the coefficient of $x_i x_j$ in a is 2 if G_i and G_j are neighbors and 0 otherwise. There are no other terms in a. Thus a can be represented as,

$$a = -\sum_{i} |NG_i| x_i^2 + 2\sum_{N(i,j)=1} x_i x_j$$
(11)

where N(i, j) is 1 if G_i and G_j are neighbors and 0 otherwise.

Because each x_i takes part in a product of the form $2x_ix_j$ exactly $|NG_i|$ times, we can rewrite the above equation as $a = -\sum_{N(i,j)=1} (x_i - x_j)^2$ which means $a \leq 0$. Thus we have proved **A** is a negative semidefinite matrix.

Theorem 5.4. A has only non-positive real eigenvalues.

Proof: Lemma 5.1 proved **A** has only real eigenvalues. A negative semidefinite matrix has all non-positive real eigenvalues and we proved in Lemma 5.3 that **A** is a negative semi definite matrix. Therefore **A** has only non-positive real eigenvalues. \Box

Theorem 5.5. A general system converges to a state where each grid box has an equal size.

Proof: Theorem 5.4 states all eigenvalues of \mathbf{A} are negative or 0. In general, the solution to a system of the form $\dot{\mathbf{s}} = \mathbf{As}$ can be written as $\mathbf{s} = \sum_i c_i \mathbf{v}_i e^{\lambda_i t}$ where λ_i are the various eigenvalues and \mathbf{v}_i is a corresponding set of linearly independent eigenvectors. In the case when such a basis of linearly independent eigenvectors cannot be found, the exponentials just get scaled by appropriately computed polynomials in t ([27]). Lemma 5.2 showed that 0 is an eigenvalue. Therefore the constants in s_i are all equal to c_0 which is equal to the average grid box size upon solving the initial value problem. All non-constant terms are negative exponentials (proved by Theorem 5.4). Therefore all s_i converge to c_0 as $t \longrightarrow \infty$.

6 Overlay Operations: Regions, Routing and Multicast

We have used the GBH underlay to build routing and multicasting operations. We have also added the ability to define arbitrary regions.

6.1 Routing and Multicast

Figure 4 shows the routing pseudocode. It assumes that each grid box node maintains a set of grid box's neighboring grid boxes. A routing message is forwarded to neighbors in either its own grid box or the closest grid box chosen by the closest() function shown in figure 5. The closest function extracts even and odd numbered digits for each grid box address (neighbors, target and own) and uses these as coordinates to calculate the Euclidean distance between two grid boxes. The neighbor chosen to route the message to is the neighbor with the smallest distance from the target grid box. The figure below shows an example route.

10

Require: nodeid is node address, gridbox is initial grid box address in base K, neighborgb is the neighbor grid box set array, neighbor is the neighbor node array, to is the target grid box, from is the source grid box

```
if msg = M_{routing\_msg}(to, from) then
  if gridbox = to then
    for all neighbor grid boxes nbg in neighborgb do
       if nb.qridbox = qridbox then
         send M_{routing\_msg}(nbg, to, from)
       end if
    end for
  else
    closest_ngb \leftarrow closest(neighborgb, gridbox, to)
    for all neighboring nodes nq in neighbors do
       if ng.gridbox = closest_ngb or nb.gridbox = gridbox then
         send M_{routing\_msg}(nb, to, from)
       end if
    end for
  end if
end if
```

Figure 4: Routing algorithm

Require: nodeid is node address, gridbox is node grid box address in base K, target is target grid box address in base K, neighborgb is the neighbor grid box set array, $odd \leftarrow TRUE$ $to_odd \leftarrow digits(target, odd)$ $to_even \leftarrow digits(target, \neg odd)$ $mine_odd \leftarrow digits(gridbox, odd)$ $mine_even \leftarrow digits(gridbox, \neg odd)$ $closest_dist \leftarrow sqrt((to_odd - mine_odd)^2 + (to_even - mine_even)^2)$ $closest_nqb \leftarrow nodeid$ for all neighbor grid boxes ngb in neighborgb do $nb_odd \leftarrow digits(ngb, odd)$ $nb_even \leftarrow digits(ngb, \neg odd)$ $temp_dist \leftarrow sqrt((to_odd - nb_odd)^2 + (to_even - nb_even)^2)$ if *temp_dist* < *closest_dist* then $closest_nqb \leftarrow nqb$ $closest_dist \leftarrow temp_dist$ end if end for {Returns closest_ngb}

