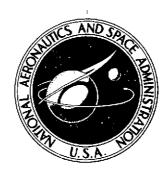
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HYPERSONIC AERODYNAMIC CHARACTERISTICS OF A FAMILY OF POWER-LAW. WING BODY CONFIGURATIONS (NASA) \$3.00

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HYPERSONIC AERODYNAMIC CHARA OF A FAMILY OF POWER-LAW, WING-BODY CONFIGURATIONS

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SUMMARY

The configurations analyzed are half-axisymmetric, power-law bodies surmounted by thin, flat wings. The wing planform matches the body shock wave shape. Analytic solutions of the hypersonic small disturbance equations form a basis for calculating the longitudinal aerodynamic characteristics. Approximate boundary-layer displacement effects on the body and wing upper surface are included. Skin friction is estimated by using compressible, laminar boundary-layer solutions. By using an effective body shape, the method is extended to small angles of attack. Three basic theoretical assumptions are made: (1) the body is slender, (2) the shock wave is strong, and (3) the Mach number is large. In comparisons with available experimental data, good agreement was obtained when these assumptions were satisfied. The method is also used to estimate the effects of power law, fineness ratio, and Mach number variations at full-scale conditions. The implementing computer program is included.

INTRODUCTION

Much research has been devoted to the hypersonic flow about half bodies of revolution mounted beneath a thin wing. Theoretical studies (refs. 1 to 3) and experimental work (refs. 4 to 7) show that with half-cone bodies these configurations combine good stability characteristics with high values of maximum lift-drag ratio. Replacing the conical bodies with those having power-law profiles generates a larger class of configurations and one which is more representative of aircraft shapes. Low wave-drag bodies in the hypersonic regime are generated by power-law curves with exponent in the range 0.5 to 0.8. (See refs. 8 to 12.) These bodies have the additional advantage of better volume distribution than cones.

The purpose of this study was to develop a method for calculating the longitudinal aerodynamic characteristics of power-law bodies with reflection-plane wings. The method applies to configurations consisting of half of an axisymmetric power-law body mounted beneath a thin wing whose planform matches the theoretical body shock shape at zero angle

of attack. Small-disturbance theory, with small perturbations for Mach number and boundary-layer displacement effects, provides a means for calculating the pressure field and shock-wave shape. This pressure field is integrated analytically to obtain the forces and moment on the body. Small angles of attack are simulated, and laminar skin friction is calculated. The computer programs which have been written to implement this method are presented in an appendix.

SYMBOLS

a ₁ .	shock-wave perturbation constant					
С	Chapman-Rubesin constant, $\frac{\mu_{ m W}/\mu_{\infty}}{T_{ m W}/T_{\infty}}$					
c_A	axial-force coefficient, $\frac{\text{Axial force}}{\bar{q}_{\infty}S}$					
c_D	drag coefficient, $\frac{D}{\bar{q}_{\infty}S}$					
c_L	lift coefficient, $\frac{L}{\bar{q}_{\infty}S}$					
$C_{\mathbf{m}}$	pitching-moment coefficient, $\frac{\text{Pitching moment}}{\bar{q}_{\infty} S \bar{c}}$					
c_{N}	normal-force coefficient, $\frac{\text{Normal force}}{\bar{q}_{\infty}S}$					
$c_{N,b}$	normal-force coefficient of body					
$c_{N,w}$	normal-force coefficient of wing					
c_p	pressure coefficient, $\frac{\bar{p}-\bar{p}_{\infty}}{\bar{q}_{\infty}}$					
$ar{\mathbf{c}}$	mean aerodynamic chord, taken as $\bar{c}_b = \frac{2\bar{l}}{m+2}$					
D	drag					
E	constant in boundary-layer displacement thickness					
2						

F similarity static-pressure variable

f fineness parameter, $\frac{\bar{i}}{\bar{r}_{b,B}}$

I boundary-layer profile parameter

J integral of F from body to shock

L lift

l length

 \mathbf{M}_{∞} free-stream Mach number

m exponent of power-law body shape

p dimensionless static pressure, $\frac{\bar{p}}{2\delta^2\bar{q}_{\infty}}$

 $\bar{\bar{p}}_{u}$ average wing upper surface pressure

 \bar{q}_{∞} free-stream dynamic pressure

R dimensionless shock-wave radius, $\frac{\overline{R}}{\delta \overline{L}}$

 $R_{\infty,l}$ free-stream Reynolds number, $\frac{\bar{\rho}_{\infty}\bar{l}\,\overline{U}_{\infty}}{\bar{\mu}_{\infty}}$

r dimensionless radial coordinate, $\frac{ar{ t r}}{\deltaar{ ilde{l}}}$

S projected planform area

 $\mathbf{s_c}$ distance from nose to upper surface center of pressure

T temperature

 $\overline{\overline{U}}_{\infty}$ free-stream axial velocity

V volume of body

x dimensionless axial coordinate, $\frac{\bar{x}}{\bar{l}}$

 α angle of attack relative to body axis

 γ ratio of specific heats

 $\delta \qquad \qquad \text{shock-wave slope parameter,} \quad \delta \equiv \frac{\overline{R}_0,B}{\overline{l}} = \frac{1}{f\eta_b}$

 δ^* dimensionless boundary-layer displacement thickness, $\frac{\bar{\delta}^*}{\delta \bar{l}}$

 ϵ_1 small perturbation parameter for Mach number, $\frac{1}{(\delta M_m)^2}$

 ϵ^* small perturbation parameter for boundary-layer displacement, $\frac{d\delta^*/ds}{dr_h/ds}$

 η similarity form of radial coordinate, $\frac{r}{R_0}$

 θ shock-wave angle

 $\kappa = \left(\frac{\delta}{\delta_e}\right)^2$

 μ viscosity coefficient

 $\nu = \frac{\mathbf{f_e}}{\mathbf{f}}$

ξ similarity form of axial coordinate

ho dimensionless density, $rac{ar
ho}{ar
ho_{\infty}}$

Subscripts:

B at base of configuration, x = 1

b body

effective body shape

max maximum

e

0

1

90

(L/D)_{max} maximum lift-drag ratio

zero-order similarity solution $(\epsilon_1 \rightarrow 0)$

first-order similarity solution $(\epsilon_1{}^2 << 1)$

free-stream value

w wall

An asterisk denotes that the quantity includes boundary-layer displacement effect. A bar over a symbol denotes a dimensional quantity.

THEORY

The method applies to the general configuration shown in figure 1(a). It consists of one-half of a body of revolution mounted beneath a thin wing at an angle of attack of 0°. By assumption, the wing acts as an endplate to maintain the axial symmetry of the flow about the body. The wing planform matches the shock-wave shape about the full body, and the body pressure field acts on the wing to provide additional lift. The method is put together from a series of pieces in order to arrive at the final aerodynamic coefficients. The basis for the development is the result in hypersonic slender-body theory that for power-law bodies, there are similarity solutions to the inviscid flow equations in the hypersonic limit. (See ref. 13.) Independent small perturbations are made to account for Mach number effects and for laminar boundary-layer displacements. (See ref. 14.) To simulate the effects of small angles of attack, a simple substitution of an effective body is made. The resulting equation for the pressure distribution is integrated analytically to obtain the pressure forces and moments on the body. Then the laminar skin-friction drag is calculated by using the analytic pressure distribution. The development outlined is explained in more detail in the following sections.

Inviscid, Power-Law Body Solution

If, in inviscid hypersonic flow about a slender body, the velocity changes in the freestream direction are neglected compared with the transverse flow velocities, the hypersonic small-disturbance equations result. When a strong, power-law shock wave occurs in such a flow at infinite Mach number, these equations indicate that the body generating the shock also has a power-law shape. (See ref. 14.) Thus in figure 1(a), the shock wave $\frac{\overline{R}_0}{\overline{l}} = \delta\left(\frac{\overline{x}}{\overline{l}}\right)^m$ is generated by the body $\frac{\overline{r}_b}{\overline{l}} = \frac{1}{f}\left(\frac{\overline{x}}{\overline{l}}\right)^m$. In dimensionless form (fig. 1(b)) these relations become $R_0 = x^m$ and $r_b = \frac{1}{\delta f} x^m$. When the dependent variables are expressed in terms of the slope of the shock wave, the axial variations may be separated from the radial variations of the variables to obtain similarity equations. Thus in similarity variables $\xi = x$ and $\eta = r/R_0$; $R_0 = \xi^m$, $r_b = \eta_b \xi^m$, and the dimensionless pressure field is $p_0 = F_0(\eta) \left(\frac{dR_0}{d\xi}\right)^2 = m^2 F_0(\eta) \xi^{2(m-1)}$. Here $F_0(\eta)$ is found by solving a set of ordinary differential equations in η . (See refs. 14 and 15.)

In order to relax the restriction to infinite Mach number, Kubota (ref. 14) applied a small perturbation procedure. This procedure results in the following first-order pressure distribution and shock-wave shape about the power-law body $r_b = \eta_b x^m$:

$$P_{1}(\xi,\eta) = m^{2}F_{0}(\eta) \xi^{2(m-1)} + \epsilon_{1}m^{2}F_{1}(\eta)$$
(1)

$$R_{1}(\xi) = \xi^{m} \left[1 + \epsilon_{1} a_{1} \xi^{2(1-m)} \right]$$
(2)

Here $\epsilon_1 \equiv (M_\infty \delta)^{-2}$ is a small parameter corresponding to the hypersonic strong shock assumption $M_\infty \sin \theta >> 1$. The necessity of simultaneously satisfying $\delta^2 << 1$ and $\epsilon_1^2 << 1$ puts a strong requirement on the Mach number. That is, the present method is limited to $M_\infty >> 1$ so that with a slender body $\delta^2 << 1$, the parameter ϵ_1 is still small. Figure 2 shows the relationship between $\delta, \ \epsilon_1$, and M_∞ and can be used to check on ϵ_1 for a given Mach number and body shape (by noting that $\delta = 1/f\eta_b$).

The perturbed pressure variable $F_1(\eta)$ and the shock-wave displacement constant a_1 are found from a second set of ordinary differential equations. (See refs. 14 and 15.) The two sets of differential equations involve only m and γ as parameters, and thus they can be solved over the needed range of values and the tabulated results used in applications to flow problems. Table I and figure 3 present the results needed for the current application. They were found by numerical integration techniques similar to those described in reference 16. (With acess to modern digital computers, the exact numerical computation has become at least as easy to carry out as the approximate technique which gives ref. 16 its title.) The integrated pressure J_0 and pressure perturbation J_1 are defined as $J_0 \equiv \int_{\eta_b}^1 F_0(\eta) \, d\eta$ and $J_1 \equiv \int_{\eta_b}^1 F_1(\eta) \, d\eta$; they will be applied to the wing undersurface.

Corrections for Boundary-Layer Displacement

In order to make a corrected approximation accounting for laminar boundary-layer growth, a perturbed body shape $r_b^*(x) = r_b + \delta^*$ is used. The displacement thickness of the boundary layer is given by $\delta^* = \frac{2m\eta_b}{3-2m} \operatorname{Ex}^{3/2-m}$ (based on a result from ref. 17 for adiabatic wall conditions). Here $E \equiv \frac{\gamma-1}{\sqrt{2\gamma}} \operatorname{M}_{\infty} f^2 \operatorname{I} \eta_b \frac{3-2m}{2m^2\sqrt{4m-1}} \sqrt{\frac{C}{R_{\infty,\ell} F_0(\eta_b)}}$ which is very small for large Reynolds numbers. By using the appropriate value for I (the sum of the transformed displacement and momentum thicknesses in refs. 18 and 19), this relation for δ^* may be applied for any constant wall temperature. If the flow outside the boundary layer is considered to be the inviscid flow about the "perturbed body" $r_b^*(x)$, the corresponding pressure distribution and shock shape are approximated as follows. In terms of the body radius $r_b = \eta_b \xi^m$, equations (1) and (2) become

$$p_1 = m^2 F_0(\eta) \xi^{2(m-1)} + \epsilon_1 m^2 F_1(\eta) = \frac{F_0(\eta)}{\eta_b^2} \left(\frac{dr_b}{d\xi}\right)^2 + \epsilon_1 m^2 F_1(\eta)$$

and

$$R_1 = \xi^m \left[1 + a_1 \epsilon_1 \xi^{2(1-m)} \right] = \frac{r_b}{\eta_b} \left[1 + a_1 \epsilon_1 \left(\frac{1}{m \eta_b} \frac{dr_b}{d\xi} \right)^{-2} \right]$$

By replacing r_b by r_b^* (as in ref. 14), these equations become

$$p_1^*(\xi,\eta) = \frac{F_0(\eta)}{\eta_b^2} \left(\frac{dr_b^*}{d\xi}\right)^2 + \epsilon_1 m^2 F_1(\eta) = m^2 \xi^{2(m-1)} (1 + \epsilon^*)^2 F_0(\eta) + \epsilon_1 m^2 F_1(\eta)$$
(3)

and

$$R_{1}^{*}(\xi) = \frac{r_{b}^{*}}{\eta_{b}} \left[1 + a_{1} \epsilon_{1} \left(\frac{1}{m \eta_{b}} \frac{dr_{b}^{*}}{d\xi} \right)^{-2} \right]$$

$$= \xi^{m} \left[1 + \frac{\delta^{*}}{r_{b}} + a_{1} \epsilon_{1} \xi^{2(1-m)} \right] + \text{terms of order } \epsilon_{1} \epsilon^{*}$$
(4)

Here $\epsilon^* = \frac{d\delta^*/d\xi}{dr_b/d\xi} = E\xi^{\frac{3}{2}-2m} << 1$ except in a small region near the nose when $m > \frac{3}{4}$.

Simulation of Angle of Attack

The pressure distribution along the pitch plane of the body at angle of attack is assumed to be the same as that about an equivalent axisymmetric body. This effective body is at zero angle of attack. It has a power-law profile which closely matches the windward element in the plane of symmetry of the actual body at angle of attack. Figure 4 shows the relation between the real and effective bodies, and the following expressions are used to obtain the effective body parameters

$$\bar{x}_{e} = \bar{x} \cos \alpha - \bar{r}_{b} \sin \alpha$$

$$\bar{r}_{b,e} = \bar{x} \sin \alpha + \bar{r}_{b} \cos \alpha$$

$$f_{e} = \frac{\bar{l}_{e}}{\bar{r}_{b,e,B}} = \frac{1 - \frac{1}{f} \tan \alpha}{\tan \alpha + \frac{1}{f}} \approx \frac{f}{1 + f \tan \alpha}$$
(5)

and

$$\mathbf{m}_{e} \equiv \frac{\log_{e}(\mathbf{\bar{r}}_{b,2,e}/\mathbf{\bar{r}}_{b,1,e})}{\log_{e}(\mathbf{\bar{x}}_{2,e}/\mathbf{\bar{x}}_{1,e})}$$

so that

$$\frac{\bar{\mathbf{r}}_{b,e}}{\bar{l}_{e}} \approx \frac{1}{f_{e}} \left(\frac{\bar{\mathbf{x}}_{e}}{\bar{l}_{e}} \right)^{m_{e}}$$

Here \bar{x}_1 and \bar{x}_2 are points selected to provide a good approximation. A lower limit of $m_e \ge 0.51$ was set to avoid computational problems associated with the theoretical limit as $m \to 0.5$.

