

# Investigation of Near-Surface Mounted Method for Shear Rehabilitation of Reinforced Concrete T-Beams using CFRP Rods

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## ABSTRACT

This paper presents the results of an investigation of reinforced concrete (RC) T-beams retrofitted in shear with near-surface mounted (NSM) fibre-reinforced polymer (FRP) rods. Six full-scale 4520-mm-long RC T-beams were tested to study the effects of important parameters such as the presence of NSM FRP rods, the presence of steel stirrups, and the steel stirrup ratio. This paper provides an insightful and comprehensive description of the behaviour of strengthened T-beams under increasing load, from the formation of the first crack to ultimate failure. The results of this study and those gathered in the presented database show that existing steel stirrups and strengthening NSM FRP did not diminish each other's effect when failure modes unrelated to shear resistance of RC beams were prevented. The experimental results of this study and those in the database were used to verify a newly proposed model to predict the shear contribution of NSM FRP rods and laminates in RC beams strengthened in shear. The proposed model showed an improved accuracy compared to the existing models in the literature.

**Keywords:** Concrete beams; fibre-reinforced polymers; retrofitting; shear resistance; near-surface mounted; FRP rods; steel stirrups; design model.

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## 22 INTRODUCTION

23 In recent years, fibre-reinforced polymer (FRP) composites as an innovative strengthening and  
24 rehabilitating material have been an attractive topic for practitioners and researchers (e.g.,  
25 Seracino *et al.* 2007a; Kotynia 2007; Rizzo and De Lorenzis 2007; Galal and Mofidi 2009;  
26 Wiwatrojanagul *et al.* 2012; Pellegrino and Vasic 2013; and Mofidi *et al.* 2014). Near-surface  
27 mounted (NSM) FRP rods or laminates have provided a promising solution to the problem of  
28 shear strengthening (e.g., De Lorenzis and Nanni 2001; Barros and Dias 2006; Kotynia 2007). In  
29 this technique, FRP rods or laminates are embedded into pre-cut grooves on the concrete cover in  
30 the webs of RC beams. The idea was originated in 1940s when Asplund (1949) grouted NSM  
31 steel rods to strengthen a bridge slab in flexure. Fifty years later, Blaschko and Zilch (1999) and  
32 Nanni *et al.* (1999) proposed use of NSM FRP rods to rehabilitate RC beams in flexure.

33 Shear strengthening using NSM FRP method was investigated for the first time by De  
34 Lorenzis and Nanni (2001) through six RC beams, focusing on variables such as the spacing of  
35 the rods, the FRP rod inclination angle, the end-anchorage of the FRP rods, and the presence of  
36 internal steel shear reinforcement. In their study, a model was proposed to predict the  
37 contribution of NSM FRP rods for the shear resistance of RC beams. Later, the model was  
38 updated by Parretti and Nanni (2004) to be applicable to NSM FRP laminates in addition to  
39 NSM FRP rods. The model is still the most rational prediction tool proposed for RC beams  
40 strengthened with NSM FRP. However, it lacks a state-of-the-art bond model. The researchers  
41 assumed a constant value of 6.9 MPa as the average bond stress between FRP and concrete in  
42 their design equations. Although the proposed value was deemed practical at the early stages of  
43 the investigations on NSM method, further studies showed that the bond stress between NSM  
44 FRP and concrete is a function of several parameters including concrete strength and cross-

45 sectional dimensions and shape of the NSM FRP material (e.g., De Lorenzis 2004 and Seracino  
46 *et al.* 2006b). Moreover, in their model the effective bond length of the FRP is limited by the  
47 cross-sectional dimensions of the RC beam or the corresponding length to FRP effective strain of  
48 4000  $\mu\epsilon$ . However, further studies showed that the effective bond length of the NSM FRP is  
49 mainly a function of concrete strength, cross-sectional and mechanical characteristics of the FRP  
50 (e.g., Seracino *et al.* 2006).

51 Next group of research studies proposed a constant value for the effective strain of the FRP  
52 in their model. Barros and Dias (2006) conducted an investigation on eight rectangular RC  
53 beams strengthened with NSM FRP strips. The experimental parameters of their studies included  
54 the spacing of the strips, the FRP strips inclination angle, the presence of longitudinal steel  
55 reinforcement, and the presence steel stirrups. In their study, a bond stress of 16.1 MPa and an  
56 effective strain of 0.0059 were assumed to calculate the shear contribution of FRP. Kotynia  
57 (2007) performed eight tests on RC beams retrofitted in shear using NSM laminates. The test  
58 parameters included the inclination and spacing of the FRP laminates. The findings suggested  
59 that the effective strain in NSM FRP could be assumed as 0.0035 to predict the FRP shear  
60 contribution. Anwarul Islam (2009) conducted tests on three RC beams retrofitted in shear with  
61 NSM FRP rods to study the effects of NSM FRP rod spacing and the presence of steel stirrups.  
62 The results suggested that the NSM effective strain should be taken as one-third of the ultimate  
63 strain of the FRP rods in calculating the FRP shear contribution. It is now established that the  
64 effective strain of the FRP is dependent on several parameters including the mechanical  
65 properties, shape, inclination of the NSM FRP and concrete strength (e.g., Dias and Barros  
66 2013). Taking the effective strain of the FRP in the abovementioned studies as a constant value  
67 might not lead to accurate predicted results.

68 Several experimental studies were conducted on different test variables without proposing  
69 separate design equations to predict the behavior of the strengthened specimens. In the  
70 investigation by Rizzo and De Lorenzis (2007), the effectiveness of FRP rods versus FRP strips  
71 was evaluated in addition to the effects of various adhesives, FRP reinforcement inclination  
72 angle, and spacing between FRP reinforcements. Wiwatrojanagul *et al.* (2012) studied the effect  
73 of FRP rod materials (Aramid FRP versus Carbon FRP), the inclination and the spacing of FRP  
74 rods on six shear strengthened RC beams with NSM FRP rods. They concluded that decreasing  
75 the spacing between FRP rods did not necessarily lead to increases in the shear capacity of the  
76 strengthened specimens, since this might lead to concrete cover splitting type of failure mode.  
77 Rahal and Rumaih (2011) investigated the effect of FRP rods inclination, FRP rods end-  
78 anchorage and NSM FRP rods type (FRP versus steel rods) on three 3250 mm-long RC beams.  
79 Extending the NSM rods into one specimen's concrete flange increased the shear resistance and  
80 prevented the concrete cover splitting in the specimen. Cisneros *et al.* (2012) studied the effect of  
81 the inclination, the cross-sectional shape (rods versus strips) and the spacing of the NSM FRP  
82 composites on sixteen test specimens. Raj and Surumi (2012) tested ten shear strengthened  
83 rectangular RC specimens using NSM FRP rods and strips. The test parameters were the FRP  
84 strips/rods inclinations and the spacing between the FRP rods/strips. Jalali *et al.* (2012)  
85 investigated the effectiveness of man-made NSM FRP rods in shear retrofit of five rectangular  
86 RC beams. The spacing of the FRP rods, the FRP rod angle, and the end-anchorage of the FRP  
87 rods were the experimented parameters of their study. Their proposed end-anchorage man-made  
88 FRP rods enhanced the shear resistance and the ductility of the test specimens. Note that most of  
89 RC beams in these studies had a span length shorter than 4 m (small-scale or medium-scale  
90 specimens). Currently, there is a lack of large-scale test specimen in the literature for full-scale

91 RC beams strengthened with NSM FRP. The size effect of RC beams strengthened with NSM  
92 FRP can be particularly important. This is due to the fact that the concrete cover thickness plays  
93 an utterly vital role in beams strengthened with NSM FRP method. The concrete cover thickness  
94 is not proportionately down-scaled compared to the rest of RC beams dimensions for a small- or  
95 medium-scale test specimen.

96         Dias and Barros (2008, 2010, 2011, and 2012) conducted comprehensive series of tests to  
97 strengthen RC beams with NSM FRP laminates. The test variables in their separate studies  
98 included concrete compressive strength, pre-cracking of the specimens, internal steel shear  
99 reinforcement, the spacing of the FRP reinforcement, and the FRP reinforcement angle. Based on  
100 their experimental results, they proposed a new design model for NSM FRP laminates (Dias and  
101 Barros 2013). According to their model, the presence of steel stirrups decreases the effective  
102 strain in NSM FRP laminates. The effective strain in the FRP is calculated based on curve fitting  
103 of the experimental results of their own test as a function of the sum of the rigidity of transverse  
104 steel reinforcement and that of transverse NSM FRP and concrete compressive strength.  
105 Although several studies have pointed out that the presence of steel stirrups has a diminishing  
106 effect on the shear contribution of FRP for RC beams strengthened with Externally-Bonded (EB)  
107 method (e.g., Mofidi and Chaallal 2011; Mofidi *et al.* 2012b; Pellegrino and Vasic 2013; Mofidi  
108 and Chaallal 2014a-b), such effect has not been thoroughly investigated for RC beams  
109 strengthened with NSM FRP method and its occurrence is in doubt.

110         This need is the main impetus of this study to conduct an extensive, comprehensive, and  
111 targeted experimental investigation involving six full-scale 4520-mm-long T-beams with  
112 different steel shear reinforcement ratios. The results of this study (and those available in  
113 literature) have been used to study the mechanism of shear resistance for RC beams strengthened

114 with NSM FRP and investigate a possible interaction between steel and FRP shear  
115 reinforcement. Moreover, a reliable design method have been proposed for shear strengthening  
116 of RC beams with NSM FRP rods and laminates that uses a state-of-the-art bond model and can  
117 predict possible failure modes. The accuracy of the predicted results have been verified using  
118 collected experimental data from the published studies on shear strengthening of RC beams  
119 using NSM FRP composites and compared with the results predicted by aforementioned design  
120 models proposed by other researchers.

121

## 122 **EXPERIMENTAL PROGRAM**

### 123 **Description of specimens**

124 The experimental program involved six tests performed on full-scale, 4520-mm-long RC  
125 T-beams (Table 1). The T-section had overall dimensions of 508 mm (flange width) by 406 mm  
126 (total depth). The thicknesses of the web and flange were 152 and 102 mm respectively (Fig. 1).  
127 The control specimens not strengthened with carbon FRP (CFRP) rods were labelled as CON.  
128 The specimens labelled as NR were RC T-beams with no internal transverse-steel stirrups. The  
129 specimens labelled as MR (moderately reinforced with internal transverse-steel reinforcement)  
130 and HR (heavily reinforced with internal transverse-steel reinforcement) had steel stirrups spaced  
131 at  $s = 3d/4$  for MR and  $s = d/2$  for HR, where  $d = 350$  mm was the effective depth of the beam  
132 cross-section. The specimens in this study are representative of RC elements designed prior to  
133 modern codes and therefore the beams in the HR series are qualified as heavily reinforced. In  
134 addition, the maximum steel stirrup spacing values proposed by modern codes,  $0.5d$  in ACI 318-  
135 11 or  $0.7d_v$  in A23.3-14 (where  $d_v$  is the greater of  $0.9d$  or  $0.72h$ ,  $h$  is the height of the member)  
136 are for design and field practice to avoid brittle shear failure. This limit, however, is conservative

137 for shear strengthening research purposes. The specimens strengthened with NSM were labelled  
138 as NSM. The spacing between the NSM FRP rods was 130 mm for all the strengthened  
139 specimens.

140 The longitudinal steel reinforcement consisted of four 25M bars (diameter 25.2 mm, area  
141  $500 \text{ mm}^2$ ) laid in two layers at the bottom and six 10M bars (diameter 10.3 mm, area  $100 \text{ mm}^2$ )  
142 laid in one layer at the top. The bottom bars were anchored at the support with 90-degree hooks  
143 to prevent premature anchorage failure. The steel stirrups (where applicable) were 8 mm in  
144 diameter (area  $50 \text{ mm}^2$ ). The longitudinal steel reinforcement had a nominal yield strength of  
145 470 MPa for the NR and HR series and 650 MPa for the MR series. The steel stirrups had a  
146 nominal yield strength of 540 MPa for the HR series and 650 MPa for the MR series.

147 A commercially available concrete delivered to the laboratory by a local supplier was used.  
148 The specimens were cast in two phases using separate concrete batches of the same mix design  
149 and supplier. NR-CON, HR-CON, NR-NSM, and HR-NSM specimens were cast in the first  
150 phase and MR-CON and MR-NSM specimens in the second phase. Standard compression tests  
151 on control cylinders yielded an average 28-day concrete compressive strength of 25.0 MPa and  
152 29.6 MPa for the first and second phases respectively. For each concrete batch, the scatter among  
153 the compression test results for the cylinder specimens was negligible.

154 To apply the NSM FRP shear strengthening system, the following steps were performed:  
155 (1) grooves of 15 mm width and 15 mm depth and spaced at 130 mm were made on both lateral  
156 sides of the beam; (2) the grooves were cleaned by compressed water and air; (3) two-third of the  
157 grooves' volume was filled with epoxy blended according to the supplier's recommendations; (4)  
158 a thin layer of the supplier's epoxy adhesive was applied around the 9.5-mm-diameter CFRP

159 rods; (5) the 9.5-mm-diameter CFRP rods were installed into the groove on both sides of the  
160 beam; and (6) the excess epoxy adhesive was removed.

161 Sand-coated CFRP rods were used to strengthen the RC T-beams. The tensile strength,  
162 elongation at break, and modulus of elasticity of the sand-coated CFRP rods were 1885 MPa,  
163 1.27% and 148 GPa respectively. The reported results are the mean values of several test results  
164 conducted on the steel bars, concrete specimens and CFRP rods. The mechanical properties of  
165 the adhesive as specified by the manufacturer were: 21 MPa bond strength, 1% elongation at  
166 break, 75 MPa compressive strength, and 3656 MPa compressive modulus.

167

### 168 **Test setup and instrumentation**

169 All T-beam specimens were tested in a simply supported three-point bending  
170 configuration, as shown in Fig. 1. The load was applied at a distance  $a = 3d$  from the nearest  
171 support, which corresponds to the case of a slender beam in which the shear resistance is  
172 governed by the beam action mechanism. The vertical displacement of the beam was measured  
173 at the position under the applied load using linear variable differential transducers (LVDT, 150  
174 mm measuring range). The longitudinal steel reinforcement was instrumented with a strain gauge  
175 at the point of loading. Strain gauges were also installed on the transverse-steel stirrups located  
176 in the loading zone along the anticipated plane of shear failure. The deformations experienced by  
177 the CFRP rods were measured using strain gauges installed on the rods. These gauges were  
178 attached vertically to the CFRP rods before the rods were epoxy-bonded into the pre-cut grooves.  
179 The maximum strain range of the strain gauges used in this study was 2% per manufacturer's  
180 data.