Figure 5: Closest Algorithm to choose closest neighboring grid box to target grid box

Require: gridbox is node grid box address in base K, odd for odd numbered digits

```
for all digits i in gridbox do

if odd and i\%2 = 1 then

append gridbox[i]

else if \neg odd and i\%2 = 0 then

append gridbox[i]

end if

end for

{Returns final}
```

Figure 6: Digit Algorithm to extract even and odd digits of a grid box address)

6.2 Defining regions

A region of sensors, specified either as a set of sensors (e.g., close to a given object) or as geographical region, can be mapped to an aggregated region address. The region is comprised of the set of grid boxes that contain at least one sensor node intersecting with the region specified. The region can then be specified using the collection of names of these grid boxes. Any subset of grid boxes from this can be

0000	0001	0100	0101
0010	0011	0110	→ 0111
1000	1001	1100	1101
1010	1011	1110	1111

Figure 7: Routing from 1000 to 0111

aggregated if they comprise all grid boxes that are descendants of an internal node in the GBH. For example, (1000, 1001, 1010, 1011, 0100, 0101) can be rewritten as " $10^{**}+010^{**}$. A region-based routing protocol for this destination region will anycast the message to one grid box in the 10^{**} region (i.e., one of 1000, 1001, 1011 and 1010) and to one grid box in the 010^{*} region (0100 or 0101) since these are separated subregions. A region-based multicast protocol follows up these anycasts with either flooding or tree-based or gossip-based multicast among all grid boxes within each of these subregions.

7 Simulation Results

We have simulated the above protocols with N = 512, K = 8 which implies that there are 64 grid boxes. The area of simulation is 10×10 and the radio range is 1.0. We are assuming each node knows its location and thus knows which grid box it is in. Results for protocol performance under approximate locations are also studied. The simulation proceeds in rounds. During each round, all messages intended for each node are delivered and the node takes actions and sends messages which get delivered in the next round. Note that though we use round numbers to stand for running time of the protocol, the protocols proposed do not need time synchronization.

7.1 Leader-Based Diffusion

7.1.1 Variance in Grid Box Sizes

Figure 8 shows the variance in grid box sizes from K as the protocols (DN and AN) proceed. It can be seen that both protocols rapidly decrease the variance as time proceeds. AN uses a larger neighborhood information than DN and converges faster. Note that here AN uses 4 neighbor (2 and 3 for edge and corner cases respectively) grid box information.

7.1.2 Movement of Grid Box Centroids

Figures 9 and 10 show movement of grid box centroids when compared to their initial positions. Three curves for maximum, average and minimum movement show that grid box movement is very small. Comparing Figures 9 and 10, we see that centroid movement is smaller in AN when compared to DN due to larger neighborhood information. Small grid box movement means lesser skewing of the initial grid box structure (based on locations) imposed on the system. This is very important for the naming scheme that was initially used on the grid boxes to be useful when the system reaches a balanced state.



Figure 8: Variance in grid box sizes vs. round number for DN and AN



Figure 9: Distance of final grid box centroids from the initial centroid positions for DN

7.2 Decentralized Probabilistic Diffusion

7.2.1 Grid Box Size Variance

Figure 11 shows the variance in grid box sizes from K. The different curves in the figure are the variance curves for different constant probabilities of transfer. Probability experiments that decide transfers are done every T = 30 rounds.

7.2.2 Frequency of Node Transfers

Figure 12 shows the number of node transfers that happen until variance becomes less than 1.0 (a common objective). More node transfers happen when a higher probability is used due to node oscillations. Node transfers need to be informed across two grid boxes and hence consume energy. This gives a natural application-dependent tuning factor viz., a higher probability results in faster convergence but larger energy loss. For a constant probability of 0.1 which has really fast convergence, only 82 broadcasts per node is required. Note that about 60 of these broadcasts happen only at the start of the protocol when nodes flood to announce their presence in a grid box.