The approximating pressure distribution along the body at angle of attack is then

$$p_{1,e}^{*}(\eta_{b,e}) = \frac{m_{e}^{2}}{\kappa} \left[\left(1 + 2\nu^{2}E_{e}x_{e}^{\frac{3}{2}-2m_{e}}\right)F_{0}(\eta_{b,e})x_{e}^{2(m_{e}-1)} + \kappa\epsilon_{1}F_{1}(\eta_{b,e}) \right]$$
(6)

where

$$\nu \equiv \frac{f_e}{f} = \frac{1}{1 + f \tan \alpha}$$

$$\kappa = \left(\frac{\delta}{\delta_{e}}\right)^{2} = \nu^{2} \left(\frac{\eta_{b,e}}{\eta_{b}}\right)^{2}$$

and E_e is the same as E with m_e replacing m. (The factor κ appears since $p_{1,e}^* = \frac{p_{1,e}^*}{2\bar{q}\delta_e^2} = \frac{1}{\kappa} \frac{p_{1,e}^*}{2\bar{q}\delta_e^2}$) By following reference 6 which uses a similar angle-of-attack method for half-cone wing configurations, this pressure distribution is applied over the entire body surface. The pressure distribution under the wing from $\eta_b \le \eta \le 1$ is assumed to be the same as that in the flow field of the effective body from $\eta_{b,e} \le \eta \le 1$. Since this equivalent body approach does not attempt to account for the actual flow under the wing, its use necessarily limits the present method to very small angles of attack. For this reason all calculated results presented are in the range $\frac{1}{2} \le \nu \le 2$. Instead of calculating the wing upper surface pressure in detail, an average pressure is used. This value is taken from the charts of reference 20, which includes viscous-interaction effects on the pressure and skin friction on delta wings at angle of attack in hypersonic flow. Since the viscous effects are approximately proportional to $\kappa^{-1/2}$, delta-wing results for which $\int \int \kappa^{-1/2} dr \, d\kappa$ and the span equal to those of the power-law wing are used. The base pressure is set equal to free-stream static pressure p_∞ .

Skin Friction

The skin-friction contribution is the remaining term of the axial-force coefficient to be evaluated. In this report laminar boundary layers are assumed for all calculations. The wetted area is divided into the body surface, wing upper surface, and the exposed part of the wing underside, each of which is treated separately. For the skin-friction calculations for the body and the wing lower surface, the longitudinal pressure distribution is modified in the nose region by keeping a higher order term in the pressure equation. These calculations then use a scheme given in reference 18 for incompressible laminar boundary layers. Two transformations of the independent variables allow its use with the two-dimensional compressible laminar-boundary-layer similar solutions of reference 19 for the present cases. For the body, the Mangler transformation (ref. 18) changes the axial coordinate to that for an equivalent two-dimensional body. For the relatively small exposed-wing undersurface, a simplified flow model is applied, that is, streamlines are taken as parallel to the body surface, and the pressure is taken as varying parabolically from the body to the shock wave. In both cases the Stewartson transformation (ref. 19) changes the surface length and exterior velocity distribution to the form for an equivalent incompressible flow; the method of reference 18 is then applied. For the wing upper surface, the average skin friction from the appropriate charts of reference 20 is used just as for the upper surface pressure.

Longitudinal Aerodynamic Coefficients

Integrations of the appropriate components of the surface pressures over the body and wing give expressions for the axial force, the normal force on the body and on the

wing, and the pitching moment. In coefficient form the expressions are (to first order in ϵ_1 and ϵ^*):

$$\begin{split} C_{A} &= \frac{\pi(m+1)\delta^{2}m_{e}^{2}}{f\kappa} \frac{S}{S_{b}} \left\{ \left[\frac{1}{2(m_{e}+m-1)} + \frac{4\nu^{2}E_{e}}{4m-1} \right] mF_{0}(\eta_{b,e}) + \frac{\epsilon_{1}\kappa}{2} \left[F_{1}(\eta_{b,e}) - \frac{1}{\gamma m_{e}^{2}} \right] \right\} + C_{A,F} \\ C_{N,b} &= \frac{2m_{e}^{2}\delta^{2}}{\kappa} \left\{ \left(\frac{1}{2m_{e}+m-1} + \frac{4\nu^{2}E_{e}}{2m+1} \right) (m+1)F_{0}(\eta_{b,e}) + \epsilon_{1}\kappa \left[F_{1}(\eta_{b,e}) - \frac{1}{\gamma m_{e}^{2}} \right] \right\} \right\} \\ C_{N,w} &= \frac{2m_{e}^{2}\delta^{2}}{\kappa} \frac{\delta^{2}}{S_{b}} \left\{ \left(\left(\frac{1}{2m_{e}+m-1} + \frac{4\nu^{2}E_{e}}{2m+1} \right) \left(\frac{1-\eta_{b}}{1-\eta_{b,e}} \right) J_{0,e} + \frac{2}{\gamma+1} \left[\frac{4mE}{(3-2m)(4m_{e}-2m+1)} \right] \right\} \\ &+ \frac{\epsilon_{1}a_{1}}{2m_{e}-m+1} \right\} \left\{ (m+1) + \epsilon_{1}\kappa \left(\frac{1-\eta_{b}}{1-\eta_{b,e}} J_{1,e} - \frac{1-\eta_{b}}{\gamma m_{e}^{2}} \right) \right\} \\ C_{N} &= C_{N,b} + C_{N,w} - \frac{\bar{p}_{u}-p_{\infty}}{q_{\infty}} \\ C_{m} &= -\frac{(m+1)(m+2)m_{e}^{2}\delta^{2}}{\kappa} \left\{ \frac{1}{S_{b}\bar{c}_{b}} \left(\frac{1}{2m_{e}+3m-2} + \frac{4\nu^{2}E_{e}}{6m-1} \right) mF_{0}(\eta_{b,e}) \right. \\ &+ \frac{\epsilon_{1}\kappa}{3f^{2}} \left[F_{1}(\eta_{b,e}) - \frac{1}{\gamma m_{e}^{2}} \right] + \left(\frac{1}{2m_{e}+m} + \frac{4\nu^{2}E_{e}}{2m+3} \right) \left[F_{0}(\eta_{b,e}) + \frac{1-\eta_{b}}{1-\eta_{b,e}} \frac{\bar{J}_{0,e}}{\eta_{b}} \right] \\ &+ \frac{2}{(\gamma+1)\eta_{b}} \left[\frac{4mE}{(3-2m)(4m_{e}-2m+3)} + \frac{\epsilon_{1}a_{1}}{2m_{e}-m+2} \right] + \frac{\epsilon_{1}\kappa}{m+2} \left[F_{1}(\eta_{b,e}) \right. \\ &+ \frac{1-\eta_{b}}{1-\eta_{b,e}} \frac{J_{1,e}}{\eta_{b}} - \frac{1}{\gamma m_{o}^{2}\eta_{b}} \right] + \frac{\bar{p}_{u}-p_{\infty}}{q_{\infty}} \frac{s_{c}}{\bar{c}} \end{split}$$

The pitching-moment reference center is at the nose of the body (x = 0). For the corresponding zero-order and inviscid relations, set $\epsilon_1 = 0$ and E = 0, respectively. Note that the factors η_b and m+1 are associated with the actual planform area used in normalizing the coefficients.

These equations have been programed for calculation by a high-speed digital computer. The program includes the skin-friction calculations on the body and the wing

undersurface. There is a subsidiary program which computes the parameters required to get the upper surface pressure and skin friction from reference 20. The appendix presents an exposition of these programs. The basic program requires only 21600 octal storage locations after compilation on the Control Data Corporation 6600 computer at the Langley Research Center and runs an average case with 11 angles of attack in about 3 seconds of central processor time.

DISCUSSION OF RESULTS

Evaluation of Method

There have been no reported comprehensive experimental evaluations of the power-law, wing-body configurations to which the theoretical analysis applies. The data available fall into two groups: (1) drag of complete power-law bodies of revolution (no wing) at several Mach numbers and fineness ratios, and (2) aerodynamic characteristics of conical (m=1.0) wing-body configurations. Only a small part of these data satisfy the high Mach number, the slender body, and the strong shock criteria required for strict application of the similarity theory. Data for which the criteria are not well satisfied can be used to determine the limits for practical application of the method.

Power-law bodies of revolution.- The zero-angle-of-attack drag of these bodies is already calculated as part of the present method. Figure 5 contains four sets of comparisons with experimental data. The drag coefficients have been based on the length squared as reference area in each case to form a uniform basis of comparison. In parts (a) and (b) of figure 5, the ratio V/t^3 was held constant and yielded a small variation in the fineness ratio as the power-law exponent was varied to obtain the different bodies for the tests. Figure 5(a) is for tests at Mach 21.6 in helium (ref. 12). The agreement is very good. The coefficients in figure 5(b) are for tests at Mach 10.03 in air (ref. 21); the calculations are in good agreement with experiment. Figure 5(c) shows good agreement at Mach 10.35 for a series of power-law bodies having nearly equal fineness ratios. In figure 5(d) the data for the same bodies at Mach 5.96 is not predicted.

The range of agreement obtained in figure 5 should be considered in light of the basic assumptions of the theory as discussed in the previous section. For this reason the pertinent parameters are shown in the legends of figure 5 and also in figure 2. Since $\delta << 1$ for all cases, the slender body condition is well satisfied. The hypersonic assumption $\left(M_{\infty} >> 1\right)$ is generally considered to be satisfied for M > 5 and so should not cause the discrepancies in figure 5. However, the strong shock assumption $\left(\epsilon_1^{\ 2} << 1\right)$ is satisfied only for figure 5(a), where the agreement is very good. This result shows the

importance of evaluating ϵ_1 to determine whether the theory can reasonably be applied to any particular configuration and free-stream conditions.

As an additional comparison with the present method and the experimental data, drag coefficients based on the simple Newtonian pressure equation $C_p = 2 \sin^2\!\theta_b$ and on inviscid conical flow were calculated and are presented in figure 5. The Newtonian prediction and inviscid conical solution drag values are low since viscous interaction effects on the surface pressure become important on high-fineness-ratio bodies at high Mach numbers.

As noted in reference 22, entropy layer effects become important for power-law exponents less than $m=\frac{\gamma+1}{2\gamma+1}$ ($m\approx 0.63$ for $\gamma=1.4$); therefore, the theoretical predictions (which do not include these effects) can be expected to be poorer in that range. A less subtle limitation occurs at m=0.5, where $\eta_b=0$; that is, the ratio of shock-wave radius to body radius becomes infinite. This case is the "blast wave" solution for blunt-nosed bodies of negligible thickness (for example, a cylindrical rod) as described in references 15 and 22. For bodies with nonzero radius, as in figure 5, the predicted shock-wave radius goes to infinity as $m\to 0.5$ and so does the wave drag. Thus, the theory is not useful for the blunter shapes.

Wing, conical-body configurations. Theoretical estimates for wing conical body configurations can be compared with the experimental data in reference 23. The bodies in this reference were halves of right, circular cones, corresponding to m=1. The wings were thin flat plates. The normal- and axial-force coefficients for configurations with the first-order Mach number and boundary-layer thickness corrections to the wing planform shapes are presented in figure 6. The present theory is in good agreement with the experimental data near an angle of attack of 0° , but deviates from it elsewhere. The deficiency in the angle-of-attack method is such that the errors in C_A and C_N are generally about equal and in the same direction. This condition results in the good prediction of the lift-drag curve (drag polar) shown in figure 7, which produces lift-drag ratios agreeing well with the experimental values. Figure 7 also shows the pitching-moment coefficient, the theory generally agreeing well with experiment near $\alpha=0^{\circ}$.

Other data for comparison with theory may be found in references 6 and 7. The wings for the configurations tested had delta planforms with several leading-edge sweeps. Consequently, they cannot match the shapes used by the theory, but at small angles of attack, where the wing alone produces little lift or drag, the aerodynamic coefficients should be comparable if they are based on the areas of delta wings approximating the theoretical planforms. Figure 8 shows such a comparison at Mach numbers 6.86 (ref. 6) and 20 (ref. 7). The theoretical drag polars and the lift variation with angle of attack

at M=6.86 agree well with the experimental points, especially near $\alpha=0^{\circ}$ (fig. 8(a)). The pitching moment about x=2l/3 is predicted well near $C_L=0$, but the slope shows an almost neutrally stable trend whereas the experimental data show the configuration to be somewhat more stable. The difference in the distribution of wing area between the experiment and theory would contribute to this effect.

Maximum lift-drag ratios for the same configurations (and some with smaller cone angles) in helium at Mach 20 are shown in figure 8(b). The predicted values agree fairly well with experiment considering the differences in wing shape and area.

Example Application of Method

The preceding comparisons with experimental results have shown that the present theoretical method gives good predictions of the lift, drag, and lift-drag ratio and fair estimates of the pitching moment for small angles of attack as long as the basic assumptions of the theory are met. Thus, the method should be useful for studying the general characteristics of the power-law-body flat-wing configurations at high Mach numbers. Just two parameters, the power-law exponent m and the fineness parameter f, completely specify these body shapes. For the wings the Mach number is the principal additional parameter required, although the Reynolds number, ratio of specific heats, and wall temperature also enter through the boundary-layer growth perturbation. In order to assess the effects of these three main variables, the theory was used to predict the aerodynamic characteristics of a family of full-scale configurations at two Mach numbers. The chosen altitude was 30 km for which the unit Reynolds numbers are $2.21 \times 10^6/\text{meter}$ and $4.42 \times 10^6/\text{meter}$ at the chosen Mach numbers of 6 and 12, respectively, based on the 1962 standard atmosphere (ref. 24). The body volume was set at 2500 m³, giving lengths of 28.2 m to 78.1 m (approximately 92.5 ft to 256 ft), for $0.63 \le m \le 1$ and $2.5 \le f \le 10.0$. Additional assumptions were $\gamma = 1.4$ and a ratio of wall temperature to total temperature of 0.41667. For each Mach number the range of the fineness parameter was chosen to keep $\delta^2 << 1$ and $\epsilon_1^2 << 1$. The results of these calculations are presented in figures 9 and 10.

Effect of power-law exponent. Varying the body power-law exponent while holding the fineness parameter constant at f=5 for Mach 12 flight at an altitude of 30 km produced the curves shown as figure 9(a). The drag polars in the range $0.63 \le m \le 0.75$ all cluster together, and hence so do the lift-drag ratios. Only in the conical case (m=1) does the drag fall significantly higher and the lift-drag ratio lower. The pitching moment does show a major variation with m, both in slope and intercept. As m decreases from 1.0 to 0.63, that is, as the nose becomes blunter and the aft end less flared, the

zero lift pitching moment $C_{m,0}$ increases. At the same time, the stability decreases, configurations with m < 0.75 becoming unstable for the moment reference center at $\bar{x} = 0.6\bar{l}, \bar{y} = 0.15\bar{r}_{b,B}$. Since the effect of m on the lift-drag ratio is relatively small, this parameter could be chosen to minimize the trim drag.

Effect of fineness ratio. The computed characteristics for a range of values of the fineness parameter f are shown in figure 9(b). For this family of configurations, the power-law exponent was set at m=0.75, and the curves are for Mach 12 flight at 30 km as before. At low values of f the peaks in L/D are low and broad and become higher and sharper as the bodies become finer. The stability of the configurations is practically unaffected by variations in the fineness parameter, as indicated by the almost parallel pitching-moment curves.