181



## 182 **EXPERIMENTAL RESULTS**

### 183 **Overall response**

184 Table 2 summarizes the overall experimental results obtained from the tests for all  
185 specimens. The results are presented in terms of the loads attained at failure, the experimental  
186 shear resistance due to concrete, steel stirrups, and CFRP, and the percent shear capacity gain  
187 due to CFRP, defined as  $(V_f)/(V_{total} - V_f)$ , where  $V_{total}$  is the total load at failure. In deriving some  
188 of the values in Table 2, the following assumptions were made: (a) the shear resistance due to  
189 concrete was the same whether or not the beam was retrofitted in shear with FRP and whether or  
190 not the retrofitted beam was reinforced with transverse steel; and (b) the contribution of steel  
191 stirrups was the same for both strengthened and unstrengthened beams.

192

### 193 **Crack Pattern and Failure Mode**

194 The load level at which the first diagonal shear crack occurred was of similar magnitude  
195 for all specimens. During the loading of control specimen NR-CON (unstrengthened and with no  
196 steel stirrups), diagonal shear cracks initiated at the centre of the shear span at a load of 78.8 kN.  
197 As the load increased, only one crack widened and propagated until final failure, which occurred  
198 at a load level of 122.7 kN. An MR-CON beam (unstrengthened but with steel stirrups spaced at  
199 260 mm) experienced the first diagonal shear crack at a load (79.2 kN) similar to that in NR-  
200 CON, but the final failure occurred at a much higher load (294.0 kN) due to rupture of a steel  
201 stirrup. An HR-CON beam (with steel stirrups spaced at 175 mm) showed similar behaviour,  
202 with the ultimate load reaching 350.6 kN, also due to rupture of a steel stirrup.

203 Among the NSM-strengthened specimens, beam NR-NSM (no steel stirrups, but retrofitted  
204 with 9.5-mm-diameter NSM vertical rods spaced at 130 mm) failed when the load reached 198.0

205 kN. This corresponds to a 61% increase in shear capacity with respect to the control beam, NR-  
206 CON. Only one diagonal shear crack formed in this beam at an angle of  $47^\circ$ , widening and  
207 propagating as the applied load increased. A popping noise was noted throughout the test,  
208 revealing the progressive cracking of the specimen. This caused splitting of the concrete cover in  
209 which two thick layers of concrete cover (including the NSM FRP rods) split off from the sides  
210 of the beam. After losing the NSM rods (no bond stress transfer between FRP and concrete), the  
211 beam finally failed in a diagonal tension failure mode.

212 For specimens with steel stirrups and strengthened with NSM (i.e., MR-NSM and HR-  
213 NSM), parallel diagonal cracks started to open up at relatively equal spacing and at an angle of  
214  $43^\circ$  to  $47^\circ$  with respect to the beam axis. Figure 2 shows the spacing between these shear cracks  
215 in specimen MR-NSM at failure, where the ultimate load reached 380.0 kN, which is 29.2%  
216 greater than the capacity of the corresponding control beam MR-CON. The final failure was in  
217 shear due to concrete-cover splitting (Fig. 2). For beam HR-NSM, the ultimate load was 365.0  
218 kN, which was 4% greater than the capacity of the corresponding control beam HR-CON before  
219 the global flexural failure mode occurred.

220

## 221 **Deflection response**

222 Figure 3 shows the curves representing load versus maximum deflection at the loading  
223 point for all specimens. The quasi-linear behaviour of curves corresponding to the control beams  
224 and NR-NSM specimens is characteristic of a typical shear failure. It can be seen that the NSM  
225 method generally enhanced the overall behaviour of the RC beams. Compared to the  
226 unstrengthened control specimens, the strengthened T-beams had higher ultimate loads at failure  
227 (61%, 29%, and 4% for NR-NSM, MR-NSM, and HR-NSM respectively) and greater maximum

228 deflections (234%, 4%, and 10% for NR-NSM, MR-NSM, and HR-NSM respectively) compared  
229 to their corresponding control specimens. All the tested beams except HR-NSM exhibited a  
230 brittle type of behaviour, which was characterized by a sudden drop in the load-displacement  
231 curves after the peak load (Fig. 3). In contrast, beam HR-NSM showed a ductile behaviour and  
232 failed in flexure.

233

### 234 **Strain response**

235 To obtain a better understanding of the shear resistance mechanism in the strengthened  
236 beams, extensive instrumentation was installed for strain monitoring, especially in steel stirrups  
237 and NSM rods.

238 *Transverse-steel reinforcement* — Figure 4 presents the response of applied load versus  
239 maximum measured strain in the transverse-steel stirrups for the MR and HR series that  
240 contained steel stirrups. These behaviour curves indicate that the steel stirrups went through three  
241 phases during loading. In the initial phase (phase “A”), no noticeable contribution of the  
242 transverse steel to shear resistance was observed. In the second phase (phase “B”), the first  
243 diagonal cracks initiated, and the steel stirrups started to contribute to shear resistance. This  
244 phase started at an average applied load of approximately 75.0 kN for most specimens (Fig. 4).  
245 This is close to the failure load of the unreinforced control specimen (NR-CON) at 78.8 kN and  
246 the crack opening load of the control specimen with steel stirrups (MR-CON) at 79.2 kN.  
247 Therefore, the ending load of phase “A” (starting load of phase “B”) is considered as the  
248 cracking load of the concrete specimens in this study. After Phase B (in the third phase), the  
249 strain in the steel stirrups continued to increase with increasing load at a greater rate than in the  
250 second phase until ultimate failure of the specimen. It was also found that the maximum strain in

251 the steel stirrups that intercepted the principal shear crack became greater than the yielding strain  
252 (as labelled in Fig. 4) by a significant margin before the specimen failed.

253 Figure 4 also shows that, under the same applied load, the strain level in the steel stirrups  
254 was substantially greater in the unstrengthened control specimens with no CFRP. This implies  
255 that the presence of NSM CFRP eased the strain in the transverse-steel stirrups. Moreover,  
256 yielding of the steel stirrups occurred earlier in specimens with wider spacing between steel  
257 stirrups (MR series) than in beams with tighter spacing between steel stirrups (HR series),  
258 although in MR series the yield point of the stirrups was greater than that of HR series (i.e., 650  
259 MPa versus 540 MPa).

260 *NSM CFRP rods* — Figure 5 shows the load versus maximum measured strain behaviour in the  
261 NSM CFRP rods in the strengthened specimens. The maximum strain was measured in the NSM  
262 rods that intercepted the major shear crack on both sides of the RC beams. Note that all the strain  
263 values reported in this paper are the maximum measured (captured) values. They are not  
264 necessarily the absolute maximum values experienced by the NSM rods (i.e., in cases where the  
265 strain gauges did not intercept the principal cracks). The curves in Fig. 5 display a similar  
266 tendency to those for steel stirrups, except for the last phase. The CFRP rods did not make much  
267 contribution during the initial stage (Phase “A”) of loading, but began to stretch at an applied  
268 load of 100.0 kN on average for all three series. In the last stage, however, the CFRP strain  
269 started to decrease, drastically at times, as the load increased (e.g., HR-NSM-Right, where the  
270 curve shows a reversing portion, indicating a strain decrease in the FRP with increasing load).  
271 This strain decrease can be related to local concrete cover splitting which reduced the shear  
272 transfer between the NSM FRP and the RC beams’ concrete core, accompanied by concrete  
273 cracking noises in the beams during loading.

## 274 **Behaviour of Strengthened RC Beams under Increasing Load**

275 The local behaviour of steel stirrups and NSM rods, particularly within the failure zones, is  
276 next discussed and analyzed in depth. To enhance the reliability of the results, the measured  
277 strain gauge data are further compared with associated crack formation and with patterns that are  
278 closely related to one another.

### 279 *Analysis of Steel Stirrup Behaviour at Failure*

280 Figure 6 shows the measured strain distribution at failure among the steel stirrups (S1-S4)  
281 for series MR and HR. The strain curves in solid black bars on the stirrups are drawn to scale. A  
282 horizontal line near the bottom of the beam indicates the yield point of the steel stirrups (MR:  $\varepsilon_y$   
283 = 0.0033; HR:  $\varepsilon_y$  = 0.0027). The inclination of the plane of rupture is assumed to be equal to the  
284 principal crack angle with respect to the longitudinal axis as measured at the end of the test.  
285 Although the cracking pattern in some specimens was distributed throughout the shear span, the  
286 principal shear crack was taken as the crack that passed through the entire cross section of the  
287 beams and led to ultimate shear failure. In addition to the strain at ultimate failure in each stirrup,  
288 Fig. 6 also shows the applied forces corresponding to the yield point ( $F_{yield}$ ) of each stirrup at the  
289 bottom of each beam (stacked bars). These loads are reported as a percentage of ultimate load  
290 ( $F_{ultimate}$ ) reached. The number beside each yielded stirrup indicates its sequence of yielding.  
291 Based on Fig. 6, the following observations can be made:

292 1. In general, the stirrups crossing the principal shear crack were highly strained. Yielding  
293 of the steel stirrups was observed in all cases.

294 2. For the unstrengthened control specimens (MR-CON and HR-CON), the stirrup located  
295 in the critical section yielded first, followed by the other stirrups. This corroborates the  
296 observation that the first diagonal crack appeared in the beam web, midway between the support

297 and the load application point. As the load increased, these cracks became wider and progressed  
298 simultaneously toward both the support and the load point. For the strengthened specimens (MR-  
299 NSM and HR-NSM), the first steel stirrup to yield was not located in the plane of ultimate  
300 failure. Proper strengthening of the specimens resulted in formation of concrete struts throughout  
301 the shear span of the RC beams, leading to a distributed cracking pattern. In this case, the first  
302 shear crack that caused the first steel stirrup to yield was not necessarily the principal shear crack  
303 that led to ultimate shear failure, e.g., stirrup S4 yielded first in specimen MR-NSM, but the  
304 principal shear crack passed through stirrup S3. Similar behaviour was observed in specimen  
305 HR-NSM, where stirrup S3 yielded first, but the principal shear crack passed through stirrup S2.

306         3. For the unstrengthened control specimens, yielding of steel stirrups began under a load  
307 much less than ultimate load, starting at 69% and 81% of ultimate force for specimens MR-CON  
308 and HR-CON respectively. On the other hand, for NSM-strengthened beams, yielding of steel  
309 stirrups occurred under higher shear loads, between 94% and 100% of ultimate load. This means  
310 that the presence of NSM FRP rods delayed yielding of steel stirrups. However, after stirrup  
311 yielding, the residual capacity of the specimens became minimal, if not negligible.

312         4. For specimen MR-CON, the strain in the steel stirrups was not well distributed (only  
313 stirrups S2 and S3 that intercepted the principal shear crack were significantly strained). This  
314 could have been due to the wider spacing between steel stirrups (260 mm) in this specimen,  
315 which allowed the major shear crack to pass through the concrete cross section under a lower  
316 applied force than in the HR-CON specimen, which had a stirrup spacing of 175 mm. For the  
317 NSM-strengthened specimens (MR-NSM and HR-NSM), strengthening using NSM led to  
318 formation of concrete struts throughout the specimens' shear spans. This resulted in a much more

319 even strain distribution among the steel stirrups in the strengthened beams (e.g., MR-NSM) than  
320 in the unstrengthened ones (e.g., MR-CON).

### 321 *Analysis of NSM FRP Rod Behaviour at Failure*

322 The distribution of maximum strain attained by the NSM CFRP rods (F1-F5) on both sides  
323 of the RC beams is shown in Fig. 7 for the three NSM-strengthened specimens. The clustered  
324 bars on each side of the FRP rods (labelled as L and R) are drawn to scale. The applied forces  
325 corresponding to the maximum strain on the FRP ( $F_{\epsilon-max}$ ) are also indicated at the bottom of each  
326 beam's figure (stacked bars) in terms of a percentage of ultimate force reached ( $F_u$ ). The  
327 following observations were made based on Fig. 7:

328 1. Similarly to the strain in steel stirrups, the NSM FRP rods crossing the principal shear  
329 crack were strained the most. The maximum strain in CFRP rods was generally greatest in the  
330 middle of the failure zone where the first diagonal cracks initiated and propagated  
331 simultaneously towards the support and the compression flange. This non-uniform strain  
332 distribution in the CFRP rods over the failure zone shows the importance of the CFRP anchorage  
333 length available, which was less for the NSM rods at both ends than for rods in the middle of the  
334 failure zone.

335 2. In specimen NR-NSM, although the strengthening NSM FRP proved very effective, the  
336 strain in the FRP rods was not well distributed with respect to the shear span. This could have  
337 been due to the absence of internal steel stirrups, which prevented proper formation of concrete  
338 struts across the shear span. Only NSM rods F3 and F4, which intercepted the principal shear  
339 crack, were significantly strained. The rest of the FRP rods did not efficiently contribute to shear  
340 resistance. This occurred because the specimen failed in a single-crack pattern which did not  
341 intercept FRP rods F1, F2, or F5. These NSM rods reached their maximum strain under a lower

342 load (i.e., they stopped contributing to shear resistance before ultimate failure) compared to the  
343 rest of the NSM rods. However, in specimens MR-NSM and HR-NSM, shear strengthening of  
344 specimens with NSM FRP resulted in a better strain distribution with respect to the shear span  
345 than that in the unreinforced specimen (NR-NSM). This could have been due to formation of  
346 concrete struts throughout the specimens' shear spans.

347 3. Some of the NSM rods in the critical zone that were significantly strained reached their  
348 maximum strain level under a load less than the maximum load at failure (e.g., F2 in MR-NSM  
349 and F3 in HR-NSM). This could have been due to local cracks in the concrete cover or to local  
350 debonding of NSM rods that stopped shear transfer between the NSM CFRP rods and the  
351 surrounding concrete prior to ultimate failure.

#### 352 *Effect of Steel Shear Reinforcement on the Contribution of NSM FRP to Shear Resistance*

353 One of the test parameters of the current study is this effect of transverse-steel shear  
354 reinforcement on the FRP contribution of RC beams strengthened with NSM FRP for shear  
355 resistance. For specimens NR-NSM (no transverse reinforcement) and MR-NSM (moderate  
356 transverse reinforcement), Table 2 shows that the FRP shear contribution slightly increased  
357 instead of decreasing in the presence of steel stirrups (i.e., 56.9 kN for MR-NSM versus 49.8 kN  
358 for NR-NSM). In other words, the presence of steel stirrups did not diminish the NSM FRP's  
359 shear contribution. Unlike in the EB FRP method, the highly stressed areas around NSM FRP do  
360 not significantly overlap/interact the highly stressed areas around the existing steel stirrups. This  
361 is mainly due to the fact that the location of the NSM FRP rods is generally taken with distance  
362 away from the location of steel stirrups to avoid possible damage to the steel stirrups during  
363 groove cutting for NSM FRP. Therefore, the bond quality between the NSM FRP and the  
364 concrete is not compromised by the presence of the steel stirrup. Note that in the specimens with



365 steel stirrups (MR-CON, HR-CON, MR-NSM, and HR-NSM), shear failure occurred after the  
366 steel stirrups intersecting the principal crack had yielded (i.e., the steel contribution to shear  
367 resistance was not affected by the presence of the strengthening FRP). Therefore, similar  
368 equations can be used to calculate the shear contribution of steel for both unstrengthened and  
369 strengthened specimens.