Figure 10: Distance of final grid box centroids from the initial centroid positions for AN



Figure 11: Variance in grid box sizes vs. round number for different constant probabilities of transfer

7.2.3 Movement of Grid Box Centroids

Figure 13 shows the movement in final grid box centroids with respect to the initial box centroids. The graph shows that a higher probability results in larger centroid movement. This is due to a higher number of transfers which implies a higher expected distance moved by centroids. Again, we see a tradeoff between convergence rate and protocol correctness.

7.2.4 Dispersion of Grid Box Nodes

Another parameter that is important is how close nodes within a grid box are to each other. This is shown in Figure 14 as the average area of the bounding box of each grid box. Node dispersion increases with probability of transfer since a higher number of transfers generally disperses the grid boxes more.

7.2.5 Linear Probability

Figure 15 shows the variance in grid box sizes with protocol rounds for different linear probability functions. Note that the curves are plotted for different p. The number of transfers and hence message



Figure 12: Total number of node transfers in the system vs. constant probability of transfer



Figure 13: Distance of final grid box centroids from initial centroids vs. constant probability of transfer

complexity, grid box dispersion and centroid movement is decreased. We do not show explicit graphs due to lack of space.

7.2.6 The Gap of 1 Problem

In previous simulations, node transfers do not happen when the size difference between two grid boxes is 1, because then the situation would only reverse. A typical final state for N = 512, K = 8 showing grid box sizes is shown below. Notice that there are grid boxes that differ in at most 1 from each of their neighboring boxes and this gradient slowly builds across the network. This is the cause for the base variance of 0.5 below which the previous graphs could not venture. We call this the gap of 1 problem.

10	8	8	8	8	7	8	8
9	8	8	8	8	8	7	8
9	9	8	8	9	8	8	7
8	8	8	9	9	9	7	8
8	9	9	8	9	8	7	8
9	9	9	8	8	7	7	7
8	8	8	8	8	7	7	7
8	8	8	8	7	7	7	7



Figure 14: Average final grid box area vs. constant probability of transfer



Figure 15: Variance in grid box sizes vs. round number for different linear probabilities of transfer (plotted for the various constants shown)

Now, we allow a node transfer across a gap of 1 boundary with a certain small probability. The intuition is that a transfer can open up differences that are greater than 1 and thus reduce variance by balancing. This is shown in the final state below, where the gradient has disappeared and most grid boxes are of size K after 10000 rounds.

8	8	8	8	8	8	8	8
9	8	8	8	7	8	8	8
8	9	8	8	8	8	8	8
7	8	9	8	9	7	8	7
8	8	8	8	8	9	8	8
8	8	8	8	9	8	8	8
8	8	7	8	7	8	8	8
8	8	8	8	8	8	8	8

The variances in grid box sizes corresponding to the above two systems are shown in Figure 16. However note that this small probability of transfer implies there will always be little oscillation in the system depending on the value of the probability.



Figure 16: Variance in grid box sizes vs. round number for different linear probabilities of transfer (plotted for the various constants shown) with transfers across gaps of size 1

7.2.7 Naming Algorithms

We now measure how good the naming scheme is on top of the decentralized protocol. Since the recursive and linear naming schemes are the same when N = 512, K = 8, we obtain results using N = 512, K = 2. Figure 17 shows the performance of linear probability based transfer protocol using linear and recursive naming schemes respectively. The curve shows average distance between nodes having certain maximum common prefix length in grid box addresses. This is important in aggregation protocols as pointed out in [5] because nodes that share a common prefix take part at the same level of aggregation and hence require to be proximal to each other. It can be seen that recursive naming scheme not only achieves lower average distance between nodes sharing a common prefix but also the lower maximum distance between such nodes.