Effect of Mach number.- Figure 9(c) shows a comparison of Mach 6 calculations with those for Mach 12 for configurations having three of the power-law body shapes. Note that the change in Mach number makes a change in the wing planform for each body shape. The effect on the drag polars shows clearly in the three sets of curves. At Mach 6 the zero lift-drag coefficient $C_{D,0}$ is higher but the drag due to lift is lower than at Mach 12. Since the curves cross before $(L/D)_{max}$ is reached, the Mach 6 curves of L/D peak higher and at larger C_L values than the Mach 12 curves. If the same reference area had been used, the C_L difference would have been larger since the Mach 12 design wing is smaller. The pitching-moment curves are little affected by the Mach number change.

Summary of calculations.- The results of the Mach 6 and 12 calculations for flight at 30 km are summarized in figure 10. As was indicated in figure 9, the effect of the power-law exponent m on $(L/D)_{max}$ is relatively small. For the low fineness ratios, the curves form broad maxima centered near m=0.7; they become more peaked and move toward m=0.8 as the fineness ratio increases. This result compares with the value m=0.75 determined from the Newtonian pressure law as the power-law exponent for minimum drag bodies under length and diameter (that is, fineness ratio) constraints. There is a stronger dependence of the associated lift coefficient $C_{L,(L/D)_{max}}$ on the value of m, particularly for the less fine bodies. The effect of the fineness parameter on $(L/D)_{max}$ and $C_{L,(L/D)_{max}}$ is opposing in that increasing f increases $(L/D)_{max}$ (and its dependence on m) but decreases $C_{L,(L/D)_{max}}$ (and its dependence on m). (At any given lift coefficient in the range of calculation, however, L/D can be increased by going to a finer body; see fig. 9(b).) The curves of $\alpha_{(L/D)_{max}}$ are included in figure 10 in order to show that the calculations of $(L/D)_{max}$ occur within the range of small angles of attack for which the present method gives its best results. (See fig. 6.)

CONCLUDING REMARKS

This paper has presented a method for calculating the longitudinal aerodynamic characteristics of a family of configurations in hypersonic flow. These configurations each consist of a half-axisymmetric power-law body surmounted by a thin flat wing for which the planform matches the analytical shock-wave shape about the body at an angle of attack of 0°. The method is based on the power-law similarity solutions of the hypersonic small-disturbance equations. These solutions require three basic assumptions: the Mach number is large, the body is slender, and the shock wave is strong. A first-order perturbation allows the calculation of Mach number effects, and a perturbation to the body shape provides for the boundary-layer growth. Skin friction is accounted for by using compressible, laminar boundary-layer solutions at the computed pressure distributions integrated over the body and wing surfaces. A computer program has been written implementing this method; sample computations using the program have taken only a few seconds per case.

When compared with experimental data for axisymmetric power-law bodies and for wing—conical-body configurations, the present method gave good agreement where the basic assumptions were satisfied. An example series of computations with variations in the principal parameters at a full-scale flight condition showed that varying the power-law exponent has a greater effect on longitudinal stability and trim than on the lift-drag ratio. The computations for Mach 6 gave higher maximum lift-drag ratios, higher drag coefficients at zero lift, but essentially the same stability characteristics as their counterparts for Mach 12.

Langley Research Center,

National Aeronautics and Space Administration,

Hampton, Va., October 25, 1973.

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APPENDIX

COMPUTER PROGRAM FOR CALCULATING THE AERODYNAMIC CHARACTERISTICS OF POWER-LAW WING-BODY CONFIGURATIONS

The calculation procedure described in the main body of the paper for obtaining the aerodynamic coefficients for power-law wing-body configurations at hypersonic speeds has been programed for high-speed digital computation. The program will also compute the zero angle-of-attack drag for an axisymmetric power-law body alone. The purpose of this appendix is to provide a description of the necessary input and available output as well as a FORTRAN IV (ref. 25) listing of the source program. A separate program to compute the parameters needed to obtain two input values from the figures of reference 20 is also listed and described.

Description of Program

First, the program reads all the input variables describing the case to be computed. After calculating geometric constants, it goes through the angles of attack, computing the body axis forces and moments, interpolating the similarity solution parameters from a stored table. Skin friction is calculated for each angle of attack and added to the axial force. The results are then transformed to the stability axes. If at least three angles of attack are included in a case, a quadratic interpolation of the drag polar is made to obtain $(L/D)_{max}$ and other quantities, which are printed out along with the body- and stability-axis coefficients. A summary subroutine assembles certain quantities for separate printout after completion of all cases.