370 In order to better investigate this effect with more experimental results, a database of more  
371 than 69 RC beams strengthened with NSM FRP rods and laminate that failed due to NSM FRP  
372 strengthening system failure (debonding or concrete cover splitting) was collected (Table 3). The  
373 database includes most of the relevant data in the existing literature of the tested beams  
374 strengthened with NSM FRP including the geometric properties of the test specimens and of the  
375 FRP composites, the elastic and mechanical properties of the materials used, and the load at  
376 failure ( $V_{total}$ ), and the contribution of the FRP to shear resistance ( $V_f$ ).

377 Fig. 8 displays the FRP shear contribution for NSM-strengthened RC beams versus the  
378 internal steel stirrup reinforcement ratios,  $\rho_{sv} = (A_{sv}) / (b_w \times s)$ , where  $A_{sv}$  and  $s$  are the total area of  
379 the cross-section and the spacing of the transverse steel reinforcement. Fig. 8 clearly shows that  
380 the shear contribution of FRP did not decrease (in fact slightly increased when considering a  
381 linear trend line) with the increase in the shear transverse reinforcement ratio. Furthermore, in  
382 order to normalize the shear contribution of FRP for RC beams with different cross-sectional  
383 dimensions, the variations of the strengthening factor  $\kappa_f$  versus the increases in  $\rho_{sv}$  is represented  
384 in Fig. 9. The FRP strengthening factor  $\kappa_f$  is defined as  $(V_f) / (V_{max})$ , where  $V_{max} = 0.25f'_c b_w d_v$  is  
385 the maximum shear resistance of the cross-section based on CSA A23.3-14. Fig. 9 reveals that  
386 the FRP strengthening factor slightly increases when the steel shear reinforcement ratio  
387 increases. It can be concluded that unlike EB FRP method, the presence of the internal steel

388 shear reinforcement does not influence the contribution of FRP to the shear resistance for shear-  
389 strengthened RC beams with NSM FRP method. These results are in correlation with the  
390 experimental results of this study and those reported by De Lorenzis and Nanni (2001) among  
391 others.

392

### 393 **PROPOSED SHEAR DESIGN EQUATIONS**

394 For practical design purposes, a design model is proposed in this paper for RC beams  
395 strengthened in shear using NSM FRP rods and laminates, which can predict possible failure  
396 modes including debonding of FRP and concrete-cover splitting.

397

#### 398 **Description of model**

399 For RC beams strengthened with NSM FRP rods and laminates, the FRP contribution to  
400 shear resistance can be written in the following form (Kotynia 2007, Anwarul Islam 2009, Jalali  
401 *et al.* 2012):

$$402 \quad V_f = \frac{A_f \cdot E_f \cdot \varepsilon_{fe} \cdot d_{fv}}{s_f} \quad (1)$$

403 where  $A_f$ ,  $E_f$ ,  $d_{fv}$ ,  $\varepsilon_{fe}$ , and  $s_f$  are respectively the FRP cross-sectional area on both sides of the  
404 beam, the FRP rod or laminate modulus of elasticity, the effective shear depth of the cross-  
405 section, the effective strain in the FRP rod or laminate, and the spacing between the NSM FRP  
406 rods or laminates. The effective shear depth can be taken as the greater of  $0.72h$  and  $0.9d$  as per  
407 CSA/S806 (2012). The FRP effective strain is the average of the maximum strain experienced by  
408 the actively involved FRP rods or laminates at the ultimate point. Precise predictions of effective  
409 strain for all potential failure modes of the specimen constitute an important step towards  
410 achieving accuracy in calculating the FRP shear contribution at the ultimate loading stage. The

411 corresponding FRP effective strain at the ultimate point due to the applicable failure mode  
412 should be evaluated on each side of the major shear crack. Because failure occurs on the side of  
413 the crack with the lesser effective strain corresponding to an applicable failure mode, the value of  
414 the lesser effective strain is the governing effective strain and should be used in Eq. (1) to  
415 calculate the FRP contribution to shear resistance.

#### 416 *Failure due to Debonding of NSM FRP at the Concrete/Epoxy Interface*

417 Debonding of NSM FRP is a common failure mode for RC beams strengthened using  
418 NSM FRP (De Lorenzis and Nanni 2001; Rizzo and De Lorenzis 2007). According to previous  
419 experimental pull-off tests on NSM FRP plates, debonding at the concrete/epoxy interface has  
420 been the major failure mode among all the failure modes considered (Blaschko 2003; Seracino *et*  
421 *al.* 2007a). Failure at the concrete/epoxy interface is characterized by cracking in the concrete  
422 layer adjacent to the epoxy-bonded layer. The FRP ultimately debonds from the concrete surface  
423 with a thin layer of concrete (in some cases, only mortar with no aggregate attached to the FRP).  
424 According to Seracino *et al.* (2007b), the pull-off force ( $P_{fb}$ ) of the CFRP laminate at the  
425 concrete/epoxy interface (failure by cracking in the concrete layer adjacent to the epoxy-bonded  
426 layer) can be calculated as follows:

$$427 \quad P_{fb} = 0.85\varphi_f^{0.25} \cdot f_c'^{0.33} \sqrt{L_{per} E_f A_f} \quad (2)$$

428 where units of Newtons and millimetres are used,  $\varphi_f$  is the debonding-failure plane aspect ratio  
429 and is equal to  $(d_f)/(b_f)$ ;  $b_f$  is the length of the failure plane parallel to the concrete surface (at the  
430 FRP/concrete interface), which for NSM laminates and rods is taken to be the width of the  
431 groove plus 2 mm; and  $d_f$  is the length of the failure plane perpendicular to the concrete surface,  
432 which for NSM plates is taken to be the depth of the groove plus 1 mm, where width and depth  
433 of the groove in the current study are taken equal to 1.5 times the rod diameter (based on pull-off

434 tests of Wiwatrojanagul *et al.* 2012). The other important parameter in Eq. (2) is  $L_{per}$ , which is  
 435 the debonding failure plane in cross section and was set equal to  $(2d_f + b_f)$  under the assumption  
 436 that the effective bond length ( $L_{ef}$ ) of the FRP plates or rods was fully available. However, for  
 437 RC beams strengthened in shear with NSM FRP, the effective length of the FRP might not  
 438 always be physically available. The effective bond length is the length beyond which any  
 439 increase in bond length does not translate into an increase in bond force. The pull-off force of the  
 440 NSM FRP at the concrete/epoxy interface is a linear function of the embedment length of NSM  
 441 FRP rods on both sides of the major crack, where the effective bond length represents the upper  
 442 bound of FRP bond length (Seracino *et al.* 2007a). According to Seracino *et al.* (2007b), the  
 443 effective bond length of the NSM FRP plates is given by:

$$444 \quad L_{ef} = \left( \frac{\pi}{2\lambda} \right) \quad (3)$$

$$445 \quad \lambda^2 = \left( \frac{\tau_{max} L_{per}}{\delta_{max} E_f A_f} \right) \quad (4)$$

446 where

$$447 \quad \tau_{max} = (0.802 + 0.078\phi_f) f_c'^{0.6} \quad (5)$$

$$448 \quad \delta_{max} = \left( \frac{0.976\phi_f^{0.526}}{0.802 + 0.078\phi_f} \right) \quad (6)$$

449 where units of Newtons and millimetres are used,  $\lambda$  is a constant, and  $\tau_{max}$  and  $\delta_{max}$  are  
 450 respectively the maximum shear stress and the maximum slip, assuming a bilinear bond-slip  
 451 relationship at the concrete/epoxy interface. The maximum shear stress and maximum slip were  
 452 calculated on the basis of an empirical equation extracted from a statistical analysis (Seracino *et*  
 453 *al.* 2007a).

454 As mentioned earlier, in many shear-strengthening field cases, the effective length of the  
 455 FRP might not always be physically available. For this case, a modification factor ( $k_{ef}$ ) is  
 456 proposed in this study to account for the effect of effective bond length in calculating the  
 457 corresponding maximum FRP strain for the debonding failure mode, i.e.,

$$458 \quad k_{ef} = \left( \frac{k_g L_{total}}{L_{ef}} \right) \quad (7)$$

459 where  $k_g$  is an experimental coefficient to consider the group effect (the original bond model was  
 460 calibrated for single NSM FRP bonded to concrete blocks) for all active NSM FRP rods and  
 461 laminates ( $k_g$  is taken equal to 0.75 and 0.50 for rods and laminates, respectively),  $L_{total}$  is the  
 462 total length of the NSM FRP rods or laminates that are actively contributing to shear resistance  
 463 (i.e., intersecting the principal shear crack with proper bond length on both sides of the crack) at  
 464 ultimate failure. Therefore,  $L_{total}$  is the sum of the shorter parts of all NSM FRP rods or laminates  
 465 that pass the 45 degrees major shear crack (as illustrated in Fig. 10 for a template cross-sectional  
 466 size and NSM FRP spacing), where the upper bound of the shorter part of NSM FRP rods or  
 467 laminates is  $L_{ef}$ . In Fig. 10,  $L_1$  is the dimension of the shorter part of the first NSM FRP that  
 468 passes the shear crack.  $L_2$  and  $L_3$  are the dimensions of the shorter parts of the second and the  
 469 third NSM FRP that pass the shear crack, the dimensions of which are limited by the upper  
 470 bound, i.e.,  $L_{ef}$ .  $L_4$  is the dimension of the shorter part of the last NSM FRP and is represented by  
 471 term  $r_f$  in the general form calculations below. The total length,  $L_{total}$ , is indeed a parameter  
 472 dependent on beam size ( $d_{fv}$ ), NSM FRP spacing ( $s_f$ ), and effective length of NSM FRP rods or  
 473 laminates ( $L_{ef}$ ).  $L_{total}$  can be calculated for different scenarios as follows:

474 (1) If  $\frac{d_{fv}}{2} < L_{ef}$ :

475  $L_{total} = \left( [n_f] - \left\lfloor \frac{n_f}{2} \right\rfloor \right) \cdot r_f + s_f \cdot \left\lfloor \frac{n_f}{2} \right\rfloor \cdot \left( \left\lfloor \frac{n_f}{2} \right\rfloor + 1 \right) = \left( \left\lfloor \frac{n_f}{2} \right\rfloor + 1 \right) \times \left( r_f + s_f \left\lfloor \frac{n_f}{2} \right\rfloor \right) : [n_f] \text{ is an odd number (8)}$   
 476

477  $L_{total} = \left( [n_f] - \left\lfloor \frac{n_f}{2} \right\rfloor \right) \cdot r_f + s_f \cdot \left\lfloor \frac{n_f}{2} \right\rfloor^2 = \left\lfloor \frac{n_f}{2} \right\rfloor \times \left( r_f + s_f \left\lfloor \frac{n_f}{2} \right\rfloor \right) : [n_f] \text{ is an even number (9)}$   
 478

479 where  $[n_f]$  and  $\left\lfloor \frac{n_f}{2} \right\rfloor$  are the integer parts of  $\left( \frac{d_{fv}}{s_f} \right)$  and  $\left( \frac{d_{fv}}{2s_f} \right)$ , respectively, and  $r_f = d_{fv} - s_f$

480  $[n_f]$ .

481 (2) If  $\frac{d_{fv}}{2} \geq L_{ef}$  :

482 
$$L_{total} = \left( \frac{d_{fv} - 2L_{ef}}{s_f} + 1 \right) \cdot L_{ef} + \left\lfloor \frac{n'_f}{2} \right\rfloor \times \left( r'_f + s_f \cdot \left\lfloor \frac{n'_f}{2} \right\rfloor \right) \quad (10)$$

483 where  $[n'_f]$  and  $\left\lfloor \frac{n'_f}{2} \right\rfloor$  are the integer parts of  $\left( \frac{2L_{ef}}{s_f} \right)$  and  $\left( \frac{L_{ef}}{s_f} \right)$ , respectively, and

484  $r'_f = 2L_{ef} - s_f \cdot [n'_f]$ .

485 Consequently, the effective FRP strain corresponding to NSM FRP debonding at the  
 486 concrete/epoxy interface, ( $\epsilon_{ef-b}$ ), can be written as:

487 
$$\epsilon_{ef-b} = \frac{0.4k_{ef} \cdot \varphi_f^{0.25} \cdot f'_c{}^{0.33} \sqrt{L_{per}}}{\sqrt{E_f A_f}} \quad (11)$$

488 Note that the equations proposed in this paper are for vertical NSM FRP rods. The  
 489 corresponding equations for inclined NSM FRP rods and laminates will be presented in a  
 490 separate study by the authors.

491

492 *Failure due to Concrete-Cover Splitting*

493 Concrete-cover splitting at the RC beam's web for specimens shear-strengthened with  
494 NSM FRP occurs entirely in the concrete when the stresses in the failure zone reach the concrete  
495 tensile strength. This failure mode can be expected more often in specimens with weak concrete  
496 and tightly spaced NSM FRP. In an experimental study to investigate the bond behaviour of  
497 NSM FRP laminates bonded to concrete blocks, Seo *et al.* (2012) proposed a concrete-cover  
498 splitting model for grouped NSM FRP bonded to concrete. According to their model, the  
499 concrete splitting capacity for NSM FRP laminates bonded to concrete blocks ( $P_{fc}$ ) can be  
500 calculated as follows:

501 
$$P_{fc} = 0.57\beta\sqrt{f'_c}A_{cf} \quad (12)$$

502 Where  $f'_c$ ,  $\beta$ , and  $A_{cf}$  are respectively the compressive strength of concrete in MPa, an experimental  
503 coefficient equal to 0.7, and the surface area of splitting failure of concrete in mm<sup>2</sup>. Seo *et al.* (2012)  
504 proposed an equation to calculate the concrete surface area of splitting failure for one NSM FRP  
505 laminate as follows:

506 
$$A_{cf} = 2w_f\sqrt{L_{mb}^2 + b_{e1}^2} + L_{mb}(t_f + b_{e1}) \quad (13)$$

507 where  $w_f$ ,  $t_f$ ,  $L_{mb}$ , and  $b_{e1}$ , are the width, thickness, embedment length of FRP laminates and  $b_{e1}$  is  
508 taken equal to  $0.3L_{mb}$ . In this study,  $A_{cf}$  is modified to consider the effect of all active NSM FRP  
509 rods or laminates in concrete cover splitting failure for RC beams strengthened in shear with NSM  
510 FRP as follows:

511 
$$A_{cf} = L_{total}(2w_f + 0.3L_{mb} + t_f) \quad \text{for FRP plates} \quad (14)$$

512 
$$A_{cf} = L_{total}(3D_f + 0.3L_{mb}) \quad \text{for FRP rods} \quad (15)$$

513 where the embedment length can be taken equal to minimum of  $L_{eff}$  and  $\left(\frac{d_{fv}}{2 \sin \alpha}\right)$ . Hence, the  
 514 concrete-cover splitting force can be used to calculate the FRP effective strain corresponding to the  
 515 concrete-cover splitting failure mode as follows:

$$516 \quad \varepsilon_{fe-c} = \frac{0.4\sqrt{f'_c}A_{cf} \cdot s_f}{A_f \cdot E_f \cdot d_f} \quad (16)$$

517 Note that the effective strain in the NSM FRP rods or laminates at ultimate load can be  
 518 taken as the minimum of the strain due to NSM FRP debonding at the split between the  
 519 concrete/epoxy interface and the concrete cover, i.e.,

$$520 \quad \varepsilon_{fe} = \min(\varepsilon_{fe-b}, \varepsilon_{fe-c}) \quad (17)$$

521

## 522 **Verification of the proposed design equations**

523 The experimental contributions of FRP to shear resistance of the retrofitted specimens in  
 524 this study are compared with the shear resistance predicted by the proposed equations (Table 4).  
 525 The calculated values of effective strain developed in the NSM FRP rods corresponding to each  
 526 failure mode are shown in Table 4. The governing failure mode can thus be identified. The FRP  
 527 shear contribution is then calculated based on the critical effective strain of the governing failure  
 528 mode. Finally, the experimental results of this study are compared to the results calculated using  
 529 the proposed equations (Table 4). For specimens NR-NSM and MR-NSM, the governing shear  
 530 failure mode according to the calculation is concrete-cover splitting, where the calculated FRP  
 531 shear contribution ( $V_{f-g}$ ) for these specimens was 47.8 and 52.0 kN respectively. The  
 532 experimental FRP shear contribution for these two specimens is 49.8 and 56.9 kN respectively,  
 533 resulting in a calculated  $V_f$  to experimental  $V_f$  ratios of 0.96 and 0.91 respectively. This indicates



534 a fairly accurate and conservative prediction by the proposed equations compared with  
535 experimental results.