Figure 17: Average distance between nodes vs. length of maximum common prefix in grid box addresses for both naming scheme

7.2.8 Maintenance

Figure 18 shows the maintenance phase with node death between rounds 3000 and 4000 followed by resurrection of half of the dead nodes between rounds 7000 and 7500. Note that this is a drastic loss rate and results in about 100 sensors out of 512 being removed over a span of 1000 rounds and 50 added over 500 rounds. The variance initially goes up and then the maintenance mechanism kicks in stabilizing the system. During node losses (network failures), the behavior of the protocol is incorrect, but when the network returns to normal, the protocol stabilizes and returns to correct execution. Note that we have however ensured that network partitions do not occur. Testing resiliency of the protocol under network partitions is part of our future work.



Figure 18: Variance in grid box sizes vs. round number for linear probability (0.005) of transfer under drastic node loss followed by node resurrection

7.2.9 Grid box Final State

A sample final state after decentralized balancing with a linear probability of transfer function is shown in Figure 19(a). The bounding boxes of grid boxes are shown with the grid box's linear address in the center. Notice that the boxes are very big and there are several overlapping areas. This is not good for the system because overlapping boxes implies inter box bandwidth contention and loss of locality for intra box operations. We now restrict transferrable nodes to be the set of nodes that are within 1.0 distance units from the destination box's centroid. This results in much better grid box shapes as shown in Figure 19(b). It however reduced the rate of convergence and a higher probability of transfer was used.

7.2.10 Approximate Locations

The decentralized protocol uses locations for nodes to arrive at an initial grid box assignment. In this section, we show that the protocol performs well even under coarse location knowledge. A node's assumed location is shifted in an arbitrary direction by a randomly chosen distance from 0 to 70% of the communication radius (1.0 in this case). The final grid box shapes obtained are shown in Figure 19(c). Notice that the boxes are slightly larger, but the general layout is still maintained. Hence the protocol can perform well under approximate location information.



Figure 19: (a) Grid boxes at the end of 10000 rounds (b) Grid boxes at the end of 10000 rounds with transfer restrictions (c) Grid boxes at the end of 10000 rounds under approximate locations

7.2.11 Routing

Endpoints	Hops	GBH routing latency
0 - 63	17	18.16
9 - 54	12	14.85
8 - 45	9	9.75
25 - 30	10	11.42
0 - 7	14	17.5

Section 6 described a protocol for routing a message from a node in a grid box to any node in a destination grid box. The table below shows the performance of GBH based routing in terms of its routing latency vs. the shortest distance. The table shows routing endpoints (grid boxes), the shortest path length between them and the latency over GBH routing. GBH based routing can achieve a routing latency that is really close to the shortest path without having to flood between the source and destination. The endpoints were chosen to exercise different kinds of paths viz., diagonal, horizontal, edge aligned etc.

8 Related Work

Clustering algorithms have been proposed in ad hoc networks using the notion of a cluster-head. [18] proposes the Mobility-Adaptive Clustering for Ad Hoc networks protocol. This ensures that nodes elect themselves as cluster-heads only if they have a sufficiently high weight (in the neighborhood) which defines a measure of permanency. The weight of a node can be fixed based on several parameters. A naive way is to elect the lowest ID node ([19]). A weight based on energy available at the nodes was proposed in [20]. Cluster-heads that are low mobility nodes were used in [21]. A robust hierarchical clustering algorithm for the amorphous computing model has been proposed in [15] which uses the persistent nodes ([17]) to obtain a hierarchy called the PNHierarchy.

The work of Corradi et all [23] investigates simple diffusion based policies for dynamic load balancing using only a local view of the system. The work is based on the physical phenomenon of diffusion that forces a system towards a homogenous distribution relying only on local state information. Each element tries to move in the direction of decreasing energy. They prove that in the static load situation, the execution of a diffusive load balancing policy results in global balancing.