Program Listing

The FORTRAM IV listing of the source program used on the Control Data series 6600 computer system at the Langley Research Center is as follows:

```
PPCGRAM HYPAERO(INPUT=20], BUTPUT=40], TAPFS=INPUT, TAPE7=601)

C

HYPERSONIC AERODYNAMIC CHARACTERISTICS OF POWER-LAW WING-BODY CONFIGURATIONS

DIMENSION HEAD(8), Y(6), YE(5), VARD(13,6), VARI(13), ANGL(11), A 2
1 SINE(11), COSE(11), PBBPOL(11), CFDCFO1(11), PUPIQI(11), CNB(11), A 3
2 CND(11), CNW(11), DPSRYOS(11), CN(11), CAP(11), CAF(11), CA(11), A 4
3 CL(11), CD(11), CLCD(11), CMCG(11), CDANGL(11,2), CDALO(2), A 5
4 CDALN(2), X(19), XW(19), PB(19), DSWCOS(19), DSWCSL(7,6), A 6
5 CCSSL(18), TXSE(18), DELR(18), PTWP1(18)
EQUIVALENCE (Y,ETAB), (Y(2),FO), (Y(6),A1), (YE,ETABE), A 8
1 (YE(2),FOE), (YE(3),FIE), (YE(4),DJOE), (YE(5),DJIE), A 9
2 (ANGL,CD(12),CDANGL(12))
```

```
COMMON &P, ZIME, E2U2, FOE, FIEK, THG12G, TWM, EMBF2, D2ME2K, X2M, WING, F01,
                                                                                     11
     1 Flik, DLR, FTB, ONETB, XSE, GMA, GM1, GM12, GP12, EM, EM1, EM32, ZMM, ZEM11,
                                                                                     12
                                                                                     13
                                                                                  Δ
     2 THP 2M, &MCH2, DEL, TWEM, AEP
      NAMELIST /DATA/NCASE,GAM,TINE,AMCH,NALE,ANGL,EM,F,REL,SSB,XCG,YCG,
                                                                                     14
                                                                                     15
     1 PRPT, CAFACTR, ANGO, XOUT, PBBPOL, CFDCFO1, ALAMCR, BDYONLY, DEL, EPS, XSE
                                                                                  Δ
                                                                                  Δ
                                                                                     16
     2 /CUT/T,ANG,ANGO,FME,YE,EMI,CAFB2,CAFU,CAFL,AI,PTWP1
    VARY = EM, VARD = ASSOCIATED VALUES OF ETAB, FO, F1, DJO, DJ1, A1 FROM TABLE
                                                                                    Ţ
۴
      DATA X/0.,.0003,.0006,.0009,.0012,.0018,.0024,.0036,.005,.0085,
                                                                                     17
                                                                                     18
      1 .015,.025,.045,.08,.14,.25,.45,.7,1./, PI,PIF,DTOR/3.14159265359,
                                                                                  A
     2 2.6586808,.01745329252/, KP, LLIM, ML, ML1, NCASE/-1,19,18,17,1/,
                                                                                  Д
                                                                                     19
     3 VART, VARD/1 - - - 95, -9, -85, -8, -75, -7, -666667, -633333, -6, -55, -53, -51,
                                                                                     20
                                                                                  Δ
     4 .914934, .91034, .90465, .89743, .88798, .87507, .85648, .8388, .81391,
                                                                                  Δ
                                                                                     21
                                                                                  A
                                                                                     22
     5 .77647, .66414, .56901, .37221, .87445, .84711, .8163, .78174, .74265,
     6 .69806, .64662, .60763, .55403, .51478, .42678, .385, .33757, .9179,
                                                                                  ٨
                                                                                     23
     7 1:0591,1.2306,1.4286,1.6887,1.9811,2.2986,2.4964,2.6392,2.6593,
                                                                                     24
     8 2.251,1.8876,1.411, .07323,.07589,.07909,.08303,.08799,.09444,
                                                                                  A
                                                                                     25
                                                                                  Δ
     9 .10318, .11098, .12129, .13554, .17318, .20119, .25443, .0841, .09551,
                                                                                     26
     X .11044, .13067, .15918, .20098, .26458, .32562, .40794, .51763, .74598,
                                                                                     27
                                                                                  Δ
     1 .86687,1.0411, .47569,.52709,.58604,.65291,.72741,.80732,.88631,
                                                                                  ٨
                                                                                     28
                                                                                     29
     2 .93216, .96566, .98034, .96791, .96377, .97539/,
                                                                     GAM/1.4/+
                                                                                  A
     3 SSB, TWTT, PBPJ, CAFACTR, XE, XOUT/0., 415667, 1., 1., . 10, . FALSE./ ..
                                                                                     30
                                                                                  A
      ENGICAL TEMIN, BOYONLY, WING, XOUT
                                                                                  Α
                                                                                     31
                                                                                  ٨
                                                                                     32
      EXTERNAL FUNT
                                                                                  A
                                                                                     33
      BDYONLY=.F4LSE.
                                                                                  ٨
                                                                                     34
      PEAD 38, HEAD
Į
                                                                                  Ą
                                                                                     35
      IF (ENDFILE 5) 32+2
                                                                                  ٨
                                                                                     36
      PEAD DATA
2
                                                                                  Δ
                                                                                     37
      CLDMX=0.
                                                                                  ۸
                                                                                     38
      COMIN=1.
                                                                                  Δ.
                                                                                     39
      TFMIN=.FALSE.
      GO TO (3,4,5,6), NCASE
                                                                                     40
    NCASE = 1) GAM, 2) AMCH, TINF, 3) EM, 4) F, REL, SSB HAVE NEW VALUES
C
                                                                                     41
      GM1=GAM-1.
3
                                                                                     42
                                                                                  Δ
      ZGM1=2./GM1
                                                                                  A
                                                                                     43
      GM12=.5*GMl
                                                                                  A
                                                                                     46
      CPI=GAM+1.
                                                                                     45
                                                                                  ۸
      GP12=+5*GP1
                                                                                  A
                                                                                     46
      F01=1./GP12
                                                                                  A
                                                                                     47
      GMA=GAM
                                                                                  Δ
                                                                                     48
      GP14=.25*GP1
                                                                                  A
                                                                                     49
      ZGG1=GAM*ZGM1
                                                                                  ٨
                                                                                     50
      7G1G=-4./ZGG1
                                                                                     51
                                                                                  Δ
      GMT=1./GAM
      ZG2G=GMJ-.F
                                                                                  A
                                                                                     52
      GP1G=GP1*GMI
                                                                                  ٨
                                                                                     53
                                                                                  ٨
                                                                                     54
      GF=.12*(2.*GAM)**1.5*GP12**GP1G
                                                                                     55
                                                                                  A
      GX1=-GM1*GMT
                                                                                     56
                                                                                  Δ
      G77=-.77/GX1
                                                                                     57
      THG12G=1.-.5*GX1
      RT8GT=1./SQRT(8.*GAM)
                                                                                  A
                                                                                     58
                                                                                  ٨
                                                                                     59
      AT1=1.217*TWTT+.4704
                                                                                  A
                                                                                     50
       AT2=TWTT++34A
      RTTWTT=SQRT(TWTT)
                                                                                  ۵
                                                                                     61
                                                                                  A
                                                                                     62
       AMCH2=AMCH*AMCH
                                                                                  A
                                                                                     63
       AMCH3=AMCH*AMCH2
                                                                                  ۸
                                                                                     64
      AMI=1./AMCH2
                                                                                  ٨
                                                                                     65
       TTBTI=1.+GM12*AMCH2
      RTTTBTI = SQRT(TTBTI)
                                                                                  A
                                                                                     66
      SUTH=198.6/(TINE*TTBT!)
                                                                                  Α
                                                                                     67
                                                                                  Δ
                                                                                     68
       ALAM=((1.+SUTH)/(TWTT+SUTH))*RTTWTT
       SUTHI=198.5/TINE
                                                                                     69
      C2=((1.+SUTH)/(1.+SUTHI))*RTTTBTI
                                                                                  A
                                                                                     70
                                                                                  A
                                                                                     71
       PTC1=SQPT(ALAM/C2)
       TPTT=.273+(.195+.532*TWTT)*TTBTT
                                                                                  Δ
                                                                                     72
      PTC3=SQPT((1.+SUTHI)/(TPTI+SUTHI)*SQRT(TPTI))
                                                                                     73
                                                                                  A
                                                                                     74
                                                                                  Δ
       GCMG=GF*PTC1*AMCH**GP1G
                                                                                     75
      PO=2.*AMI*GMI
```

```
5
      EMP1=EM+1.
                                                                                  76
      FMP12=.5*FMP1
                                                                                  77
      EMP2=EM+2.
                                                                               A
                                                                                  78
      FMM1=FM-1.
                                                                               A
                                                                                  70
      7MM1=?.*EMM1
                                                                               A
                                                                                  80
      TWM=7.*EM
                                                                               A
                                                                                  81
      THR2M=3.-TWM
                                                                               A
                                                                                  82
      ZMM=2.-EM
                                                                               A
                                                                                  83
      EMI=1./FM
                                                                               A
                                                                                  84
      ZFMI1=2.*(EMI-1.)
                                                                               A
                                                                                  85
      FM32=1.5*EMI-2.
                                                                               A
                                                                                  86
      ZGM132=1.F+ZMM1*GMI
                                                                               A
                                                                                  87
      ZMP1I=1./(EMP1+EM)
                                                                               A
                                                                                  88
      TWM3I=1./(EMP1+EMP2)
                                                                               A
                                                                                  89
      EM4I=1./(4.*EM+1.)
                                                                               A
                                                                                  90
      SIXMI=1./(6.*EM-1.)
                                                                               Á
                                                                                  91
      THRMM != 1 . / (3 . - EM)
                                                                               Α
                                                                                  92
      FIV2M1=1./(5.-TWM)
                                                                               Δ
                                                                                  93
      FM4019=.4019*EM
                                                                               A
                                                                                  94
      FMX1!=1./(1.5303-FM4019)
                                                                                  95
                                                                               Δ
      FMX152M=FTV2MT/EMX11
                                                                               A
                                                                                  96
      EMX2=.5/(.9274+EM4019)
                                                                               A
                                                                                  97
      TP=20.*(1.05-EM)
                                                                               A
                                                                                  98
      AI=AT1-AI2*EMM1/(EMM1-G37/EM4I)
                                                                               Δ
                                                                                  99
      CALL MTLUP (EM, Y, 2, 13, 13, 6, IP, VARI, VARD)
                                                                               A
                                                                                 100
      ETABI=1./ETAB
                                                                               A
                                                                                 101
      ONETET=ETABI-1.
                                                                               A 102
      ZG1ET=ETABI/GP12
                                                                               A 103
      ETB=ETAB
                                                                               A 104
      ONET8=1./(1.-ETAB)
                                                                               A 105
      AMCHN=(1.-ZMM1*(AMCH-1.))**GMI
                                                                               A 106
      GETIEMF=GCMG*ETAB*AI*SQRT(EM41)*(EM*EM*FO)**ZGZG/AMCHN
                                                                               A 107
      F11=F01*(A1*(ZGG1+2./GP1G-EMI/GM1)-EMI*EMI/ZGG1)
                                                                               A 108
      F[=1./F
6
                                                                               A 109
      EMBF7=(EM*FI)**2
                                                                               A 110
      FSQ=F*F
                                                                               A 111
      FM1M2F2=EMP1*EMP2/FSQ
                                                                               A 112
      RTRELI=1./SQRT(REL)
                                                                               A 113
      ESAV=GM1*AMCH*FSQ*RTC1*RTRELI*RT8GI
                                                                               A 114
      DEL=ET4B1*FI
                                                                               A 115
      FPS=AMY/(DEL*DEL)
                                                                               A 116
      AEP=A1*EPS
                                                                               A 117
      EMSAV=4.*ESAV*AT*ETAB/(EM*SQRT(FO/EM4I))
                                                                               A 118
      TWEM=EMSAV*.5.
                                                                               A 119
      RSE=SORT(GETTEME*RTRELI*DEL**ZG1G*XE**ZGM132)
                                                                               A 120
      PT2P1=PTOT(RSE)
                                                                               A 121
      RTROLT=SQRT(AMCH*PTTTBTI**3/(C2*PEL*PT2P1))
                                                                               A 122
      AEPX=AEP=EMX152M
                                                                               A 123
      EM32X=+25*EMSAV*EMX11
                                                                               A 124
      G2MRF=+69053*GM12*AMCH3*RTC3*RTRELI
                                                                               A 125
      EMFSAV=0.
                                                                               A 126
¢
C
    WING GEOMETRIC PARAMETERS AND FLOW CONSTANTS
      SISTSB=ETABI*(1.+FMP1*(AEP*THRMMI+EMS4V*FIV2MI))
                                                                               A 127
      SBBYS=1./SISTSB
                                                                               A 128
      IF (SSB.GT.O.) SBBYS=1./SSB
                                                                               A 129
      SISTBYS=SISTSB*SBBYS
                                                                               A 130
      DEL?=DEL*DEL
                                                                               A 131
      PTMS=.5*PT*EMP1*SBBYS
                                                                               A 132
      RTCRELT=SQRT((1.+AEP+TWEM)/(PIF*(EMX2+AEPX+EM32X)))
                                                                               A 133
      XSC=FMP12
                                                                               4 134
      ALAMCR=G2MRC*RTCRELI
                                                                               A 135
      POLAM=-PO*ALAMCR
                                                                               A 136
      CFOCR=1.328*RTC1*PTRELI*RTCRELI*S1STBYS
                                                                               A 137
      CAFLC=2.*ALAM*AMI*RTROLI
                                                                               A 138
      CFCON=PT2P1*C4FLC
                                                                               A 139
```

```
A 140
      FMETS=EMP1*ETAB1*SBBYS
                                                                               A 141
      M=3
                                                                               A 142
      KK1 = (ML-1)/M+1
                                                                               A 143
      KK=KK1+1
                                                                               A 144
      K≂K<sub>K</sub>
                                                                                A 145
      MK = M * (K-2) + 1
                                                                               A 144
      OSWCOS(LLIM) =PIMS
                                                                               A 147
     PB(LLTM)=ETAB
      Ll=tliw
                                                                               A 148
                                                                               A 149
      COSSL=0.
                                                                               A 150
      PS=1.+TWEM+AEP
      XW(KK)=].
                                                                               A 151
                                                                               A 152
      COSSL(KK)=1./SQRT(1.+EMBF2)
                                                                                4 153
      DO 8 LL=1,4L1
                                                                               A 154
      L=LLIM-LL
                                                                               'A 155
      XL=X(L)
                                                                                A 156
      XM=XL**FM
                                                                               A 157
      DSWCOS(L)=PIMS*XM
                                                                               A 158
      IF (BDYONLY) GO TO 8
                                                                               A 159
      PR(L)=FTAB*XM
                                                                                A 160
      IF (MK.NE.L) GO TO 8
                                                                               A 161
      K1=K
                                                                                8 162
      K=K-1
      MK = M * (K-2) + 1
                                                                                A 163
                                                                                A 154
      XW(K) = XL
                                                                               A 165
      XSE=.5*(XW(K1)+XL)
                                                                               A 166
      TXSE(K)=XSE
                                                                               A 167
      PTWP1(K)=PTOT2(RSE)
                                                                               A 168
      DELP(K)=RSE-ETAB*XSE**EM ...
                                                                                A 169
      RSK1=RS
                                                                                4 170
      XM12=(XM/XL)**2
      PS=XM*(1.+(TWEM/SQPT(XL)+AEP)/XM12)
                                                                               A 171
                                                                                A 172
      COSSL(K)=1./SQRT(1.+EM8F2*XM12)
                                                                               A 173
      DRMIS=EMETS*(RSK1-RS-RB(LI)+RB(L))
                                                                                4 174
      DSWCSL(K,K)=DRM1S*.25*(COSSL(K)+COSSL(K1))
                                                                               A 175
      Ll=t.
                                                                               A 176
      00 7 J=K1,KK
      DSWCSL(J+K)=DRM1S*COSSL(J)
                                                                                A 177
7
                                                                               A 178
      CONTINUE
R
                                                                               A 179
      DSWCOS=PIMS*(-1*X(2))**EM
      IF (BDYONLY) GC TO 10
                                                                                A 180
                                                                                A 181
      XW=0.
                                                                                A 182
      XSE=.5*X\(2)
                                                                                A 183
      TXSE=XSE
                                                                                A 184
      PTWP1=PTGT2(RSE)
                                                                                A 185
      DELR=PSE-ETAB*XSE**EM
      DRMIS=EMETS*(RS-RB(L1))
                                                                                A 186
                                                                                A 187
      DSkCSt=DRMIS*.25*COSSL(2)
                                                                                A 188
      DO 9 J=2,KK
      DSWCSL(J, 1) = DRM1S*COSSL(J)
                                                                                A 189
9
      XL1=X(6)
                                                                                A 190
                                                                                A 191
      XL2=X(1.6)
      PL1=88(6)
                                                                                A 192
                                                                                A 193
      PL2=RB(16)
C
C
    ANGLE OF ATTACK VARIATION
r
      ANGO=DEL#(9B(ML)-ETAB)/(1.-X(ML))
                                                                                A 194
      PRINT DATA
                                                                                A 195
10
                                                                                A 196
      PRINT 36, HEAD
                                                                                A 197
      NANG=NALF
                                                                                A 198
      DO 28 1=1, NANG
                                                                                A 199
      ANG=DTDP*ANGL(I)
                                                                                A 200
      TE (NCASE-3) 12,11,11
```

```
Z92 ₹
                                                                    Eijk=Eij*EK
192 ₹
                                                                    09Z ¥
                                                                     EK≖ED2¢C∀A
652 ¥
                                                      EESVA=7°\(\SWEW-7°)+EVAN
852 ¥
                                                              ECOM=EECOS+INDII
                 EEPOUS=0.**U2*(ESAV*A1*ETA BE*THR 2ME/(EME2*SORT(FOE*FRME1)))
152 A
952 V
                                                                    DSw20==35w20
$52 ¥
                                                                 Dak25=5**DSW2
                                                             DSWS=DSWESK#286AS
952 ₹
€52 ¥
                                                          DSWESK=DECS*EMES/CVA
                                                               CA*TARTH*SU=YAT
7 52 V
                                                                                    ءَڃَ
              BODA WX/2 COEFFICIENTS FROM INTEGRATED WING AND BODY PRESSURES
                                                                                     Э
                                                                                     J
¥ 521
                                                       THETA-DUCE*ETEII*ONFIEL
V 250
                                                                 とりとはゴーをいりませいだ
692 ₹
                                                                    EOEM=EOE≠EM
842 ¥
                                                                 CMESI≃CMI\EMES
                                                                    SIME-2.-IME
745 A
9+2 ¥
                                             V1=011-015*EWEI\(EWEJ-031*EKWEI)
                                                                    EWEI=EWE-I*
    A
542
                                                                  1H65WE=3"-IWE
442 V
E + 2 V
                                                                    ZMEM=ZME+EM
242 ¥
                                                                     SWE=S° *EWE
                                                                  Eskej=EbWE-j.
THZ Y
                                                                    EGNE=4.4EME
0+2 ¥
SEZ V
                                                                   さいしゅうしゅう こうしょうしょうしょう
8 £ Z ¥
                                                           FTELT=1./(L.-ETABE)
₹ 23 ₹
                                                             18AT9=4364T2=TA9T9
                                  CALL MILUP (EME, YF, 2, 13, 13, 5, 19, VARI, VARD)
SES A
582 A
                                                                     EMESVA=EME
                                                                                    22
AES A
                                                     LE (EWE-EWERVA) SS*S3*SS
                                                                                    1.2
EE2 8
                                                                        EWE=1.0
                                                                                    02
                                                                       14 OT 00
232
    ٧
                                                                        "S"=3W3
TEZ ¥
                                                                                    ōΪ
A 230
                                                         1E (EWE-21) 10*57*51
                          EWE=ALGGIRHOPAT)/ALGG((XL2-PL2*TN)/(XL1-RL1*TN))
622 ¥
                                                                                    8 r
                                                          IE (RHOPAT) 19,19,18
822 A
TSS A
                                             RHORAT = (RL2 + XL2 + TN) / (RL1 + XL1 + TN)
                                                         IF (FM.EQ.1) GC TO 20
922 A
                                                            13=1 *\(1 * + E + LN | + + 5
ZZZ A
722 V
                                                            IN=SING(I)\CGSE(I)
                                   EEEECLIAE BODA SHVDE DAE 10 VACTE DE VILVÇK
                                                                                     C
V 223
                             DB2BA02(1)=2721BA2*(b0FFW*bBBb0F(1)-bNbIOI(I))
                                                                                    Lī
                                                  PRINT 22. ANGL(II, PUPIQI(I)
Z22 ¥
122 A.
                                                         bNb101(1)=b0*(b0E-I*)
                                                         ie (₽∩€,LT.0.) POE=0.
OSS A
                                                       b0E=(I*-@WIS*C@0)**S@0I
                                                                                    91
612 ¥
                                                                       72 DI 09
812 A
                                                                         EME=FM
TIS A
                                                                           1=01
A. 216
                                                                           15=11
ZIS A
                                                                                    śΙ
                                           0.058Y05(1)=515T8Y5*P0LAM*P8BP0L(1)
A 214
                                                                       85 01 00
EIS A
                                                             baint 324 ANCE(I)
A 212
112
    ٧
                                                                    NVVC=NVNC-I
                                                    TE (ANGC.LE.ANG) GO TO LT
                                                                                    41
A 210
                                                  PRINT 33, AMGL(I), PUPIQI(I)
4 209
                                                         t*[-S0d]*0d=[1]10]dNd
805 A
                                  bu2=1"+CVM*LVO*(CbIKU+2061(I"+CbIKO+*5))
TOS A
¥ 50€
                                                               CbikOc=Cbic*CVO
                                                                                    ٤1
                                                             1E (VAC) 13+12+10
502
    A
                                                             CVC=VBS(AMCH*ANG)
402 A
EOS A
                                                  CO2E(1)=2061(1"-21ME(1)**5)
                                                                                    15
205. A
                                                              CIVE(1)=2IN(#NC)
                                                             It (100) 14-12-11
                                                                                     11
IOS A
                                                     MING UPPEP SURFACE PRESSURE
```