536 To further assess the validity of the proposed theoretical predictions, test results from the  
537 database are also used (Table 3). The 69 specimens presented in Table 3 all failed due to  
538 debonding of NSM FRP or concrete cover splitting (the results of specimens failed with no  
539 major contribution of NSM FRP to the shear resistance, those of specimens failed due to  
540 unrelated failure modes to the shear resistance, and those of specimens with special anchorage of  
541 NSM FRP is not presented here). The accuracy of the predicted contributions of FRP to the shear  
542 resistance by the proposed model is compared to that of the existing design equations in  
543 literature proposed by De Lorenzis and Nanni (2001), Kotynia (2007), Anwarul Islam (2009),  
544 and Dias and Barros (2013). Figures 11(a) to 11(e) show the  $V_{f\text{ cal}}$  values calculated using the  
545 proposed model and each of the existing design models versus the experimental values of  $V_{f\text{ exp}}$ .  
546 The results of this study show that the proposed model's accuracy ( $R^2 = 0.55$ ) is superior to the  
547 existing design models [Fig. 11(a)]. The proposed model can calculate the shear contribution of  
548 FRP for both beams strengthened with rods and laminates with high accuracy ( $R^2 = 0.58$  and  $R^2$   
549  $= 0.53$ , respectively, when FRP rods and laminates are considered separately). The predicted  
550 results by De Lorenzis and Nanni (2001) for NSM FRP rods show reasonable accuracy with the  
551 experimental results ( $R^2 = 0.34$ ) [Fig. 11(b)]. However, the modified version by Parretti and  
552 Nanni (2004) to make the model applicable to NSM FRP laminates does not show good  
553 correlation with experimental results ( $R^2 = 0.15$ , the results are not included in Table 3). This  
554 could be due to the fact that the model is not originally calibrated for NSM FRP laminates. The  
555 results produced by Kotynia (2007) and Anwarul Islam (2009) [Fig. 11(c)] do not show a great  
556 correlation with experimental results in database ( $R^2 < 0.1$ ). Dias and Barros (2013) model

557 (applicable to NSM FRP laminates) predicts  $V_f$  with reasonable accuracy when compared to  
558 experimental results of RC beams strengthened with NSM laminates ( $R^2 = 0.44$ ) [Fig. 11(d)].  
559 However, when the experimental results directly used by the researchers to calibrate their model  
560 are removed, the accuracy of Dias and Barros (2013) model drops significantly ( $R^2 < 0.1$ ) [Fig.  
561 11(e)]. This could be due to the fact that their model considers the diminishing effect of steel  
562 stirrups on NSM FRP contribution to the shear resistance, which the experimental results  
563 analysed in this study shows is not as significant as it was observed previously for EB FRP.

564 The predicted results of the models are also compared with respect to the ratio of  $(V_{f\text{ cal}})/(V_{f\text{ exp}})$   
565  $(V_{f\text{ cal}})/(V_{f\text{ exp}})$ . The proposed model and De Lorenzis and Nanni (2001) model produce accurate and  
566 conservative values with respect to  $(V_{f\text{ cal}})/(V_{f\text{ exp}})$  ratio (0.89 and 0.90 respectively). Whereas,  
567 models by Dias and Barros (2013) and Anwarul Islam (2009) produce non-conservative  
568 predictions with  $(V_{f\text{ cal}})/(V_{f\text{ exp}})$  equal to 1.17 and 1.91, respectively.

569 It should be noted that the proposed model is currently the only design model that can  
570 predict the failure mode of the shear strengthened beams with NSM FRP. When compared to the  
571 experimental results in the database, the proposed model was able to predict the failure mode of  
572 the beams with reasonable accuracy, i.e., 84% and 65% correct predicted failure modes for  
573 debonding and concrete covered splitting failure modes respectively.

574

## 575 CONCLUSIONS

576 This paper presents the results of an experimental investigation involving six tests on RC  
577 T-beams strengthened in shear using near-surface mounted FRP rods. The parameters of the  
578 experimental part of this study were: (i) the effectiveness of the NSM FRP rods, (ii) the presence  
579 of steel stirrups, and (iii) the steel stirrup ratio. This paper has provided an insightful and broad

580 description of the behaviour of RC beams strengthened in shear with NSM FRP under increasing  
581 load. The behaviour of FRP and of steel stirrups has been analyzed in depth, in particular at  
582 ultimate stage within the failure zone. The results of this study and those gathered in a database  
583 were further used to verify a newly proposed model to predict the shear contribution of RC  
584 beams strengthened with NSM FRP. The main findings of this research can be stated as follows:

- 585 • The near-surface mounting method greatly enhanced the overall behaviour of RC beams  
586 because the strengthened beams showed higher load at failure (31% on average) and  
587 greater maximum deflection than their corresponding control specimens.
- 588 • Proper NSM strengthening led to formation of concrete struts throughout the shear span  
589 of the RC beams, resulting in a distributed crack pattern. Unlike the control specimens, in  
590 the strengthened beams the first shear crack that caused the first steel stirrup to yield was  
591 not necessarily the principal shear crack that led to ultimate shear failure.
- 592 • The experimental results of this study and those presented in the database have revealed  
593 that the presence of steel stirrups did not diminish the NSM FRP shear contribution. This  
594 might have been due to the fact that the highly stressed areas around the existing steel  
595 stirrups and the FRP did not normally overlap in the NSM strengthening method.
- 596 • Yielding of steel stirrups were observed in all specimens tested in this study, as generally  
597 assumed in the design models for RC beams with steel stirrups strengthened in shear with  
598 FRP (e.g., ACI 440.2R-08 and CSA/S806-12).
- 599 • The proposed design model shows good correlation between the predicted results and the  
600 experimental results presented in the database as well as other available design models in  
601 literature. The proposed model produces accurate and conservative values with  $(V_{f\text{ cal}})/(V_{f\text{ exp}})$   
602 equal to 0.89. This new design model is also the only model that can reasonably

603 predict the possible failure modes of strengthened RC beams using NSM FRP rods and  
604 laminates.

605

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614

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Table 1: Description of the test specimens.

Specimen	Strengthening configuration	Internal transverse steel shear reinforcement		NSM FRP rods	
		Spacing (mm)	Diameter (mm)	Spacing (mm)	Diameter (mm)
NR-CON	- *	-	-	-	-
MR-CON	-	260	8	-	-
HR-CON	-	175	8	-	-
NR-NSM	NSM rods	-	-	130	9.5
MR-NSM	NSM rods	260	8	130	9.5
HR-NSM	NSM rods	175	8	130	9.5

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\*Not applicable.

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733 Table 2: Experimental results.

Specimen	Load at rupture (kN)	Total shear resistance (kN)	Resistance due to concrete (kN)	Resistance due to steel (kN)	Resistance due to CFRP (kN)	Gain due to CFRP (%)	Deflection at load point (mm)	Failure mode*
NR-CON	122.7	81.3	81.3	0.0	0.0	0	2.6	DTF
MR-CON	294.0	194.7	88.5	106.2	0.0	0	11.2	DTF
HR-CON	350.6	232.2	81.3	150.9	0.0	0	11.9	DTF
NR-NSM	198.0	131.1	81.3	0.0	49.8	61	6.1	CCS
MR-NSM	380.0	251.6	88.5	106.2	56.9	29	11.7	CCS/FLX
HR-NSM	365.0	241.7	81.3	150.9	9.5	4	13.1	FLX/CCS

734 \*Note: DTF, CCS and FLX correspond to diagonal tension, concrete cover splitting and flexural failure modes.

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Table 3: Experimental data of shear strengthening using NSM FRP.

Specimen	$b_w$ (mm)	$d$ (mm)	$f'_c$ (MPa)	FRP shape	$\rho_f$ (%)	$\rho_{sv}$ (%)	$E_f$ (GPa)	$\varepsilon_{ju}^*$ ( $\times 10^{-3}$ )	$\alpha$ ( $^\circ$ )	$V_{fcal}$ DN (kN)	$V_{fcal}$ KT (kN)	$V_{fcal}$ AN (kN)	$V_{fcal}$ DB (kN)	$V_{fcal}$ Proposed (kN)	$V_{fexp}$ (kN)
DN(B45-7)	152	356	31	Rods	0.74	0.00	105	18	45	67.9	119.1	177.2	n/a	108.7	75.1
DN(B90-5)	152	356	31	Rods	0.73	0.00	105	18	90	32.1	118.1	248.4	n/a	48.7	37.4
DN(B90-7)	152	356	31	Rods	0.52	0.00	105	18	90	11.1	84.2	177.2	n/a	25.6	24.9
BD(B10-VL)	150	123	56	Strips	0.19	0.00	150	14	90	n/a	14.6	25.3	47.0	1.22	28.6
BD(B10-IL)	150	123	56	Strips	0.18	0.00	150	14	45	n/a	13.8	16.8	89.0	5.4	23.2
BD(B12-VL)	150	123	56	Strips	0.37	0.00	150	14	90	n/a	29.3	50.5	59.0	12.6	31.8
BD(B12-IL)	150	123	56	Strips	0.35	0.00	150	14	45	n/a	27.6	33.7	82.0	22.2	36.4
DB(2S-3LV-a)	180	356	31	Strips	0.06	0.10	167	18	90	n/a	17.6	36.7	28.2	4.8	0.6
DB(2S-5LV-a)	180	356	31	Strips	0.10	0.10	167	18	90	n/a	29.4	61.3	41.4	24.0	25.2
DB(2S-8LV-a)	180	356	31	Strips	0.16	0.10	167	18	90	n/a	47.1	98.1	56.6	49.6	48.6
DB(2S-5LI45-a)	180	356	31	Strips	0.10	0.10	167	18	45	n/a	30.3	44.6	58.4	78.4	41.4
DB(2S-8LI45-a)	180	356	31	Strips	0.16	0.10	167	18	45	n/a	48.2	71.1	71.7	75.6	40.2
DB(2S-3LI60-a)	180	356	31	Strips	0.06	0.10	167	18	60	n/a	19.8	30.2	42.1	13.3	35.4
DB(2S-5LI60-a)	180	356	31	Strips	0.09	0.10	167	18	60	n/a	33.0	50.3	57.2	38.0	46.2
DB(2S-7LI60-a)	180	356	31	Strips	0.13	0.10	167	18	60	n/a	46.3	70.6	67.5	78.2	54.6
RD(NB45-73-a)	200	173	29	Rods	0.97	0.18	146	15	45	70.1	139.1	175.8	n/a	38.5	28.0
RD(NB90-45-b)	200	173	29	Rods	1.12	0.18	146	15	90	48.6	159.6	285.2	n/a	16.0	28.6
RD(NB90-73-b)	200	173	29	Rods	0.69	0.18	146	15	90	30.2	98.4	175.8	n/a	16.0	26.4
RD(NB90-73-a)	200	173	29	Rods	0.69	0.18	146	15	90	30.2	98.4	175.8	n/a	16.0	54.2
RD(NB45-146-a)	200	173	29	Rods	0.48	0.18	146	15	45	35.0	69.6	87.9	n/a	16.7	39.1
RD(NS90-73-a)	200	173	29	Strips	0.44	0.18	122	17	90	n/a	52.2	104.6	53.6	18.6	50.5
RD(NS45-146-a)	200	173	29	Strips	0.31	0.18	122	17	45	n/a	37.0	52.3	41.0	18.6	32.7
JL(VR)	200	214	36	Rods	0.09	0.19	235	15	90	17.3	128.0	248.5	n/a	6.5	33.4
JL(IR)	200	214	36	Rods	0.09	0.19	235	15	45	27.6	120.7	165.7	n/a	19.3	39.9
DB(3S-10LV-d)	180	360	59	Strips	0.13	0.10	174	16	90	n/a	41.5	79.7	69.3	65.8	65.9
DB(3S-5LI45-d)	180	360	59	Strips	0.08	0.10	174	16	45	n/a	24.3	33.0	83.6	67.6	66.1
DB(3S-5LI45F1-d)	180	360	59	Strips	0.08	0.10	174	16	45	n/a	24.3	33.0	83.6	67.6	85.8
DB(3S-5LI45F2-d)	180	360	59	Strips	0.08	0.10	174	16	45	n/a	24.3	33.0	83.6	67.6	65.4
DB(3S-9LI45-d)	180	360	59	Strips	0.13	0.10	174	16	45	n/a	42.6	57.9	110.1	107.0	101.9
DB(3S-8LI60-d)	180	360	59	Strips	0.11	0.10	174	16	60	n/a	39.9	56.1	100.1	103.3	112.3
DB(5S-5LI45-d)	180	360	59	Strips	0.08	0.16	174	16	45	n/a	24.3	33.0	62.0	67.6	74.9
DB(5S-5LI45F-d)	180	360	59	Strips	0.08	0.16	174	16	45	n/a	24.3	33.0	62.0	67.6	101.1
DB(5S-9LI45-d)	180	360	59	Strips	0.13	0.16	174	16	45	n/a	42.6	57.9	86.8	107	108.9
DB(5S-5LI60-d)	180	360	59	Strips	0.07	0.16	174	16	60	n/a	26.6	37.4	59.9	60.6	73.4
DB(5S-5LI60F-d)	180	360	59	Strips	0.07	0.16	174	16	60	n/a	26.6	37.4	59.9	60.6	72.6

Table 3: Experimental data of shear strengthening using NSM FRP (cont'd).