In section 10 we show that obtaining a GBH is equivalent to the incapacitated transportation problem. The transportation problem consists of a bipartite graph with m sources and n sinks. It has the form

$$\begin{array}{c} maximize \sum_{(i,j)\in\mathcal{A}} a_{ij}x_{ij}\\ subject \ to\\ \sum_{j\in A(i)} x_{ij} = \alpha_i, \ \ \forall i = 1,...,m,\\ \sum_{i\in B(j)} x_{ij} = \beta_j, \ \ \forall i = 1,...,n,\\ 0 \leq x_{ij}, \ \ \forall (i,j)\in\mathcal{A} \end{array}$$

It has been shown in [24] that the transportation problem can be converted to the assignment problem, i.e. assigning n persons to n objects such that the benefit, a_{ij} , of assigning person i to object j is maximized. The resulting assignment problem can be solved in a distributed manner using auction algorithms. It has been shown that such auction algorithms terminate in a finite number of iterations with an optimal assignment.

9 Conclusion

Building and maintaining the GBH is a crucial step towards implementing hierarchical gossiping algorithms in wireless sensor networks. Further, this hierarchy can be used for geographic routing and geocasting. We have presented diffusion based algorithms for constructing and continuously maintaining the GBH so that it is self-organizing and self-reconfiguring. In particular, we present two distinct approaches: one requiring a leader to be elected for each grid box and the other being completely decentralized relying on a probabilistic transfer function. However, the leader based approach is not fault tolerant and the probabilistic method stands out as a viable and efficient underlay self-assembly and selfreconfiguration protocol. Our results show that the **Diffusion Based Protocols** self-organize quickly and overcome the *gap of 1* problem. The recursive naming scheme achieves lower distances between nodes that share a higher common grid box address prefix length. In particular, the **Decentralized Probabilistic Diffusion Protocol** also recovers from node failures and node rebirths and stabilizes the variance in grid box sizes. Overall, it achieves a highly scalable, robust, energy efficient, application dependent manner of GBH self-organization and self-reconfiguration for wireless sensor networks.

10 Future Work

Consider the area being split into a set G of grid boxes G_{ij} where (i, j) is represents the position of a grid box in the matrix of boxes. Let the number of nodes in box G_{ij} be K_{ij} . Divide the set G into sets $S = \{G_{ij} | K_{ij} \ge K\}$ and $C = \{G_{ij} | K_{ij} < K\}$ which represent the suppliers and consumers respectively. Let, $G_{ij} \longrightarrow^r G_{kl}$ represent the transfer of r nodes from G_{ij} to G_{kl} . Since the transfer of nodes happen by cascading the effect of several transfers between adjacent boxes, the cost of this transfer can be represented as $C(G_{ij} \longrightarrow^r G_{kl}) = r \times (|i - k| + |j - l|)$. Now the problem reduces to finding values $\forall ijkl0 \le i, k < x \land 0 \le j, l < y, a_{ijkl}$ which represent the number of nodes to transfer from G_{ij} to G_{kl} . The constraints on the system are given below,

$$a_{ijkl} \ge 0 \tag{12}$$

$$\forall ij \sum_{kl} a_{ijkl} = K_{ij} - K \tag{13}$$

$$\forall kl \sum_{ij} a_{ijkl} = K - K_{kl} \tag{14}$$

The goal is to minimize the cost function $\sum_{ijkl} C(G_{ij} \longrightarrow G_{kl})$. This is clearly a transportation problem. The problem can be solved optimally using centralized methods such as the Simplex method or the Hungarian method. However, we would want a distributed solution and the auction method is directly applicable. Each grid box could have leaders that take part in the auction or a distributed scheme without leaders could be tried out.

In the decentralized probabilistic scheme, we have probabilities of node transfer that are proportional to the difference. We will want to factor other parameters into this probability p. We could also try to ensure maximum connectivity within a grid box by inducting the number of edges a node adds to a grid box into the probability function for transfer. For example, a node that is part of a small vertex cut (only considering edges within the grid box) should not be removed from the box too easily even if it is along the periphery.

There have been proposals for attaining uniform coverage of sensors in a sensor network after deployment. The virtual force algorithm ([26]) computes virtual forces (sensors close to each other repel, and those far apart attract) between sensors at a central location and comes up with optimal node movement to attain required sensor coverage. It is a reasonably straightforward extension to the Decentralized Probabilistic Diffusion protocol to attain a uniform distribution of nodes. Sensors instead of implicitly deciding to move to a neighboring grid box, physically move thus achieving uniform distribution in terms of grid boxes.

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