J

```
A 263
      EKGO=FK*GME?!
                                                                            4 264
      EPSEVO=E1EK-PBPT*EKGO
                                                                            A 265
      FPSAV1=F15K-EKGO
                                                                            A 256
      FPSAV2=NNETET*(FK*DJ1E*FTE11-EKGO)
                                                                            A 267
      CNR(T)=D2MS2*(FDEM1*EFSAV+EPSAV1)
      CND(I)=D2MS2*F0EM1*EME*ETPAT*EE4U2/((ZME+1.)*THR2ME)
                                                                            4 268
     CNW(1)=D2MS2*(EMP1*(DJETB*EFSAV+ZG1ET*(EMSAV/(FRME1-ZMM1)+AEP/
                                                                            A 269
                                                                            A 270
     1 (ZMF-EMM1))-EME*ETPAT*E4UM*F0E/THR2ME)+EPSAV2)
                                                                           A 271
      CAP(T)=PT*D2MS*EMP1*FT*(FOEM*(1./(ZME+ZMM1)+EE4U2*EM41)+.5*EPSAVO)
                                                                            A 272
     CN(I)=CNB(I)+CND(I)+CNW(I)+DPSBYQS(I)
     CMN=D2MSC*FMP1*(FMP2*((FOE+DJETB)*(1./ZMEM+FE4U2*TWM3I)+
                                                                             A 273
                                                                            A 274
     1 ZG1ET*(FMSAV/(FRME+THR2M)+AEP/(ZMEM-ZMM1)))+EPSAV1+EPSAV2)
                                                                            A 275
      CMA=D2MSC*EM1M2F2*(F0EM*(1./(ZMEM+ZMM1)+EE4U2*SIXMI)+EPSAVO/3.)
      CMCG(T)=CMN+CMA-XSC*DPSRYQS+.5*EMP2*(CN(I)*XCG+CAP(I)*FI*YCG)
                                                                             A 276
¢
    SKIN FRICTION ON BODY
r
                                                                             A 277
      FOE=FOE
                                                                             A 278
      E2U2=.5*EE4U2
                                                                             A 279
      APC=GAM*EME2/EK
                                                                             A 280
      SP=SPO/PT2P1
                                                                             A 281
      WING=.FALSE.
                                                                             A 282
      CAFB2=CFCON*SKNFRC(X,LLIM,DSWCOS,GAM,ALAM,FUN1)
                                                                             A 283
      IF (BDYONLY) GO TO 25
r
    SKIN FRICTION ON WING UPPER AND LOWER SURFACES
Ċ
                                                                             A 284
      CAFU=CFOCR*(1.+CFDCFO1(I))
                                                                             A 285
      CAFL=0.
                                                                             A 286
      WING=.TRUE.
                                                                             A 287
      DO 24 K=1,KK1
                                                                             A 288
      K1 = KK - K + 1
                                                                             A 289
      AP=APO/PTWP1(K)
                                                                             A 290
      DLR=DELR(K)
                                                                             A 291
      SAVXW=XW(K)
                                                                             A 292
      XW(K)=TXSE(K)
      CAFL=CAFL+PTWP1(K)*SKNFRCW(XW(K),K1,DSWCSL(K,K),GAM,ALAM,FUN1)
                                                                             A 293
                                                                             A 294
      XW(K)=SAVXW
24
                                                                             A 295
      CAFL=CAFLC*CAFL
                                                                             A 296
      IF (XOUT) PRINT OUT
C
    LIFT. DPAG, AND L / D
C.
                                                                             A 297
      CAF(I)=CAFB2+CAFU+CAFL
                                                                             A 298
      GO TO 26
                                                                             A 299
      CAF(T)=2.*CAFB?
25
                                                                             A 300
      CAP(I)=2. #CAP(I)
                                                                             A 301
      CN=C.
                                                                             A 302
      CMCG=0.
                                                                             A 303
      CA(I)=CAP(I)+CAFACTR*CAF(I)
26
                                                                             A 304
      CL(I)=CN(I)*COSE(I)-CA(I)*SINE(I)
                                                                             4 305
      CD(T)=CA(I)*COSF(T)+CN(T)*SINE(I)
                                                                             A 306
      CLCD(T)=CL(T)/CD(I)
                                                                             A 307
      IF (COMIN.LT.CD(I)) GO TC 27
                                                                             A 308
      TMTN=T
                                                                             A 309
      CDMIN=CD(I)
                                                                             A 310
      IF (CLCD(T).LT.CLDMX) GD TO 28
27
                                                                             A 311
      CLDMX=CLCD(I)
                                                                             A 312
       TMAX=T
                                                                             A 313
      CONTINUE
28
                                                                             A 314
       TE (XOUT) PRINT 36, HEAD
                                                                             A 315
       TE (NANG-3) 31,29,29
¢
     QUADRATIC INTERPOLATION OF DRAG POLAR TO GET (L/D)MAX, ETC.
r.
C.
                                                                             A 316
       TF (TMAX.LT.2) IMAX=2
29
                                                                             A 317
       IF (IMAX.GE.NANG) TMAX=NANG-1
                                                                             A 318
       IXP=IMAX+1
                                                                             A 319
     . TXM=IMAX-1
                                                                             A 320
       YI=CD(IXM)
                                                                            A 321
       Y2=CO(TMAX)
                                                                             4 322
```

```
Y3=CD(IXP)
      X1 = CL(TXM)
                                                                               A 323
      X2=CL(IMAX)
                                                                               A 324
      X3=CL(IXP)
                                                                               A 325
      X12=X1-X2
                                                                               A 326
      X2?=X2-X3
                                                                               A 327
      IF (IFMIN) GO TO 30
                                                                               A 328
                                                                               A 329
      X31 = X3 - X1
      A={Y1*X23+Y2*X31+Y3*X12}/(-X12*X23*X31}
                                                                               A 330
      XA = .5*(A*(X3+X1)-(Y3-Y1)/X3)
                                                                               A 331
      XA2YAA=Y2+X2*{2.*X4-A*X2}
                                                                               A 332
      CLMX2=X42YAA/A
                                                                               A 333
      TF (CLMX2+LT+0+) GO TO 30
                                                                               A 334
      CLMX=SQRT(CLMX2)
                                                                               A 335
      CDMX=2.*(XA2YA4-XA*CLMX)
                                                                               A 336
      CLDMX=CLMX/CDMX
                                                                               4 337
      TALL MTLUP (0.,CDALO,2,NANG,11,2,KP,CL,CDANGL)
                                                                               A 338
      CALL MTLUP (CLMX, ALPHX, 2, NANG, 11, 1, 1MAX, CL, ANGL)
                                                                               A 339
      TEMIN=.TRUE.
                                                                               A 340
      IMAX=IMIN
                                                                               A 341
      GO TO 29
                                                                               A 342
30
      Y3221=(Y3-Y2)/(Y2-Y1)
                                                                               A 343
      X3221=X23/X12
                                                                               A 344
      CLMN = .5*(Y3221*(X2+X1)-X3221*(X3+X2))/(Y3221-X3221)
                                                                               A 345
      CALL MTLUP (CLMN, CDALN, 2, NANG, 11, 2, KP, CL, CDANGL)
                                                                               A 346
C
    MAIN OUTPUTS
r
      PRINT 37, CLOMX, ALPHX, CLMX, CDMX, CDALC, CDALN, CLMN
                                                                               4 347
      CALL SUMMARY (CLDMX, ALPHX, CLMX, CDALO, CDALN, CL(IO), HEAD, NCASE)
                                                                               A 348
      PRINT 34, (ANGL(I),CL(I),CD(I),CMCG(I),CLCD(I),CN(I),CNB(I),CND(I)
31
                                                                               A 349
     I.CNW(I).DPSRYQS(I).CA(I).CAP(I).CAF(I).I=1.NANG)
                                                                               A 350
      NCASF=4
                                                                               A 351
      GO TO 1
                                                                               A 352
32
      CALL PENTSUM (CLDMX,ALPHX,CLMX,CDALO,CDALN,CL(IO),HEAD,NCASE)
                                                                               A 353
      STOP
                                                                               A 354
C
ユス
      FORMAT (F12.2,15H DEG. PUPIQI =,F10.5)
                                                                               A 355
      FORMAT (//3x,5HALPHA,8x,2HCL,8x,2HCD,8x,2HCM,7x,3HL/D,9x,2HCN,8x,
                                                                               A 356
     1 3HCNB,7X,3HCND,7X,3HCNW,6X,4HDP/Q,8X,2HCA,8X,3HCAP,7X,3HCAF//
                                                                               A 357
     2 (F7.1,3X,3F10.5,F9.2,2X,5F10.5,X,3F10.5)
                                                                               A 358
35
      FORMAT (//F8.2,28H DEG., TOO NEGATIVE FOR BODY)
                                                                               A 359
      FORMAT (1H1/20X8A10/)
36
                                                                               A 360
      FORMAT (//TIH (L/D)MAX = + F8-4 + 11H AT ALPHA = + F7-4+
                                                               26H DEGREES,
                                                                               A 361
     1 WITH CL AND CD =,2F9.6//6H CDO =,F10.8,14H, AT ALPHA 0 ±,F8.4//
                                                                               A 362
     2 9H CD MIN =,F10.8,12H, AT ALPHA =,F8.4,9H AND CL =,F8.6)
                                                                               A 363
38
      FORMAT (8A10)
                                                                               A 364
      END
                                                                               A 365-
      FUNCTION PTOT (RS)
                                                                               B
                                                                                   1
C
    TOTAL TO STATIC PRESSURE RATIO ACROSS SHOCK. AND SHOCK POSITION
                                                                                   2
                                                                               В
C
      COMMON DUMB(16),XS,GAM,GM1,GM12,GP12,EM,EM1,EM32,ZMM,ZEM11,THR2M,
                                                                               B
                                                                                   3
     1 AMCH2, DEL, TWEM, AEP
                                                                                   4
                                                                               R
r
    X POSITION FOR GIVEN SHOCK RADIUS
                                                                                   5
                                                                               В
      XSM0=RS
                                                                                   6
                                                                               В
      IXT=RS##FMI
                                                                                   7
                                                                               В
      DO 1 I=1,10
                                                                                   8
                                                                               В
      XO1M=XO**EMI
                                                                                   9
                                                                               В
      XSM=PS/(1.+(4EP+TWFM/SQRT(X01M))*(X01M/X0)**2)
                                                                                  10
                                                                               R
      1F (XSM/XSMO.GT..999) GO TO 2
                                                                                  11
                                                                               В
      XO=XSM**EMI
                                                                                  12
                                                                               8
1
      XSM0=XSM
                                                                                  13
                                                                               R
```

```
8
                                                                                   14
2
      XS=XSM**FMI
                                                                                 В
                                                                                    15
      GO TO 3
                                                                                    16
      ENTRY PTOT2
                                                                                    17
                                                                                 R
    SHOCK RADIUS AT GIVEN X POSITION
C
                                                                                 В
                                                                                    18
      XSM=XS**EM
                                                                                    19
                                                                                 B
      RS=XSM+(&EP+TWEM/SQRT(XS))*XS*XS/XSM
                                                                                    20
                                                                                 A
      XSt2M=XSM**2
3
      TTHX?={DEL*(EM*XSL2M/XS+XS*ZMM*AEP++5*THR2M*TWEM*SQRT(XS)})**2
                                                                                 В
                                                                                    21
                                                                                 R
                                                                                    22
      AM2=AMCH2*TTHX2/(XSL2M+TTHX2)
                                                                                 A
                                                                                    23
      AMG1=GP32*AM2*(1.+GM12*AMCH2)/(1.+GM12*AM2)
                                                                                 R
      AMG2=GP12/(GAM*AM2-GM12)
                                                                                    25
                                                                                 В
      PTCT=FXP((ALOG(AMG2)+GAM*ALOG(AMG1))/GM1)
                                                                                    26
                                                                                 R
      RETURN
                                                                                    27
      END
                                                                                 r
                                                                                     1
      FUNCTION SKNERC (X, LLIM, DSWCOS, GAM, ALAM, FUN1)
C
                                                       (DATA ARE FOR TH/TT = .41667)
    LAMINAR, COMPRESSIBLE SKIN FRICTION
C.
C
      DIMENSION X(19), DSWCOS(19), XI(19), U(19), BETA(19), DCF(19),
                                                                                     2
                                                                                 C
                                                                                     7
     1 BIT(3), B(15), TTH2(30), THT2(2)
                                                                                 C
                                                                                     4
      EQUIVALENCE (FWPP, THT2(2))
      DATA B, TTH2/--2, --1,0-, 05, -1, -2, -3, -4, -5, -6, -8, 1., 1.2, 1.6, 2.,
                                                                                 C
                                                                                     5
      1 .293, .2485, .2205, .2095, .1998, .1845, .1725, .1627, .1547, .1479, .137;
                                                                                 C
                                                                                      6
    2 .1285, .1218, .1116, .1107, .269, .387, .4696, .5051, .5373, .5944, .6447,
                                                                                 C
                                                                                     7
                                                                                 C
                                                                                      В
      3 .69, .73165, .7703, .8408, .9044, .9627, 1.0677, 1.1613/,
                                                                                     9
      4, GX1,GX2,ZGM1/-.2857142857143,1.285714285714,5./
                                                                                 C
     BEGIN WITH X(1) = 0., XI(1) = 0., BETA = .5 (BLUNT-NOSED BODY)
                                                                                 C
                                                                                    10
C
                                                                                 C.
                                                                                     11
       BETA(1)=.5
                                                                                 С
                                                                                    12
       TMPT2=.23209
                                                                                 C
                                                                                    13
       FPTH=.28779
                                                                                 C
                                                                                    14
       GO TO 2
                                                                                 C
                                                                                     16
       ENTRY SKNEPCW
     BEGIN WITH X(1) = XSE, XI(1) = 0., BETA = 0. (UNDERSIDE OF WING)
                                                                                 C
                                                                                     15
C
                                                                                 C
                                                                                     1.7
       BETA=0.
                                                                                 C
                                                                                     18
       TMBT2=.441
                                                                                 C.
                                                                                     19
       FPTH=. 22052
                                                                                 C
                                                                                     20
       XM=X+.1*(X{2}-X)
2
                                                                                 C.
                                                                                     21
       PEPT2=P(XM)
                                                                                 C
                                                                                     22
       UM=SQRT(ZGM1*(PEPT2**GX1-1.))
                                                                                 C
                                                                                     23
       CALL MGAUSS (X+XM+1+XTM+FUNT+FOFX+1)
                                                                                 C
                                                                                     24
       XIN=FF VM XIM
                                                                                 ¢
                                                                                     25
       TH2UP=TM8T2*XIM
                                                                                 C
       DCF(1)=PEPT2**GX2*FPTH*DSWCDS(1)*SQRT(UM**3/TH2UR)
                                                                                     26
                                                                                 C
                                                                                     27
       XT(1)=XIM
                                                                                 C
                                                                                     28
       U(1) = UM
                                                                                . С
                                                                                     29
       DO 9 IP=2.LLIM
                                                                                 C.
                                                                                     30
       XP=X(IP)
                                                                                     31
                                                                                 r
       CALL MGAUSS (XM, XP, 1, DXI, FUN1, FDFX, 1)
                                                                                 C
                                                                                     32
       DXI=ALAM*DXI
                                                                                 C
                                                                                     33
       XT(IP)=DXT+XIM
                                                                                 C
                                                                                     34
       PEPT2=P(XP)
                                                                                     35
                                                                                 C
       U(IP)=SQRT(ZG#1*(PEPT2**GX1-1.))
                                                                                  C
                                                                                     36
       ALNUP=ALOGIU(IP}/UM)
                                                                                  C.
                                                                                     37
       ALMUR2=2.*ALNUR
                                                                                  C
                                                                                     38
       DXTUTH=DXI/TH2UR
                                                                                  C
                                                                                     39
       RLAM=7.7809*(U(IP)/UM-1.)/DXIUTH
       BET=RLAM*(1.+(RLAM-1.)*((.0206737*DXIUTH-.20419)*DXIUTH+.344145))
                                                                                  C
                                                                                     40
                                                                                  r
                                                                                     41
       KK=1
                                                                                  €
                                                                                     47
       K1 = 0
     ITERATION FOR BETA (LOCAL VELOCITY-VARIATION PARAMETER)
                                                                                  C
                                                                                     43
       00 7 J=1,29
                                                                                  C-
                                                                                     44
       BITP = BET
                                                                                     45
                                                                                  C
       BTT(KK)=BET
                                                                                  C
                                                                                     46
       TF (KK+3) 5,3,3
                                                                                  C
                                                                                     47
```

```
3
       KK = 1
                                                                                    C
                                                                                       48
      P32=BIT(3)-BIT(2)
                                                                                       49
                                                                                    C
      821=8IT(2)-8IT(1)
                                                                                    Ċ
                                                                                       50
       TF [885(821+832].LT.AB5(832)) GO TO 4
                                                                                    C
                                                                                        51
       BDENOM=B32-B21
                                                                                    C
                                                                                        52
       IF (BDENOM.EQ.O.) GO TO 6
                                                                                    C
                                                                                        53
       BFT=(BTT(1)*BTT(3)-BTT(2)**2)/BDENOM
                                                                                        54
                                                                                    C
       K1=0
                                                                                       55
                                                                                    C
       GD TO 6
                                                                                    C
                                                                                       56
       8FT=(8TT(2)+BIT(31)/2.
4
                                                                                        57
                                                                                    C
       GO TO 6
                                                                                    €
                                                                                        58
5
       KK=KK+K!
                                                                                    C
                                                                                        59
       K \underline{1} = \underline{1}
                                                                                    C
                                                                                        60
       JF (BET.GT.2.) 'PET=1.4
6
                                                                                    C
                                                                                        61
       CALL MYLUP (BET.THT2,2,15,15,15,1,JP,B,TTH2)
       RFT=ALNUP2/(4LNUP+ALOG(1.+DXIUTH*(2.-BET)*THT2))
                                                                                    ¢
                                                                                        62
                                                                                    C
                                                                                        63
       TE (ABS(BET/B)TR-1.)-.0001) 8,8,7
                                                                                    C.
                                                                                        64
7
       CONTINUE
                                                                                    C
                                                                                        65
       PRINT 11, XP, BITR, BET
       BETA(TP)=BET
                                                                                    C
                                                                                        66
8
                                                                                    C
                                                                                        67
       CALL MILUP (BET, THT2, 2, 15, 15, 2, JP, B, TTH2)
       TH2UP=(1.+DXIUTH*(2.-RET)*THT2)*TH2UR
                                                                                    ¢
                                                                                        68
                                                                                    C
       DCF(IP)=PEPT2**GX2*FWPP*DSWCOS(IP)*SQRT(U(IP)**3*THT2/TH2UR)
                                                                                        69
                                                                                    C
                                                                                        70
       XM=XP
                                                                                    C
                                                                                        71
       XIM=XI(FP)
                                                                                    C
                                                                                        72
q
       UM=U(TP)
                                                                                    C
                                                                                        73
       IF (LLTM.EQ.2) GO TO 10
                                                                                        74
                                                                                    C
       SKNFRC=SUM(X,DCF,LLIM)
                                                                                        75
                                                                                    C
       RETHRN
                                                                                    C
                                                                                        76
10
       SKNFRC=.F*{DCF+DCF(2))*(X(2)-X)
                                                                                        77
                                                                                     C
       RETURN
                                                                                        78
C
                                                                                     C
                                                                                    C
                                                                                        79
       FORMAT (/26H BETA UNCONVERGED AT X/L =,F8.5,12H BETA VALUES, 2F12.8
11
                                                                                        80
                                                                                    C
      1)
                                                                                     C.
                                                                                        81-
       END
                                                                                    0
                                                                                         1
       SUBROUTINE FUNI (X, FOFX)
C
     INTEGRAND OF STEWARDSON TRANSFORMATION INTEGRAL FOR SKIN FRICTION
                                                                                    D
                                                                                         2
C
C
       COMMON AP, ZIME, E2U2, FOE, FIEK, THG12G, TWM, EMBF2, D2ME2K, X2M, WING
                                                                                    D
                                                                                         3
                                                                                         4
                                                                                    D
       LOGICAL WING
                                                                                         5
                                                                                    D
       X2F=X**TWM
                                                                                         6
       X2=X*X
                                                                                    0
                                                                                         7
       IF (WING) 2.1
                                                                                    Ð
                                                                                         8
                                                                                    D
1
       XF=X2M
                                                                                         9
       X2=1./(X2*X2M)
                                                                                    D
                                                                                    D
                                                                                        10
       GO TO 3
                                                                                        11
2
       XF=1.
                                                                                    n
                                                                                        12
                                                                                    D
       X2 = X2M/X2
3
       FOFX=P2(X)**THG12G*XF*SQRT(1.+EMBF2*X2)
                                                                                    0
                                                                                        13
                                                                                        14
                                                                                    D
       RETURN
                                                                                        15
       END
                                                                                    D
                                                                                    E
                                                                                         1
       FUNCTION P (X)
C
¢
     BODY OF WING SURFACE PRESSURE
       COMMON AP, Z1ME, E2U2, FOE, F1EK, THG12G, TWM, EMBF2, D2ME2K, X2M, WING, F01,
                                                                                         2
                                                                                    Ε
                                                                                         3
      1f11K, DLR, ETB, CNETB, DUMB(13), TWEM, AEP
                                                                                     Ε
       LOGICAL WING
                                                                                     E
       X2M=X**TWM
                                                                                     Ε
                                                                                         5
       ENTRY P2
                                                                                     ε
                                                                                         6
       TE (WING) 2.1
                                                                                         7
                                                                                     ŧ
1
       FTCE=FOE
                                                                                     E
                                                                                         В
                                                                                         9
       FT1EK=F1EK
                                                                                     E
                                                                                        10
       GO TO 3
                                                                                     F
```

```
11
2
      XM=SORT(X2M)
      ETR=(({DLR+ETB*XM})/{XM+(TWEM*SQRT(X)+AEP*X}*X/XM}-ETB)*ONETB)**2
                                                                                    12
                                                                                 Έ
                                                                                 E
                                                                                    13
      FTGE=FGE+ETR*(FG1-FGE)
                                                                                    14
      FT1EK=F1EK+ETR*(F11K-F1EK)
                                                                                    15
                                                                                 E
3
      X21ME=X**Z1ME
                                                                                 Ε
                                                                                    16
      P=AP*((1.+F2U2*X21ME/SQRT(X))*FT0E/(X21ME+D2ME2K)+FT1EK)
                                                                                    17
                                                                                 Ε
      IF (P.LT.1) RETURN
                                                                                 Ε
                                                                                    18
      PRINT 4, P,X,E2U2,D2ME2K,ETR,FT0E,FT1EK
                                                                                    19
                                                                                 E
      P=.9999999925
                                                                                    20
                                                                                 E
      RETURN
                                                                                 E
                                                                                    21
C
      FORMAT (4H P = F13.5,16H SET = 1. AT X = F10.5,10X,5E13.5)
                                                                                 E
                                                                                    22
                                                                                    23-
      FNC
                                                                                 F
                                                                                      1
      FUNCTION SUM(X,Y,N)
C
    TRAPEZOIDAL INTEGRATION FOR UNEQUAL INTERVALS
C
C
                                                                                      2
                                                                                 F
      DIMENSION X(19),Y(19)
                                                                                 F
                                                                                      3
      M=N-1
                                                                                 F
                                                                                      4
       PSUM=Y*(X(2)-X)+Y(N)*(X(N)-X(M))
                                                                                 F
                                                                                      5
       DO 1 I=2, M
                                                                                 F
       PSUM=PSUM+Y{I}*{X(I+1)-X(I-1)}
Į.
                                                                                      7
                                                                                 F
       SUM=. F*PSUM
                                                                                 F
                                                                                      8
       PETURN
                                                                                  F
                                                                                      9
       END
                                                                                      1
                                                                                  G
       SUBROUTINE SUMMAPY(A,B,C,D,E,F,H,N)
¢
     COLLECTION OF SUMMARY RESULTS ON A FILE (TAPET) FOR SEPARATE OUTPUT
C
C
                                                                                  G
                                                                                      2
       DIMENSION D(2), E(2), H(8), L(25), D(14,75)
                                                                                      3
                                                                                  G
       DATA L.T.SKIP/26*0.3H(/)/
                                                                                      4
                                                                                  G
       IF (N-3) 1,2,3
                                                                                  G
                                                                                      5
       1F (L(1).EQ-1) GO TO 6
1
                                                                                  G
                                                                                      6
       I =0
                                                                                      7
                                                                                  G
       L(1+1)=1
2
                                                                                  G
                                                                                      8
       I=!+!
 3
                                                                                  G
                                                                                      9
       0(1,1)=4
                                                                                     10
                                                                                  G
       0(2,1)=8
                                                                                  G
                                                                                     11
       0(3*1)=0
                                                                                  G
                                                                                     12
       0(4,1)=0
                                                                                  G
                                                                                     13
       0(5,1)=0(2)
                                                                                  G
                                                                                     14
       O(6 - I) = E
                                                                                  G
                                                                                     15
       0(7,1)=F(2)
                                                                                  G
                                                                                     16
       0(8,T)=F
                                                                                  G
                                                                                     17
       0(9,1)=H(2)
                                                                                  G
                                                                                     18
       C(10,1)=H(4)
                                                                                  G
                                                                                     19
       O(11,1)=H(5)
                                                                                     20
                                                                                  G
       D(12,T)=H(6)
                                                                                  G
                                                                                     21
       0(13,1)=H(7)
                                                                                  G
                                                                                      22
       0(14,1)=H(8)
                                                                                      23
                                                                                  G
       TF (J.LT.25) RETURN
                                                                                  G
                                                                                      24
       ENTRY PRNTSUM
                                                                                      25
                                                                                  G
       WR!TE(7.9)
 6
                                                                                  G
                                                                                      26
       DO 7 J=1,I
                                                                                      27
                                                                                  G
        IF (L(J).FQ.1) WPITE(7.SKIP)
                                                                                  G
                                                                                      28
       WRITE(7,8) (O(K,J),K=1,14)
                                                                                  G
                                                                                      29
 7
       L(J)=0
                                                                                  G
                                                                                      30
        T = 0
                                                                                  G
                                                                                      31
        TE (N.17.3) GC TO 2
                                                                                      32
                                                                                  G
        RETURN
        FORMAT (X2F9.4, F8.5, F9.5, F8.2, F9.4, F8.2, F8.5, 3X, 6410)
                                                                                  G
                                                                                      33
       FORMAT(1H1/16H HYPAERO SUMMARY//3X,5H(L/D), FX,5HALPHA,4X,2HCL,3X,
 8
                                                                                      34
      1 2(5X, 2HCD, 5X, 5HALPHA), 4X, 2HCL/7X, 3HMAX, 2X, 2(3X, 5HL/DMX),
                                                                                      35
                                                                                   G
                                                                                      36-
                                                                                   G
       2 2(6X,1H0,3X),2(2X,3HMIN,4X),3HA=0)
                                                                                      37
                                                                                   G
        END
```