DB(5S-8LI60-d)	180	360	59	Strips	0.11	0.16	174	16	60	n/a	39.9	56.1	77.7	103.4	122.5
DB(2S-4LV-b)	180	360	40	Strips	0.08	0.10	171	16	90	n/a	25.8	48.6	41.6	22.0	20.2
DB(2S-7LV-b)	180	360	40	Strips	0.13	0.10	171	16	90	n/a	40.7	76.8	57.1	50.6	42.1
DB(2S-10LV-b)	180	360	40	Strips	0.18	0.10	171	16	90	n/a	58.0	109.4	71.2	56.3	56.2
DB(2S-4LI45-b)	180	360	40	Strips	0.08	0.10	171	16	45	n/a	23.9	31.8	61.2	59.5	53.4
DB(2S-7LI45-b)	180	360	40	Strips	0.13	0.10	171	16	45	n/a	41.8	55.7	80.9	107.8	70.7
DB(2S-10LI45-b)	180	360	40	Strips	0.19	0.10	171	16	45	n/a	59.6	79.6	92.2	107.8	85.6
DB(2S-4LI60-b)	180	360	40	Strips	0.07	0.10	171	16	60	n/a	26.1	36.0	59.5	30.3	49.6
DB(2S-6LI60-b)	180	360	40	Strips	0.11	0.10	171	16	60	n/a	39.1	54.0	74.3	63.3	54.4
DB(2S-9LI60-b)	180	360	40	Strips	0.16	0.10	171	16	60	n/a	58.7	81.0	88.6	98.6	65.3
DB(2S-7LV-c)	180	360	19	Strips	0.13	0.10	174	16	90	n/a	41.5	79.7	41.1	31.7	28.3
DB(2S-4LI45-c)	180	360	19	Strips	0.08	0.10	174	16	45	n/a	24.3	33.1	35.2	23.3	33.9
DB(2S-7LI45-c)	180	360	19	Strips	0.13	0.10	174	16	45	n/a	42.6	57.9	46.4	73.1	48.0
DB(2S-4LI60-c)	180	360	19	Strips	0.07	0.10	174	16	60	n/a	26.6	37.4	34.5	19.0	33.1
DB(2S-6LI60-c)	180	360	19	Strips	0.11	0.10	174	16	60	n/a	39.9	56.1	43.0	39.7	42.7
DB(4S-7LV-c)	180	360	19	Strips	0.13	0.17	174	16	90	n/a	41.5	79.7	34.1	31.7	6.8
DB(4S-4LI45-c)	180	360	19	Strips	0.08	0.17	174	16	45	n/a	24.3	33.1	24.0	23.3	26.0
DB(4S-7LI45-c)	180	360	19	Strips	0.13	0.17	174	16	45	n/a	42.6	57.9	34.1	73.1	31.7
DB(4S-4LI60-c)	180	360	19	Strips	0.07	0.17	174	16	60	n/a	26.6	37.4	23.4	19.0	25.2
DB(4S-6LI60-c)	180	360	19	Strips	0.11	0.17	174	16	60	n/a	39.9	56.1	30.7	39.7	35.2
RR(B2)	150	430	44	Rods	0.34	0.19	124	15	90	34.7	76.0	137.0	n/a	37.9	70.0
RR(B4)	150	430	44	Rods	0.47	0.19	124	15	45	72.7	107.5	137.0	n/a	152.1	138.0
KT(BI-2/3B)	150	310	39	Strips	0.19	0.19	163	14	45	n/a	40.5	46.5	54.5	23.8	64.6
KT(BI-3/5A)	150	310	39	Strips	0.32	0.19	163	14	45	n/a	69.5	79.7	67.8	71.0	100.6
WA(A75-90)	250	234	39	Rods	1.57	0.15	69	16	90	74.1	183.0	336.3	n/a	39.6	45.5
WA(A300-45)	250	234	39	Rods	0.55	0.15	69	16	45	12.4	64.7	84.1	n/a	12.4	43.9
WA(C75-90)	250	234	39	Rods	0.50	0.15	72	13	90	42.0	61.9	244.9	n/a	30.0	47.5
WA(C150-90)	250	234	39	Rods	0.25	0.15	72	13	90	17.0	30.4	122.5	n/a	7.6	43.8
WA(C300-45)	250	234	39	Rods	0.18	0.15	72	13	45	7.6	21.9	61.2	n/a	7.6	33.7
RS(BR90E)	175	211	35	Rods	0.32	0.00	45	19	90	8.0	15.2	35.8	n/a	8.0	36.8
RS(BR45E)	175	211	35	Rods	0.46	0.00	45	19	45	31.9	21.5	35.8	n/a	31.8	29.4
RS(BS90E)	175	211	35	Strips	0.34	0.00	44	17	90	n/a	15.8	31.7	60.4	10.4	49.0
RS(BS90E100)	175	211	35	Strips	0.34	0.00	44	17	90	n/a	15.8	31.7	60.4	10.4	61.5
RS(BS90E75)	175	211	35	Strips	0.46	0.00	44	17	90	n/a	21.1	42.2	66.3	17.7	39.2

\*  $\epsilon_{fu}$  is the ultimate strain of the FRP.

\*\* DN = De Lorenzis and Nanni (2001); BD = Barros and Dias (2006); DB= Dias and Barros (2008, 2010, 2011, 2012, 2013); RD = Rizzo and De Lorenzis (2007); AN = Anwarul Islam (2009); JR = Jalali *et al.* (2012); RR= Rahal and Rumaih (2011); KT= Kotynia 2007; WA = Wawatrojanagul *et al.* (2012); and RS = Raj and Surumi (2012).

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Table 4: Comparison of predicted results versus experimental results

Specimen	$\epsilon_{fe-b}$	$\epsilon_{fe-c}$	$\epsilon_{fe-g}$	$V_{f-cal}^*$ (kN)	$V_{f-flx}$ (kN)	$V_{f-g}$ (kN)	$V_{f-exp}$ (kN)	$V_{f-g} / V_{f-exp}$
NR-NSM	0.0010	0.0009	0.0009	<u>47.8</u> **	174.7	47.8	49.8	0.96
MR-NSM	0.0011	0.0010	0.0010	<u>52.0</u>	81.3	52.0	56.9	0.91
HR-NSM	0.0010	0.0009	0.0009	47.8	<u>23.8</u>	23.8	9.5	2.50

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\*  $V_{f-cal}$ ,  $V_{f-flx}$ ,  $V_{f-exp}$  are the FRP shear contributions corresponding to the calculated governing effective strain at ultimate load, the calculated values at flexural failure of the beam, and experimental results respectively,  $V_{f-g}$  is the governing calculated shear contribution of FRP and  $\epsilon_{fe-b}$ ,  $\epsilon_{fe-c}$ ,  $\epsilon_{fe-g}$  are the corresponding effective strain to debonding and concrete cover splitting and the governing effective strain to calculate the shear contribution of FRP respectively.

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\*\* The shear contribution of FRP corresponding to the governing calculated failure mode is underlined (shear versus flexure failure modes).

Figure 1  
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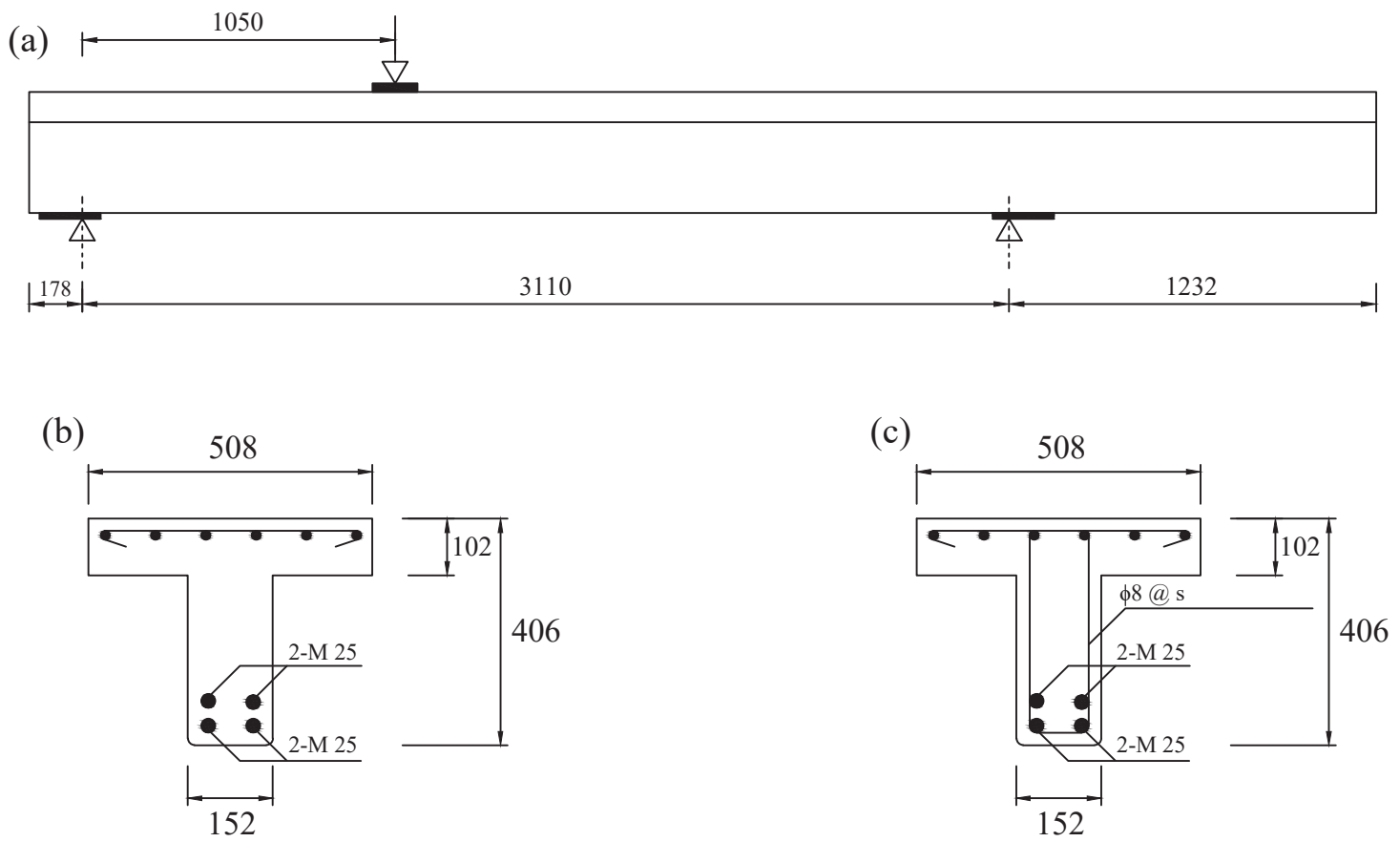


Figure 2  
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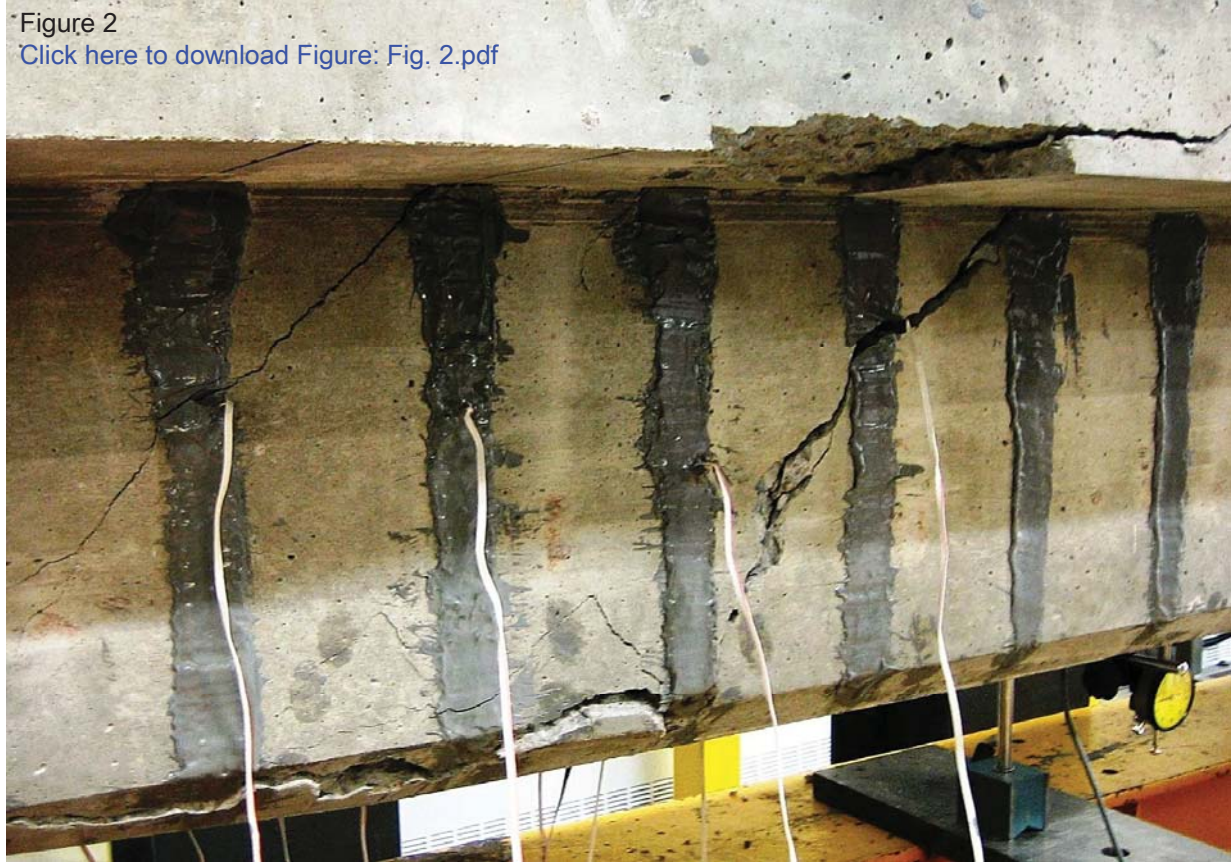
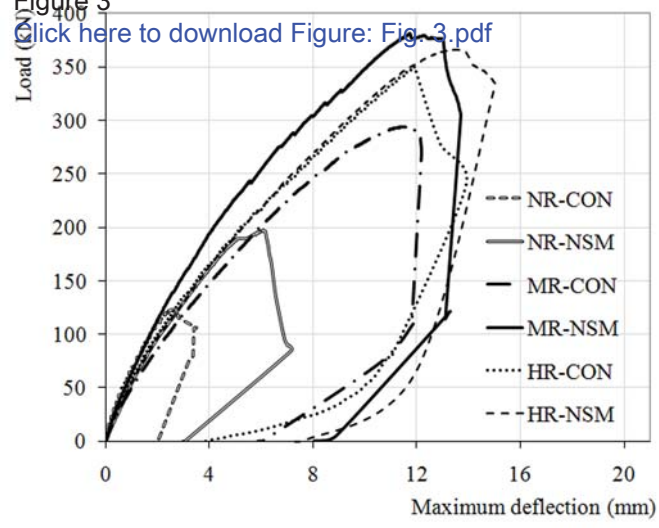