Input

A single case consists of the determination of the aerodynamic coefficients over a given set of angles of attack. The first card for each case provides a heading for the printout; it consists of 80 columns of any desired FORTRAN characters. The remaining cards for each case are interpreted by a system loading subroutine (NAMELIST) which is very flexible. The data block begins with an arbitrary name (\$DATA in the present case) and ends with the dollar sign (\$); the variables between may be in any order and need appear only if values are to be different from those preassigned or used in the previous case of the same computer run. Column one of all these cards is blank. A description of the input FORTRAN variables with their correct type and preassigned values (if any) in parentheses is as follows:

FORTRAN variable

Description

ratio of y location of moment reference center to

maximum body radius (real)

TINF free-stream static temperature, Tom OR (real) AMCH free-stream Mach number, M_{∞} (real) NALF number of angles of attack, maximum of 11 (integer) ANGL angle-of-attack array, decreasing order, deg (real) EMpower-law exponent, m (real) F body fineness parameter, f (real) REL Reynolds number based on body length, $R_{\infty,\ell}$ (real) SSB ratio of reference area for coefficients to body planform area; if zero, program uses wing planform area (real;0.) XCG ratio of x location of moment reference center to body length (real)

YCG

FORTRAN variable

Description

PBPI

ratio of base pressure to free-stream static pressure (real;1.)

CAFCTR

multiplication factor times calculated laminar skin friction (real;1.)

XOUT

extra output at each angle of attack if XOUT = .TRUE.(logical,.FALSE.)

PBBP0L

array of NALF values of wing upper surface pressure parameter $\left(\frac{\bar{P}-P_0}{\lambda_{Cr}}\right)$ in ref. 20 corresponding to angles of attack ANGL (real)

CFDCF01

array of NALF values of wing skin-friction parameter $\left(\frac{C_{F,\Delta}}{C_{F,0,cr}}-1\right)$ in ref. 20 corresponding to angles

BDYONLY

set equal to .TRUE. for axisymmetric body only, .FALSE. for half body with wing (logical; .FALSE.)

NCASE

indicator for each additional case of a run to avoid unnecessary recomputations (integer; 1 initially, 4 each case thereafter). After first case of a run set NCASE = 2 if AMCH or TINF is changed; set NCASE = 3 if EM is changed but AMCH and TINF are not; for no change to AMCH, TINF or EM use preassigned value 4.

Output

There are four possible output blocks for each case, only two of which always appear. First comes the input list with four added variables. These are GAM, the ratio of specific heats γ ; ALAMCR, a parameter ($\lambda_{\rm Cr}$) from reference 20; DEL, the slender body parameter δ ; and EPS, the shock strength parameter ϵ_1 . Next is a

list of the angles of attack with the pressure coefficient, Mach number and sine squared of the shock angle for oblique shock, and with the pressure coefficient and Mach number for Prandtl-Meyer expansion through the angle (appears only for new Mach numbers). Third is a list of variables used in the angle-of-attack and skin-friction calculations, which appears only if called by setting XOUT = .TRUE. in the input list. Fourth is the standard output of stability-axis and body-axis coefficients with the interpolated $(L/D)_{max}$. The normal-force coefficient is also broken down into contributions from the body CNB, the body boundary-layer area under the wing CND, the rest of the underwing area CNW, and the wing upper surface DP/Q. The axial force is broken into the contribution from the pressure CAP and from the skin friction CAF. In addition to these results, after all cases have been run, a summary of results is printed out for cases with angles of attack.

Example

Input cards for a run of two sample cases are presented below. The first case is for the complete configuration with m=0.75, f=7, at $M_{\infty}=12$, $R_{\infty,l}=256.26\times 10^6$ and 11 angles of attack. The second is for the axisymmetric body having the same parameters.

```
POWER-LAW TRANSPORBITER: MACH 12 EM=.7500 F=7.00 PFY=4.42E6/M PRASE=PINFINIT $DATA AMCH=12..EM=.75.F=7..REL=256.26F6.TINF=408..XCG=.6.YCG=.15; PRBPOL=2.86.3.19.3.52.3.71.3.9.4.09.4.27.4.62.4.95.5.24.5.5. CFDCF01=-.07..06..23..32..42..52..62..84.1.09.1.35.1.59.. NALF=11.ANGL=3..2..1...50...-5.-1...-2...-3...-4...-5.*
POWER-LAW BODY OF REVOL MACH 12 EM=.7500 F=7.00 RFY=4.42E6/M PRASE=PINFINIT $DATA NCASE=2.80YONLY=.TRUE..NALF=1.ANGL(1)=0..PBBPOL=0..CFDCF01=0.*
```

The output for these input cards is shown below. The total computation time on a CDC 6600 series computer at the Langley Research Center was less than 15 seconds (excluding compilation).

```
SOATA
NEASE
        = 1,
GAM
         = 0.14F+01.
TINE
         = C.498E+n2,
APCH
         = 0.37E+02.
NALE
         = 0.3E+01, 0.79+01, 0.1E+01, 7.EE+00, 0.0, +0.5E+00, +0.1E+01, -0.2F+01, -0.3F+01, -0.4F+01, -0.5E+01,
ANGL
         = C.7FF+CO.
         = 0.7F+91.
PPL
         = 0.256265+09.
SSB
         - 0.0
XCG
       ° = 0.65+40,
YCG
        = 0.15F+00.
         = 0.1F+01.
CAFACTR = 0.1F+01,
        = -9.111768771547456+00+
ANGO
XCUT
        = F.
```

PRRPOI =

```
0.286E+01, 0.319E+01, 0.352E+01, 0.371E+01, 0.39E+01, 0.499E+01, 0.427F+01, 0.462E+01, 0.49EE+01, 0.524E+01, 0.524E+01,
CFDCF01 = -0.7F-01, 0.6E-01, 0.23E+00, 0.32E+00, 0.42E+00, 0.52E+00, 0.62F+00, 0.84F+00, 0.109F+01, 0.135E+01, 0.159F+01,
ALAMER = 0.9196922174AF57E-02.
BOYENLY = F.
DEI
          = 0.163252245942776+00+
          = C.2605468F920625E+00.
xse
          = 7.4*F-02,
SEND
                        POWER-LAW TRANSPORTITER MACH 12 EM=.7500 F=7.00 REY=4.42E6/M PRASE=PINFINIT
         3.00 DEG.
2.00 DEG.
                       PUPTOT =
PUPTOT =
PUPTOT =
                                     -.00454
         1.00 DEG.
.FO DEG.
--FO DEG.
                                     -.00257
                                      --00137
                       PUPTOT =
        -1.90 DEG.
                       = 1019U9
                                       .00746
        -2.00 DEG.
        -3.00 OFG.
                       PUPTOT =
                                       .01262
        -4.00 DEG.
        -F.OA DEG.
                       PUPICE =
                                       02632
(L/D)MAX = 5.8468 AT ALPH4 = -.0225 DEGREES, WITH CL AND CD = .034100 .005832
COC = .00282901, AT ALPMA 0 = -3.3872
CO MIN = _30282*59. AT ALPHA = -3.4989 AND CL =-.001197
                                                                                                                                            CA .
                                                                                                                                                      CAP
                                                                                                                                                                      CAF
                                                                                                                            DP/Q
  ALPHS
                   ۲L
                                CO
                                             C۶
                                                         1.70
                                                                        CN
                                                                                      CNB
                                                                                                   CNO
                                                                                                                CNW
                                                         4.91
5.30
5.65
5.79
5.85
                                                                                                                                                                    .00043
                                                                                                                                         .00970
                                                                                                                                                       .00926
                                                                                    .04397
                                                                                                 .00011
                                                                                                              .01492
                                                                                                                           .00578
    3.0
                 .06419
                              -11308
                                           .00211
                                                                      .05478
                                                                      .05450
.05457
.03934
                 .05418
.4424
                              .01071
                                         -00192
                                                                                   .03764
03174
                                                                                                              .01250
.01027
    2.0
                                                                                                 .00011
                                                                                                                           .00425
                                                                                                                                          .00832
                                                                                                                                                       -00790
                                                                                                                                                       .00663
                                                                                                                                                                    .00040
    I. 0
5
                                                                                                 .00011
                                                                                                                           .00225
                                                                                                                                          .00704
                 .03432
.03432
.02925
                              .00507
.00507
                                         -.00314
-.00447
-.00593
                                                                                    02897
                                                                                                                                          .00644
                                                                                                 . 00011
                                                                                                              .00923
                                                                                                                           .00103
                                                                      03432
02931
                                                                                    .02632
.02381
                                                                                                 .00011
                                                                                                              .00825
                                                                                                                          -.00036
                                                                                                                                         .00587
                                                                                                                                                                    -00039
                                                                                                                                                       -00548
                                                         5.78
5.54
4.20
                                                                                                                          -.00192
                                                                                                                                                       .00495
                                                                                                                                                                    .00039
                                         -.00754
-.0112*
-.01572
-.02105
                                                                      .02428
.01415
.07384
                 .02426
                              .00440
                                                                                   .D2142
                                                                                                                         -.00369
-.00788
                                                                                                                                          +004B2
                                                                                                 - 00011
                                                                                                              _00844
                                                                                                                                         .00389
                                                                                                                                                       .00352
                                                                                                              .00484
                                                                                                                                                                    .00037
   -2.0
                                                                                                                                                                    .00036
  -3.0
                .004.00
-.004.54
                              .00289
                                                                                    - 01 332
                                                                                                 -00011
                                                                                                              .90347
                                                                                                                          --01307
                                                        -2.26
-5.06
                                                                      -.09672
                                                                                    .01018
                                                                                                 0001
                                                                                                              00234
                                                                                                                          - 01935
                                                                                                                                          -00243
                                                                                                                                                       -00207
   -4.0
                                                                                                              .00144
                                                                                                                          -.02682
                                                                                                                                                       .00155
                                                                                                                                                                    .00035
   -5. A
               --01737
                              -00343
                                         --02731
                                                                     -.01760
                                                                                    -00767
                                                                                                 .00011
SOATA
NCASE
          = 2,
GAM
          = 0.14E+C1,
          = 0.408E+03.
TINE
          = 0.126+02,
AMCH
NAL E
          = 1.
            0.0, C.2E+01, 0.1E+01, 0.5E+00, 0.0, -0.5E+00, -0.1F+01, -0.2E+01, -0.7E+01, -0.4E+01, -0.5E+01+
ANGL
Eм
          = 0.75E+CO+
          0.7F+01,
REL
              0.256268+09,
SSB
          = 0.0.
        = 0.65+00+
XCG
YCG
          = 0.15F+CD+
PBPI
          = 0.1E+01+
CAFACTR = 0.16+01.
ANGO
          = -0.111768771547456+00,
XCUT
         = 0.0, 0.319E+01, 0.352E+01, 0.371E+01, 0.39E+01, 0.409E+01, 0.427E+01, 0.462E+01, 0.495E+01, 0.524E+01, 0.55E+01,
PBBPOL
              0.0, C.6E=01, 0.23F+00, 0.32E+00, 0.42E+00, 0.52E+00, 0.62E+00, 0.84E+00, 0.109E+01, 0.135E+01, 0.159E+01,
CEDCEOL =
```

```
ALAMCR = 0.91969221746557E-02,

BDYONLY = T,

DEL = 0.16325224594277E+00,

EPS = 0.26056685920625E+00,

XSE = 0.13996004141169E-02,

$END
```

POWER-LAW BODY OF REVOL MACH 12 EMS.7500 FS7.00 REYS4.42E6/M PBASESPINFINIT

```
ALPHE
             CL
                        ĊO
                                             L/D
                                                          CN
                                                                     CNB
                                                                                CND
                                                                                           CNW
                                                                                                    DP/Q
                                                                                                                 CA
                                                                                                                            CAP
                                                                                                                                      CAF
          0.00000
                      .01128
                                0.00000
0.0
                                             0.00
                                                       0.00000
                                                                              .00011
                                                                   .07637
                                                                                         .00825
                                                                                                  9.00000
                                                                                                                -01128
                                                                                                                          -01096
                                                                                                                                     .00032
```

HYPAEPO SUMMARY

MAX L/DMX 1/DMX 0 0 MTN MEN A=0

5.8468 --0225 -03410 -00283 -3.38 -0028 -3.50 -03432 TER MACH 12 FM=.7500 F=7.00 REY=4.42E6/M PBASE=PINFINIT

COMPUTER PROGRAM FOR CALCULATING K_0 AND λ_{cr}

The main program requires as inputs values of two parameters describing wing upper surface conditions. These values are an average wing upper surface pressure parameter (PBBP0L) and an average wing upper surface skin-friction parameter (CFDCF01). They are plotted in reference 20 (figs. 4 and 11 of the reference, respectively) as $\frac{\overline{P} - P_0}{\lambda_{Cr}} \text{ and } \frac{C_{F,\Delta}}{C_{F,0,cr}} - 1 \text{ for delta wings as functions of } \lambda_{cr} \text{ (a viscous interaction parameter) and } K_0 \text{ (=-}M_{\infty}\alpha). \text{ This program calculates } K_0 \text{ for each angle of attack and the value of } \lambda_{cr} \text{ for the delta wing corresponding to the power-law wing.}}$ As mentioned in the main body of the paper, the correspondence is based on the viscous

effects, which are assumed to be approximately equal for wings with equal spans and equal values of $\iint x^{-1/2} dr dx$. For the power-law wings, this integral involves gamma functions which are approximated analytically in the program.

PROGRAM UPPRESS(INPUT=201,OUTPUT=201,TAPE1=INPUT) DIMENSION ANGL(11), CAO(11), PO(11), HEAD(8), PBBPOL(11) NAMELIST /DATA/ REL,F,AMCH,TINF,EM,ETAB,FO,AI,NCASE,NALF,ANGL,XCG, ISSB, YCG DATA GAM, TWTT, PTF, ASAV/1.4,.41667, 2.65868, 0./ GM1=GAM-1. GM1T=1./GM1 Δ GM83=GAM*8./3. GM12=.5*GM1 A GP 14= (GAM+1.)/4. Α 10 ZGGt=GAM/GM12 ٨ 11 1 READ 11, HEAD A 12 IF (ENDFILE 1) 9,2 13 READ DATA 14 IF (ANGL.EQ.ASAV) GO TO 7 ٨ 15 ASAV=ANGL Δ 16 DO 6 T=1.NALF ٩ 17 ANG=.0174533*ANGL(1) Δ 18 CAO(I) =-AMCH+ANG 19

```
IF (CAO(1)) 4,5,3
                                                                                  20
                                                                               ٨
      GP1K04=GP14*CAO(1)
3
                                                                                  21
      RTGK4=SQPT(1.+GP1K04**2)
                                                                                 22
      PO(T)=1.+G4M*CAO(I)*(GP1KO4+RTGK4)
                                                                                 23
      P9BPOL(T)=GM83*(RTGK4+GP1K04*(2.+GP1K04/RTGK4))/SQRT(P0(I))
                                                                               A
                                                                                  24
      GO TO 5
                                                                                  25
      GM12K=1.+GM12*CAO(T)
                                                                                  26
      P9(T)=GM12K**ZGG1
                                                                                  27
      IF (PO(T).LT.O.) PO(T)=0.
                                                                                 28
                                                                                  29
      PBBPOL(I)=GM83*GM12K**GM1I
                                                                               B
      GO TO 6
                                                                                  30
      PO(I)=1.
                                                                                  31
      PBBPOL(T)=GM83
                                                                                  32
      CONTINUE
                                                                                  33
7
      ZM=2.*FM
                                                                                  34
      PRINT 12, HEAD
                                                                               Δ
                                                                                 35
      IF (FM_FQ.BSAV) GO TO 8
                                                                                  36
      BSAV=FM
                                                                               8
                                                                                  37
      EMMI=EM-I.
                                                                                  38
      EM4]=4.*FM-1.
                                                                                  39
      EM4019=.4019*EM
                                                                                  40
      EMX1=1.5303-FM4019
                                                                               A
                                                                                 41
      EMX2=.5/(.9274+EM4019)
                                                                              Δ
                                                                                  42
      AT = . 9775- . 7627*EMMI/(EMMI+1.295*EM41)
                                                                              A
                                                                                  43
      EMG=GM3*AT*ETAB/(EM*SQRT(2.*G&M*EM41*FO))
                                                                                  44
      AEP=AT*(FTAB*F/AMCH)**2
                                                                                  45
                                                                               A
      ASPX=AFP*EMX1/(5.-ZM)
                                                                                  46
      TTBTJ=1.+GM12*AMCH*AMCH
                                                                                  47
      TWTT=TWTT*TTRTT
                                                                                  48
      TPTI=.273+(.195+.532*TWTT)*TTBTI
                                                                               â
                                                                                  49
      SUTHI=198.6/TINE
                                                                                  50
      C1=(1.+SUTHI)/(TWTI+SUTHI)*SQRT(TWTI)
                                                                                  51
      C3=(1.+SUTHI)/{TPT[+SUTH!)*SQRT(TPT])
                                                                                  52
      ZEM32=EMG*AMCH*F*F*SQPT(C1/PEL)
                                                                                  53
      EM32X=.5+ZEM32/EMX1
                                                                                  54
      G2MRC=.49053*GM12*(AMCH**3)*SQRT(C3/REL)
                                                                                  55
                                                                               à
      TREL=P*F*(EMX2+&EPX+EM32X)/(1.+&EP+ZEM32)
                                                                                  56
      ALAMCP=G2MRC/SQRT(CREL)
                                                                                  57
                                                                                  58
      PRINT 10, EM.F.AMCH.COEL.ALAMCR.(ANGL(I).CAO(I).PO(I).PBBPOL(I).I=
     11, NALF)
                                                                                  59
      GO TO 1
                                                                                  60
      STOP
                                                                                  61
                                                                                  52
      FORMAT (///15%, 2HEM, 9%, 1HE, 8%, 4HMACH, 6%, 5HCRE/L, 7%, 11H(LAMROA)CRE/
10
                                                                                  63
     1/9x,FlO.4,2FlO.2,Fl2.6,El7.6///6x,FH4NGLF,6x,4H(K10,7x,4H(P10,7x,6
                                                                                  54
     2HLAM=0..9X,13H(P-P0)/LAMBDA,6X,11H(CFD/CF0)-1/(/F11.2,F11.4,2F11.5
                                                                                 5 F
     311
                                                                                  56
11
      FORMAT (8410)
                                                                              Ò,
                                                                                  67
      FORMAT (1H1,5X8410)
12
                                                                              ٨
                                                                                  68
      END
                                                                                  69-
```

Input

A single case consists of calculations for a single configuration over a set of angles of attack. The first card is a heading consisting of any 80 FORTRAN characters. The remaining cards use the same loading subroutine as does the main program; the data block begins with \$DATA and ends with \$. The necessary input variables are TINF, AMCH, NANG, ANGL, EM, F, REL, ETAB, F0, and A1. Of these the first seven are the same as for the main program and the last three are from the similarity solution results.

APPENDIX - Concluded

See figure 3 and table I where ETAB = η_b , F0 = F₀(η_b), and A1 = a₁. The program is set up so that the input cards to the main program may be used with these three variables added. Here is the input for the first sample case given with the main program:

```
POWER-LAW TRANSPORBITER MACH 12 EM=.7500 F=7.00 RFY=4.42E6/M ***** HPPRESS $DATA AMCH=12..EM=.75.F=7..REL=256.26F6.TINF=408..XCG=.6.YCG=.15.ETAB=.87507.F0=.69806.A1=.80732, NALF=11.ANGL=3..72.,10..5.0.,-.5..1..,-2..-3...-4...-5.$
```

Output

The output for the same case is shown in this section. In it (LAMBDA)CRE = $\lambda_{\rm CR}$ and (K)0 = K₀ are needed for use with reference 20. Also printed are the length ratio of the delta to the power-law wing, CRE/L; the ratio of inviscid surface pressure to free-stream static pressure, P0; and the average pressure parameter for λ = 0, LAM = 0. This latter value is a useful aid sometimes in interpolating values from the figures of reference 20.

POWER-LAW TRANSPORBITER MACH 12 EM=.7500 F=7.00 REY=4.42E6/M ***** UPPRESS

	EM	F	MACH	CRF/L	(LAMBDA)CPE	
	.7500	7.00	12.00	1.056144	9.196840E-03	
ANGLE	(K)0	(P)0	į, A (M=0.	(P-PO)/LAMBDA	(CFD/CF0)-1
3.00	6287	-39062	2.66	866		
2.00	4189	.54 202	2.99	986		
1.00	2094	.74116	3.35	458	•	
. 50	1047	.86229	3.540	092		
0.00	-0.1000	1.00000	3.73	333		
50	-1047	1.15611	3.92	899		
-1.00	- 2094	1.33237	4.123	332		
-2.00	-4189	1.75205	4.498	371		•
-3.00	.6283	2.27170	4.84	414		
-4.00	.8378	2.90224	5-150	151		
-5.00	1.0472	3.65262	5.414	k72		

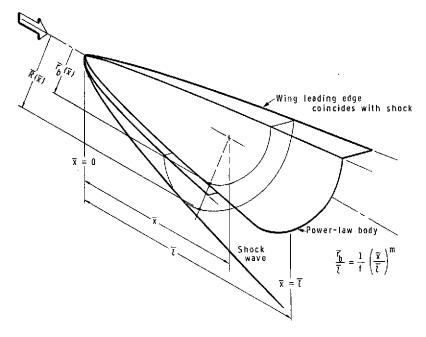
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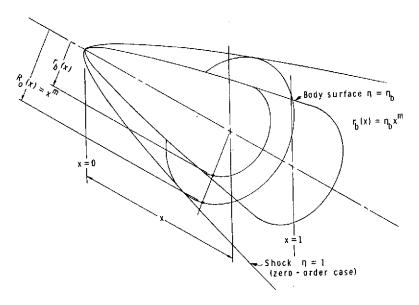
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TABLE I.- SOLUTIONS TO THE HYPERSONIC SIMILARITY EQUATIONS FOR POWER-LAW BODIES OF REVOLUTION

m	η_{b}	$F_0(\eta_b)$	$\mathbf{F}_{1}(\eta_{b})$	$^{ m J}_{ m 0}$	J ₁	^a 1
	 	<u> </u>	$\gamma = 7/5$			
1,00000	0.91492	0.87342	0.9179	0.07323	0.08410	0,47546
.95000	.91034	.84711	1.0591	.07589	.09551	.52709
.90000	.90465	.81630	1.2306	.07909	.11044	.58604
.85000	.89743	.78174	1,4386	.08303	.13067	.65291
.80000	.88798	.74265	1.6887	.08799	.15918	.72741
.75000	,87507	.69806	1.9811	.09444	.20098	.80732
.70000	.85648	.64662	2.2986	.10318	.26459	.88631
.66667	.83880	.60763	2.4964	.11098	.32565	.93216
.63333	.81391	.56403	2.6392	.12129	.40794	.96566
.60000	.77647	.51478	2.6593	.13564	.51763	.98034
.55000	.66414	.42678	2.2510	.17318	.74598	.96791
.53000	.56901	.38500	1.8876	.20119	.86687	.96377
.51000	.37221	.33757	1.4110	.25443	1.04110	.97539
.50500	.27299	.32450	1.2766	.28069	1,11845	.98249
.50000	.00000	.31077	1.1366	.35808	1.36841	.99182
			$\gamma = 5/3$		·•	
1,00000	0.87041	0.81065	0.7836	0,10244	0.10987	0.46531
.95000	.86429	.78363	.9017	.10532	.12597	.51356
.90000	.85679	.75282	1.0433	.10872	.14660	.567 88
.85000	.84740	.71823	1.2122	.11283	.17364	.62833
.80000	.83532	.67912	1,4108	.11787	.20994	.69402
.75000	.81919	.63448	1.6356	.12422	.25974	.76228
.70000	.79658	.58296	1.8685	.13248	.32919	.82727
.66667	.77569	.54389	2.0053	.13956	.39031	.86398
.63333	.74719	.50016	2.0956	.14850	.46626	.89116
.60000	.70595	.45067	2.0942	.16025	.55904	.90627
.55000	.59076	.36177	1,7872	.18792	.73266	.91473
.53000	.49985	.31912	1.5217	.20647	.81845	.92427
.51000	.32217	.26988	1.1590	.23916	.93877	.94825
.50500	.23542	.25600	1.0506	.25495	.99164	.95764
.50000	.00000	.24113	.9315	.30378	1.16431	.96872



(a) General power-law, wing-body configuration.