Figure 3



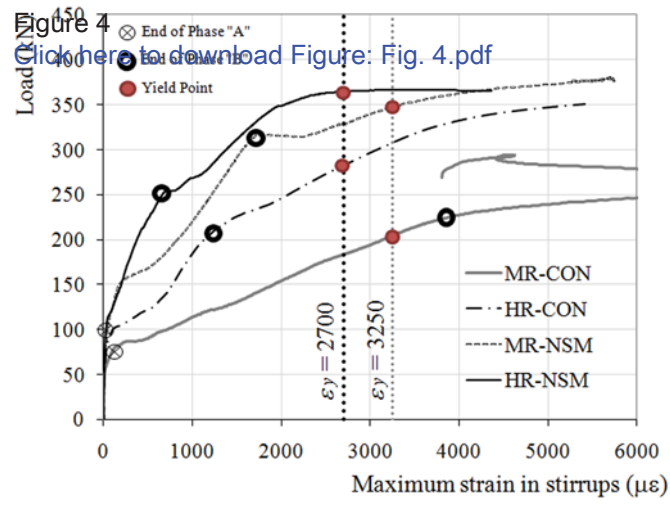


Figure 5  
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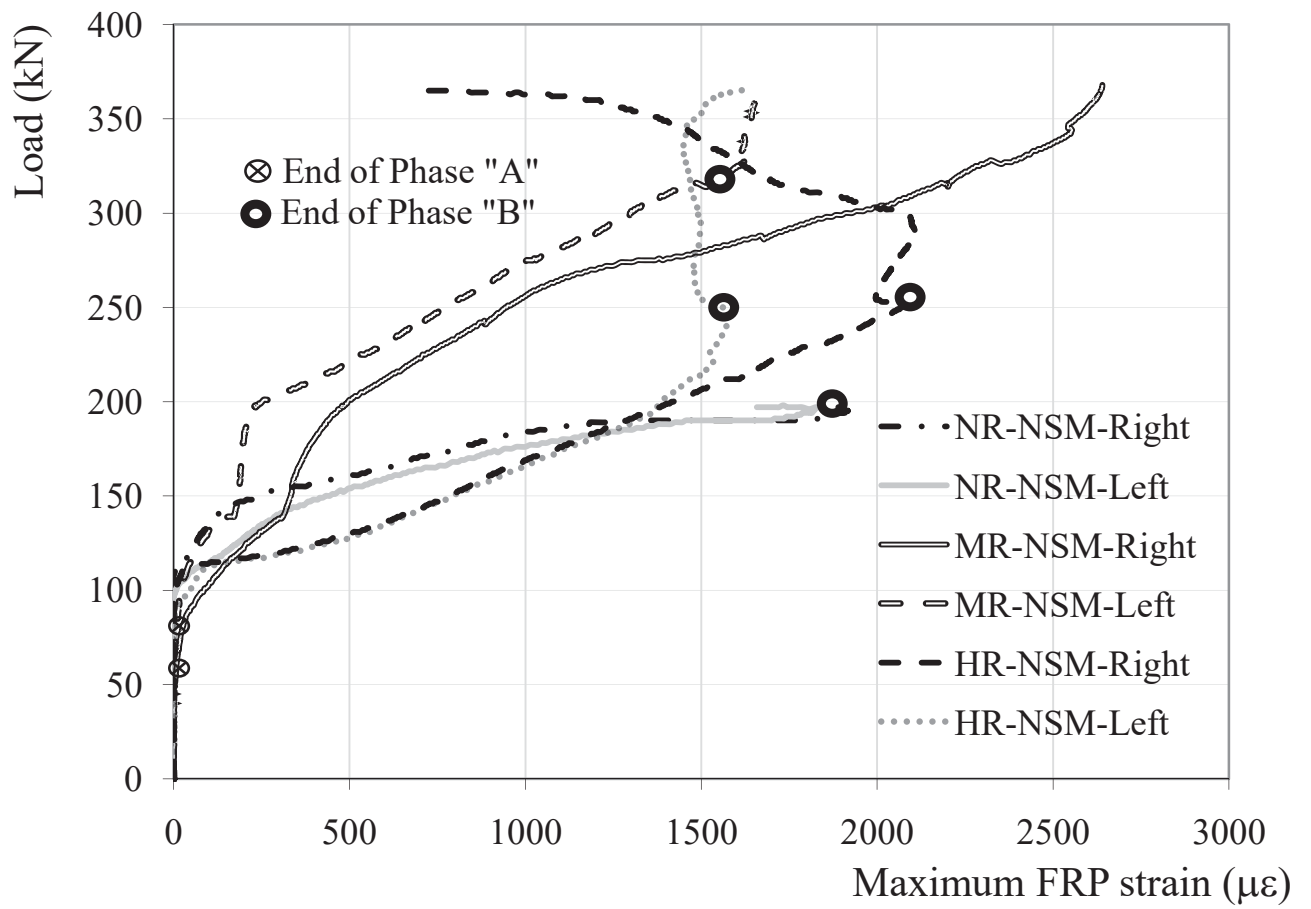
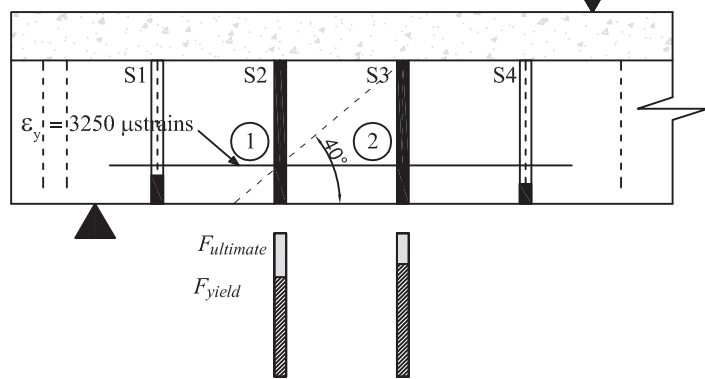


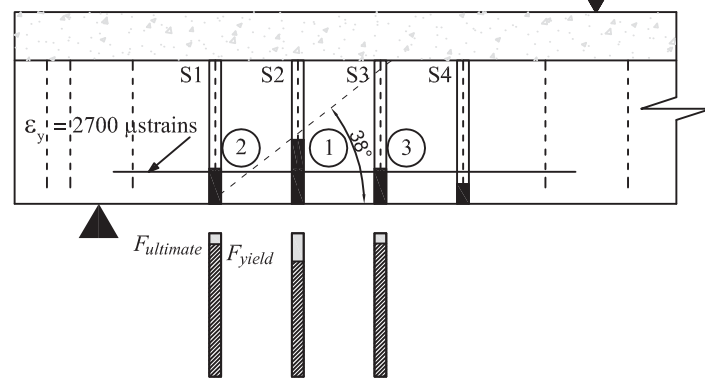


Figure 6  
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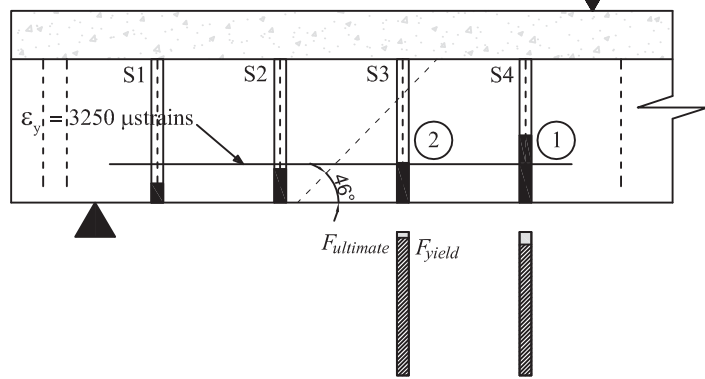
### MR-CON



### HR-CON



### MR-NSM



### HR-NSM

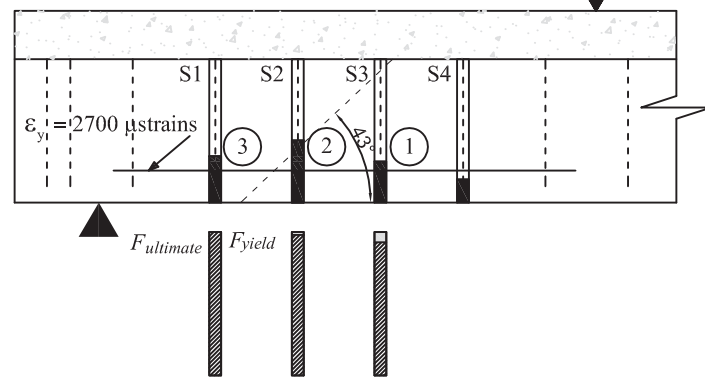


Figure 7  
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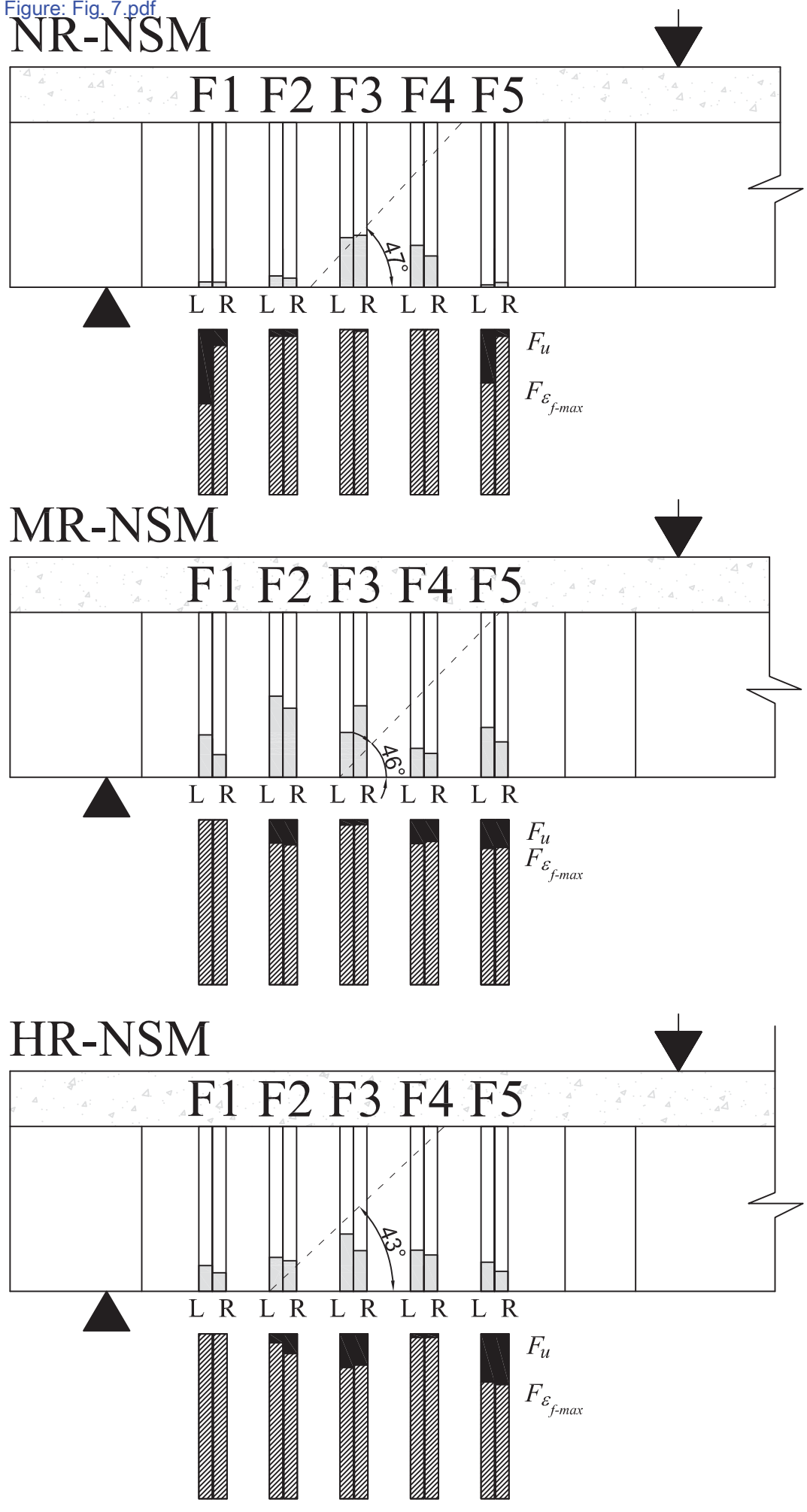


Figure 8  
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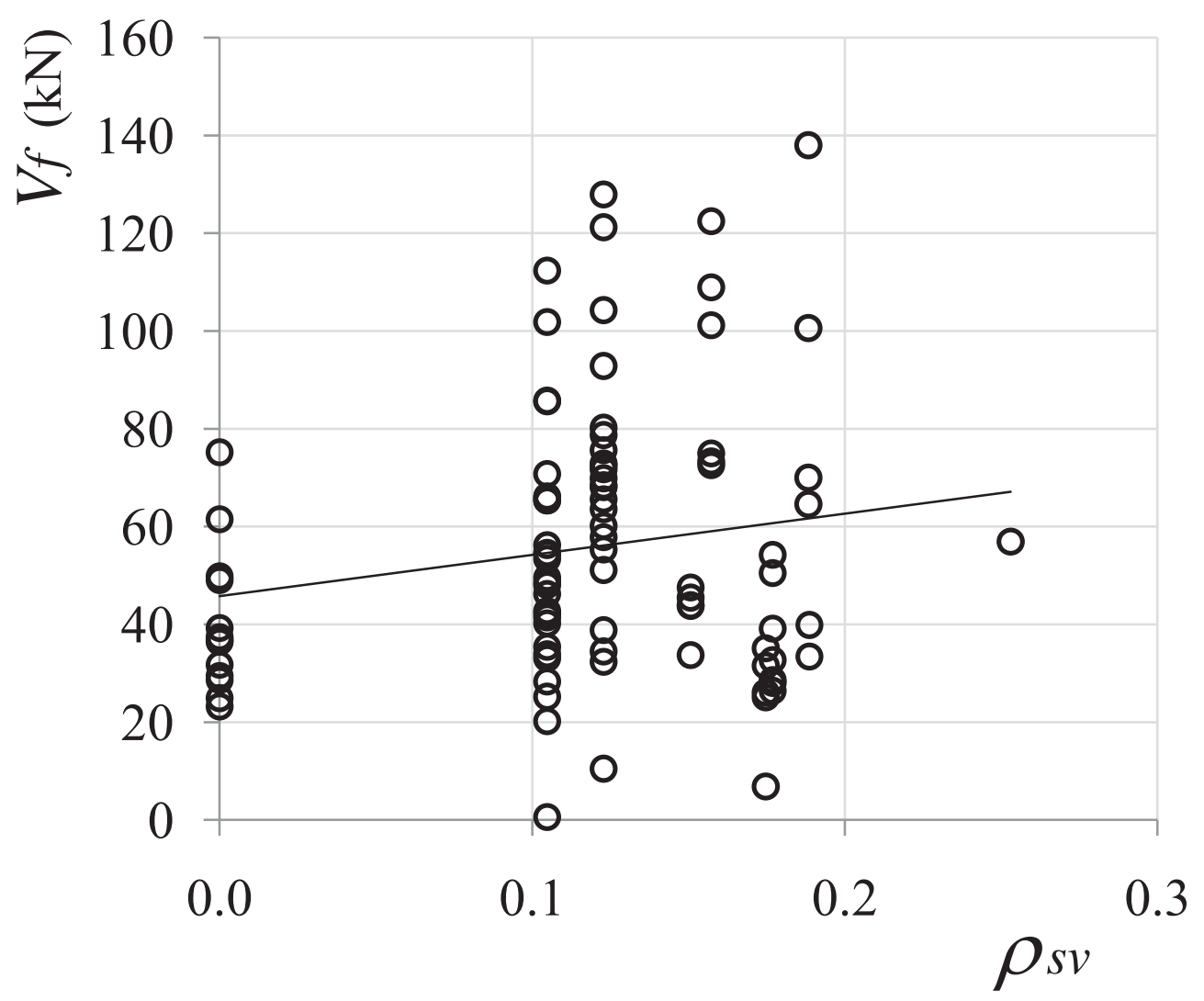


Figure 9  
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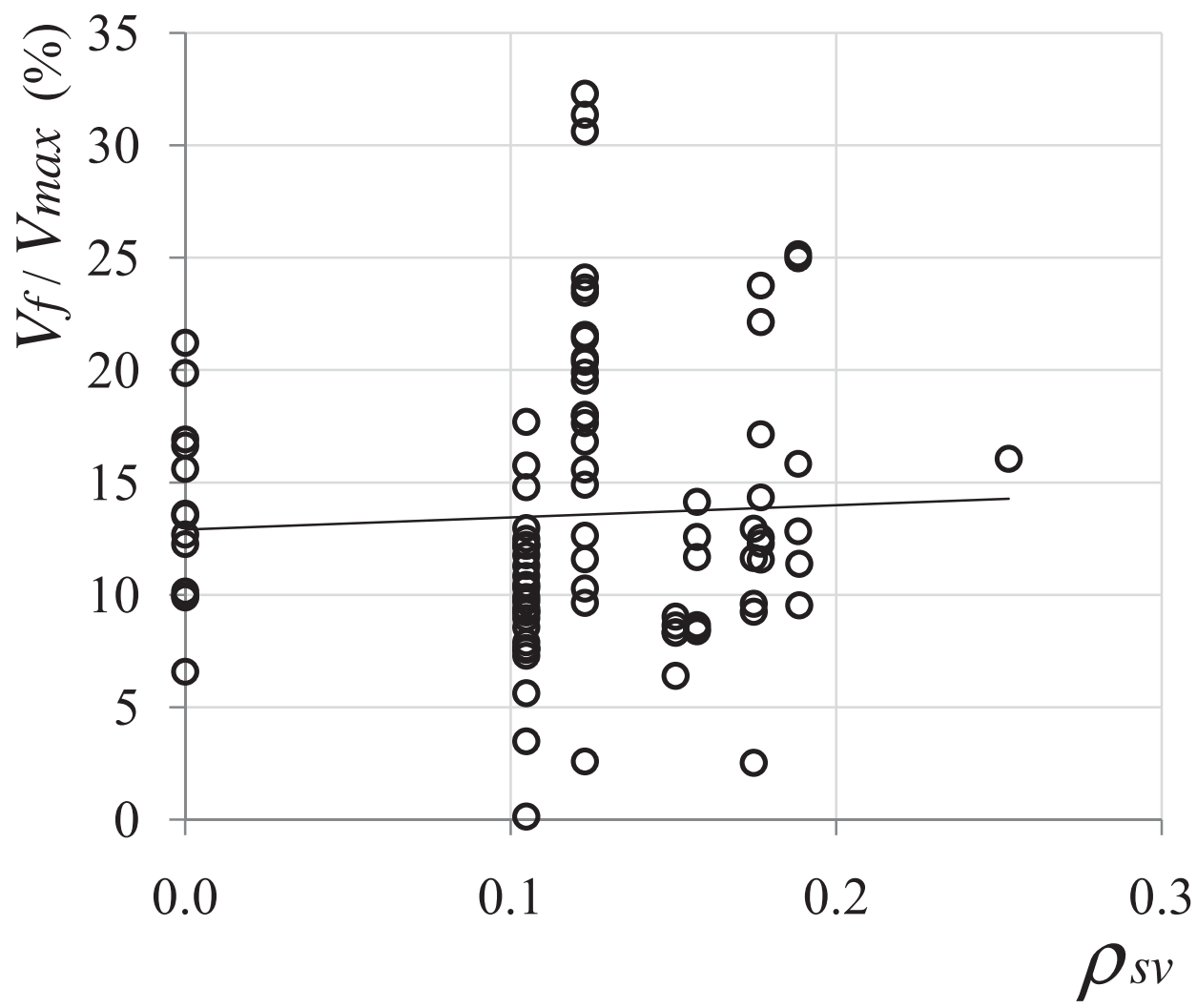
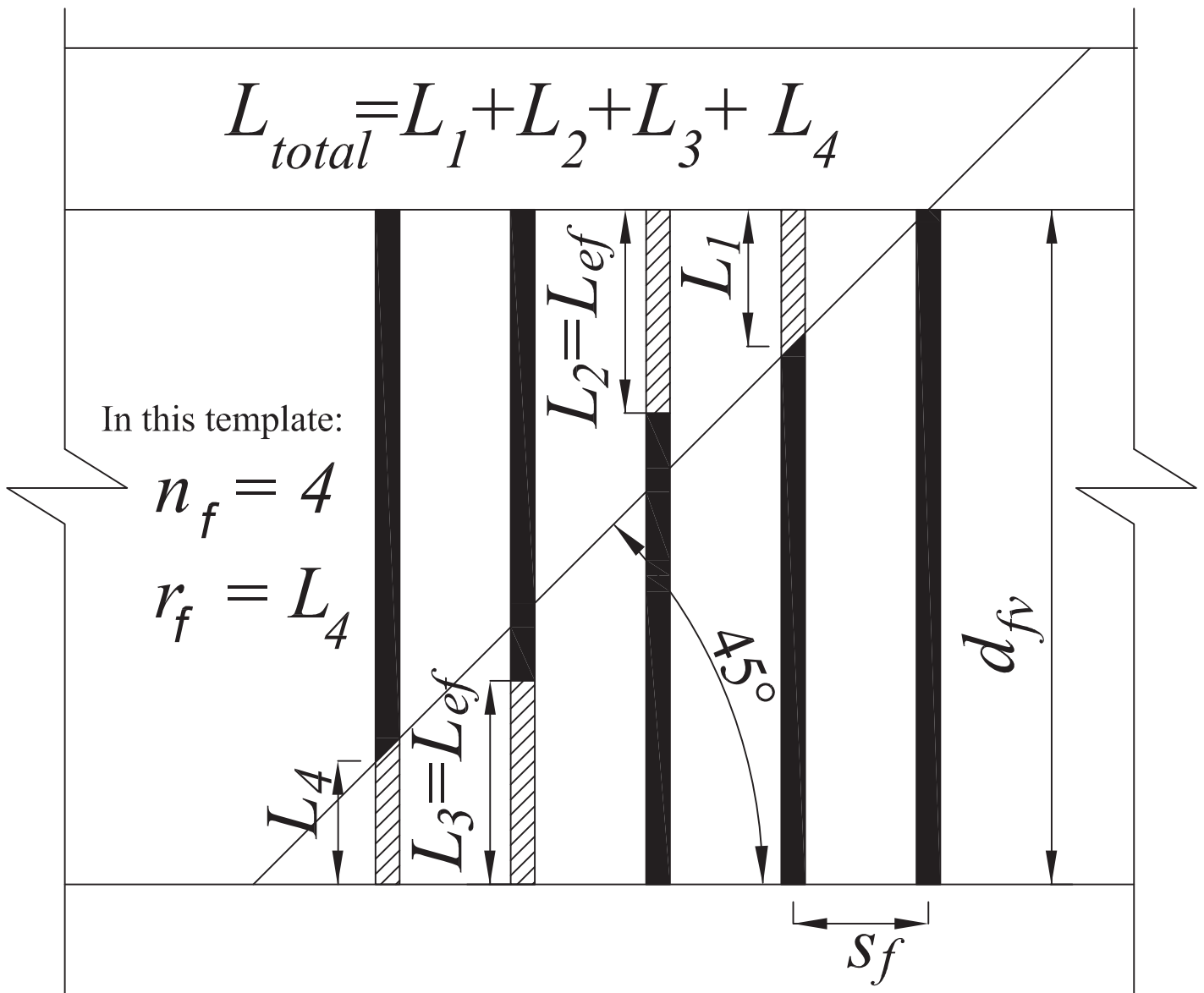
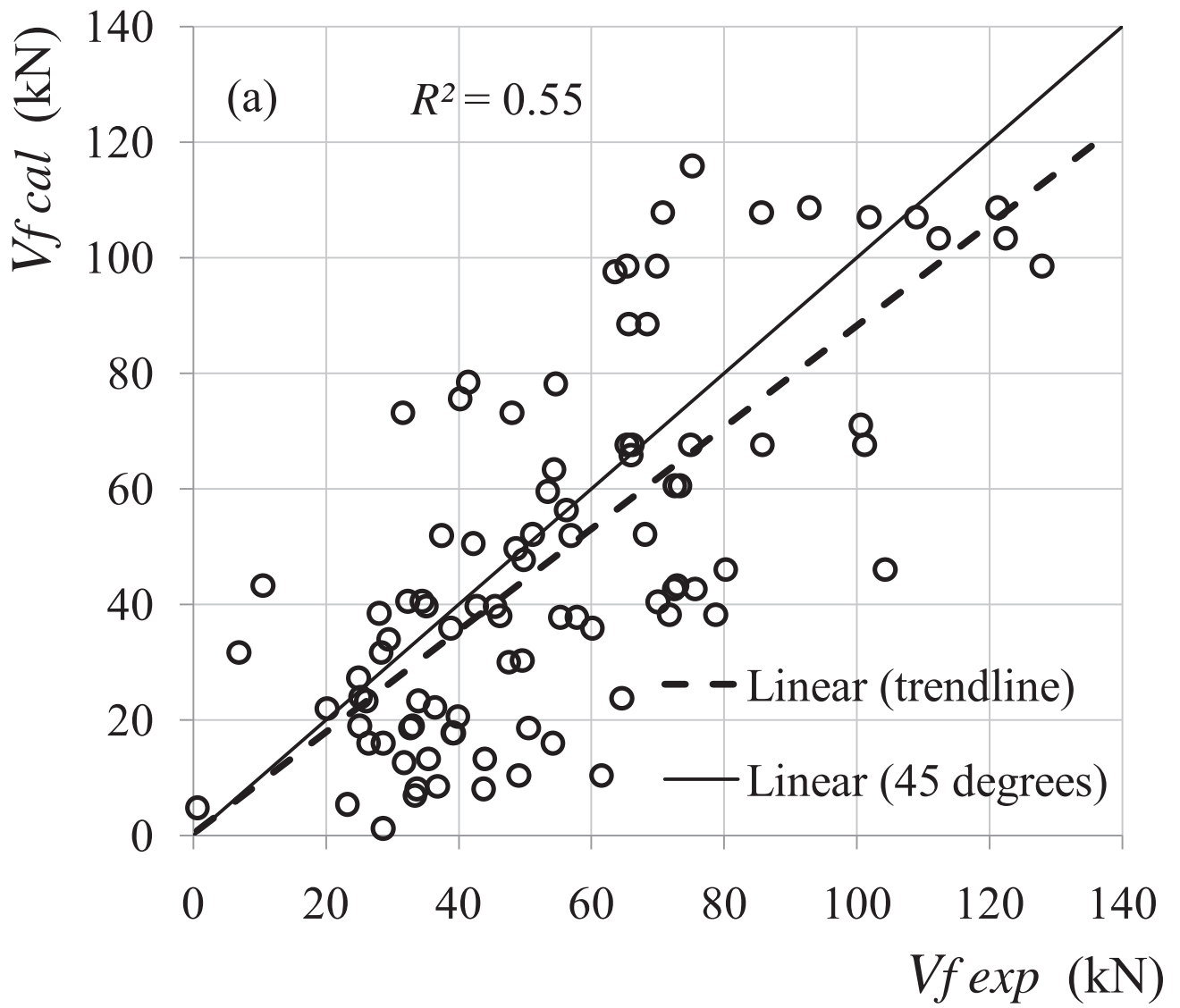
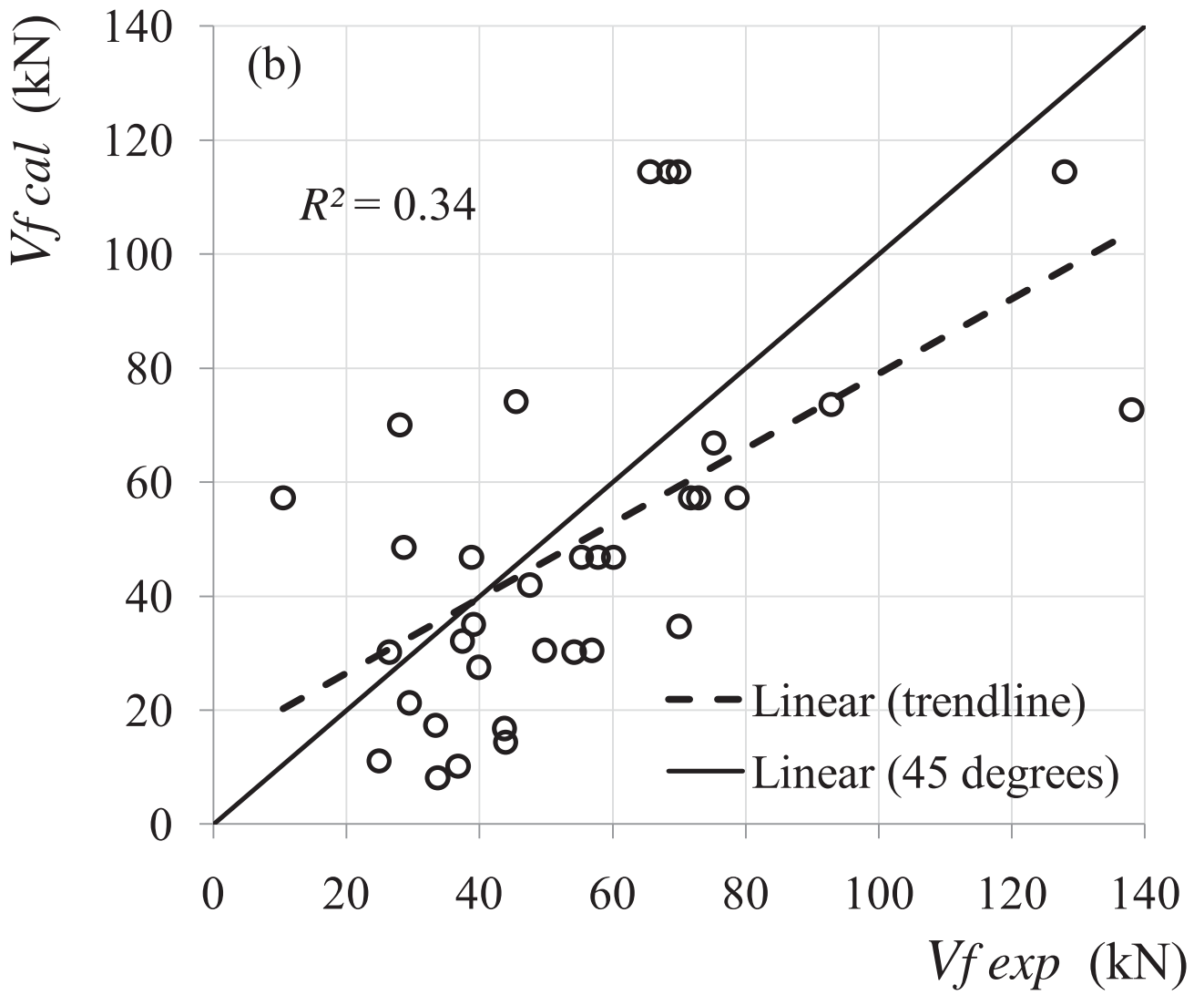
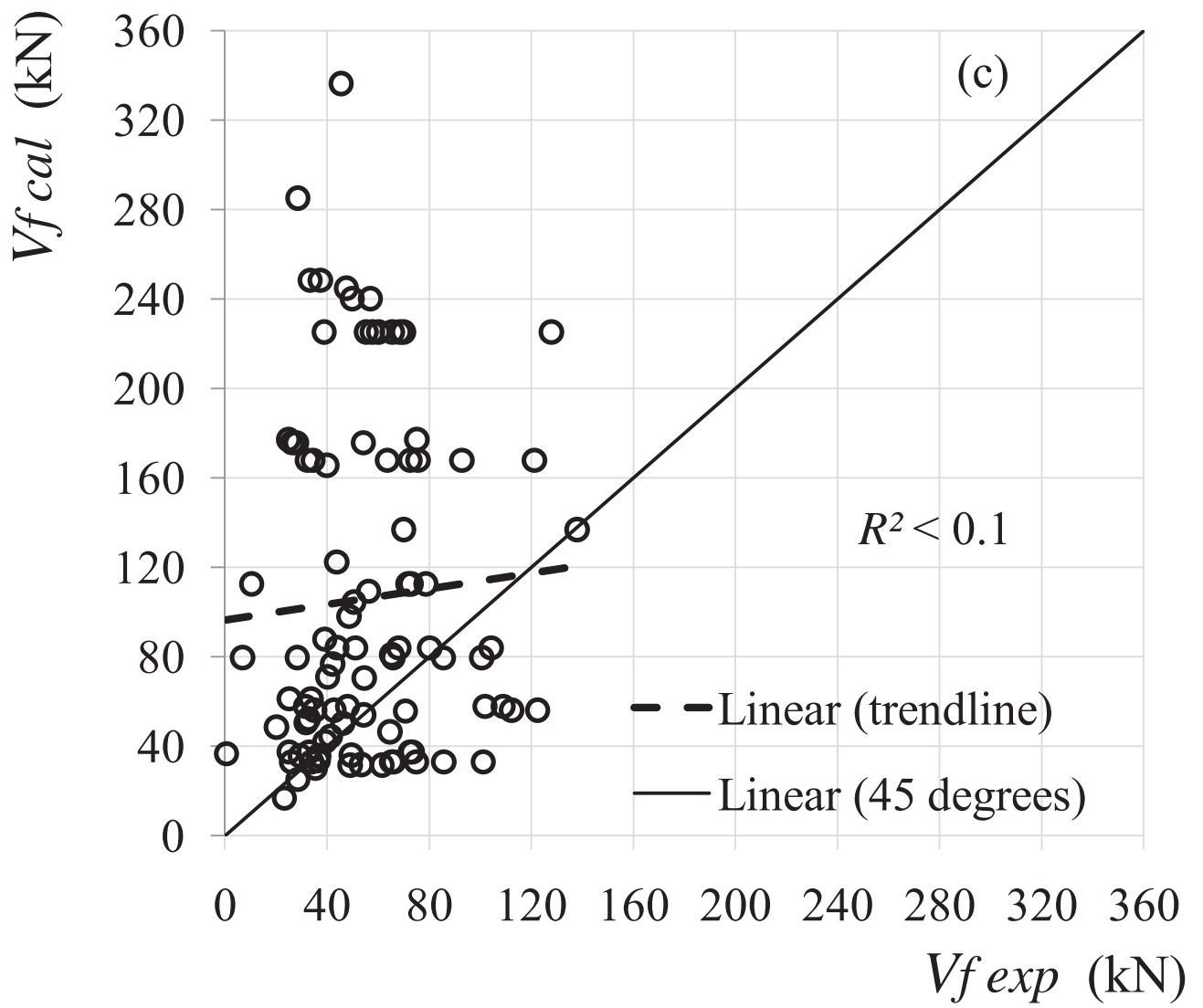