(b) Body of revolution in nondimensional coordinates.

Figure 1.- Configuration studied, showing relation between physical and nondimensional coordinates.

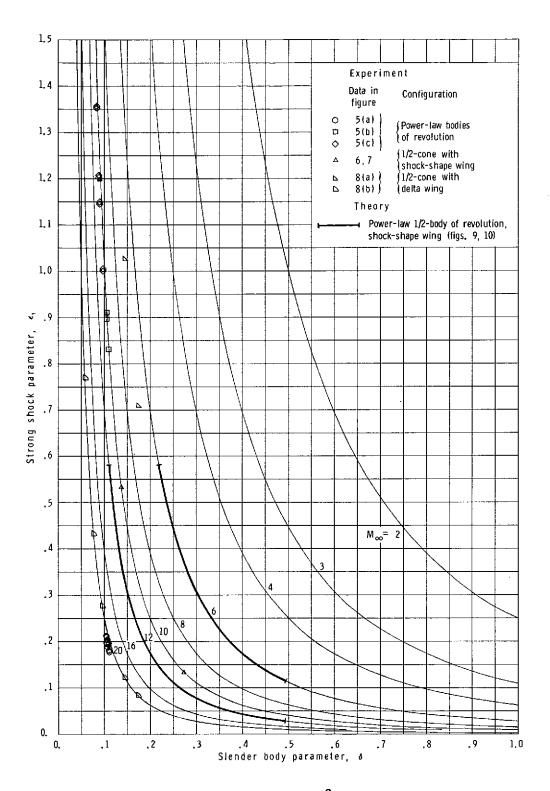


Figure 2.- Graph of the relation $\epsilon_1 = 1/(M_\infty \delta)^2$ for several Mach numbers and showing the values of δ and ϵ_1 for various sets of experimental data.

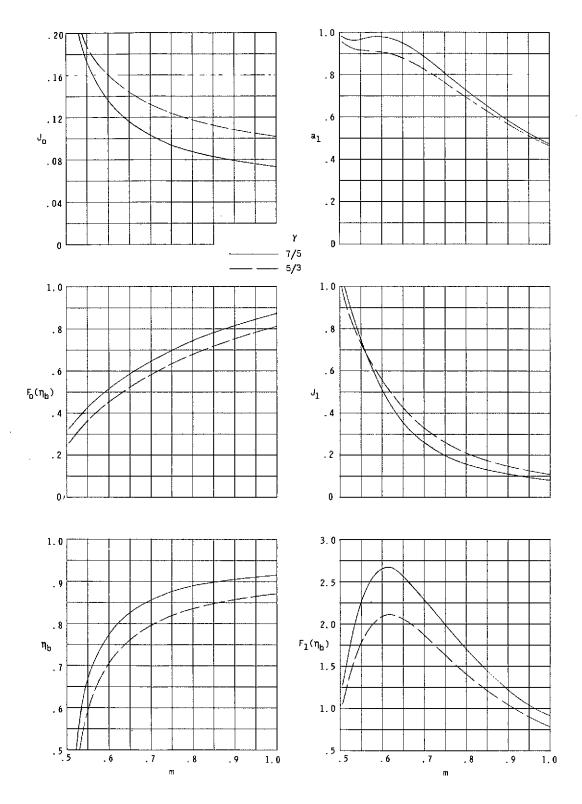


Figure 3.- Variation of similarity solution parameters with power-law exponent m.

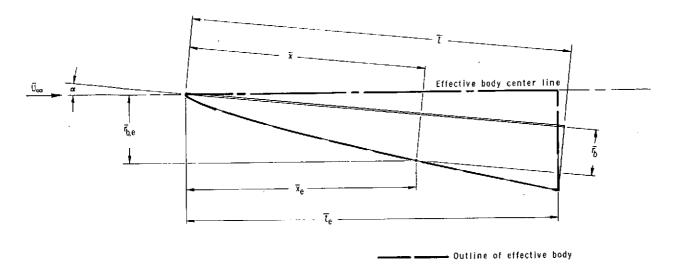


Figure 4.- Effective body for estimating aerodynamic characteristics at angle of attack (shown for f=6, m=2/3).

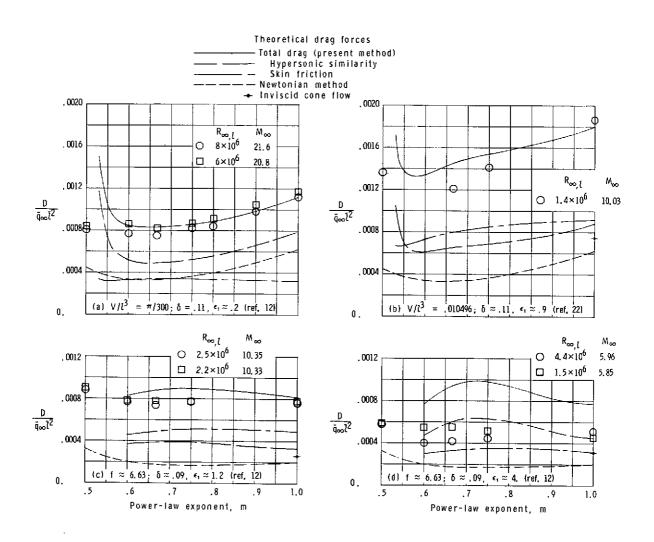


Figure 5.- Comparisons of theoretical drag coefficient at zero angle of attack with experiment for power-law bodies of revolution. The theory is shown for the larger Reynolds number in each case.

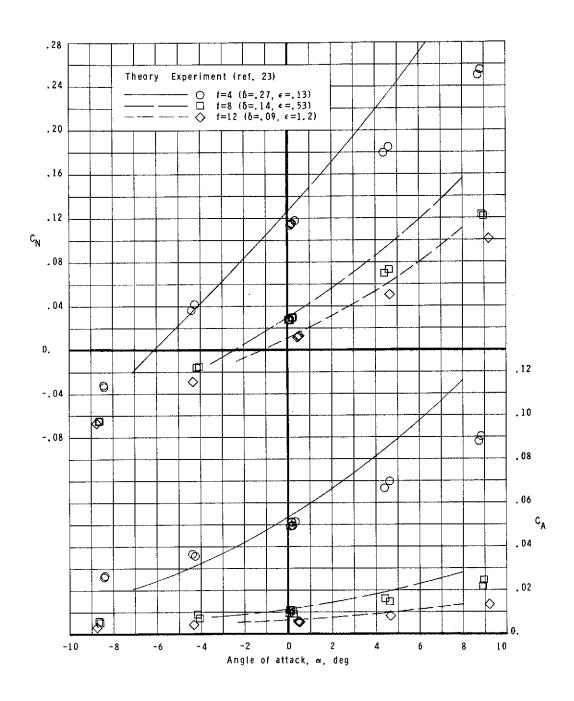


Figure 6.- Comparison of theoretical normal and axial forces with experiment for wing—conical-body configurations (m = 1) at Mach 10.03.

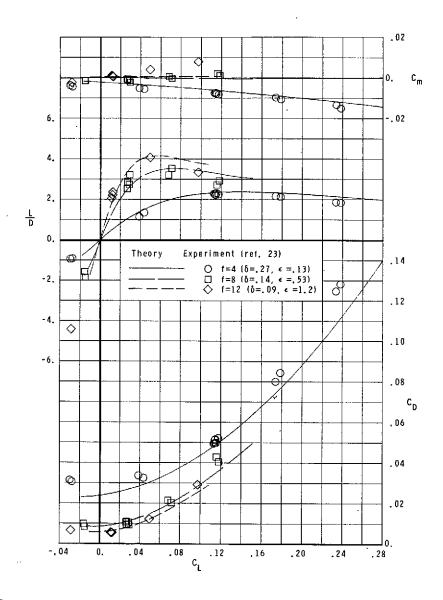
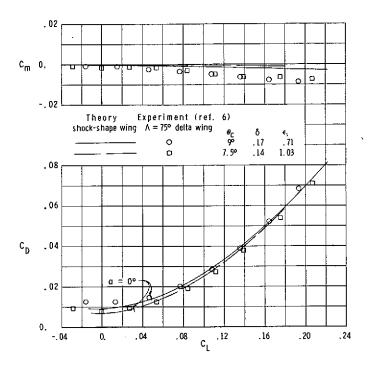
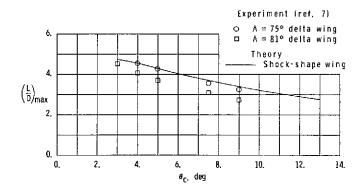


Figure 7.- Comparison of theoretical drag polar, lift-drag ratio, and pitching-moment curves with experiment for wing—conical-body configurations (m = 1) at Mach 10.03.

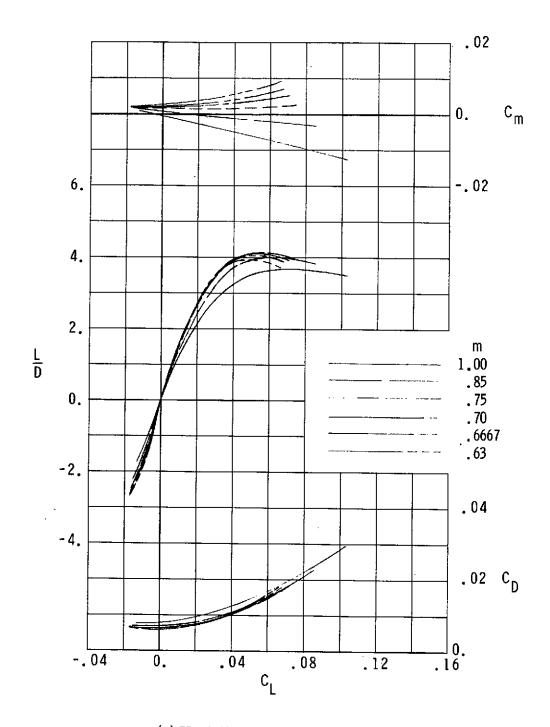


(a) Drag polars and pitching moment at Mach 6.86 in air.



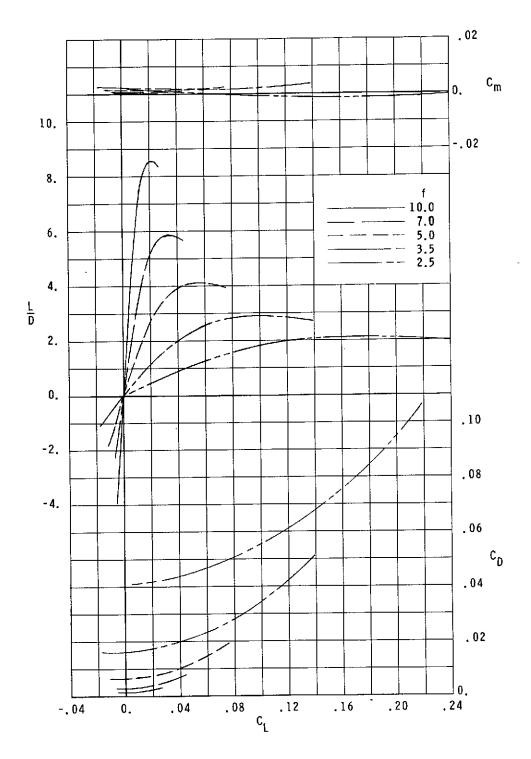
(b) Maximum lift-drag ratio at Mach 19.9 in helium.

Figure 8.- Comparisons of calculated performance of half-cone bodies having shock-shape-matching wings with experimental data for the same bodies having delta-planform wings.

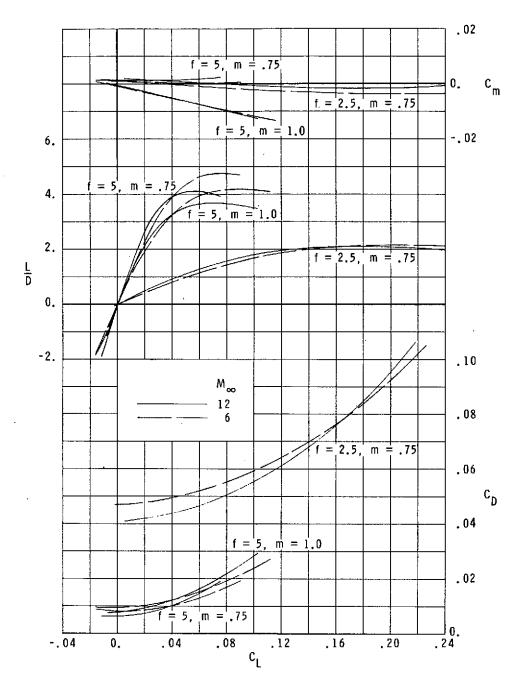


(a) Variation with m for f = 5.

Figure 9.- Comparison of calculated aerodynamic characteristics for Mach 12 flight at an altitude of 30 km. Volume = 2500 m 3 ; moment reference center at $\overline{x} = 0.6 \mathcal{I}$, $\overline{y} = 0.15 \overline{r}_{b,B}$.



(b) Variation with f for m = 0.75. Figure 9.- Continued.



(c) Comparison of three configurations with Mach 6 designs for the same body shapes.

Figure 9.- Concluded.

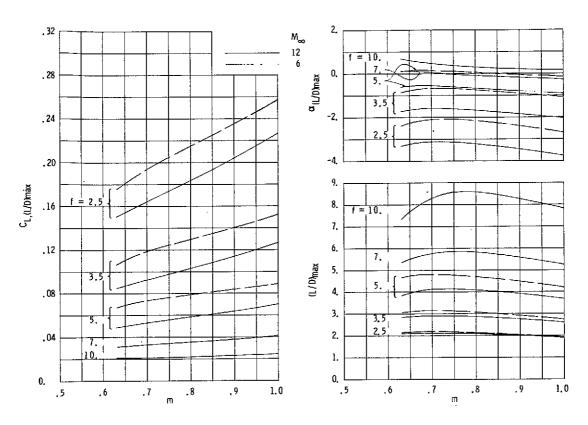


Figure 10.- Summary of theoretical aerodynamic characteristics for configurations of volume 2500 $\rm m^3$ at Mach 6 and 12 and at an altitude of 30 km.