Figure 10  
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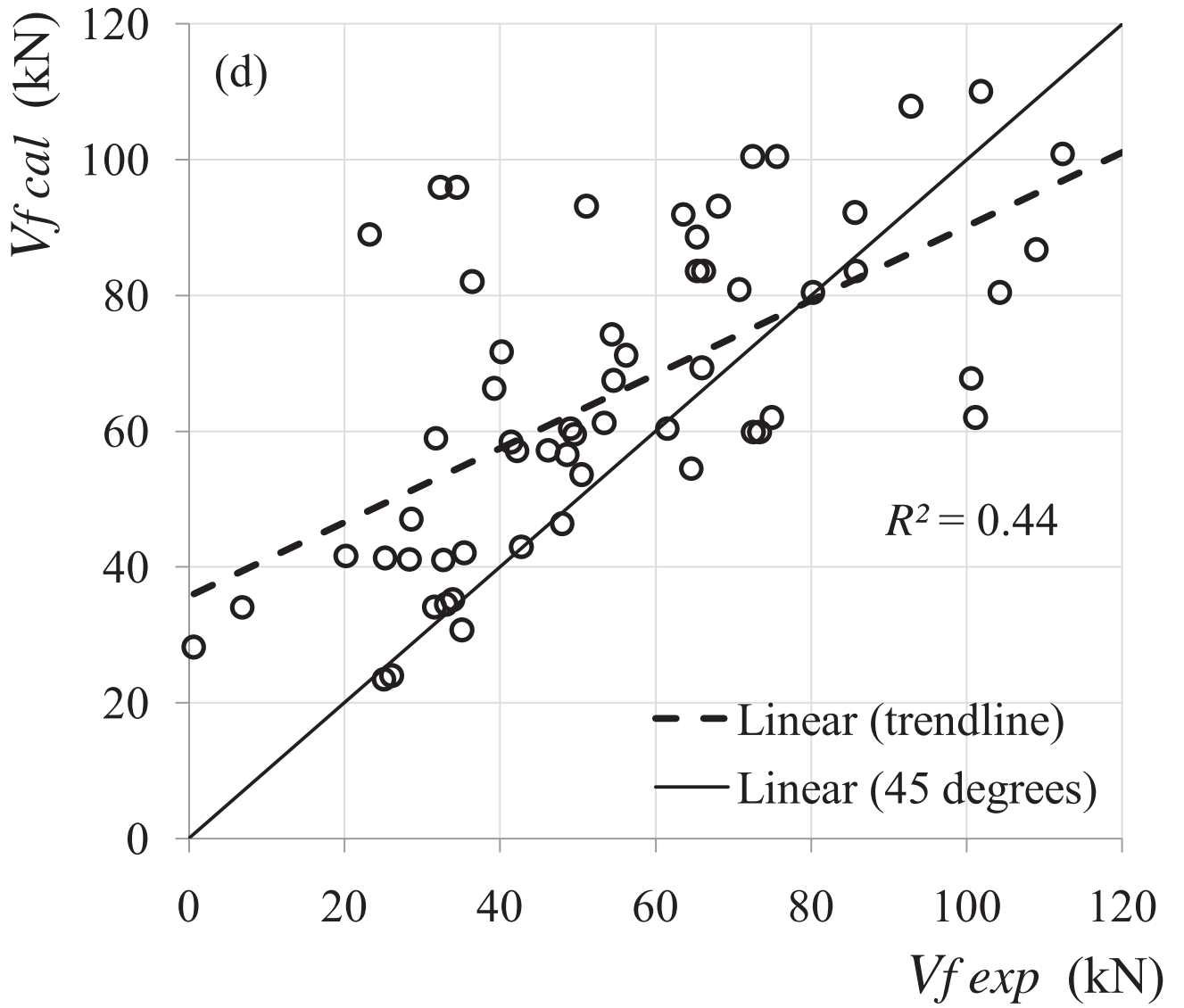












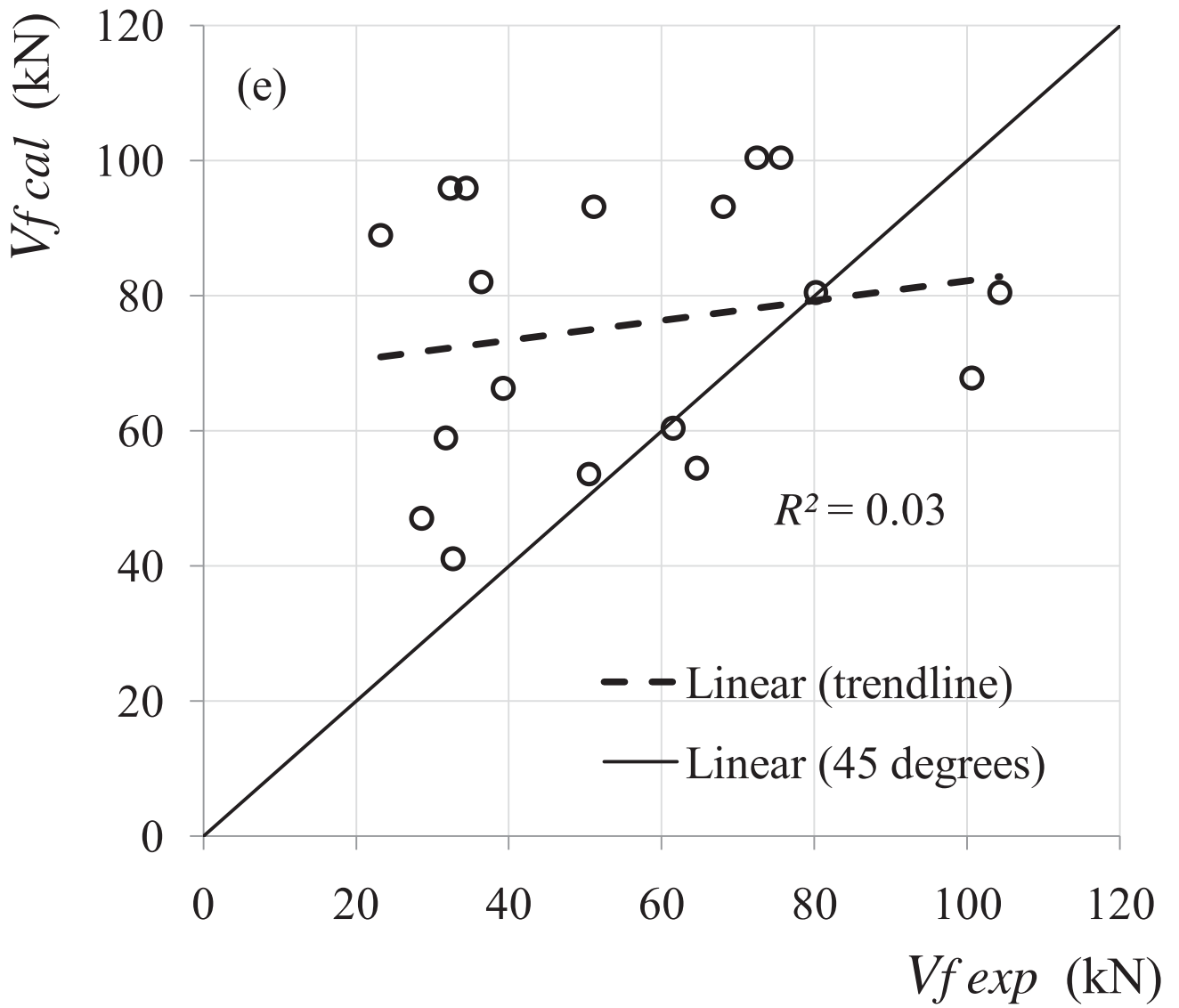


Fig. 1: Details of the tested specimens: (a) elevation; (b) cross-section of specimens with no steel stirrups; and (c) cross-section of specimens with steel stirrups. Dimensions in mm.

Fig. 2: Distributed diagonal cracking in specimen MR-NSM.

Fig. 3: Load versus maximum deflection at the load point.

Fig. 4: Load versus maximum strain in the steel stirrups: MR and HR series.

Fig. 5: Load versus maximum strain in NSM FRP rods in each side of the web for all the strengthened specimens.

Fig. 6: Distribution of ultimate strains in the stirrups within the failure zone

Fig. 7: Distribution of maximum strains in the CFRP rods.

Fig. 8: Contribution of FRP to the shear resistance versus steel stirrups reinforcement ratio (the straight line is the linear trend line).

Fig. 9: FRP strengthening factor  $\kappa_f = V_f/V_{max}$  versus steel stirrups reinforcement ratio (the straight line is the linear trend line).

Fig. 10: Calculation of  $L_{total}$  for RC beams strengthened with NSM FRP.

Fig. 11: Predicted versus experimental result using (a) the proposed model; (b) De Lorenzis and Nanni (2001) for NSM FRP rods; (c) Anwarul Islam (2009); (d) Dias and Barros (2013) for laminates; and (e) Dias and Barros (2013) for laminates (the experimental results that are directly used to calibrate the model are not considered in comparison).